

NLO precise top mass from the b-jet energy peak

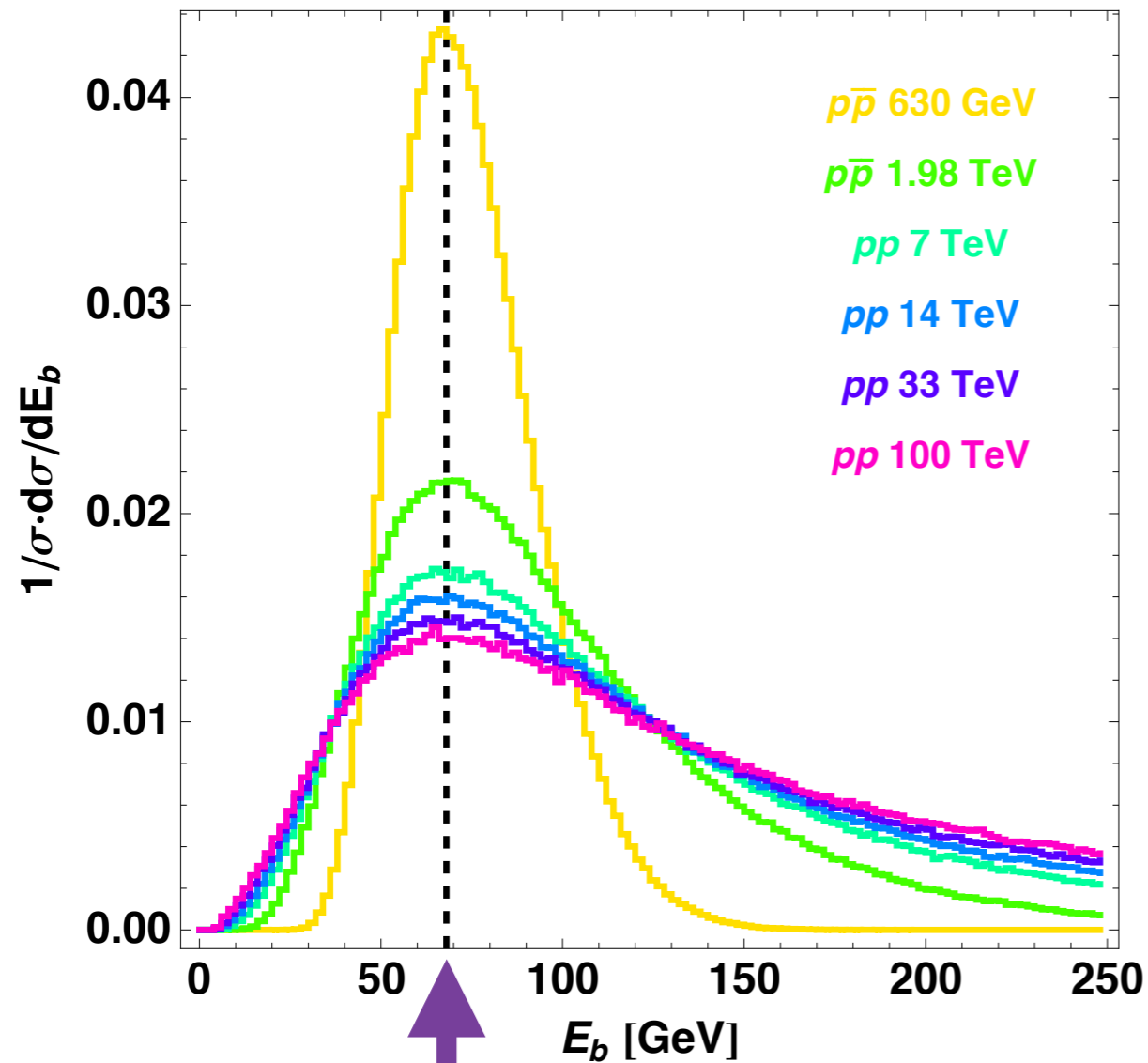
Roberto Franceschini (CERN)
November 17th 2015

Work in Progress with K. Agashe, D. Kim and M. Schulze

Energy peak invariance

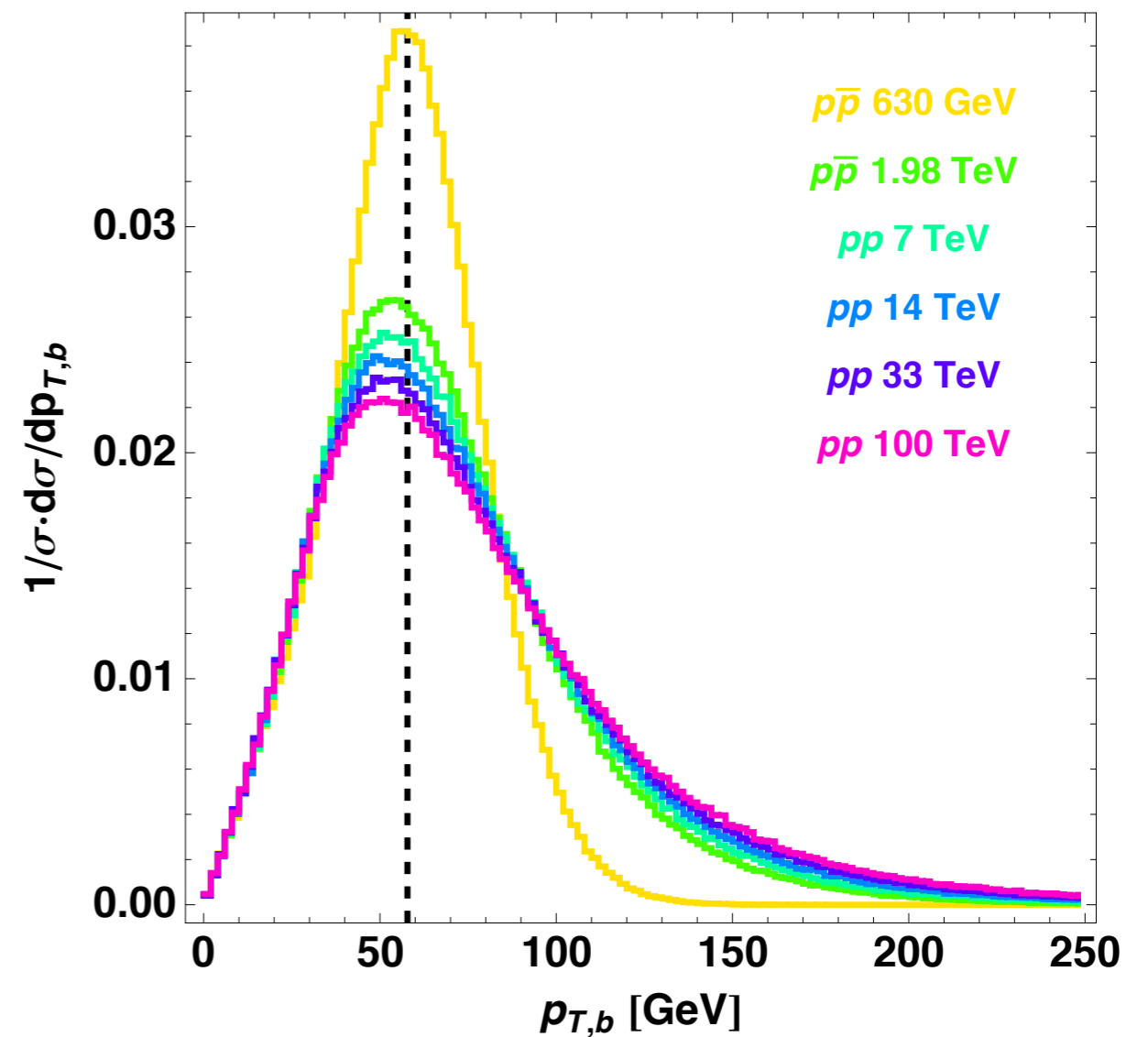
1209.0772 - Agashe, RF and Kim

Shape changes, peak doesn't!



$$E_b^* = \frac{m_t^2 - m_W^2 + m_b^2}{2m_t}$$

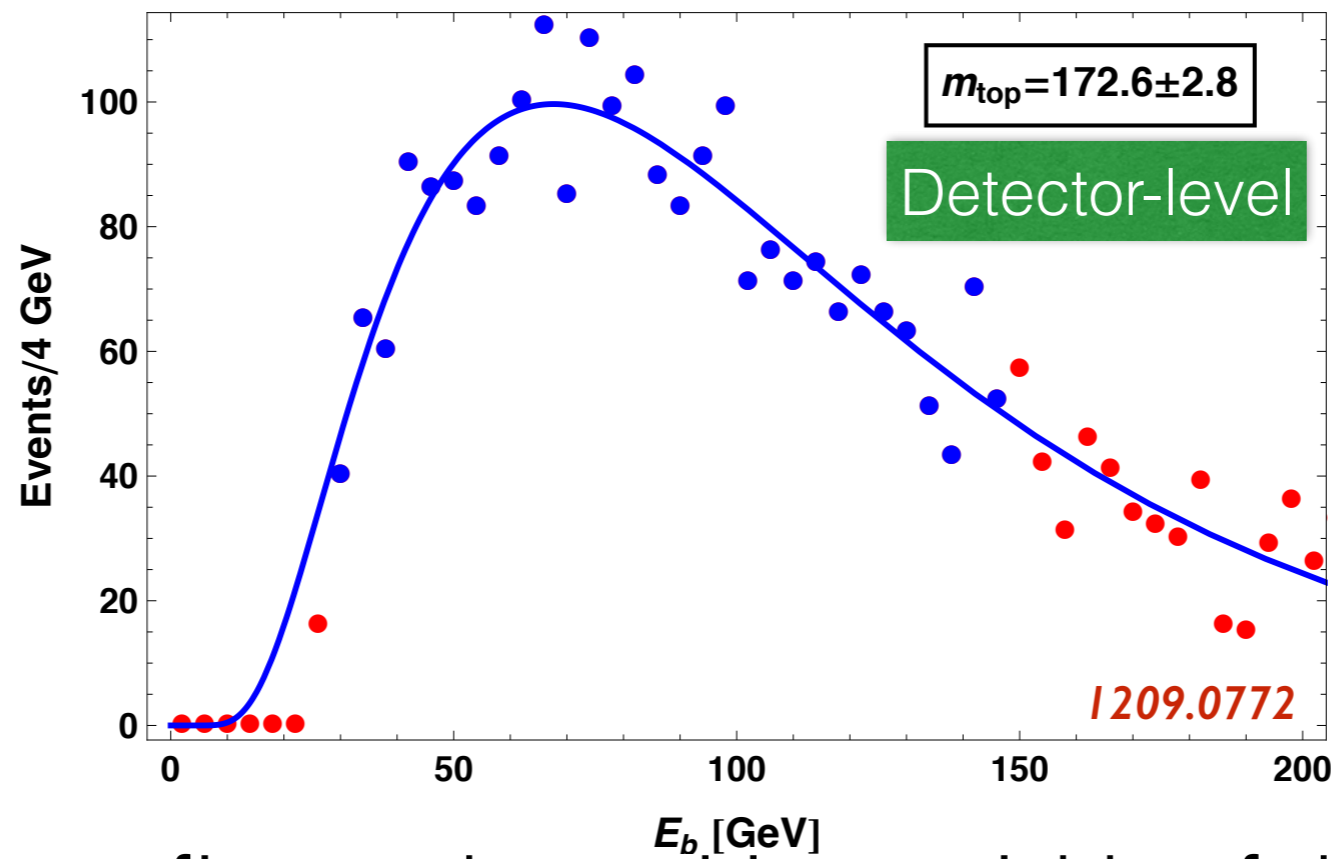
Shape changes, peak does too



The sensitivity to the **boost distribution** is the key

b-jet energy (LO+PS)

100 pseudo-experiments from [MadGraph5+Pythia6.4+Delphes](#) (**ATLAS-2012-097**)



2-parameters fit: peak position, width of the distribution

Proof of the concept: 5/fb LHC 7 TeV

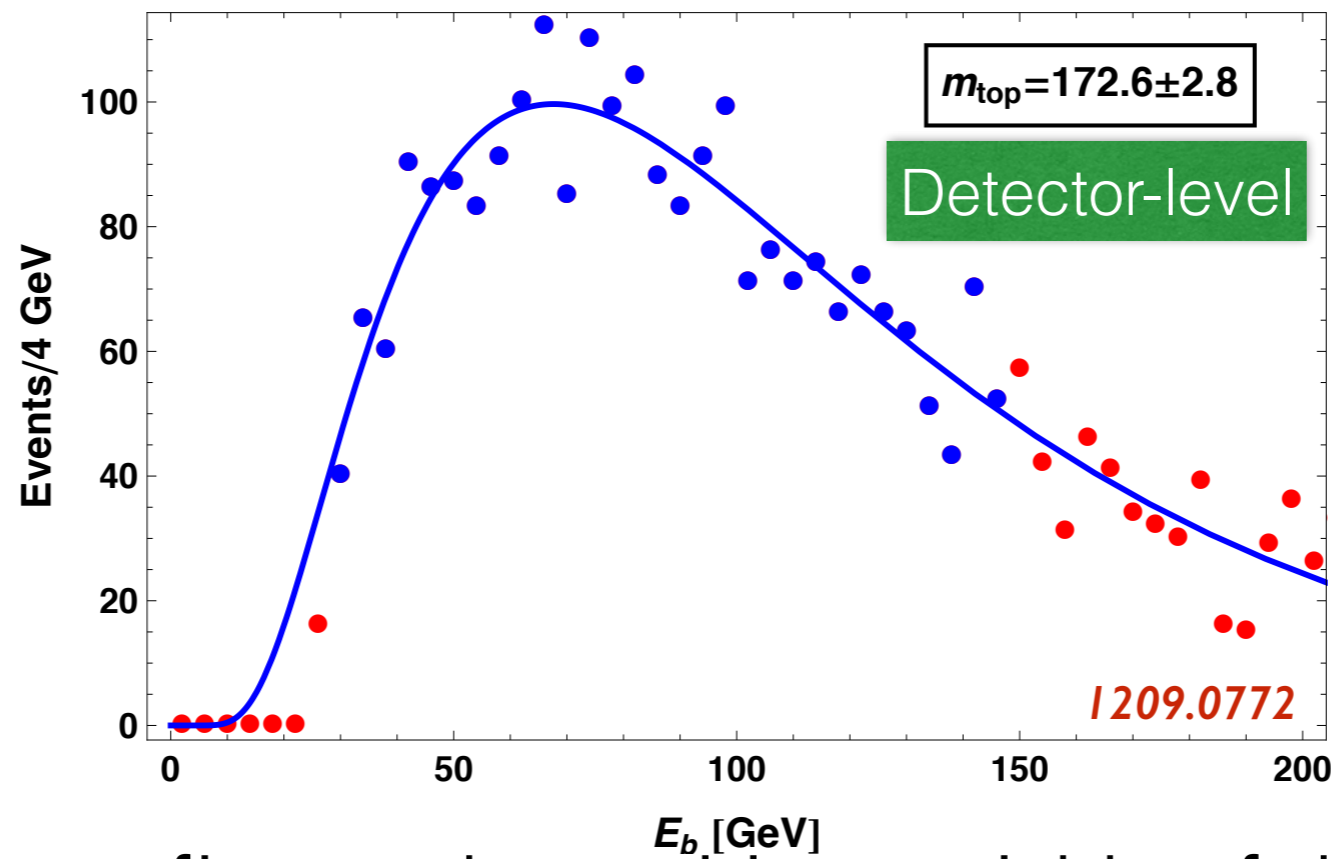
$m_{\text{top}} = 173.1 \pm 2.5 \text{ GeV (stat)}$

1209.0772 - Agashe Franceschini and Kim

message: LO effects are well under control → CMS at work!

b-jet energy (LO+PS)

100 pseudo-experiments from [MadGraph5+Pythia6.4+Delphes](#) (**ATLAS-2012-097**)



2-parameters fit: peak position, width of the distribution

Proof of the concept: **5/fb LHC 7 TeV**

$$m_{\text{top}} = 173.1 (1 \pm \alpha/\pi) \pm 2.5 \text{ GeV (stat)}$$

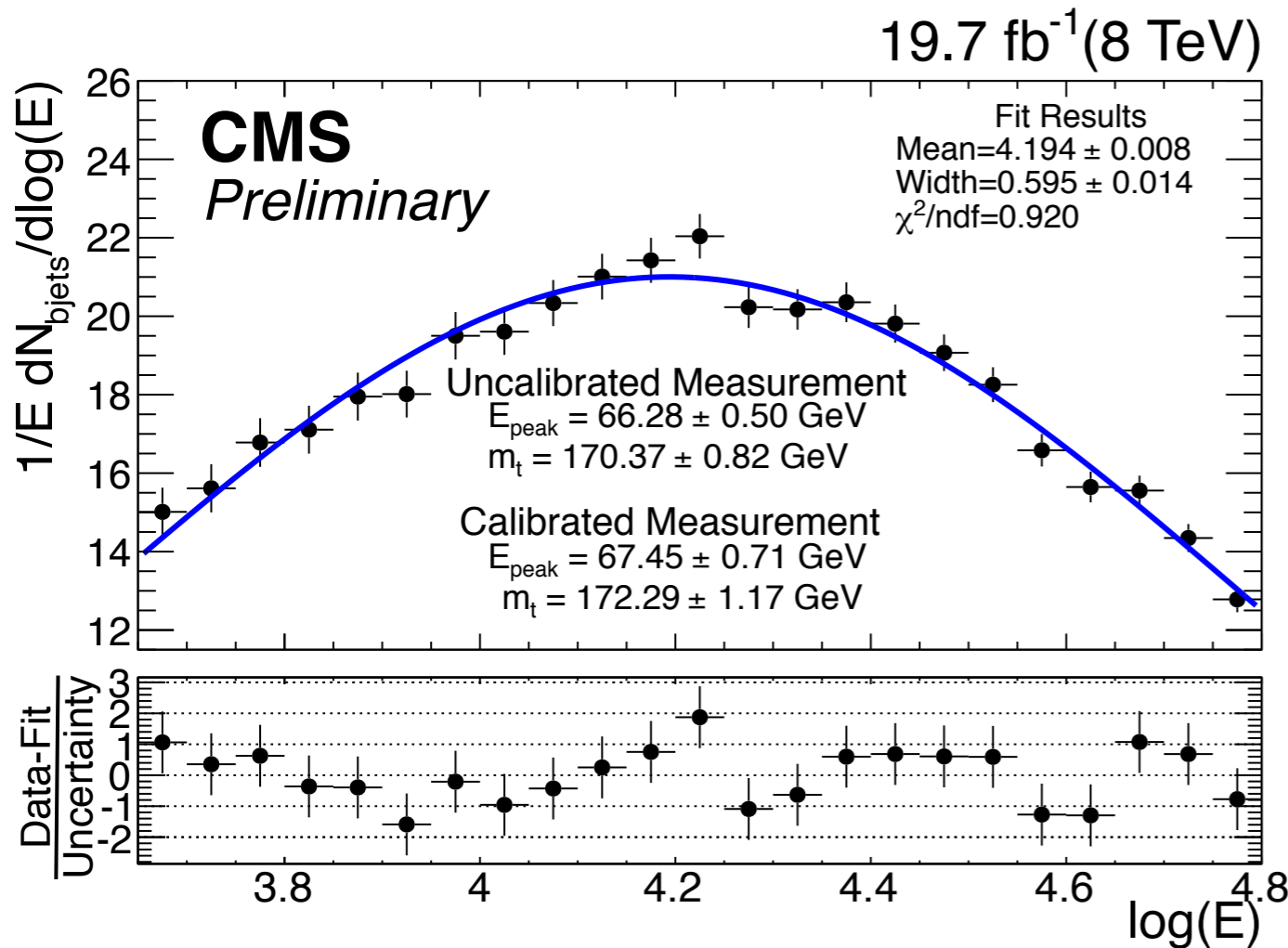
1209.0772 - Agashe Franceschini and Kim

message: LO effects are well under control → CMS at work!

CMS PAS TOP-15-002

$$m_t = 172.29 \pm 1.17 \text{ (stat.)} \pm 2.66 \text{ (syst.) GeV}$$

Just released !!!



Source of uncertainty	δE_{peak} (GeV)	δm_t (GeV)
Experimental uncertainties		
Jet energy scale	0.74	1.23
b jet energy scale	0.14	0.22
Jet energy resolution	0.18	0.30
Pile-up	0.01	0.02
b-tagging efficiency	0.12	0.20
Lepton efficiency	0.02	0.03
Fit calibration	0.14	0.24
Backgrounds	0.21	0.34
Modeling of hard scattering process		
Generator modeling	0.91	1.50
Renormalization and factorization scales	0.13	0.22
ME-PS matching threshold	0.24	0.39
Top p_T reweighting	0.90	1.49
PDFs	0.13	0.22
Modeling of non-perturbative QCD		
Underlying event	0.22	0.35
Color reconnection	0.38	0.62
Total	1.62	2.66

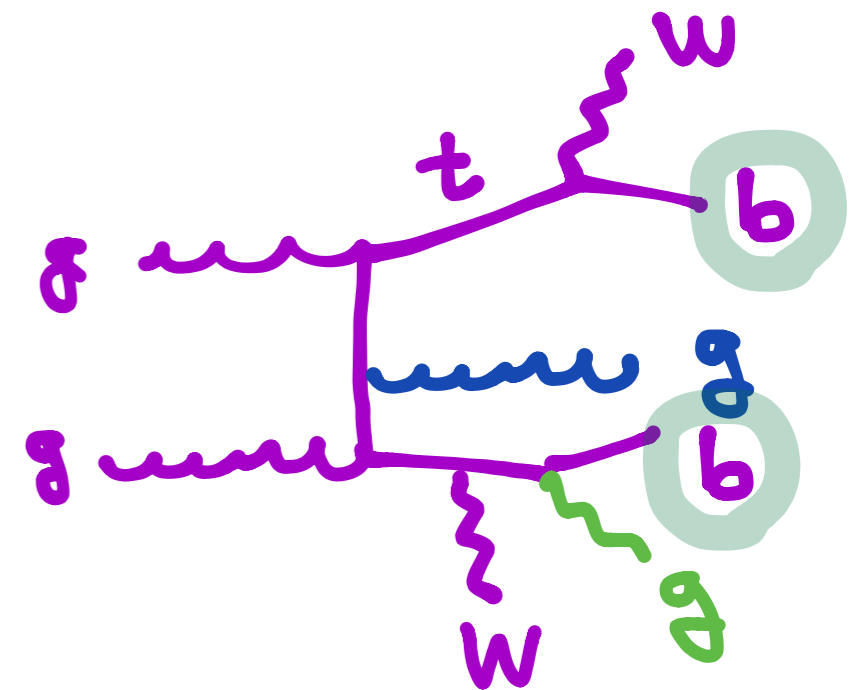
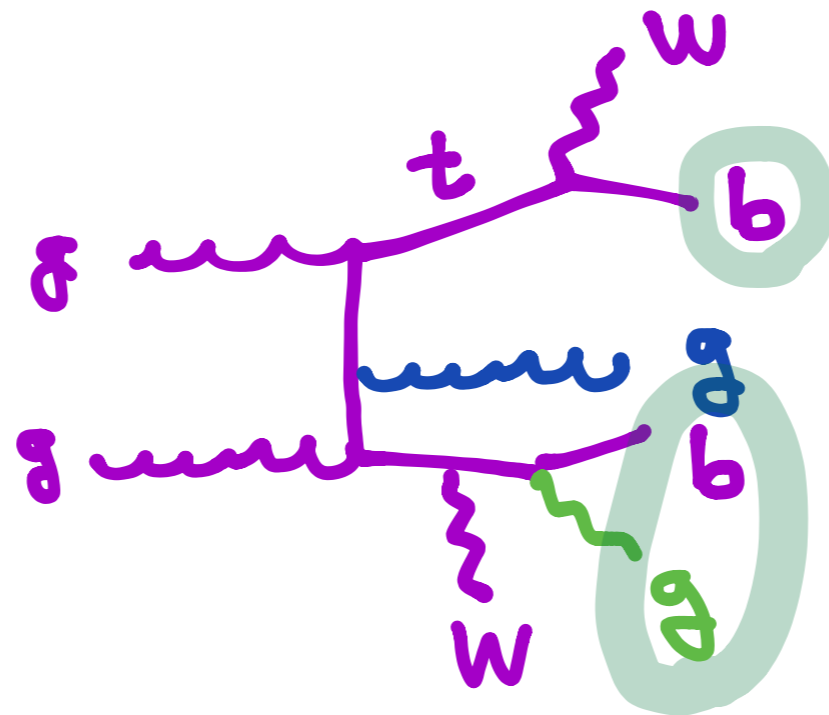
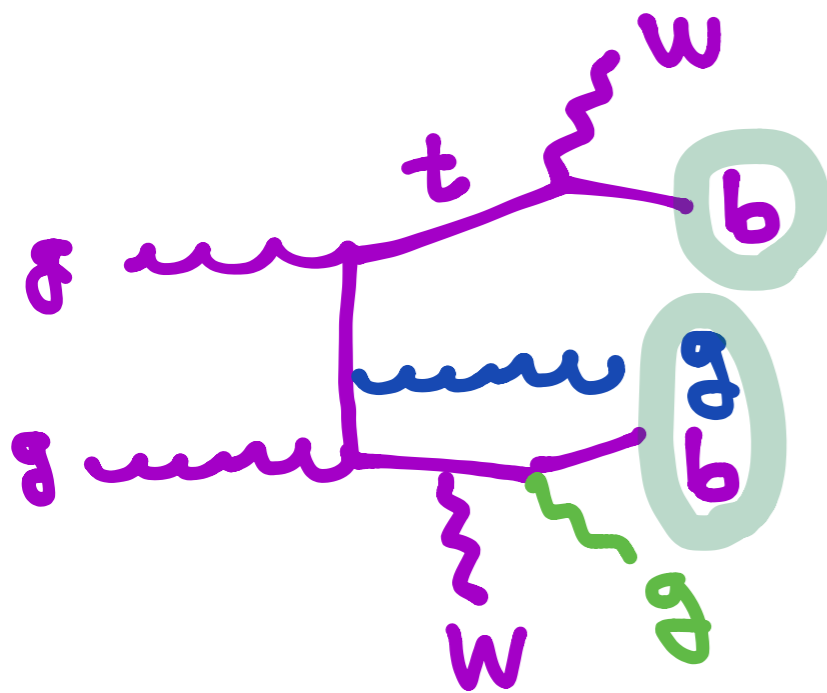
leading uncertainty from theory can be reduced

$p_T(\text{top})$ reweighting smaller than other methods (L_{xy} , $p_T \ell$...)

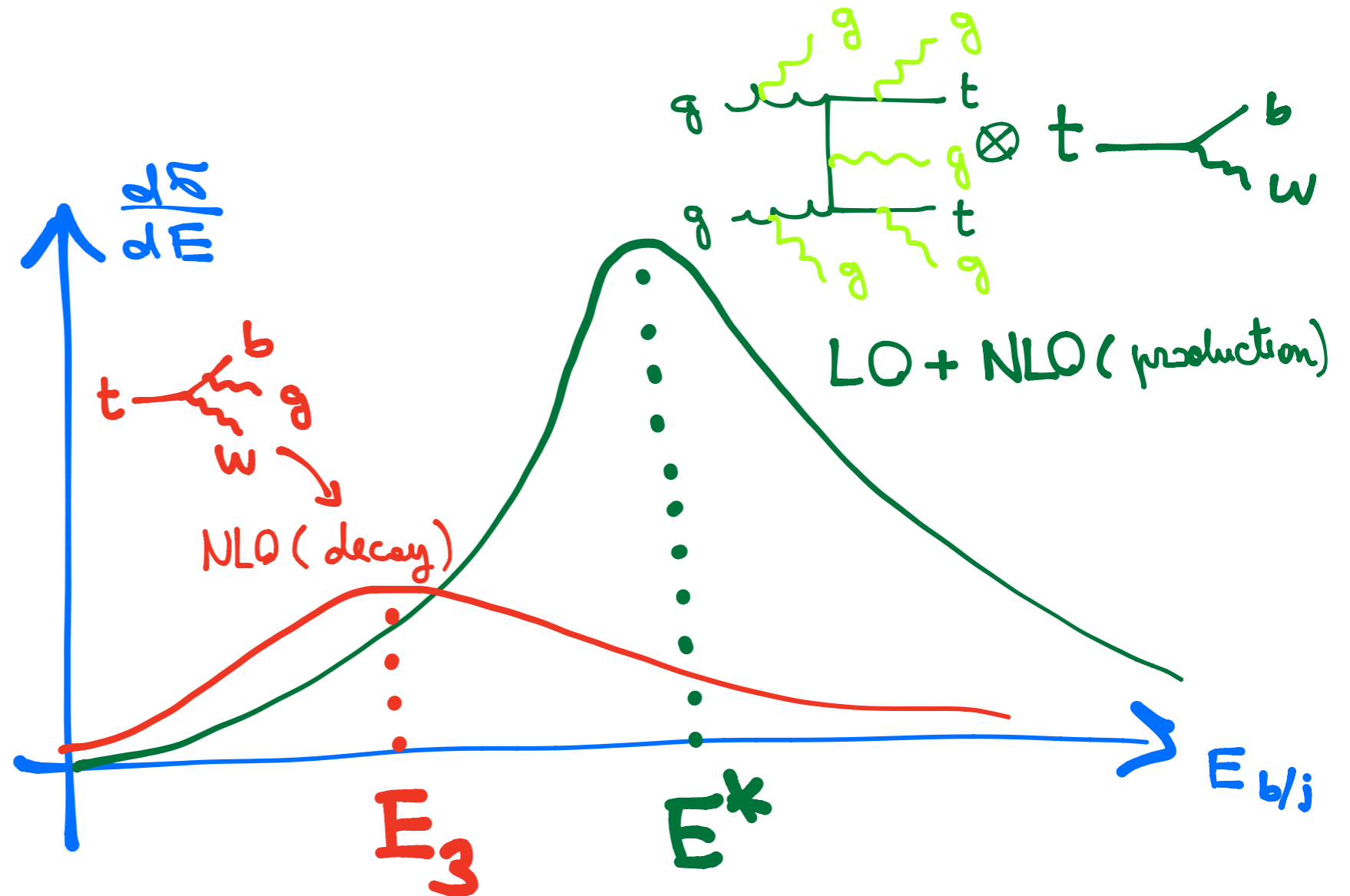
NLO: production & decay

(MCFM)

Agashe, Franceschini, Kim, Schulze - in preparation

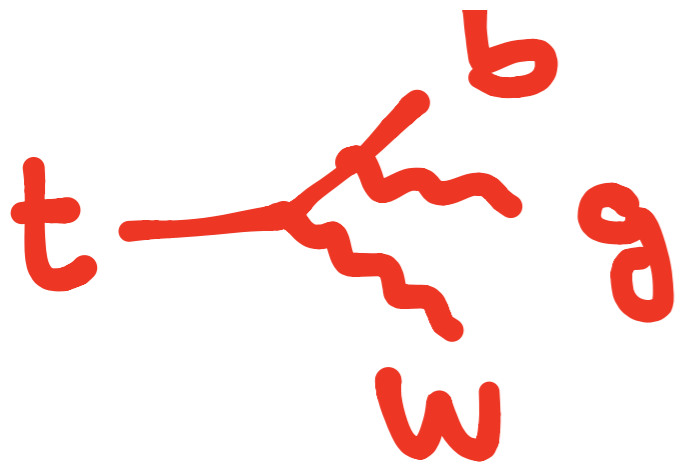


Peak shift at NLO



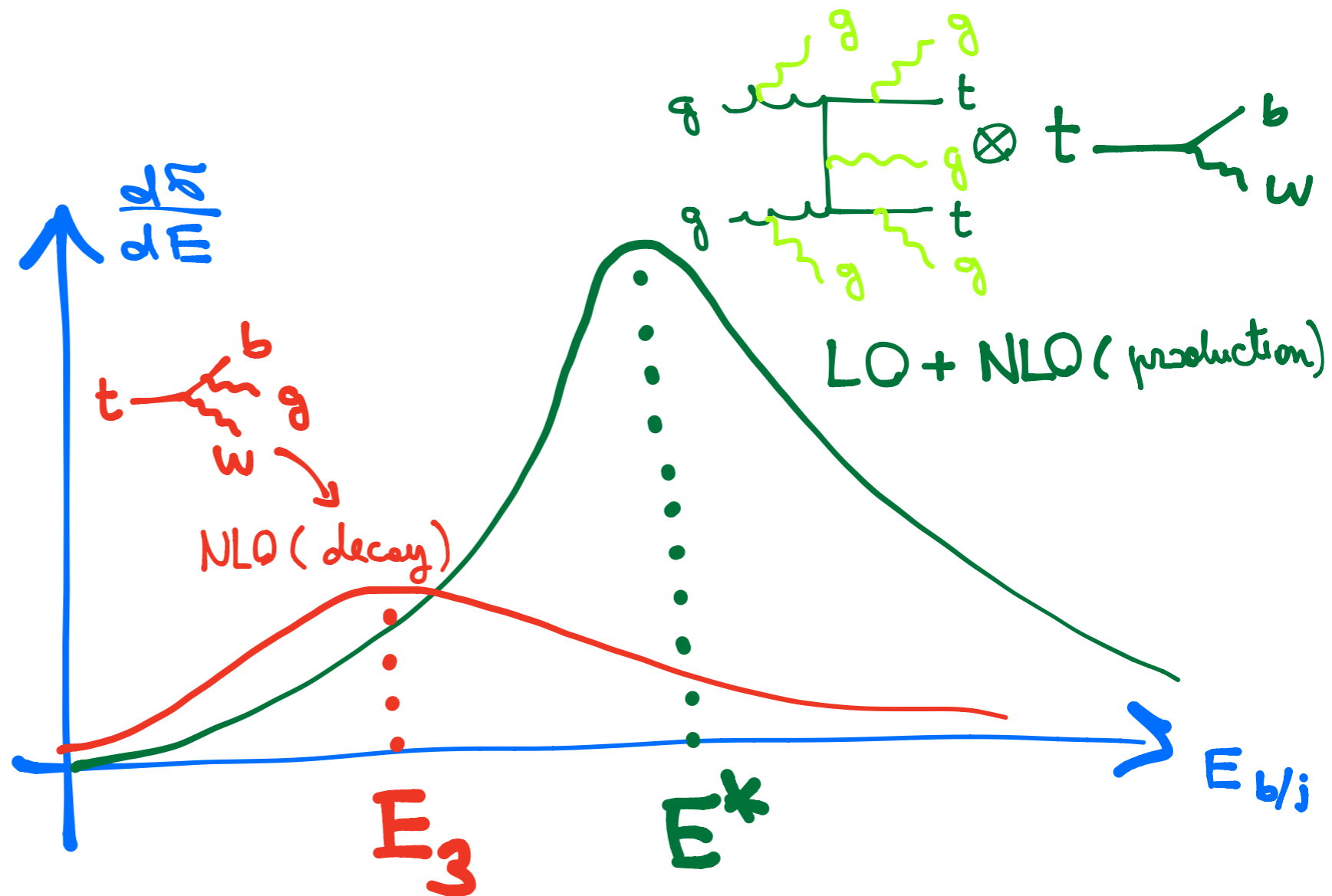
$$E^{\text{peak}} = E^* + O(1) \frac{\alpha}{4\pi} E_3$$

Peak shift at NLO



BR($t \rightarrow bWg$)
MadGraph5@LO

hard glue	Br
$p_T > 30$ GeV $dR > 0.2$	0.061
$p_T > 30$ GeV $dR > 0.4$	0.043
$p_T > 20$ GeV $dR > 0.2$	0.10
$p_T > 20$ GeV $dR > 0.4$	0.074

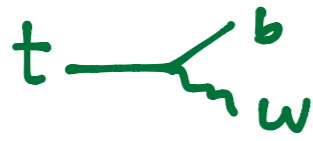


$$E^{\text{peak}} = E^* (1 - \Delta_{\text{TH}}) + \Delta_{\text{TH}} E_3$$

$$\Delta_{\text{TH}} = \text{BR}(t \rightarrow bWg) / \text{BR}(t \rightarrow bW) \approx 0.05$$

