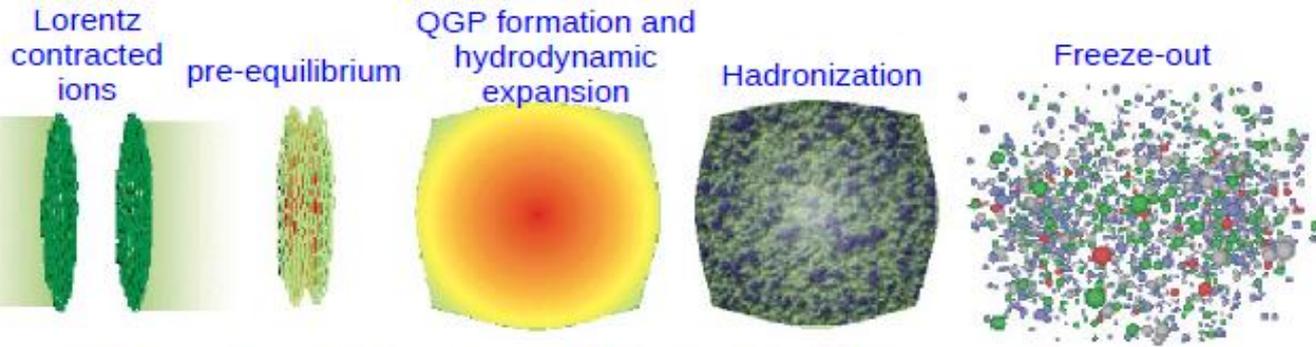


# Scaling properties of the mean multiplicity and pseudorapidity density in $e^-+e^+$ , $e+p$ , $p+p$ , $p+A$ and $A+A(B)$ collisions

