

# FLAVOUR OSCILLATIONS

in

## Dense Baryonic Matter

28. June 2016

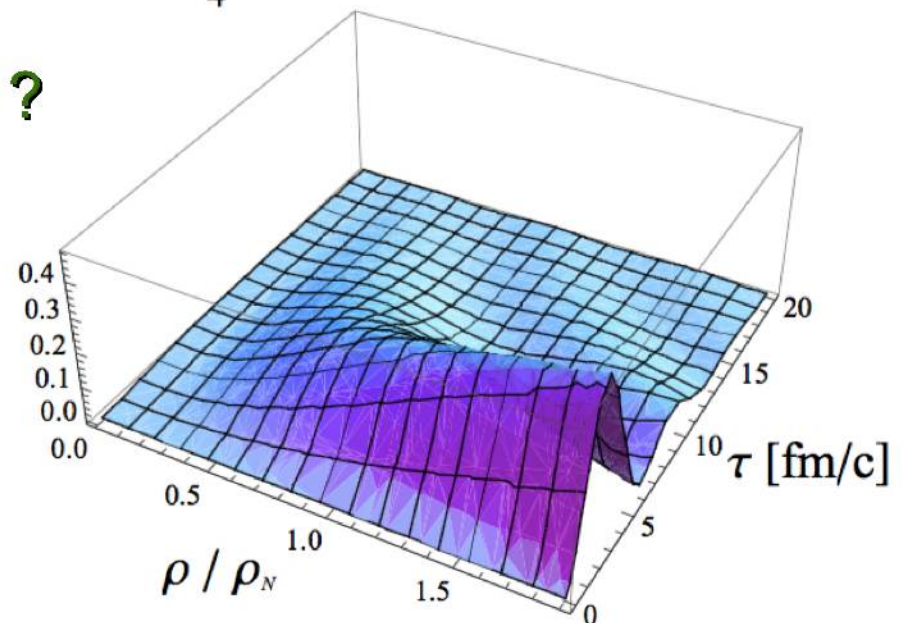
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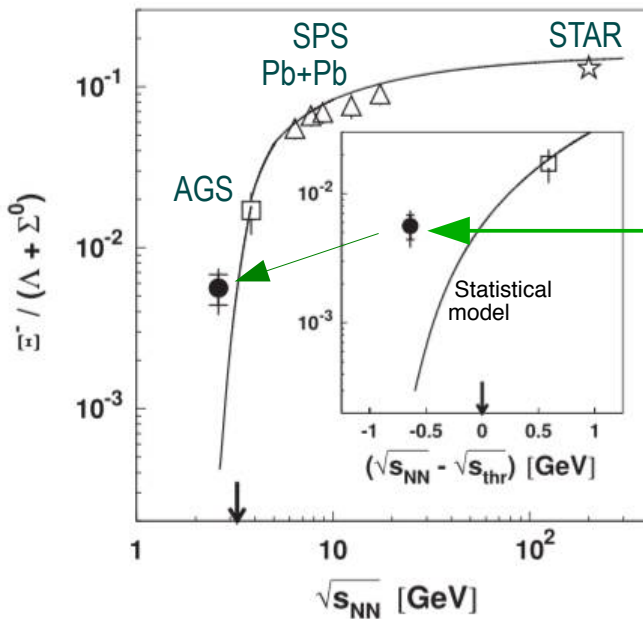
- Motivation:  $\Xi^-$  (dss) excess
- Strangeness is not conserved ?
- $K^0(ds')$   $\rightarrow$   $\bar{K}^0(d's)$
- $K^{0*}(896) \rightarrow \bar{K}^{0*}(896)$  [ in medium ]
- $D^0$  or  $D^{0*}$  oscillations ?
- Conclusions

$$|g_-(\tau)|^2 = \frac{1}{4} [e^{-\tau\Gamma_1} + e^{-\tau\Gamma_2} - 2\cos[\Delta M \cdot \tau] e^{-\tau(\Gamma_1 + \Gamma_2)/2}]$$

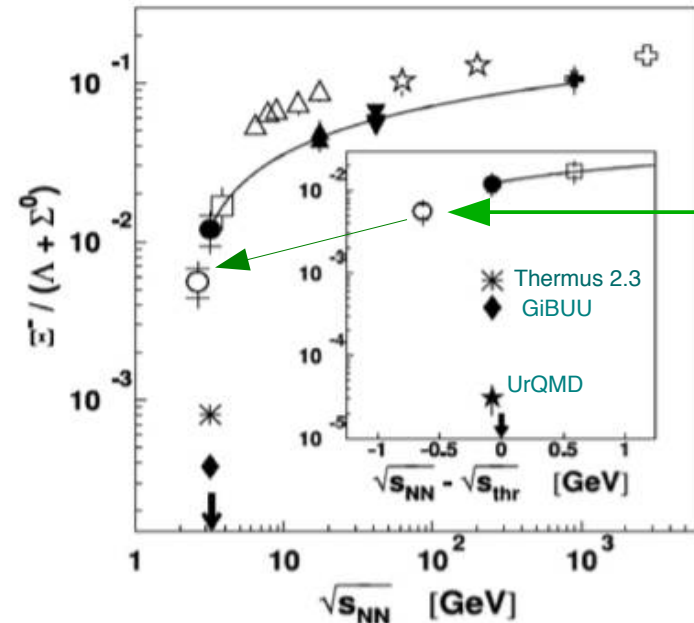


# MOTIVATION: $\Xi(ssd)$ excess

- There still is the unexplained **puzzle** of the strongly enhanced  $\Xi^-$  yield at the HADES
- SQM2013: Jour. of Phys. Conf. Ser. 509 (2014) 012002



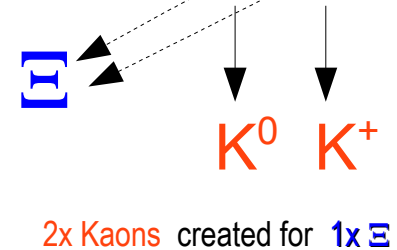
Ar+KCl  
HADES  
excess > 20x



p+Nb  
HADES

subthreshold production of  $\Xi^-$  means: not enough energy for  $[s\bar{s}+s\bar{s}]$

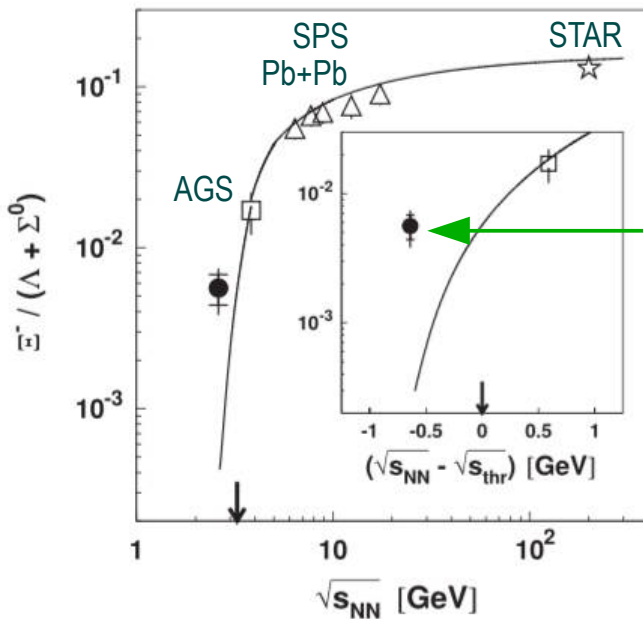
- Production of  $(s\bar{s})$  pair requires  $(\bar{s}\bar{s})$  creation
- 2 kaons with  $2 \times 497 \text{ MeV} = 1 \text{ GeV}$  of  $\text{Mass} \cdot c^2$
- Models + MC generators underestimate DATA



- Strangeness conservation means  $[\bar{s}\bar{s}] = 2x K$  for every  $[s\bar{s}]$  pair.

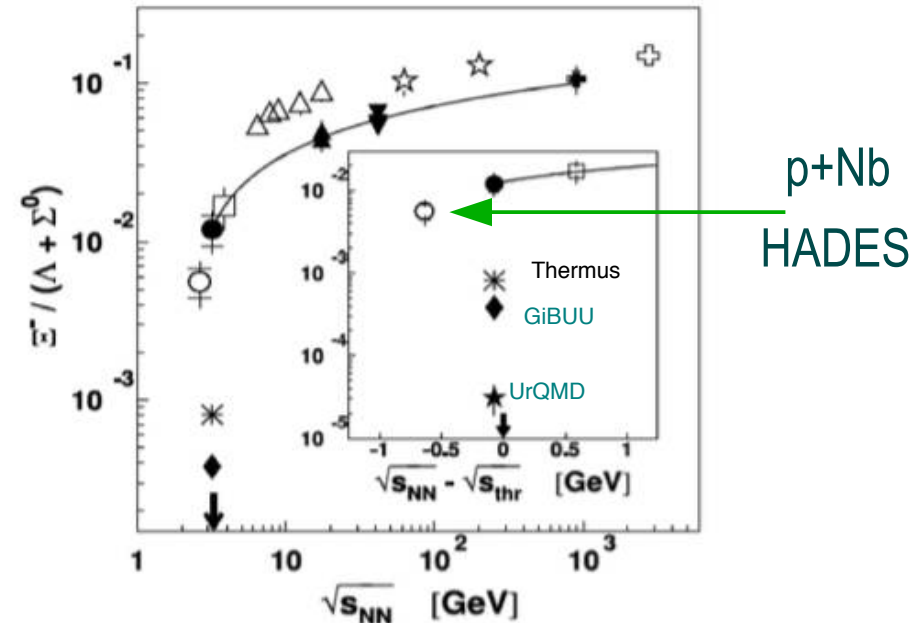
# MOTIVATION: $\Xi(ssd)$ excess

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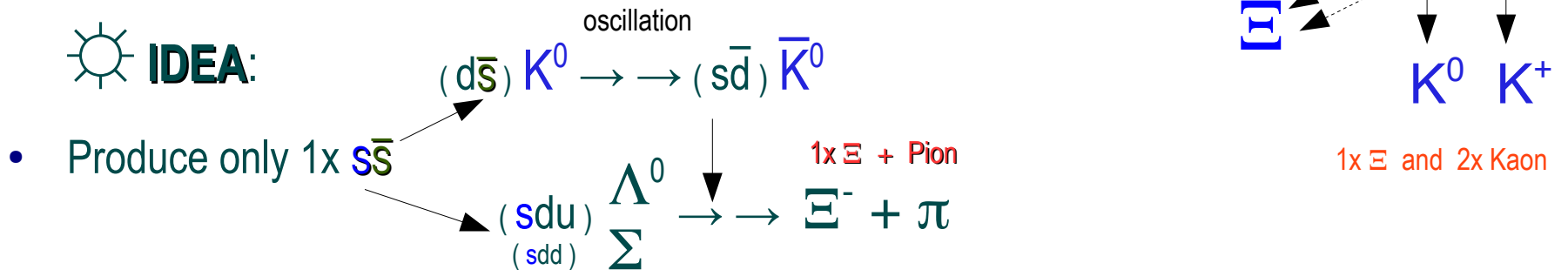
Ar+KCl  
HADES

excess  $\approx 20x$



subthreshold production of  $\Xi(ssd)$  means: not enough energy for  $[s\bar{s}+s\bar{s}]$

☀ **IDEA:**



- Strangeness non-conservation ( $K^0 \xrightarrow{\text{oscillation}} \bar{K}^0$ ) process in medium ?

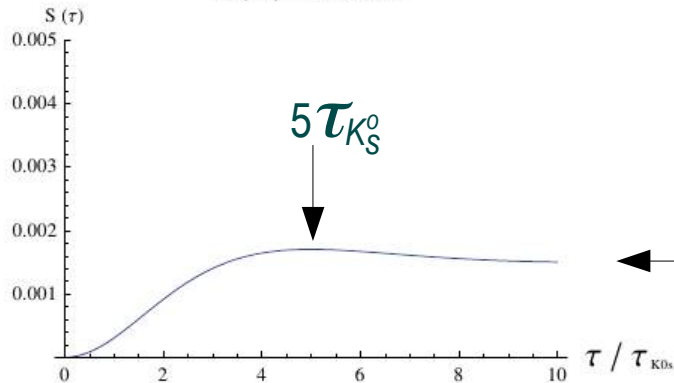
# Is strangeness conserved? **No!**

Physical Review D2 (1970) 540, in Eq.(7) CPT symmetry assumed

$$|\langle K_2^0 | K_1^0 \rangle| = \delta_{cp} \approx 10^{-3}$$

$$S(\tau) = \frac{\langle K_2^0 | K_1^0 \rangle [e^{-\gamma_1 \tau} + e^{-\gamma_2 \tau} - 2e^{-(\gamma_1 + \gamma_2)\tau/2} \cos(m_2 - m_1)\tau]}{e^{-\gamma_1 \tau} + e^{-\gamma_2 \tau} - 2e^{-(\gamma_1 + \gamma_2)\tau/2} \langle K_2^0 | K_1^0 \rangle^2 \cos(m_2 - m_1)\tau}$$

S(τ) in Vacuum



Let us produce:

$[K^0 \bar{K}^0]$  at  $\tau = 0$

$$\frac{\rho(\bar{s}) - \rho(s)}{\rho(\bar{s}) + \rho(s)} = S(\tau)$$

- Small =  $10^{-3}$  effect in Vacuum
- Takes long time  $\tau = 5\tau_{K_S^0} \gg 10\text{fm}/c$   $K_L \sim (1 + \epsilon_L)^{(d\bar{s})} K^0 - (1 - \epsilon_L) \bar{K}^0$
- Asymptotic value  $1.5 \times 10^{-3}$  due to  $K_L^0$  containing more  $K^0(d\bar{s})$  than  $\bar{K}^0(s\bar{d})$

when CP is violated: net-strangeness  $\rho(\bar{s}) - \rho(s)$  is not conserved

# Is strangeness conserved ? No!

$$|\langle K_2^0 | K_1^0 \rangle| = \delta_{cp} \approx 10^{-3}$$

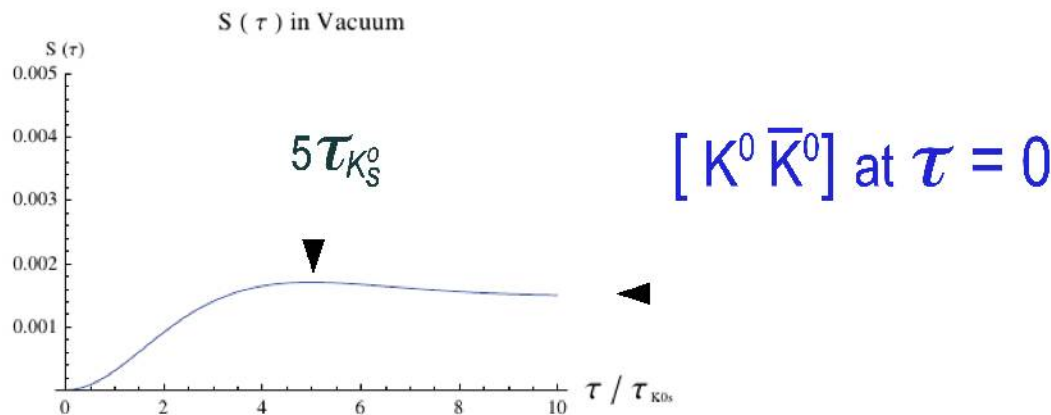
$$S(\tau) = \frac{\langle K_2^0 | K_1^0 \rangle [e^{-\gamma_1 \tau} + e^{-\gamma_2 \tau} - 2e^{-(\gamma_1 + \gamma_2)\tau/2} \cos(m_2 - m_1)\tau]}{e^{-\gamma_1 \tau} + e^{-\gamma_2 \tau} - 2e^{-(\gamma_1 + \gamma_2)\tau/2} \langle K_2^0 | K_1^0 \rangle^2 \cos(m_2 - m_1)\tau}$$

$$\Delta M_K = 3.48 \times 10^{-12} \text{ MeV}$$

MASS:  $(K_2 - K_1)$

Oscillation Length  $\rightarrow$

$$\frac{\rho(\bar{s}) - \rho(s)}{\rho(\bar{s}) + \rho(s)} = S(\tau)$$



- Small =  $10^{-3}$  effect in Vacuum

- Takes long time  $\tau = 5\tau_{K_S^0} \gg 10\text{fm}/c$

$$K_L \sim (1 + \epsilon_L) K^0 - (1 - \epsilon_L) \bar{K}^0$$

- Asymptotic value  $1.5 \times 10^{-3}$  due to  $K_L^0$  containing more  $K^0(d\bar{s})$  than  $\bar{K}^0(s\bar{d})$

when CP is violated: net-strangeness  $\rho(\bar{s}) - \rho(s)$  is not conserved.

