

Multi-strange hadrons and the precision extraction of QGP properties in the RHIC-BES domain

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Abstract. We systematically compare an event-by-event transport+viscous hydrodynamics hybrid model to data from the RHIC beam energy scan using a general Bayesian method. We demonstrate how the inclusion of multistrange hadron observables affects the outcome of the Bayesian analysis and conduct an in depth analysis of the viability of ϕ and Ω as probes of the transition region between a deconfined quark-gluon plasma and hadronic phase in heavy ion collisions at higher-end RHIC collision energies. Utilizing UrQMD to model the final hadronic interactions, we examine the collision rates of ϕ and Ω and the modification to their transverse momentum spectra due to these interactions.

1. Introduction

Many modern models of relativistic heavy ion collisions employ a so called hybrid approach, where the hydrodynamical model of quark-gluon plasma evolution is coupled to a hadron transport “afterburner”, allowing the chemical and kinetic freeze-outs to happen dynamically. However, this approach introduces an additional parameter to the model; namely, the switching condition between hydrodynamics and hadron transport. Typically this switching condition is either a particular value of temperature T_{SW} , or energy density ϵ_{SW} , which is close to, but below the transition temperature or energy density.

The justification of this approach comes from the assumption that both hydrodynamics and hadron transport describe the same system over a range of temperature / energy density values, and thus the exact value of T_{SW} or ϵ_{SW} should not matter. However, to make quantified statements about the actual size of the overlap between the two descriptions, one needs to identify the experimental observables which probe the transition region.

Multi-strange hadrons ϕ and Ω are potential probes of the transition stage, as they are produced at the phase boundary during hadronization of the quark-gluon plasma and exhibit small scattering cross section in the hadronic phase [1]. In this Article, we perform a detailed

comparison of an event-by-event transport+viscous hydrodynamics hybrid model [2] to ϕ and Ω data from the RHIC beam energy scan [3, 4, 5].

2. Hybrid model

In the hybrid approach, the heavy ion collision is modeled in three separate phases.

The initial pre-equilibrium phase is simulated with UrQMD hadron+strings cascade [6, 7]. The hydrodynamical evolution starts after the two colliding nuclei have passed through each other: $\tau_0 \geq 2R_{\text{nucleus}}/\sqrt{\gamma_{CM}^2 - 1}$. At this point, the particle properties such as energy and baryon number are converted to densities using 3D Gaussians with “smearing” parameters R_{trans} , R_{long} , each equal to $\sqrt{2}$ times the respective Gaussian width parameter σ_{trans} , σ_{long} .

In the local equilibrium phase, the system is evolved according to 3+1D viscous hydrodynamics [8], with viscosity parameter η/s kept constant during the full evolution. At the lower collision energies, the equation of state needs to include the effects of nonzero net-baryon density. For this purpose, a chiral model equation of state [9] is utilized in this investigation.

Finally, the transition from hydrodynamical evolution back to hadron transport (“particization”) happens when energy density ϵ drops below the chosen energy density value ϵ_{SW} . A hypersurface with constant energy density is constructed [10] and particles are sampled from this hypersurface according to the Cooper-Frye formula and propagated further using UrQMD. Both chemical and kinetic freeze-out thus happen dynamically.

As all ϕ s will decay before the end of the simulation, we output the full interaction histories of the afterburner hadron cascades for each event. We search these histories for ϕ s, and label the ones which have both their decay products surviving to the end of simulation as “detectable”. It should be noted that the survivor decay products are allowed to have interacted via processes which preserve their identity. However, we have found that the fraction of survivor products which have interactions is less than 15% at investigated energies.

3. Statistical analysis and simulation setup

The optimal input parameter values are determined using Bayesian analysis similar to Refs. [11, 12]. The posterior distribution is sampled with Markov chain Monte Carlo (MCMC) method. We perform thousands of random walks in input parameter space, where step proposals are accepted or rejected based on a relative likelihood. However, it is not feasible to run the full hybrid model simulation for each evaluation of the likelihood function. To circumvent this problem, we use Gaussian processes to emulate the simulation output, based on ≈ 100 training points, which are samples of the input parameter space. The Latin hypercube method is used to achieve close to uniform distribution of training points on all 5 parameter dimensions.