*Roy A. Lacey & Peifeng Liu  
Stony Brook University*

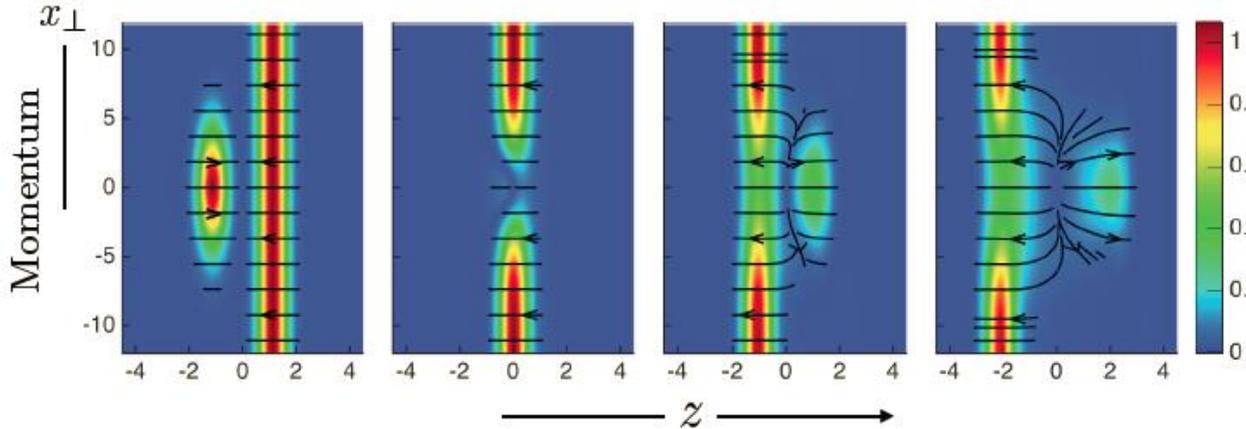
# Backdrop

A+A  
collision

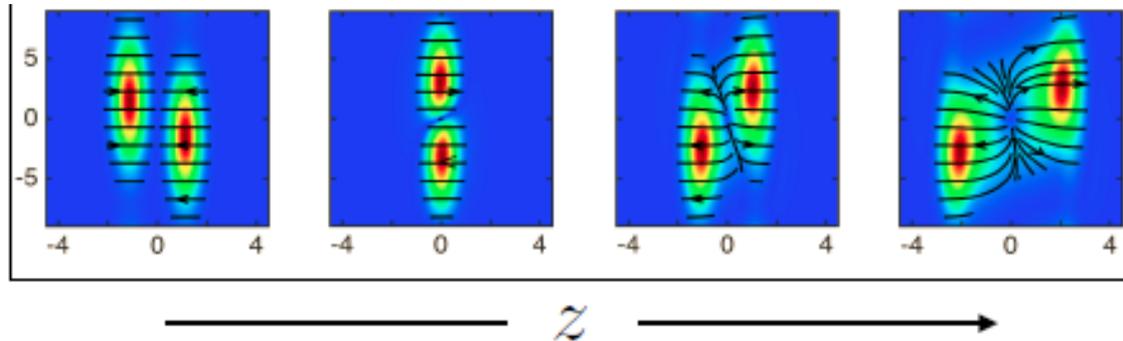


S. Bass

p+A  
collision

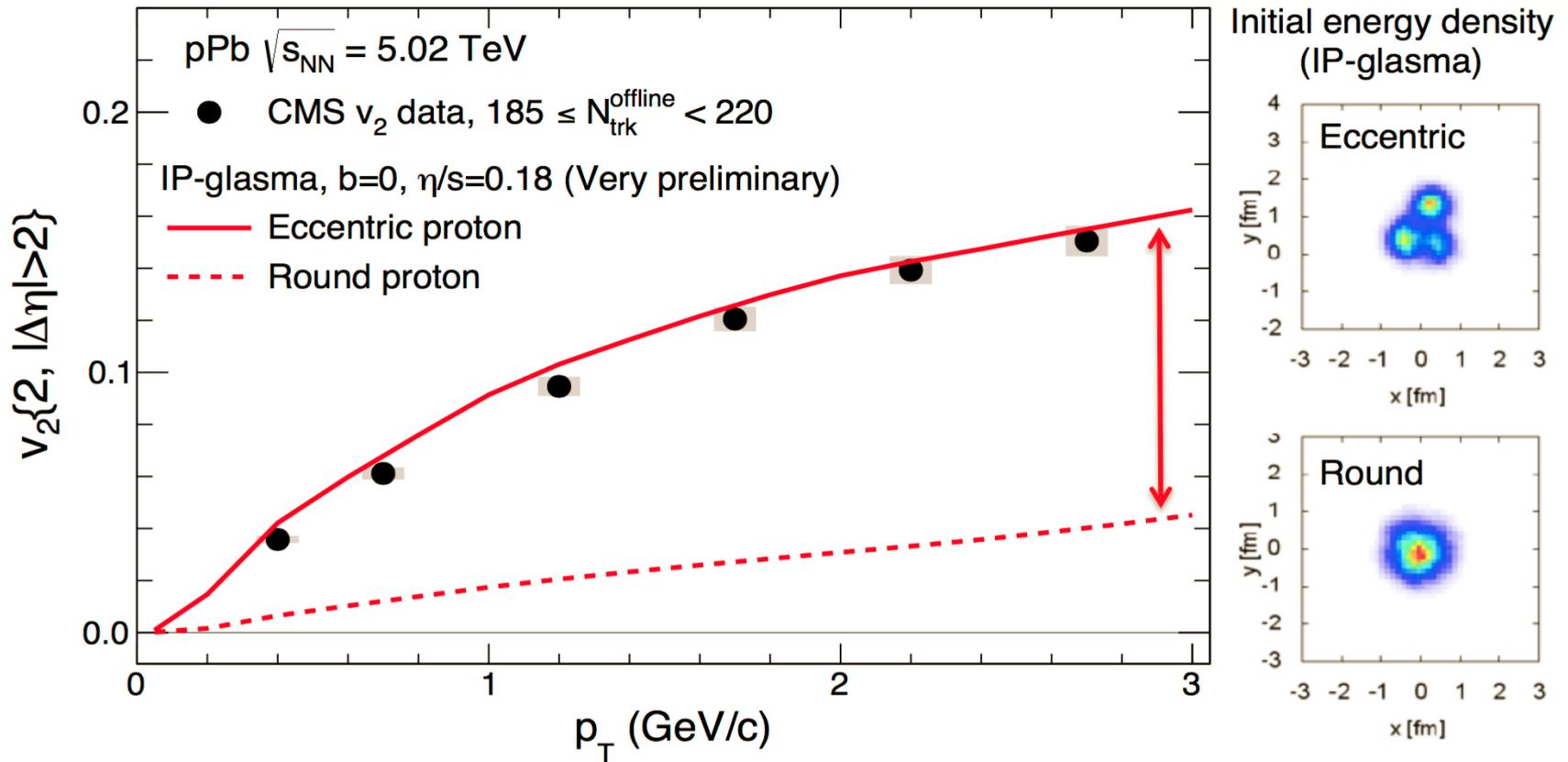


p+p  
collision



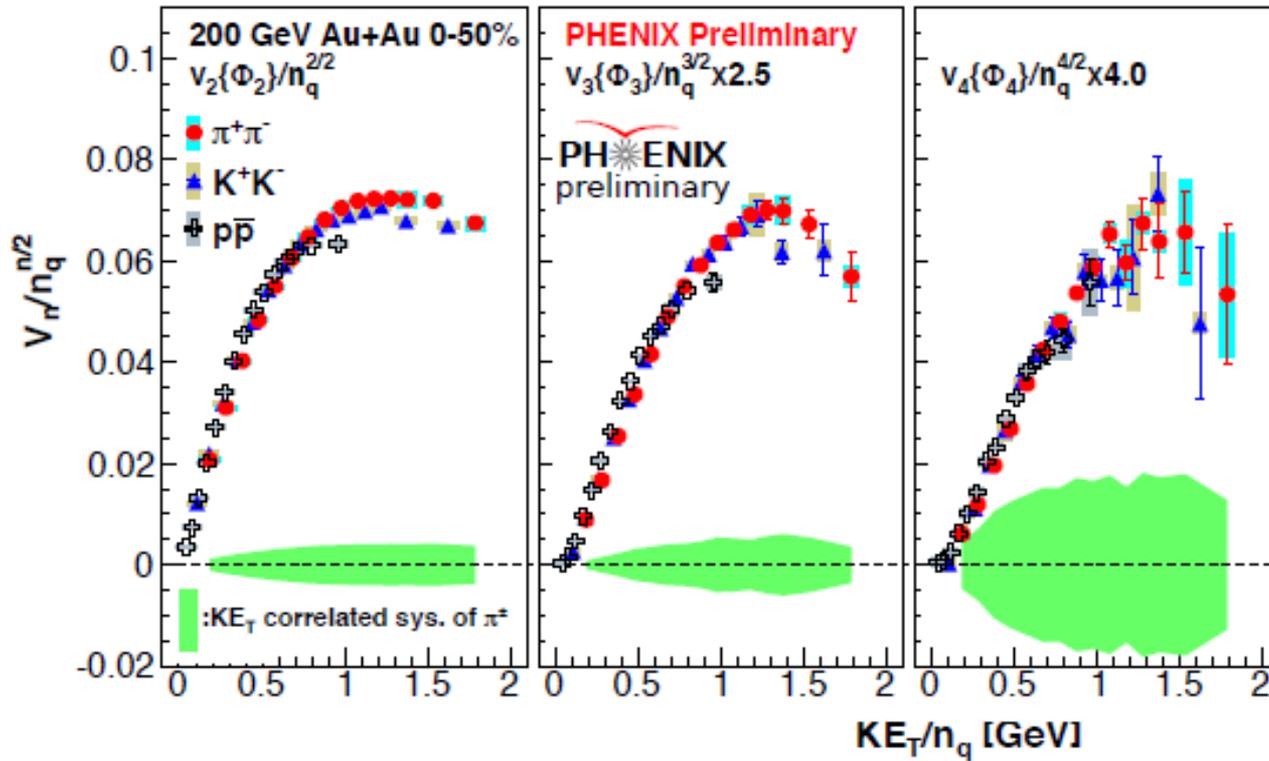
P. Chesler  
Hydrodynamic expansion dynamics for sizes as small as  $RT \sim 1$

➤ **Is hydro-like expansion dynamics maintained with reduced system size, and how do we tell?**



➤ **What is the relevant substructure of the nucleon?  
- valence quarks?**

## $v_n$ PID scaling



Expectation validated:  $v_n(KE_T) \sim v_2^{n/2}$  or  $\frac{V_n}{(n_q)^{n/2}}$

➤ Are valence quark degrees of freedom relevant?

# Strategy

Test for similarities in the particle production mechanism for  $p+p$ ,  $p+A$ ,  $A+A(B)$  collisions  
 $\langle N_{chg} \rangle$  and  $\frac{dN_{chg}}{d\eta}$  scaling

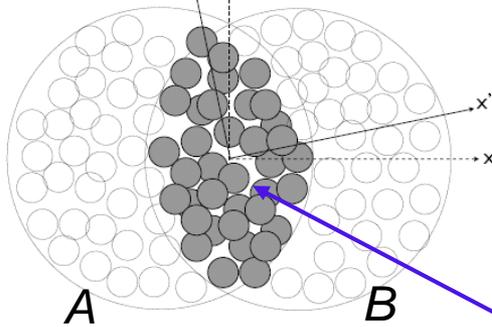
RT  
link

Test for similarities in the expansion dynamics for  $p+p$ ,  $p+A$ ,  $A+A(B)$  collisions  
**Acoustic scaling of  $v_n$**   
**HBT radii, etc**

**The scaling properties of  $\langle N_{chg} \rangle$ ,  $\frac{dN_{chg}}{d\eta}$ ,  $v_n$ , etc can provide key insights**

- ✓ **Scaling coefficients provide crucial constraints for transport coefficients**

## Nucleon Glauber



Phys. Rev. C 81, 061901(R) (2010)

$$S_{nx} \equiv S_n \cos(n\Psi_n^*) = \int d\mathbf{r}_\perp \rho_s(\mathbf{r}_\perp) \omega(\mathbf{r}_\perp) \cos(n\phi)$$

$$S_{ny} \equiv S_n \sin(n\Psi_n^*) = \int d\mathbf{r}_\perp \rho_s(\mathbf{r}_\perp) \omega(\mathbf{r}_\perp) \sin(n\phi),$$

$$\Psi_n^* = \frac{1}{n} \tan^{-1} \left( \frac{S_{ny}}{S_{nx}} \right)$$

$$\varepsilon_n = \langle \cos n(\phi - \Psi_n^*) \rangle$$

$$\frac{1}{\bar{R}} = \sqrt{\left( \frac{1}{\sigma_x^2} + \frac{1}{\sigma_y^2} \right)}$$

$N_{part}$

## Quark Glauber

$n$ - $n$  cross section

$p$ - $p$  profile

✓ Elastic scattering measurements

rms radius

- **Consistency between nucleon and quark Glauber**
- ✓ **Geometric fluctuations included**