# OSCILLATION LENGTHS in VACUUM

Table 1: Oscillation parameters of neutral  $K^0$ ,  $D^0$ ,  $B^0$ , and  $B_s^0$  mesons in vacuum.

	$K^0$	$D^0$	$B^0$	$B_s^0$
$\Delta m$ [MeV]	$3.5 \times 10^{-12}$	$\approx 6.3 \times 10^{-12}$	$3.3 \times 10^{-10}$	$11.7 \times 10^{-9}$
$\Delta m$ [ $\frac{10^{10} \hbar}{s}$ ]	$0.529 \pm 0.001$	$0.95 \pm 0.44$	$51.0 \pm 0.3$	$1776 \pm 2$
$\tau_0$ [ $10^{-12} s$ ]	89.5*	0.401	1.52	1.51
$\tau_{osc}$ [ $10^{-12} s$ ]	1187	$\approx 660$	12.3	0.35
$\tau_{osc}/\tau_0$	13.1*	$\approx 1650$	8.2	0.23
$c \cdot \tau_0$	2.7* cm	0.123 mm	0.45 mm	0.45 mm
$c \cdot \tau_{osc}$	35 cm	$\approx 20$ cm	3.7 mm	0.11 mm

$$\cos(\Delta m \tau)$$

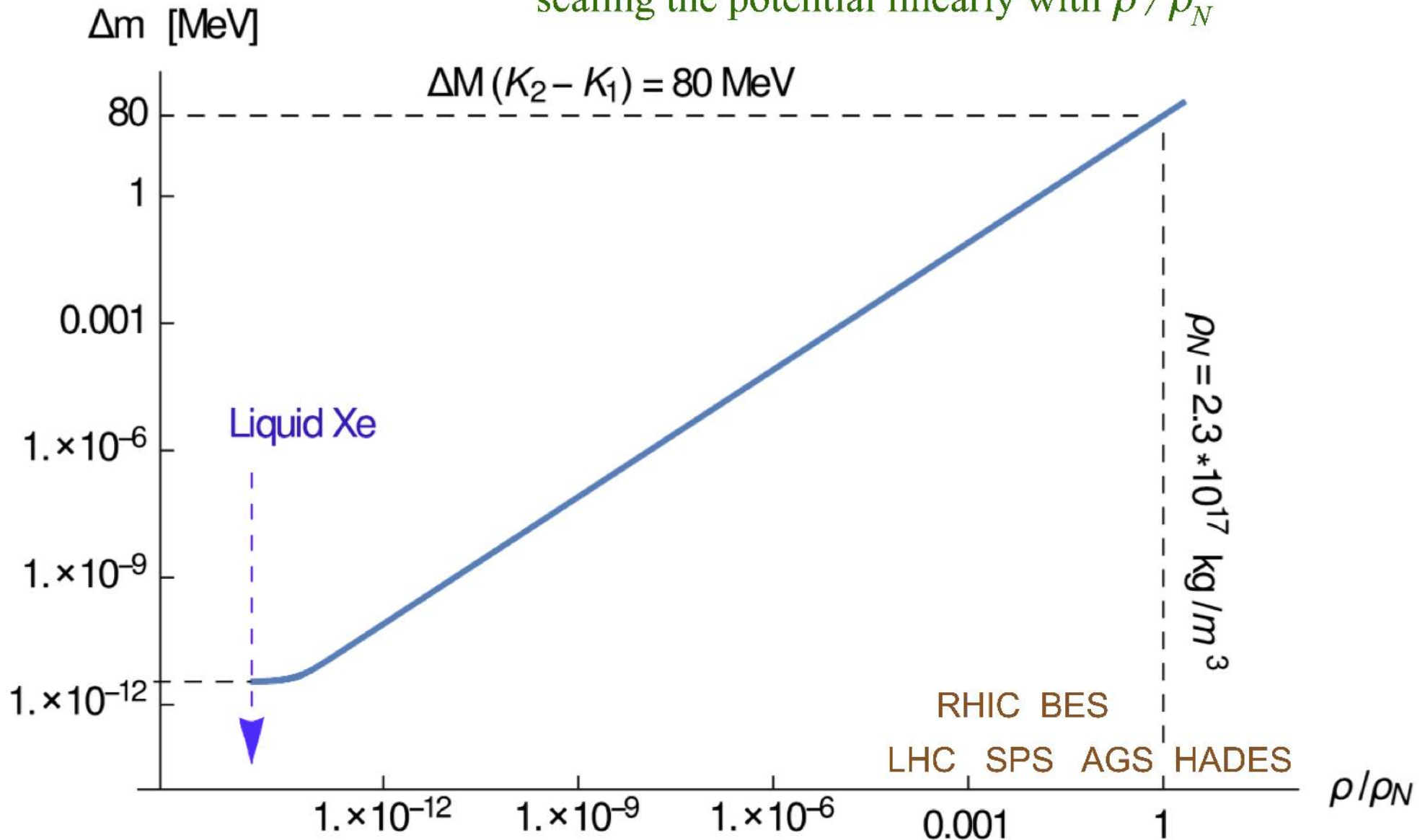
$$c\tau_{osc} = \frac{2\pi \hbar c}{\Delta m} = 15 \text{ fm} \left. \vphantom{\frac{2\pi \hbar c}{\Delta m}} \right\} \text{ in Nuclei}$$

$\swarrow$   $197 \text{ MeVfm}$        $\searrow$   $80 \text{ MeV}$

# Kaon Mass Difference in MEDIUM

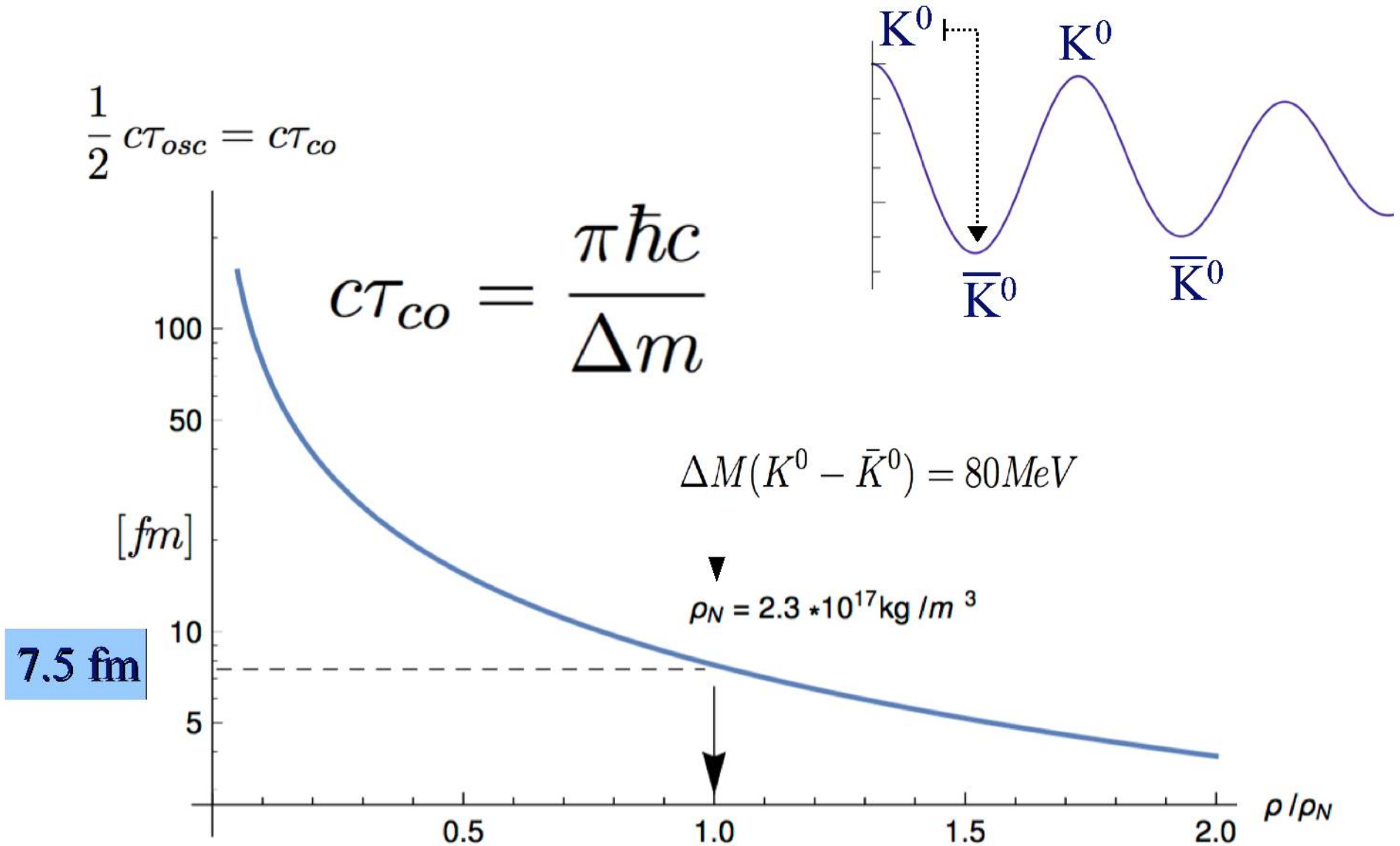
(assuming potential diff:  $|\bar{K}^0 - K^0| = 80 \text{ MeV}$  at  $\rho_N$ )

scaling the potential linearly with  $\rho / \rho_N$



# $K^0 \rightarrow \bar{K}^0$ conversion in dense Baryonic Matter

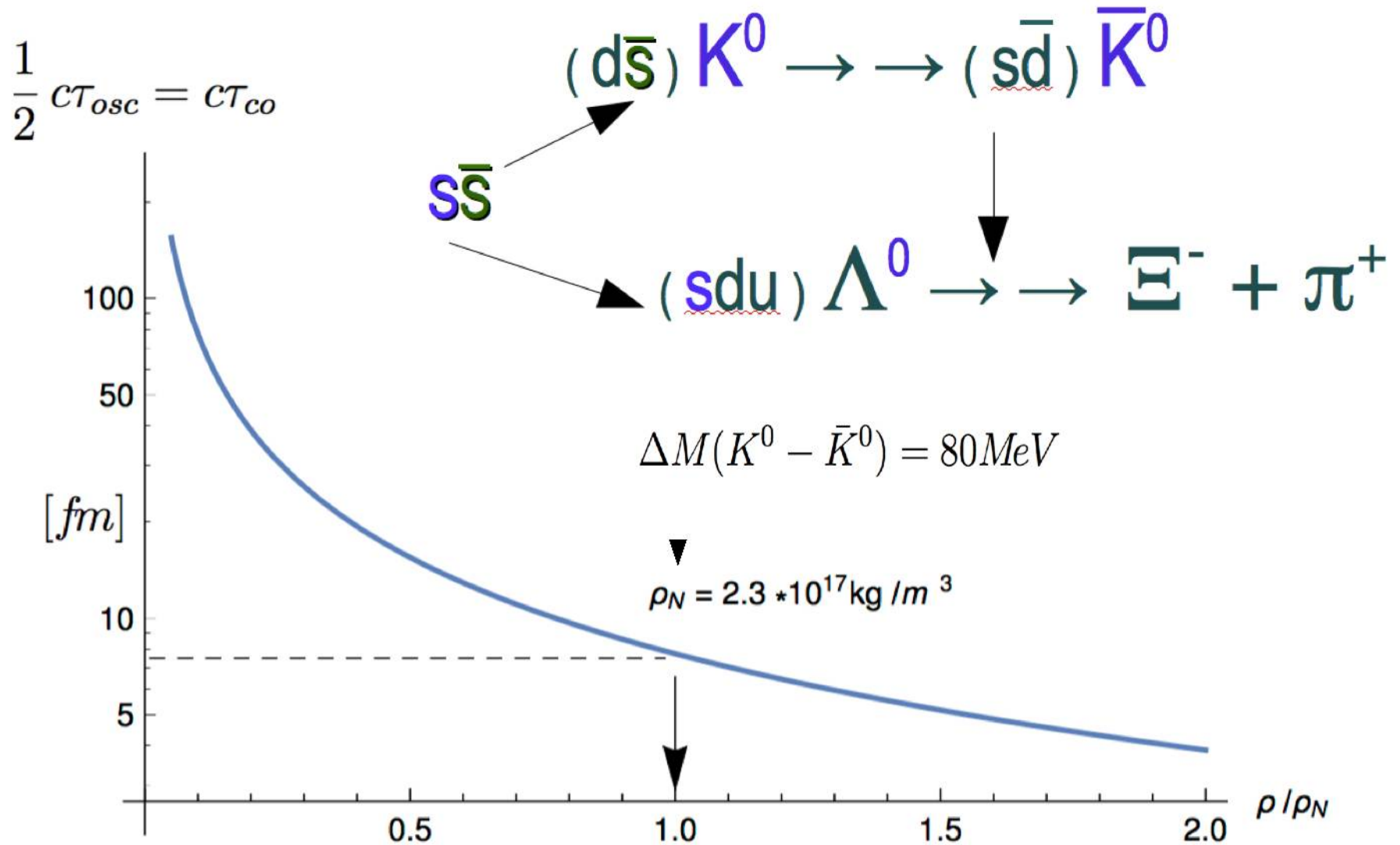
(assuming:  $\Delta M = 80 \text{ MeV}$  at  $\rho_N$ )





# $K^0 \rightarrow \bar{K}^0$ conversion in Baryonic Matter

can be fast enough for  $\Xi(ssd)$  to be created from 1x  $(s\bar{s})$  pair.



# Optimistic Observation:

1)  $K^0$  oscillation is modified in medium ( $\Delta m_K$ )

at  $\rho = \rho_N$  (dense baryonic matter)  $\tau_0 \approx 10 \text{ fm}/c$

$\Rightarrow$  conversion  $(d\bar{s}) \rightarrow (\bar{d}s)$  may be possible  
within very short time during hadronic phase of HIC

2) It might be related to  $\Xi(ssd)$  excess  
observed by HADES in Ar+KCl, p+Nb DATA  
+ other anomalies in Kaon production at AGS, SPS, GSI

# Calculation of $K^0 \rightarrow \bar{K}^0$ in Medium

$$\mathbb{H}' = \begin{bmatrix} \tilde{M}_{11} & M_{12} \\ M_{21} & \tilde{M}_{22} \end{bmatrix} - \frac{i}{2} \begin{pmatrix} \tilde{\Gamma}_{11} & \Gamma_{12} \\ \Gamma_{21} & \tilde{\Gamma}_{22} \end{pmatrix}$$

assuming **CPT symmetry violation**

$$\begin{aligned} \tilde{M}_{11} &= M_{11} + V_{K^0}(\rho_B) \quad , & \tilde{M}_{22} &= M_{22} - \bar{V}_{\bar{K}^0}(\rho_B) \\ \tilde{\Gamma}_{11} &= \Gamma_{11} + \gamma_{K^0}(\rho_B) \quad , & \tilde{\Gamma}_{22} &= \Gamma_{22} + \bar{\gamma}_{\bar{K}^0}(\rho_B) \end{aligned}$$

absorption  $K^0$ 
absorption  $\bar{K}^0$

$$\mathbb{M}_{K^0} = \begin{bmatrix} \overset{+ 20 \text{ MeV}}{497.7 + \underline{V_{K^0}(\rho_B)}} & e^{i\xi_M} 1.74 \cdot 10^{-12} \\ e^{-i\xi_M} 1.74 \cdot 10^{-12} & 497.7 - \underline{\bar{V}_{\bar{K}^0}(\rho_B)} \end{bmatrix}$$

60 - 80 MeV at  $\rho_N$

# Calculation of $K^0 \rightarrow \bar{K}^0$ in Medium

assuming CPT symmetry violation

$$|\langle \tilde{K}_2^0 | \tilde{K}_1^0 \rangle| = \delta_{cp} \rightarrow |\langle P_H | P_L \rangle|^2 = \frac{(1 + \delta_{cp}^2)|1 - \theta^2| - (1 - \delta_{cp}^2)(1 - |\theta|^2)}{(1 + \delta_{cp}^2)|1 - \theta^2| + (1 - \delta_{cp}^2)(1 + |\theta|^2)}$$

$$\rightarrow |P_L\rangle = p_L|P^0\rangle - q_L|\bar{P}^0\rangle \quad \frac{q_L}{p_L} = (1 - \theta) \frac{\Delta\mu}{2H_{12}}$$

