

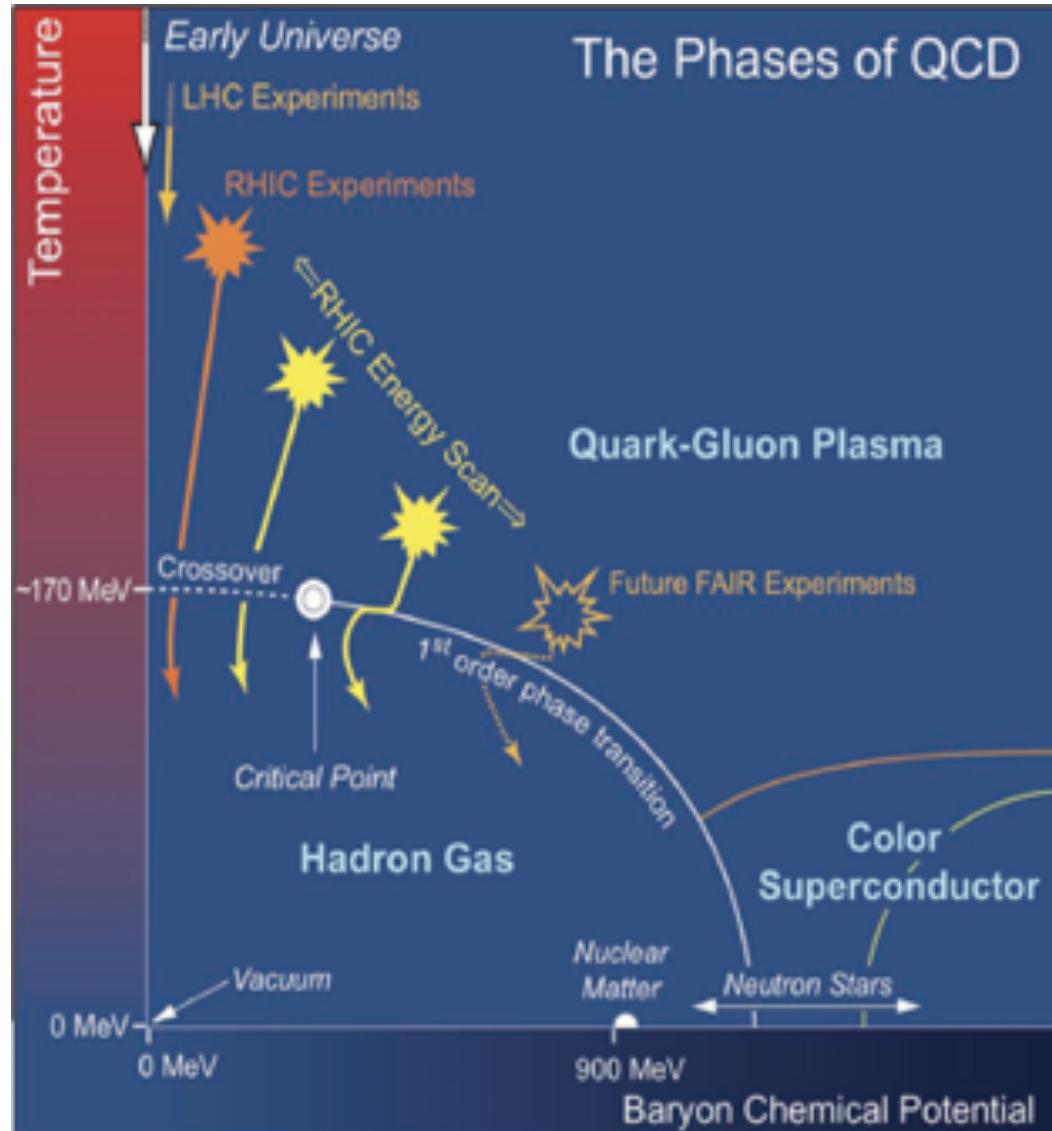
# Higher Moments of Net-Kaon Multiplicity Distributions at STAR

Ji Xu for the STAR Collaboration  
Central China Normal University  
Lawrence Berkeley National Laboratory



- Introduction
- Analysis Techniques and Details
- Results
- Summary

# QCD Phase Diagram



- Crossover at  $\mu_B=0$ .
- First order phase transition expected at large  $\mu_B$ .
- QCD Critical Point: The end point of first order phase transition boundary.
- Where is CP(Critical Point) ?

STAR Note 0598

- Sensitive to correlation length ( $\xi$ ) and probe non-gaussian fluctuations near the Critical Point.

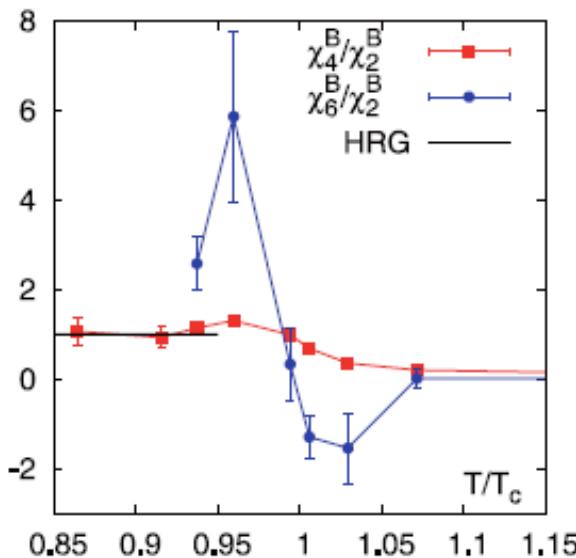
$$\langle (\delta N)^2 \rangle \sim \xi^2, \langle (\delta N)^3 \rangle \sim \xi^{4.5}, \langle (\delta N)^4 \rangle - 3\langle (\delta N)^2 \rangle^2 \sim \xi^7$$

M. A. Stephanov, Phys. Rev. Lett. 102, 032301 (2009).

M. A. Stephanov, Phys. Rev. Lett. 107, 052301 (2011).

M. Asakawa, S. Ejiri and M. Kitazawa, Phys. Rev. Lett. 103, 262301 (2009).

- Direct connection to the susceptibility of the system.



$$\chi_q^{(n)} = \frac{1}{VT^3} \times C_{n,q} = \frac{\partial^n(p/T^4)}{\partial(\mu_q)^n}, q = B, Q, S$$