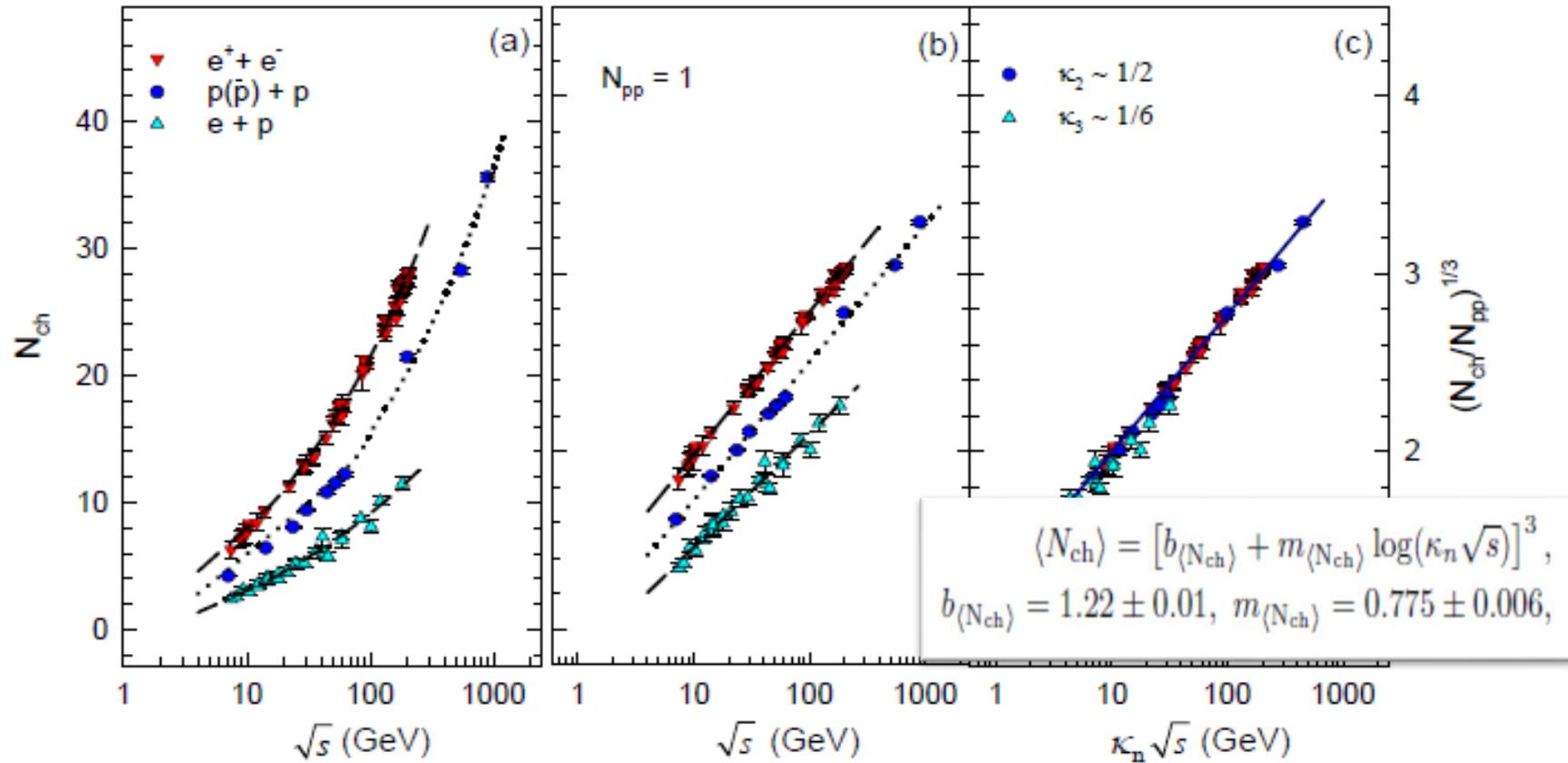
$\sigma_x$  &  $\sigma_y \rightarrow$  RMS widths of density distribution

# $\langle N_{chg} \rangle$ and $\frac{dN_{chg}}{dn}$ scaling

## Operational Ansatz

$$S \sim (TR)^3 \sim \text{const.}, \quad N_{npp, qpp}^{1/3} \propto R \text{ for early-time thermalization}$$

$$\langle N_{chg} \rangle, \frac{dN_{chg}}{dn} \propto S$$

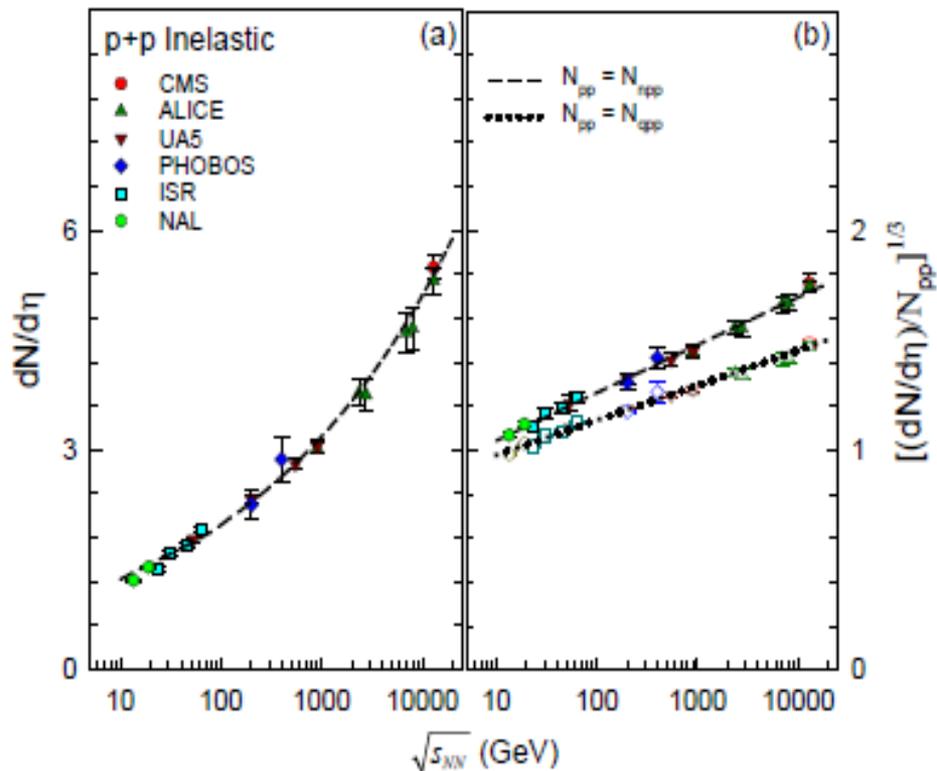


**Scaling validates important role of quark participants**

- ✓ Large fluctuations – leading particle effect
- ✓  $\kappa_{2,3}$  related to number of quark participants