**Eigenvectors:**

$$\rightarrow |P_H\rangle = p_H|P^0\rangle + q_H|\bar{P}^0\rangle \quad \frac{q_H}{p_H} = (1 + \theta) \frac{\Delta\mu}{2H_{12}}$$

$$\theta = \frac{M_{22} - M_{11} - \frac{i}{2}(\Gamma_{22} - \Gamma_{11})}{\sqrt{4H_{12}H_{21} + (H_{22} - H_{11})^2}}$$

**CPT violation Complex parameter**

see e.g. G. Branco et al. Book  
"CP Violation" Eq.(6.25 - 6.32)

$$|K^0\rangle(t) = [g_+(t) - \theta g_-(t)]|K^0\rangle + \frac{q_H}{p_H}(1 - \theta)g_-(t)|\bar{K}^0\rangle \quad \text{Time evolution of}$$

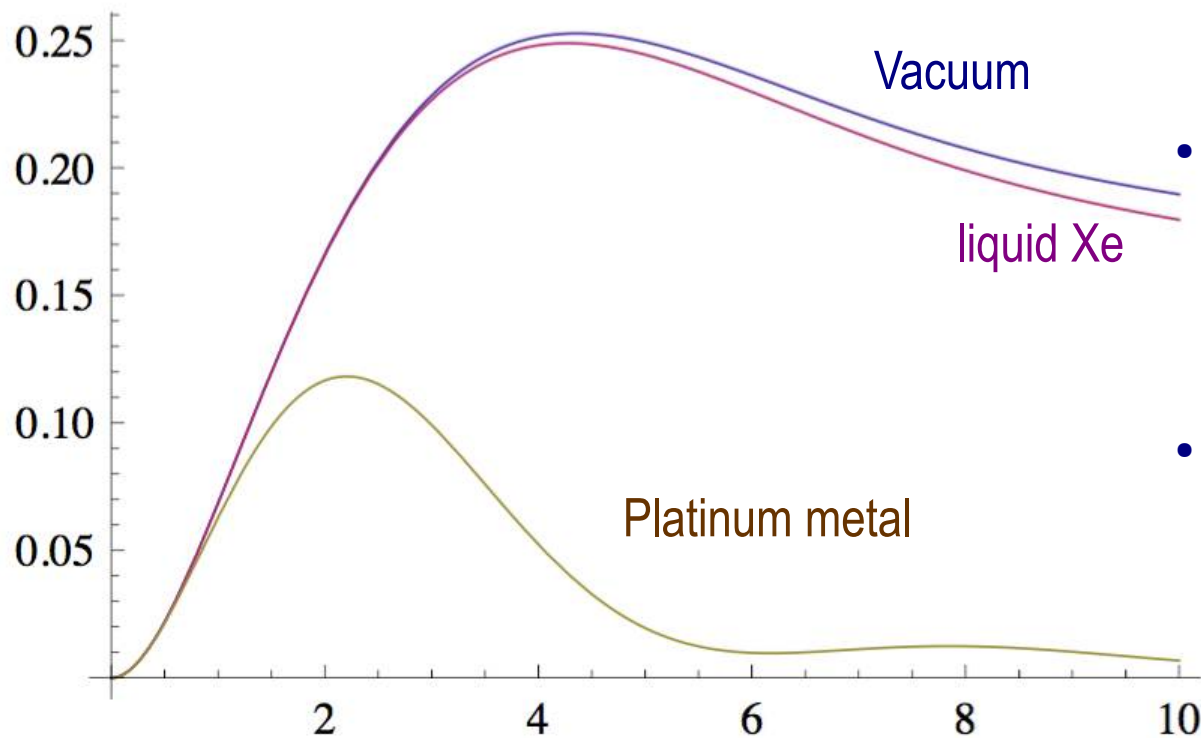
$$|\bar{K}^0\rangle(t) = [g_+(t) + \theta g_-(t)]|\bar{K}^0\rangle + \frac{p_L}{q_L}(1 - \theta)g_-(t)|K^0\rangle \quad \text{strong } K^0 \text{ states}$$

**For eigenvalues one has:**  $\Delta\mu = M_H - M_L - \frac{i}{2}(\Gamma_H - \Gamma_L) = \sqrt{4H_{12}H_{21} + (H_{22} - H_{11})^2}$

# Strangeness oscillation in medium:

$$[K^0 \rightsquigarrow \bar{K}^0]_{(\tau)} = \left| \frac{q_H}{p_H} \right|^2 |g_-(\tau)|^2 |(1 - \theta)|^2 \quad \text{Branco et al.: CP Violation Eq.(9.8)}$$

P [ $K^0 \rightarrow \text{anti-}K^0$ ]



- Probability P[ $K^0 \rightarrow \bar{K}^0$ ] is suppressed in medium

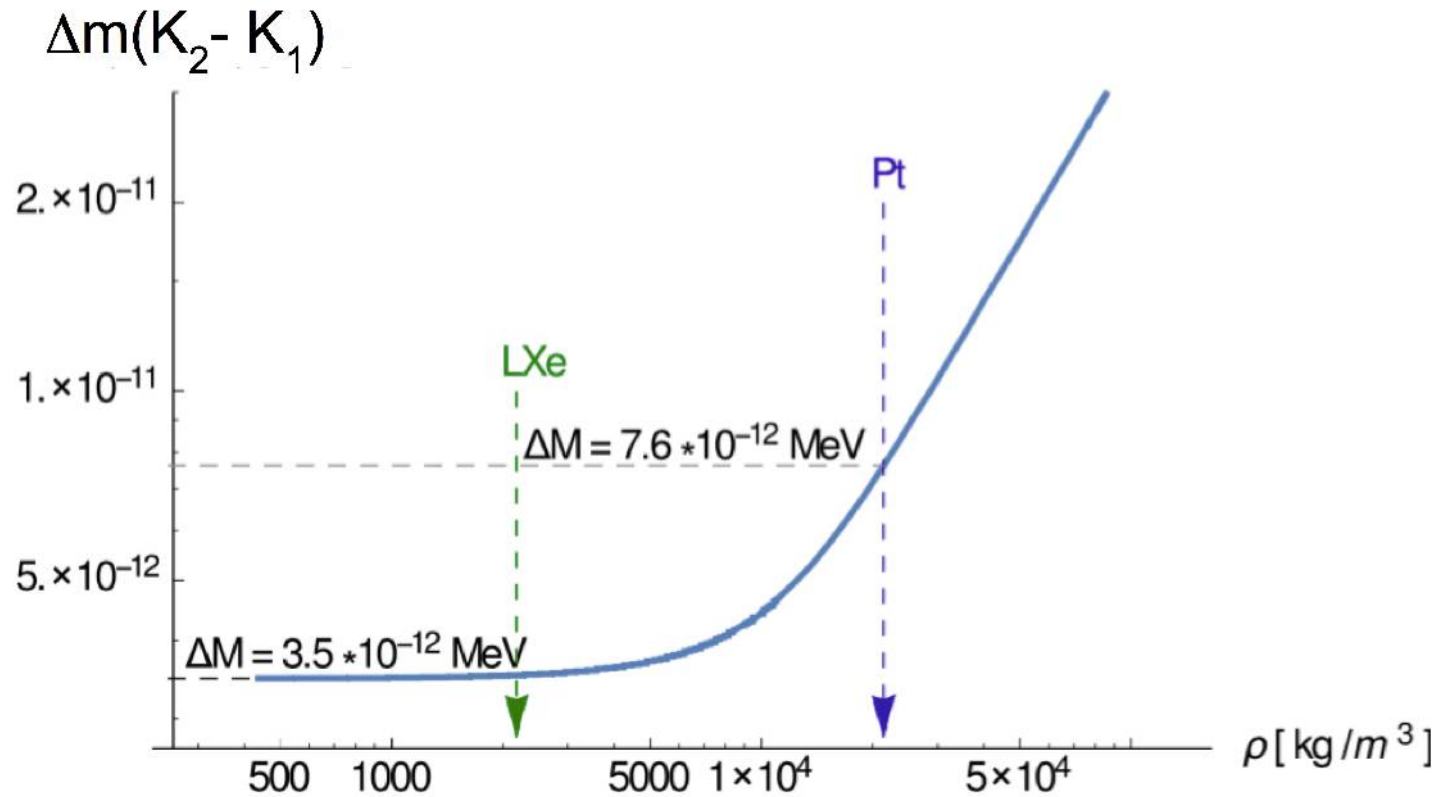
- And: oscillation length becomes shorter

$\tau / \tau_{K^0s}$

- is weakly affected in Liquid detector media (compared to Vacuum)
- Relativistic  $\gamma$  factor neglected here (increases effective medium density)

(absorption neglected)

# Mass difference $\Delta m(K_2 - K_1)$ in medium:



Absorption of kaons in medium not taken into account here

- Eigenvalues:  $\Delta\mu = \underline{M_H - M_L} - \frac{i}{2}(\Gamma_H - \Gamma_L) = \sqrt{4H_{12}H_{21} + (H_{22} - H_{11})^2}$

# $K^0 \rightarrow \bar{K}^0$ conversion in Nuclear Medium

$$[K^0 \rightsquigarrow \bar{K}^0]_{(\tau)} = \left| \frac{q_H}{p_H} \right|^2 |g_-(\tau)|^2 |1 - \theta|^2$$

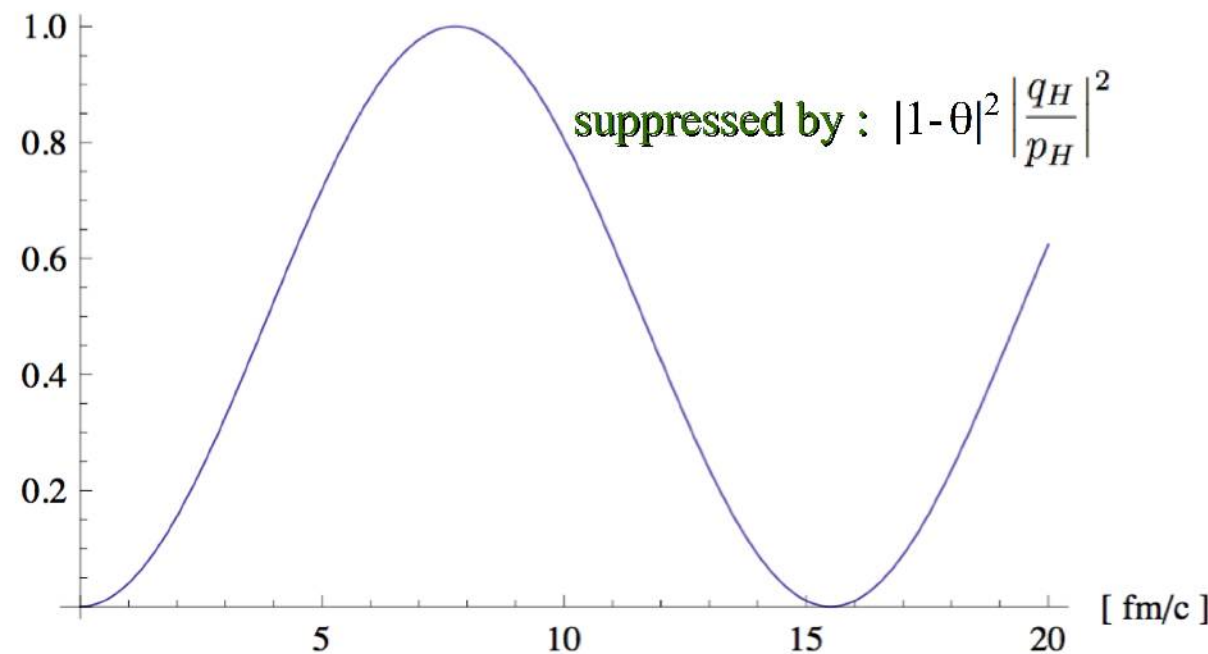
if CP symmetry holds

$$\left| \frac{p_L}{q_L} \right| = \left| \frac{q_H}{p_H} \right|$$

$$[\bar{K}^0 \rightsquigarrow K^0]_{(\tau)} = \left| \frac{p_L}{q_L} \right|^2 |g_-(\tau)|^2 |1 - \theta|^2$$

oscillation

$$|g_-(\tau)|^2 = \frac{1}{4} \left[ e^{-\tau\Gamma_H} + e^{-\tau\Gamma_L} - 2 \cos(\Delta\tilde{m}\tau) e^{-\tau(\Gamma_H+\Gamma_L)/2} \right]$$



$K^0 \rightarrow \bar{K}^0$  the same as  $\bar{K}^0 \rightarrow K^0$   
if  
CP violation is neglected

it would modify  $dN(\bar{K}^0)/dy$   
only if  
 $N(K^0) \gg N(\bar{K}^0)$   
anyway would't be visible  
in  $K^0_S$  spectra

for dense Baryonic medium (e.g. Niobium nucleus)  
Assuming potential difference  $dV(K-\bar{K}) = 80 \text{ MeV}$

# SUPPRESSION FACTOR ESTIMATE

$$P(K^0 \rightarrow \bar{K}^0) = \left| \frac{q_H}{p_H} \right|^2 |1 - \theta|^2 |g_-(\tau)|^2$$

see G.C. Branco et al.  
in book: "CP Violation"  
Eq.(9.8) Eq.(6.29-32)

$$\left| \frac{q_H}{p_H} \right|^2 = \frac{4|H_{21}|^2}{|\Delta\mu|^2} \frac{1}{|1 - \theta|^2}$$

$$P(K^0 \rightarrow \bar{K}^0) = \frac{|2H_{21}|^2}{|4H_{12}H_{21} + (H_{22} - H_{11})^2|} |g_-(\tau)|^2$$

$$\approx \frac{|2H_{21}|^2}{|H_{22} - H_{11}|^2} |g_-(\tau)|^2 = \frac{4|M_{21} - i\Gamma_{21}/2|^2}{\Delta V^2} |g_-(\tau)|^2$$

for  $|H_{12}H_{21}| \ll |H_{22} - H_{11}|^2 \approx \Delta V^2$

$\rightarrow 10^{-12}$   
 $(80 \text{ MeV})^2$   
 $\rho = \rho_N$



# $K^0 \rightarrow \bar{K}^0$ conversion in Nuclear Medium

$$[K^0 \rightsquigarrow \bar{K}^0]_{(\tau)} = \left| \frac{q_H}{p_H} \right|^2 |g_-(\tau)|^2 |1 - \theta|^2$$

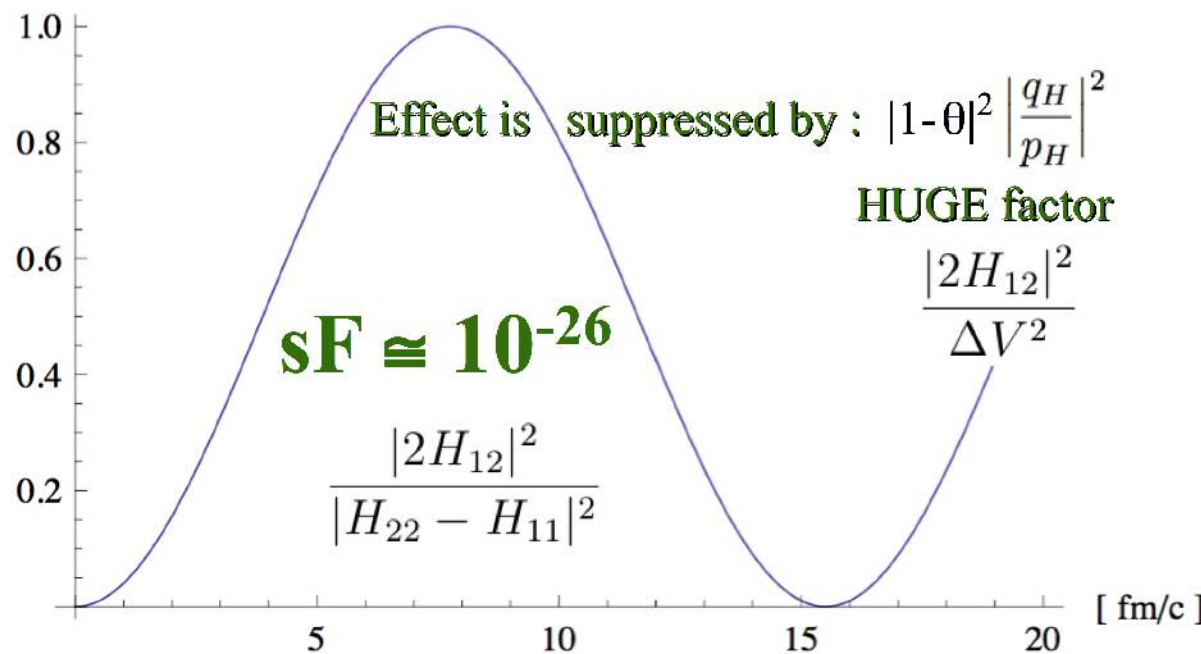
if CP symmetry holds

$$\left| \frac{p_L}{q_L} \right| = \left| \frac{q_H}{p_H} \right|$$

$$[\bar{K}^0 \rightsquigarrow K^0]_{(\tau)} = \left| \frac{p_L}{q_L} \right|^2 |g_-(\tau)|^2 |1 - \theta|^2$$

oscillation

$$|g_-(\tau)|^2 = \frac{1}{4} \left[ e^{-\tau\Gamma_H} + e^{-\tau\Gamma_L} - 2 \cos(\Delta\tilde{m}\tau) e^{-\tau(\Gamma_H+\Gamma_L)/2} \right]$$