- S. Ejiri et al, Phys.Lett. B 633 (2006) 275.  
 Cheng et al, PRD (2009) 074505. B. Friman et al., EPJC 71 (2011) 1694.  
 F. Karsch and K. Redlich , PLB 695, 136 (2011).  
 S. Gupta, et al., Science, 332, 1525(2011).  
 A. Bazavov et al., PRL109, 192302(12) // S. Borsanyi et al., PRL111, 062005(13) // P. Alba et al., arXiv:1403.4903

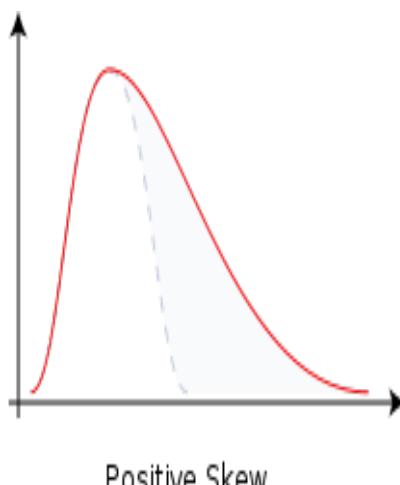
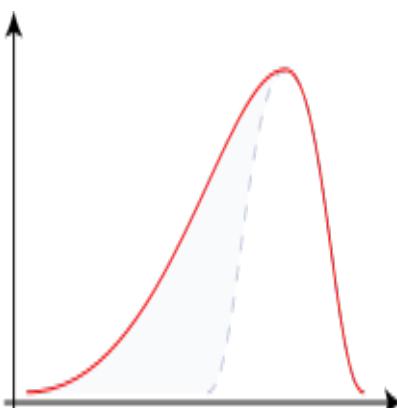
# Higher Moments (fluctuations)

“Shape” of the fluctuations can be measured: non-Gaussian moments (cumulants):

$$C_{1,x} = \langle x \rangle, C_{2,x} = \langle (\delta x)^2 \rangle,$$

$$C_{3,x} = \langle (\delta x)^3 \rangle, C_{4,x} = \langle (\delta x)^4 \rangle - 3 \langle (\delta x)^2 \rangle^2$$

$$S = \frac{C_{3,N}}{(C_{2,N})^{3/2}} = \frac{\langle (N - \langle N \rangle)^3 \rangle}{\sigma^3}$$



$$\kappa = \frac{C_{4,N}}{(C_{2,N})^2} = \frac{\langle (N - \langle N \rangle)^4 \rangle}{\sigma^4} - 3$$

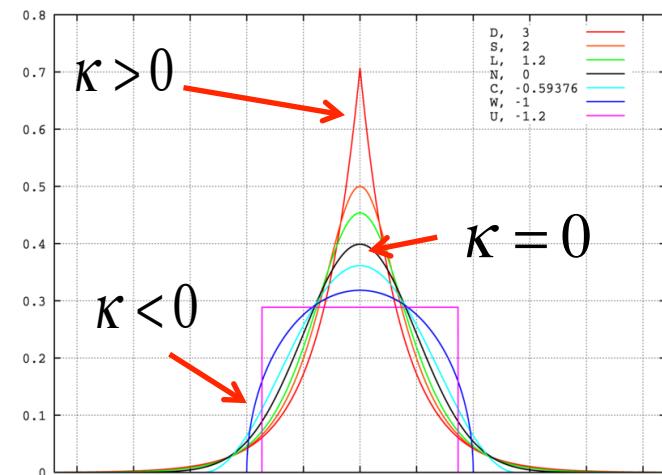


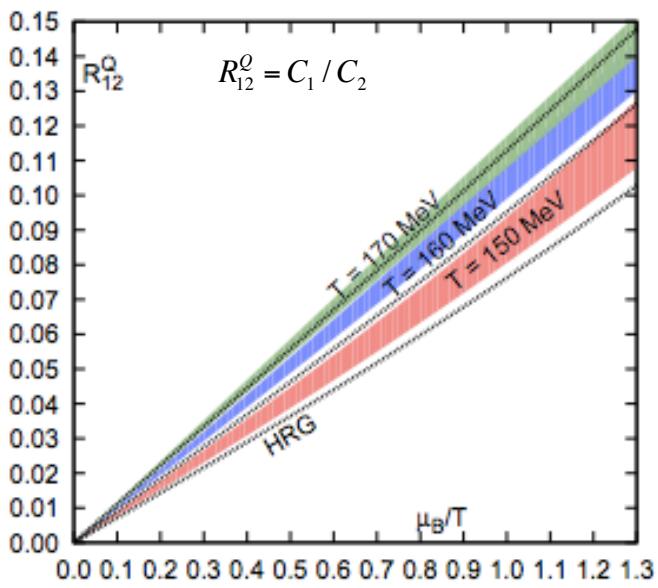
Figure from wikipedia

## ➤ Cumulant Ratios

$$\kappa \sigma^2 = \frac{C_{4,q}}{C_{2,q}}, \quad S \sigma = \frac{C_{3,q}}{C_{2,q}}$$

# Experimental Observables

- We measured the net-particle multiplicity fluctuations: net-charge, net-proton (proxy for net-baryon), net-kaon (proxy for net-strangeness). The main observables are volume independent cumulant ratios.



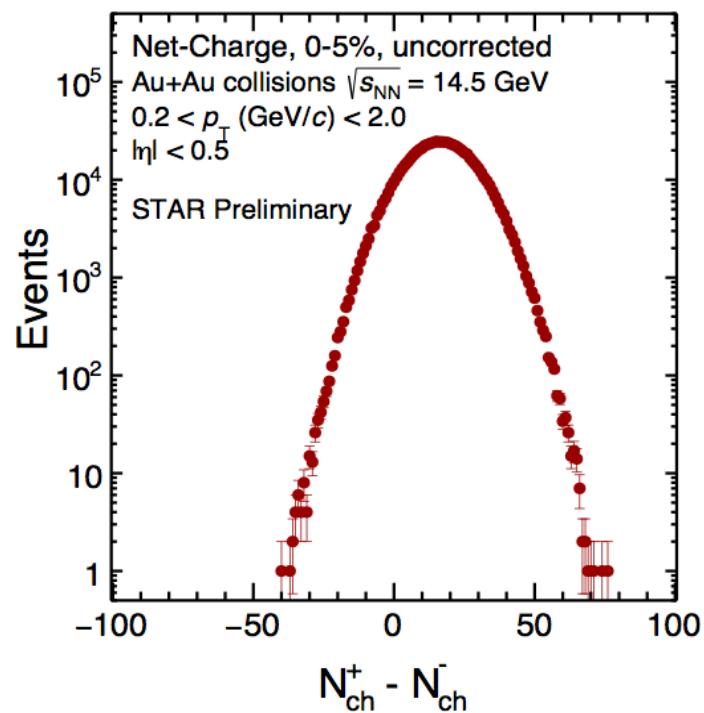
HotQCD, PRL109, 192302 (2012)  
WB Group, PRL111, 062005 (2013)