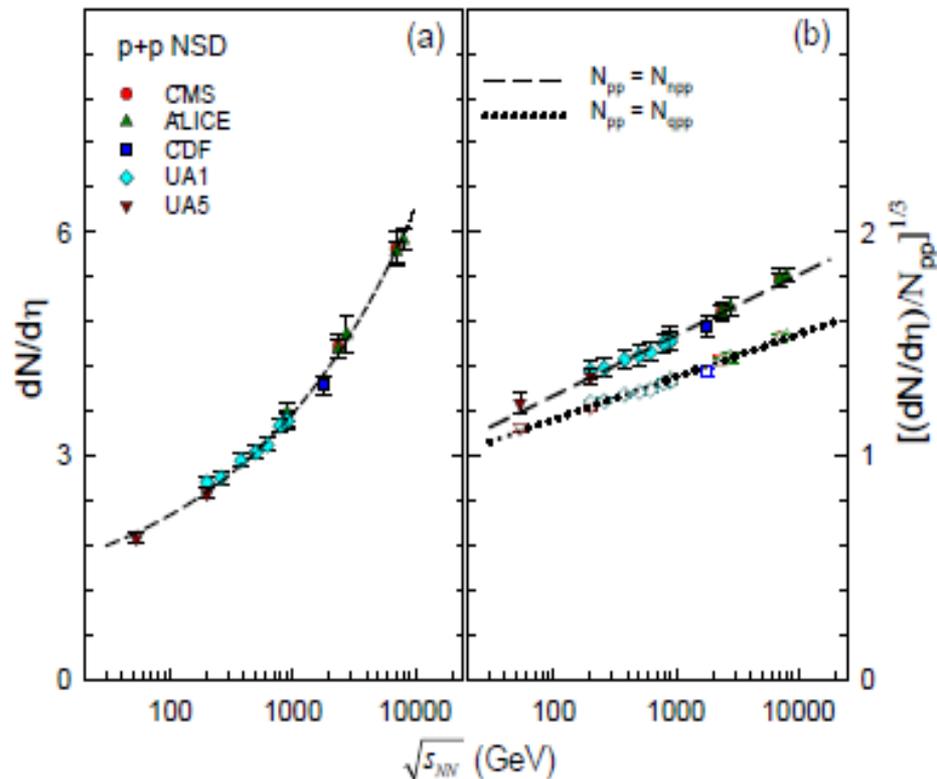
→ fraction of available cm energy

# $\frac{dN_{chg}}{d\eta}$ scaling p+p



$$dN_{ch}/d\eta|_{INE} = [b_{INE} + m_{INE} \log(\sqrt{s_{NN}})]^3,$$

$$b_{INE} = 0.826 \pm 0.008, \quad m_{INE} = 0.220 \pm 0.004,$$



$$dN_{ch}/d\eta|_{NSD} = [b_{NSD} + m_{NSD} \log(\sqrt{s_{NN}})]^3,$$

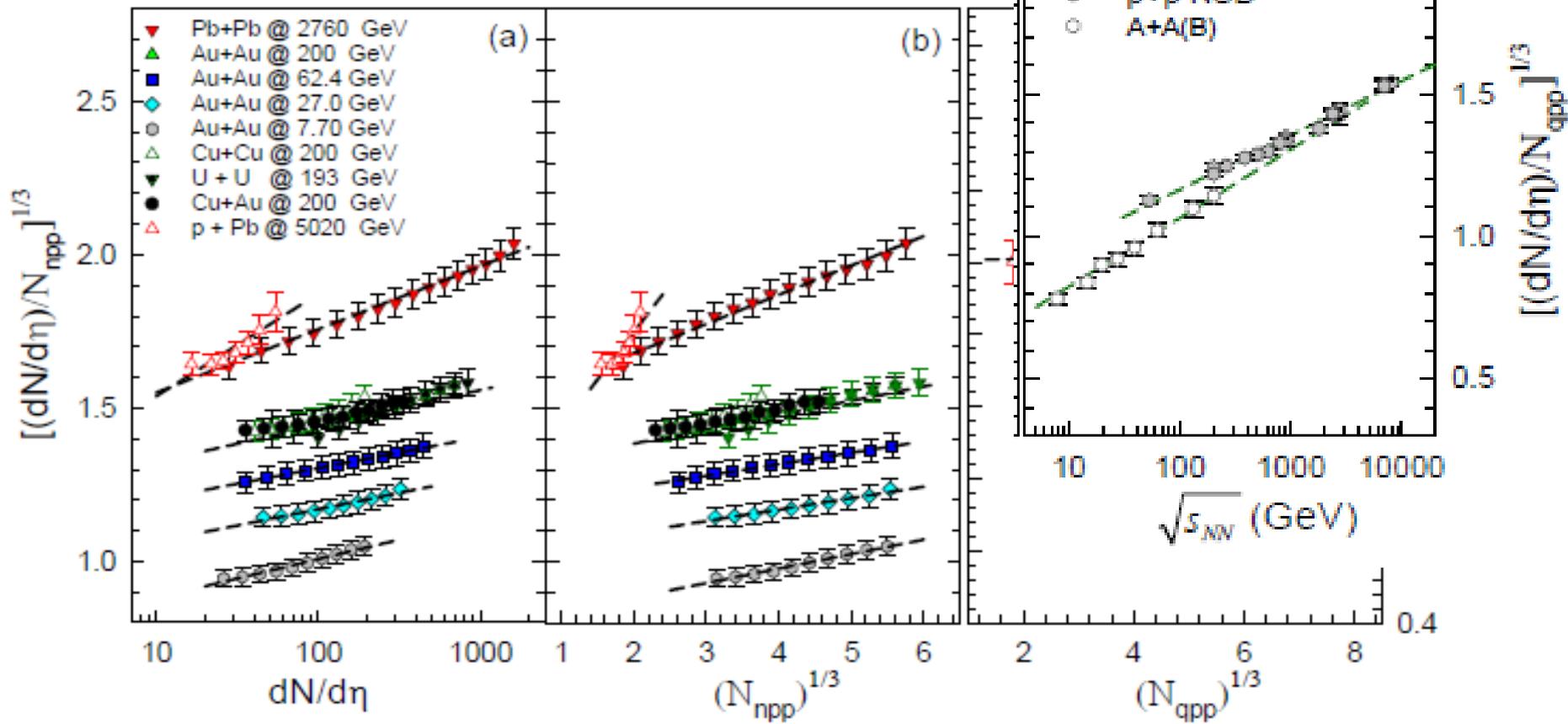
$$b_{NSD} = 0.747 \pm 0.022, \quad m_{NSD} = 0.267 \pm 0.007,$$

**Further scaling validation over full range of  $\sqrt{s_{NN}}$  for p+p**

- ✓ **Similar  $\sqrt{s_{NN}}$  trend for quark and nucleon scaled multiplicity density**

# $\frac{dN_{chg}}{d\eta}$ scaling p+A & A+A(B)

$$S \sim (TR)^3 \sim$$



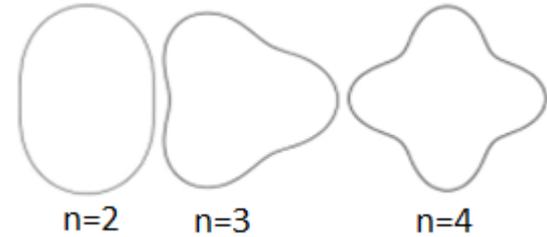
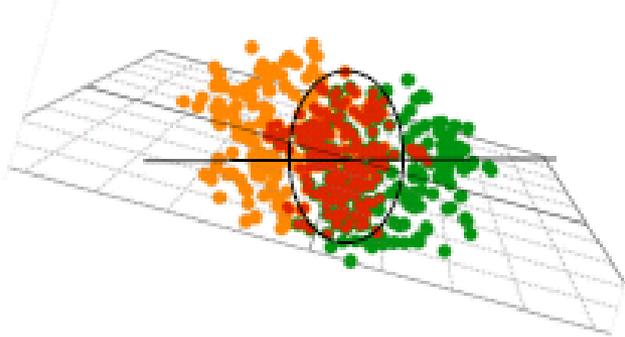
$$dN_{ch}/d\eta|_{|\eta|=0.5} = N_{qpp} [b_{AA} + m_{AA} \log(\sqrt{s})]^3,$$

$$b_{AA} = 0.530 \pm 0.008, \quad m_{AA} = 0.258 \pm 0.004,$$

## Scaling validated for p+A & A+A(B) systems

- ✓ Similar patterns for A+A(B) systems at the same  $\sqrt{s_{NN}}$ .
- ✓ Logarithmic dependence of  $\langle p_T \rangle$  on multiplicity

Flow is acoustic



$$\frac{dN}{d\phi} \propto \left( 1 + 2 \sum_{n=1} v_n \cos[n(\phi - \Psi_n)] \right)$$

$$k = n / \bar{R}$$

$$t \propto \bar{R}$$

Acoustic viscous modulation of  $v_n$

$$\delta T_{\mu\nu}(t, k) = \exp\left(-\frac{2}{3} \frac{\eta}{s} k^2 \frac{t}{T}\right) \delta T_{\mu\nu}(0)$$

Staig & Shuryak arXiv:1008.3139

$$\delta T_{\mu\nu}(n, t) = \exp(-\beta n^2) \delta T_{\mu\nu}(0), \quad \beta = \frac{2}{3} \frac{\eta}{s} \frac{1}{\bar{R}^2} \frac{t}{T}$$

Scaling expectations:

$n^2$  dependence

$$\left( \frac{v_n(p_T)}{\epsilon_n} \right) \propto \exp\left(-\frac{\beta'}{RT} n^2\right)$$

Straightforward to include bulk viscosity

$v_n$  's are related

$$\frac{(v_n(p_T))^{1/n}}{(v_{n'}(p_T))^{1/n'}} \sim \frac{(\epsilon_{n'})^{1/n'}}{(\epsilon_n)^{1/n}} \cdot \exp\left(-\frac{\beta'}{RT} (n - n')\right)$$