$K^0 \rightarrow \bar{K}^0$  the same as  $\bar{K}^0 \rightarrow K^0$   
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anyway would't be visible  
in  $K^0_s$  spectra

for dense Baryonic medium (e.g. Niobium nucleus)  
Assuming potential difference  $dV(K-\bar{K}) = 80$  MeV

# Realistic Observation:

- 1)  $K^0 \rightarrow \bar{K}^0$  oscillation is potentially fast enough in ( $\rho = \rho_N$ ) dense baryonic medium:  $\tau_o \sim 10 \text{ fm}/c$
- 2) Subthreshold production needed:  $N(\bar{K}) \ll N(K)$  to violate strangeness conservation (if  $\delta_{CP} = 0$ )

$\Rightarrow$  **Suppression factor at  $\rho \cong \rho_N$ :  $sF \sim 10^{-26}$**

makes  $K^0(d\bar{s}) \rightarrow \bar{K}^0(\bar{d}s)$  process negligible

**Don't Give UP for free!**

# Think about $K^{0*}(896)$ oscillations !

$J=1$

$$(d\bar{s}) \leftrightarrow (\bar{d}s)$$

## $K_S^{0*}$ and its uses

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(Received 27 November 1979)

We point out that Primakoff conversion of  $K_L^0$ 's produces  $K_S^{0*}$ 's.

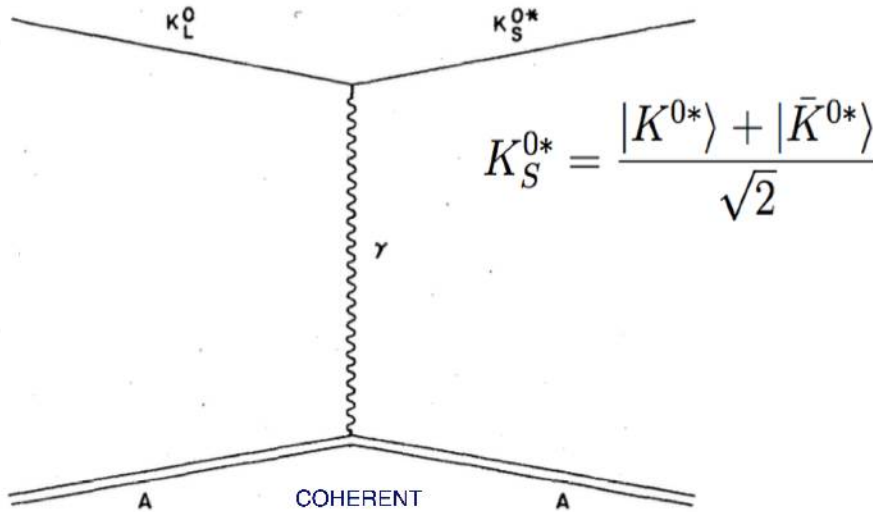
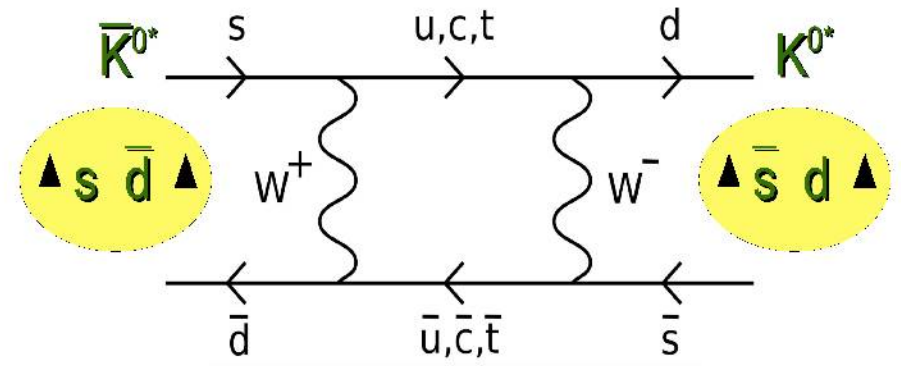


FIG. 1. Primakoff excitation of  $K^*$ .

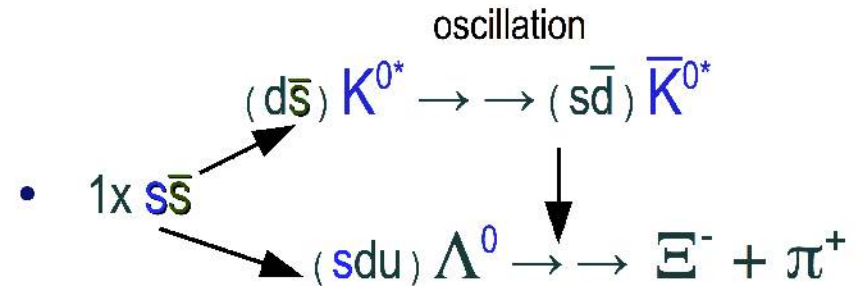
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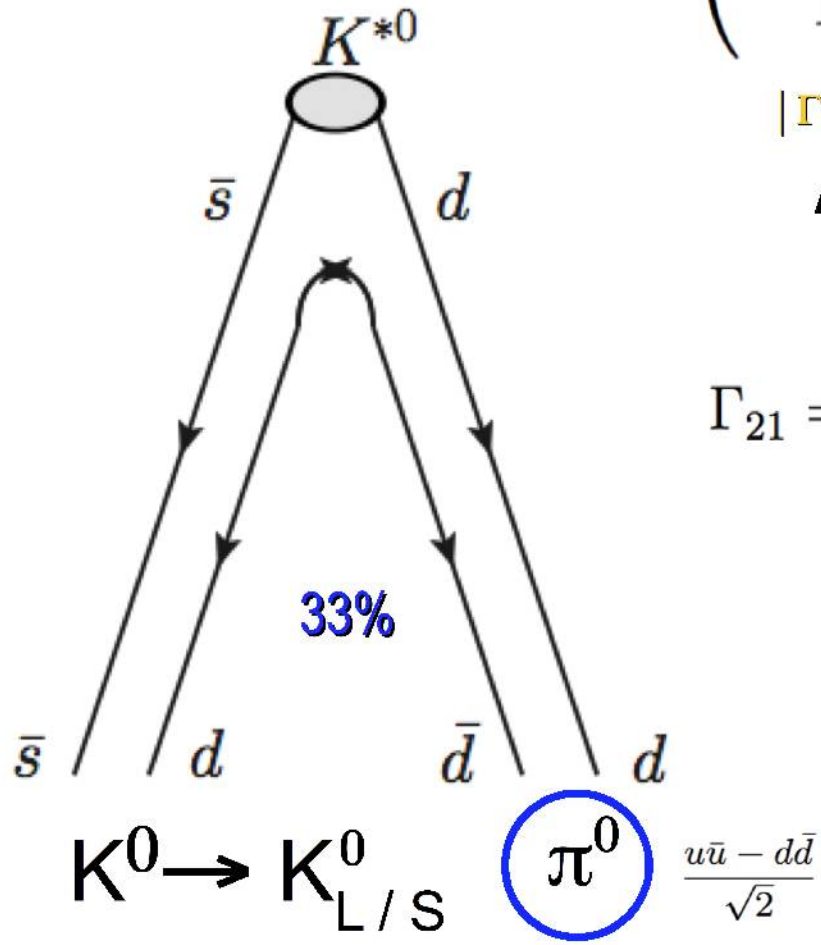
$$M_{21} = M_{21}^* = \langle \bar{K}^{0*} | H_{wk} | K^{0*} \rangle$$

assume  $M_{12}$  the same as for  $K^0(497)$



- $K_S^{0*}$  quantum state exists and it can be produced.

# $K^{0*}(896)$ decay matrix (Hamiltonian)



$$\Gamma_{11} = 48 \text{ MeV} \quad |\Gamma_{12}| = 16 \text{ MeV}$$

$$\Gamma_{K^{0*}} = \begin{pmatrix} 48 + \overset{\text{absorption}}{\gamma_{K^{0*}}(\rho_B)} & 16 e^{i\xi_{G^*}} \\ 16 e^{-i\xi_{G^*}} & 48 + \underset{\text{Absorption}}{\bar{\gamma}_{\bar{K}^{0*}}(\rho_B)} \end{pmatrix}$$

$|\Gamma_{21}| = 16 \text{ MeV}$

$\Gamma_{22} = \text{strong decay width} = 48 \text{ MeV}$

$$\Gamma_{21} = \Gamma_{21}^* = \pi \sum_F \rho_f \langle \bar{K}^{0*} | H_{wk} | F \rangle \langle F | H_{wk} | K^{0*} \rangle$$

$\pi^0 K_{L,S}^0$

$K^{*0} \Rightarrow K_L^0 \pi^0$  or  $K_S^0 \pi^0$   $8 \text{ MeV}$   $0.33 \times 48 = 16 \text{ MeV}$

$\bar{K}^{*0} \Rightarrow K_L^0 \pi^0$  or  $K_S^0 \pi^0$   $8 \text{ MeV}$   $0.33 \times 48 = 16 \text{ MeV}$

the same final states

# Hamiltonian for $K^{0*}(896)$

$$\mathbb{G}_{K^{0*}} = \begin{pmatrix} 48 + \gamma_{K^{0*}}(\rho_B) & \underline{16 e^{i\xi_{G^*}}} \\ \underline{16 e^{-i\xi_{G^*}}} & 48 + \bar{\gamma}_{\bar{K}^{0*}}(\rho_B) \end{pmatrix}$$

$$\mathbb{G}_{K^0} = \begin{pmatrix} 3.7 \cdot 10^{-12} + \gamma_{K^0}(\rho_B) & e^{i\xi_G} 3.48 \cdot 10^{-12} \\ e^{-i\xi_G} 3.48 \cdot 10^{-12} & 3.7 \cdot 10^{-12} + \bar{\gamma}_{\bar{K}^0}(\rho_B) \end{pmatrix}$$

**SUBSTANTIAL**

**decay width**

$K^{0*}$  **differences**  $K^0$

observe:  $\mathbf{\Gamma}_{12}$  of  $K^{0*}$

comparable to  $\Delta V_{K^*}$

$$\mathbb{M}_{K^{0*}} = \begin{bmatrix} \underline{896} + \overset{+ 20 \text{ MeV}}{V_{K^{0*}}(\rho_B)} & e^{i\xi_{M^*}} 1.7 \cdot 10^{-12} \\ e^{-i\xi_{M^*}} 1.7 \cdot 10^{-12} & \underline{896} - \underline{\bar{V}_{\bar{K}^{0*}}(\rho_B)} \end{bmatrix}$$

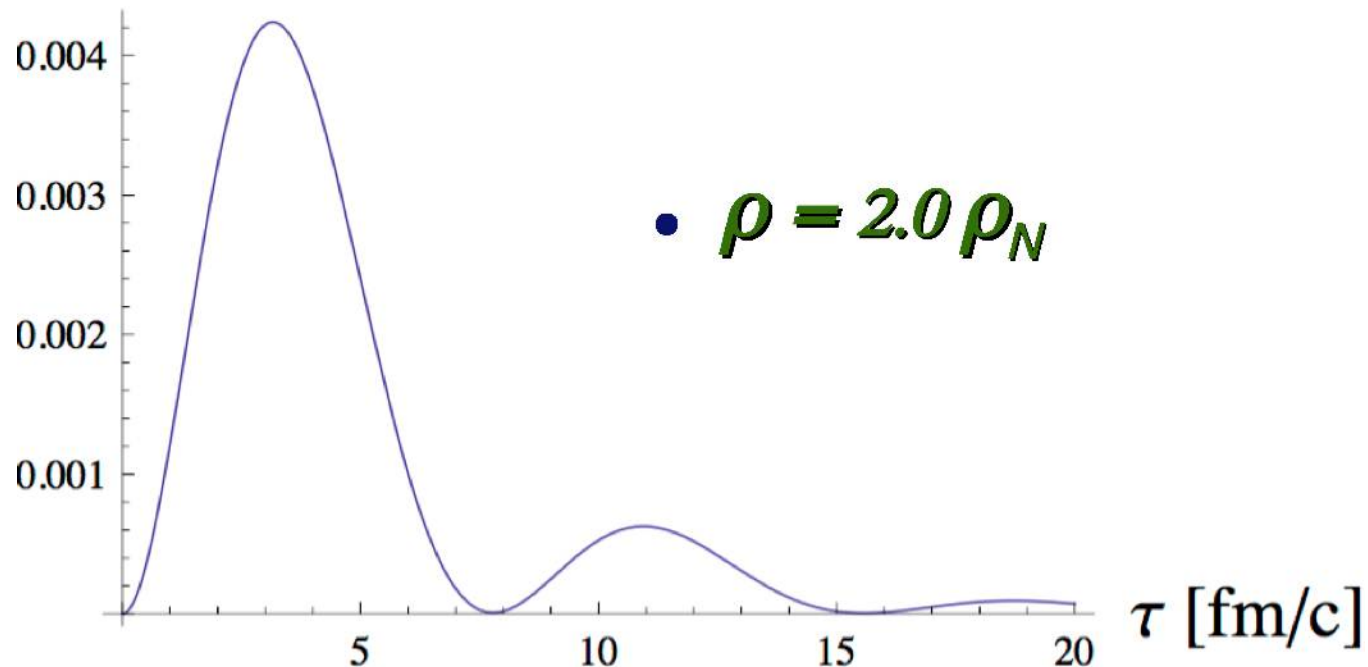
- 60 MeV

**Assuming  
the same  $K$   
in-medium  
potentials.**

# Results for $K^{0*}$ oscillations

Probability of  $K^{0*} \Rightarrow \bar{K}^{0*}$  process:

