

# Hadron production in high energy nuclear collisions and the QCD phase diagram

Outline:

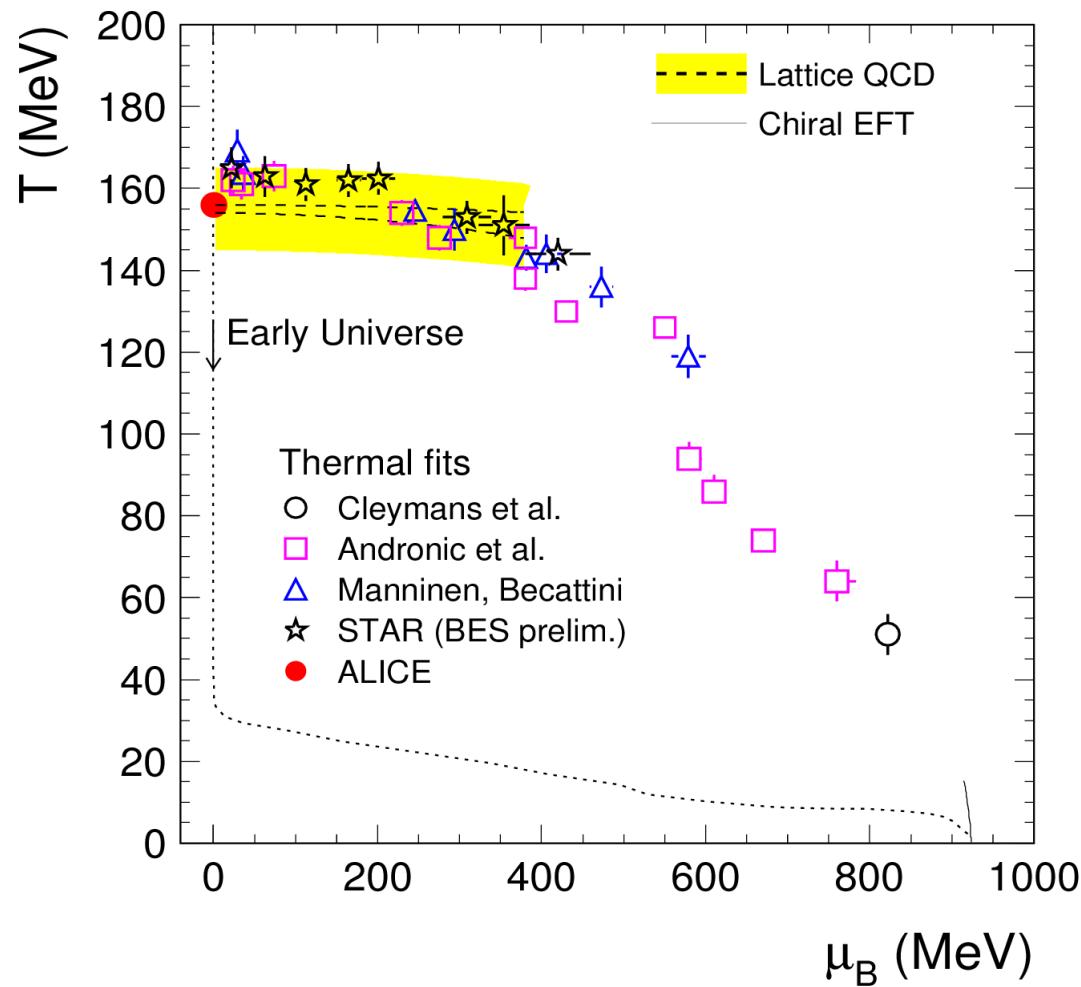
- the QCD phase diagram in lattice QCD
- hadron production at the LHC
- production of nuclei, anti-nuclei and exotica
- hadron yields and statistical model from AGS to SPS to RHIC
- connection to phase boundary
- direct connection of LHC data to lattice QCD on 2nd order critical fluctuations

work done in collaboration with  
A. Andronic, P. Braun-Munzinger, und K. Redlich

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Johanna Stachel, Physikalisches Institut, U. Heidelberg  
CCNU Wuhan, July 28, 2015

# Phase diagram of strongly interacting matter - today



# Theoretical knowledge of the phase diagram

theory of strong interaction: QCD

Lagrangian density:  $\mathcal{L}_{\text{QCD}} = \frac{1}{2g^2} \text{Tr} (F_{\mu\nu}(x)^2) + \bar{q}(x) (i\gamma_\mu D_\mu + m) q(x)$

in limit where renormalized running coupling constant  $\alpha(q^2) = g^2(q^2)/4\pi$  small, QCD perturbation theory gives precise results (cf. QED)

- in hadronic matter and in QGP at T a few times  $T_c$ , coupling not small!

already in 1974 proposed by Wilson: put field theory (e.g. QCD) on 4 d lattice in Euclidian space-time

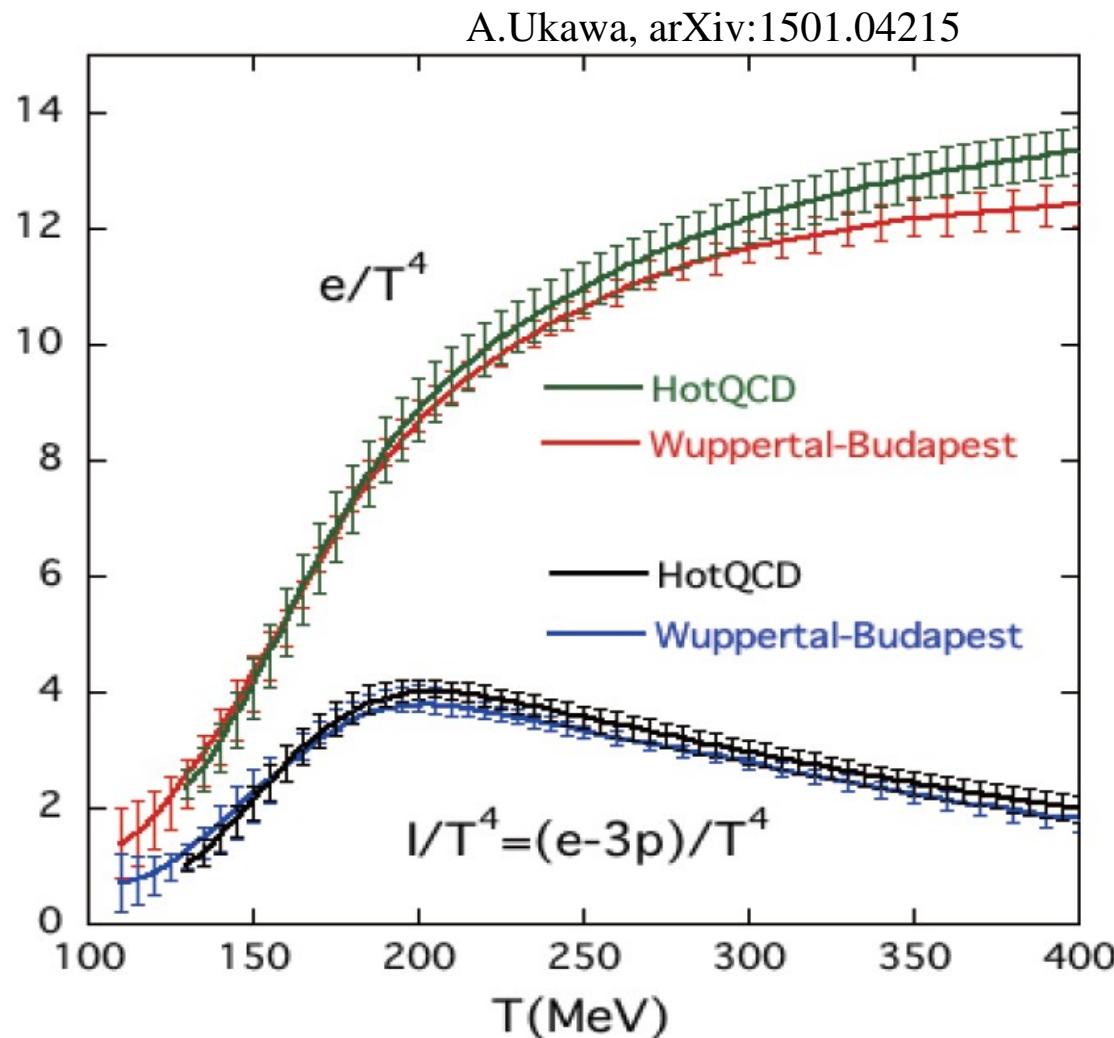
from 1979 possibility to numerically calculate observables on a computer  
“birth of lattice QCD”

in the past 35 years tremendous development due to availability of parallel super computers (to good part also driven by lQCD community) and better algorithms

- now lattice QCD is a mature technique with increasingly reliable results

# Equation of state of hot QCD matter in lattice QCD

computation of QCD EoS one of the major goals in lQCD community since 1980



consolidated results on EoS from different groups, extrapolated to continuum and chiral limit

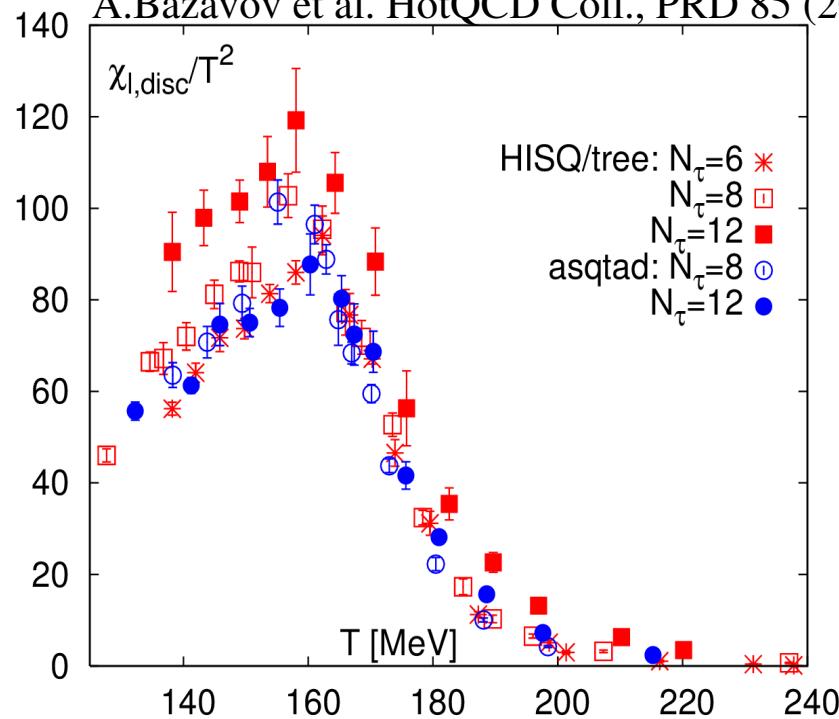
rapid rise of energy density (normalized to  $T^4$  rise for relativistic gas)  
- signals rapid increase in degrees of freedom due to transition from hadrons to quarks and gluons  
- lQCD points to continuous cross over transition

# Measure for chiral symmetry restoration in lQCD

order parameter: chiral condensate, its susceptibility peaks at  $T_c$

S.Borsayi et al. Wuppertal-Budapest Coll., JHEP 1009 (2010) 073

A.Bazavov et al. HotQCD Coll., PRD 85 (2012) 054503



$$\langle \bar{\Psi} \Psi \rangle = \frac{T}{V} \frac{\partial \ln Z}{\partial m}$$

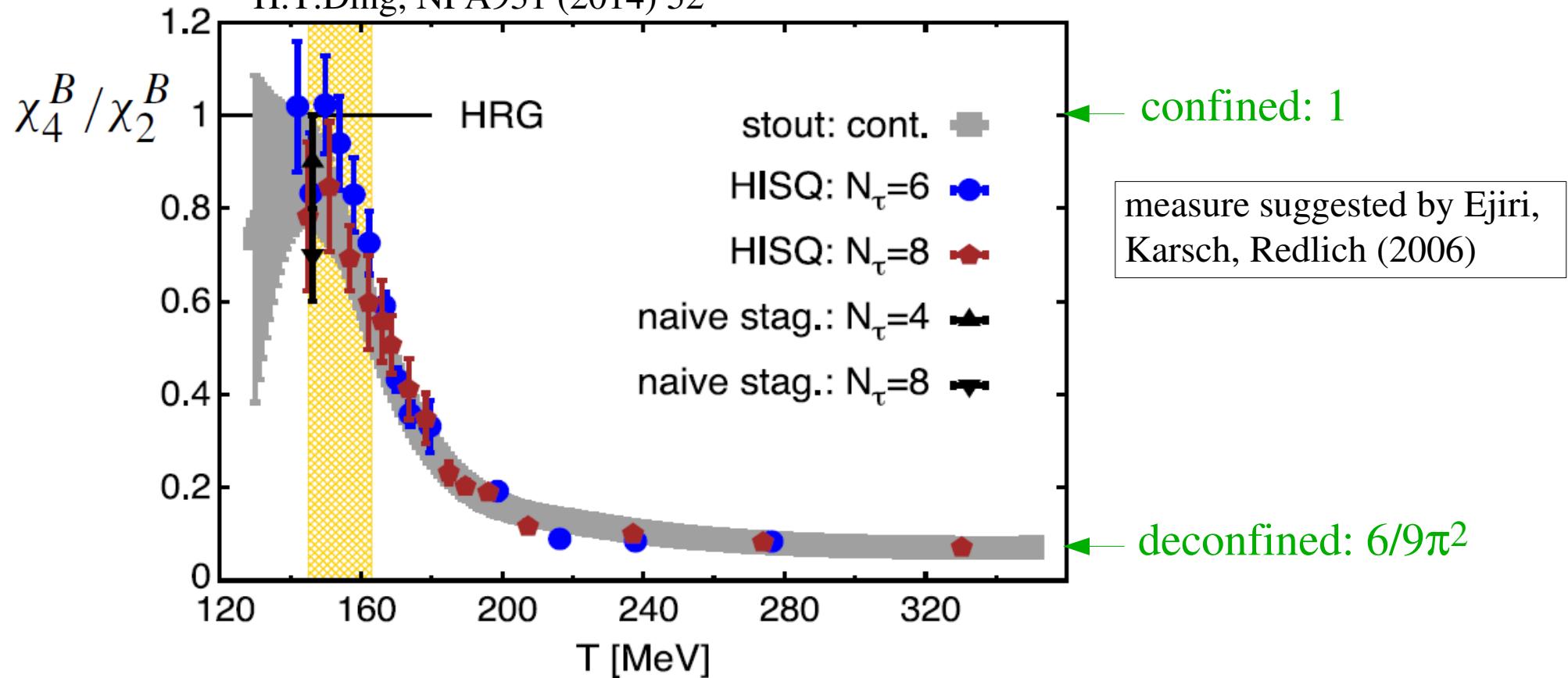
$$\chi_{\bar{\Psi} \Psi} = \frac{T}{V} \frac{\partial^2 \ln Z}{\partial m^2}$$

comparing different measures and different fermion actions, consensus:  
 $T_c = 150 - 160$  MeV for chiral restoration

# Measure of deconfinement in lQCD

$$\chi_4^B / \chi_2^B \propto \text{baryon number}^2$$

H.T.Ding, NPA931 (2014) 52



rapid drop suggests: chiral cross over and deconfinement appear in the same narrow temperature range

# Experiment

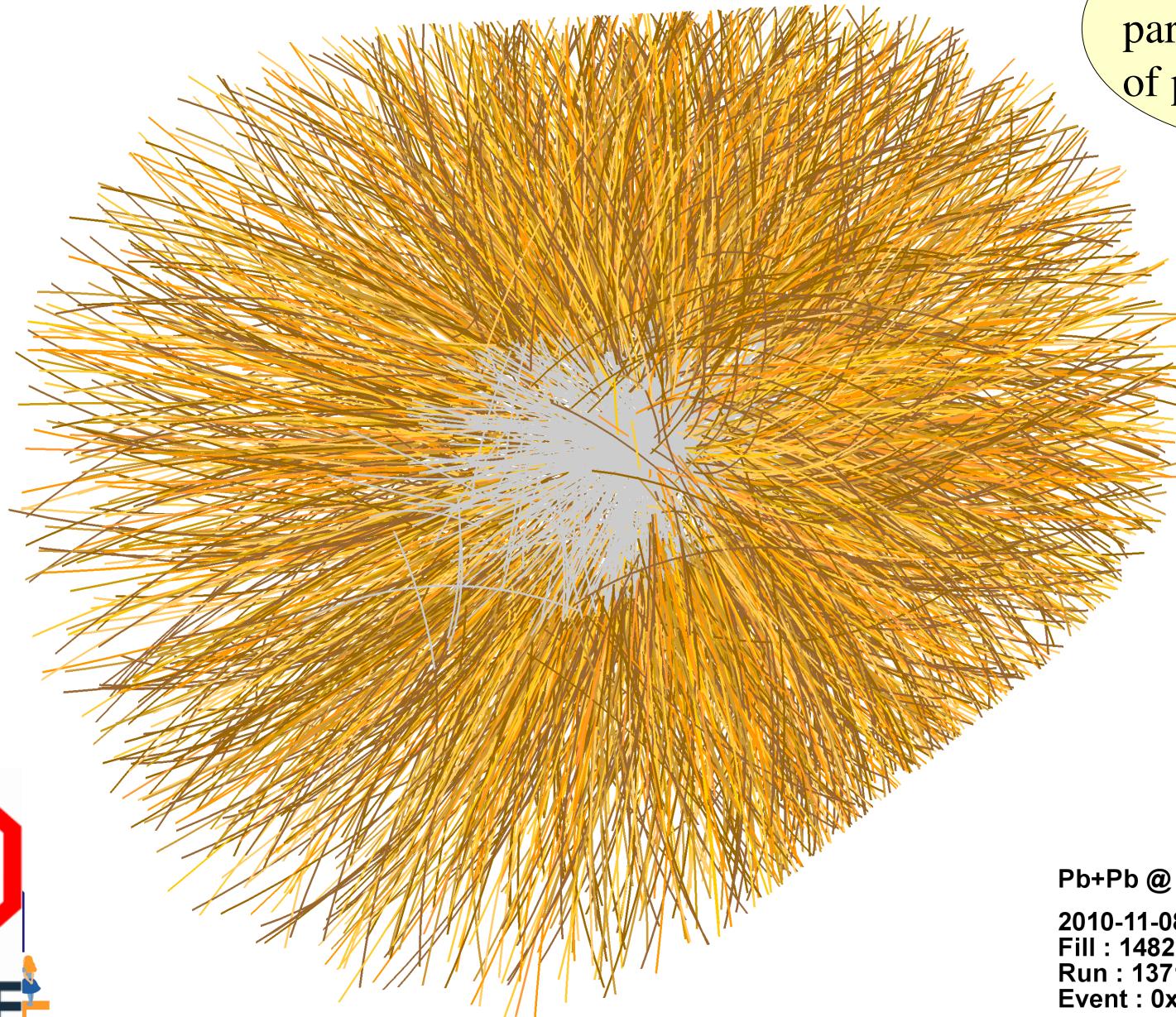
QGP and phase diagram studied in high energy collisions of nuclei since 1987 at AGS/SPS, since 2000 at RHIC, since 2010 at the LHC at  $\sqrt{s_{NN}} = 2.76 \text{ TeV}$



# a central PbPb collision at LHC at $\sqrt{s} = 2.76$ A TeV

first collisions with stable beams:

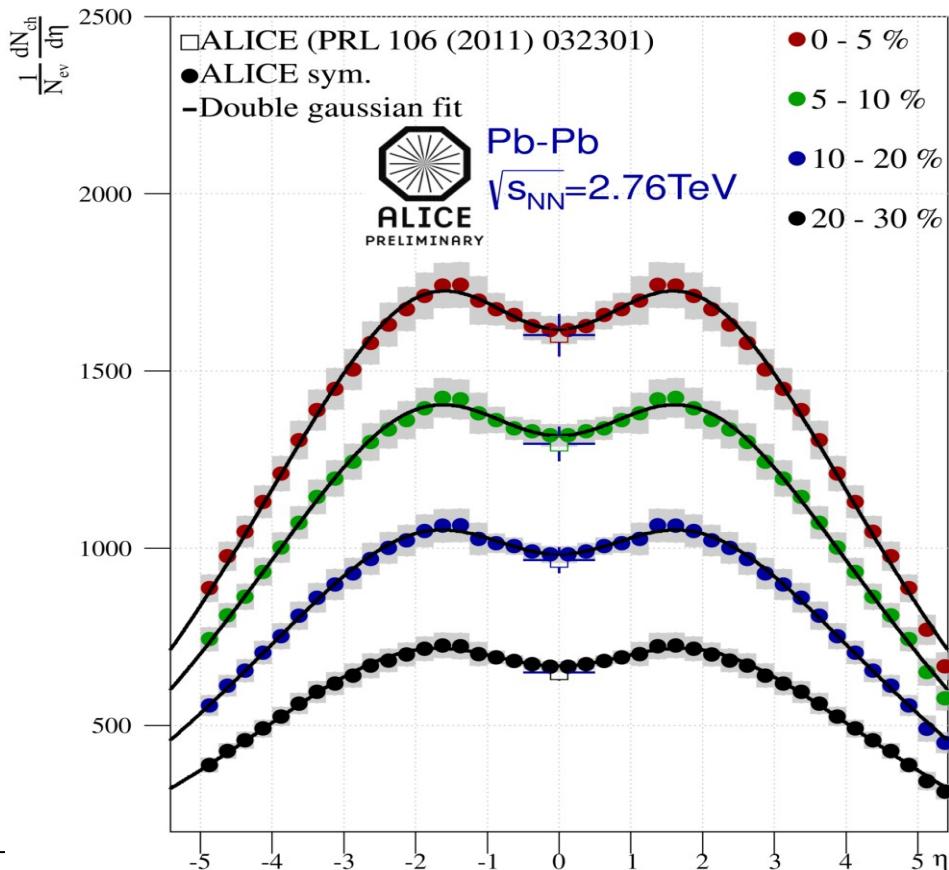
Nov 8 - Dec 6, 2010



Pb+Pb @  $\text{sqrt}(s) = 2.76$  ATeV  
2010-11-08 11:30:46  
Fill : 1482  
Run : 137124  
Event : 0x00000000D3BBE693

# Charged Particle Multiplicity

probes density of gluons initially liberated from the colliding nucleons  
expect order of 10 000 (question of shadowing and of gluon saturation)  
in a statistical ensemble measure of initial entropy density  
each gluon (boson) contributes 3.6 units to the entropy  
preserved for isentropic expansion



central PbPb at 2.76 TeV

$$dN_{\text{ch}} / d\eta = 1600$$

using arguments by Bjorken  
initial energy density

$$\varepsilon_0 = 146 \text{ GeV/fm}^3$$

$$T \approx 0.68 \text{ GeV} \approx 4 T_c \approx 10^{13} \text{ K}$$

$$\text{pressure } P \approx 49 \text{ GeV/fm}^3 = 7.9 \cdot 10^{36} \text{ Pa}$$

$$\text{entropy density } \approx 290/\text{fm}^3$$

$$\text{total entropy of fireball: } 36\,000$$



# the Hadro-Chemical Composition of the Fireball

what are the 20 000 hadrons observed in final state at LHC?

## QGP and hadron yields

QCD implies duality between quarks/gluons and hadrons

- hadron gas: equilibrated state of all known hadrons
- QGP: equilibrated state of quarks and gluons

at pseudocritical temperature  $T_c$ , QGP converts to hadrons

existence of QGP in central nuclear collisions implies that:

- hadron yields correspond to **equilibrium state** of common temperature  **$T$**
- hadron yields must agree with predictions using the **full QCD partition function** at this temperature  **$T$**

near  $T_c$ , hadron densities very large, can rapidly drive system into equilibrium between hadronic species by multi-particle reactions (critical opalescence)

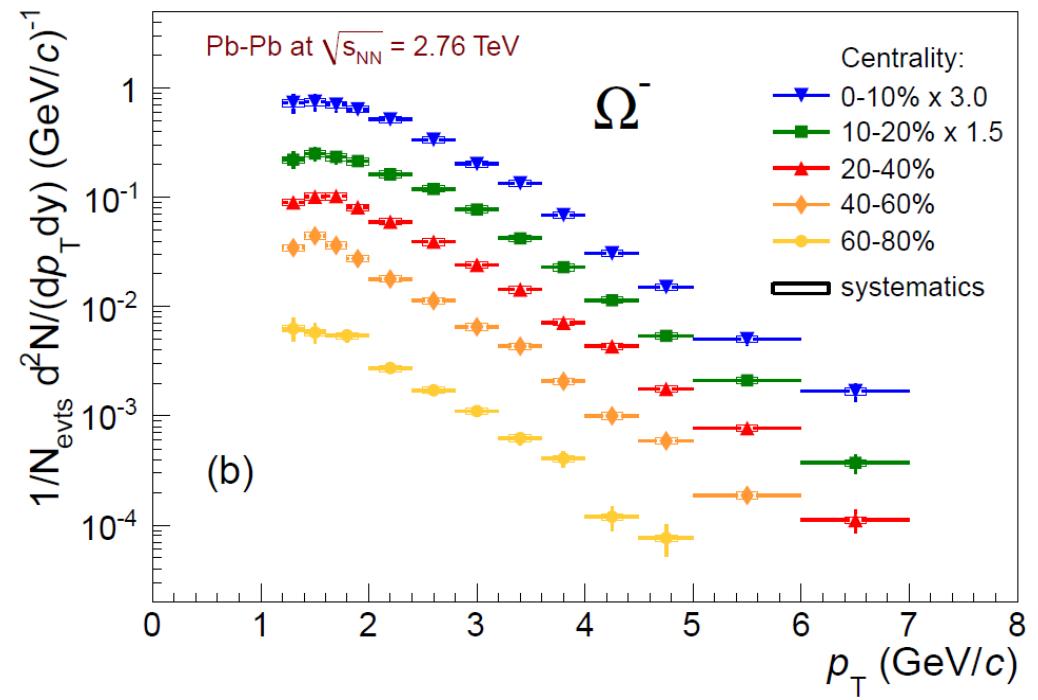
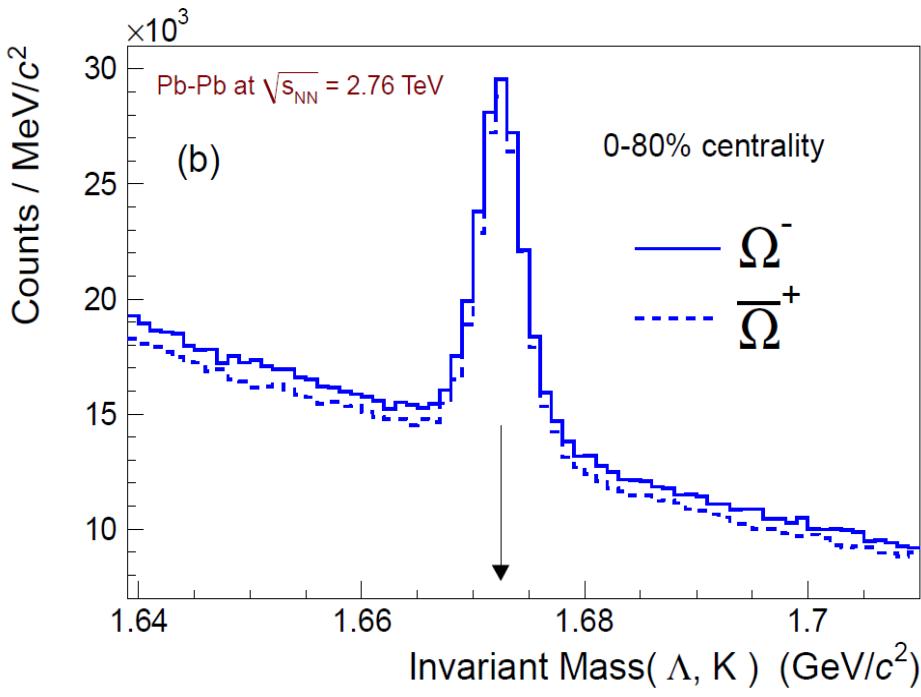
- conversely, rapidly dropping densities (reduction of dof and  $T^3$  drop of entropy density) imply cooling system falls out of equilibrium, i.e. freezes out  **$T$  bounded by  $T_c$  within a few MeV**

analysis of hadron production → experimental determination of  $T_c$

# Production of different hadron species

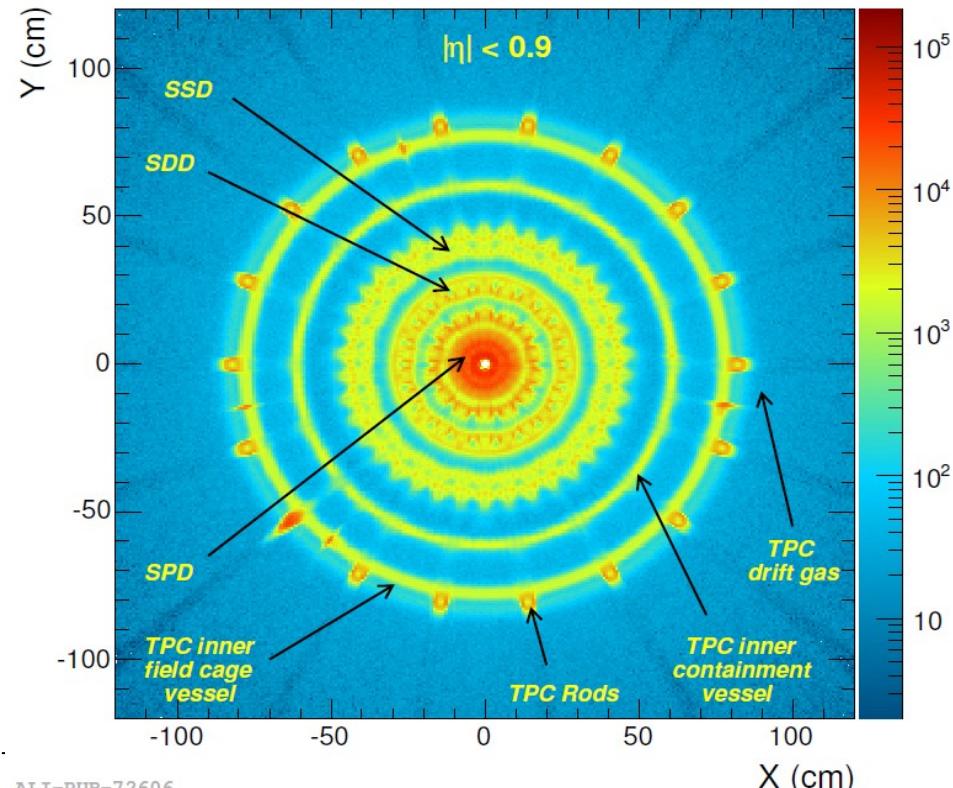
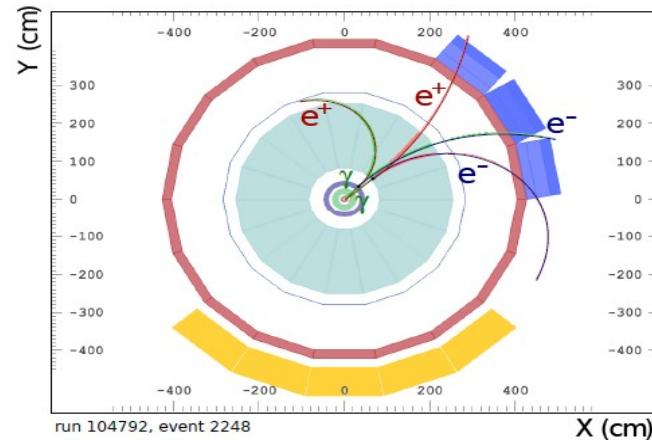
measure and integrate spectra of identified hadrons

