



U.S. DEPARTMENT OF  
**ENERGY**

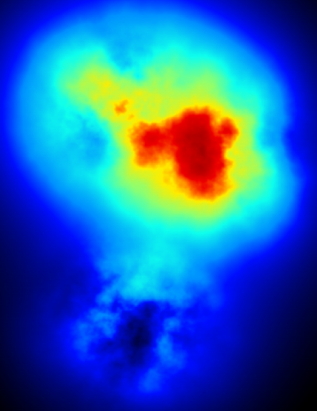
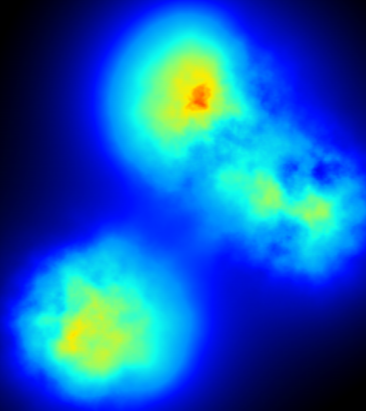
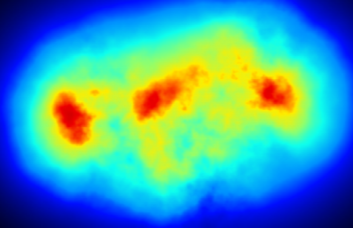
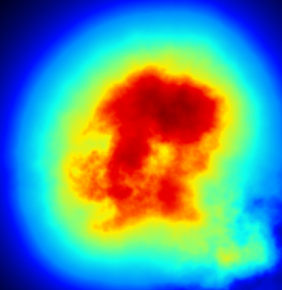
Office of  
Science

**BROOKHAVEN**  
NATIONAL LABORATORY

# COLLECTIVITY IN SMALL SYSTEMS: INITIAL CORRELATIONS OR FINAL STATE FLOW?

Björn Schenke

Brookhaven National Laboratory



June 28, 2016

Strangeness in Quark Matter

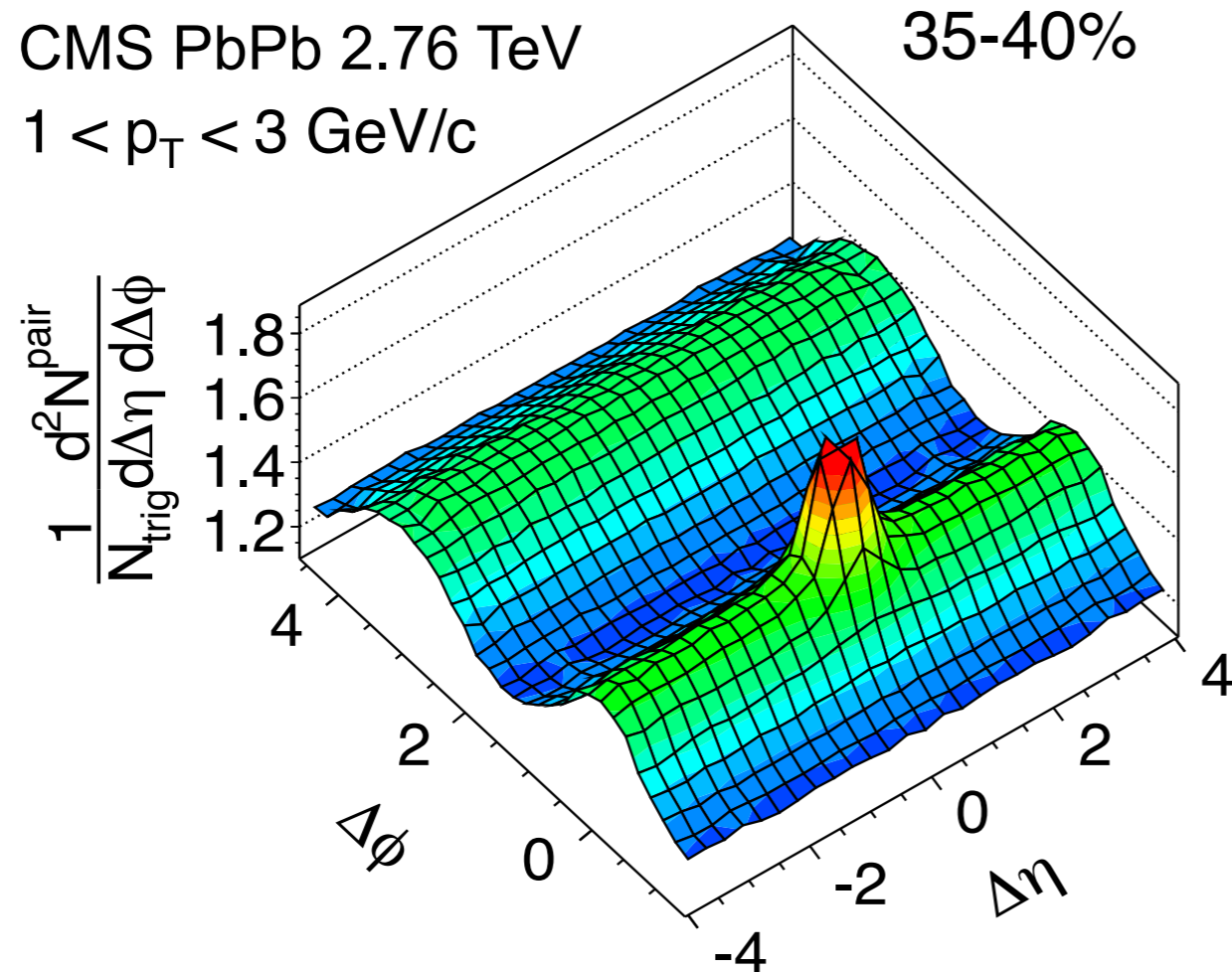
UC Berkeley

# TWO PARTICLE CORRELATIONS

2-particle correlation as a function of  $\Delta\eta$  and  $\Delta\phi$

$\Delta\eta$ : DIFFERENCE IN PSEUDO-RAPIDITY

$\Delta\phi$ : DIFFERENCE IN AZIMUTHAL ANGLE



**Ridge:**

Structure that is long range in  $\Delta\eta$  and generally shows two bumps in  $\Delta\phi$   
"double-ridge"

# RIDGE IN HEAVY ION COLLISIONS

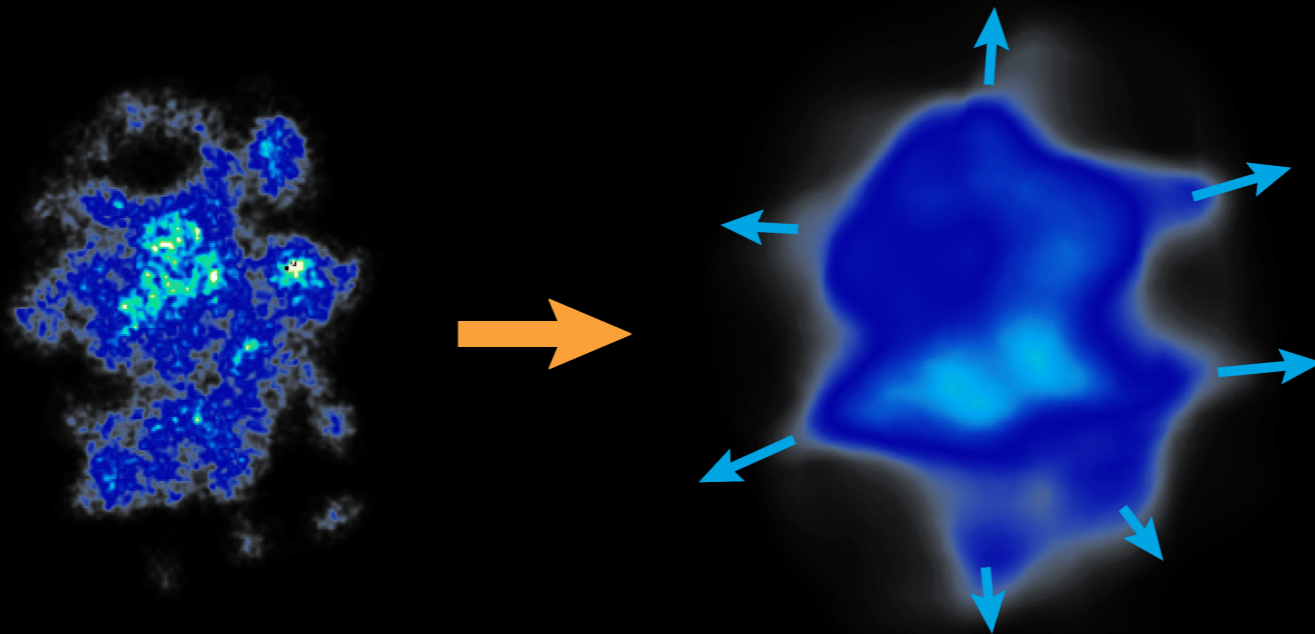
First seen in heavy ion collisions at RHIC

STAR COLLABORATION, PHYS. REV. C80 (2009) 064912

PHOBOS COLLABORATION, PHYS. REV. LETT. 104 (2010) 062301

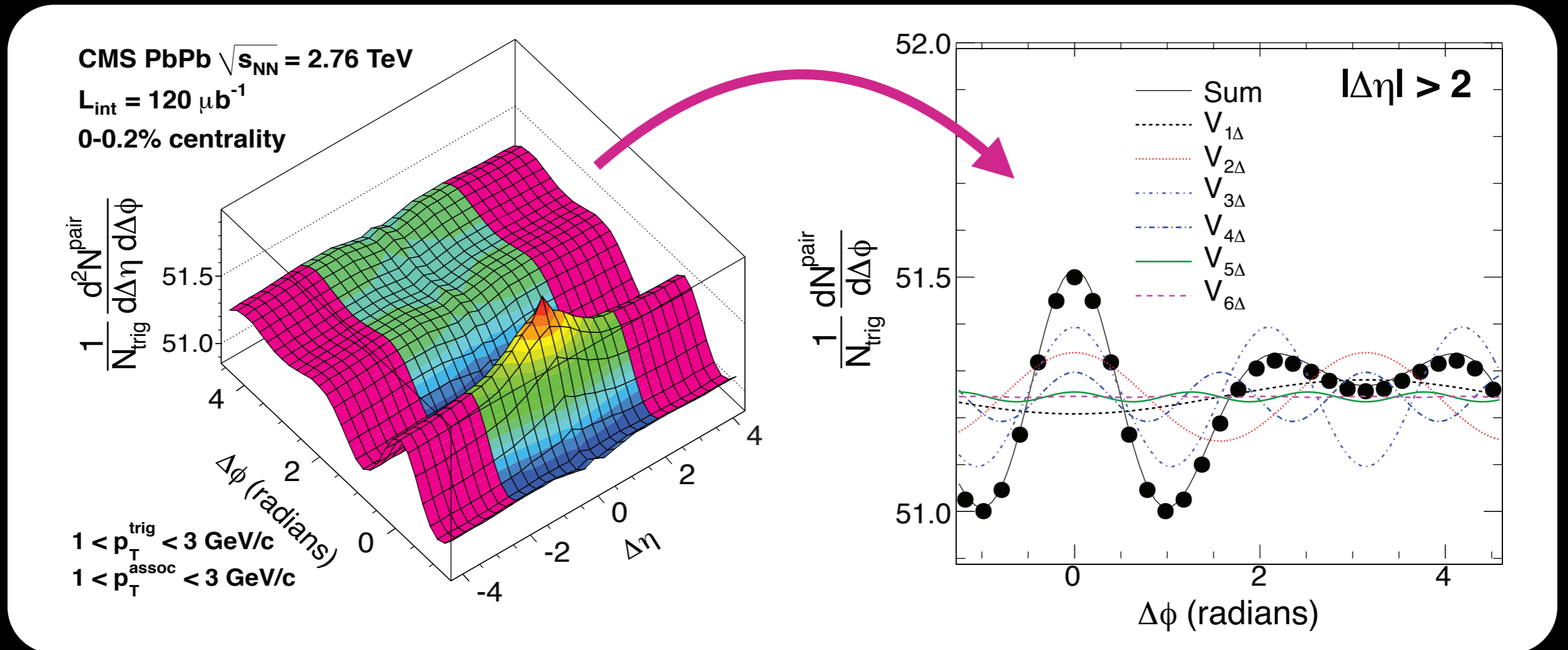
Interpretation in heavy ion collision:

- Long range correlations emerging from early times (causality)
- Azimuthal structure formed by the medium response to the initial transverse geometry (well described by hydrodynamics)



# RIDGE IN HEAVY ION COLLISIONS

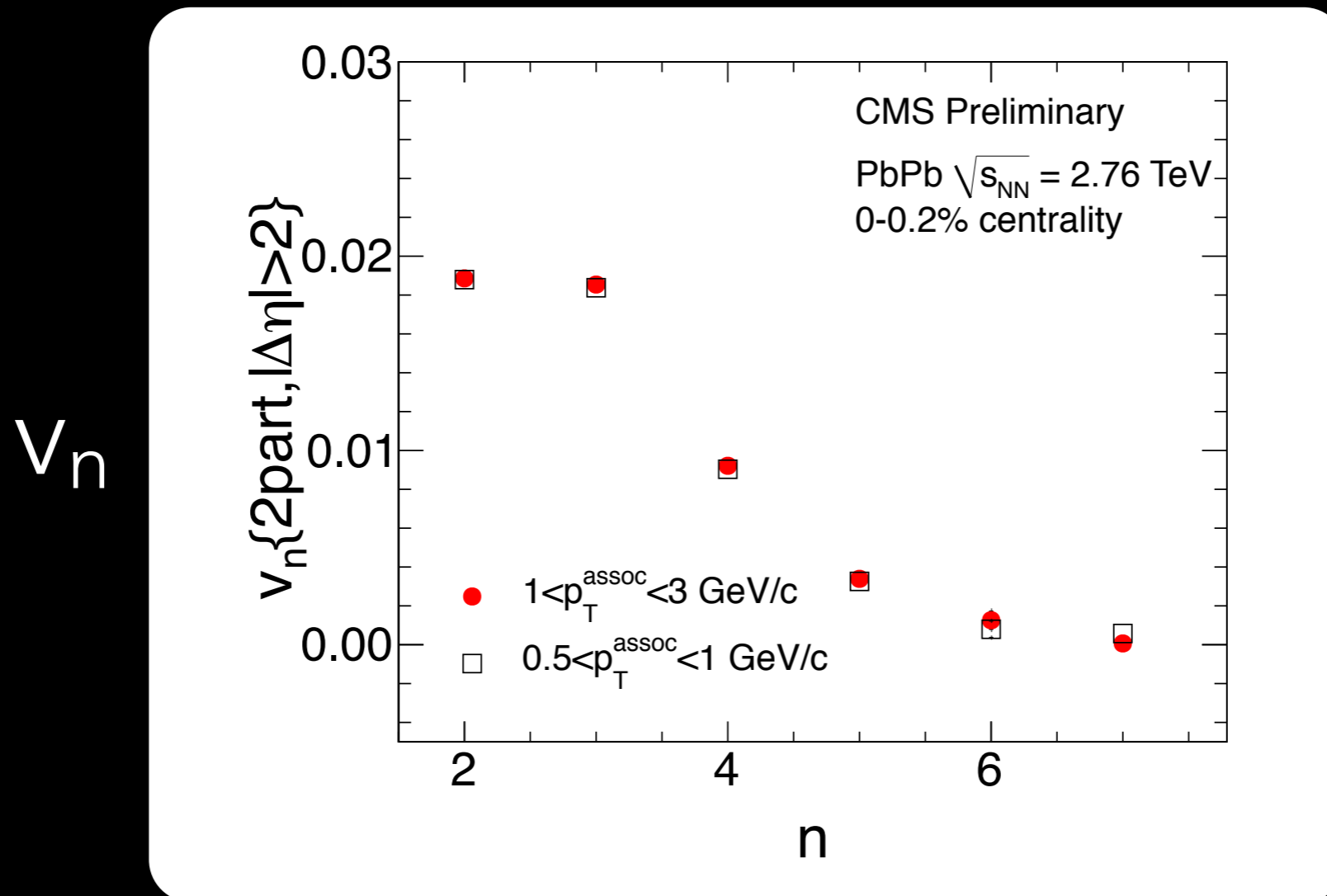
Azimuthal structure quantified using Fourier expansion



$$\frac{1}{N_{trig}} \frac{dN^{pair}}{d\Delta\phi} \sim 1 + 2 \sum_{n=1}^{n=\infty} V_{n\Delta}(p_T^{trig}, p_T^{assoc}) \cos(n\Delta\phi) \quad v_n = \sqrt{V_{n\Delta}}$$

# RIDGE IN HEAVY ION COLLISIONS

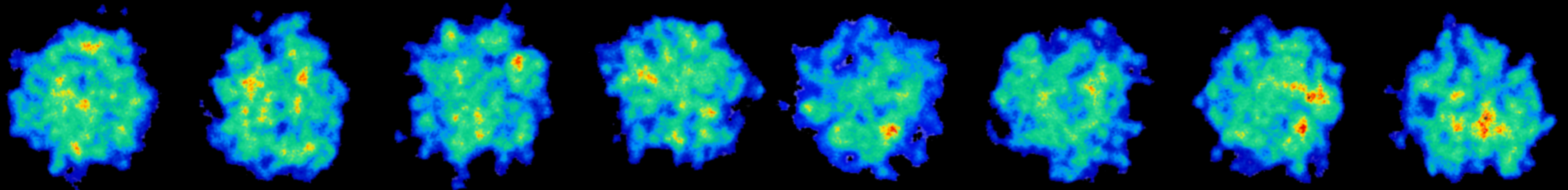
Azimuthal structure quantified using Fourier expansion



$$\frac{1}{N_{trig}} \frac{dN^{pair}}{d\Delta\phi} \sim 1 + 2 \sum_{n=1}^{n=\infty} V_{n\Delta}(p_T^{trig}, p_T^{assoc}) \cos(n\Delta\phi) \quad v_n = \sqrt{V_{n\Delta}}$$

# THEORETICAL DESCRIPTION IN HEAVY IONS

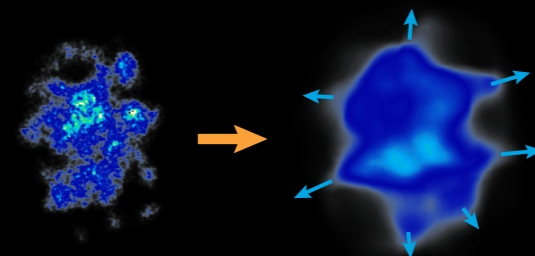
Fluctuating nucleon positions and color charges →  
Fluctuating deposited energy



High energy: Initial energy density can be computed in the  
color glass condensate framework (effective theory of QCD)  
It includes gluon saturation at high densities  
( small  $x$  and small transverse momentum  $p_T \lesssim Q_s$  )

B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL108, 252301 (2012), PRC86, 034908 (2012)

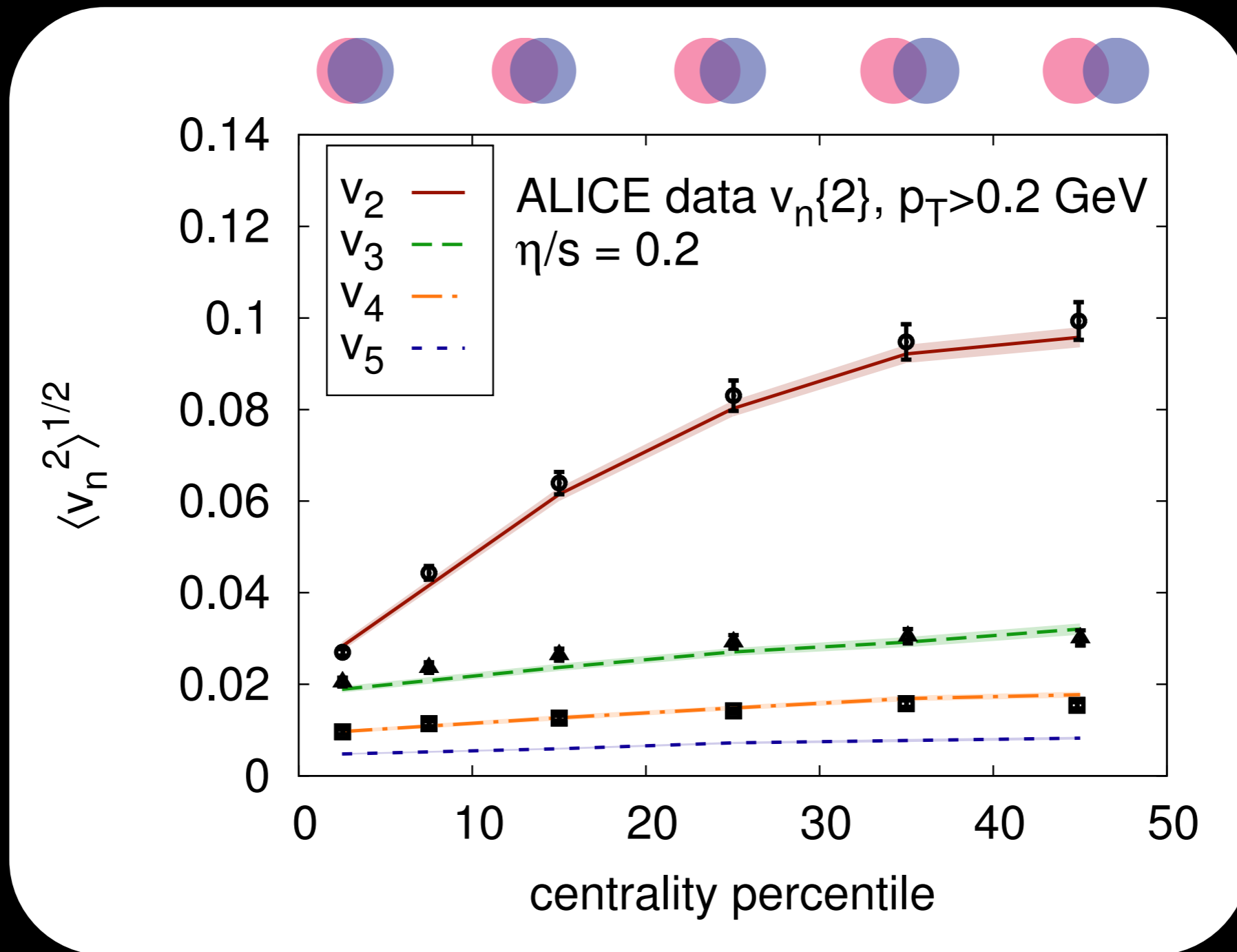
Pressure gradients drive the evolution  
Described by hydrodynamics



C.GALE, S.JEON, B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL110, 012302 (2013)

# COMPARISON OF THEORY TO EXPERIMENT

C. GALE, S. JEON, B.SCHENKE, P.TRIBEDY, R.VENUGOPALAN, PRL110, 012302 (2013)



Quantitative description of the experimental data!