$$|q_H/p_H|^2 |1-\theta|^2 |g_-(\tau)|^2 \quad K^0 \rightarrow \bar{K}^0$$

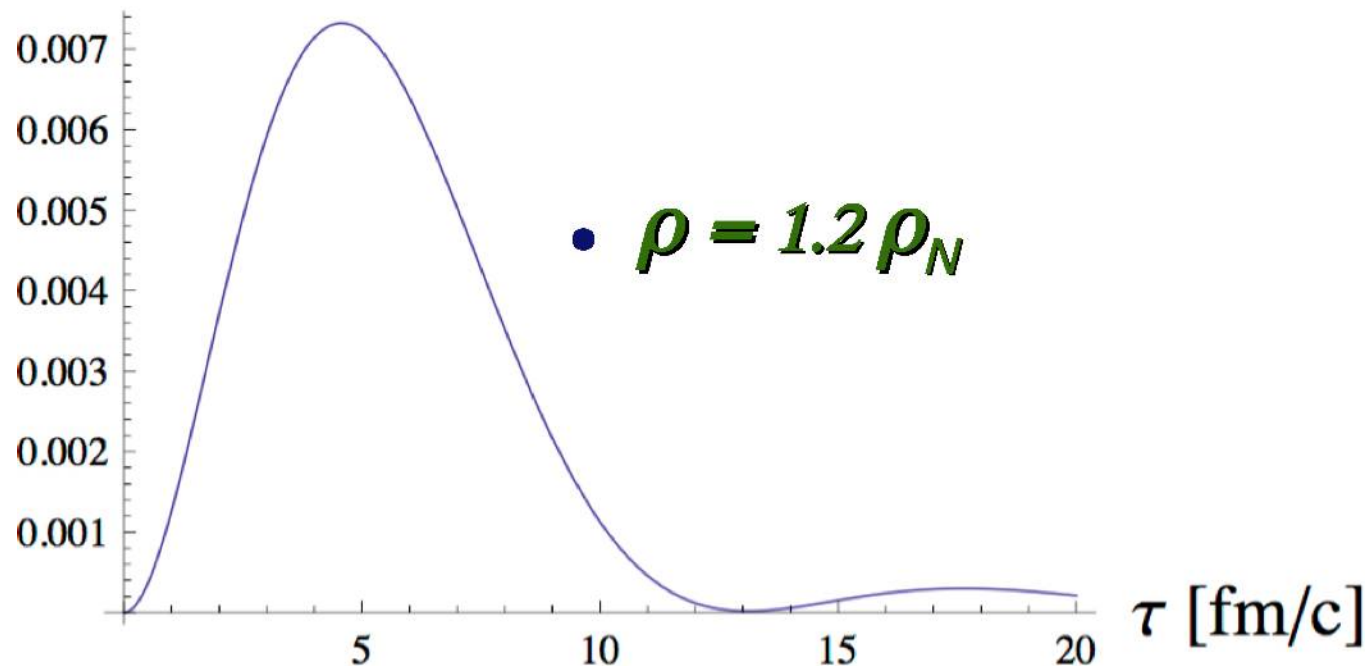


- With absorption:  $\Gamma_{22} = 48+12$  MeV,  $\Gamma_{11} = 48+5$  MeV

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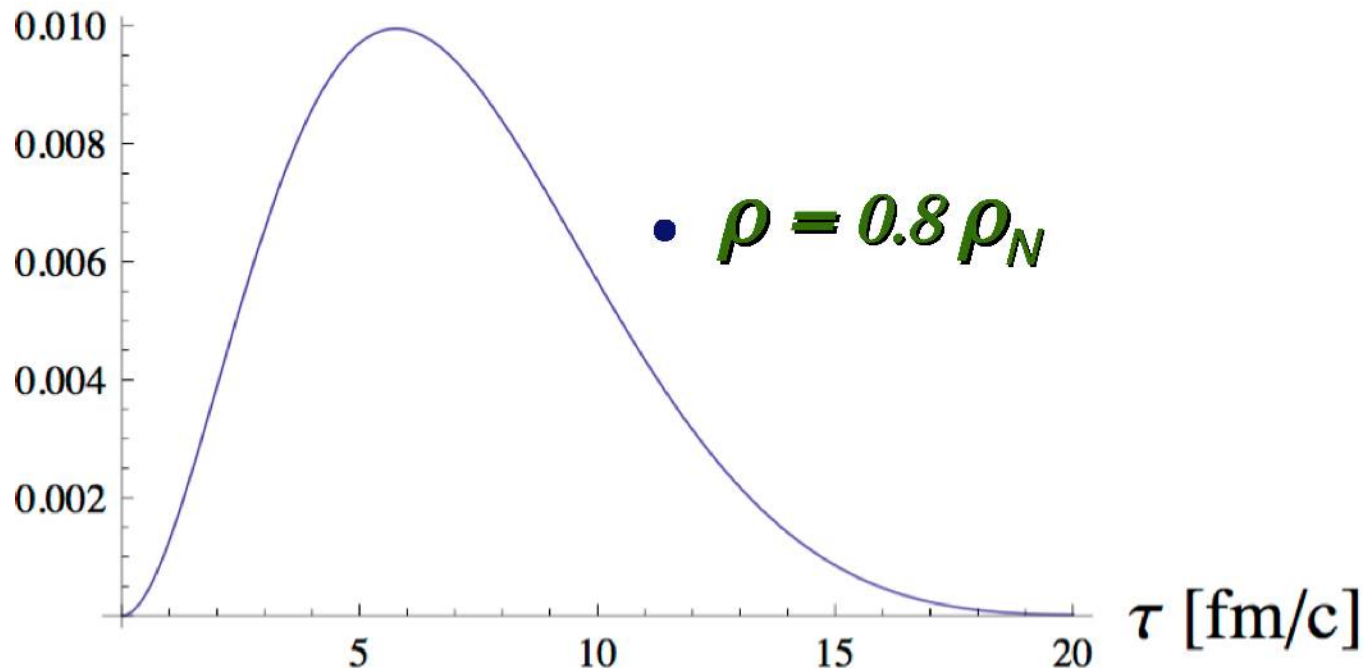


- With absorption:  $\Gamma_{22} = 48+12$  MeV,  $\Gamma_{11} = 48+5$  MeV

# Results for $K^{0*}$ oscillations

Probability of  $K^{0*} \Rightarrow \bar{K}^{0*}$  process:

$$|q_H/p_H|^2 |1-\theta|^2 |g_-(\tau)|^2 \quad K^0 \rightarrow \bar{K}^0$$



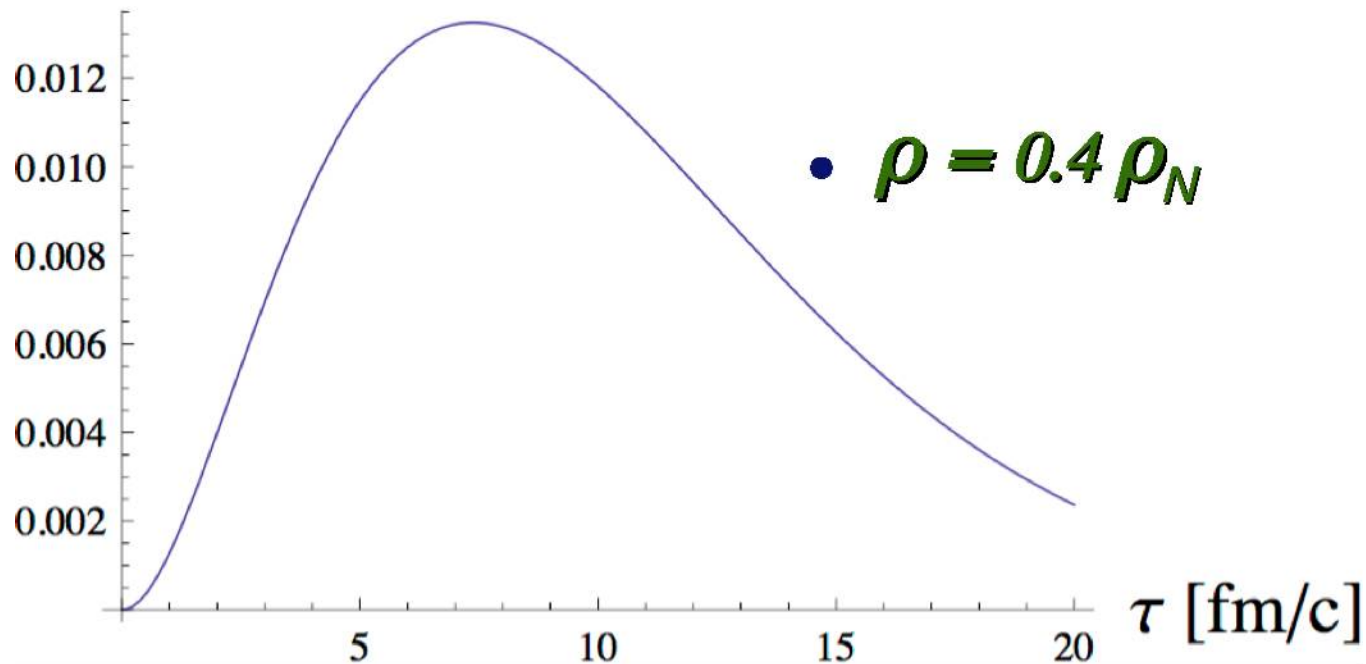
- With absorption:  $\Gamma_{22} = 48+12$  MeV,  $\Gamma_{11} = 48+5$  MeV



# Results for $K^{0*}$ oscillations

Probability of  $K^{0*} \Rightarrow \bar{K}^{0*}$  process:

$$|q_H/p_H|^2 |1-\theta|^2 |g_-(\tau)|^2 \quad K^0 \rightarrow \bar{K}^0$$

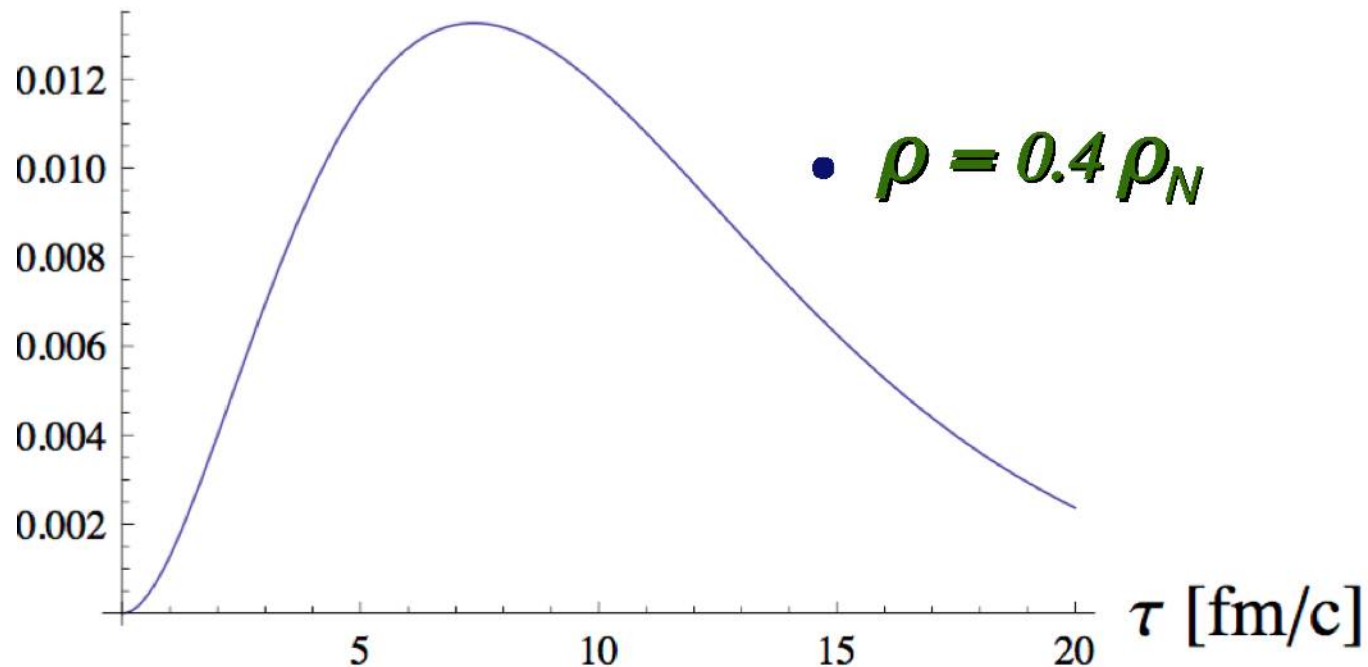


- With absorption:  $\Gamma_{22} = 48+12$  MeV,  $\Gamma_{11} = 48+5$  MeV

# Results for $\bar{K}^{0*}$ oscillations

## Probability of $\bar{K}^{0*} \Rightarrow K^{0*}$ reverse process

$$|p_L/q_L|^2 |1-\theta|^2 |g_-(\tau)|^2 \quad aK^0 \rightarrow K^0$$

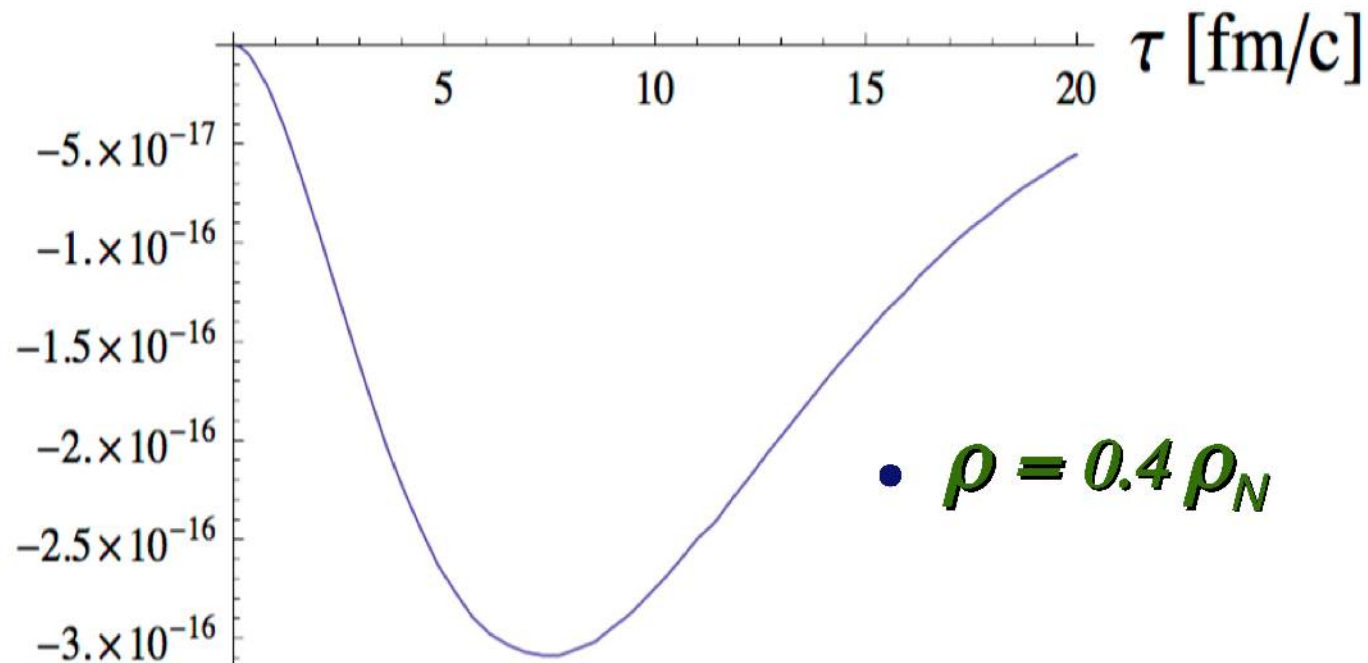


- With absorption:  $\Gamma_{22} = 48+12$  MeV,  $\Gamma_{11} = 48+5$  MeV

# Results for $K^{0*}$ oscillations

Difference between  $\bar{K}^{0*} \Rightarrow K^{0*}$  and  $K^{0*} \Rightarrow \bar{K}^{0*}$

$$(|p_L/q_L|^2 - |q_H/p_H|^2) |1 - \theta|^2 |g_-(\tau)|^2$$



- With absorption:  $\Gamma_{22} = 48+12$  MeV,  $\Gamma_{11} = 48+5$  MeV

# Observed Features:

1) Probability of  $K^{0*} \Rightarrow \bar{K}^{0*}$  is 0.5% - 1.5%

2) Process ( $\bar{s} \rightarrow s$ ) occurs within  $\tau = 4 - 10$  fm/c

if net baryon density  $\rho_B = [0.1 - 2.0] \rho_N$  [0.16 fm<sup>-3</sup>]

