



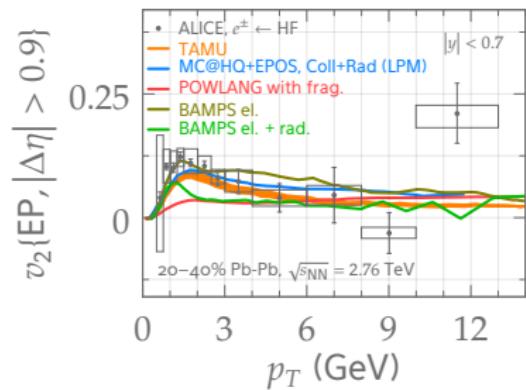
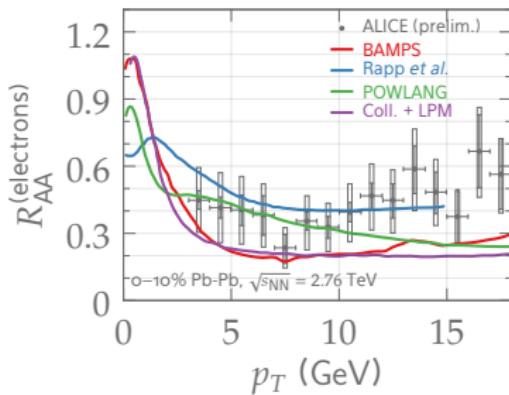
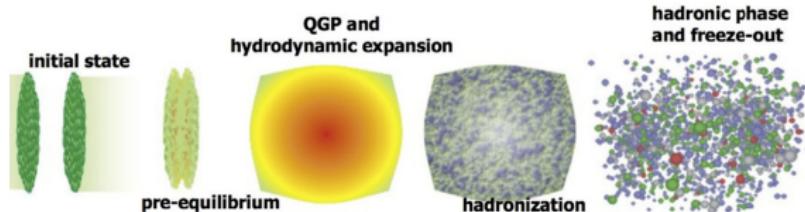
Heavy flavor R_{AA} and v_n in event-by-event viscous relativistic hydrodynamics

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Jorge Noronha and Alexandre A. P. Suaide

Strangeness in Quark Matter 2016

Status quo

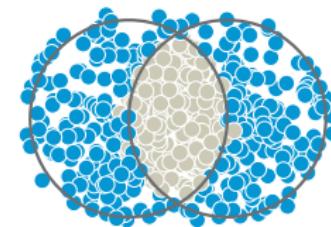


Open questions

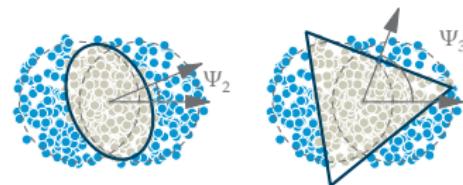
- What happens with the higher Fourier harmonics?
- How sensitive are these observables to the energy loss model?
- Is there collectivity in the heavy flavor sector?
- How do fluctuations in an event-by-event approach affect these observables?

Observables

- Nuclear Modification Factor: $R_{\text{AA}}(p_T, \varphi) = \frac{\frac{dN_{\text{AA}}}{dp_T d\varphi}}{N_{\text{coll}} \frac{dN_{\text{pp}}}{dp_T}}$;
- Collective flow:
 $E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T dy} \left\{ 1 + \sum_n 2v_n \cos[n(\varphi - \Psi_n)] \right\}$;



- Multi-particle Cumulants:
 - 2-, 4-, 6- and 8-particle.



Details of the modeling

- Develop a Monte Carlo simulation;
 - C++ programming language;
 - ROOT and Pythia8.
- Modular paradigm (QCD factorization);
 - Initial conditions (MCKLN);
 - Event-by-event hydrodynamics (v-USPhydro);
 - Energy loss model;
 - Hadronization;
 - Meson decay;
- Heavy quarks (bottom and charm) are probes:
 - What happens in the heavy-flavor sector?
 - High multiplicity experiments allow for the heavy-flavor study.
 - Sampled at the beginning of the simulation and evolved with the medium.
 - We currently neglect any effect of the probes on the medium.