- hadrons reconstructed from weak decay products ( $\Lambda$ ,  $\Xi$ ,  $\Omega$ )
- specific energy loss  $dE/dx$  and time-of-flight

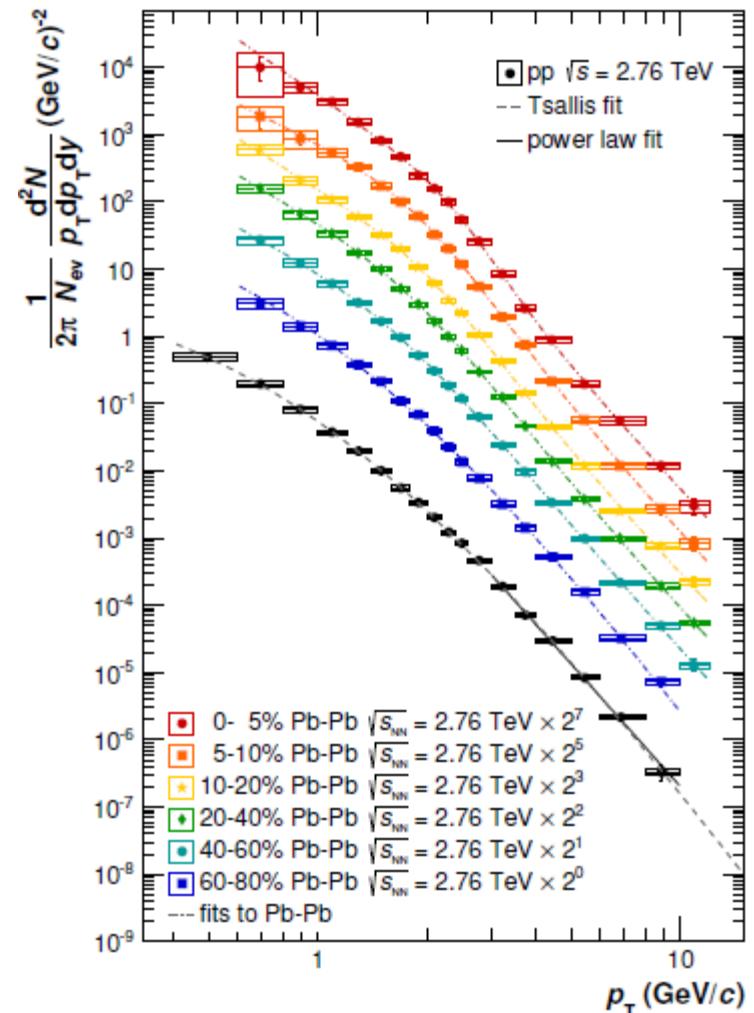


data: ALICE PLB 728 (2014) 216

# Neutral pions from decay photon conversion in detector

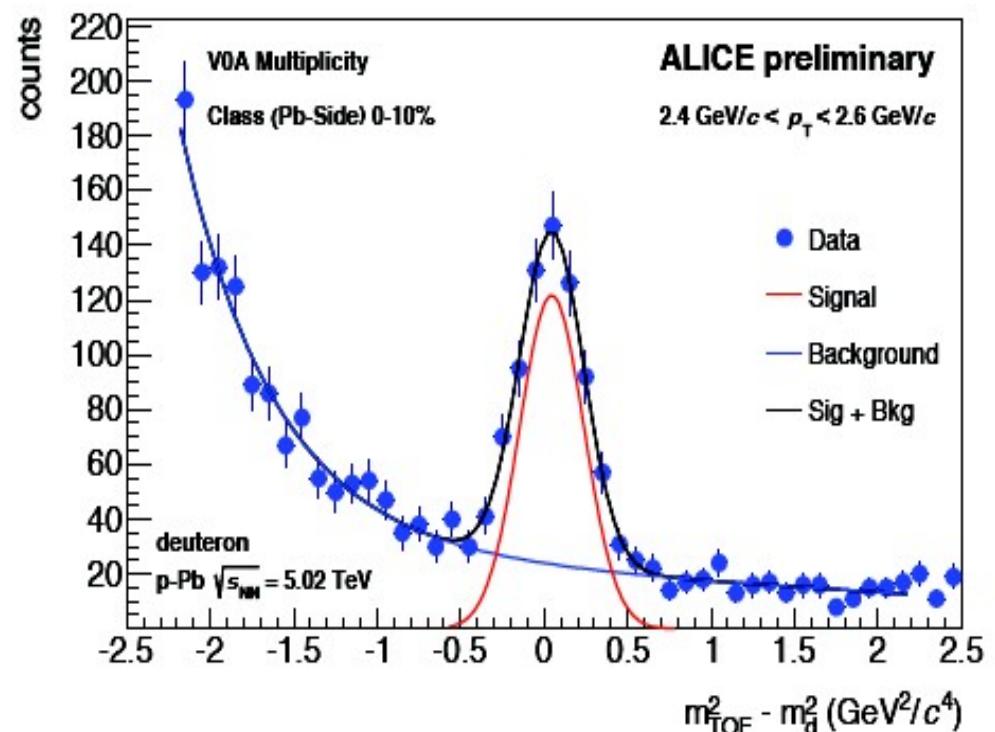
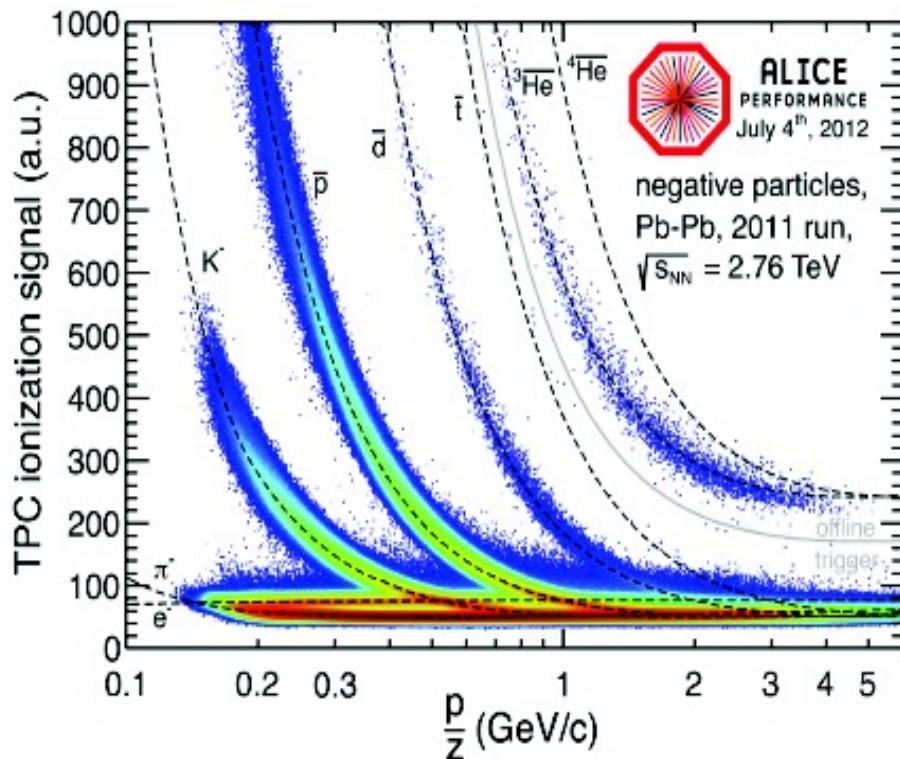


ALICE, EPJ C74 (2014) 10, 3108



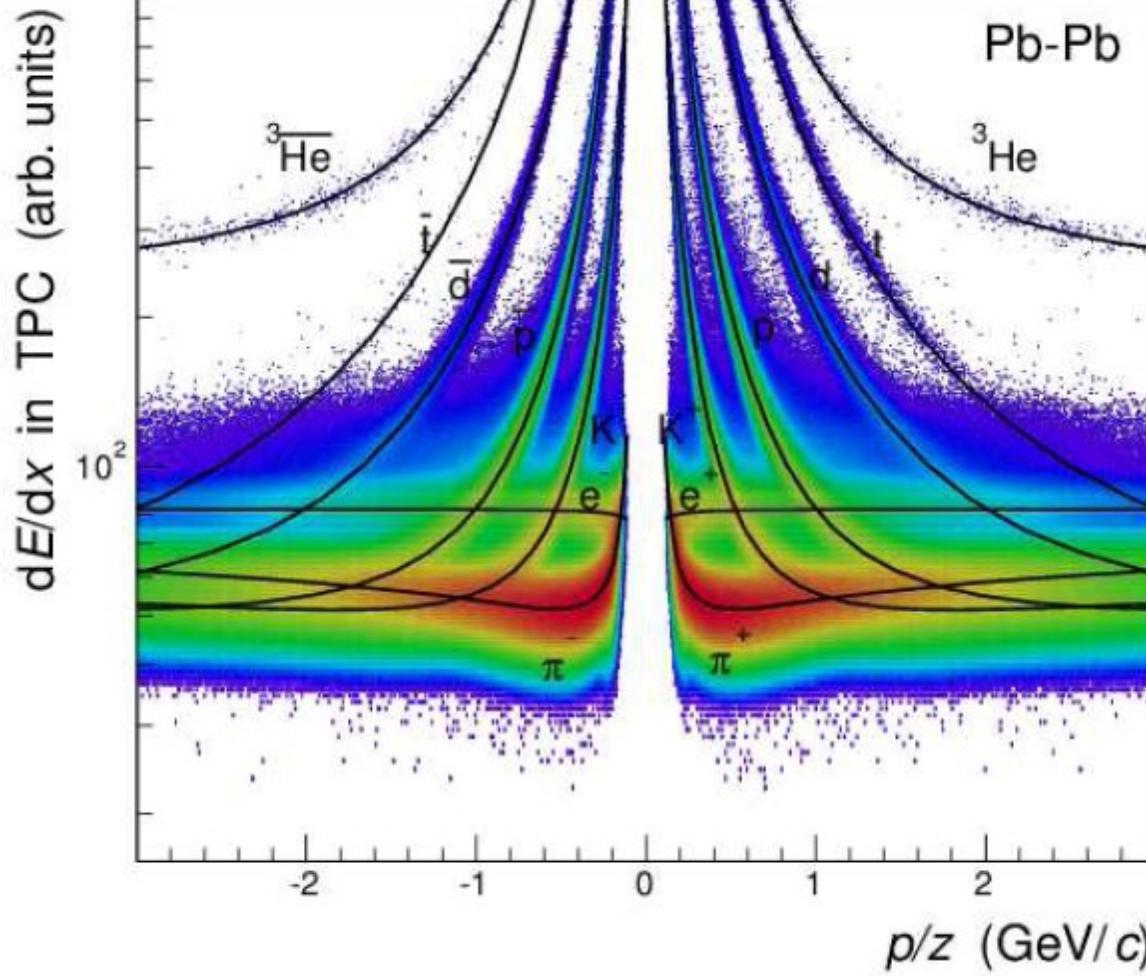
allows to determine the material thickness up to middle of TPC of 11%  $X_0$  with accuracy of 4.5%

# Particle identification via dE/dx in the TPC and TOF



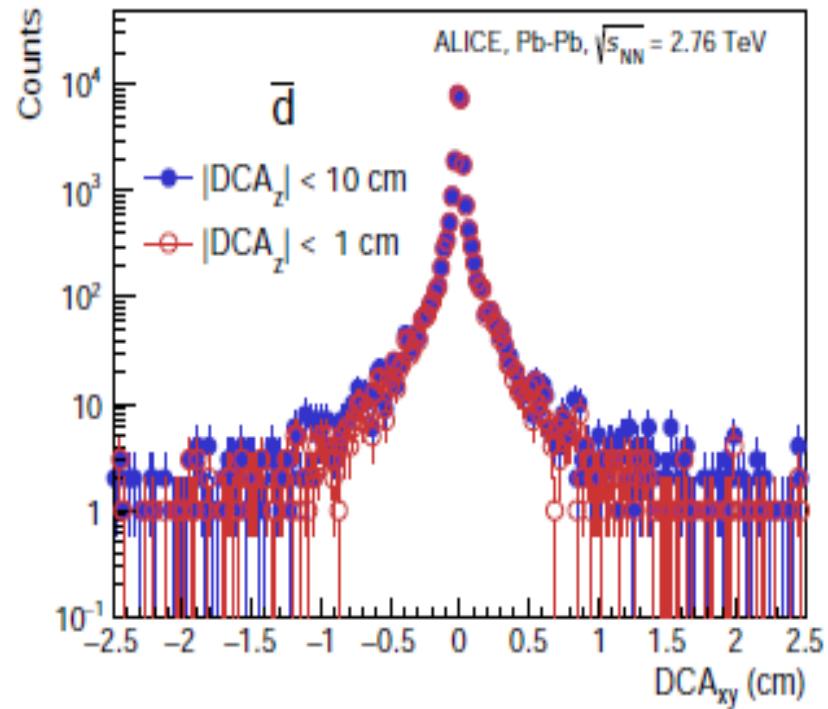
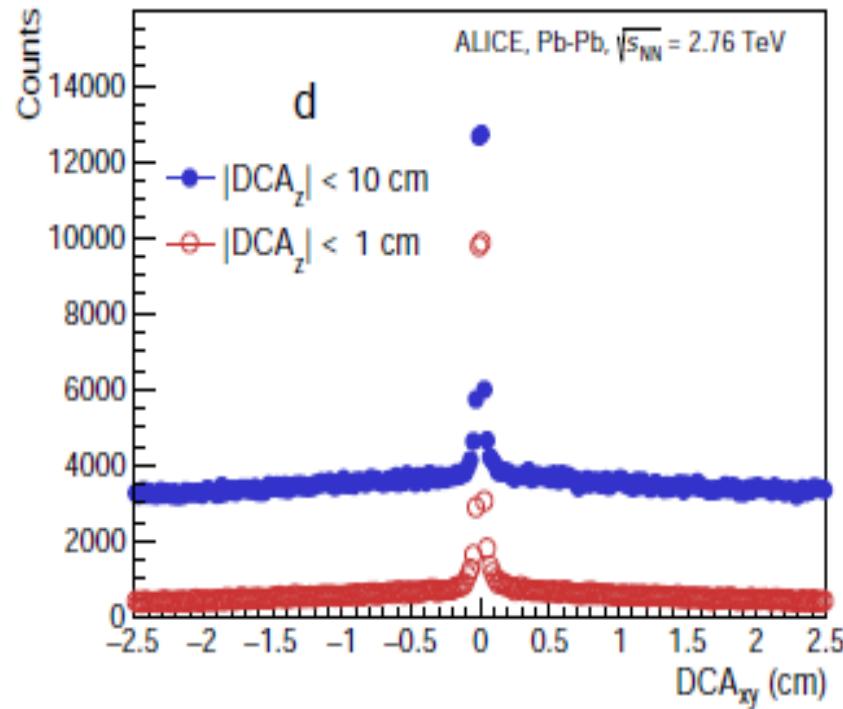
- all particles from e to  $^4\text{He}$  identified via the TPC specific energy loss (resol 6 %) plus TOF at crossings
- 2011 run  $2.3 \times 10^7$  events and in those 10 anti- $^4\text{He}$

# Difficulty for production of nuclei: secondaries from spallation



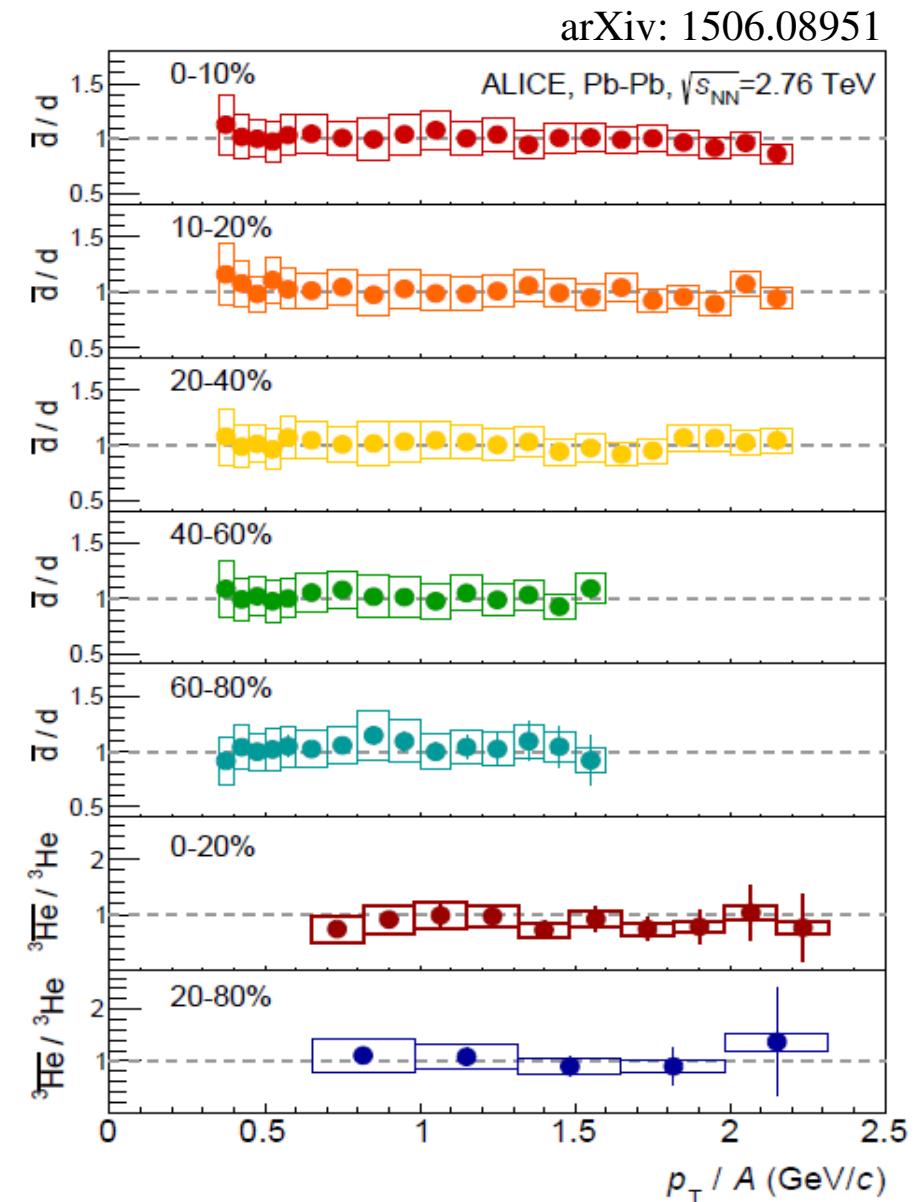
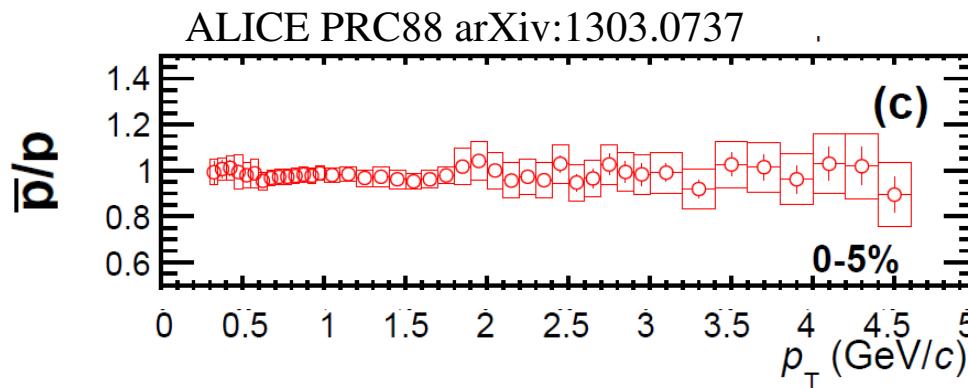
data ALICE - arXiv:1506:08951  
loose vertex cuts  
centrality: 0-80%  
apparent asymmetry between  $t$  and  
anti- $t$  is caused by large spallation  
background at low momentum for  
tritons  
anti- $t/t$  yield consistent with 1 after  
final cuts

# Separation of secondaries from primaries



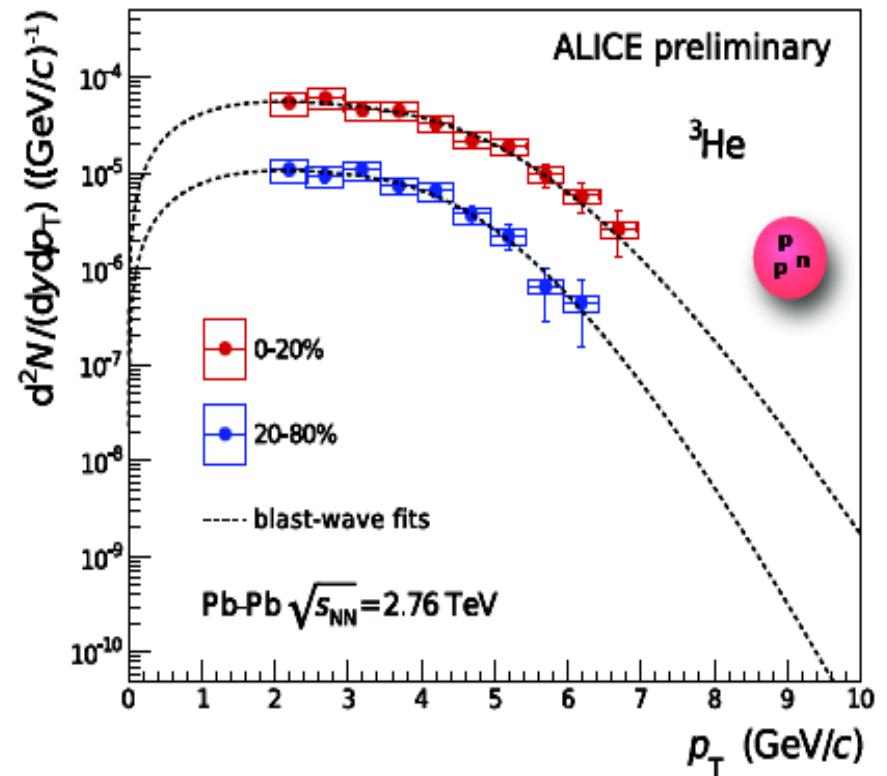
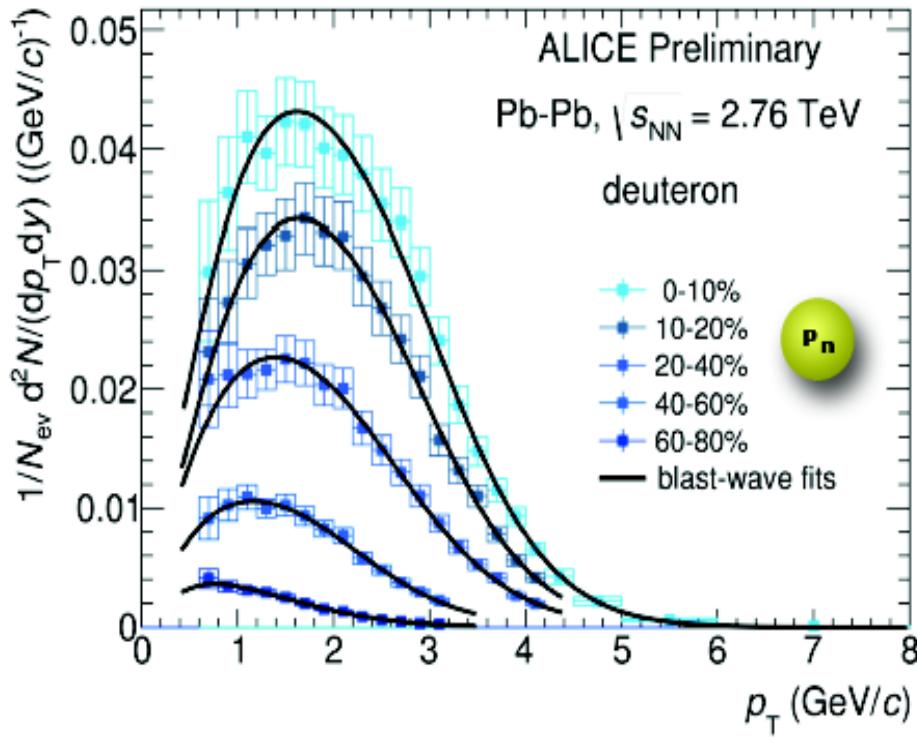
DCA = distance of closest approach of a track from the primary vertex  
separation of primaries from secondaries through vertex cut -  
important for particles, not anti-particles

# Production of nuclei and anti-nuclei at the LHC



- matter and anti-matter produced in equal proportions at LHC
- consistent with net-baryon free central region, ( $\mu_b < 1$  MeV)

# Measurement of transverse momentum spectra



composite objects participate in hydrodynamic flow  
spectra described by hydro-inspired 'blast wave' approach  
obtain  $\langle \beta \rangle \approx 0.6$

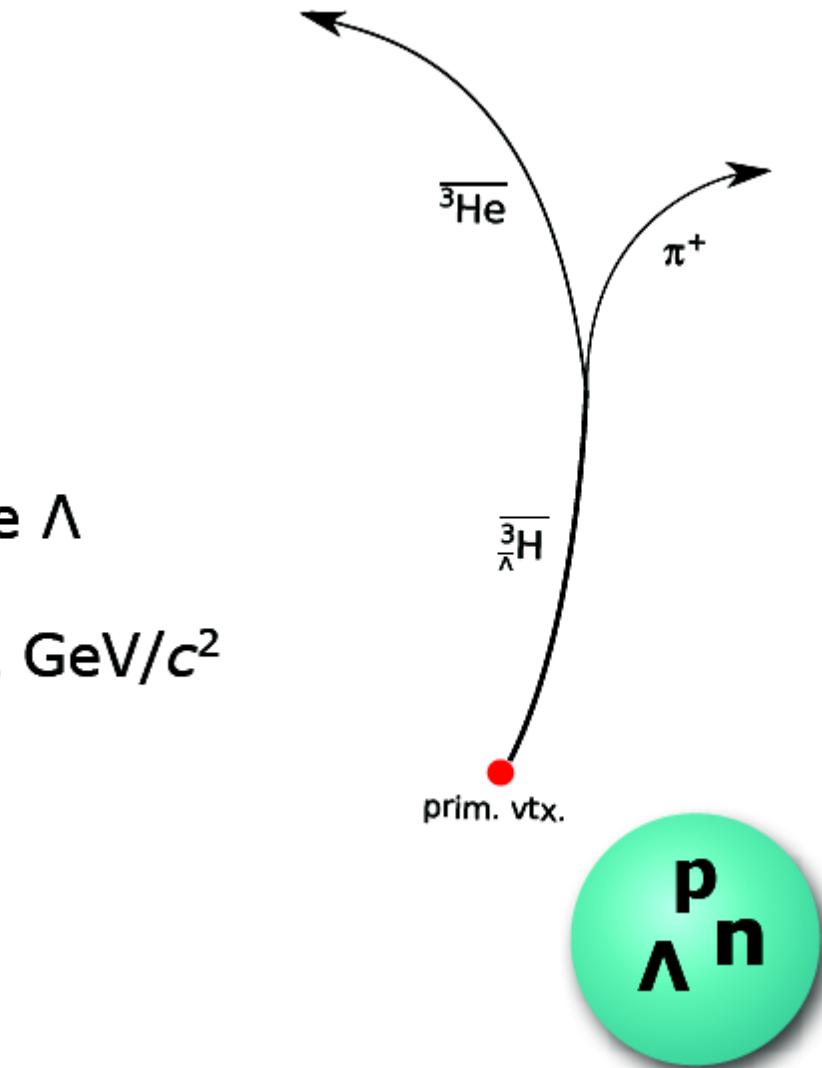
# Hypertriton identification via particle ID and vertex measurements

Identification of light nuclei  
which are daughter tracks  
originating from decay vertices

