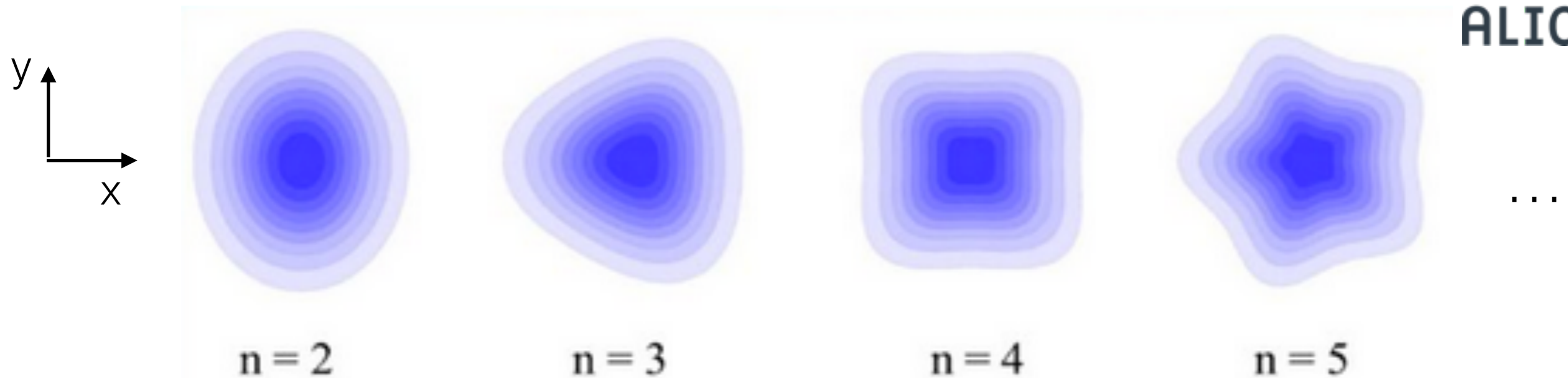


# Measurement of higher harmonic flow coefficients of identified hadrons in Pb-Pb collisions at $\sqrt{s_{NN}}=2.76$ TeV

**Naghmeh Mohammadi**  
**Nikhef**  
for the **ALICE Collaboration**  
results in arXiv: 1606.06057





Flow harmonics are sensitive to:

- Initial conditions
- Transport properties ( $\eta/s$ )

For different particle species, probe in addition:

- Effects of hadronisation mechanism, e.g. quark coalescence
- Effects of hadronic rescattering

$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T d\eta} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n(p_T, \eta) \cos[n(\varphi - \Psi_n)] \right\}$$

$$v_n = \langle \cos[n(\varphi - \Psi_n)] \rangle$$

azimuthal angle

symmetry plane angle

$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T d\eta} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n(p_T, \eta) \cos[n(\varphi - \Psi_n)] \right\}$$

Scalar product method:

azimuthal angle

symmetry plane angle

$$v_n^a(p_T) = \frac{\left\langle \left\langle \vec{u}_n^k(p_T) \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle_{k \in a} \right\rangle}{\sqrt{\left\langle \frac{\vec{Q}_n^a}{M^a} \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle}}$$

M: Multiplicity

$$\vec{Q}_n = \sum_{k \in RP}^M e^{in\varphi_k}$$

total flow vector

u: unit flow vector

$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T d\eta} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n(p_T, \eta) \cos[n(\varphi - \Psi_n)] \right\}$$

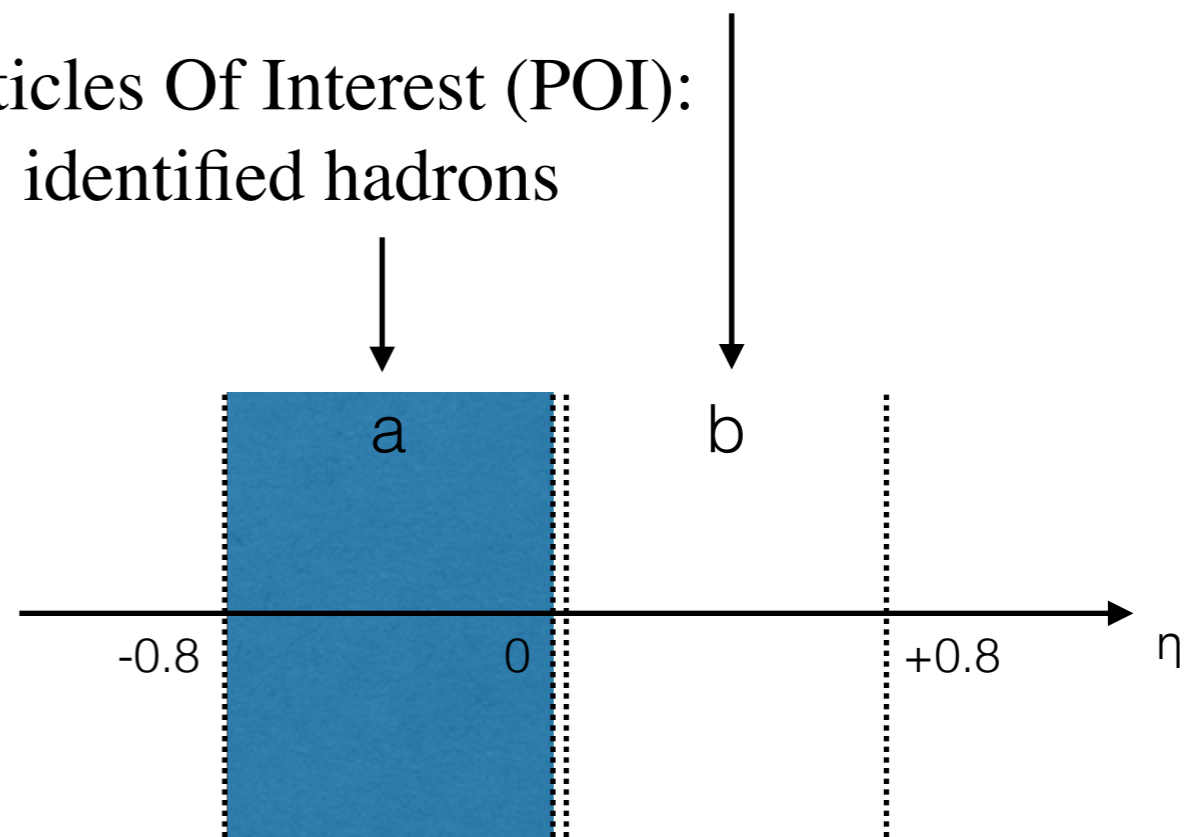
Scalar product method:

$$v_n^a(p_T) = \frac{\left\langle \left\langle \vec{u}_n^k(p_T) \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle_{k \in a} \right\rangle}{\sqrt{\left\langle \frac{\vec{Q}_n^a}{M^a} \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle}}$$

No  $\eta$  gap non-overlapping subevents

Reference Particles (RP):  
charged particles

Particles Of Interest (POI):  
identified hadrons



TPC acceptance

$$E \frac{d^3N}{dp^3} = \frac{1}{2\pi} \frac{d^2N}{p_T dp_T d\eta} \left\{ 1 + 2 \sum_{n=1}^{\infty} v_n(p_T, \eta) \cos[n(\varphi - \Psi_n)] \right\}$$

Scalar product method:

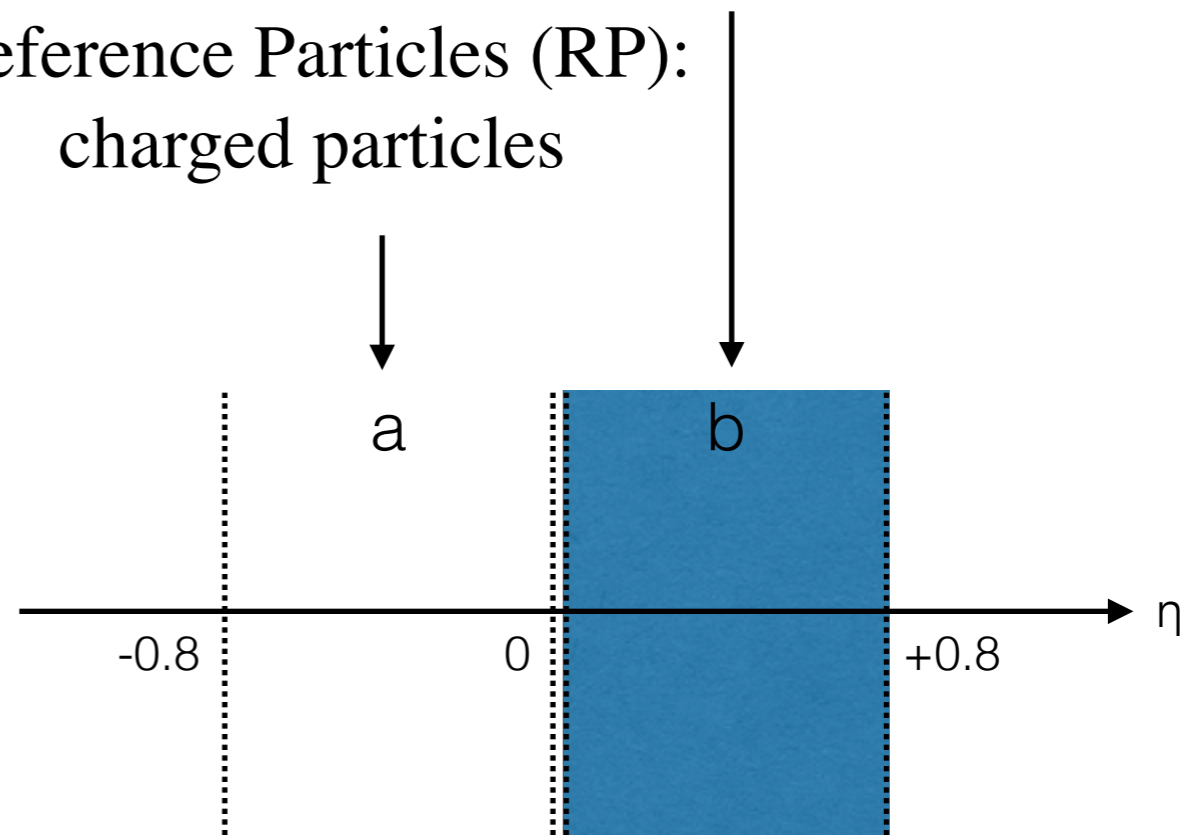
$$v_n^b(p_T) = \frac{\left\langle \left\langle \vec{u}_n^k(p_T) \cdot \frac{\vec{Q}_n^{a*}}{M^b} \right\rangle_{k \in b} \right\rangle}{\sqrt{\left\langle \frac{\vec{Q}_n^a}{M^a} \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle}}$$

No  $\eta$  gap non-overlapping subevents

$v_n =$  Average of  $v_n^a$  and  $v_n^b$

Particles Of Interest (POI):  
identified hadrons

Reference Particles (RP):  
charged particles



TPC acceptance

2-particle azimuthal correlation  $\left\{ \begin{array}{l} \text{Anisotropic flow} \\ \text{Resonance decays, jets a.k.a. non-flow} \end{array} \right.$

Subtract non-flow estimate:

- $v_n^{\text{sub}}(p_T) = v_n^{\text{AA}}(p_T) - \delta_n^{\text{AA,pp}}(p_T)$
- $v_n^{\text{AA}}$ : flow coefficients measured in Pb-Pb collisions
- $\delta_n^{\text{AA,pp}}$ : estimate of non-flow  $\longrightarrow$  from pp + Pb-Pb events
  - Assumption: scales with  $1/M$

$$\delta_n^{(a)\text{AA,pp}}(p_T) = \frac{\langle M \rangle^{\text{PP}} \left\langle \left\langle \vec{u}_n^k(p_T) \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle_{k \in a} \right\rangle^{\text{PP}}}{\langle M \rangle^{\text{AA}} \sqrt{\left\langle \frac{\vec{Q}_n^a}{M^a} \cdot \frac{\vec{Q}_n^{b*}}{M^b} \right\rangle^{\text{AA}}}}$$

# Analysis Details

**Data sample:**

- Pb-Pb at  $\sqrt{s_{NN}}=2.76$  TeV

**Trigger:**

- 0-10% (central),
- 10-50% (SemiCentral)

**Statistics:**

- 25M events analysed

**Data sample:**

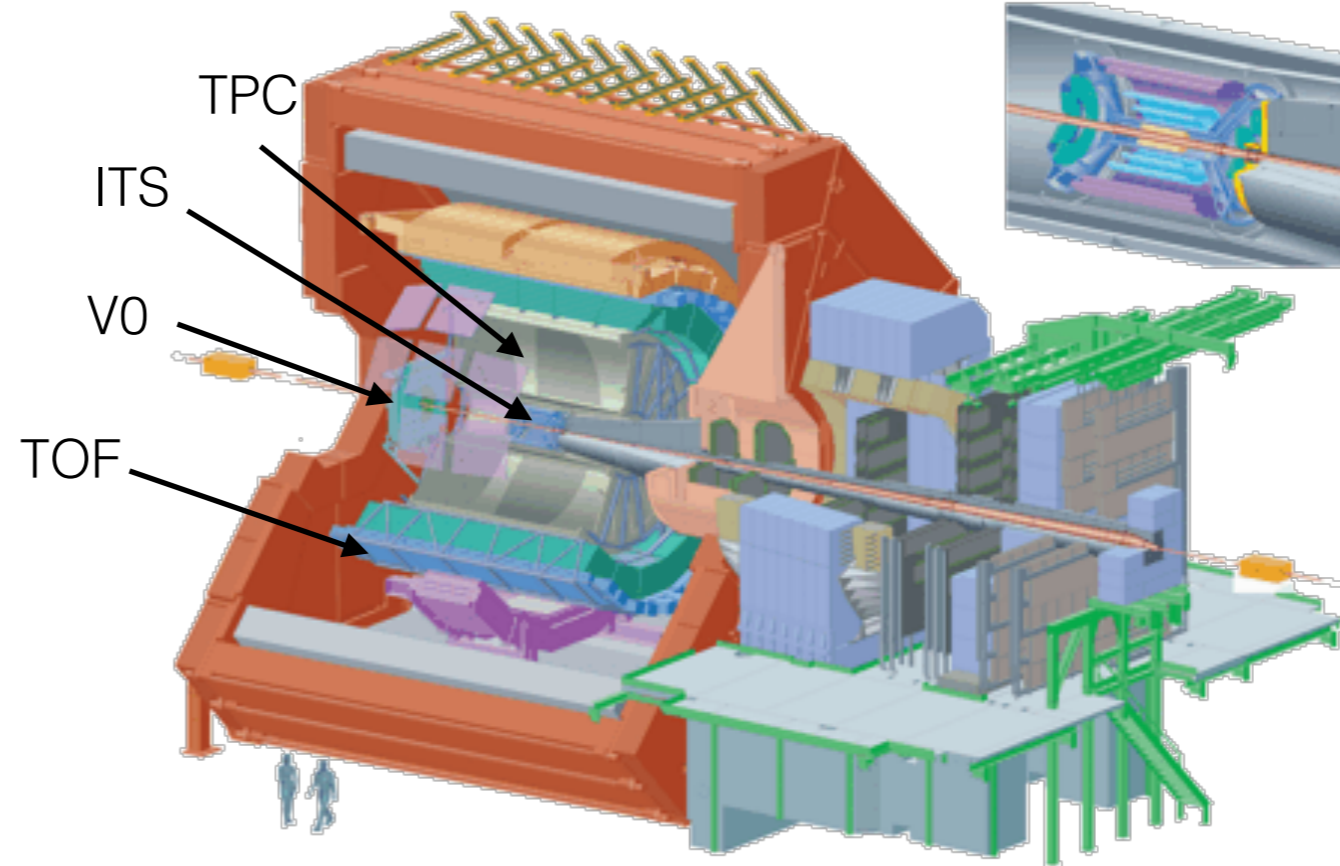
- pp at  $\sqrt{s_{NN}}=2.76$  TeV

**Trigger:**

- Minimum bias

**Statistics:**

- 20M events analysed



Tracks used:  $-0.8 < \eta < 0.8$

Particles of interest (POI):

- $\pi^\pm$ ,  $K^\pm$ ,  $p(\bar{p})$

Reference Particles (RP):

- All charged particles

POI  $p_T$  range:

- $\pi^\pm$ :  $0.3 < p_T < 6$  GeV/c

- $K^\pm$ :  $0.3 < p_T < 4$  GeV/c

- $p(\bar{p})$ :  $0.4 < p_T < 6$  GeV/c

RP  $p_T$  range:

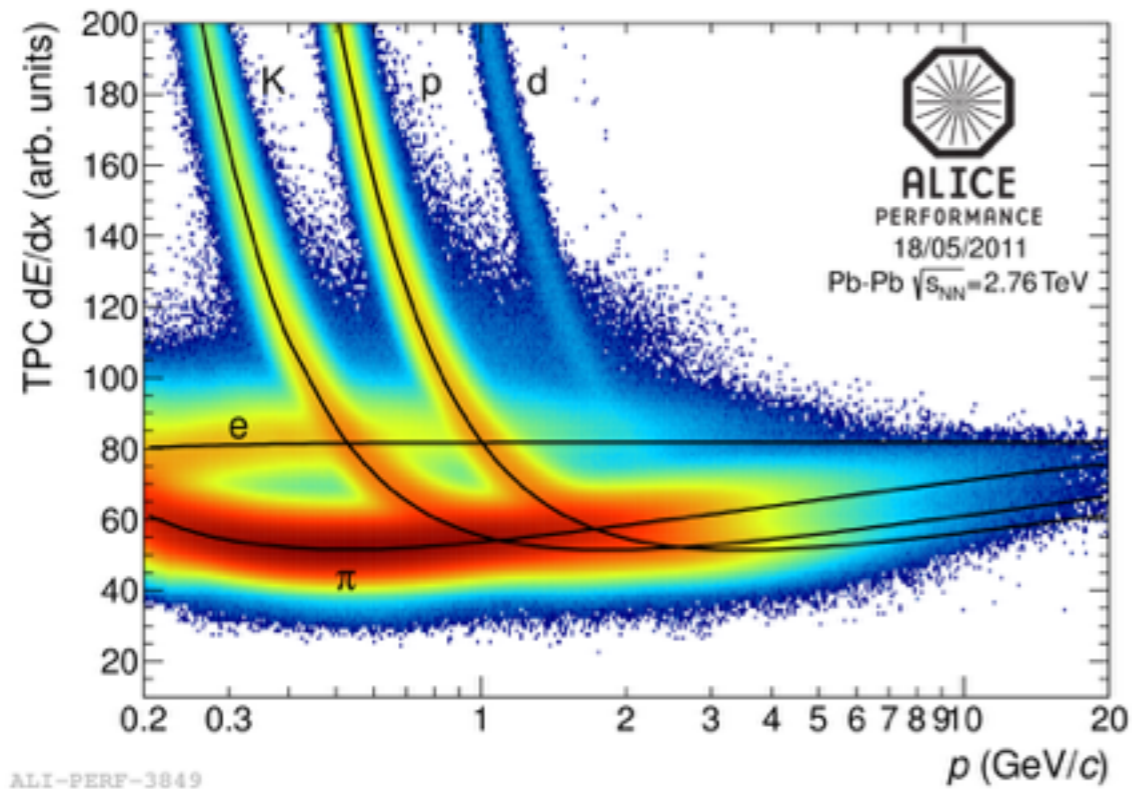
- $0.2 < p_T < 5$  GeV/c



## Time Projection Chamber (TPC)

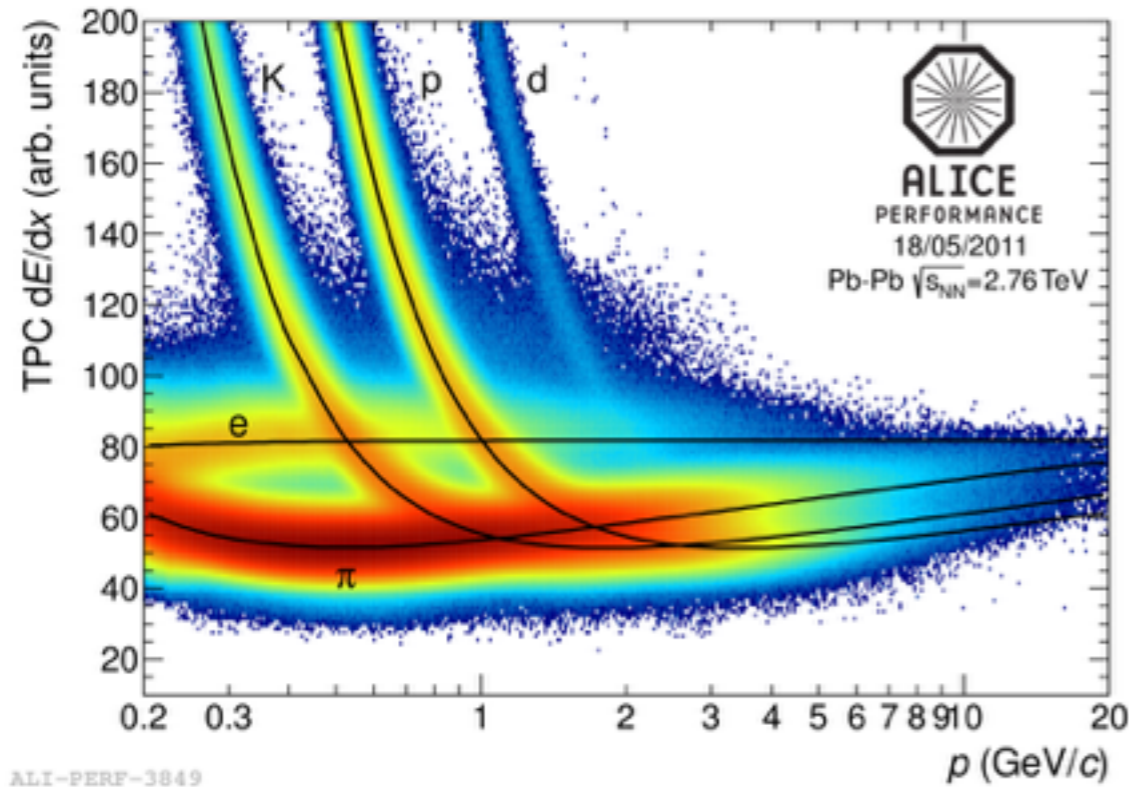
$dE/dx$  : the specific energy loss

Resolution:  $\sigma_{dE/dx} \approx 5\%$



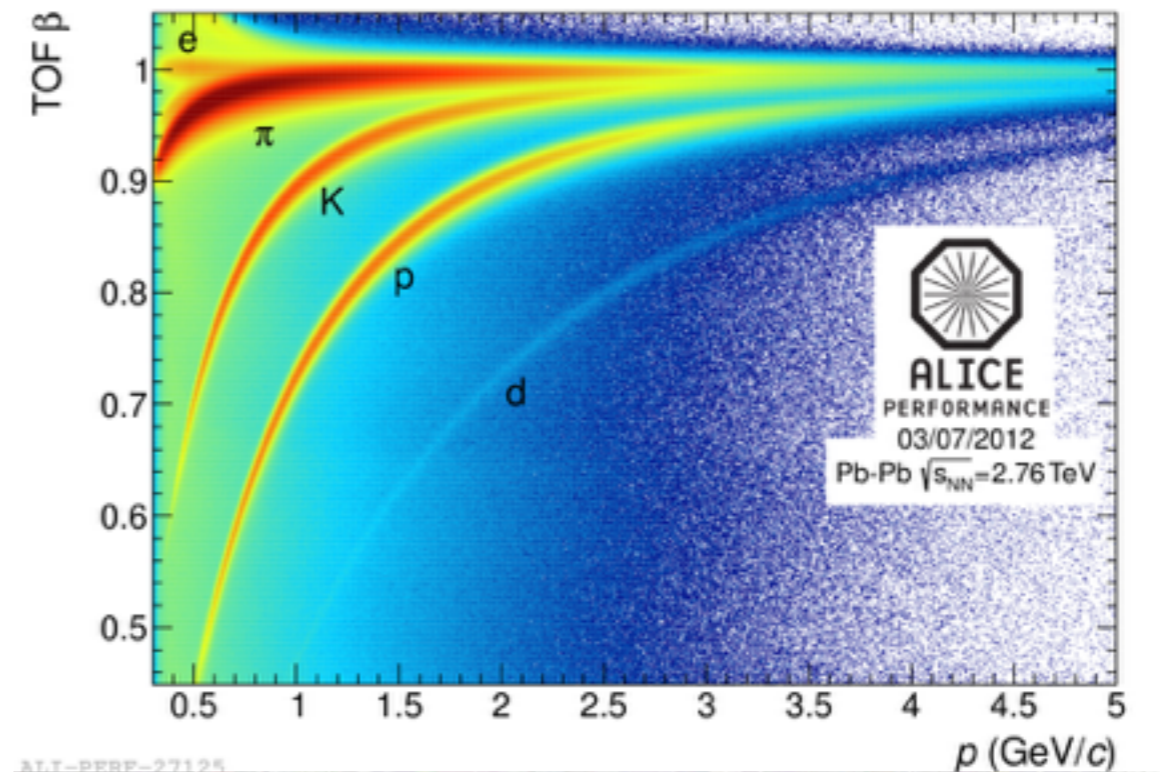
## Time Projection Chamber (TPC)

$dE/dx$  : the specific energy loss  
 Resolution:  $\sigma_{dE/dx} \approx 5\%$



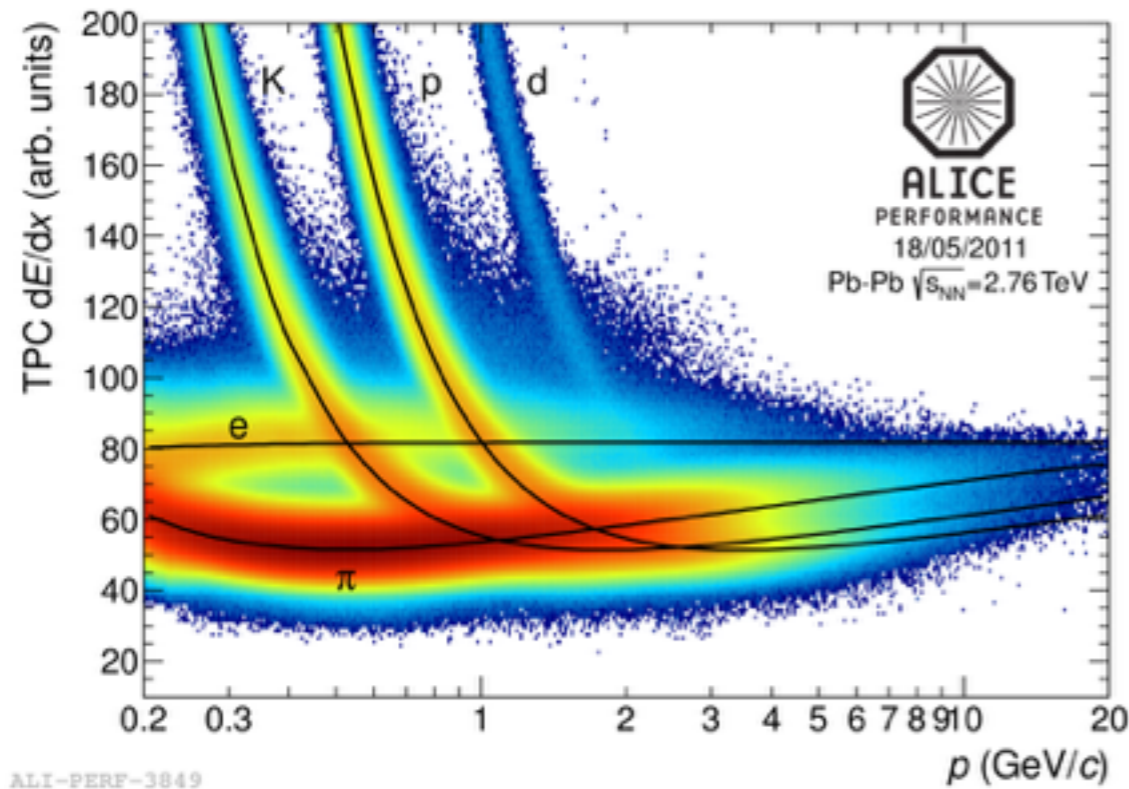
## Time of Flight (TOF)

$\beta$  = Track length/arrival time  
 Resolution:  $\sigma_{\text{TOF}} \approx 86\text{ ps}$  for Pb-Pb collisions



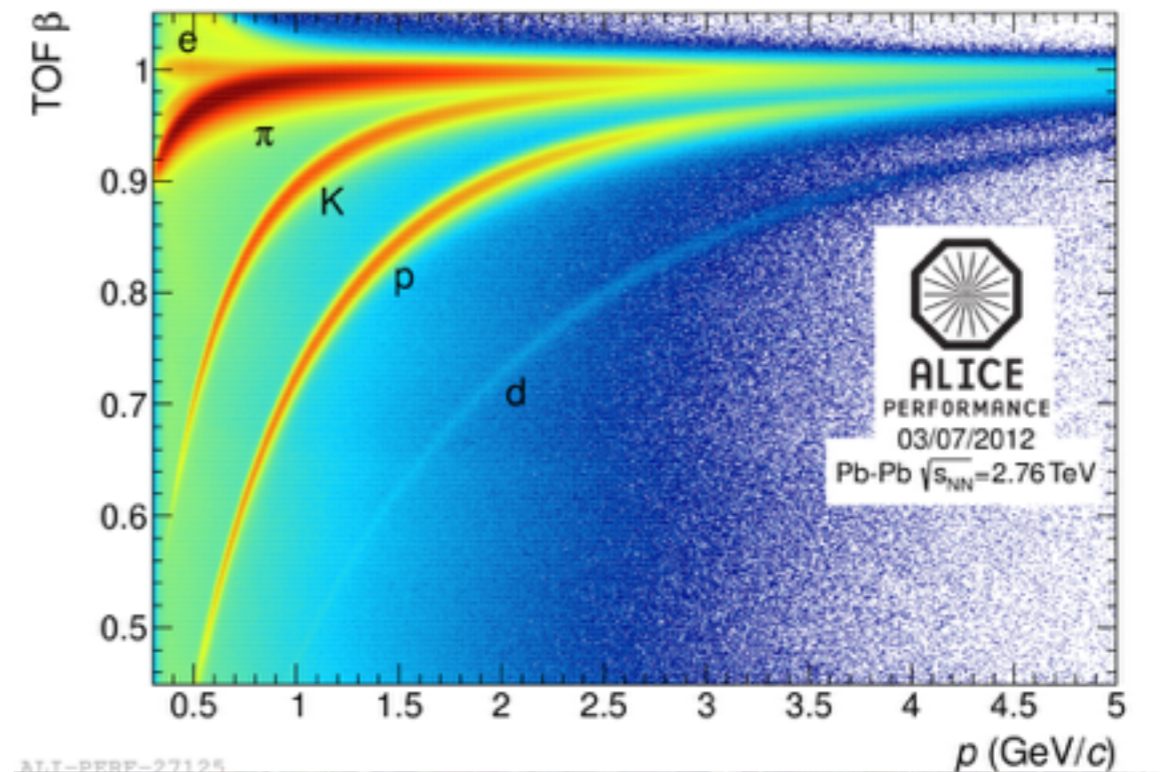
## Time Projection Chamber (TPC)

$dE/dx$  : the specific energy loss  
 Resolution:  $\sigma_{dE/dx} \approx 5\%$



## Time of Flight (TOF)

$\beta$  = Track length/arrival time  
 Resolution:  $\sigma_{TOF} \approx 86$  ps for Pb-Pb collisions

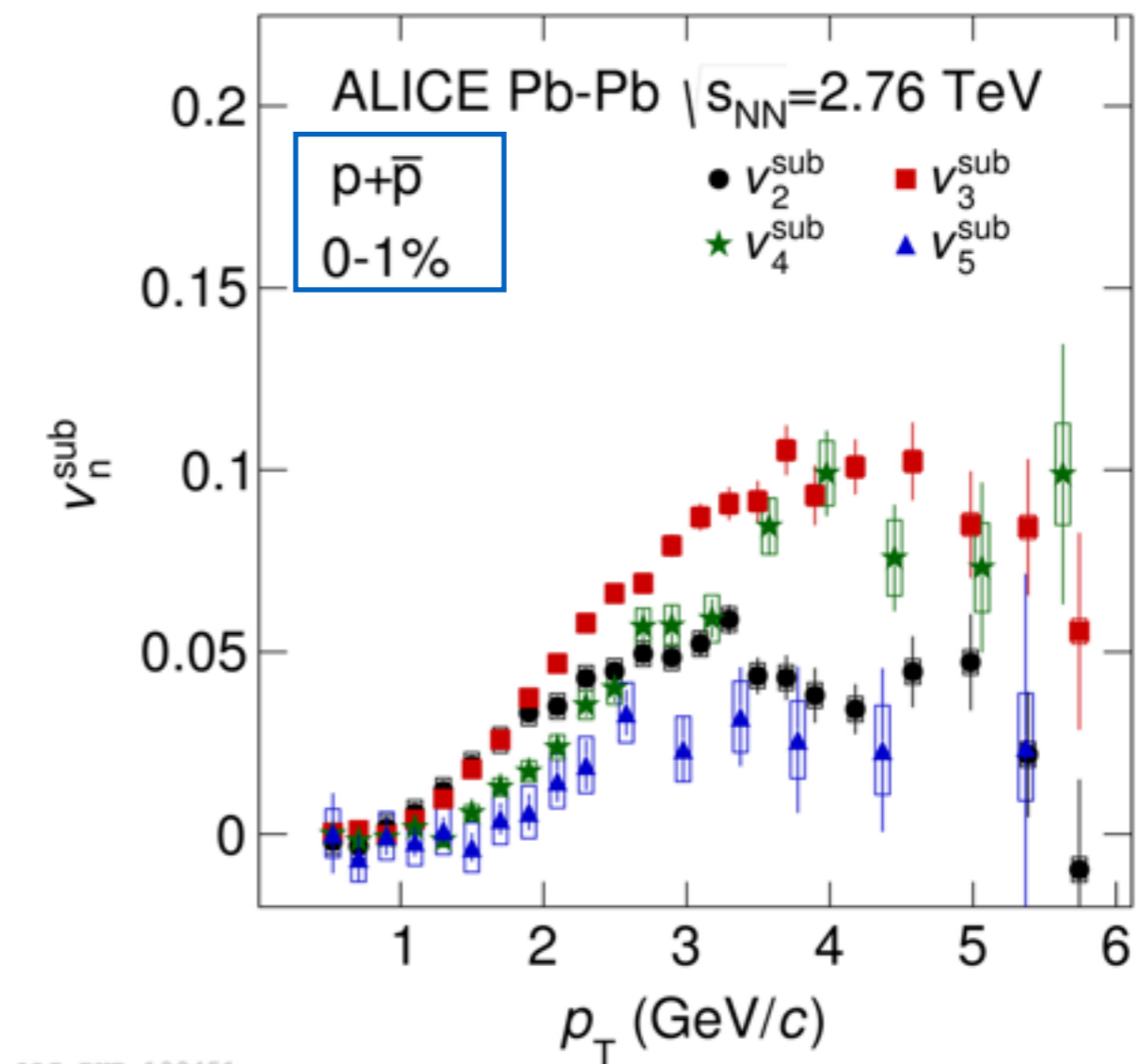
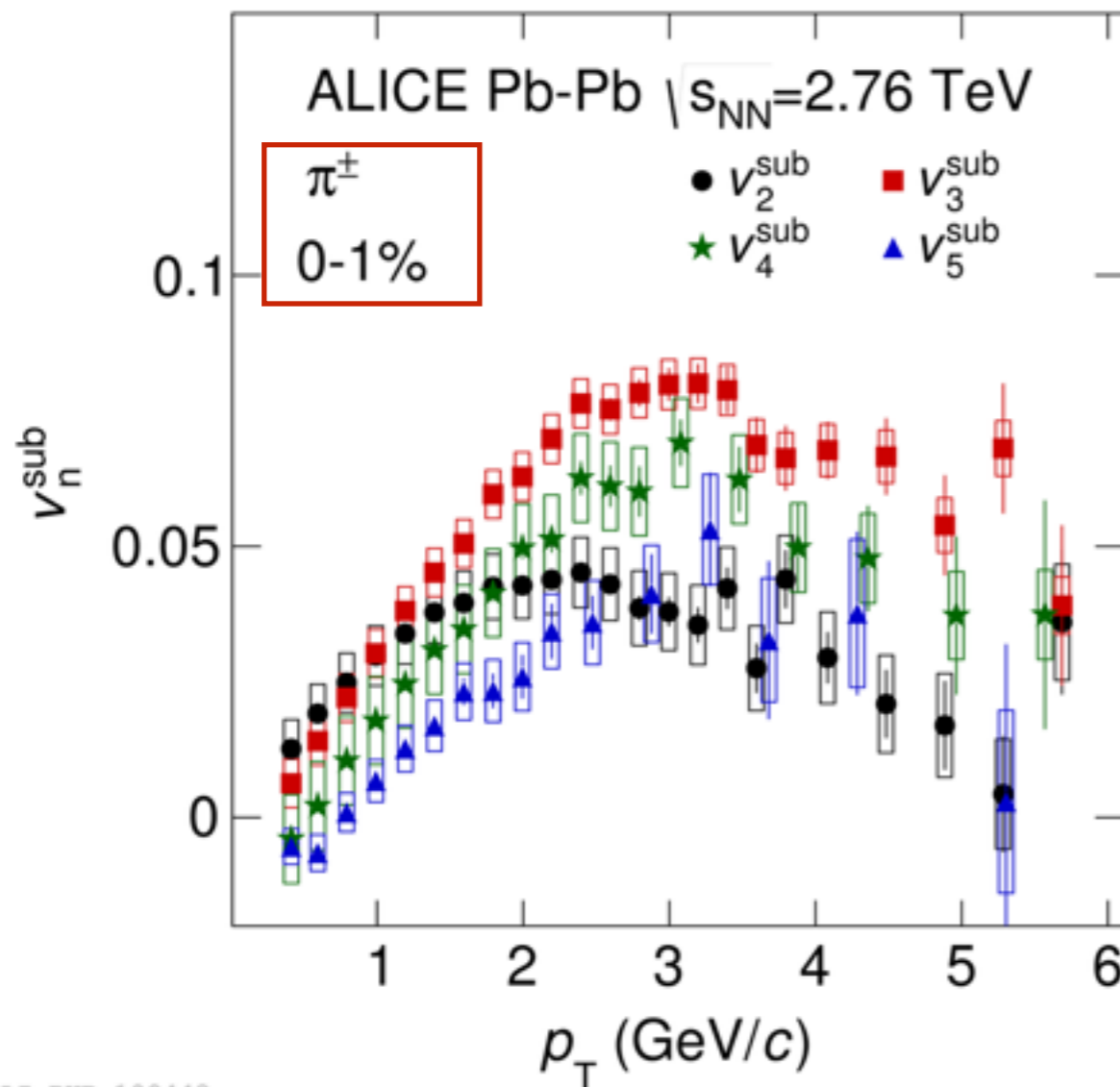


Bayesian PID (arXiv:1602.01392):

- Input quantities:  $\langle dE/dx \rangle$ ,  $\beta$
- Identification Probability  $> 90\%$