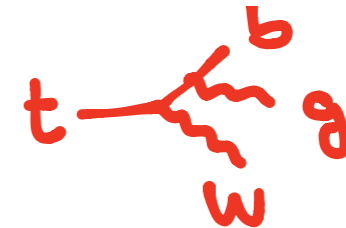
NLO: production & decay

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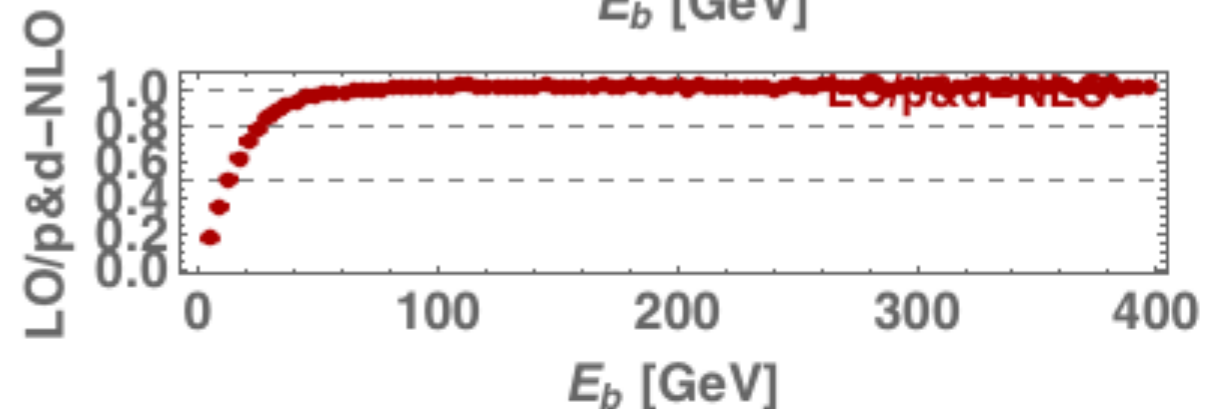
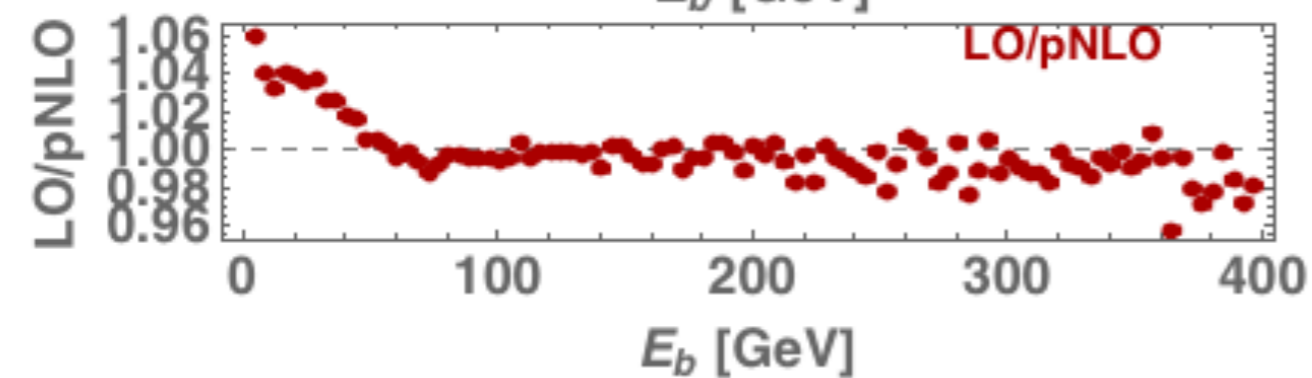
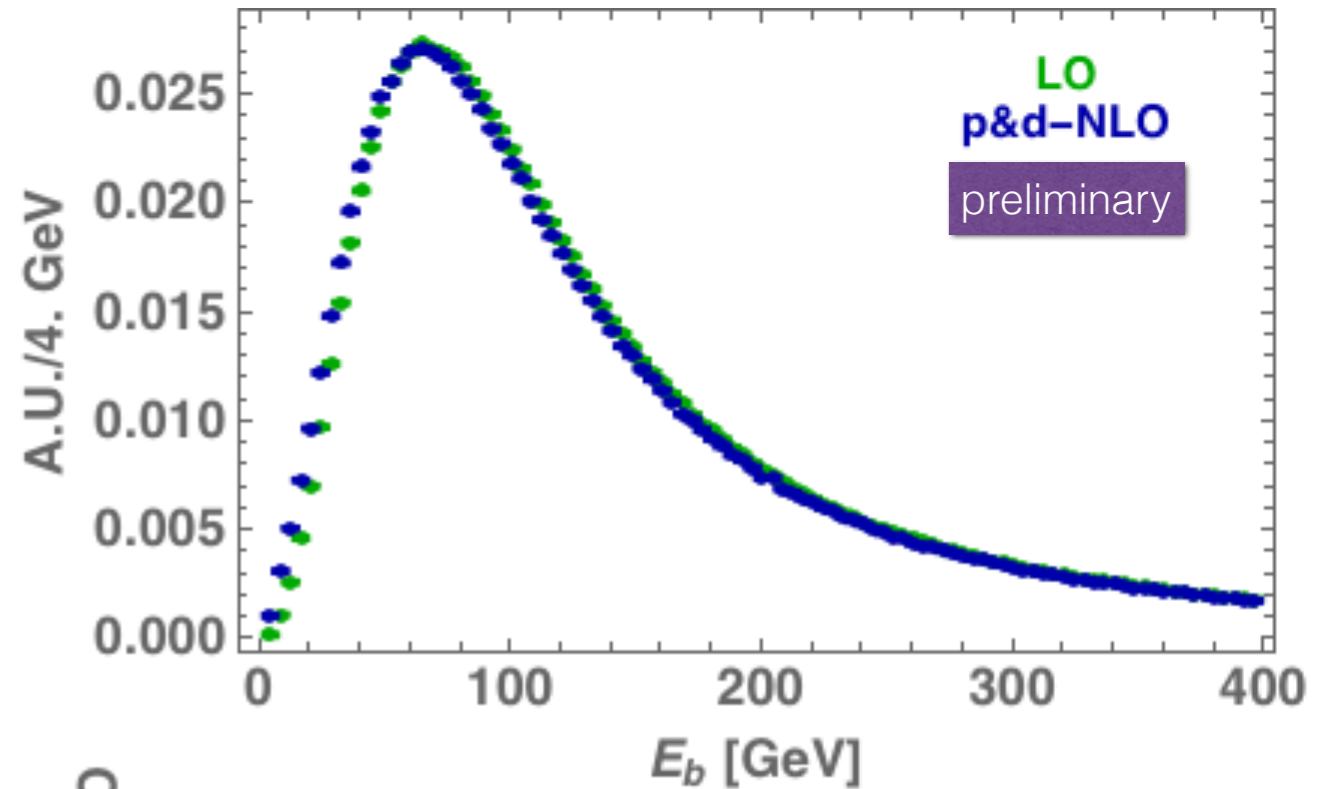
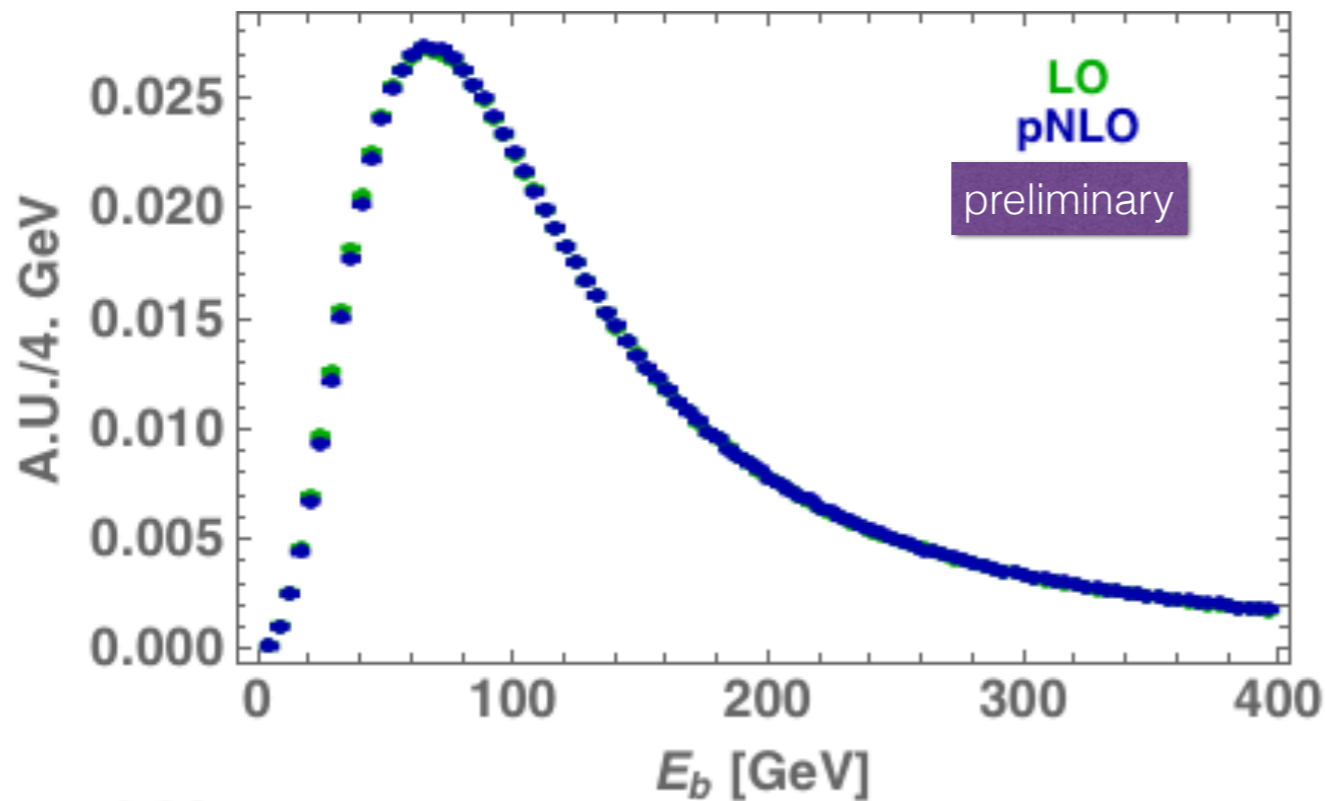


decay at LO

Energy of b



decay at NLO



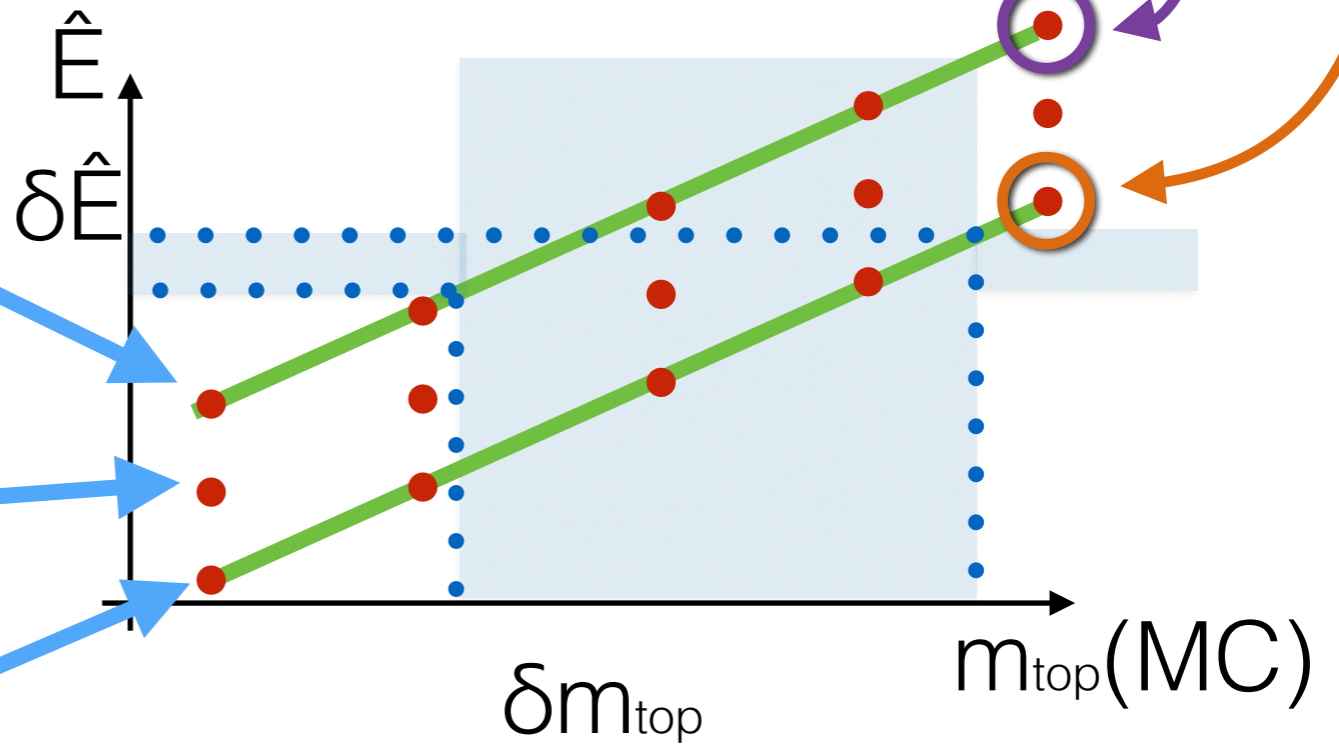
pQCD prediction: $\hat{E}(m_{\text{top}})$

1. pick top pole mass
2. pick ren./fact. scales
3. energy distribution $d\sigma/dE_b$
4. peak of the distribution \hat{E}
5. $\hat{E}(m_{\text{top}})$

pQCD

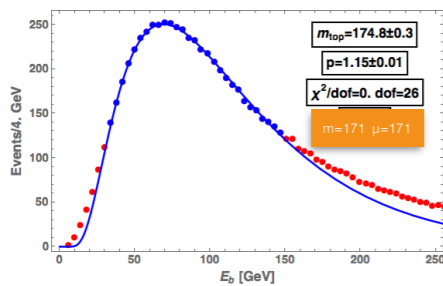
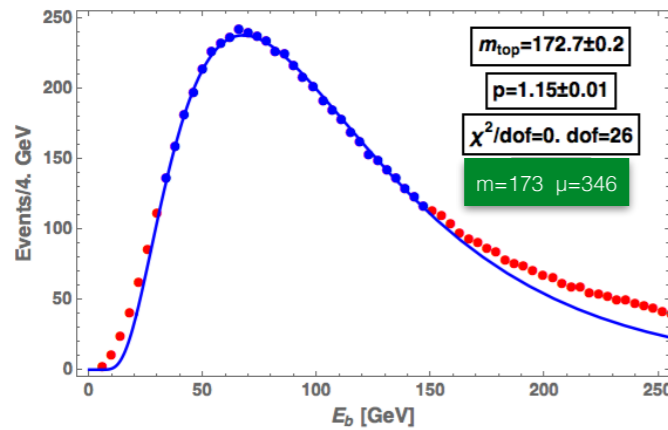
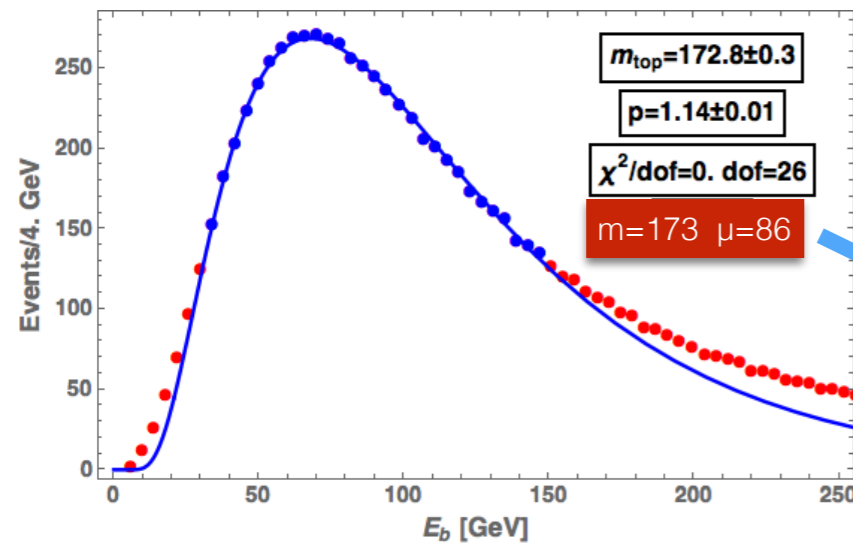
energy peaks

$$\mu \in [\mu_{\text{low}}, \mu_{\text{high}}]$$



Best:

- narrow band between μ_{high} and μ_{low}
- steep E vs. m_{top} $E_b^* = \frac{m_t^2 - m_w^2 + m_b^2}{2m_t}$



NLO $E^*(m_{\text{top}})$

Agashe, RF, Kim, Schulze - in preparation

$p_{Tj} > 30 \text{ GeV}$, $\eta_j < 2.4$, $p_{T\ell} > 20 \text{ GeV}$, $\eta_\ell < 2.4$

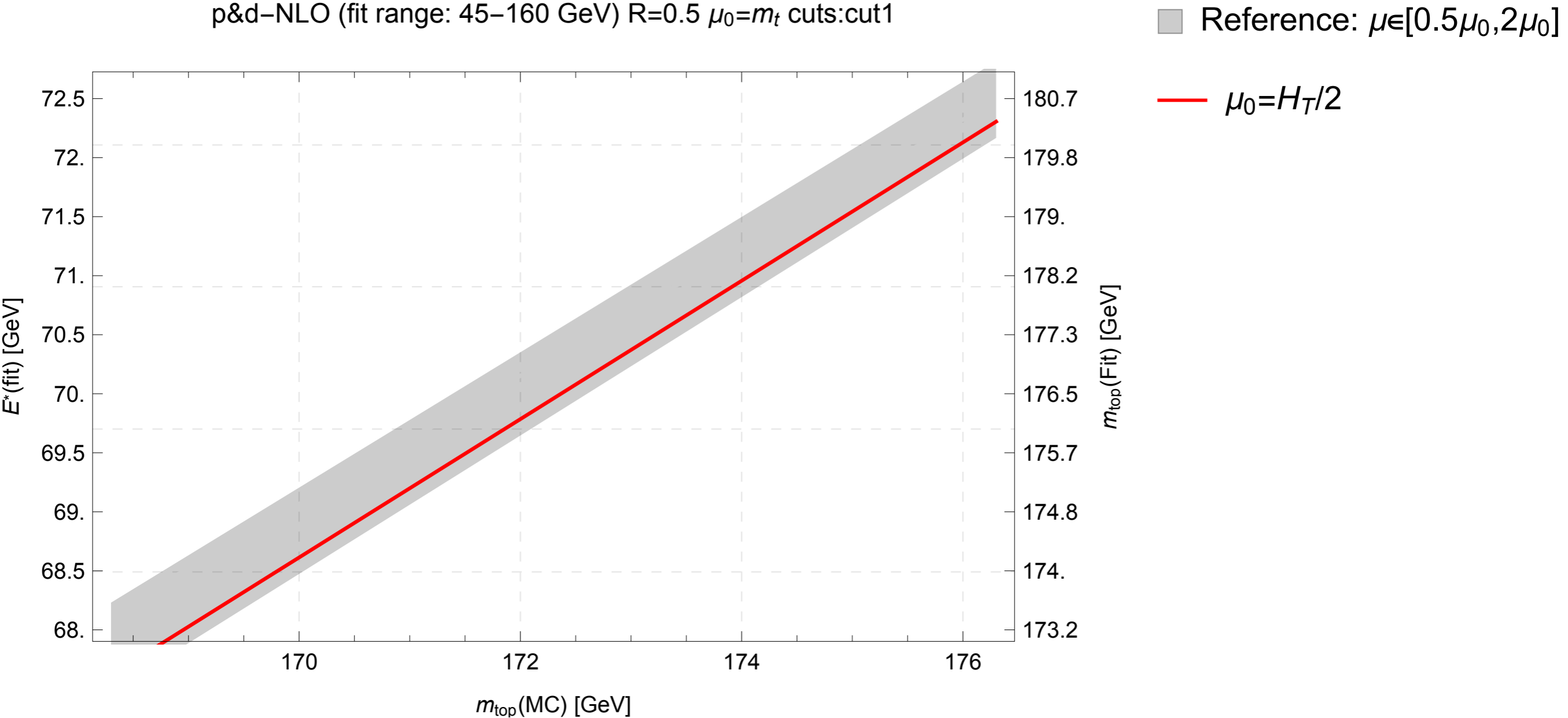
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Reference: $\sqrt{S} = 14 \text{ TeV}$ MSTW08NLO

p&d-NLO (fit range: 45–160 GeV) $R=0.5$ $\mu_0 = m_t$ cuts: cut1



NLO sensitive to the scale choice: $\pm 1 \text{ GeV}$ on m_{top}

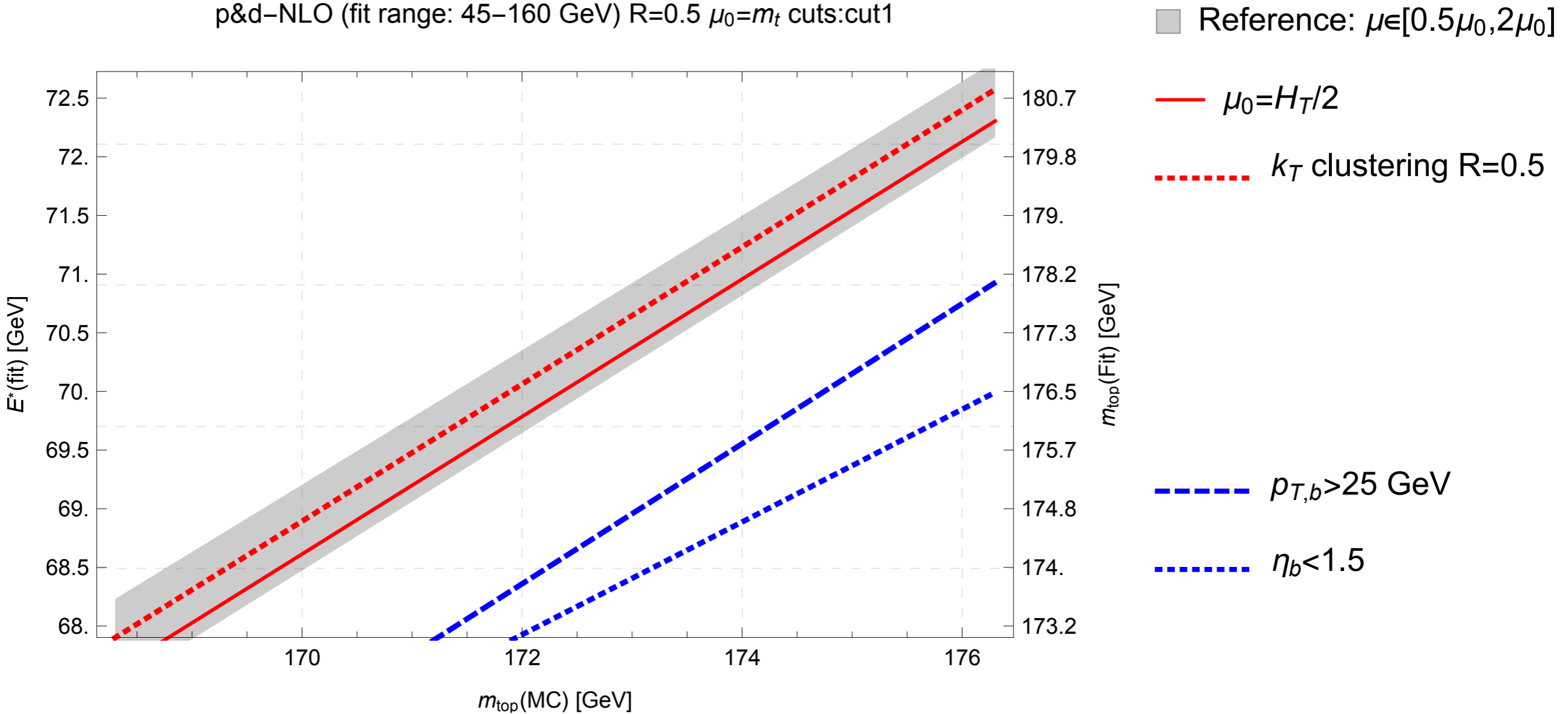
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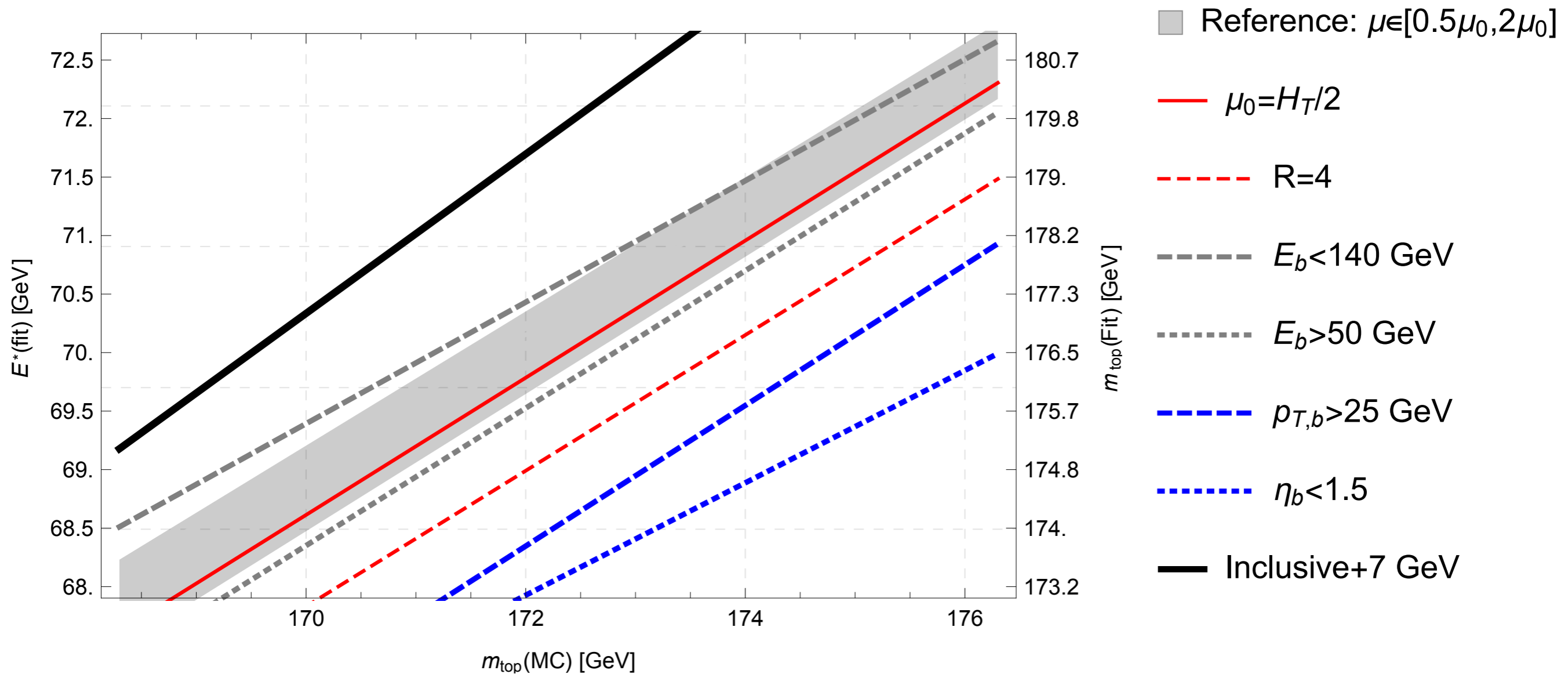
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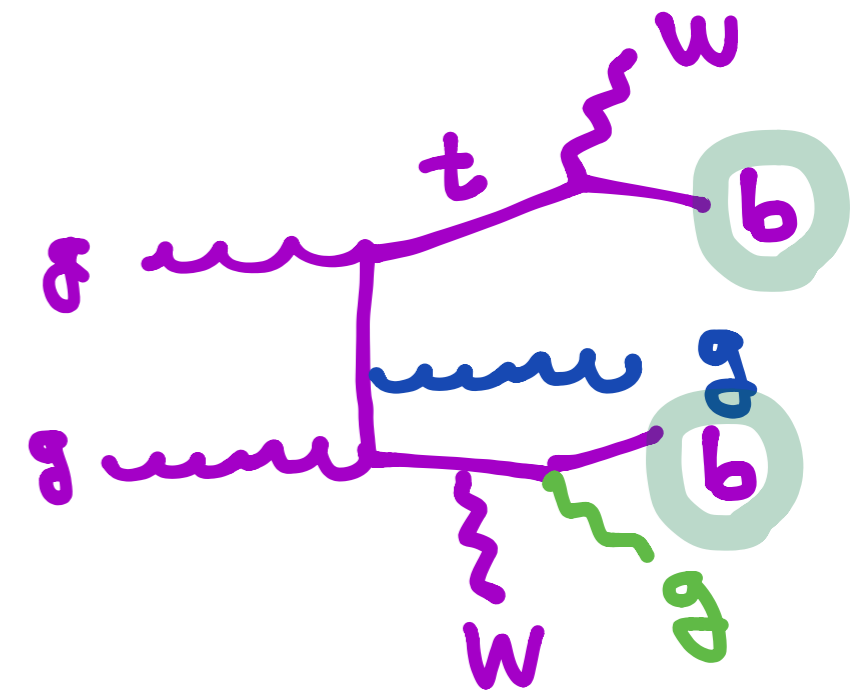
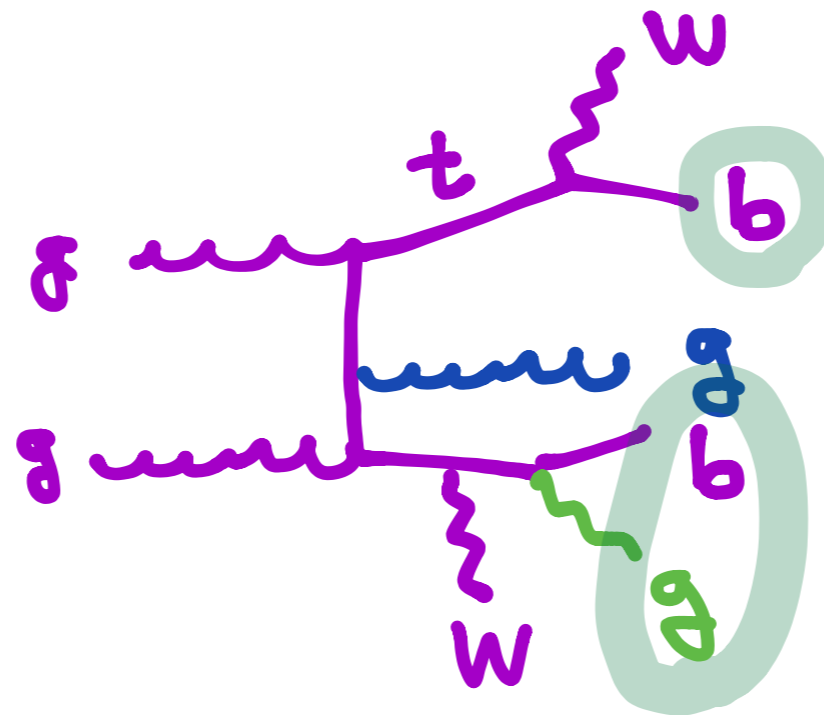
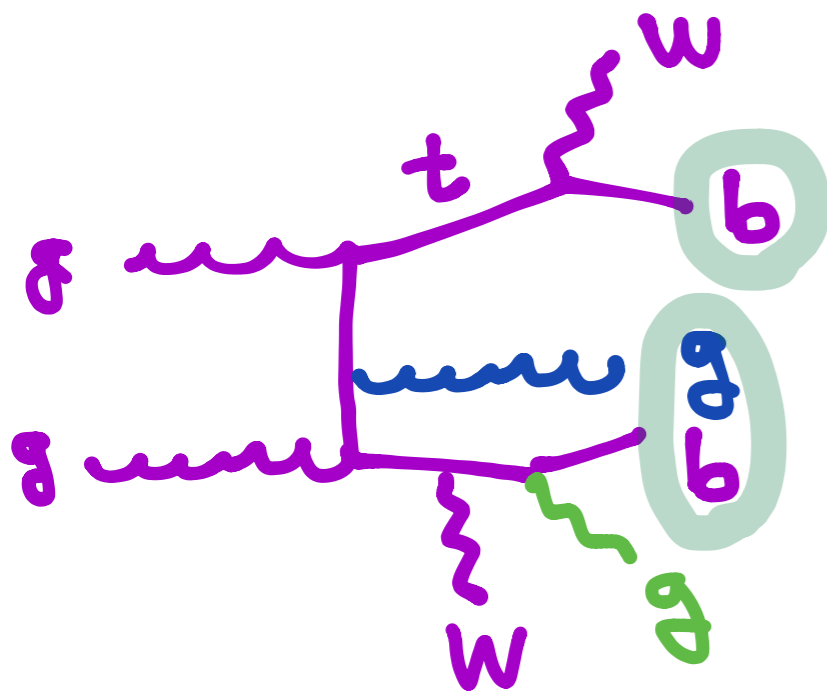


NLO sensitive to the scale choice: $\pm 1 \text{ GeV}$ on m_{top}

Parton shower uncertainties

Sensitivity to shower parameters

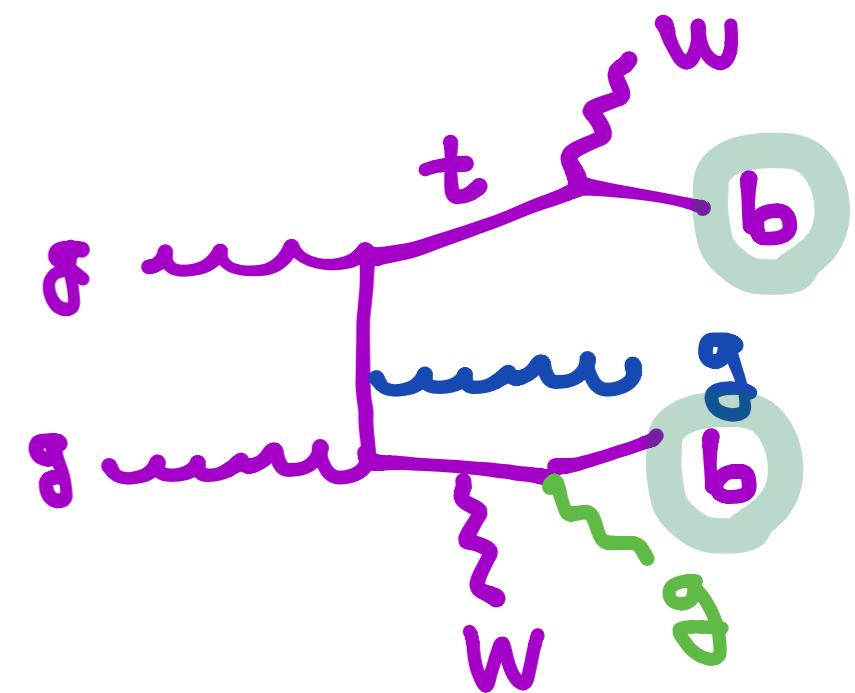
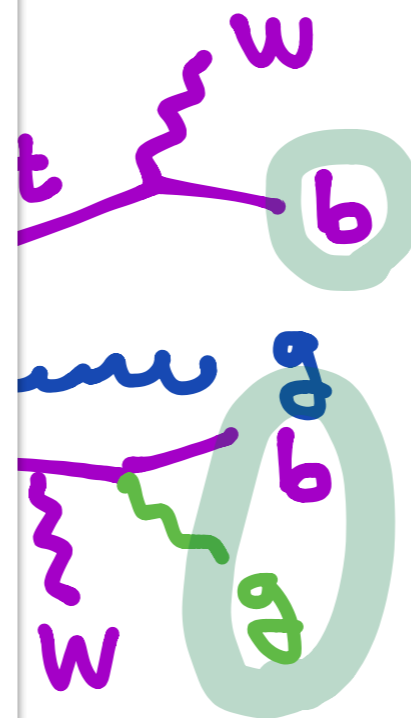
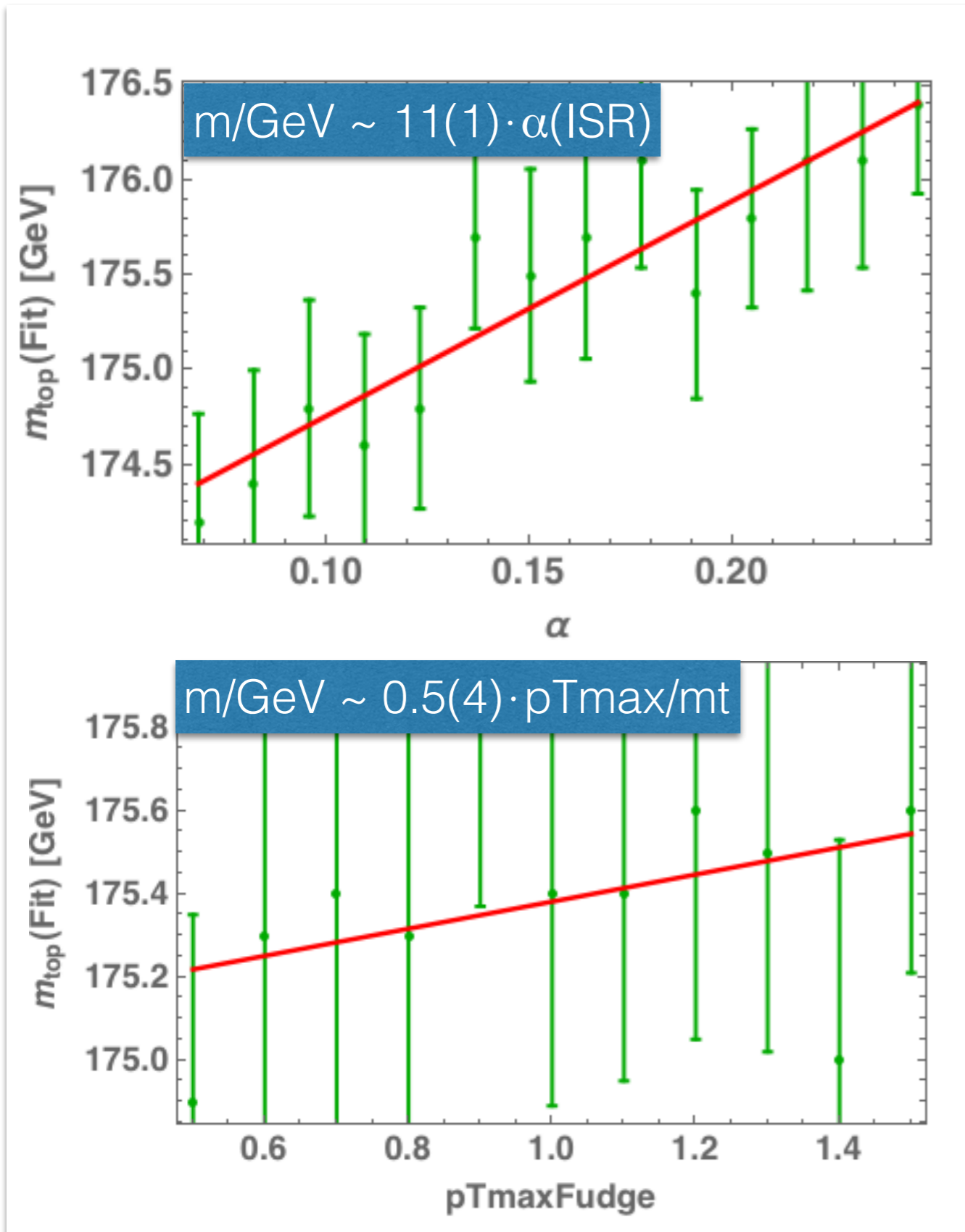
Agashe, RF, Kim, Schulze - in preparation



