

# Study of the $A(e, e'n)$ reaction



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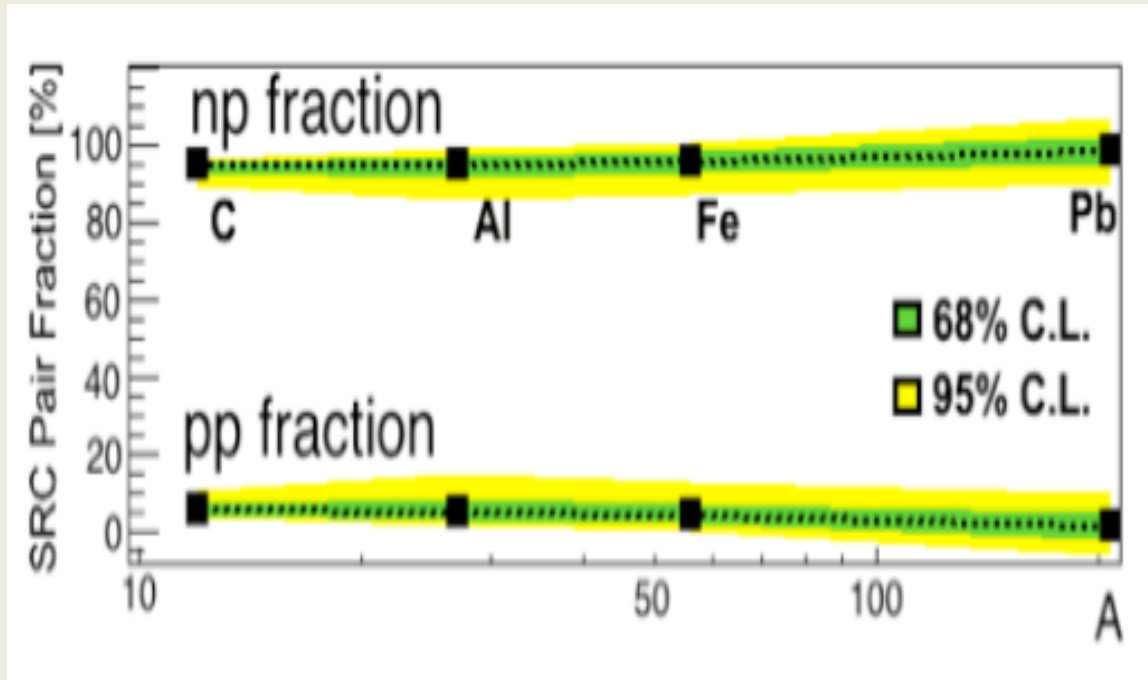
**International Workshop on Experimental and Theoretical  
Topics in CLAS Data Mining**

# Layout



- \* **Introduction and motivation**
- \* **Calculating  $\frac{(e,e'p)_A}{(e,e'n)_A}$  ratio**
- \* **Missing momentum  $(e, e'p)$  vs.  $(e, e'n)$**
- \* **Calculating  $\frac{{}^{12}\text{C}(e,e'p)_{P_{\text{miss}}\text{-high/low}}}{{}^{12}\text{C}(e,e'n)_{P_{\text{miss}}\text{-high/low}}}$**

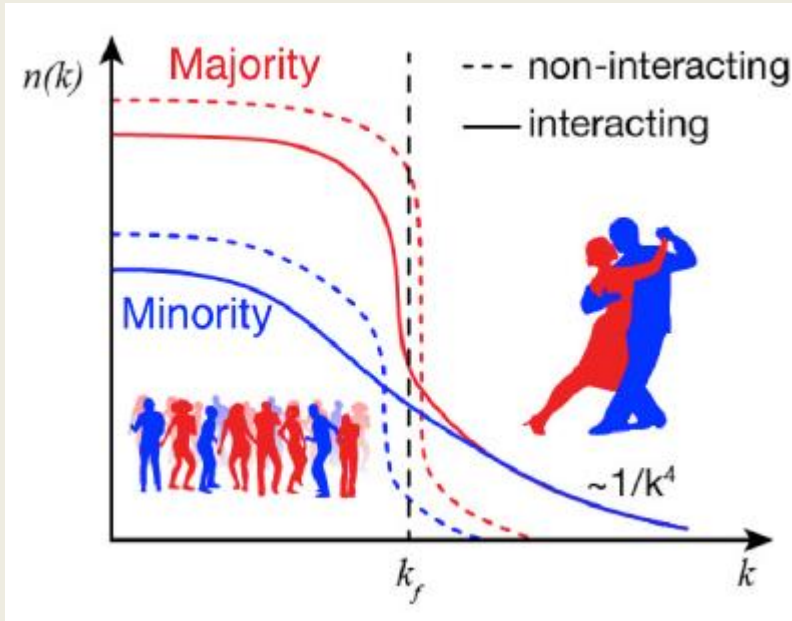
# np Dominance



**np/pp SRC  
pairs ratio**

**O. Hen et al., Science 346, 614 (2014)**

# np- dominance in asymmetric neutron rich nuclei



## Universal nature of SRC:

**A proton have greater probability than a neutron to be above the Fermi sea.**

$$(k > K_F)$$

**Pauli principle**



$$\langle K_n \rangle > \langle K_p \rangle$$

?

**SRC**



$$\langle K_p \rangle > \langle K_n \rangle$$



**Possible inversion of the momentum sharing.**

# Protons move faster than neutrons in $N > Z$ nuclei

## Light nuclei $A < 12$

Variational Monte-Carlo calculations by the Argonne group.

Nucleus	Asymmetry (N-Z)/A	$\langle T_p \rangle$ [MeV]	$\langle T_n \rangle$ [MeV]	$\langle T_p \rangle / \langle T_n \rangle$
${}^8\text{He}$	0.5	30.13	18.60	1.62
${}^6\text{He}$	0.33	27.66	19.60	1.41
${}^9\text{Li}$	0.33	31.39	24.91	1.26
${}^3\text{He}$	-0.33	14.71	19.35	0.76
${}^3\text{H}$	0.33	19.61	14.96	1.31
${}^8\text{Li}$	0.25	28.95	23.98	1.21
${}^{10}\text{Be}$	0.20	30.20	25.95	1.16
${}^7\text{Li}$	0.14	26.88	24.54	1.09
${}^9\text{Be}$	0.11	29.82	27.09	1.10
${}^{11}\text{B}$	0.09	33.40	31.75	1.05

R. B. Wiringa, R. Sehiavilla, S.C. Pieper, J. Carlson, Phys. Rev. C89, 024305 (2014).

# Heavy nuclei ( $A > 12$ )

$$\langle T_{p(n)} \rangle = \int n_{p(n)}(\mathbf{k}) \cdot \frac{k^2}{2m} \cdot d^3k$$

**Taking a simple np- dominance model:**

$$n_p(k) = \begin{cases} \eta \cdot n_{MF}(k) & k \leq k_0 \\ \frac{a_{2(A/d)} \cdot n_d(k)}{2 \cdot Z/A} & k \geq k_0 \end{cases}$$

$$n_n(k) = \begin{cases} \eta \cdot n_{MF}(k) & k \leq k_0 \\ \frac{a_{2(A/d)} \cdot n_d(k)}{2 \cdot N/A} & k \geq k_0 \end{cases}$$

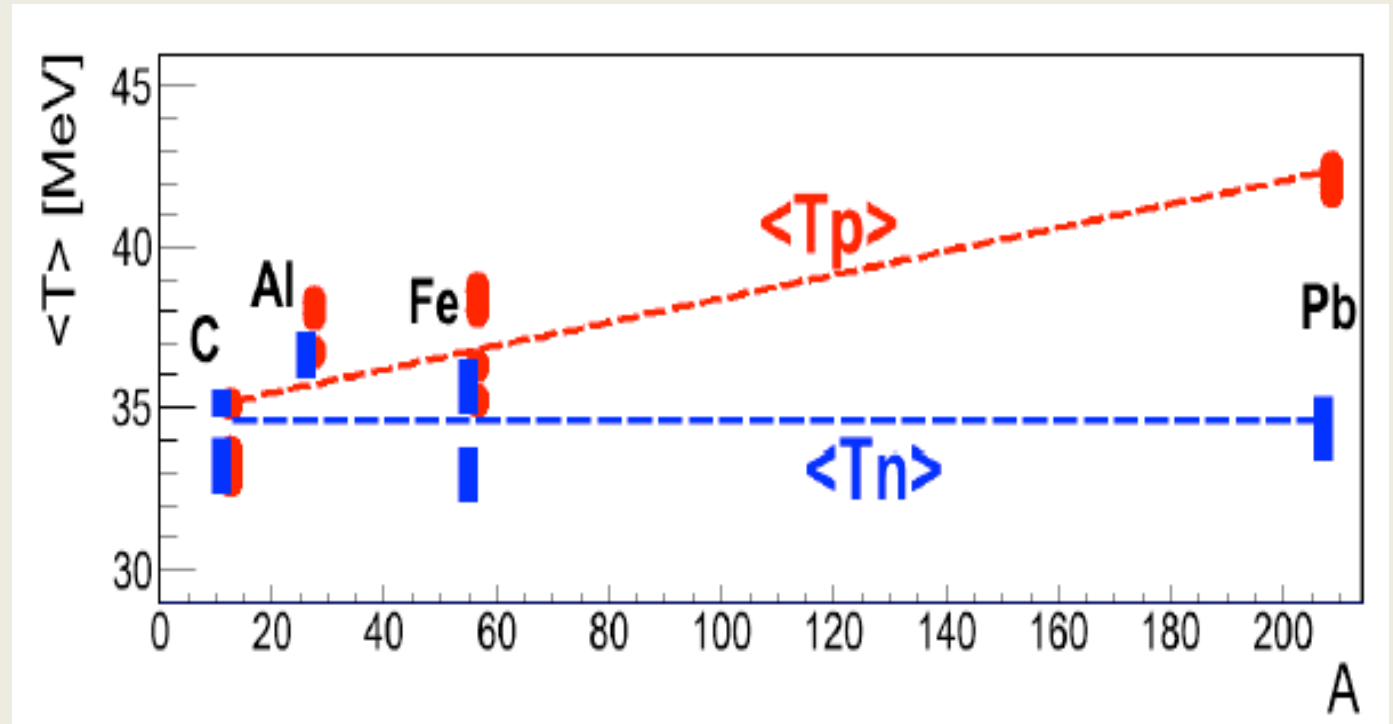
where  $\eta$  is determined by:  $4\pi \int n_{p(n)}(k) k^2 dk = 1$

