

# Evolutionary algorithms to improve plasma confinement

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# Outline

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Equilibrium

Crossover GA

Grid Computing

- Overview

- Implementation

Mutation-based GA

- Overview

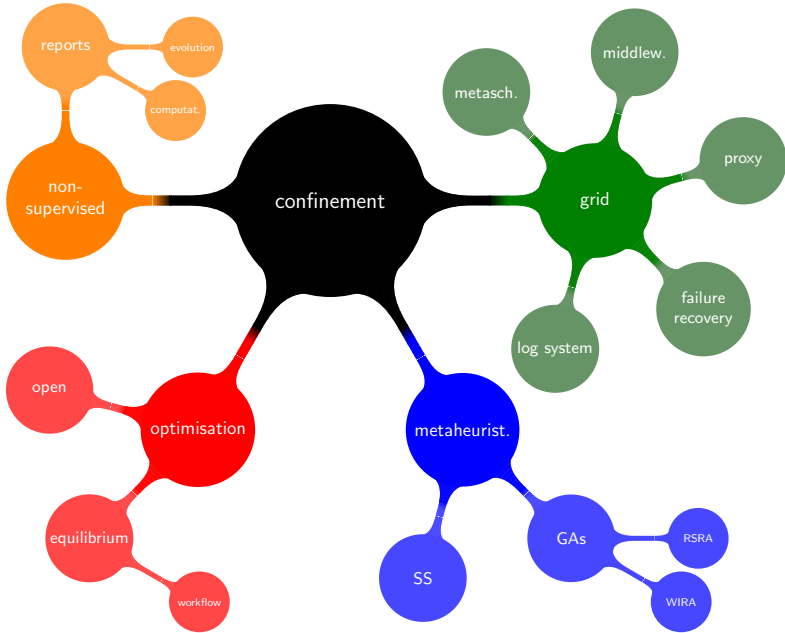
- Replacement

Scatter Search

Results

- Computational results

- Evaluation results

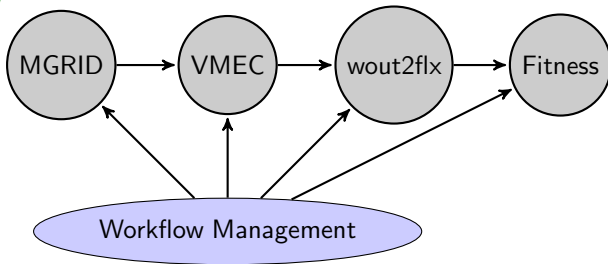


# Measuring the equilibrium

## Function

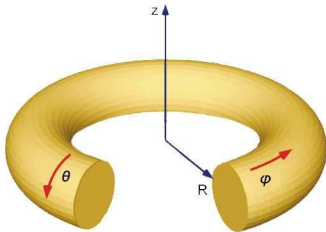
$$F_{target\_function} = \sum_{i=1}^N \left\langle \left| \frac{\vec{B} \times \vec{\nabla} |B|}{B^3} \right| \right\rangle_i$$

## Workflow



# VMEC

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What VMEC solves

$$R(\rho, \theta, \phi) = \sum_{mn} R_{mn}(\rho) \cos(m\theta - n\phi)$$

$$Z(\rho, \theta, \phi) = \sum_{mn} Z_{mn}(\rho) \sin(m\theta - n\phi)$$

$$B(\rho, \theta, \phi) = \sum_{mn} B_{mn}(\rho) \cos(m\theta - n\phi)$$

# Measuring the equilibrium

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## Problems of the workflow

- Required time for optimal configurations: 45 min.
- Huge solution space.

## Our idea

- Use GAs to look for improved configurations.
- Use grid computing.
- Highly customizable system.

## Some problems still remain

- Time required to find optimal configurations is still high.
- The number of iterations we can evaluate will be low.

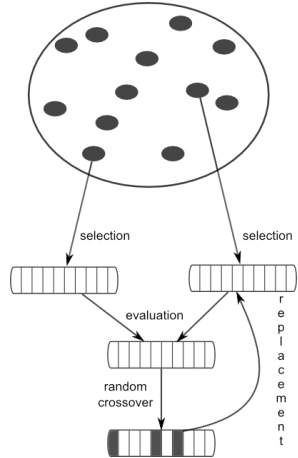
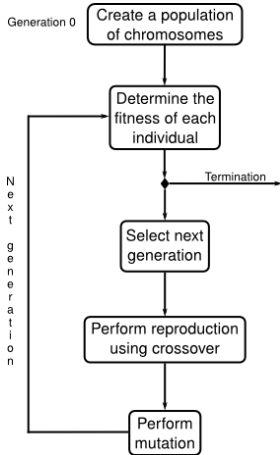
# Crossover GA

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## Considerations

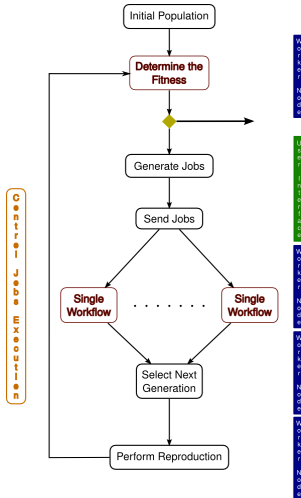
- Long time for a single function.
- Each individual within a generation can be calculated independent from the others.
- Parallel and distributed processing appears to be the best option.
- Master node managing the different slaves.
- Fully configurable via XML files.
  - Number of individuals.
  - Chromosomes.
  - Stop conditions.
  - Selection method.
  - Replacement method.