3) CP violation is not important = not needed

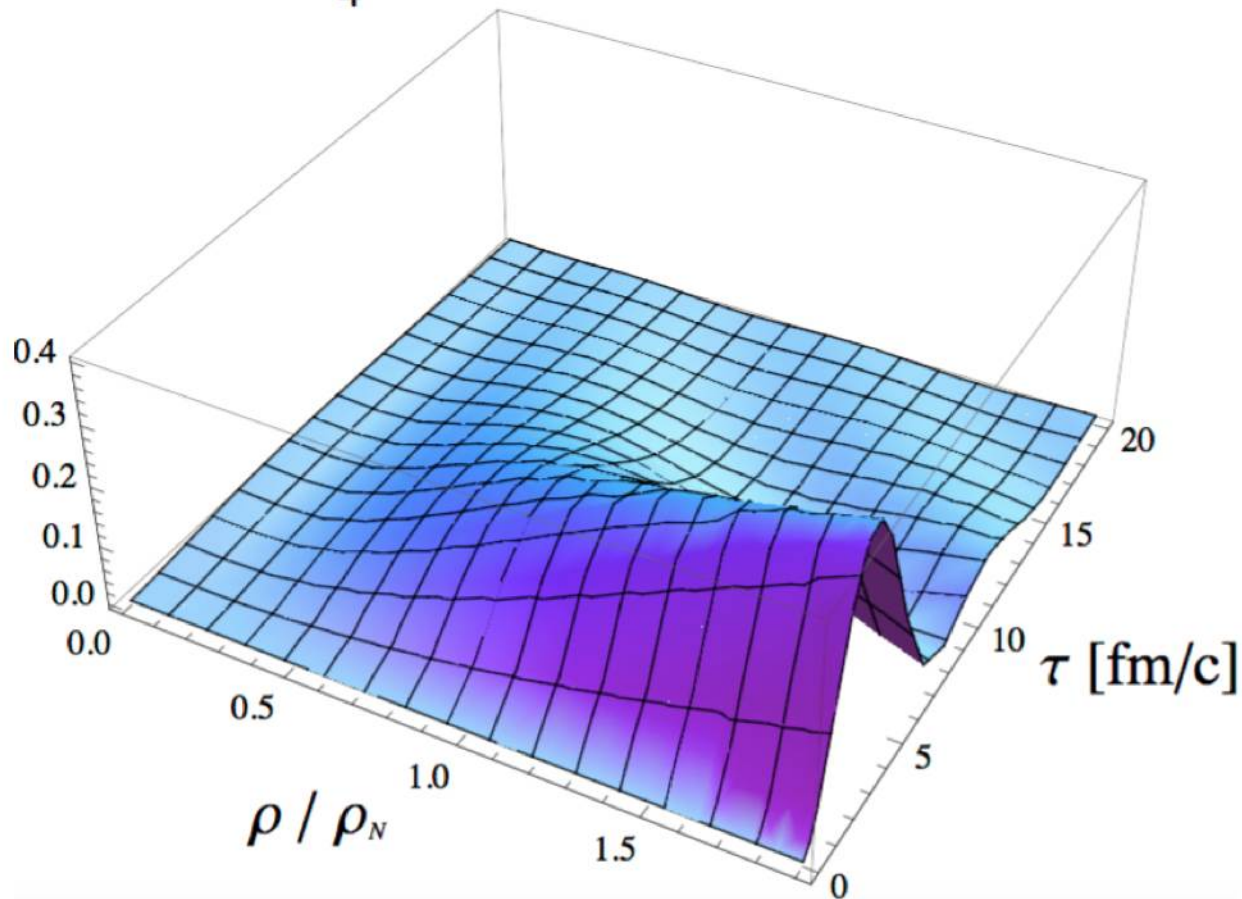
(opposite process  $\bar{K}^{0*} \Rightarrow K^{0*}$  has the same probability)

process ( $\bar{s} \rightarrow s$ ) becomes relevant = IF primordial  $N(K^{0*}) \gg N(\bar{K}^{0*})$

# More results for $K^{0*}$ oscillations

Oscillation term for  $K^{0*} \Rightarrow \bar{K}^{0*}$  process:

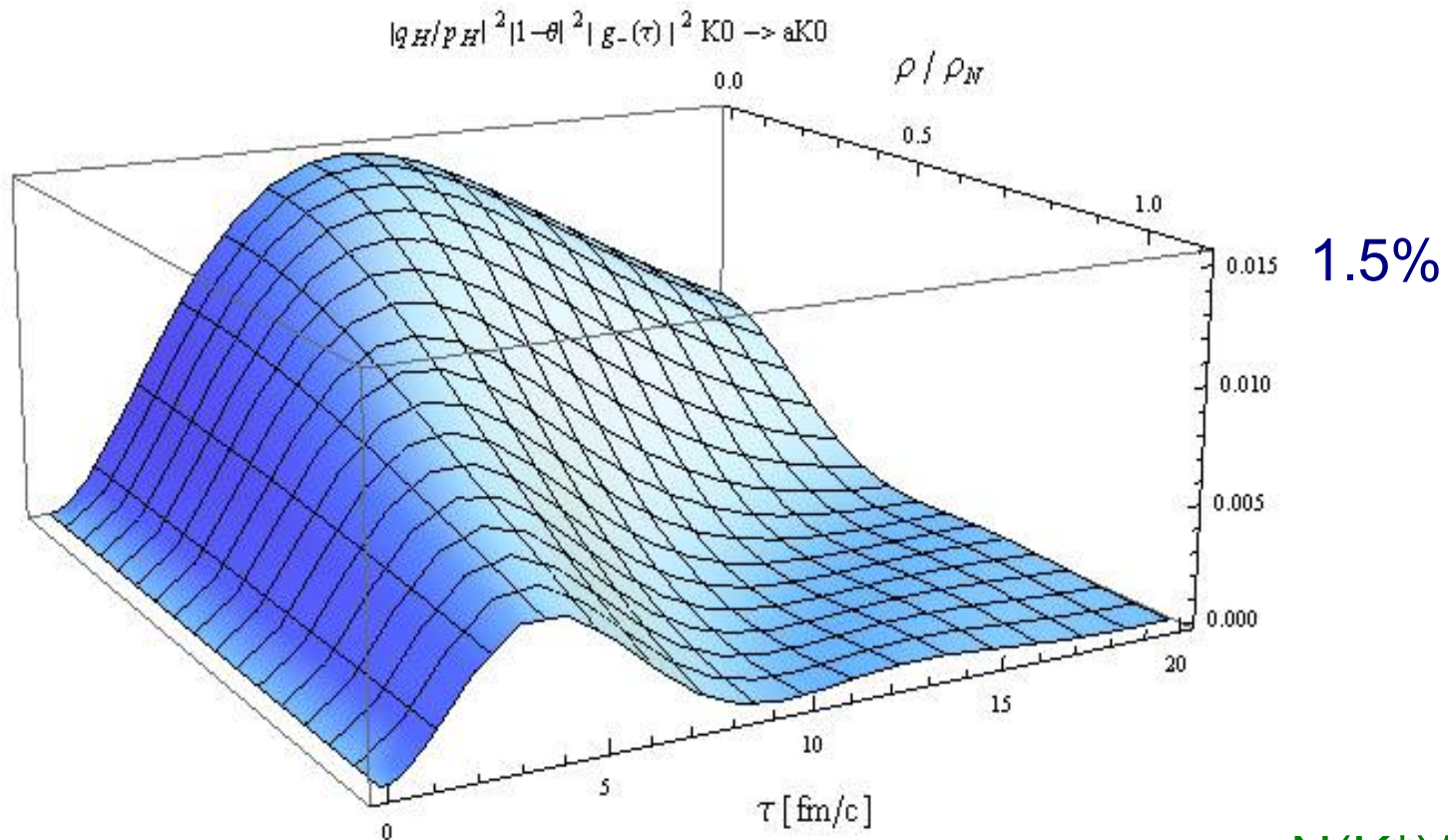
$$|g_-(\tau)|^2 = \frac{1}{4} [e^{-\tau\Gamma_1} + e^{-\tau\Gamma_2} - 2\text{Cos}[\Delta M^* \tau] e^{-\tau(\Gamma_1 + \Gamma_2)/2}]$$



Suppression factor not shown.

# More results for $K^{0*}$ oscillations

Transition probability  $K^{0*} \Rightarrow \bar{K}^{0*}$ :

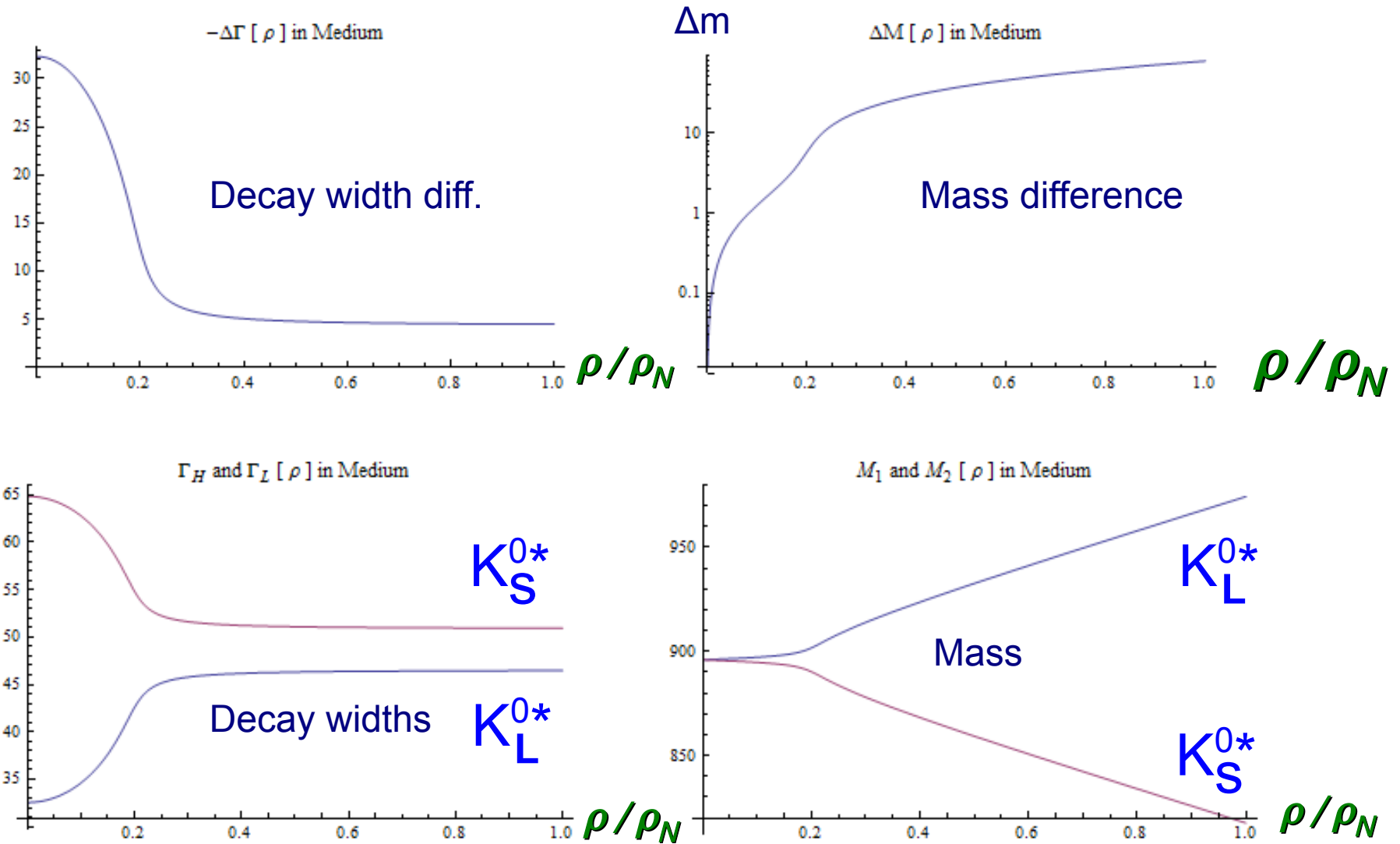


However:  $N(K^*)/N(\bar{K}^*)$   
is smaller.

If suppression factor is included, at small  $\rho_B$  we have larger Probability.

# More results for $K^{0*}$ , $\bar{K}^{0*}$ in medium

## Decay widths and Masses of eigenstates $K_L^{0*}$ , $K_S^{0*}$

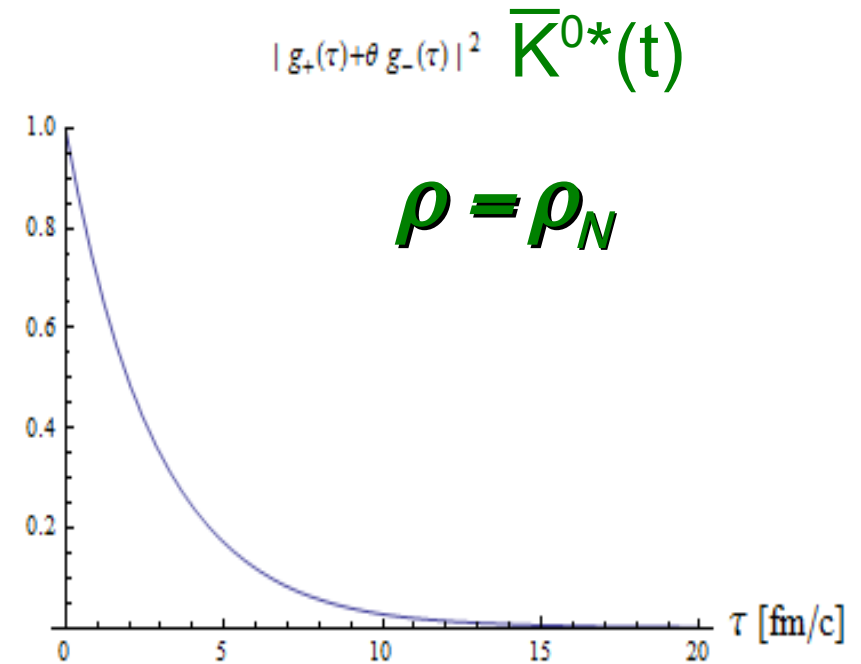
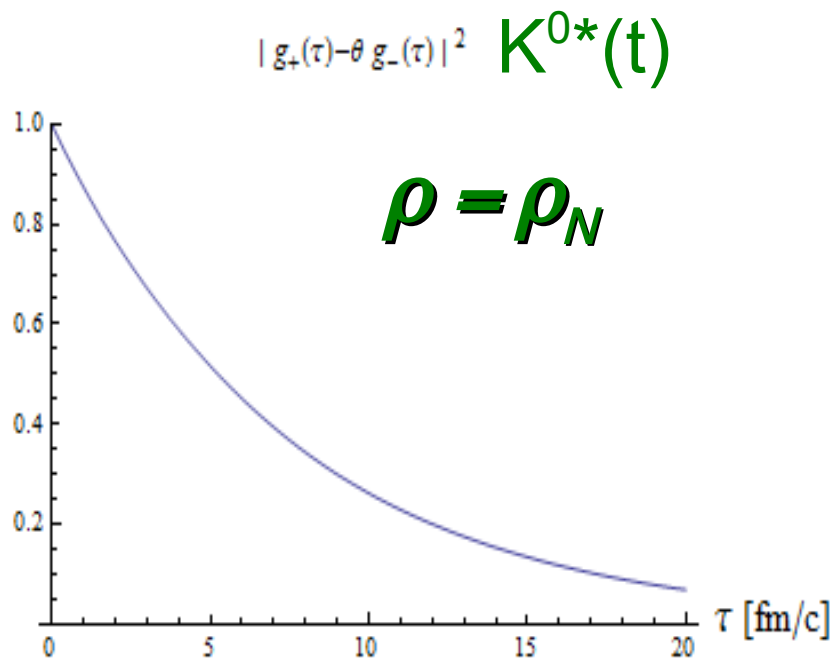


$\Gamma_{22} = 49 + 7.4$  MeV,  $\Gamma_{11} = 49 + 3$  MeV,  $\Delta V = 80$  MeV at  $\rho_N$

Survival  $K^{0*} \Rightarrow K^{0*}$  and  $\bar{K}^{0*} \Rightarrow \bar{K}^{0*}$  probability:

$$[P^0(t) \rightarrow P^0]_{(\tau)} = |\langle P^0 | P^0(\tau) \rangle|^2 = |g_+(\tau) - \theta g_-(\tau)|^2$$

$$[\bar{P}^0(t) \rightarrow \bar{P}^0]_{(\tau)} = |\langle \bar{P}^0 | \bar{P}^0(\tau) \rangle|^2 = |g_+(\tau) + \theta g_-(\tau)|^2$$



Substantially different absorption cross sections assumed here.