# Considered 3 models for $n_{MF}(k)$ :

- \* Wood Saxon
- \* Serot – Walecka
- \* Ciofi and Simula

# Considered 2 values of $k_0$ :

- \* 300 MeV/c
- \*  $k_F$



## How to check this hypothesis experimentally?

**Problem:** One body momentum distributions are not observables.

**Solution:** Define proxy which:

1. Reflects well the difference between proton and neutron momentum distributions.
2. Can be well determined experimentally.

**Compare it to calculation.**



# A direct consequence of np- dominance for asymmetric nuclei:

**Protons** move faster than **neutrons**

$$\langle K_p \rangle > \langle K_n \rangle \quad \langle T_p \rangle > \langle T_n \rangle$$

$${}^{208}\text{Pb}: \quad N = 128 \quad Z = 82$$

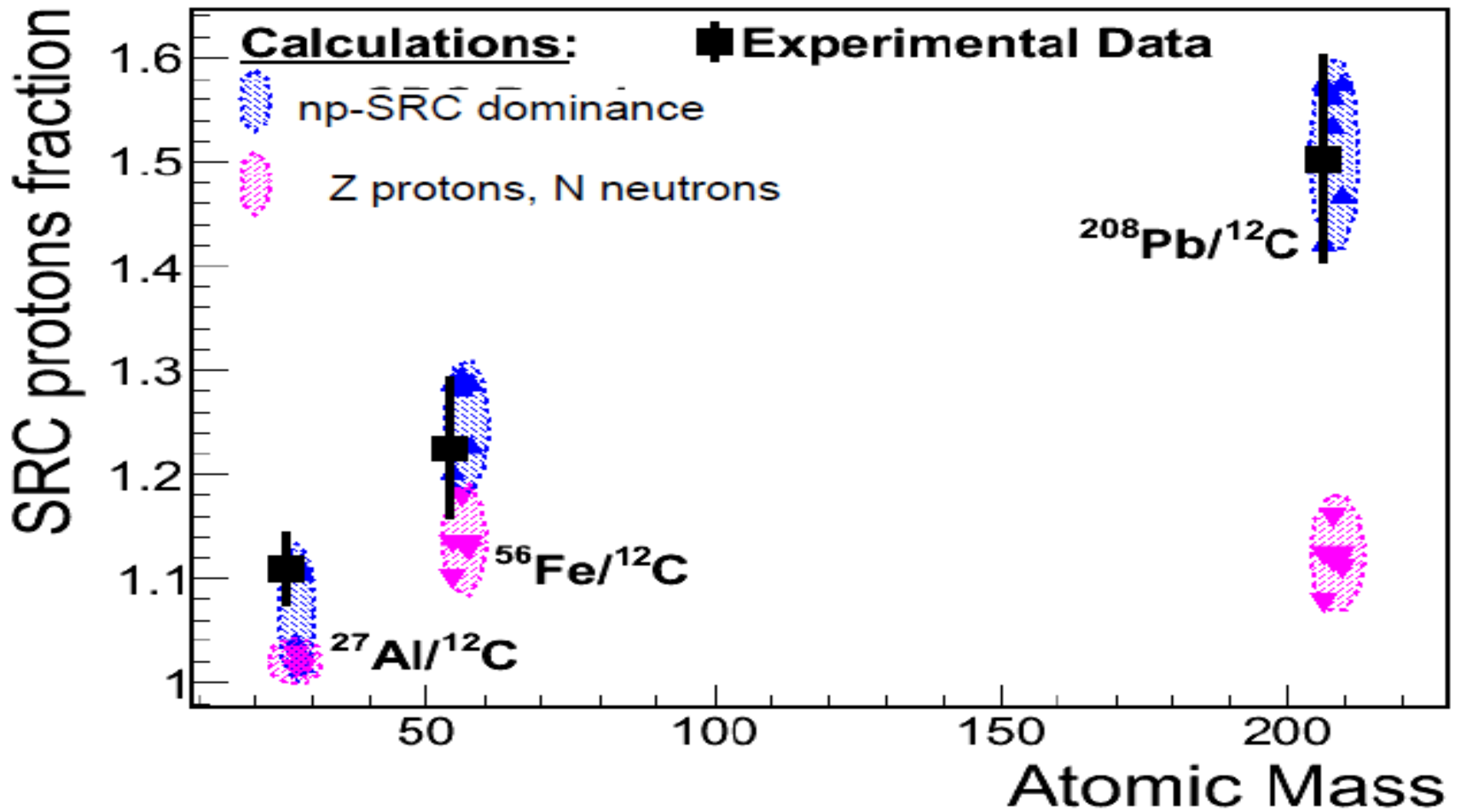
$$R_p = \frac{\# \text{ protons} |_{k > K_F}}{\# \text{ protons} |_{k < K_F}} \approx \frac{16}{82-16} \approx 0.25$$

$$R_n = \frac{\# \text{ neutrons} |_{k > K_F}}{\# \text{ neutrons} |_{k < K_F}} \approx \frac{16}{128-16} \approx 0.15$$

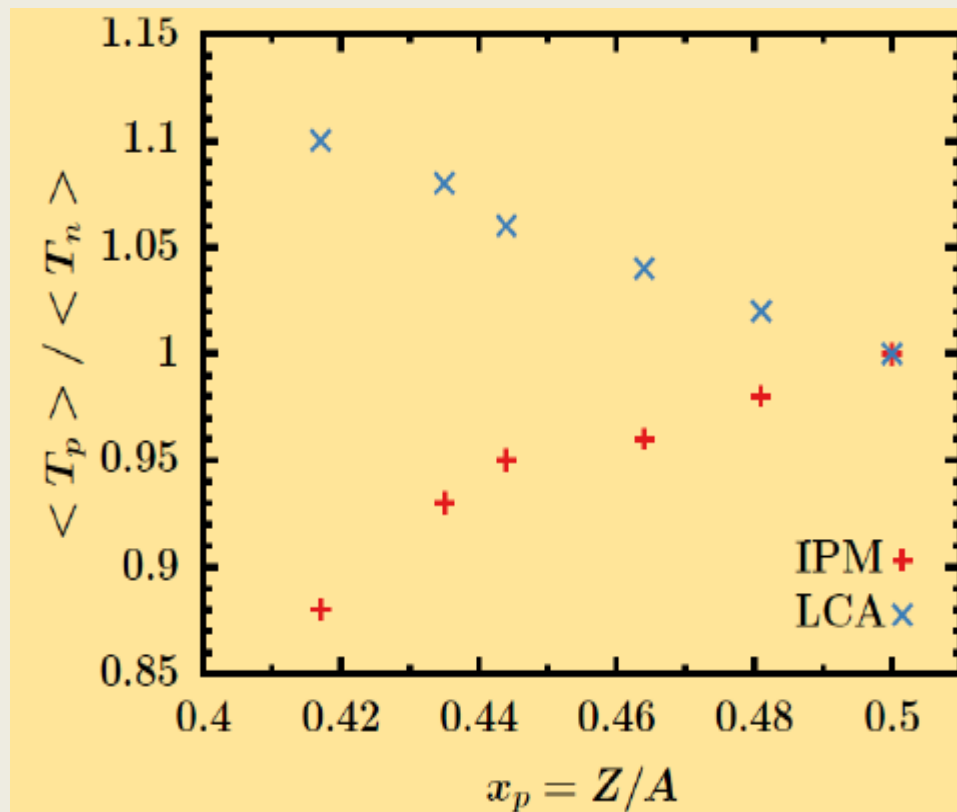
$$\frac{R_p}{R_n} \approx 1.7$$

$$\frac{A(e, e'p) / {}^{12}C(e, e'p) |_{\text{high}}}{A(e, e'p) / {}^{12}C(e, e'p) |_{\text{low}}}$$

# $(e, e'p)$ double ratio



# Another prediction for $\langle T_p \rangle / \langle T_n \rangle$ ratio

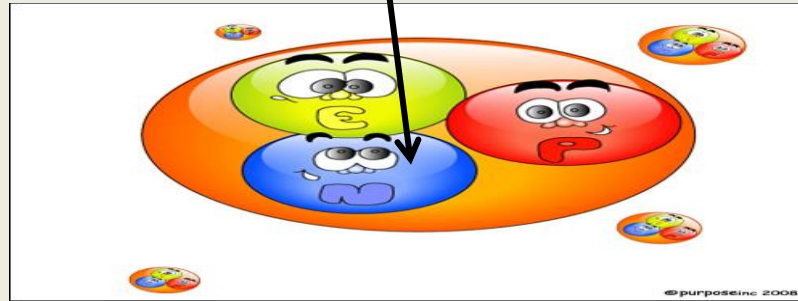


## Average kinetic energy per nucleon

	$\langle T_N \rangle$ (MeV)			
	PM (p)	IPM (n)	LCA (p)	LCA(n)
$^{27}\text{Al}$	16.61	16.92	30.93	30.26
$^{40}\text{Ca}$	16.44	16.42	31.23	31.18
$^{48}\text{Ca}$	15.64	17.84	33.04	30.06
$^{56}\text{Fe}$	16.71	17.45	32.33	31.13
$^{108}\text{Ag}$	16.48	17.81	33.55	31.16

# What's next?

## Neutrons



- \* **Detecting neutrons in the EC – M. Braverman thesis (2014).**

### The goal:

Calculating  $\frac{A(e,e'n)/^{12}\text{C}(e,e'n)|_{high}}{A(e,e'n)/^{12}\text{C}(e,e'n)|_{low}}$  ratio.