Parton shower uncertainties

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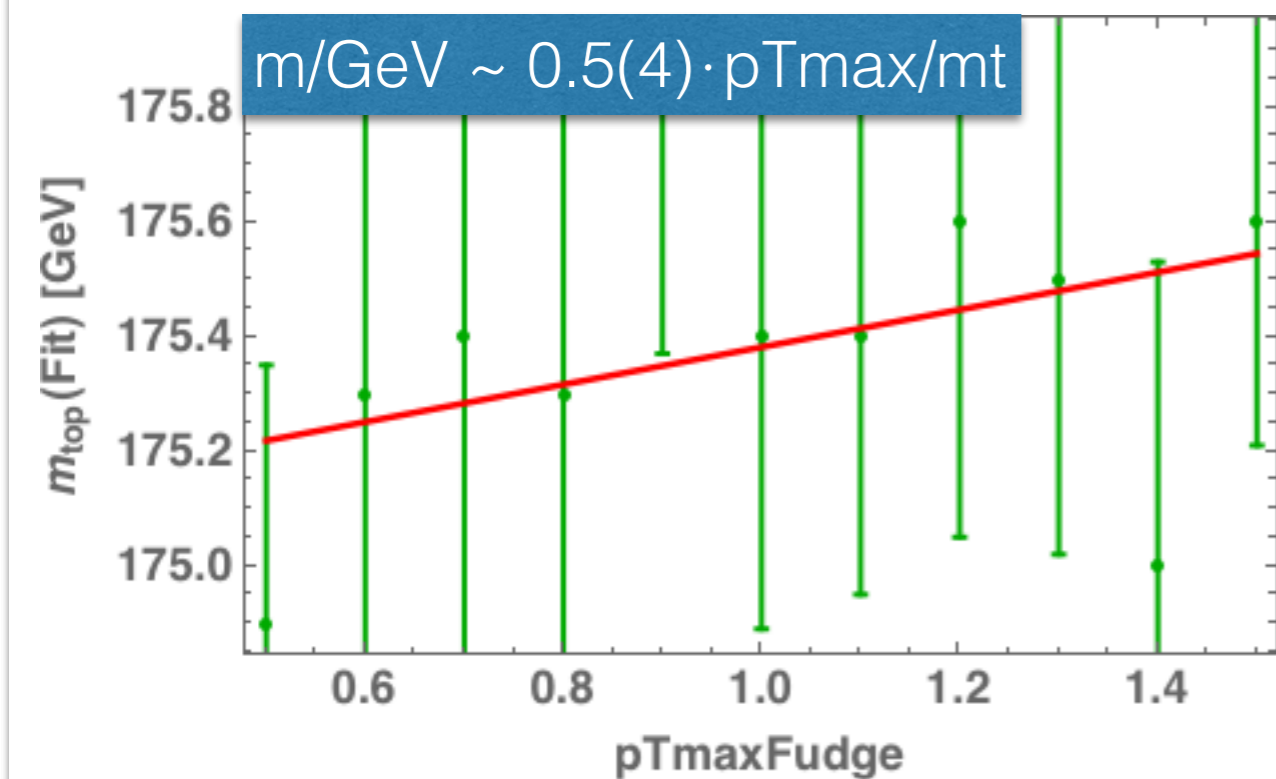
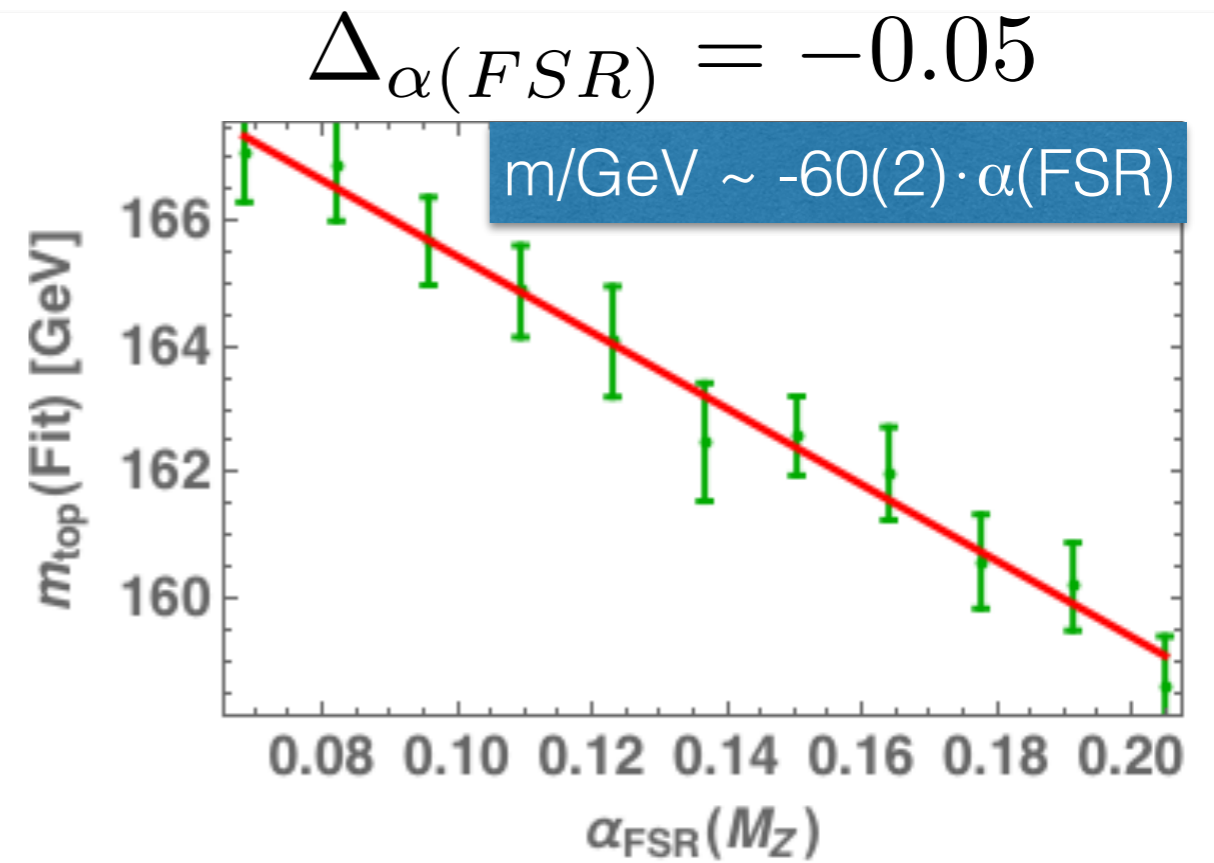
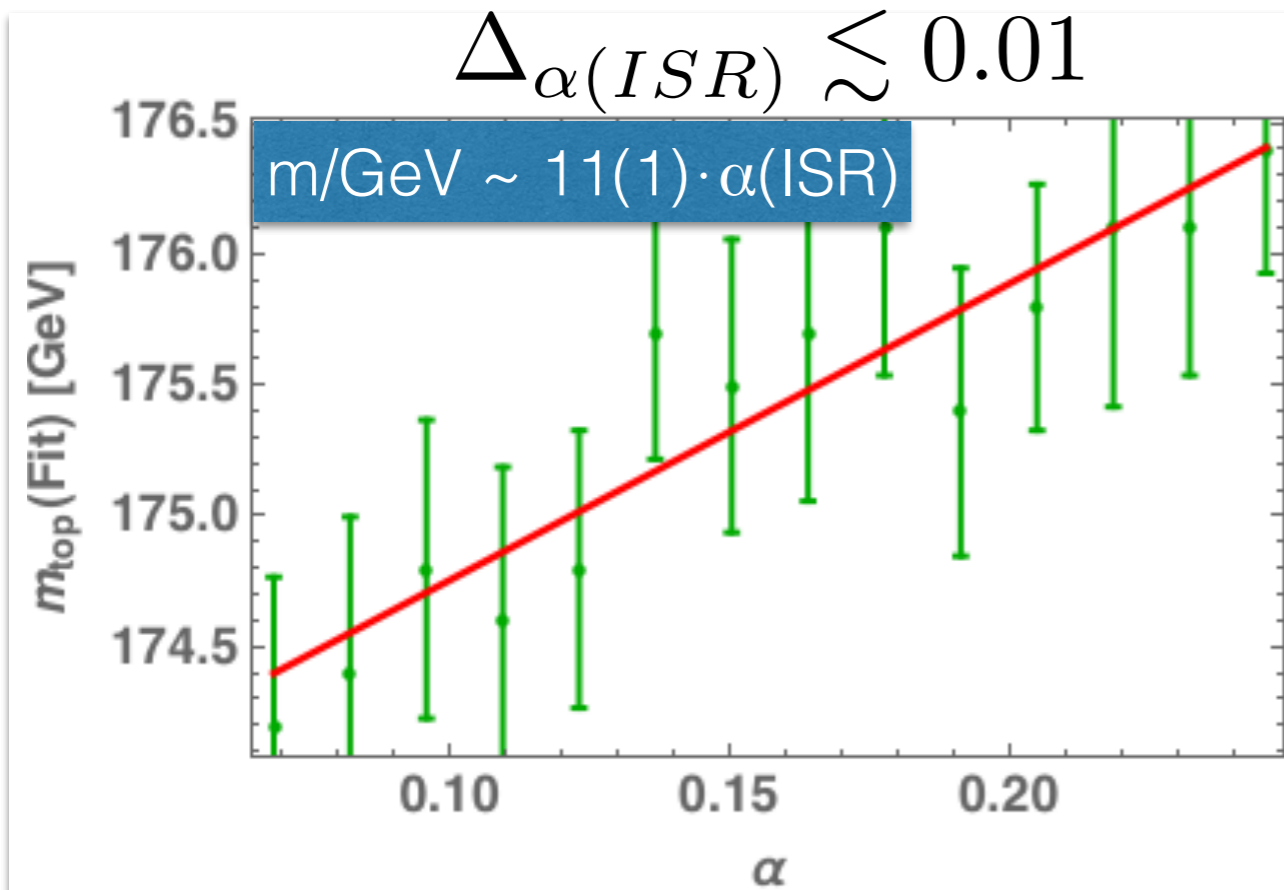
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Parton shower uncertainties

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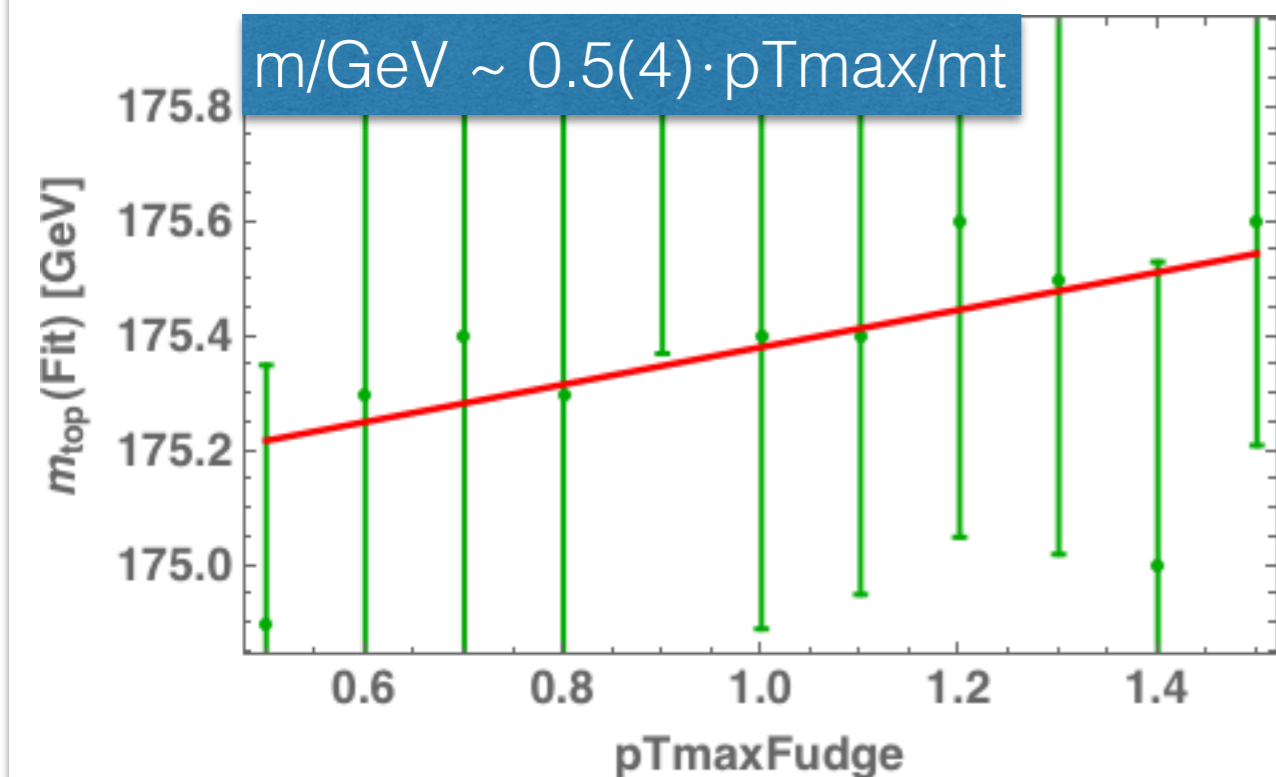
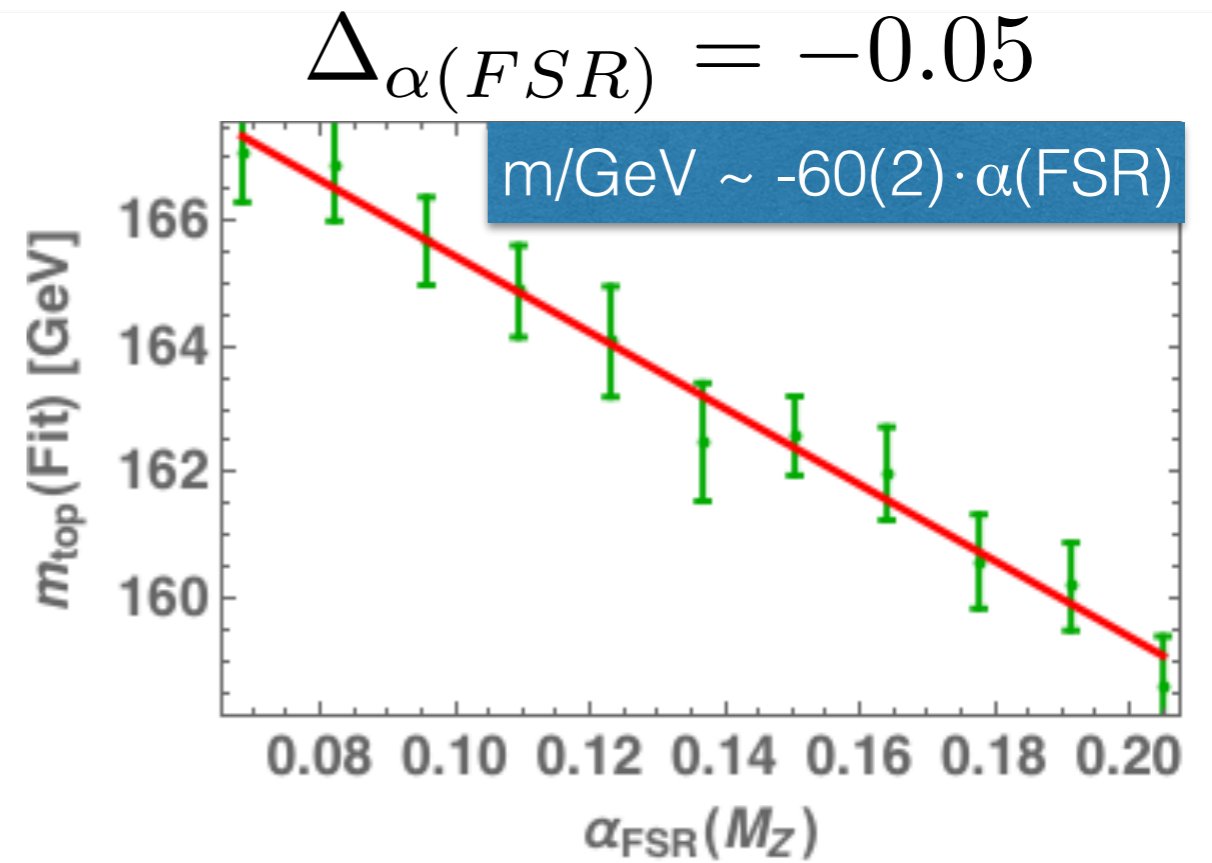
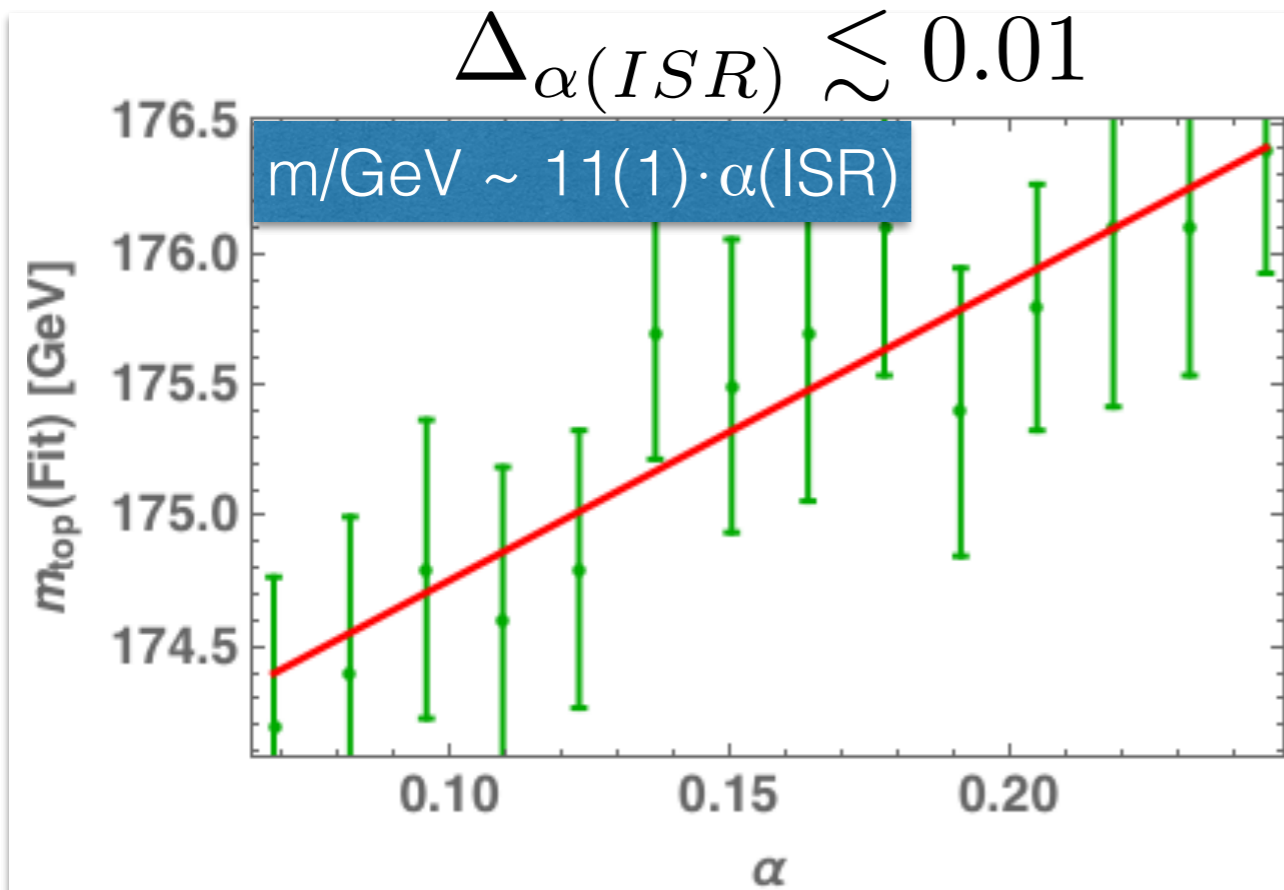
Agashe, RF, Kim, Schulze - in preparation



Parton shower uncertainties

Sensitivity to shower parameters

Agashe, RF, Kim, Schulze - in preparation



my take:

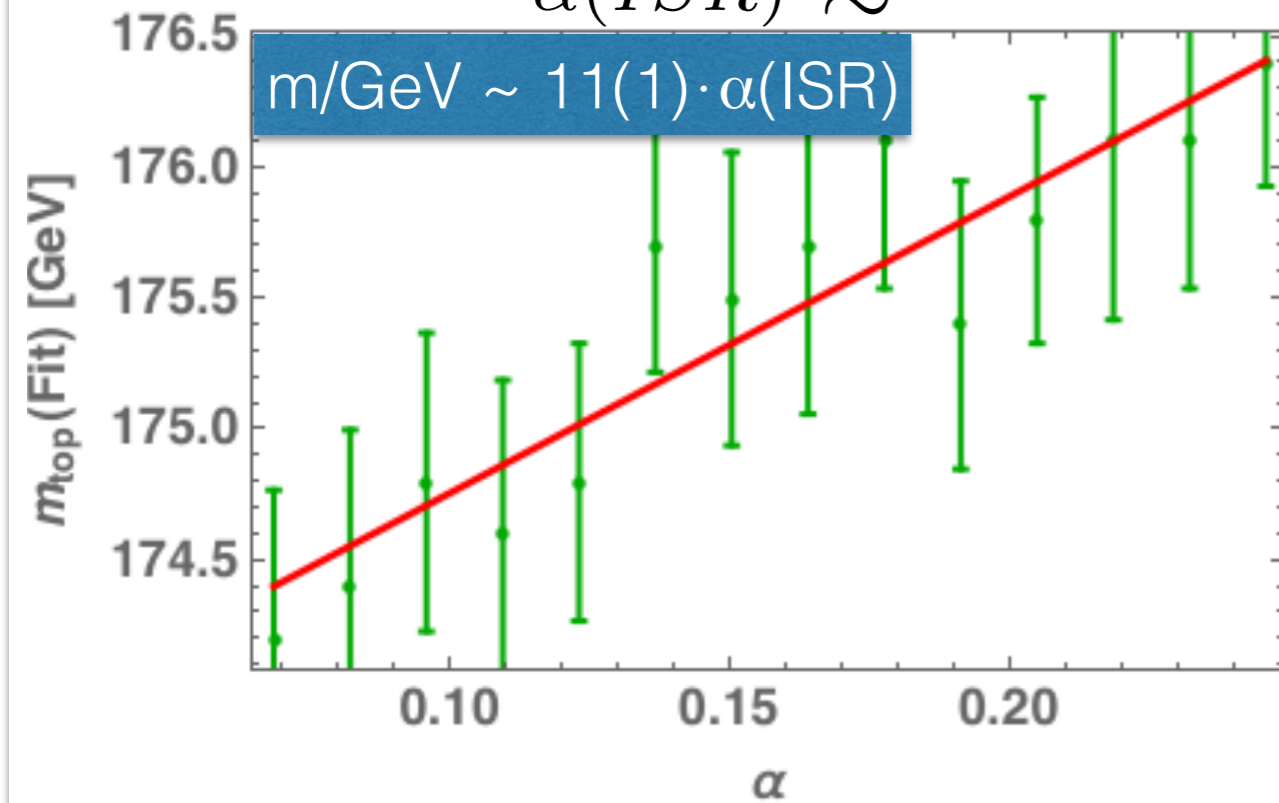
definitively ok to quote uncertainty from missing shower (well) below 1 GeV

Parton shower uncertainties

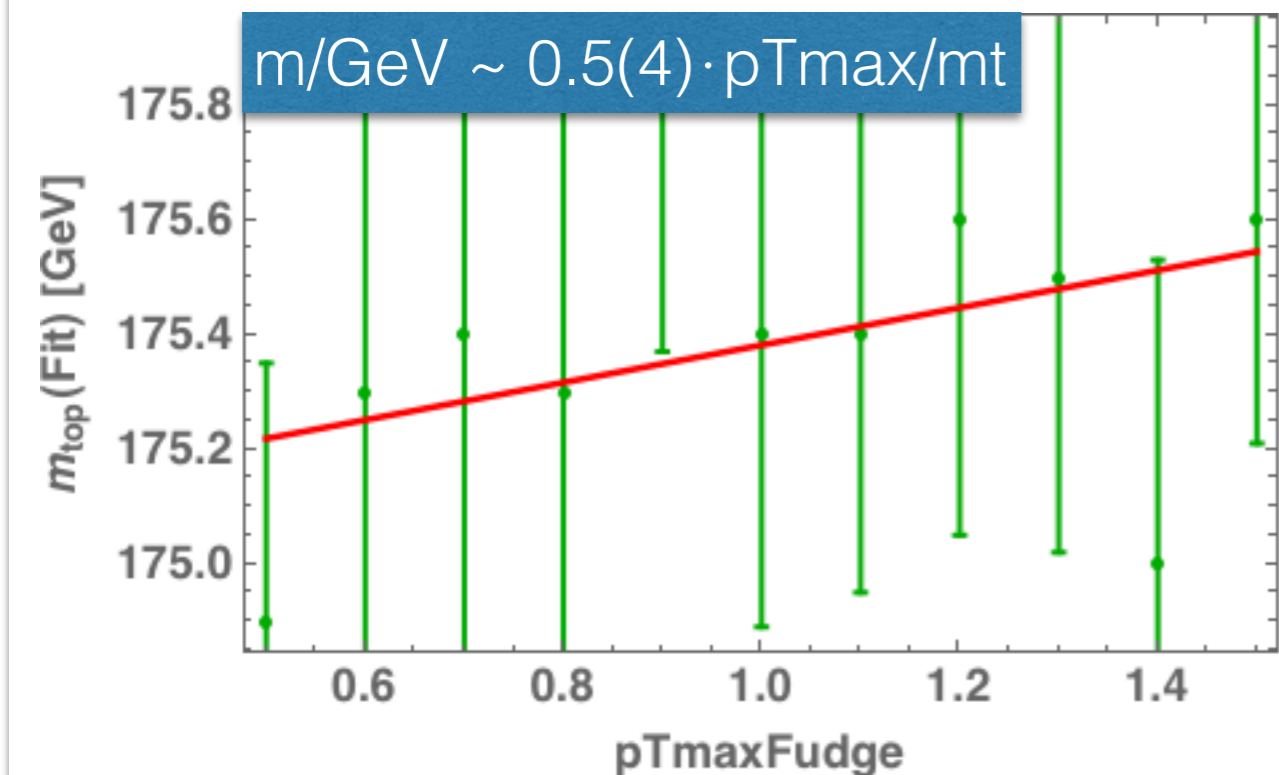
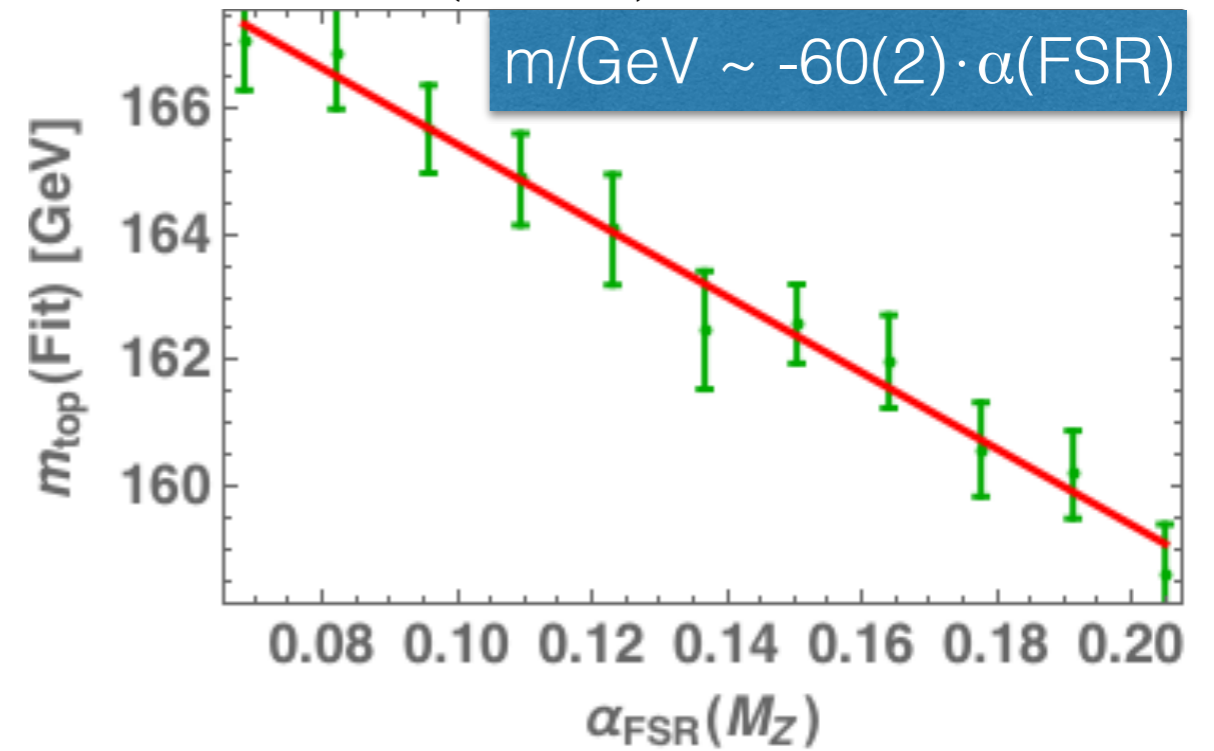
Sensitivity to shower parameters

Agashe, RF, Kim, Schulze - in preparation

$$\Delta_{\alpha}(ISR) \lesssim 0.01$$



$$\Delta_{\alpha}(\text{FSR}) = -0.05$$

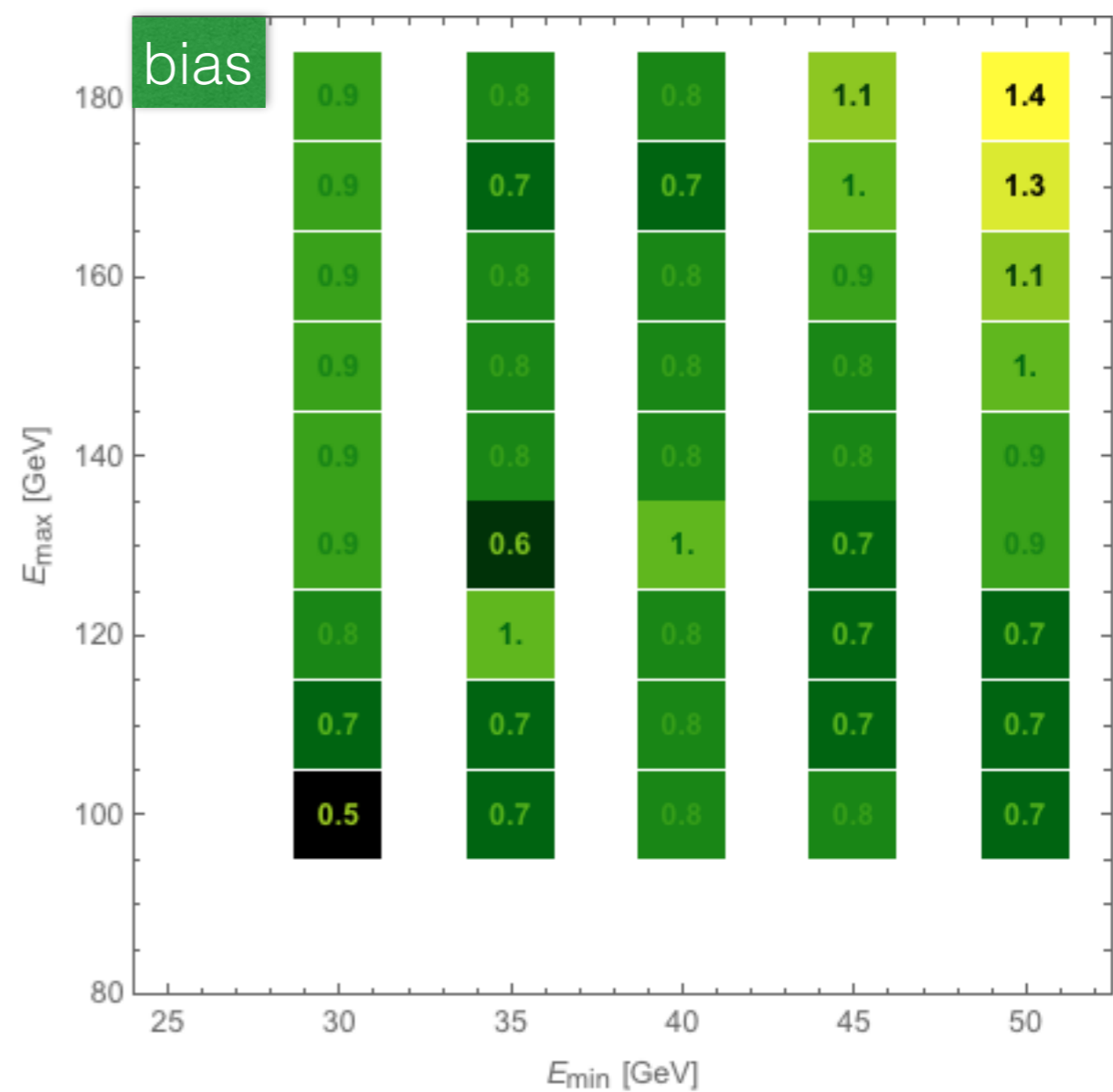
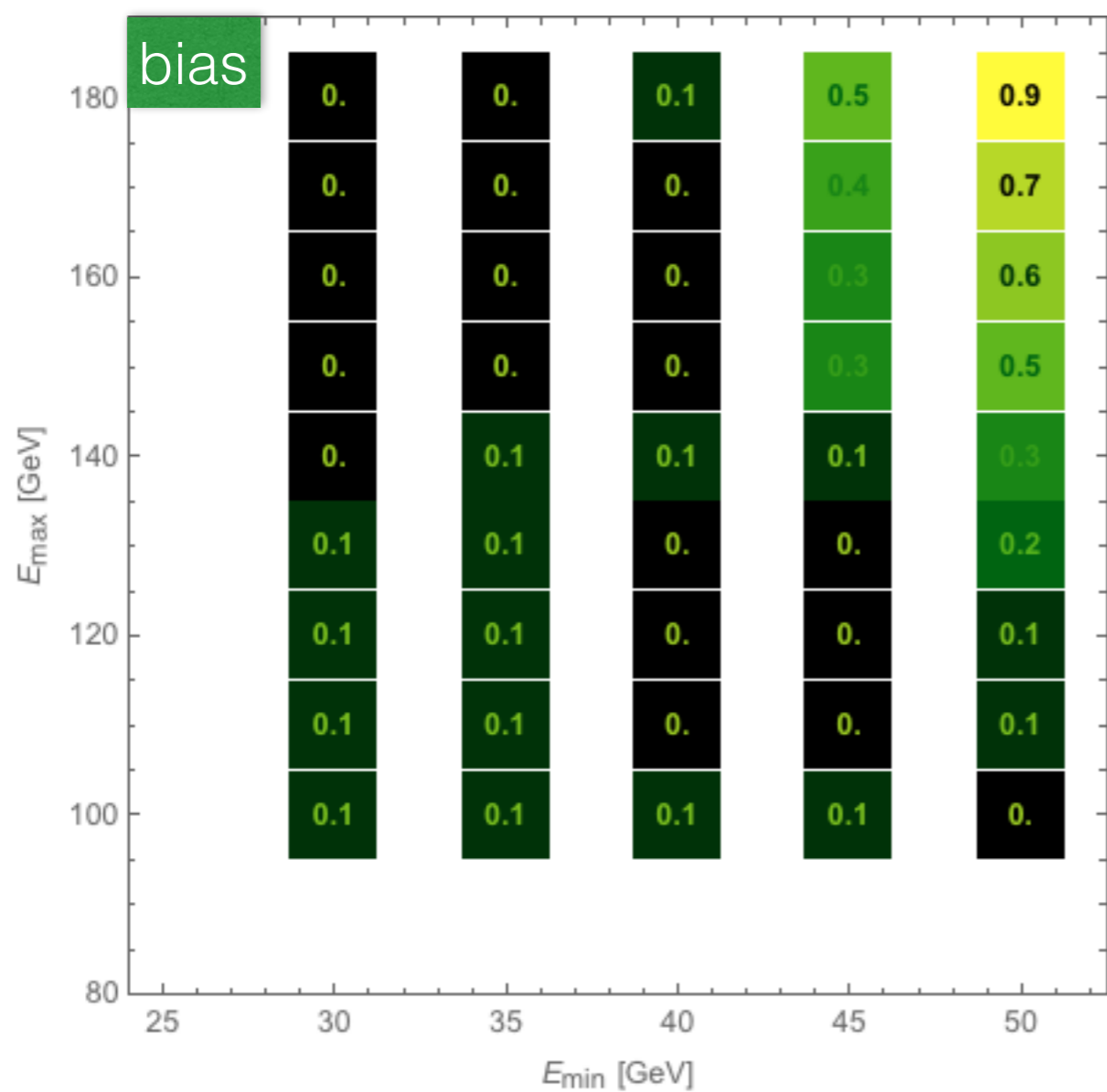
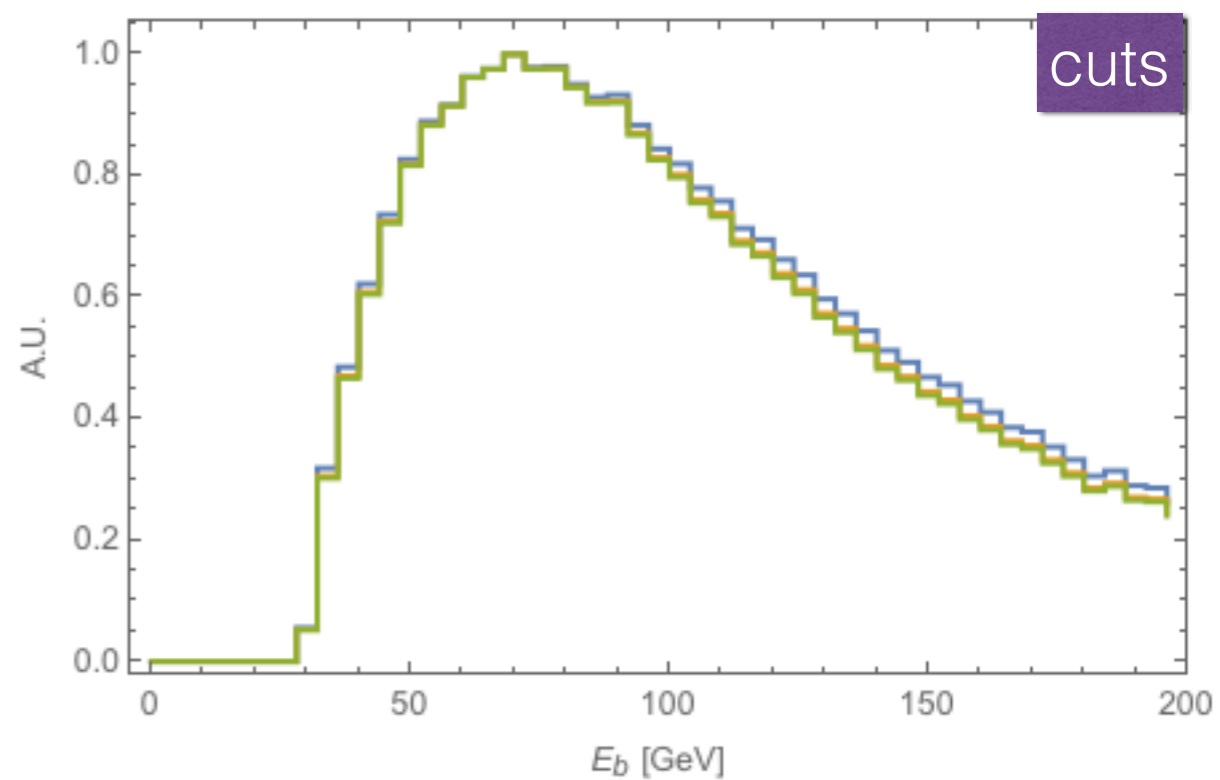
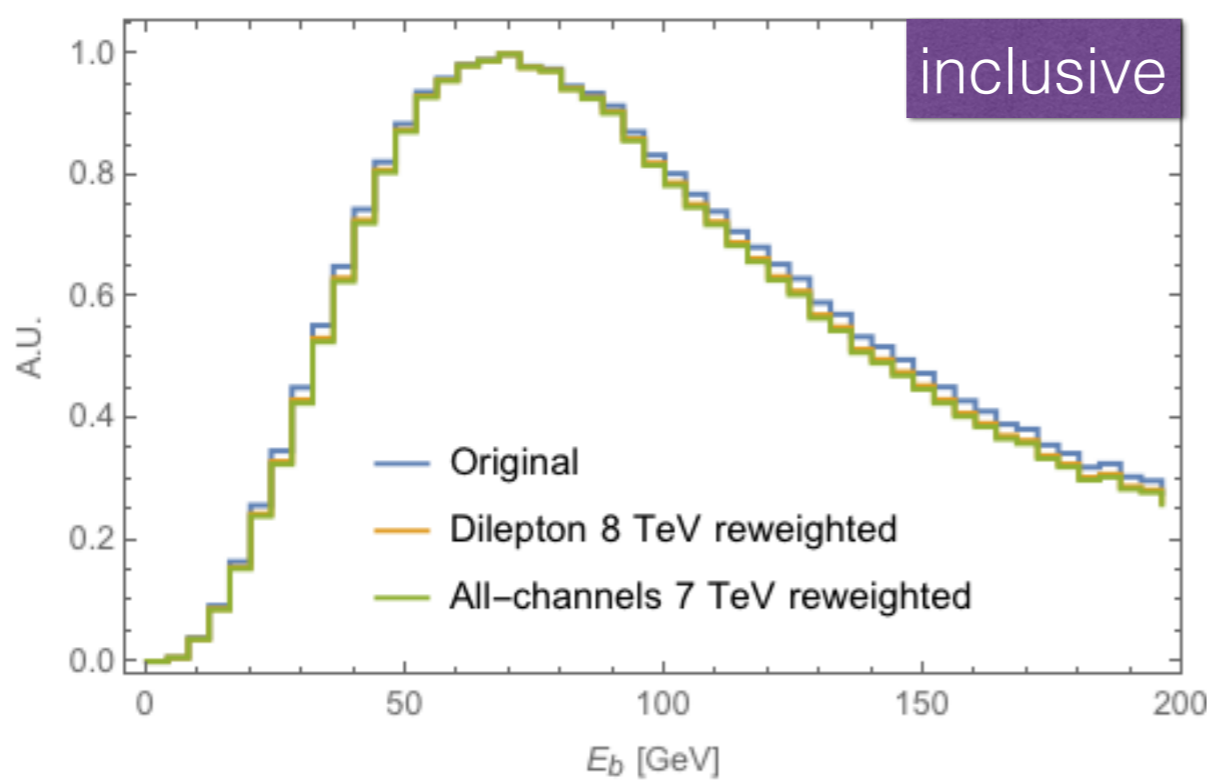


my take:

definitively ok to quote uncertainty from missing shower (well) below 1 GeV

$m(\text{pole})$ up to FSR variations?

pT(top) reweighting



What next?

ATLAS?

