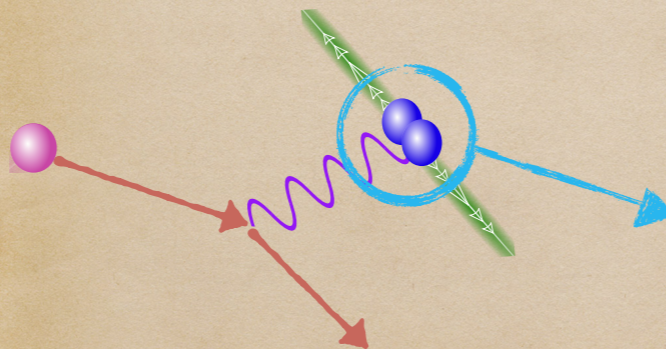


pp-SRC c.m. motion



Erez. O. Cohen,
Or Hen,
Eli Piasetzky,
Meytal Duer,
Igor Korover
Tel Aviv University

Int. Workshop on Exp. and Theo. topics in CLAS Data-Mining
Buffalo (NY), July-28, 2015

OUTLINE

- ◆ Motivation

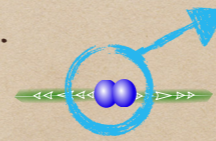
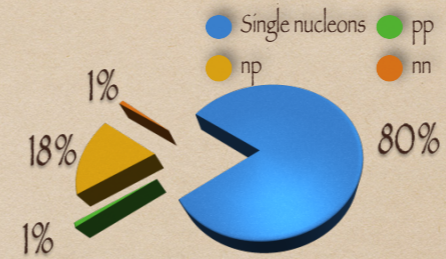
- **2N-SRC.**

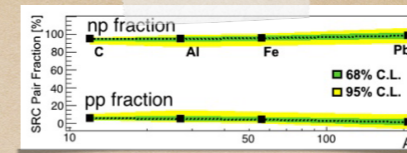
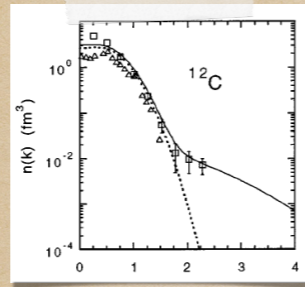
- Exclusive 2N-SRC study

- The ground state picture of **pp-SRC.**

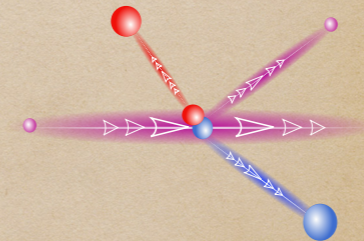
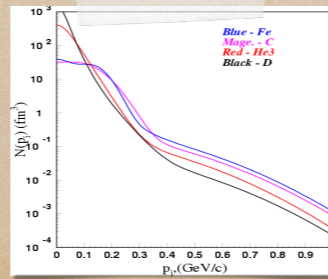
- ◆ **EG2 analysis** of pp-SRC.

- ◆ **Acceptance correction** and work under way.





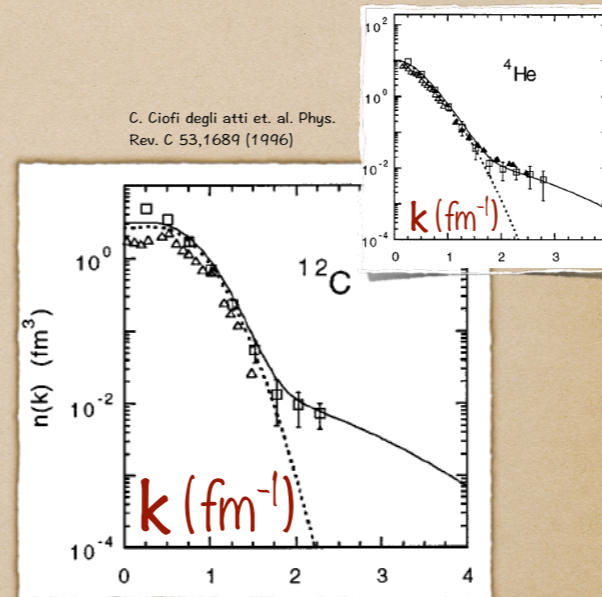
Motivation



Nucleon momentum distributions

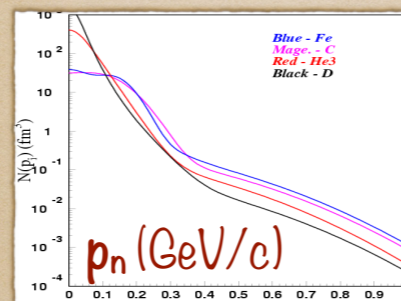
- ◆ IPM do not produce enough high-momentum nucleons.
- ◆ Including correlations shifts strength from low to high momentum.

☞ correlations build high-momentum tail.



What is 2N-SRC

C. Ciofi degli atti et. al. Phys. Rev. C 53,1689 (1996)



- ◆ Large relative & Small c.m. momentum (w.r.t Fermi).
- ◆ High momentum part has the same shape for all nuclei (Scaling)

$$n_A(k) = a_2(A, Z) \cdot n_2(k), \quad \text{for } k > k_F$$

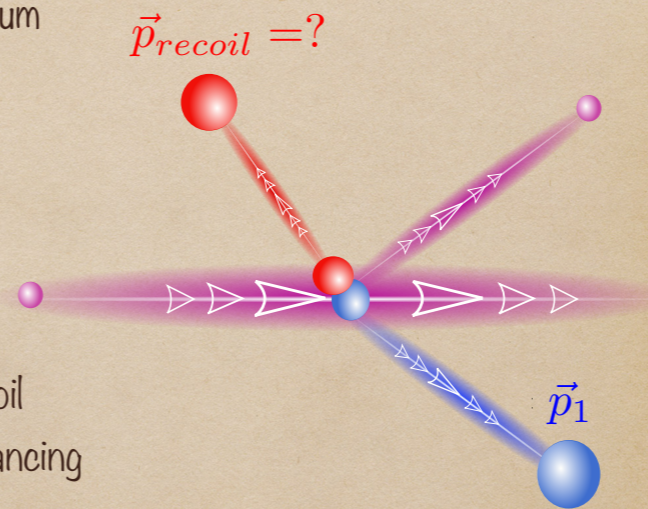
$$|\vec{k}_1 + \vec{k}_2| < k_F$$

$$|\vec{k}_1|, |\vec{k}_2| > k_F$$

$$\vec{k}_1 \simeq -\vec{k}_2$$

Exclusive 2N-SRC studies

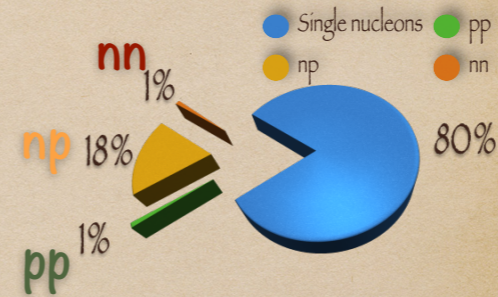
- ◆ Knock out of high-momentum proton.
- ◆ Reconstruct the initial momentum of the knocked proton.
- ◆ Look for emission of a recoil proton with momentum balancing the struck proton.