### To do so:

- \* **Identify  $(e, e'n)$  mean field events.**
- \* **Identify  $(e, e'n)$  SRC events.**

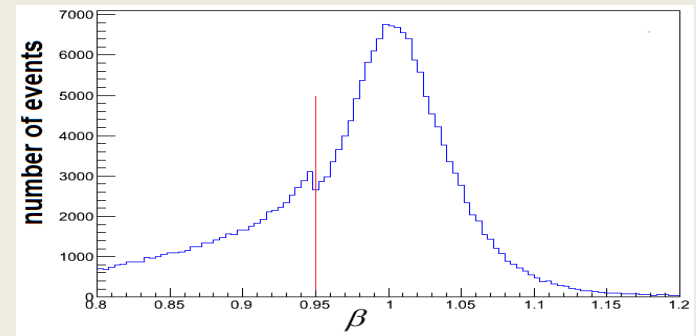
# Calculating $\frac{(e,e'p)}{(e,e'n)}$ ratio

- \* **EG<sub>2</sub> data:**  $^2d$  ,  $^{12}C$  ,  $^{27}Al$  ,  $^{56}Fe$  ,  $^{208}Pb$
- \* **Select (e,e'p) QE events**
- \* **Identify (e,e'n) QE events**
- \* **Check the event selection**
- \* **Apply corrections**
- \* **Calculate  $\frac{(e,e'p)}{(e,e'n)}$  ratio**

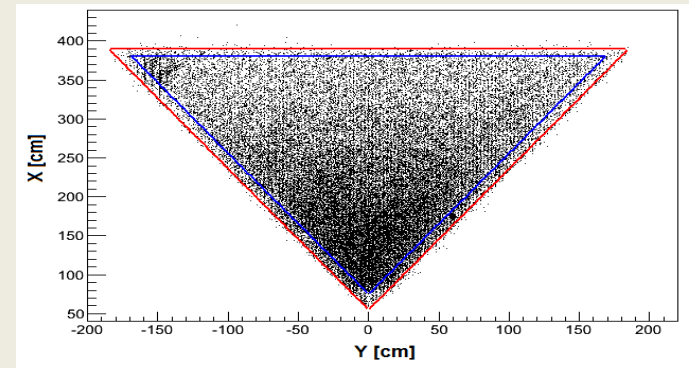
# Select $(e, e'p)$ events

\*  $(e, e'p)$  events were taken with acceptance similar to neutrons:

1.  $\beta < 0.95$



2. EC fiducial cut



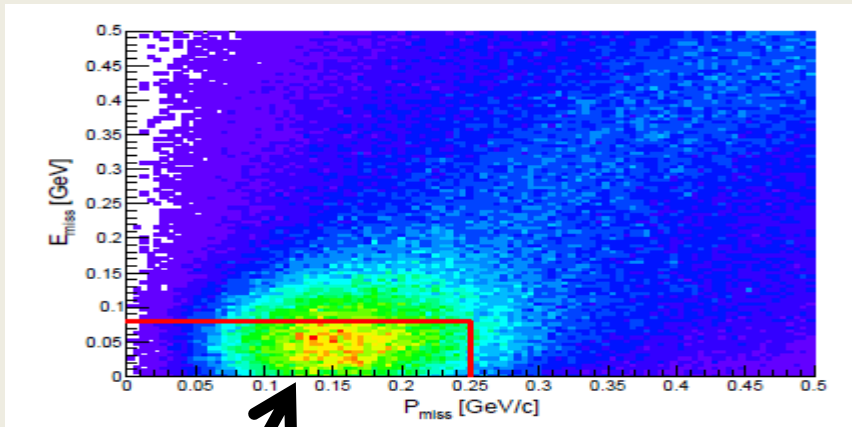
3.  $|\vec{p}| < 2.34 \text{ GeV}/c$

# Selecting Quasi-Elastic events

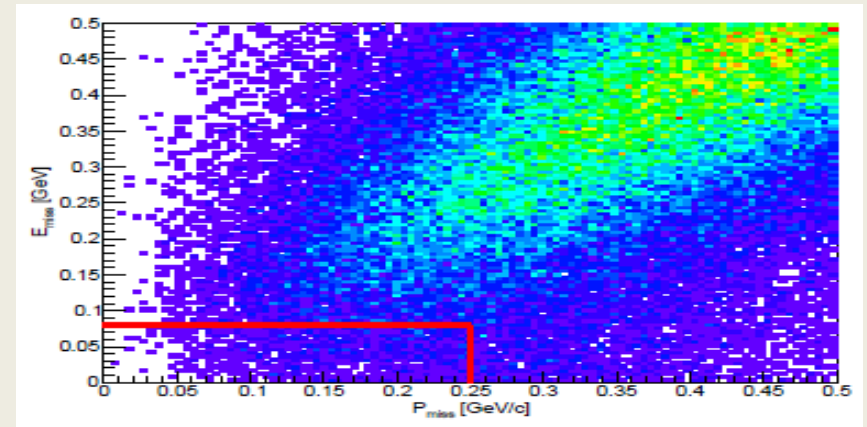
**Problem:** Low resolution in the EC -  $\Delta P \sim 200 \frac{\text{MeV}}{c}$ .

**Solution 1:** Using smeared protons.

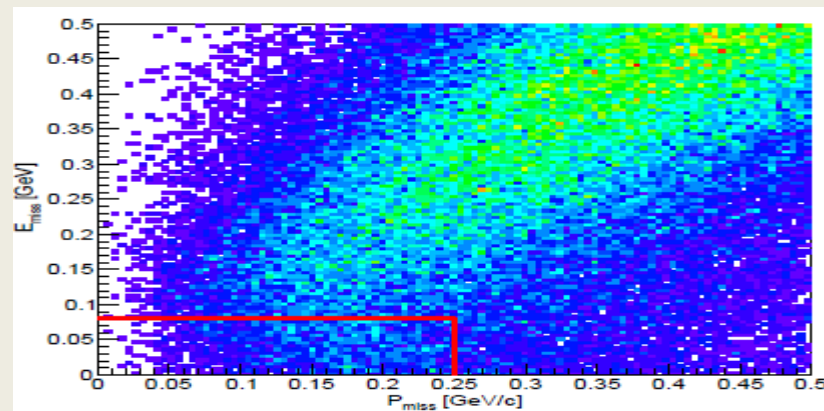
protons



smeared protons



neutrons



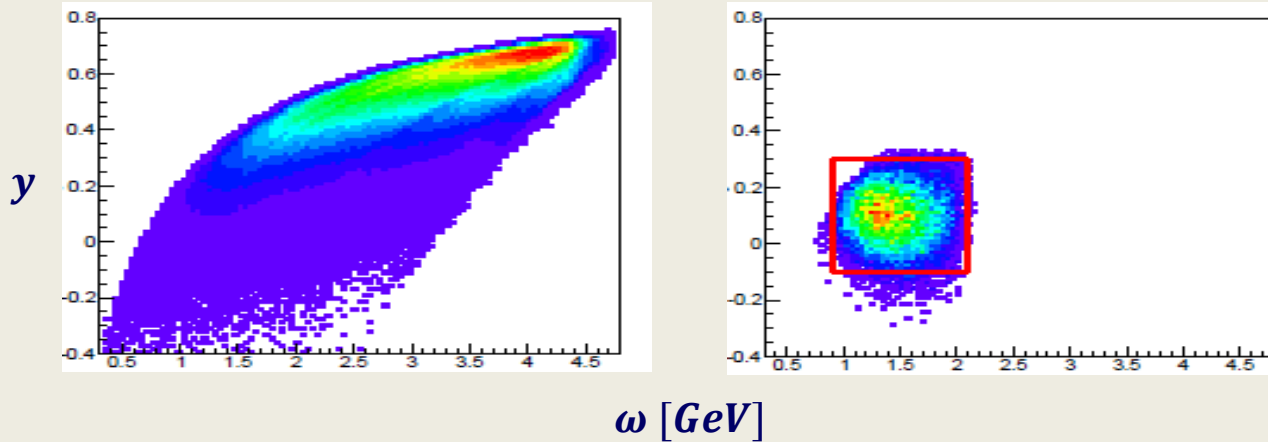
$E_{miss}$  vs.  $P_{miss}$

QE pick:

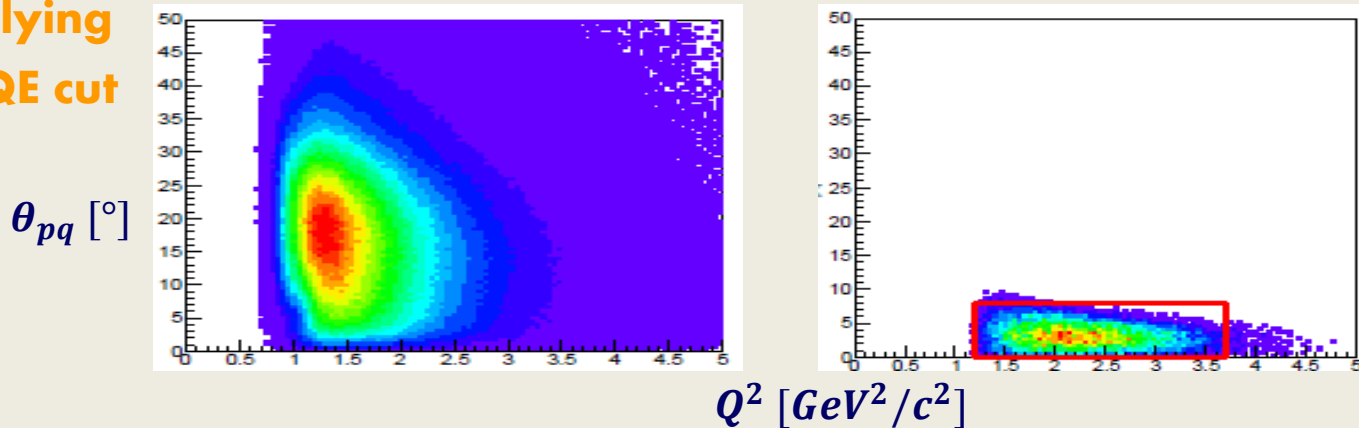
$$P_{miss} < 0.25 \text{ GeV}/c$$

$$E_{miss} < 0.08 \text{ GeV}$$

# Solution 2: Using electron quantities and scattering angle of the nucleon.



before  
applying  
the QE cut



after  
applying  
the QE cut

$$y \equiv \left( (M_A + \omega) \sqrt{\Lambda^2 - M_{A-1}^2 W^2} - q\Lambda \right) / W^2$$

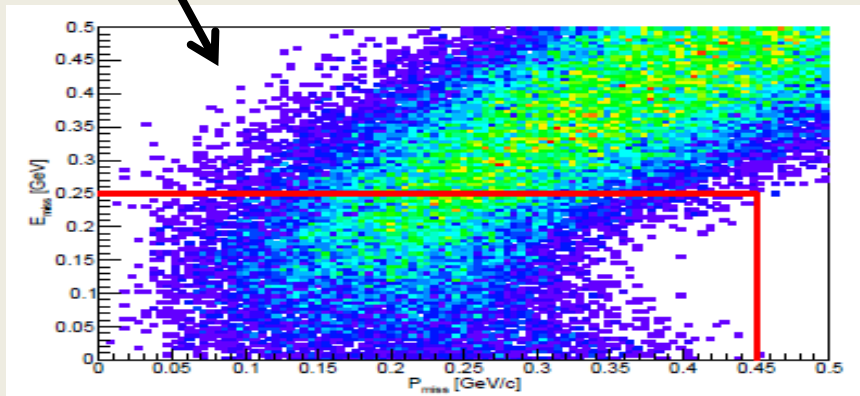
$$\Lambda = (M_{A-1}^2 - M_N^2 + W^2) / 2 \quad W = \sqrt{(M_A + \omega)^2 - q^2}$$



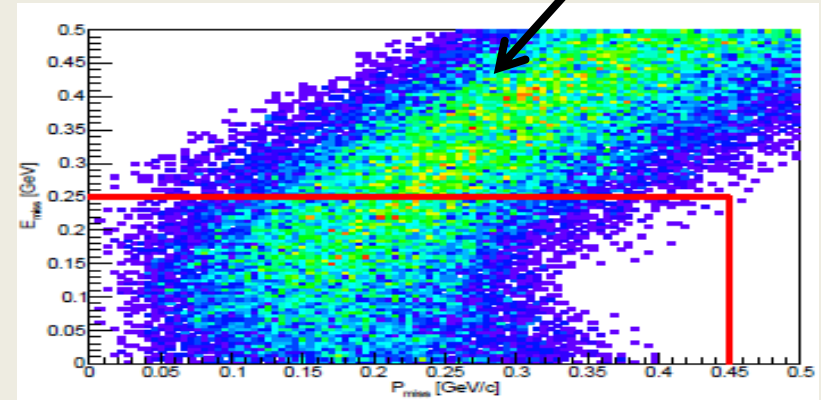
# We applied the following cuts:

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $\theta_{pq} < 8^\circ$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$

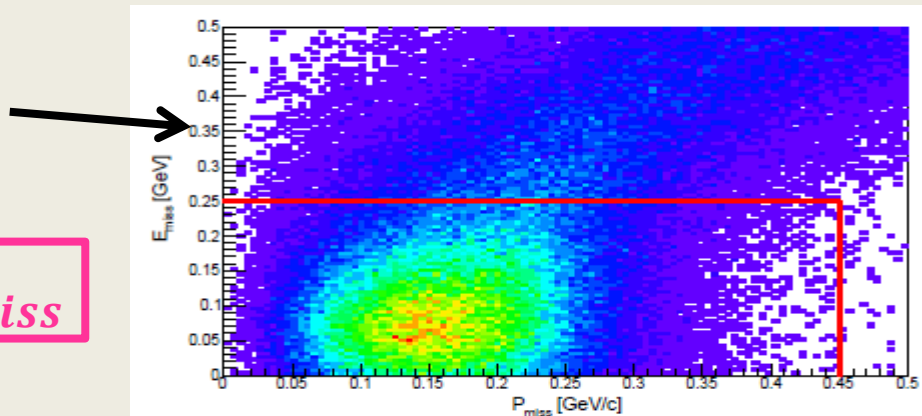
**smearred protons**



**neutrons**



**un-smearred  
protons**



$E_{miss} \text{ vs. } P_{miss}$

**The selected  
cuts:**

$$P_{miss} < 0.45 \text{ GeV}/c$$

$$E_{miss} < 0.25 \text{ GeV}$$

# Checking Selection - 1

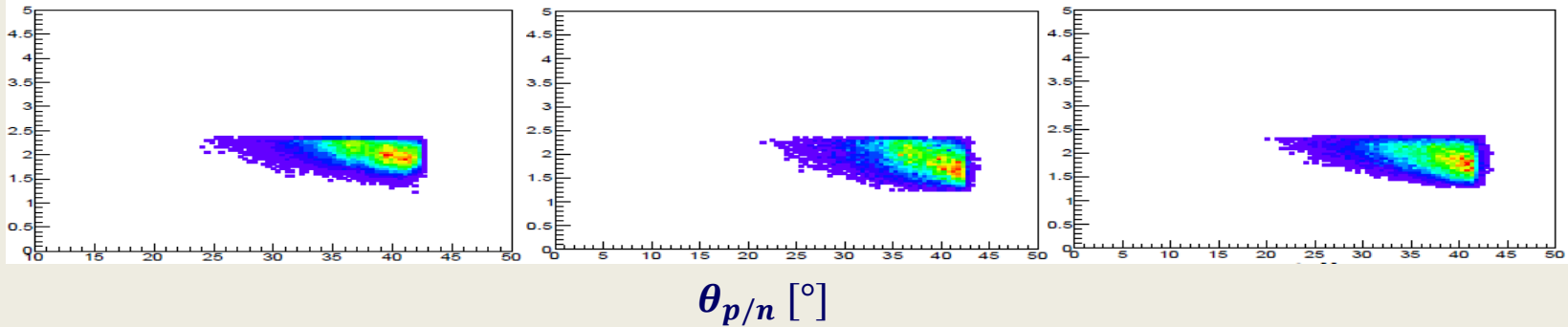
- \* We looked at pairs of kinematic variables which supposed to be correlated according to 2-body kinematics.