System size dependence

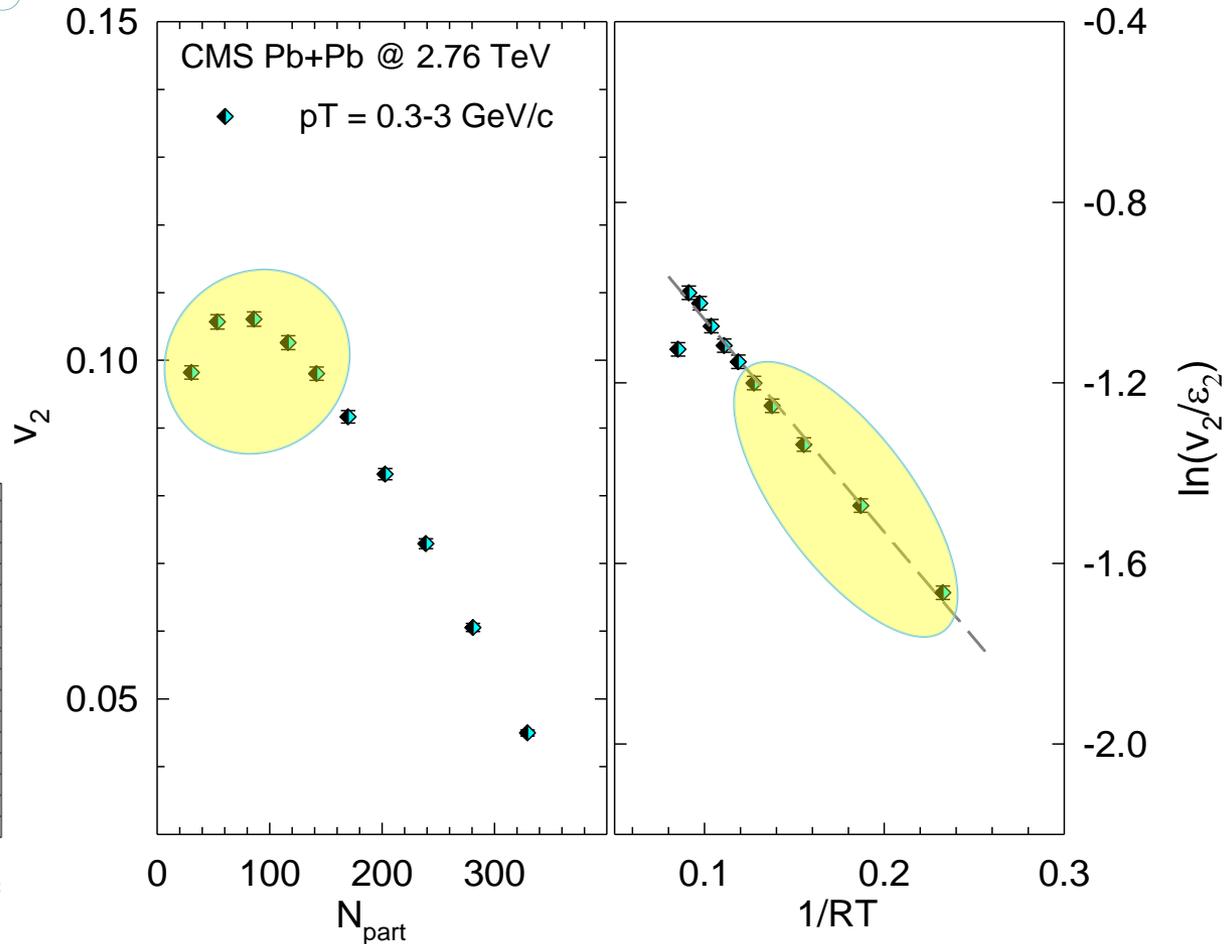
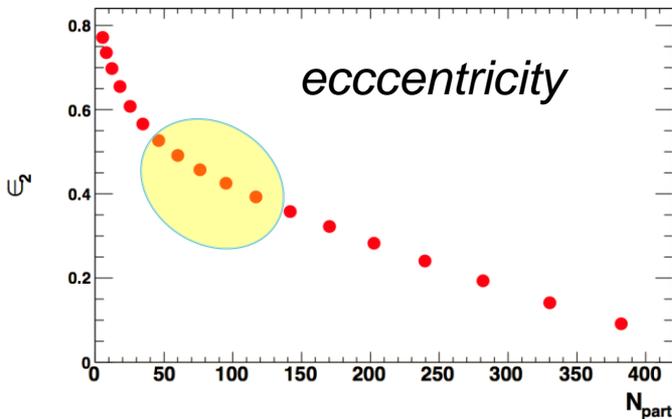
$$\ln\left(\frac{v_n}{\epsilon_n}\right) \propto \frac{-\beta''}{RT}$$

The factors which influence anisotropic flow – well understood

# Acoustic Scaling – RT

$$\ln \left( \frac{v_n}{\varepsilon_n} \right) \propto \frac{-\beta''}{RT}$$

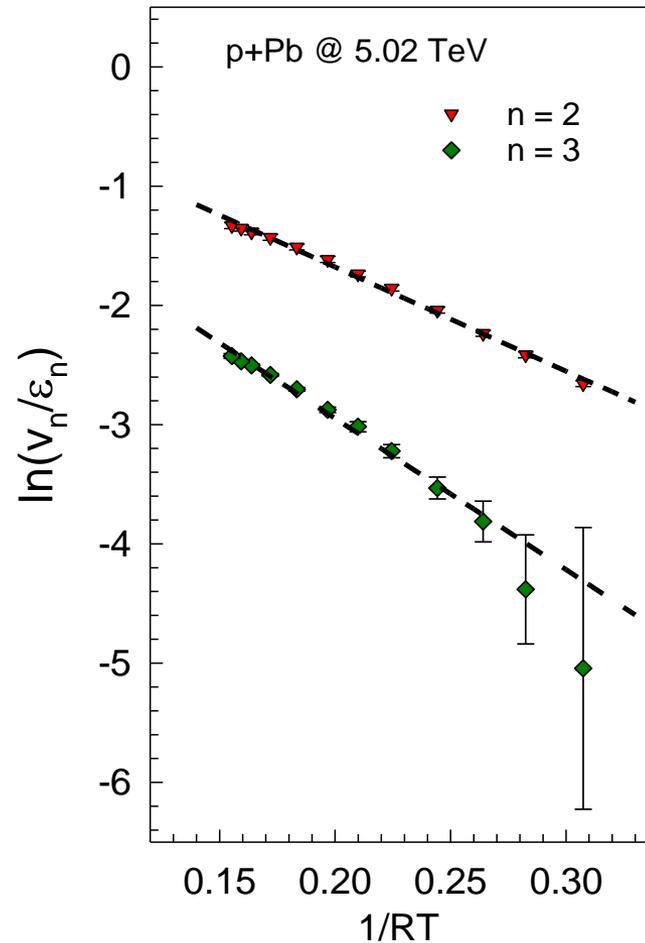
$$RT \propto \left( \frac{dN_{chg}}{d\eta} \right)^{1/3}$$



➤ **Eccentricity change alone is not sufficient**

- ✓ **Characteristic 1/(RT) viscous damping validated**
- ✓ **Similar patterns for other  $p_T$  selections**
- ✓ **Important constraint for  $\eta/s$  &  $\zeta/s$**

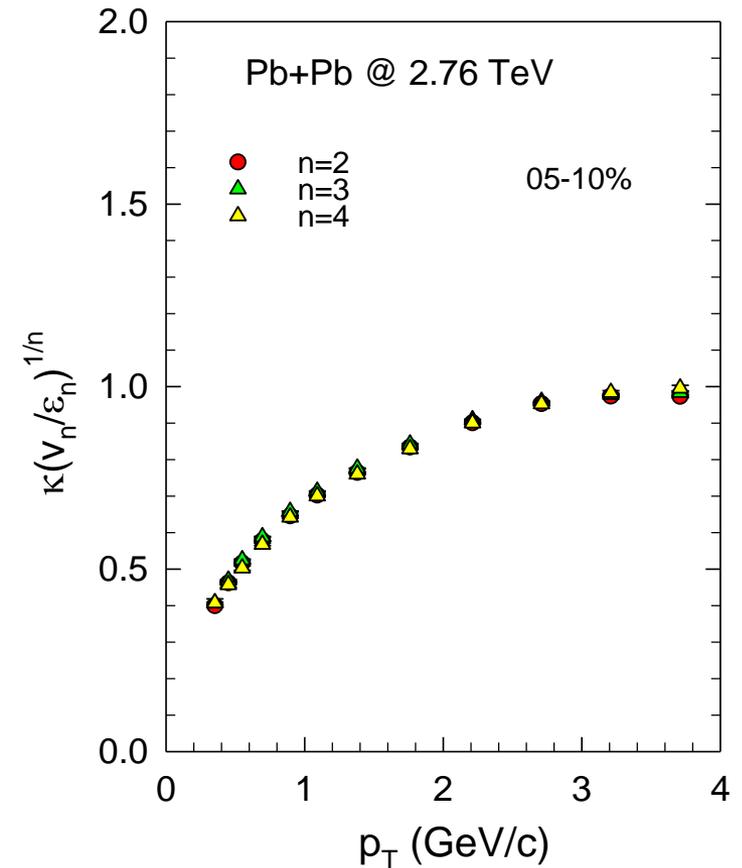
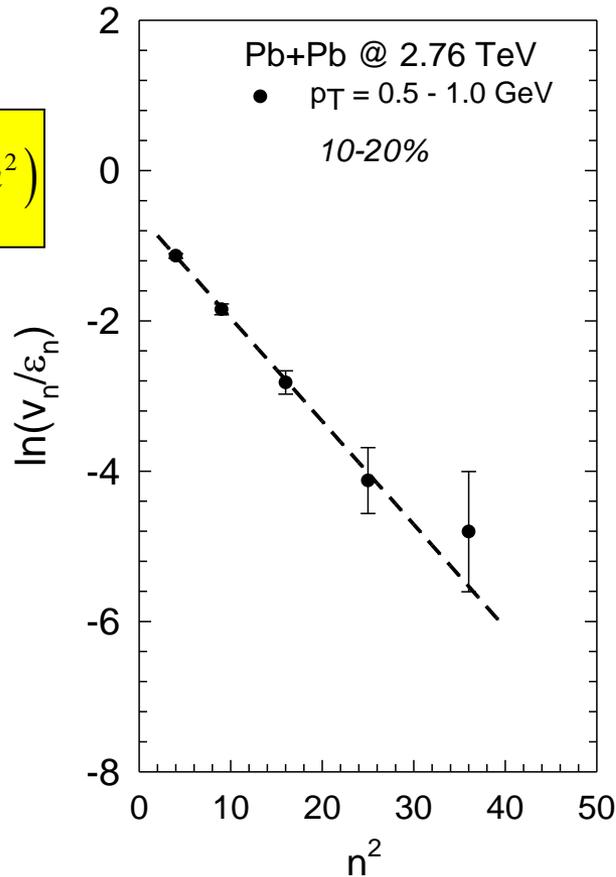
$$\ln\left(\frac{v_n}{\varepsilon_n}\right) \propto \frac{-\beta''}{RT}$$
$$RT \propto \left(\frac{dN_{chg}}{d\eta}\right)^{1/3}$$