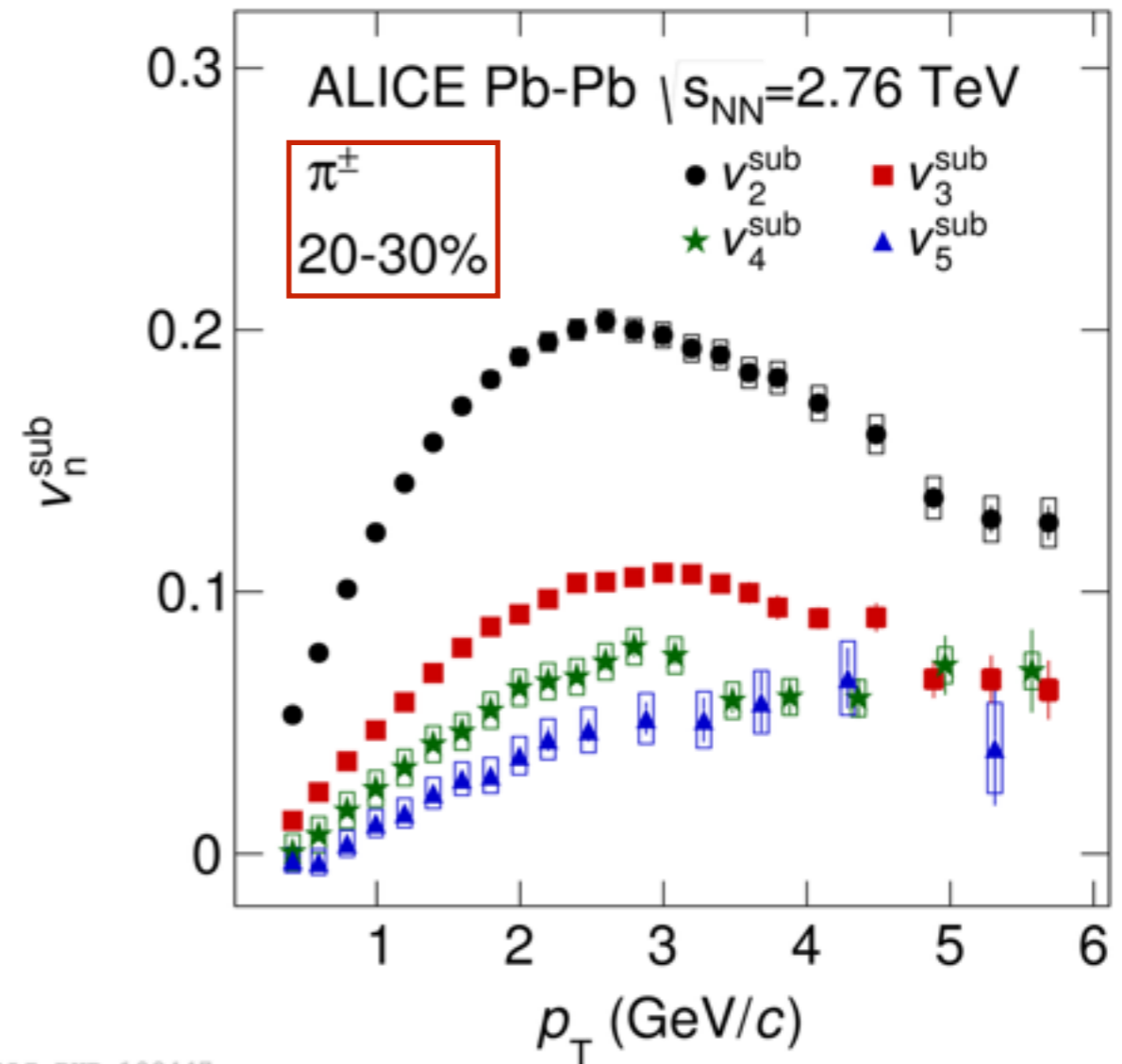
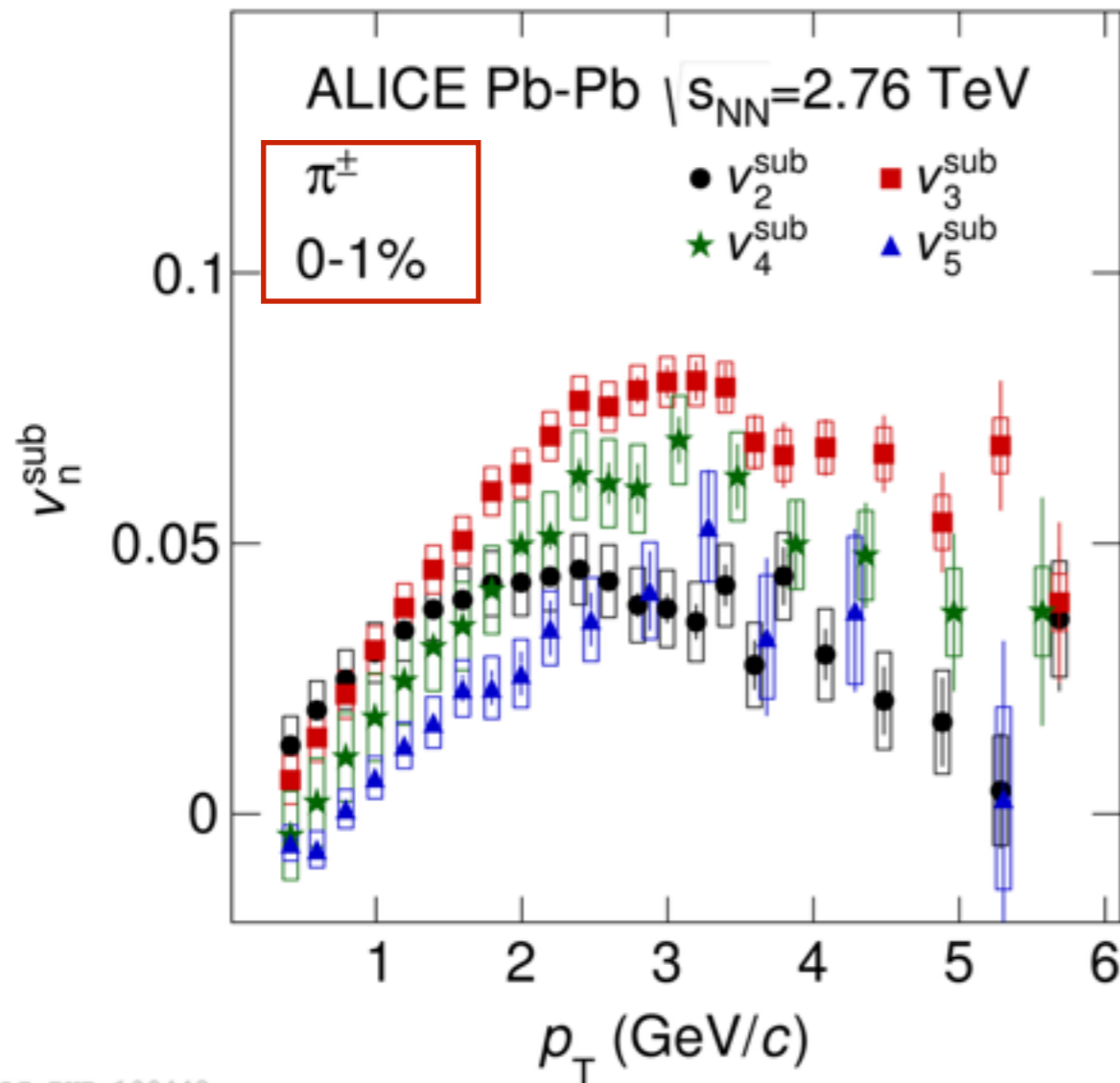
# Results

- Depending on  $p_T$  for most central (0-1%):  $v_3 > v_4 > v_5 \sim v_2$
- Crossing between  $v_2$  and other harmonics shows a mass dependence
  - interplay of different flow harmonics with radial flow

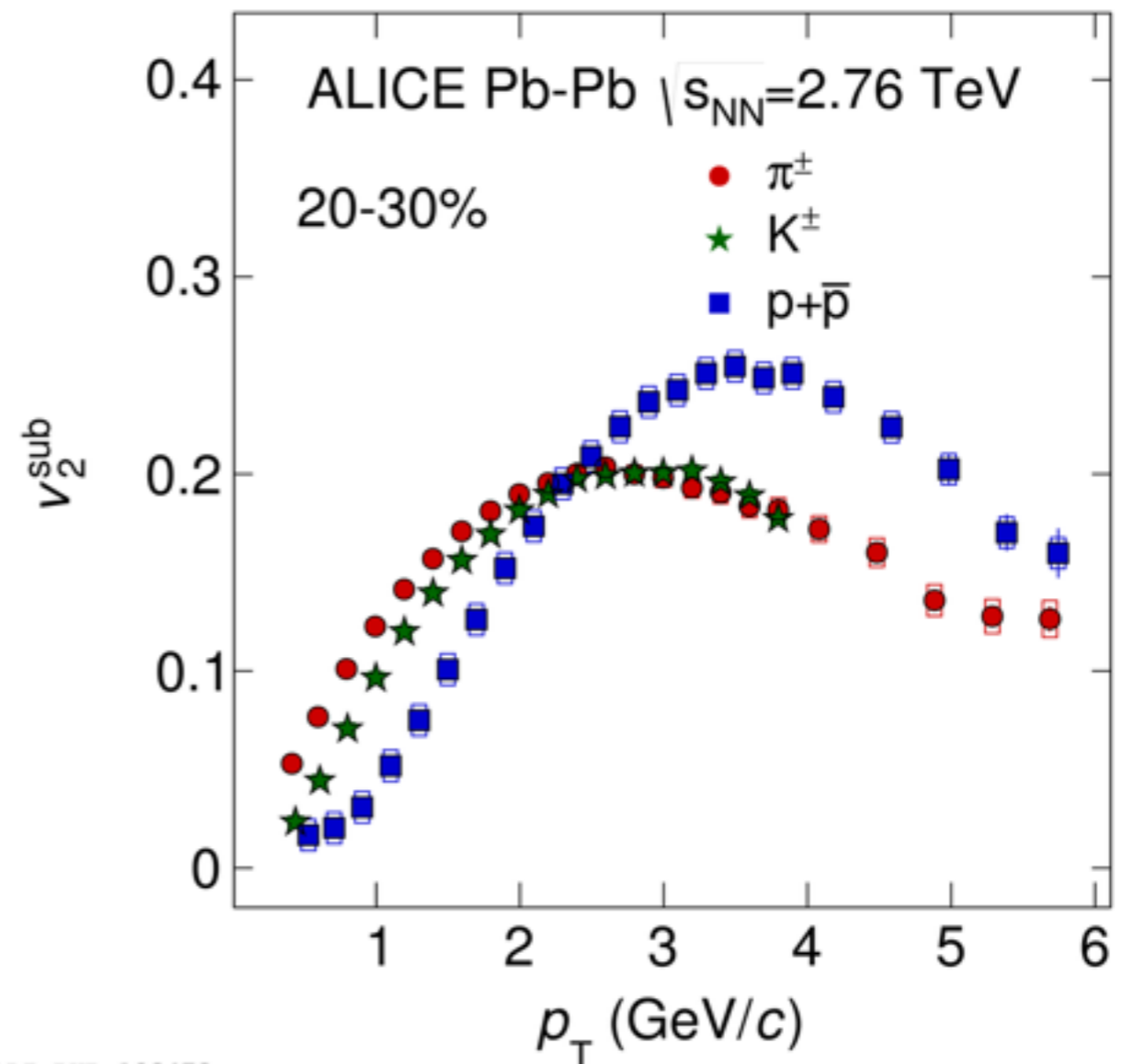
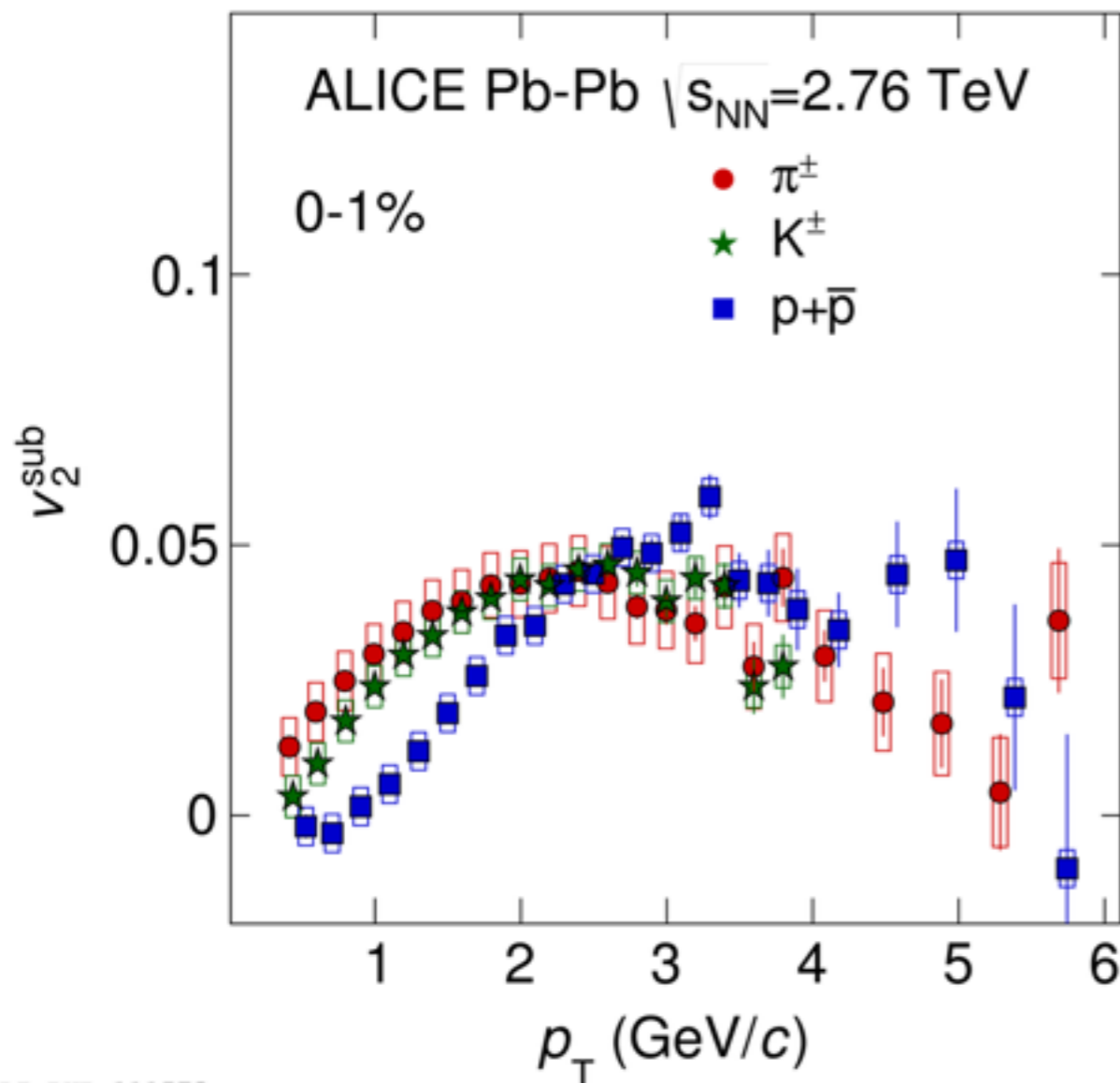


# $p_T$ evolution of flow harmonics: 0-1% vs. 20-30%

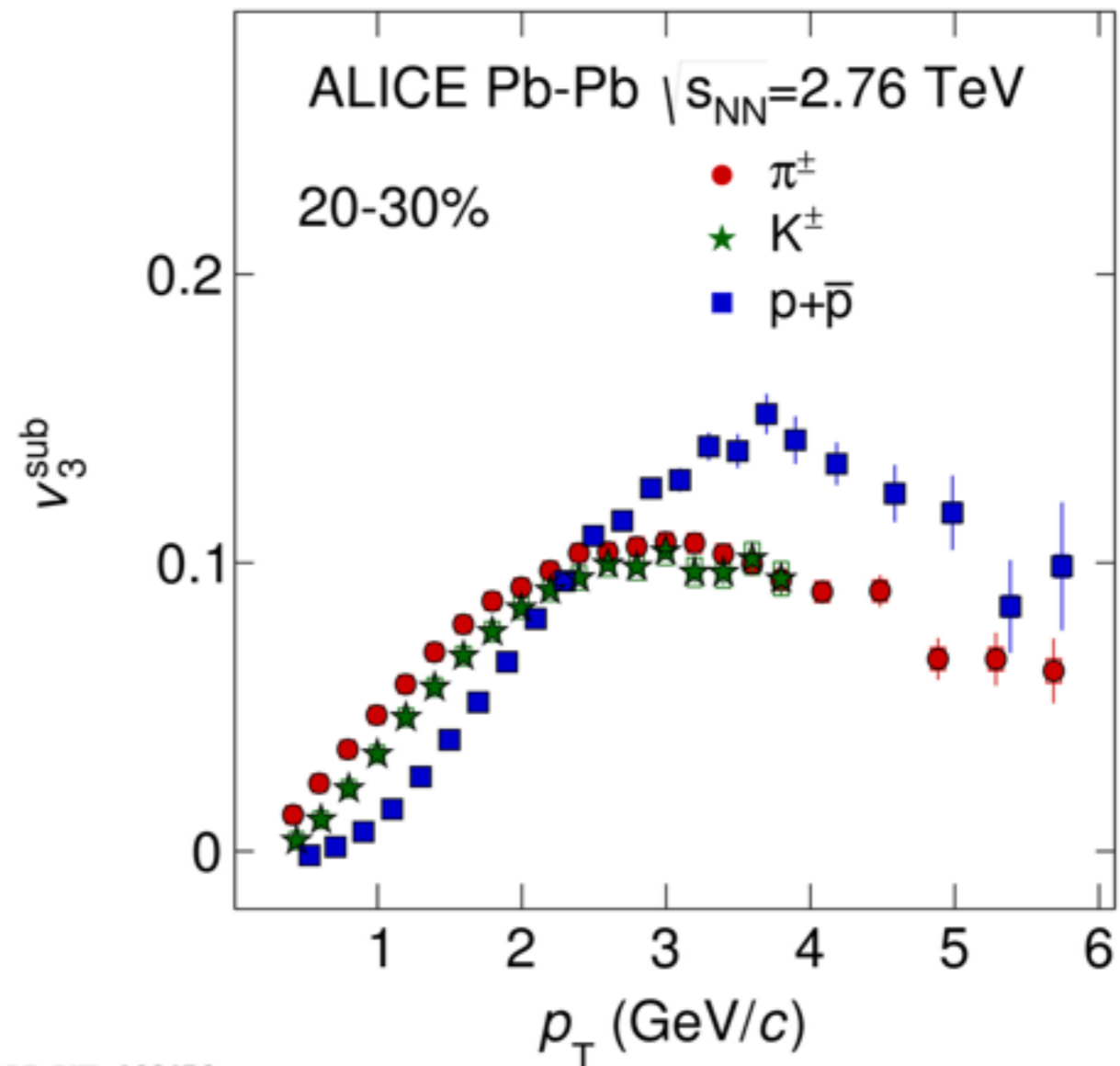
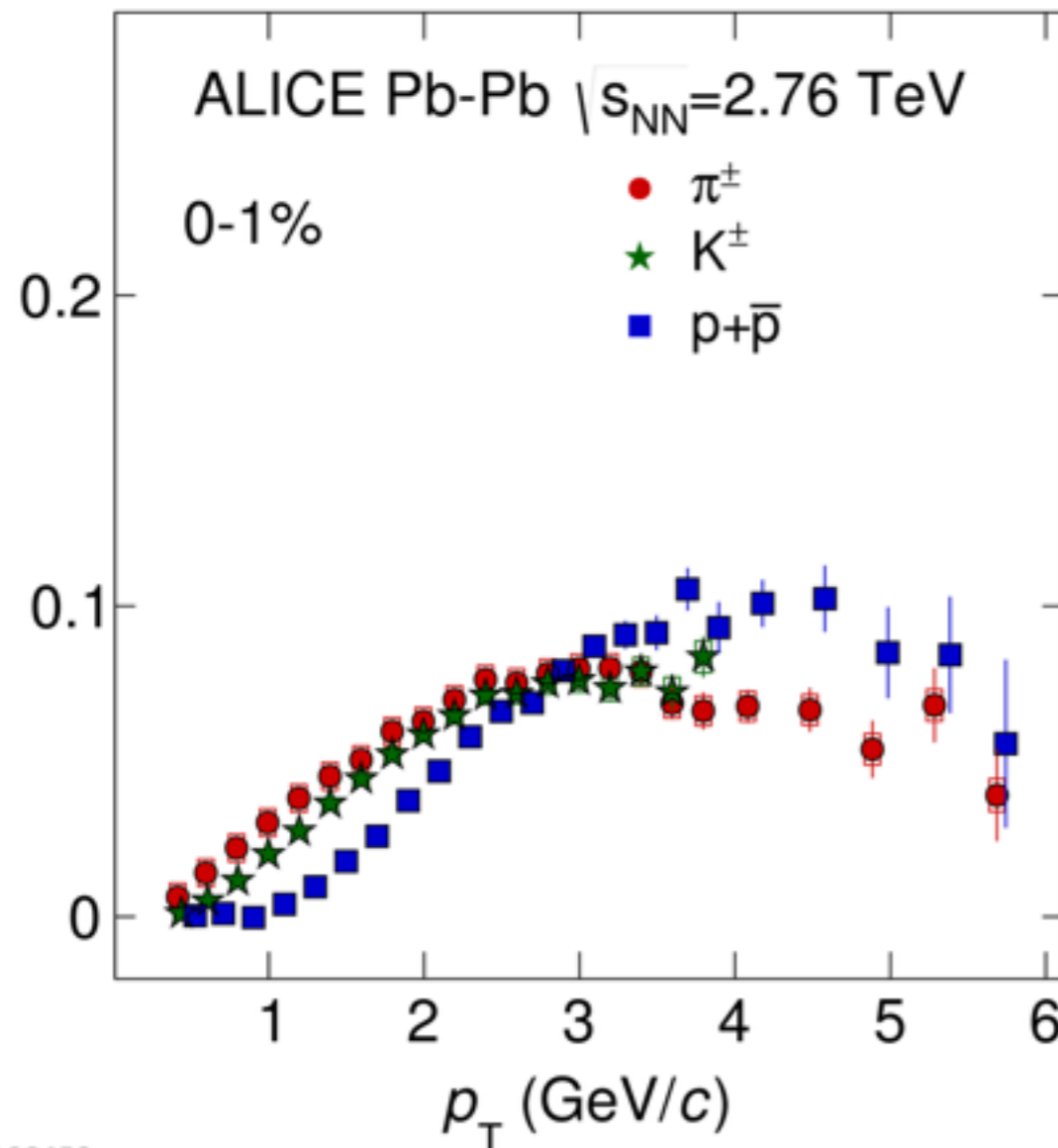
- For mid central (20-30%):  $v_2 > v_3 > v_4 > v_5$



- $p_T < 2.5 \text{ GeV}/c$ : mass ordering indicative of radial flow
- $p_T \sim 2.5\text{-}3 \text{ GeV}/c$ : crossing between  $v_2^{\text{sub}}$  of  $\pi^\pm$ ,  $K^\pm$  and  $p+\bar{p}$
- $p_T > 3 \text{ GeV}/c$ : baryon-meson grouping, approximate NCQ scaling (within  $\sim 20\%$ )