protons

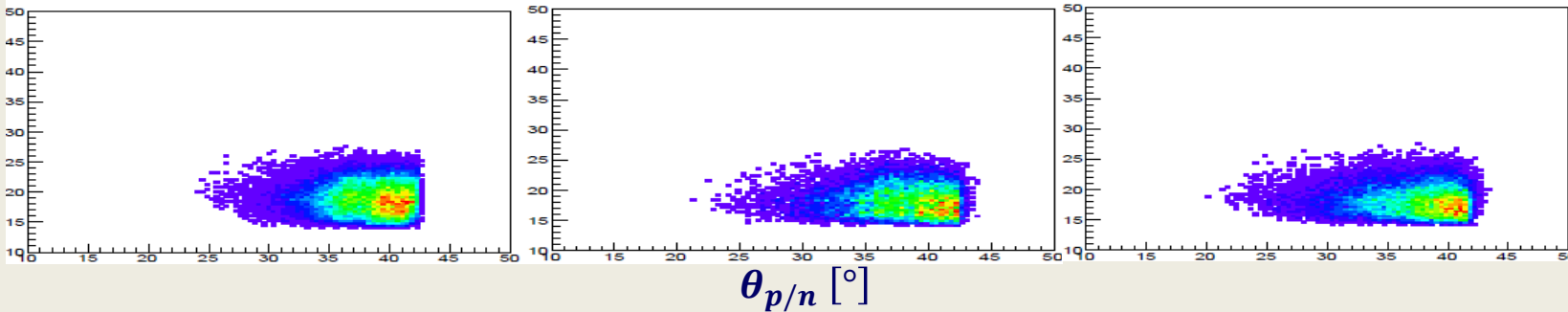
smearred protons

neutrons

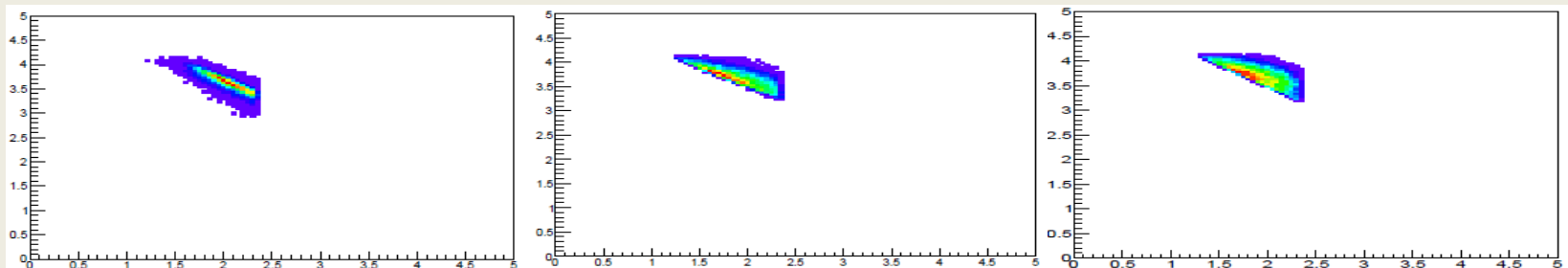
$$p_{n/p} \left[ \frac{\text{GeV}}{c} \right]$$



$$\theta_e \text{ [}^\circ\text{]}$$



$$P_e \left[ \frac{\text{GeV}}{c} \right]$$



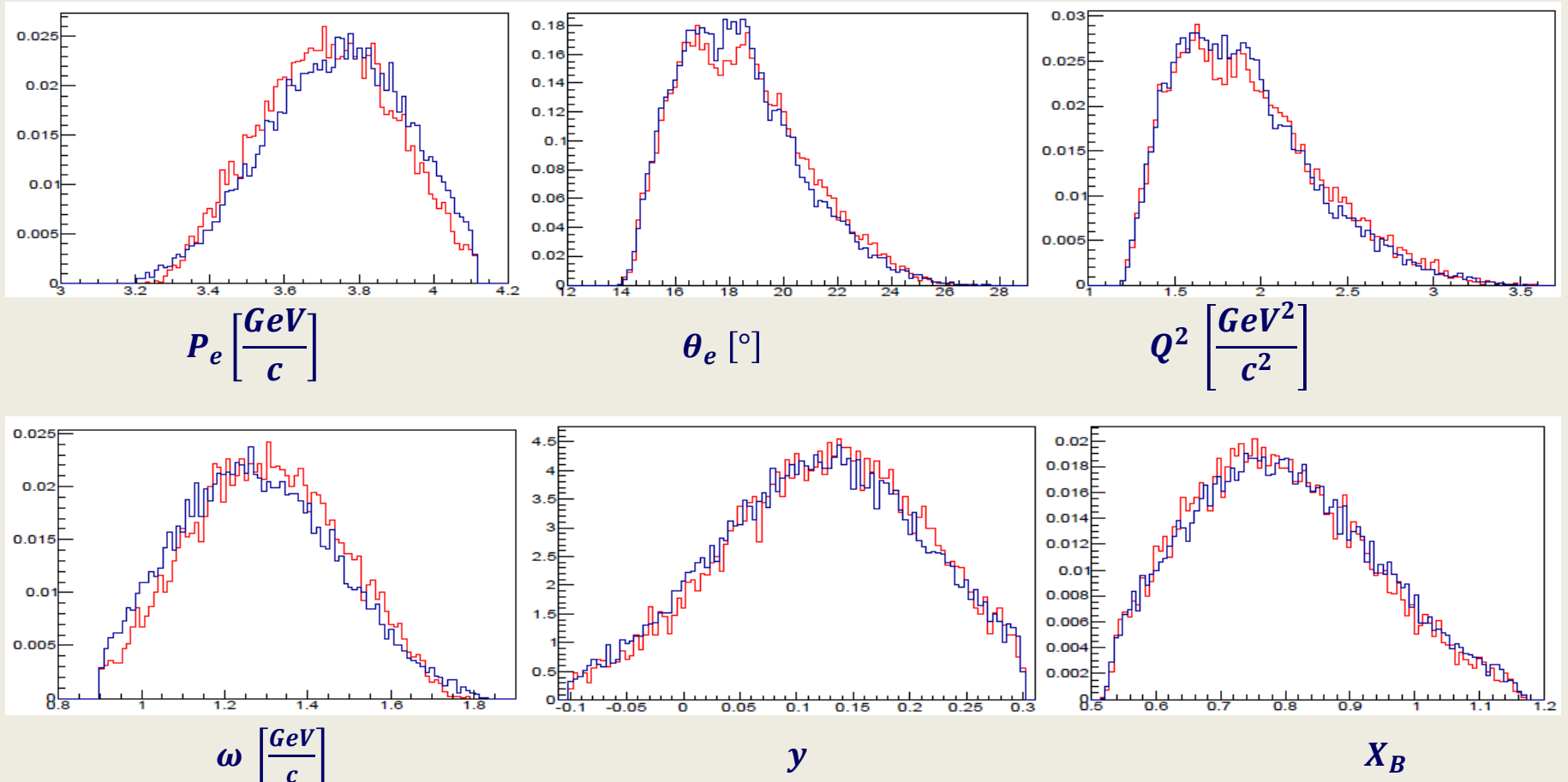
$$p_{p/n} \text{ [GeV / c]}$$

# Checking Selection - 2

\* We looked at the electron quantities distributions.

**smear** **protons**

**neutrons**

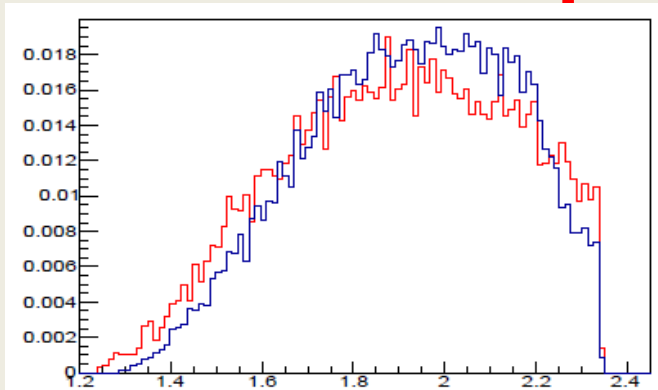


# Checking Selection - 3

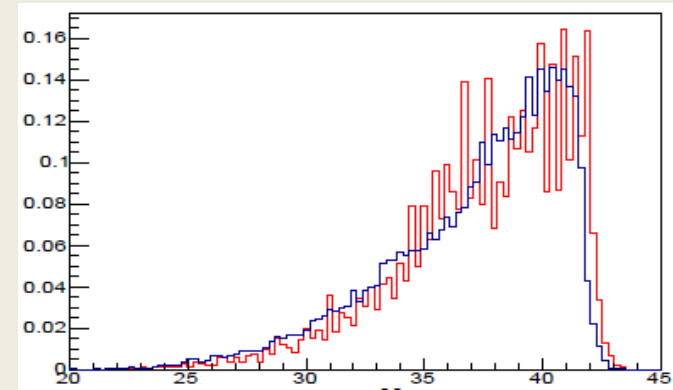
- \* We looked at the smeared proton and neutron quantities.