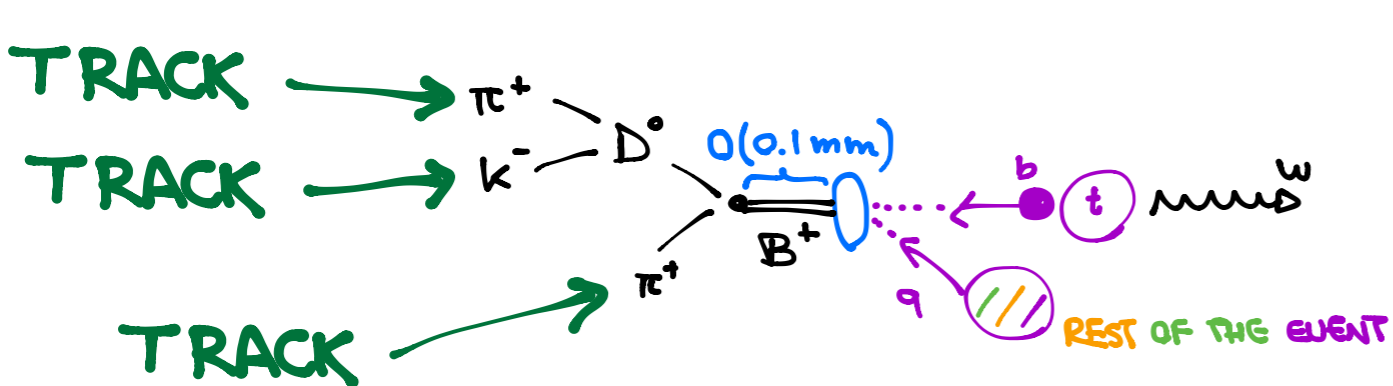
More (B hadron) peak observables

The strength of the future LHC top mass measurement will build on the **diversity of methods**
⇒ not very useful to talk about “*single best measurement*”

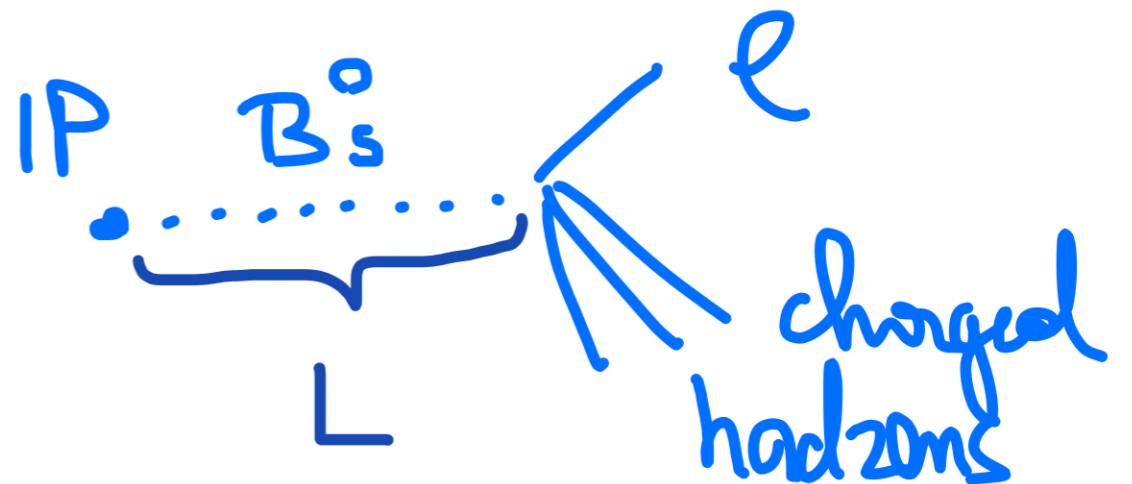
$$\frac{d\sigma}{dE_b} \propto \frac{d\sigma}{d\gamma_b} \propto \frac{d\sigma}{d\lambda}$$

hadron energy peak

get the hadron energy entirely from tracks



mean decay path peak



COMING SOON

Exclusive Decay

(Fully reconstructible with tracks)

J/psi modes

$$b \xrightarrow{\text{few} \cdot 10^{-3}} J/\psi + X \xrightarrow{10^{-1}} \ell \bar{\ell} + X$$

$$B_s^0 \rightarrow J/\psi \phi \rightarrow \mu^- \mu^+ K^+ K^- \quad 1106.4048$$

$$B^0 \rightarrow J/\psi K_S^0 \rightarrow \mu^- \mu^+ \pi^+ \pi^- \quad 1104.2892$$

$$B^+ \rightarrow J/\psi K^+ \rightarrow \mu^+ \mu^- K^+ \quad \begin{array}{l} 1101.0131 \\ 1309.6920 \end{array}$$

$$\Lambda_b \rightarrow J/\psi \Lambda \rightarrow \mu^+ \mu^- p \pi^- \quad 1205.0594$$

$$B^+ \rightarrow J/\psi K^+ (1270) \rightarrow J/\psi \rho^0 K^+ \rightarrow J/\psi \pi^+ \pi^- K^+$$

D modes

$$B^0 \xrightarrow{3 \cdot 10^{-3}} D^- \pi^+ \xrightarrow{10^{-2}} K_S^0 \pi^- \pi^+$$

$$B^0 \xrightarrow{3 \cdot 10^{-3}} D^- \pi^+ \xrightarrow{10^{-2}} K^- \pi^+ \pi^- \pi^+$$

$$B^0 \xrightarrow{3 \cdot 10^{-3}} D^- \pi^+ \xrightarrow{3 \cdot 10^{-2}} K_S^0 \pi^+ \pi^- \pi^+$$

$$B^- \xrightarrow{5 \cdot 10^{-3}} D^0 \pi^- \xrightarrow{4 \cdot 10^{-2}} K^- \pi^+ \pi^-$$

$$B^- \xrightarrow{5 \cdot 10^{-3}} D^0 \pi^- \xrightarrow{2 \cdot 10^{-2}} K^{*-} (892) \pi^+ \pi^- \rightarrow K_S^0 \pi^- \pi^+ \pi^-$$

$$B^- \xrightarrow{5 \cdot 10^{-3}} D^0 \pi^- \xrightarrow{6 \cdot 10^{-3}} K_S^0 \rho^0 \pi^-$$

$$B^- \xrightarrow{5 \cdot 10^{-3}} D^0 \pi^- \xrightarrow{5 \cdot 10^{-3}} K^- \pi^+ \rho^0 \pi^-$$

What next to next?

Precision Observable Programme on the TOP



M_{top} related observables

Distributions used for top mass should be well under control



Suitable to look for subtle effects

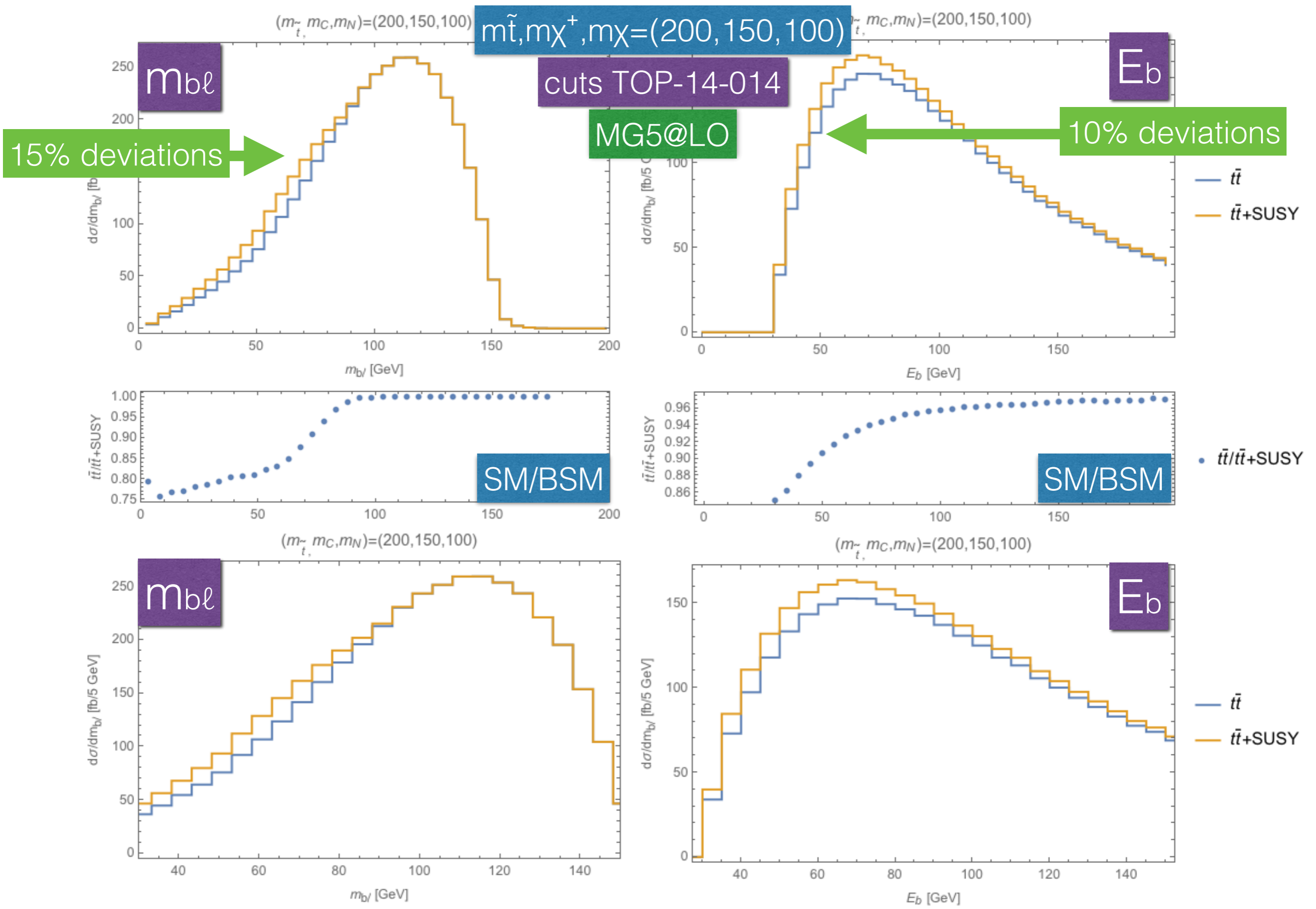
my guess for $\tilde{t} \rightarrow t\chi^0$

- $\max(m_{b\ell, \min})$ (truly?) unaffected
- m_{T2} larger end-point
- E_b affected by top polarization (maybe small)
- $p_{T\ell}, L_{xy}, s(ttj)$, affected by top boost (maybe small)

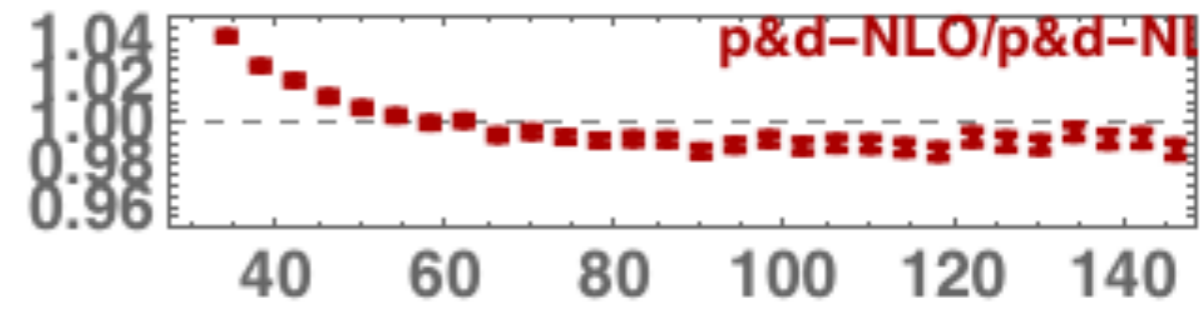
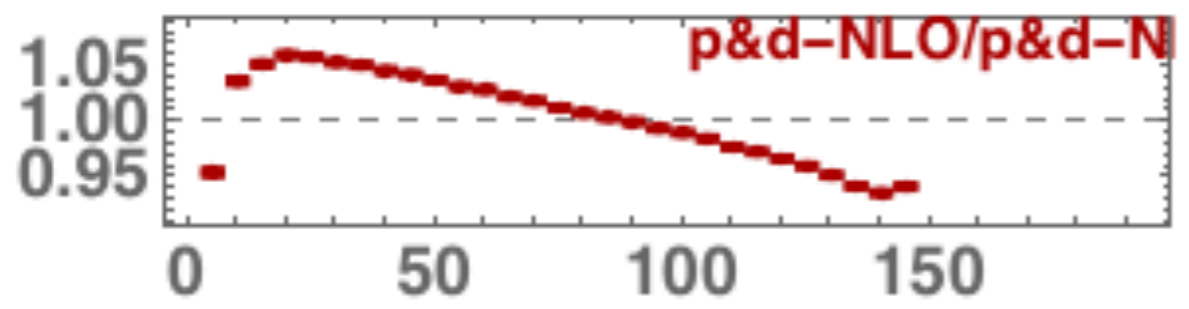
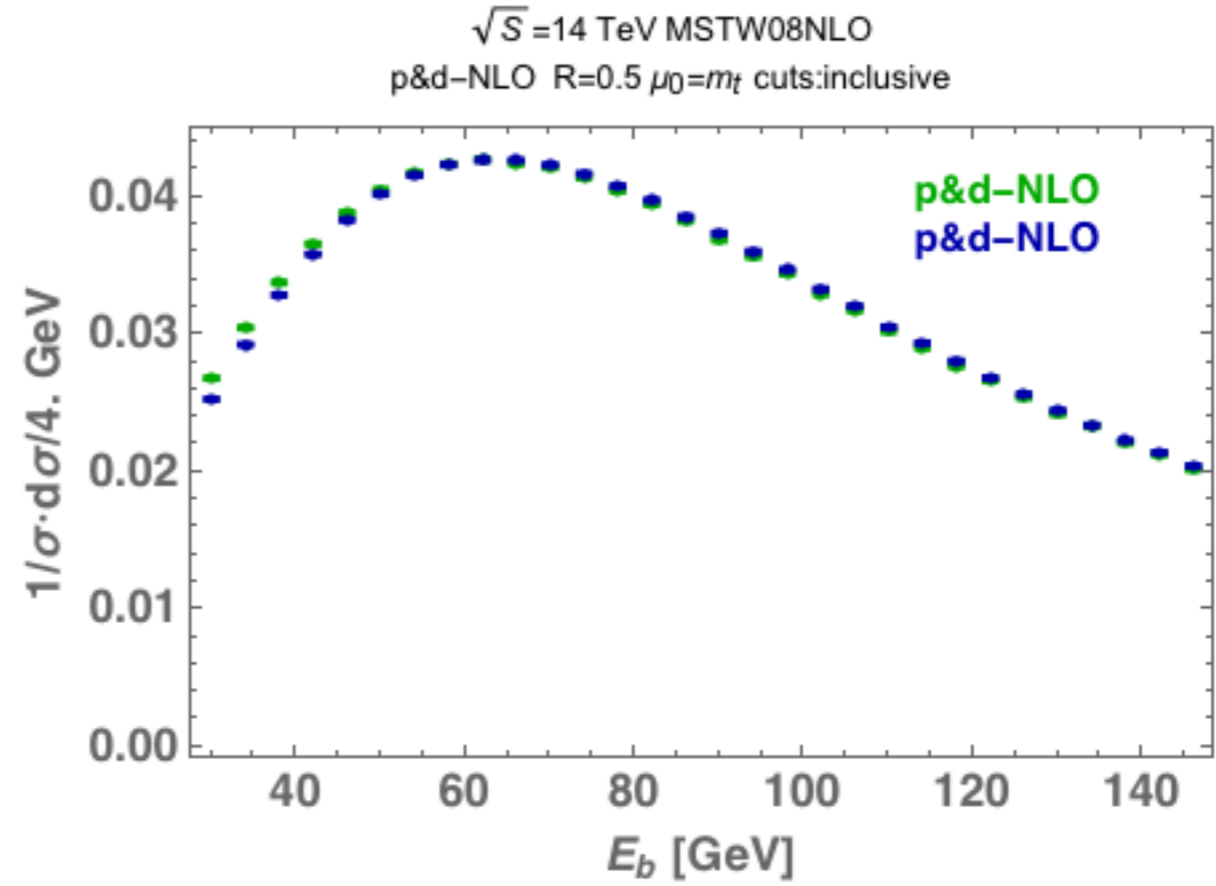
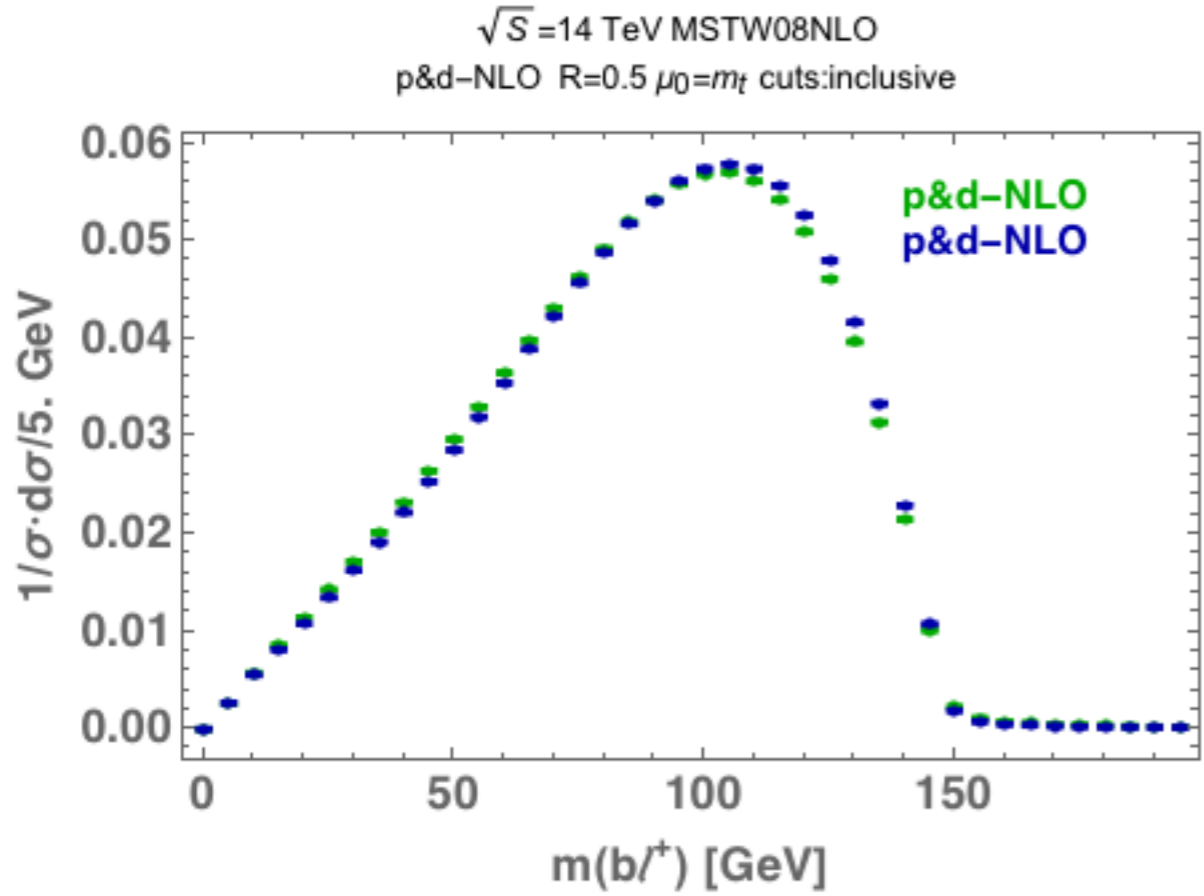
To know the answer we need to see signal injections

New physics effect on $m_{b\ell}$ and E_b

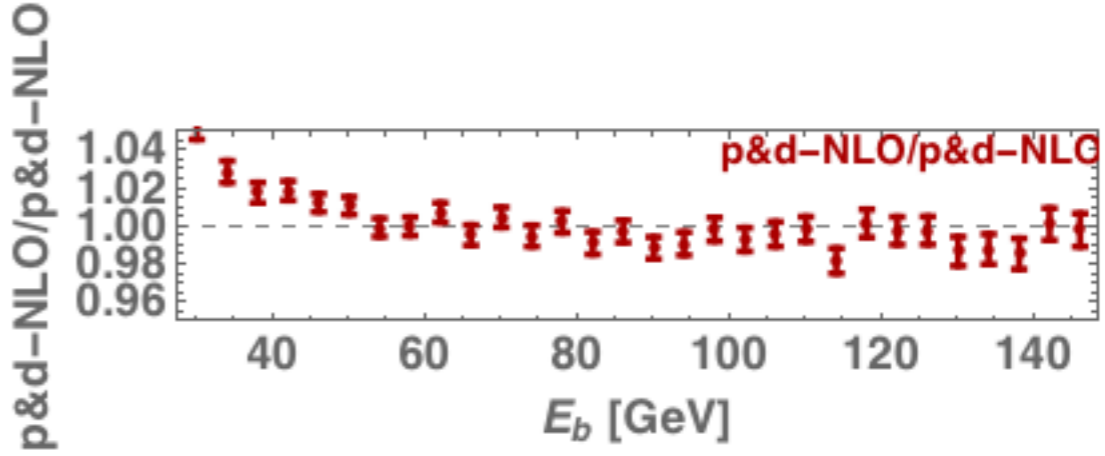
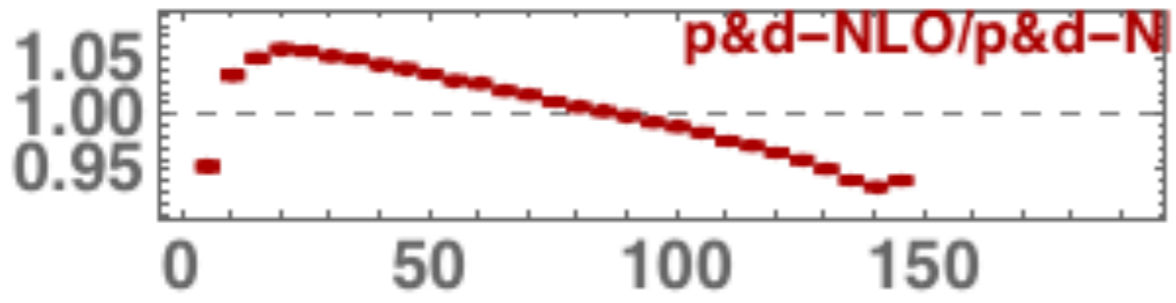
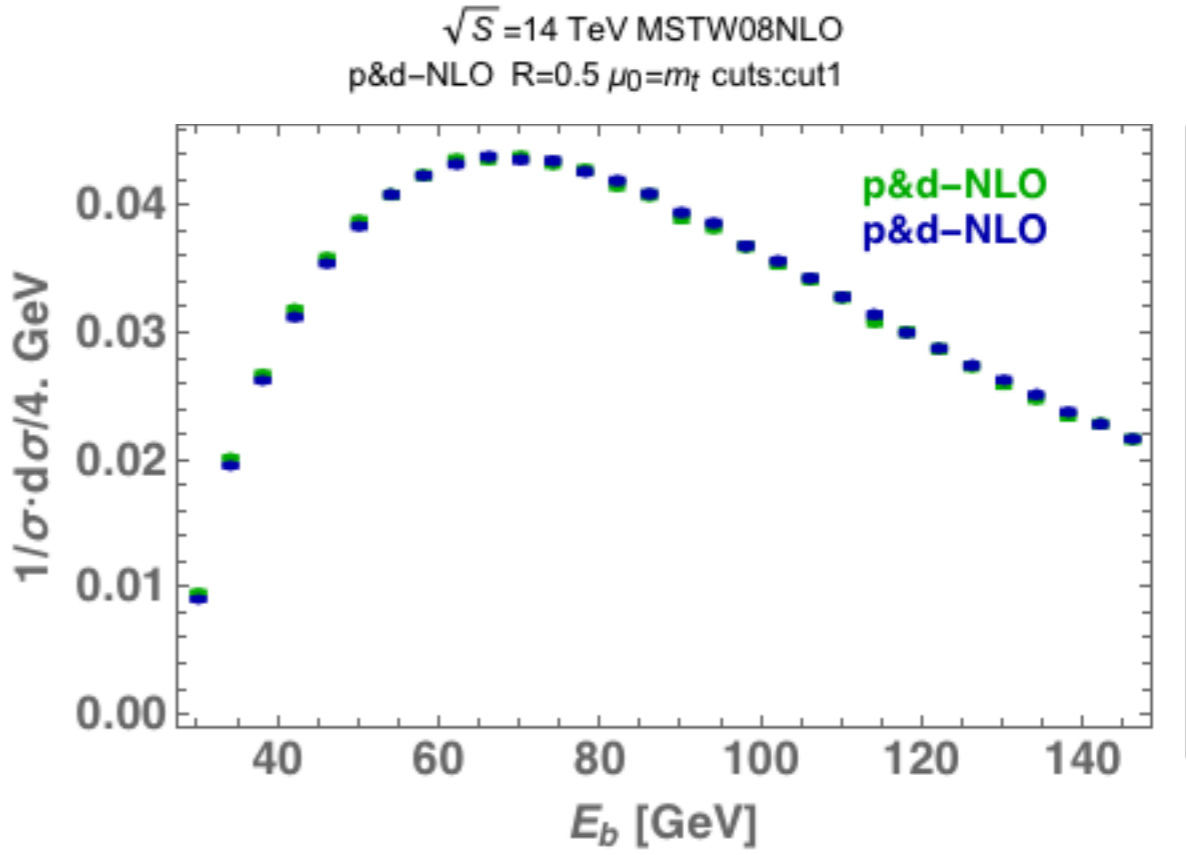
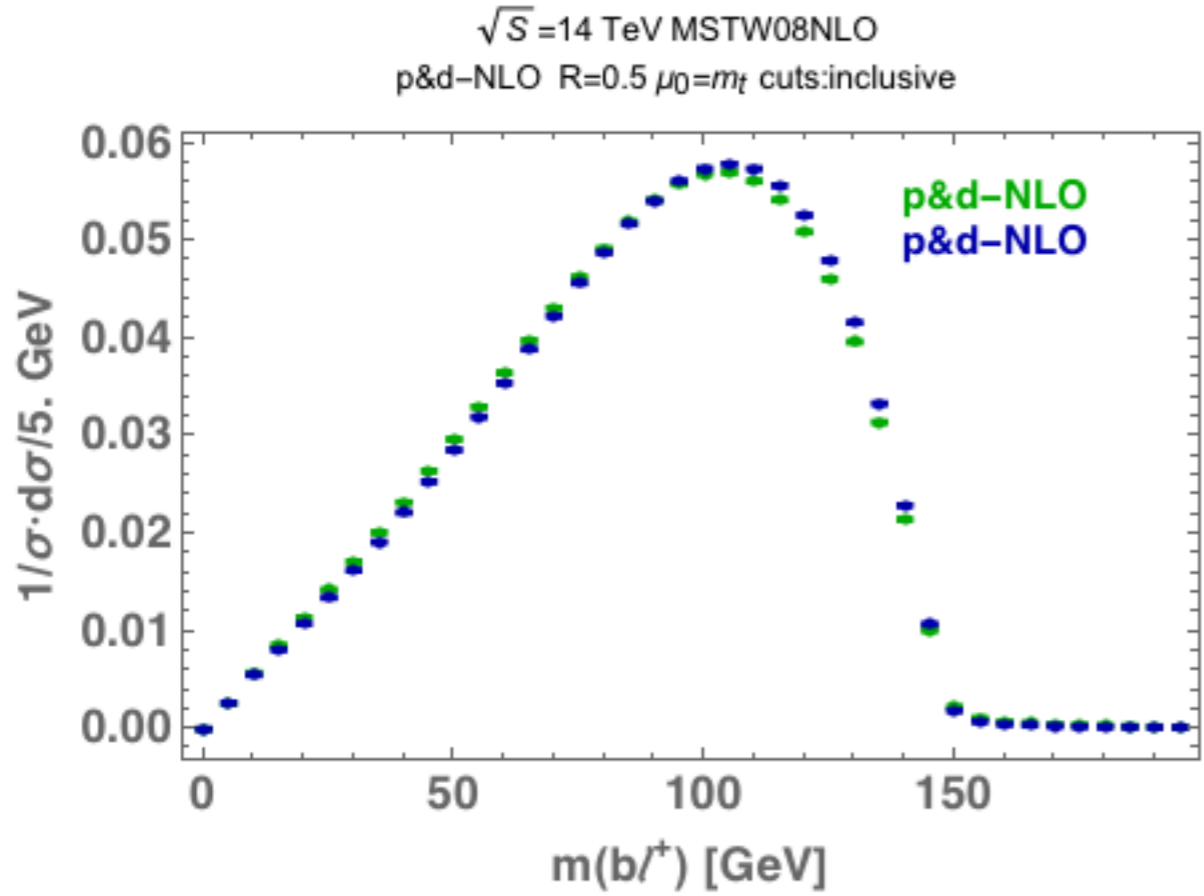
with G. Polesello



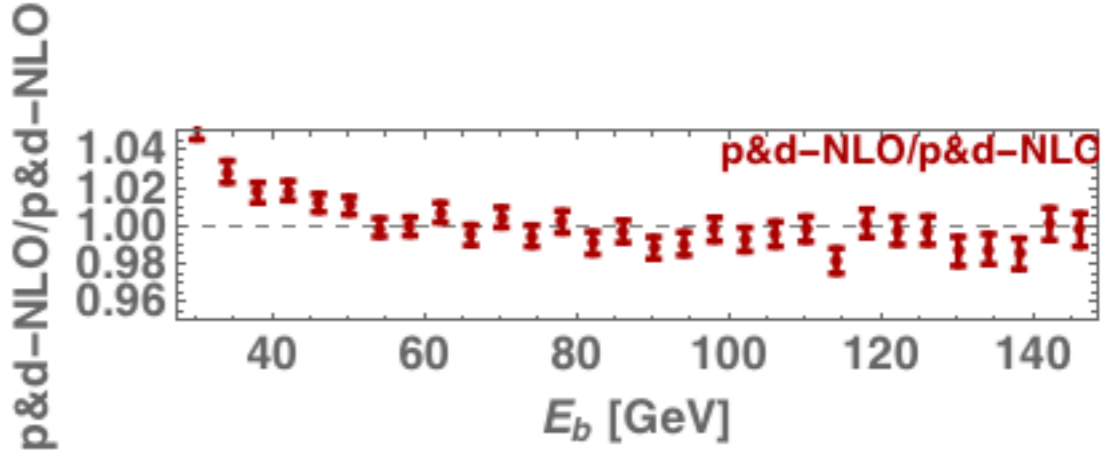
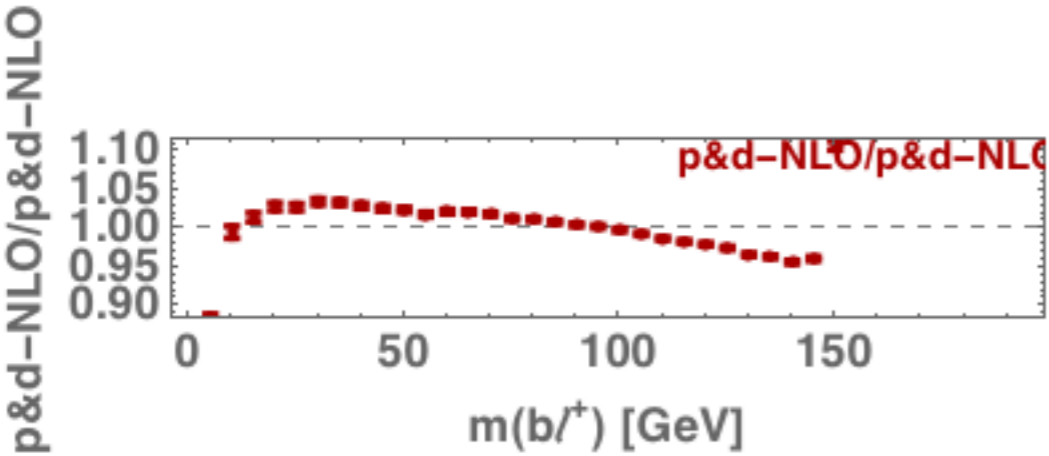
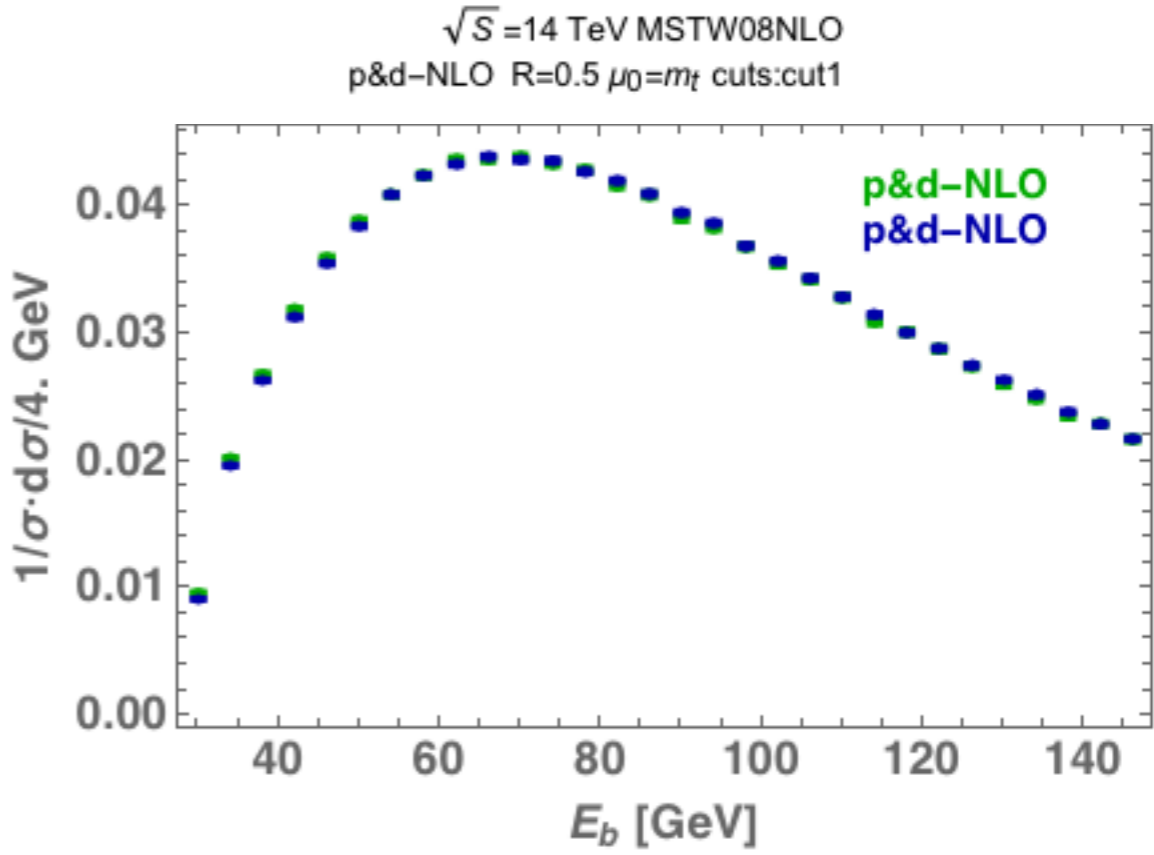
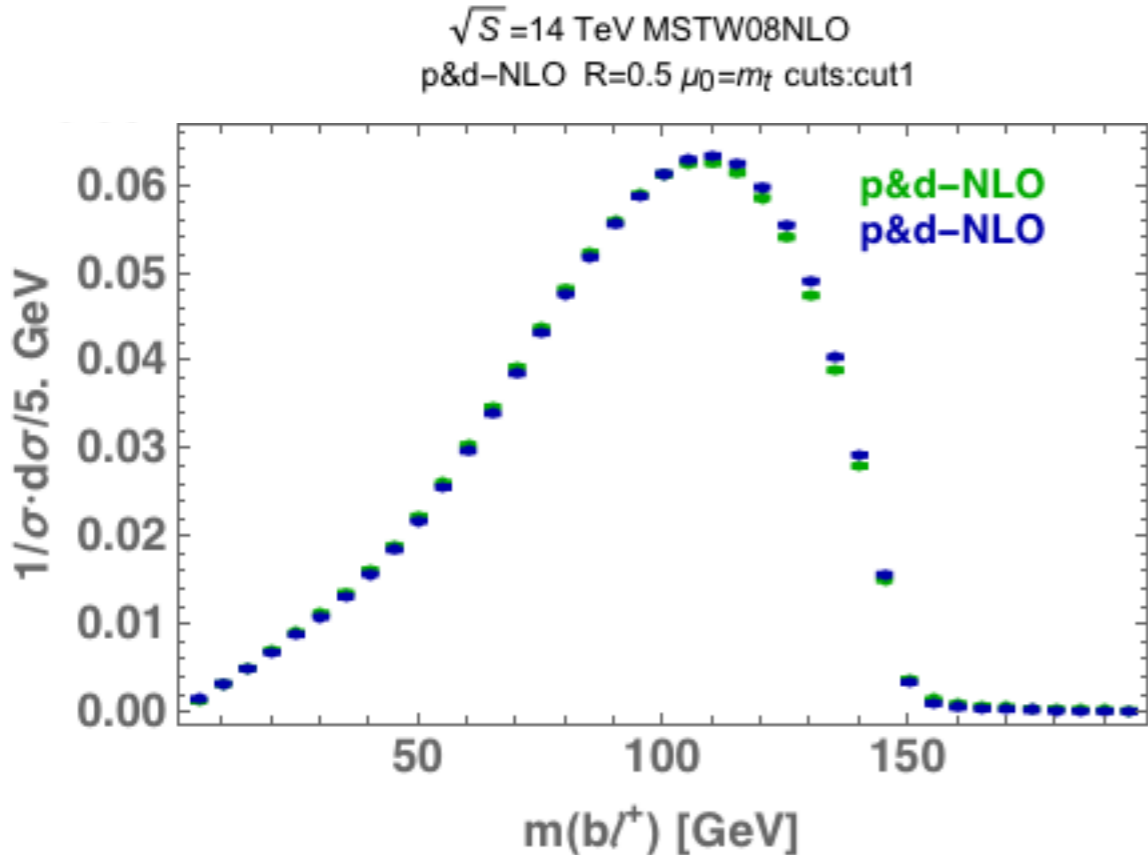
A first look at scale uncertainties