- Simple energy loss model: $\frac{dE}{dx}(T, v; \alpha) = \alpha \Gamma_{\text{flow}} f(T, v);$

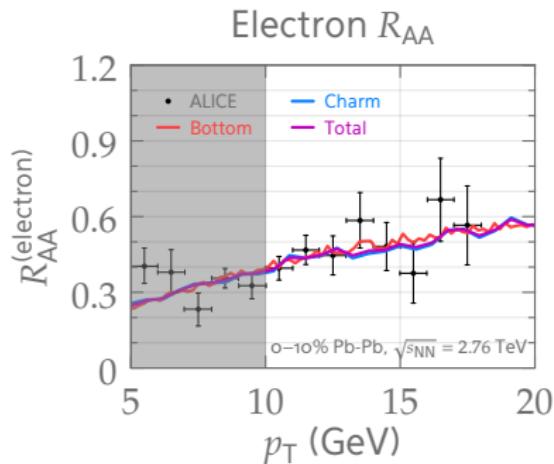
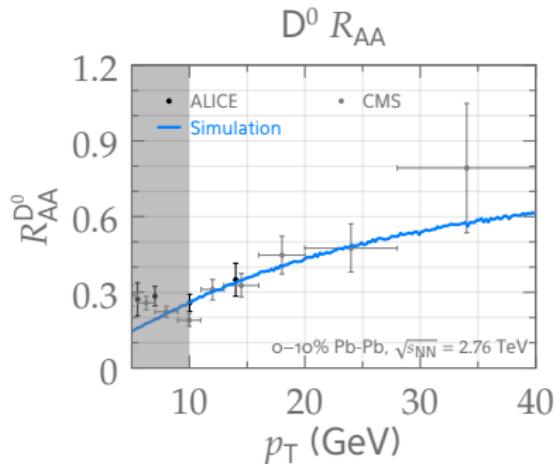
$$\Gamma_{\text{flow}} = \gamma [1 - v \cos(\varphi_{\text{quark}} - \varphi_{\text{flow}})].$$

PRC 72 064910 (2005); arXiv:1602.03788 [nucl-th].

- Fit the α parameter:
 - Fit α_{charm} using $D^0 R_{\text{AA}}$ data;
 - With fixed α_{charm} , fit α_{bottom} using electron R_{AA} data;
- The energy loss model can be changed at will.
- Hadronization using Peterson fragmentation function:
 - Occurs after heavy-quarks have crossed T_{frag} isothermal;
 - Currently not implementing coalescence;
- Decays performed by Pythia8.

Nuclear modification factor

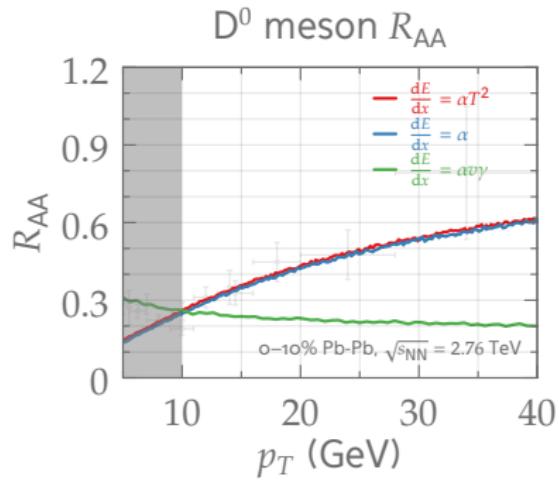
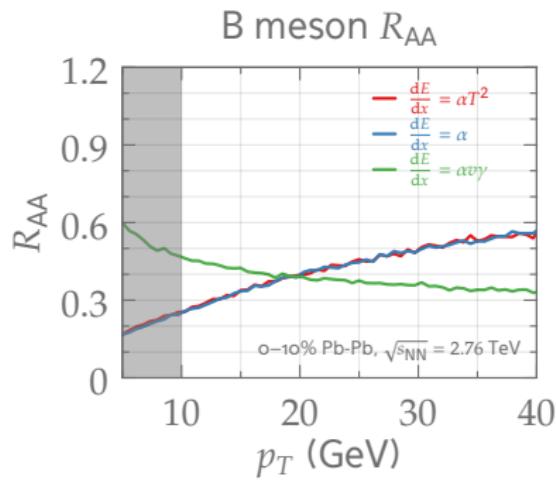
- $\frac{dE}{dx} = \alpha \Gamma_{\text{flow}}$ $T_{\text{frag}} = 140 \text{ MeV.}$ PLB **747** 260–264 (2015)