Lifetime similar to lifetime of free  $\Lambda$

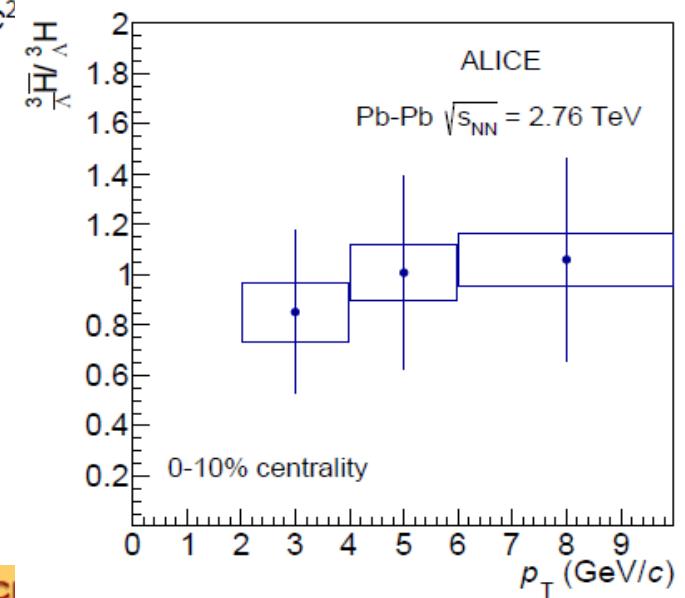
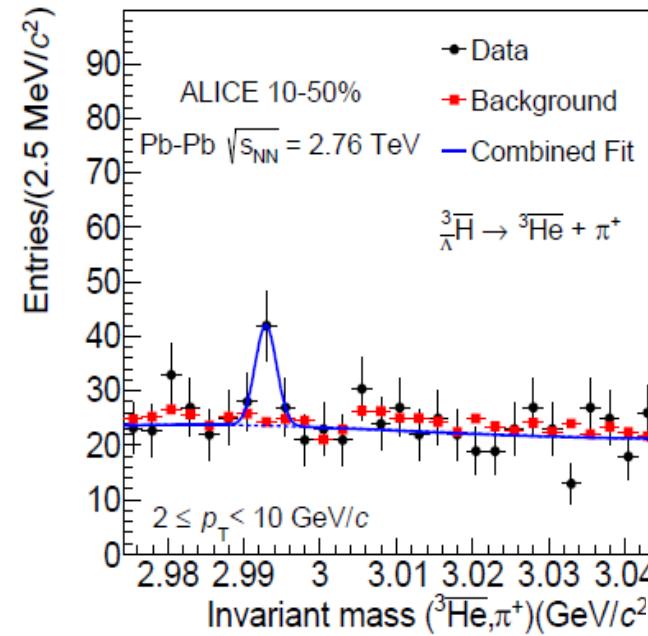
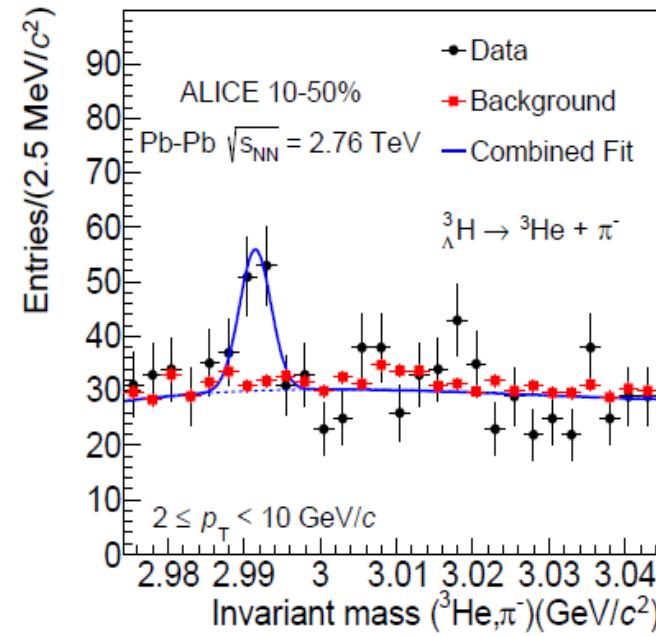
$$m(\text{Hypertriton}) = 2.991 \pm 0.002 \text{ GeV}/c^2$$

investigated decay channel:  
 $\text{Hypertriton} \rightarrow {}^3\text{He} + \pi^-$



# Hypertriton results

arXiv:1506.08453



# Statistical hadronization model and experimental data

## starting point: the statistical model – grand canonical

partition function:  $\ln Z_i = \frac{Vg_i}{2\pi^2} \int_0^\infty \pm p^2 dp \ln(1 \pm \exp(-(E_i - \mu_i)/T))$

particle densities:  $n_i = N/V = -\frac{T}{V} \frac{\partial \ln Z_i}{\partial \mu} = \frac{g_i}{2\pi^2} \int_0^\infty \frac{p^2 dp}{\exp((E_i - \mu_i)/T) \pm 1}$

for every conserved quantum number there is a chemical potential:

$$\mu_i = \mu_B B_i + \mu_S S_i + \mu_{I_3} I_i^3$$

but can use conservation laws to constrain  $V, \mu_S, \mu_{I_3}$



**fit at each energy provides values for T and  $\mu_b$**

- get yields of all hadrons

for  $dN/dy$  need in addition volume per unit  $y$  - fix to  $dN_{ch}/dy$

**good fit to data for central collisions of heavy nuclei at AGS, SPS, RHIC, LHC**

see e.g. A. Andronic, P. Braun-Munzinger, J.S. Nucl. Phys. A722(2006)167 nucl/th/0511071

## implementation of our statistical model

in total 426 hadrons and composites (nuclei etc.) included – all states considered confirmed by PDG

precision of e+e- data and LHC data requires this  
(currently updating for newly found states)

finite volume correction

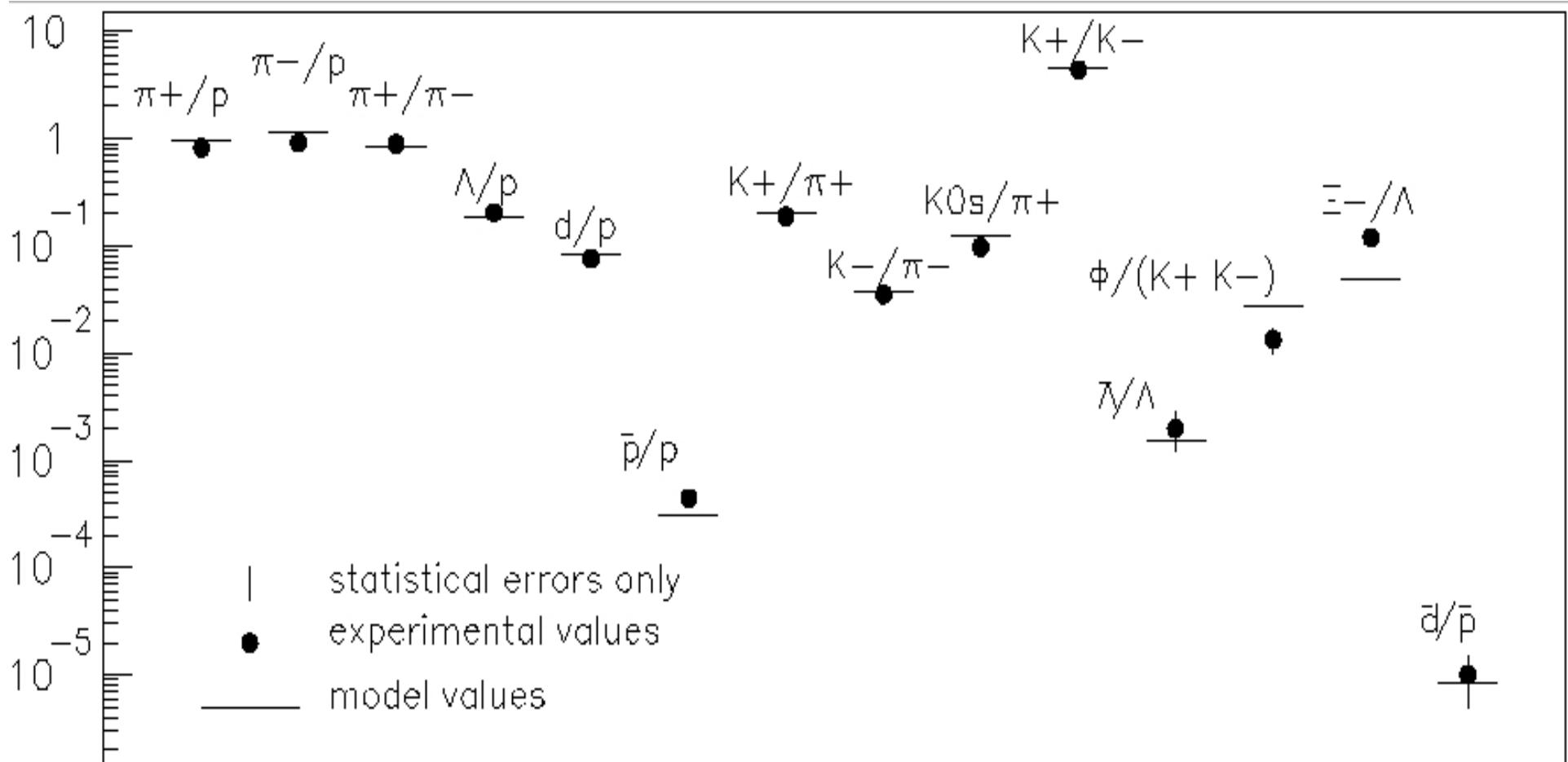
interactions as Van der Waals gas via excluded volume

for inclusion of charm-quarks canonical correction factors

# first successful application of thermal model - AGS data

14.6 A GeV/c central Si + Au collisions and GC statistical model

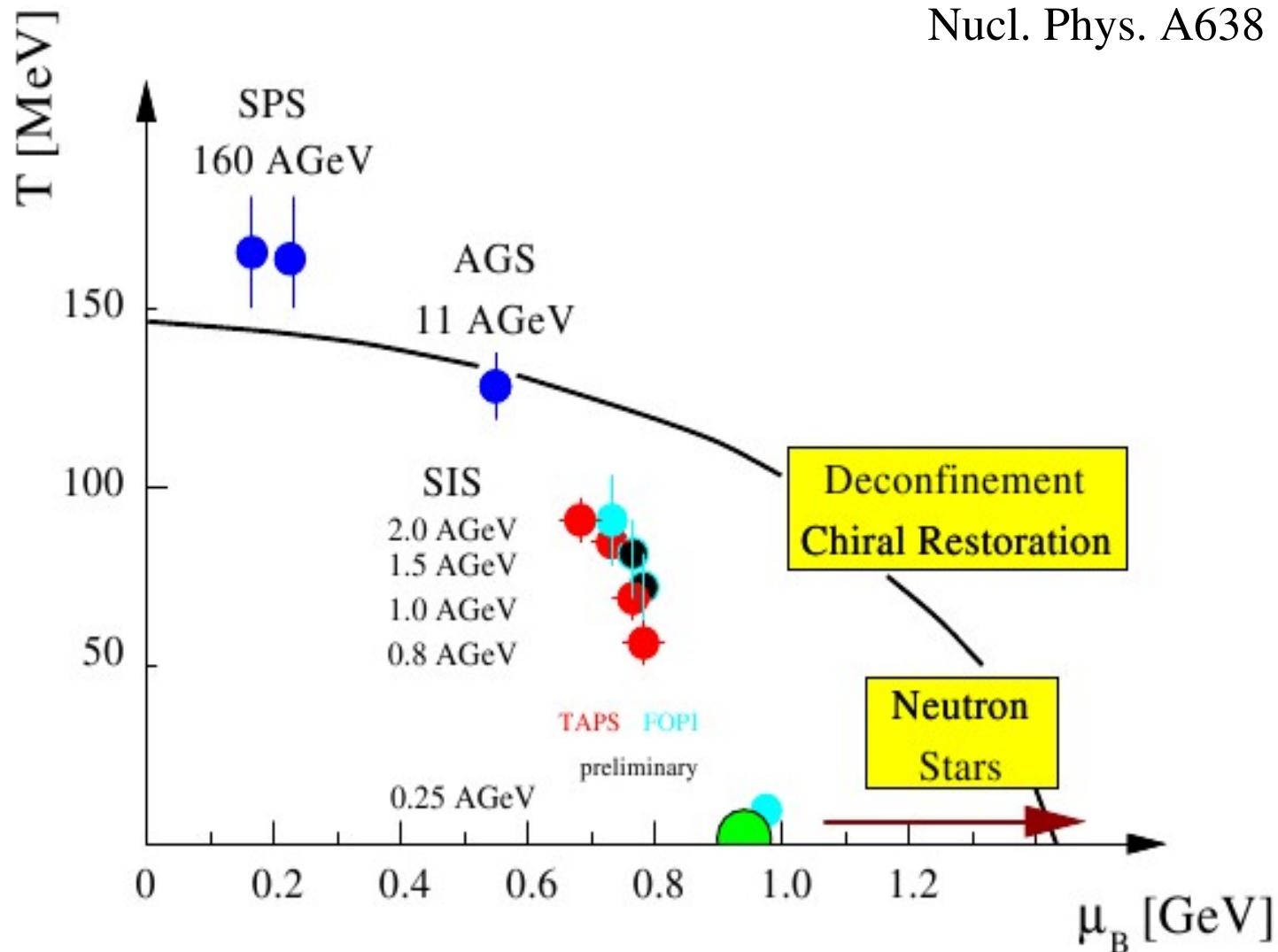
P. Braun-Munzinger, J. Stachel, J.P. Wessels, N. Xu, PLB 1994



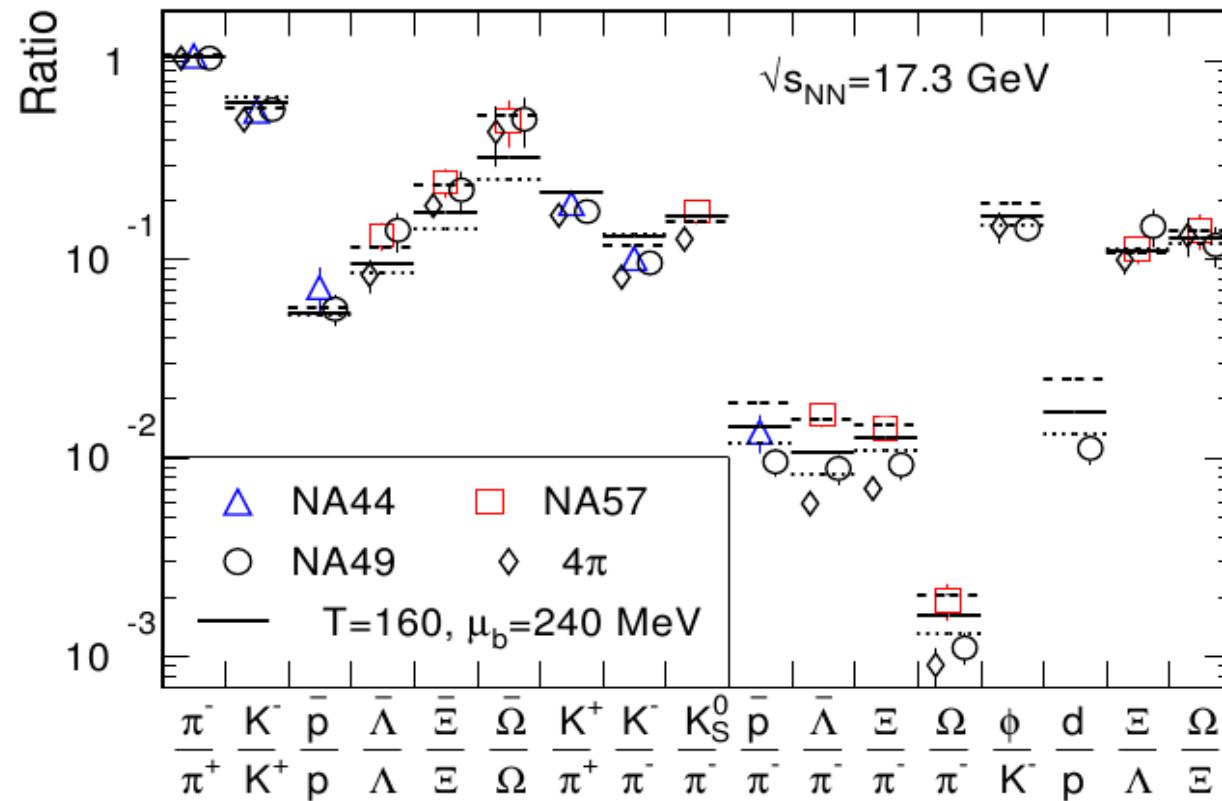
dynamic range: 9 orders of magnitude! No deviation

# leading to the first phase diagram with experimental points

P.Braun-Munzinger and J. Stachel, nucl-th/9803015,  
Nucl. Phys. A638 (1998) 3

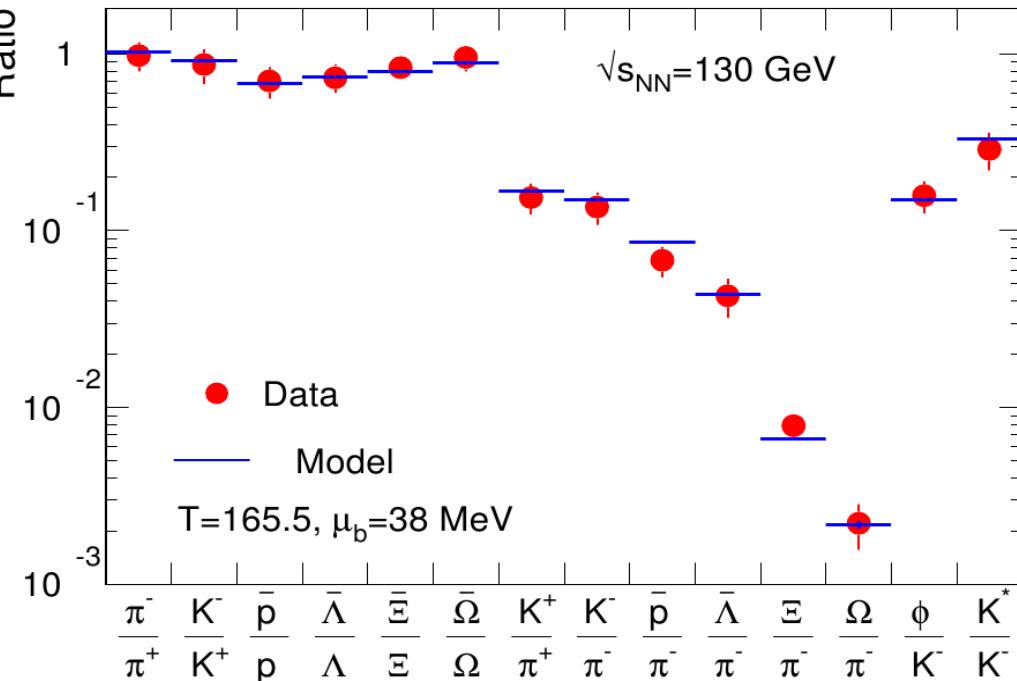


# SPS data and thermal model

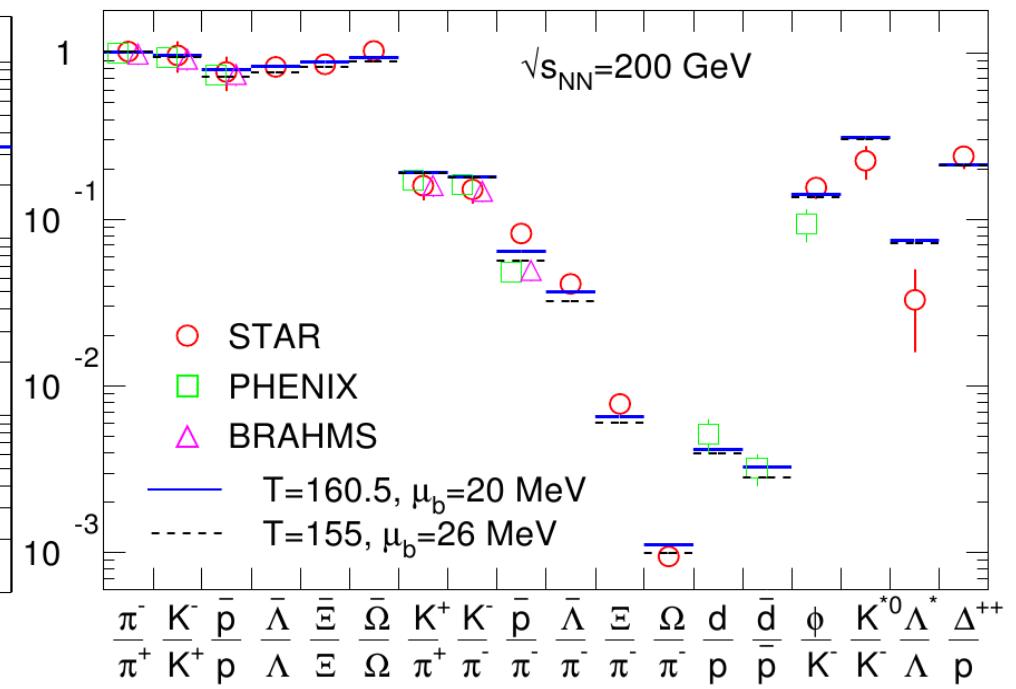


# RHIC hadron yields reproduced really well compared to statistical model (GC)

130 GeV data in excellent agreement  
with thermal model **predictions**



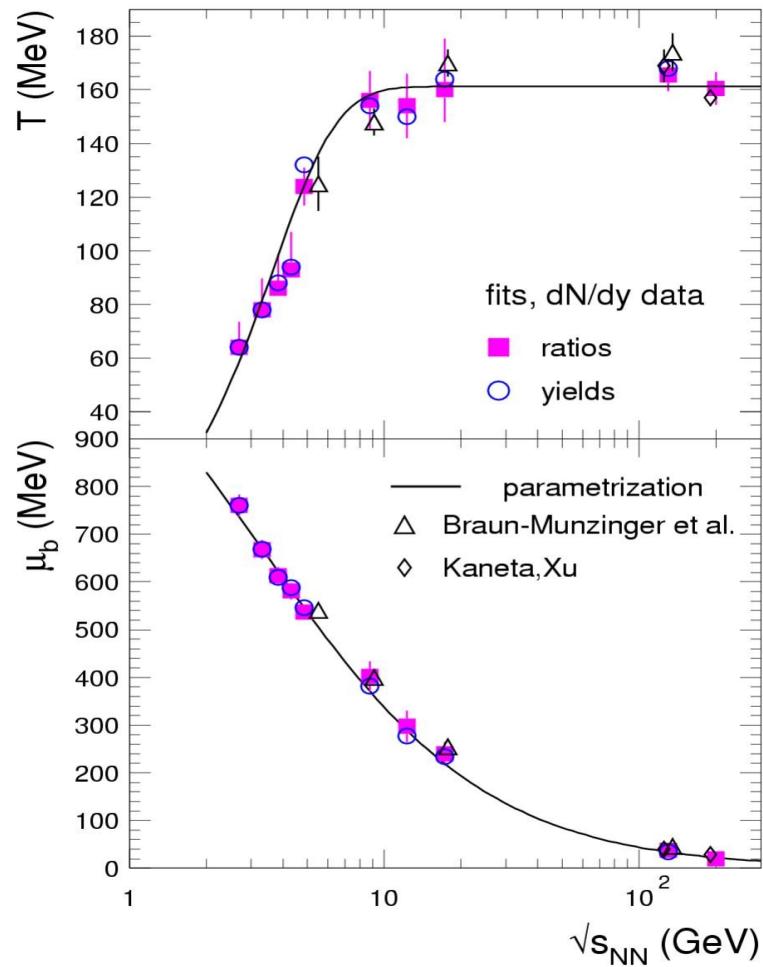
prel. 200 GeV data fully in line  
still some experimental discrepancies



chemical freeze-out at:  $T = 165 \pm 5 \text{ MeV}$

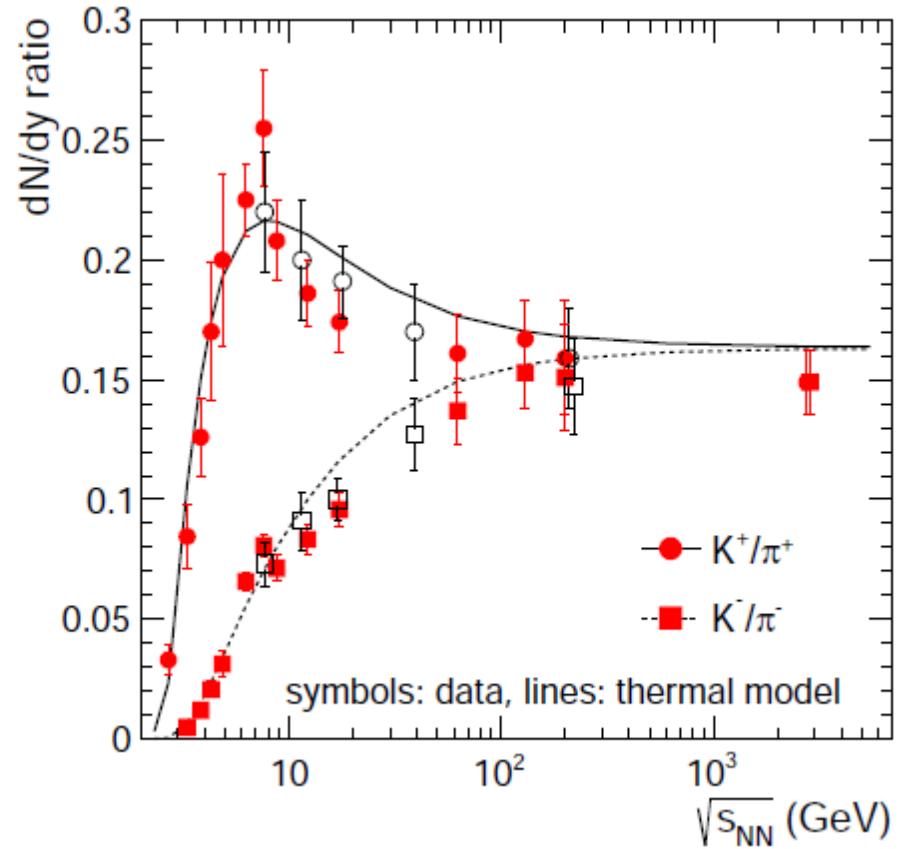
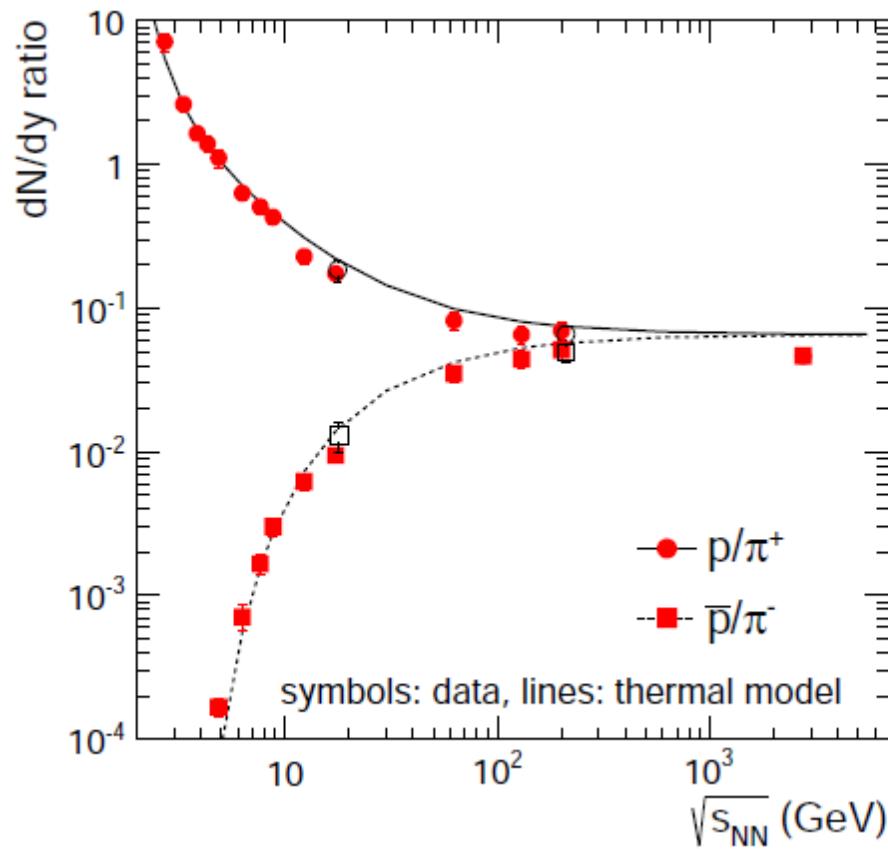
P. Braun-Munzinger, D. Magestro, K. Redlich, J. Stachel, Phys. Lett. B518 (2001) 41  
A. Andronic, P. Braun-Munzinger, J. Stachel, Nucl. Phys. A772 (2006) 167  
confirmed by Xu and Kaneta and by F. Becattini