A first look at scale uncertainties

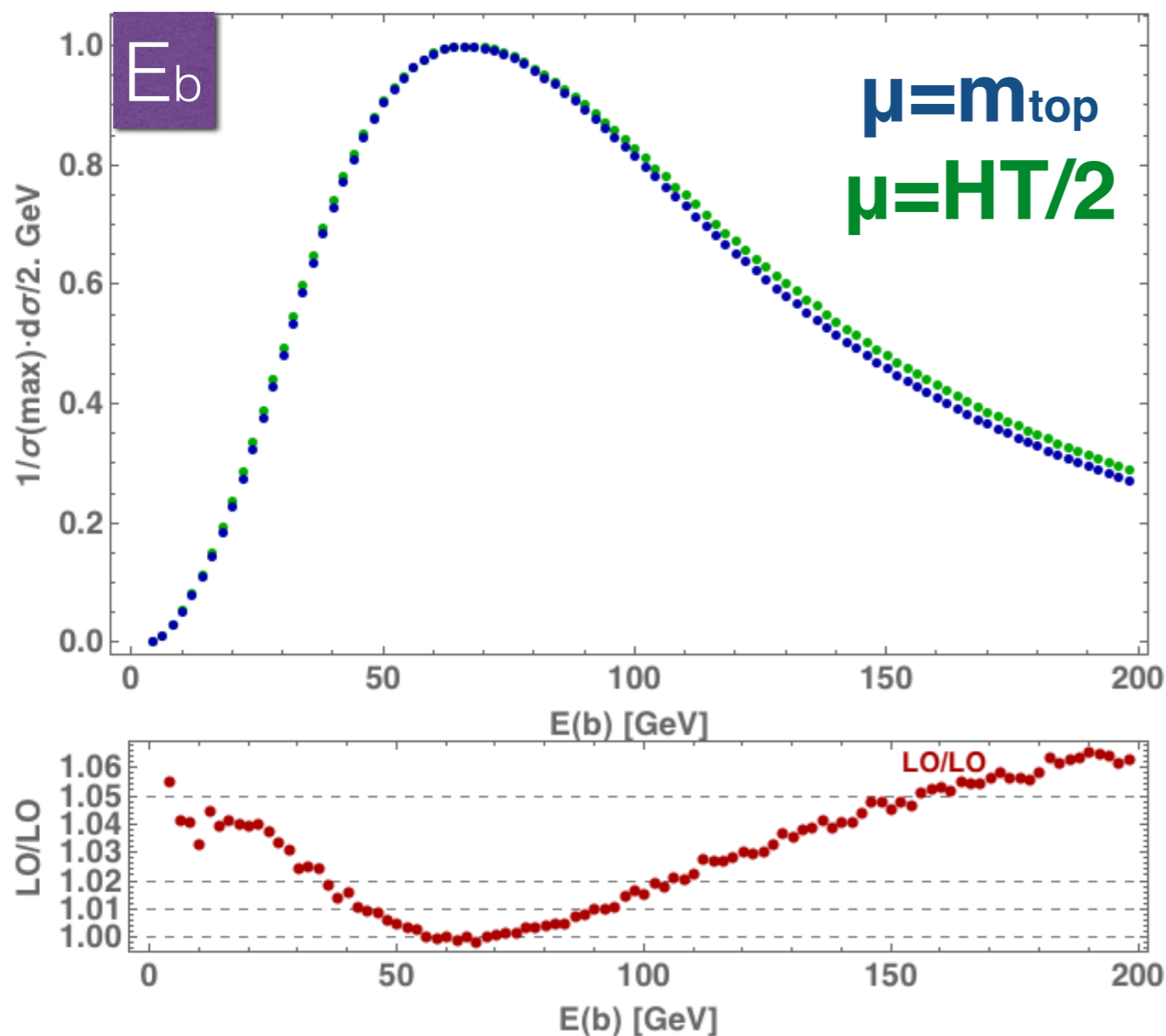


A first look at scale uncertainties



Subtleties of the subtle effects

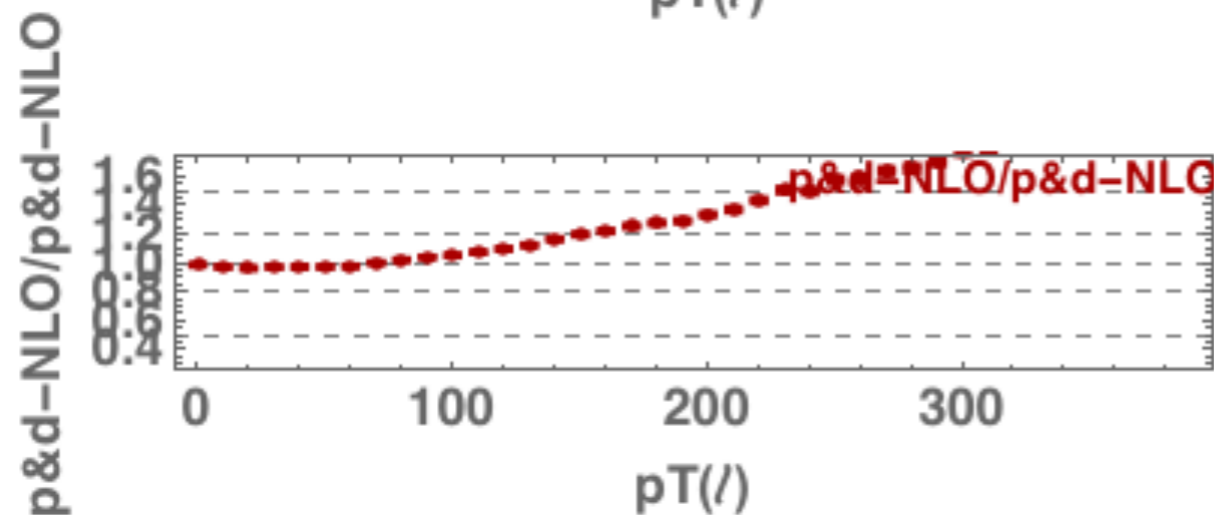
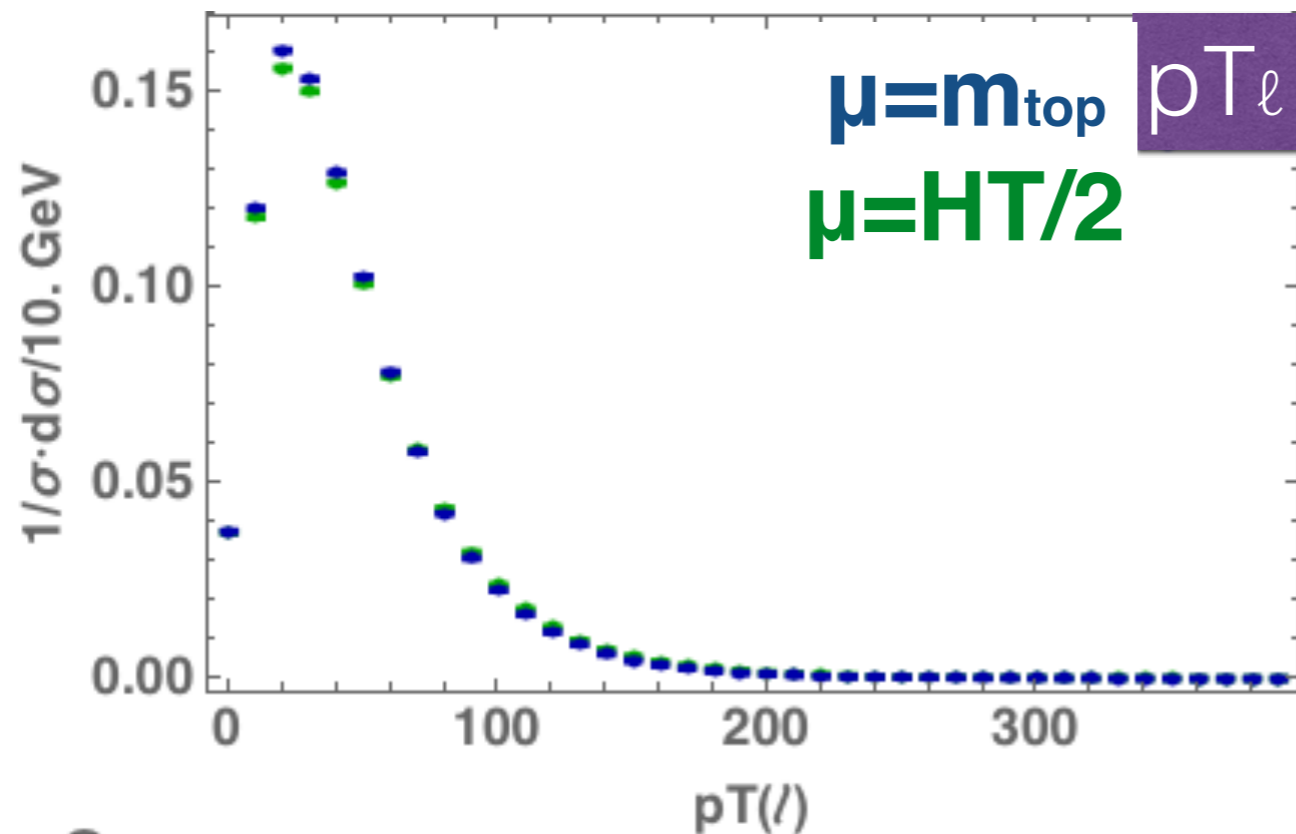
$\Delta m_{\text{top}} \lesssim 300$ MeV despite 5% deviations in the tails



- despite “large” difference in the tails, m_{top} is unaffected
- good for m_{top}
- would be terrible if this was the effect of new physics sought for in m_{top}

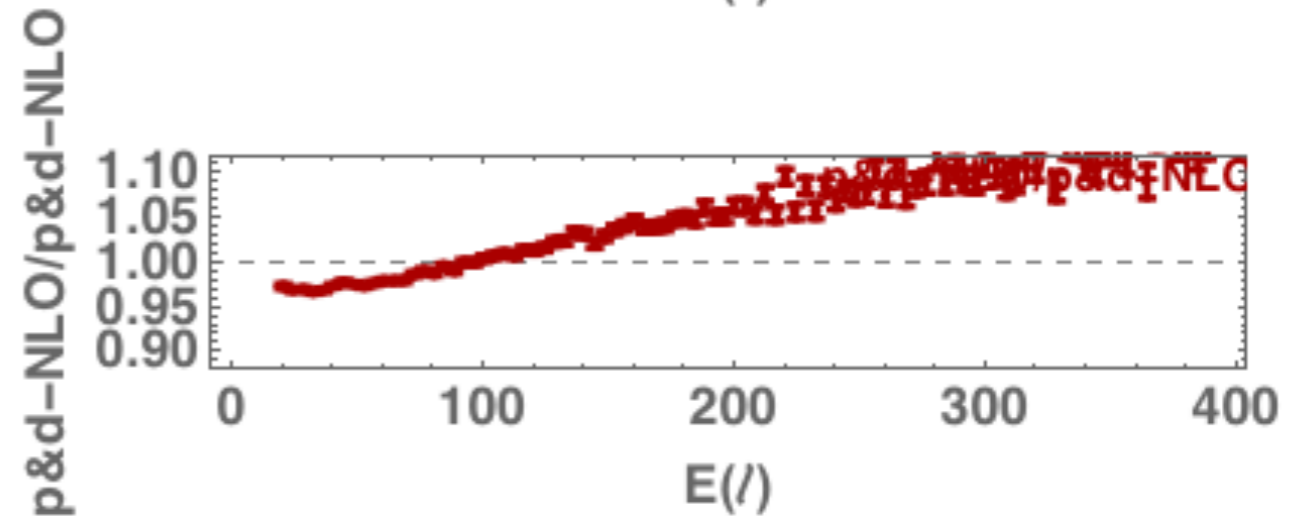
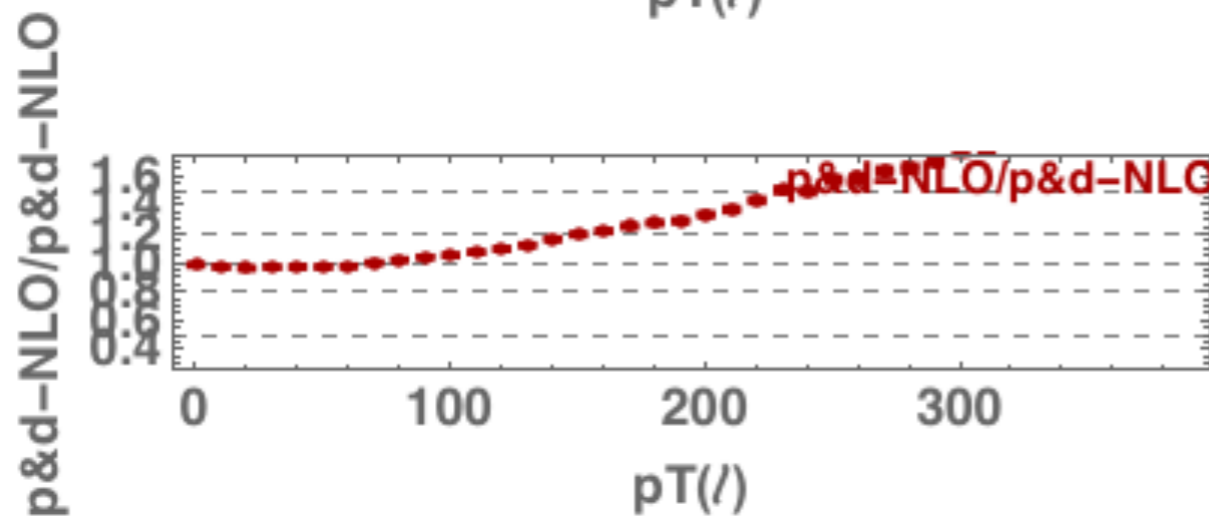
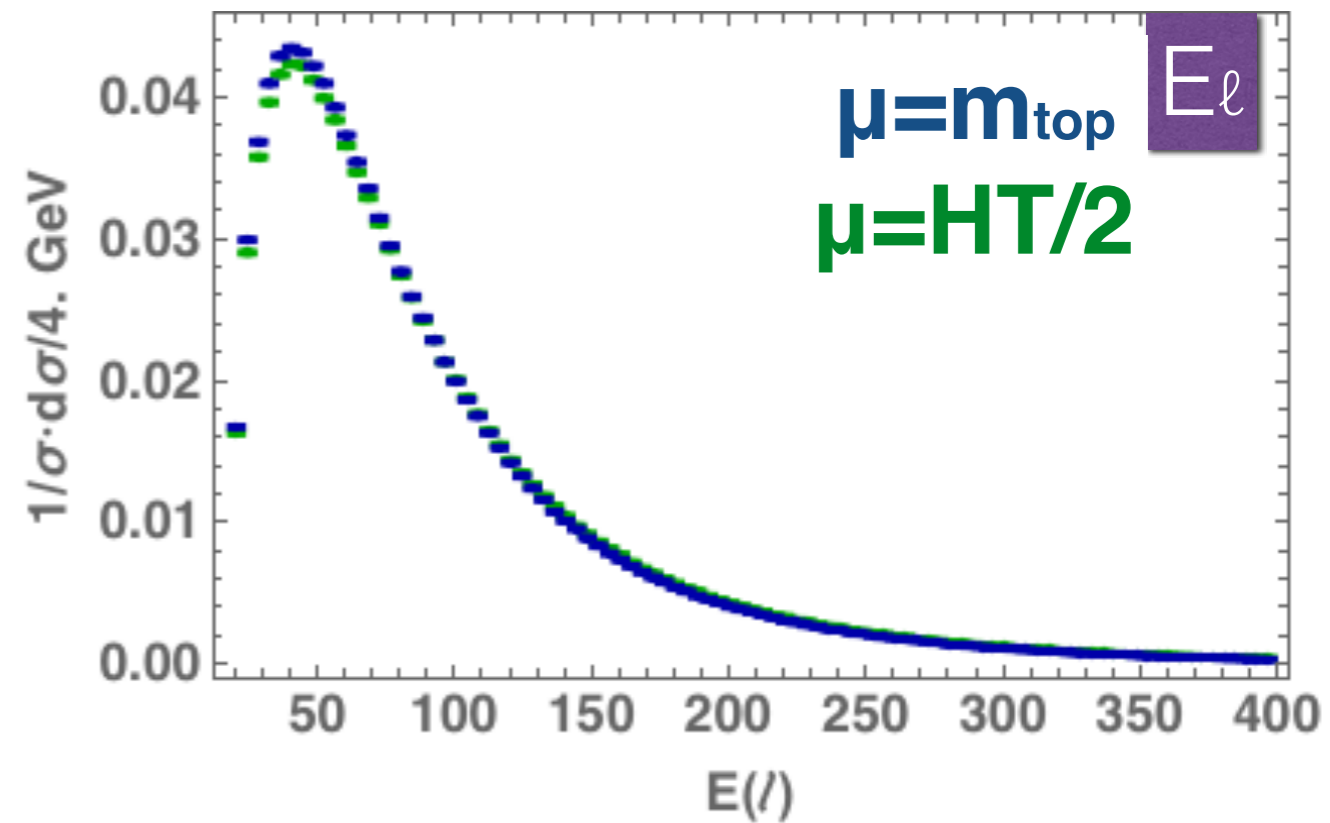
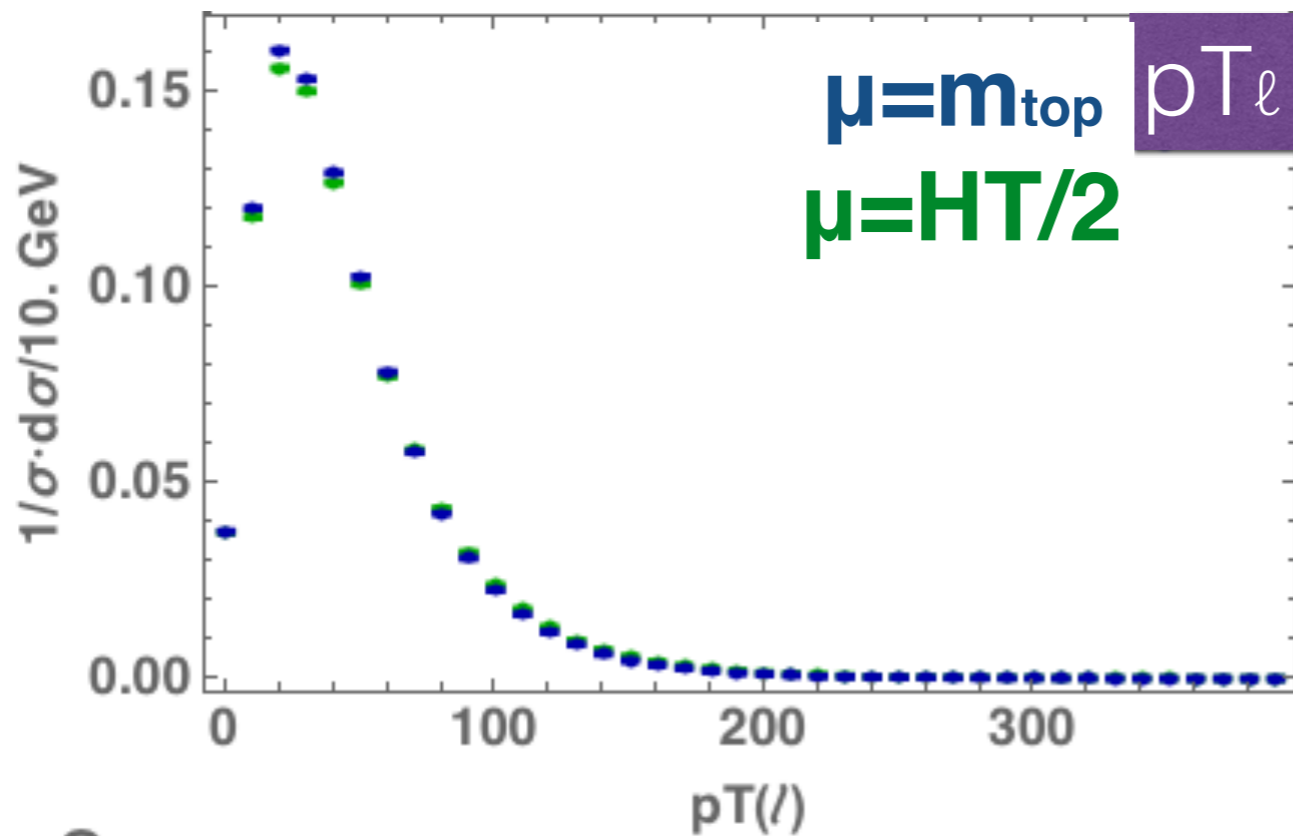
Subtleties of the subtle effects

$\Delta m_{\text{top}} \approx 1$ GeV and large deviations in the tails



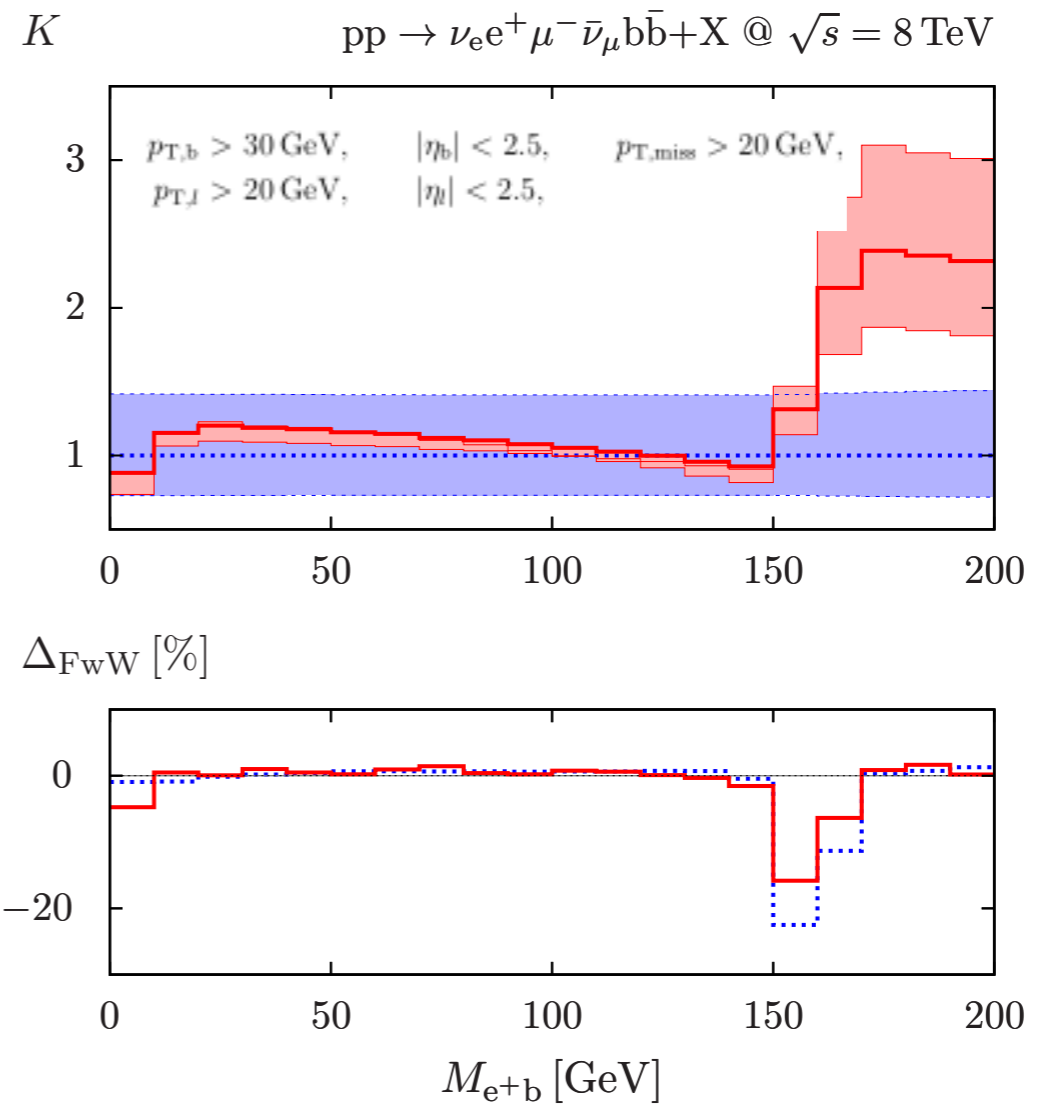
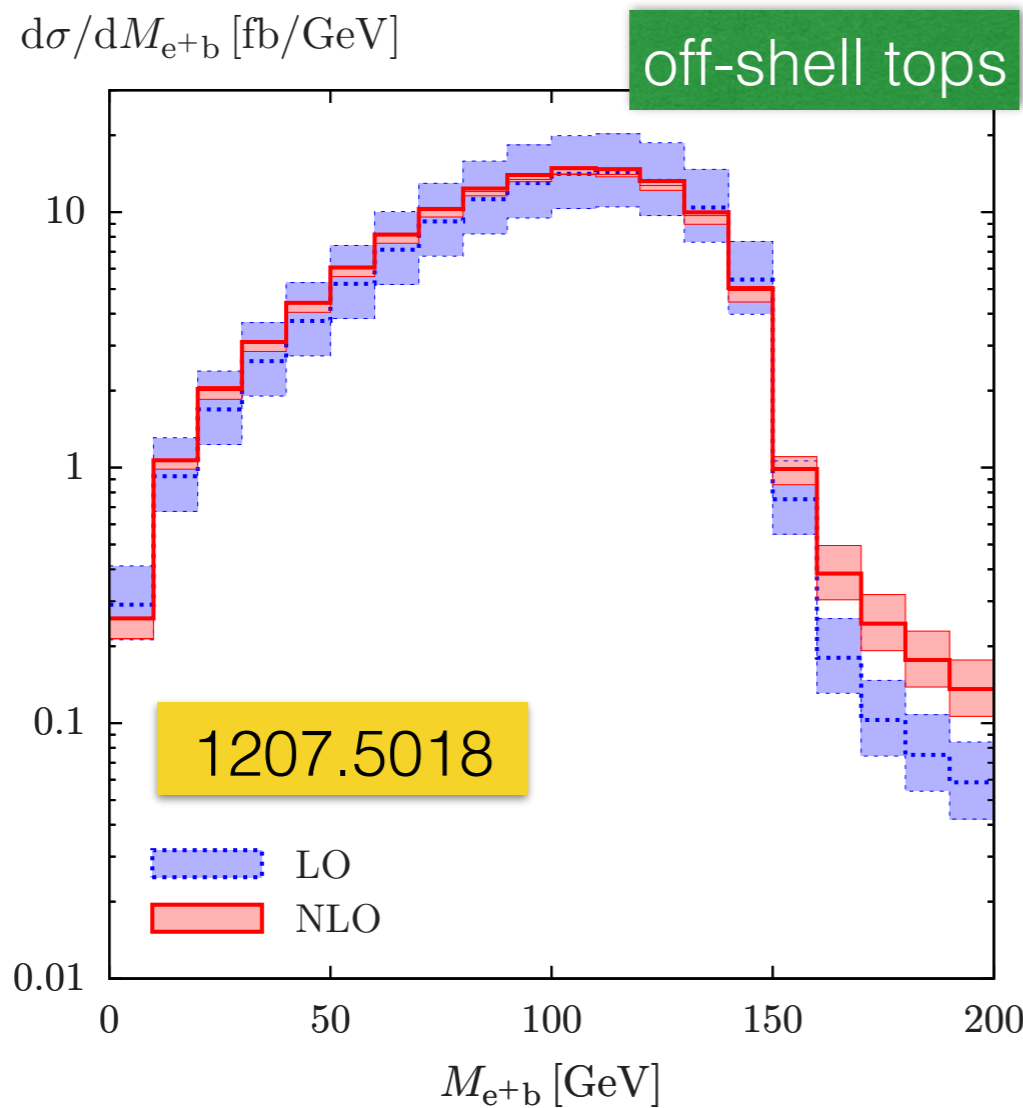
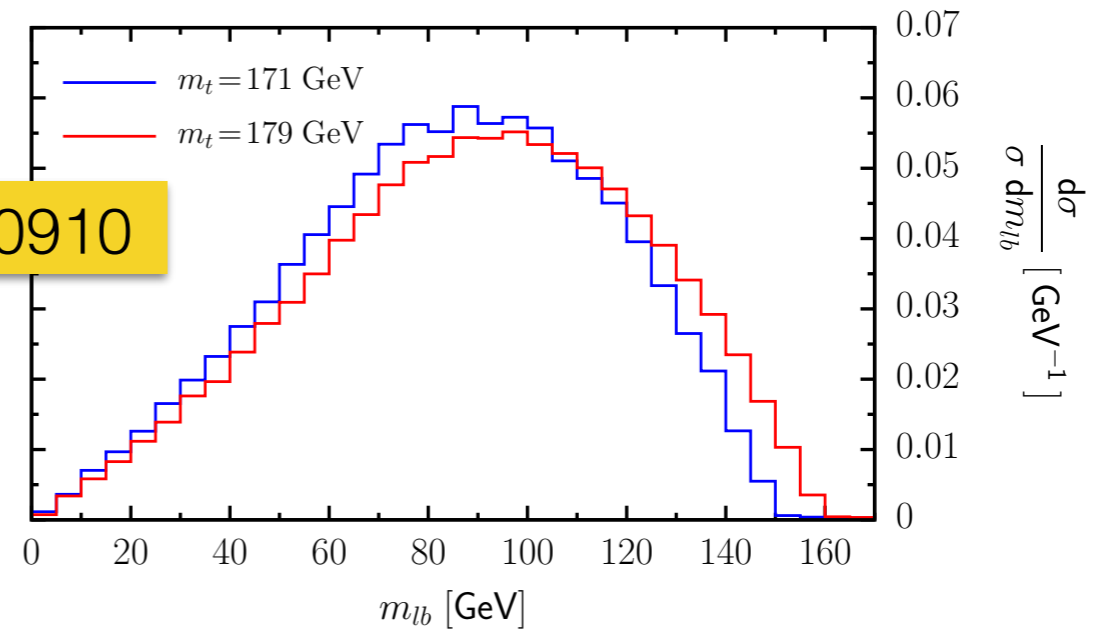
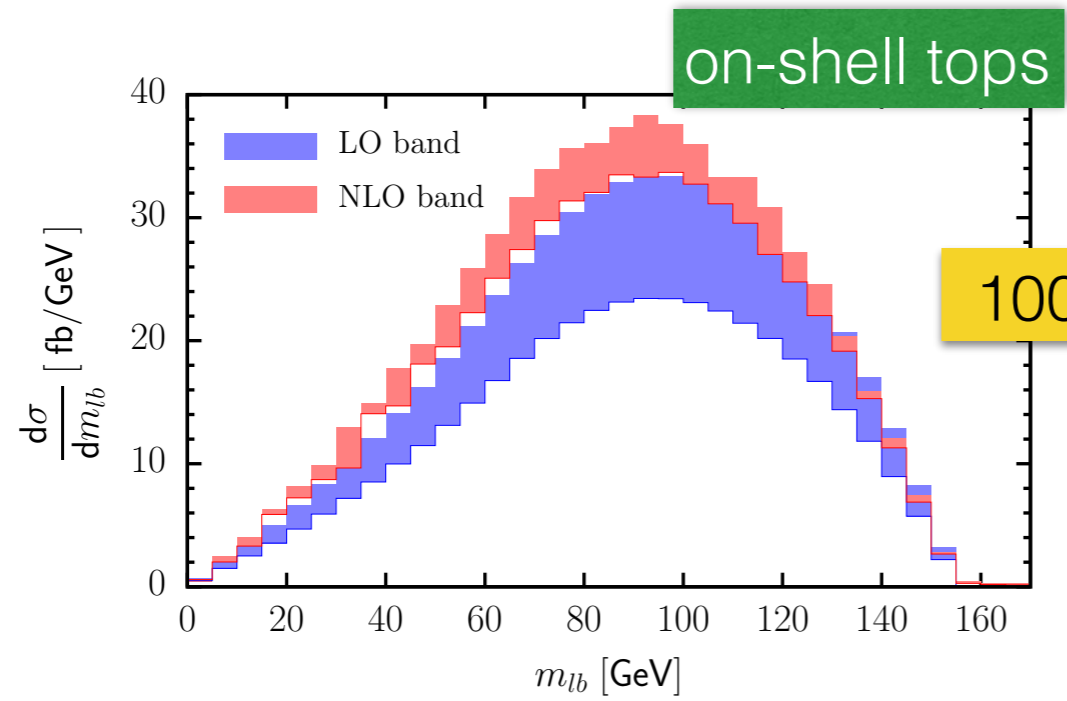
- “large” difference in the tails, m_{top} is affected
- not too bad for m_{top} (1407.2763)
- would be terrible if this was the effect of new physics sought for in these tails

Subtleties of the subtle effects



Thank you

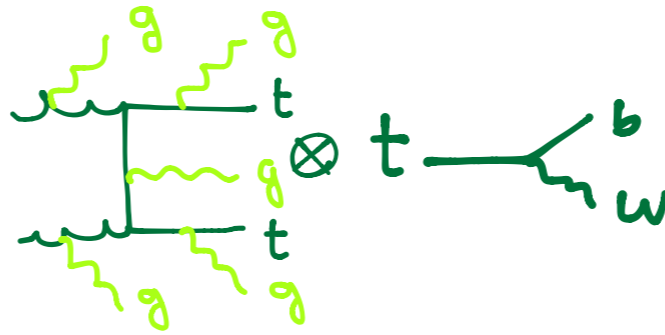
$m_{b\ell}$ at NLO



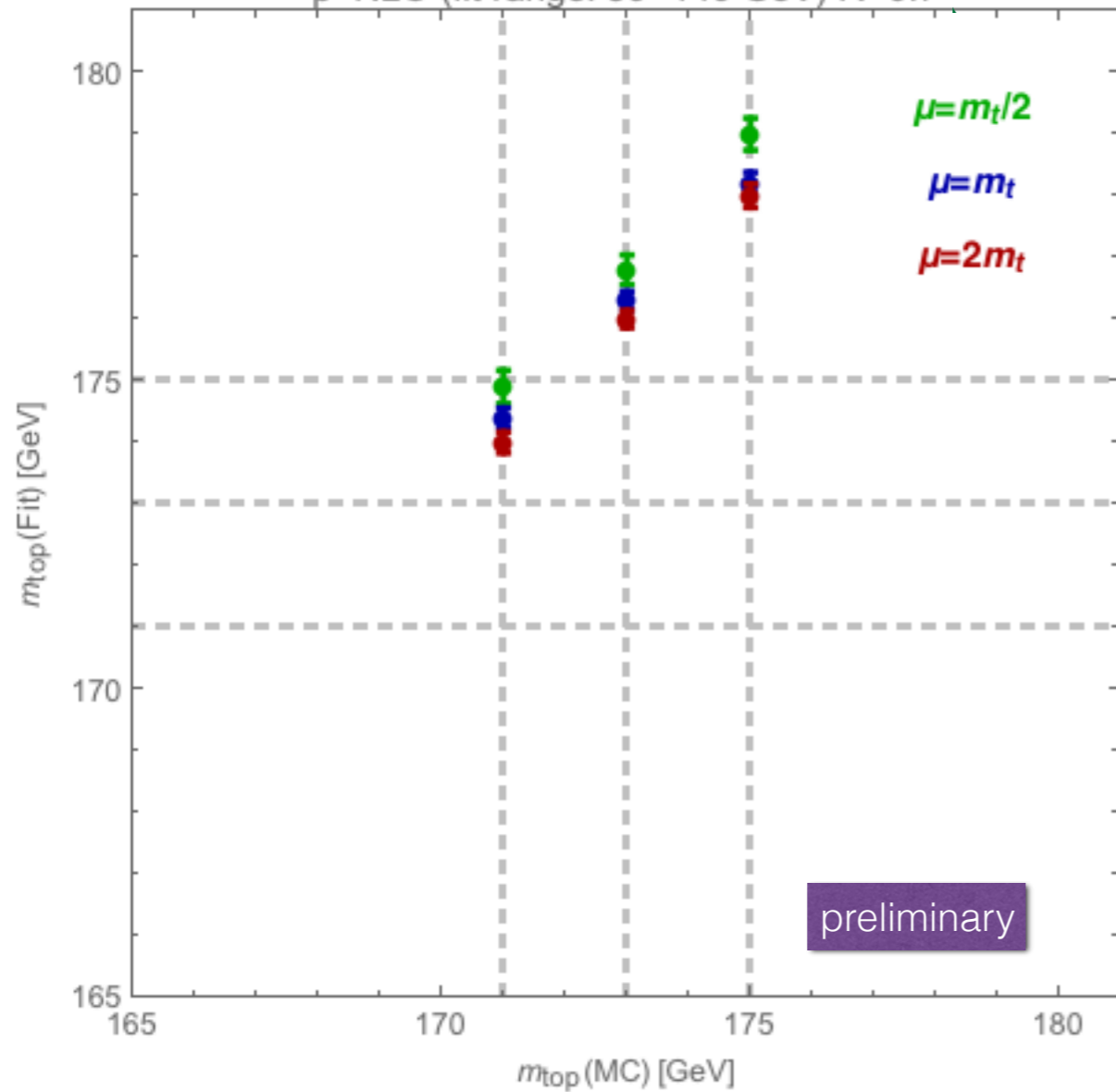
	pdNLO	pNLO	LO		pdNLO	pNLO	LO
$2\mu_0$	-3.	0.4	-0.2	$2\mu_0$	5.	7.4	7.
μ_0	-4.1	0.7	0.	μ_0	4.7	7.5	7.2
$0.5\mu_0$	-5.3	0.8	-0.2	$0.5\mu_0$	3.9	7.6	7.3

NLO: production

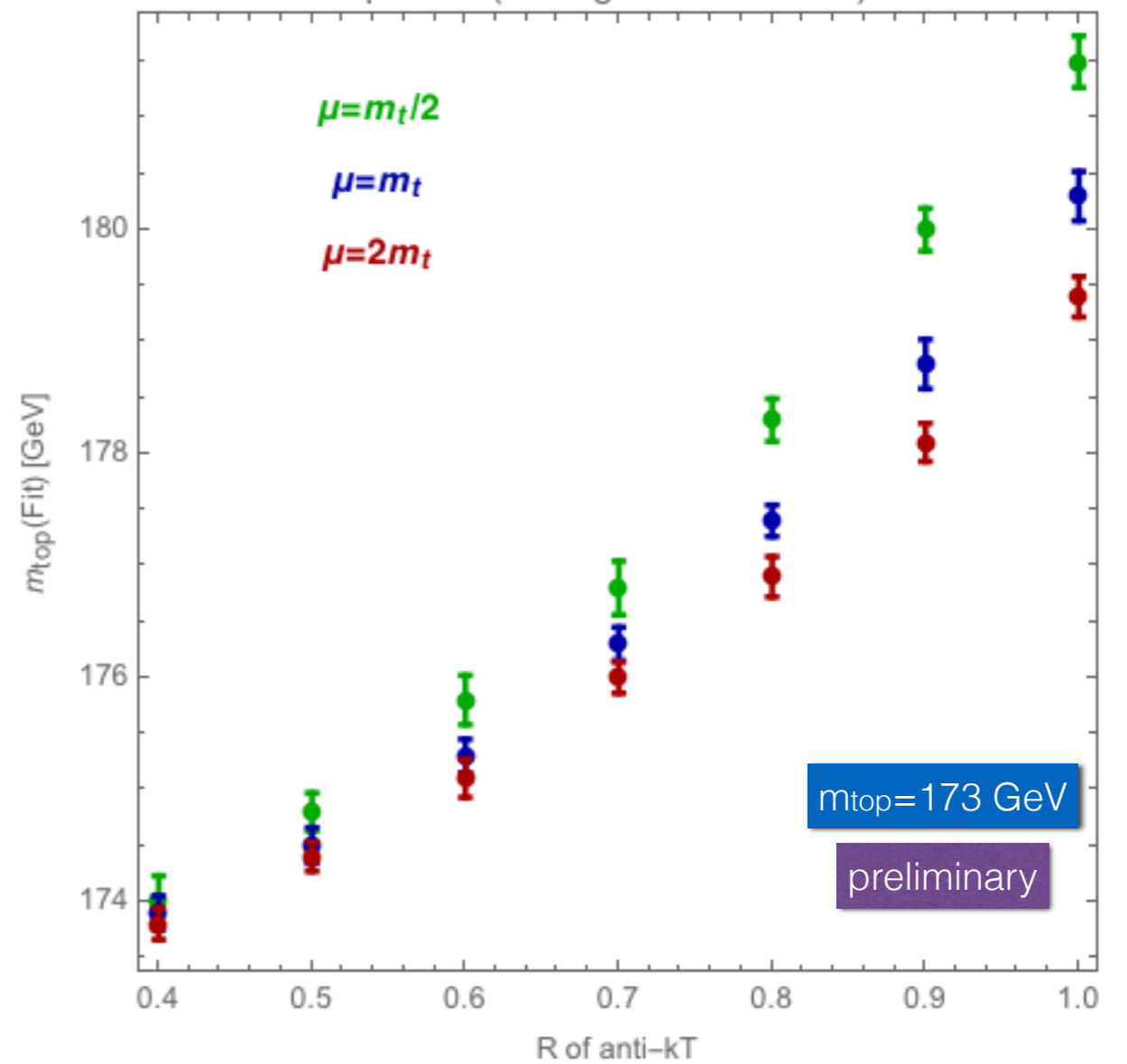
(MCFM)



p-NLO (fit range: 30–140 GeV) $R=0.7$



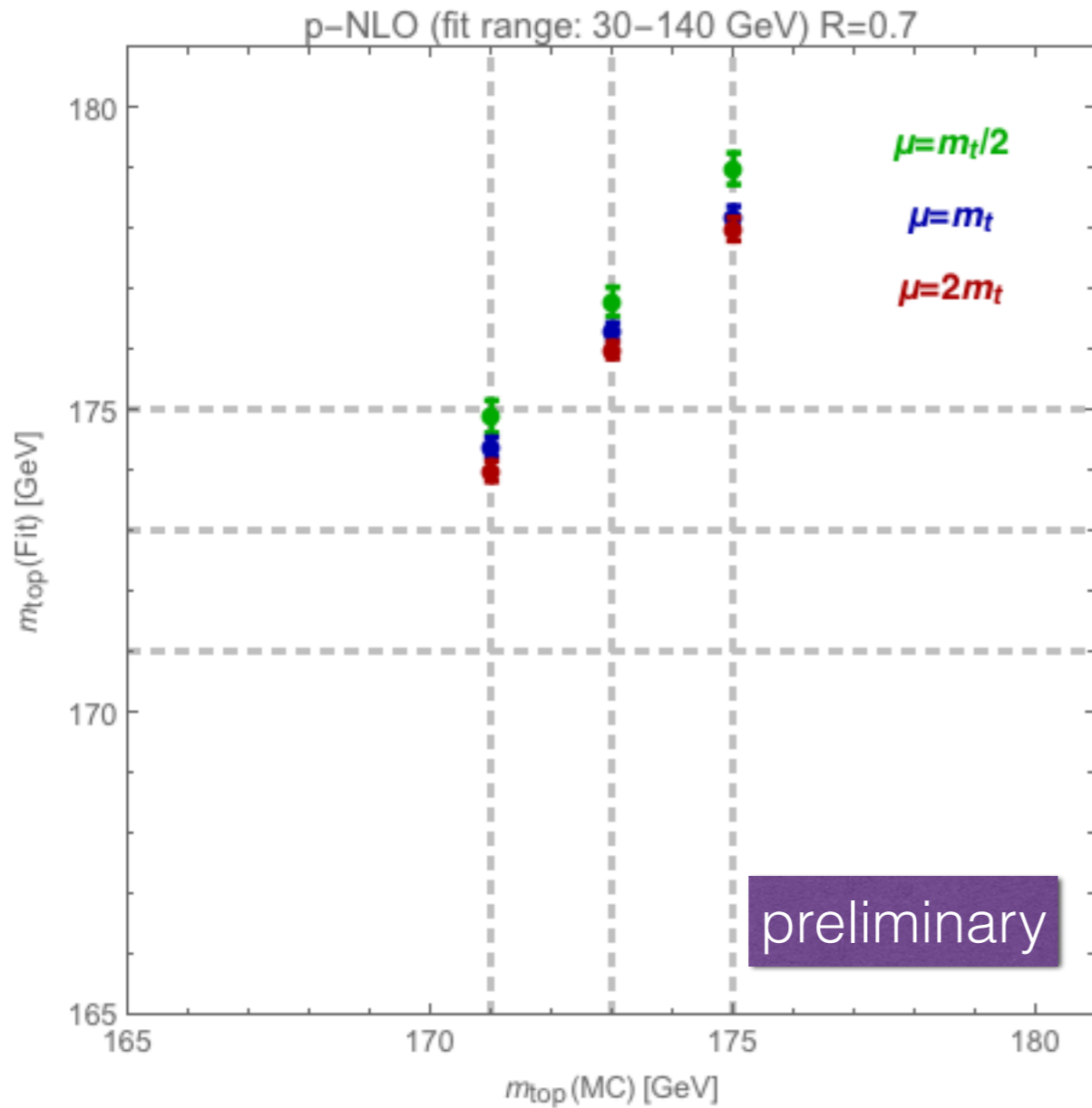
p-NLO (fit range: 30–140 GeV)