$$\frac{\chi_2^i}{\chi_1^i} = (\sigma^2/M)^i = \frac{c_2^i}{c_1^i}$$

$$\frac{\chi_3^i}{\chi_2^i} = (S\sigma)^i = \frac{c_3^i}{c_2^i}$$

$$\frac{\chi_4^i}{\chi_2^i} = (\kappa\sigma^2)^i = \frac{c_4^i}{c_2^i}$$

$$i = B, Q, S$$



Theory



Experiment

- In the first phase of the Beam Energy Scan (BES) program at RHIC, eight beam energies have already been analyzed from  $\sqrt{s}_{NN}=7.7\text{GeV}$  to 200GeV.

$\sqrt{s}$ (GeV)	Statistics (Millions)	Year	$\mu_B$ (MeV)	T (MeV)	$\mu_B / T$
7.7	~4	2010	420	140	3.020
11.5	~12	2010	315	152	2.084
14.5	~ 20	2014	266	156	1.705
19.6	~36	2011	205	160	1.287
27	~70	2011	155	163	0.961
39	~130	2010	115	164	0.684
62.4	~67	2010	70	165	0.439
200	~350	2010	20	166	0.142

$\mu_B, T$  : J. Cleymans et al., PRC 73, 034905 (2006)

### Study QCD Phase Structure

- Onset of sQGP
- Phase boundary and **critical point**.