# Systematic evolution of T and mu\_b with beam energy

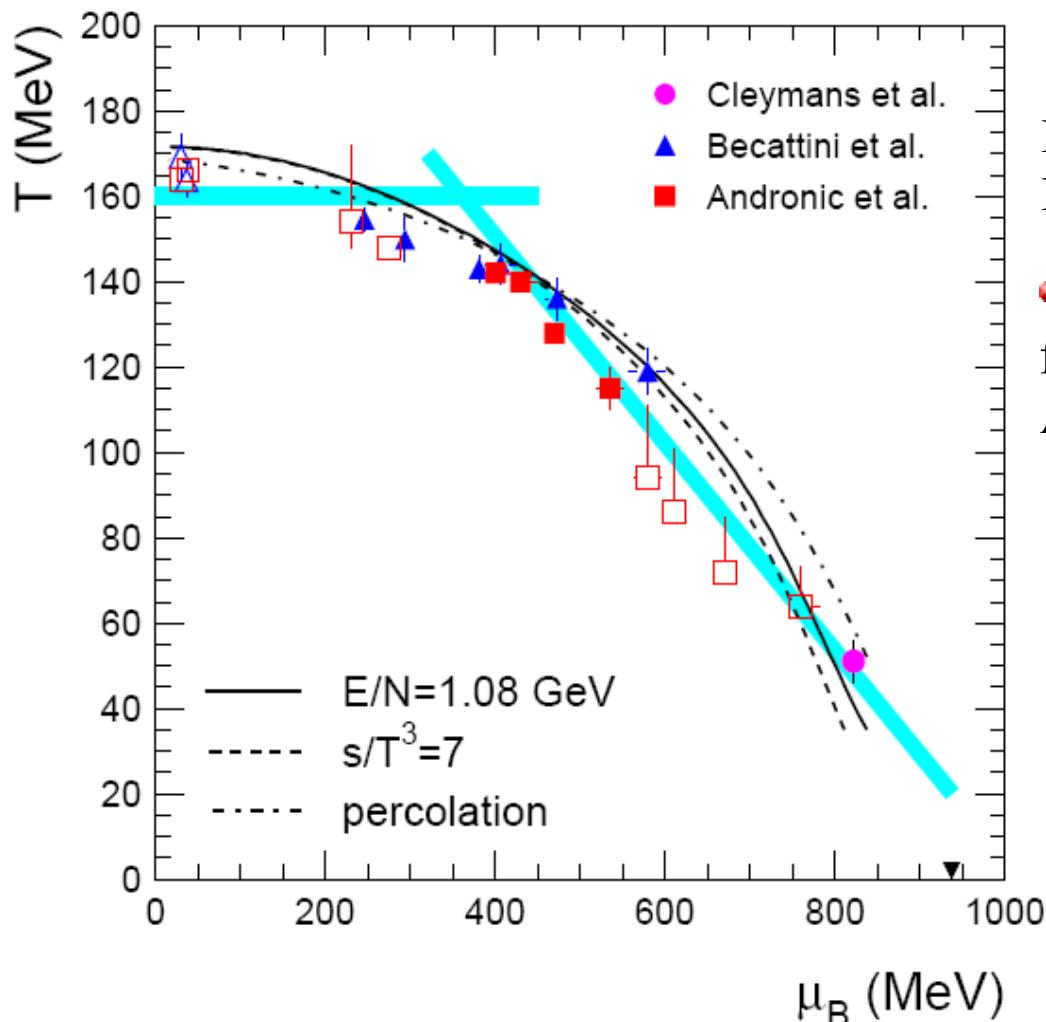


# beam energy dependence of hadron yields from AGS to LHC

following the observed evolution of  $T$  and  $\mu_b$ , detailed features of proton/pion and kaon/pion ratios reproduced in detail



# experimental knowledge of the QCD phase diagram



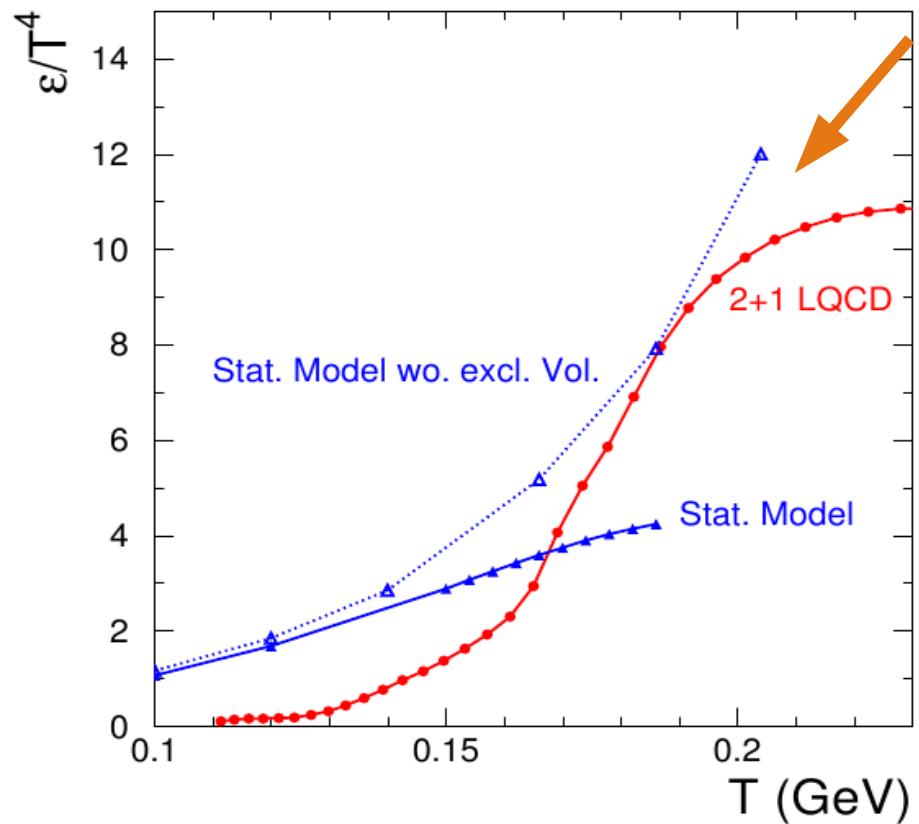
- agreement between groups doing finite temperature lattice gauge theory:  
 $T_c(\mu=0) = 150-160 \text{ MeV}$   
Bazavov & Petreczky, arXiv:1005.1131 [hep-lat] S. Borsanyi et al., arXiv:1005.3508 [hep-lat]
- data points 'chemical' freeze-out of hadrons from abundancies  
A. Andronic, P. Braun-Munzinger, J. S., Nucl. Phys. A772 (2006) 167

$T_{\text{chem}}$  saturates  
apparently at  $T_c$   
not trivial

# equilibration driven by high densities near $T_c$

rapid equilibration within a narrow temperature interval around  $T_c$  by multi-particle collisions due to steep temperature dependence of densities

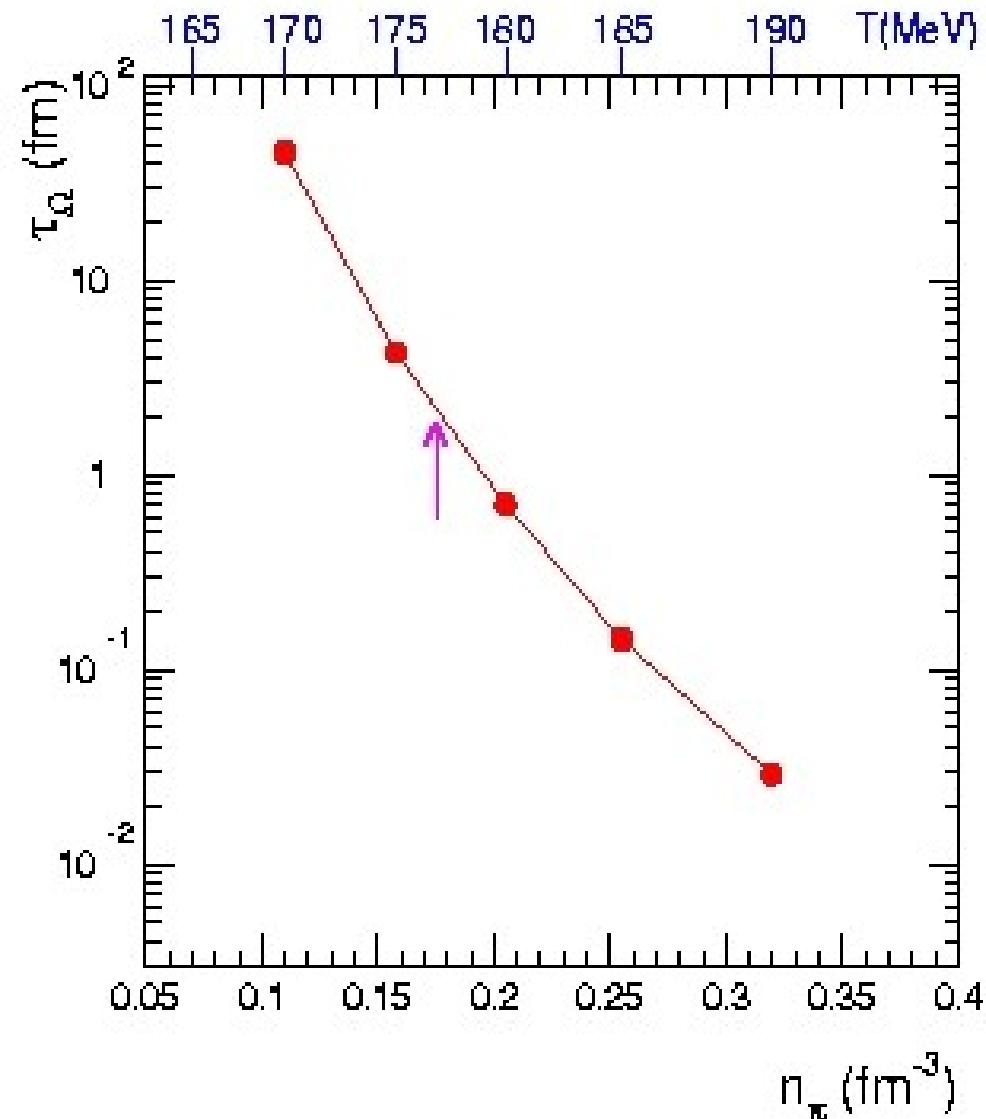
P. Braun-Munzinger, J. Stachel, C. Wetterich, Phys. Lett. B596 (2004)61



for  $T_{ch}$  20-30 MeV below  $T_c$   
very hard to maintain  
scenario of simultaneous  
freeze-out of all hadron species  
estimate upper limit of  
 $T_c - T_{ch} = 5$  MeV

requires  $T_c \approx 160$  MeV  
experimental determination!

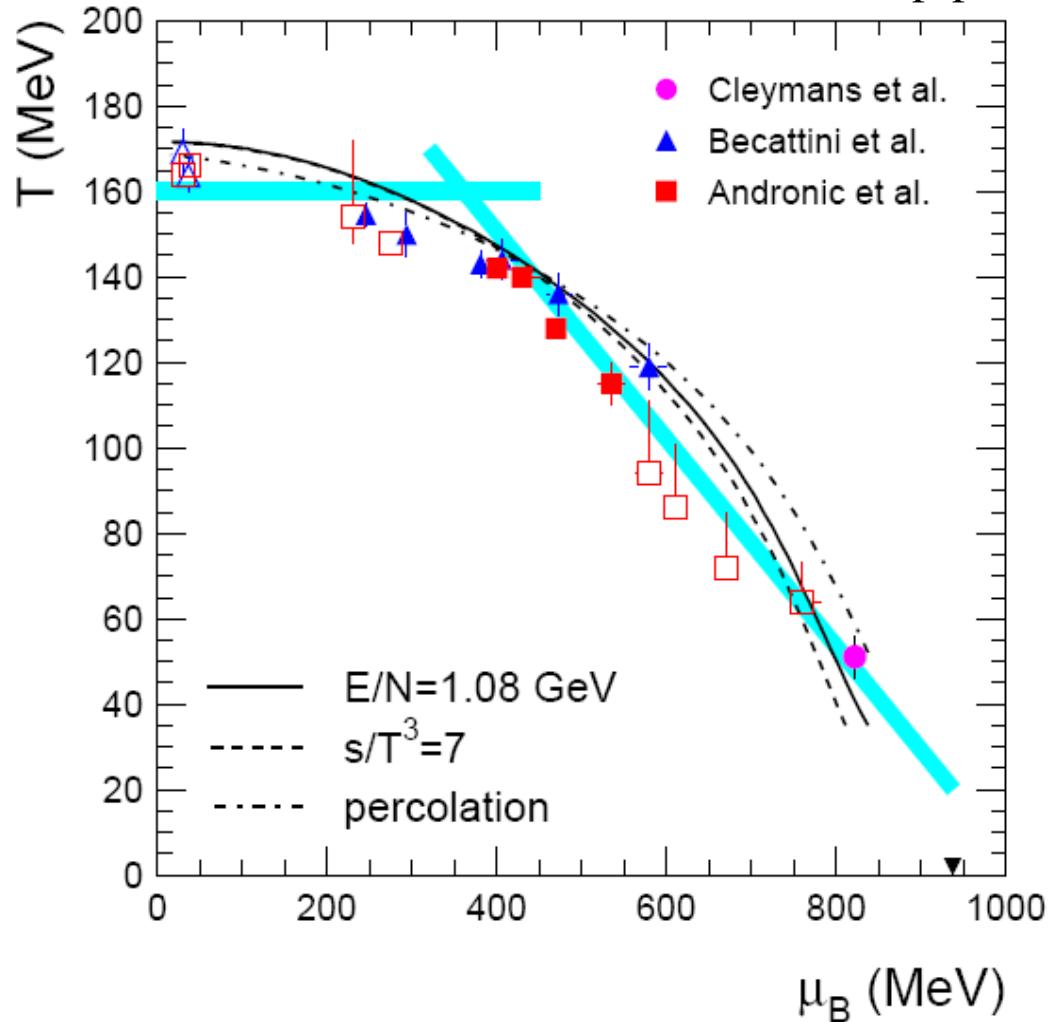
# density dependence of characteristic time for strange baryon production



- near phase transition particle density varies rapidly with  $T$  (see previous slide)
- for SPS energies and above reaction such as  $2\pi + \text{KKK} \rightarrow \Omega \bar{\Lambda}$  bring multi-strange baryons close to equilibrium rapidly
- in region around  $T_c$  equilibration time  $\tau_\Omega \propto T^{-60}!$
- increase  $n_\pi$  by 1/3:  $\tau = 0.2 \text{ fm}/c$   
(corresponds to increase in  $T$  by 8 MeV)  
decrease  $n_\pi$  by 1/3:  $\tau = 27 \text{ fm}/c$
- all particles freeze out within a very narrow temperature window due to the extreme temperature sensitivity of multi-particle reactions

# phase diagram and chemical freeze-out points 2009

A. Andronic et al. ArXiv 0911.4806[hep-ph]



based on this prediction for LHC:

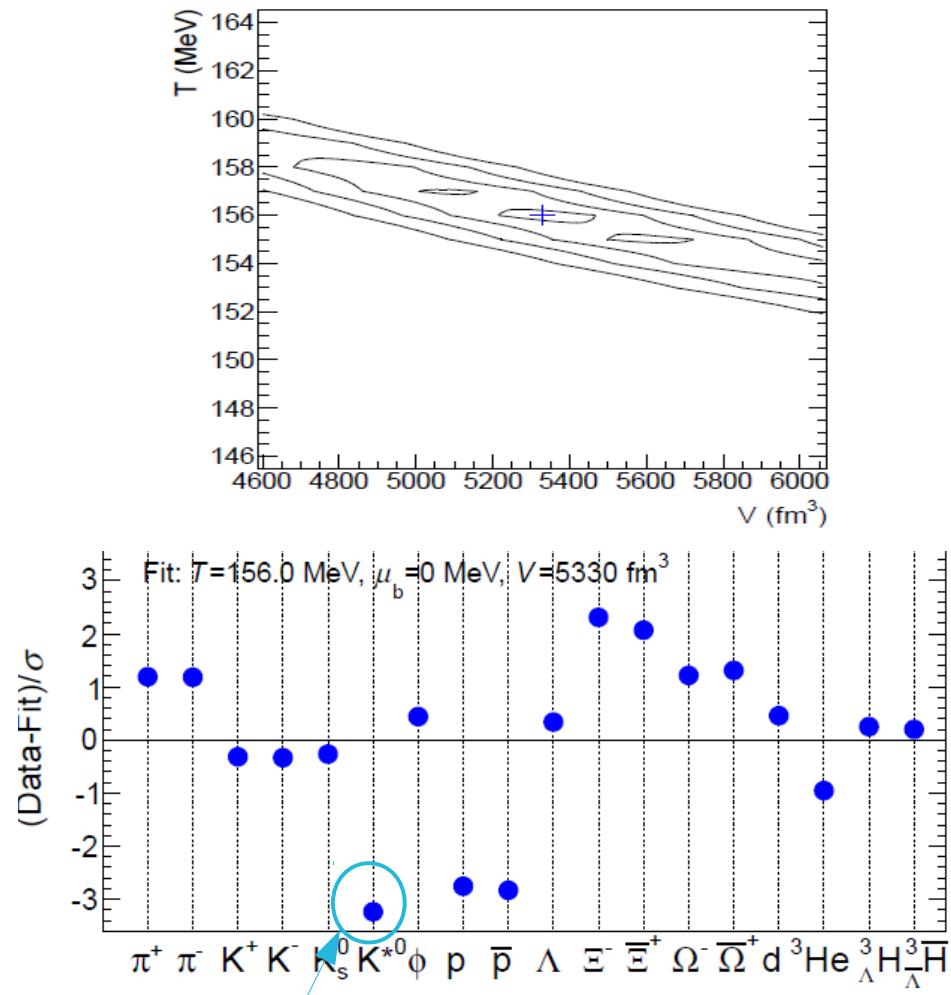
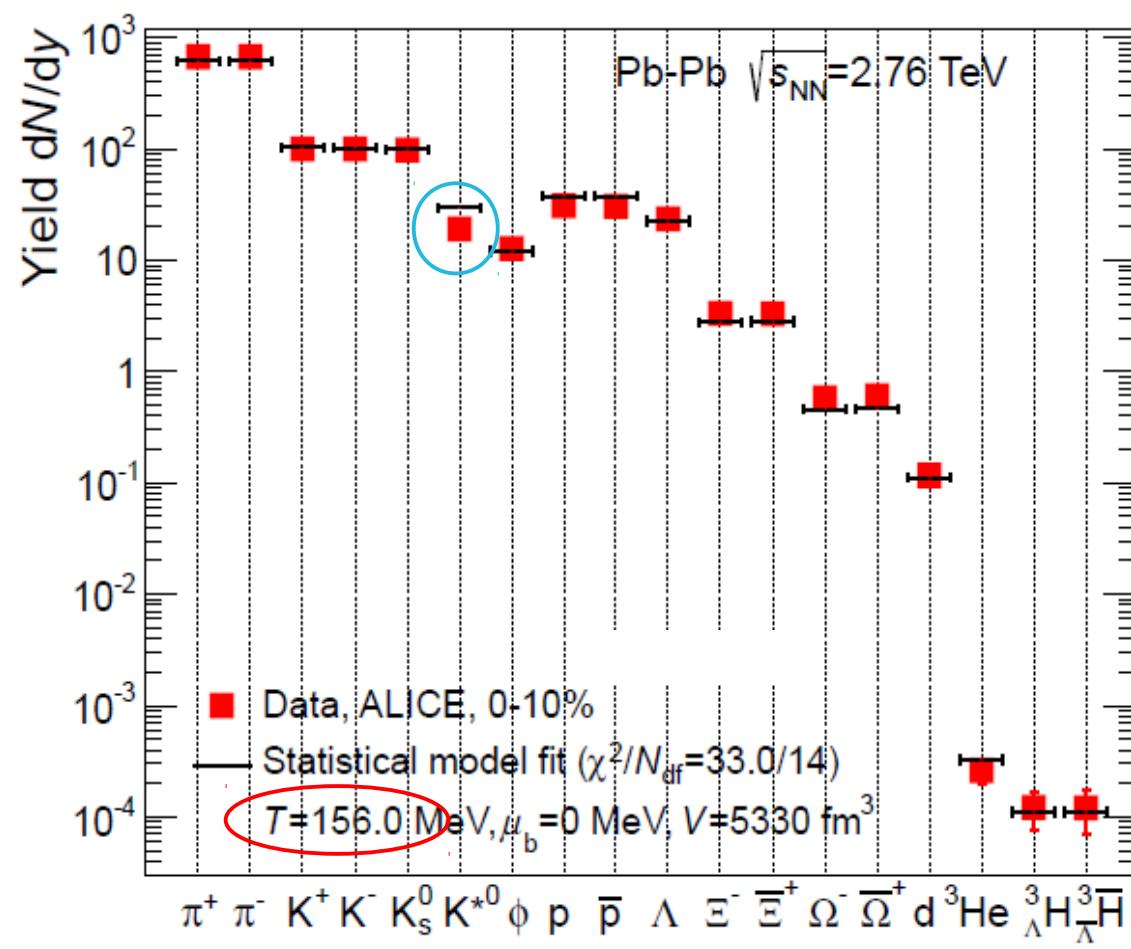
$$T = 161 \pm 4 \text{ MeV} \text{ and } \mu_b = 0.8^{+1.2}_{-0.6} \text{ MeV}$$

A. Andronic, P. Braun-Munzinger, J.S.  
arXiv:0707.4076 [nucl-th]

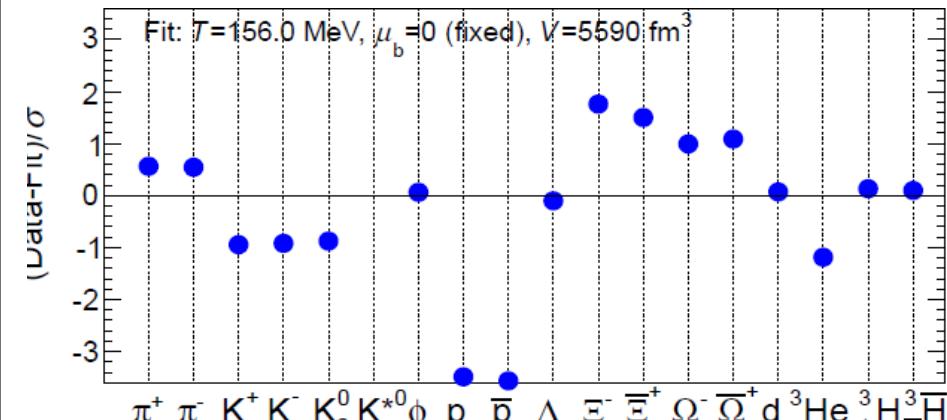
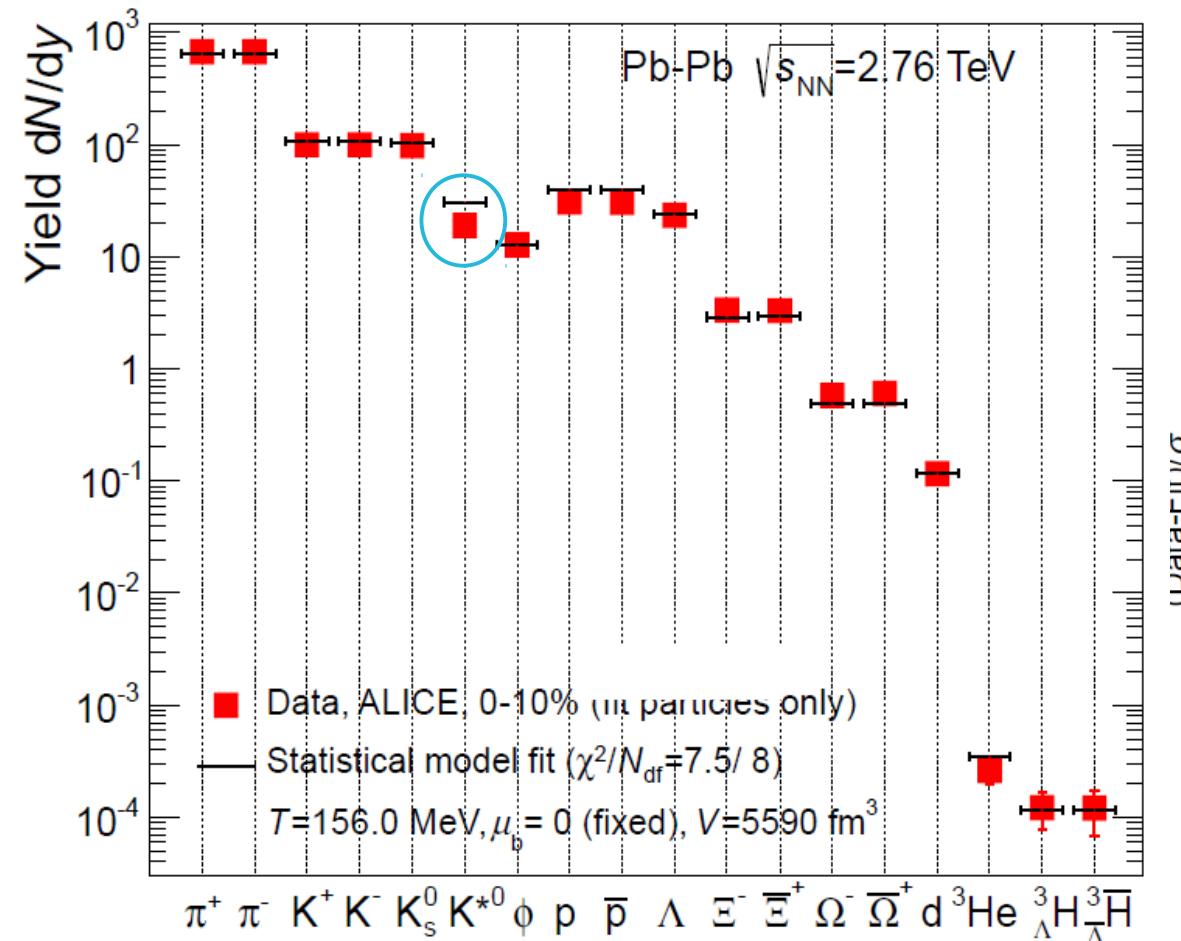
over the coming years these numbers  
moved a little due to RHIC data

# LHC data

# Fit to data from ALICE at the LHC



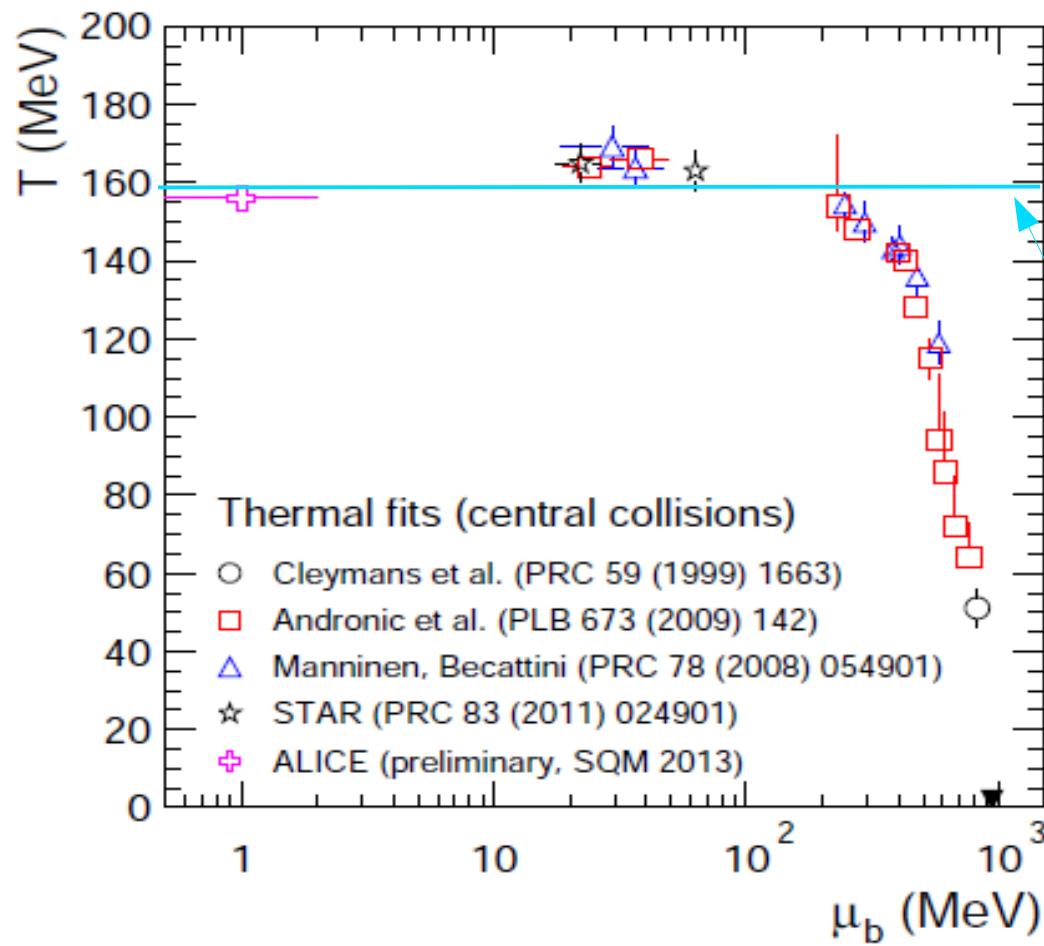
# fit excluding protons



excluding protons: T unchanged  
perfect fit for other hadrons

# Energy dependence of temperature and baryochem pot.

temperature vs. baryochemical potential



hadron yields for Pb-Pb central collisions from LHC down to RHIC, SPS, AGS and even SIS energies well described by a statistical ensemble