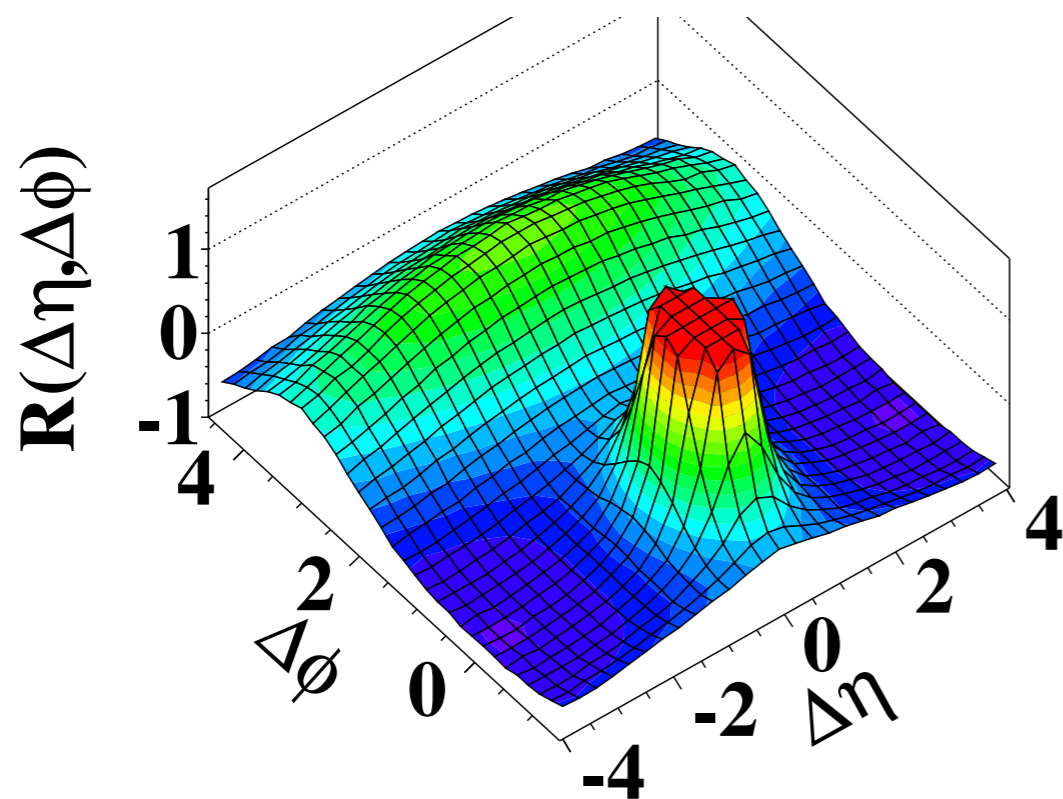
ALICE COLLABORATION, PHYS. REV. LETT. 107, 032301 (2011)

# RIDGE IN SMALL COLLISION SYSTEMS

minimum bias p+p

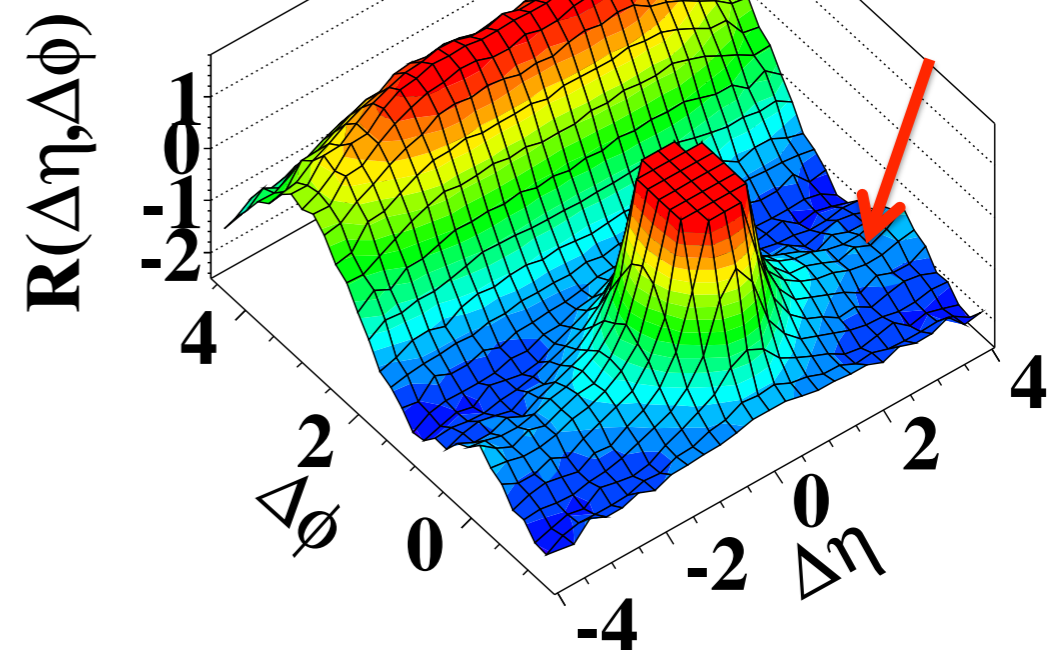
high multiplicity p+p

CMS MinBias,  $1.0\text{GeV}/c < p_T < 3.0\text{GeV}/c$



CMS pp 7 TeV,  $N_{\text{trk}} > 110$

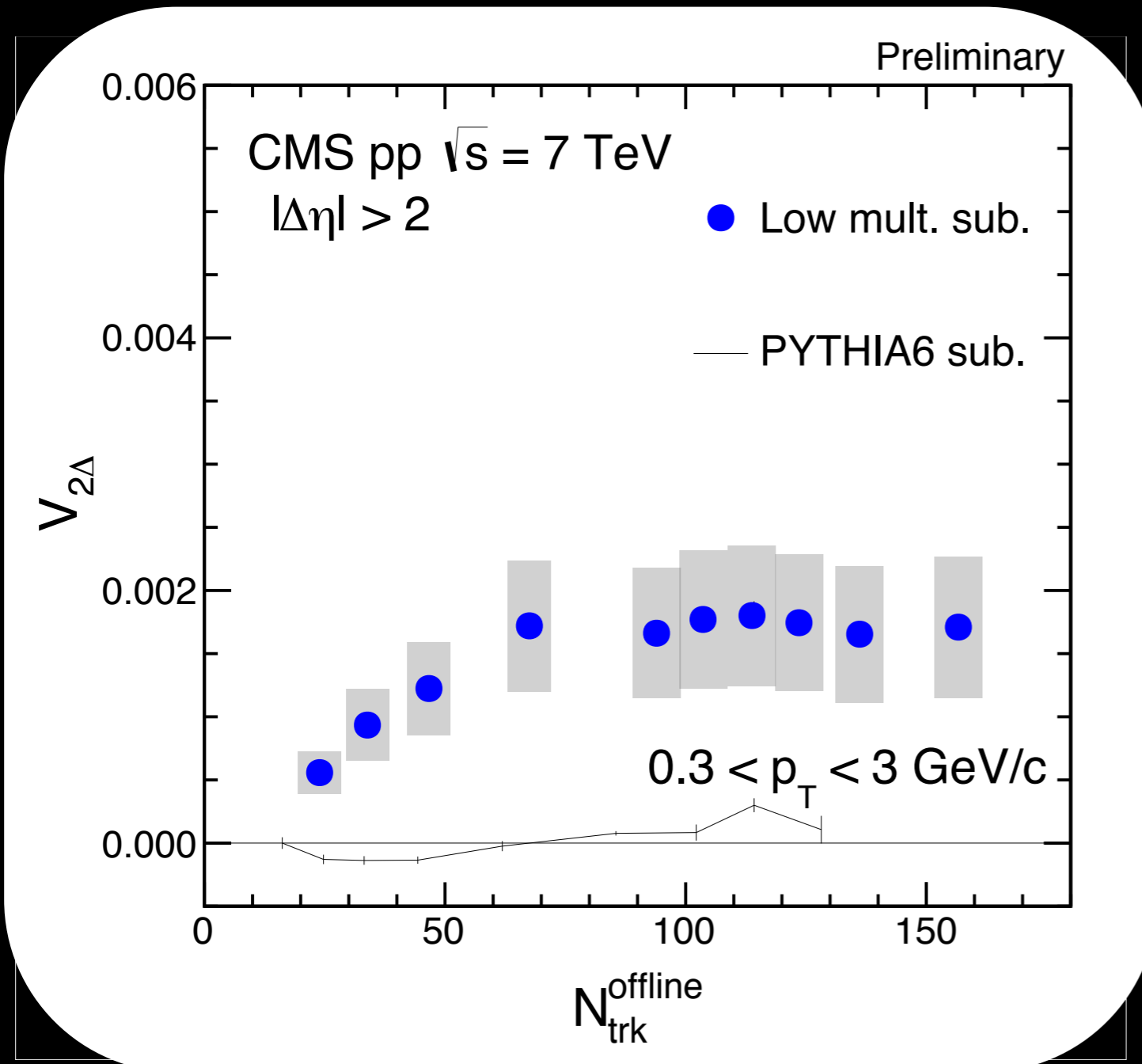
$1 < p_T < 3 \text{ GeV}/c$





# $V_{2\Delta}$ IN p+p COLLISIONS

Result after correcting for back-to-back jet correlations estimated from low multiplicity events



No ridge in PYTHIA

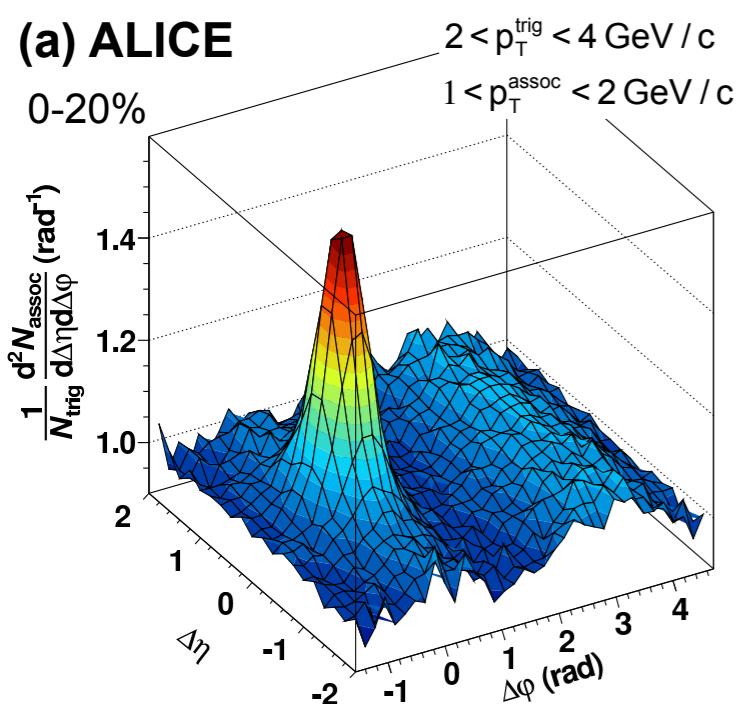
CMS PAS HIN-15-009

# RIDGE IN p+Pb COLLISIONS

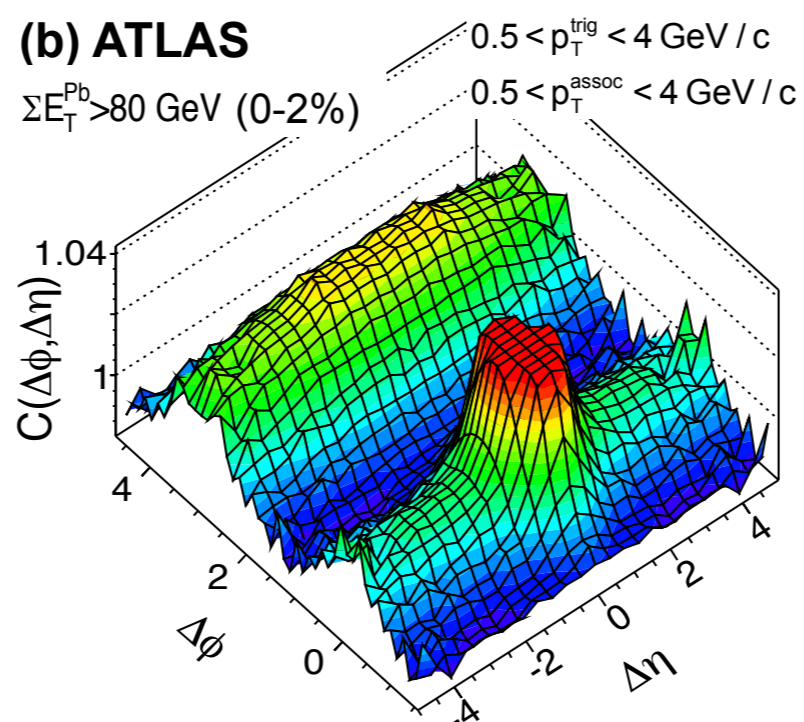
high multiplicity p+Pb

pPb  $\sqrt{s_{NN}} = 5.02$  TeV at the LHC

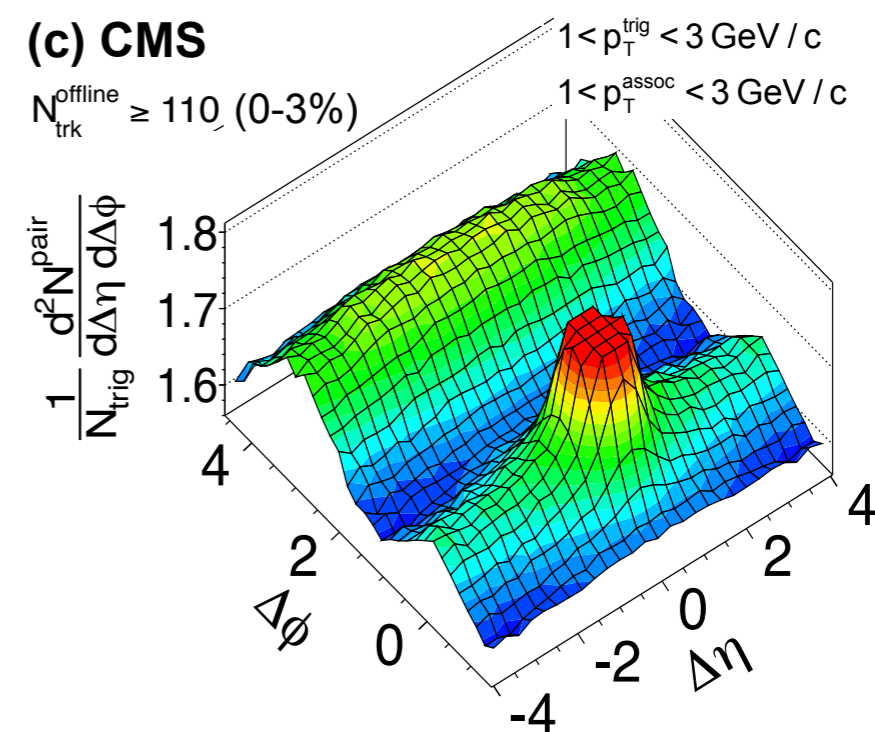
(a) ALICE



(b) ATLAS



(c) CMS

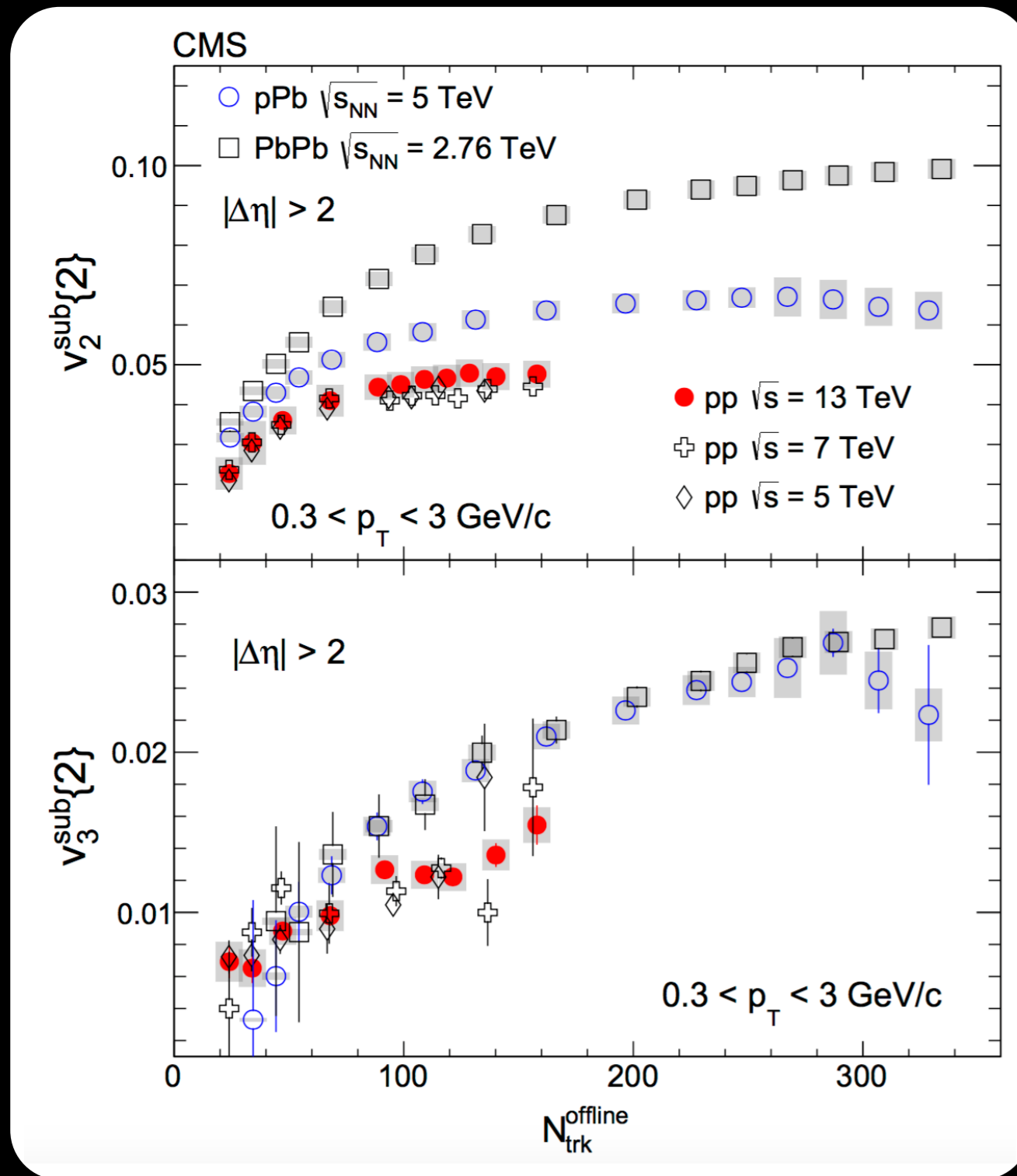


ALICE COLLABORATION, PHYS. LETT. B 719 (2013) 29

ATLAS COLLABORATION, PHYS. REV. LETT. 110 (2013) 182302

CMS COLLABORATION, PHYS. LETT. B 718 (2013) 795

# $v_2$ IN p+p, p+Pb, Pb+Pb COLLISIONS



SEE ALSO:

ALICE COLLABORATION  
 PHYS. LETT. B719 (2013) 29-41; PHYS.  
 REV. C 90, 054901

ATLAS COLLABORATION  
 PHYS. REV. LETT. 110, 182302 (2013);  
 PHYS. REV. C 90.044906 (2014)

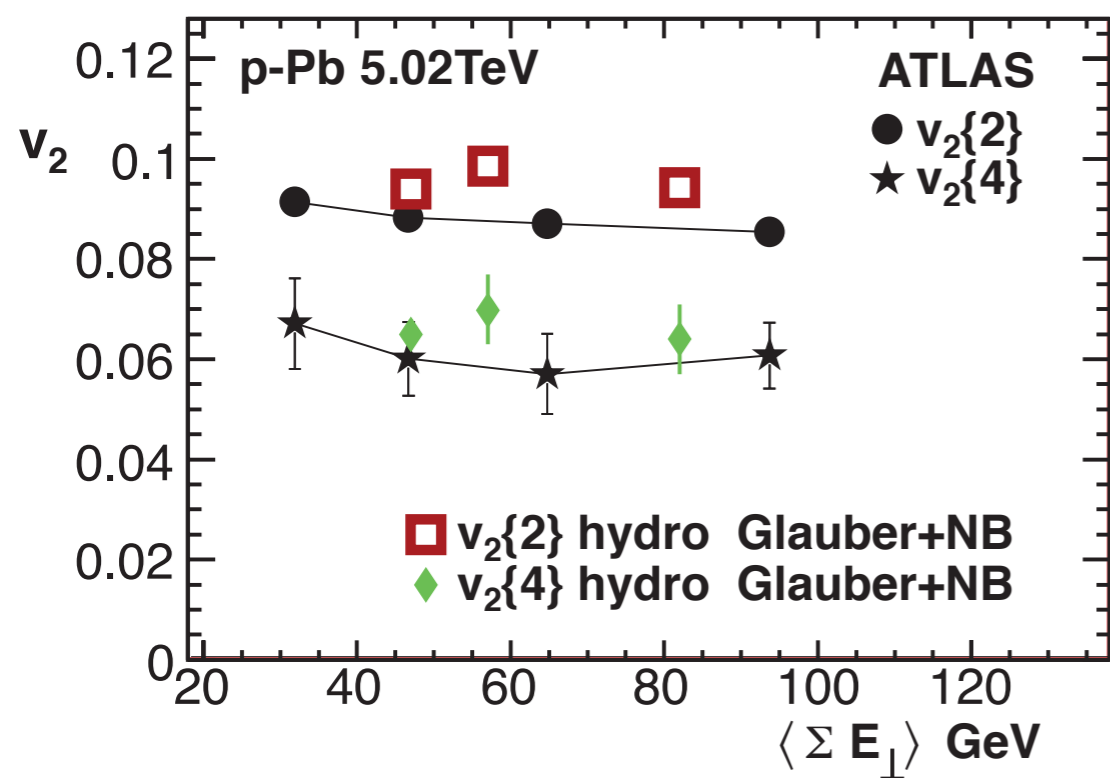
CMS COLLABORATION  
 PHYS.REV.LETT. 115, 012301 (2015)



CMS COLLABORATION, ARXIV:1606.06198

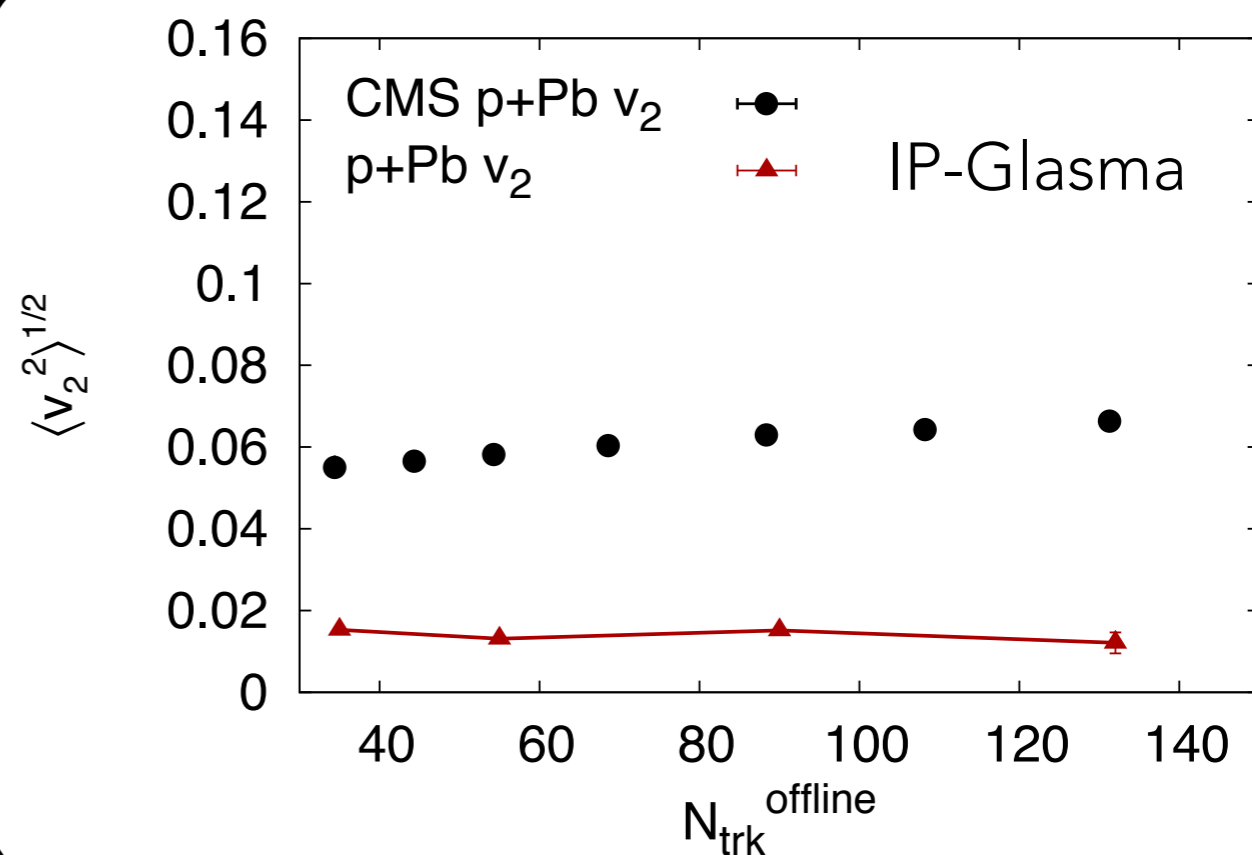
# STRONG FINAL STATE EFFECTS IN SMALL SYSTEMS? EVEN HYDRODYNAMICS?

Simple initial state  
+ hydro works



BOZEK, BRONIOWSKI  
PRC88 (2013) 014903

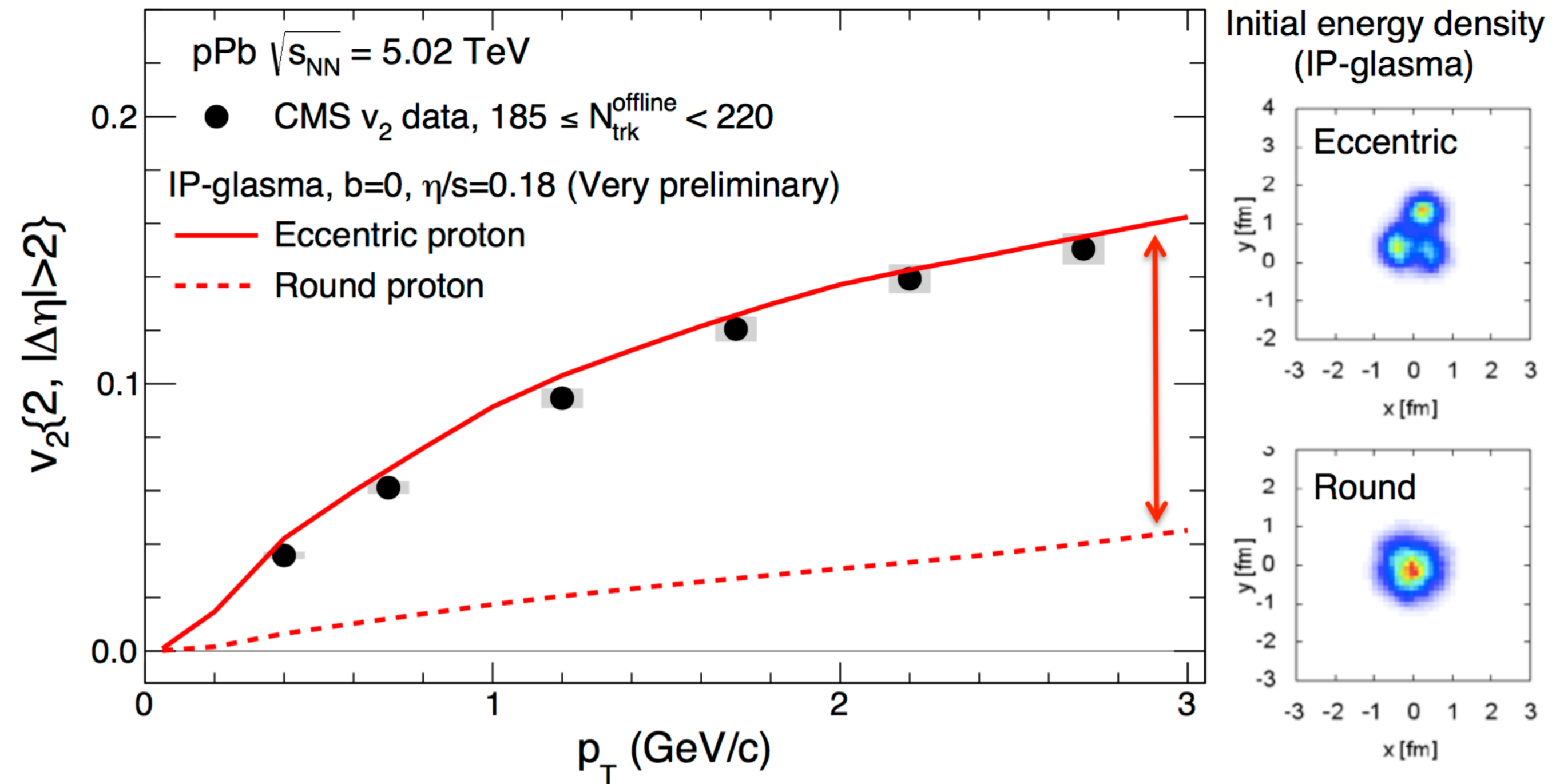
Calculation I showed before  
does not work in p+Pb



SCHENKE, VENUGOPALAN  
PRL113 (2014) 102301

OTHER CALCULATIONS: KOZLOV, LUZUM, DENICOL, JEON, GALE; WERNER, GUIOT, KARPENKO, PIEROG; ROMATSCHKE, ...

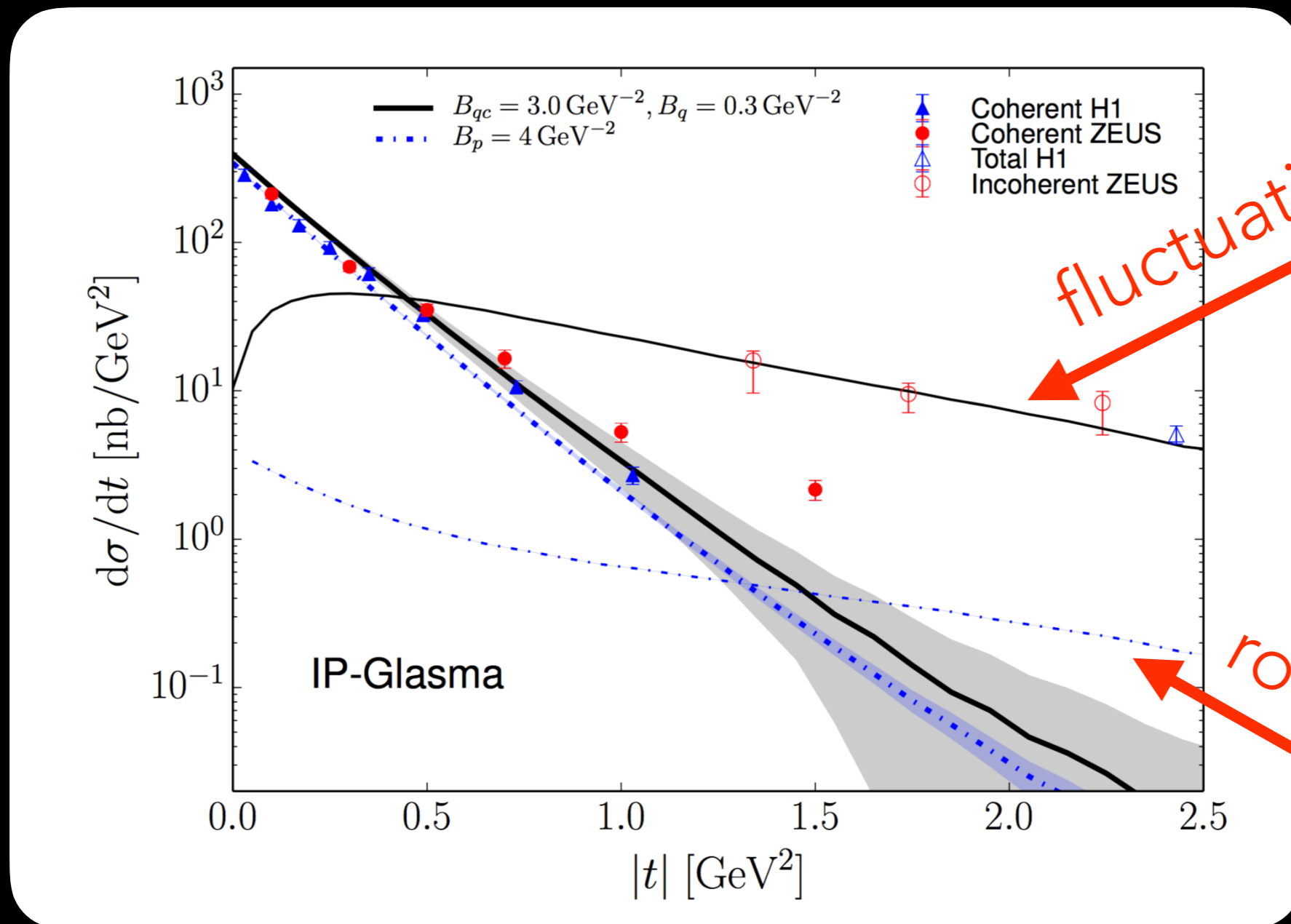
# WITH FLUCTUATING PROTON IP-GLASMA **DOES** DESCRIBE p+Pb $v_2$



# MORE EVIDENCE FOR PROTON SHAPE FLUCTUATIONS

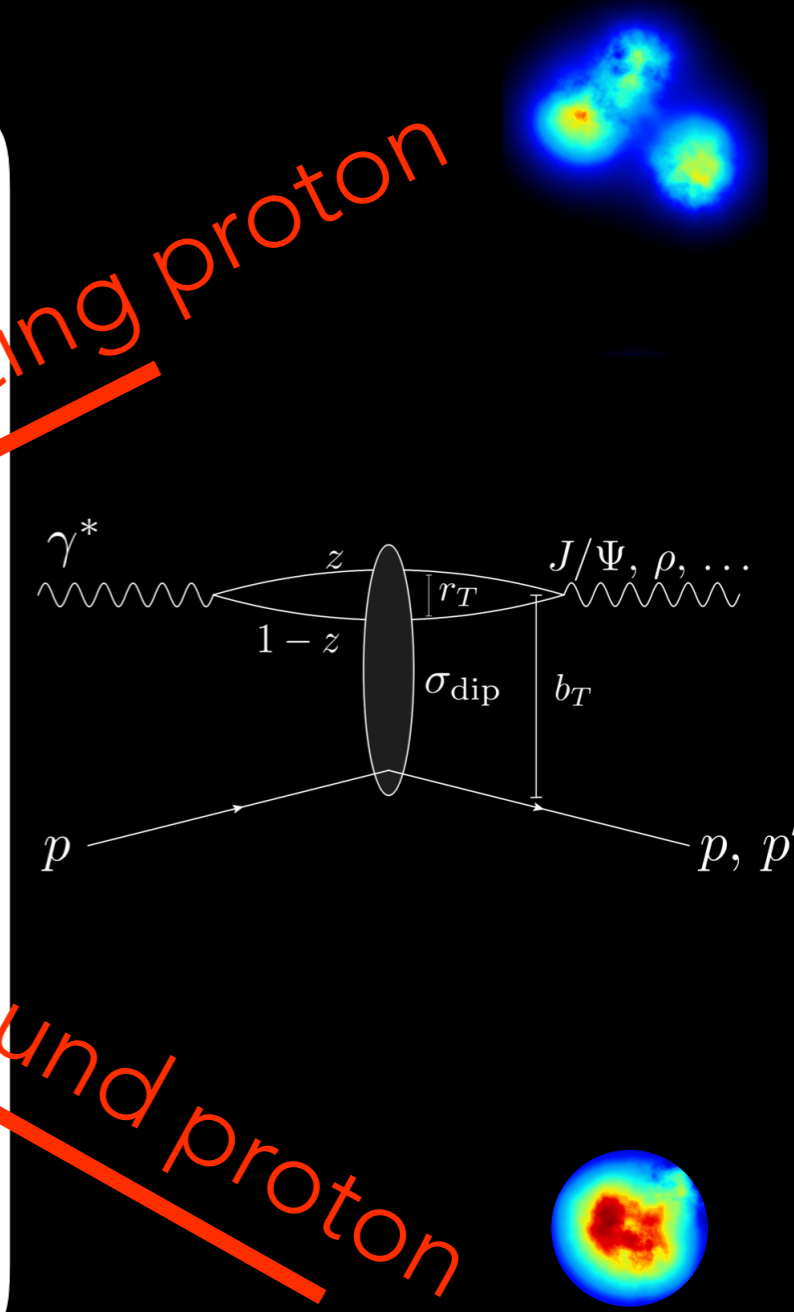
H. MÄNTYSAARI, B. SCHENKE, ARXIV:1603.04349, PRL IN PRINT