EEMC

Magnet

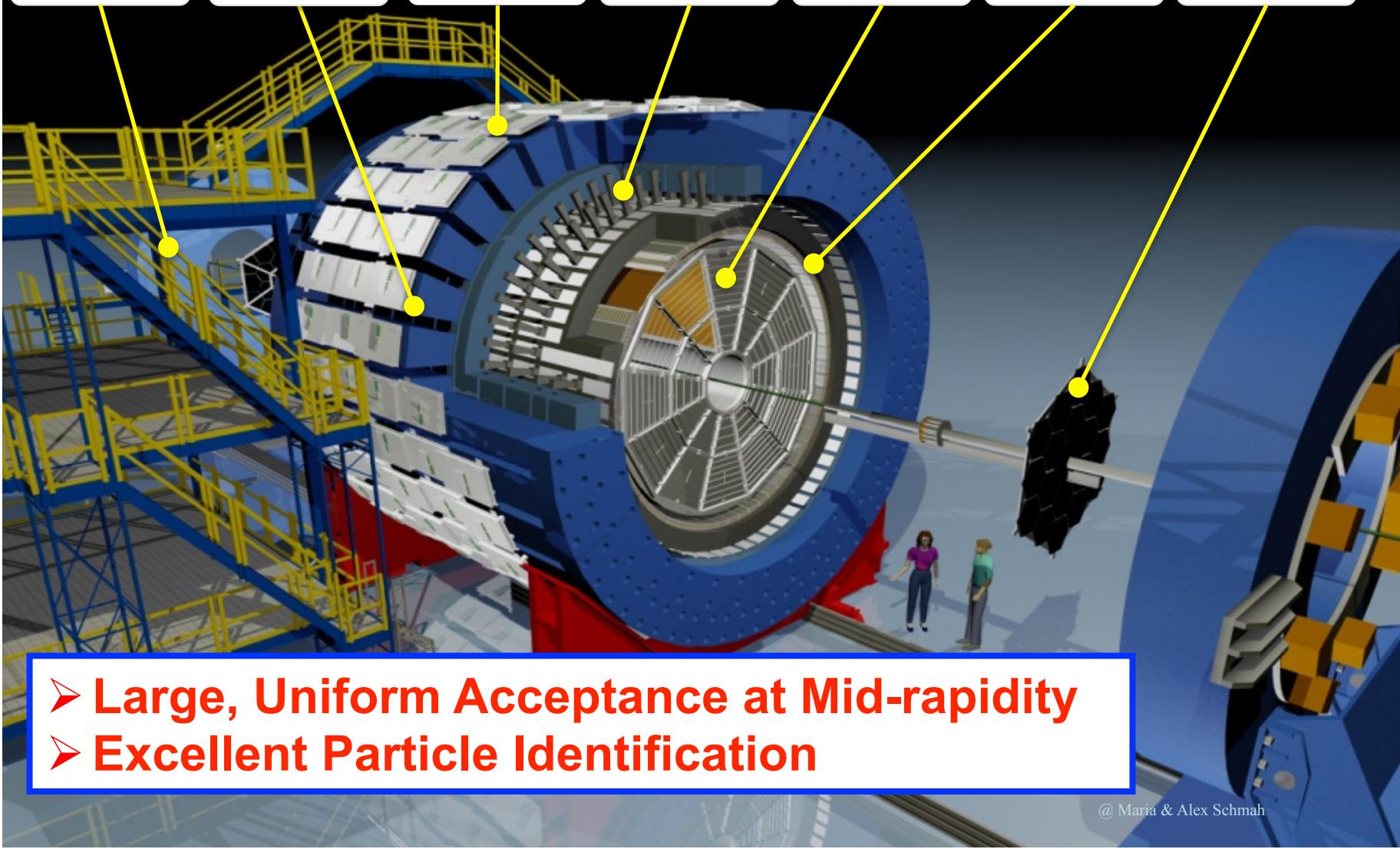
MTD

BEMC

TPC

TOF

BBC

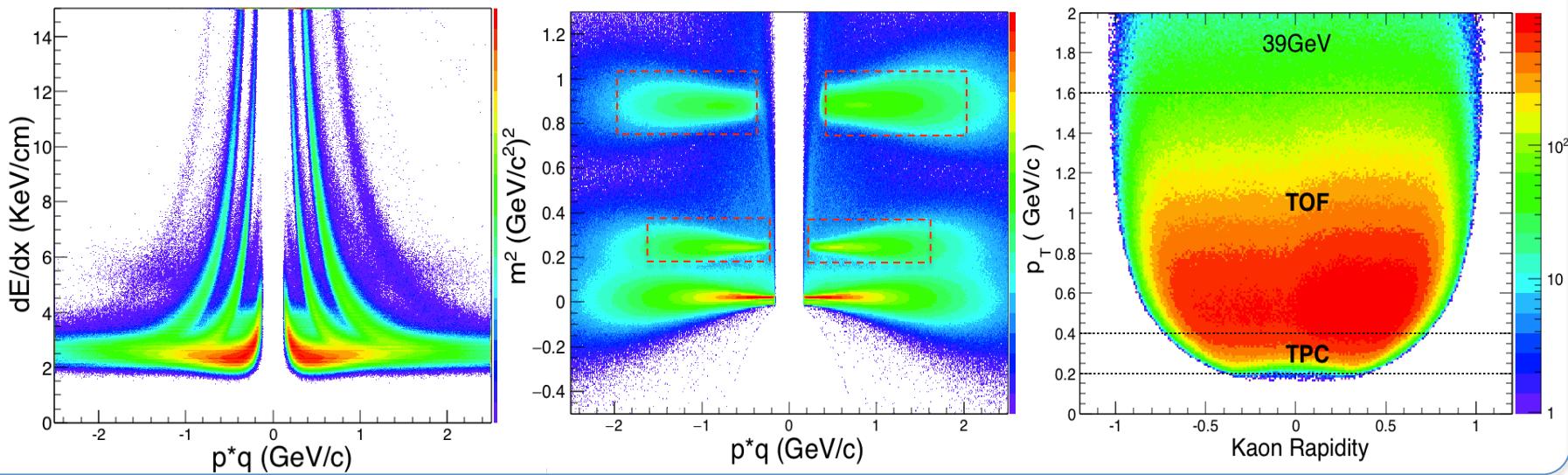
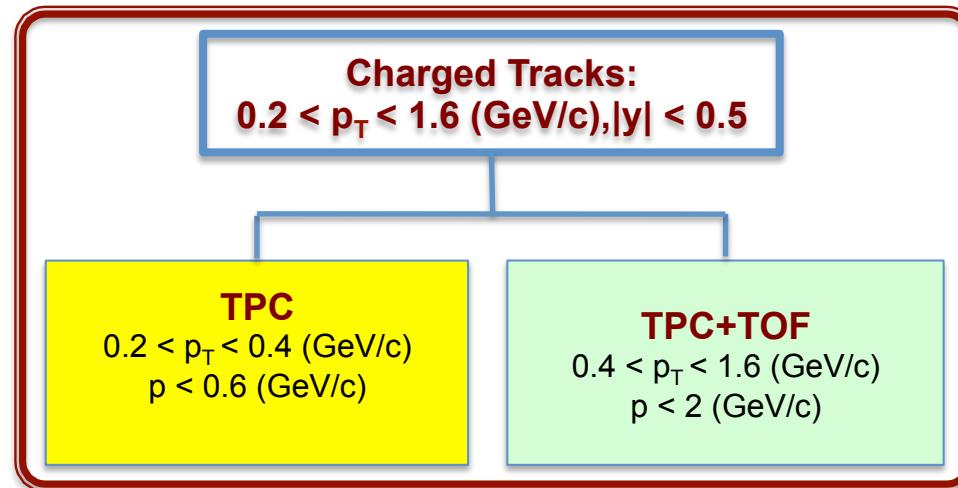


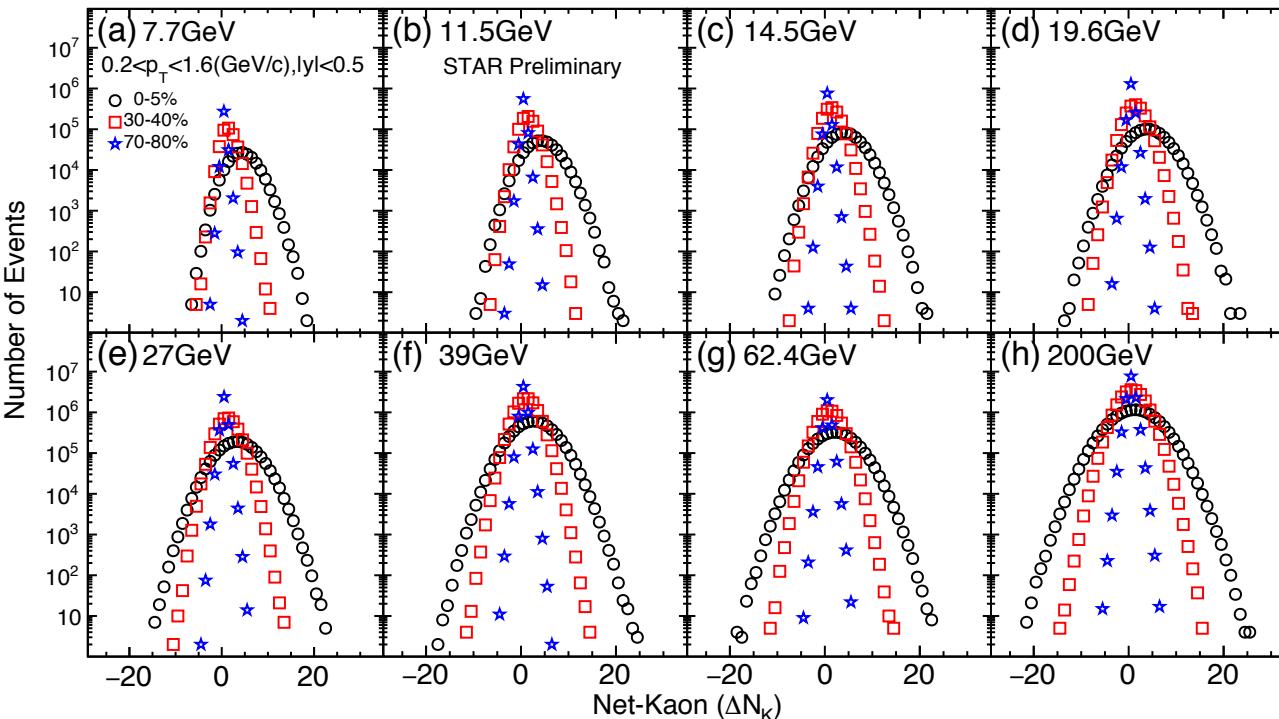
- Large, Uniform Acceptance at Mid-rapidity
- Excellent Particle Identification

@ Maria &amp; Alex Schmah

# Kaon ID with STAR Detectors

- PID: Energy loss ( $dE/dx$ ) in Time Projection Chamber and mass-squared ( $m^2$ ) from Time of Flight are used to identify kaons within  $0.2 < p_T < 1.6 \text{ (GeV/c)}$  and at mid-rapidity  $|y| < 0.5$ .