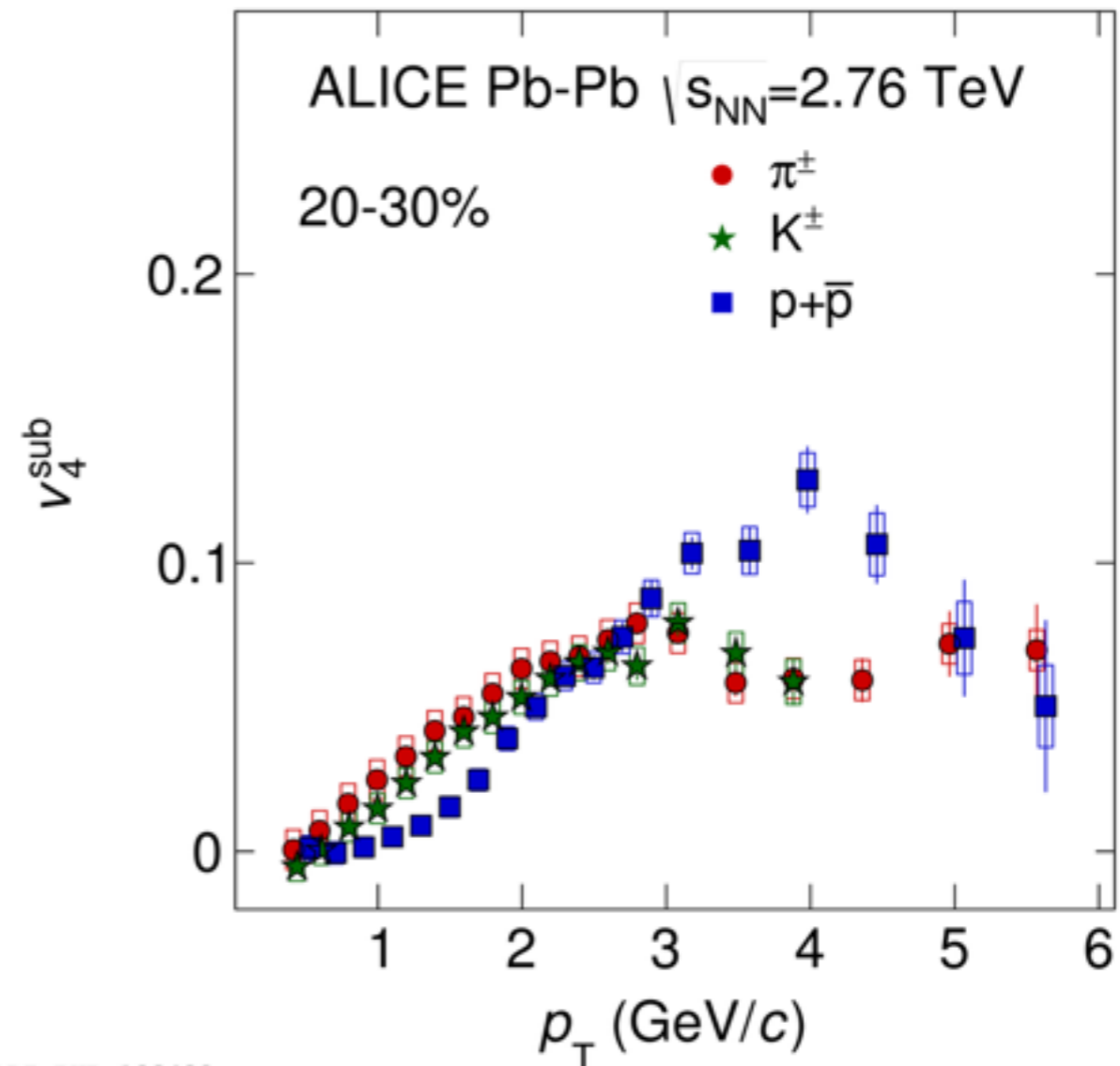
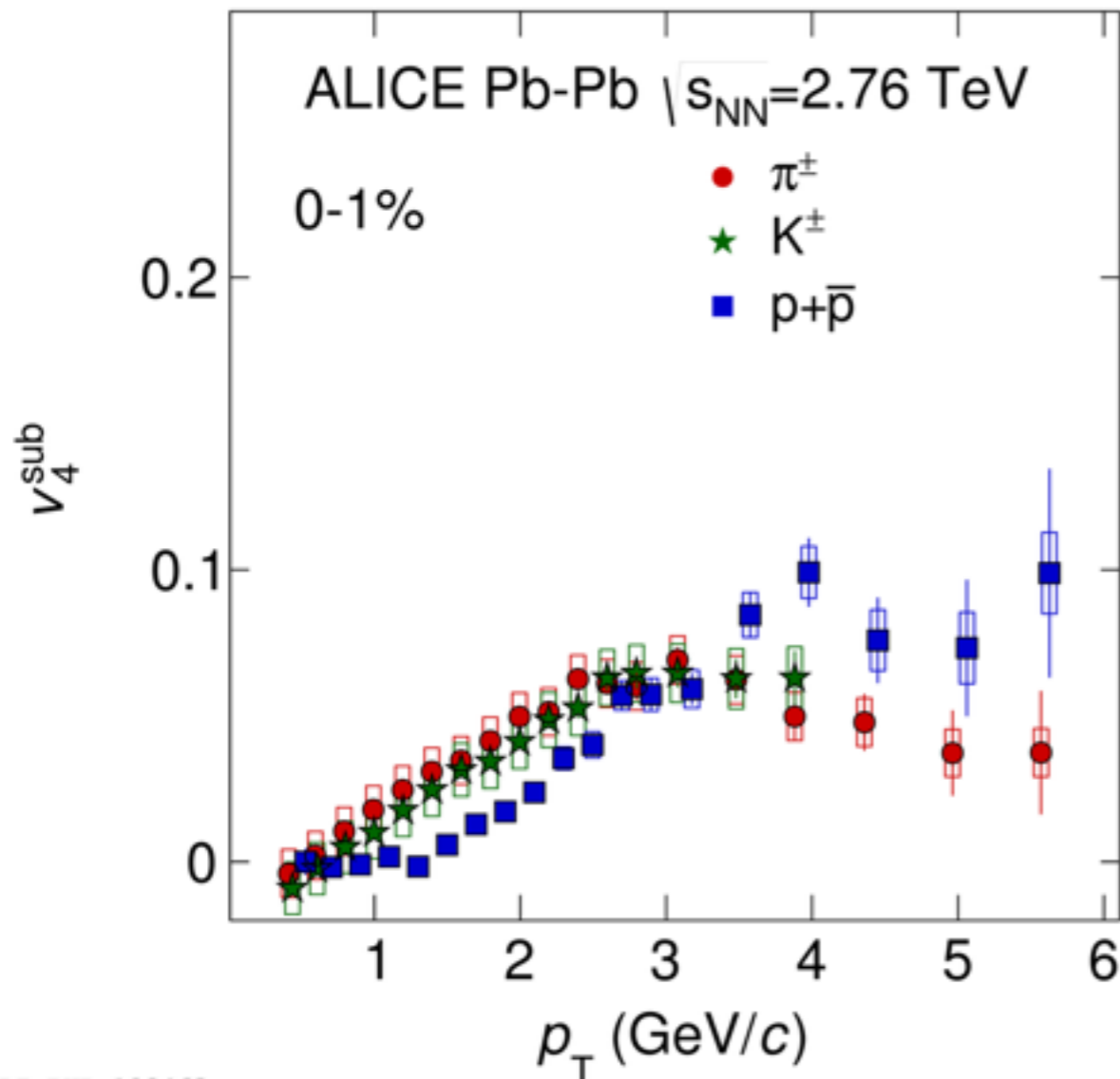


- $p_T < 2.5 \text{ GeV}/c$ : mass ordering indicative of radial flow
- $p_T \sim 2.5\text{-}3 \text{ GeV}/c$ : crossing between  $v_3^{\text{sub}}$  of  $\pi^\pm$ ,  $K^\pm$  and  $p+\bar{p}$
- $p_T > 3 \text{ GeV}/c$ : baryon-meson grouping, approximate NCQ scaling (within  $\sim 20\%$ )

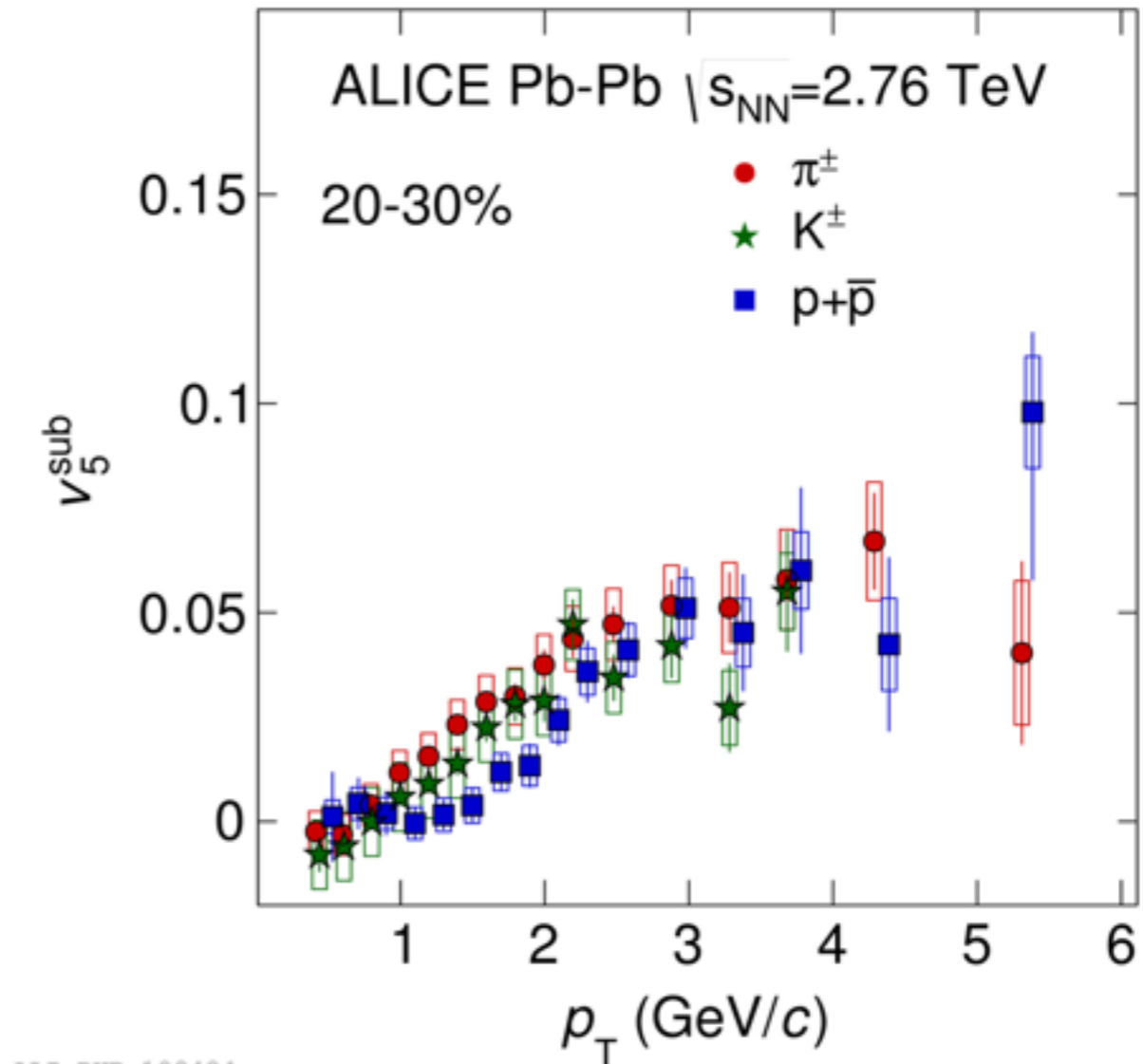
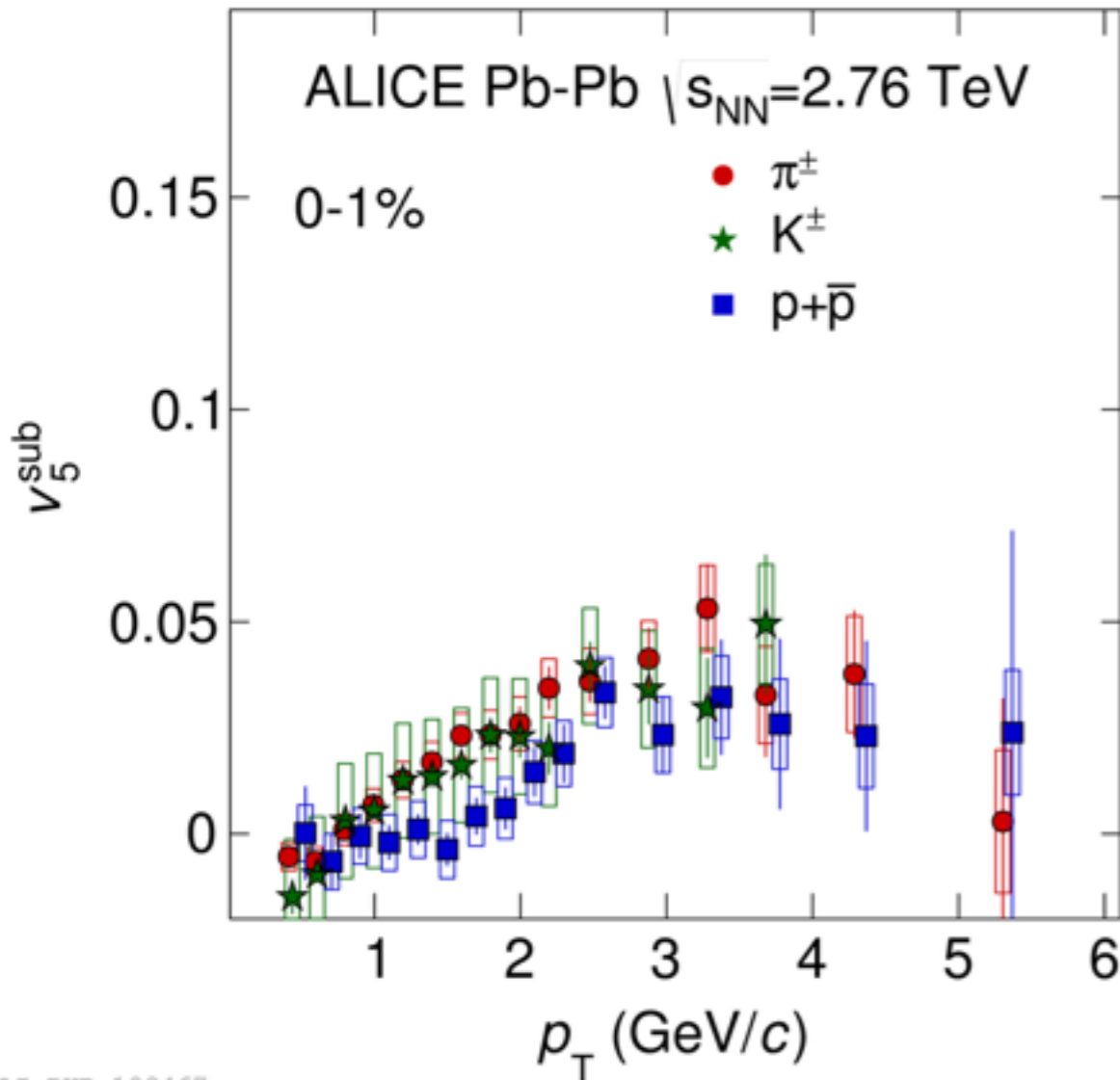




- $p_T < 2.5 \text{ GeV}/c$ : mass ordering indicative of radial flow
- $p_T \sim 2.5\text{-}3 \text{ GeV}/c$ : crossing between  $v_4^{\text{sub}}$  of  $\pi^\pm$ ,  $K^\pm$  and  $p+\bar{p}$
- $p_T > 3 \text{ GeV}/c$ : baryon-meson grouping, approximate NCQ scaling (within  $\sim 20\%$ )



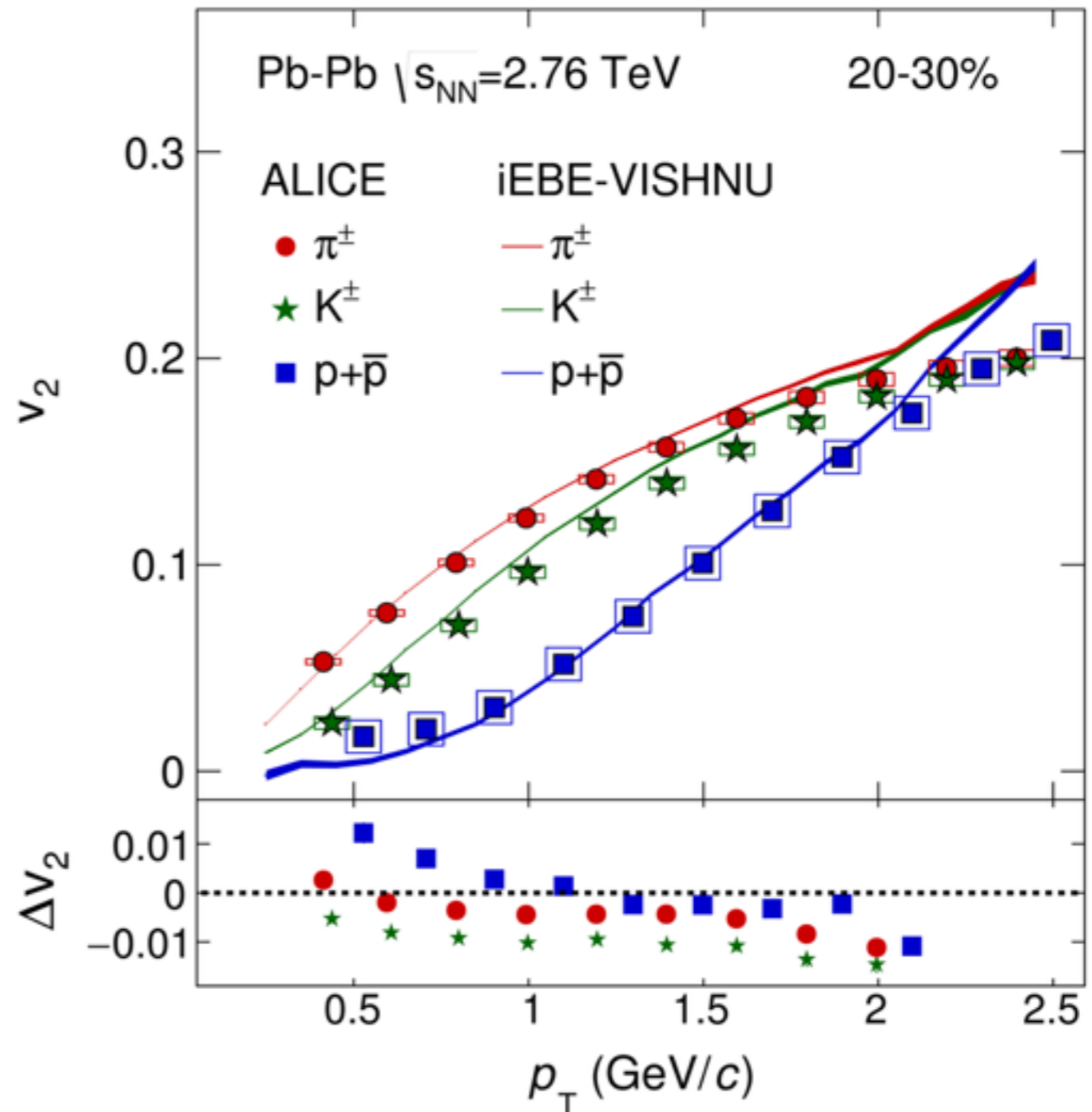
- $p_T < 2.5$  GeV/c: mass ordering indicative of radial flow within statistical and systematic uncertainties
- $p_T \sim 2.5-3$  GeV/c: crossing between  $v_5^{\text{sub}}$  of  $\pi^\pm$ ,  $K^\pm$  and  $p+\bar{p}$
- $p_T > 3$  GeV/c: baryon-meson grouping, approximate NCQ scaling (within  $\sim 20\%$ )



## Model comparison

- iEBE-VISHNU:
  - 2+1 dimensional viscous hydrodynamics (VISH2+1) coupled to hadron cascade model (UrQMD)
  - $\eta/s = 0.08$