## Exclusive diffractive $J/\Psi$ production



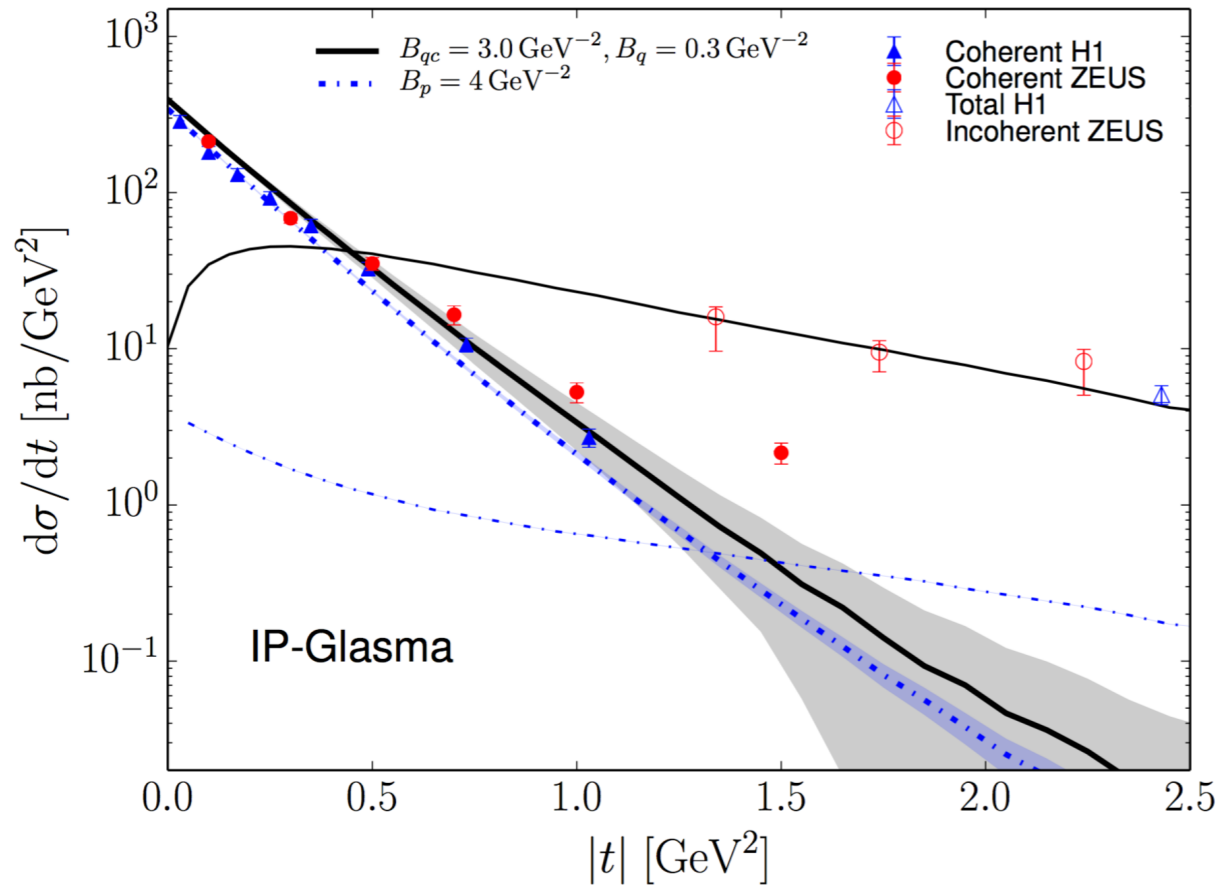
fluctuating proton

round proton

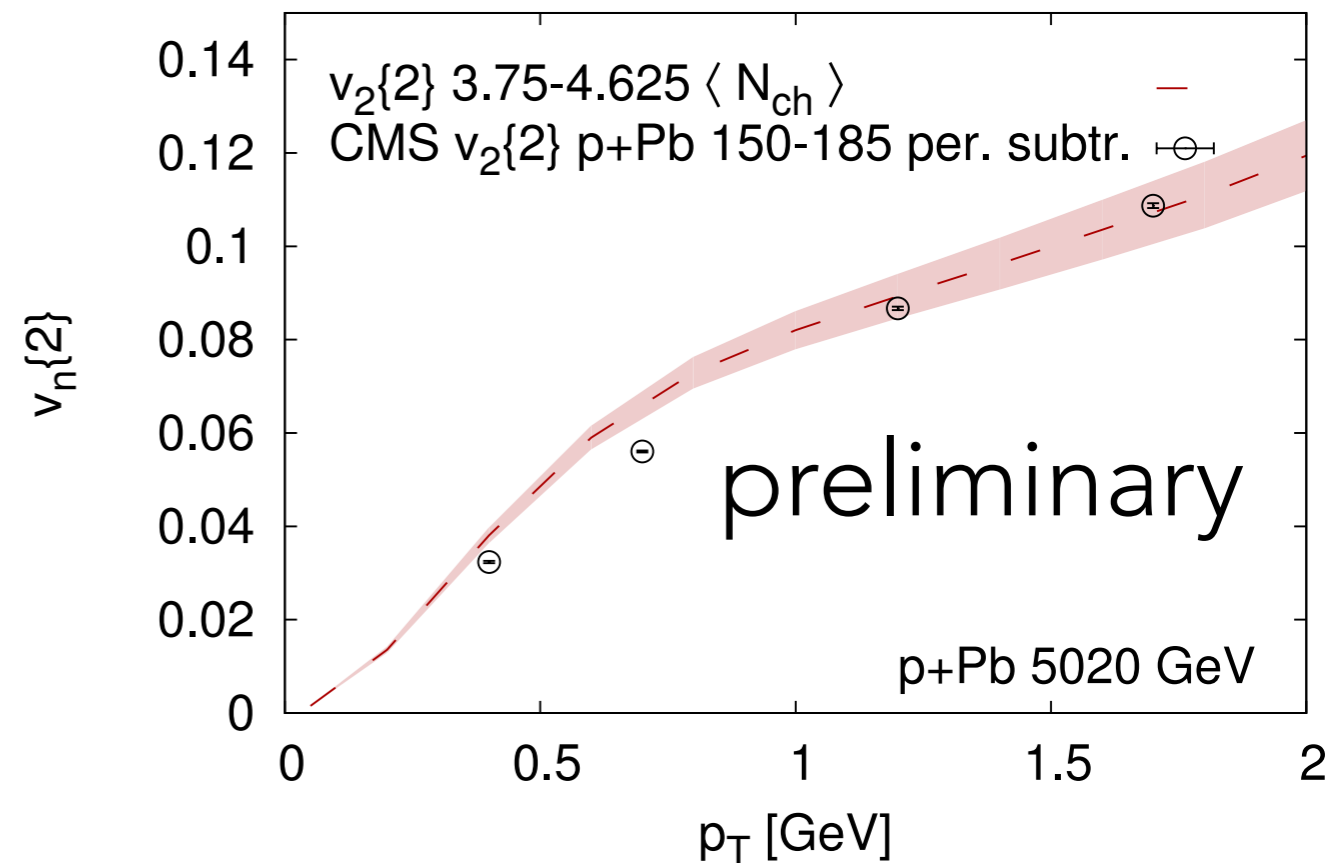


# STRATEGY: CONSTRAIN PROTON FLUCTUATIONS WITH J/ $\Psi$ PRODUCTION AND PREDICT FLOW IN p+Pb COLLISIONS

H. MÄNTYSAARI, P. TRIBEDY, B. SCHENKE, IN PREPARATION



Use constrained proton to predict  $v_2$  in p+Pb collisions

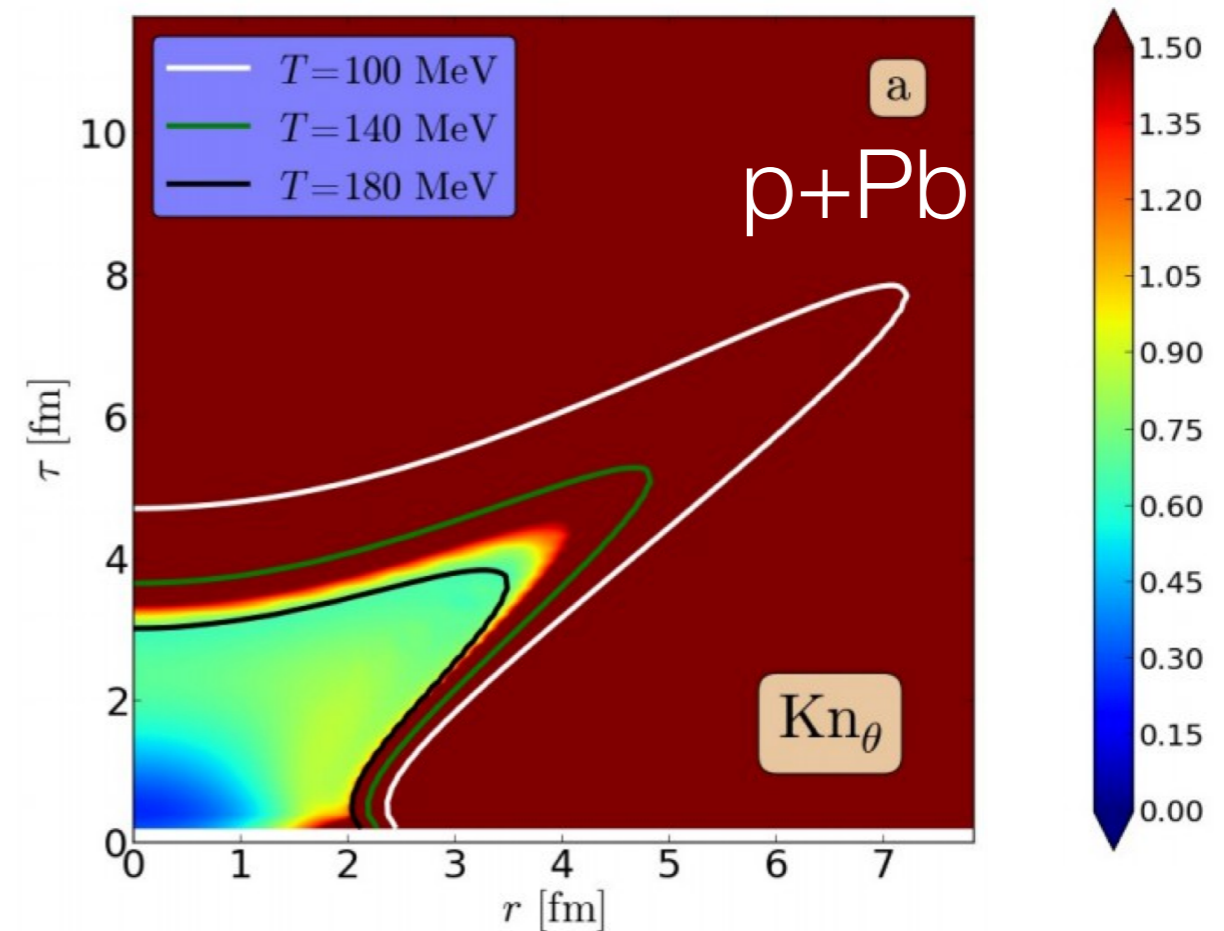
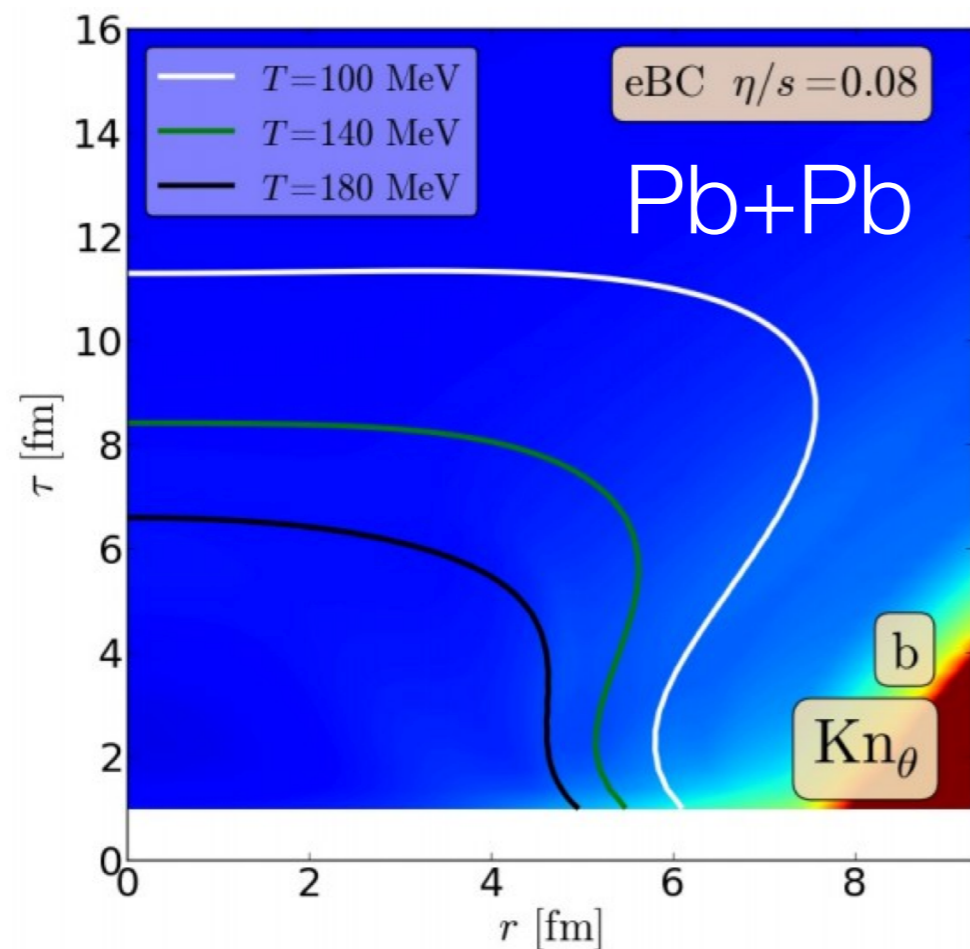


Temperature dependent  $\eta/s$  constrained in A+A collisions

G. DENICOL, A. MONNAI, B. SCHENKE  
 PHYS.REV.LETT. 116 (2016) NO.21, 212301

# PROBLEM WITH HYDRODYNAMICS

Knudsen number: ratio of a microscopic to a macroscopic scale  
Small Knudsen number means hydrodynamics is valid



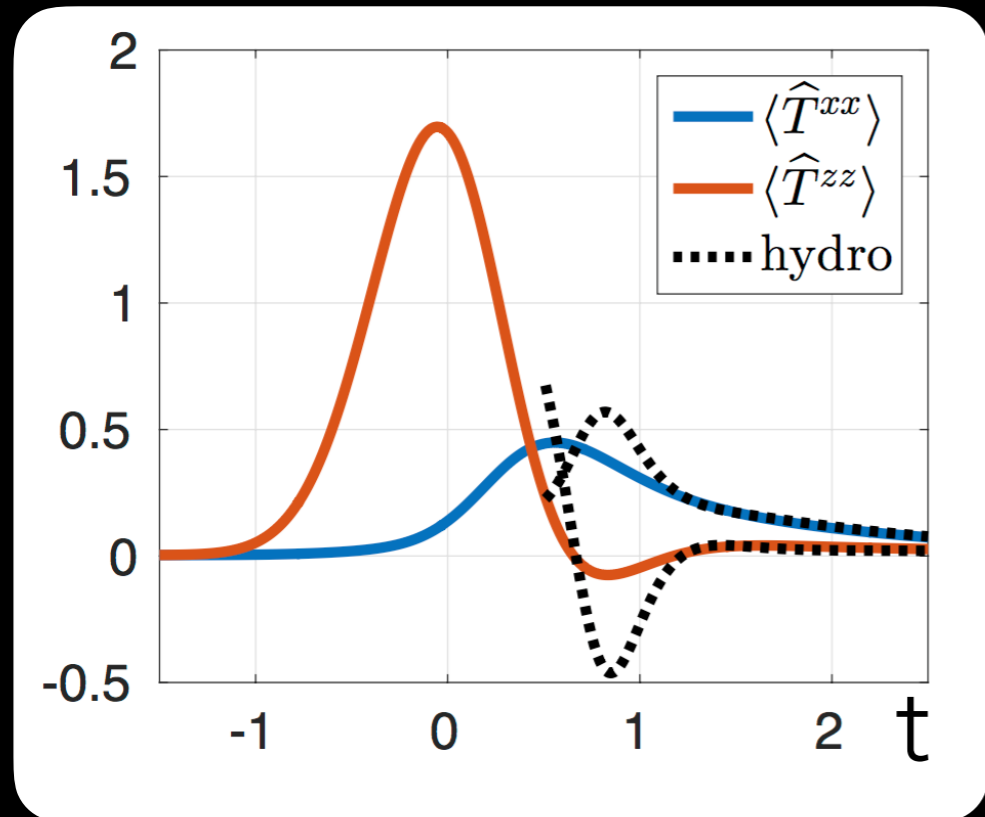
H. NIEMI, G.S. DENICOL, E-PRINT: ARXIV:1404.7327



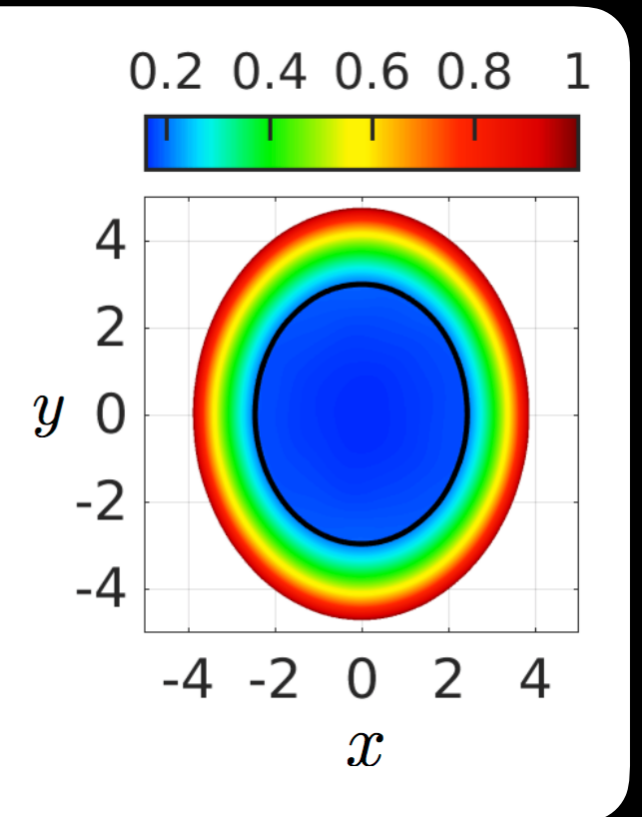
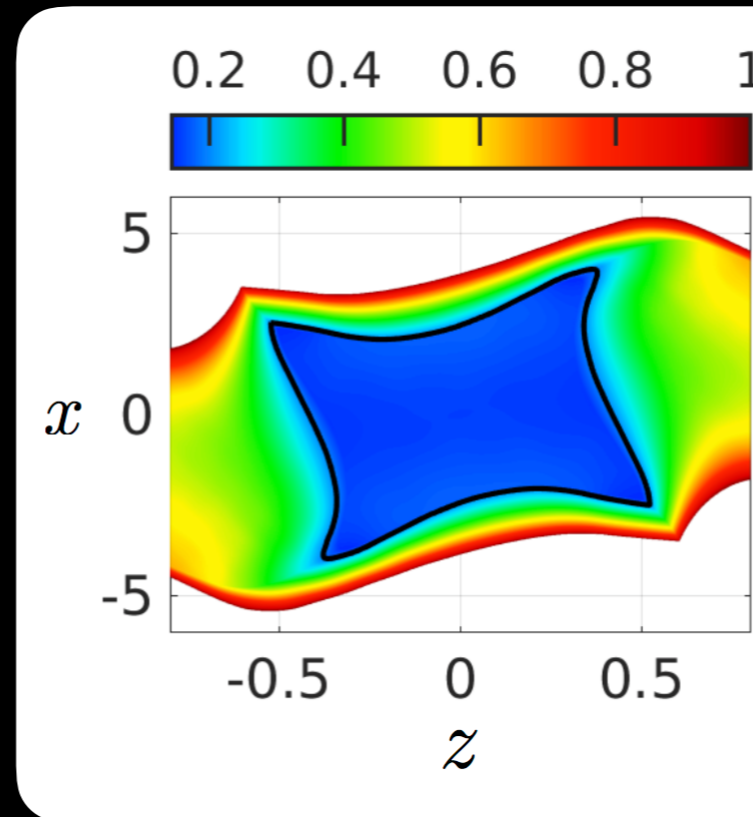
# BUT ADS/CFT SAYS IT'S OK

P. CHESLER, JHEP 1603 (2016) 146

Degree of "hydrodynamization"  $\Delta(t, \mathbf{x}) \equiv \max_{t' \geq t} \left[ \frac{||\langle T^{\mu\nu}(t', \mathbf{x}) \rangle - T_{\text{hydro}}^{\mu\nu}(t', \mathbf{x})||}{p(t', \mathbf{x})} \right]$