$$\vec{p}_{miss} = \vec{p}_1 - \vec{q}$$

Previous results

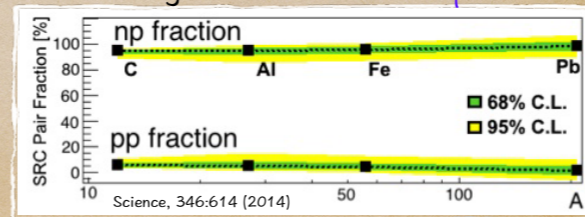
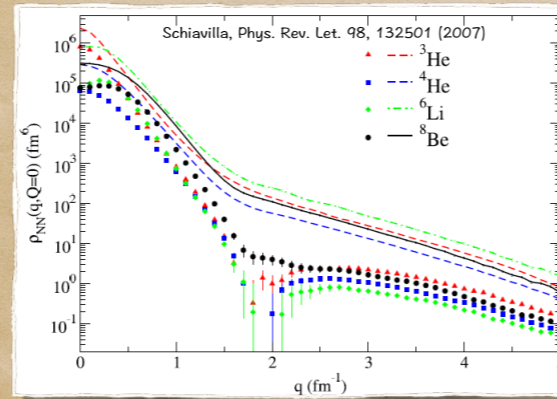
- Exclusive $^{12}\text{C}(p,p'pn)$ and $^{12}\text{C}(e,e'pN)$ measurements probed the high-momentum tail of the nuclear wave-function.



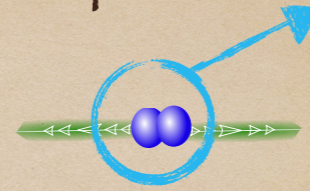
- Results show that for

$$0.3 < |p_{\text{miss}}| < 0.6 \text{ GeV}/c$$

almost all high momentum N are a part SRC.



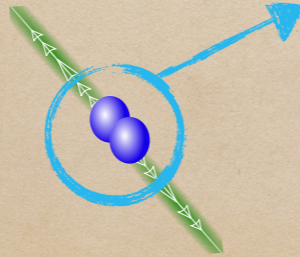
c.m. motion of the 2N-SRC pair - Properties



- ◆ We expect c.m. momentum to be:
 - smaller than the typical momentum of a nucleon in a nucleus,
 - That it will depend on the quantum numbers of the pair,
 - That small c.m. is an important criterion to distinguish 2N- from 3N- SRC.
- ◆ Goal of this work: extract the c.m. momentum of the pp-SRC pair.

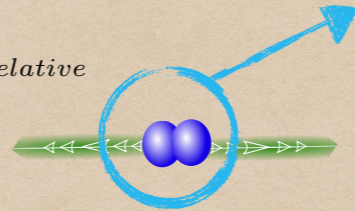
$p_{c.m.}$
 $\sigma_{c.m.}$

The ground state picture
of pp-SRC



The g.s. picture of pp-SRC

$$\vec{p}_{miss} = \frac{\vec{p}_{c.m.}}{2} + \vec{p}_{relative}$$



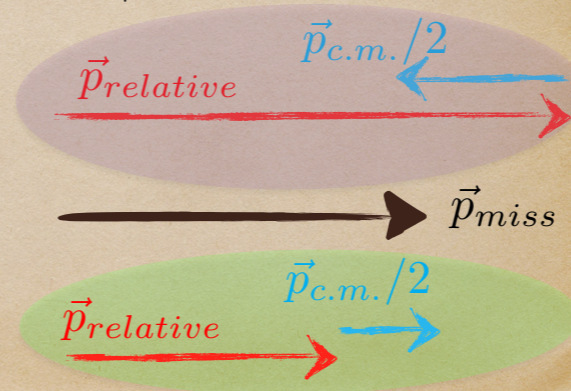
$$\vec{p}_{recoil} = \frac{\vec{p}_{c.m.}}{2} - \vec{p}_{relative}$$

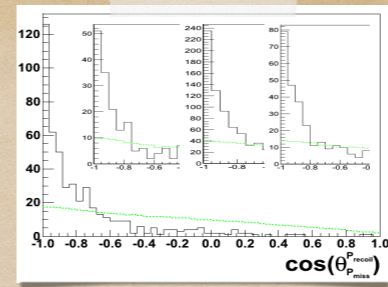
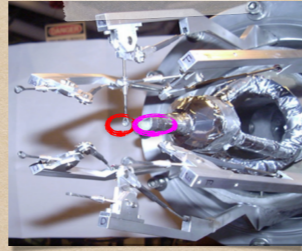
(Due to the **c.m. motion** of the pair)

$$|\vec{p}_{miss}| \neq |\vec{p}_{recoil}|$$

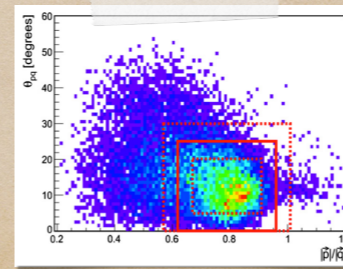
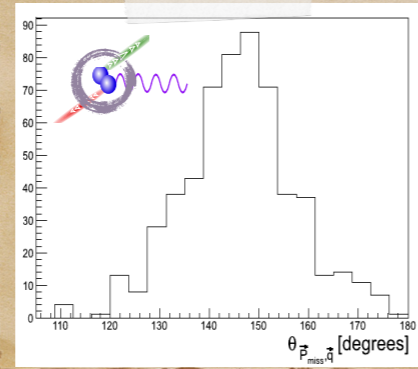
More likely to find a high p_{miss} nucleon with

- $p_{relative} < |p_{miss}|$.
- $p_{c.m.}$ aligned in p_{miss} direction.





EG2 Analysis of pp-SRC

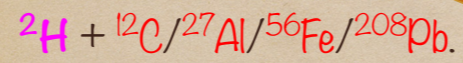


EG2 experiment

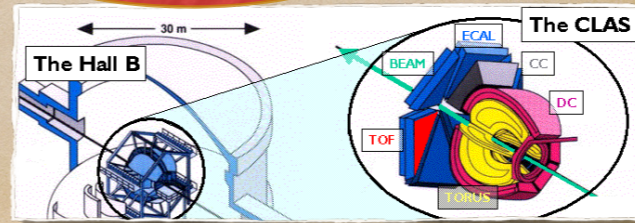
♦ 2004 at Hall-B, JLAB.

♦ 5 GeV e-beam.

♦ Target - D + solid foils
(simultaneously):



Q: Was the beam energy 5.009 GeV at EG2 experiment?