- there is a limiting temperature for a hadronic system

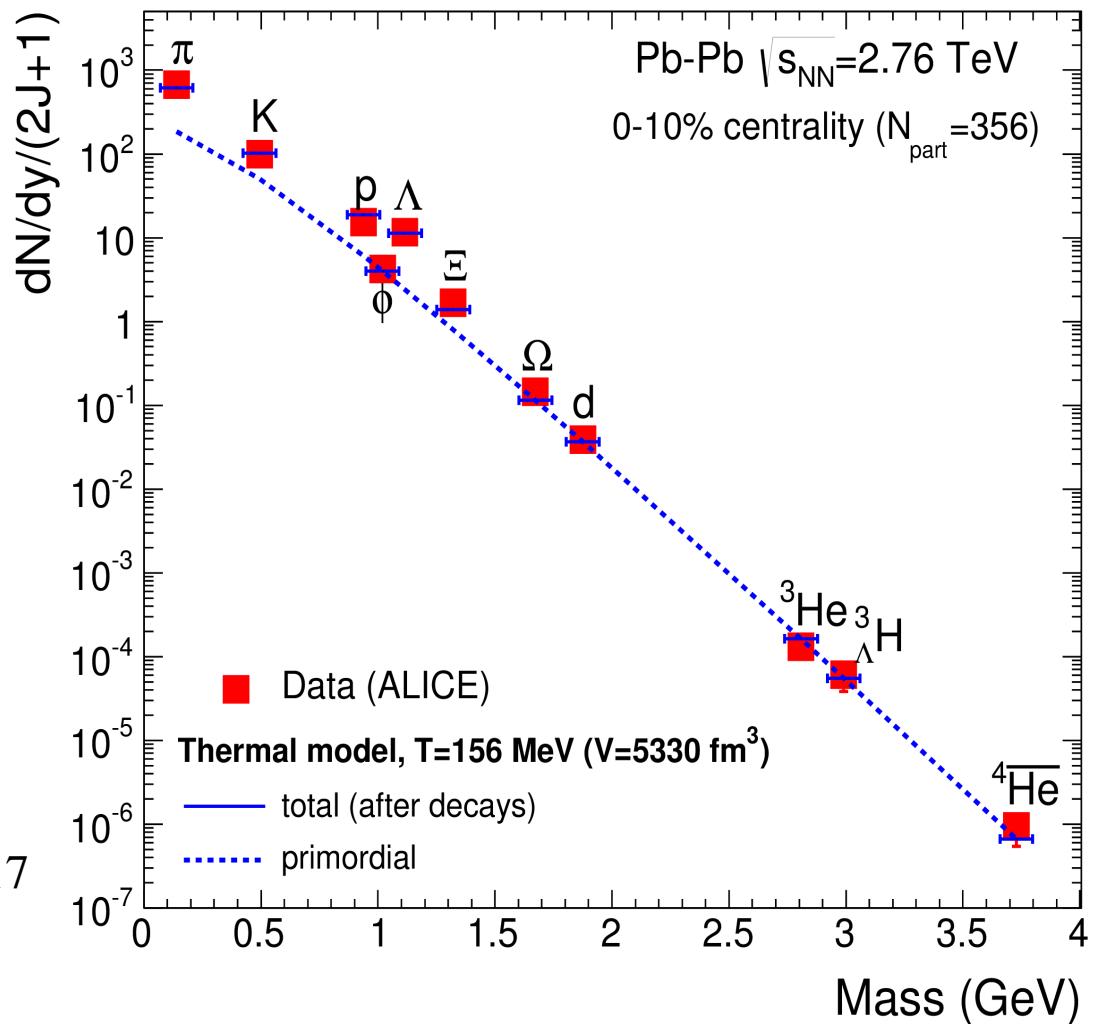
$$T_{\text{lim}} = 159 \pm 3 \text{ MeV}$$

reached for  $\sqrt{s_{\text{NN}}} \geq 10 \text{ GeV}$

# Quark- hadron duality

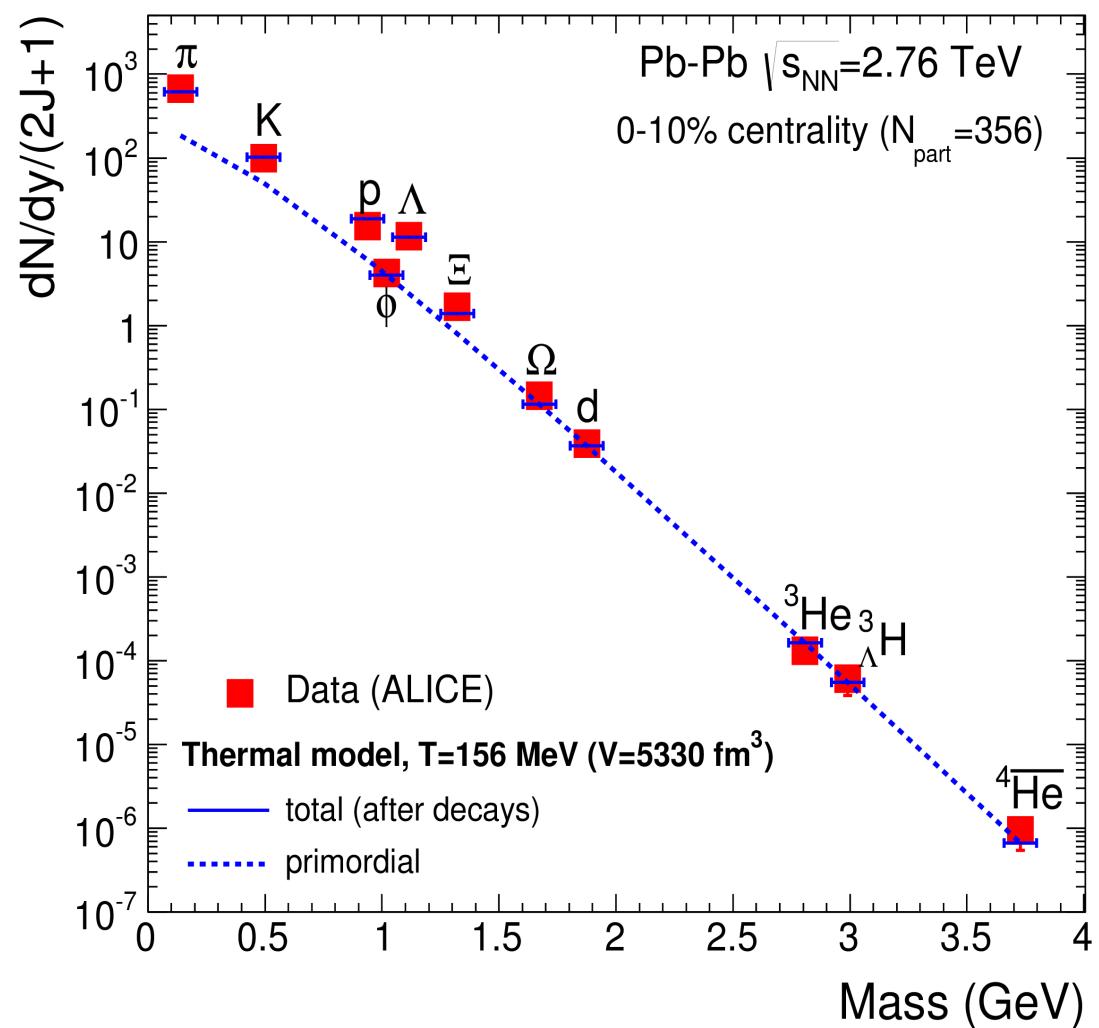
agreement over 9 orders of magnitude with QCD statistical operator prediction  
(- strong decays need to be added)

works equally well for nuclei and loosely bound (anti)hyper-nuclei  
prediction P. Braun-Munzinger, J.S., J.Phys. G28 (2002) 1971-1976, J.Phys. G21 (1995) L17  
strong indication of isentropic expansion in hadronic phase



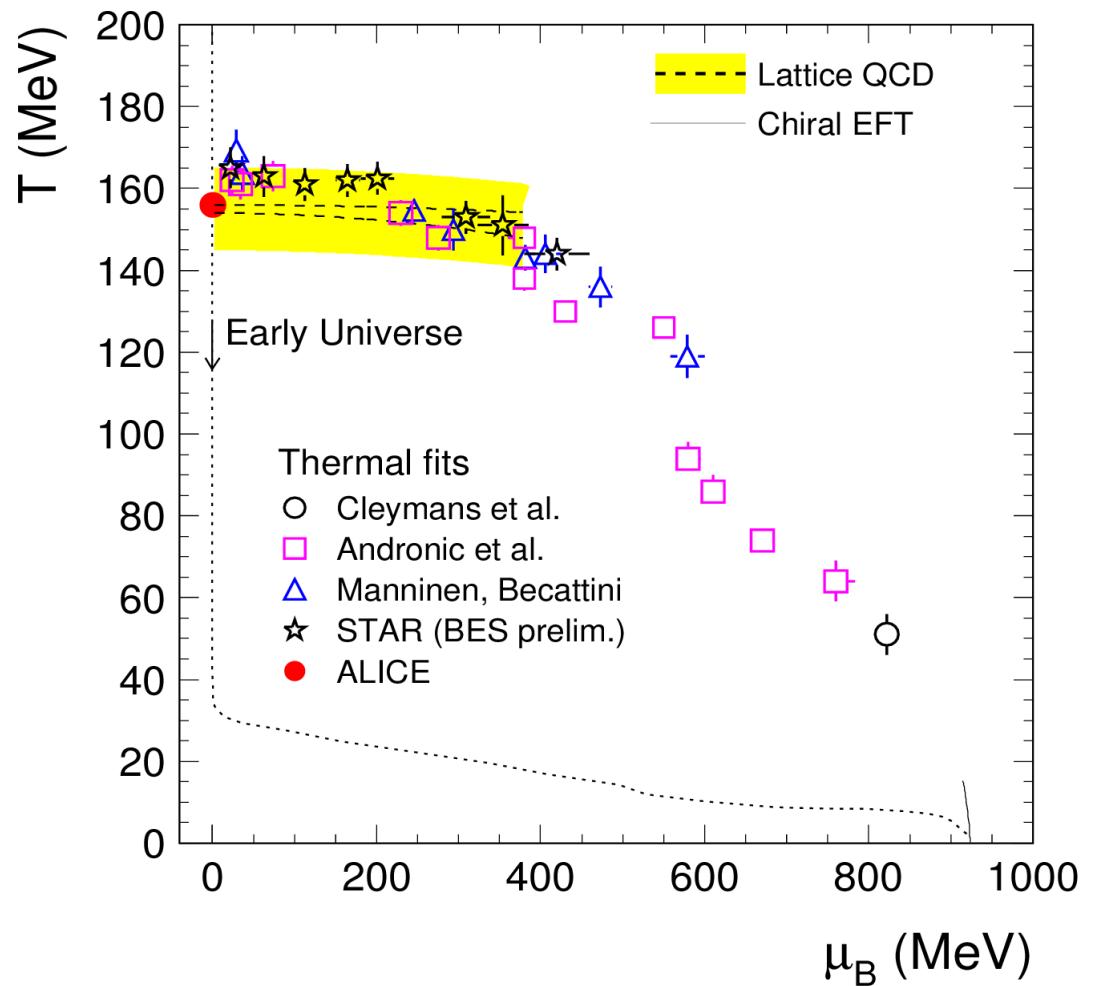
# Loosely bound states in PbPb collisions

PbPb central collisions: even Efimov-like states (hypertriton) produced with yields fixed at the phase boundary  
T 3 oom higher than Lambda separation energy



# The QCD phase diagram – experiment and lattice QCD

experimental hadronic freeze-out points coincide with pseudocritical temperature  $T_c$  from state-of-the-art lattice QCD for high collision energies

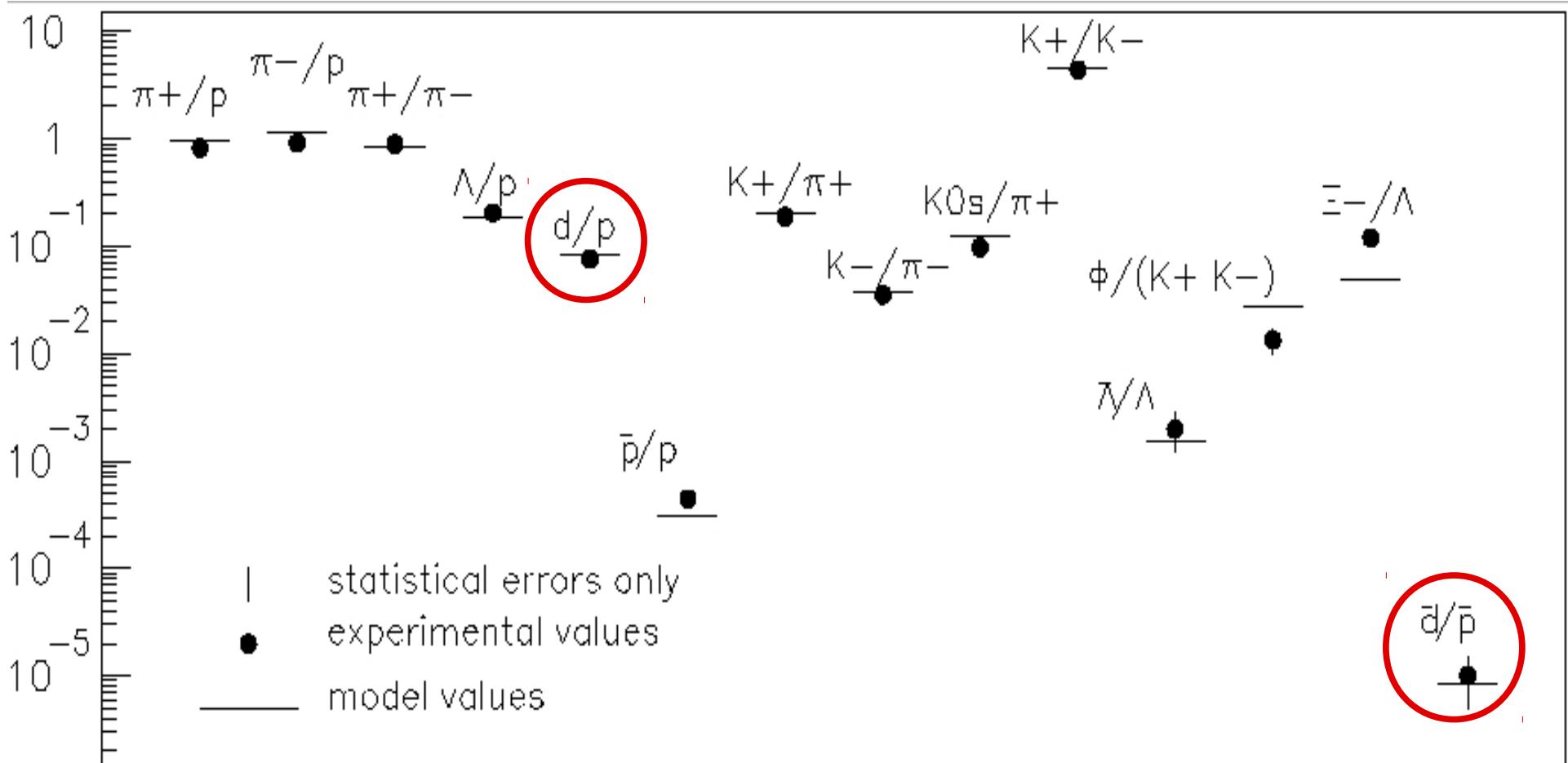


# Revisit formation of (anti-)nuclei

# first fit to AGS data – reproduces yields of d and dbar

14.6 A GeV/c central Si + Au collisions and GC statistical model

P. Braun-Munzinger, J. Stachel, J.P. Wessels, N. Xu, PLB 1994



dynamic range: 9 orders of magnitude! No deviation

# Should nuclei follow prediction of statistical hadronization at all?

Argument has been made, that coalescence is responsible for their formation and this is different mechanism

However: for system in thermal equilibrium, statistical ensemble and coalescence results agree

$d/p$  is given by entropy per baryon (see already Siemens and Kapusta  
PRL 43 (1979) 1486 -  $S/A \mu -\ln(d/p)$  )

while lightly bound nuclei may well be destroyed and built again during isentropic expansion, ratio of their abundance is frozen in by S/B and doesn't change

# for system in thermal equilibrium statistical and coalescence yields agree

P. Braun-Munzinger, J. Stachel, J. Phys. G21 (1995) L17

Particles	Thermal Model		A.J. Baltz, C.B. Dover, et al., Phys. Lett. B315 (1994) 7
	$T = .120 \text{ GeV}$	$T = .140 \text{ GeV}$	
d	15	19	11.7
t + $^3\text{He}$	1.5	3.0	0.8
$\alpha$	0.02	0.067	0.018
$H_0$	0.09	0.15	0.07
$^5_{\Lambda\Lambda}\text{H}$	$3.5 \cdot 10^{-5}$	$2.3 \cdot 10^{-4}$	$4 \cdot 10^{-4}$
$^6_{\Lambda\Lambda}\text{He}$	$7.2 \cdot 10^{-7}$	$7.6 \cdot 10^{-6}$	$1.6 \cdot 10^{-5}$
$^7_{\Xi^0\Lambda\Lambda}\text{He}$	$4.0 \cdot 10^{-10}$	$9.6 \cdot 10^{-9}$	$4 \cdot 10^{-8}$
$^{10}_1\text{St}^{-8}$	$1.6 \cdot 10^{-14}$	$7.3 \cdot 10^{-13}$	
$^{12}_1\text{St}^{-9}$	$1.6 \cdot 10^{-17}$	$1.7 \cdot 10^{-15}$	
$^{14}_1\text{St}^{-11}$	$6.2 \cdot 10^{-21}$	$1.4 \cdot 10^{-18}$	
$^{16}_2\text{St}^{-13}$	$2.4 \cdot 10^{-24}$	$1.2 \cdot 10^{-21}$	
$^{20}_2\text{St}^{-16}$	$9.6 \cdot 10^{-31}$	$2.3 \cdot 10^{-27}$	

# Production of light nuclei and antinuclei at the AGS

data cover 10 oom!

addition of every nucleon

-> penalty factor  $R_p = 48$

but data are at very low  $p_T$

use  $m$ -dependent slopes following systematics up to deuteron

->  $R_p = 26$

GC statistical model:

$$R_p \propto \exp [(\mu_n - \mu_b) / T]$$

for  $T=124$  MeV and  $\mu_b = 537$  MeV

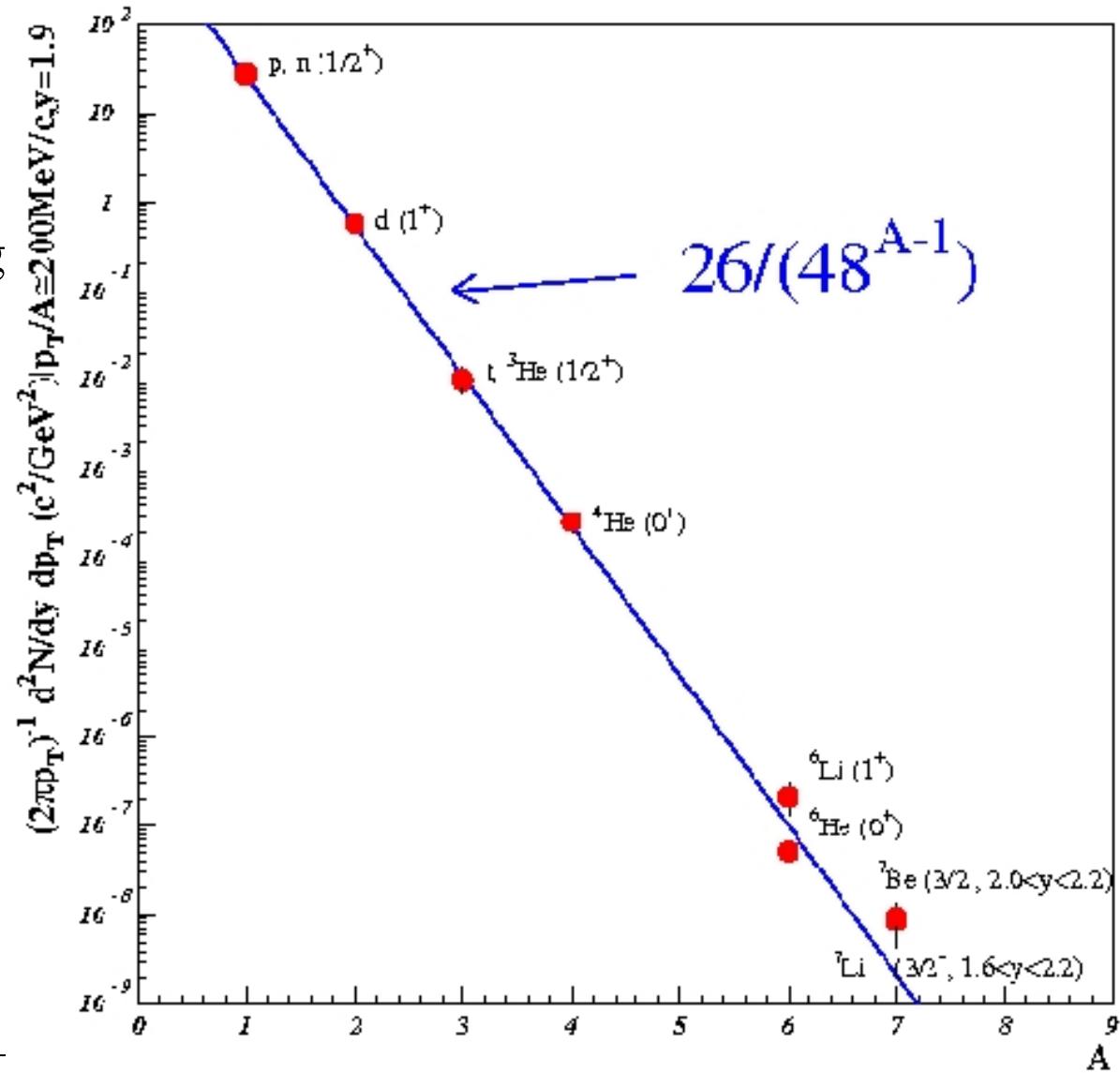
$R_p = 24$  good agreement

also good for **antideuterons**:

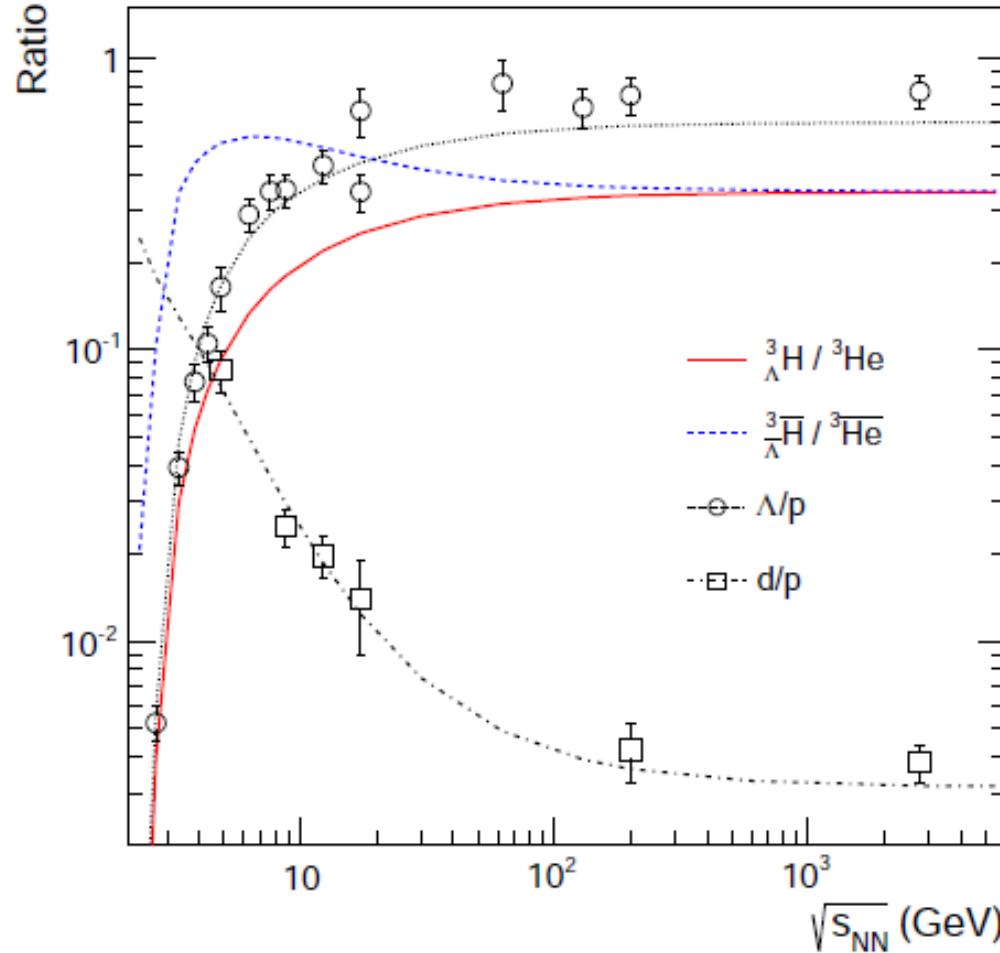
data:  $R_p = 2 \pm 1 \cdot 10^5$  SM:  $1.3 \cdot 10^5$

P. Braun-Munzinger, J. Stachel,  
J. Phys. G28 (2002) 1971

E864 Coll., Phys. Rev. C61 (2000) 064908



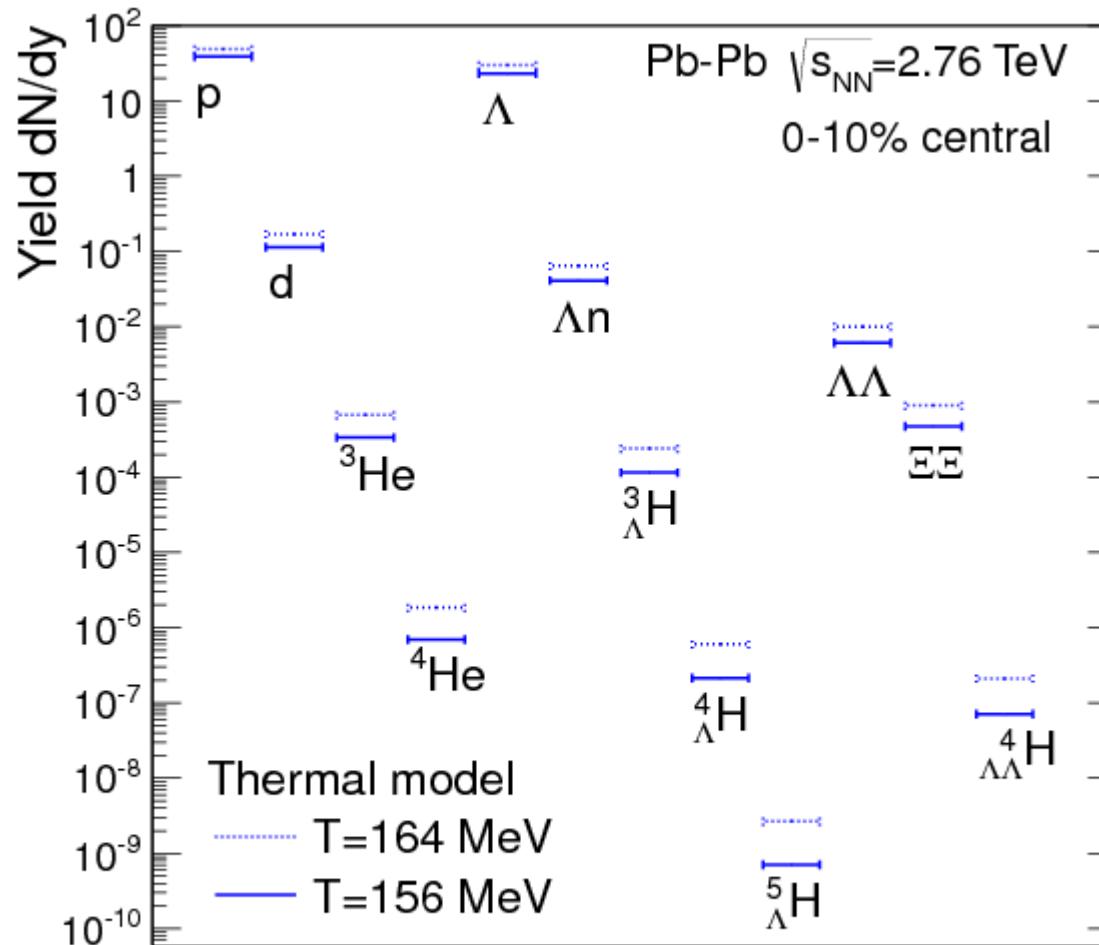
# energy dependence of d/p ratio and thermal model prediction



agreement of data from Bevalac/SIS energies up to LHC  
with thermal model prediction