$x=y=z=0$

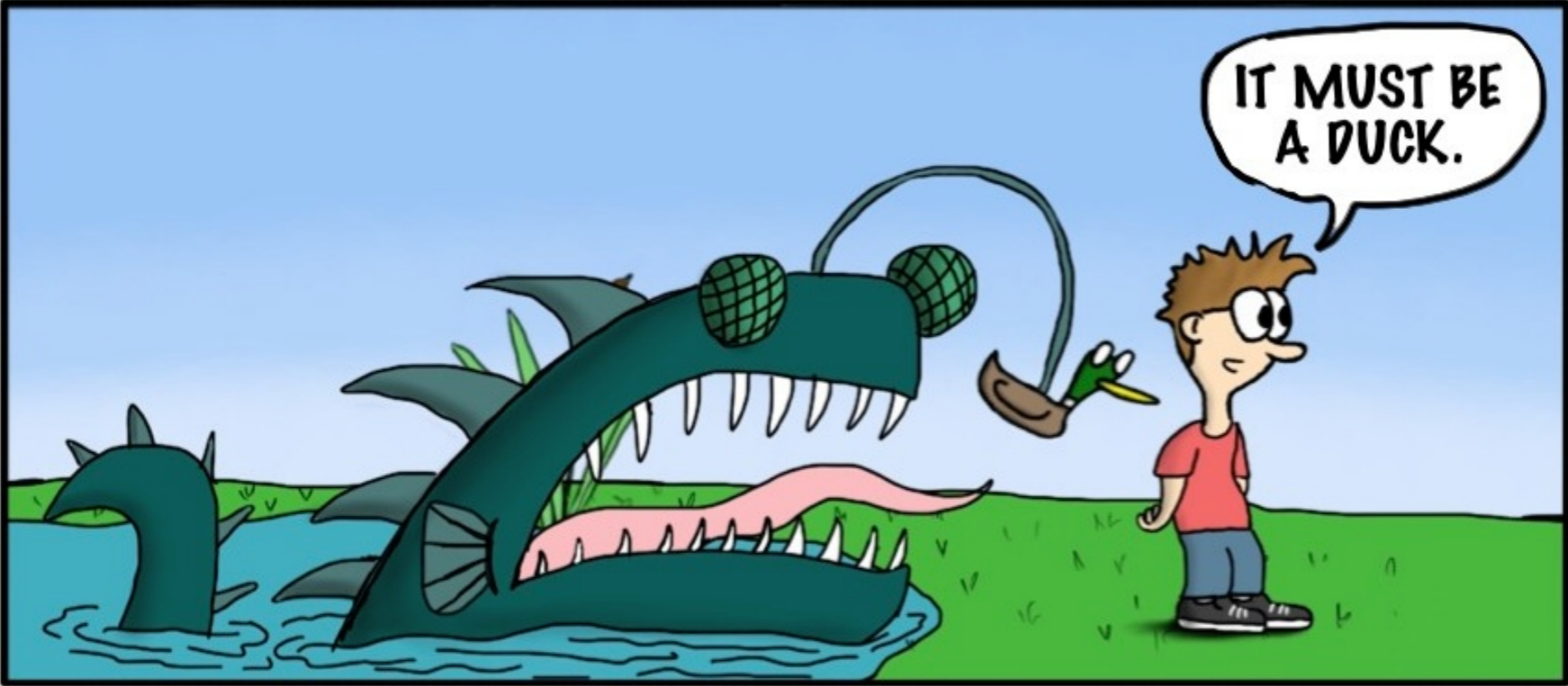
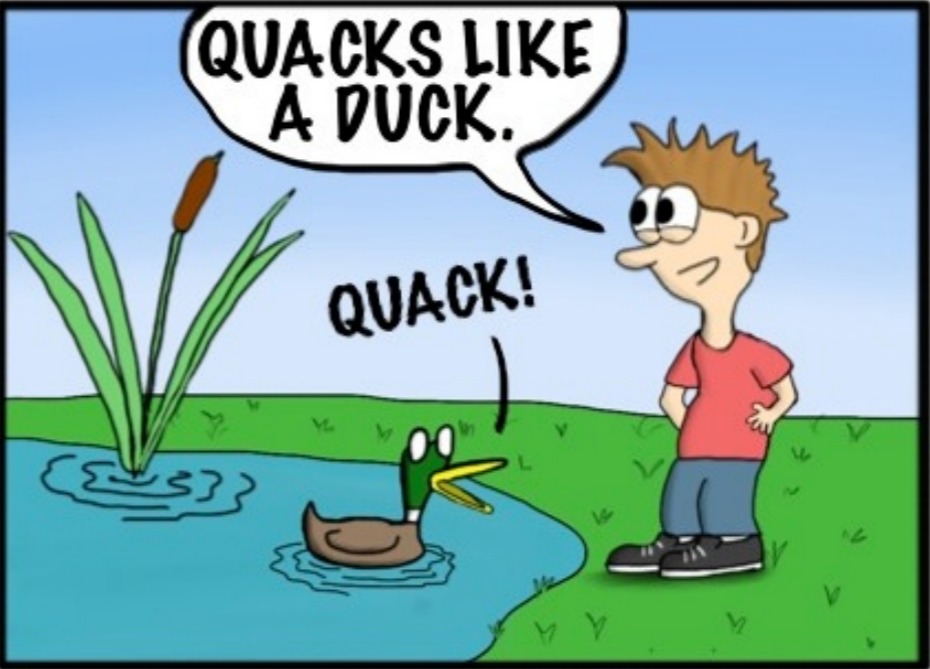
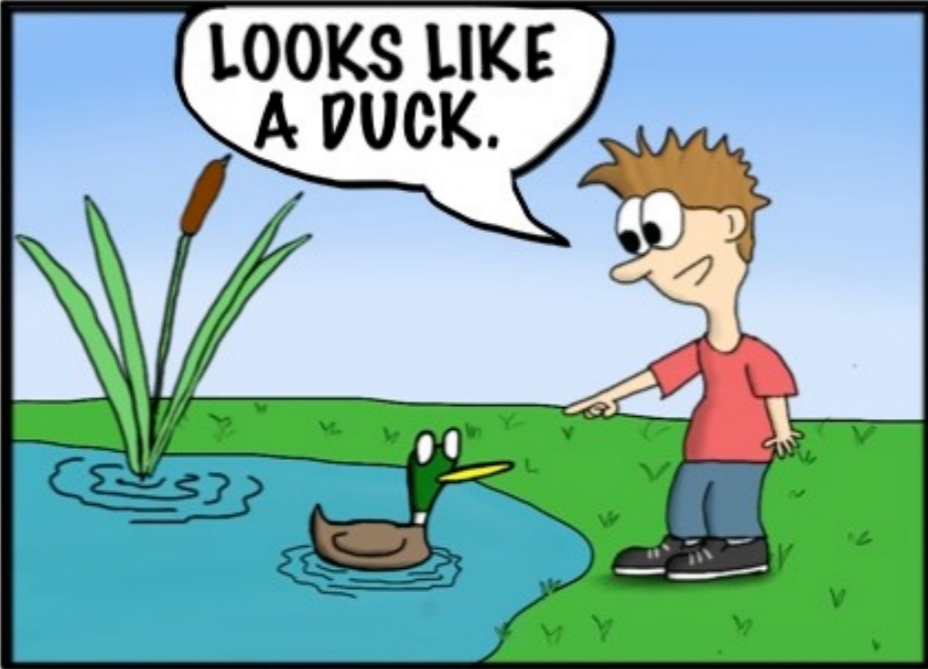


$t = 1.5 \approx 0.375$  fm

$\Delta \lesssim 0.2$  hydrodynamic

$\Delta \gtrsim 0.8$  really not hydrodynamic

# OTHER EXPLANATIONS



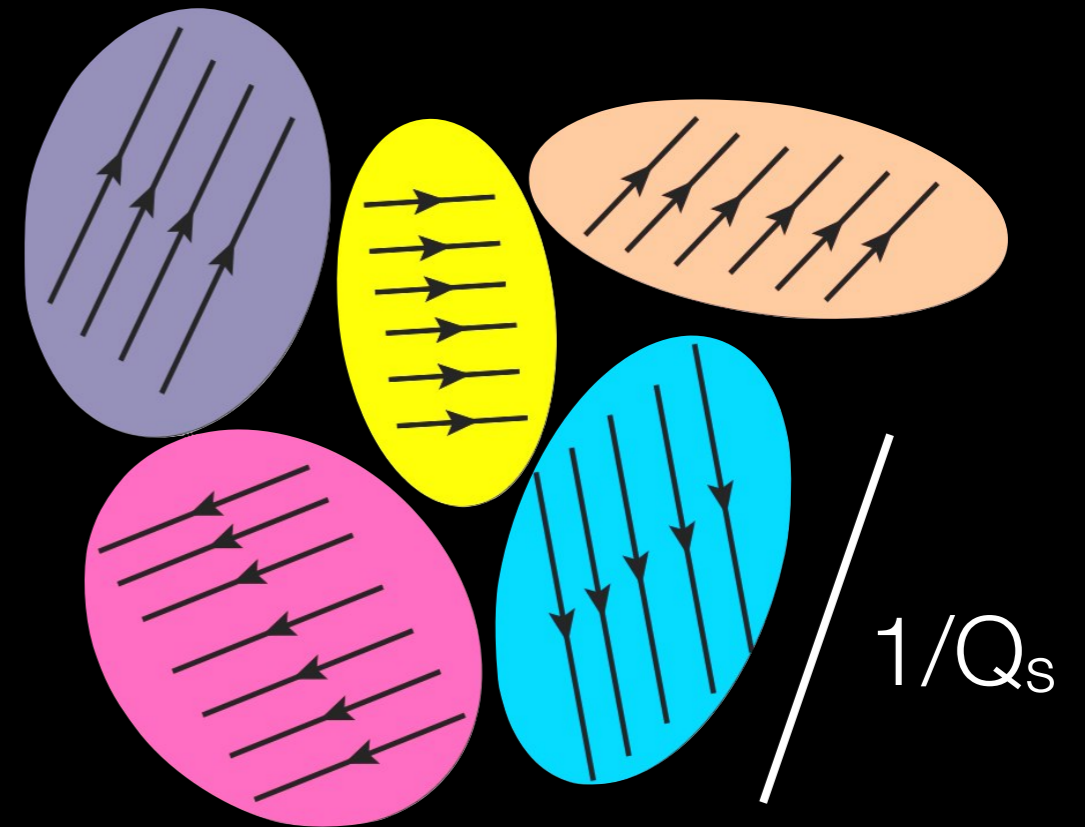
Jared Wood vikingalligator.deviantart.com

# OTHER EXPLANATIONS: INITIAL STATE

## Intuitive picture:

Quarks or gluons are produced from color field domains in the Pb or p target

Particles that come from the same domain are correlated



Effect is suppressed by the number of colors and the number of domains (it is small for heavy ions)

FIGURE: T. LAPPI, B. SCHENKE, S. SCHLICHTING, R. VENUGOPALAN, JHEP 1601 (2016) 061  
SEE ALSO: A. DUMITRU, A.V. GIANNINI, NUCL.PHYS.A933 (2014) 212; A. DUMITRU, V.  
SKOKOV, PHYS.REV.D91 (2015) 074006; A. DUMITRU, L. MCLERRAN, V. SKOKOV,  
PHYS.LETT.B743 (2015), 134; V. SKOKOV. PHYS.REV.D91 (2015) 054014

# CORRELATIONS FROM THE INITIAL STATE

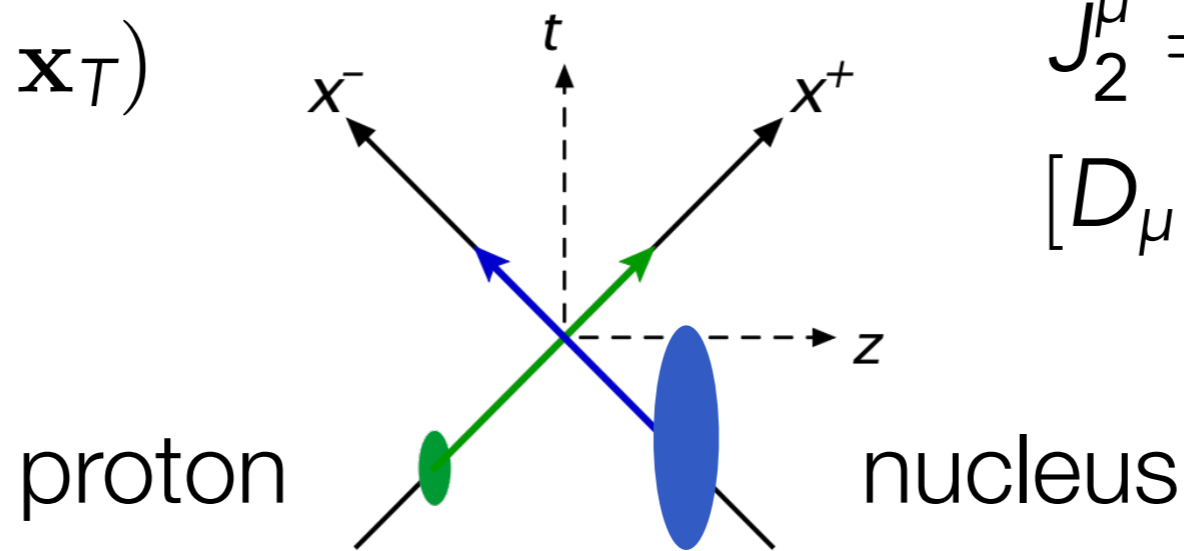
SCHENKE, SCHLICHTING, VENUGOPALAN, PHYS. LETT. B747, 76-82 (2015)

p+A collisions in the Color Glass Condensate:

High multiplicity events: Target and projectile are dense objects  
→ Classical Yang-Mills framework

$$J_1^\mu = \delta^{\mu+} \rho_1(x^-, \mathbf{x}_T)$$

$$[D_\mu, F^{\mu\nu}] = J_1^\nu$$



$$J_2^\mu = \delta^{\mu-} \rho_2(x^+, \mathbf{x}_T)$$

$$[D_\mu, F^{\mu\nu}] = J_2^\nu$$

KRASNITZ, VENUGOPALAN, NUCL.PHYS. B557 (1999) 237

Compute the gluon momentum distribution from the initial fields after the collision - Then analyze its anisotropy

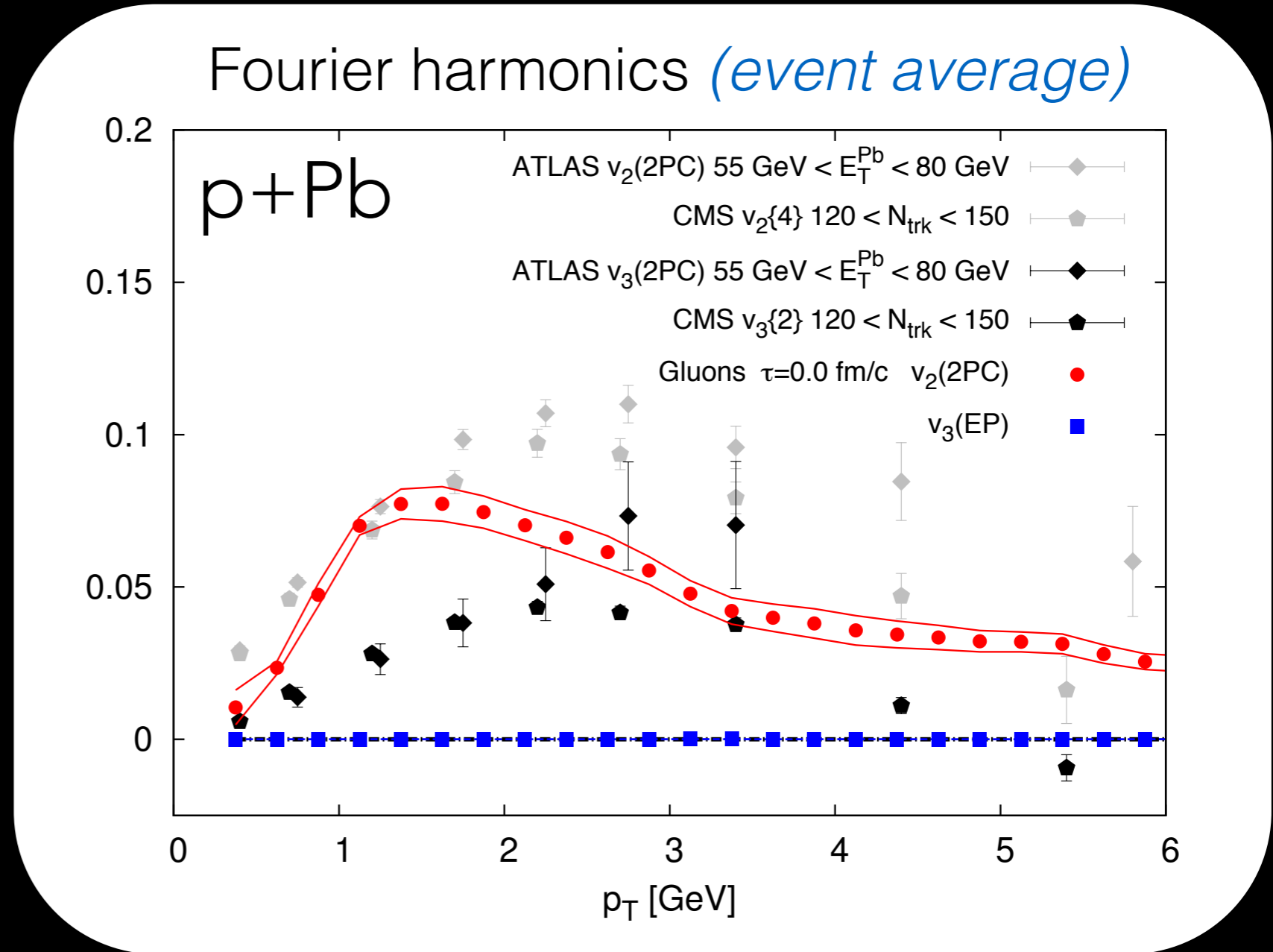
# CORRELATIONS FROM THE INITIAL STATE

SCHENKE, SCHLICHTING, VENUGOPALAN, PHYS. LETT. B747, 76-82 (2015)

$\tau=0.0$  fm/c  
gluons

$V_2, V_3$

data to guide the eye



Significant  $v_2$  at time 0

No odd harmonics for gluons without final state interactions

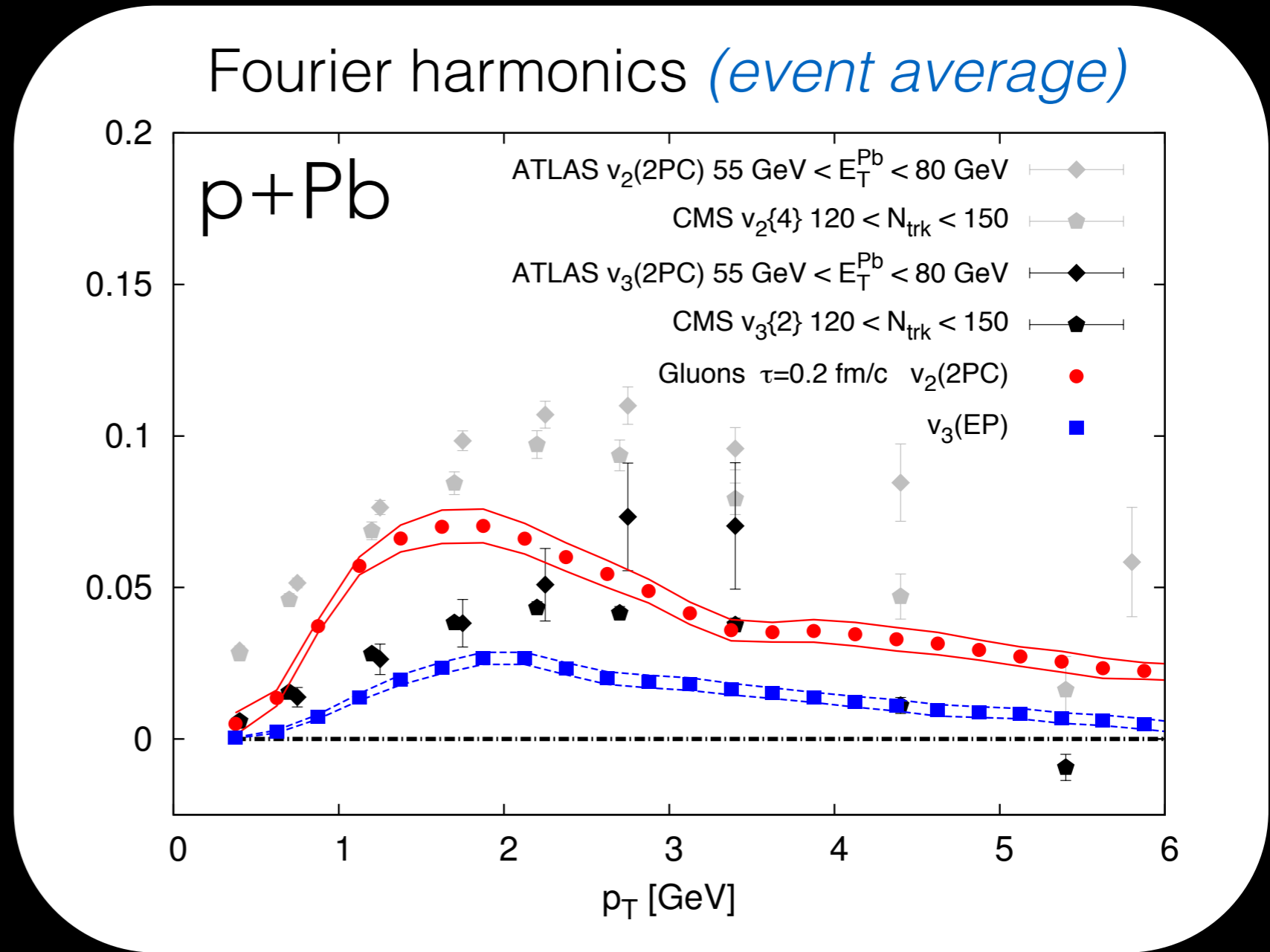
# CORRELATIONS FROM THE INITIAL STATE

SCHENKE, SCHLICHTING, VENUGOPALAN, PHYS. LETT. B747, 76-82 (2015)