*Gray area: where coalescence should be important.

Nuclear modification factor

- R_{AA} is highly affected by the energy loss model!
- $T_{\text{frag}} = 140 \text{ MeV}$.



Multi-particle cumulants

First calculation of cumulants event-by-event for heavy-quarks!!!

- $c_n\{4\} = \langle\langle 4 \rangle\rangle - 2 \langle\langle 2 \rangle\rangle^2$

$$v_n\{4\}(p_T) = \frac{-d_n\{4\}}{\left(-c_n\{4\}\right)^{3/4}};$$

- $c_n\{6\} = \langle\langle 6 \rangle\rangle - 9 \langle\langle 4 \rangle\rangle \langle\langle 2 \rangle\rangle + 12 \langle\langle 2 \rangle\rangle^3$

$$v_n\{6\}(p_T) = \frac{d_n\{6\}}{\left[4(c_n\{6\})^5\right]^{1/6}};$$

- $c_n\{8\} = \langle\langle 8 \rangle\rangle - 16 \langle\langle 6 \rangle\rangle \langle\langle 2 \rangle\rangle - 18 \langle\langle 4 \rangle\rangle^2 + 144 \langle\langle 4 \rangle\rangle \langle\langle 2 \rangle\rangle^2 - 144 \langle\langle 2 \rangle\rangle^4$

$$v_n\{8\}(p_T) = \frac{-d_n\{8\}}{\left[33(-c_n\{8\})^7\right]^{1/8}}.$$

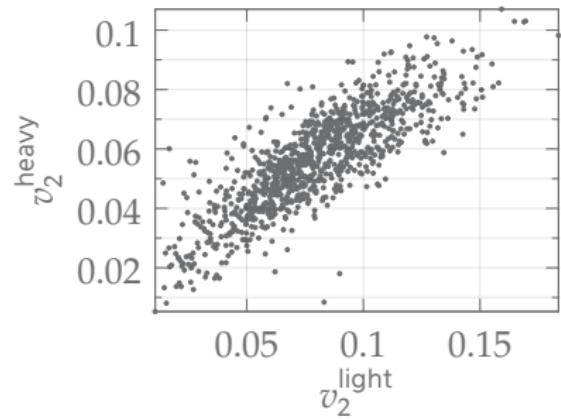
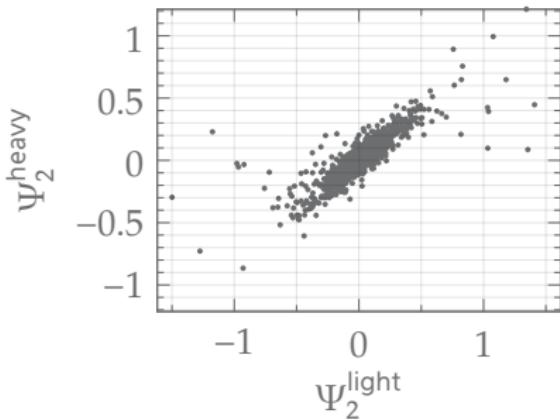
PRC **83** 044913 (2011); PRC **89** 064904 (2014); CMS-PAS-HIN-15-014 (CMS).

