

FCC-ee Lepton Collider

Frank Zimmermann

FCC Physics, Detector and Accelerator Workshop
Istanbul Aydin University, 11 March 2016

many thanks to M. Aiba, R. Assmann, S. Aumon, E. Belli, M. Benedikt, A. Blondel, A. Bogomyagkov, M. Boscolo, O. Brunner, H. Burkhardt, A. Butterworth, Y. Cai, R. Calaga, F. Cerutti, A. Doblhammer, O. Etisken, A. Faus-Golfe, A. Ferrari, K. Furukawa, C. Garion, E. Gianfelice, S. Glukhov, G. Guillermo, B. Haerer, B. Holzer, P. Janot, M. Jimenez, J. Jowett, R. Kersevan, I. Koop, M. Koratzinos, L. Lari, E. Levichev, R. Martin, L. Medina, V. Mertens, M. Migliorati, S. Ogur, K. Ohmi, K. Oide, J. Osborne, Y. Papaphilipou, P. Piminov, R. Rossmanith, G. Rumolo, A. Saa Hernandez, J. Seeman, D. Shatilov, D. Shwartz, S. Sinyatkin, M. Sullivan, M.A. Valdivia, J. Wenninger, U. Wienands, ...



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Outline

- e^+e^- collider landscape & lessons learnt
- FCC-ee baseline parameters
- synchrotron radiation
- RF system, cryo & wall-plug power
- FCC-ee optics
- polarization, energy calibration & mono-chromatization

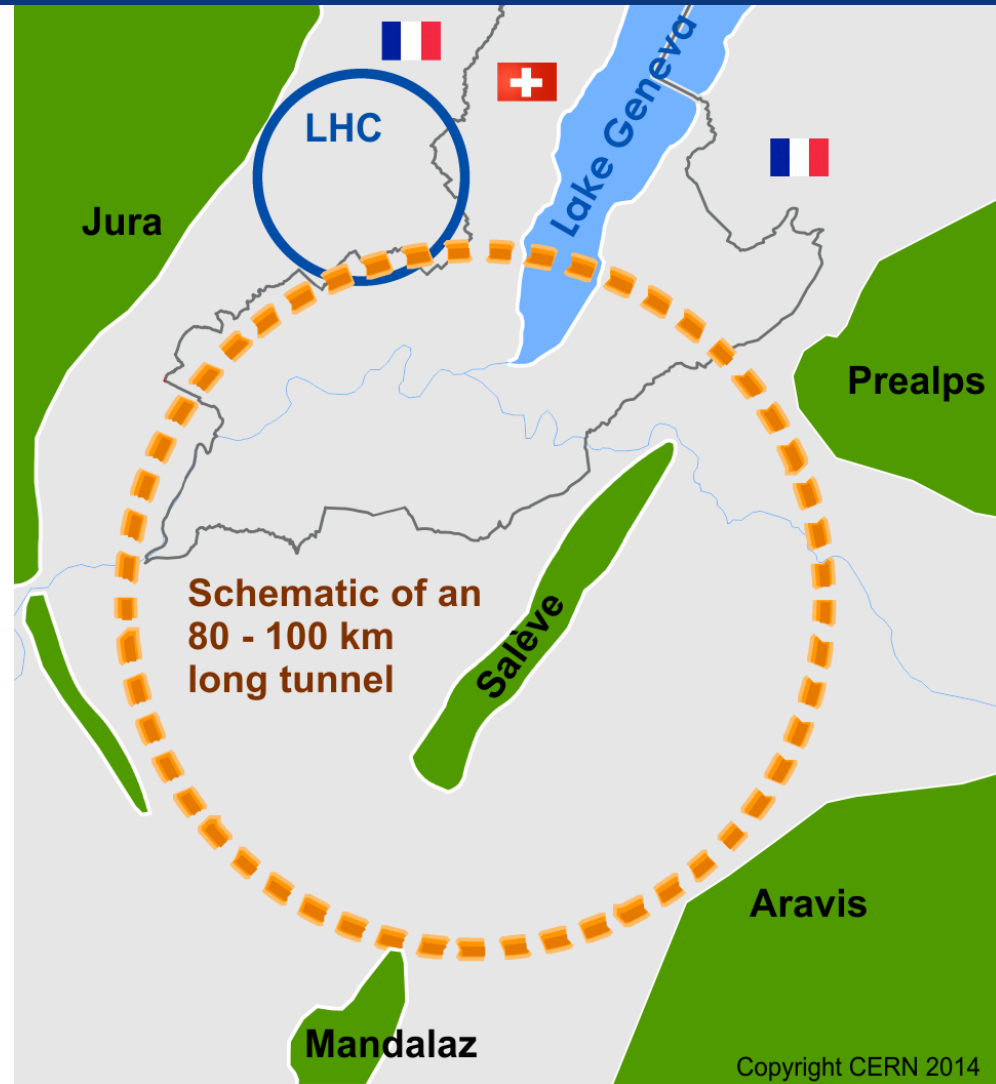
*e^+e^- collider landscape
& lessons learnt*

Future Circular Collider Study

GOAL: CDR and cost review for the next ESU (2018)

International FCC collaboration (CERN as host lab) to study:

- ***pp*-collider (FCC-hh)**
→ main emphasis, defining infrastructure requirements
~16 T ⇒ 100 TeV *pp* in 100 km
- **80-100 km infrastructure** in Geneva area
- ***e⁺e⁻* collider (FCC-ee) as potential intermediate step / as a possible first step**
- *p-e* (FCC-he) option, HE-LHC ...



CepC/SppC study (CAS-IHEP) 54 km (baseline)

e^+e^- collisions ~2028; pp collisions ~2042



easy access
300 km east
from Beijing
3 h by car
1 h by train

Image © 2013 DigitalGlobe
Data SIO, NOAA, U.S. Navy, NGA, GEBCO
© 2013 Mapabc.com
Image © 2013 TerraMetrics

Yifang Wang

“Chinese Toscana”

Google earth



FCC Lepton Collider Design

Frank Zimmermann

Istanbul FCC Workshop 11 March 2016



FCC–ee physics requirements

A. Blondel,
J. Ellis ,
C. Grojean,
P. Janot,
et al.

- **beam energy range from 35 GeV to ≈ 200 GeV**
- **highest possible luminosities** at all working points
- physics programs / energies:
 - Z (45.5 GeV) Z pole, ‘TeraZ’ and high precision M_Z & Γ_Z*
 - W (80 GeV) W pair production threshold, high precision M_W*
 - H (120 GeV) ZH production (maximum rate of H’s)*
 - t (175 GeV): $t\bar{t}$ threshold, H studies*
 - more (α_{QED} etc.)*
- possibly *H* (63 GeV) direct s-channel production with
monochromatization
- **some polarization up to ≥ 80 GeV** for beam energy calibration

LEP/LEP2: highest energy so far

circumference 27 km

in operation from 1989 to 2000

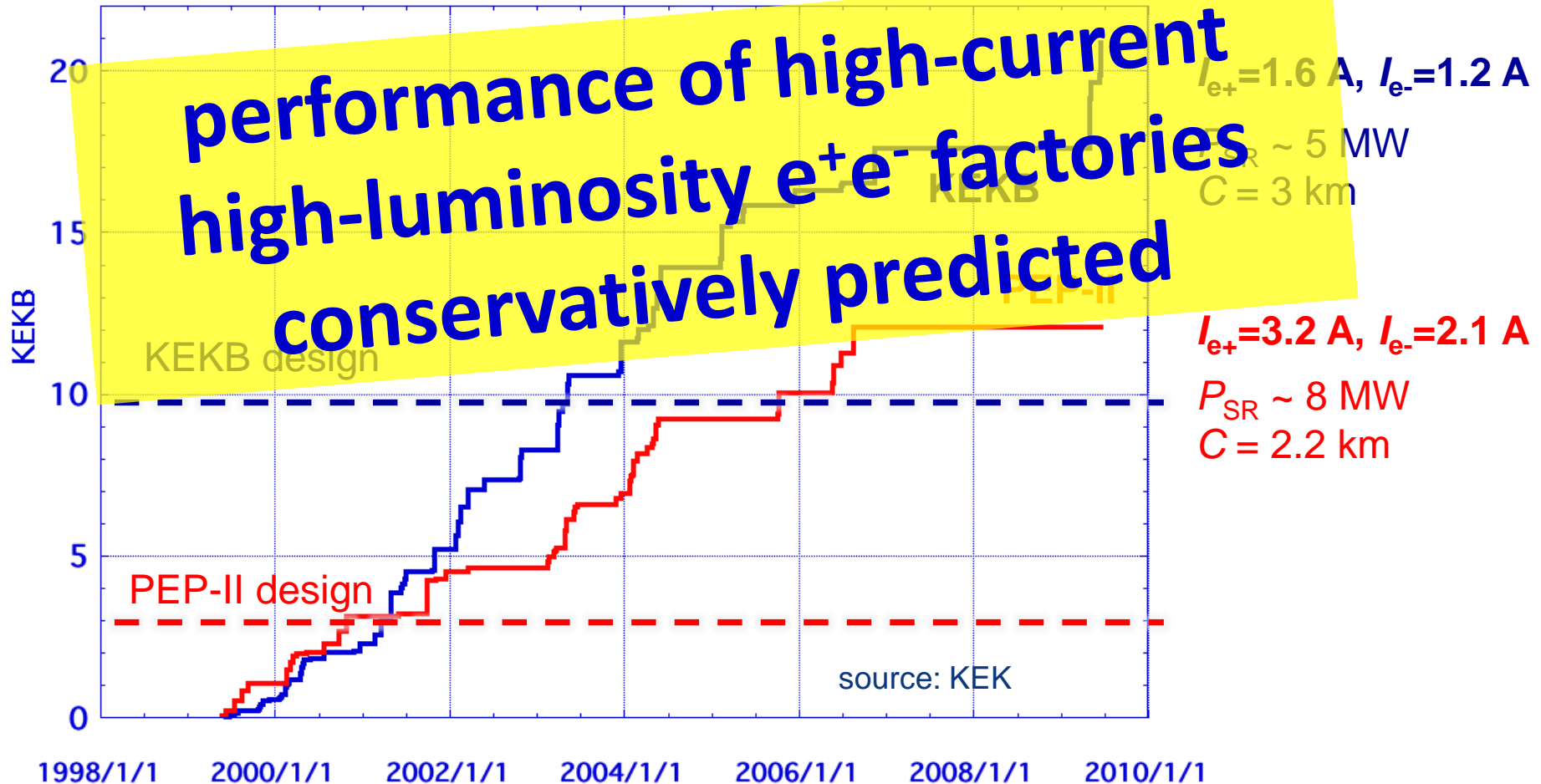
maximum c.m. energy 209 GeV

maximum synchrotron radiation power 23 MW

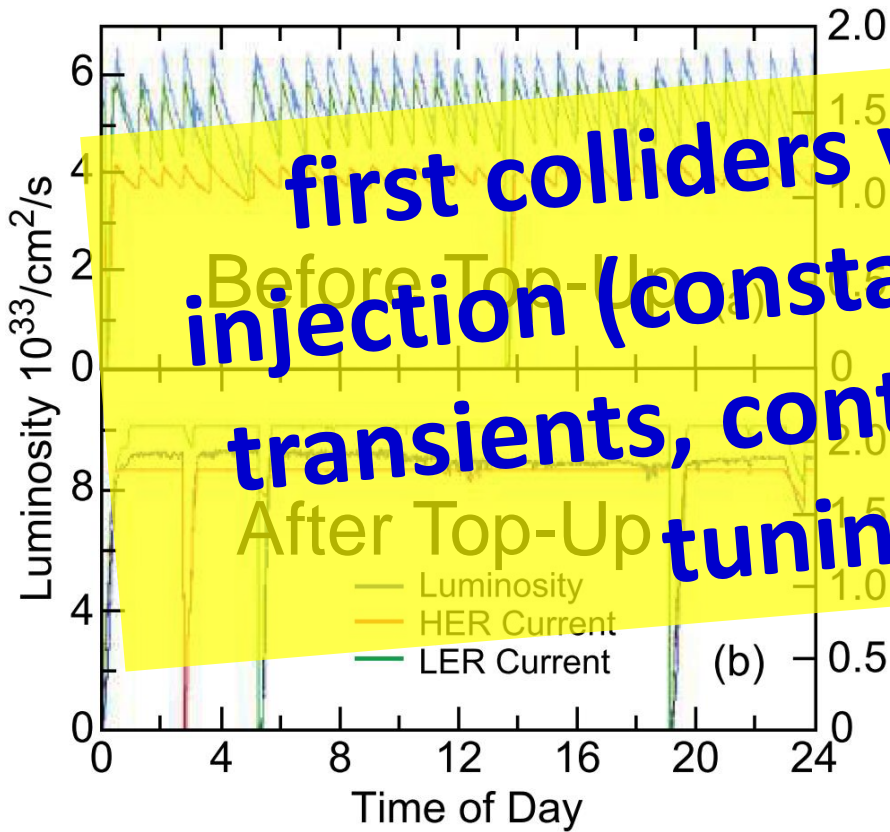
**LEP energy close to FCC-ee target
+ record synchrotron radiation
with \sim MeV photons**

KEKB & PEP-II: high current, high L

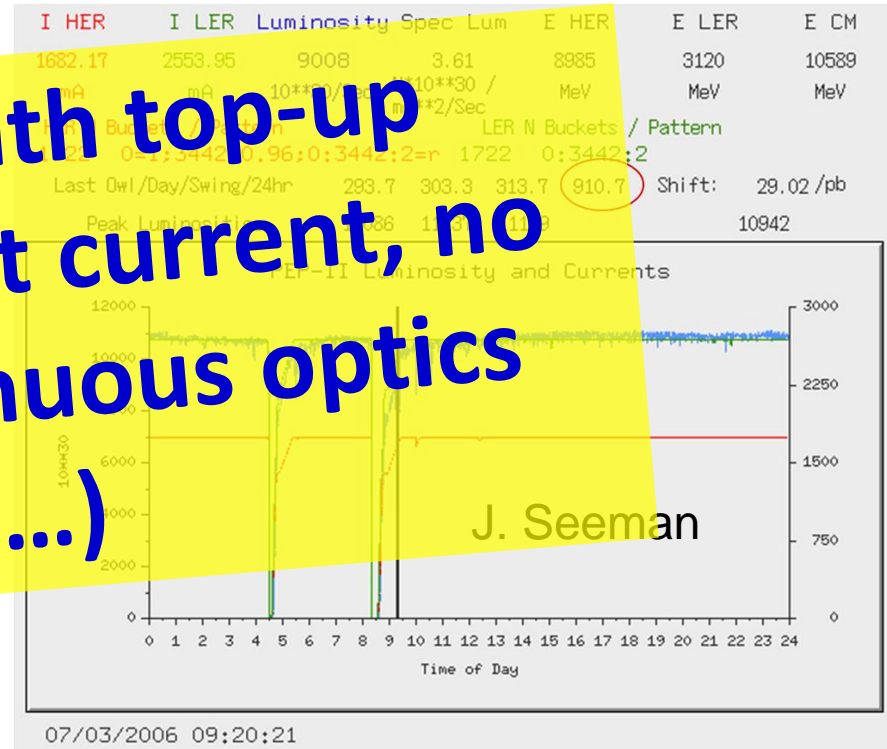
Trend of Peak Luminosity



KEKB & PEP-II: top-up injection



first colliders with top-up injection (constant current, no transients, continuous optics tuning,...)



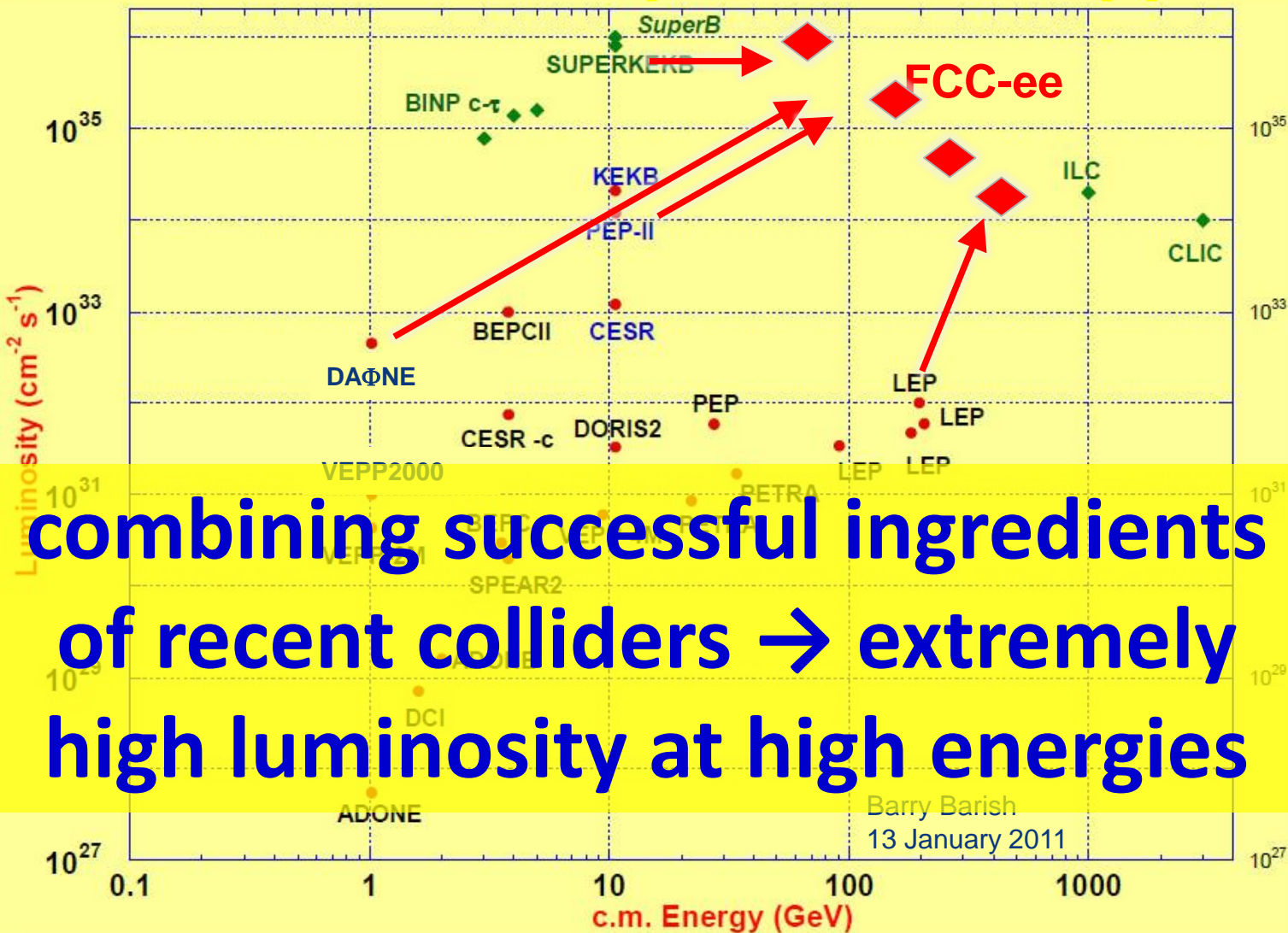
J. Seeman

average luminosity \approx peak luminosity

similar results from KEKB



FCC-ee exploits lessons & recipes from past e^+e^- and pp colliders



LEP:

high energy
SR effects

KEKB & PEP-II:

high beam currents,
top-up injection

DAΦNE: crab waist

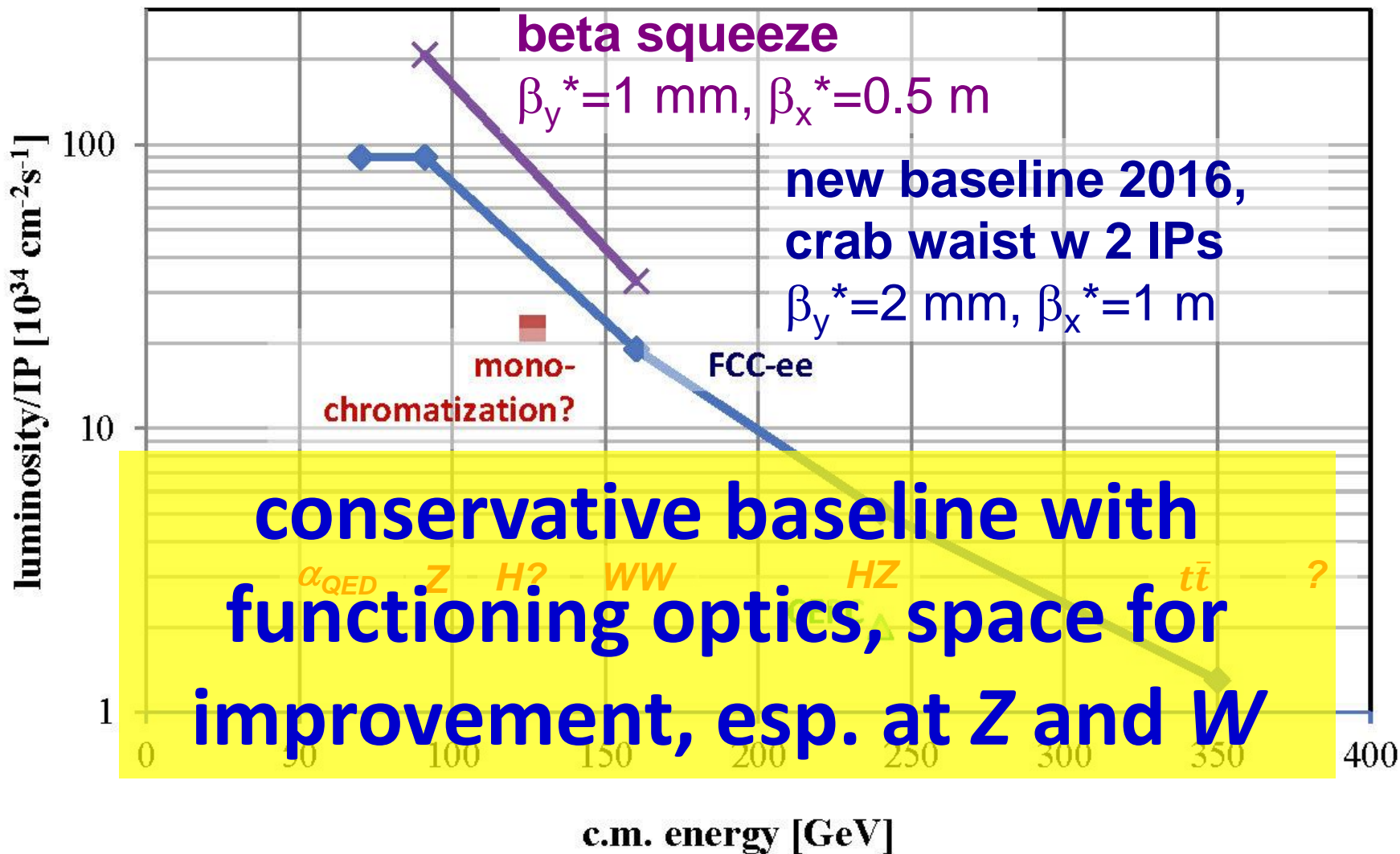
S-KEKB: low β_y^*

KEKB: e^+ source

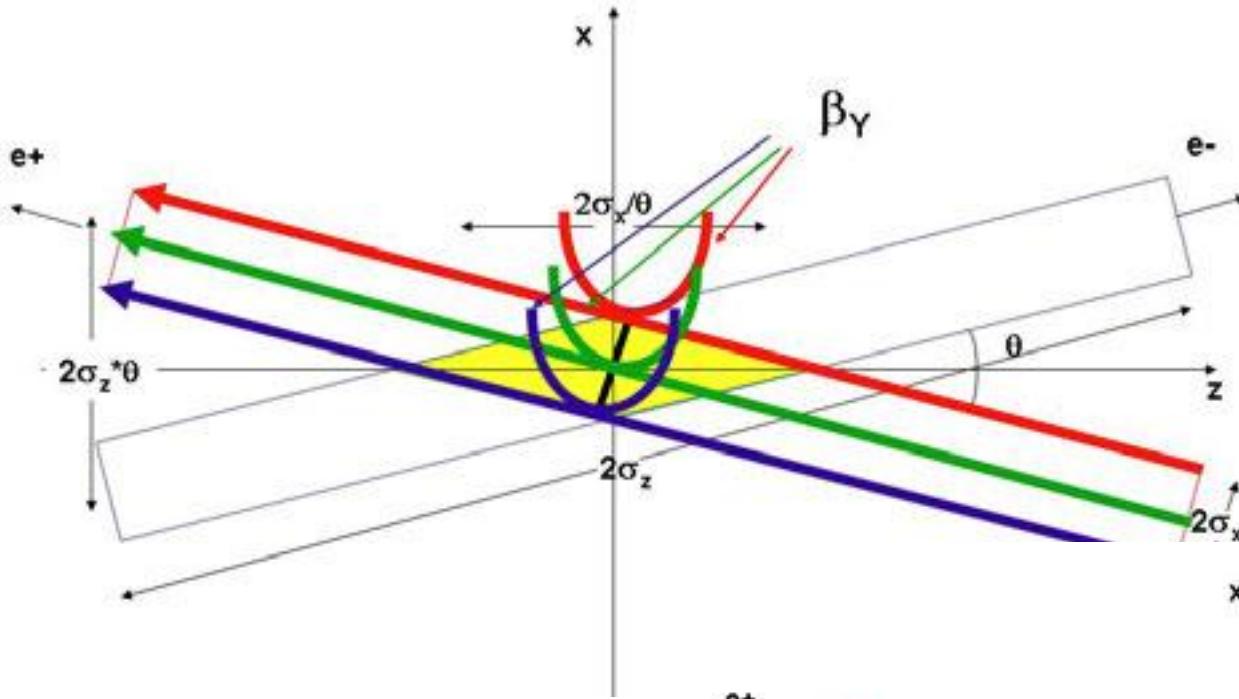
HERA, LEP, RHIC:
spin gymnastics



*FCC-ee baseline
parameters*

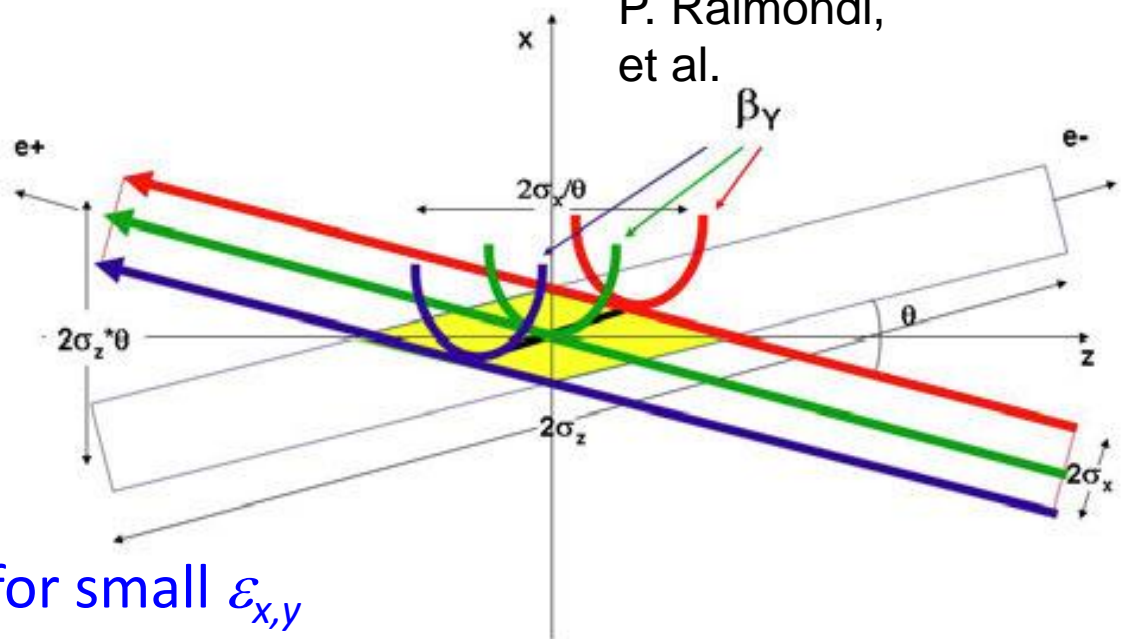


crab-waist crossing for flat beams



regular crossing

P. Raimondi,
et al.



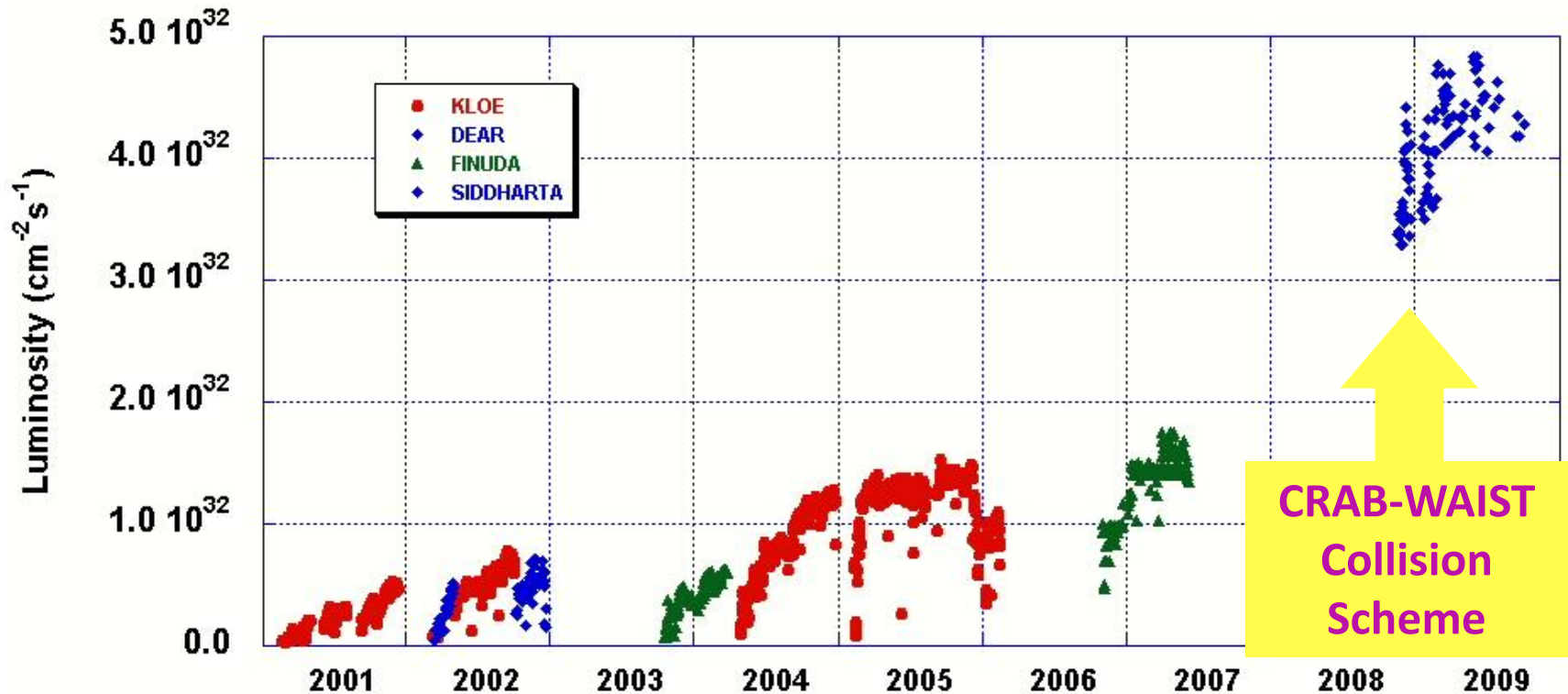
crab waist -

vertical waist position
in s varies with horizontal
position x

- allows for small β_Y^* and for small $\varepsilon_{x,y}$
- and avoids betatron resonances (\rightarrow higher beam-beam tune shift)

DAΦNE: “crab waist” collisions

DAΦNE Peak Luminosity



Design Goal

M. Zobov



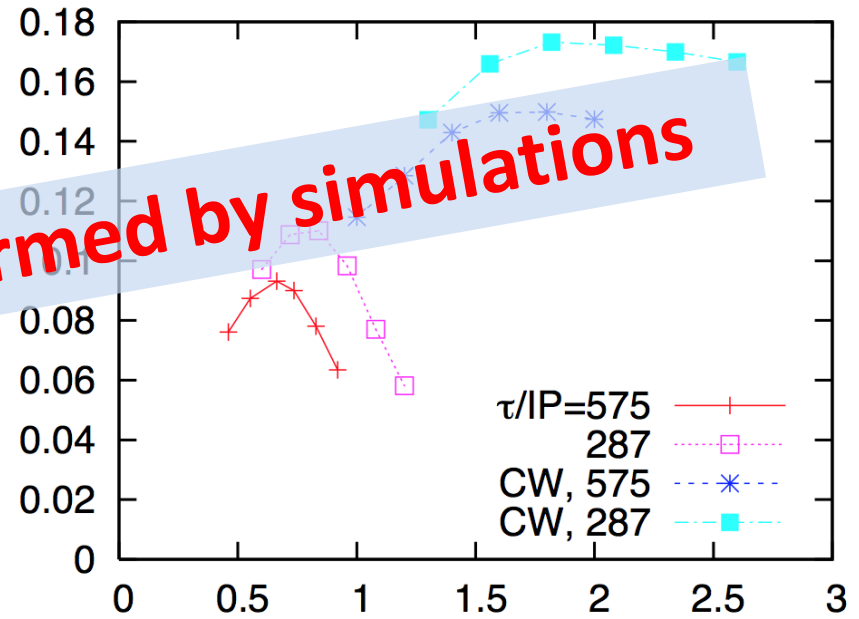
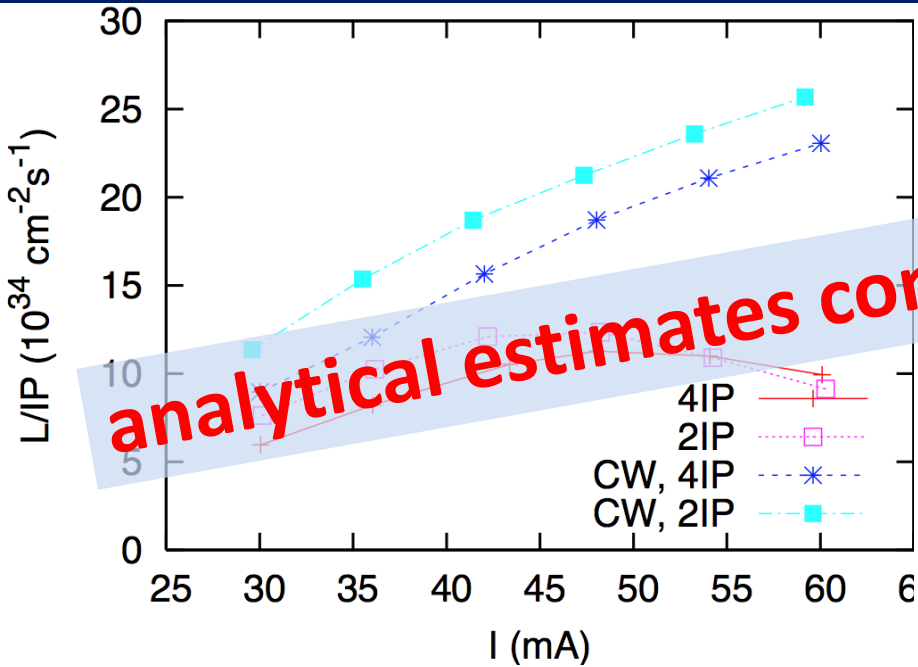
2016 baseline parameters

parameter	FCC-ee				CEPC	LEP2
energy/beam [GeV]	45.6		120	175	120	105
bunches/beam	30.2k	91.5k	770	78	50	4
beam current [mA]	1450		30	6.6	16.6	3
luminosity/IP x $10^{34} \text{ cm}^{-2}\text{s}^{-1}$	207	90	5.1	1.3	2.0	0.0012
energy loss/turn [GeV]	0.03		1.67	7.55	3.1	3.34
synchrotron power [MW]	100				103	22
RF voltage [GV]	0.4	0.2	3.0	10	6.9	3.5
rms bunch length SR+tot [mm]	1.2,6.7	1.6,3.8	2.0,2.4	2.1, 2.5	2.1,2.6	12, 12
rms emittance $\varepsilon_{x,y}$ [nm, pm]	0.09, 1		0.61, 1	1.3, 2.5	6, 18	22, 250
$\beta^*_{x,y}$ [m,mm]	0.5,1.0	1, 2.0	1, 2.0	1, 2.0	0.8,1.2	1.2, 50
longit. damping time [turns]	1320		72	23	39	31
crossing angle [mrad]	30		30	30	0	0
beam lifetime [min]	94	185	67	57	61	434