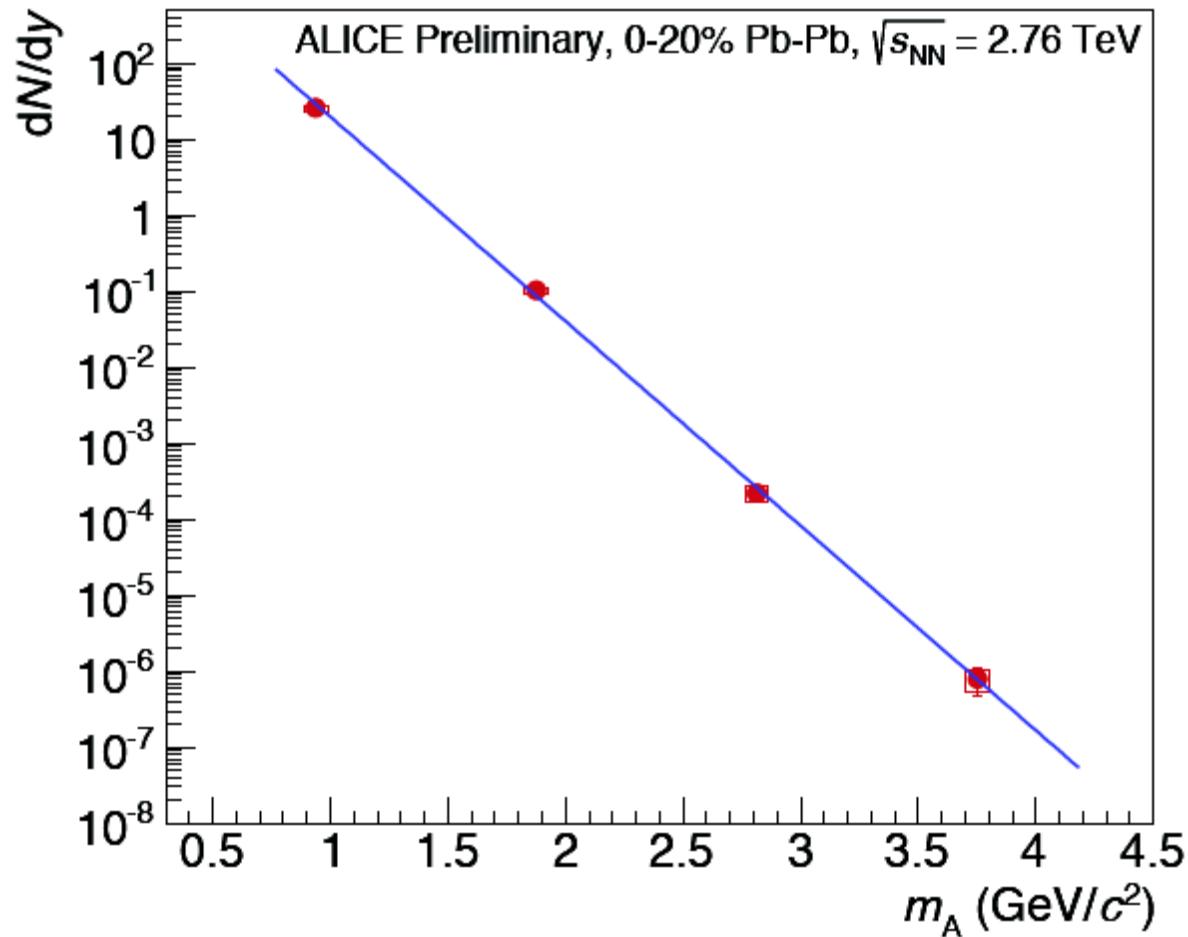
A. Andronic, P. Braun-Munzinger, J.S., H. Stöcker, PLB697 (2011)203

# Predictions for nuclei and hypernuclei and exotica



values for  $^4\text{He}$ ,  $^3\text{He}$  and  $^3\Lambda\text{H}$  were predictions and are in excellent agreement with new data from ALICE  
test of statistical hadronization model over another 3 orders of magnitude

# Production of light anti-nuclei at LHC energy



penalty factor  $\exp(-m/T) \approx 300$

# a direct comparison of LHC data and lattice QCD

fluctuations of conserved charges (baryon number, strangeness, charge) sensitive to criticality related to spontaneous breaking of chiral symmetry

$$\frac{\chi_N}{T^2} = \frac{\partial^2 \hat{P}}{\partial \hat{\mu}_N^2} \quad \frac{\chi_{NM}}{T^2} = \frac{\partial^2 \hat{P}}{\partial \hat{\mu}_N \partial \hat{\mu}_M}$$

with  $\hat{P} = P/T^4$ ,  $\hat{\mu}_N = \mu_N/T$  and  $N, M = (B, S, Q)$

- exhibit characteristic properties governed by universal part of free energy in 1QCD chiral transition in O(4) critical region  
**can we see signs of this criticality in experimental data?**
- direct measurement of higher moments of fluctuations of conserved charges very challenging, for LHC under way (very statistics hungry!)
- 2nd order cumulants of conserved charges can be obtained from measured inclusive distributions in case probability distribution of number of particles and antiparticles are Poissonian and uncorrelated

# Fluctuations of net charges

susceptibilities of a conserved charge related to variance of net charge distribution

$$\hat{\chi}_N = \frac{1}{VT^3} (\langle N^2 \rangle - \langle N \rangle^2)$$

if e.g. baryon and antibaryon distributions are Poisson, the net baryon distribution is a Skellam distribution

variance of Skellam distribution given by mean of total number of baryons + antibaryons

$$\frac{\chi_N}{T^2} = \frac{1}{VT^3} (\langle N_q \rangle + \langle N_{-q} \rangle)$$

can be directly computed from measured ALICE data using rapidity densities of measured baryon and antibaryon yields:

$$\begin{aligned} \frac{\chi_B}{T^2} \simeq & \frac{1}{VT^3} [\langle p \rangle + \langle N \rangle + \langle \Lambda + \Sigma^0 \rangle + \langle \Sigma^+ \rangle + \langle \Sigma^- \rangle \\ & + \langle \Xi^- \rangle + \langle \Xi^0 \rangle + \langle \Omega^- \rangle + \text{antiparticles}], \end{aligned}$$

and equivalent for strangeness using strange hadron yields or electric charge/strangeness correlations using charged strange hadron yields

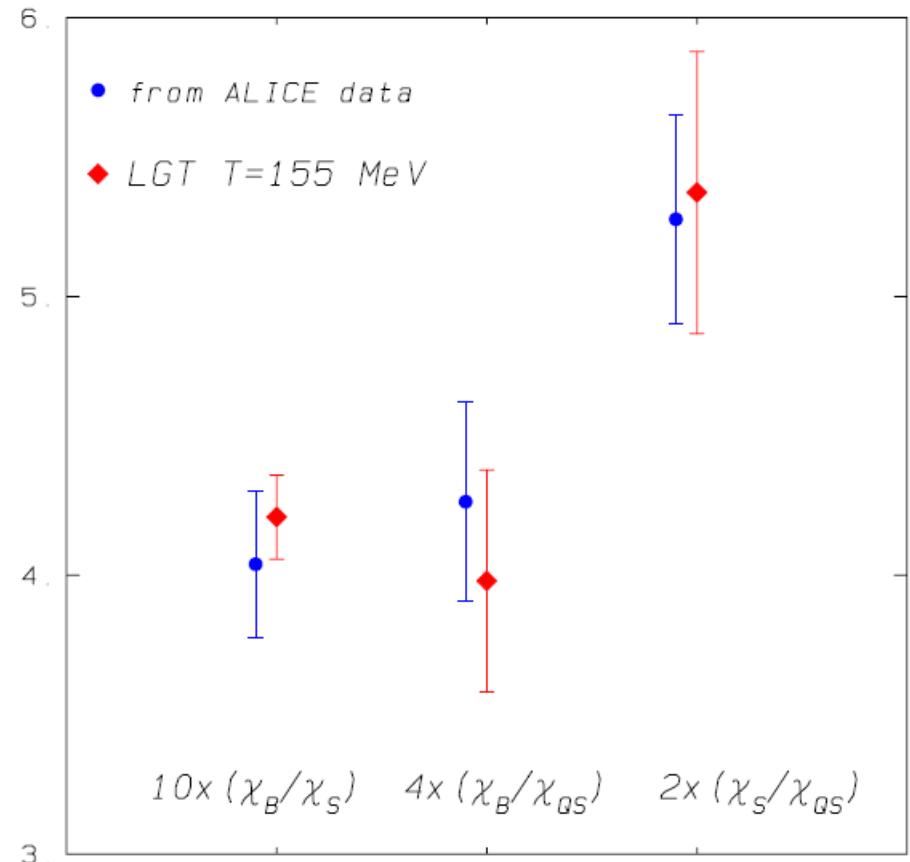
# Comparison chiral susceptibilities data and lQCD

ALICE data:

$$\frac{\chi_B}{T^2} \simeq \frac{1}{VT^3} (203.7 \pm 11.4)$$
$$\frac{\chi_S}{T^2} \simeq \frac{1}{VT^3} (504.2 \pm 16.8)$$
$$\frac{\chi_{QS}}{T^2} \simeq \frac{1}{VT^3} (191.1 \pm 12).$$

- in ratios of susceptibilities volume and temperature drop out
- compare to lattice QCD at pseudo-critical temperature for  $\mu_b = 0$  and extrapolated to continuum limit

A.Basavov et al., PRL 113 (2014) 072001 and PRD 86 (2012) 034509

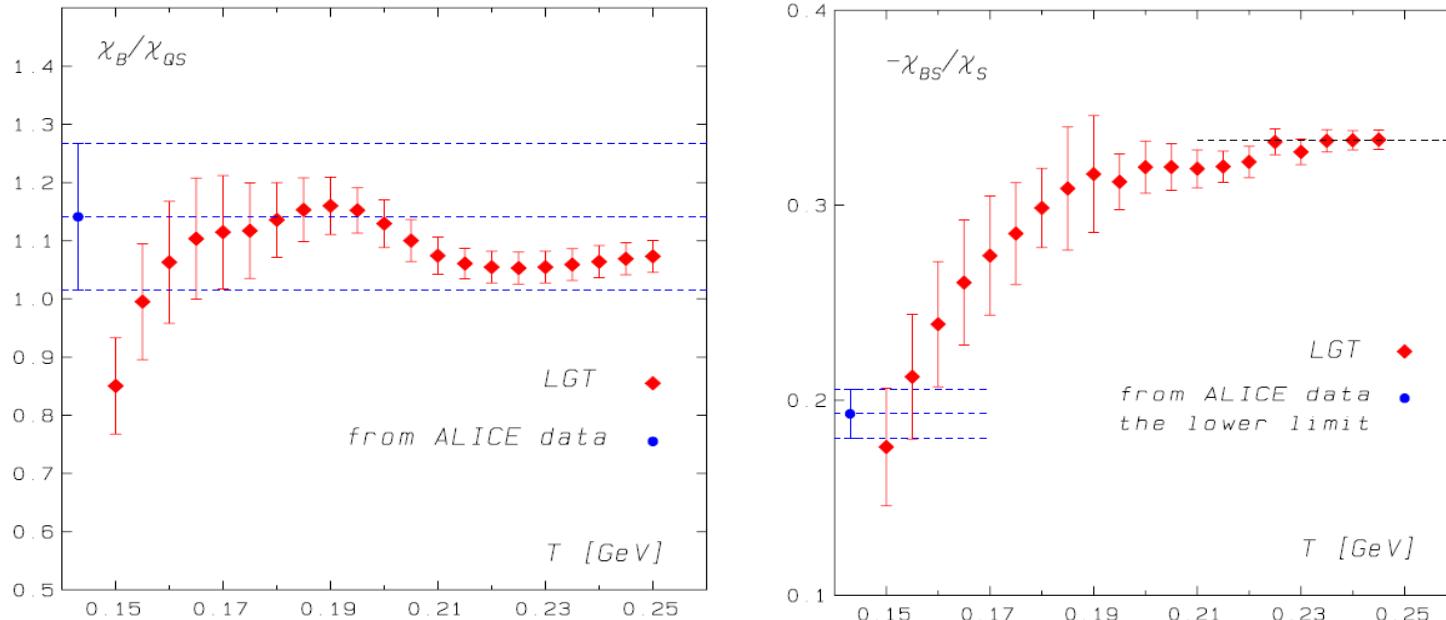


very good agreement data and lQCD

strongly suggests: fluctuations are of thermal origin and indeed established at the phase boundary

# Can one limit temperature range by comparison to data?

evaluate susceptibilities from lQCD for a range of temperatures and compare to data



combination of these two plots:  $T > 150$  MeV and  $T < 165$  MeV  
and independently: for  $T > 163$  MeV, lQCD thermodynamics cannot be described  
by hadronic degrees of freedom (Karsch 2014)

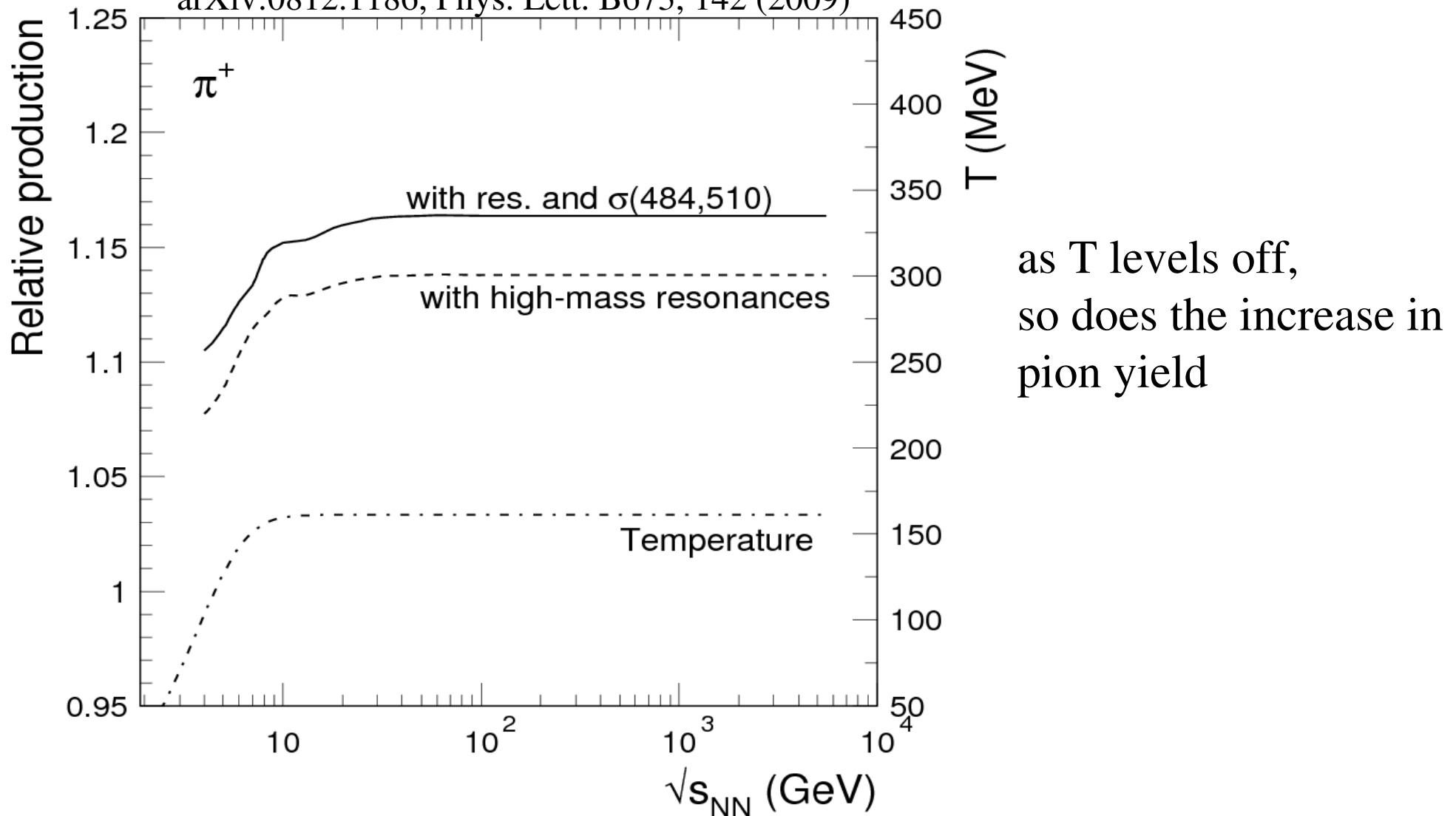
## summary

- good knowledge of QCD phase diagram from lattice QCD close to  $\mu_b=0$
- comprehensive set of data on hadron yields from AGS to LHC energies  
data consistent with QCD statistical operator over 9 oom, chemical freeze-out very close to pseudocritical temperature from lQCD
- same pictures applies to the formation of (anti-)nuclei and hypernuclei
- fluctuations of conserved charges: linked to mean multiplicities  
values consistent with lQCD, indicative of thermal fluctuations at phase boundary

# backup

## relative change in pion yield with more high mass resonances and the $\sigma$

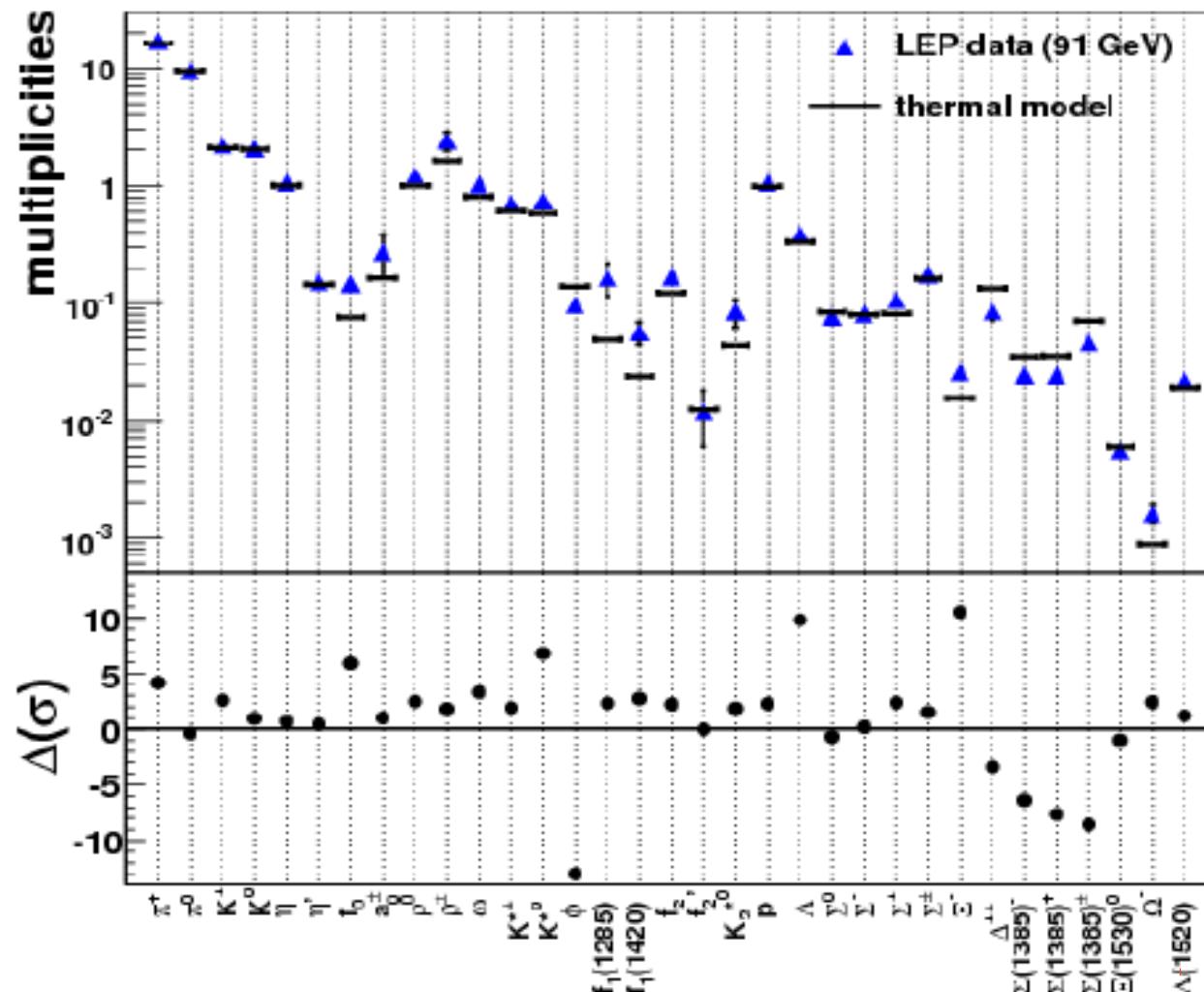
A. Andronic, P. Braun-Munzinger, J. Stachel,  
arXiv:0812.1186, Phys. Lett. B673, 142 (2009)



# e+e- collisions: initialize thermal model with u,d,s,c,b – jets according to measurement (weak isospin)

A. Andronic, P. Braun-Munzinger, F. Beutler, K. Redlich, J. Stachel, Phys. Lett. B678 (2009)

arXiv 0804.4132

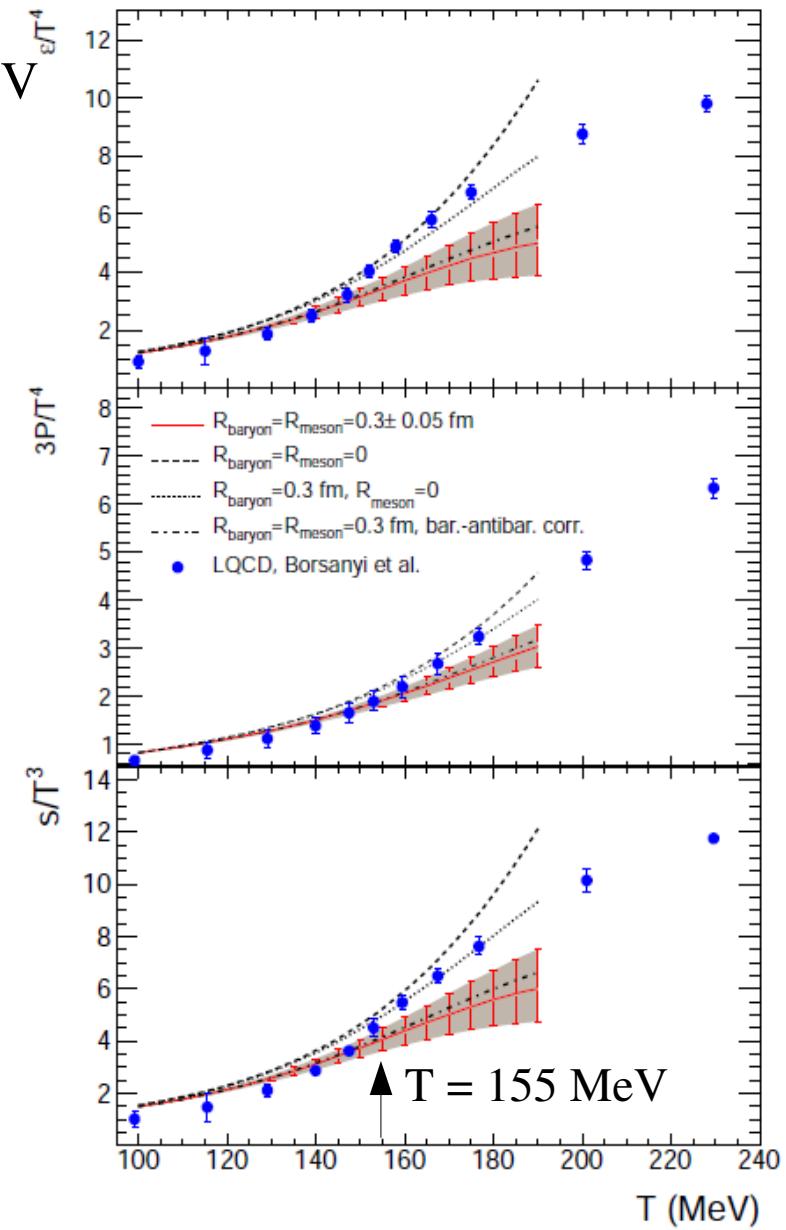
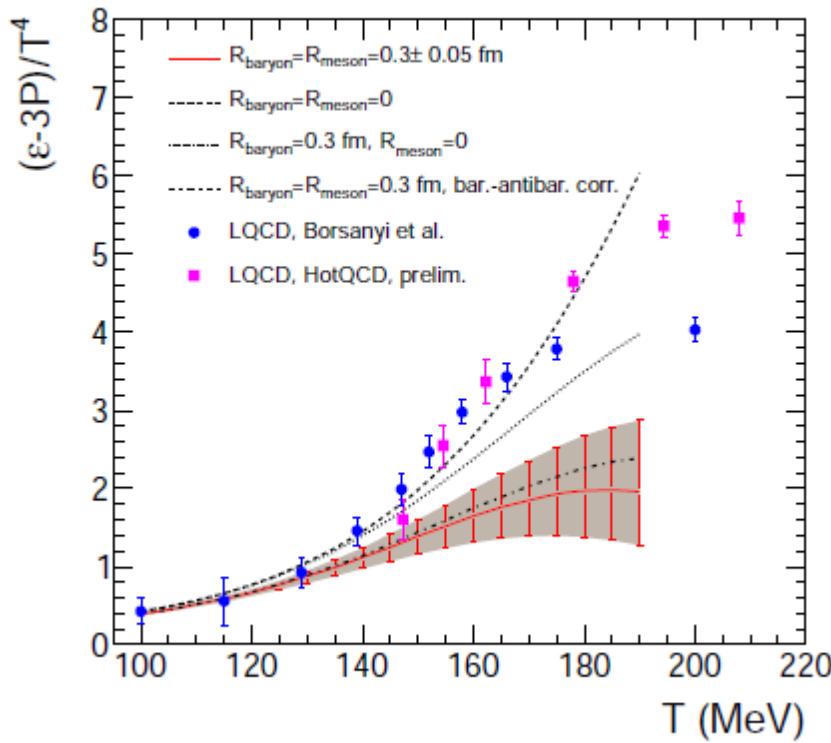


strangeness  
supressed – fit  
still not good!

parameter set:  $T=164 \text{ MeV}$ ,  $V=20 \text{ fm}^3$ ,  $\gamma_s=0.72$  with  $\chi^2=718/30$

# Lattice QCD and various hadron resonance gas predictions for thermodynamic quantities

interactions become visible around  $T = 140$  MeV  
but no well constrained; modeled here with  
excluded volumes



Andronic, Braun-Munzinger, JS, Winn,  
Phys. Lett. B718 (2012) 80

# top AGS energy Au + Au data

GC statistical model applied first time successfully to 10.7 A GeV/c Au + Au collisions P. Braun-Munzinger, J.S., J.P. Wessels, N.Xu, Phys. Lett. B344 (1995) 43