Elliptic flow

- Correlation between light quarks in a small p_T bin and heavy quarks:

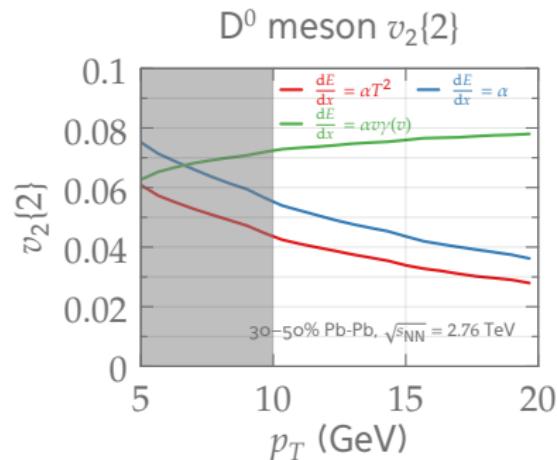
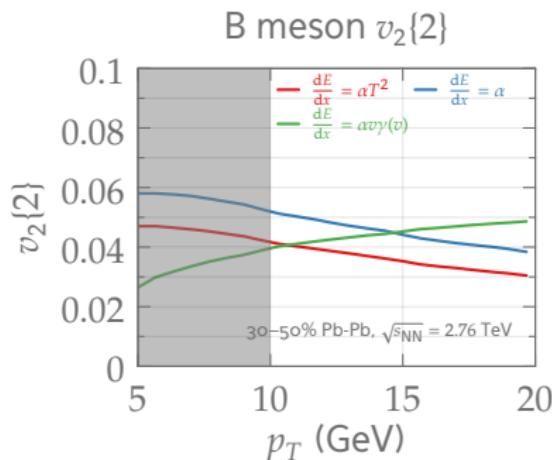
$$v_n\{2\}(p_T) = \frac{\left\langle v_n^{\text{heavy}}(p_T) v_n^{\text{light}} \cos[n(\Psi_n^{\text{heavy}}(p_T) - \Psi_n^{\text{light}})] \right\rangle}{\sqrt{\left\langle (v_n^{\text{light}})^2 \right\rangle}}.$$

- Heavy sector inherits geometrical fluctuations of soft sector;
 PRL **116** 252301 (2016).



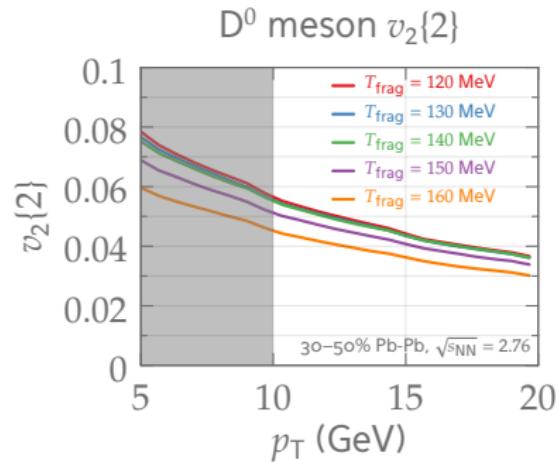
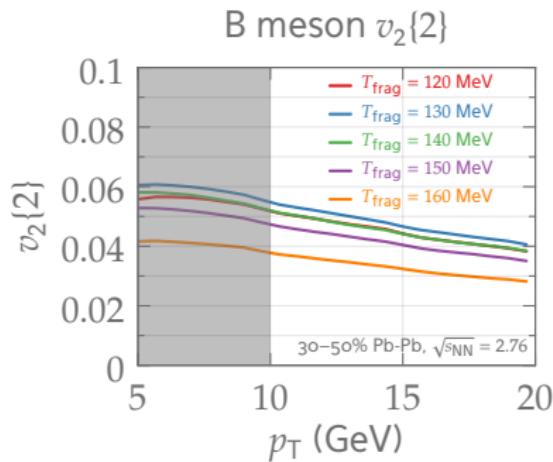
$v_2\{2\}$ — Energy loss dependence

- $T_{\text{frag}} = 140 \text{ MeV}$;
- $v_2\{2\}$ depends heavily on the energy loss model.