- ✓ **Characteristic  $1/(RT)$  viscous damping validated**
- ✓ **Important constraint for  $\eta/s$  &  $\zeta/s$**

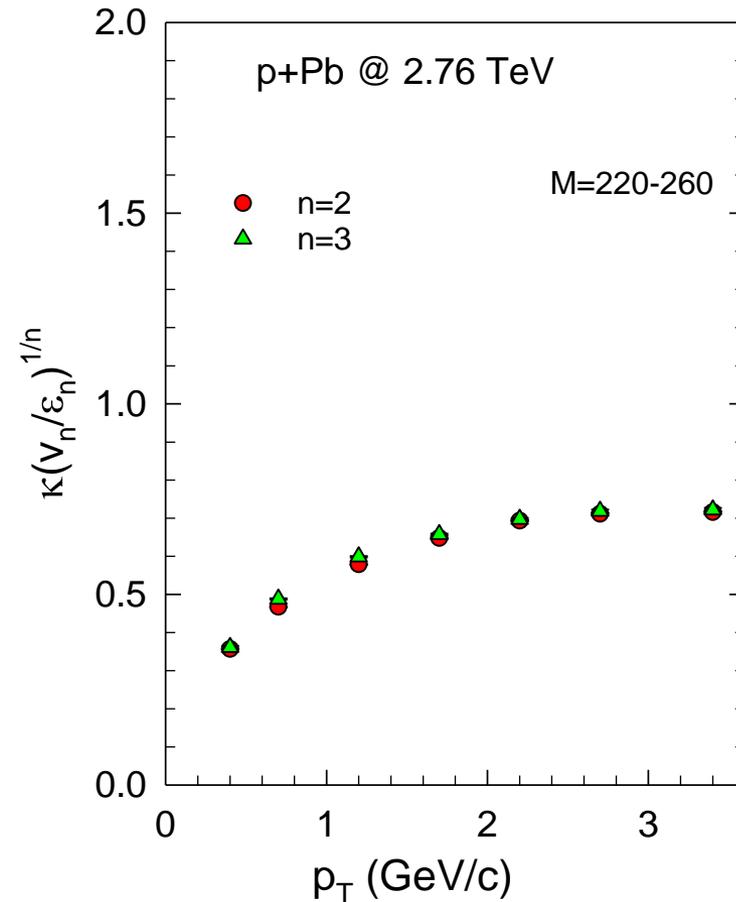
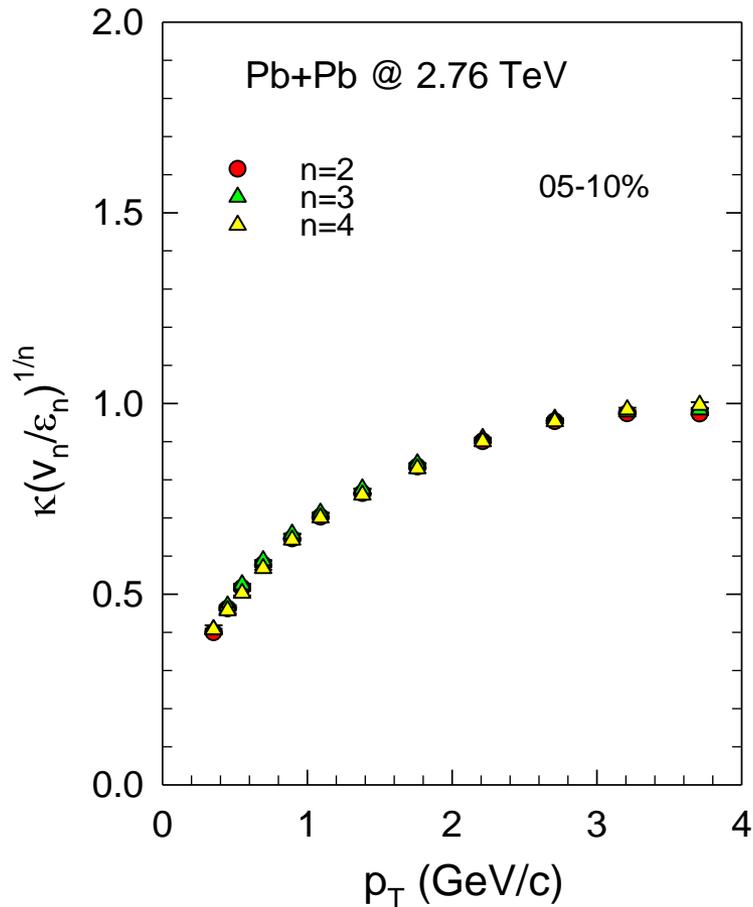
$$\left(\frac{v_n(p_T)}{\varepsilon_n}\right)^{1/n} \propto \exp(-\beta' n)$$

$$\left(\frac{v_n}{\varepsilon_n}\right) \propto \exp(-\beta' n^2)$$



- ✓ **Characteristic  $n^2$  viscous damping validated**
- ✓ **Similar patterns for other centrality selections**
- ✓ **Important constraint for  $\eta/s$  &  $\zeta/s$**

## System-size dependence



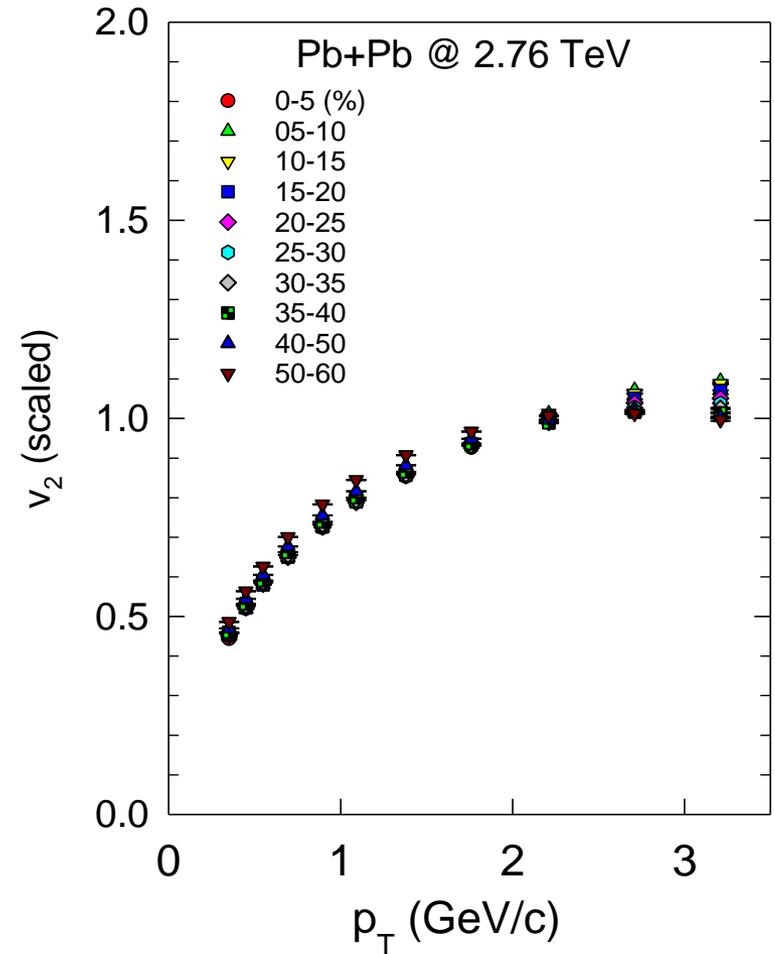
- ✓ **Similar acoustic patterns for p+Pb and Pb+Pb**
- ✓ **Similar results for other small systems**