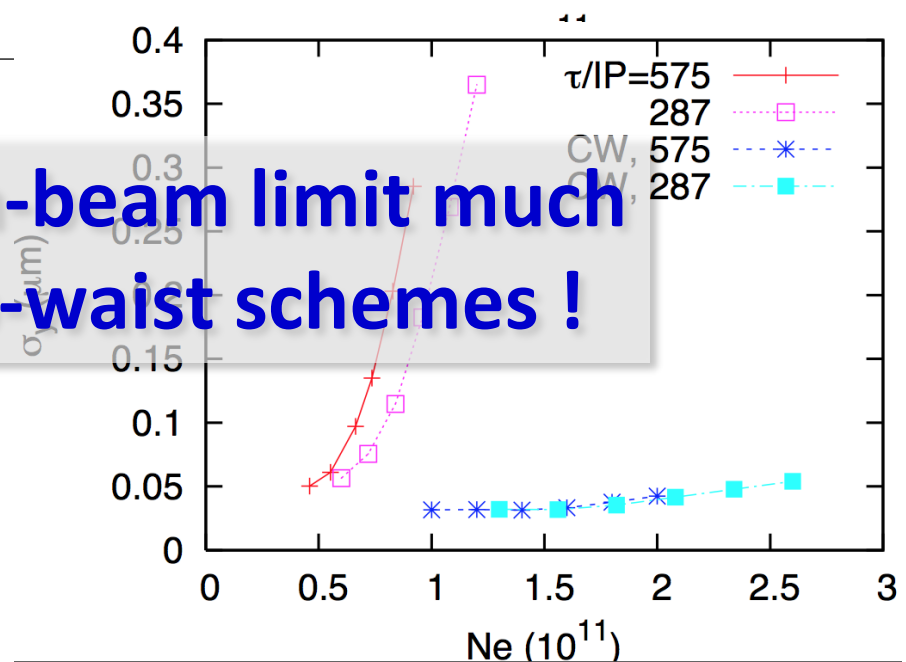
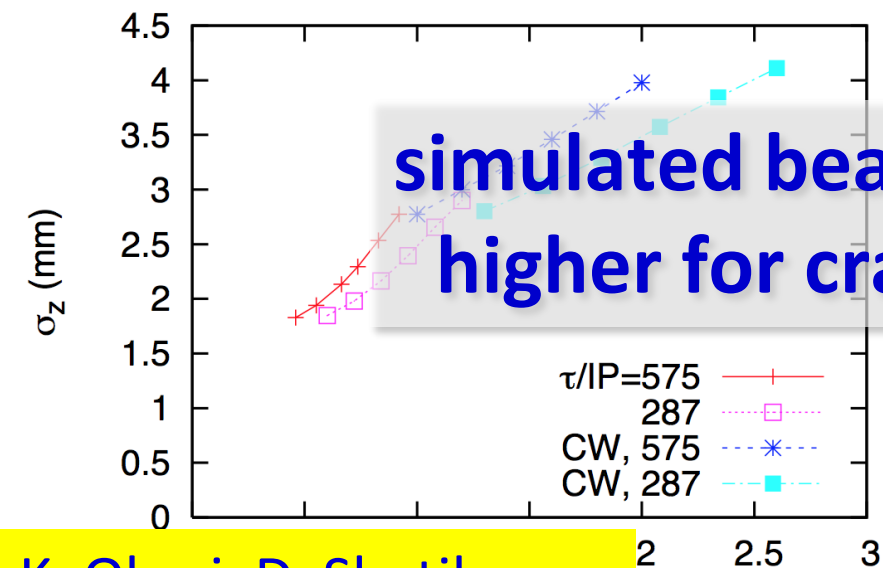
FCC-ee: 2 separate rings

CEPC: single beam pipe like LEP

beam-beam simulations



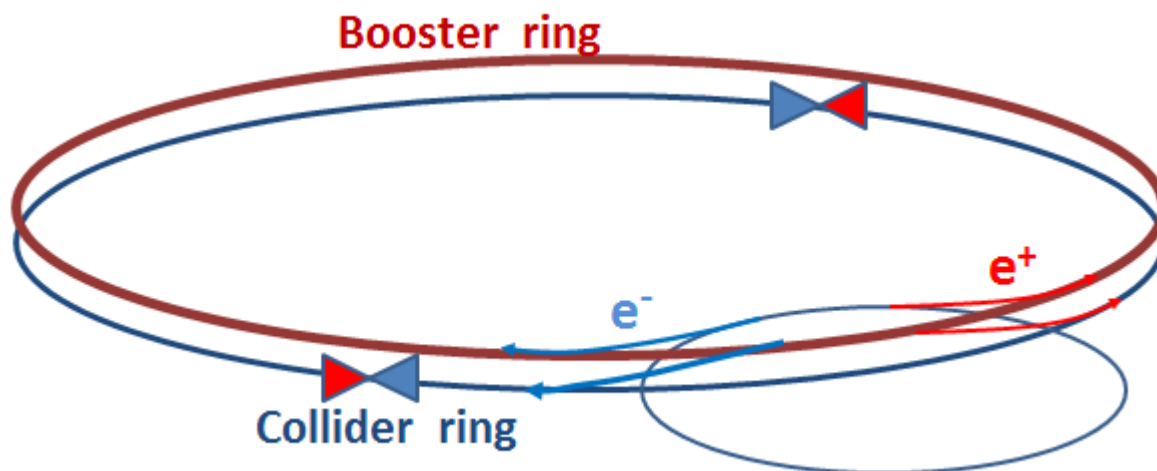
analytical estimates confirmed by simulations



simulated beam-beam limit much higher for crab-waist schemes !

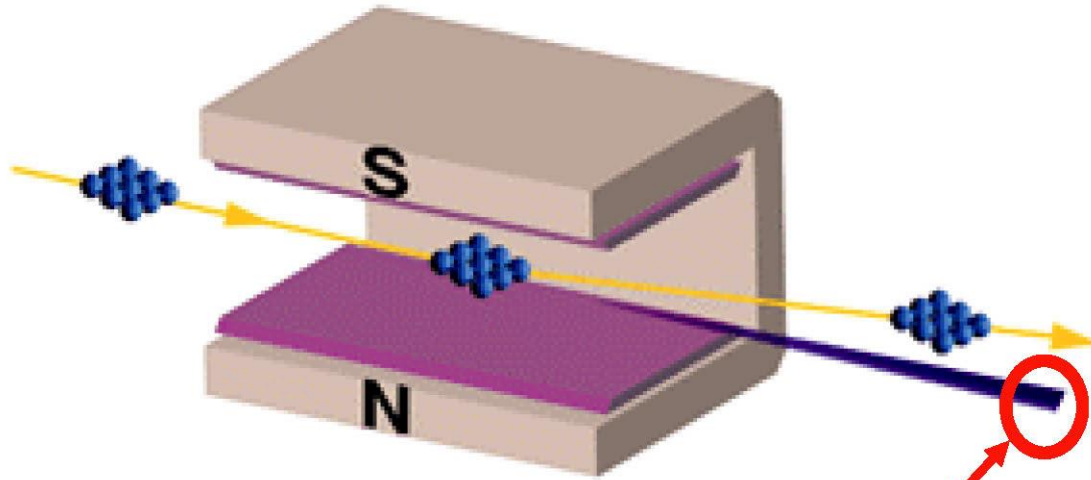
beside the collider ring(s), a booster of the same size (same tunnel) must provide beams for top-up injection to sustain the extremely high luminosity

- same size of RF system, but low power (\sim MW)
- top up frequency ≈ 0.1 Hz
- booster injection energy $\approx 5-20$ GeV
- bypass around the experiments



synchrotron radiation

curved orbit of e^- in magnetic field



Accelerated charge →

Electromagnetic radiation

L. Rivkin

arc synchrotron radiation (SR) 1

energy loss per turn $U_0 = \frac{e^2 \gamma^4}{3\epsilon_0 \rho}$

$$\frac{1}{\rho} = \frac{eB}{p}$$

$$U_0[\text{keV}] = 88.46 \frac{E[\text{GeV}]^4}{\rho[\text{m}]}$$

numerical values
for electrons

$$\propto E^4/m^4 \propto \gamma^4$$

→ RF voltage

synchrotron radiation power

$$P_{SR} = \frac{2U_0 I_b}{e}$$

$$\propto E^4/m^4 \propto \gamma^4$$

→ RF power

electrons: $P_{SR} = 23$ MW for LEP, 100 MW for FCC-ee
protons: $P_{SR} = 0.01$ MW for LHC, 5 MW for FCC-hh

**critical (typical)
photon energy**

$$E_{\gamma,c} = \frac{3}{2} \hbar c \frac{\gamma^3}{\rho}$$

→ shielding

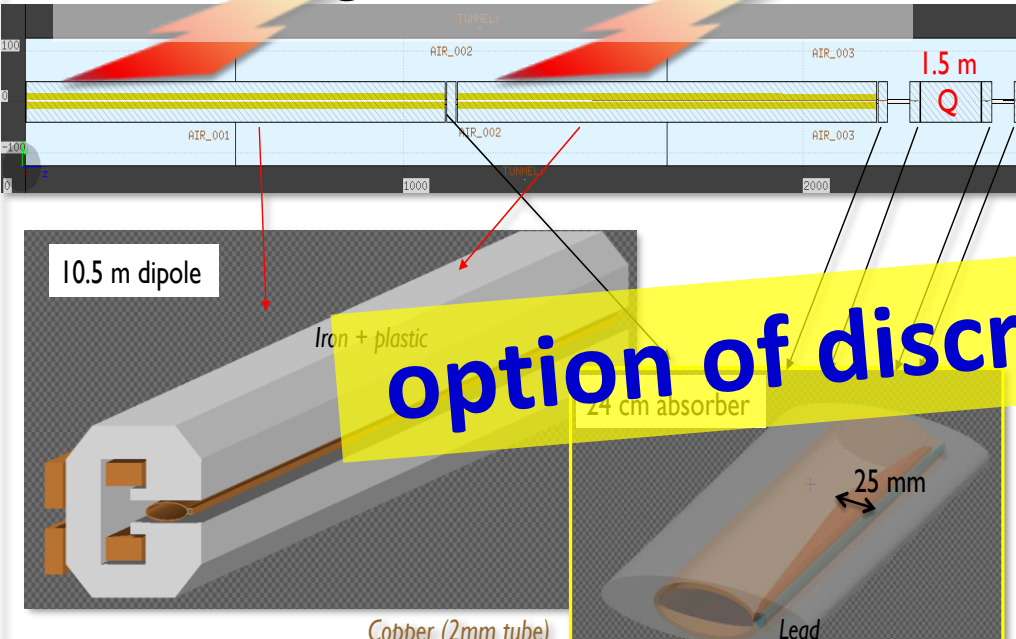
electrons: $E_{c,\gamma} \sim 1$ MeV for LEP and FCC-ee;
protons: $E_{c,\gamma} \sim 40$ eV LHC, ~ 4 keV FCC-hh

arc SR– heat & shielding

	PEP-II	SPEAR3	FCC-ee Z	FCC-ee H
E [GeV]	9	3	45.5	120
I [A]	3	0.5	1.45	0.03
ρ [m]	165	7.86	11000	11000
linear power [W/cm]	101.8	92.3	7.2	7.2

SR heat per meter much lower than for many operating rings

shielding SR at 175 GeV



option of discrete absorbers

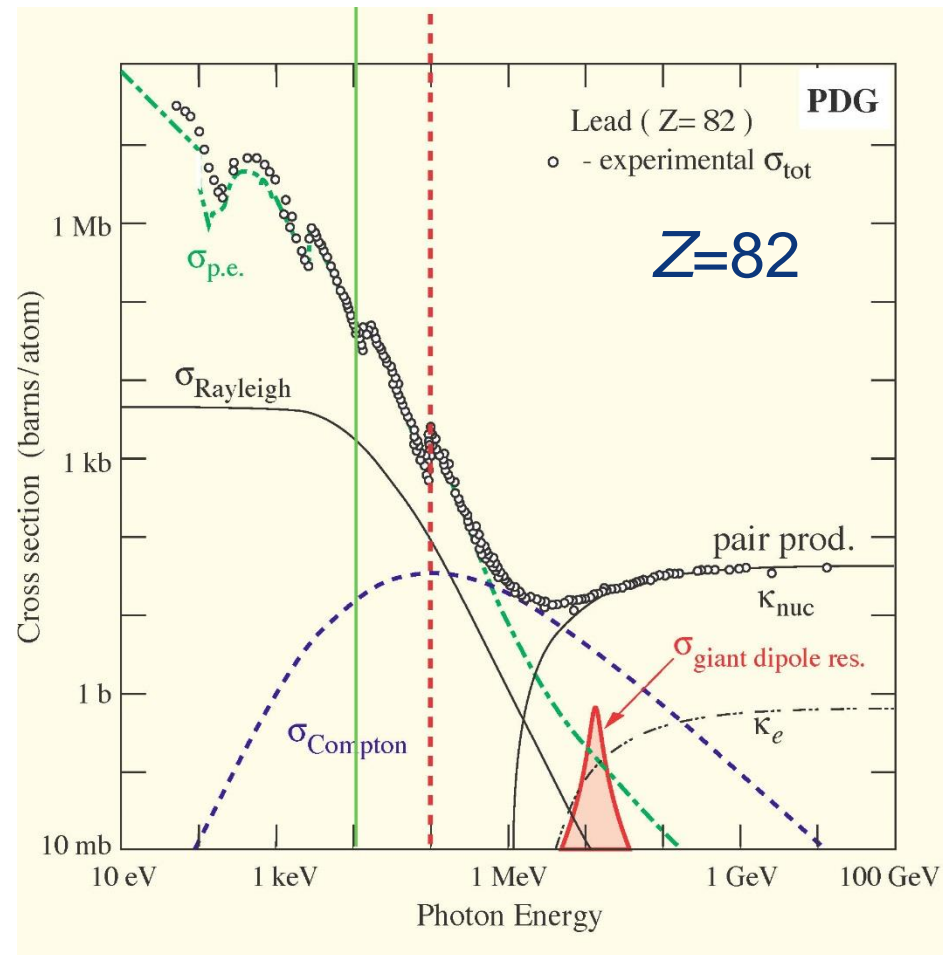
N. Kurita, U. Wienands, SLAC

FLUKA geometry layout for half FODO cell, dipole details, preliminary absorber design incl. 5 cm external Pb shield

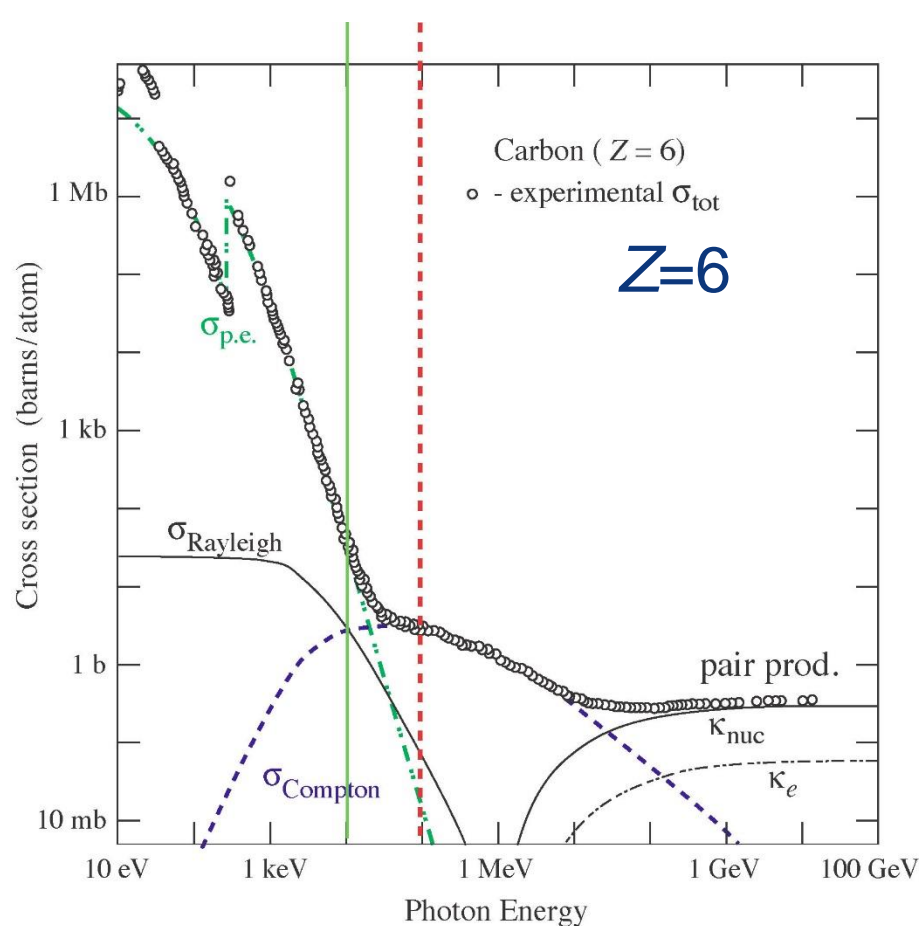
L. Lari, F. Cerutti, A. Ferrari, A. Mereghetti