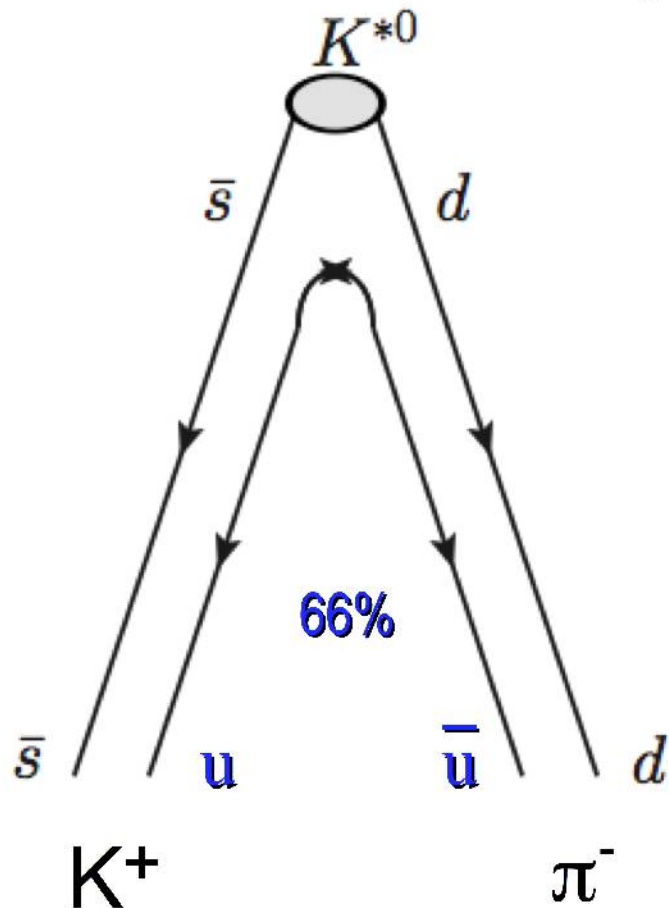
$$\Gamma_{11} = 48+30 \text{ MeV}, \quad \Gamma_{22} = 48+74 \text{ MeV} \quad \text{at } \rho = \rho_N$$



# $K^{0*} \rightarrow \bar{K}^{0*}$ oscillation: CONSEQUENCE 1.

For a sub-threshold  $\bar{K}^{0*}$  production:  $100 * N(\bar{K}^{0*}) < N(K^{0*})$

→ more  $\bar{K}^{0*}$  observed than expected:



$\bar{K}^{0*} \rightarrow K^- \pi^+$  channel

$K^{0*} \rightarrow K^+ \pi^-$  channel

Can be distinguished

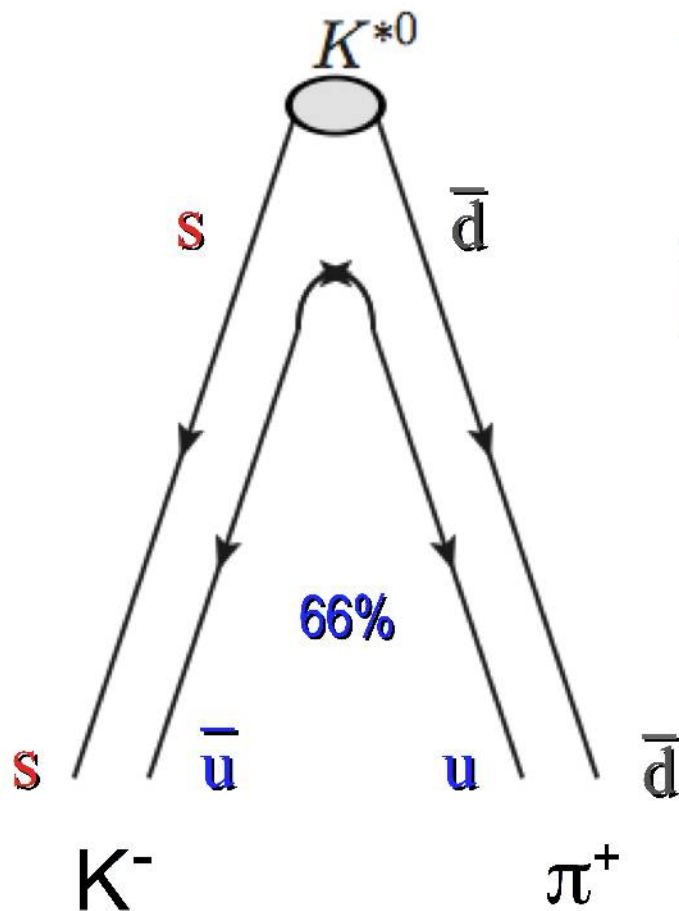
Note: no AGS data were published on  $K^{0*} / \bar{K}^{0*}$

# $K^{0*} \rightarrow \bar{K}^{0*}$ oscillation: CONSEQUENCE II

Assume sub-threshold  $\bar{K}^*$  production:  $N(\bar{K}^*) \ll N(K^*)$

$\rightarrow$  more  $\bar{K}^{0*}$  than expected

$\bar{K}^{0*} \rightarrow K^- \pi^+$  gives excessive  $K^-$



$K^-/K^+$  or  $K^-/\pi$  anomaly  
may appear in exp. Data.

# SUMMARY Ia

1)  $K^0 \rightarrow \bar{K}^0$  in A+A , p+A collisions is negligible

suppression factor  $\leq 10^{-26}$

2)  $K^{0*} \rightarrow \bar{K}^{0*}$  oscillation can be significant + fast enough  
→ it may affect  $\bar{K}$  yields and ratios

(just in case of sub-threshold anti- $K^*$  production)

3) Production of (2ss) hyperons may thus be enhanced  
via secondary strangeness-exchange reactions.



# $D^0 - \bar{D}^0$ oscillation in Vacuum

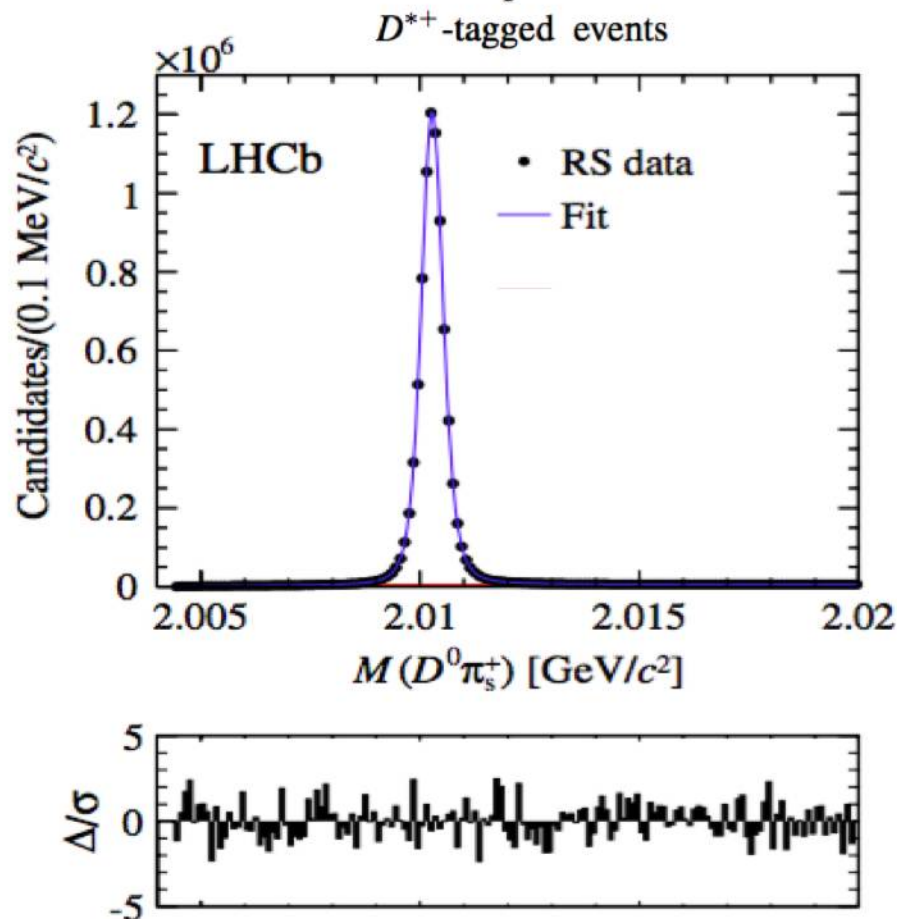
PHYSICAL REVIEW LETTERS



## Observation of $D^0 - \bar{D}^0$ Oscillations

(LHCb Collaboration)

(Received 6 November 2012; published 5 March 2013)



$$c\tau_{osc} = 2\pi\hbar c/\Delta m$$

$D^0, \bar{D}^0$  decay too fast, for typical oscillation pattern in vacuum to be clearly visible. Instead, LHCb measures rising Ratio of “WS/RS” decays.

probability corresponding to 9.1 standard deviations

PRL 110, 101802 (2013)

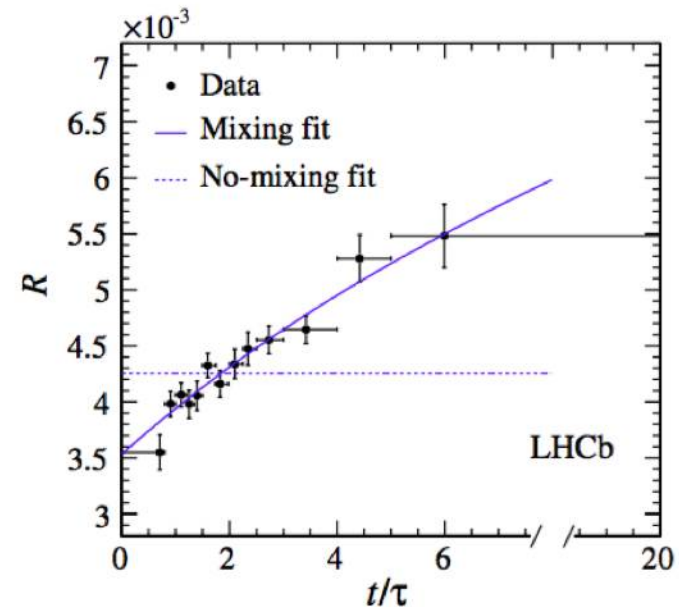


FIG. 2 (color online). Decay-time evolution of the ratio,  $R$ , of WS  $D^0 \rightarrow K^+ \pi^-$  to RS  $D^0 \rightarrow K^- \pi^+$  yields (points) with the projection of the mixing allowed (solid line) and no-mixing

# $D^{0*}$ (2007) and $D^0$ behavior in Medium

Table 1: Oscillation parameters of neutral  $K^0$ ,  $D^0$ ,  $B^0$ , and  $B_s^0$  mesons in vacuum.

	$K^0$	$D^0$	$B^0$	$B_s^0$
$\Delta m$ [MeV]	$3.5 \times 10^{-12}$	$\approx 6.3 \times 10^{-12}$	$3.3 \times 10^{-10}$	$11.7 \times 10^{-9}$
$\Delta m$ [ $\frac{10^{10} \hbar}{s}$ ]	$0.529 \pm 0.001$	$0.95 \pm 0.44$	$51.0 \pm 0.3$	$1776 \pm 2$
$\tau_0$ [ $10^{-12}$ s]	89.5*	0.401	1.52	1.51
$\tau_{osc}$ [ $10^{-12}$ s]	1187	$\approx 660$	12.3	0.35
$\tau_{osc}/\tau_0$	13.1*	$\approx 1650$	8.2	0.23
$c \cdot \tau_0$	2.7* cm	0.123 mm	0.45 mm	0.45 mm
$c \cdot \tau_{osc}$	35 cm	$\approx 20$ cm	3.7 mm	0.11 mm

$D^0$ ,  $\bar{D}^0$  decays too fast, for typical oscillation pattern in vacuum to be clearly visible. Eigenstate  $D_1^0$  or  $D_2^0$  exists virtually, but it has no time to be formed.

$$c\tau_{osc} = \frac{2\pi \hbar c}{\Delta m} = 30 \text{ fm} \quad \left. \vphantom{\frac{2\pi \hbar c}{\Delta m}} \right\} \text{ in Nuclei}$$

$\underbrace{2\pi \hbar c}_{197 \text{ MeVfm}} \quad \underbrace{\Delta m}_{40 \text{ MeV}}$

optical potential difference  $\bar{D}^0 - D^0$

# Oscillation of $D^0(1865)$ in Medium

$$M_{D^0} = \begin{bmatrix} 1865 + \underline{V_{D^0}(\rho_B)} & e^{i\xi_M} 3.1 \cdot 10^{-12} \\ e^{-i\xi_M} 3.1 \cdot 10^{-12} & 1865 - \underline{\bar{V}_{\bar{D}^0}(\rho_B)} \end{bmatrix}$$

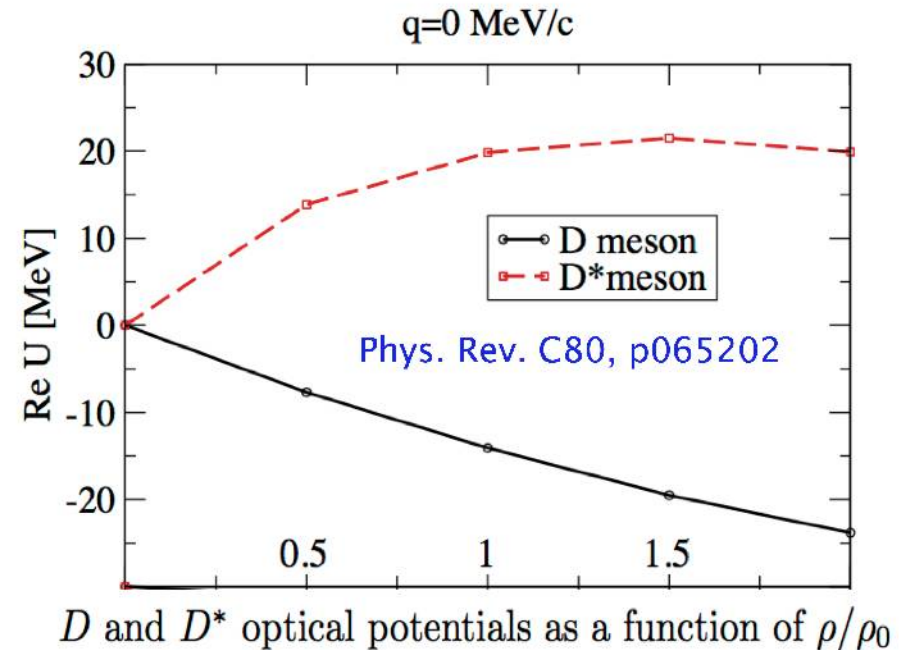
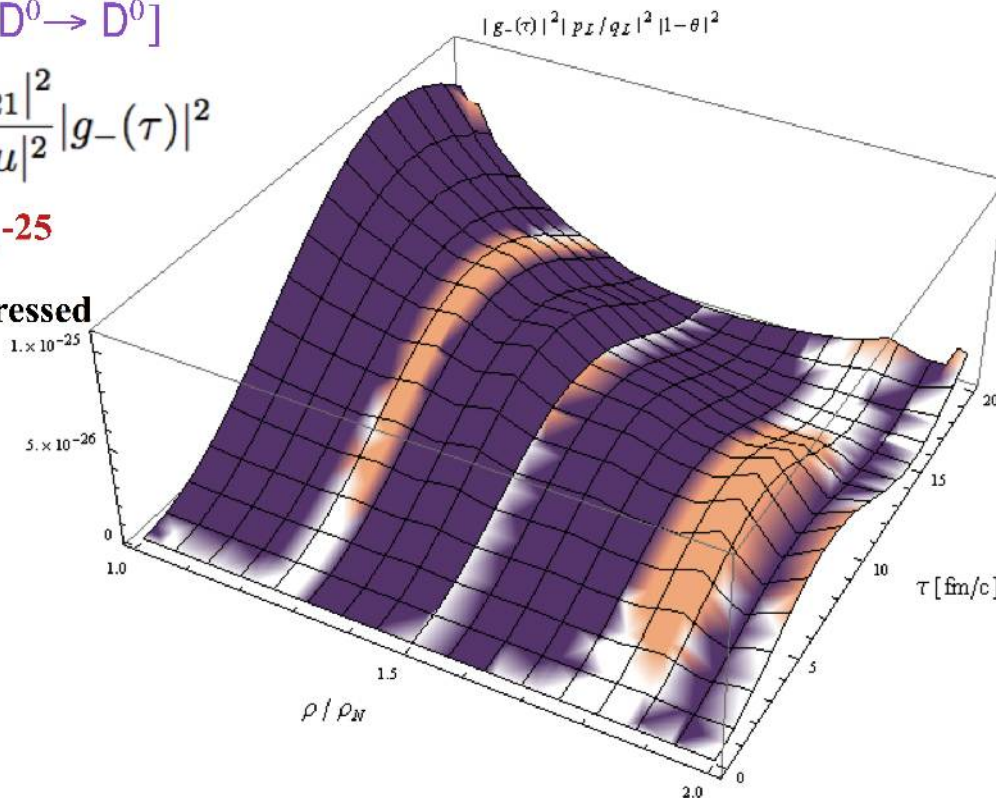
assuming  $M_{12}$  and  $\Gamma_{12}$  are not changed in hadronic medium

$$\mathbb{G}_{D^0} = \begin{pmatrix} \underline{1.58 \cdot 10^{-9}} + \gamma_{D^0}(\rho_B) & e^{i\xi_G} 1.04 \cdot 10^{-11} \\ e^{-i\xi_G} 1.04 \cdot 10^{-11} & \underline{1.58 \cdot 10^{-9}} + \bar{\gamma}_{\bar{D}^0}(\rho_B) \end{pmatrix}$$