### **No fundamental change in the particle production mechanism and expansion dynamics, with reduced system size**

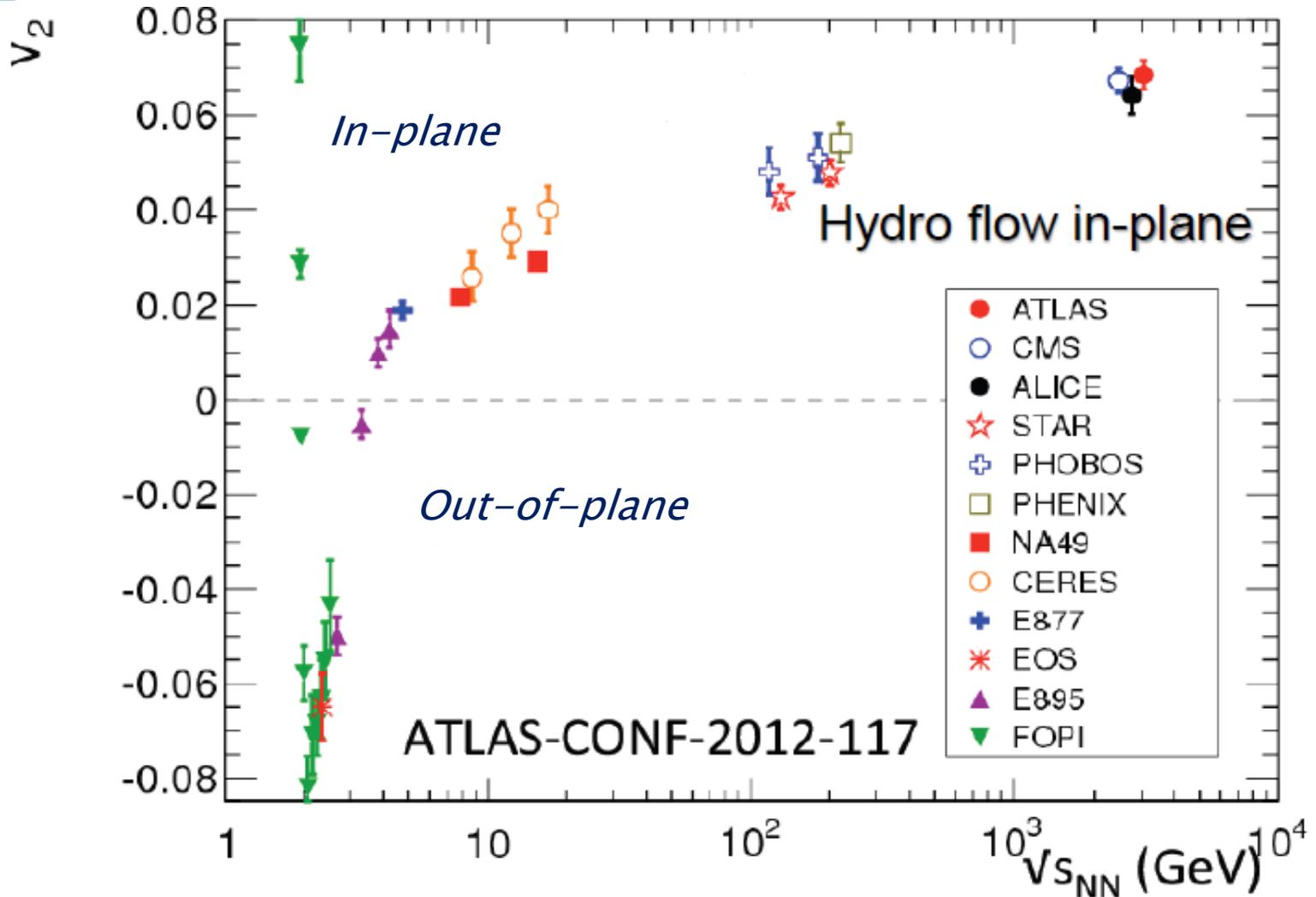
- **Similar particle production mechanism for large (A+A(B)) and small (p+p, p+A) system**
  - ✓  $\langle N_{chg} \rangle$  and  $\frac{dN_{chg}}{d\eta}$  scaling over  $\sim$  four orders of magnitude *in*  $\sqrt{s_{NN}}$
  - ✓ **Important role for quark participants**
- **Similar Acoustic dynamics validated in “large” and “small” systems**
  - ✓ **Strong evidence for the important role of final-state interactions.**
  - ✓ **Important constraints for transport coefficients**

**Acoustic dynamics fully predictable for other systems and energies**

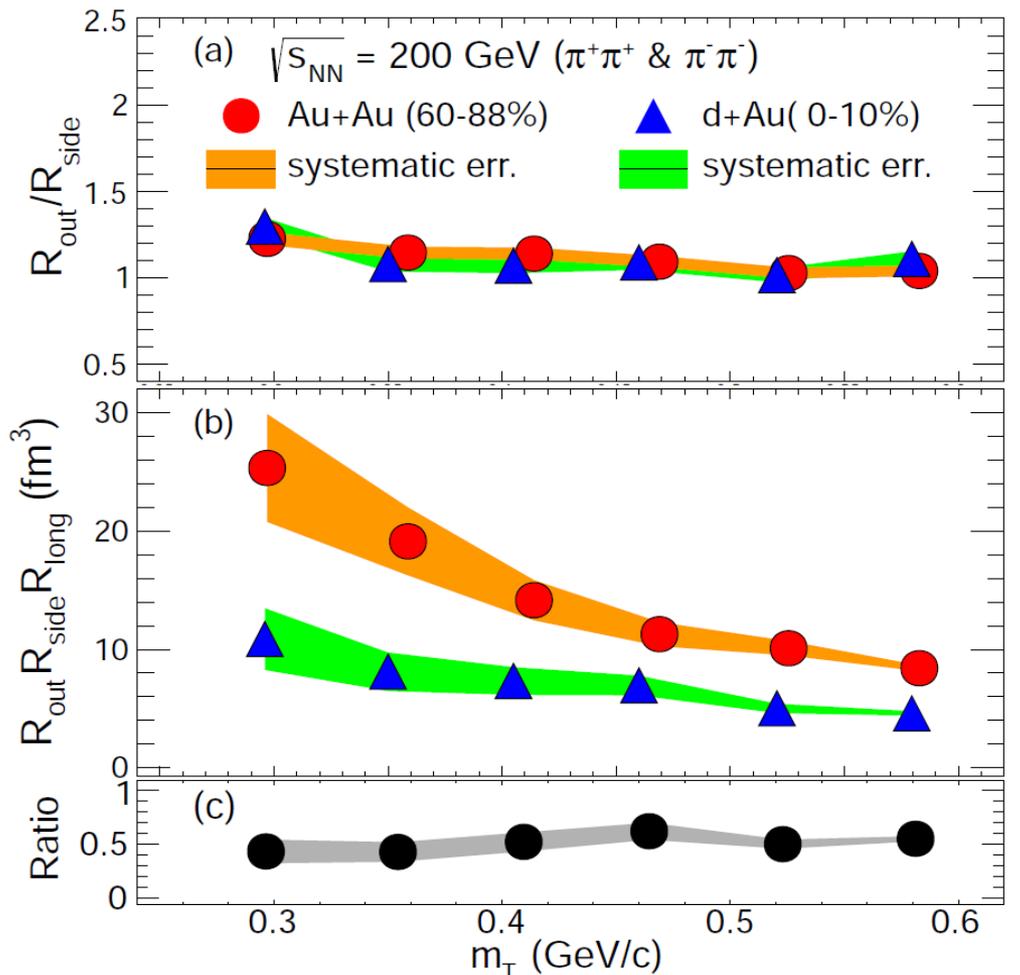
***End***



✓ *Combined scaling understood*



# Comparison of Au+Au and d+Au collisions – $m_T$ dependence



$$R_{out}^2 = \frac{R_{geom}^2}{1 + \frac{m_T}{T} v^2} + \frac{1}{2} \left( \frac{T}{m_T} \right)^2 \beta_T^2 \tau_0^2$$