SR shielding

10 keV 100 keV



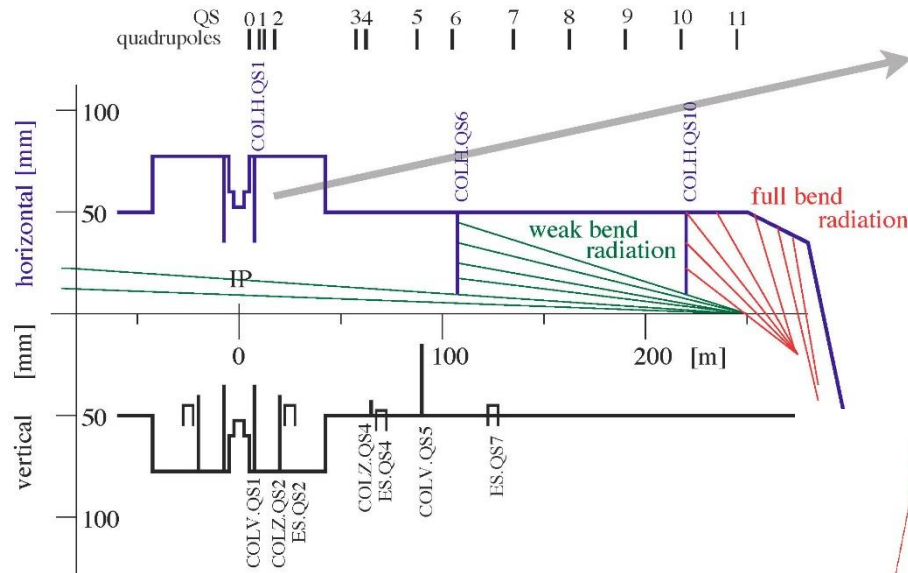
10 keV 100 keV



H. Burkhardt

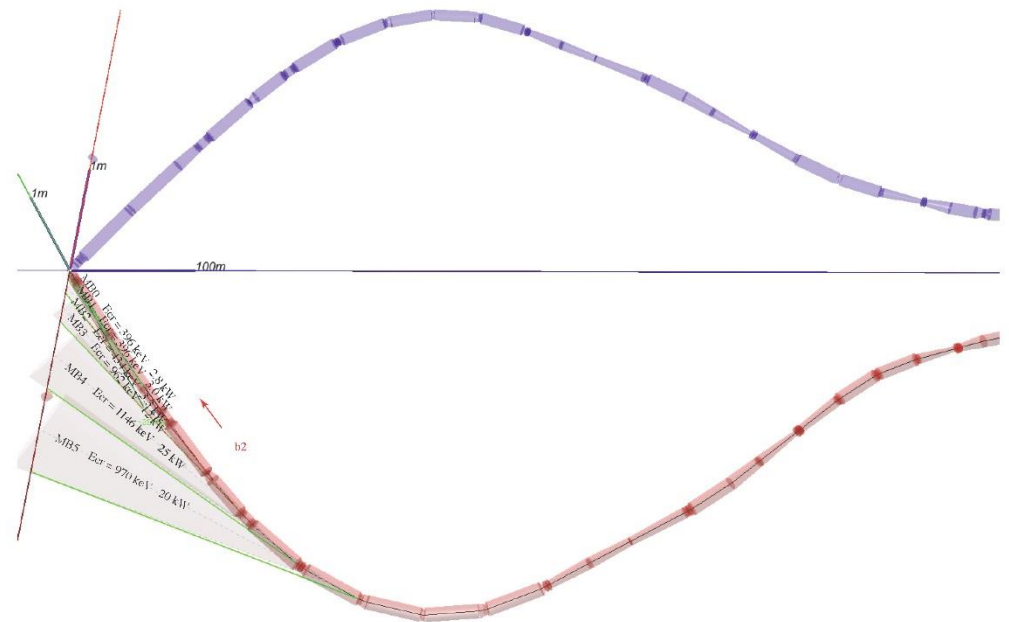
difficult for $E_\gamma \geq 100$ keV, n production for $E_\gamma \geq 1$ MeV

synchrotron radiation in the IR



weak bends and
SR masks for LEP

IR SR fans for one
FCC-ee optics



H. Burkhardt, A. Bogomoyagkov

arc synchrotron radiation 2

radiation damping of transverse and longitudinal motion
→ beam shrinkage

$$\tau_{||} = \tau_x / 2 = (C/c)E / U_0$$

electrons: $\tau_{||} \sim 3$ ms for LEP, 20 ms FCC-ee at 240 GeV cm

protons: $\tau_{||} \sim 13$ h for LHC, 0.5 h FCC-hh

equilibrium emittance due to balance of radiation damping
and quantum excitation

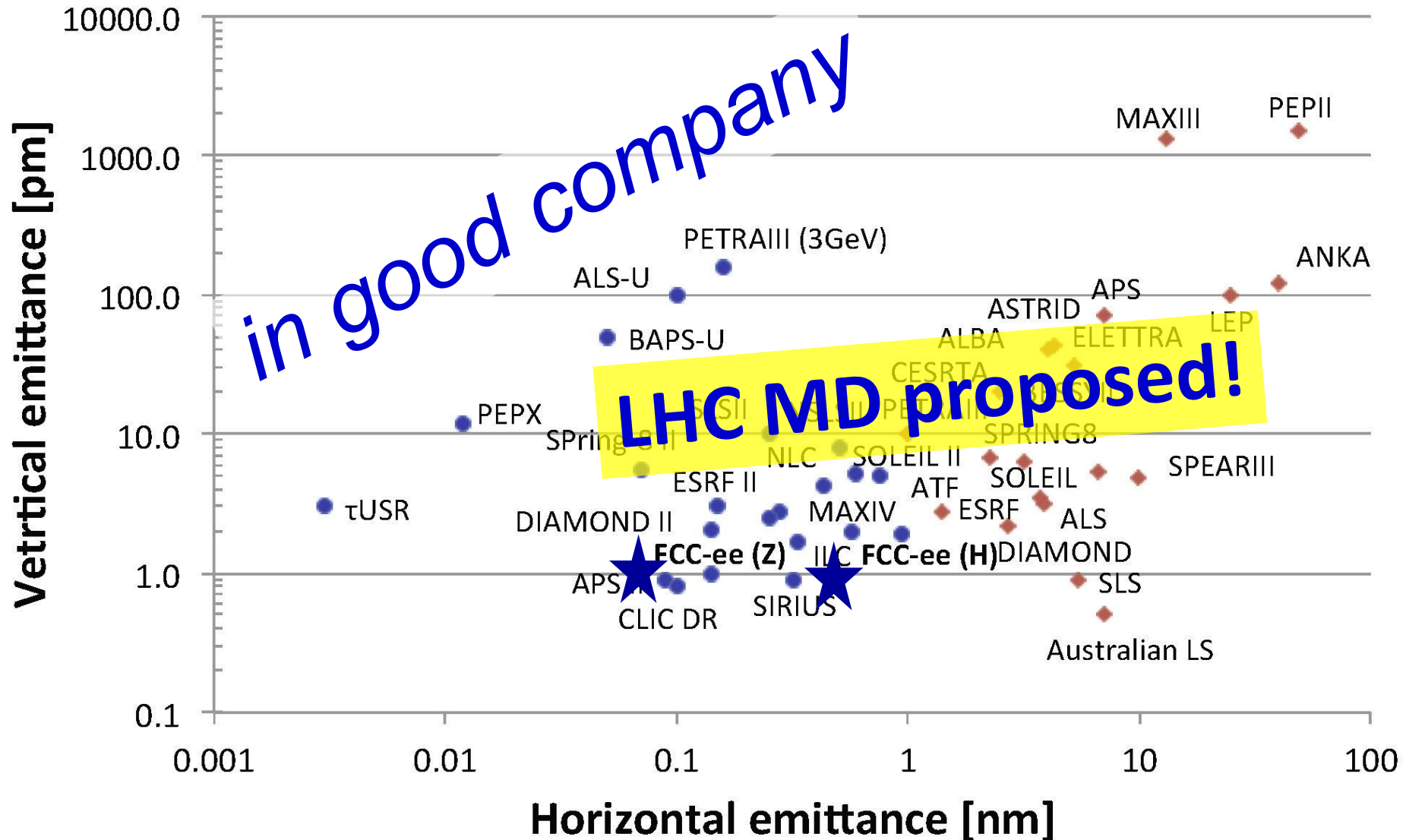
$$\varepsilon_x = C_q \gamma^2 l_b^3 F / \rho^3 \quad l_b: \text{length of half cell}$$

$$C_q = \frac{55}{32\sqrt{3}} \frac{\hbar c}{mc^2} \approx \begin{cases} 4 \times 10^{-13} \text{ m for electrons} \\ 2 \times 10^{-16} \text{ m for protons} \end{cases}$$

→ cell length

$F \approx 3$ for standard arc optics (90 deg FODO cell)

increase of emittance with energy is over-compensated by large radius (ρ)+short cell length (l_b)



beam instabilities

main impedance sources:

100-km vacuum chamber, RF cavities

beam energy higher than LEP, injection synchrotron
tune higher, bunch charge lower

→ no TMCI instability, but **μ -wave instability threat**

coupled bunch instabilities driven by cavity modes

e-cloud instability could appear in e^+ ring
(antechamber to absorb photoelectrons)

and...

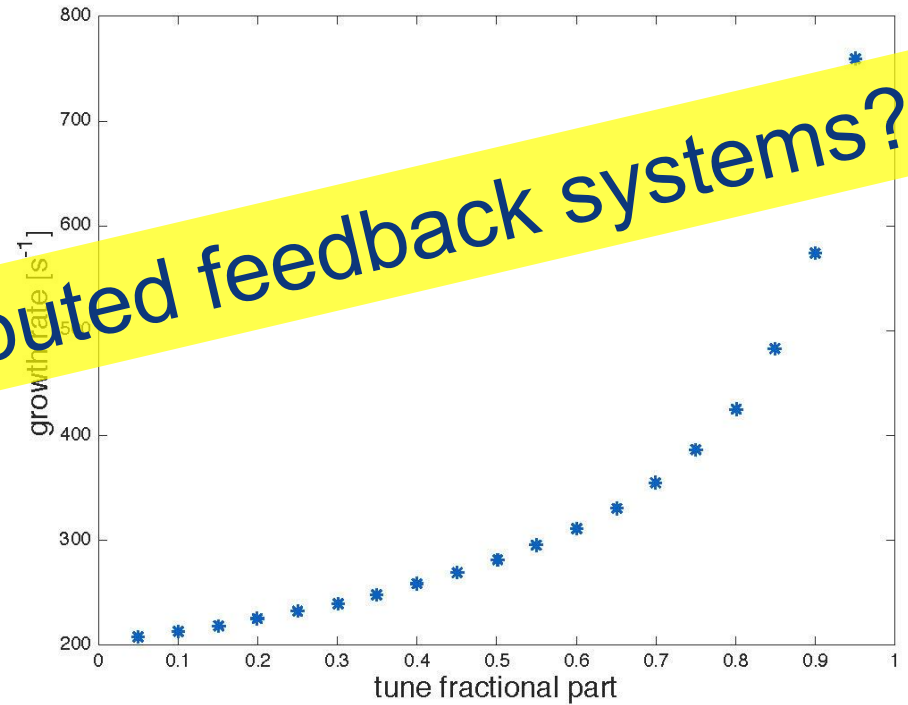
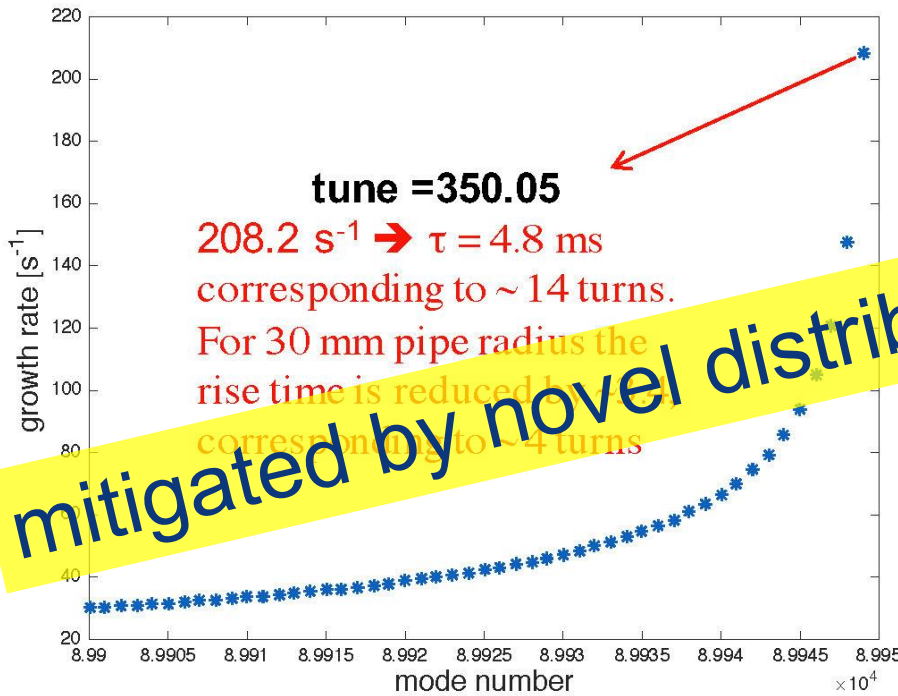
M. Migliorati, N. Mounet, K. Ohmi, G. Rumolo

transverse resistive-wall instability

considering $b=45$ mm (pipe radius)

The worst case (lowest energy and highest beam current) is the Z-pole

$$\alpha = \frac{\text{beam current } cN_b I_b}{\text{energy } 4\pi(E/e)Q_\beta} \frac{L}{2\pi b^3} \sqrt{\frac{LZ_0}{\pi|1 - \nu_\beta| \sigma_c}} G_\perp \left(\frac{\sigma_z}{c} \omega'_q \right)$$



mitigated by novel distributed feedback systems?

M. Migliorati



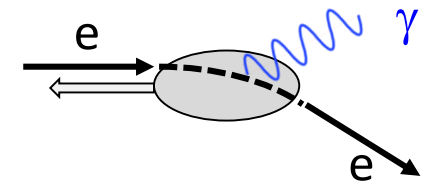
beamstrahlung – a new limit at 175 GeV

- hard photon emission at the IPs, '*Beamstrahlung*', can become lifetime / performance limit for large bunch populations (N), small hor. beam size (σ_x) & short bunches (σ_s)

$$\tau_{bs} \propto \frac{\rho^{3/2} \sqrt{\eta}}{\sigma_s} \exp(A \eta \rho) \quad \frac{1}{\rho} \approx \frac{N r_e}{\gamma \sigma_x \sigma_s}$$

η : ring energy acceptance

lifetime expression by V. Telnov, modified version by A. Bogomyagkov et al



ρ : mean bending radius at the IP (in the field of the opposing bunch)

- for acceptable lifetime, $\rho \times \eta$ must be sufficiently large
 - *flat beams (large σ_x) !*
 - *bunch length !*
 - *large momentum acceptance: aiming for $\geq 1.5\%$ at 175 GeV*
 - LEP: $< 1\%$ acceptance, SuperKEKB $\sim 1.5\%$

RF system

power considerations

continually supplying circulating beam with

$P_{SR}=100$ MW power (SR losses) requires

$$\text{wall-plug power } P_{wall} = P_{SR}/\eta + P_{cryo}$$

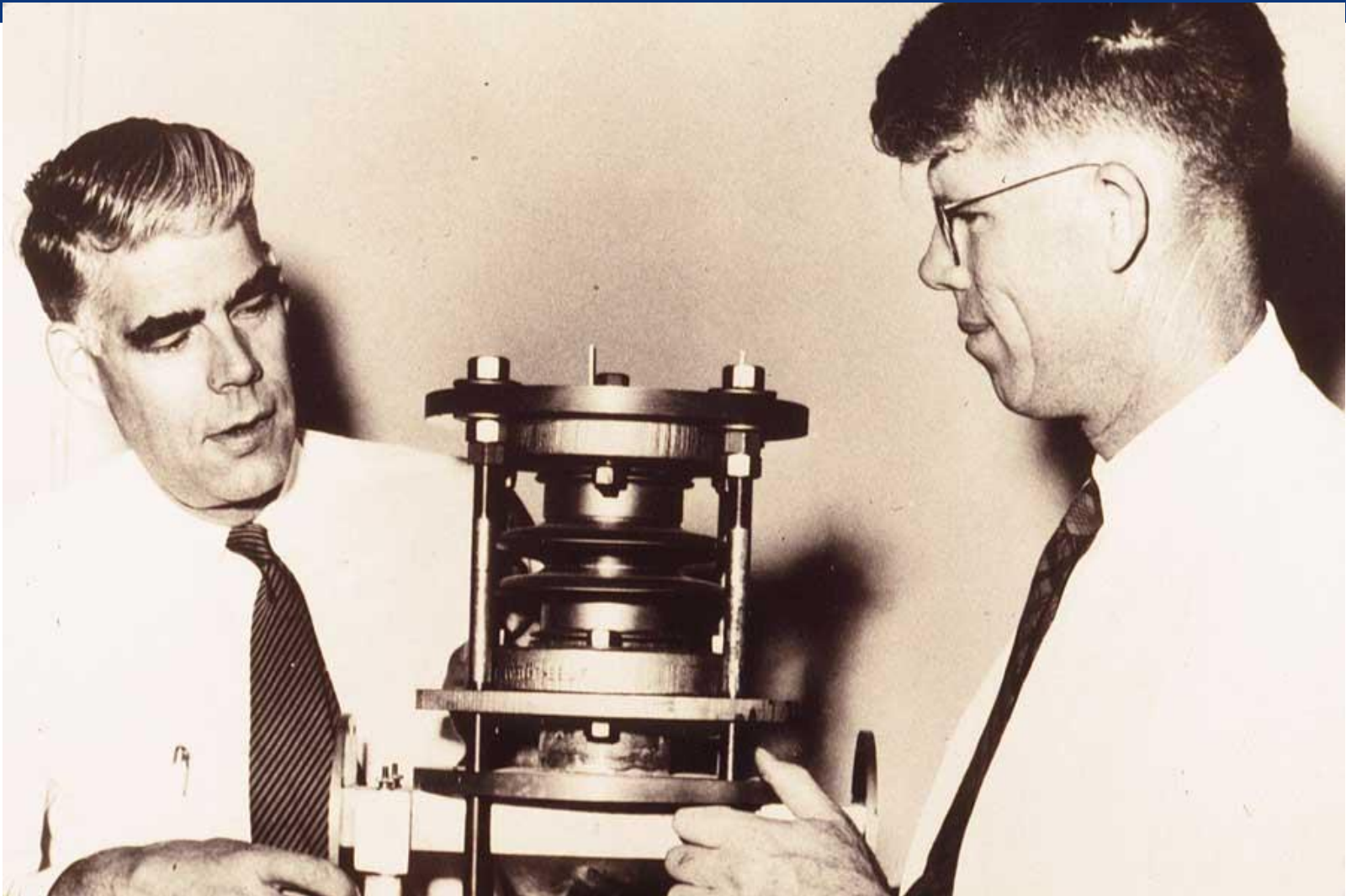
with η =conversion efficiency wall-plug \rightarrow beam

FCC target: $\eta \geq 50\%$

(achieved at PEP-II and LEP)

note: cw RF systems for storage rings are more efficient than those for pulsed linacs

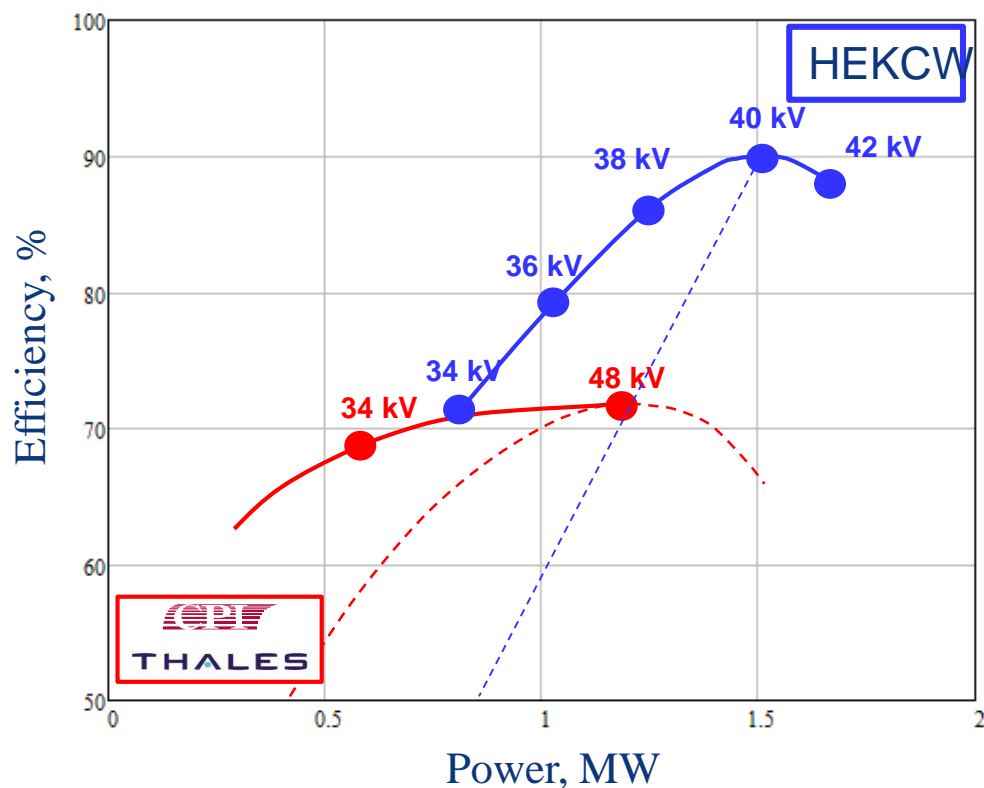
classical rf power source: klystron



Russell & Sigurd Varian invented it at Stanford in 1937

after 80 years a breakthrough in klystron efficiency!