4. Results

Figure 1 demonstrates the variance in transverse momentum distributions of ϕ s and Ω s over the training points for $\sqrt{s_{NN}} = 39$ GeV. To eliminate some possible sources of discrepancies between simulation and experimental results, we follow the experimental method [3] and do also Levy fits on the transverse momentum spectra points which are within the p_T range reported by the experiments. We see that ϕ yield at low p_T is underpredicted by most of the input parameter combinations. This suggests that our criterion for ϕ meson detection is too stringent compared to the experimental reconstruction methods.

To verify the result of the statistical analysis, a full simulation was performed using the median values from the posterior distributions of the input parameters. The resulting Ω transverse momentum distributions for $\sqrt{s_{NN}} = 39$ GeV is shown in the right frame of Fig. 1. Although only the lowest transverse momentum bin was used for the calibration of model parameters, the experimental data is very well reproduced for the whole p_T spectrum.

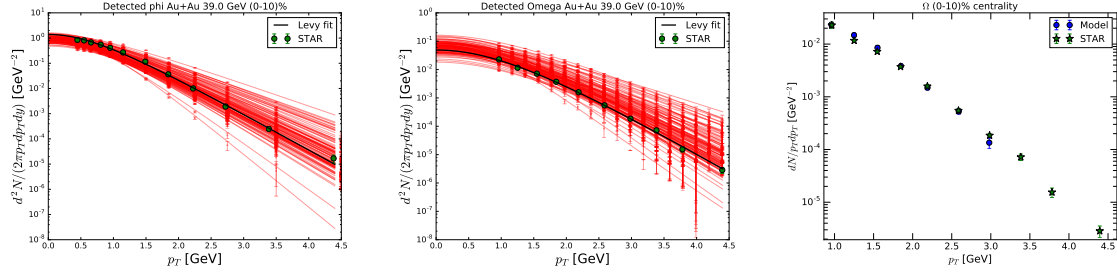


Figure 1. Transverse momentum spectra of ϕ (left) and Ω (middle) at $\sqrt{s_{NN}} = 39$ GeV. Curves represent Levy fits on model or STAR data points. Right: Transverse momentum spectrum of Ω at $\sqrt{s_{NN}} = 39$ GeV using the median values from statistical analysis. STAR data from [5].

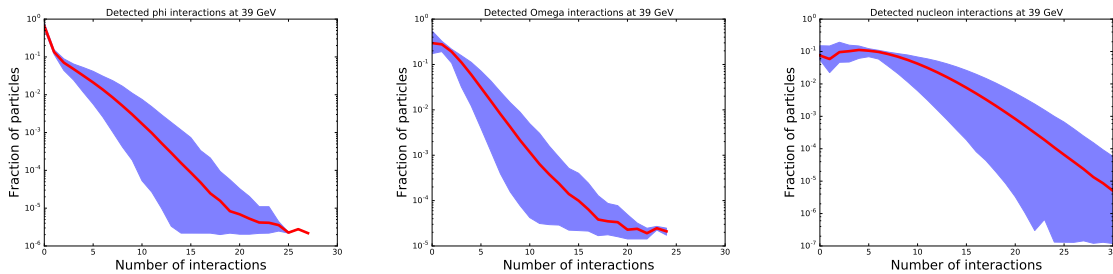


Figure 2. Distribution of average number of interactions for ϕ , Ω and N at $\sqrt{s_{NN}} = 39$ GeV. Red line represents the mean over all training points. Blue band represents the full range of values over all training points.

In addition of the yields, we can also calculate the mean p_T from the particle spectra. As we are interested in using ϕ and Ω as probes of the phase transition region, we need to quantify the change on $\langle p_T \rangle$ during the hadron gas phase. We find the detectable ϕ mean transverse momentum to be about 20% larger than the value at the hypersurface. The increase is slightly smaller, $\approx 15\%$, when including “undetectable” ϕ s; this equals the change in $\langle p_T \rangle$ seen for Ω .