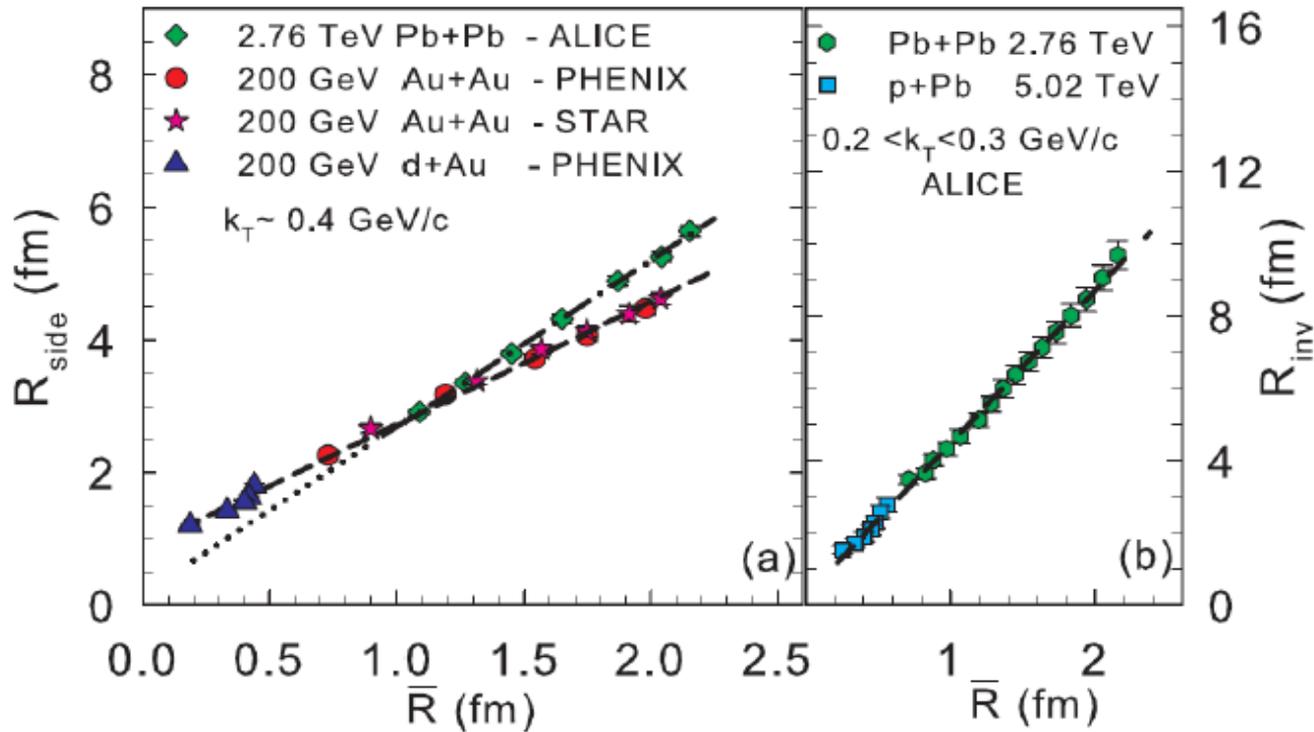
$$R_{side}^2 = \frac{R_{geom}^2}{1 + \frac{m_T}{T} v^2}$$

$$\frac{R_{out}}{R_{side}} \propto \Delta \tau$$

Similar  $m_T$  dependence for Both systems

d+Au indicates a smaller freeze-out volume!

## Scaling of the transverse radii



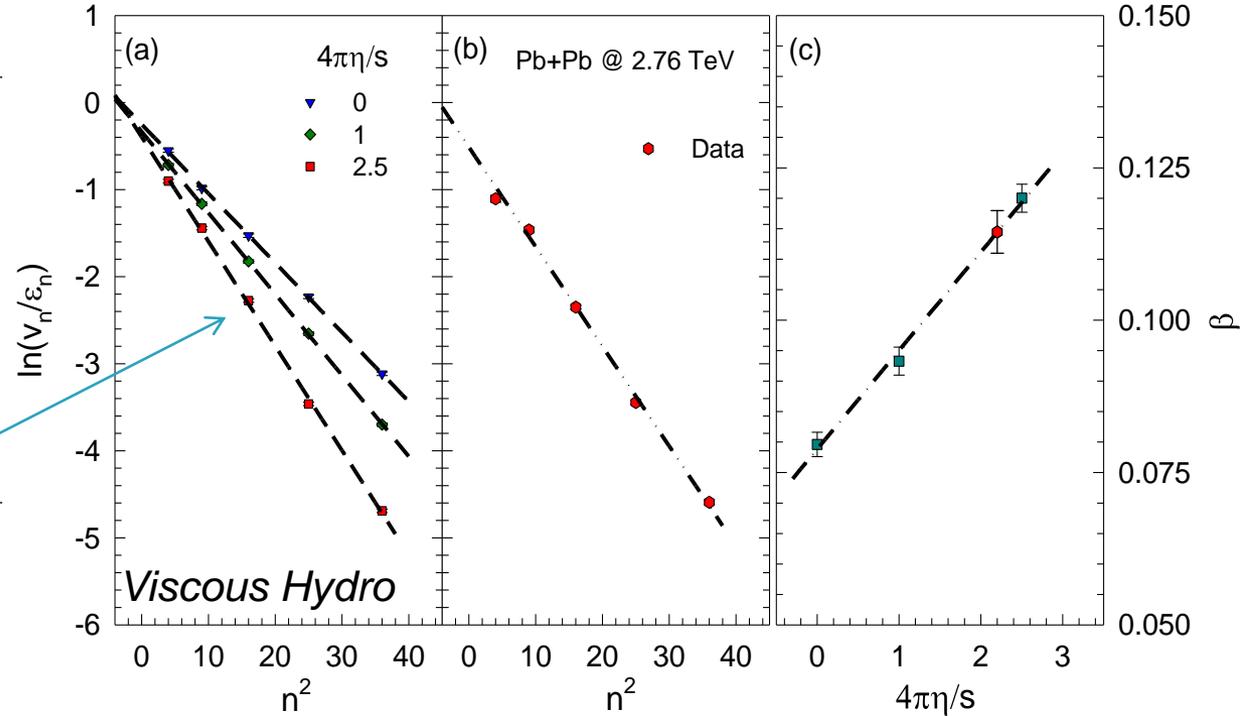
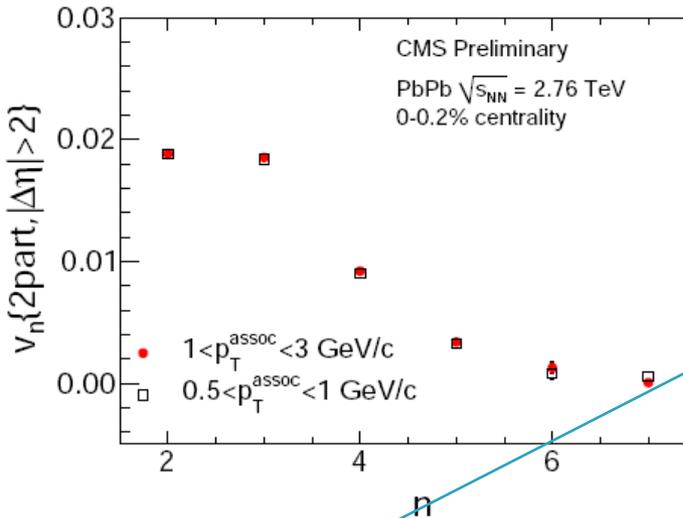
**d+Au, Cu+Cu and Au+Au radii scale for the same beam energy**

- Expansion dynamics of the d+Au system appears to be strongly influenced by final state effects
- Larger expansion rate at the LHC

# Extraction of $\eta/s$

$$\frac{v_n(p_T)}{\varepsilon_n} \propto \exp(-\beta' n^2)$$

arXiv:1301.0165 & CMS PAS HIN-12-011



Slope sensitive to  $\eta/s$

**Characteristic  $n^2$  viscous damping validated in viscous hydrodynamics; calibration  $\rightarrow 4\pi\eta/s \sim 2.2 \pm 0.2$**   
**Extracted  $\eta/s$  value (LHC) insensitive to initial conditions**