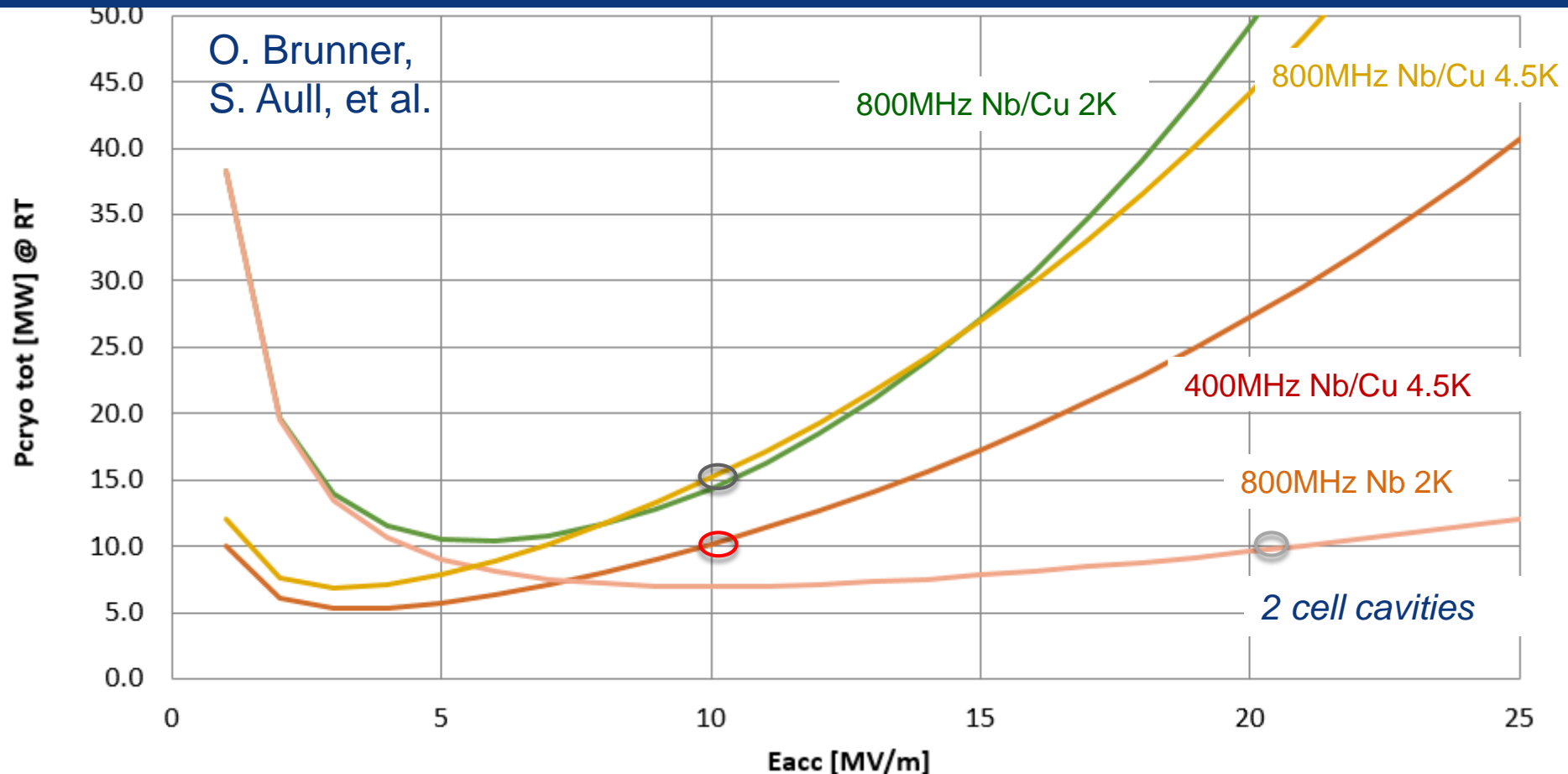
comparing simulated performances of **MBIOT** and **HEKCW MBK**



I. Syrathev

*demonstration
in Russia
this month ?!*

cryo power for FCC-ee “Z” SRF



Static losses dominate @ low fields, dynamic losses @ high fields

4.5k vs 2K operation: 400MHz Nb/Cu @ 10MV/m \approx 800MHz bulk Nb @ 20MV/m; 800MHz Nb/Cu @ 4.5K \approx 50% higher

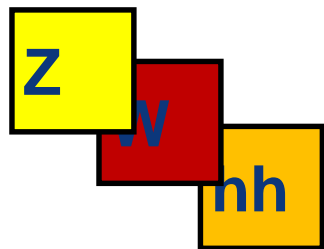
model for RF system optimization with interrelations and limits

f = 400.00 MHz

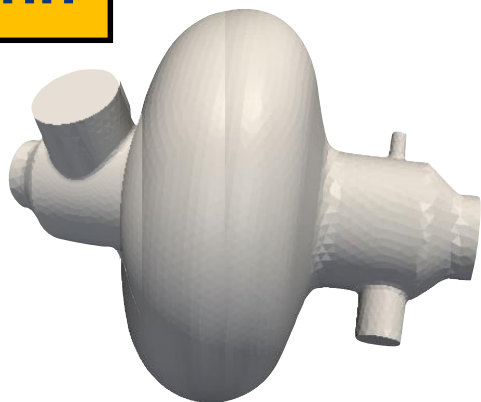
f
400 MHz

FCC-RF-Working Group
S. Aull, O. Brunner, A. Butterworth,
N. Schwerg, M. Therasse

ex. RF cavities for low and high energy



“Z” RF units

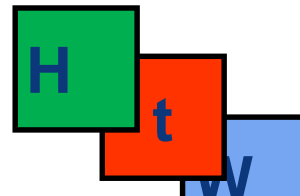


400 MHz (1 cell)

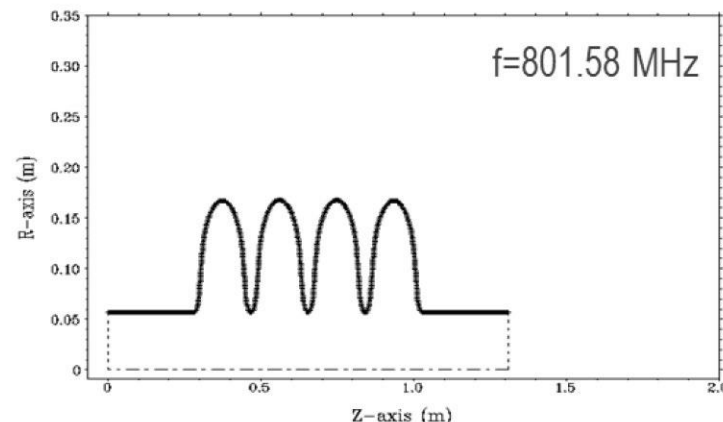
RF Power \approx 0.5 - 1 MW

HOM Power up to 4 kW

Niobium on Copper @ 4.5 K



“Higgs” RF units



800 MHz (4 cells)

RF Power \approx 50 - 200 kW

cryo power \gg MW

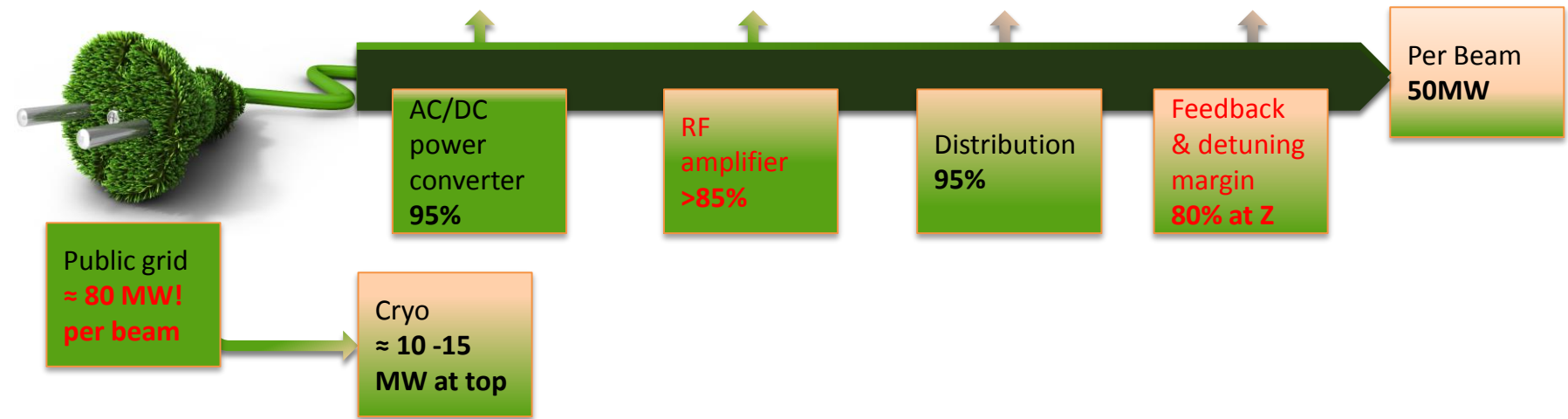
bulk *Nb* at 2 K or new materials
(e.g. *Nb₃Sn*) at 4.5 K

O. Brunner

RF cavities & cryo power (example)

	Z	W	ZH	ttbar
total voltage / beam [GV]	0.2	0.8	3	10
no. cavities / beam	150	150	300	300
RF frequency [MHz]	400		800	
cells / cavity	1		4	
cavity length [m]	0.38	0.38	0.75	0.75
Q_0 [10^9]	4	4	10	8
material & temperature	<i>Nb/Cu 4.5K</i>		<i>Nb at 2K or Nb₃Sn/Nb at 4.5K</i>	
gradient [MV/m]	3.5	14	13	21
voltage / cavity [MV]	5.3	5.3	10	16
input power / cavity [MW]	0.33		0.17	
HOM loss / cavity [kW]	3.1	0.7	0.80	0.36
total HOM power [MW]	0.93	0.21	0.48	0.22
cryo wall power / cav. [kW]	0.1	2.0	17	50
total cryo power [MW]	<0.5	4.5	<5	<15

grid power consumption - RF & cryo



- ❖ The whole system must be optimized – not one efficiency alone
 - ❖ RF amplifiers & feedback overheads
- ❖ Total ≈ 162 MW + booster ring RF system

O. Brunner

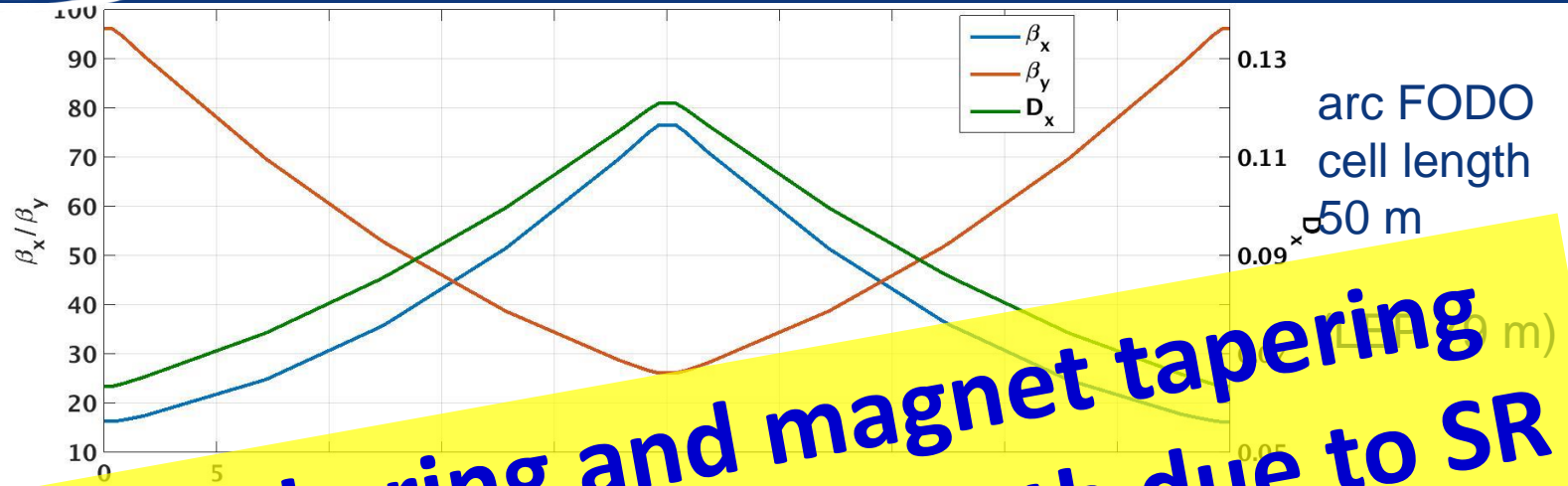
rough estimate of total power [MW]

subsystem	Z	W	H	ttbar
collider total RF power	162	162	155	155
collider cryogenics	1	5	5	15
collider magnets	3	10	24	50
booster RF + cryo	4	4	4	4
booster magnets	0	1	2	5
injector complex	10	10	10	10
physics detectors (2)	25	25	25	25
cooling	15	15	15	15
ventilation	30	30	30	30
total	250	262	270	309

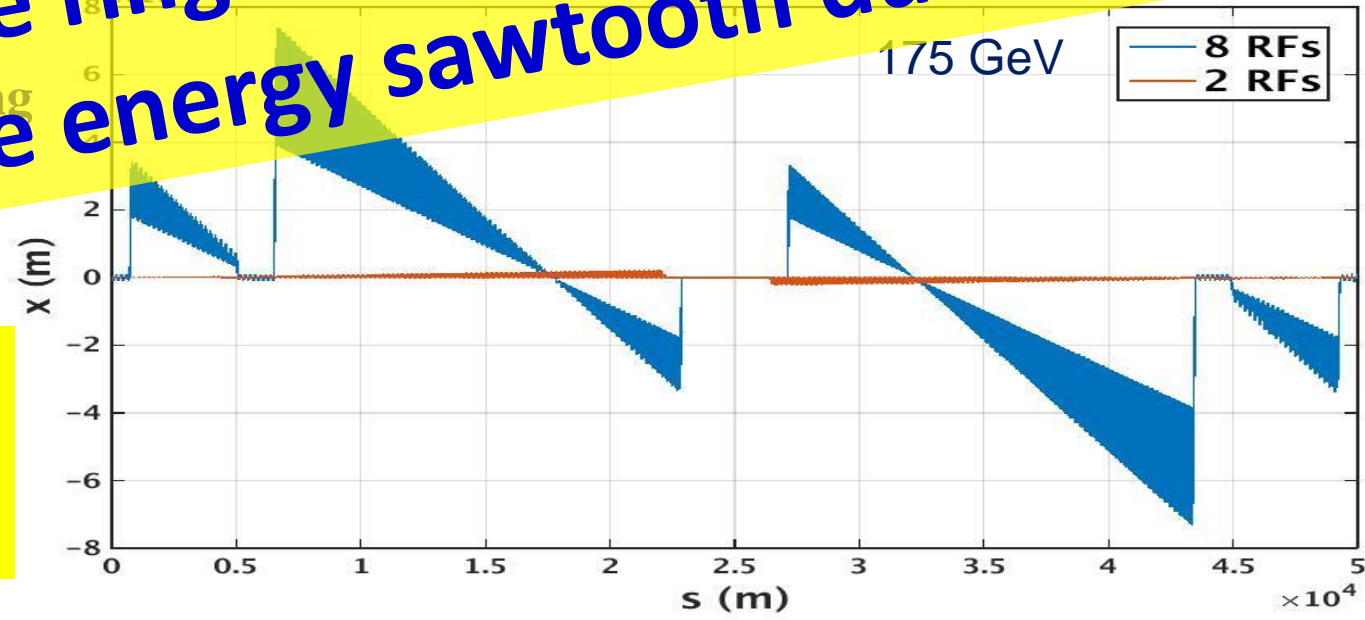
for comparison, CERN LEP complex in 1998 used 237 MW

Also see: M. Ross, "Wall-Plug (AC) Power Consumption of a Very High Energy e⁺/e⁻ Storage Ring Collider," 3 August 2013, <http://arxiv.org/pdf/1308.0735.pdf>; A. Blondel et al., "Comments on "Wall-plug (AC) Power Consumption of a Very High Energy e⁺/e⁻ Storage Ring Collider" by Marc Ross," 12 August 2013, <http://arxiv.org/pdf/1308.2629.pdf>