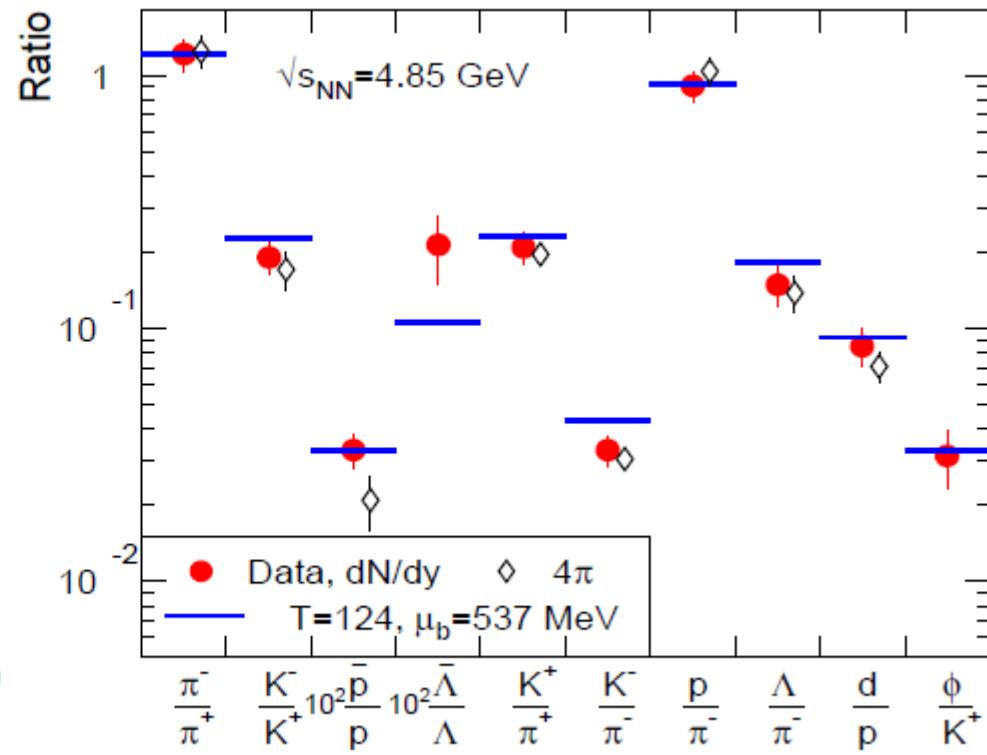
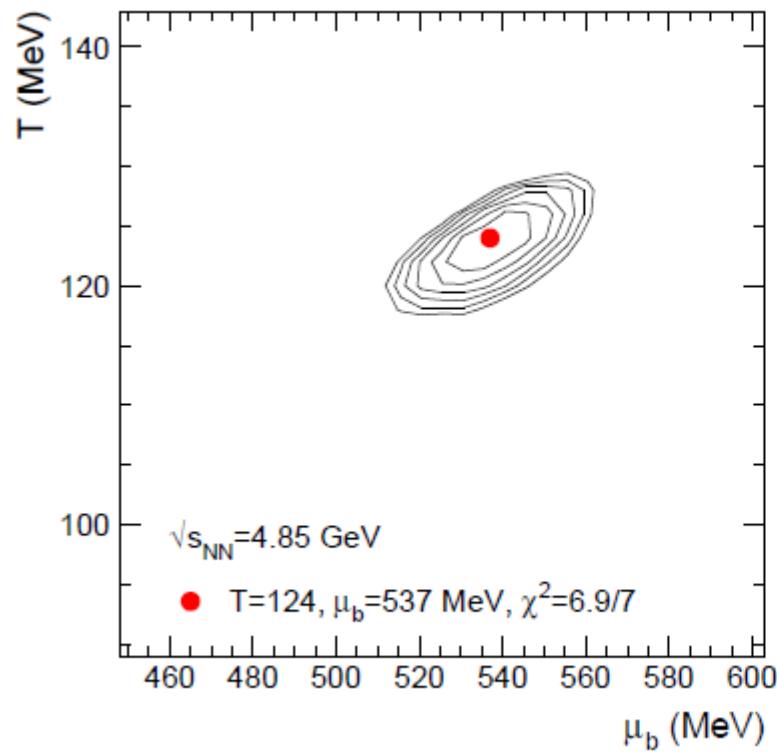
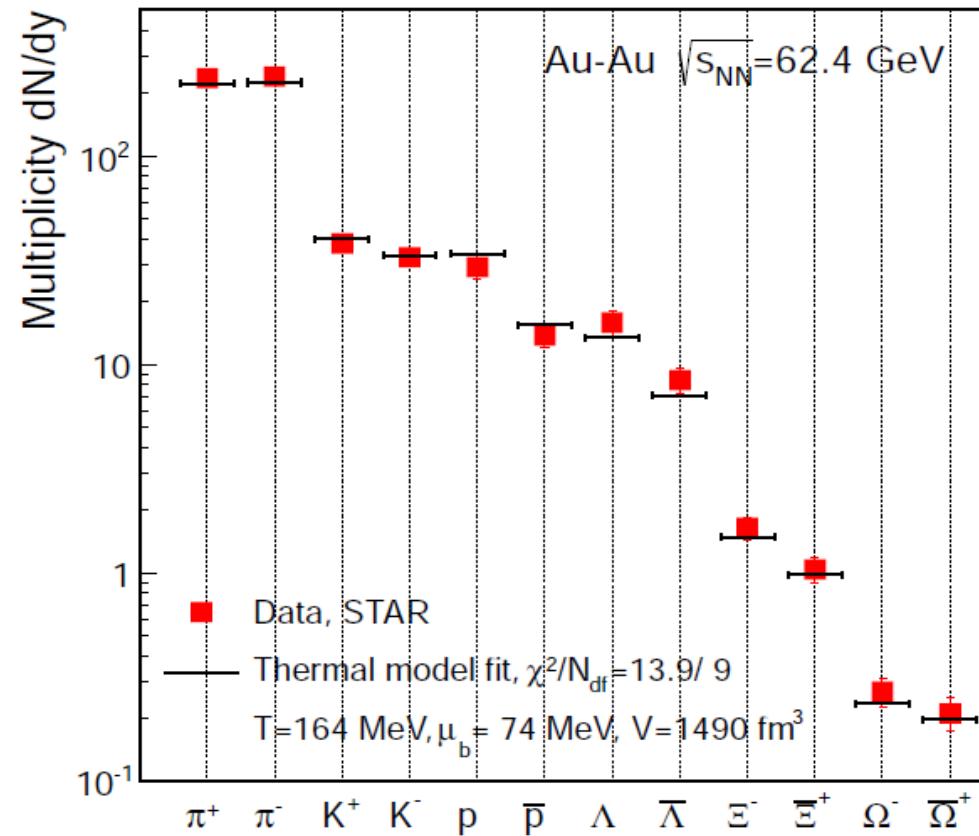
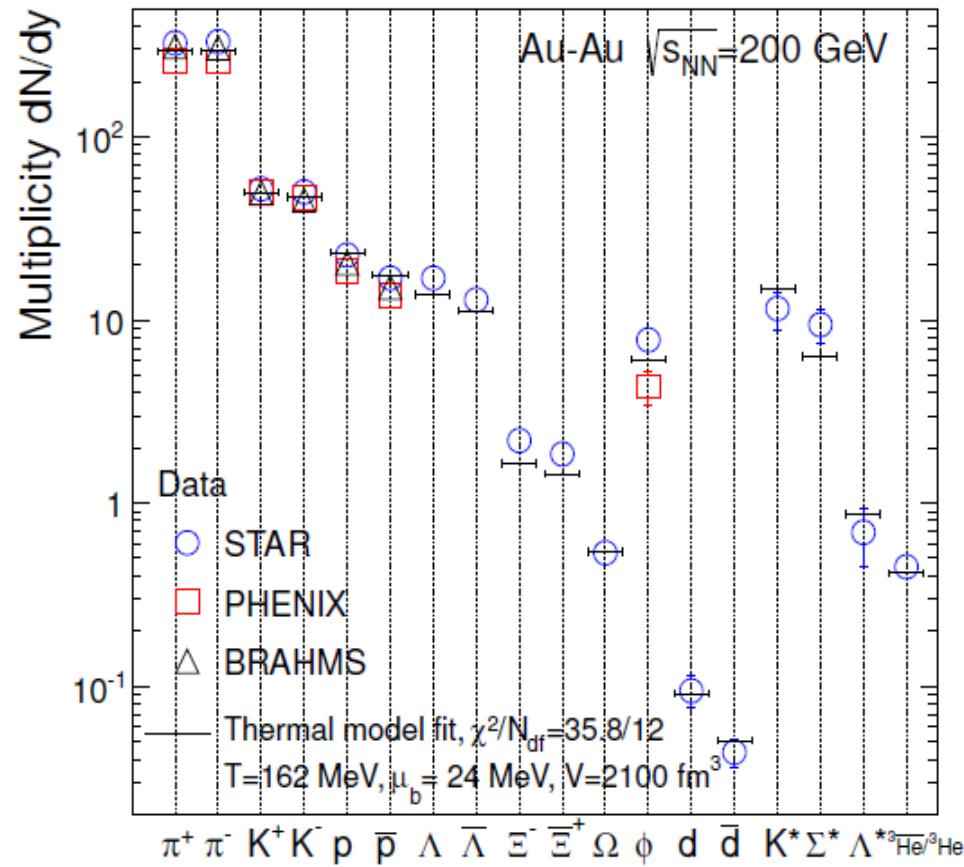


Figure from A. Andronic, P. Braun-Munzinger, J.S. Nucl. Phys. A772 (2006) 167

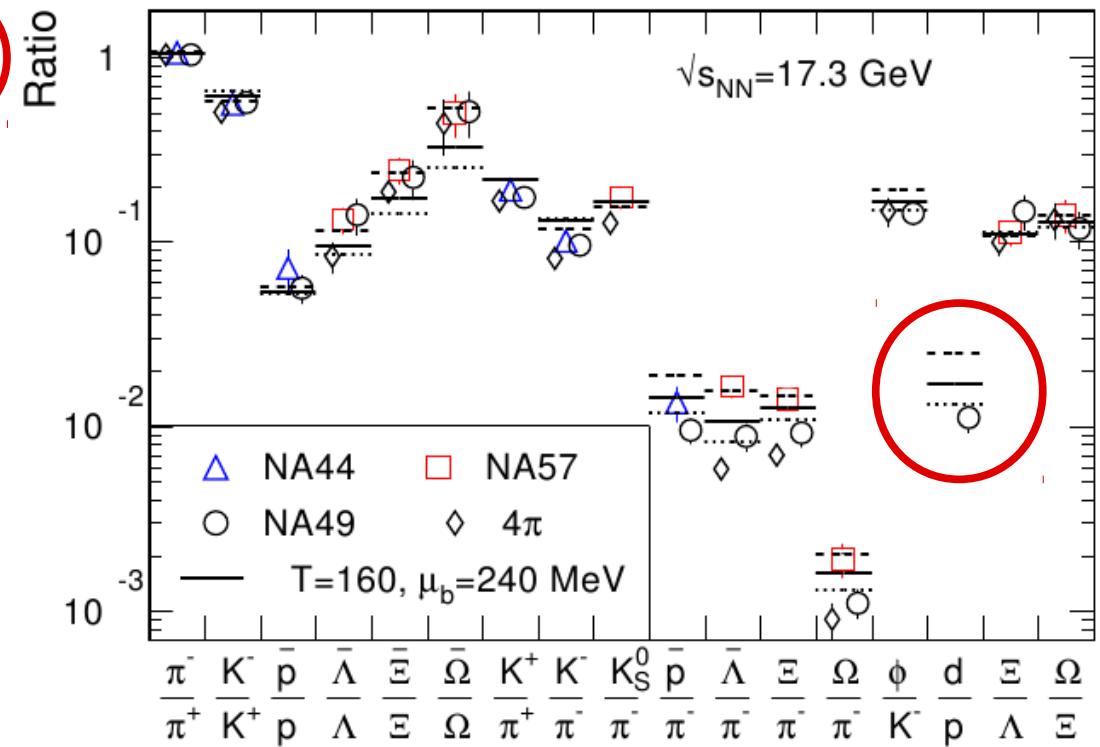
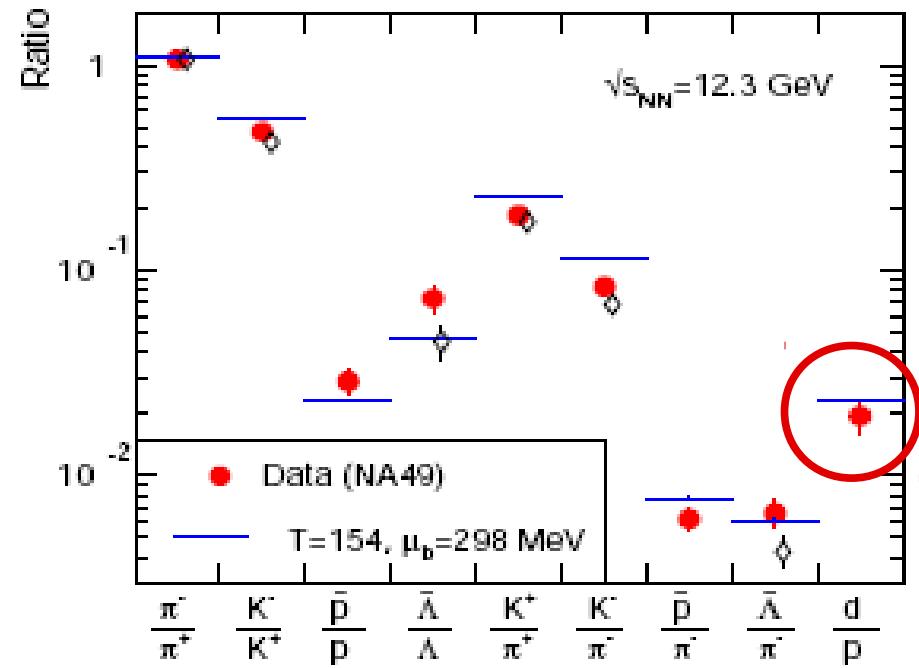
# lower RHIC energies, - STAR data only



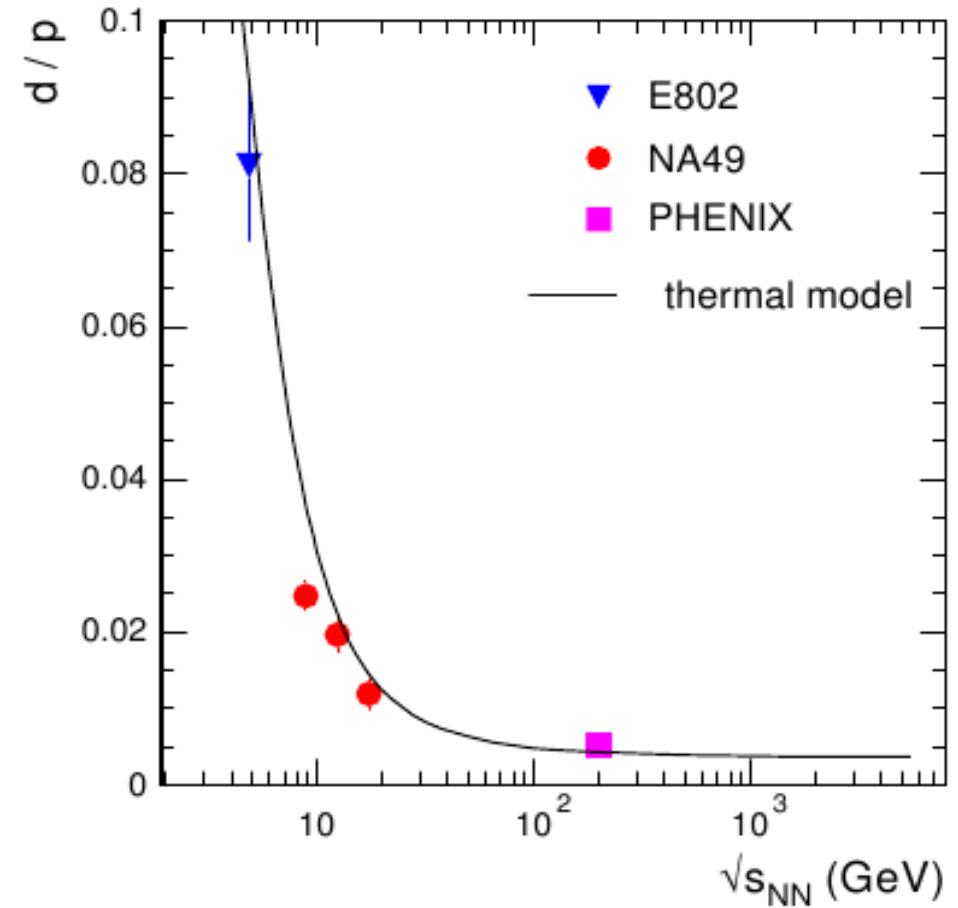
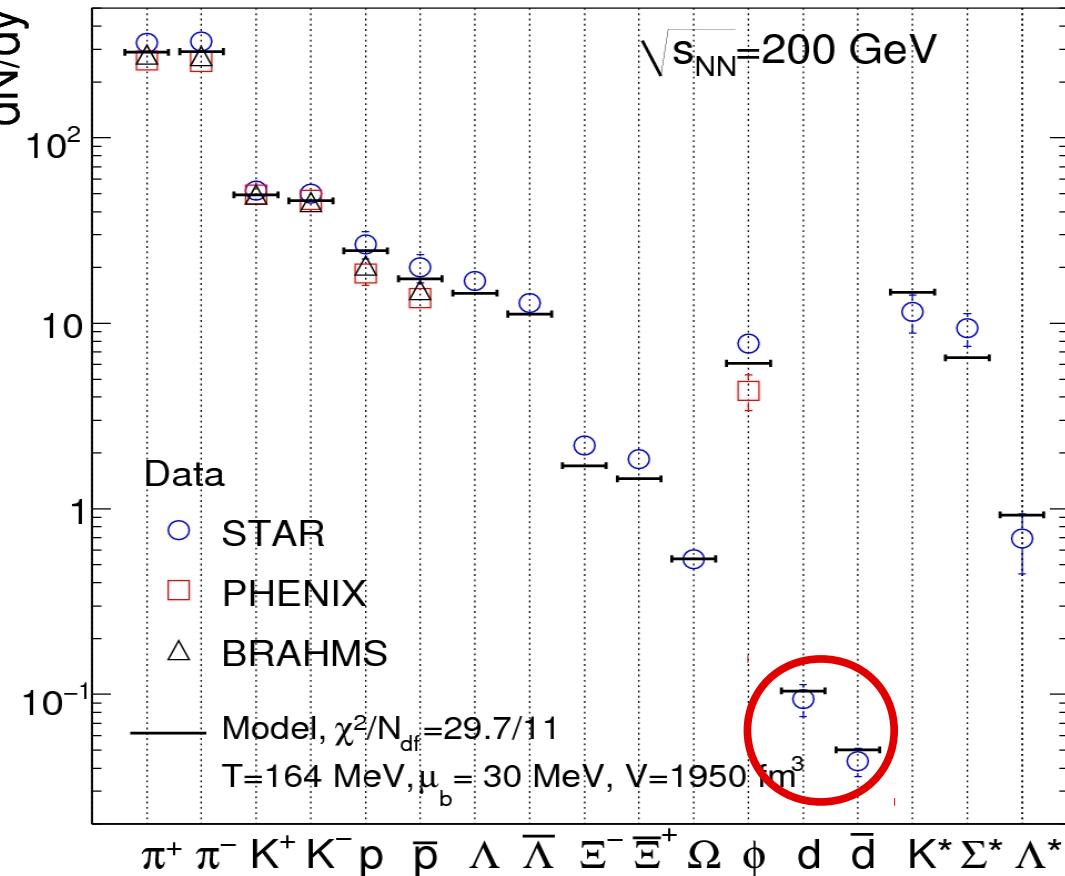
# Latest statistical model fit to all RHIC data



# Deuterons at SPS energies reproduced as well

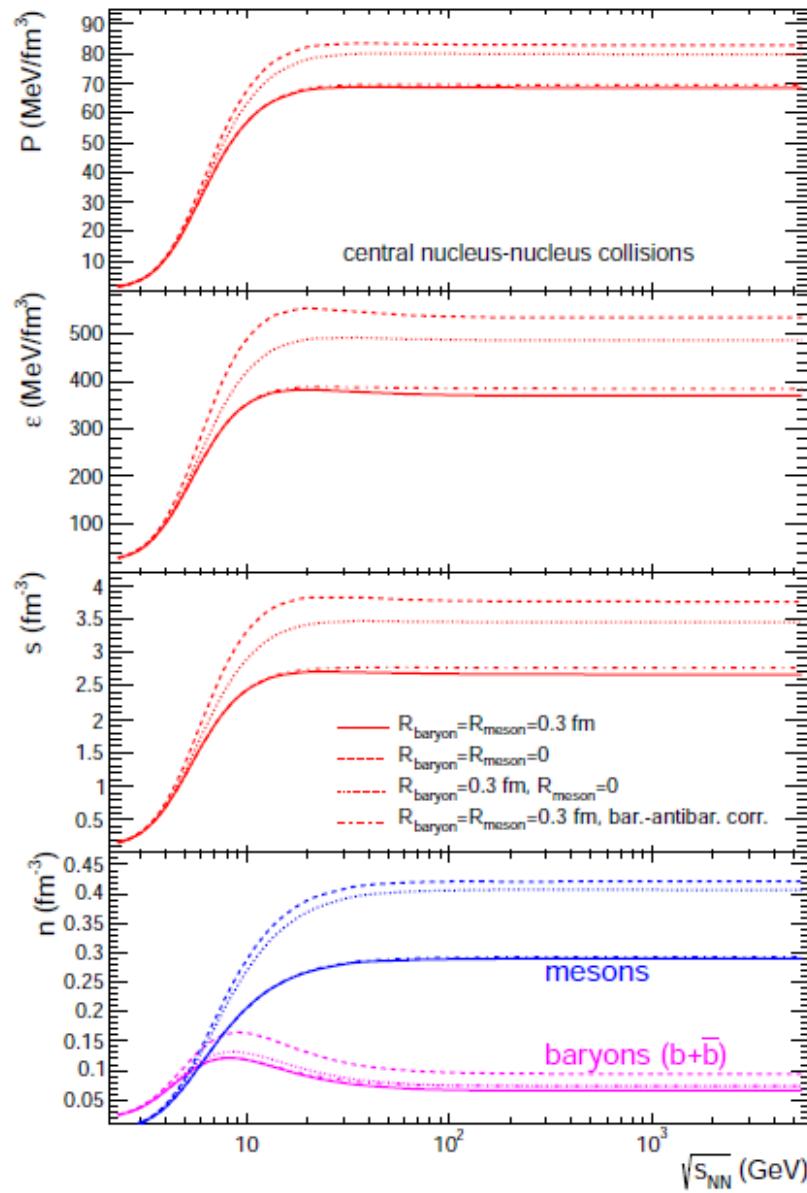


and at RHIC description equally good  
 - beam energy dependence driven by  $\mu_b$



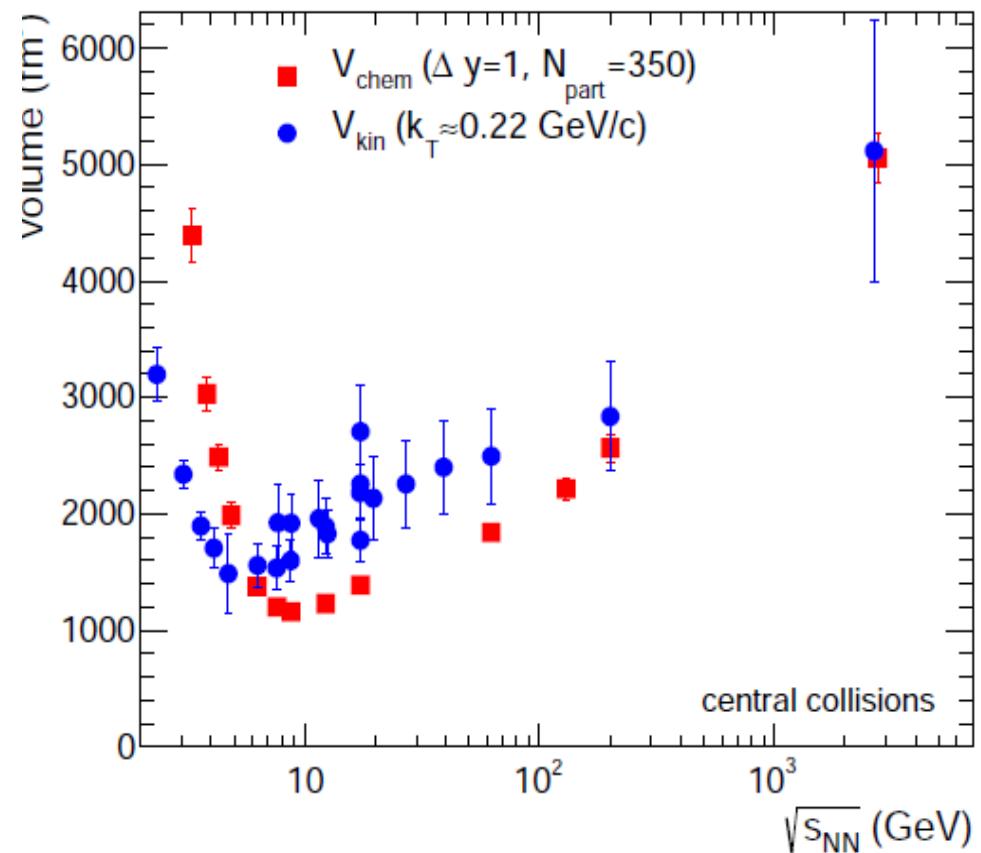
# Cluster production and entropy

$$S = s V = \text{const} \ln(d/n)$$

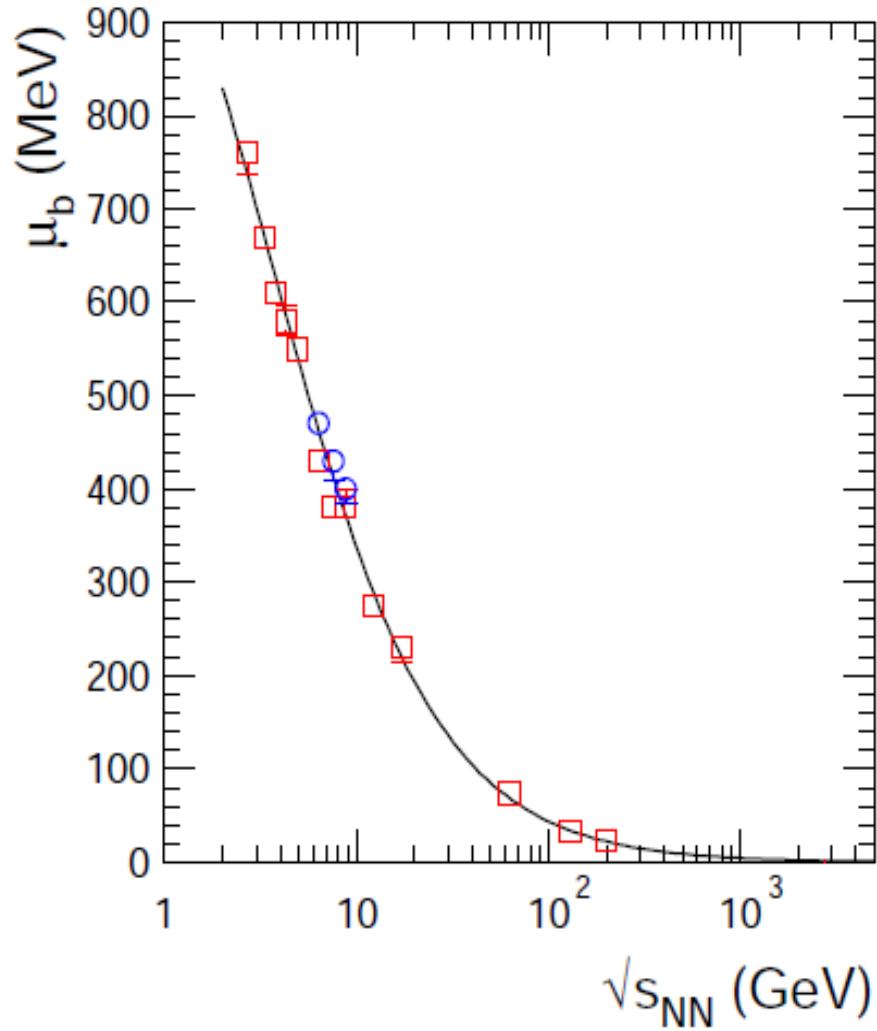
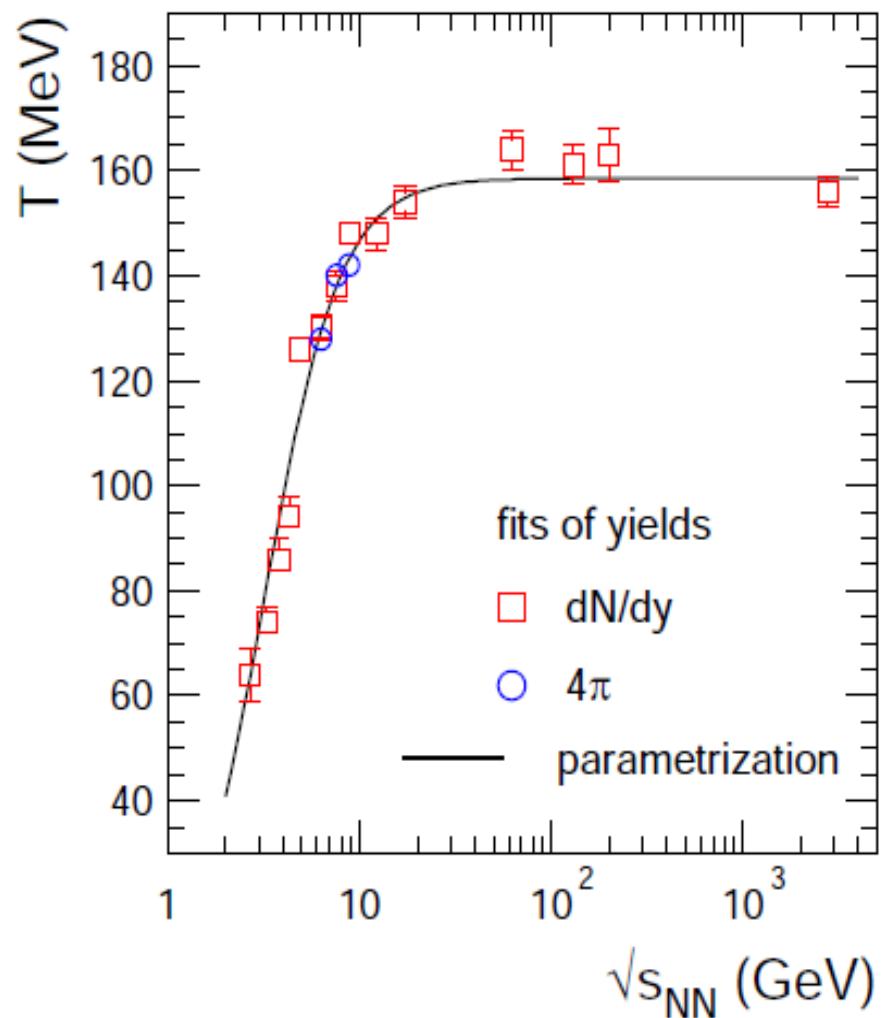


Interacting hadronic source gas meets lattice QCD  
[arXiv:1201.0693](https://arxiv.org/abs/1201.0693)

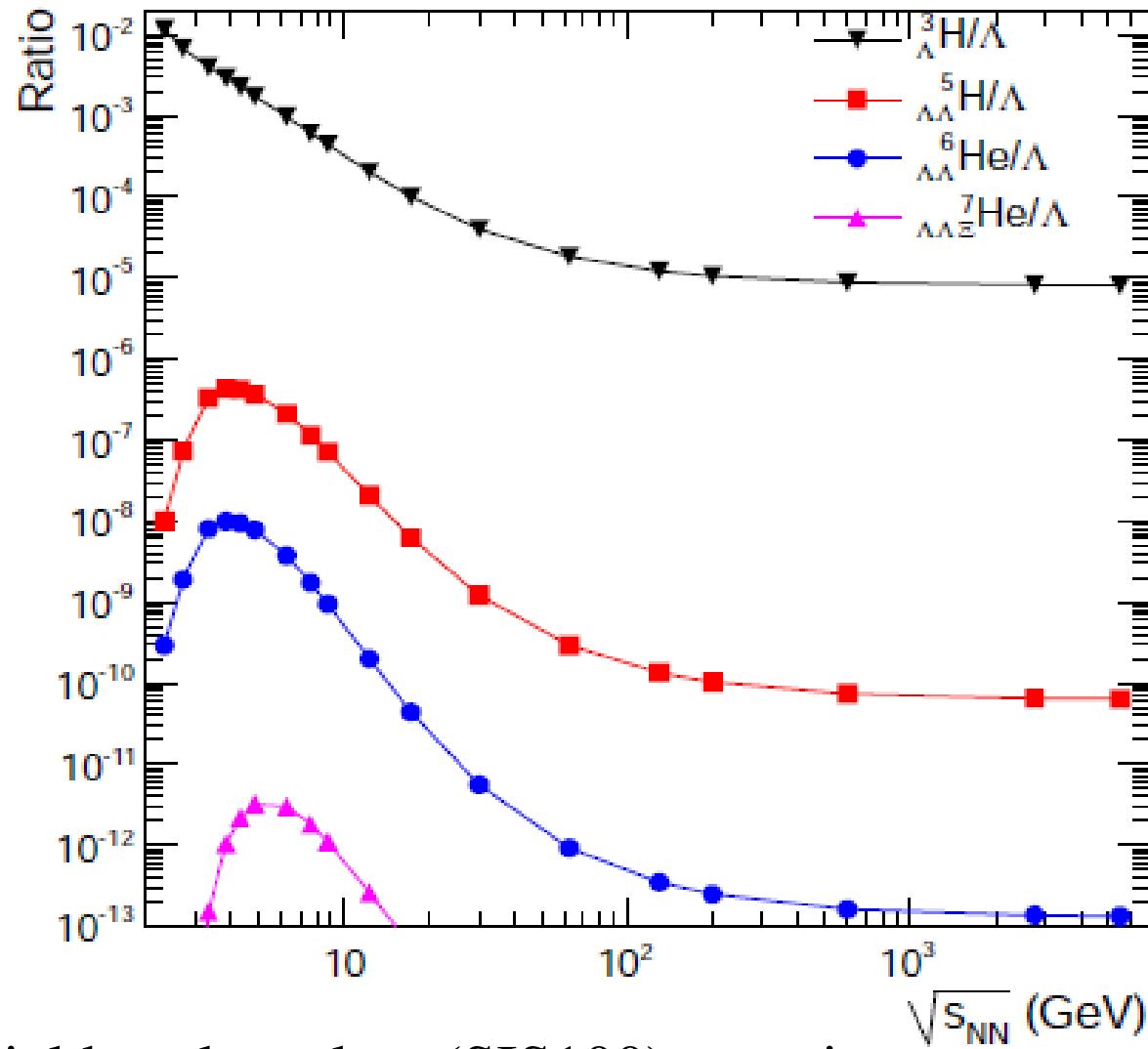
A. Andronic <sup>a,b</sup>, P. Braun-Munzinger <sup>a,c,d,e</sup>, J. Stachel <sup>f</sup>,  
M. Winn <sup>f</sup>