**smeared protons**

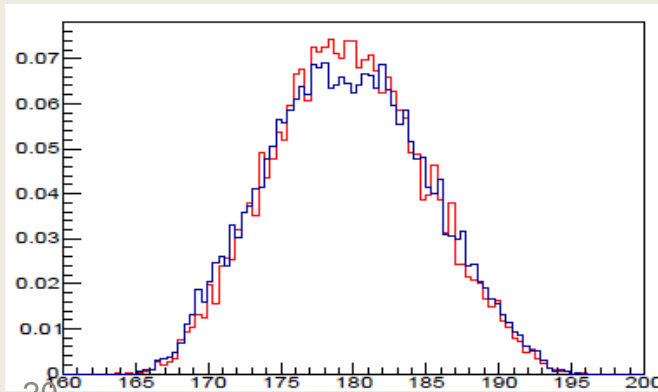
**neutrons**



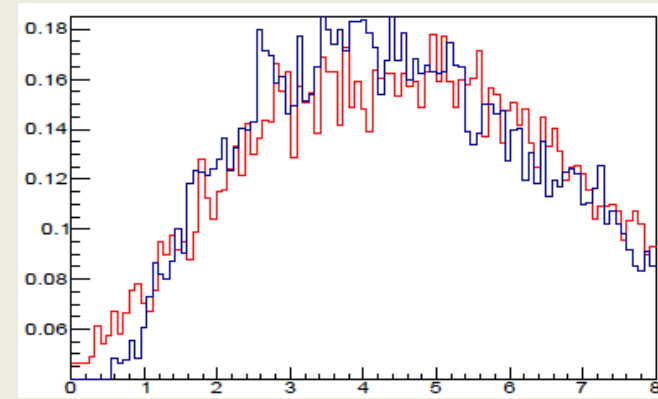
$p_{p/n} \left[ \frac{GeV}{c} \right]$



$\theta_{p/n} [^\circ]$



$|\varphi_{p/n} - \varphi_e| [^\circ]$



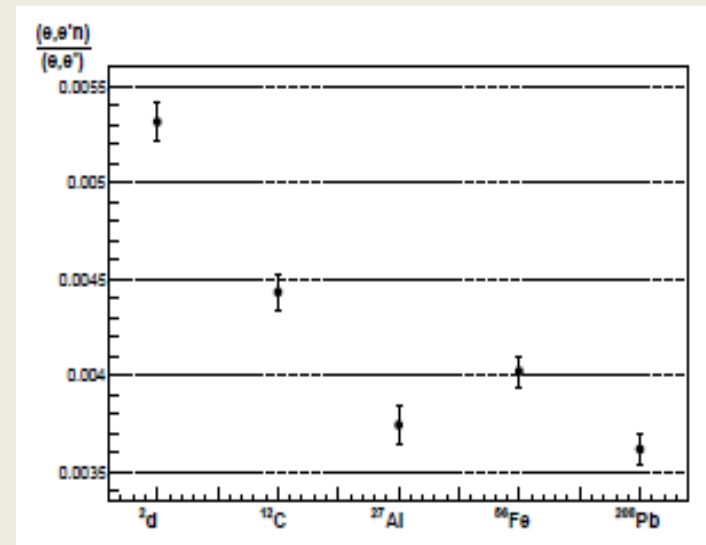
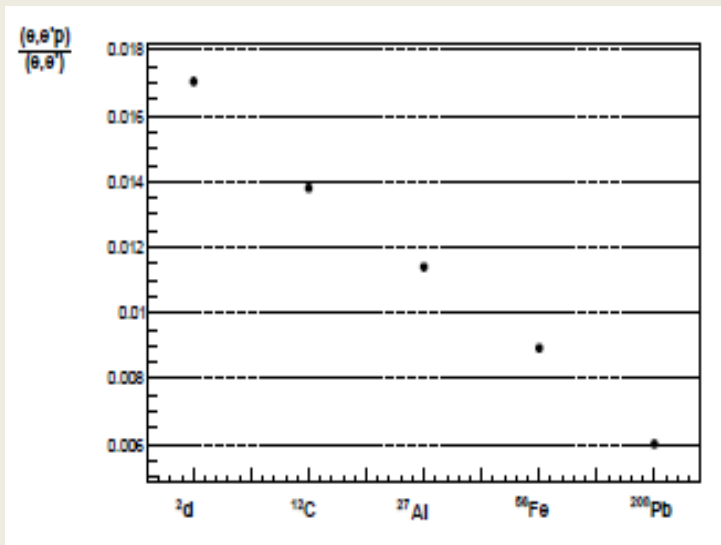
$\theta_{pq \setminus nq} [^\circ]$

# Checking Selection 4 - Transparency

- \* We expect that the amount of  $(e,e'p)$  and  $(e,e'n)$  relatively to  $(e,e')$  will decrease as a function of  $A$ .

un-smearred protons

neutrons



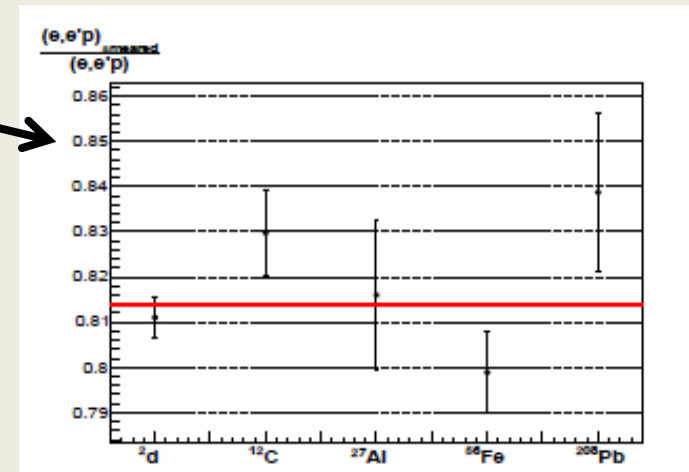
# Corrections

## Protons:

- \* **Coulomb correction**
- \* **Using CLAS Monte-Carlo simulation:**
  1. **Acceptance correction**
  2. **Detection efficiency**

## Neutrons:

- \* **Correction for neutron resolution**
- \* **Using CLAS Monte-Carlo simulation:**
  1. **Acceptance correction**
  2. **Detection efficiency**
  3. **EC fiducial cut**



$$\eta = 0.814 \pm 0.04(0.06) \quad \chi^2/NDF = 1.9$$

# Acceptance + Detection Efficiency

- \* **Same good  $e$**

- \* **10,000  $(e, e'p)$  events:**

$$p \sim U(1.3, 2.4)$$

$$\theta_p \sim U(10, 50)$$

- \* **For each of them: 30 times  $\varphi_p \sim U(0, 2\pi)$**

- \* **GSIM Monte-Carlo simulation**

- \* **GPP**

- \* **RECSIS**

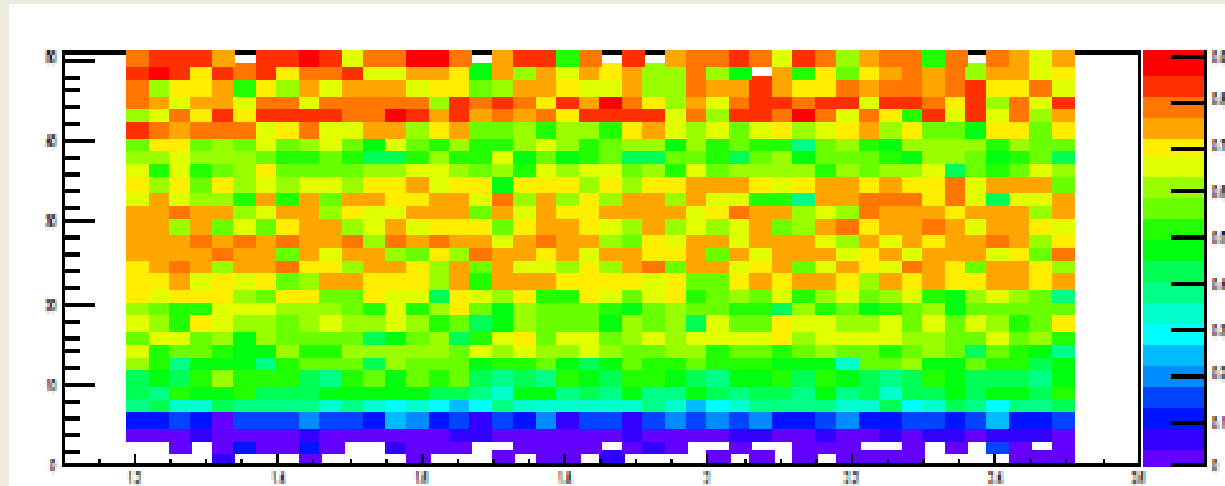
- \* **Dividing in discovered/generated by binning in**

$p$  and  $\theta_p$

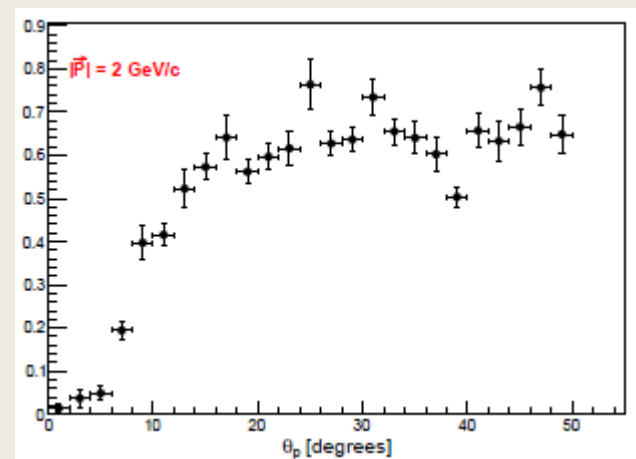
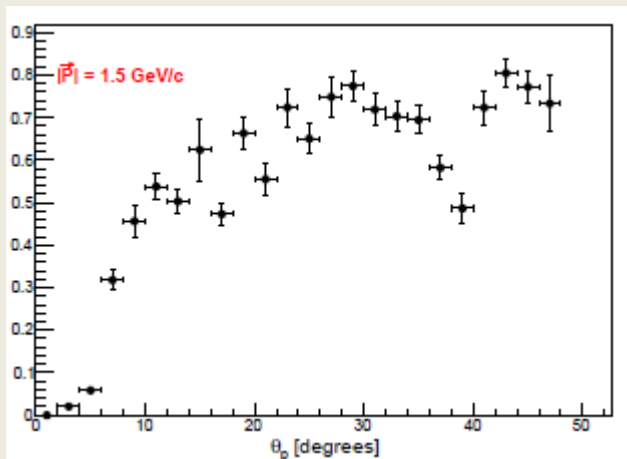
# Acceptance + Detection Efficiency