FCC-ee optics

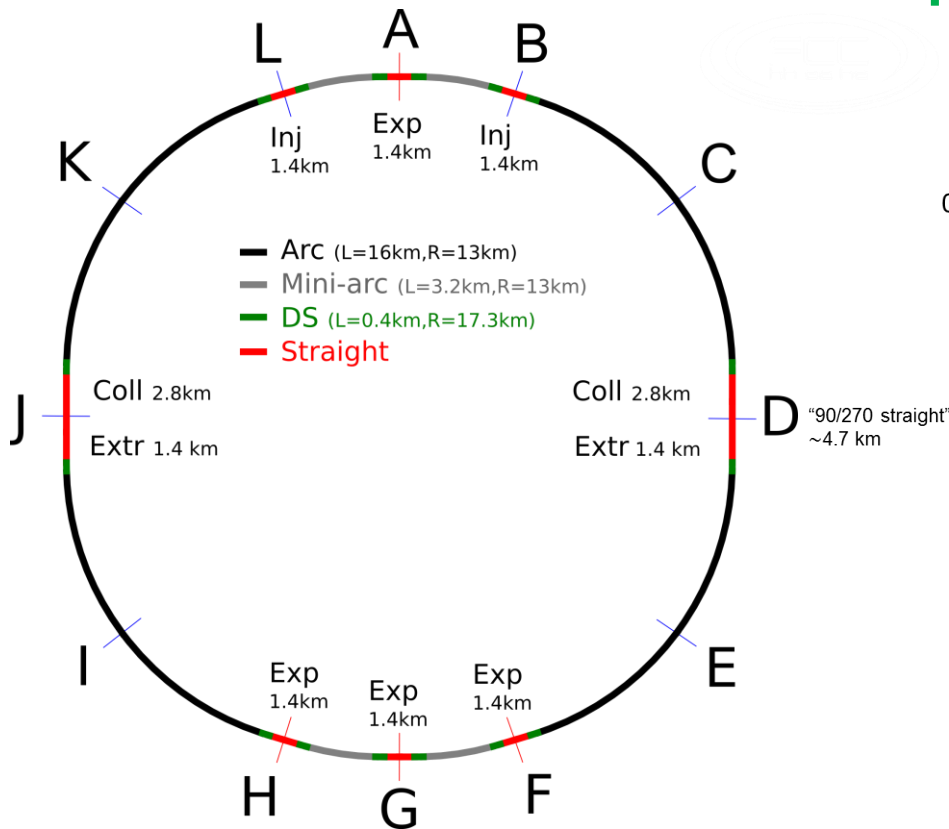


**double ring and magnet tapering
 remove energy sawtooth due to SR**

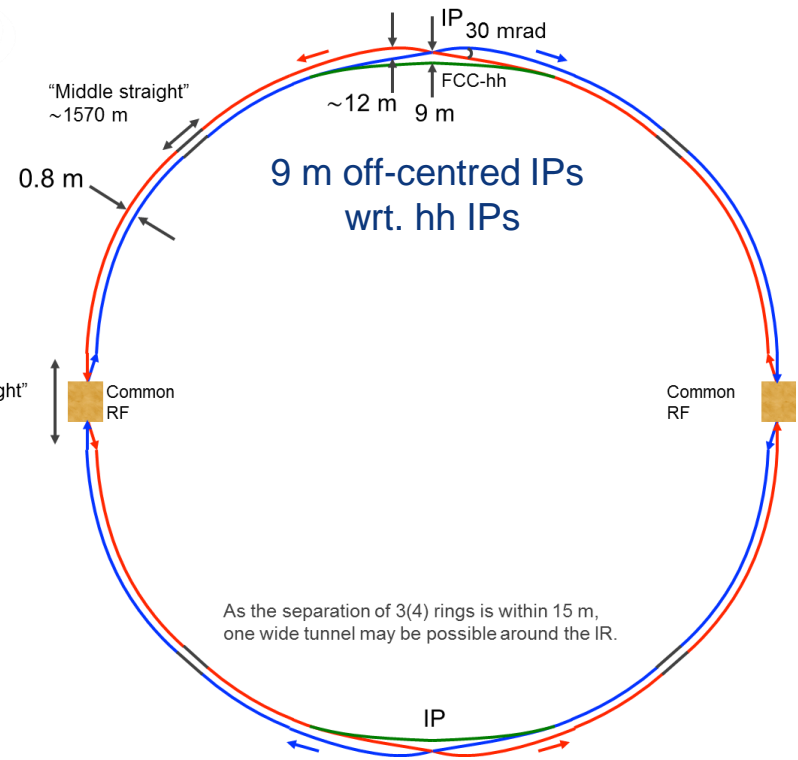


Sandra Aumon,
 Bastian Härer,
 Andreas Doblhamer,
 Bernhard Holzer

FCC-hh



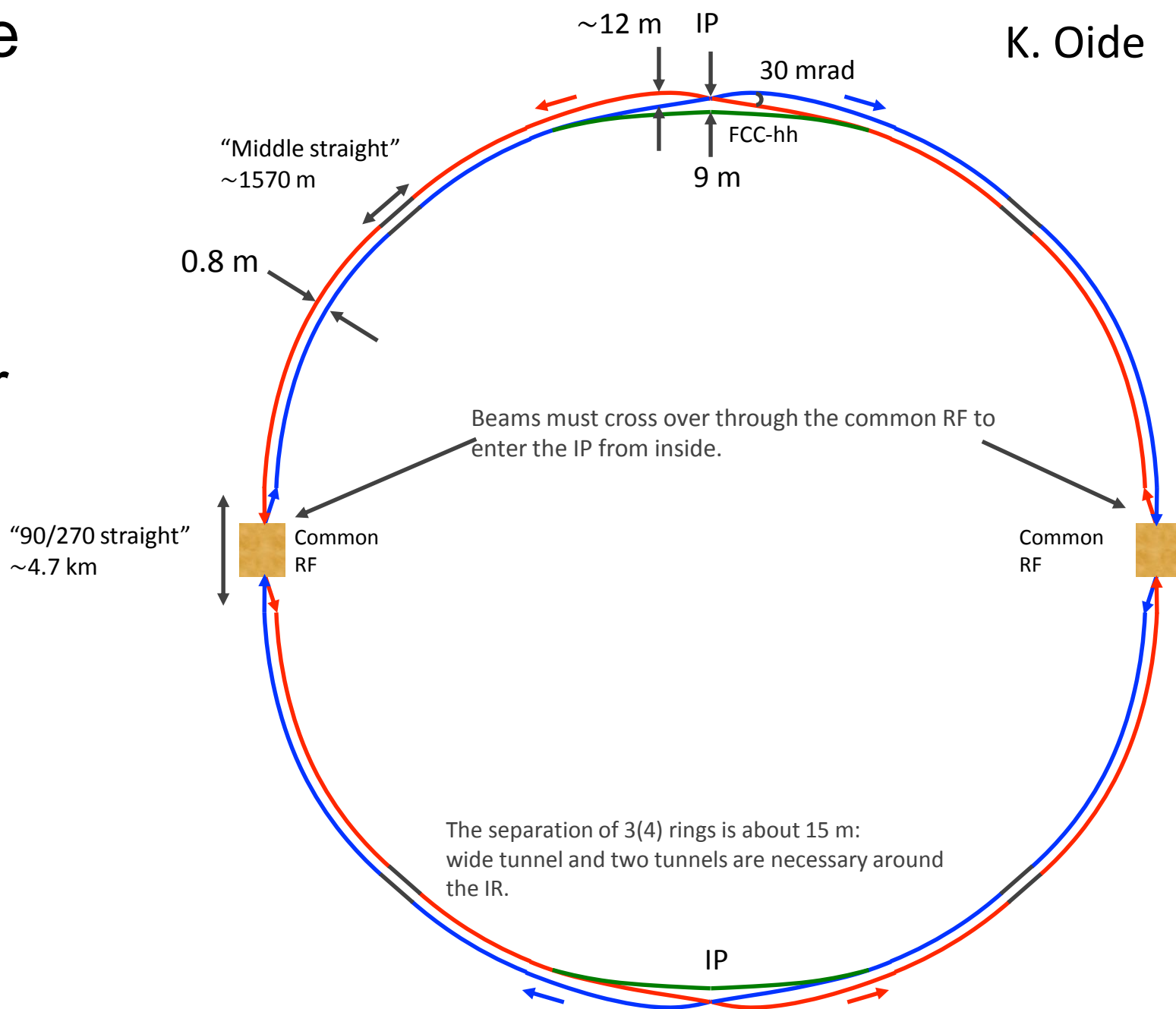
FCC-ee 1, FCC-ee 2, FCC-ee booster (FCC-hh footprint)



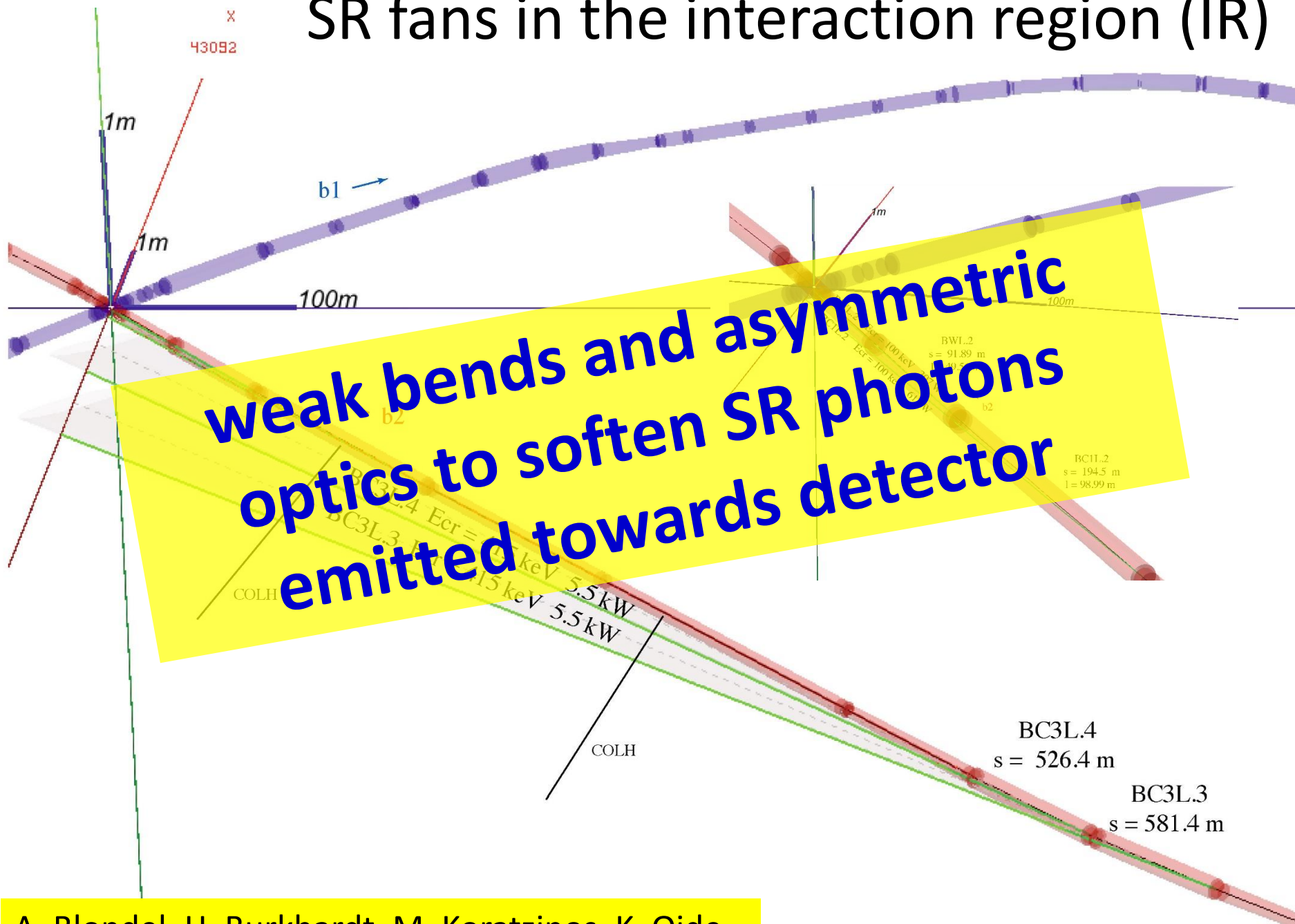
Closed optics solutions for full ring for both machines available

FCC-ee layouts with space for booster

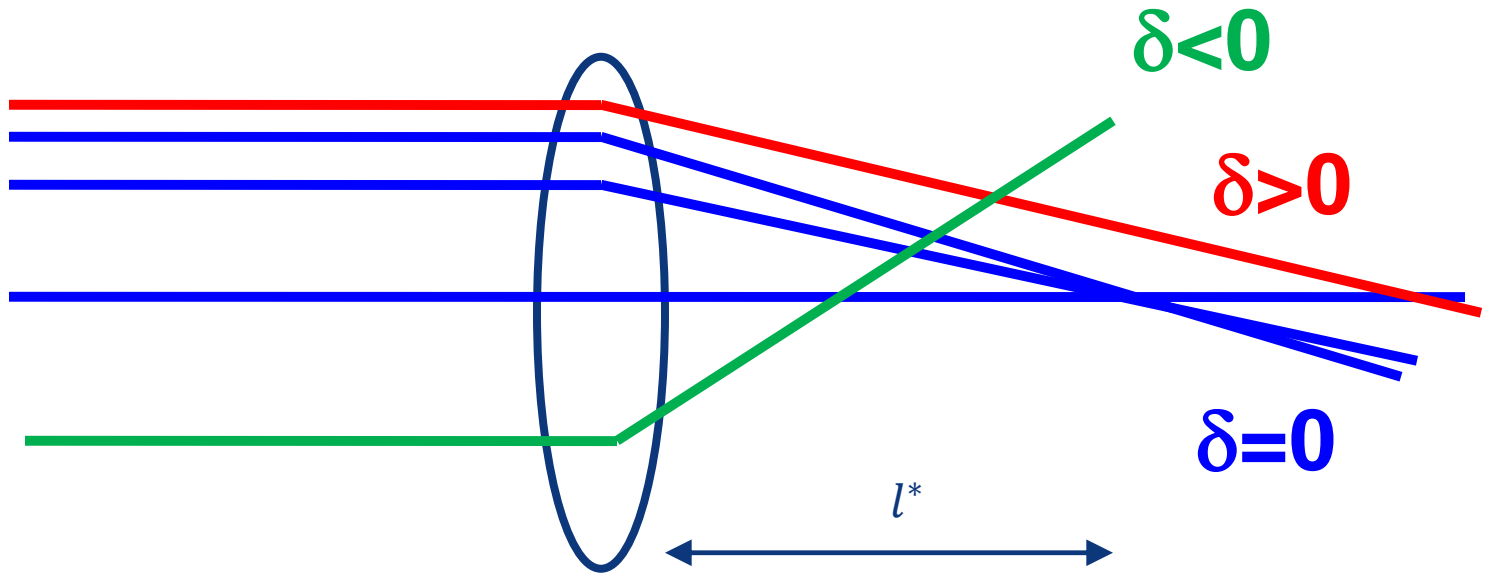
K. Oide



SR fans in the interaction region (IR)



final focus chromaticity



$$\frac{\Delta \sigma_y^*}{\sigma_{y0}^*} = \xi \delta_{rms}$$

$$\sigma_{y0}^* \equiv \sqrt{\beta_y^* \varepsilon_y}, \quad \xi \approx \frac{l^*}{\beta^*}$$

spot size increase due to
(uncorrected) chromaticity,

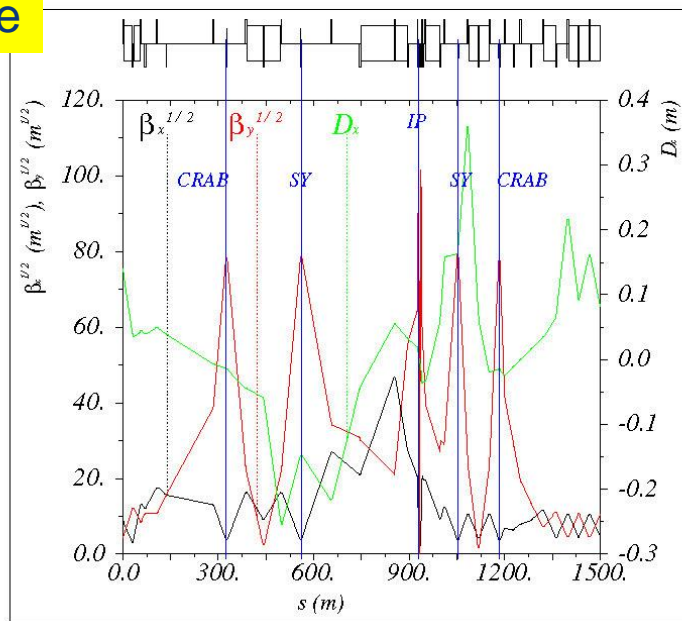
FCC-ee IR optics – two variants

with required momentum acceptance and dynamic aperture
 both feature crab waist optics & local chromatic correction

Interaction Region: KO v. 51-14

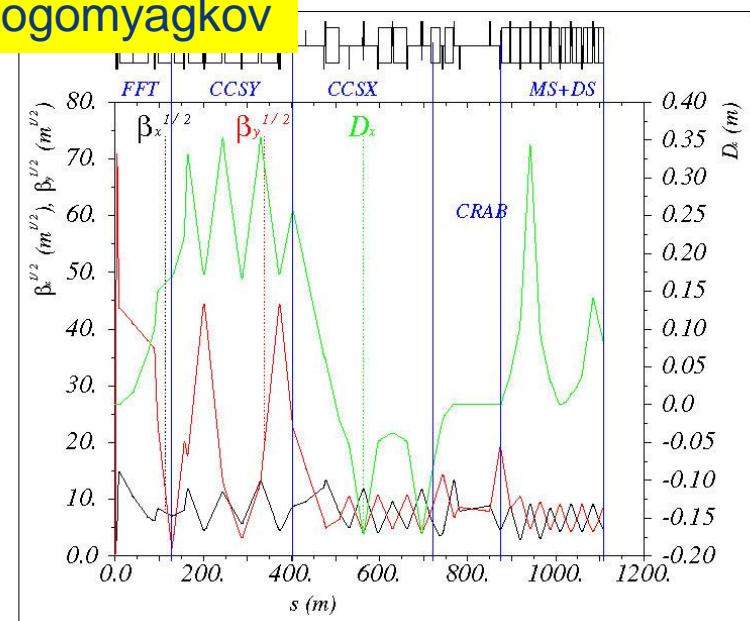
Interaction Region: AB v. 8-1 ($\beta_x^* = 1 \text{ m}$, $\beta_y^* = 2 \text{ mm}$)

K. Oide



synchrotron radiation $E_{\gamma,c} \leq 100 \text{ keV}$,
 2 sextupoles: vert. chromatic
 correction + “virtual” crab waist

A. Bogomyagkov



synchrotron radiation $E_{\gamma,c} \leq 400 \text{ keV}$,
 5 sextupoles: hor.+ vert. chromatic
 correction + crab waist

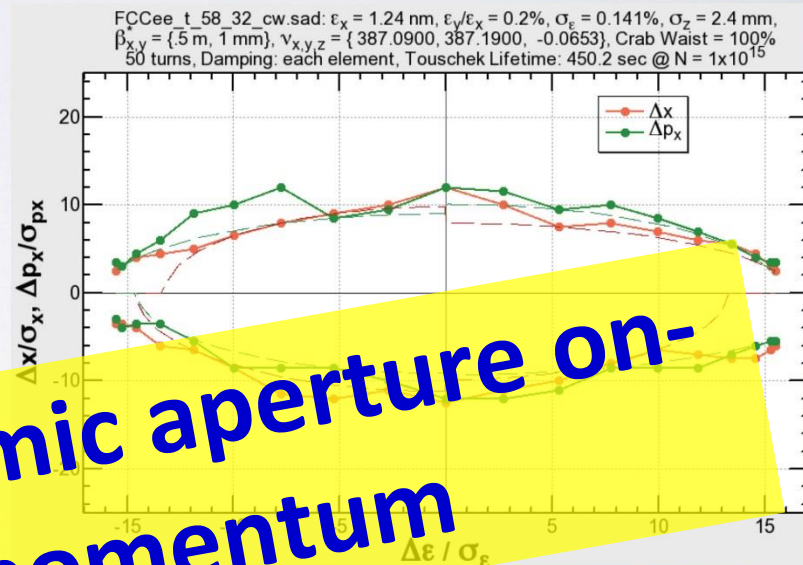
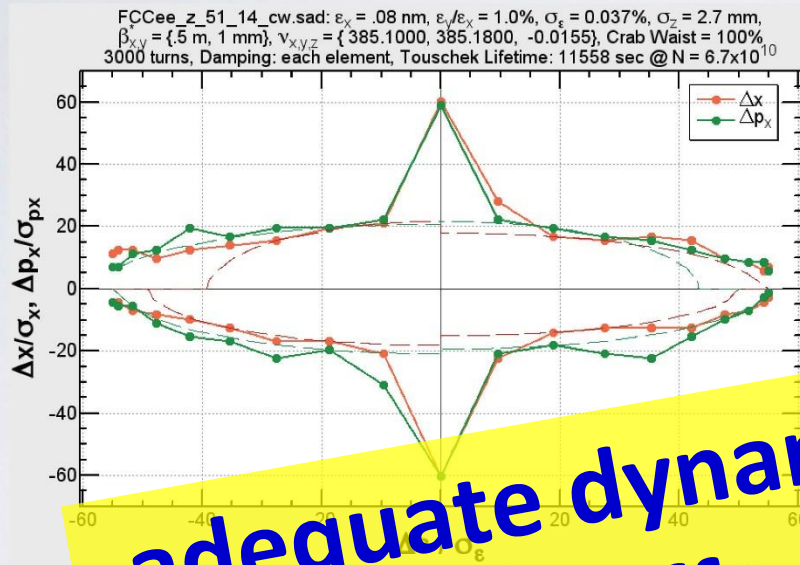
dynamic aperture