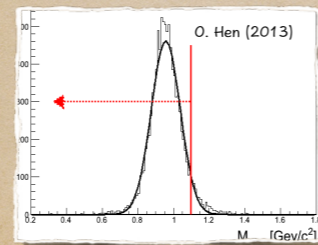


(e,e'p) SRC event selection

◆ Kinematics

- $x_B > 1.2$
- $1000 > |p_{\text{miss}}| > 300 \text{ MeV}/c$

[$Q^2 > 1.5 (\text{GeV}/c)^2$]

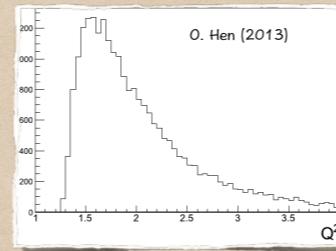
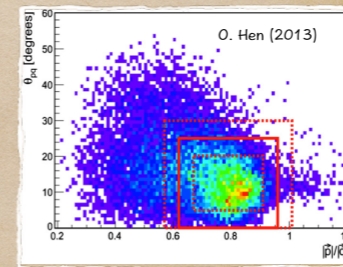


◆ Missing Mass

- $M(\text{miss}) < M(N) + M(\pi)$

◆ Leading proton

- $\theta_{pq} < 25^\circ$
- $0.62 < |p|/|q| < 0.96$

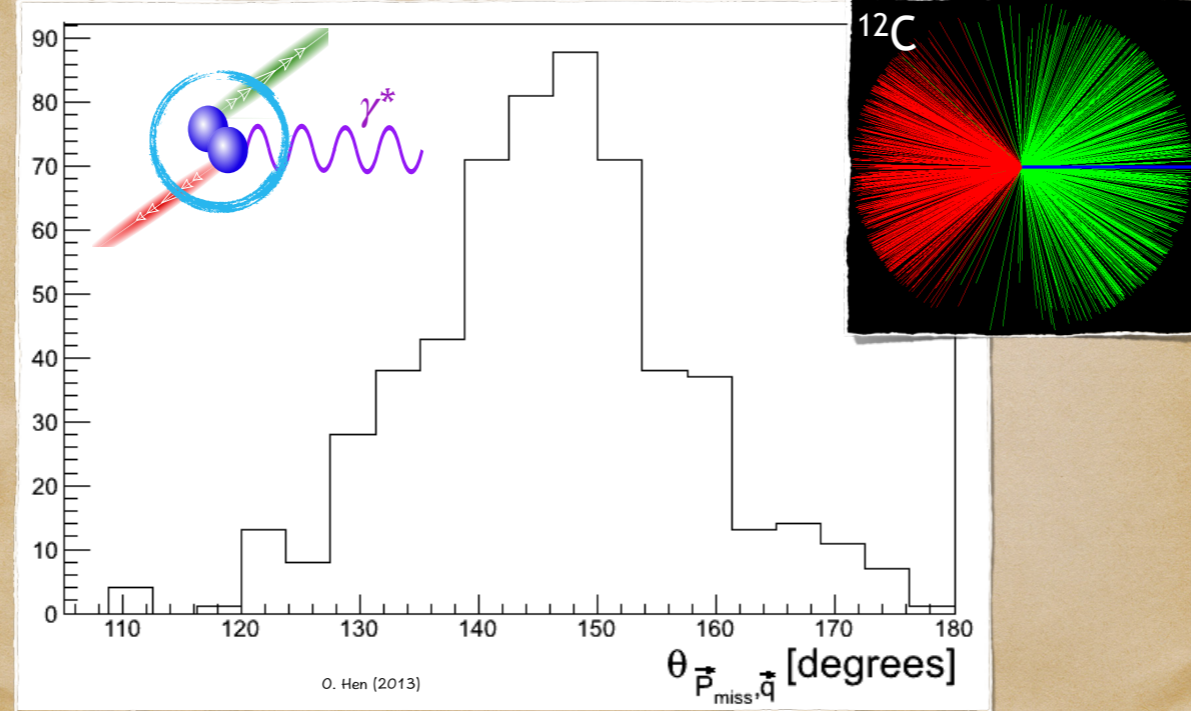


$(e, e'pp)$ event selection

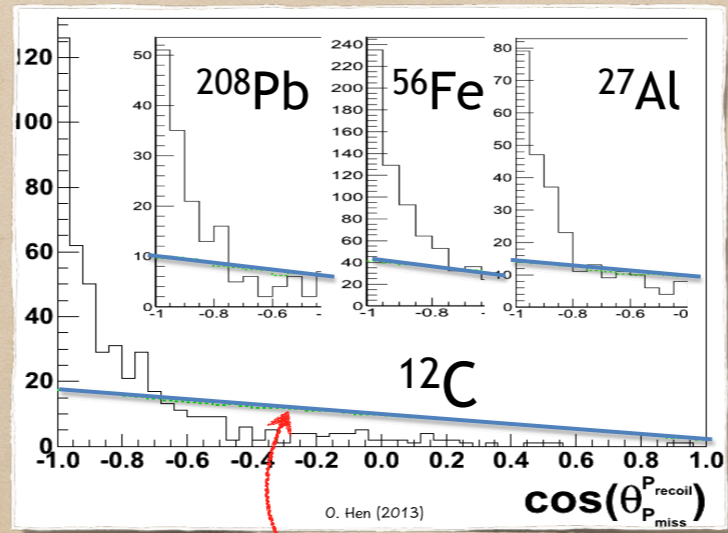
- ◆ $(e, e'p)$ events, in which a recoil proton is detected with momentum $> 350 \text{ MeV}/c$



(e,e'pp) kinematics

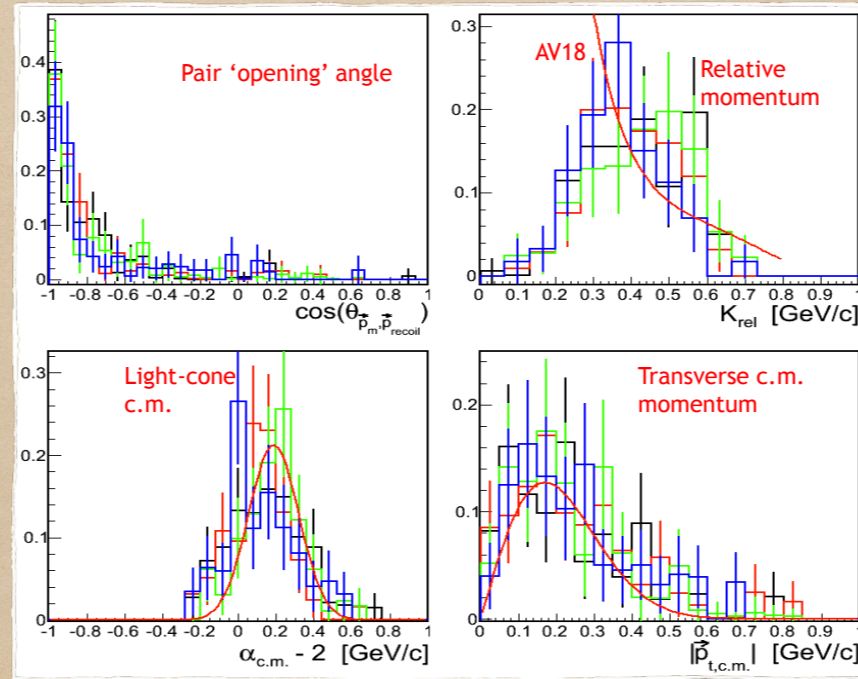


Opening angle



Mixed Events "phase-space"