$\tau = 0.2 \text{ fm}/c$   
gluons

data to guide the eye

$V_2, V_3$



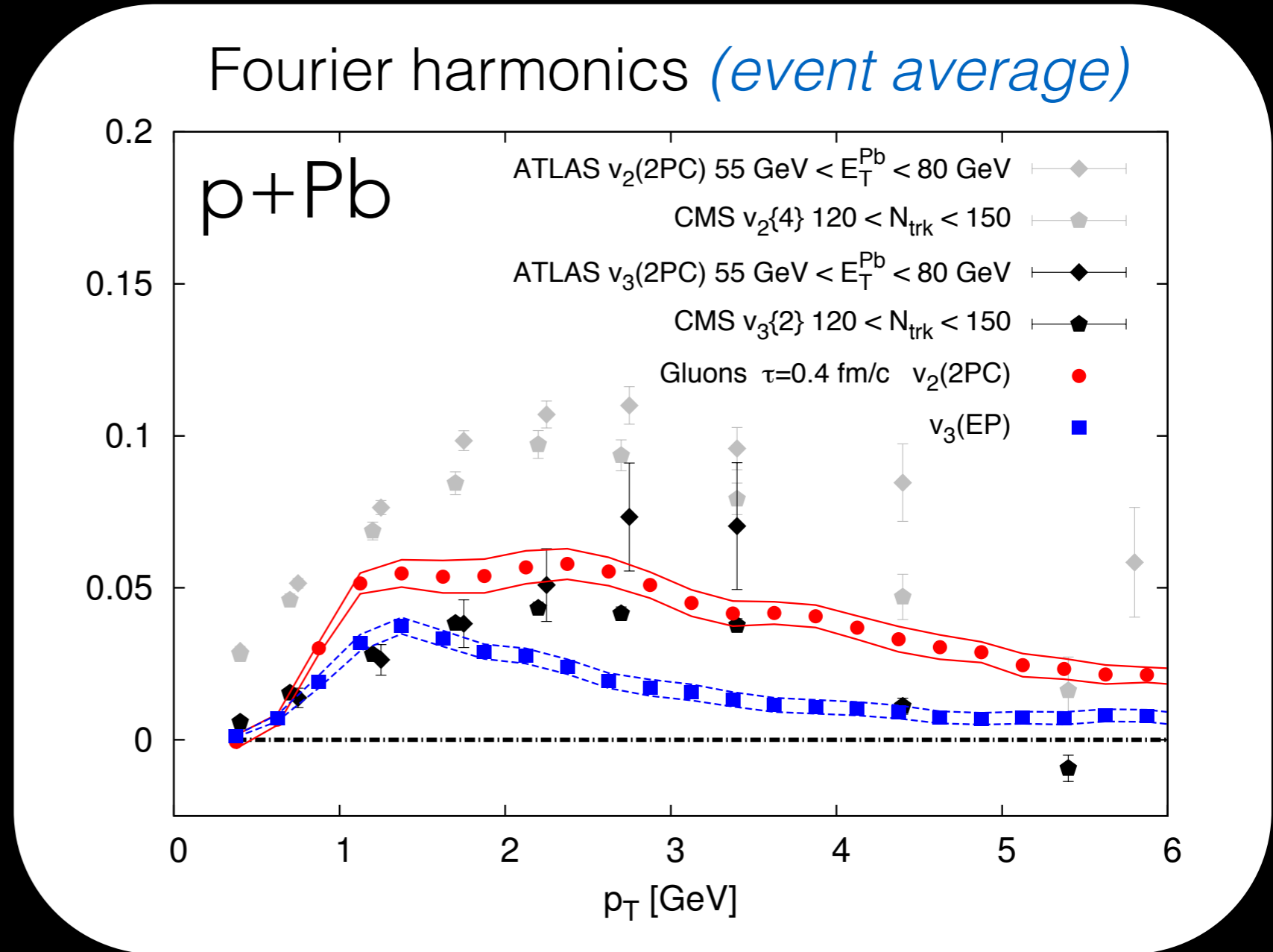
# CORRELATIONS FROM THE INITIAL STATE

SCHENKE, SCHLICHTING, VENUGOPALAN, PHYS. LETT. B747, 76-82 (2015)

$\tau = 0.4 \text{ fm}/c$   
gluons

$V_2, V_3$

data to guide the eye



Odd harmonics generated by pre-equilibrium dynamics

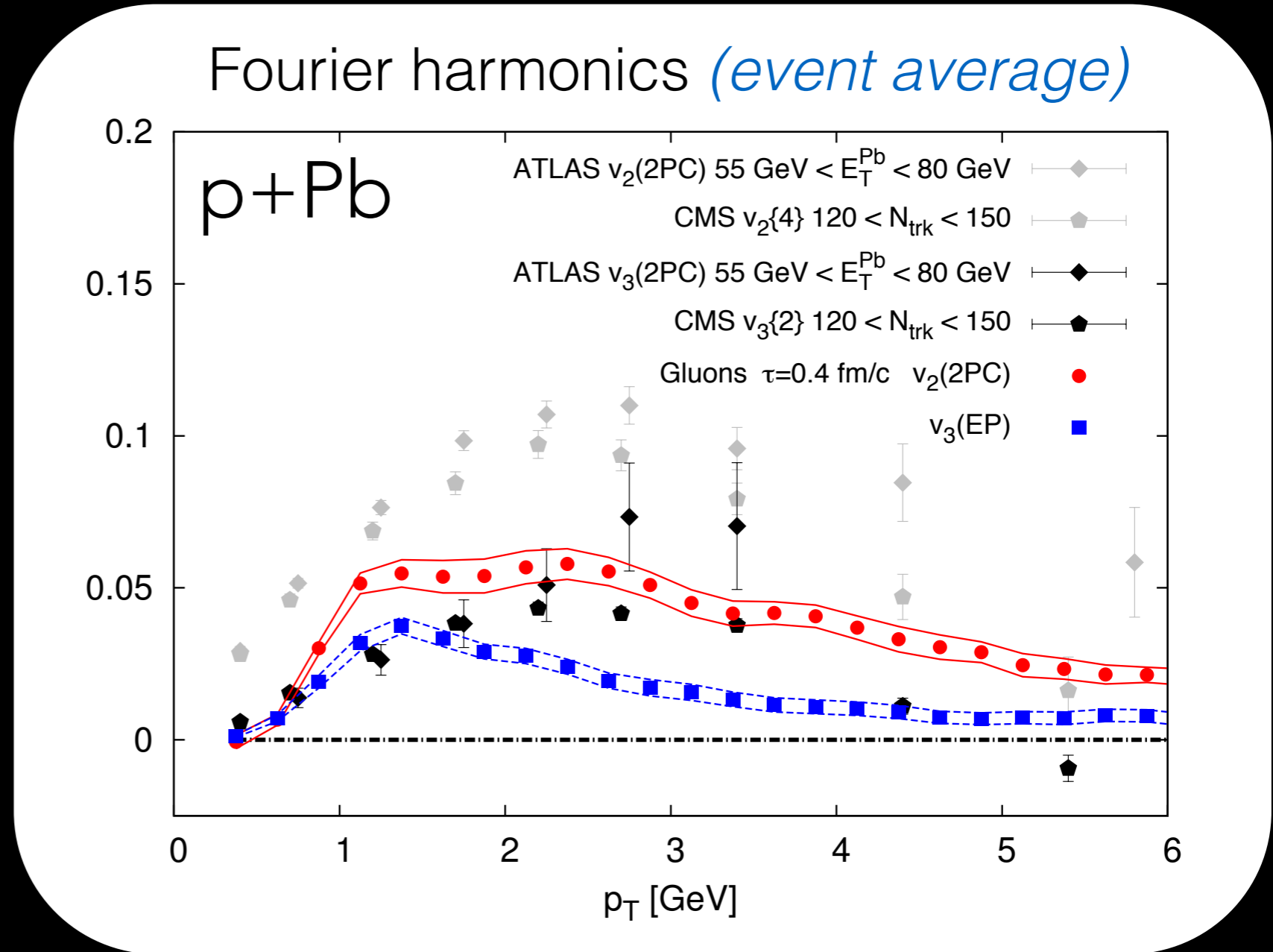
# CORRELATIONS FROM THE INITIAL STATE

SCHENKE, SCHLICHTING, VENUGOPALAN, PHYS. LETT. B747, 76-82 (2015)

$\tau = 0.4 \text{ fm}/c$   
gluons

$V_2, V_3$

data to guide the eye

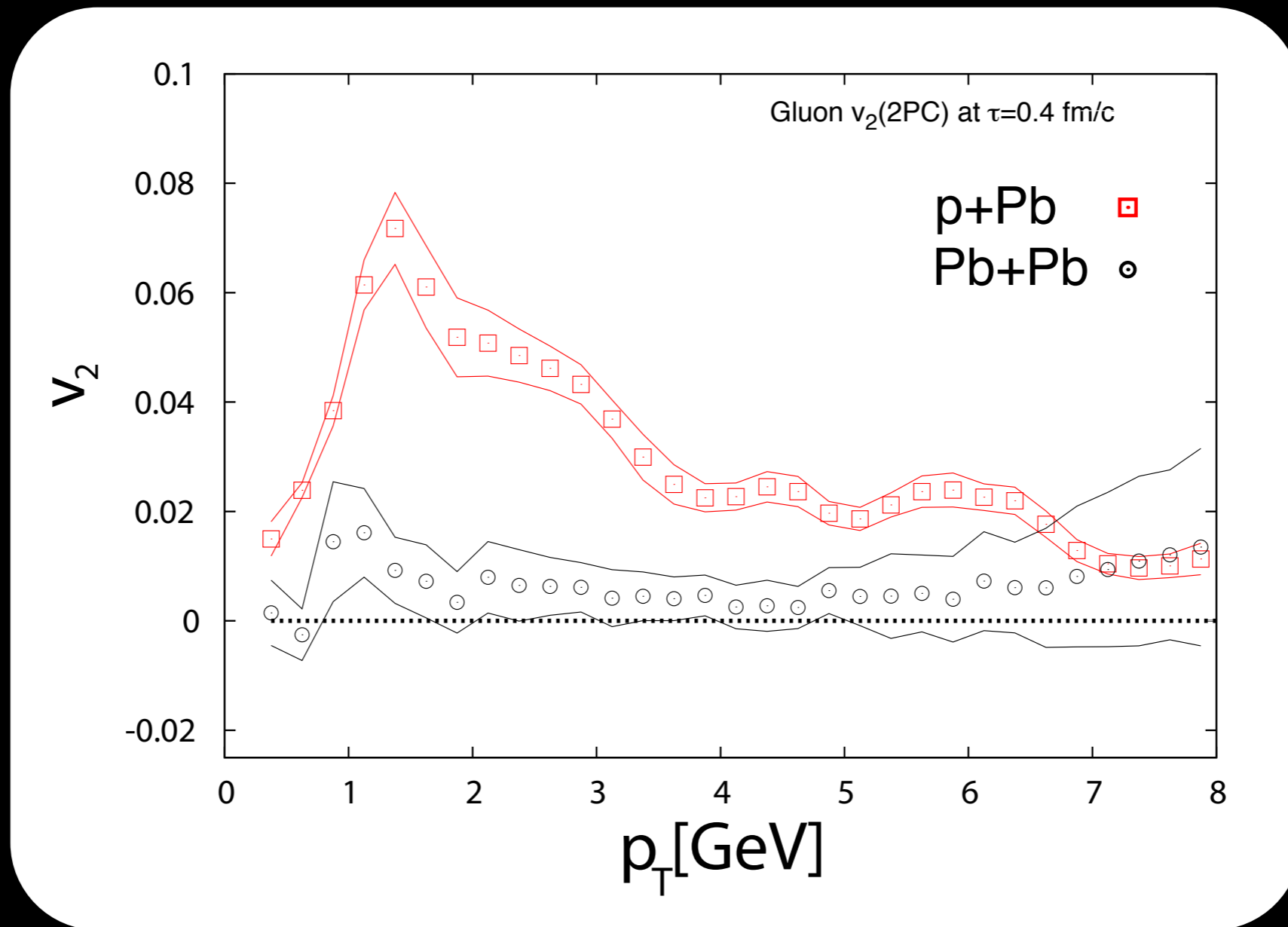


No correlation with global geometry ( $\epsilon_2, \epsilon_3$ ) !



# SENSITIVITY TO SYSTEM SIZE

SCHENKE, SCHLICHTING, VENUGOPALAN, PHYS. LETT. B747, 76-82 (2015)



$Pb+Pb$  not described in initial state picture. Reason:  
Gluons produced from many uncorrelated color field domains

# FRAGMENTATION OF THE CYM RESULT

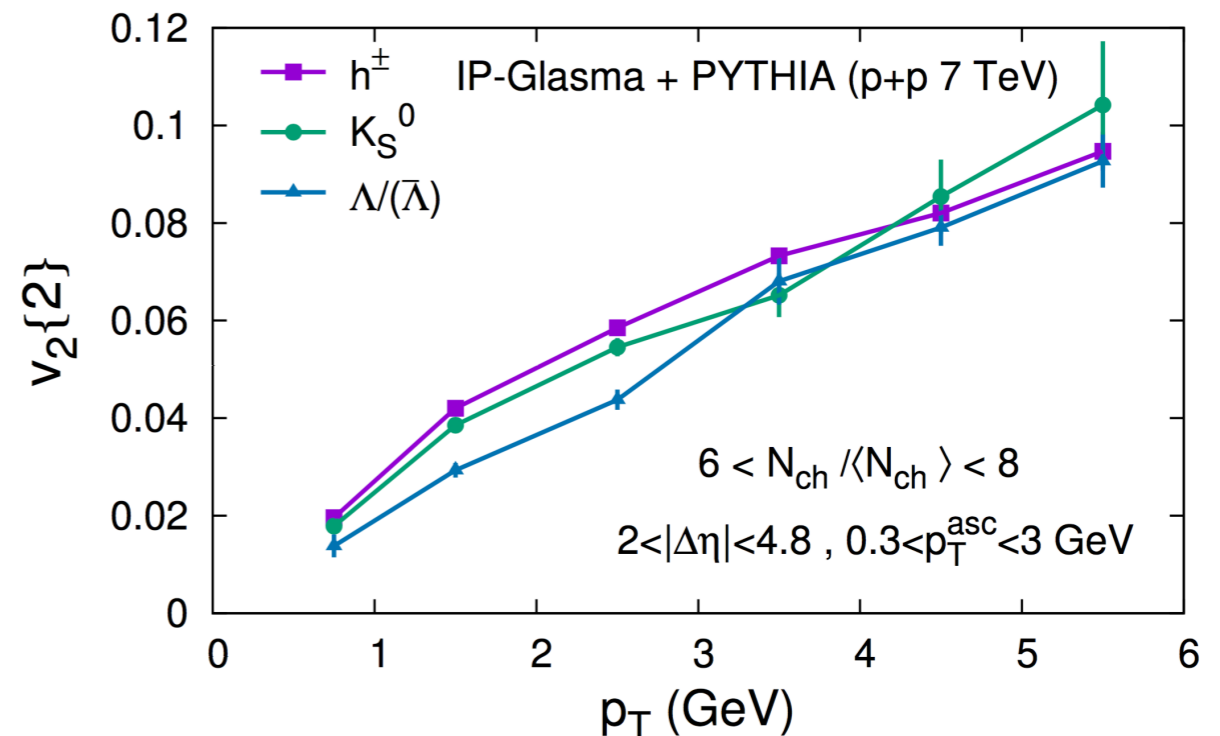
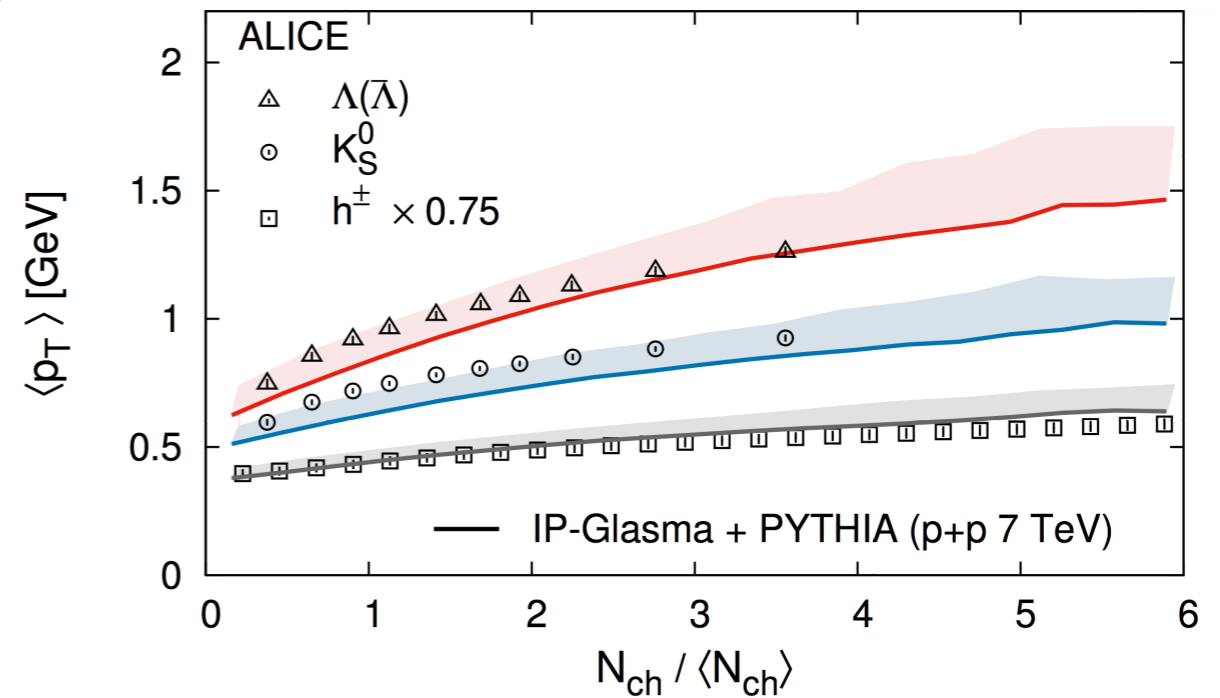
SCHENKE, SCHLICHTING, TRIBEDY, VENUGOPALAN, IN PREPARATION

Do we see mass splitting without hydro?

Classical Yang-Mills coupled to PYTHIA's Lund fragmentation

Gluon  $v_2$  is translated to hadron  $v_2$

Mass splitting in  $\langle p_T \rangle$  and  $v_2$ !



# MANY CALCULATIONS OF RIDGE EFFECT FROM INITIAL STATE

Many different calculations using different approximations exist

Dumitru, Dusling, Fernandez-Fraile, Gavin, Gelis, Jalilian-Marian, Kovchegov, Lappi, McLerran, Dominguez, Marquet, McLerran, Moschelli, Schenke, Schlichting, Skokov, Venugopalan, Wu, ...

They all find a ridge without any hydrodynamics

Some are compared in

T. LAPPI, B. SCHENKE, S. SCHLICHTING, R. VENUGOPALAN, JHEP 1601 (2016) 061

See the review article

K. DUSLING, W. LI, B. SCHENKE, INT. J. MOD. PHYS. E25, 1630002 (2016)

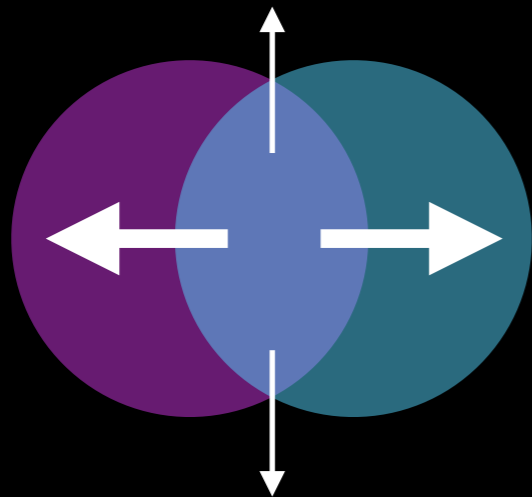
# KINETIC THEORY "ANISOTROPIC ESCAPE"

A. BZDAK, G.-L. MA, PRL 113 (2014)

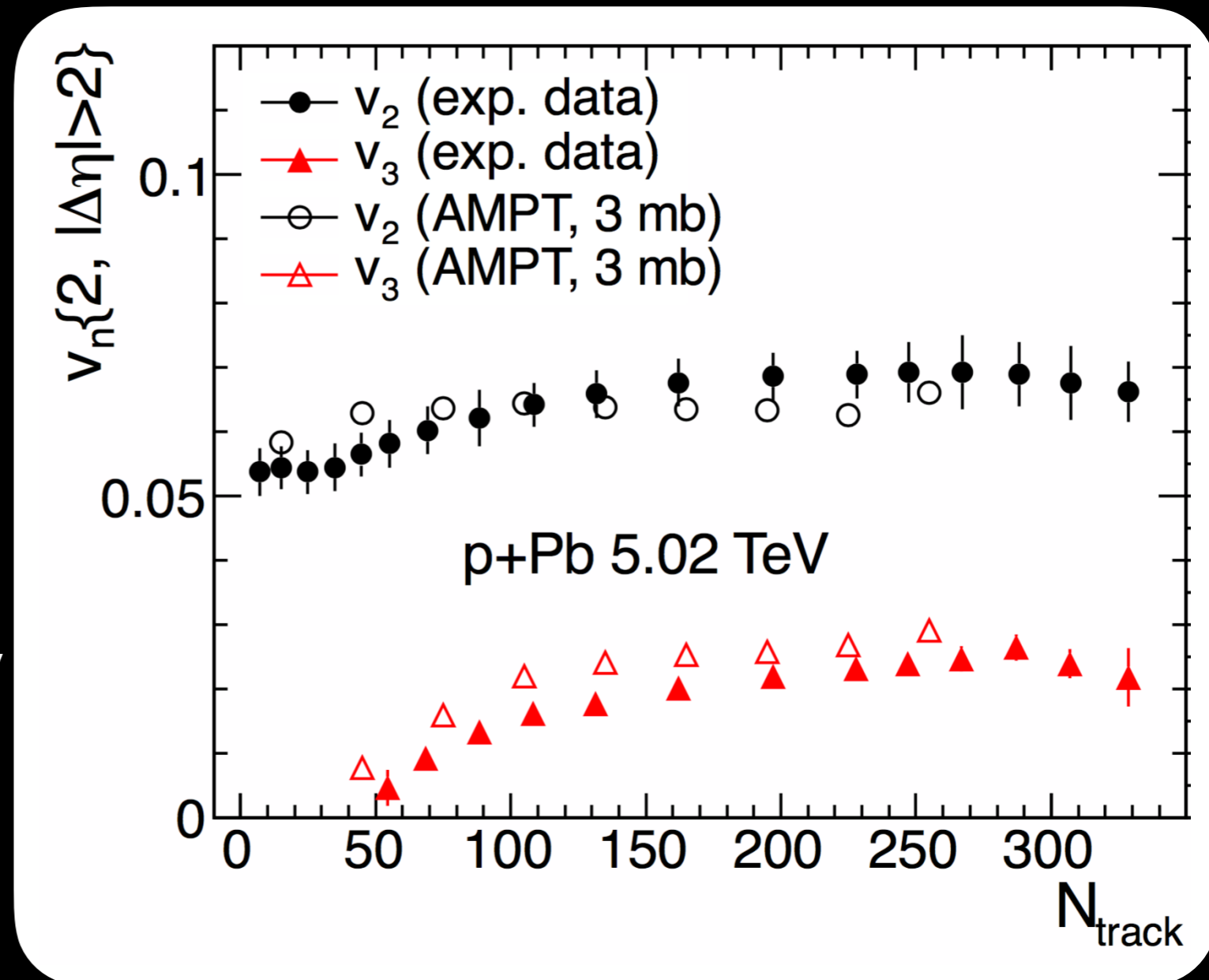
L. HE, T. EDMONDS, Z.-W. LIN, F. LIU, D. MOLNAR, F. WANG, PLB753 (2016)

Final state effect, but weakly interacting (3 mb x-sect.)