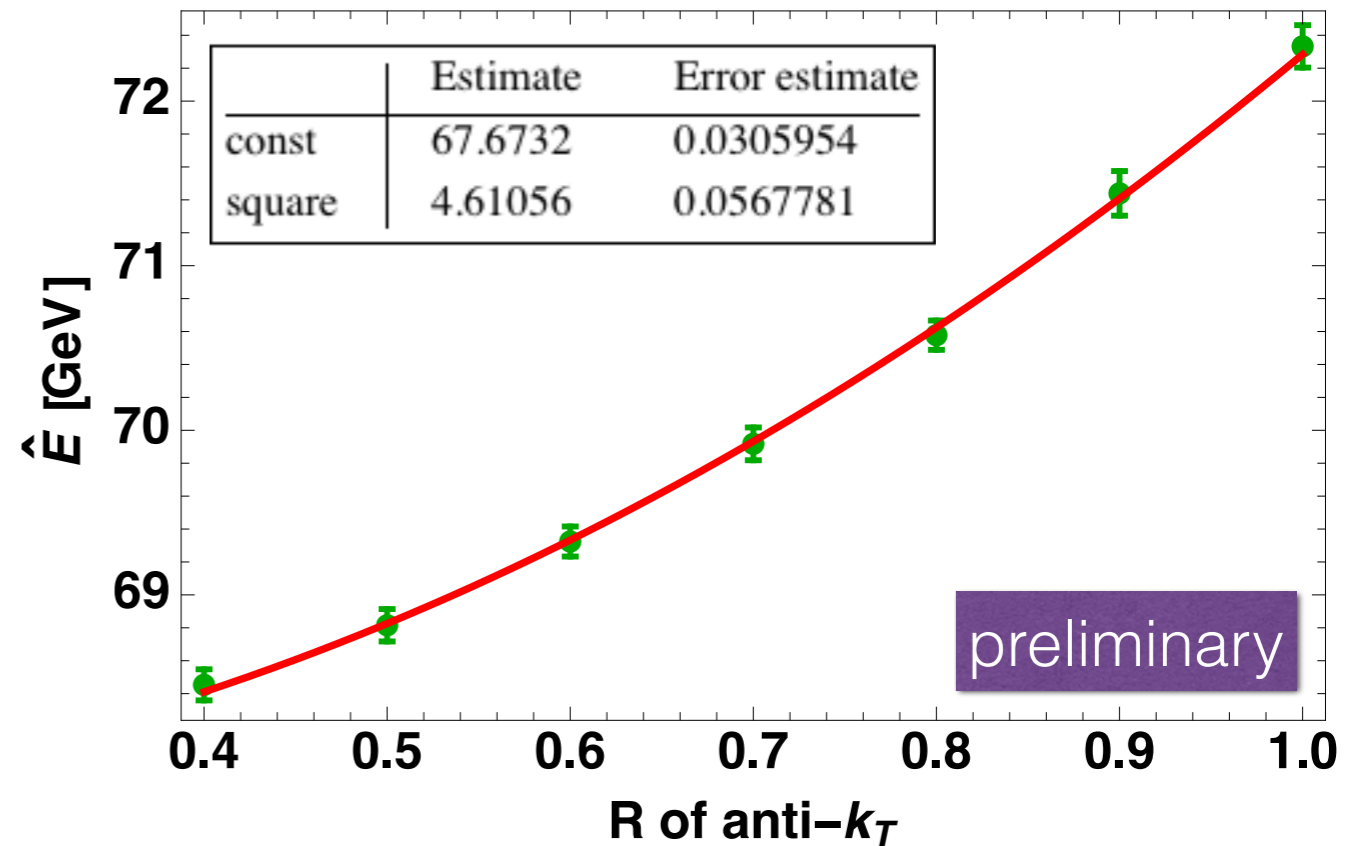
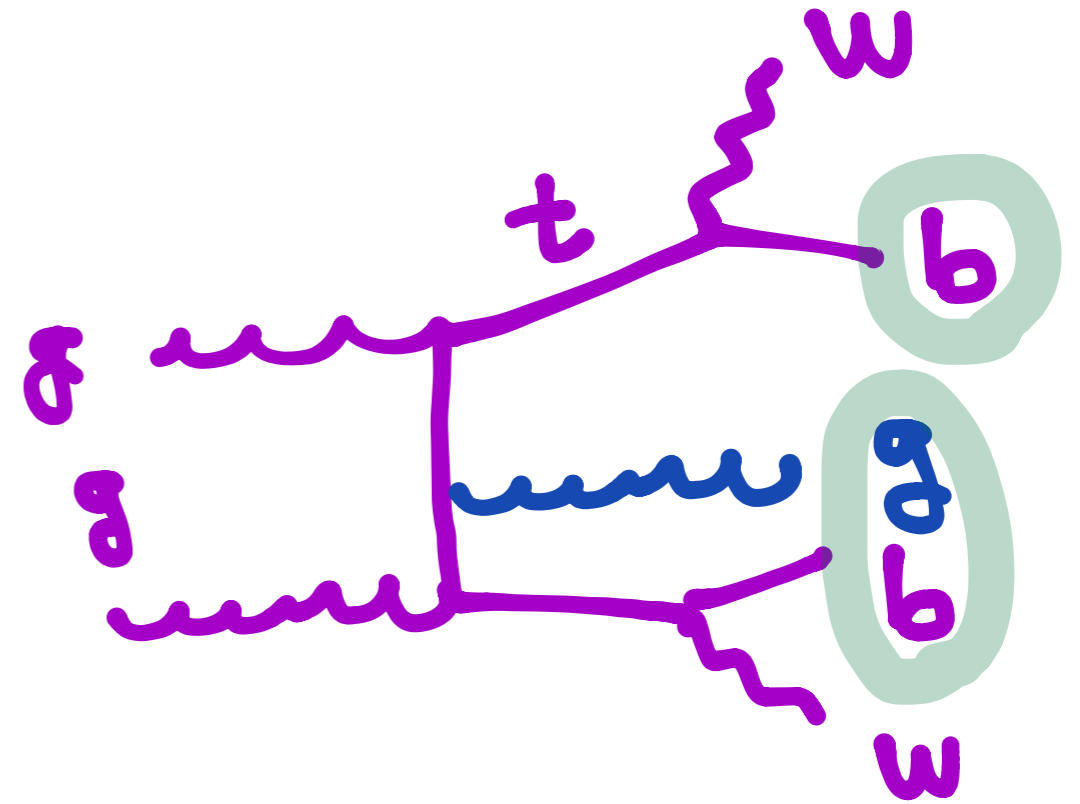
very little sensitive to the scale choice (less than 400 MeV on m_{top})

NLO: production

(MCFM)

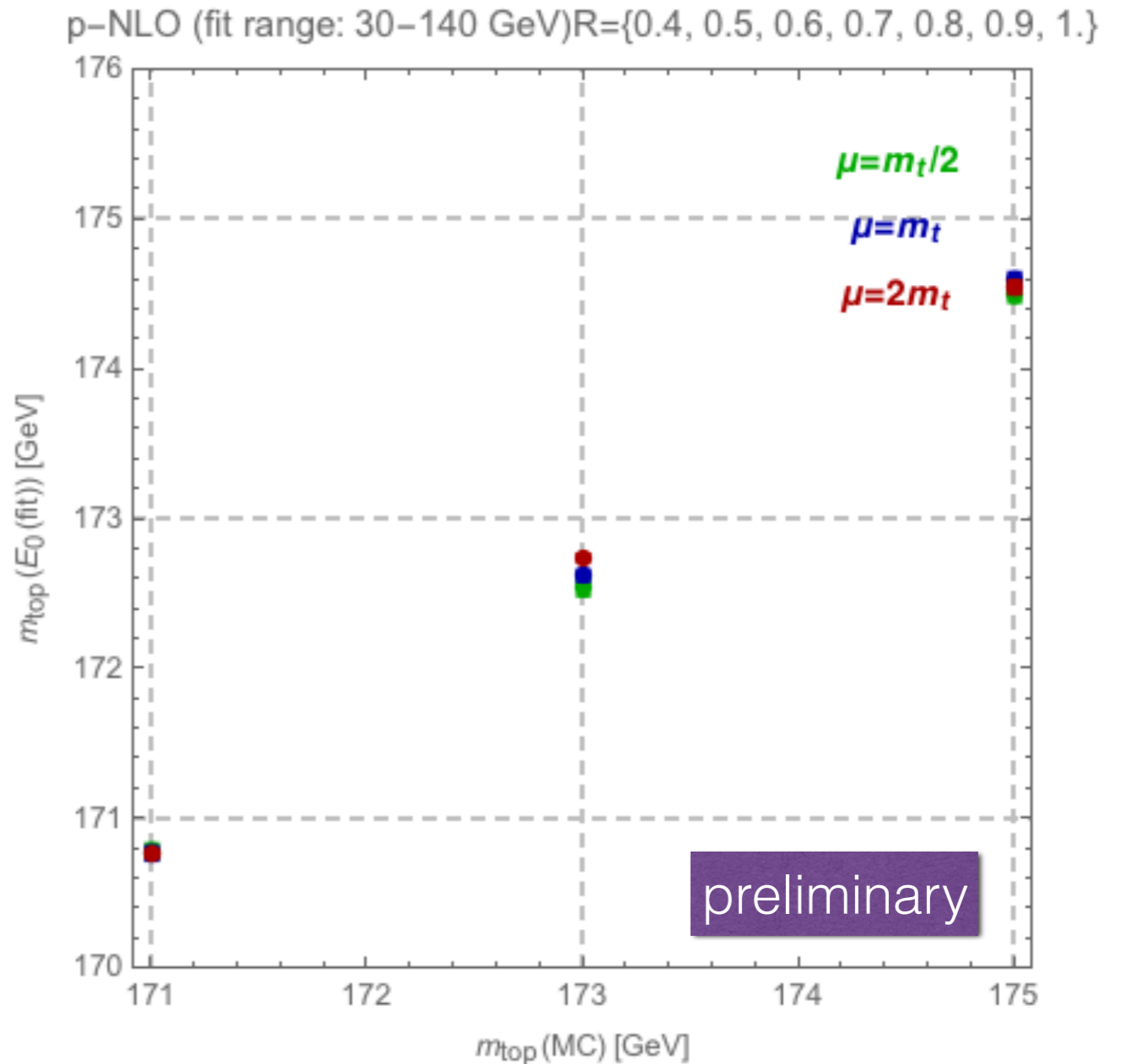
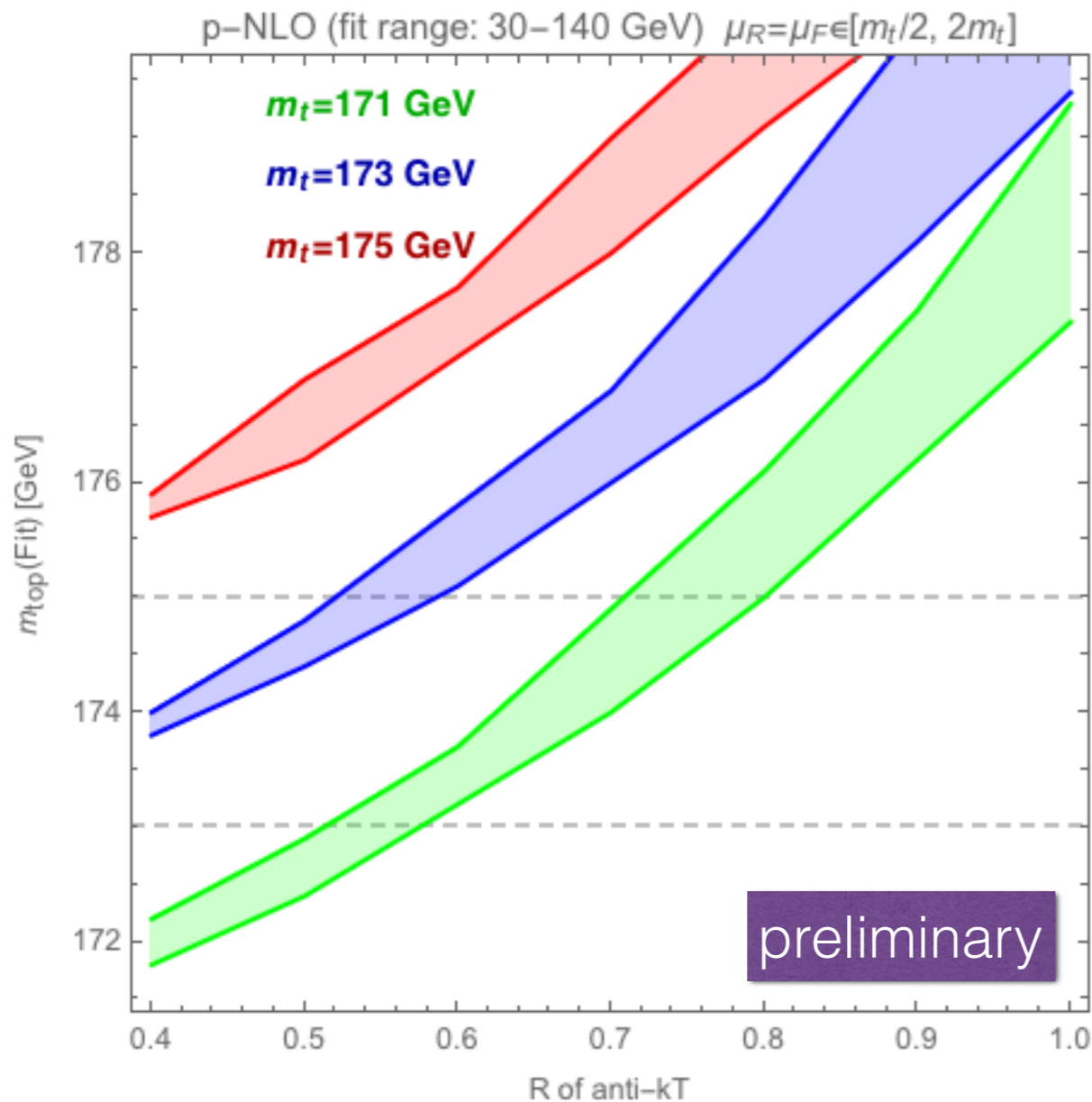


shift $\sim R^p$ (p~2 jet area)
 shift $\sim 1/\mu$ (real radiation)



NLO: production

(MCFM)

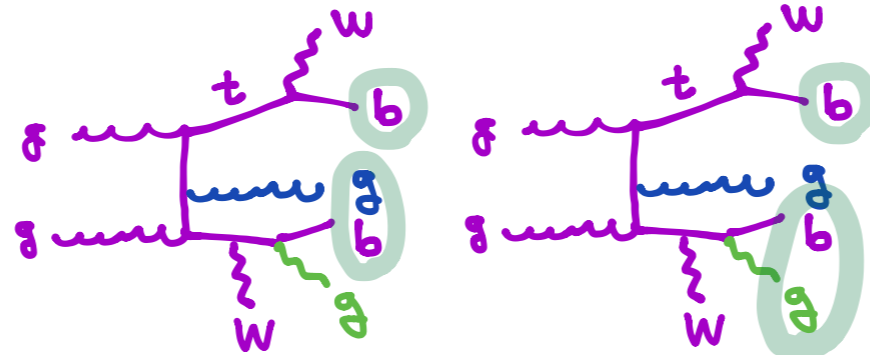


shift $\sim R^p$ ($p \sim 2$ jet area)
 shift $\sim 1/\mu$ (real radiation)

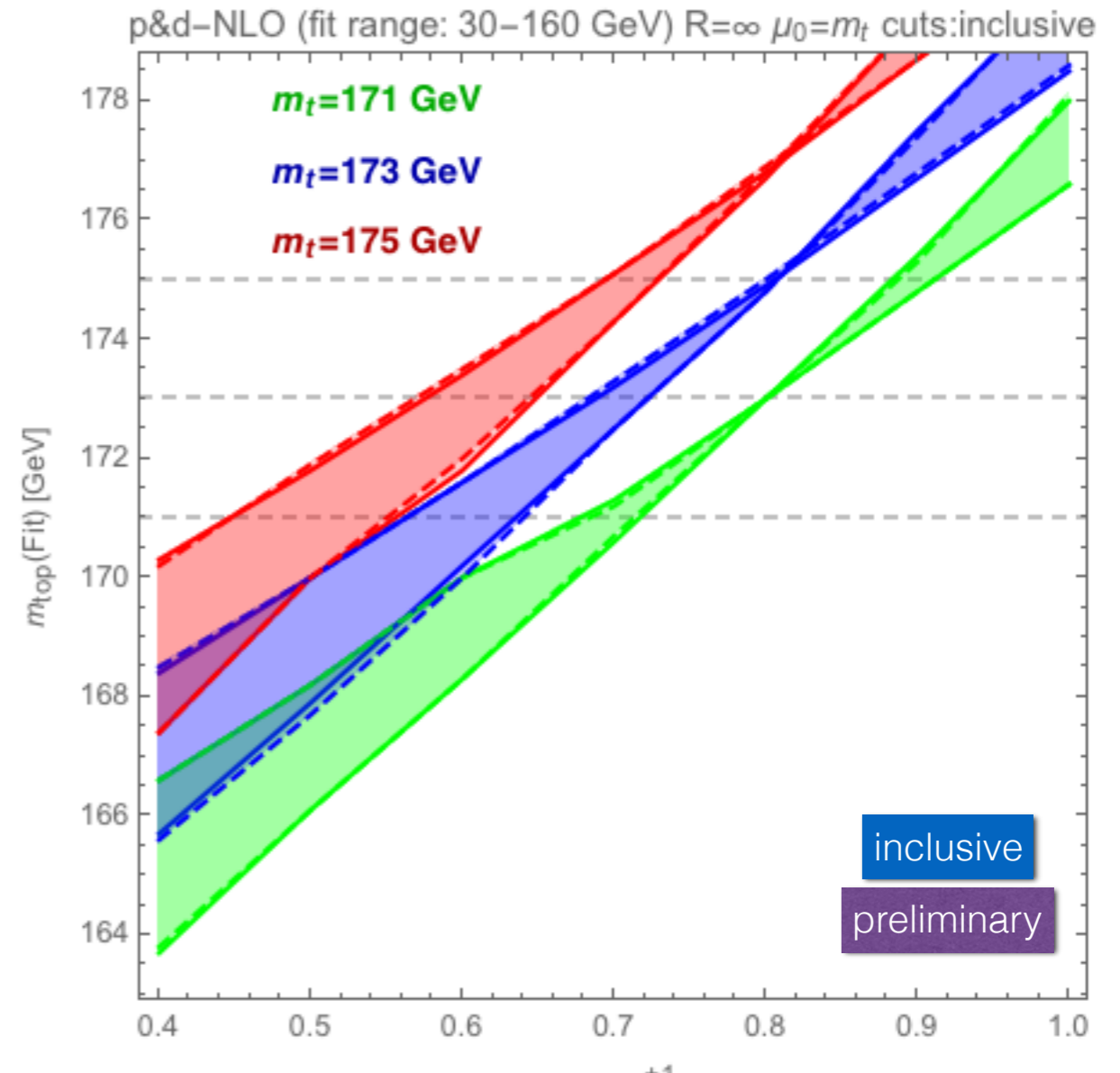
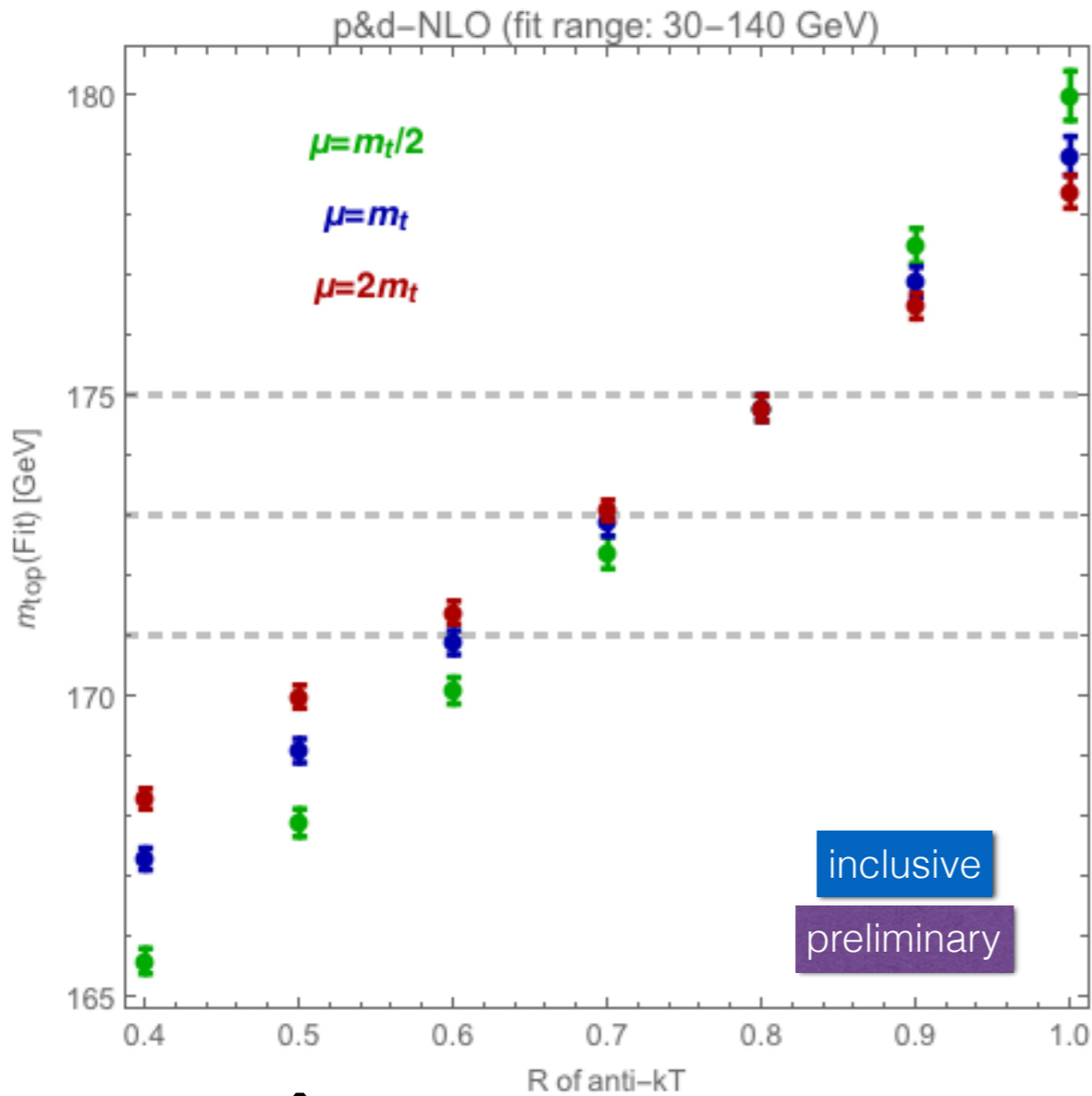
$$\hat{E} = E_0 + \alpha(\mu) \cdot p \cdot R^2 + \dots$$

$E_b^x = \frac{m_t^2 - m_w^2 + m_b^2}{2m_t}$

NLO: production & decay



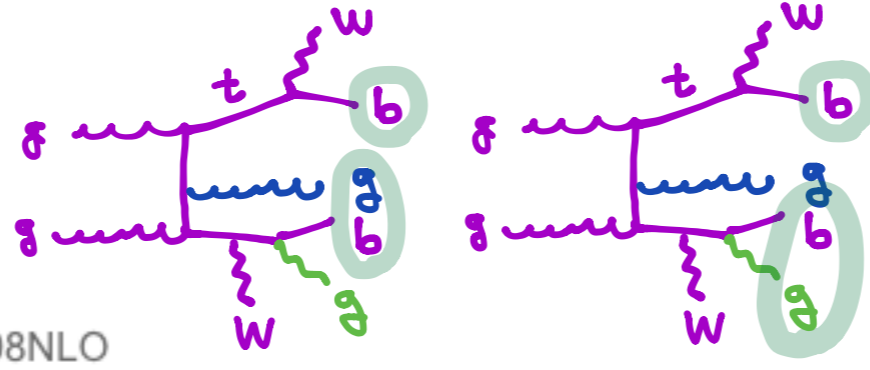
$\sqrt{S} = 14 \text{ TeV}$ MSTW08NLO



$$\hat{E} = E_0 + \alpha(\mu) \cdot [p \cdot R^2 + p \cdot \log R] + \dots$$

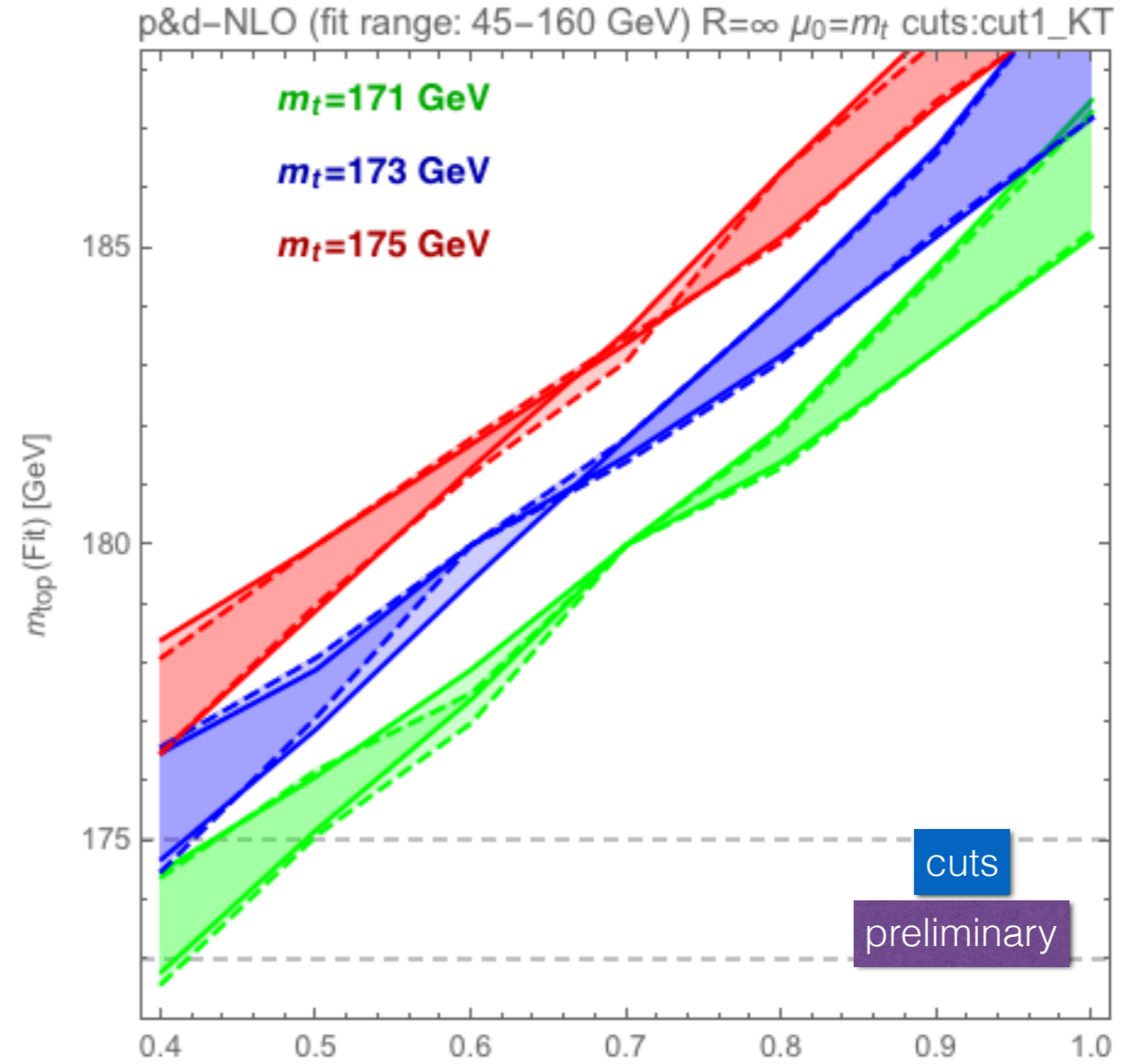
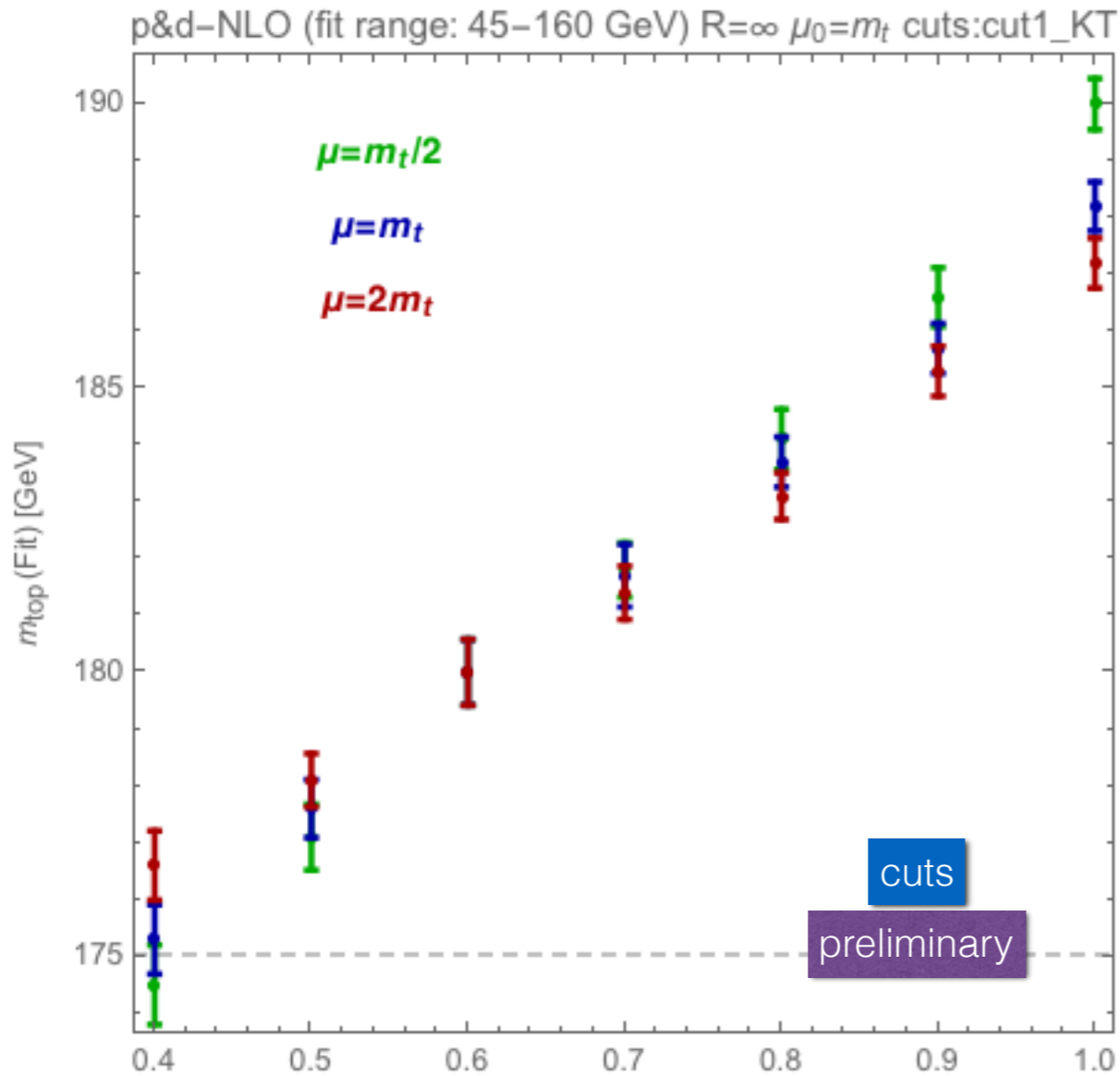
decay NLO sensitive to the scale choice: $\pm 1 \text{ GeV}$ on m_{top}