LC analysis - pp-pair motion



^{12}C

^{27}Al

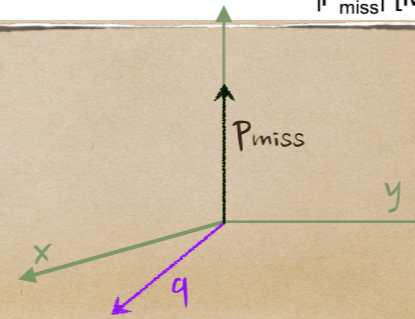
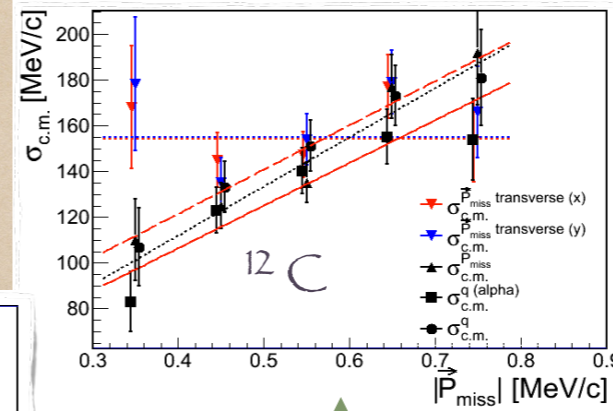
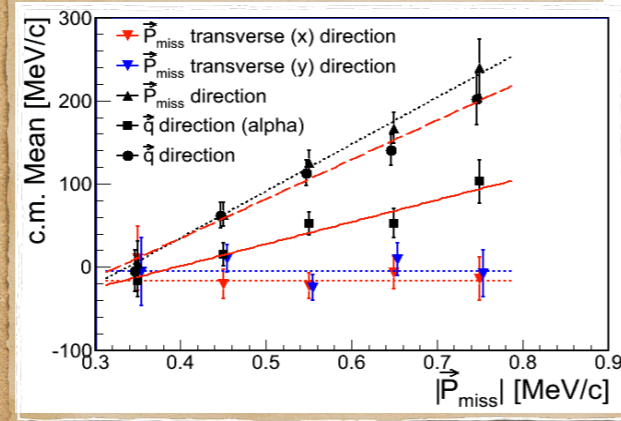
^{56}Fe

^{208}Pb

NOT CORRECTED FOR ACCEPTANCE YET

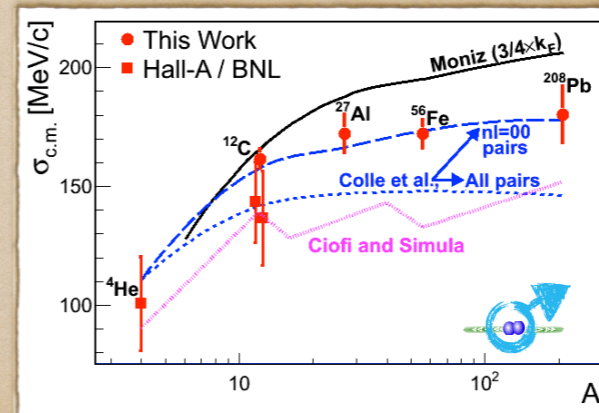
EG2 Analysis results

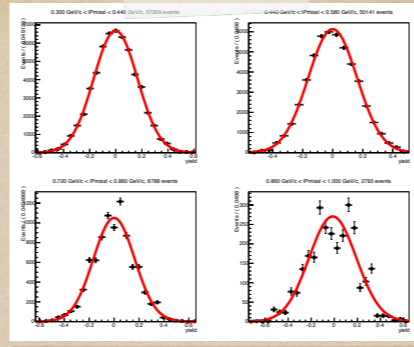
- width of $|p_{c.m.}|$.
- shift along p_{miss} / q direction.



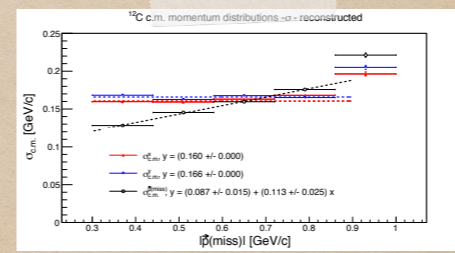
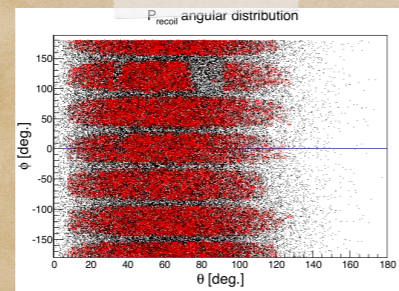
Conclusions from the results

- ◆ The **c.m. motion** is smaller than the momentum of a **typical nucleon** in the nucleus .
- ◆ The **c.m. motion** corresponds with the assumption that the pair is from the same shell with relative **quantum numbers** $n=0$ and $l=0$.





Acceptance correction



Aiming for pair momentum dist.

- ◆ To get the momentum distribution we need to correct for **CLAS** phase-space and cuts biasing 🤔

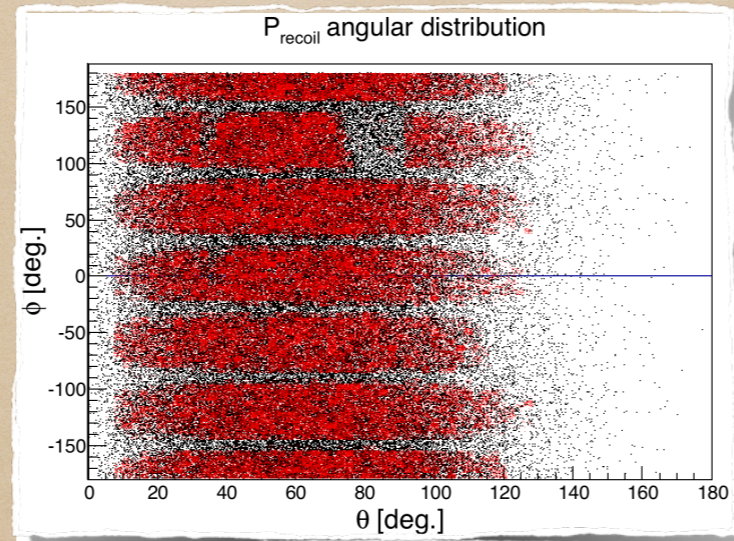
- ◆ Strategy:

- Take SRC $(e,e'p)$ data.
- Move to q -frame and generate c.m. motion.
- Generate a **recoil** proton according to this c.m.
- Run **GSIM** with the $(e,e'pp)$ events.

Q: Do We need to perform Coulomb correction post GSIM?