## Protons

$\theta_p$  [°]

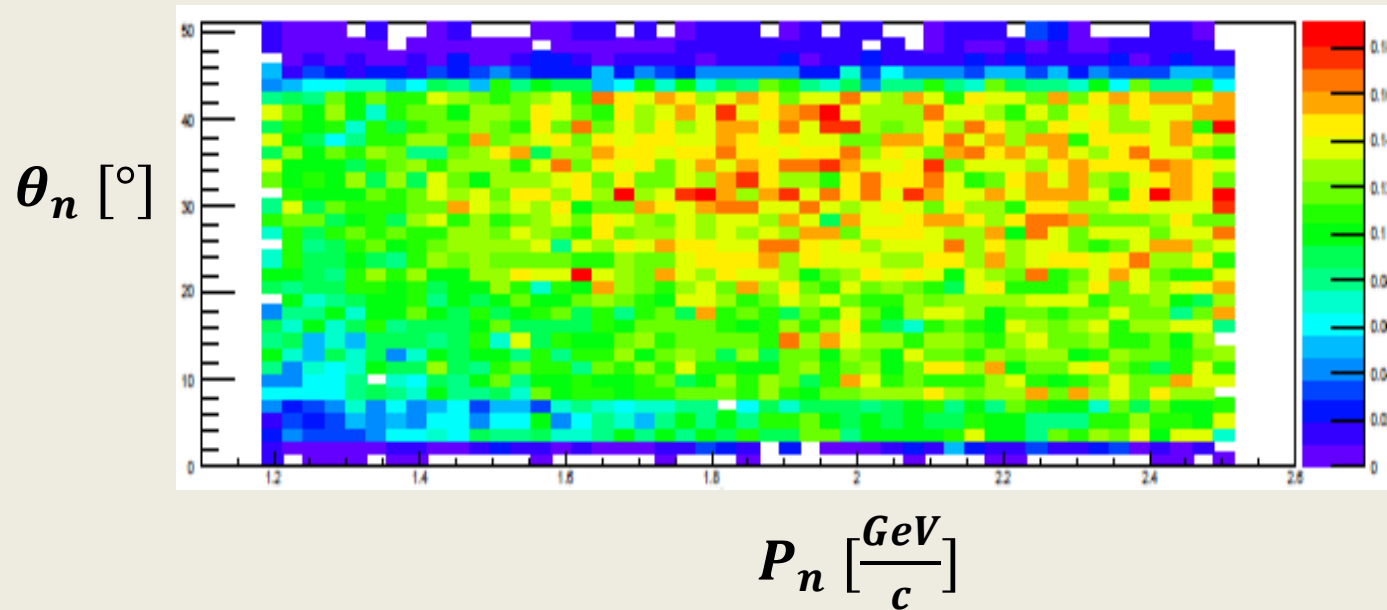


$P_p$  [ $\frac{\text{GeV}}{c}$ ]

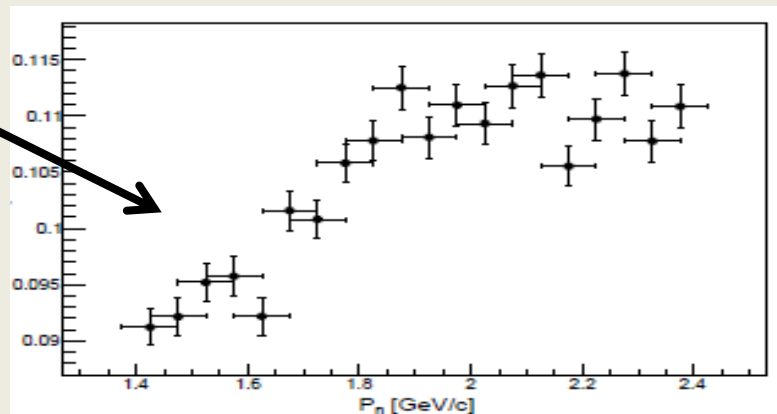




# Acceptance + Detection Efficiency + Fiducial Cut Neutrons



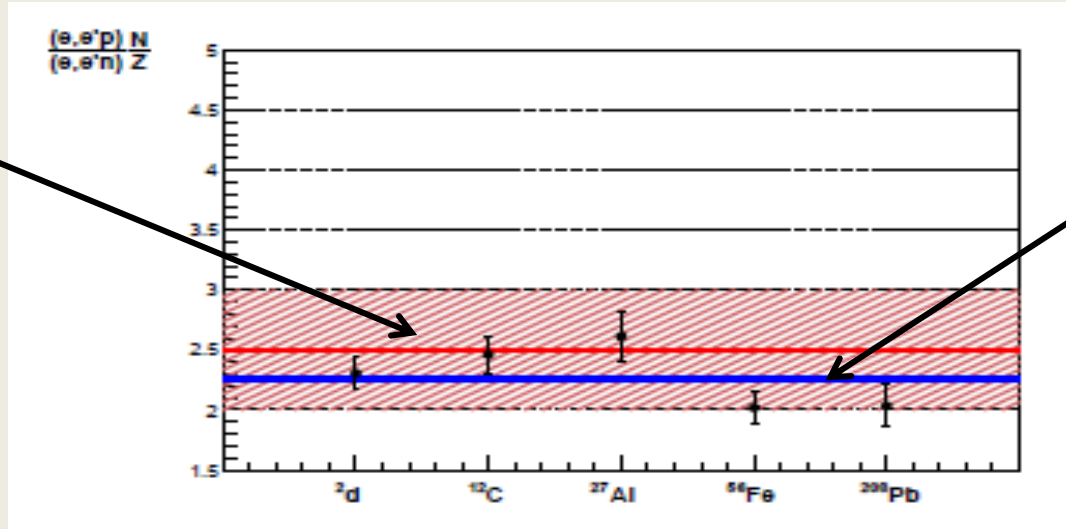
$\theta_n \approx 30^\circ$



# $\frac{(e,e'p)}{(e,e'n)} \frac{Z}{N}$ ratios

$E_{beam} = 5.009 \text{ GeV}$

$2.5 \pm 0.5$



$2.26 \pm 0.13$   
(0.20)

$\frac{\chi^2}{NDF} = 2.3$

**Red Lines** =  $\frac{\sigma_p}{\sigma_n}$  and its  $\pm 1\sigma$  limits as taken from [1].

**Blue Line** = our result to a constant fit.

[1] J. Lachniet, et al. Phys. Rev. Lett. 102, 192001 (2009).

# Smearred $P_{miss}$ vs. un-smearred

$^{12}\text{C}(e, e'p)$  &  $^{12}\text{C}(e, e'p_{smearred})$

\*  $-0.1 < y < 0.3$

\*  $\theta_{pq} < 8^\circ$

\*  $0.9 < \omega < 2.1 \text{ GeV}$

\*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$

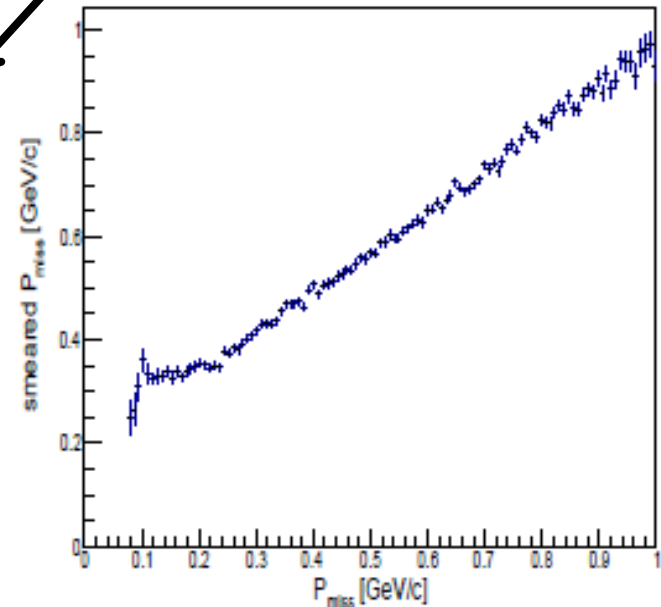
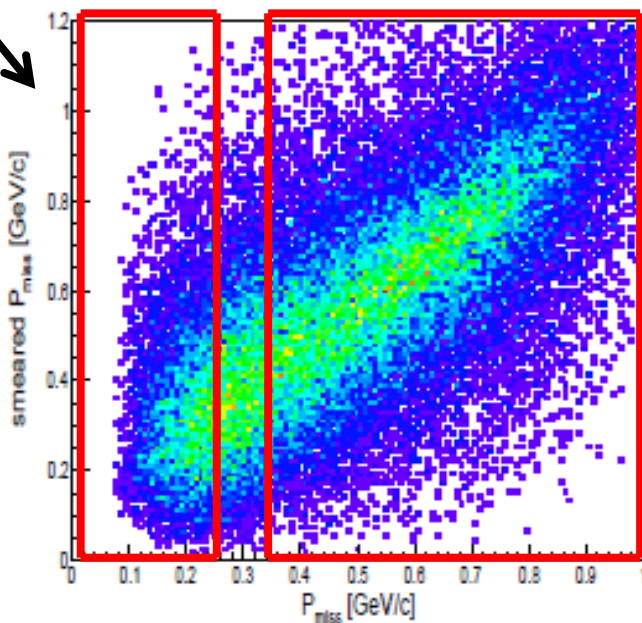
\*  $\beta < 0.95$