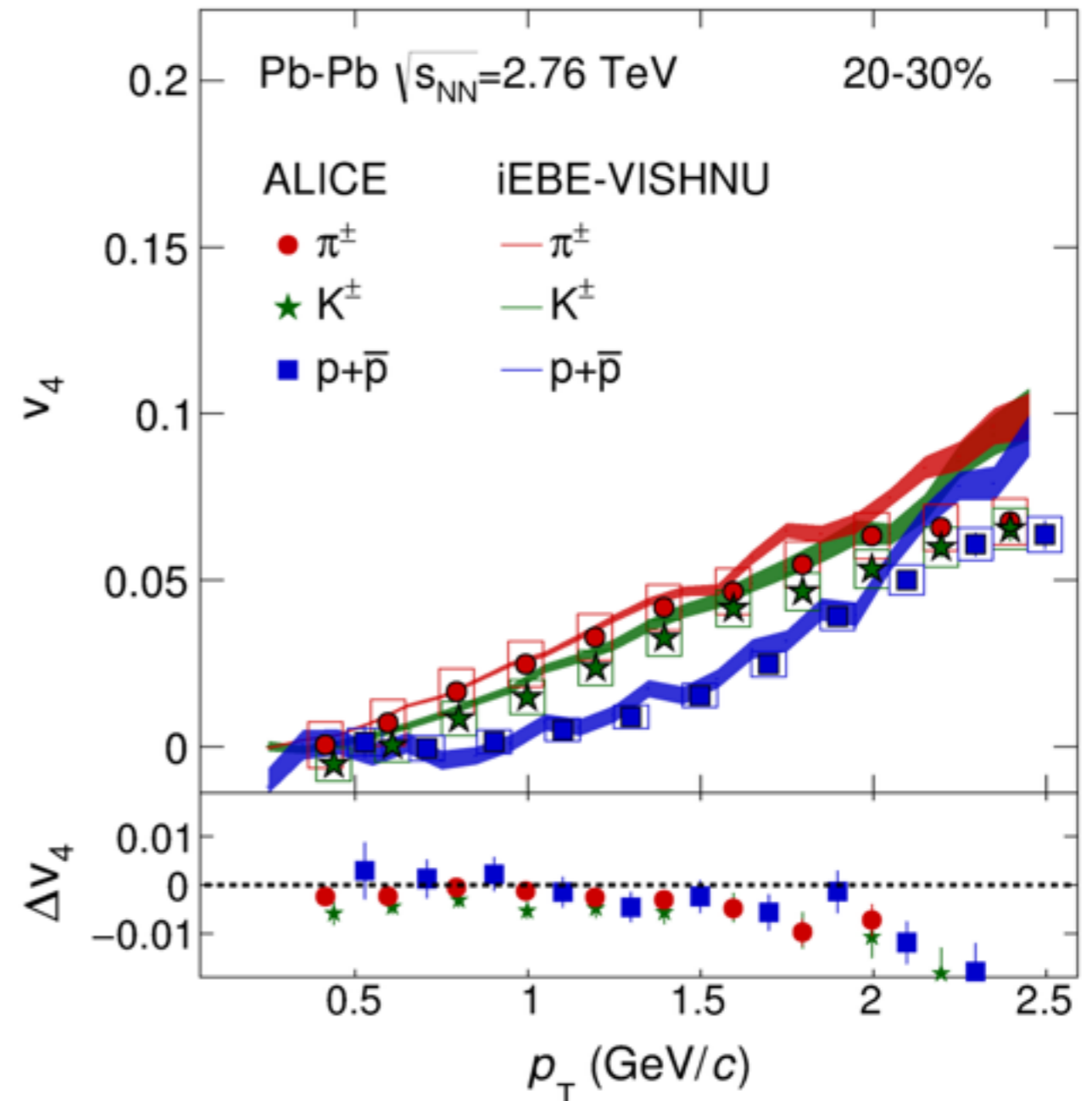
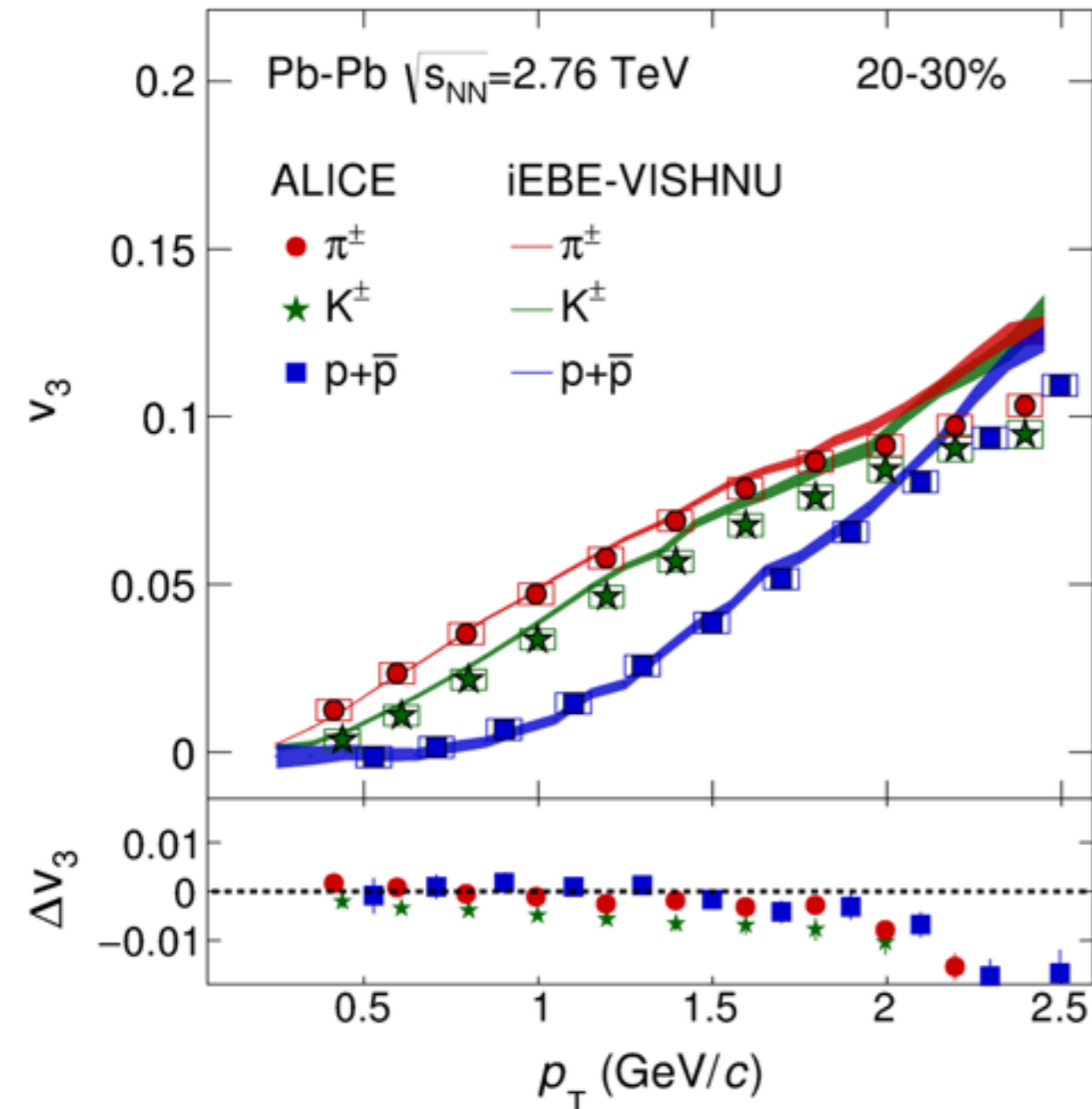
- iEBE-VISHNU:
  - 2+1 dimensional viscous hydrodynamics (VISH2+1) coupled to hadron cascade model (UrQMD)
  - $\eta/s = 0.08$
  - reproduces the observed mass ordering of  $v_2$  for  $p_T < 2 \text{ GeV}/c$
  - describes the measurements for  $v_2$  within 15%



ALI-PUB-109488

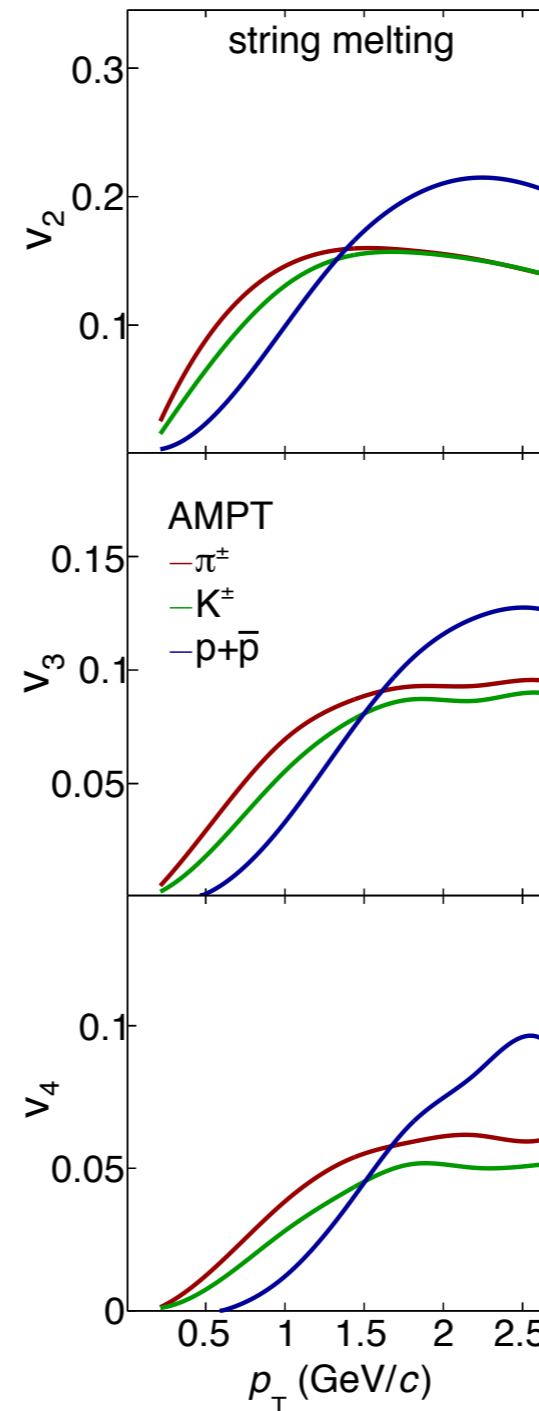
- iEBE-VISHNU:
- reproduces the observed mass ordering of  $v_3$  and  $v_4$  for  $p_T < 2$  GeV/c

- describes the measurements for  $v_3$  and  $v_4$  within 5%



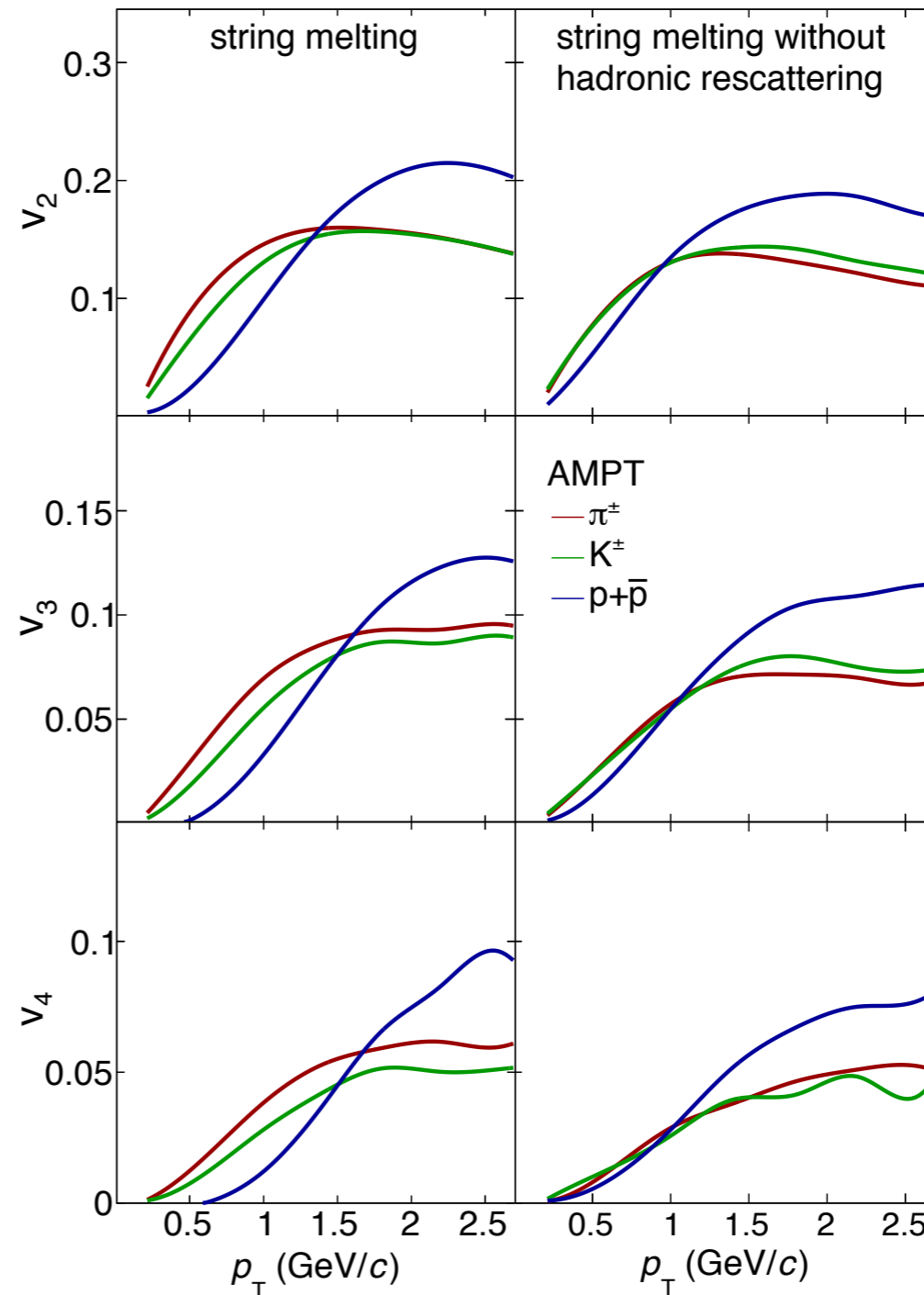
- AMPT versions:
  - String melting (+quark coalescence) with hadronic rescattering
  - String melting (+quark coalescence) without hadronic rescattering
  - default (No string melting)
- This comparison allows one to study:
  - Effects of hadronic rescattering
  - Effects of quark coalescence

- AMPT version:
  - String melting (+quark coalescence) with hadronic rescattering
- Distinct mass ordering in low  $p_T$  region
- baryon-meson grouping in intermediate  $p_T$  region

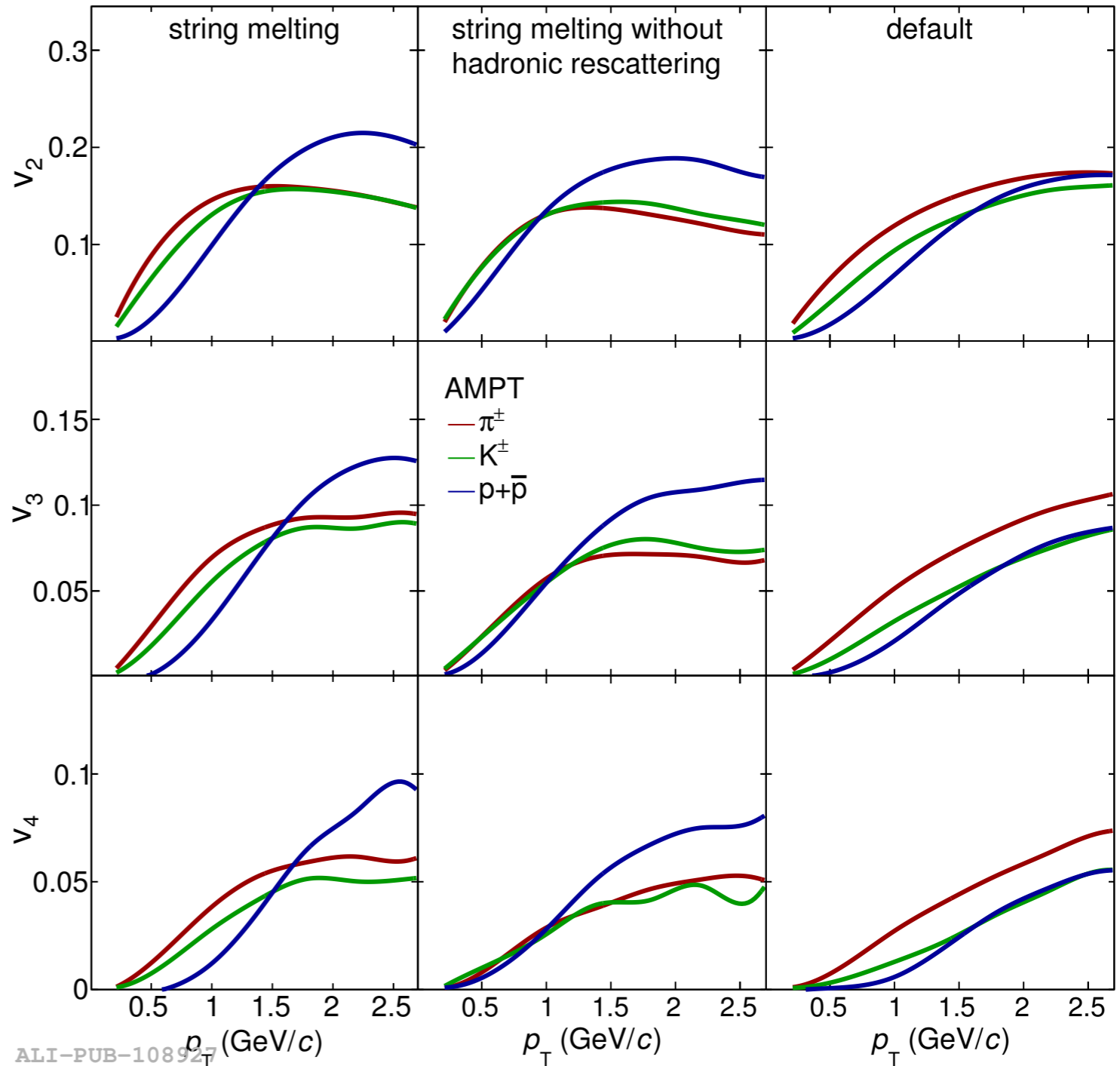




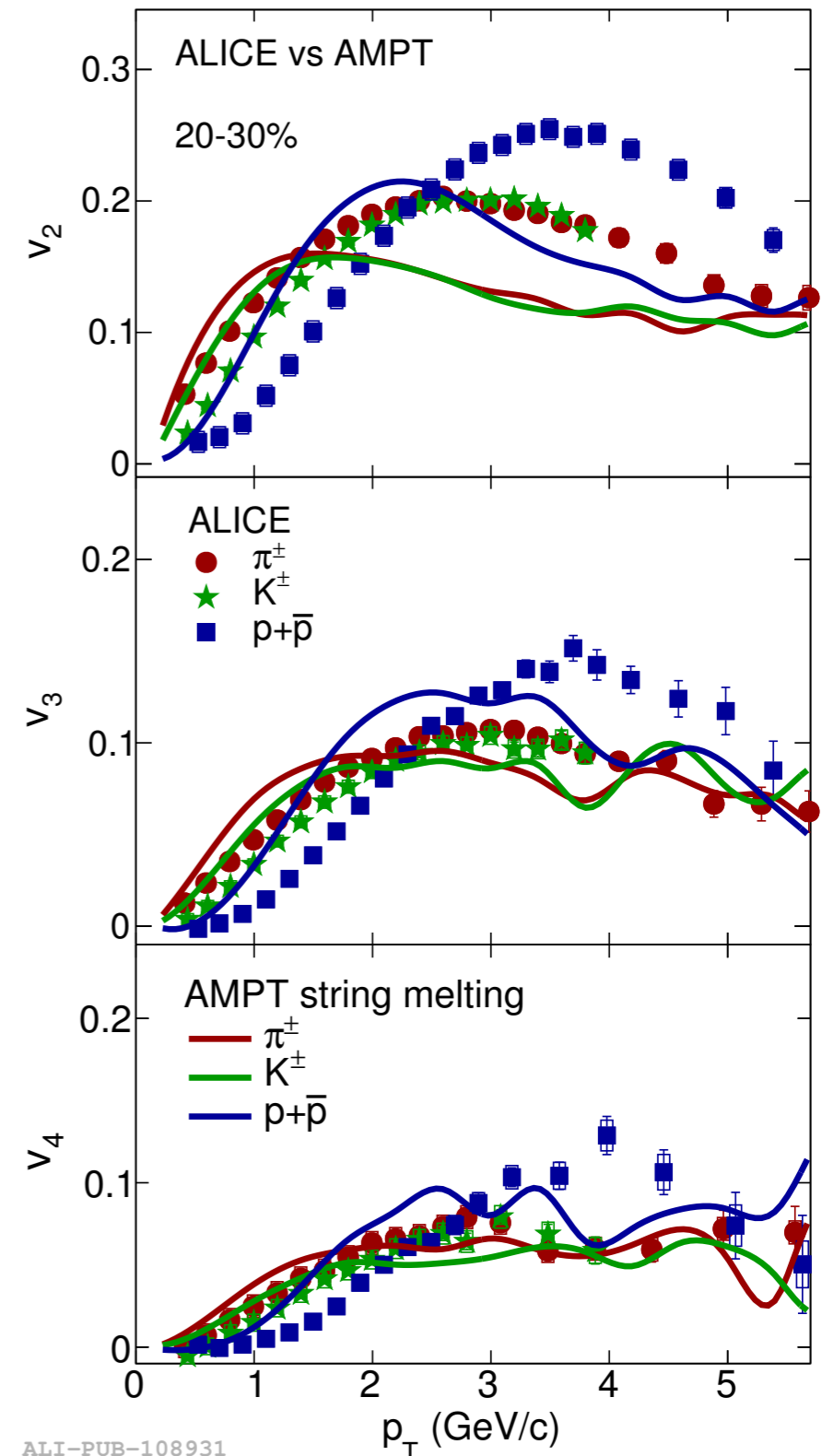
- AMPT versions:
  - String melting (+quark coalescence) with hadronic rescattering
  - String melting (+quark coalescence) without hadronic rescattering
- Distinct mass ordering in low  $p_T$  region:
  - Effect of hadronic rescattering in development of radial flow