Data

Generated recoil proton falls mostly in the fiducial region due the back-to-back correlation



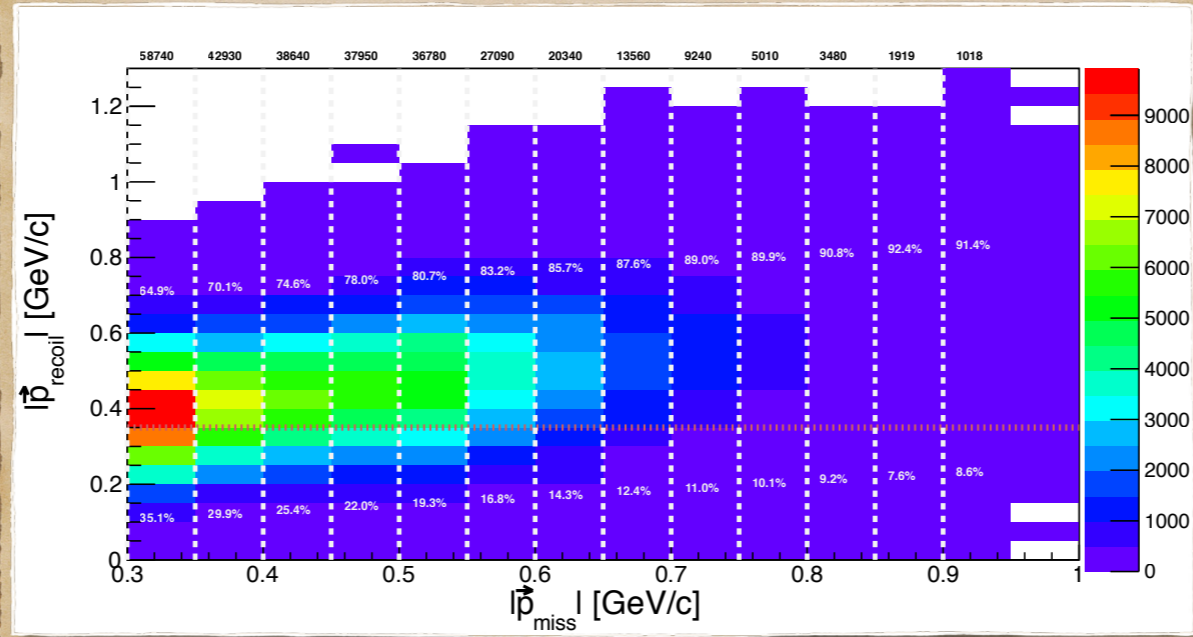
● Generated

● Accepted

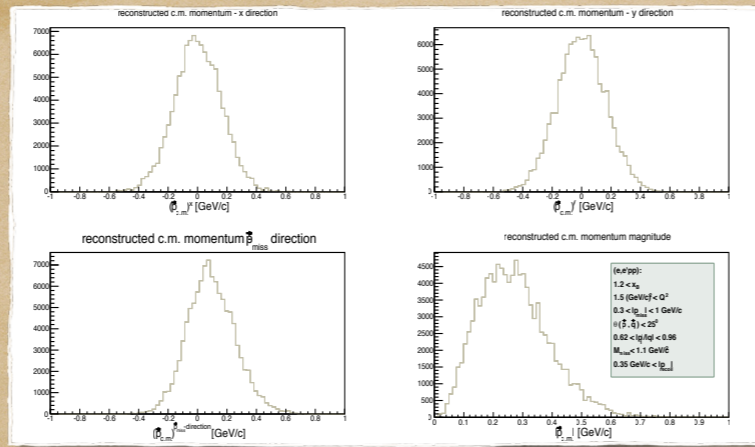
SRC($e, e'p$) already does selection for the recoil:

p_{lead} is accepted - and so p_{recoil} is accepted

$p_{\text{miss}} - p_{\text{recoil}}$ relation in the EG

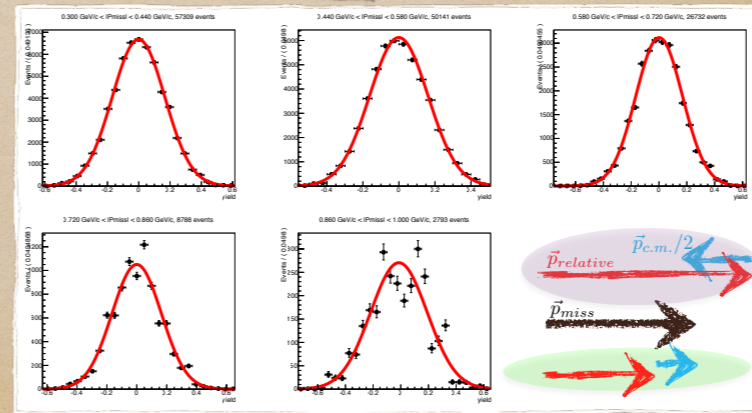


The effect of $p_{\text{recoil}} > 0.35 \text{ GeV}/c$ cut will have more impact at the low p_{miss}

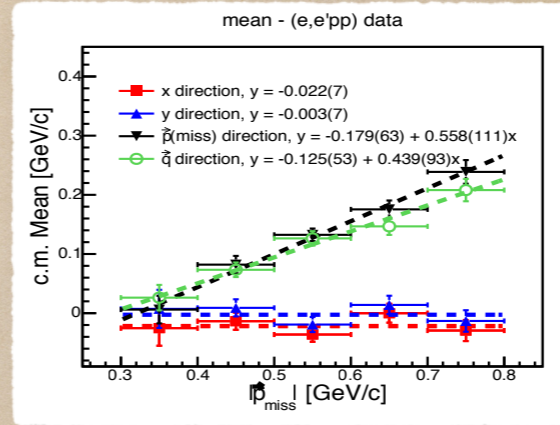
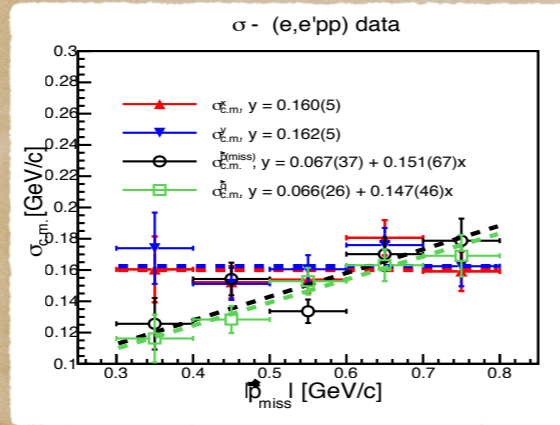


Match pp-SRC
kinematical cuts in
simulated data.