# Crossover GA





# Overview of the GA using the Grid



# Grid implementation

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## Features

- Set of Python scripts interacting with grid infrastructure.
- Backup system.
- Error recovering.
- Proxy management.
- Log system.
- Highly configurable system through XML files.

# Jog management

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## Solution to job failures

- Our system manages all submitted jobs by querying the metascheduler.
- Due to failures in the infrastructure, jobs can fail.
- Some configurations can be wrong.
- Failed jobs are resubmitted one time.
- Jobs taking extra-time are killed and resubmitted once.

# Mutation-based GA

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## Features

- Floating point representation.
- Tournament selection.
- Use the sample standard deviation for mutation.
  - Each selected chromosome is added or subtracted with a value in the range  $(0 - \sigma]$ .
- Random number of chromosomes to mutate ( $[1 - \textit{number\_of\_chromosomes}]$ ).
- Based on experience:
  - Some binary chromosomes.
  - These chromosomes are randomly selected and crossed.

# Replacement

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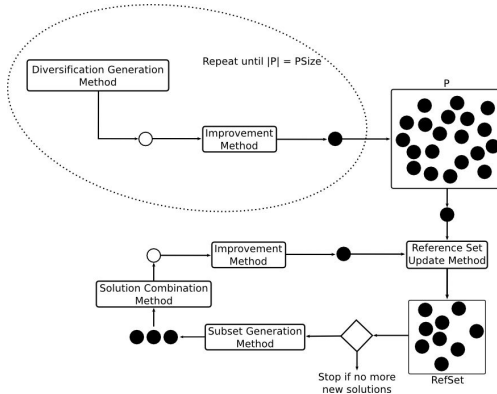
## RSRA

- This version of the algorithm replaces one element within the population randomly.
- High dispersion.
- Poor evolution.

## WIRA

- This version uses a sorted list of the individuals.
- The worst individual previously evaluated is selected for replacement.

# Scatter Search



## Crossover GA after 50 generations

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Parameter	Value
Number of Fitness Evaluations	48,158
Aggregated Execution Time	74,551:15:34
Average Execution Time	01:32:53
Execution Time	1,834:57:31

## Mutation-based GA after 50 generations

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Parameter	RSRA	WIRA
Number of evaluations	5,245	5,845
Cumulative CPU time	7,823:09:52	8,102:31:44
Average execution time	01:29:49	01:23:17
Speedup	12.80	16.56
Efficiency	0.20	0.26

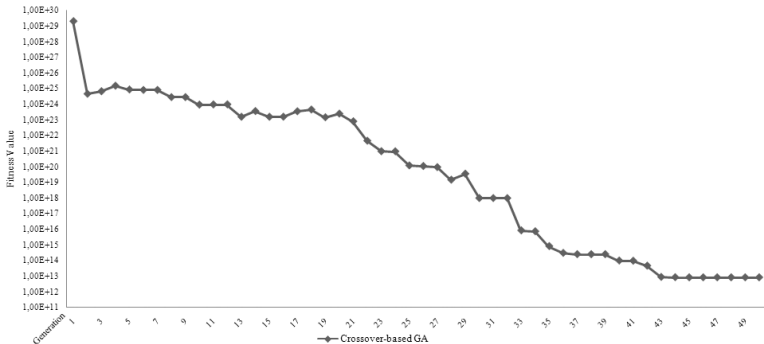


## Scatter Search Results

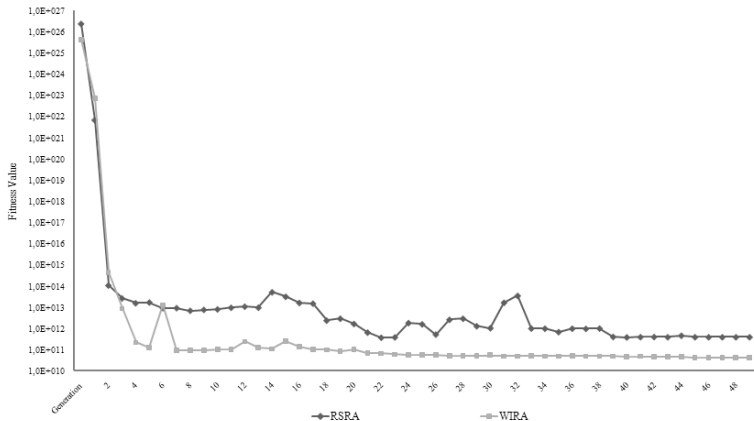
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Parameter	Test1	Test2	Test3	Test4
Chromosomes	100	100	100	100
Population size	100	100	100	50
RefSet size	10	10	10	5
Local search	Deactivated	Deactivated	Activated	Activated
Iterations	2	50	2	50
Evaluations	574	12,361	11,427	6,781
Execution time	36:10:19	535:36:25	495:12:51	310:12:53
Cumulative CPU time	783:07:21	9,095:41:07	8,727:29:07	5,321:03:57

# Evolution of crossover GA



# Evolution of mutation-based GA



## Scatter Search best results

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Test	Best Value
2 Iterations - Local Search Deactivated	1.76781E+05
50 Iterations - Local Search Deactivated	7.056280E+03
2 Iterations - Local Search Activated	1.47256E+04
50 Iterations - Local Search Activated - Smaller Population	1.02314E+04

## Summary

- Workflow to optimise nuclear fusion devices.
- Crossover GA.
- Two implementations of a mutation-based GA.
- Grid-oriented Scatter Search.
- Non-supervised distributed GAs and EA using grid computing:
  - Master-slave model.
  - Failure recovery.
  - Job management.

## Open problems

- We have to wait for the entire generation to be evaluated to get a new one ⇒ asynchronous methods.
- Add more optimisation criteria.

Thank you for your attention!!

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