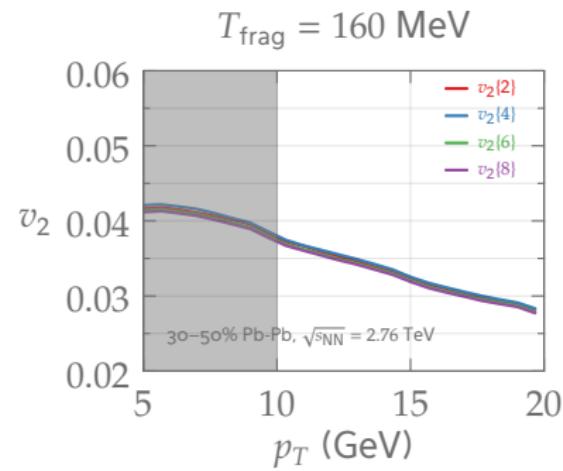
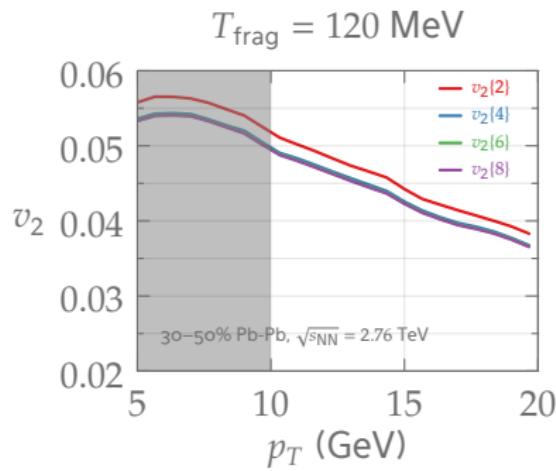
$v_2\{2\} - T_{\text{frag}}$ dependence

- $\frac{dE}{dx} = \alpha \Gamma_{\text{flow}}$;
- The increase of T_{frag} decreases the flow.



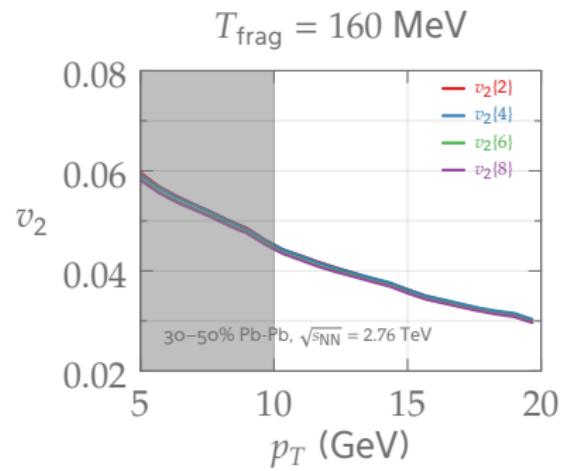
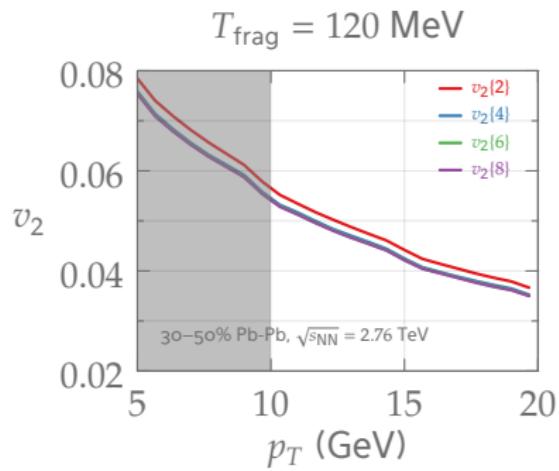
Convergence of cumulants!