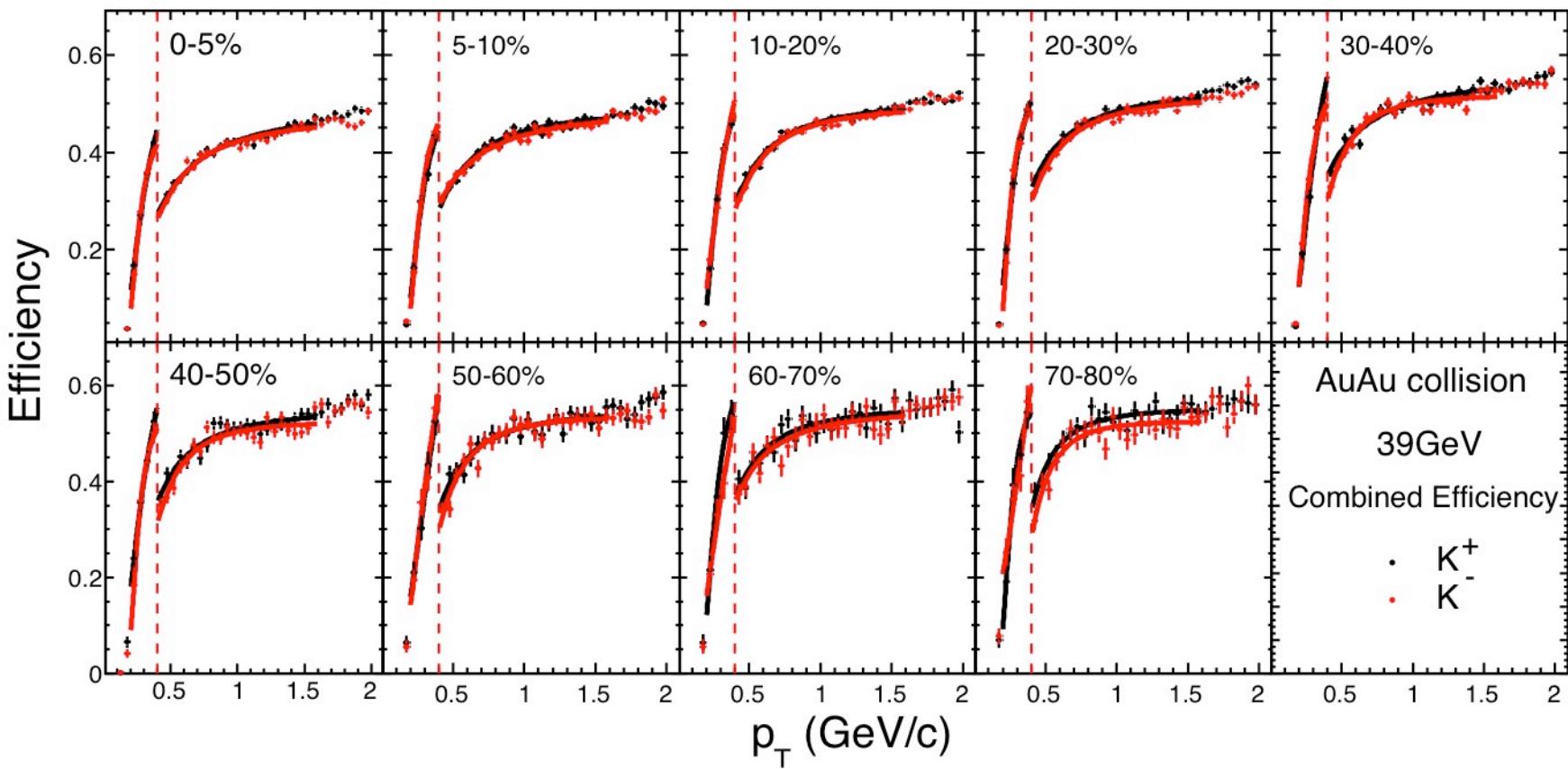


- Most central collisions have a wider distribution compared with peripheral collisions.
- The peak of the net-kaon distributions shift slightly towards the positive direction as the energy decreases.

Effects that need to be addressed to get final moments/cumulants:

1. Auto-correlation effects.
2. Effects of volume fluctuations.
3. Finite detector efficiency .

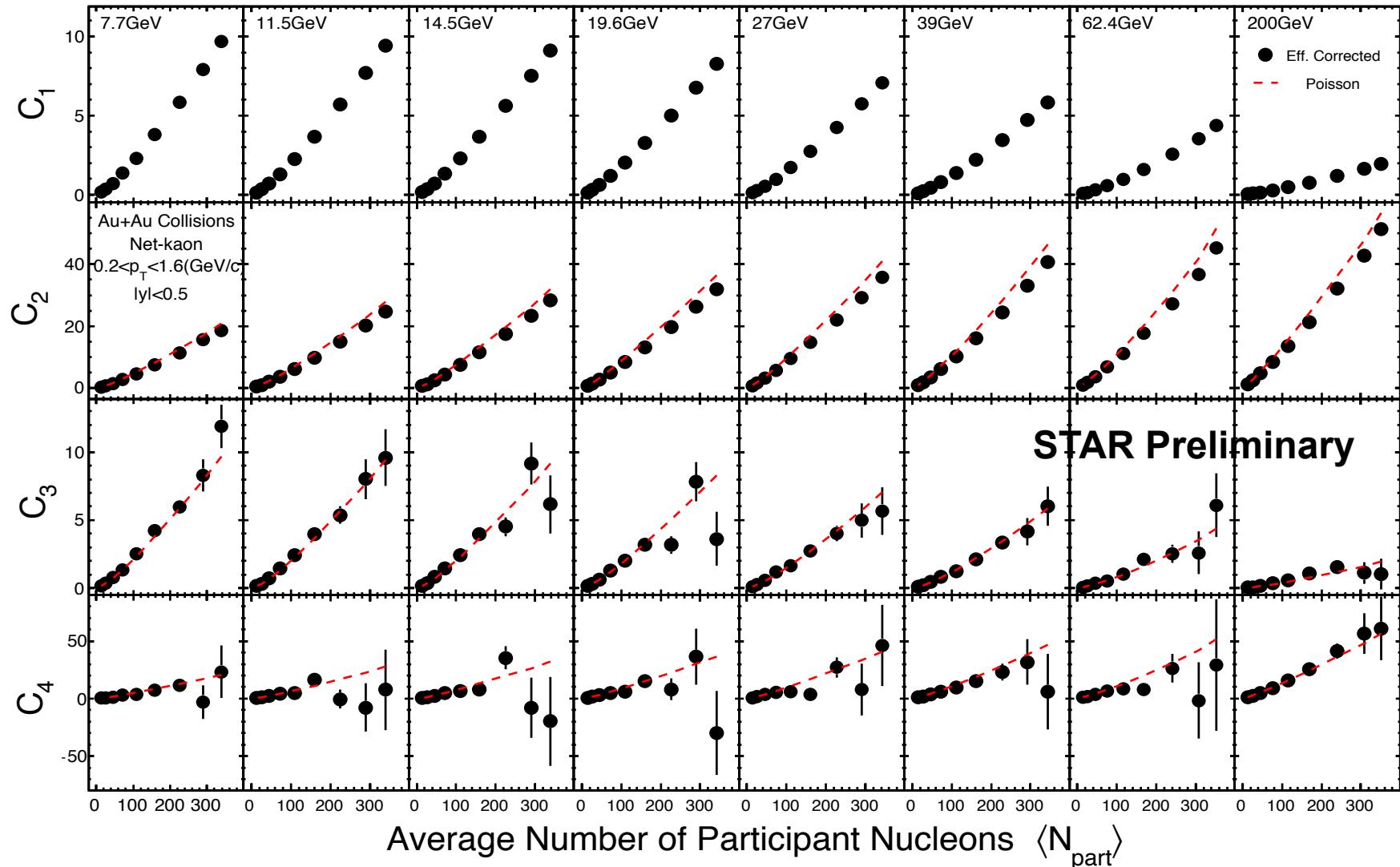
A. Bzdak, et al. PRC91, 027901 (2015)  
 X.Luo, Phys. Rev. C 91, 034907 (2015)  
 X.Luo, et al. J. Phys. G40, 105104(2013)