We also investigate the average number of interactions ϕ and Ω experience in the hadronic matter (Fig. 2). The analysis verifies that detectable ϕ mesons have hardly any interactions, and Ω baryons are likely to have only a few, compared to the 5-10 interactions of a typical nucleon.

To check the effect of multistrange hadron observables on the posterior distributions, the statistical analysis was performed with and without Ω yield data for $\sqrt{s_{NN}} = 19.6, 39,$ and 62.4 GeV. As seen in Figs. 3 and 4, the analysis without Ω yields was not able to produce any constraints on switching energy density value, whereas the analysis including the Ω provide clear peak regions in probability distributions, revealing a visible dependence on the collision energy.

5. Summary

We have performed a detailed investigation of multistrange hadrons in relativistic heavy ion collisions, focusing on collision energies $\sqrt{s_{NN}} = 39$ and 62.4 GeV.

Based on their low number of interactions and the relatively small changes on their mean transverse momentum during the hadron gas phase, we find the assumption of ϕ and Ω as clear probes of the phase transition region justified. Performing a Bayesian analysis with and without Ω yield data has demonstrated the large effect the inclusion of multistrange hadron data can have on model-to-data comparisons when determining the “true” parameter values.

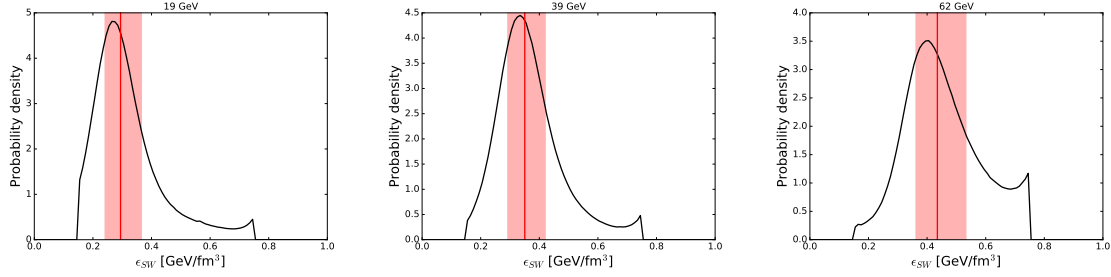


Figure 3. Posterior probability distributions of the switching energy density ϵ_{SW} for different collision energies: 19.6 GeV (left), 39 GeV (middle), and 62.4 GeV (right). Colored bands and median lines correspond to respective boxes and median lines in the right frame of Fig. 4.

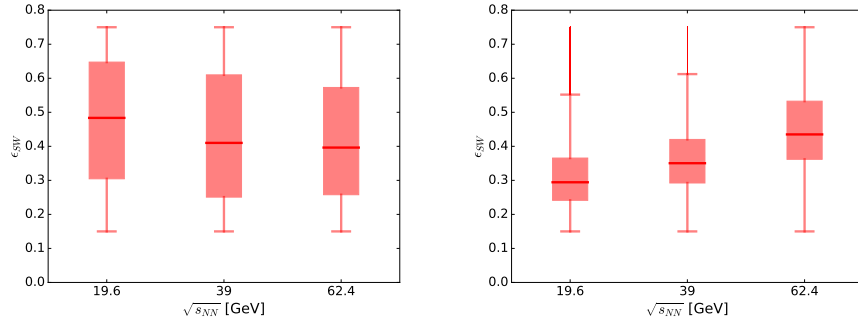


Figure 4. Box-whisker plots of the Bayesian posterior distribution of the switching energy density ϵ_{SW} vs. $\sqrt{s_{NN}}$. Left: without Ω yields. Right: with Ω yields. Boxes and median lines of the right-side figure correspond to respective colored bands and median lines in Fig. 3.

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