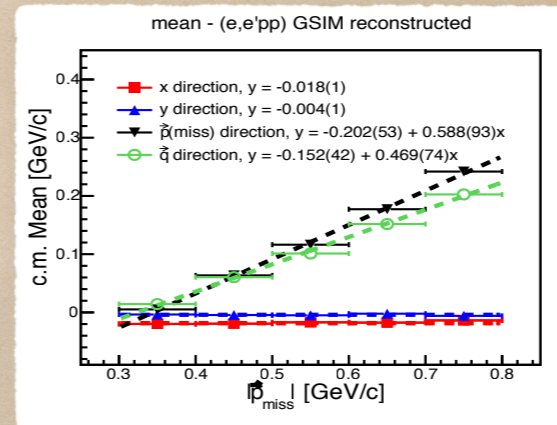
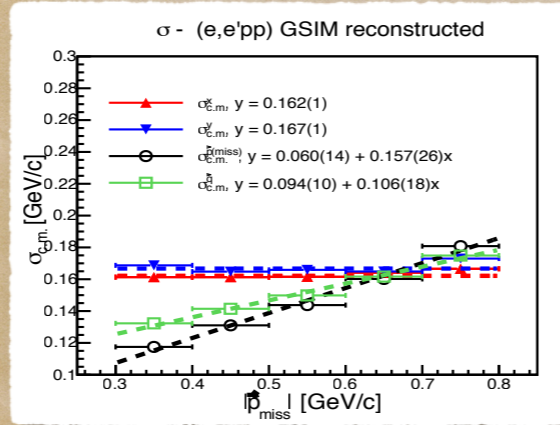
Divide the data into
bins in $|\vec{p}_{miss}|$



(e,e'pp) data in bins of $|p_{\text{miss}}|$

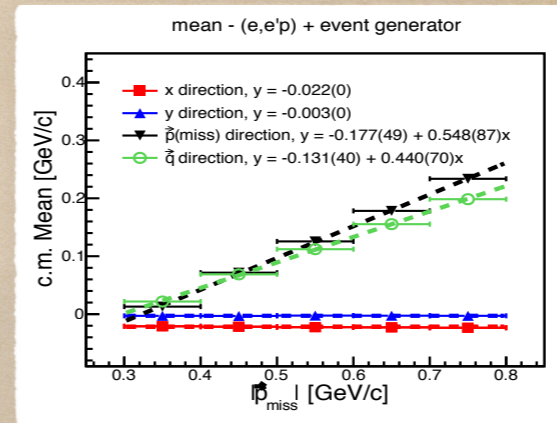
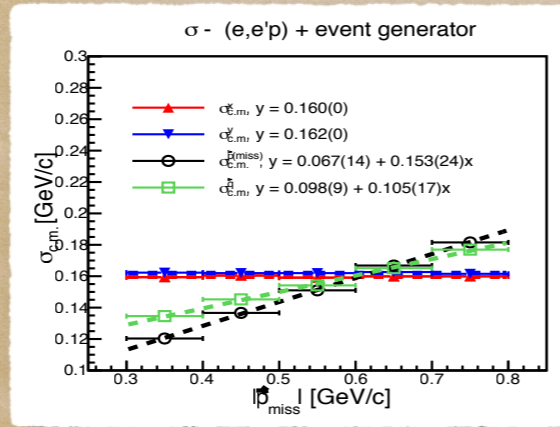


GSIM (e,e'pp) reconstructed vs. $|p_{\text{miss}}|$



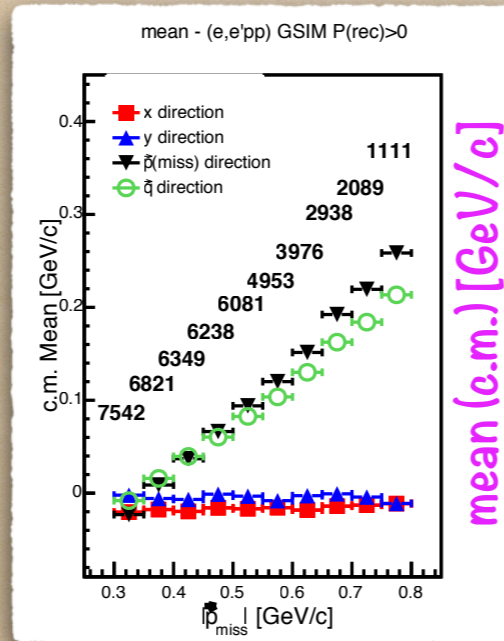
GSIMulation I do is reasonable

GSIM (e,e'pp) generated vs. $|p_{\text{miss}}|$

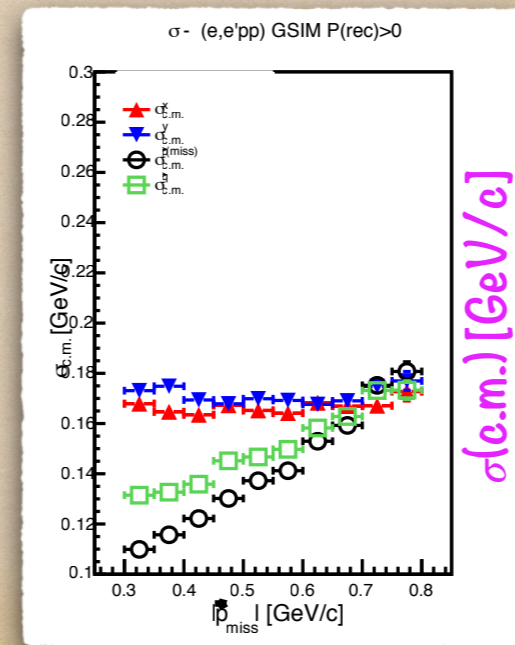


Acceptance has little effect

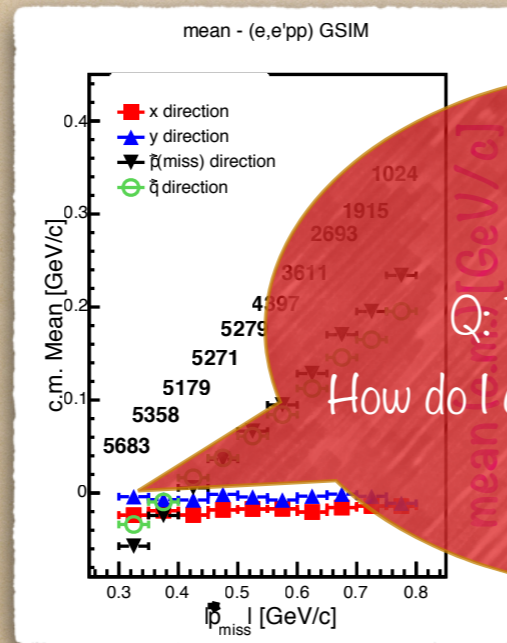
However, there is acceptance effect



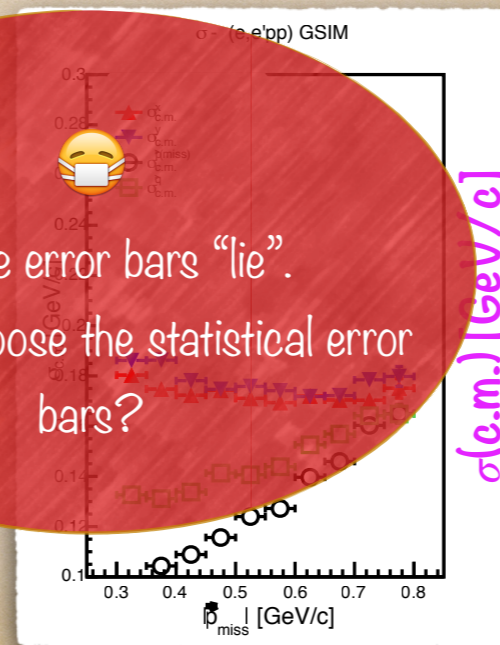
Without $p_{\text{recoil}} > 0.35$ GeV/c cut