- $\frac{dE}{dx} = \alpha \Gamma_{\text{flow}}$ B meson;
- Convergence may indicate collectivity in the heavy sector.



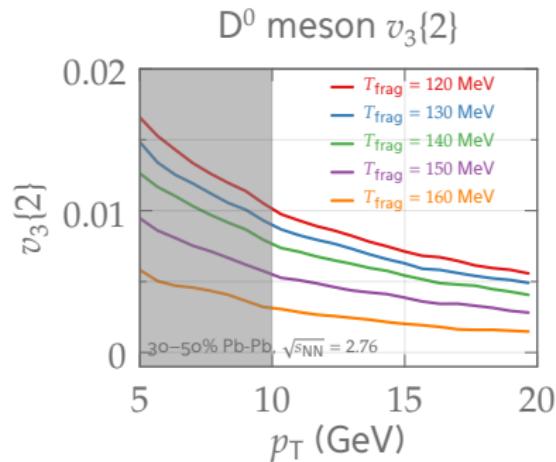
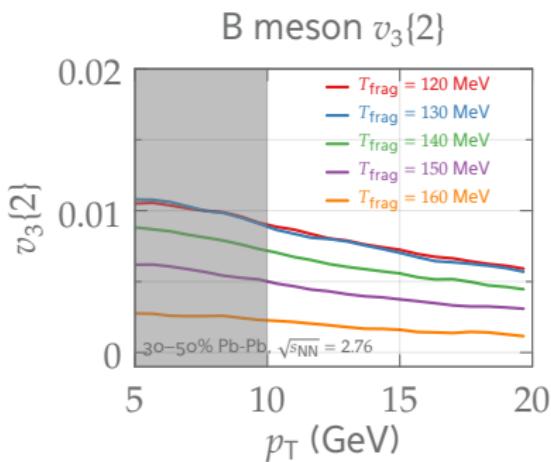
Convergence of cumulants!

- $\frac{dE}{dx} = \alpha \Gamma_{\text{flow}}$ D^0 meson.
- Convergence may indicate collectivity in the heavy sector.



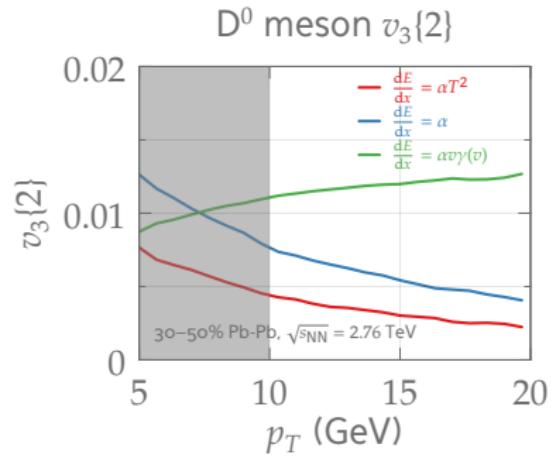
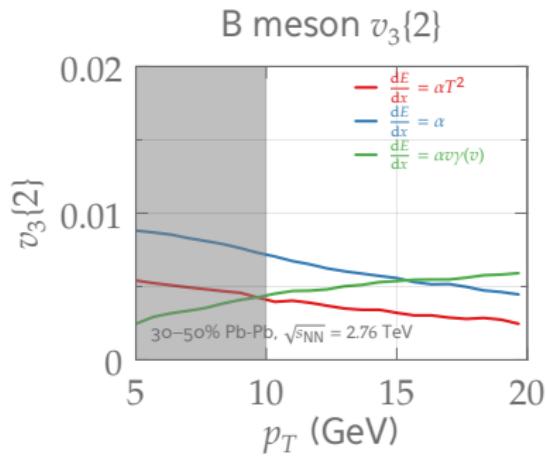
v_3 for heavy flavor!