**SMALL**  
decay constants  
compared to  $\Delta V$

$$\Delta V [\rho = \rho_N] \cong 40 \text{ MeV}$$

$P[D^0 \rightarrow \bar{D}^0]$   
 $4 \frac{|H_{21}|^2}{|\Delta\mu|^2} |g_-(\tau)|^2$   
 $\times 10^{-25}$   
suppressed



# Oscillation of $D^{0*}$ (2007) in Medium

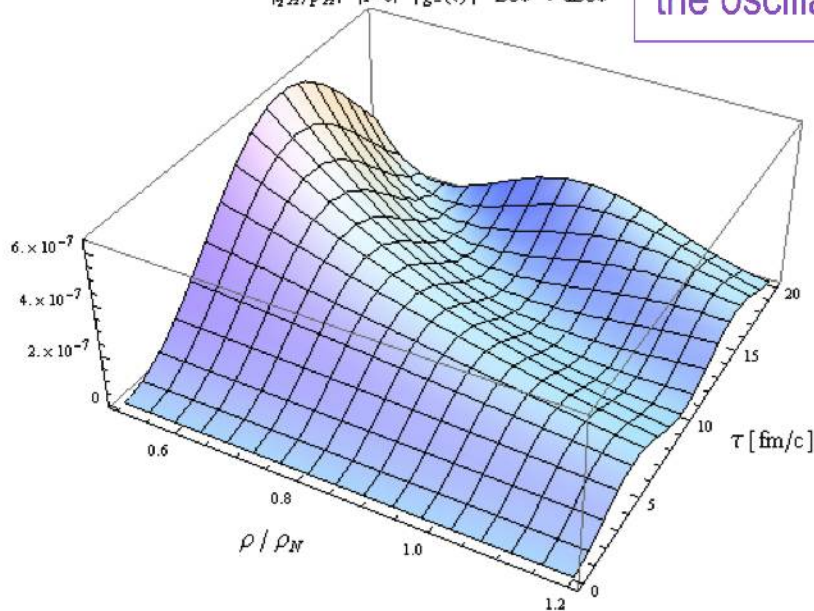
$$M_{D^{0*}} = \begin{bmatrix} 2007 + \underline{40 \text{ MeV}} & e^{i\xi_{M^*}} 3 \cdot 10^{-12} \\ e^{-i\xi_{M^*}} 3 \cdot 10^{-12} & 2007 - \underline{\bar{V}_{\bar{D}^{0*}}(\rho_B)} \end{bmatrix}$$

assuming  $M_{12}$  and  $\Gamma_{12}$  are not changed in hadronic medium

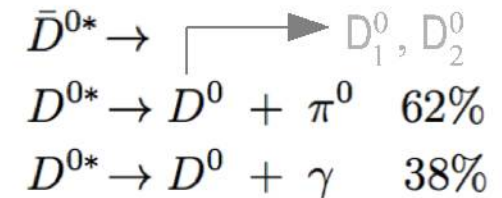
$$G_{D^{0*}} = \begin{pmatrix} \underline{0.04} + \gamma_{D^{0*}}(\rho_B) & \underline{0.04} e^{i\xi_{G^*}} \\ \underline{0.04} e^{-i\xi_{G^*}} & \underline{0.04} + \bar{\gamma}_{\bar{D}^{0*}}(\rho_B) \end{pmatrix}$$

$P[D^{0*} \rightarrow \bar{D}^{0*}]$

$|g_{\pi^+} / p_{\pi^+}|^2 |1 - \theta|^2 |g_{\pi^0}|^2 |D^{0*} \rightarrow \bar{D}^{0*}|^2$



maximal possible value:  
gives upper estimate for  
the oscillation probability



$\Gamma_{D^{*o}} \approx 40 \text{ keV}$  and hence

*Physics Letters B* 418 (1998) 383–388

$$\Gamma_{D^{*++}} \approx 3 \Gamma_{D^{*o}} \left| \frac{P_{\pi(D^{*++})}}{P_{\pi D_o^*}} \right|^3 \approx 90 \text{ keV.}$$

small  
decay widths  
compared to  $\Delta V$

$\Delta V [\rho = \rho_N] \approx 80 \text{ MeV}$

TABLE II. The shifts of the masses and decay constants of the heavy mesons in nuclear matter, where NLO (LO) denotes that contributions up to the next-to-leading order (leading order) are included; the unit is MeV.

	$\delta m_D$	$\delta m_{D^*}$	$\delta m_{D_0}$	$\delta m_{D_1}$	$\delta m_B$	$\delta m_{B^*}$	$\delta m_{B_0}$	$\delta m_{B_1}$
NLO	-72	-102	80	97	-473	-687	295	522
LO	-47	-70	54	66	-329	-340	209	260
[13]	-48							
[16]	+45				+60			
[15]	-46							

PHYSICAL REVIEW C 92, 065205 (2015)

# Oscillation of $D^{0*}$ (2007) in Medium

$$M_{D^{0*}} = \begin{bmatrix} 2007 + \underline{40 \text{ MeV}} & e^{i\xi_{M^*}} 3 \cdot 10^{-12} \\ e^{-i\xi_{M^*}} 3 \cdot 10^{-12} & 2007 - \underline{\bar{V}_{\bar{D}^{0*}}(\rho_B)} \end{bmatrix}$$

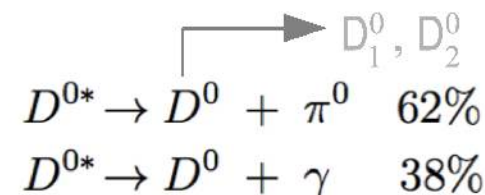
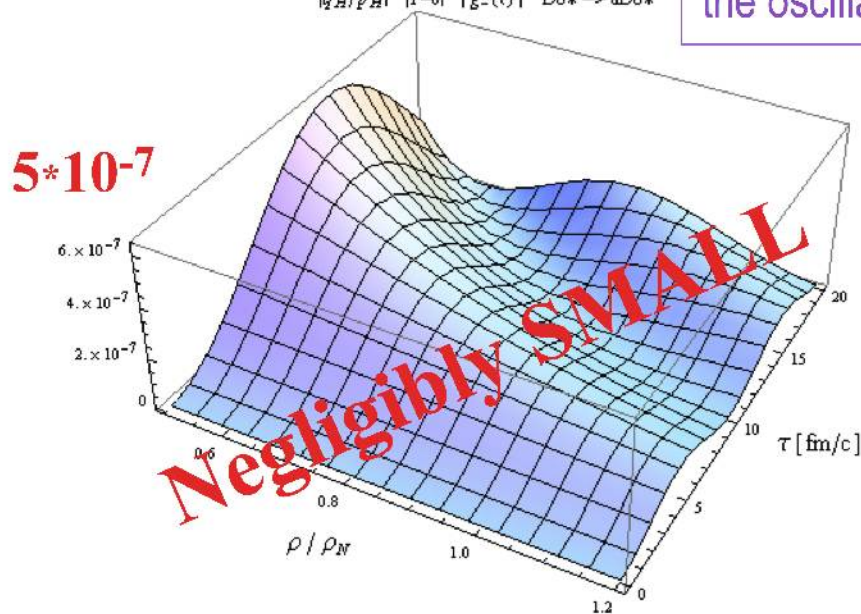
assuming  $M_{12}$  and  $\Gamma_{12}$  are not changed in hadronic medium

$$G_{D^{0*}} = \begin{pmatrix} \underline{0.04} + \gamma_{D^{0*}}(\rho_B) & \underline{0.04} e^{i\xi_{G^*}} \\ \underline{0.04} e^{-i\xi_{G^*}} & \underline{0.04} + \bar{\gamma}_{\bar{D}^{0*}}(\rho_B) \end{pmatrix}$$

$P[D^{0*} \rightarrow \bar{D}^{0*}]$

$|g_{\pi^+} / p_{\pi^+}|^2 |1 - \theta|^2 |g_{\pi^-}(\tau)|^2 D^{0*} \rightarrow \bar{D}^{0*}$

maximal possible value:  
gives upper estimate for  
the oscillation probability



$\Gamma_{D^{*o}} \approx 40 \text{ keV}$  and hence

*Physics Letters B* 418 (1998) 383–388

$$\Gamma_{D^{*++}} \approx 3 \Gamma_{D^{*o}} \left| \frac{P_{\pi(D^{*++})}}{P_{\pi D^{*o}}} \right|^3 \approx 90 \text{ keV.}$$

**small  
decay widths  
compared to  $\Delta V$**

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TABLE II. The shifts of the masses and decay constants of the heavy mesons in nuclear matter, where NLO (LO) denotes that contributions up to the next-to-leading order (leading order) are included; the unit is MeV.

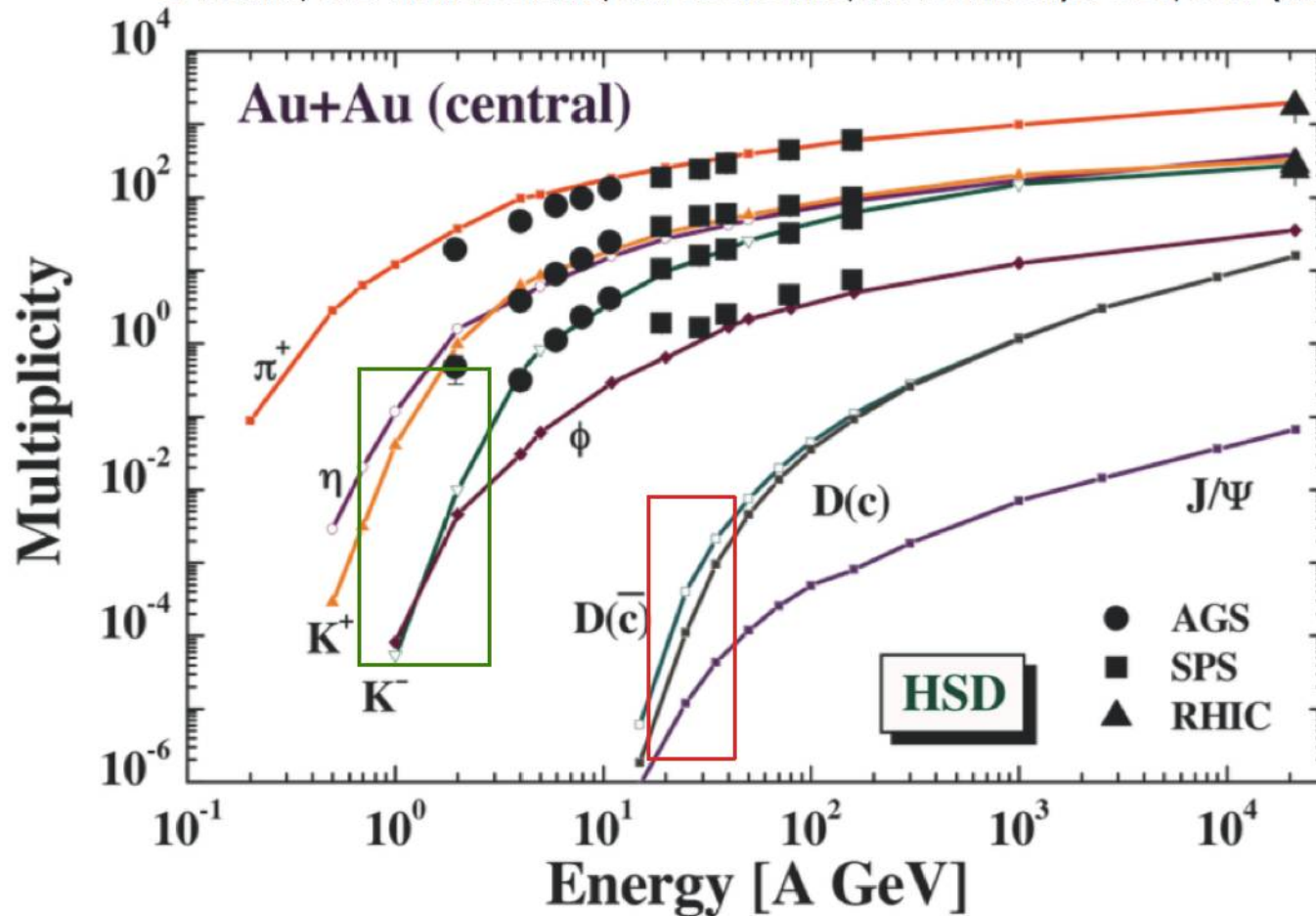
	$\delta m_D$	$\delta m_{D^*}$	$\delta m_{D_0}$	$\delta m_{D_1}$	$\delta m_B$	$\delta m_{B^*}$	$\delta m_{B_0}$	$\delta m_{B_1}$
NLO	-72	-102	80	97	-473	-687	295	522
LO	-47	-70	54	66	-329	-340	209	260
[13]	-48							
[16]	+45				+60			
[15]	-46							

PHYSICAL REVIEW C 92, 065205 (2015)



# (sub)Threshold D, K meson Production Ratios

O. LINNYK, E. L. BRATKOVSKAYA, and W. CASSING, *Int. J. Mod. Phys. E* **17**, 1367 (2008)



Charm is conserved

because  $\bar{D} / D < 10$  makes  $\bar{c} \rightarrow c$  negligible

when  $K^* / \bar{K}^* \geq 10^2$ , process  $\bar{s} \rightarrow s$  is significant

# CONCLUSIONS.

- 1) oscillation  $\bar{K}^{0*} \leftrightarrow K^{0*}$  in dense baryonic matter possible  
(processes  $s \rightarrow \bar{s}$  and  $\bar{s} \rightarrow s$  having same probability)
- 2) if  $N(K^0, K^{0*}) \gg N(\bar{K}^0, \bar{K}^{0*})$  due to  $s$  quarks taken by  $\Lambda, \Sigma$   
real or virtual  $K^{0*}(\bar{s}d) \rightarrow \bar{K}^{0*}(s\bar{d})$  transitions may:
  - enhance the Yields of  $\bar{K}^{0*}$  and  $K^-$  in  $A+A, p+A$  coll.
  - effectively violate strangeness conservation at high  $\rho_B$
- 3)  $\Xi^-(dds)$  sub-threshold production may be explainable  
using strangeness exchange reaction  $\Lambda + \bar{K}^{0sc} \rightarrow \Xi + \pi$
- 4) Charm is conserved ! Strangeness is not at high  $\rho_B$

THANK YOU

FOR  
hospitality



***ATTENTION***

# SUPPRESSION FACTOR ESTIMATE

$$P(K^0 \rightarrow \bar{K}^0) = \left| \frac{q_H}{p_H} \right|^2 |1 - \theta|^2 |g_-(\tau)|^2$$

see G.C. Branco et al.  
in book: "CP Violation"  
Eq.(9.8) Eq.(6.29-32)

$$\left| \frac{q_H}{p_H} \right|^2 = \frac{4|H_{21}|^2}{|\Delta\mu|^2} \frac{1}{|1 - \theta|^2}$$

$$P(K^0 \rightarrow \bar{K}^0) = \frac{|2H_{21}|^2}{|4H_{12}H_{21} + (H_{22} - H_{11})^2|} |g_-(\tau)|^2$$

$\xrightarrow{K^{0*}} (16 \text{ MeV})^2$

$$\approx \frac{|2H_{21}|^2}{|H_{22} - H_{11}|^2} |g_-(\tau)|^2 = \frac{4|M_{21} - i\Gamma_{21}/2|^2}{\Delta V^2} |g_-(\tau)|^2$$

for  $|H_{12}H_{21}| \ll |H_{22} - H_{11}|^2 \approx \Delta V^2$

$(80 \text{ MeV})^2$   
 $\rho = \rho_N$