However, there is acceptance effect



With $p_{\text{recoil}} > 0.35 \text{ GeV}/c$ cut



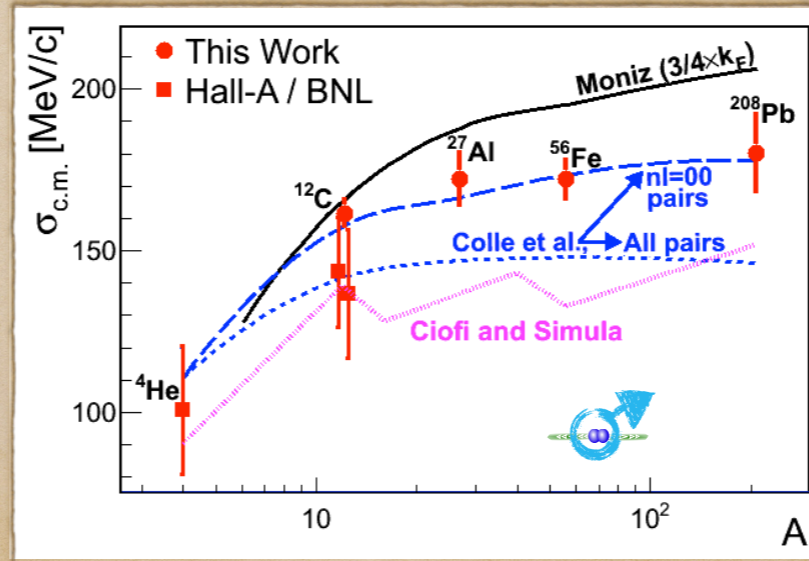
Q: The error bars "lie".
How do I choose the statistical error bars?

mean [GeV/c]

$\sigma_{\text{c.m.}}$ [GeV/c]

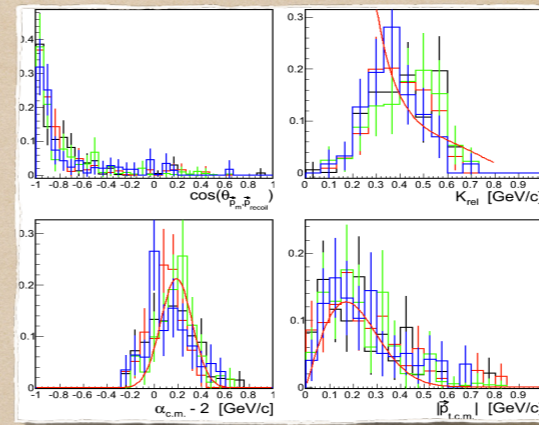
Generated vs. GSI reconstructed

We now need to get back to our results and apply the acceptance correction, but conclusions will be the same since the correction is small.



Next steps

- ◆ pp-SRC pair distributions:
- ◆ events Mott weighting.
- ◆ Flux factor corrections.



- ◆ Study the ratio of $(e,e'pp)/(e,e'p)$ as a function of p_{miss} is SRC kinematics (GSIMulation).

Thank you for your time...

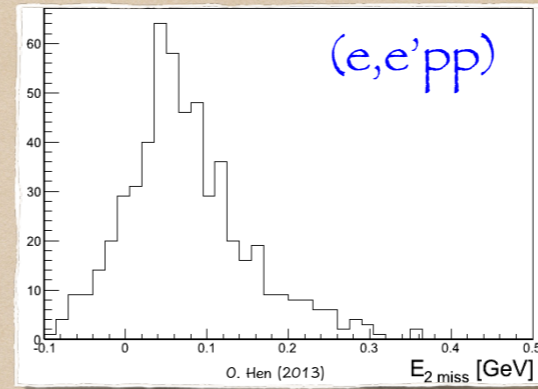
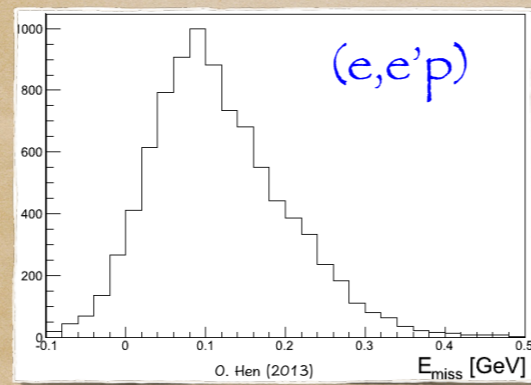


*Comments/Suggestions/Questions:
cohen.erez7@gmail.com*

Extra-slides

Excitation energies

$$E_{miss} = \omega - T_p - T_{A-1}$$

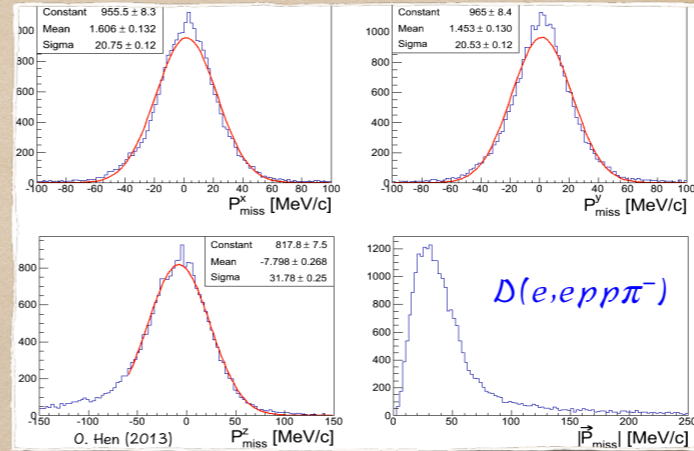


$$E_{2-miss} = \omega - T_{lead} - T_{recoil} - T_{A-2}$$

CLAS resolution contribution to width of c.m.

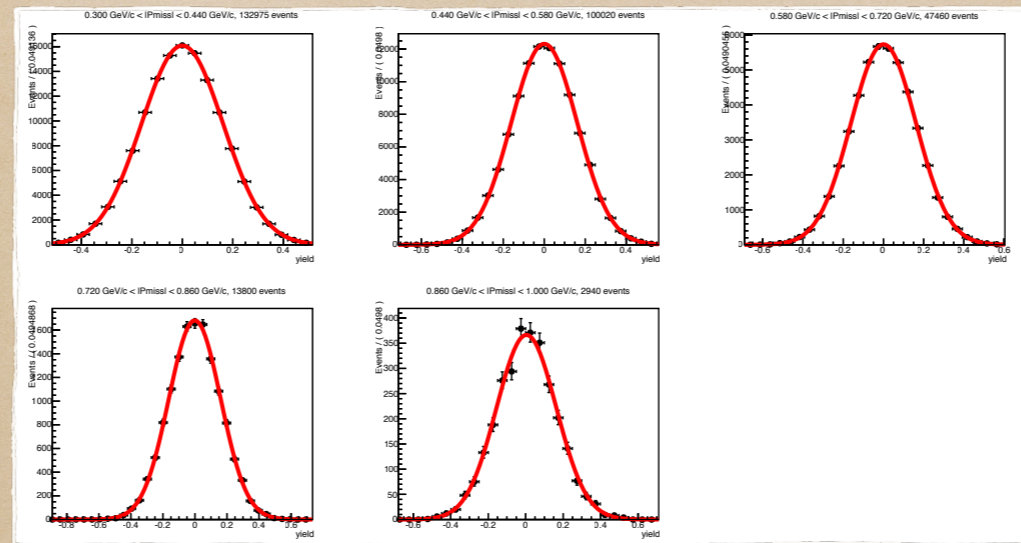
$$\sigma_{c.m.} = \sqrt{\sigma_{exp}^2 - \sigma_{res}^2}$$