- $\frac{dE}{dx} = \alpha \Gamma_{\text{flow}}$;
- First calculation of $v_3\{2\} \neq 0$ for heavy-quark!!!
- $v_3\{2\}$ also decreases with the increase of T_{frag} .



v_3 for heavy flavor!

- $T_{\text{frag}} = 140 \text{ MeV}.$
- $v_3\{2\}$ very sensitive to energy loss models;



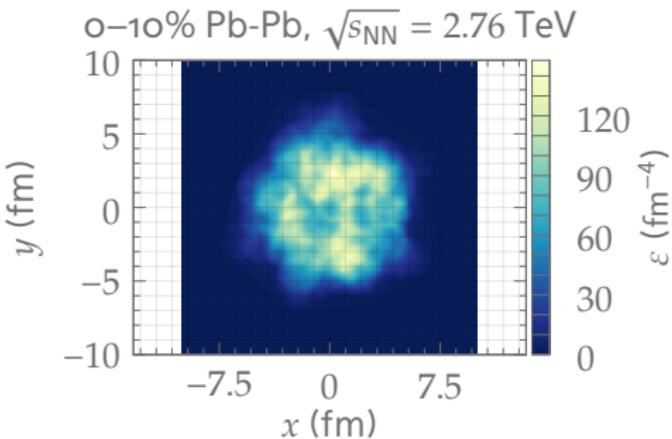
Conclusions and outlook

- New framework to study hard probes in an event-by-event hydrodynamics expanding QGP;
- First prediction of heavy-quark cumulants:
 - Convergence of cumulants: collectivity in the heavy-flavor sector?
- First prediction of $v_3\{2\}$ for heavy-flavor;
- Future work:
 - Improvement in the low- p_T sector;
 - Correlations between v_n in the heavy-flavor sector;
 - Soft hard event engineering in the heavy-flavor sector;
 - Check the influence of a T dependent shear and bulk viscosities;
 - Check different beam energies;
 - Symmetric cumulants $SC(n, m)$.

Backup

Initial Conditions

- Actual input of the program;
- 2D profiles for the hydro:
 - Energy density;
 - Temperature;
 - Transverse velocity;
- MCKLN initial conditions;
- Quarks position given by number of binary collisions;
 - Initial momentum distribution given by pQCD (FONLL).



- Viscous event-by-event 2D+1 hydrodynamics:
v-USPhydro [1]:
 - $\eta/s = 0.11$;

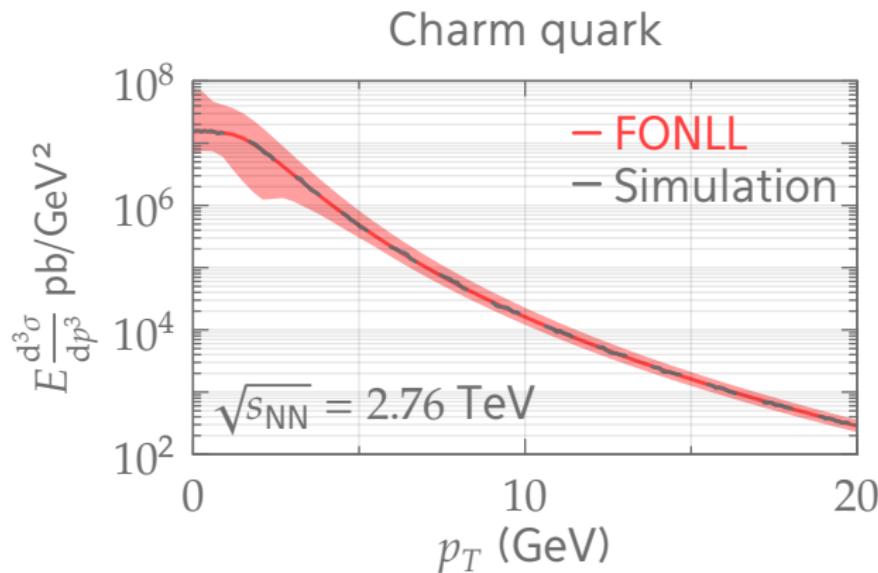
$$T^{\mu\nu} = \varepsilon u^\nu u^\nu - p \Delta^{\mu\nu} + \pi^{\mu\nu}, \quad \partial_\mu T^{\mu\nu} = 0$$