Described in AMPT

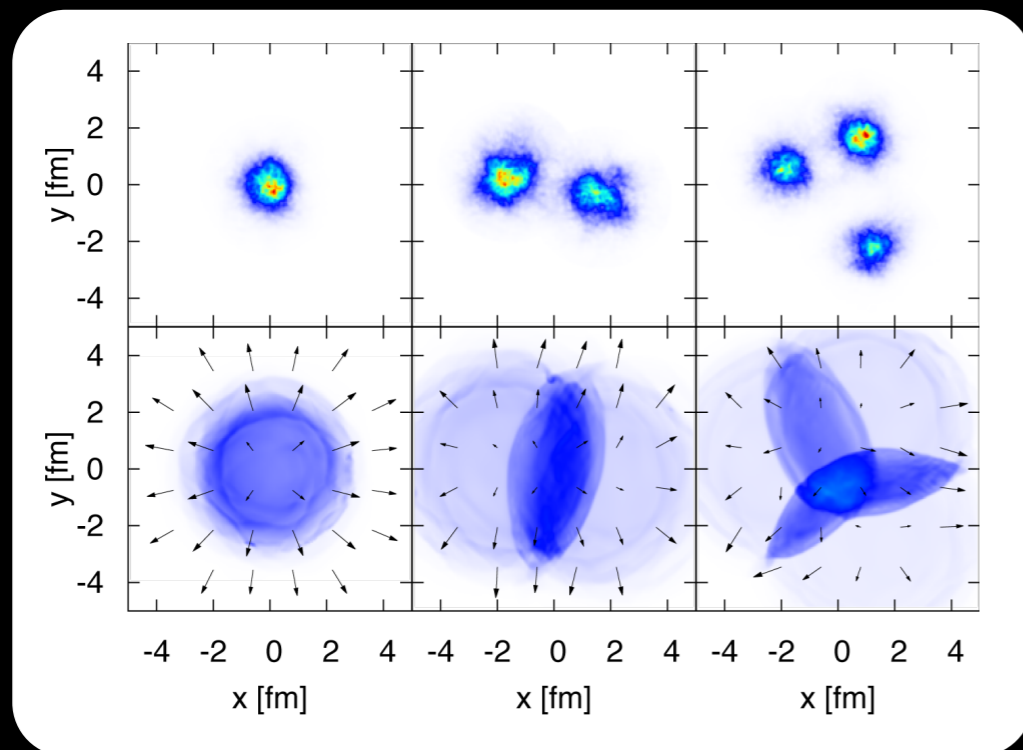


Partons are more likely to escape in the short direction  $\rightarrow v_n$



# HOW TO DISTINGUISH "FLOW" FROM AN "INITIAL STATE" SCENARIO

- **$^3\text{He}+\text{Au}$ ,  $\text{d}+\text{Au}$ : Systematics of flow in different systems Explained by hydrodynamics. Initial state: no calculation**



MEASUREMENT:

PHENIX COLLABORATION, PRL115,

CALCULATIONS:

BOZEK, BRONIOWSKI, PLB739 (2014) 308

NAGLE ET AL, PRL113 (2014)

BOZEK, BRONIOWSKI, PLB747 (2015) 135

SCHENKE, VENUGOPALAN, NPA931 (2014) 1039

ROMATSCHKE, EUR. PHYS. J. C75 (2015) 305

...

- Higher order cumulants: Data shows that

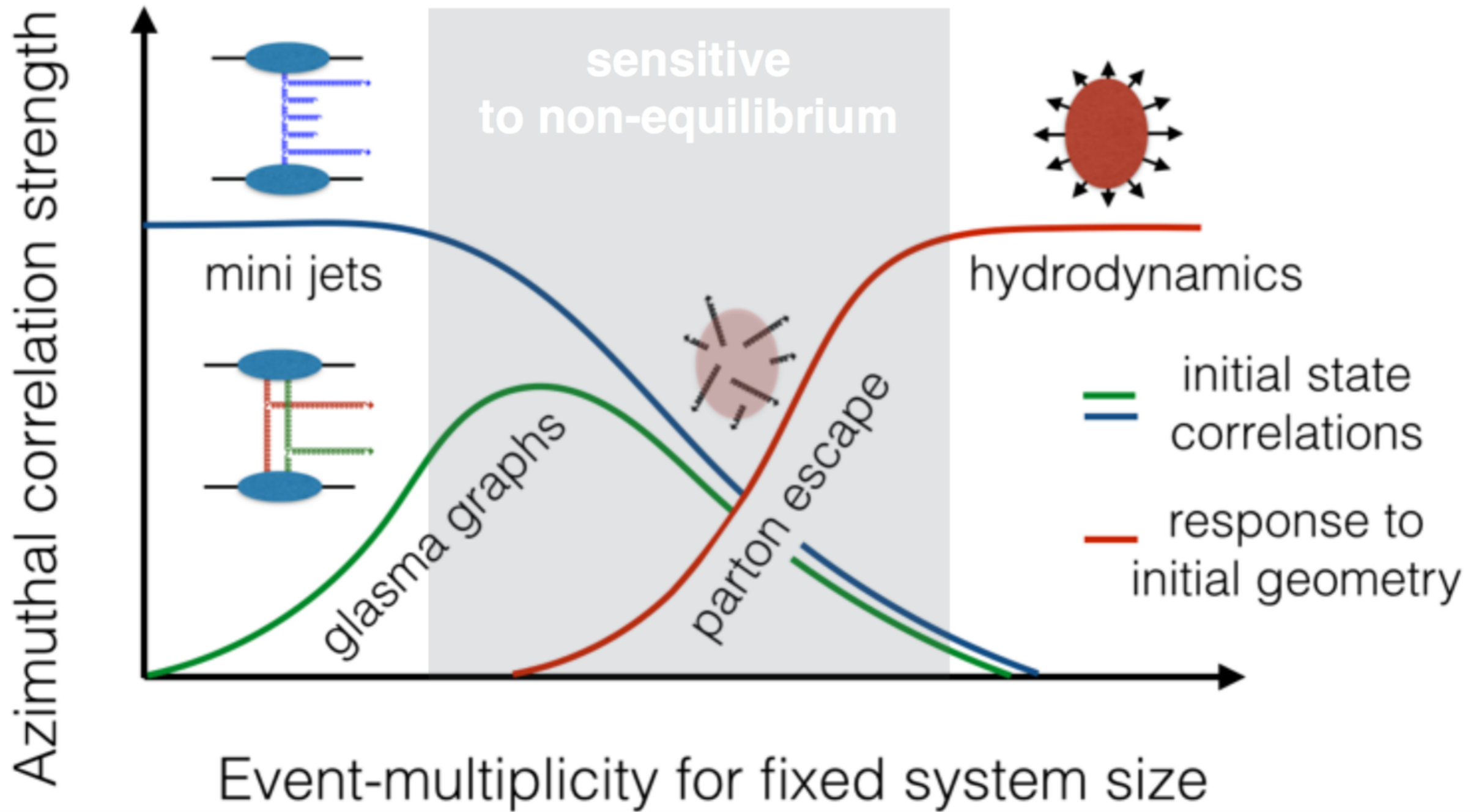
$$v_2\{4\} \approx v_2\{6\} \approx v_2\{8\} \dots$$

Natural in hydrodynamics but not a unique feature

# HOW TO DISTINGUISH "FLOW" FROM AN "INITIAL STATE" SCENARIO

- **Mass splitting of mean  $p_T$  and  $v_n$ : (probably not good)**  
Natural in any situation where particles are produced from a common boosted source: e.g. fluid cell, strings
- **$c_2\{4\}$  turning positive as multiplicity increases**  
could mean collectivity sets in but also alternative explanations  
[DUMITRU, MCLERRAN, SKOKOV, PHYS.LETT. B743 \(2015\) 134-137](#)
- **HBT: Relative radii in p+p, p+Pb and Pb+Pb: Data favors description that yields similar radii in p+p and p+Pb**  
[ALICE COLLABORATION, PHYS. LETT. B 739 \(2014\) 139-151](#)

# COMPLETE PICTURE



# SUMMARY



U.S. DEPARTMENT OF  
**ENERGY**

Office of  
Science

- Azimuthal anisotropies in A+A collisions well understood
- Results in p+p and p+A look very similar
- Final state effect or initial state correlations?
- Probably we have a mixture of both - need to determine what effect dominates in which system/multiplicity

In any case: Exciting opportunity to learn about fluctuating proton shape and/or correlated multi-gluon distributions in nuclei!



# BACKUP

# MANY CALCULATIONS OF RIDGE EFFECT FROM INITIAL STATE

T. LAPPI, B. SCHENKE, S. SCHLICHTING, R. VENUGOPALAN, JHEP 1601 (2016) 061

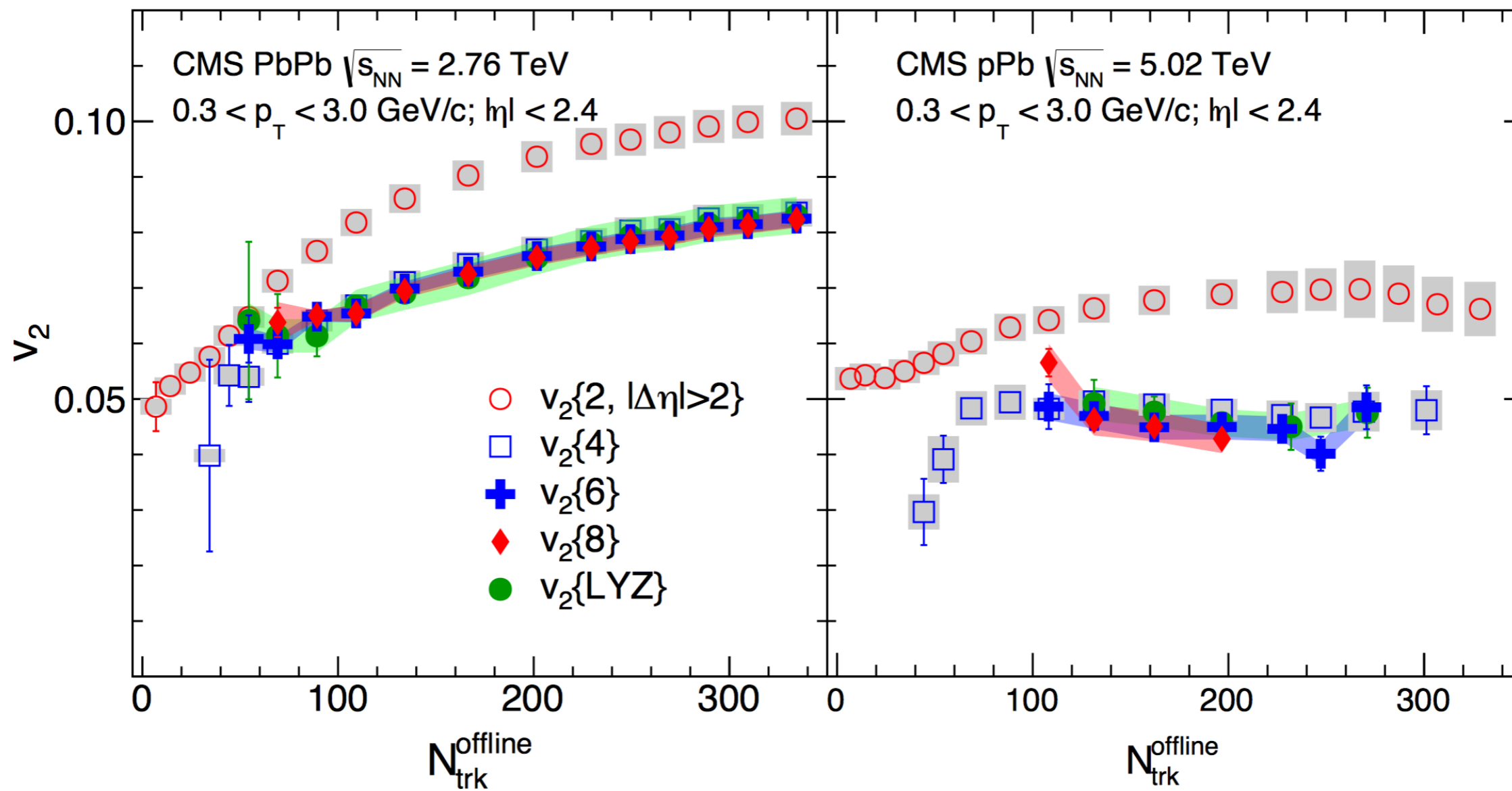
## 1. Dilute-dense limit:

- **Glasma graph approximation** Dumitru, Dusling, Fernandez-Fraile, Gavin, Gelis, Kovchegov, Jalilian-Marian, Lappi, McLerran, Moschelli, Venugopalan, ...  
two gluon exchange (not more) and Gaussian statistics of color charges (MV model) - closer to dilute-dilute limit
- **Nonlinear Gaussian approximation** Dominguez, Marquet, Wu; Lappi, Schenke, Schlichting, Venugopalan  
resums multiple gluon exchanges, neglects non-Gaussianities
- **JIMWLK evolution** Lappi, Phys.Lett. B744 (2015) 315-319  
introduces non-Gaussianities via evolution
- **Color Domain Model** A. Dumitru, A.V. Giannini, L. McLerran, V. Skokov  
introduces additional non-Gaussian correlations (like the ones introduced by JIMWLK evolution (small) or intrinsic four point correlations of significant magnitude)

## 2. Dense-dense limit:

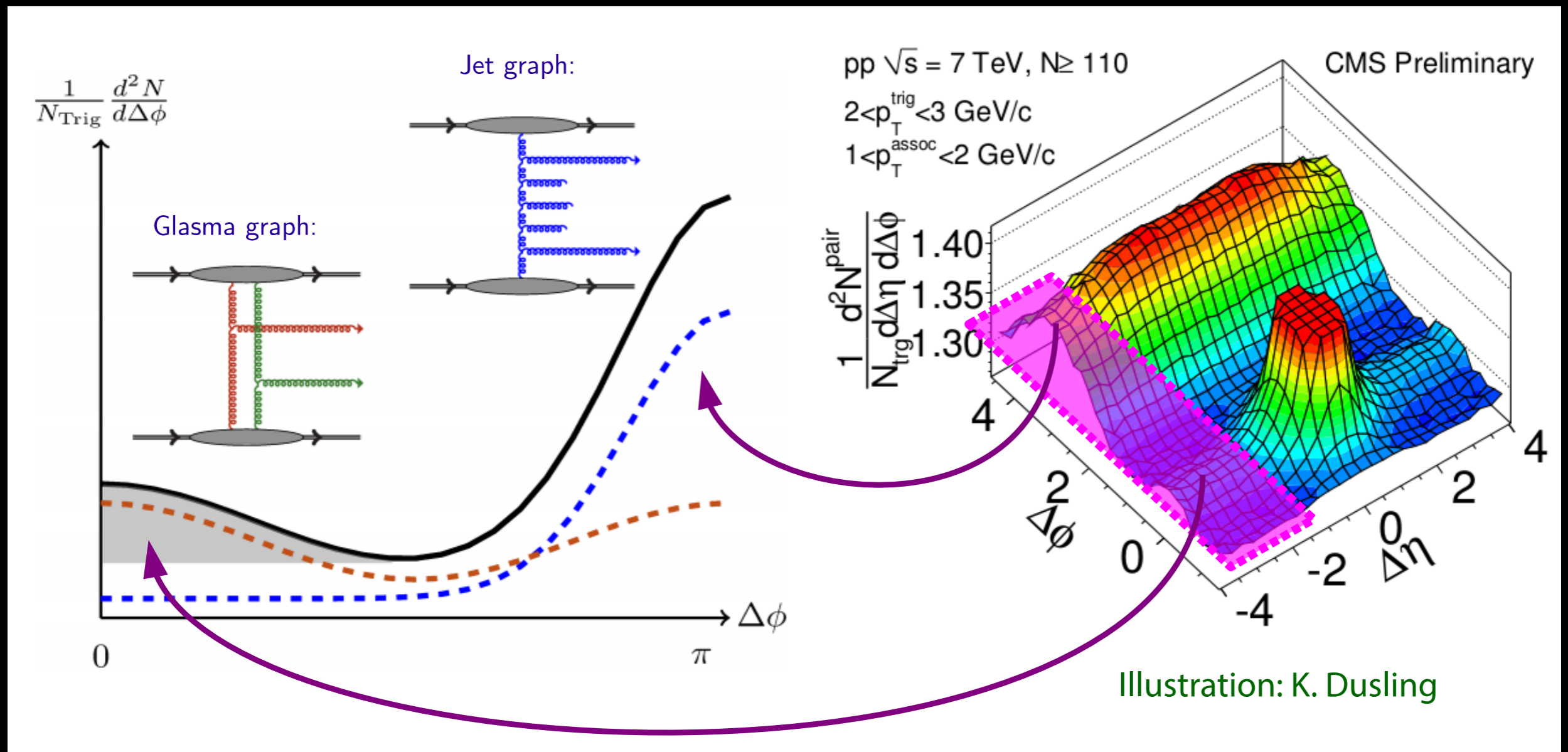
- **Classical Yang-Mills calculation** Schenke, Schlichting, Venugopalan  
includes multiple-gluon exchange, "rescattering"

# $v_2$ IN p+Pb COLLISIONS MULTI-PARTICLE CORRELATIONS



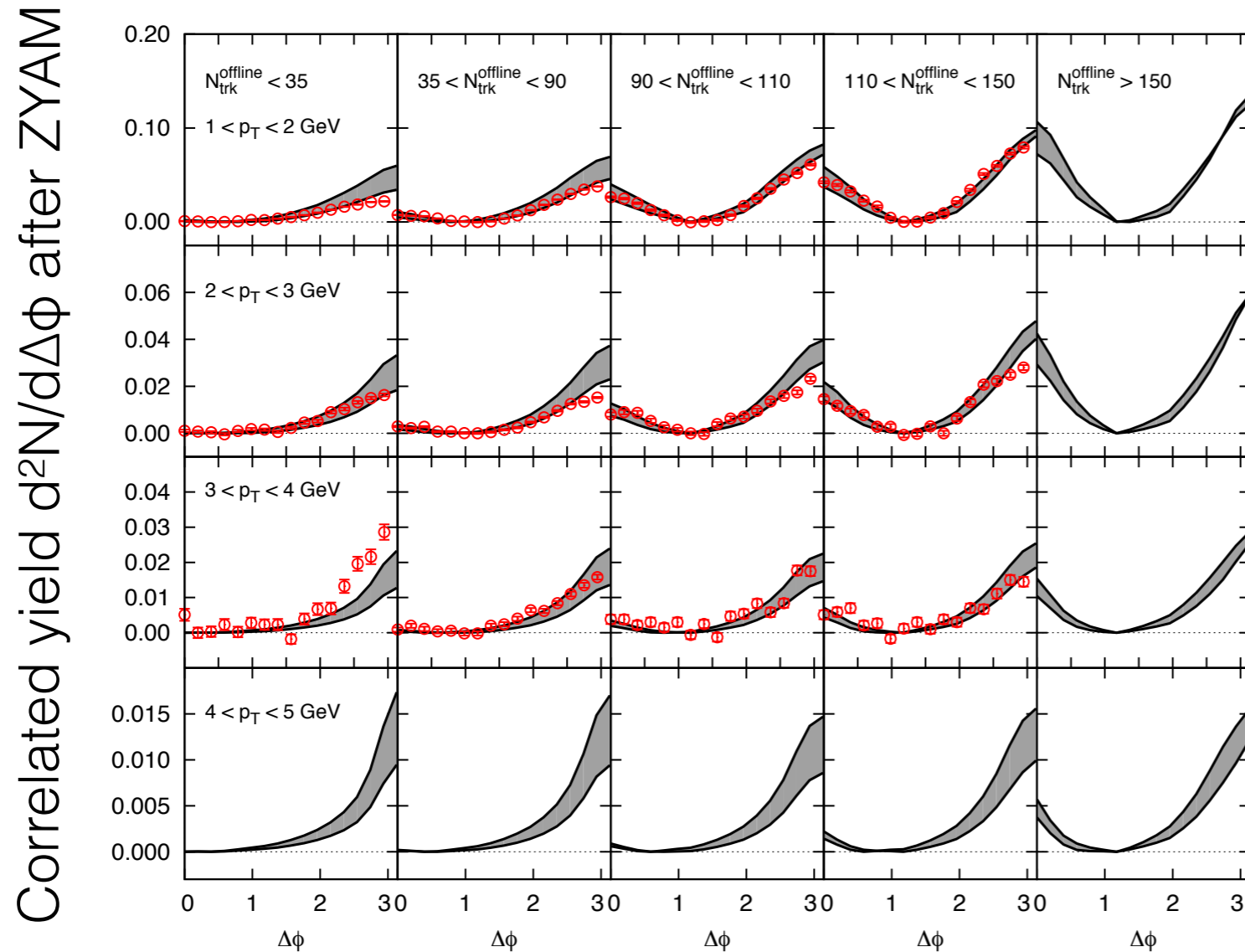
# GLASMA GRAPH APPROXIMATION

Dusling, Venugopalan, Phys.Rev. D87 054014 (2013)