- AMPT versions:
  - String melting (+quark coalescence) with hadronic rescattering
  - String melting (+quark coalescence) without hadronic rescattering
  - default (No string melting)
- Distinct mass ordering in low  $p_T$  region:
  - Effect of hadronic rescattering in development of radial flow
- Baryon-meson grouping:
  - Effect of quark coalescence



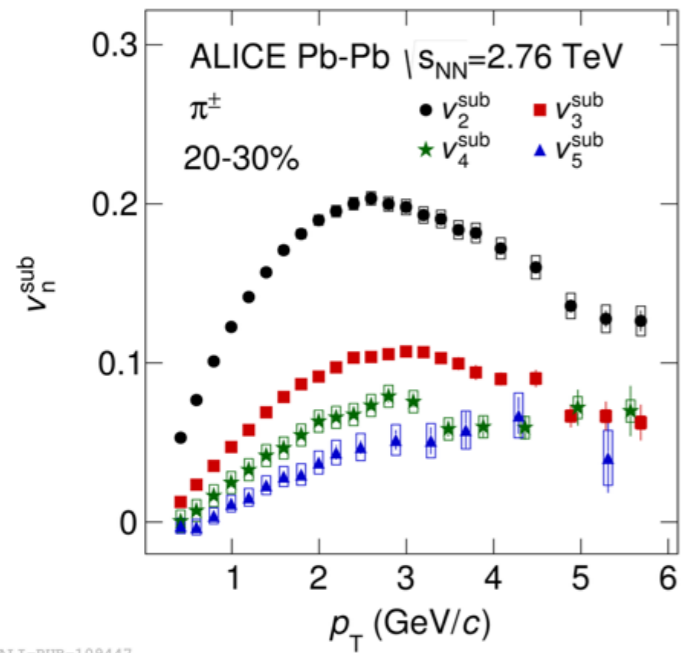
- AMPT string melting version:
  - Reproduces both the mass ordering and the baryon-meson grouping at low and intermediate  $p_T$  for all harmonics
  - Fails to quantitatively reproduce the measurements
- This discrepancy could rise from:
  - Radial flow in AMPT 25% lower than the measured value at the LHC



ALI-PUB-108931



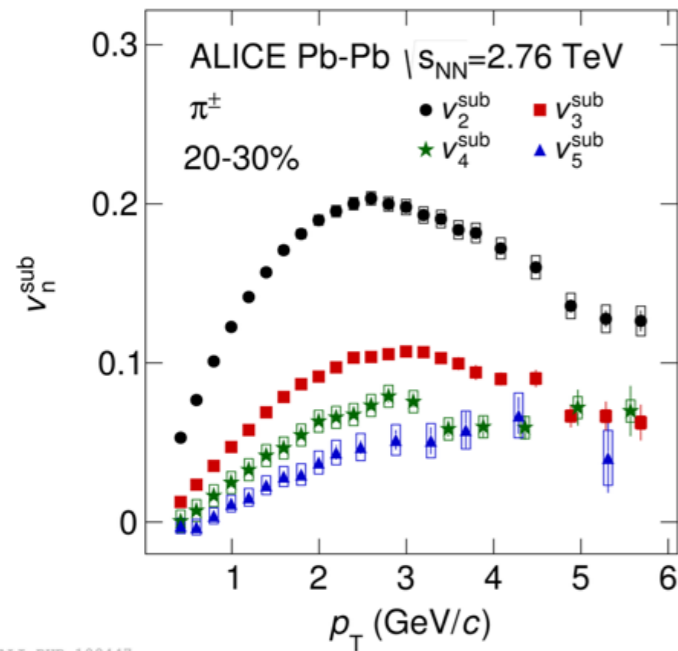
- ultra-central:  $v_3 > v_4 > v_5 \sim v_2$
- mid-central:  $v_2 > v_3 > v_4 > v_5$



ALI-PUB-109447

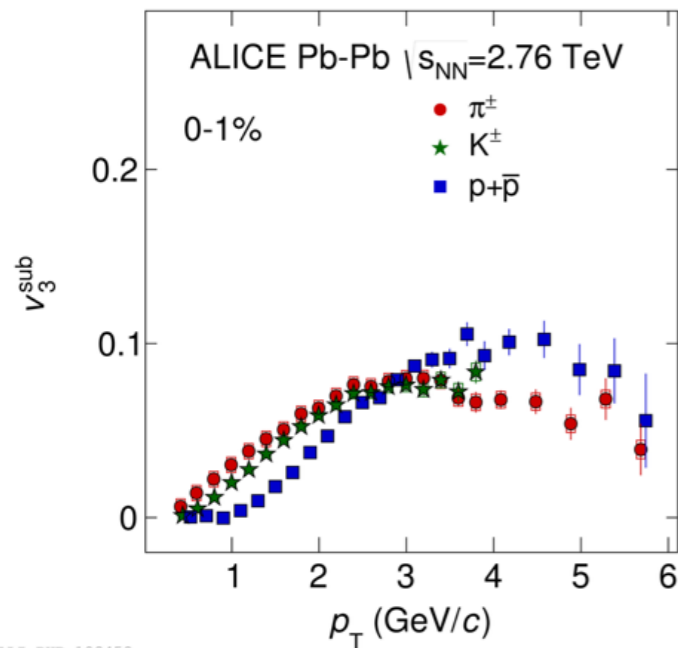


- ultra-central:  $v_3 > v_4 > v_5 \sim v_2$
- mid-central:  $v_2 > v_3 > v_4 > v_5$



ALI-PUB-109447

- For all flow harmonics:
  - mass ordering
  - baryon-meson grouping

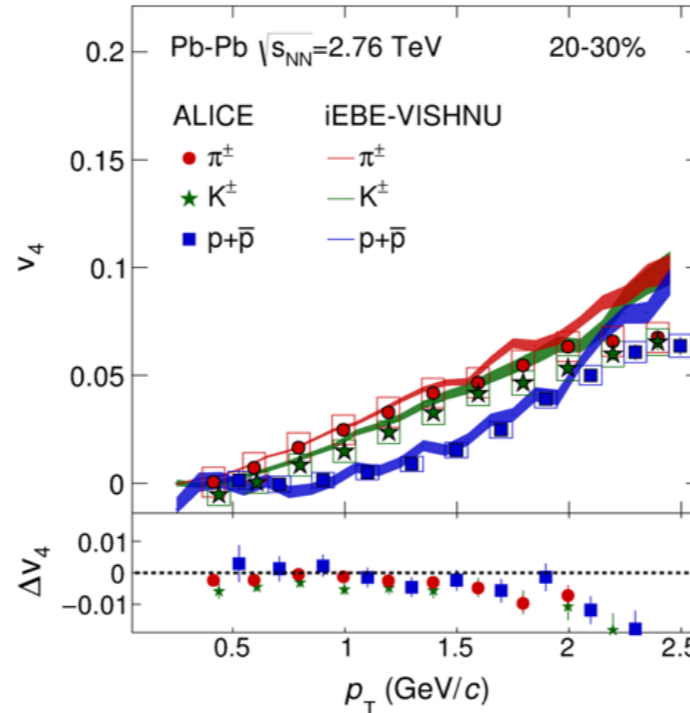
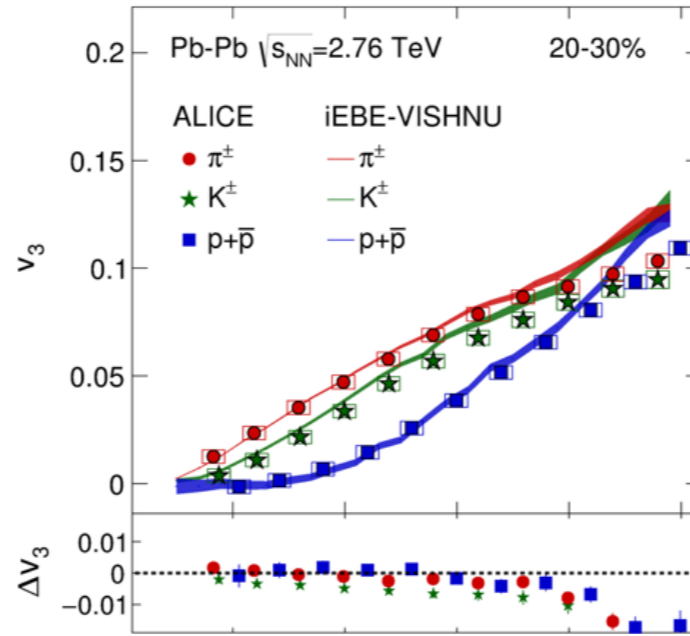
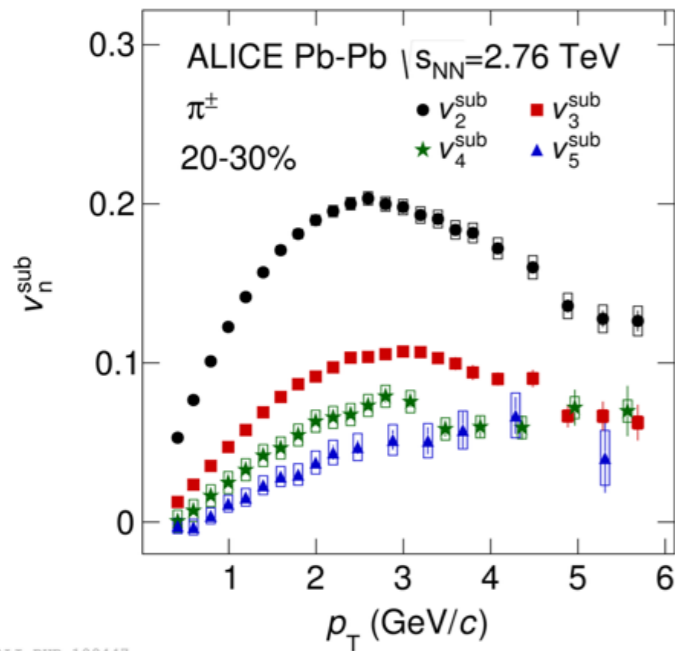


ALI-PUB-109459

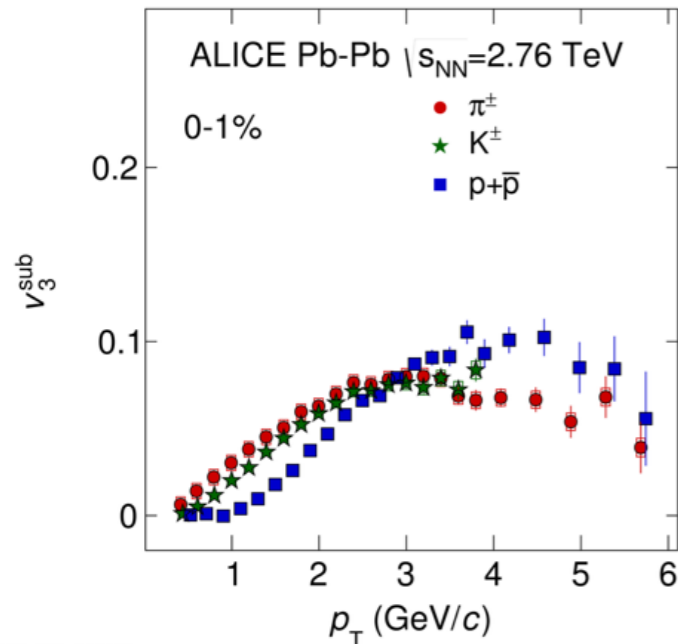


- ultra-central:  $v_3 > v_4 > v_5 \sim v_2$
- mid-central:  $v_2 > v_3 > v_4 > v_5$

- **iEBE-VISHNU:**
  - reproduces the observed mass ordering for  $v_2$ ,  $v_3$  and  $v_4$
  - describes data  $\sim 5-15\%$



- For all flow harmonics:
  - mass ordering
  - baryon-meson grouping



ALI-PUB-109496

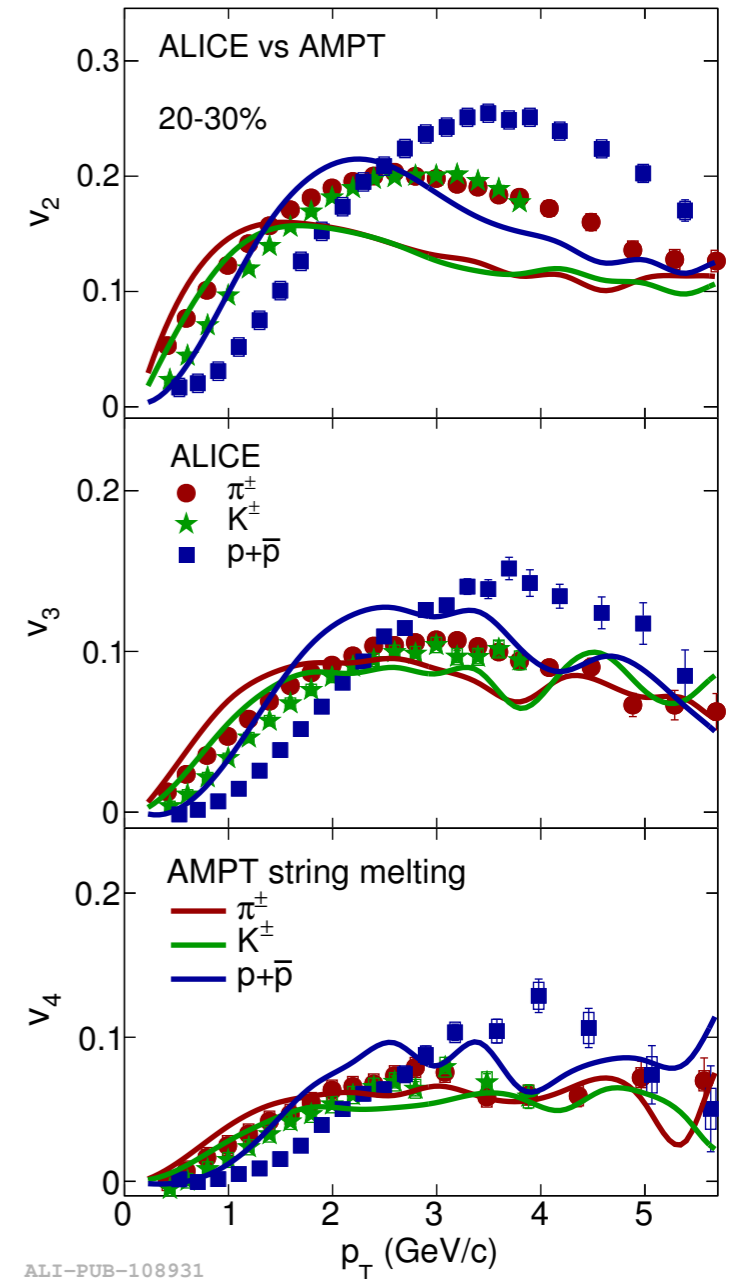
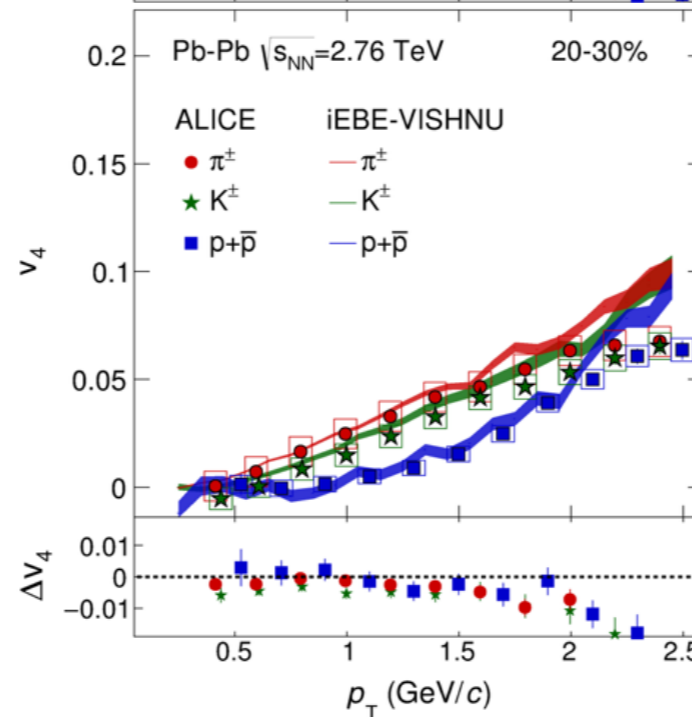
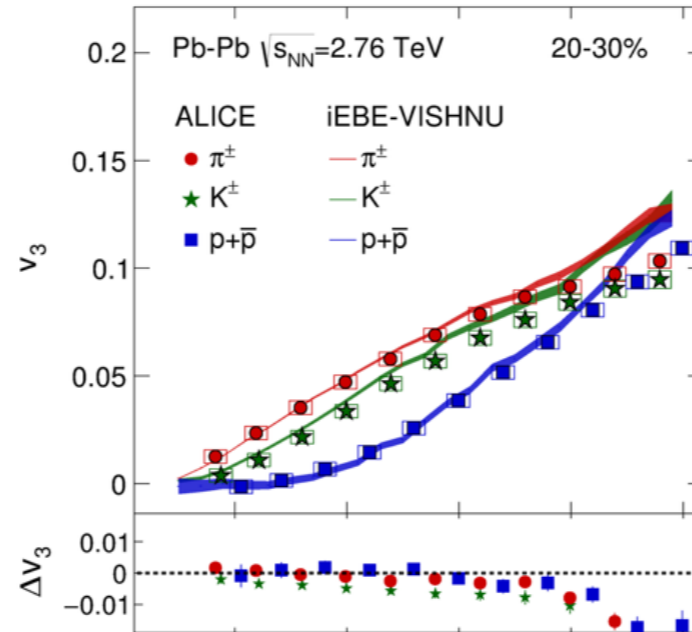
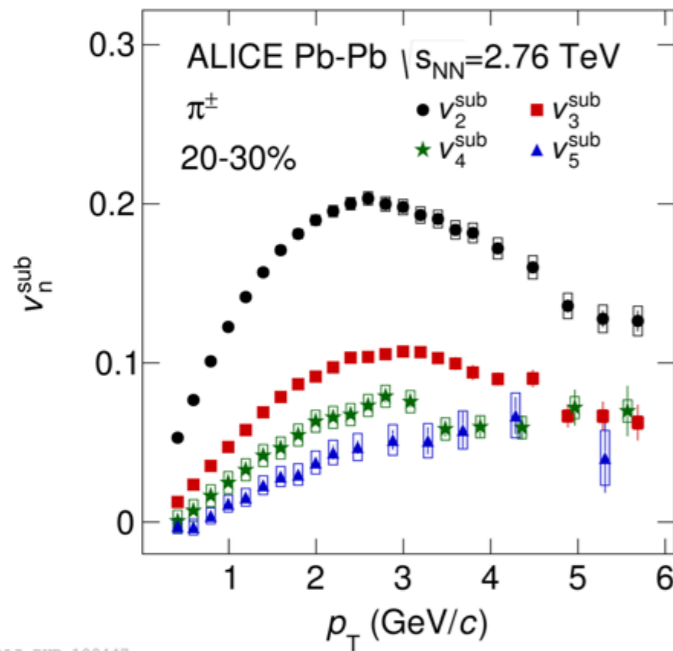
ALI-PUB-109459