Combined Efficiency for  $K^+$  and  $K^-$ 

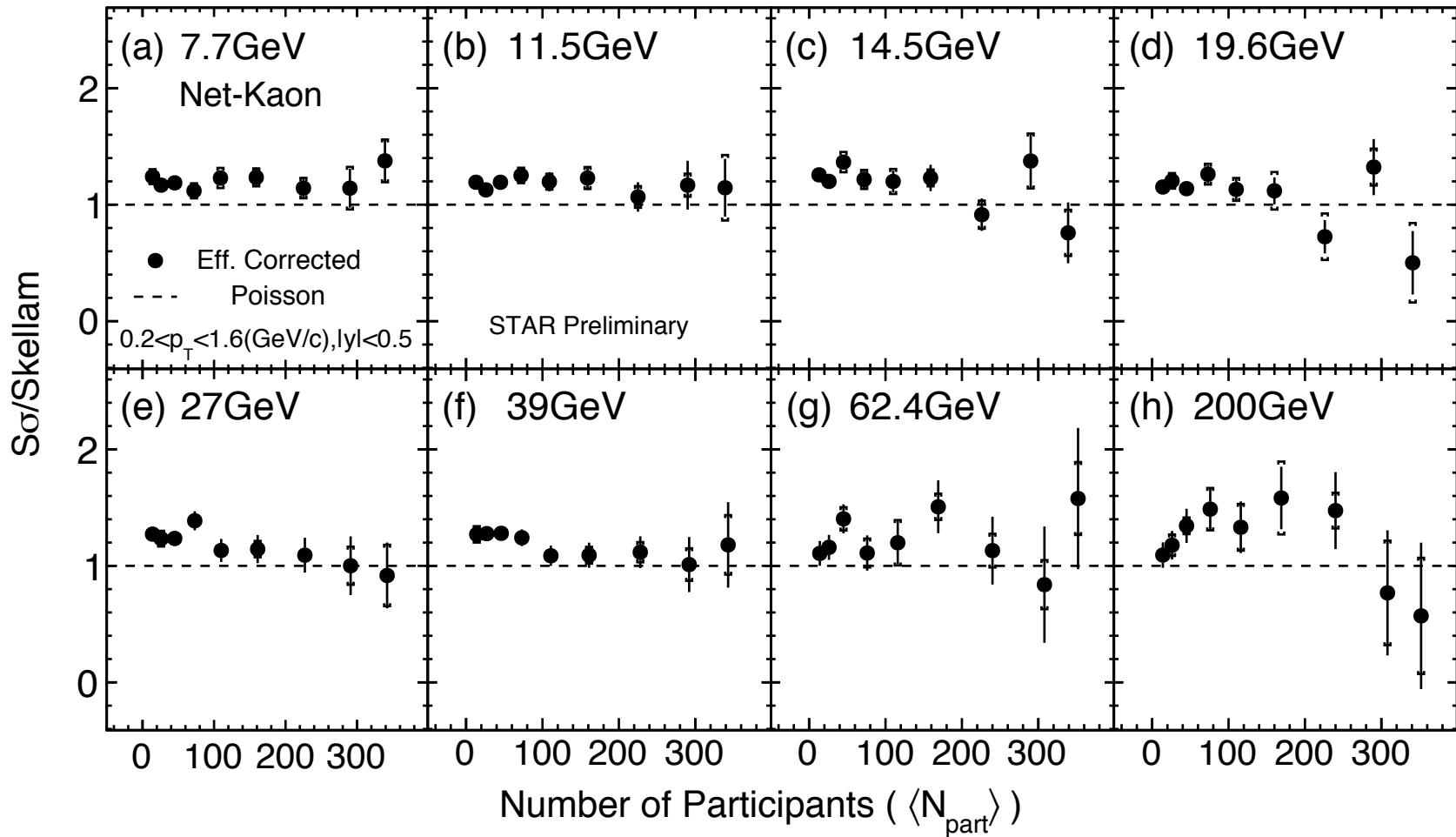
- $0.2 < p_T < 0.4$  (GeV/c), TPC only
- $0.4 < p_T < 1.6$  (GeV/c), TPC+TOF  
Efficiency=Efficiency(Tracking)\*Efficiency(TOF match)
- The input number is the  $p_T$  weighted average efficiency.