# Correlated yield vs. angular difference

Dusling, Venugopalan, Phys.Rev. D87 054014 (2013), Exp: CMS collaboration, Phys. Lett. B 718 795 (2013)



Systematics well described

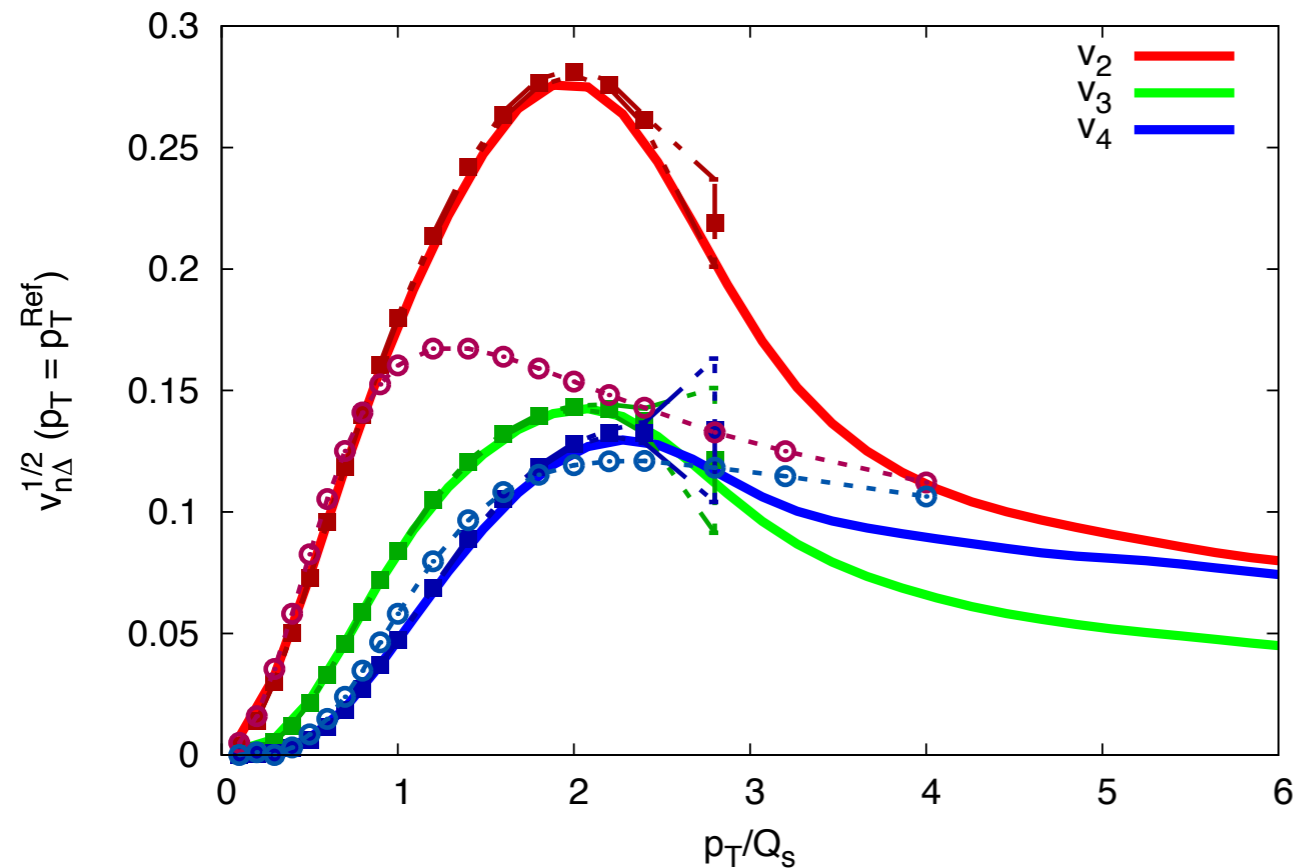
Ridge larger in p+A than in p+p because of larger saturation scale

# Dilute-dense limit: approximation schemes

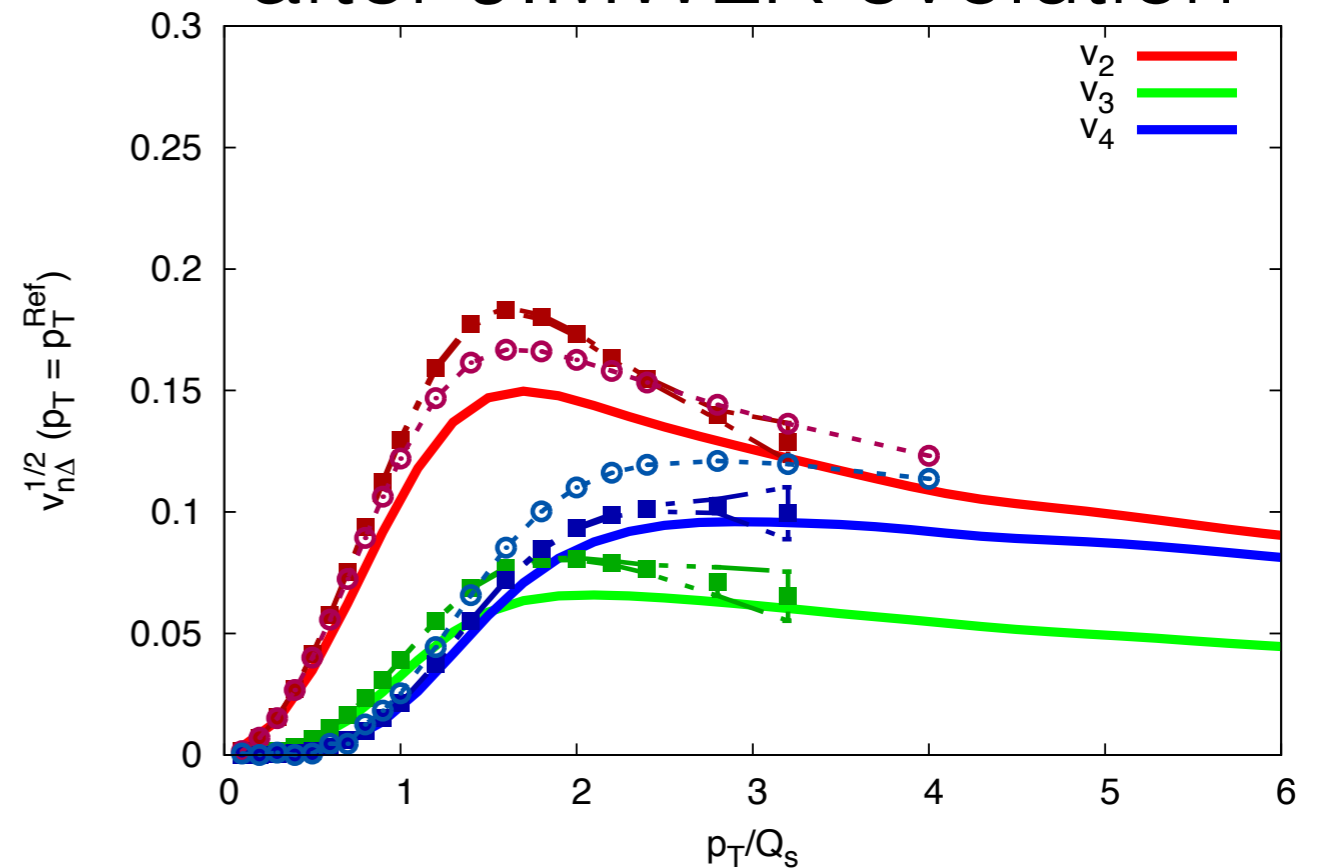
T. Lappi, B. Schenke, S. Schlichting, R. Venugopalan, JHEP 1601 (2016) 061

## Scattering of two independent quarks off a large nucleus

### MV model



### after JIMWLK evolution



solid: numerical JIMWLK  
dash-dotted (squares):  
non-linear Gaussian  
dotted (circles): glasma graph

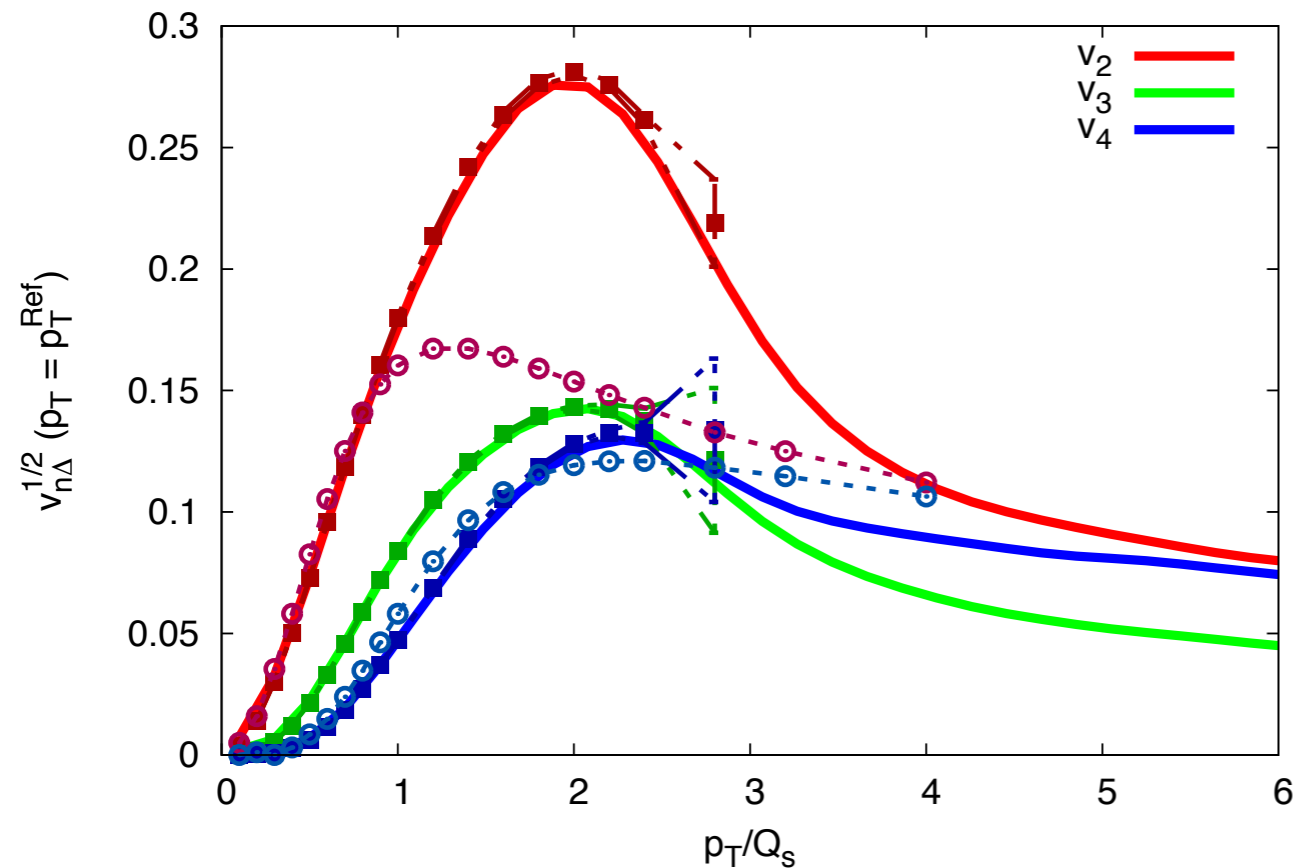
The two approximate schemes use the dipole operator extracted from the numerical JIMWLK evolution <sup>38</sup>

# Dilute-dense limit: approximation schemes

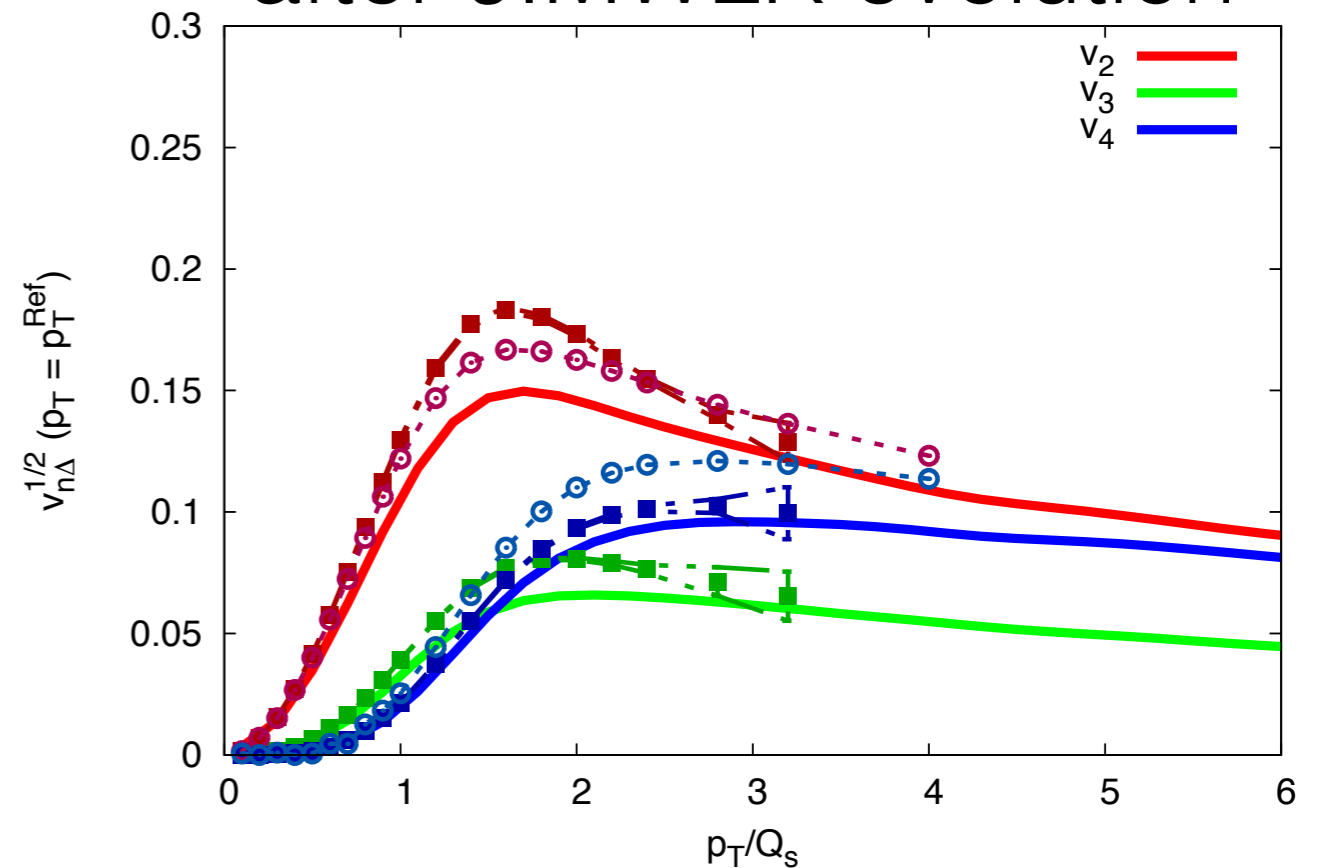
T. Lappi, B. Schenke, S. Schlichting, R. Venugopalan, JHEP 1601 (2016) 061

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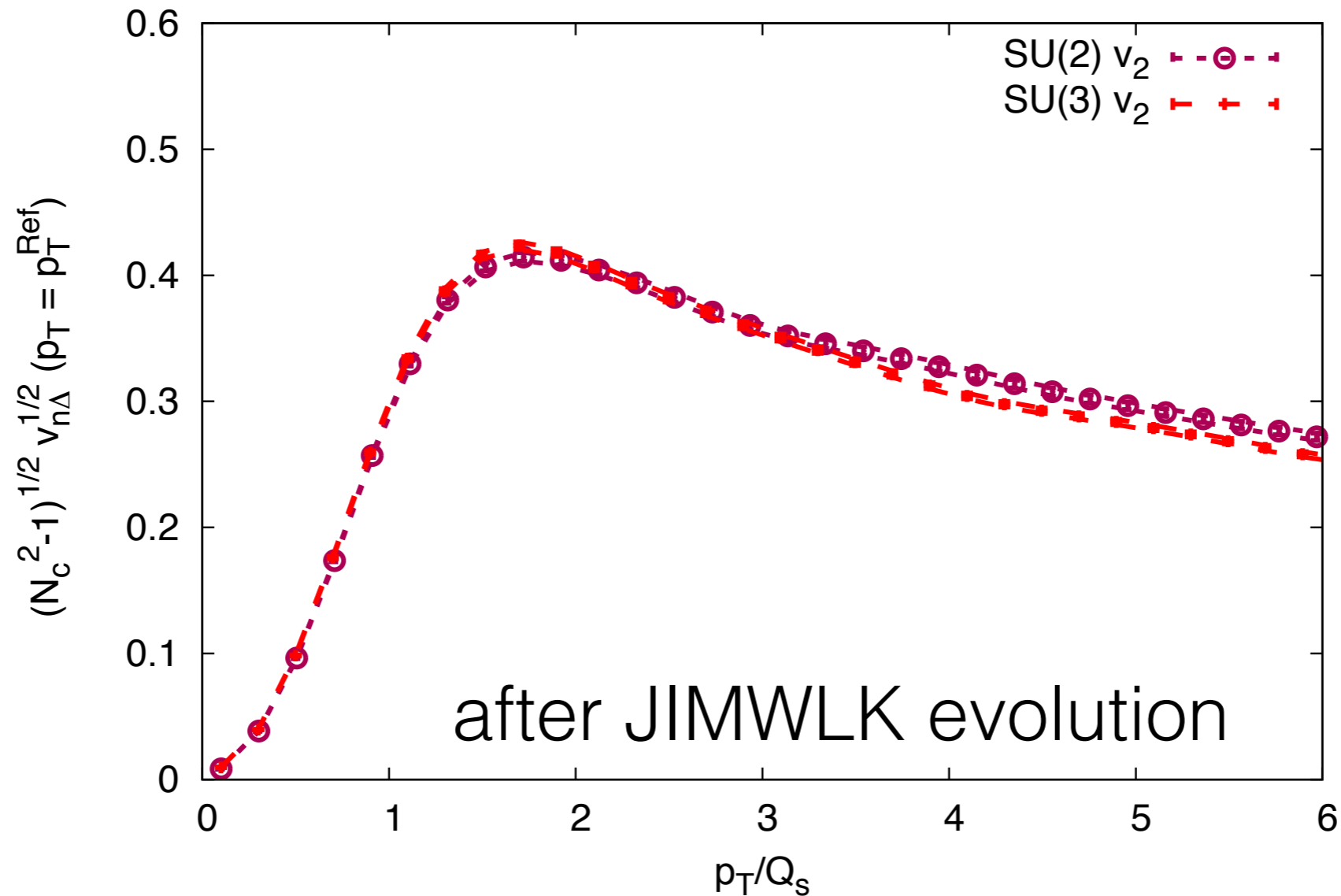


- No odd  $v_n$  in glasma graph approximation by symmetry
- Perfect agreement between non-linear Gaussian approximation and numerical result in MV (must be)

# Correlations are suppressed by the number of colors

T. Lappi, B. Schenke, S. Schlichting, R. Venugopalan, JHEP 1601 (2016) 061

## Scattering of two independent quarks off a large nucleus



$v_n$  scales as  $(N_c^2 - 1)^{-\frac{1}{2}}$

azimuthal correlations in the double inclusive spectrum  $\sim (N_c^2 - 1)^{-1}$