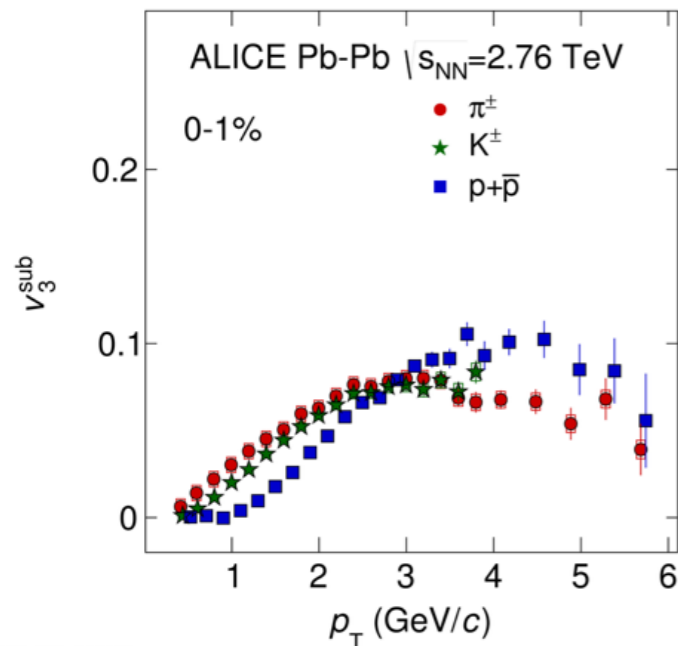
- ultra-central:  $v_3 > v_4 > v_5 \sim v_2$
- mid-central:  $v_2 > v_3 > v_4 > v_5$

- **iEBE-VISHNU:**
  - reproduces the observed mass ordering for  $v_2$ ,  $v_3$  and  $v_4$
  - describes data  $\sim 5-15\%$

- **AMPT:**
  - hadronic rescattering
  - quark coalescence



- For all flow harmonics:
  - mass ordering
  - baryon-meson grouping



ALI-PUB-109496

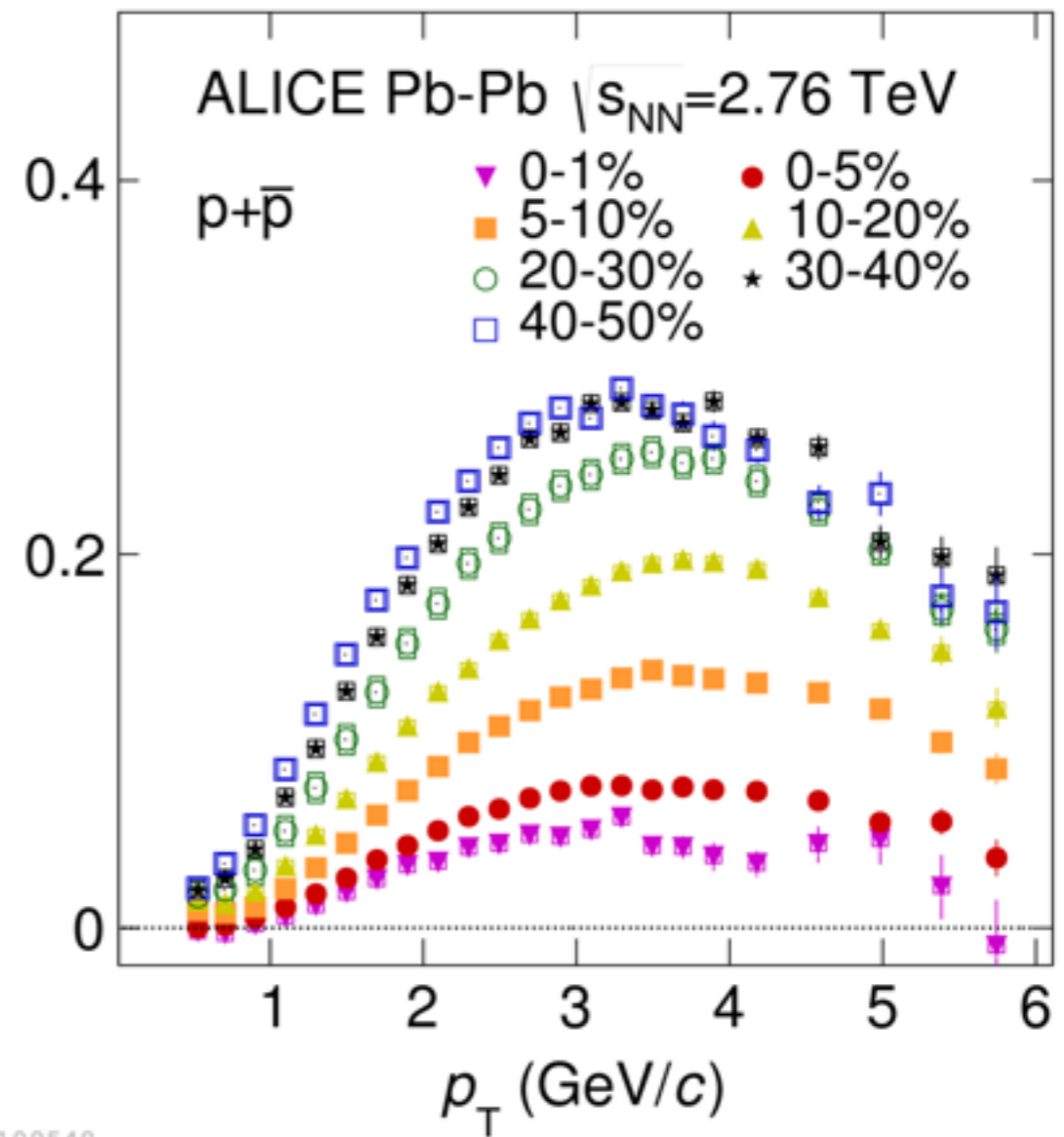
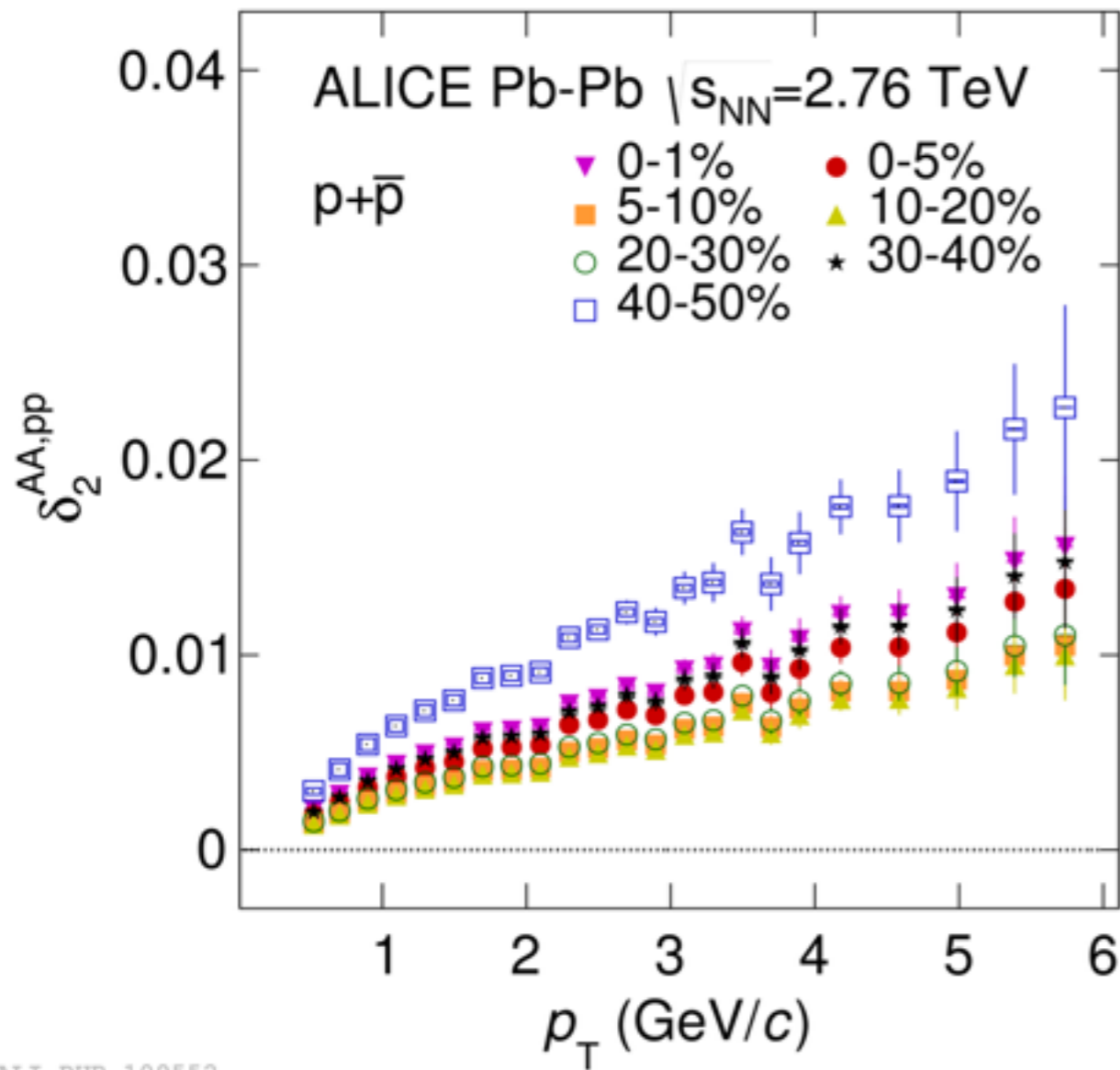
ALI-PUB-108931

ALI-PUB-109459

# Back up

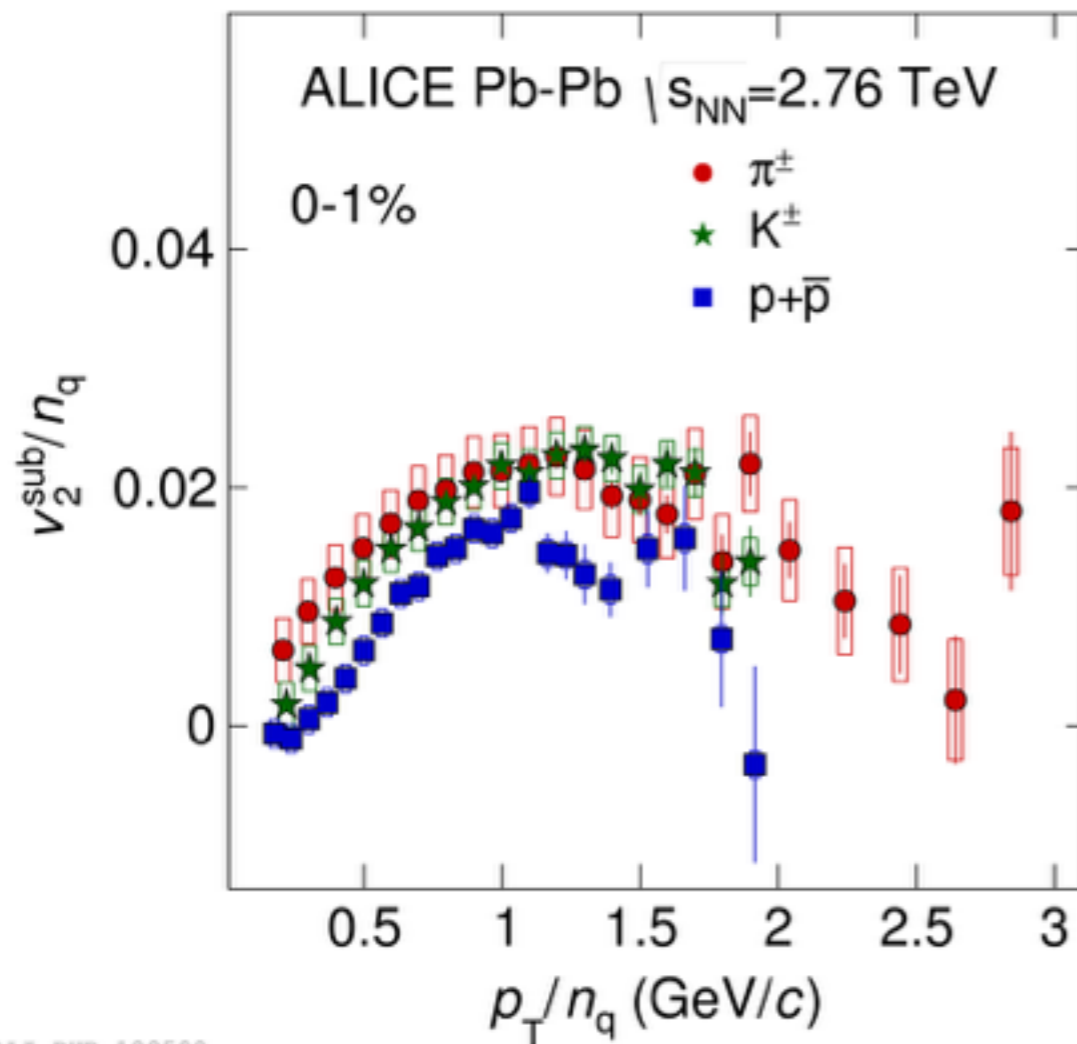


- Value of  $\delta_n^{AA,pp}$  depends on centrality
  - interplay of decreasing multiplicity and increasing reference flow
- $\delta_n^{AA,pp}$  dependence on  $p_T$  is different from  $v_n$
- Value of  $\delta_n^{AA,pp}$  depends on centrality
- For 0-1%:  $\delta_2^{AA,pp} \sim 20\%$  of  $v_2^{AA}$       • For 40-50%:  $\delta_2^{AA,pp} \sim 7\%$  of  $v_2^{AA}$

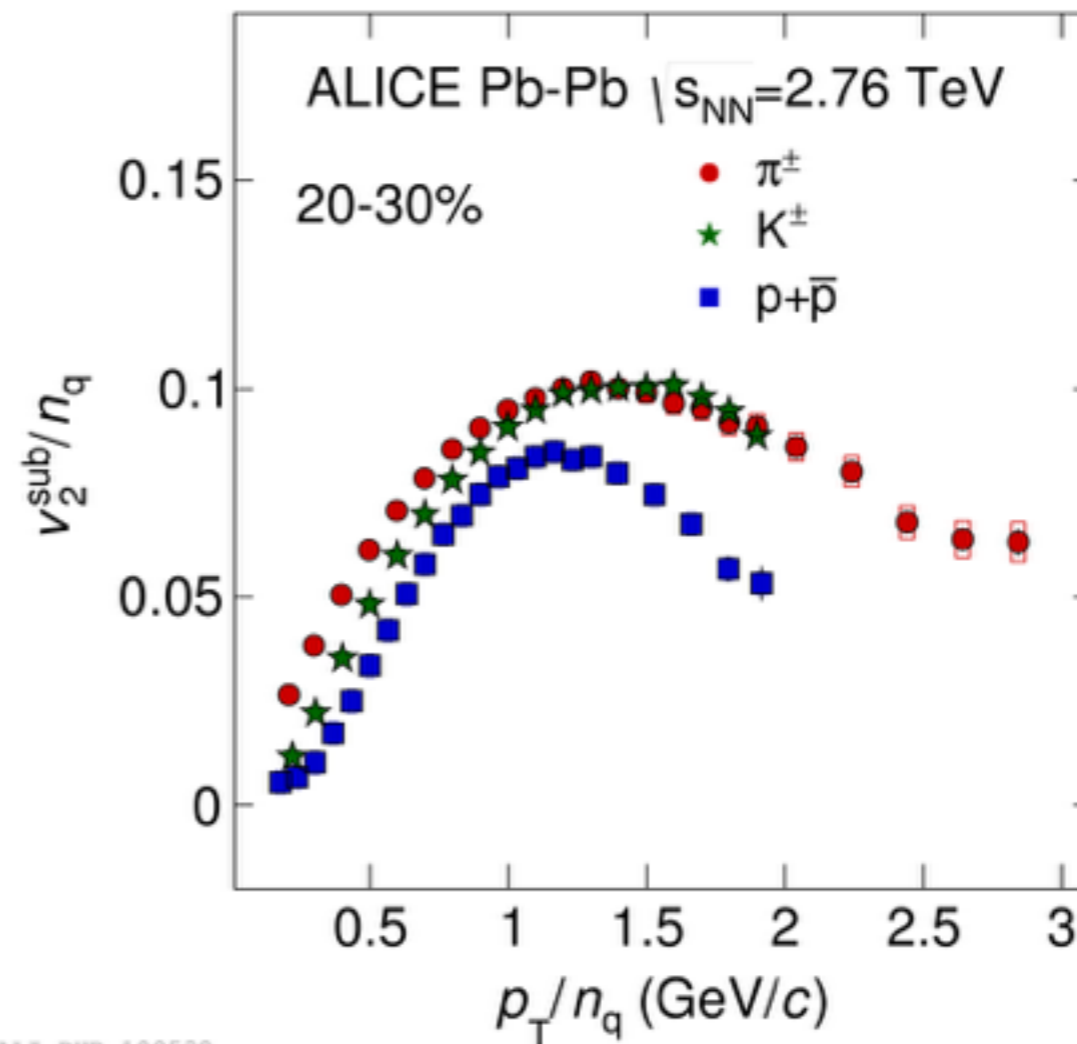


Intermediate  $p_T$  ( $p_T > 3 \text{ GeV}/c$ ):  $v_n$  of baryons  $>$   $v_n$  of mesons

- Particle production mechanism: Quark coalescence?
- NCQ scaling:  $p_T/n_q \rightarrow$  Proposed at RHIC



ALI-PUB-109500

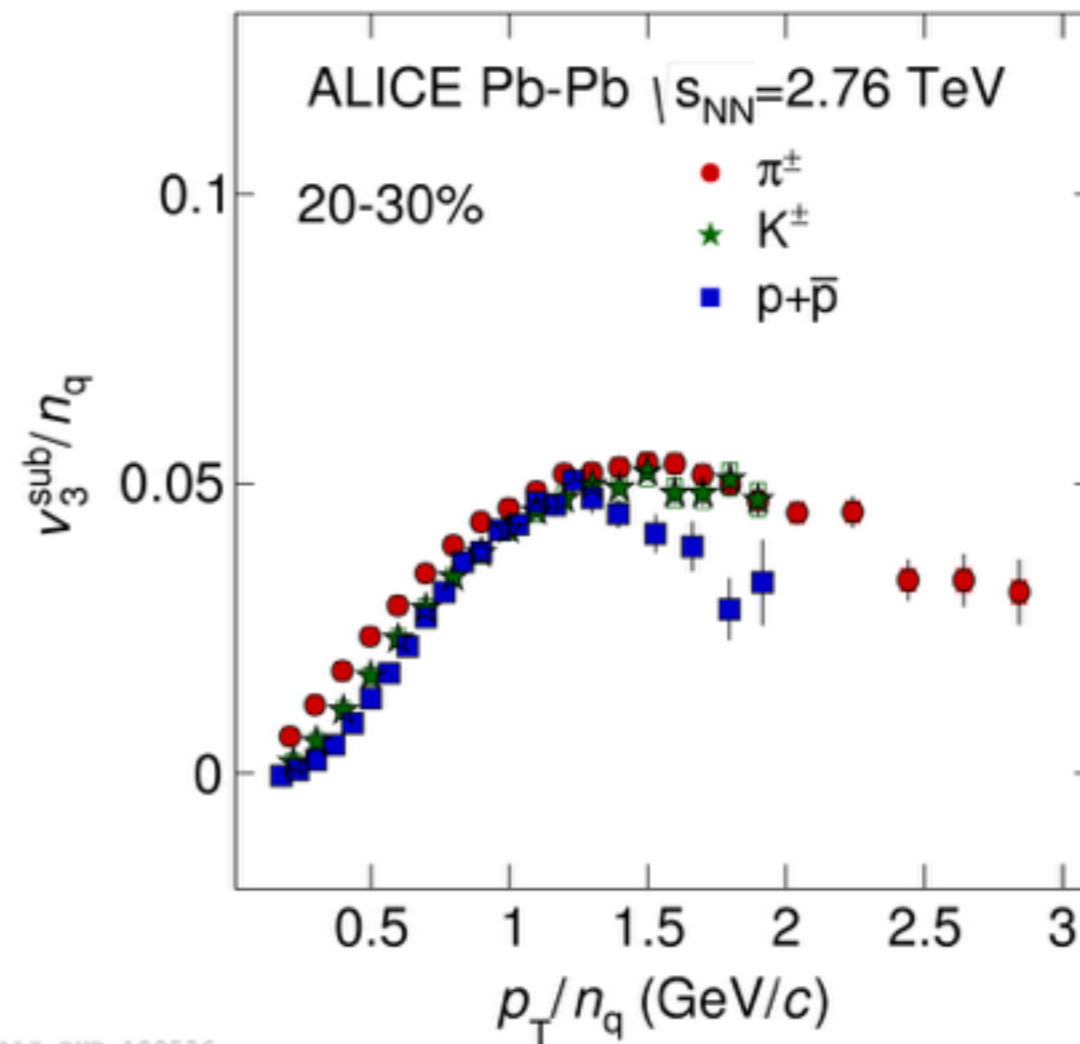
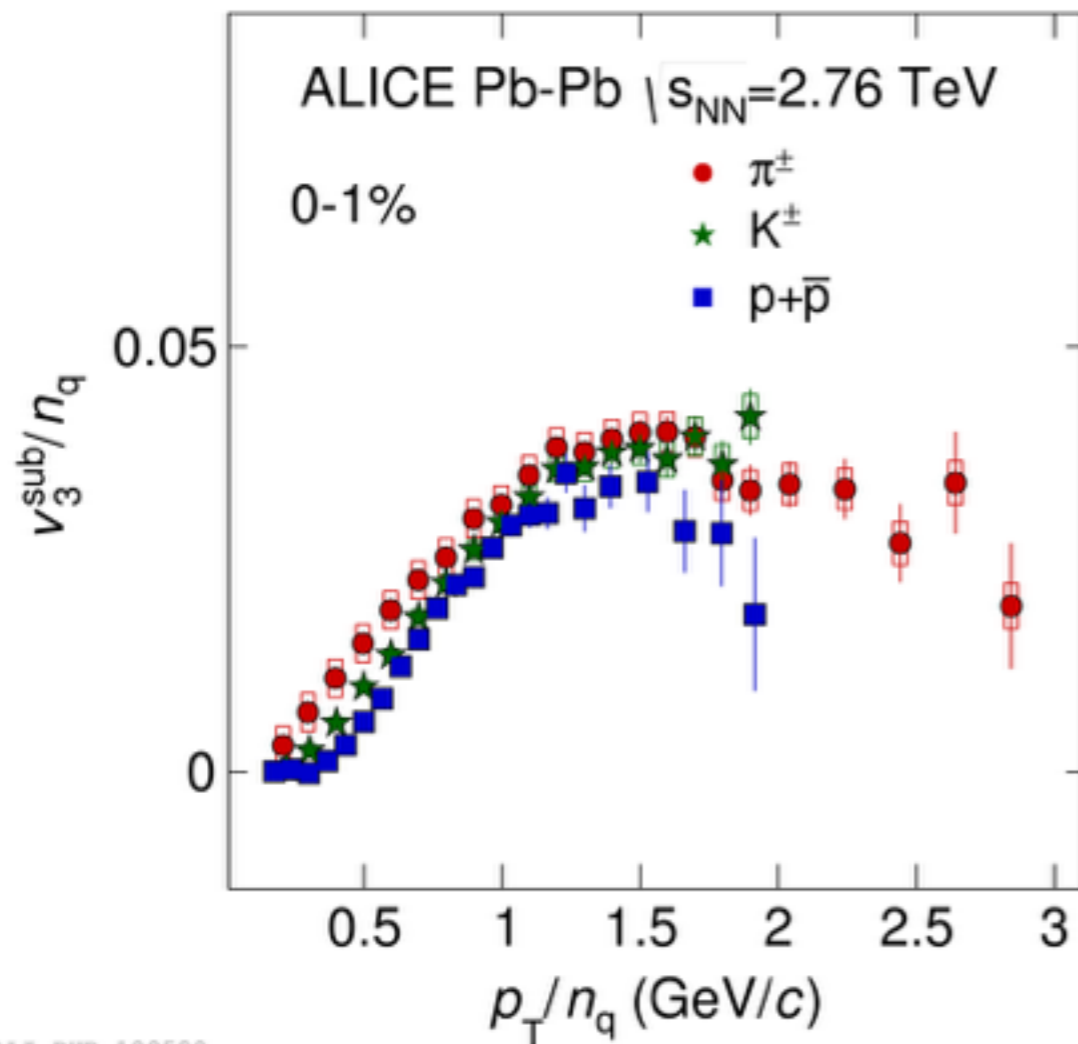