NLO: production & decay



$\sqrt{S} = 14 \text{ TeV}$ MSTW08NLO

$\sqrt{S} = 14 \text{ TeV}$ MSTW08NLO



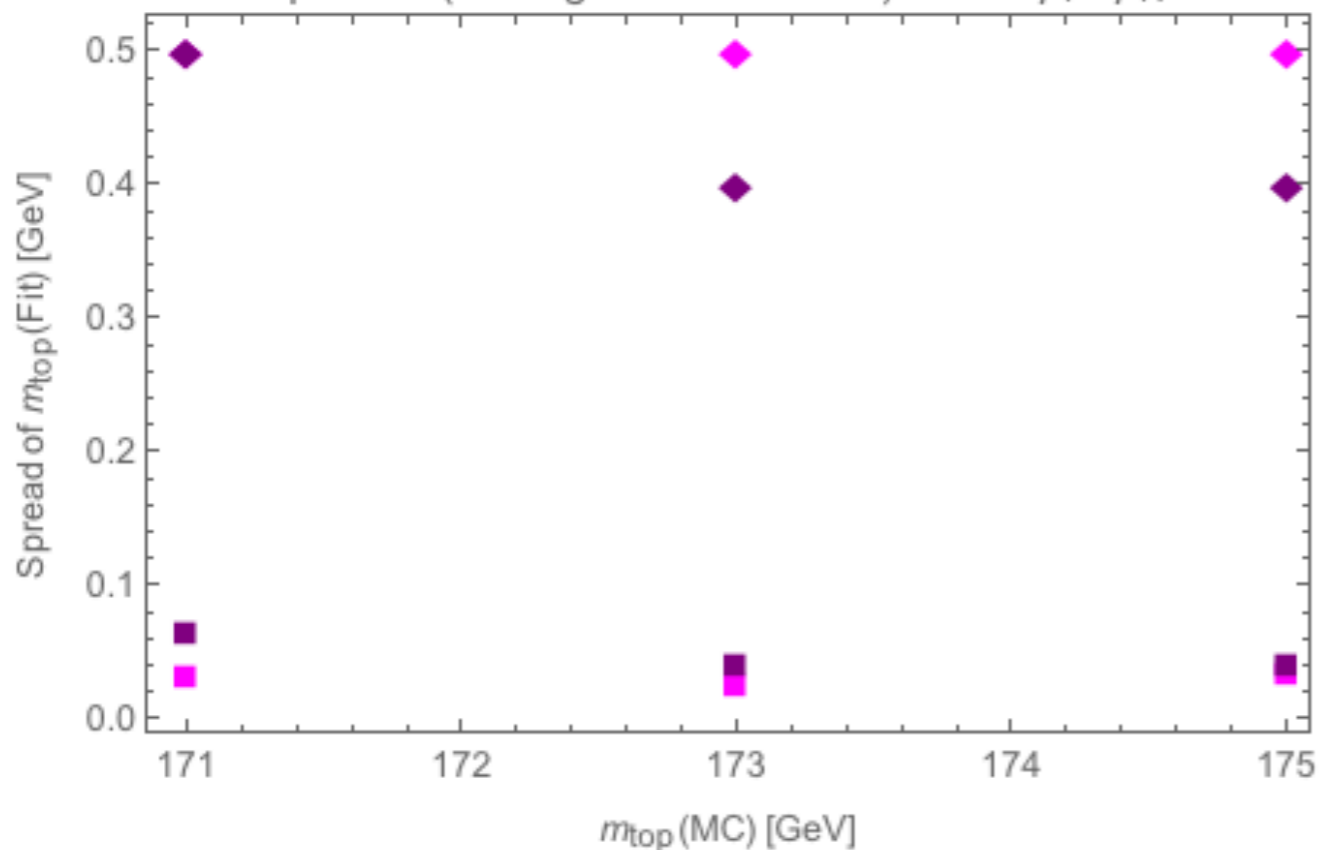
$$\hat{E} = E_0 + \alpha(\mu) \cdot [p \cdot R^2 + p \cdot \log R] + \dots$$

decay NLO sensitive to the scale choice: $\pm 1 \text{ GeV}$ on m_{top}

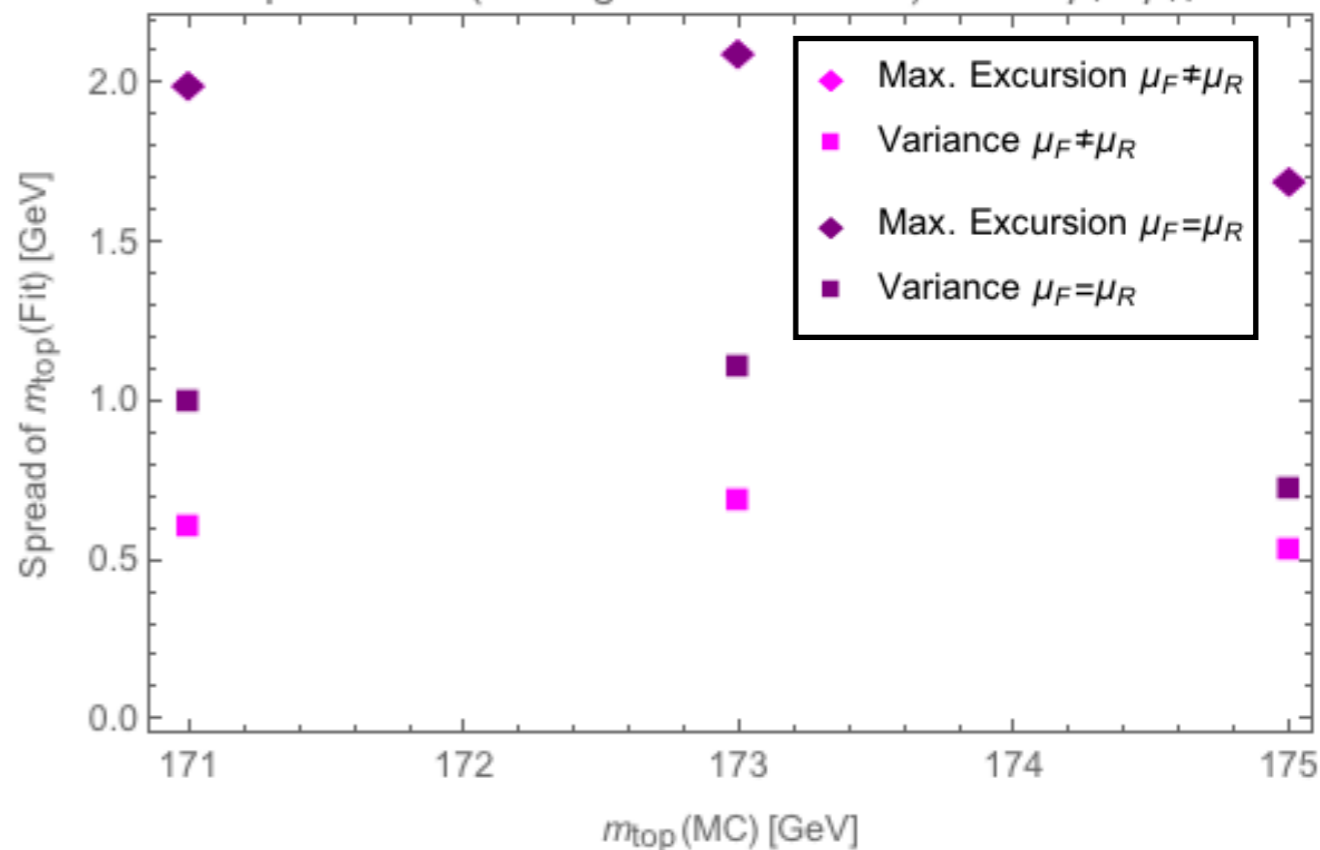
Dependence on the scales

R=0.5 pNLO vs. pdNLO

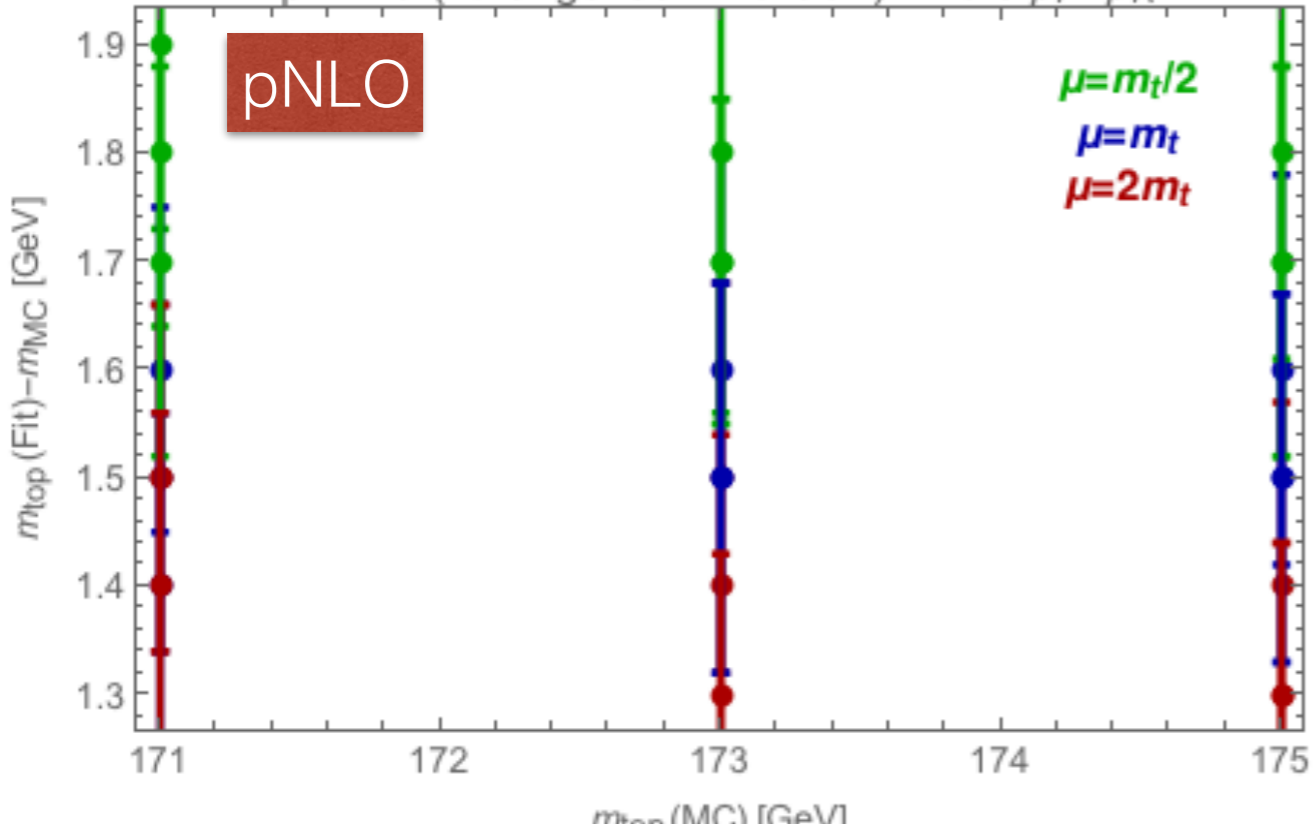
p-NLO (fit range: 30–140 GeV) $R=0.5$ $\mu_F \neq \mu_R$



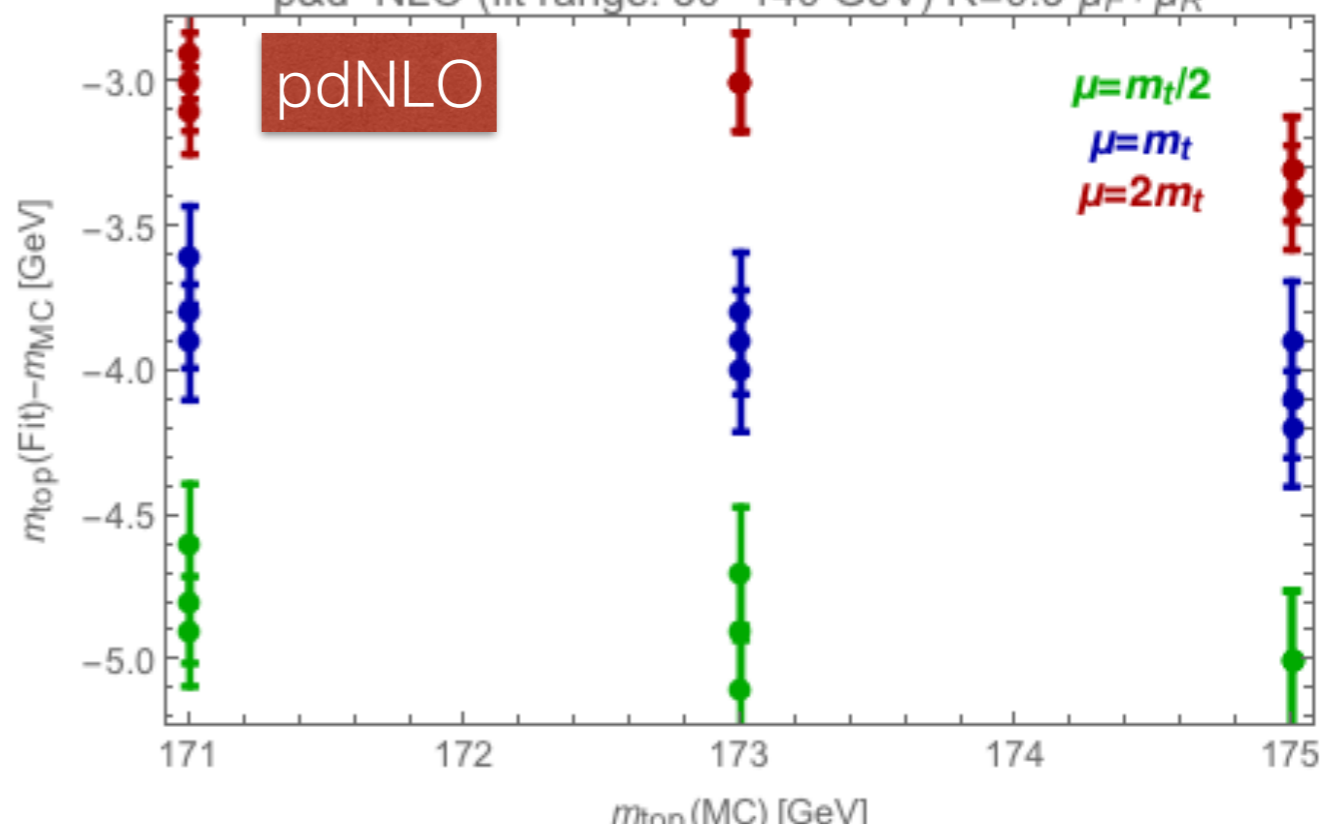
p&d-NLO (fit range: 30–140 GeV) $R=0.5$ $\mu_F \neq \mu_R$



p-NLO (fit range: 30–140 GeV) $R=0.5$ $\mu_F \neq \mu_R$



p&d-NLO (fit range: 30–140 GeV) $R=0.5$ $\mu_F \neq \mu_R$

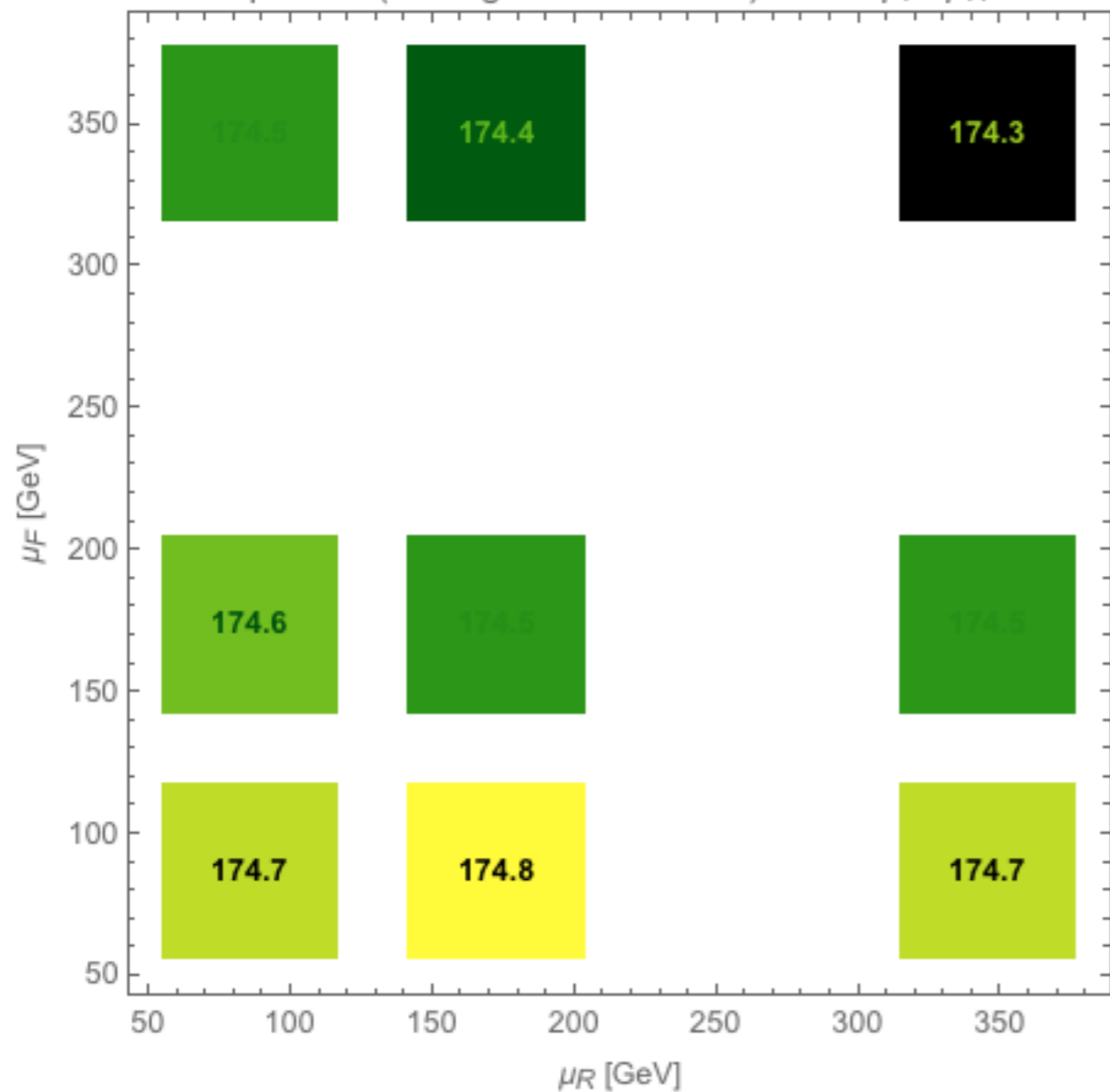


Dependence on the scales

R=0.5 pNLO vs. pdNLO

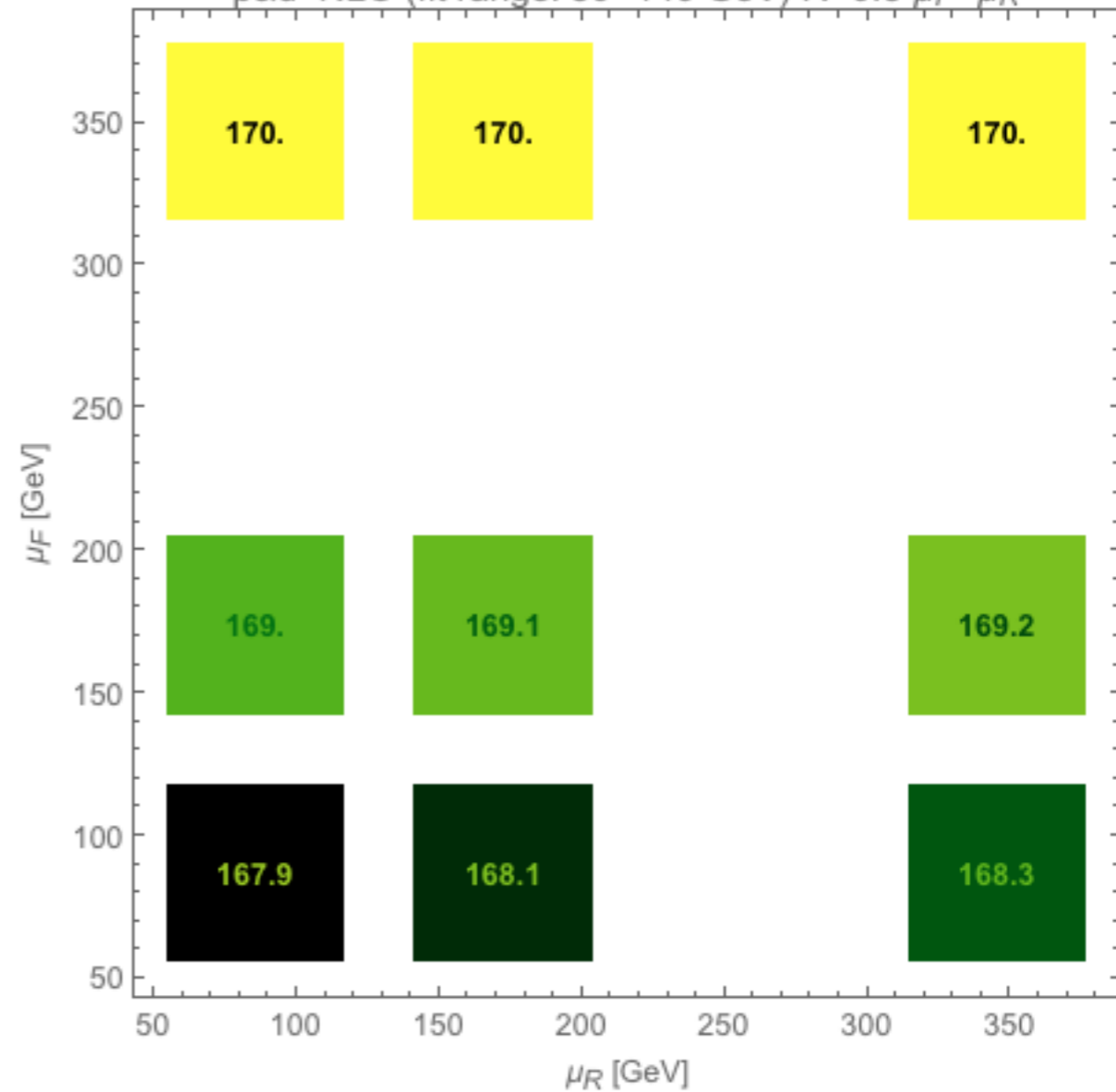
pNLO

p-NLO (fit range: 30–140 GeV) $R=0.5$ $\mu_F \neq \mu_R$



pdNLO

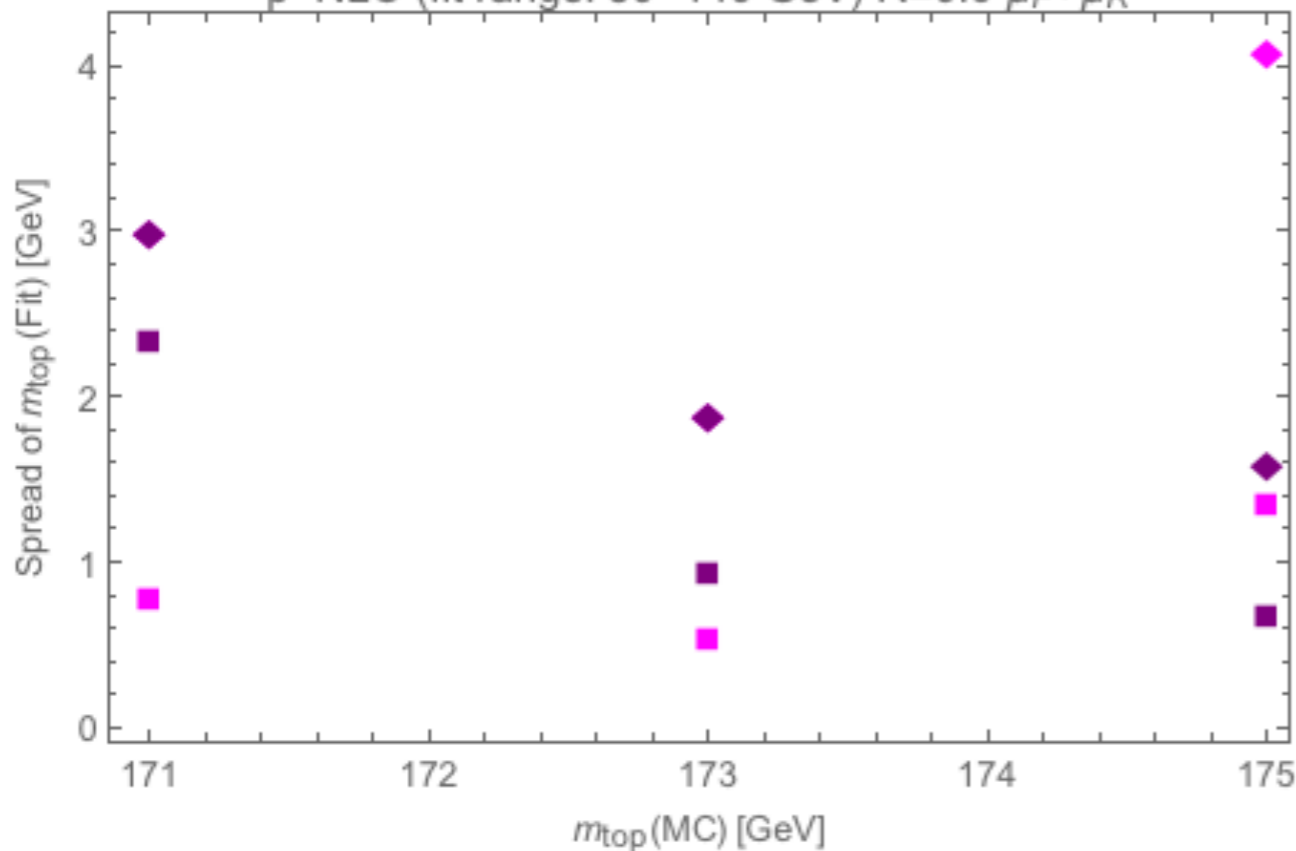
p&d-NLO (fit range: 30–140 GeV) $R=0.5$ $\mu_F \neq \mu_R$



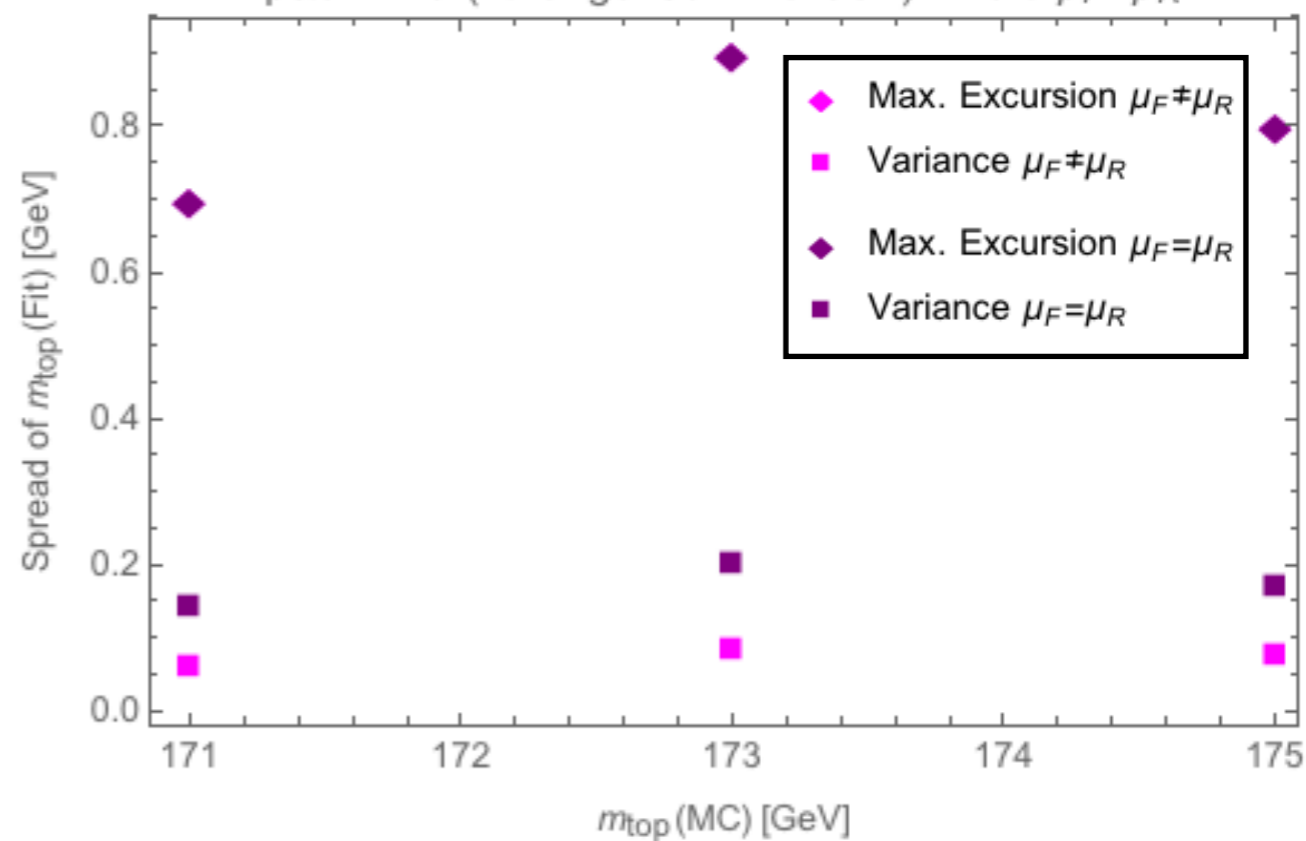
Dependence on the scales

R=0.9 pNLO vs. pdNLO

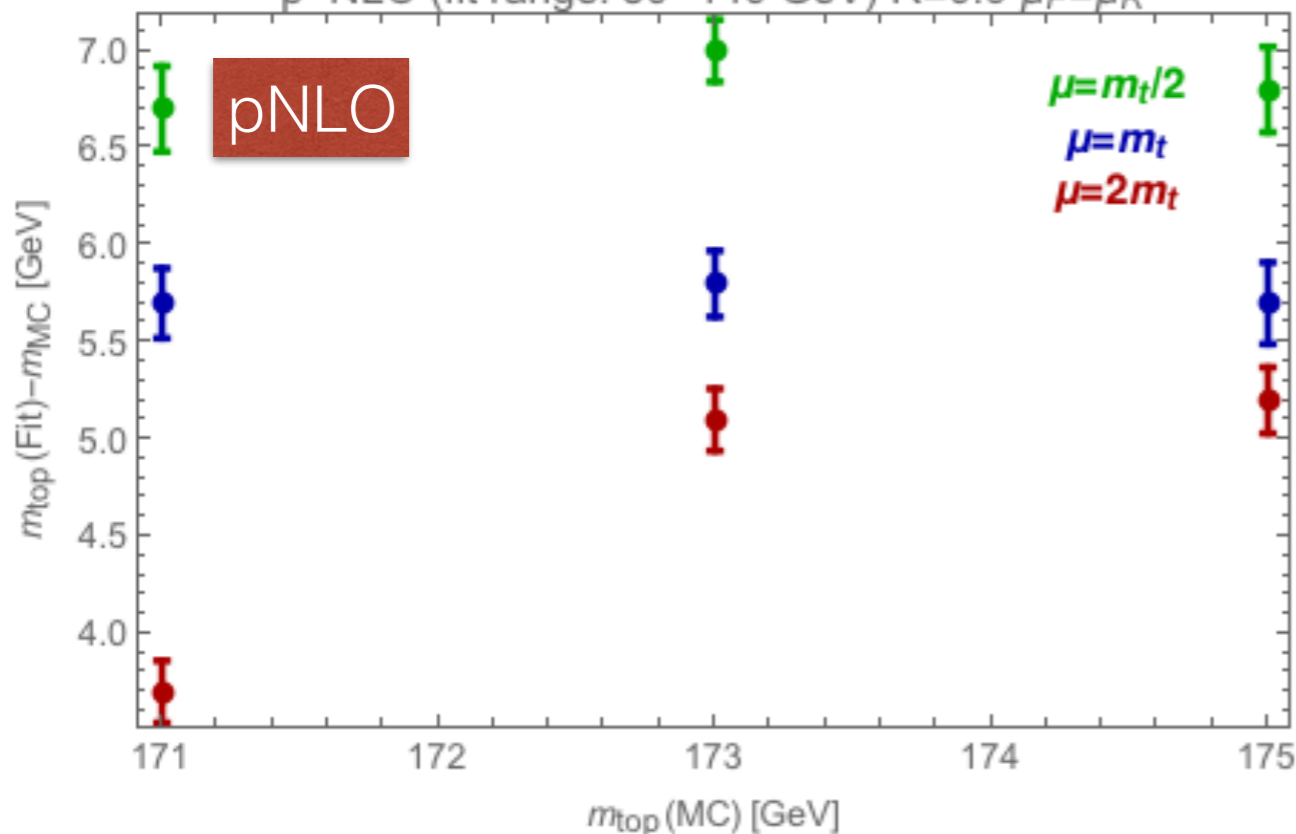
p-NLO (fit range: 30–140 GeV) $R=0.9$ $\mu_F \neq \mu_R$



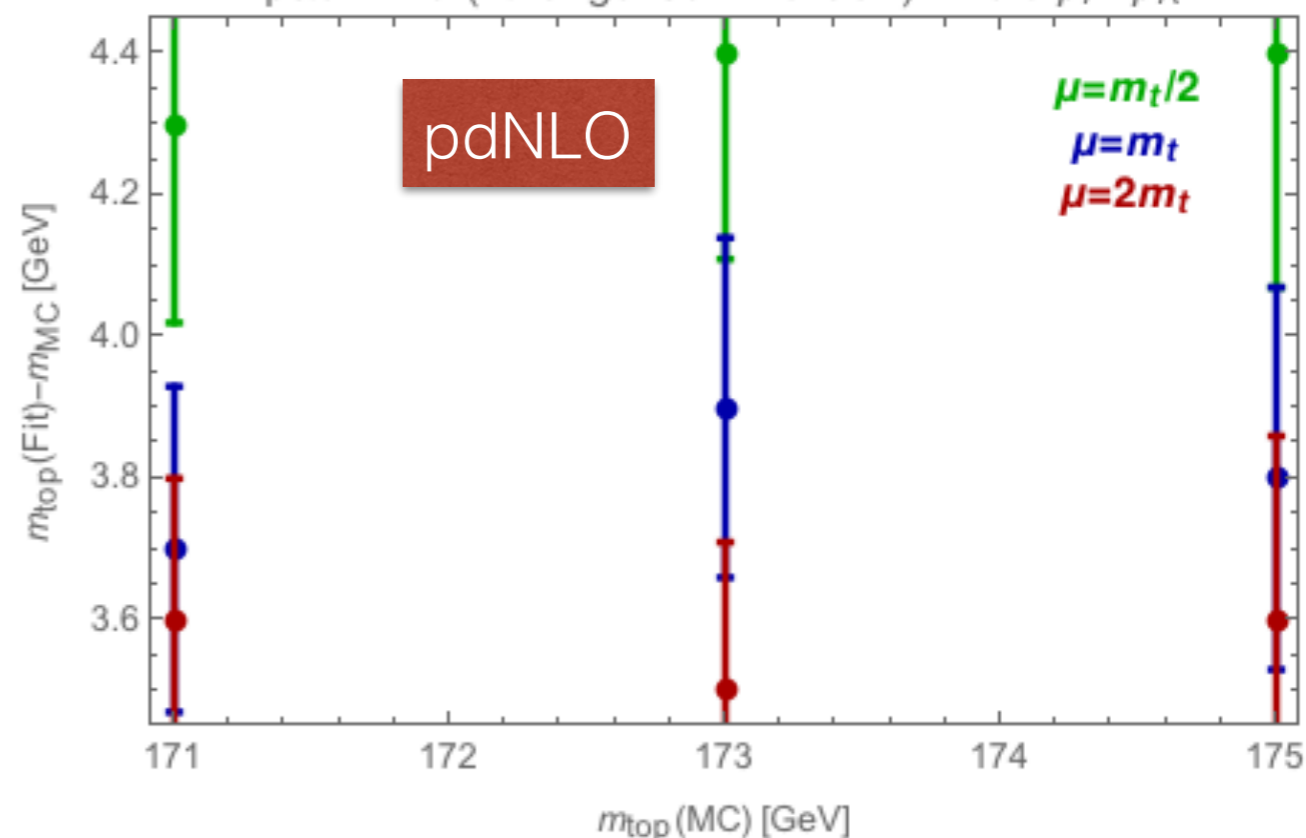
p&d-NLO (fit range: 30–140 GeV) $R=0.9$ $\mu_F \neq \mu_R$



p-NLO (fit range: 30–140 GeV) $R=0.9$ $\mu_F = \mu_R$



p&d-NLO (fit range: 30–140 GeV) $R=0.9$ $\mu_F = \mu_R$



Dependence on the scales

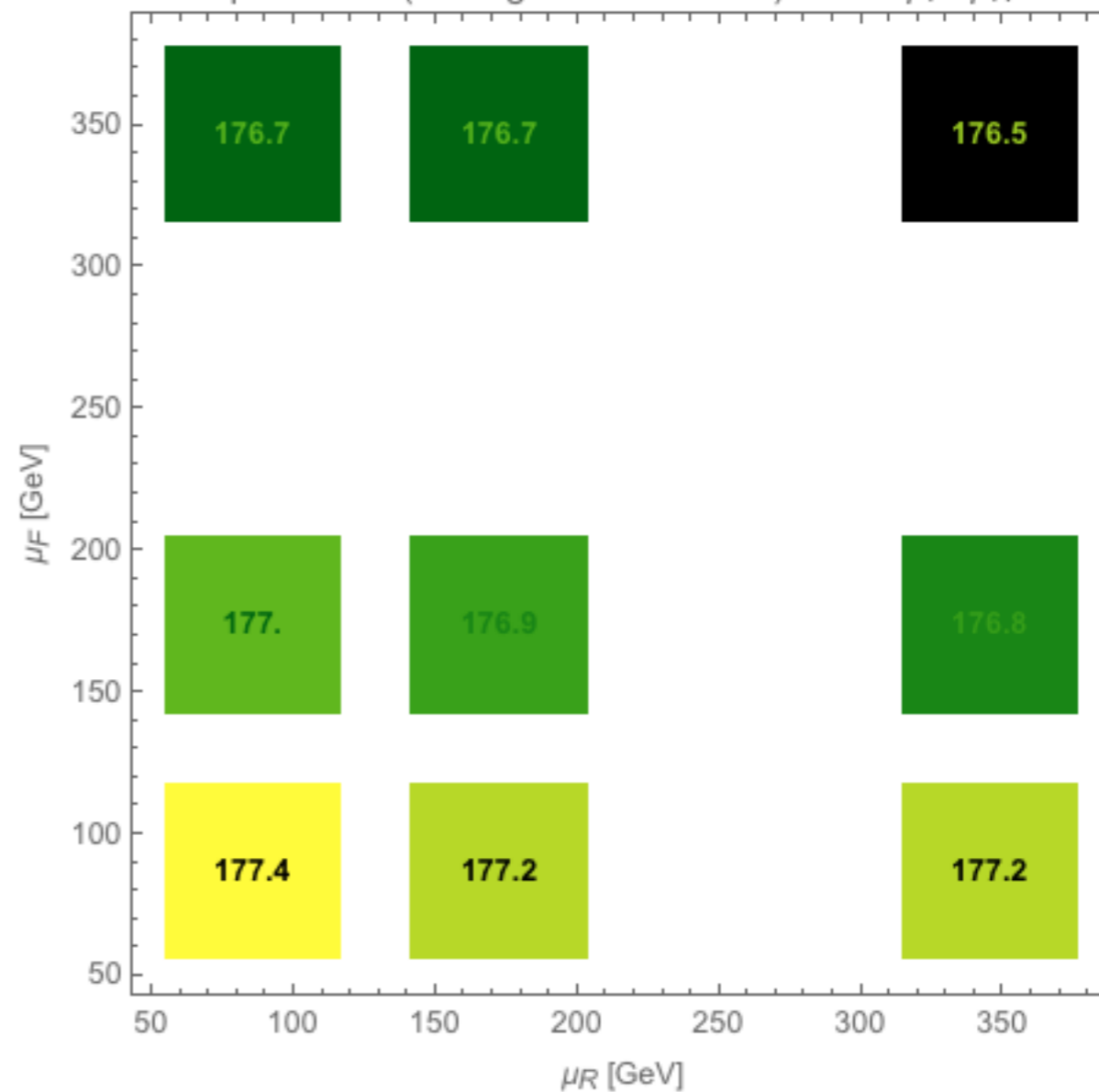
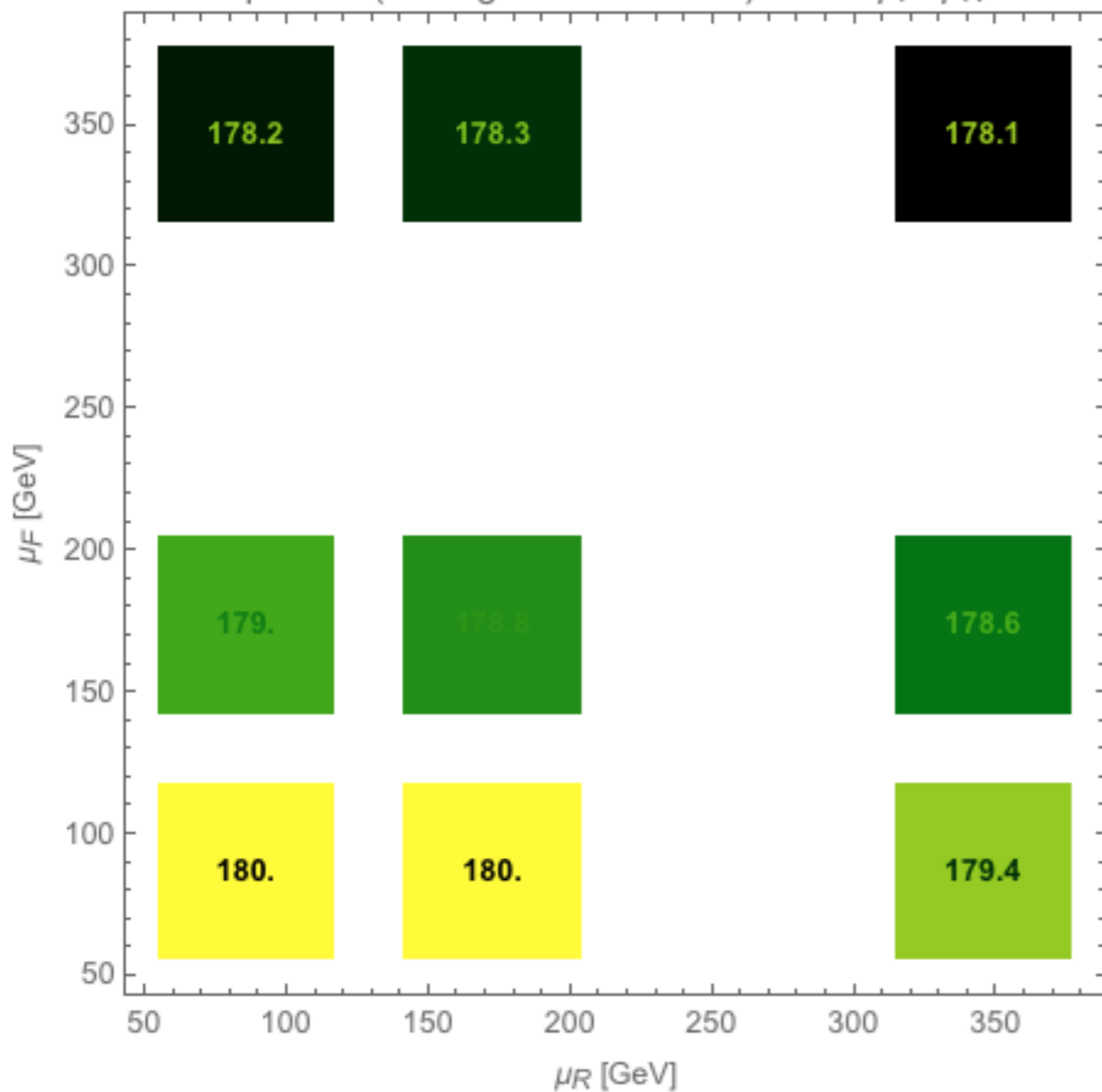
R=0.9 pNLO vs. pdNLO