- Equations of motion solved using Smoothed Particle Hydrodynamics (SPH) algorithm:
 - SPH-particles: Lagrangian method;
 - Fast computational time;
 - Well tested algorithm.
- Freeze-out: Cooper-Frye prescription including viscous corrections.
 - $T_{FO} = 120$ MeV.

[1] arXiv:1602.03788 (2016); PRC **90**, 034907 (2014); PRC **88** 044916 (2013)

Heavy-flavor production

- Quark initial momentum: pQCD (FONLL).
- Quark initial direction (φ): random;

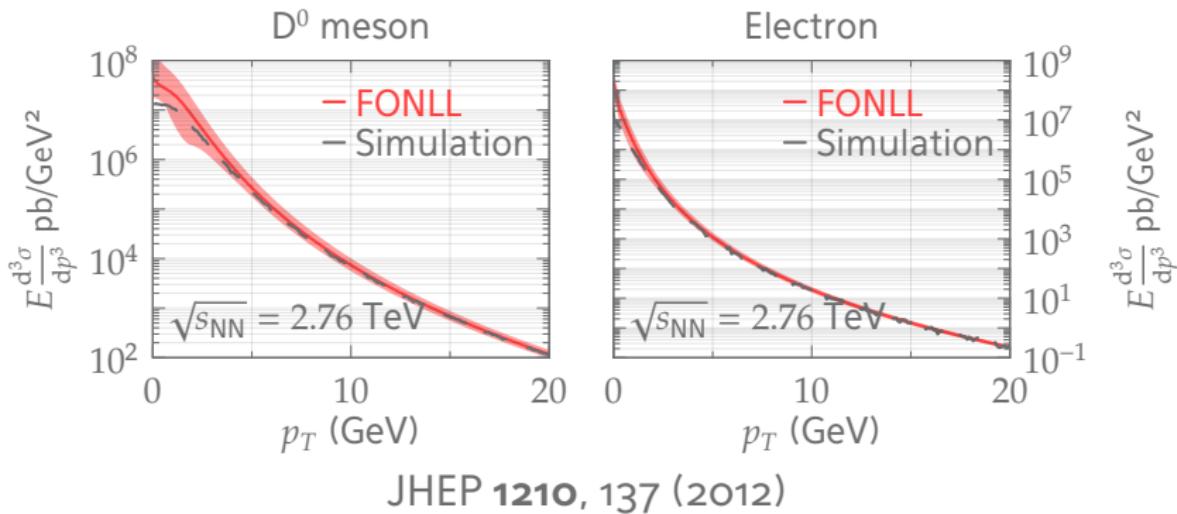


JHEP 1210, 137 (2012)

Heavy-flavor production

Check consistency of the code:

- Turn off energy loss: get the same as FONLL predictions.



- Hadronization:

- Heavy quarks hadronize after crossing the T_{frag} isothermal.
- We use Peterson fragmentation function:

$$D(z) \propto \frac{1}{z \left(1 - \frac{1}{z} - \frac{\varepsilon}{1-z}\right)^2};$$

- Currently we're not implementing coalescence (future work);
- Decays:
 - Performed using Pythia8;
 - Only semi-leptonic channels selected;