ALI-PUB-109532

- Scaling for  $v_2$ :  $\pm 20\%$

Intermediate  $p_T$  ( $p_T > 3 \text{ GeV}/c$ ):  $v_n$  of baryons  $>$   $v_n$  of mesons

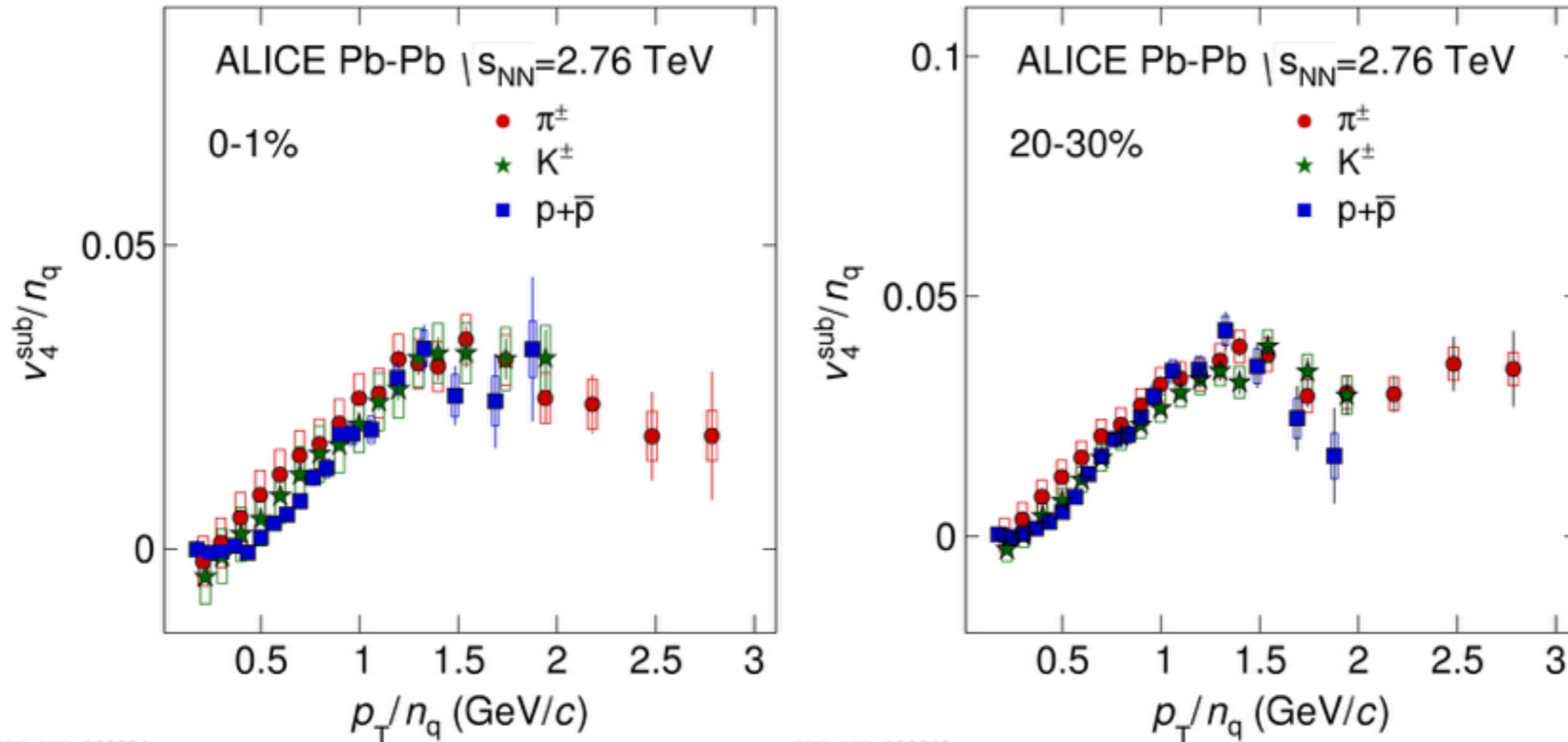
- Particle production mechanism: Quark coalescence?
- NCQ scaling:  $p_T/n_q$   $\longrightarrow$  Proposed at RHIC



- Scaling for  $v_3$ :  $\pm 20\%$  within the statistical and systematical uncertainties

Intermediate  $p_T$  ( $p_T > 3 \text{ GeV}/c$ ):  $v_n$  of baryons  $>$   $v_n$  of mesons

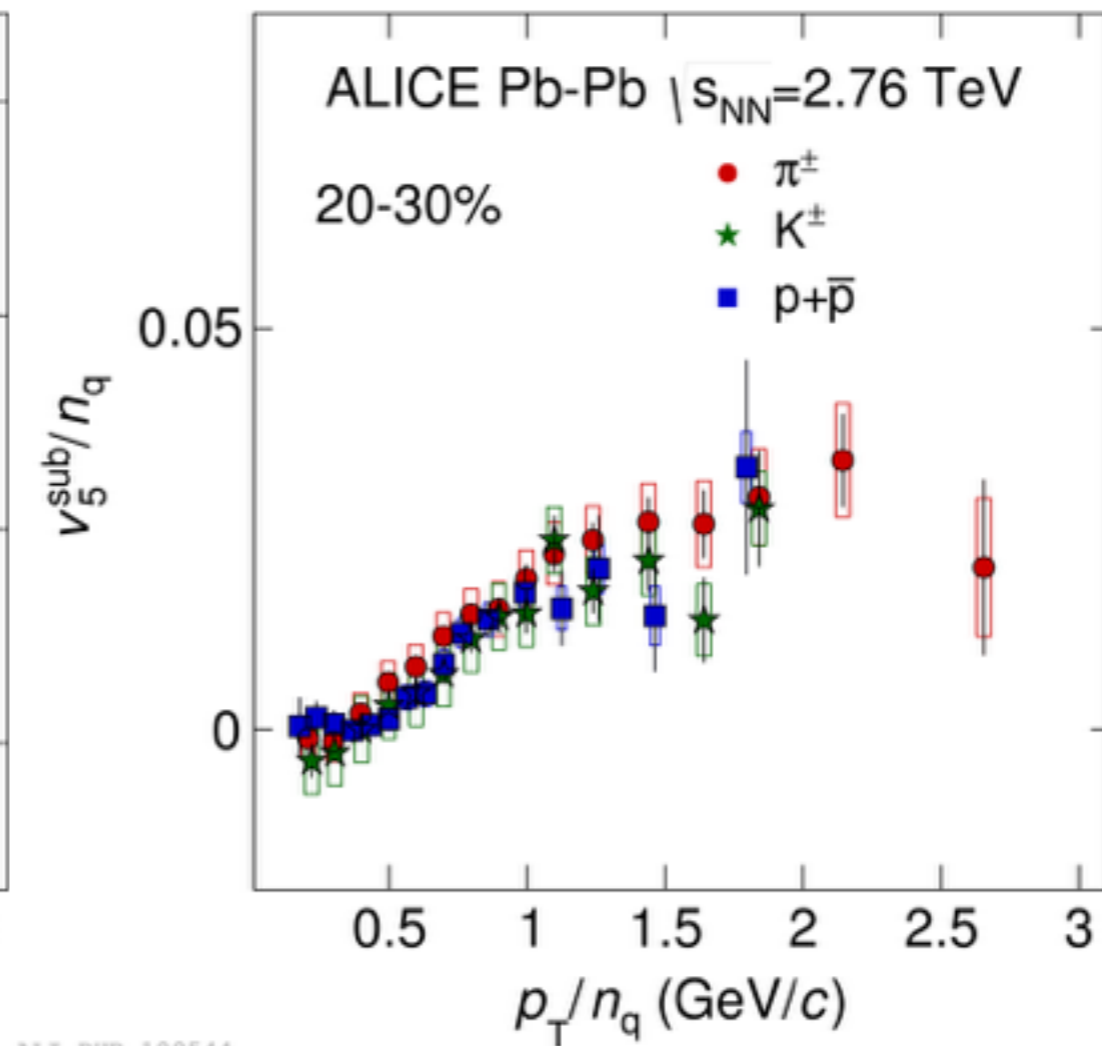
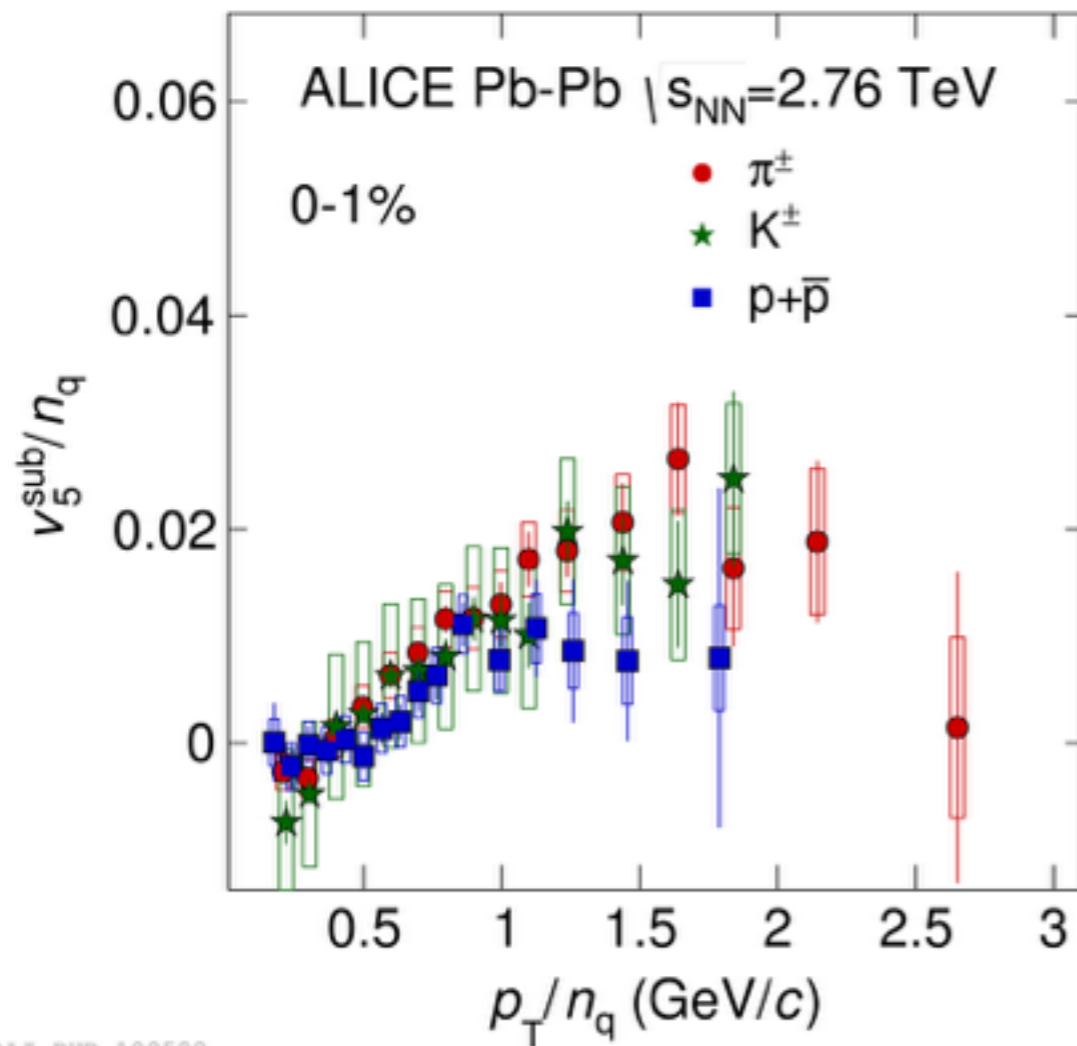
- Particle production mechanism: Quark coalescence?
- NCQ scaling:  $p_T/n_q \longrightarrow$  Proposed at RHIC



- Scaling for  $v_4$ :  $\pm 20\%$  within the statistical and systematical uncertainties

Intermediate  $p_T$  ( $p_T > 3 \text{ GeV}/c$ ):  $v_n$  of baryons  $>$   $v_n$  of mesons

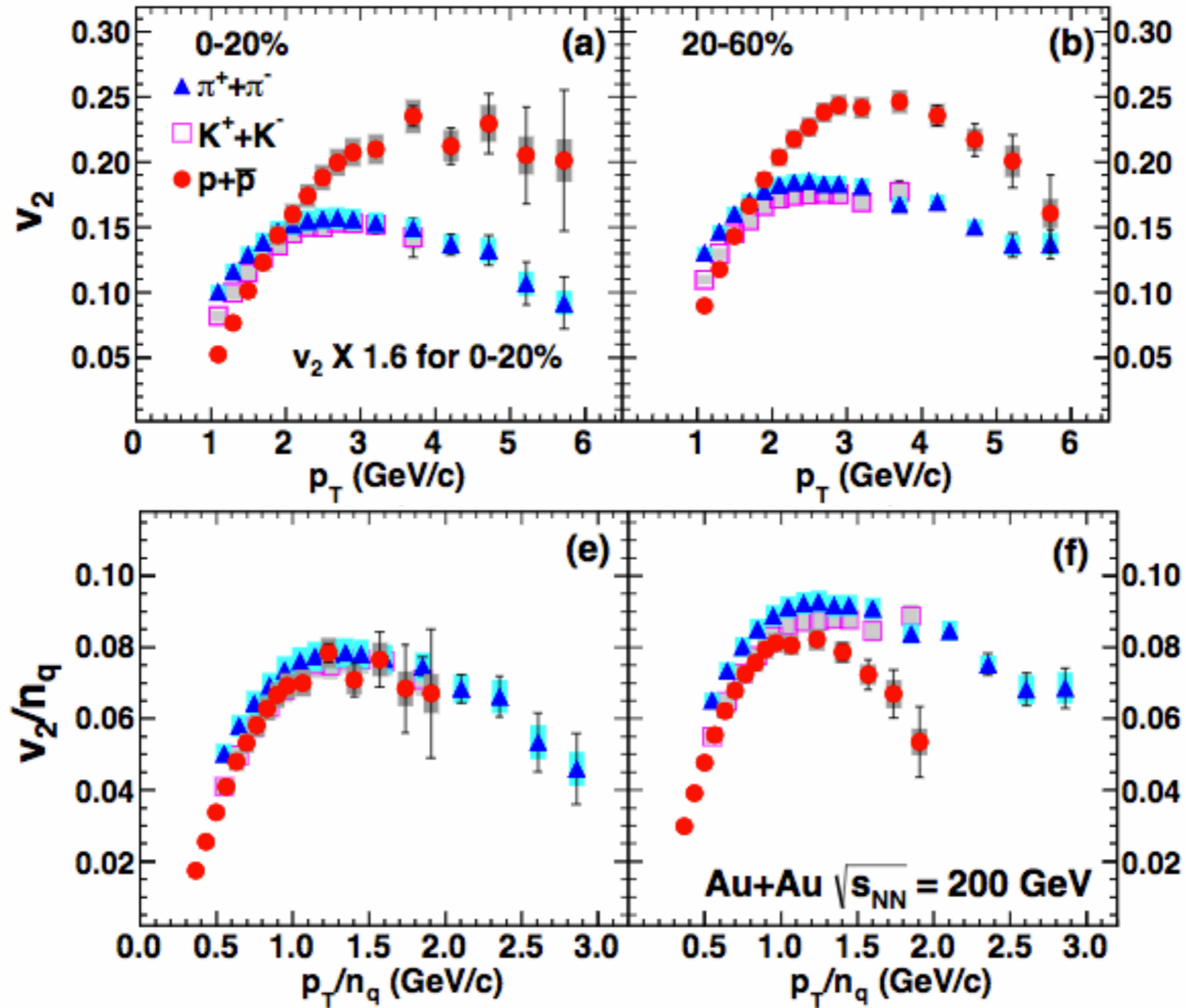
- Particle production mechanism: Quark coalescence?
- NCQ scaling:  $p_T/n_q$  Proposed at RHIC



- Scaling for  $v_5$ :  $\pm 20\%$  within the statistical and systematical uncertainties

# NCQ scaling: PHENIX

arXiv:1203.2644v1



- Different particle species are identified by requiring a minimum probability of 90%.
- for pions and protons: efficiency > 95% up to  $p_T \approx 2.5$  GeV/c, contamination < 5%
- for kaons: efficiency = 60% at 2.5 GeV/c with a minimum of 25% at 4 GeV/c, contamination < 10%

$$\begin{pmatrix} \pi_{\text{meas}} \\ K_{\text{meas}} \\ p_{\text{meas}} \end{pmatrix} = \begin{pmatrix} \epsilon_{\pi\pi} & \epsilon_{\pi K} & \epsilon_{\pi p} \\ \epsilon_{K\pi} & \epsilon_{KK} & \epsilon_{Kp} \\ \epsilon_{p\pi} & \epsilon_{pK} & \epsilon_{pp} \end{pmatrix}^T \cdot \begin{pmatrix} \pi_{\text{true}} \\ K_{\text{true}} \\ p_{\text{true}} \end{pmatrix}$$

$$\epsilon_{ii} = \frac{N_i \text{ identified as } i}{A_{\text{true}}^i} \quad \vec{A}_{\text{true}} = (\epsilon_{\text{PID}}^T)^{-1} \times \vec{A}_{\text{meas}}$$

contamination:

$$c_{ji} = \frac{N_i \text{ identified as } j}{A_{\text{meas}}^j}, i \neq j$$

$$c_{ji} = \frac{\epsilon_{ij} A_{\text{true}}^i}{\epsilon_{jj} A_{\text{true}}^j + \sum_{j \neq k} \epsilon_{jk} A_{\text{true}}^k}$$