pNLO

pdNLO

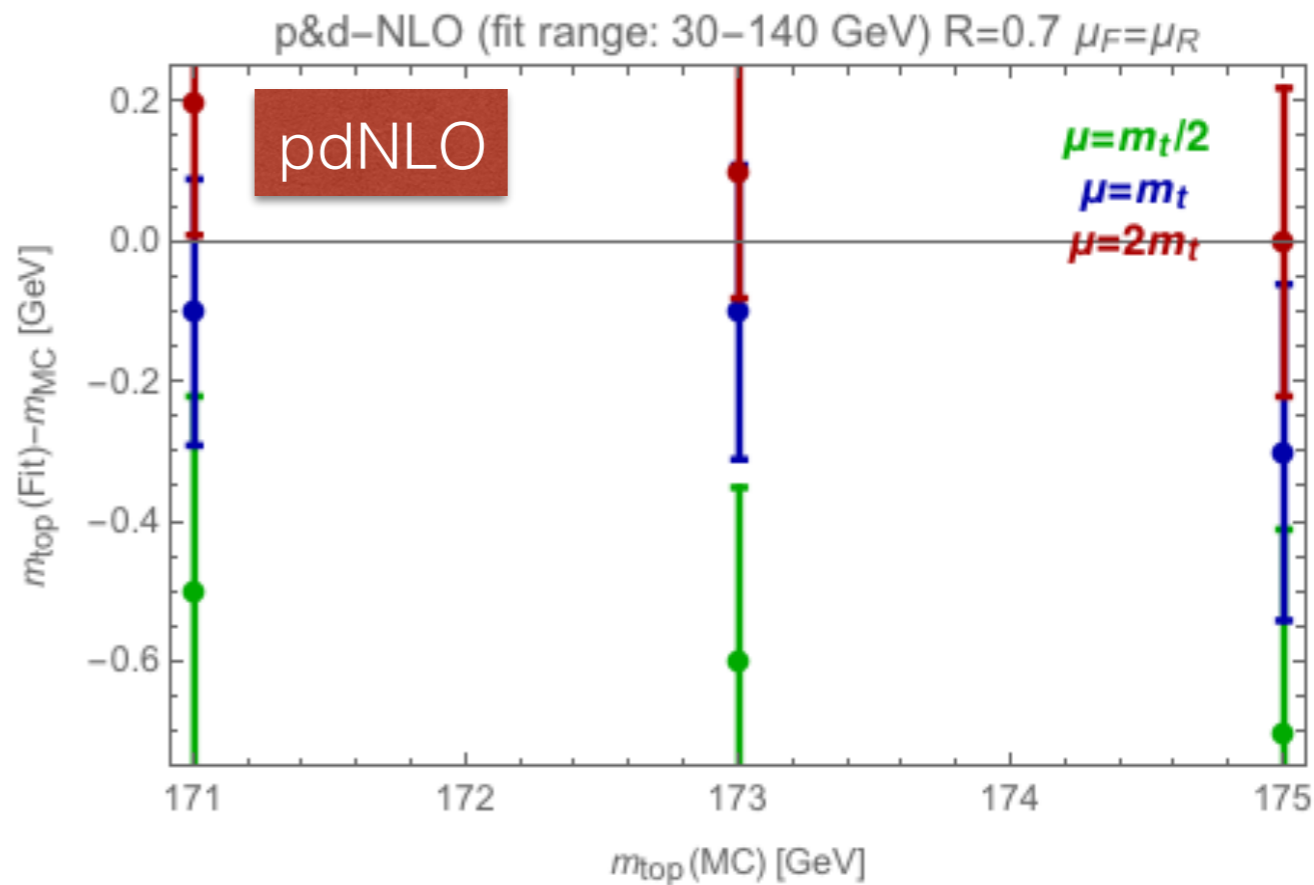
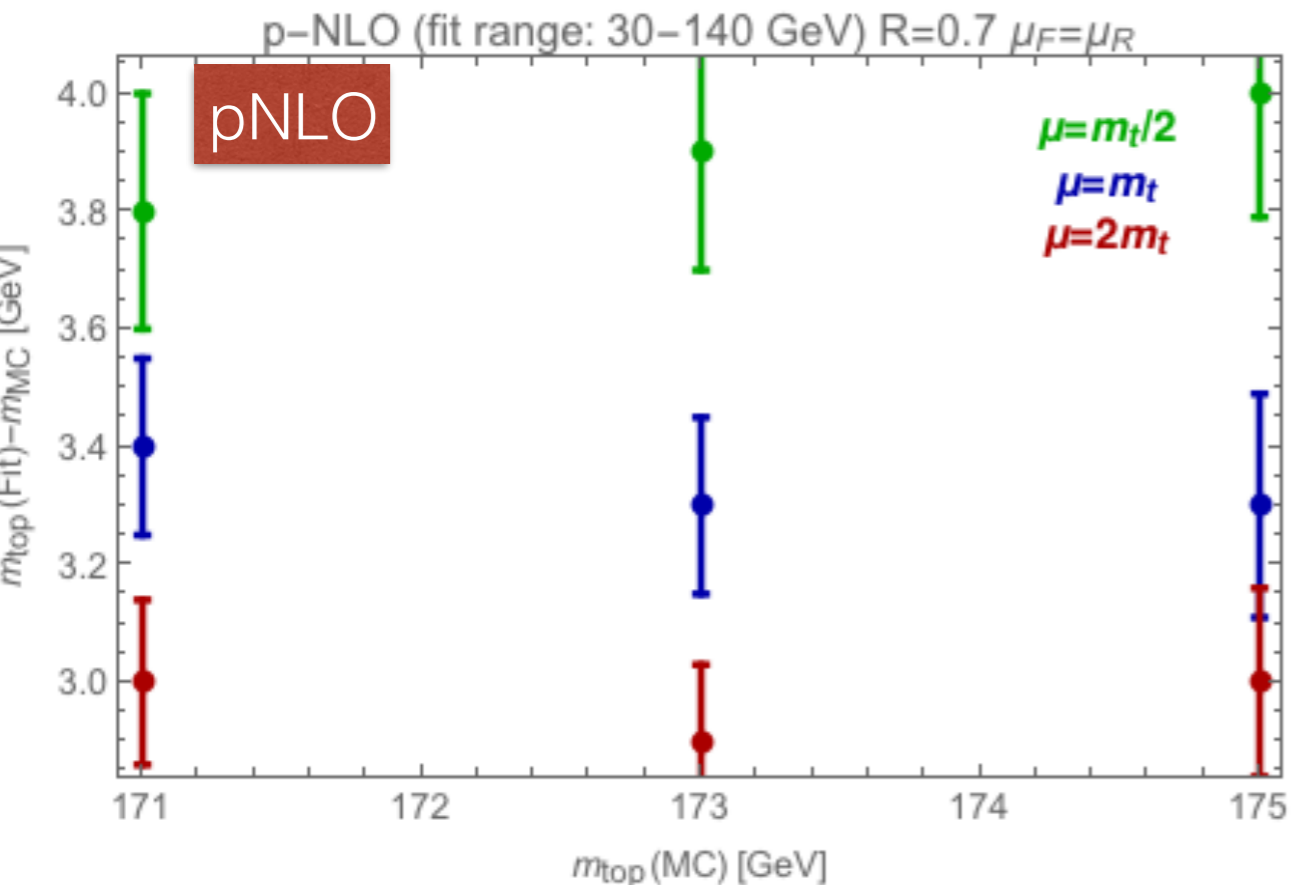
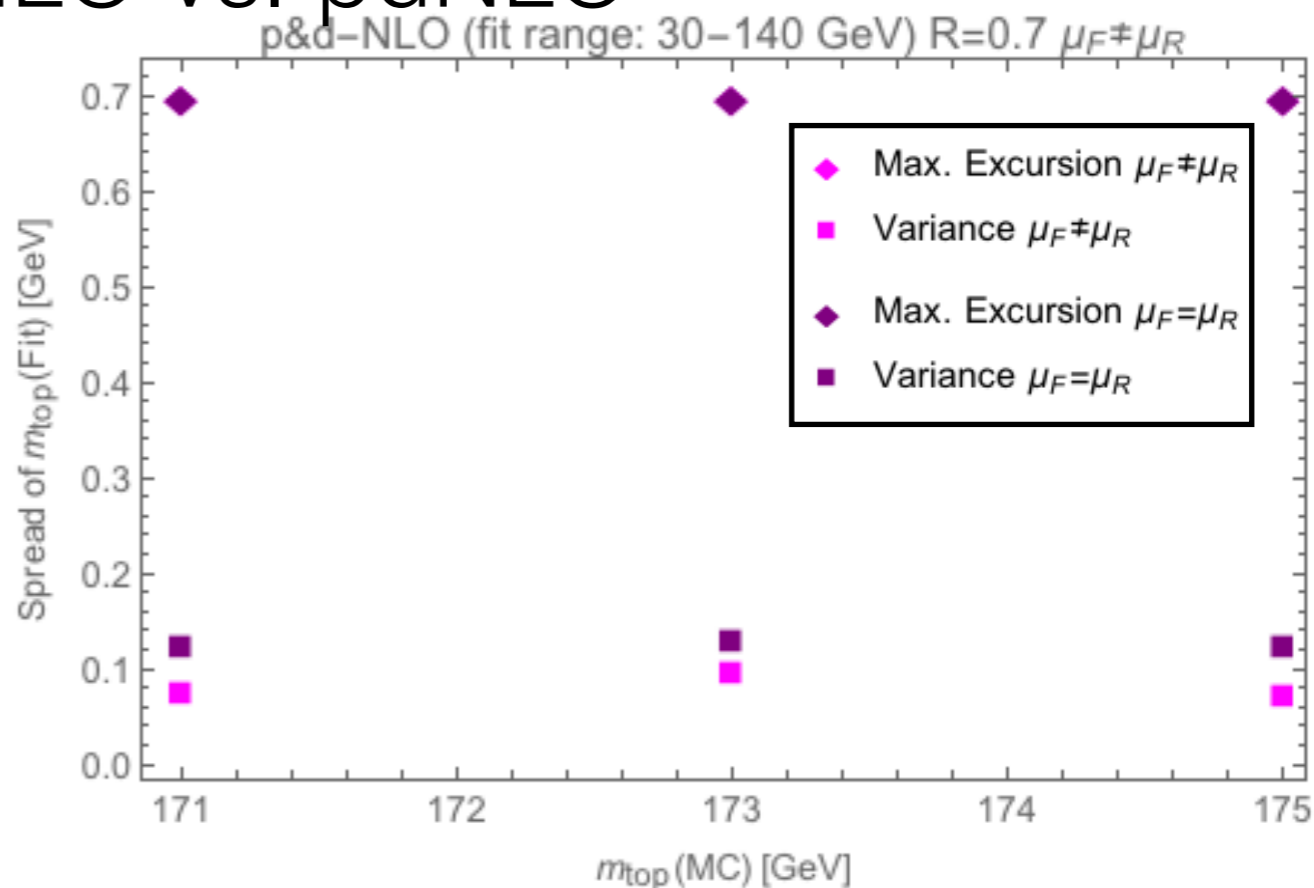
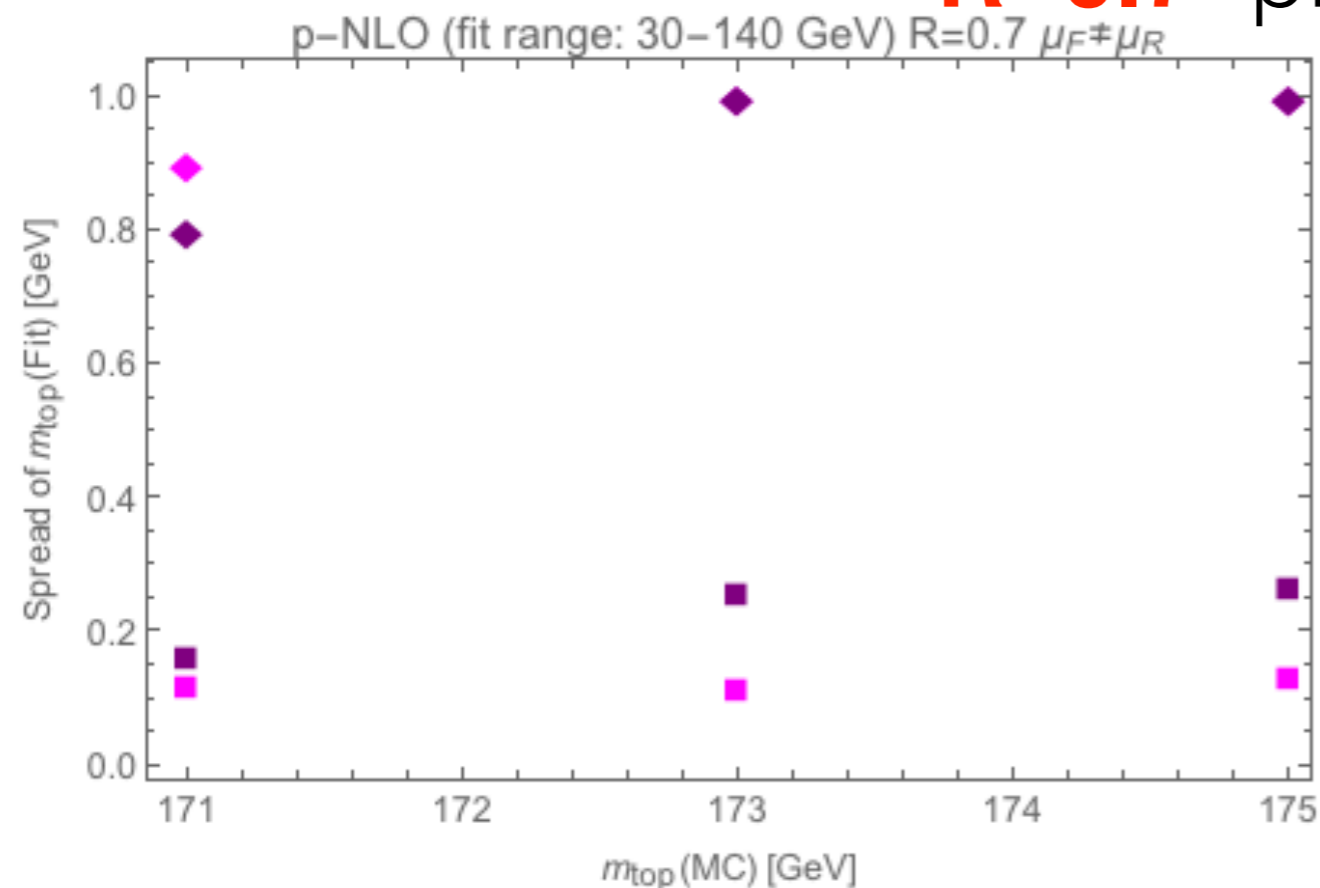
p-NLO (fit range: 30–140 GeV) $R=0.9$ $\mu_F \neq \mu_R$

p&d-NLO (fit range: 30–140 GeV) $R=0.9$ $\mu_F \neq \mu_R$



Dependence on the scales

R=0.7 pNLO vs. pdNLO



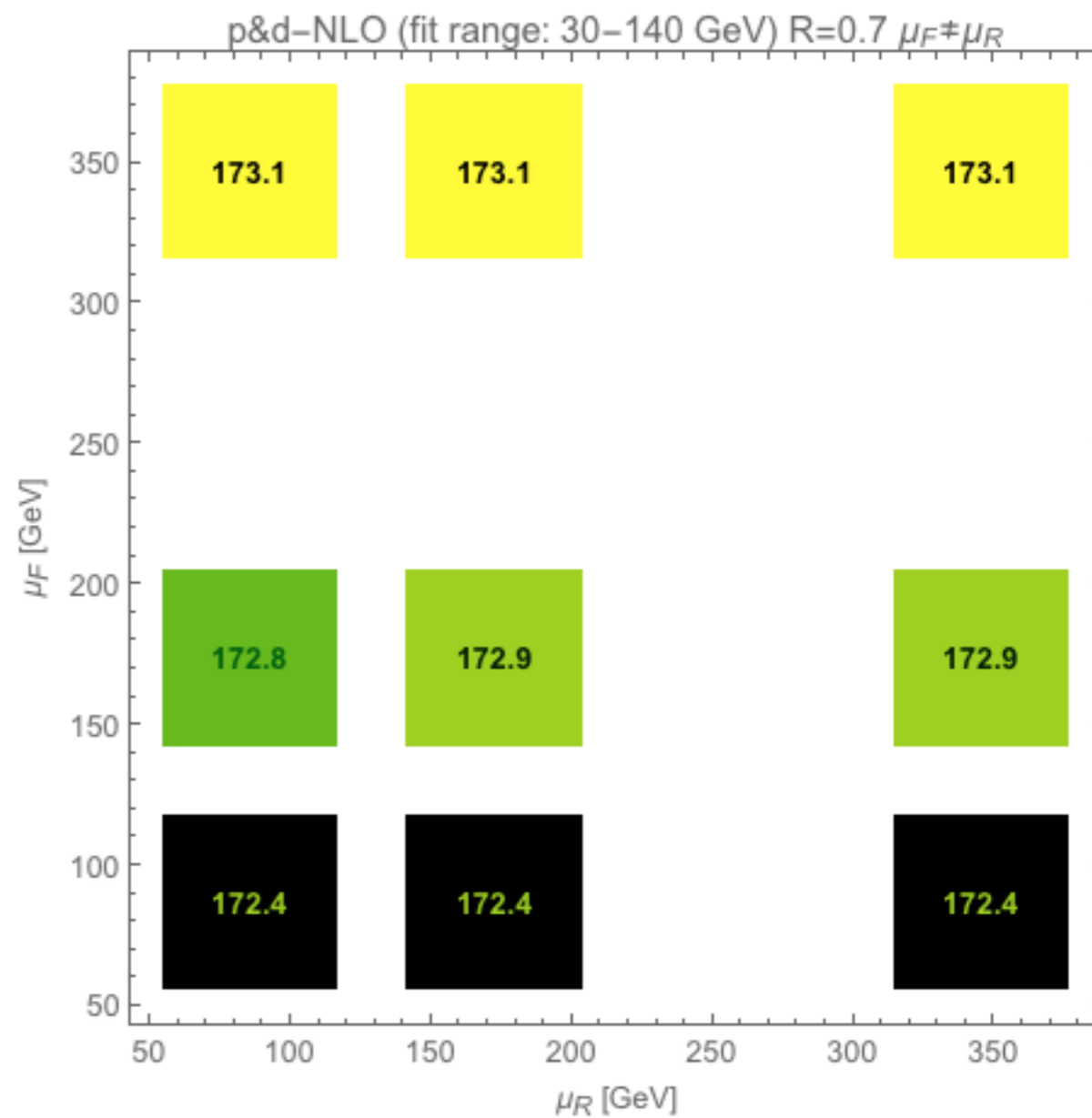
Dependence on the scales

R=0.7 pNLO vs. pdNLO

pNLO

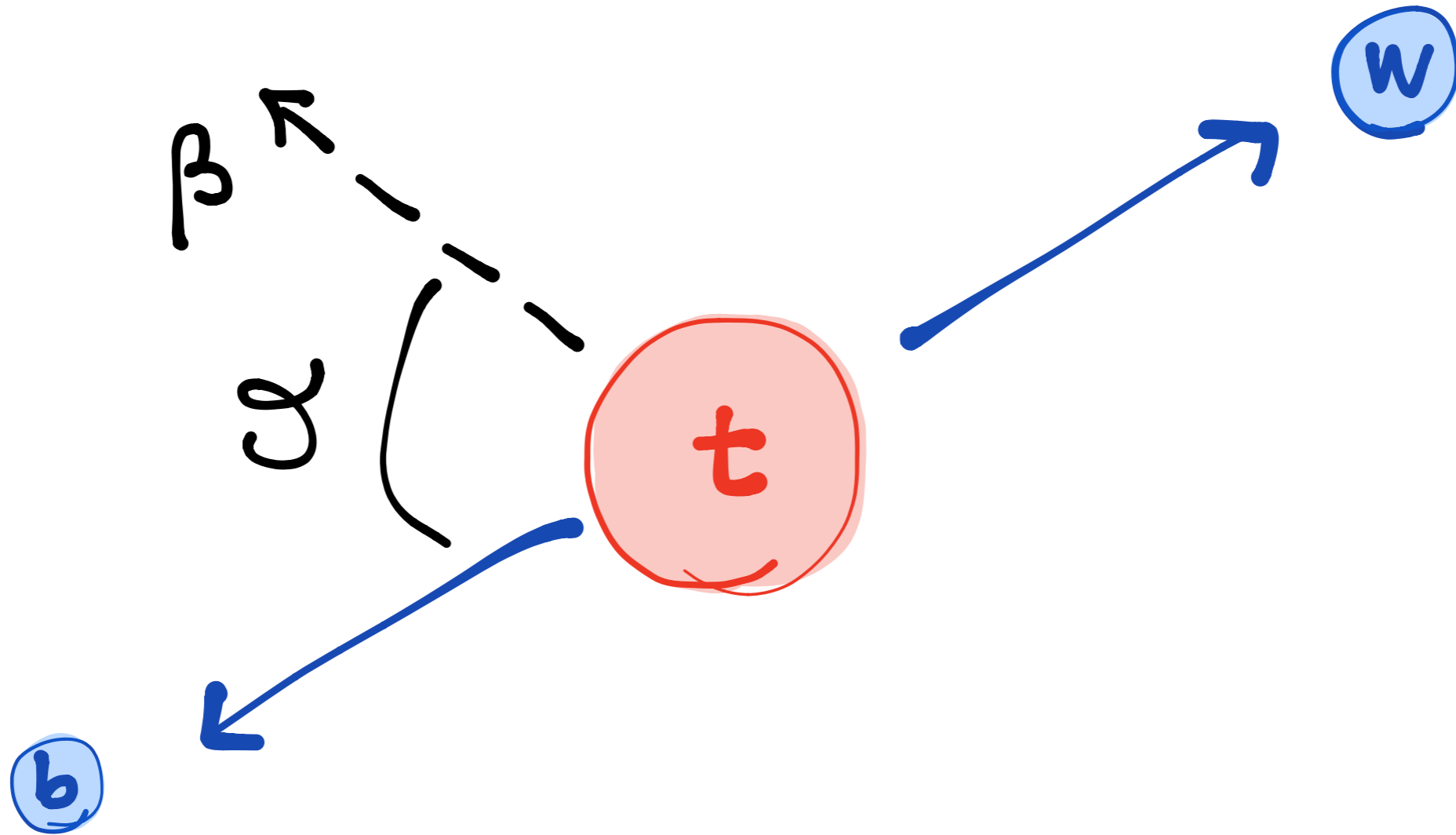


pdNLO



A simple, yet subtle, invariance of the two body decay

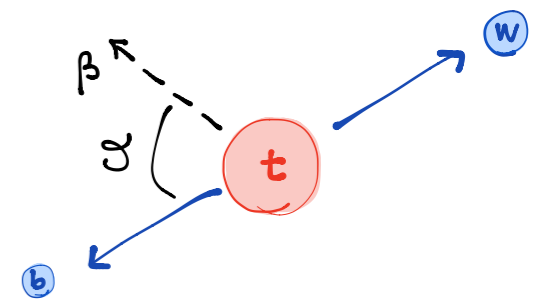
1209.0772 - Agashe, Franceschini and Kim



$$E_{\text{lab},b} = E_b^* \gamma + p_b^* \gamma \beta \cos \vartheta$$

Event-by-event we cannot tell anything

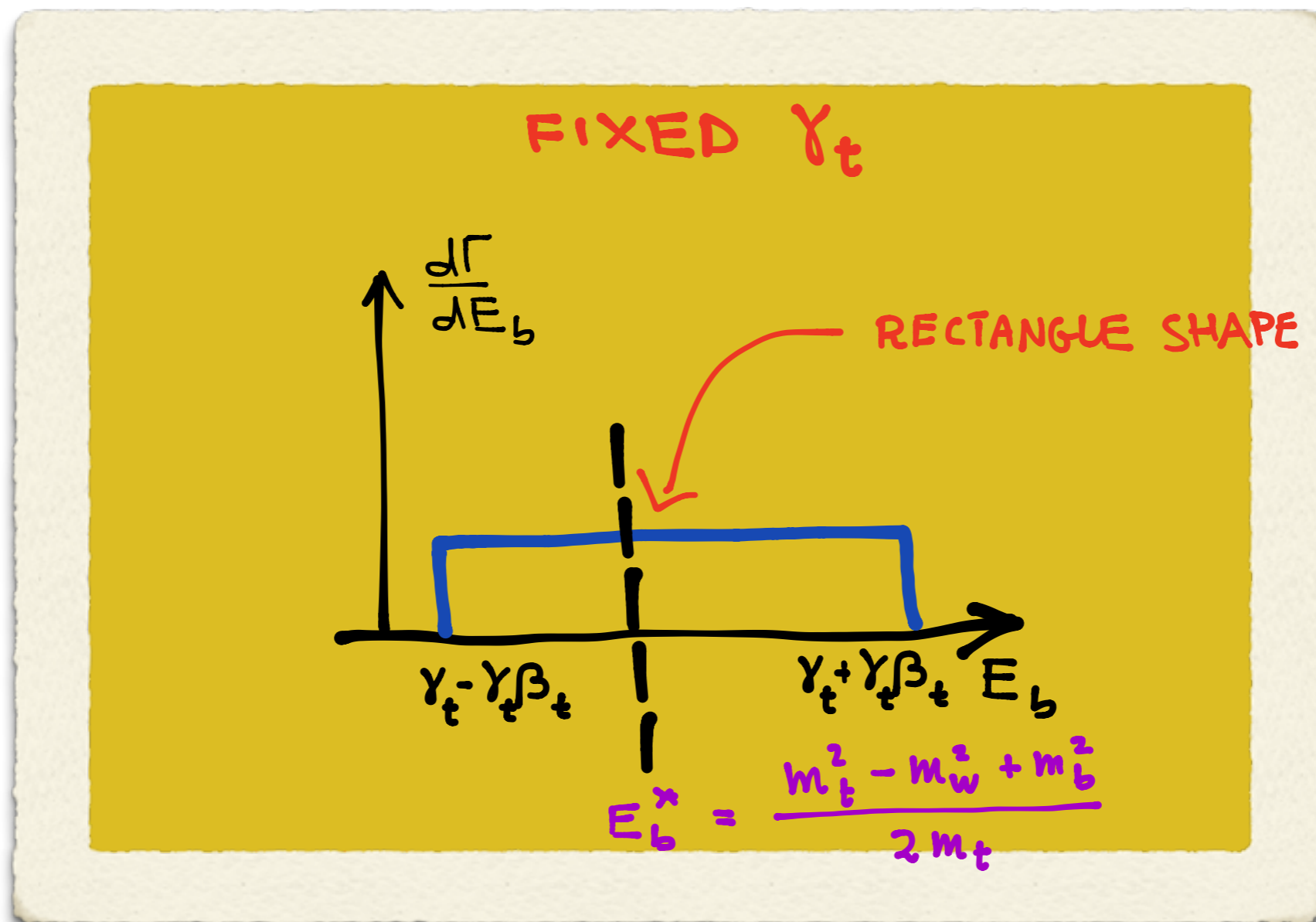
Fixed top boost decay



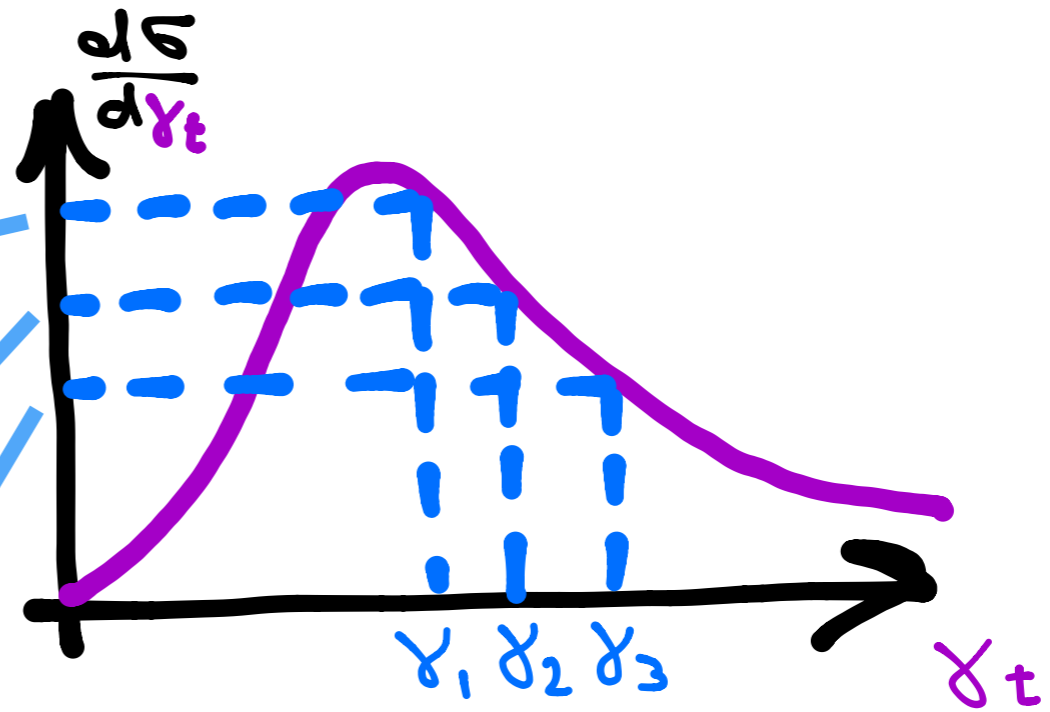
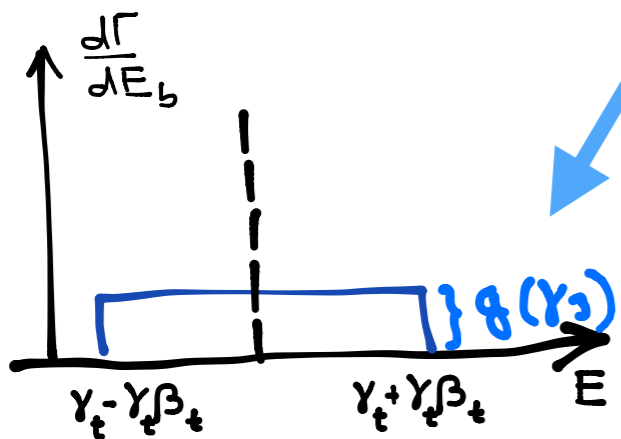
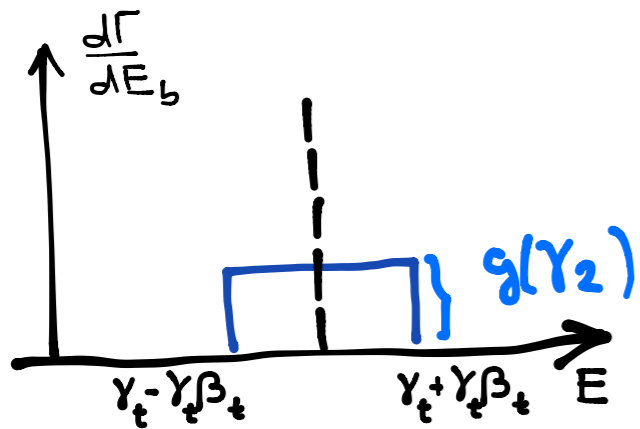
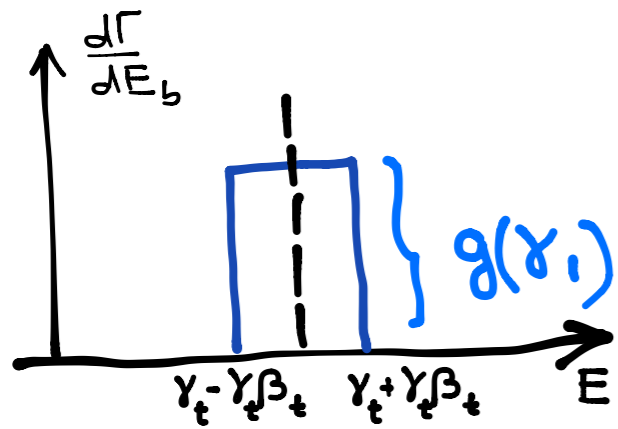
Massless b-quark (for now)

$$E_{lab,b} = E_b^* (\gamma + \gamma\beta \cos\vartheta)$$

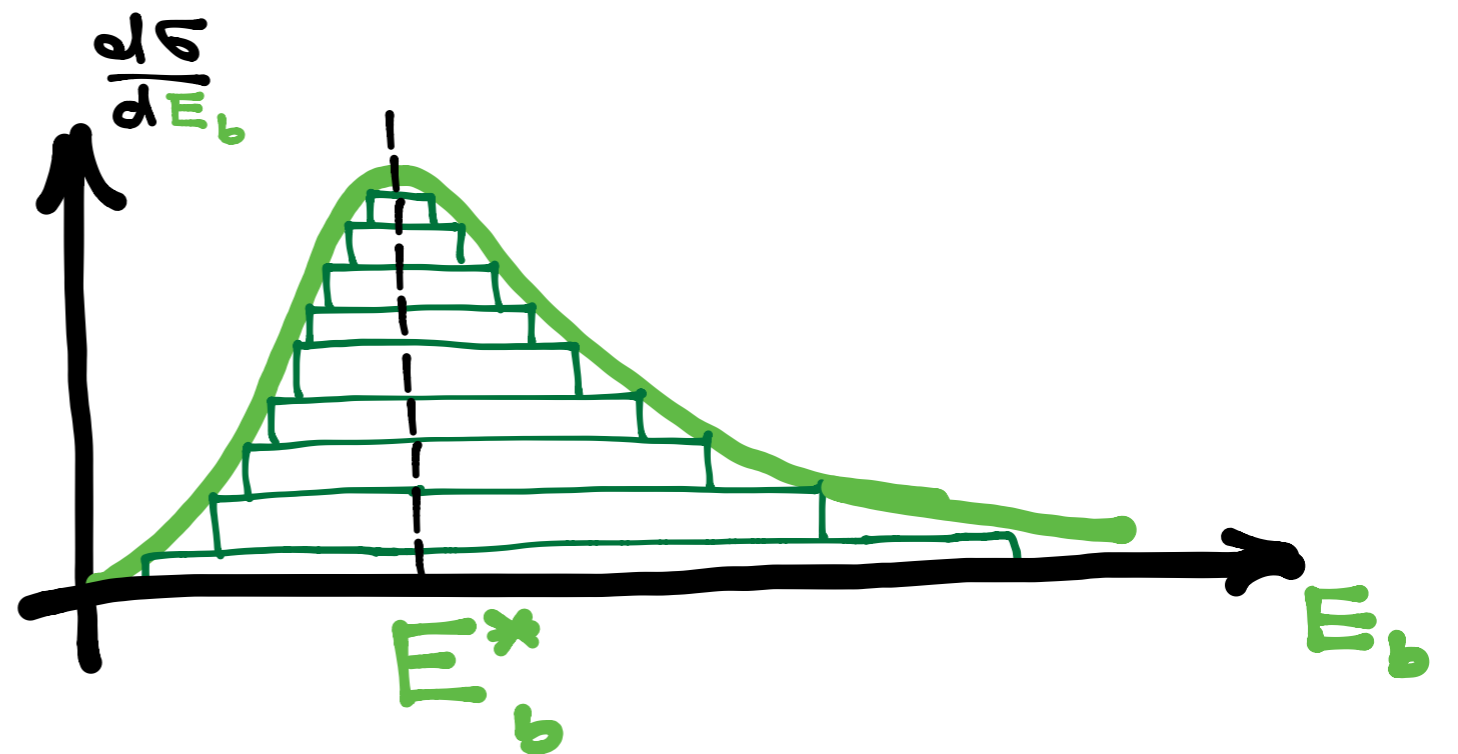
unpolarized top sample \rightarrow $\cos\theta$ is flat



Summing over the top boosts



THE ENERGY DISTRIBUTION IN THE LAB IS THE SUM OF ALL THE RECTANGLES

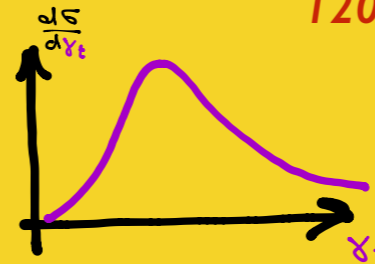


Lab-frame energy distribution

1209.0772 - Agashe, Franceschini and Kim

also Stecker 1971

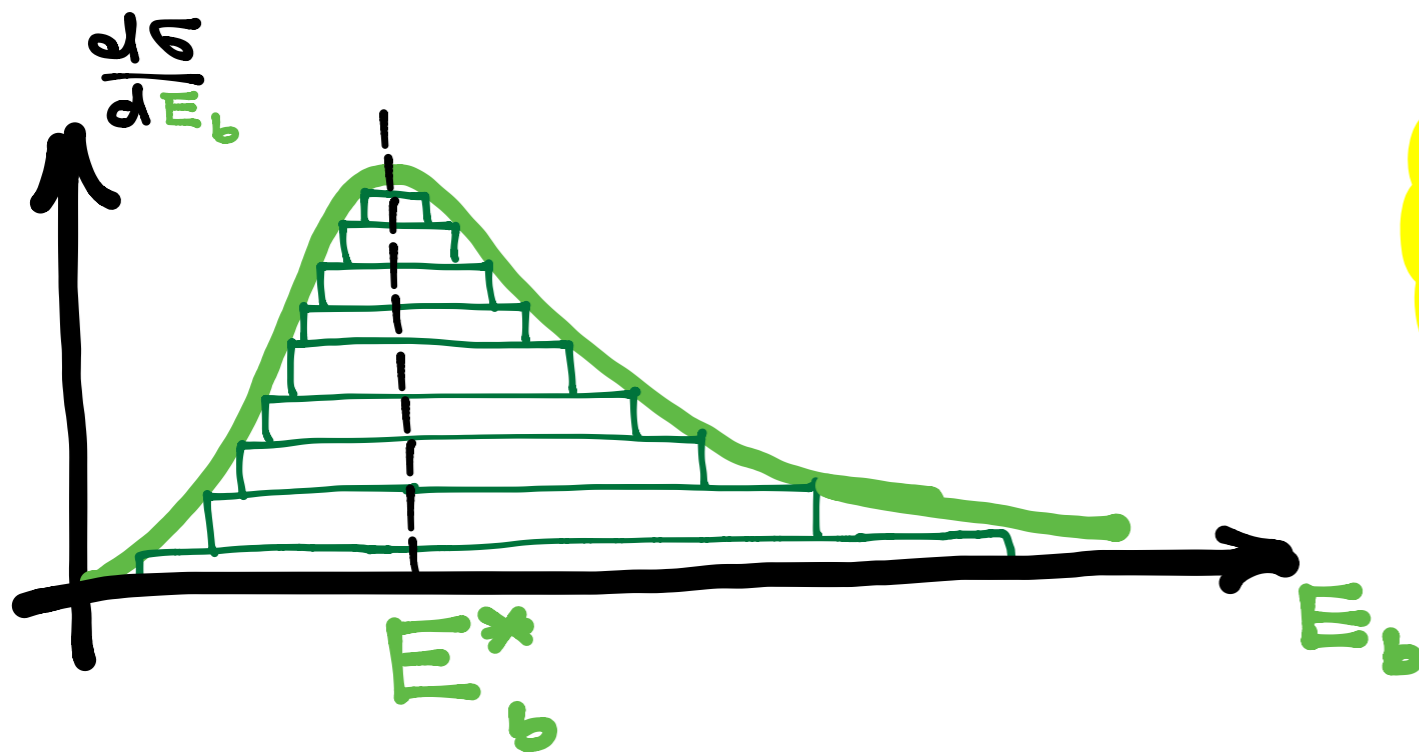
for any top boost distribution



the peak:

- is the same as in the rest frame
- encodes invariant

$$E_b^* = \frac{m_t^2 - m_w^2 + m_b^2}{2m_t}$$



THE FRAME-DEPENDENT
ENERGY DISTRIBUTION ENCODES
THE INVARIANT E_b^* IN A
VERY SIMPLE WAY

There is no difference when the b-mass is taken into account provided $\gamma_{top} < 500$

back