X. Luo, PRC91, 034907 (2015); A. Bzdak and V. Koch, PRC91, 027901 (2015)

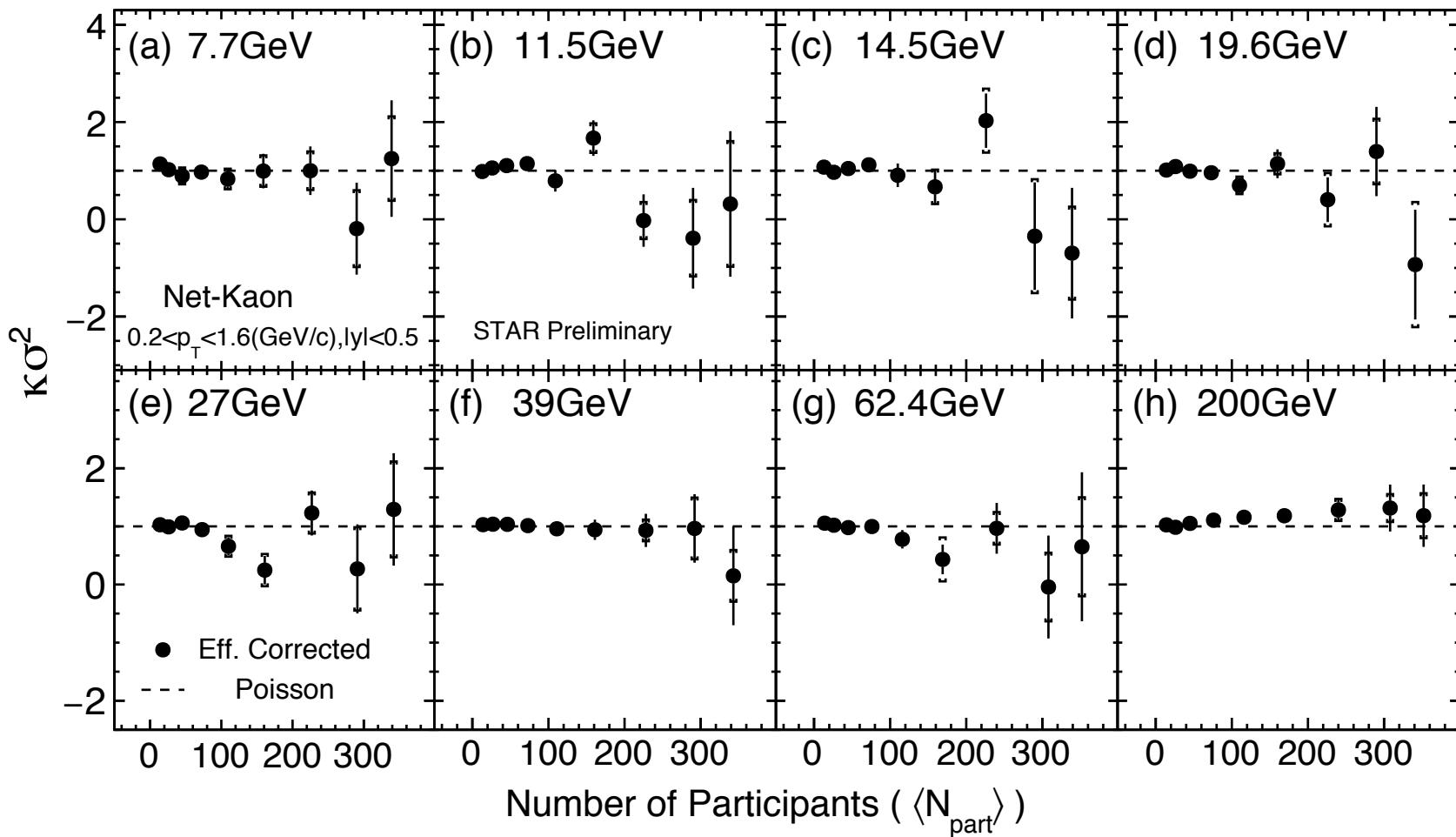
## Cumulants for Net-Kaon



$C_3$  and  $C_4$  generally consistent with Poisson expectation.

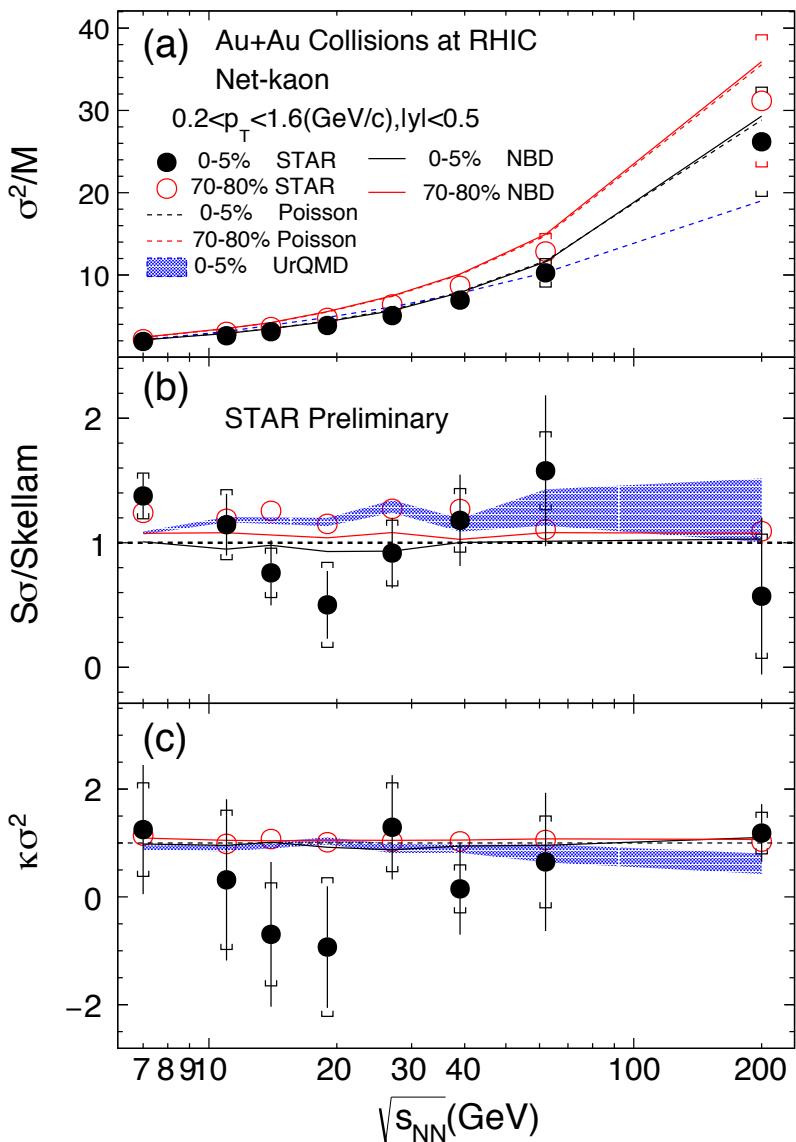
Centrality Dependence of  $C_3/C_2$ 

- The values of  $S\sigma/\text{Skellam}$  are consistent with unity within uncertainties.