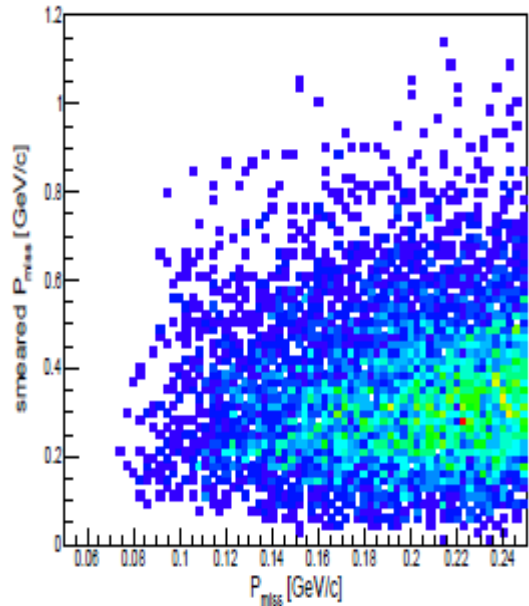
\* **EC fiducial cut**

\*  $|\vec{p}| < 2.34 \text{ GeV}/c$

low

high

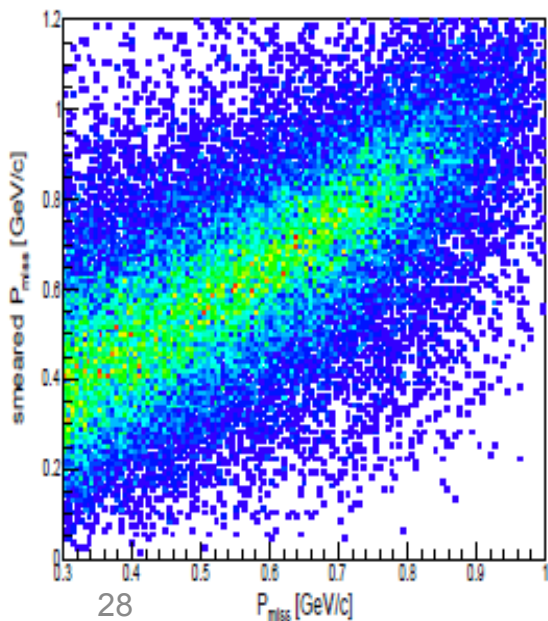




**Low (lost events)**

$$0 < P_{miss} < 0.25 \text{ GeV}/c$$

$$\eta_{low} = \frac{\#(e,e'p)_{smeared}}{\#(e,e'p)} \Big|_{P_{miss} < 0.25} = 0.63 \pm 0.01$$



**High (gain events)**

$$0.35 < P_{miss} < 1 \text{ GeV}/c$$

$$\eta_{high} = \frac{\#(e,e'p)_{smeared}}{\#(e,e'p)} \Big|_{0.35 < P_{miss} < 1} = 1.17 \pm 0.02$$

**Statistical error**



# Back to neutrons

With  $E_{\text{miss}} < 0.25$  GeV:

$$\frac{\sigma_p}{\sigma_n} = 2.26 \pm 0.2$$

$$\frac{\left. \frac{{}^{12}\mathcal{C}(e, e'n)}{{}^{12}\mathcal{C}(e, e'p)} \right|_{P_{\text{miss}} < 0.25}}{\eta_{\text{low}} \cdot \frac{\sigma_p}{\sigma_n}} = 1.05 \pm 0.13(0.10)$$

Statistical error

$$\frac{\left. \frac{{}^{12}\mathcal{C}(e, e'n)}{{}^{12}\mathcal{C}(e, e'p)} \right|_{0.35 < P_{\text{miss}} < 1}}{\eta_{\text{high}} \cdot \frac{\sigma_p}{\sigma_n}} = 1.02 \pm 0.17(0.14)$$

Acceptance, detection efficiency, statistical,  $\eta_{\text{low,high}}$ ,  $\frac{\sigma_p}{\sigma_n}$ , neutron resolution, fiducial cut (neutrons)

# Before looking at the A-dependence:

$$* R_p = \frac{{}^{12}\mathcal{C}(e,e'p)_{0.35 < p_{miss} < 1}}{{}^{12}\mathcal{C}(e,e'p)_{p_{miss} < 0.25}}$$

$$* R_n = \frac{{}^{12}\mathcal{C}(e,e'n)_{0.35 < p_{miss} < 1}}{{}^{12}\mathcal{C}(e,e'n)_{p_{miss} < 0.25}}$$

$$? \\ R_p \approx R_n$$

- \* **Review all the uncertainties of the ratios presented**
- \* **Prepare a review for the CLAS analysis committee**

# Future Plans

$$\begin{array}{l} \textit{np-dominance} \\ A(e, e'n) / {}^{12}C(e, e'n) | \textit{high} \\ \hline A(e, e'n) / {}^{12}C(e, e'n) | \textit{low} \end{array}$$

*2N - SRC*  
*(e, e'np<sub>back</sub>)*

*3N - SRC*  
*(e, e'npp)*

# **Backup slides**



# $(e, e')$ selection

**In order to select  $(e, e')$  events we applied the following cuts:**

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$

# $(e, e'n)$ selection

In order to select  $(e, e'n)$  events we applied the following cuts and corrections:

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$
- \*  $\theta_{pq} < 8^\circ$
- \*  $\beta < 0.95$
- \* **EC fiducial cut**
- \*  $|\vec{p}| < 2.34 \text{ GeV}/c$
- \*  $P_{\text{miss}} < 0.45 \frac{\text{GeV}}{c}$
- \*  $E_{\text{miss}} < 0.25 \text{ GeV}$
- \* **Acceptance correction + detection efficiency + EC fiducial cut**
- \* **Effectiveness of the EC**

# $(e, e'p)$ selection

**In order to select  $(e, e'p)$  events we applied the following cuts and corrections:**

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$
- \*  $\theta_{pq} < 8^\circ$
- \*  $\beta < 0.95$
- \*  $|\vec{p}| < 2.34 \text{ GeV}/c$
- \*  $P_{\text{miss}} < 0.45 \frac{\text{GeV}}{c}$
- \*  $E_{\text{miss}} < 0.25 \text{ GeV}$
- \* **Acceptance correction + detection efficiency**
- \* **Coulomb correction**

# $\frac{(e, e' p_{\text{smeared}})}{(e, e' p)}$ selection

In order to select  $(e, e' p)$  smeared and un-smeared events we applied the following cuts and corrections:

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$
- \*  $\theta_{pq} < 8^\circ$
- \*  $\beta < 0.95$
- \* **EC fiducial cut**
- \*  $|\vec{p}| < 2.34 \text{ GeV}/c$
- \*  $P_{\text{miss}} < 0.45 \frac{\text{GeV}}{c}$
- \*  $E_{\text{miss}} < 0.25 \text{ GeV}$
- \* **Coulomb correction**

$$\frac{(e, e' p_{\text{smearred}})}{(e, e' p)} \Big|_{p_{\text{miss-low/high}}} \quad \text{selection}$$

**In order to select  $(e, e' p)$  smeared and un-smeared events we applied the following cuts and corrections:**

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$
- \*  $\theta_{pq} < 8^\circ$
- \*  $\beta < 0.95$
- \* **EC fiducial cut**
- \*  $|\vec{p}| < 2.34 \text{ GeV}/c$
- \*  $P_{\text{miss}} < 0.25 \frac{\text{GeV}}{c}$  or  $0.35 < P_{\text{miss}} < 1 \text{ GeV}/c$
- \* **Coulomb correction**

# $(e, e'n)$ selection

**In order to select  $(e, e'n)$  events we applied the following cuts and corrections:**

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$
- \*  $\theta_{pq} < 8^\circ$
- \*  $\beta < 0.95$
- \* **EC fiducial cut**
- \*  $|\vec{p}| < 2.34 \text{ GeV}/c$
- \*  $E_{miss} < 0.25 \text{ GeV}$
- \*  $P_{miss} < 0.25 \frac{\text{GeV}}{c}$  or  $0.35 < P_{miss} < 1 \text{ GeV}/c$
- \* **Acceptance correction + detection efficiency + EC fiducial cut**
- \* **Divided by**  $\eta_{low} = 0.63 \pm 0.01$  or  $\eta_{high} = 1.17 \pm 0.02$

# $(e, e'p)$ selection

In order to select  $(e, e'p)$  events we applied the following cuts and corrections:

- \*  $-0.1 < y < 0.3$
- \*  $0.9 < \omega < 2.1 \text{ GeV}$
- \*  $1.2 < Q^2 < 3.7 \text{ GeV}^2/c^2$
- \*  $\theta_{pq} < 8^\circ$
- \*  $\beta < 0.95$
- \*  $|\vec{p}| < 2.34 \text{ GeV}/c$
- \*  $E_{miss} < 0.25 \text{ GeV}$
- \*  $P_{miss} < 0.25 \frac{\text{GeV}}{c}$  or  $0.35 < P_{miss} < 1 \text{ GeV}/c$
- \* **Acceptance correction + detection efficiency**
- \* **Coulomb correction**