# Latest global fit to T and m<sub>b</sub>



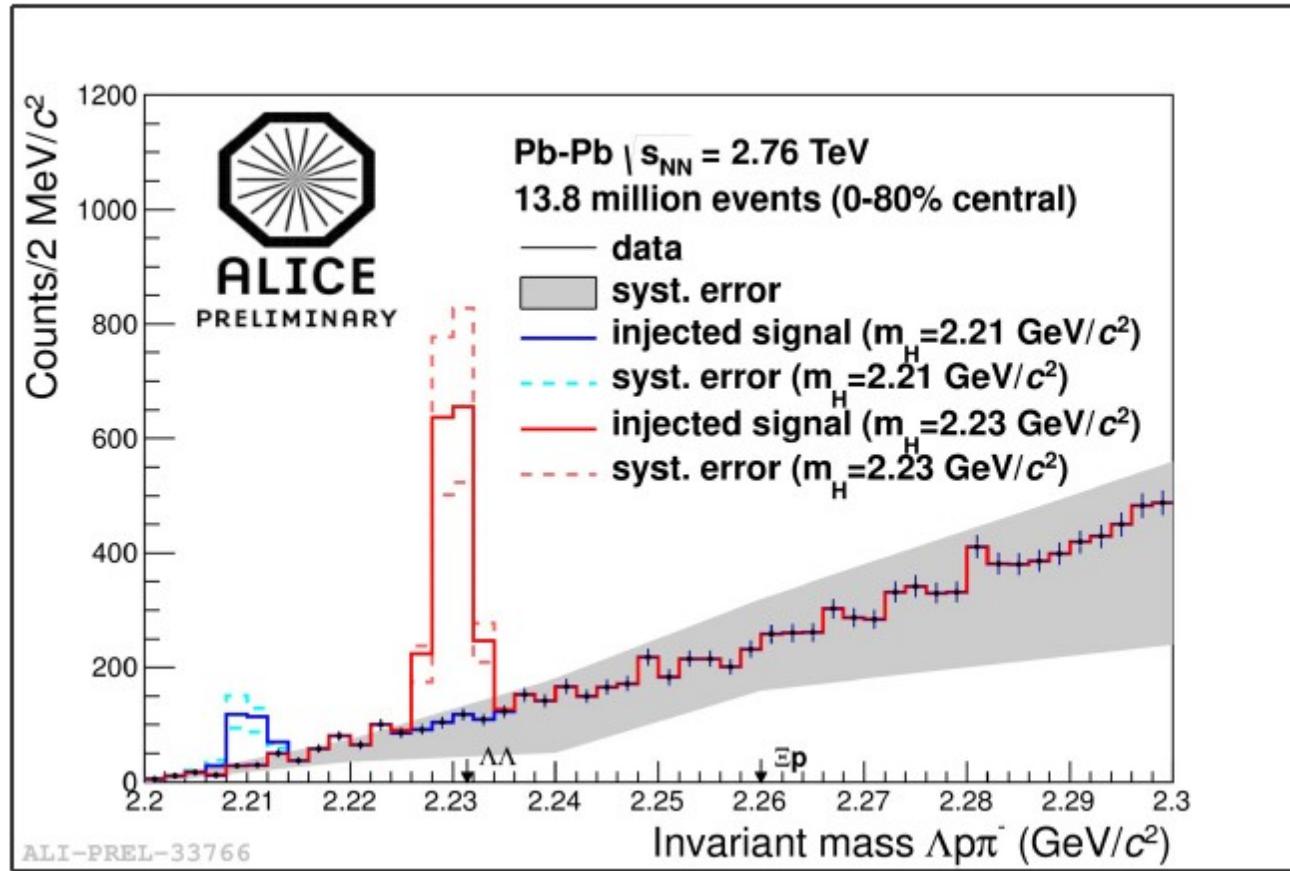
# Energy dependence of the yields of exotic objects



note: yield peaks at low (SIS100) energies  
an exciting but tough prospect for FAIR

# example: search for H-Dibaryon

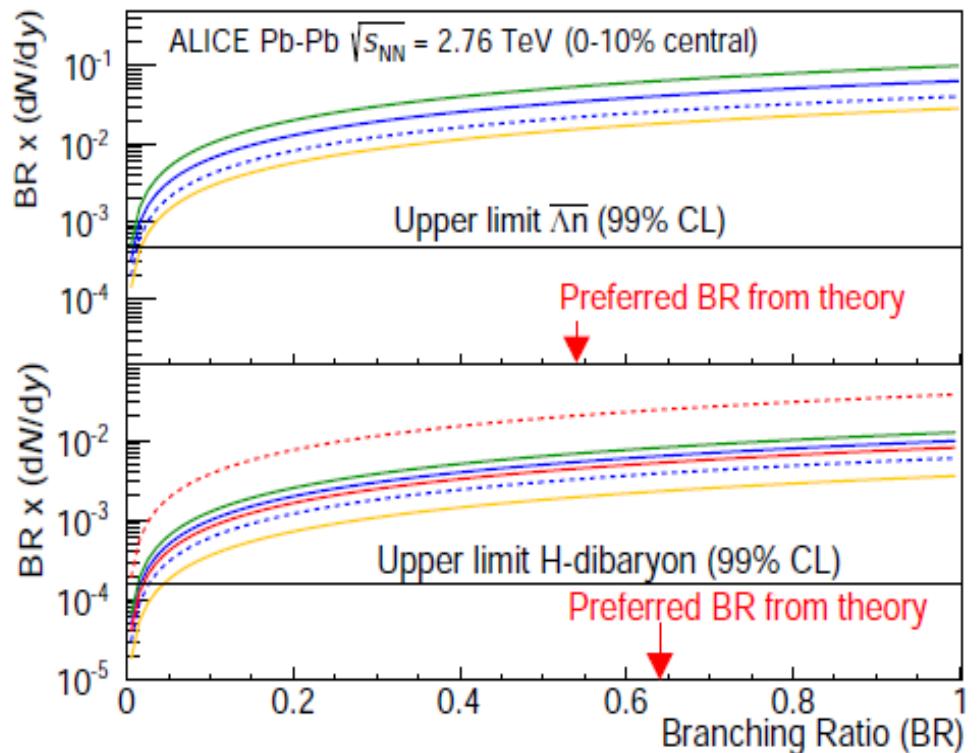
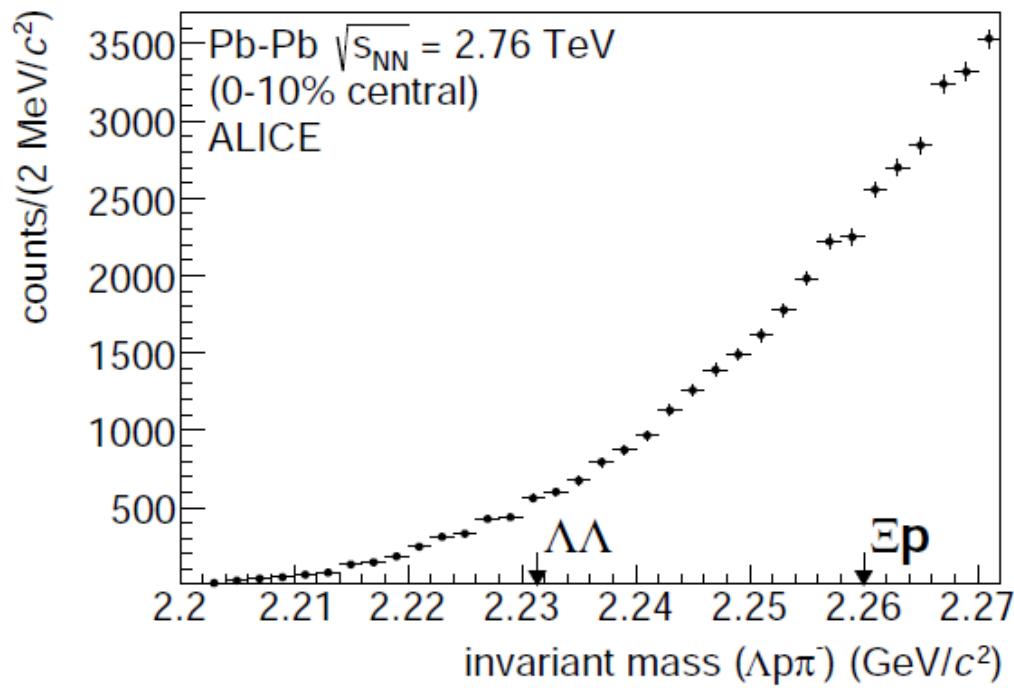
Ramona Lea, SQM2013



No signal observed, H yield is < 0.1 x (thermal model prediction)  
Much more stringent limits to come soon

# searches for exotic bound states

Nicole Martin and Benjamin Doenigus, ALICE



no H, Lambda-n bound states

arXiv:1506.07499

# possible reasons for low proton yield

Incomplete hadron spectrum

Annihilation in the hadronic phase

Non-equilibrium scenario with new parameters  
other?

# Effect of incomplete hadron spectrum

we studied this for  $K/\pi$  ratio:

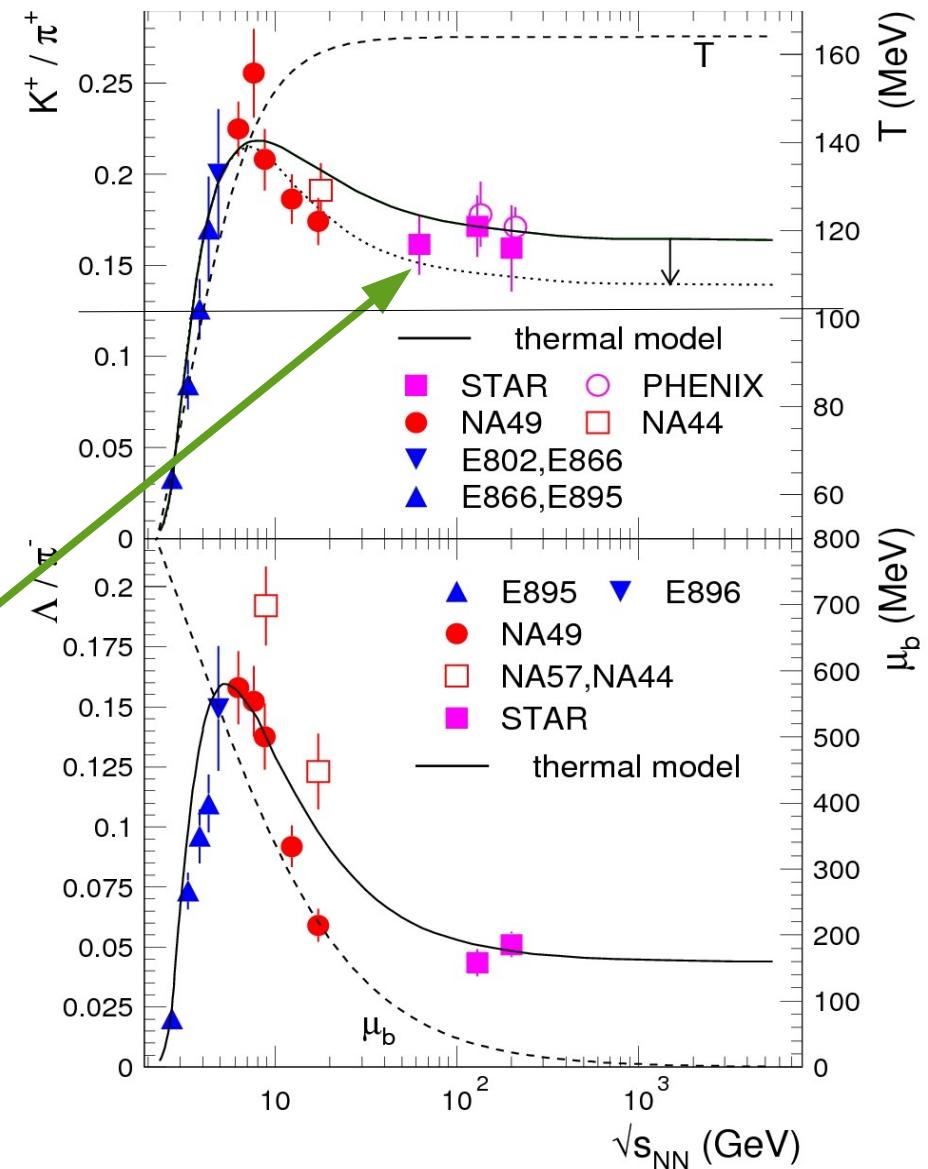
(Andronic, Braun-Munzinger, JS Phys. Lett. B673 (2009) 142)

estimate effect by extending mass spectrum beyond 3 GeV based on  $TH = 200$  MeV and assumption how states decay

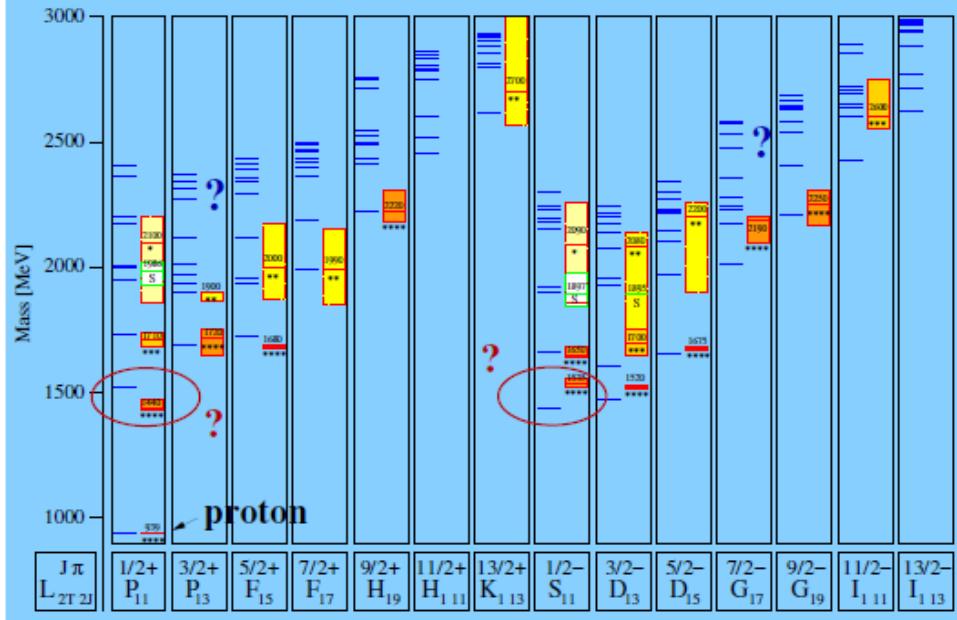
strongest contribution to kaon from  $K^*$  producing one K

all high mass resonances produce multiple pions

-> further reduction of  $K^+/\pi^+$



there could be a lot more unfound baryons at low mass  
and with high spin (degeneracy)



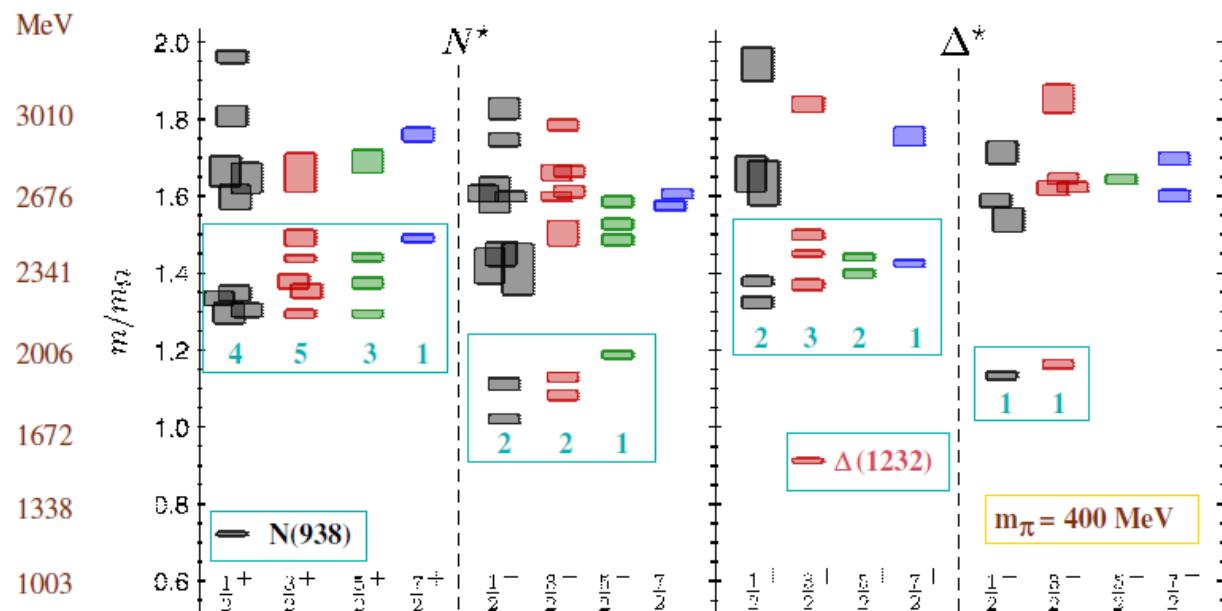
from talk U. Thoma DPG2013

non-strange  $N^*$  resonances

U. Loering, B. Metsch, H. Petry et al.

relativistic quark model

Constituent quarks, confinement potential  
+ residual interaction



# annihilation in the hadronic phase?

F. Becattini et al., Phys. Rev. C85 (2012) 044921 and arXiv: 1212.2431  
Evaluate hadronic interactions after statistical hadronization using RQMD  
find significant effect of apparent cooling due to hadron rescattering

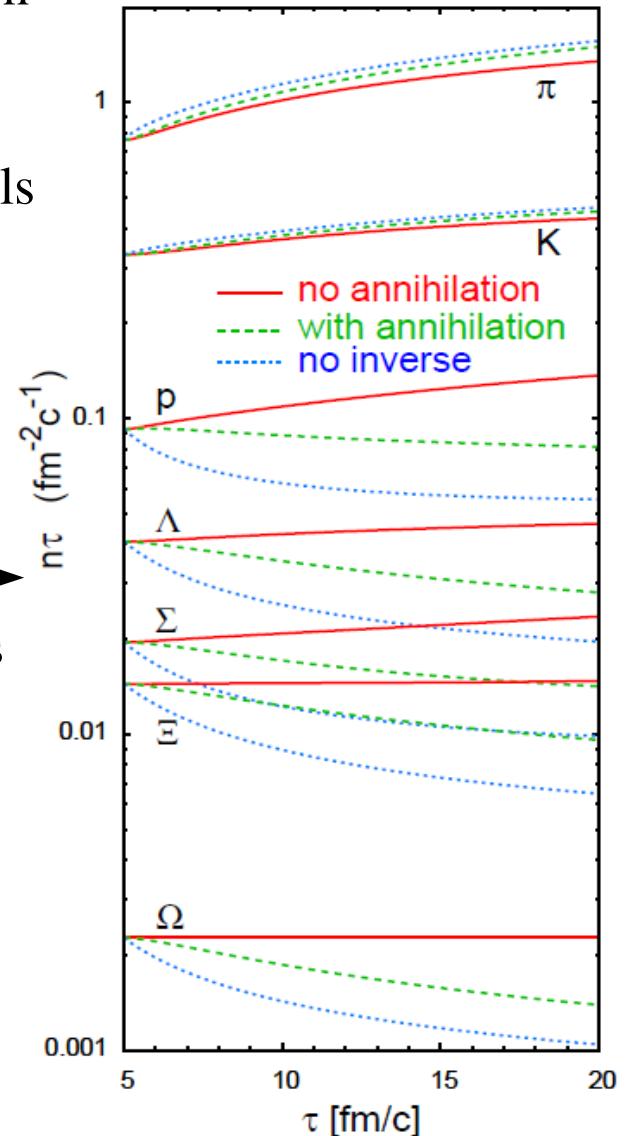
# annihilation in the hadronic phase?

- but need to take into account full detailed balance, backreaction like  $5\pi \rightarrow p\bar{p}$  (not in RQMD)

analysis by Rapp and Shuryak 2008 for SPS energies: this cancels the annihilation effect,  
equilibrium value at  $T_{\text{chem}}$  is recovered

recent analysis by Pan and Pratt, PRL 110 (2013) 042501:  
taking account backreaction cancels half of the effect of annihilation

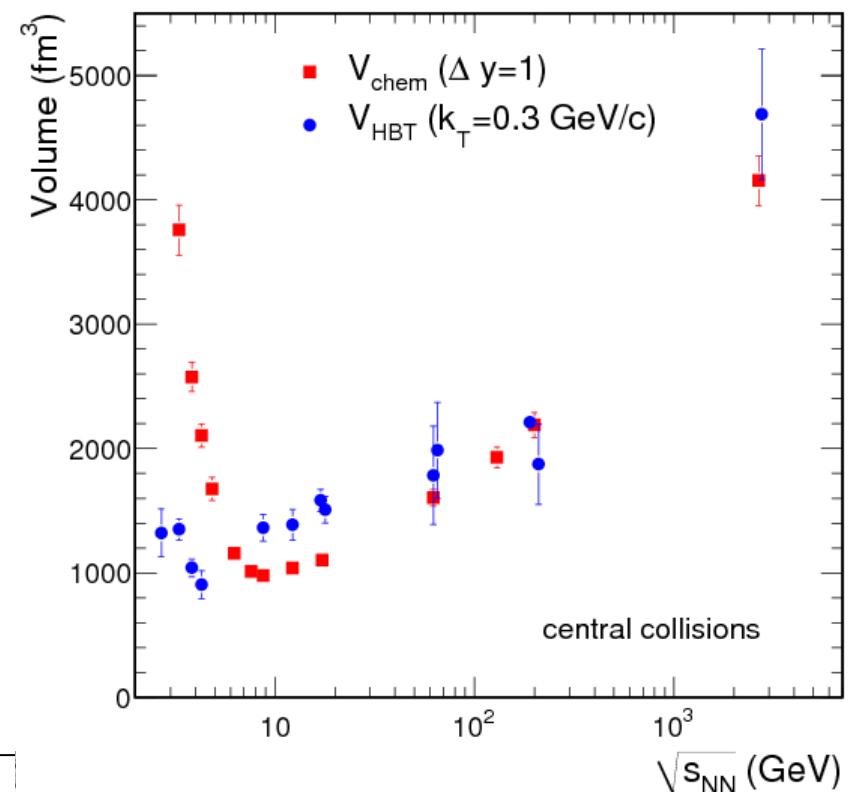
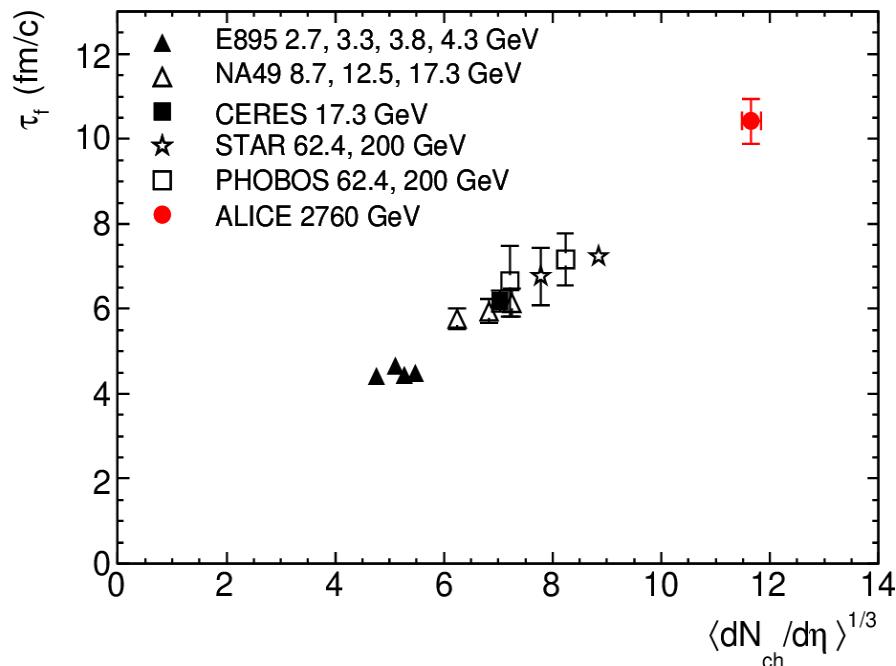
- Why should only proton be affected? and not hyperons? Cross sections should be very similar, e.g.  $\Omega + N\bar{p} \rightarrow 2\pi + 3K$  evaluate 10 mb at threshold Braun-Munzinger, JS, Wetterich, Phys. Lett. B596 (2004) 61
  - they show if anything opposite effect
- what about nuclei?? they fit perfectly and their cross sections are larger



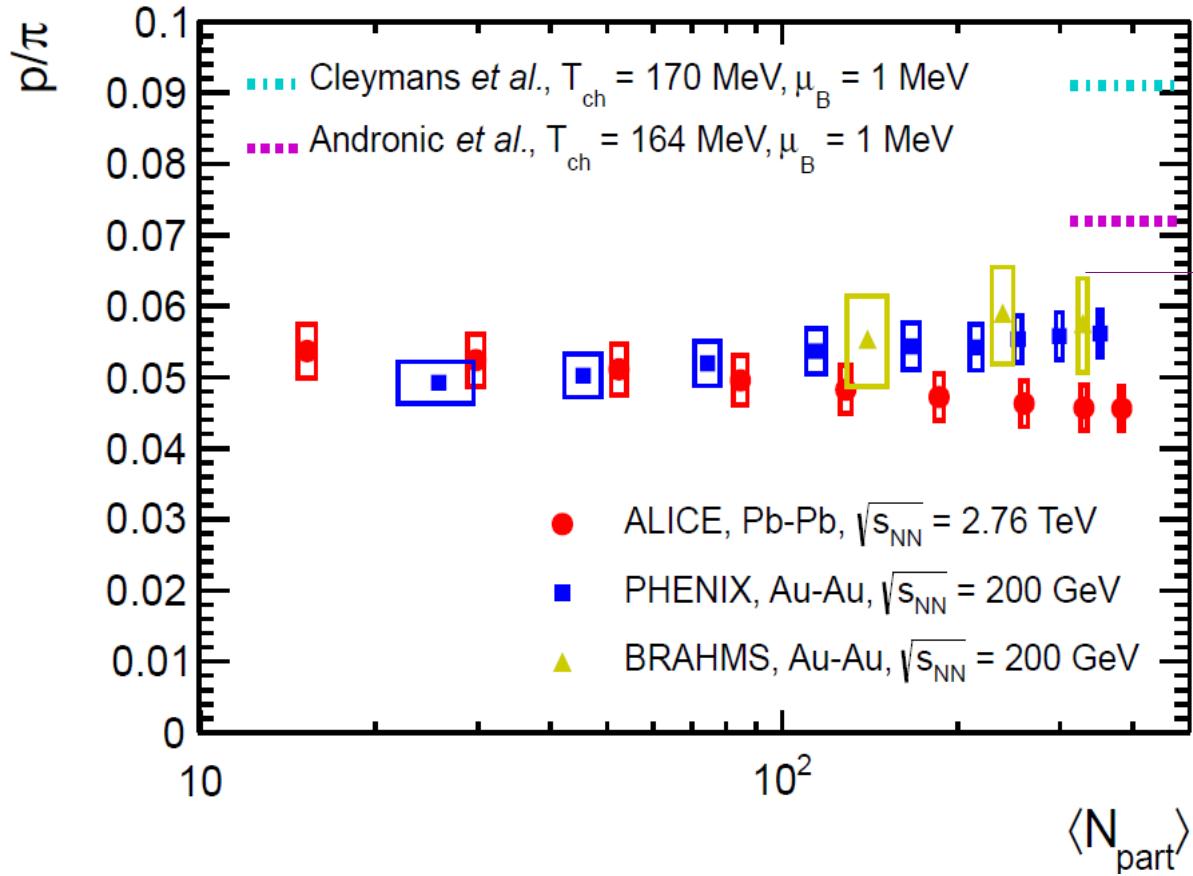
# annihilation in hadronic phase

all of this casts serious doubts on the reduction of protons only due to annihilation in hadronic phase

additional argument: in RQMD lifetime of hadronic phase significantly too long  
 (from HBT: total lifetime of system = 10 fm/c – and volume change between  
 chemical and thermal freeze-out does not allow for longlived hadronic phase)  
 shorter lifetime reduces effect



# Centrality dependence of proton to pion ratio



different centrality dependence for RHIC and LHC is a real puzzle

- does not support annihilation picture
- is it real? physics origin?

# Out-of-equilibrium model of hadronization

J. Rafelski and collaborators

introduction of additional chemical potentials

- systematic variation of parameters with beam energy?
- yield of deuterons prop to  $\gamma_q^6$  - comparison to data: strong deviation