Centrality Dependence of  $C_4/C_2$ 

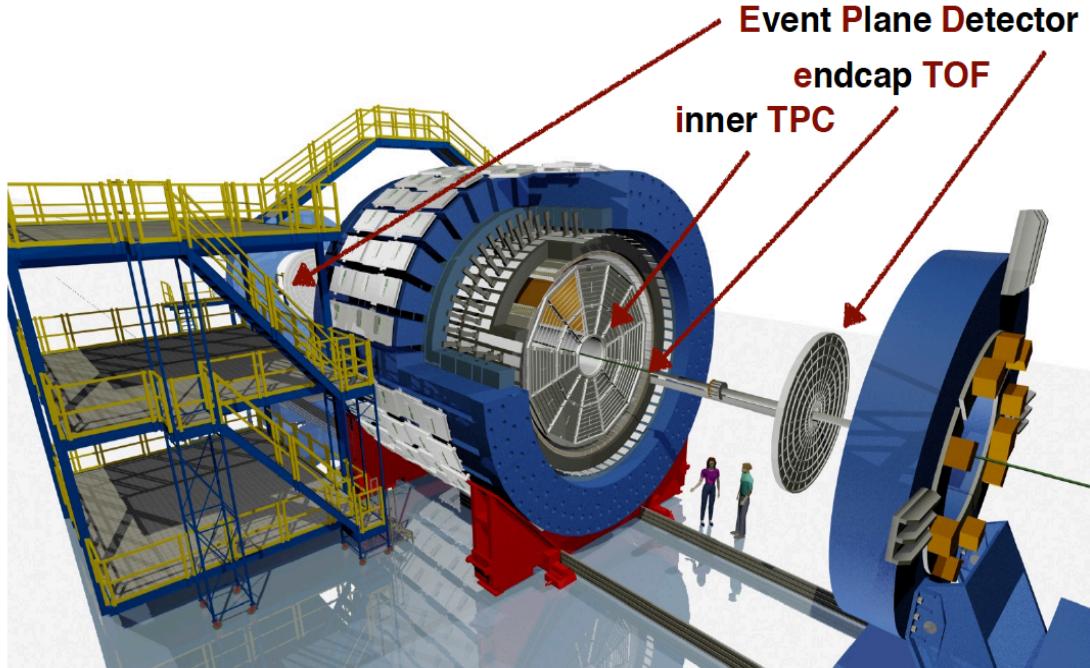
- The values of  $\kappa\sigma^2$  are consistent with unity within uncertainties.

# Energy Dependence of Net-kaon

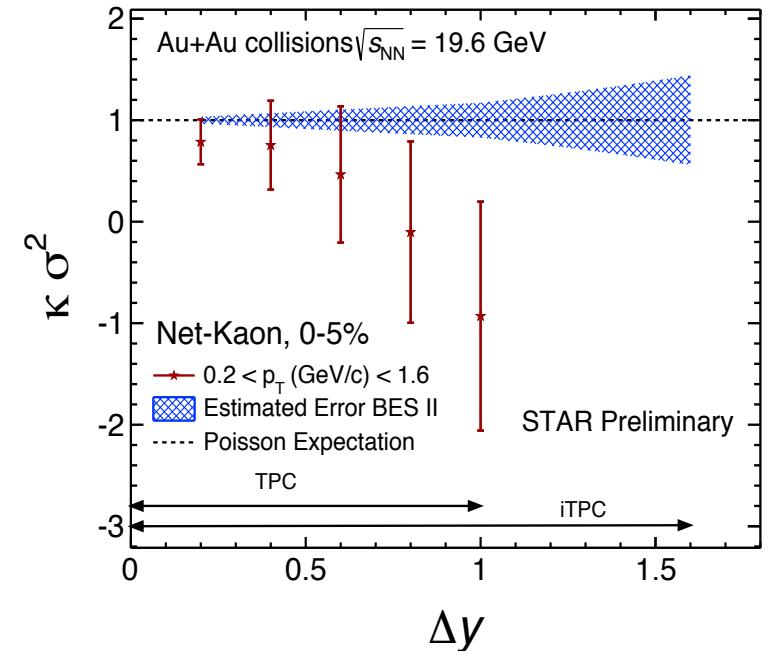


- The values of  $\sigma^2/M$  increase as the energy increases.
- The values of  $S\sigma/\text{Skellam}$  are consistent with poisson and negative binomial distribution baseline within uncertainties.
- The values of  $\kappa\sigma^2$  are consistent with poisson and negative binomial distribution baseline within uncertainties.
- UrQMD (no Critical Point), shows no energy dependence for  $S\sigma/\text{Skellam}$  and  $\kappa\sigma^2$ .

# Beam Energy Scan II



iTPC proposal: <http://drupal.star.bnl.gov/STAR/starnotes/public/sn0619>  
 BES-II whitepaper: <http://drupal.star.bnl.gov/STAR/starnotes/public/sn0598>



- Inner TPC(iTPC) upgrade :  $|\eta| < 1$  to  $|\eta| < 1.5$ , better  $dE/dx$  resolution and higher tracking efficiency.
- Event Plane Detector (EPD): Centrality and Event Plane Determination.  
 $2.1 < |\eta| < 5.1$
- eTOF: Larger rapidity coverage extends PID in forward direction  $-1.6 < \eta < -1.1$ .

More details see talks by Alexander Schmah, Jinlong Zhang, and Chi Yang.

- STAR new results on collision energy and centrality dependence of net-Kaon cumulants and their ratios, within the kinematic range [ $|y| < 0.5$ ,  $0.2 < p_T < 1.6$  (GeV/c)], for Au +Au collisions at  $\sqrt{s}_{NN} = 7.7, 11.5, 14.5, 19.6, 27, 39, 62.4$  and 200 GeV are presented.
- The values of net-Kaon's  $\kappa\sigma^2$  and  $S\sigma$ /Skellam are consistent with poisson and negative binomial distribution baseline within errors.
- BES-II (2019-2020) will improve on Kaon's:
  - rapidity, purity, and efficiency
  - systematic control