$$\sigma_{res} \sim 20 \text{ MeV}/c$$

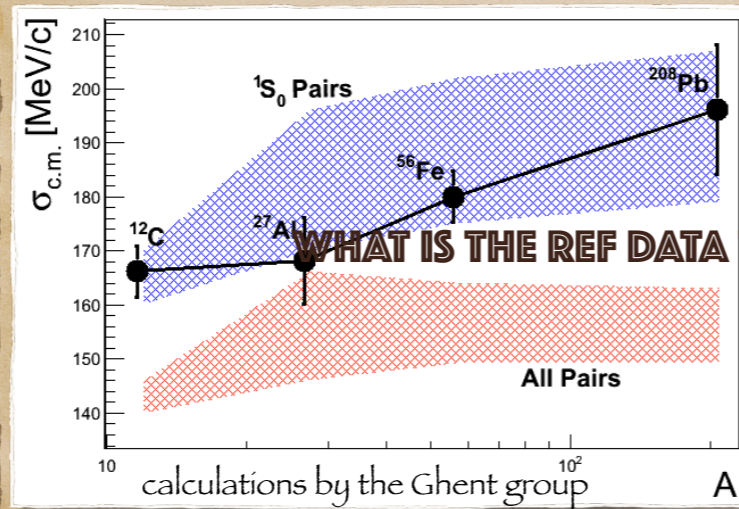


Correction $\sim 3 \text{ MeV}/c$ for $\sigma_{exp} \sim 160 \text{ MeV}/c$

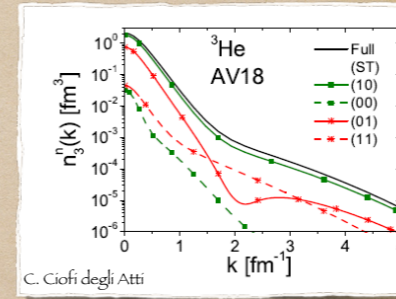
Using RooFit for un-binned fitting



C.M. motion width



WHAT IS THE REF DATA? PRELIMINARY BY OR?



nucleus	σ_x [MeV/c]	σ_y [MeV/c]
^{12}C	169 ± 7	164 ± 6
^{27}Al	162 ± 10	180 ± 13
^{56}Fe	179 ± 6	182 ± 7
^{208}Pb	208 ± 18	186 ± 16

The spin-Isospin contribution to the momentum distribution

Light cone

Light-cone fraction study

$$\alpha = A \frac{E_p - p_z}{m_A}$$

- ◆ The Light-Cone fraction has less sensitivity to FSI.
- ◆ Goes together with the transverse momentum

flux calculated for the moving nucleon

$$\frac{d\sigma}{dE'_e d\Omega'_e d^3p_f d^3p_{rec}} = \frac{j_N}{j_A} A \sum_N \sigma_{eN}(p_f, k_e, k'_e) D^N(\vec{p}_m, E_m, \vec{p}_{rec})$$

Sargsian, Abrahamyan, Strikman and Frankfurt, Phys. Rev. C 71, 044615

electron - off-shell eN scattering

2N-SRC Decay function formalism

$$\frac{d\sigma}{dE'_e d\Omega'_e d^3p_f d^3p_{rec}} = \frac{j_N}{j_A} A \sum_N \sigma_{eN}(p_f, k_e, k'_e, E_m, \vec{p}_{rec})$$



The decay function is a convolution of two density matrices representing the relative and c.m. momentum distribution

$$D = \rho_{rel} \cdot \rho_{c.m.} \frac{\alpha_{rec}}{\alpha_{c.m.}} \times \delta \left(P_{R+} - \frac{m^2 - (p_{rec})_T^2}{m\alpha_{rec}} - \frac{M_{A-2}^2 + (p_{c.m.})_T^2}{m(A - \alpha_{c.m.})} \right)$$



E. Piasezky et al., Phys.Rev.Lett. 97 (2006) 162504

LC component of the residual A-1 nuclear state

Light-cone fraction study

$$\alpha = A \frac{E_p - p_z}{m_A}$$

- Define the equivalents of detected, missing, c.m. and recoil light cone fraction of momenta

$$\alpha_{miss} = \alpha_{initial} = \alpha_{lead} - \alpha_q$$

$$\alpha_{c.m.} = \alpha_{miss} + \alpha_{rec}$$

where $\alpha_q = \frac{\omega - |q|}{m}$

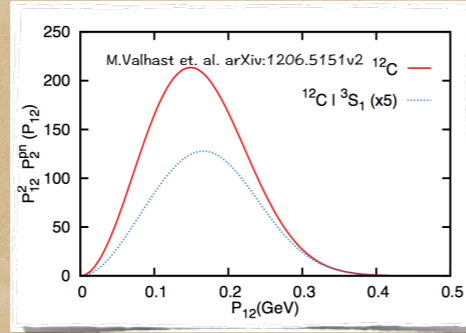
$$(p_{c.m.})_T = (p_{miss})_T + (p_{rec})_T$$

$$(p_{rel})_T = (p_{rec})_T - \frac{\alpha_{rec}}{\alpha_{c.m.}} (p_{c.m.})_T$$

2N-SRC Decay function formalism

$$\frac{d\sigma}{dE_e' d\Omega_e' d^3p_f d^3p_{rec}} = \frac{j_N}{j_A} A \sum_N \sigma_{eN}(p_f, k_{rel}, E_m, \vec{p}_{rec})$$

E. Piasetzky et al., Phys.Rev.Lett. 97 (2006) 162504



$$D = \rho_{c.m.} \times \delta \left(P_{R+} - \frac{m^2 - (p_{rec})_T^2}{m\alpha_{rec}} - \frac{M_{A-2}^2 + (p_{c.m.})_T^2}{m(A - \alpha_{c.m.})} \right)$$

- The 2-body c.m. momentum distribution can be parametrized in terms of Gaussian distribution.

$$\rho_{rel}(\alpha_{rel}, (p_{rel})_T) = a_2(A/d) \frac{\psi_D^2(k_{rel})}{2 - \alpha_{rel}} \sqrt{m^2 + k_{rel}^2}$$

$$\rho_{c.m.}(\alpha_{c.m.}, (p_{c.m.})_T) = \frac{2m}{(2\pi\sigma_{c.m.}^2)} e^{-\frac{m^2(2 - \alpha_{c.m.})^2 + (p_{c.m.})_T^2}{2\sigma_{c.m.}^2}}$$