K. Oide

$$\beta_{x,y}^* = (0.5 \text{ m}, 1 \text{ mm})$$

$E_{\text{beam}} = 45.6 \text{ GeV}$
3,000 turns

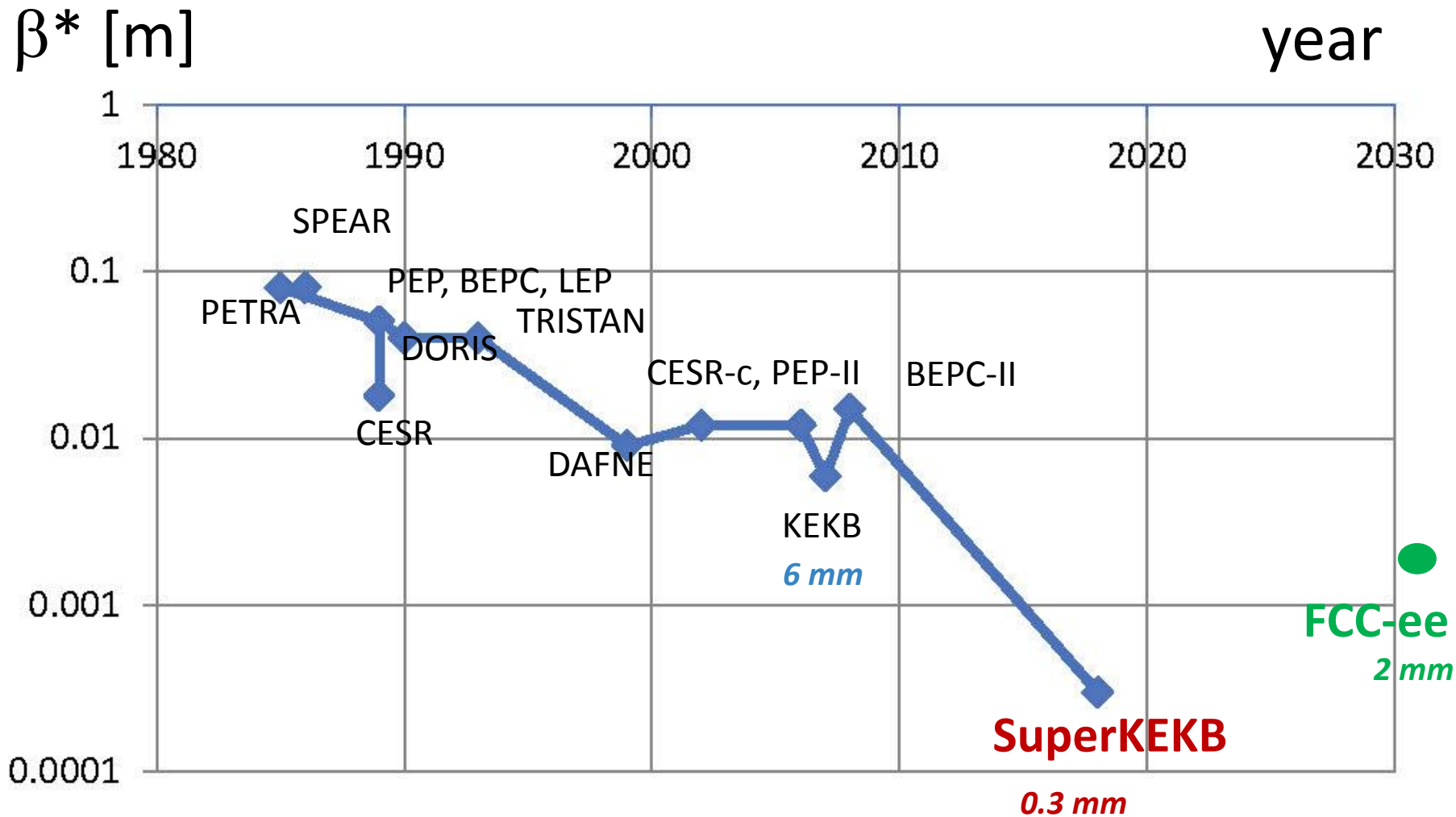
$E_{\text{beam}} = 175 \text{ GeV}$
50 turns



adequate dynamic aperture on-
and off-momentum

- Sextupoles must be optimized at each beam energy.
- 3,000 turns are enough to determine the aperture at 45.6 GeV (long. damping = 1,500 turns).
- $\pm 2\%$ acceptance is not necessary for beamstrahlung, but may be useful for synchrotron injection.
- The on-momentum peak of the transverse aperture is recovered due to weaker radiation.

β_y^* evolution over 40 years



entering a new regime for ring colliders –
SuperKEKB will pave the way towards $\beta^* \leq 2$ mm

SuperKEKB: extremely low β^*

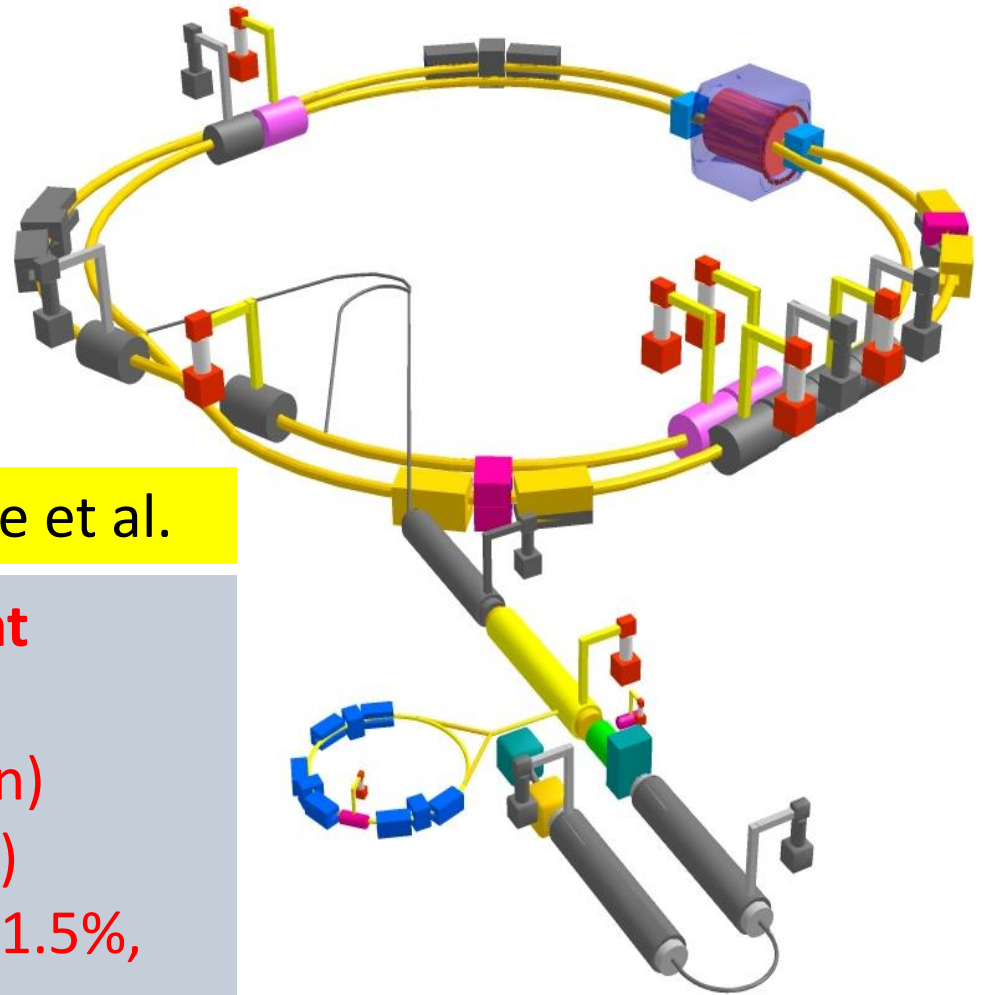
$$I_{e^+}=3.6 \text{ A}, I_{e^-}=2.6 \text{ A}$$

$$P_{\text{SR}} \sim 13 \text{ MW}$$

$$C = 3 \text{ km}$$

beam commissioning
starting this year

K. Oide et al.



top up injection at high current

$\beta_y^* = 300 \mu\text{m}$ (FCC-ee: 1 mm)

lifetime 5 min (FCC-ee: ≥ 20 min)

$\varepsilon_y/\varepsilon_x = 0.25\%$ (similar to FCC-ee)

off momentum acceptance ($\pm 1.5\%$,
similar to FCC-ee)

e^+ production rate ($2.5 \times 10^{12}/\text{s}$, FCC-
ee: $< 1.5 \times 10^{12}/\text{s}$ (Z cr.waist))

*SuperKEKB goes beyond
FCC-ee, testing all concept*

*polarization,
energy calibration,
and mono-chromatization*

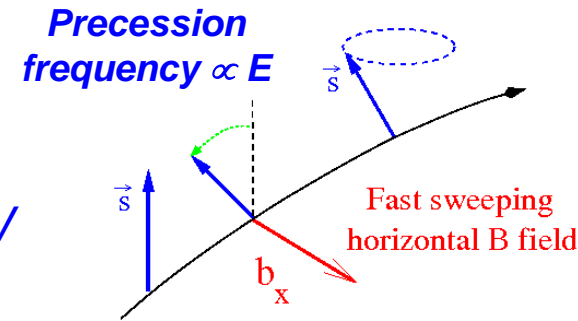
two primary interests:

accurate energy calibration using resonant depolarization \Rightarrow measurement of M_Z , Γ_Z , M_W

- o *appealing feature* – δM_Z , $\delta \Gamma_Z \sim 0.1 \text{ MeV}$, $\delta M_W \sim 0.3 \text{ MeV}$

physics with longitudinally polarized beams

- o *transverse polarization must be rotated into the longitudinal plane using spin rotators (see e.g. HERA)*



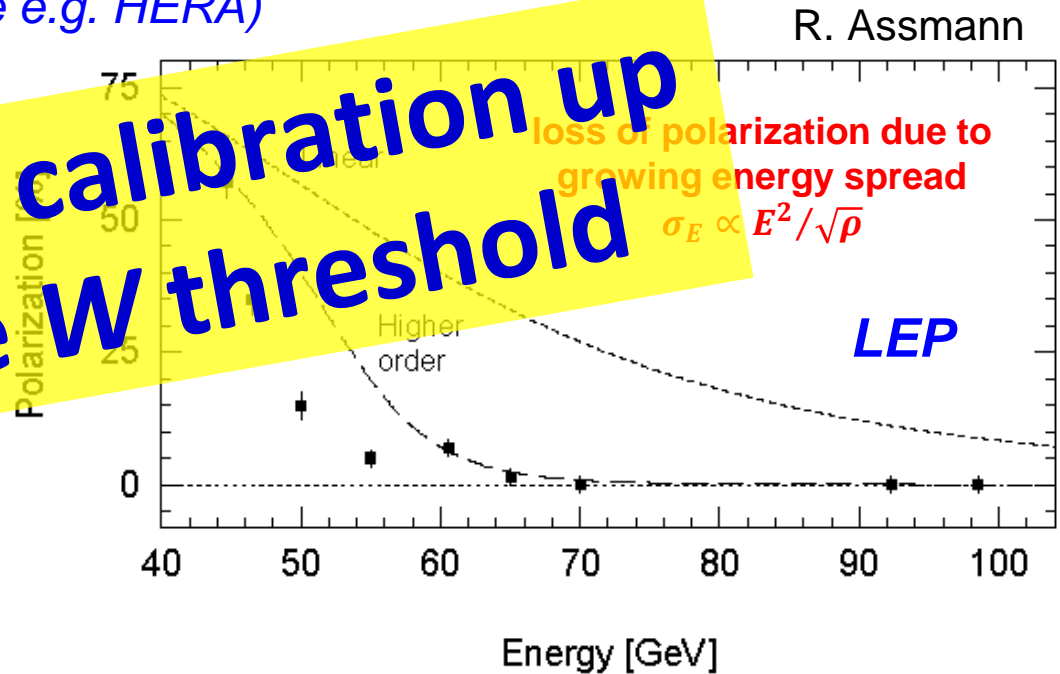
scaling from LEP observations:

polarization expected up to the WW threshold

LEP like calibration up to the W threshold

integer spin resonances are spaced by 440 MeV:

energy spread should remain below $\sim 60 \text{ MeV}$



transverse polarization build-up (Sokolov-Ternov) is slow at FCC-ee
(large bending radius ρ)

build-up is ~40 times
slower than at LEP

wigglers may lower τ_p to ~12 h,
limited by $\sigma_E \leq 60$ MeV and power

*due to power loss the wigglers can
only be used to pre-polarize some
bunches (before main injection)*

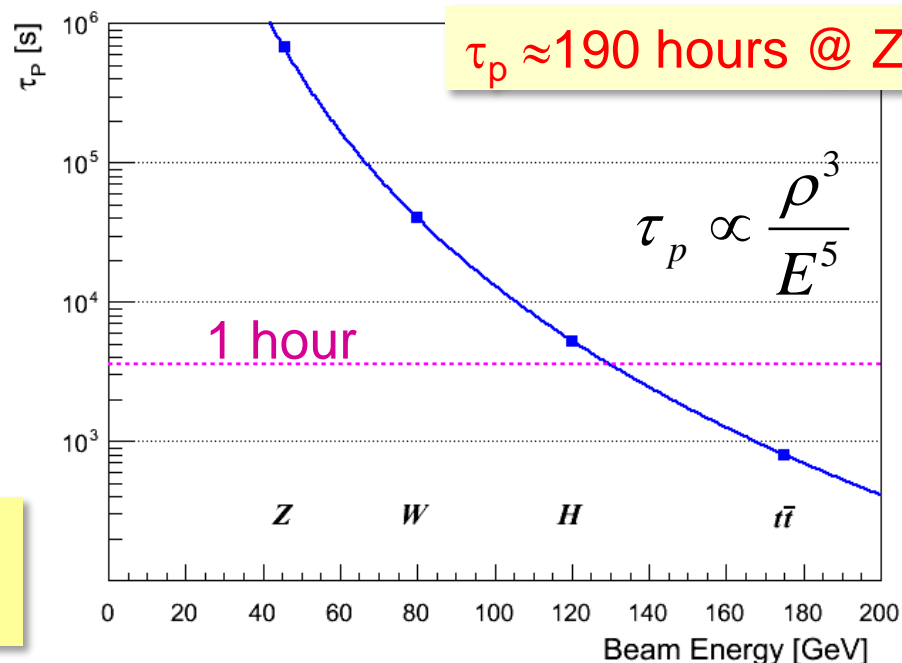


≈ OK for energy calibration
(few % P sufficient)

longitudinal polarization: levels of $\geq 40\%$ required on both beams;
excellent resonant compensation needed

*expected to be difficult, requires spin rotators or snakes, most likely only
possible at lower intensity and luminosity*

SLIM, PETROS, SITF etc. simulations



A. Blondel, U. Wienands,
E. Gianfelice, J. Jowett,
R. Rossmanith, J. Wenninger

at Z and W : frequent resonant-depolarization measurements with non-colliding bunches

- ✓ much better resolution than at LEP, few tens of keV
- ✓ measurement of energy spread?
- ✓ extrapolation from average to individual IPs
- ✓ OR: injecting polarized beam

at higher energies, H and $t\bar{t}$:

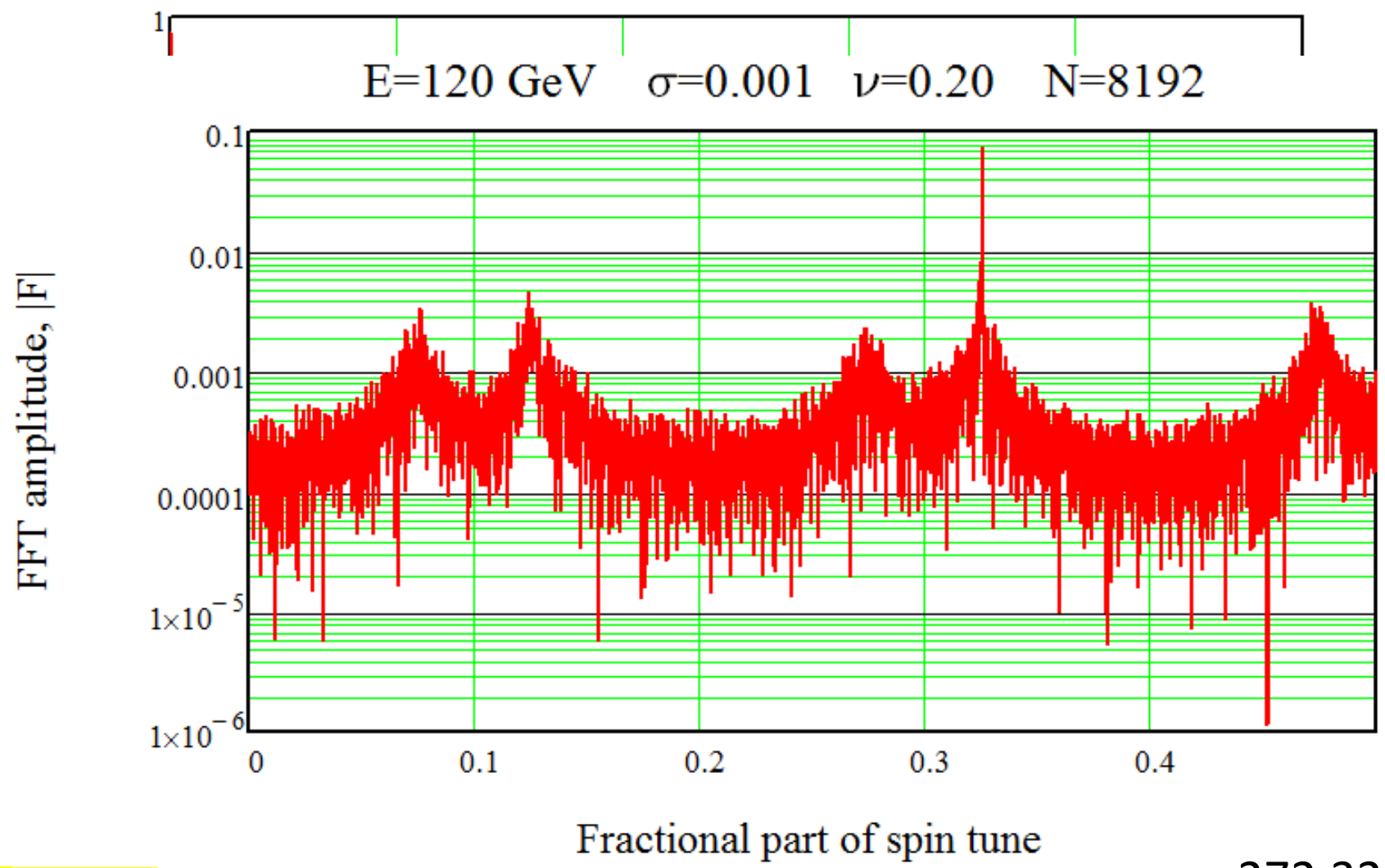
- ✓ use physics measurements
- ✓ other? (laser back scattering / spectrometer?)
- ✓ OR: injecting polarized beam

injecting polarized beam & free spin precession

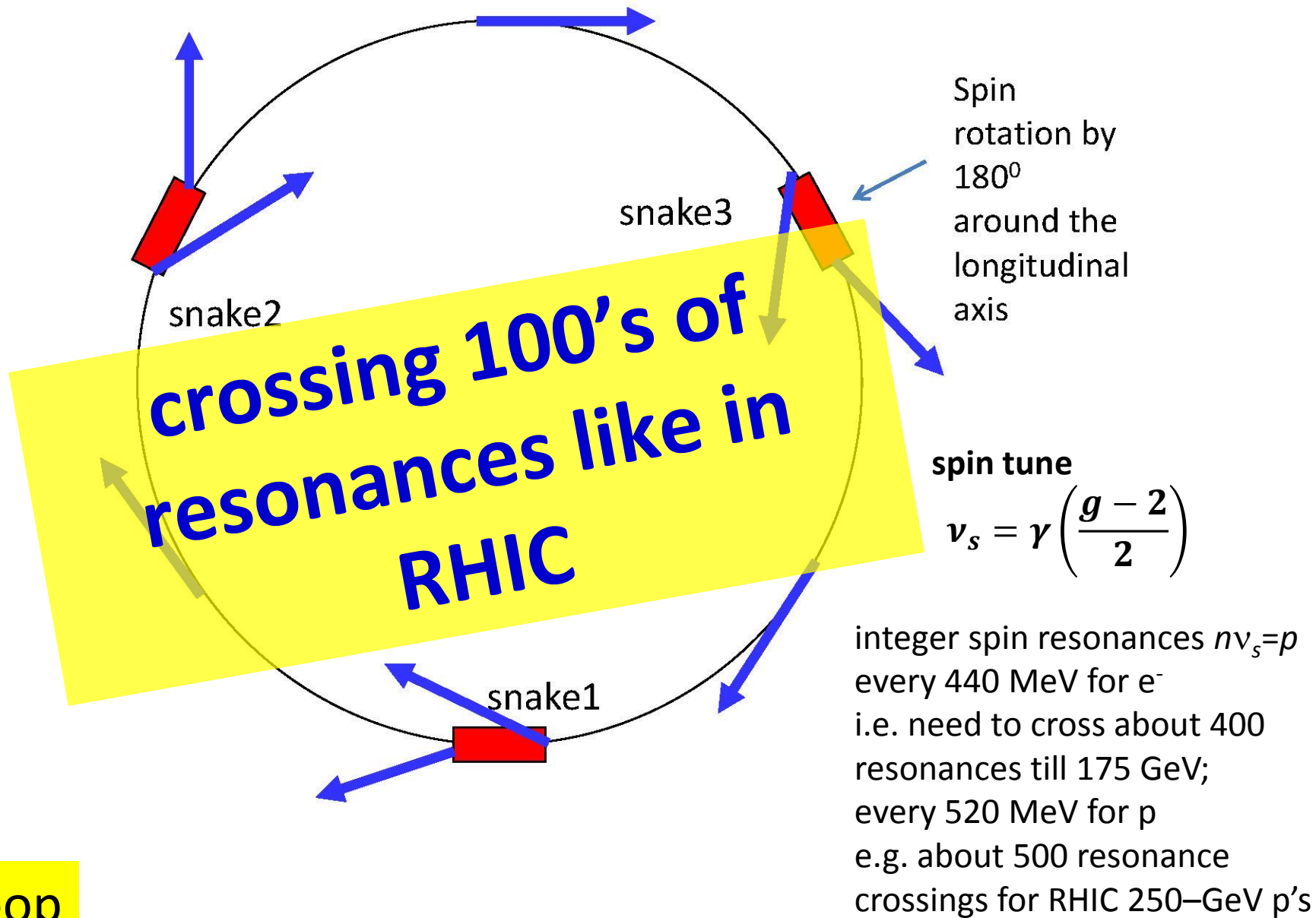
120 GeV

$E=120 \text{ GeV}, \sigma=0.001, \nu=0.2, \tau=72 \text{ turns}$

$E=120 \text{ GeV} \quad \sigma=0.001 \quad \nu=0.20 \quad N=8192$



preserving polarization in the booster



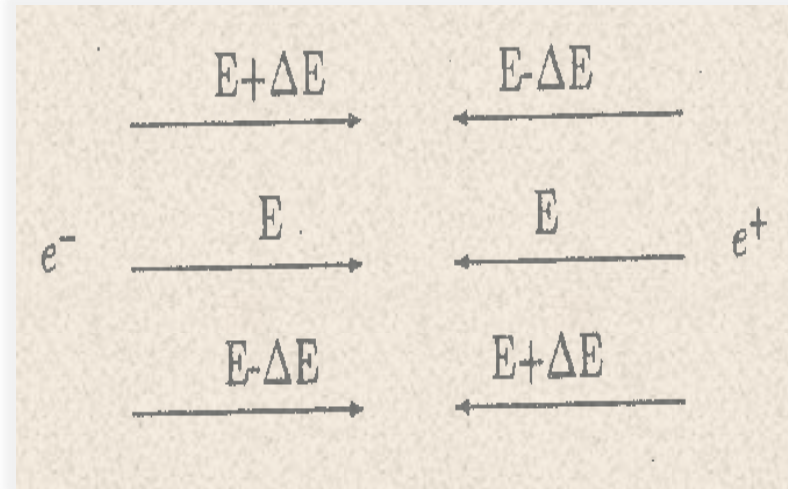
mono-chromatization at 2x63 GeV?

direct s channel Higgs production $e^+e^- \rightarrow H$

rms beam energy spread at 63 GeV ~ 30 MeV
total width of SM Higgs $\Gamma \sim 4$ MeV

effective collision energy spread is decreased
by introducing opposite-sign IP dispersion

$$\frac{\sigma_W}{W} = \sqrt{\frac{2\varepsilon_x}{\left(\frac{D_x^*}{\beta_x^*} + \frac{\varepsilon_x}{\sigma_\epsilon^2}\right)}}$$



first proposed by A. Renieri (1975); historical studies for VEPP4, SPEAR, LEP, τ -c factory; never tested experimentally

reducing cm energy spread x1/10 w/o loss of luminosity?!
implementation for crab-waist scheme?

summary

SR effects of LEP
high currents of KEKB and PEP-II
top-up of KEKB and PEP-II
crab waist of DAFNE
low β_y^* of SuperKEKB
 e^+ source of KEKB
cryo availability of LHC
spin gymnastics of RHIC (?)



FCC-ee

individual parameters
mostly relaxed compared
with those in “demonstrator
machines”

baseline **luminosity performance predicted w confidence**;
further increases possible

optics footprint matched to the hadron collider layout

FCC-ee would bring the **tunnel**, the **infrastructure**, the
time needed for high-field magnet production, and
possibly also an even stronger **physics motivation** (and
precise target energy) **for FCC-hh**

“An e^+e^- storage ring in the range of a few hundred GeV in the centre of mass can be built with present technology...” “...the most useful project on the horizon.”



B. Richter, 1976



...surely great times ahead!



spare slides

chromaticity in selected FF systems

project	status	β_y^* [mm]	l^* [m]	l^*/β_y^*	σ_y^* [nm]
LEP	measured	50	3.7	74	3200
LHC	measured	600	23	38	16000
KEKB	measured	6.0	2.4	400	940
FCC-hh	design	1100	46	42	7000
S-KEKB	design	0.3	1.5	5000	50
FCC-ee	design	2.0	2.2	1100	50
CepC	design	1.2	1.5	1250	150
SLC	measured	2.0	2.2	1100	500
FFTB	measured	0.167	0.4	2400	70
ATF2	measured	0.1	1.0	10000	~40
ILC	design	0.4	3.5	8750	6
CLIC	design	0.09	3.5	39000	1

circular

linear

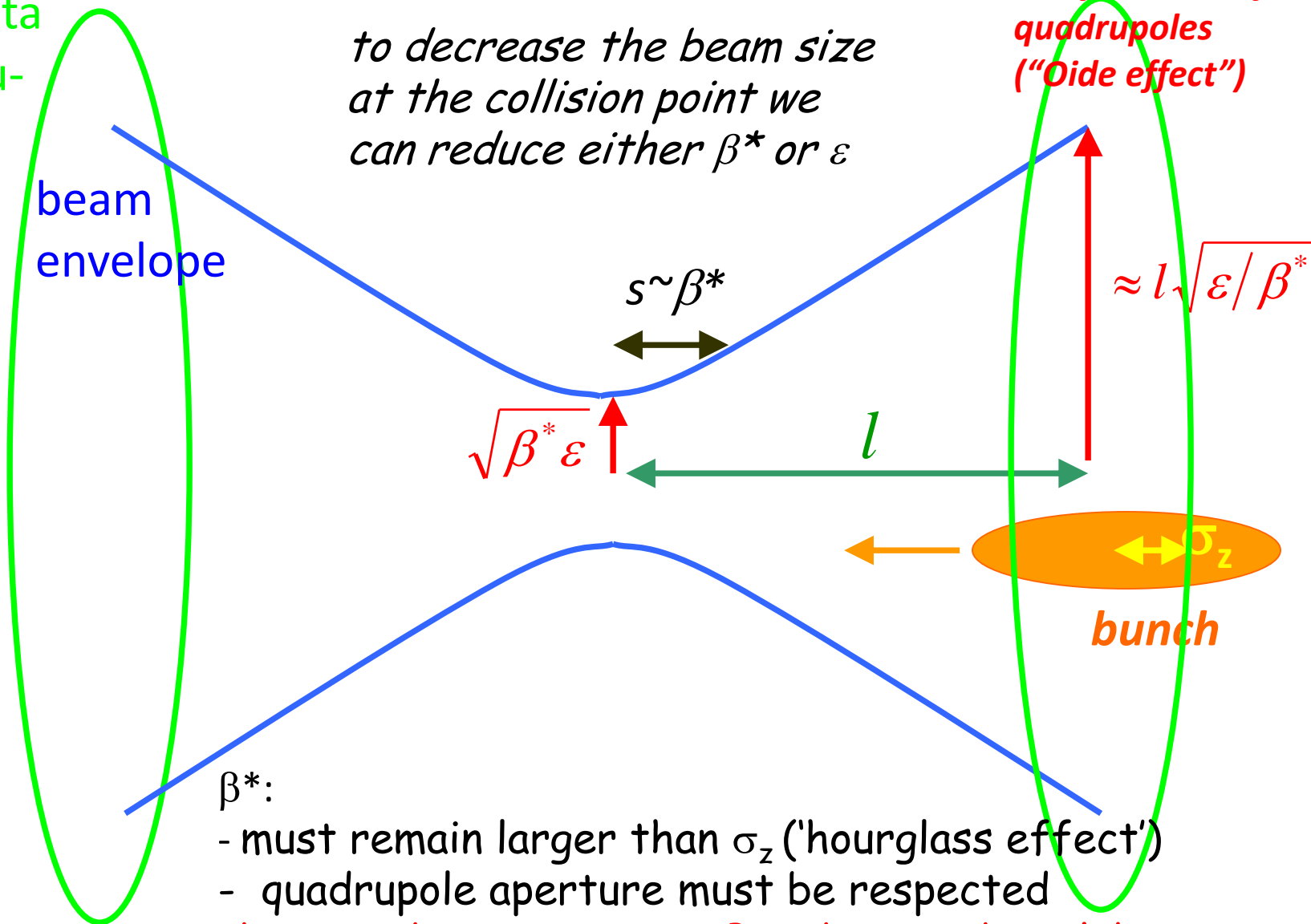
limits on collider spot size

other limits from beam-beam effects and from SR in final quadrupoles ("Oide effect")

to decrease the beam size at the collision point we can reduce either β^ or ε*

low-beta quadrupole

beam envelope



β^* :

- must remain larger than σ_z ('hourglass effect')
- quadrupole aperture must be respected

reducing ε decreases σ at IP and at quadrupole!

coherent synchrotron radiation (CSR)?

at wave lengths $\lambda > 2\pi\sigma_z \sim 0.012$ m (or $E_\gamma < 0.1$ meV)
all e^- in an FCC-ee bunch could radiate coherently

$$P_{SR,coh} \approx N_b P_{SR}$$

at smaller wave lengths still portions of the bunch could radiate coherently ("microbunching instability")

large bending radius and vacuum chamber suppress CSR effects

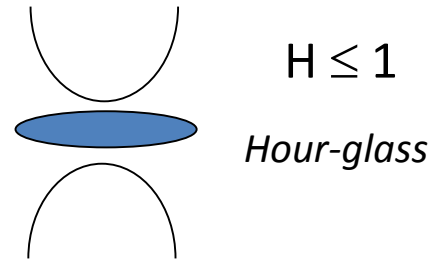
FCC-ee vacuum chamber (full width w , height $h \sim 6$ cm)

suppresses radiation at* $\lambda > 2 \sqrt{\frac{h^2 w}{\rho}} \approx 0.00028$ m
(or $E_\gamma < 4$ meV)

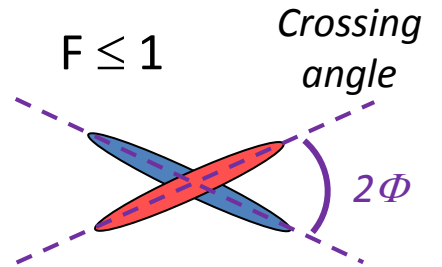
*Y. Derbenev et al., DESY TESLA FEL 95-05, 1995

luminosity scaling: larger E & ρ

$$e f k N = \text{beam current} \propto \frac{1}{E^4}$$



$$L = \frac{f k N^2}{4\pi\sigma_x\sigma_y} F H$$



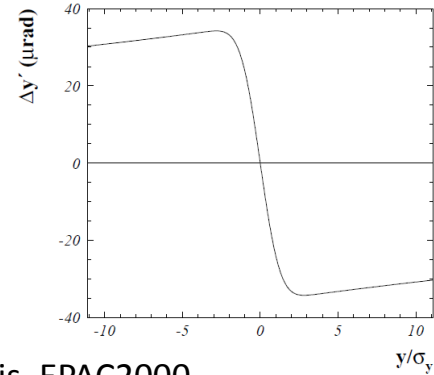
$$\xi_y \propto \frac{\beta_y^* N}{E\sigma_x\sigma_y} \leq \xi_y^{\max}(E) \quad \text{Beam-beam parameter}$$

- σ = beam size
- k = no. bunches
- f = rev. frequency
- N = bunch population
- P_{SR} = synch. rad. power
- β^* = betatron fct at IP
(beam envelope)

$$L \propto \frac{\rho P_{SR}}{E^3} \frac{\xi_y}{\beta_y^*}$$

luminosity scaling: damping

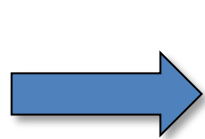
- beam-beam parameter ξ measures strength of field sensed by the particles in a collision
- beam-beam parameter limits are empirically scaled from LEP data (4 IPs)



$$\xi_y \propto \frac{\beta_y^* N}{E \sigma_x \sigma_y} \leq \xi_y^{\max}(E)$$

$$\xi_y^{\max}(E) \propto \frac{1}{\tau_s^{0.4}} \propto E^{1.2} \quad \text{x4.5}$$

FCC-ee
vs LEP



x4

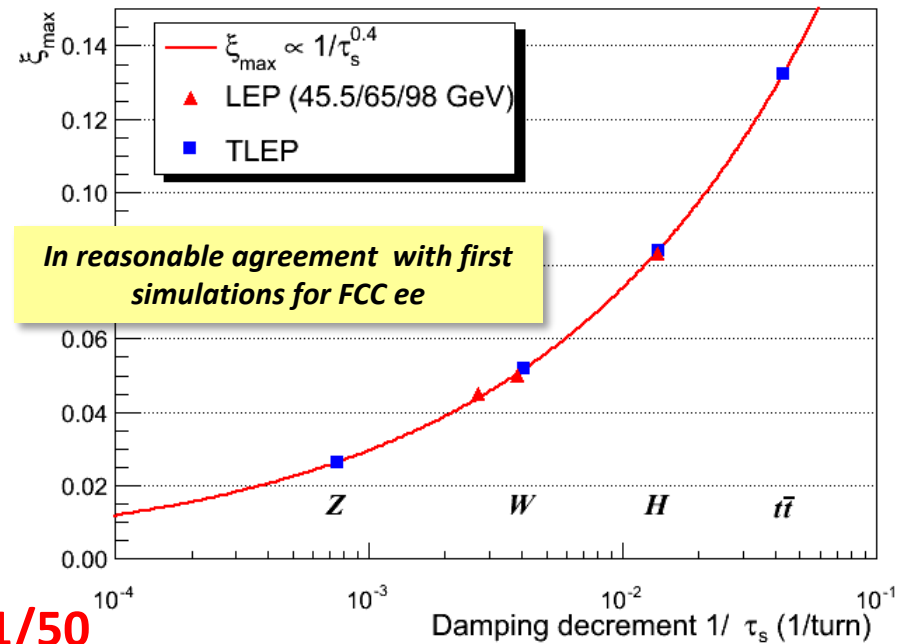
$$L \propto \frac{\rho P_{SR}}{E^{1.8}} \frac{1}{\beta_y^*}$$

<x2

x1/25-1/50

→ extremely high luminosity

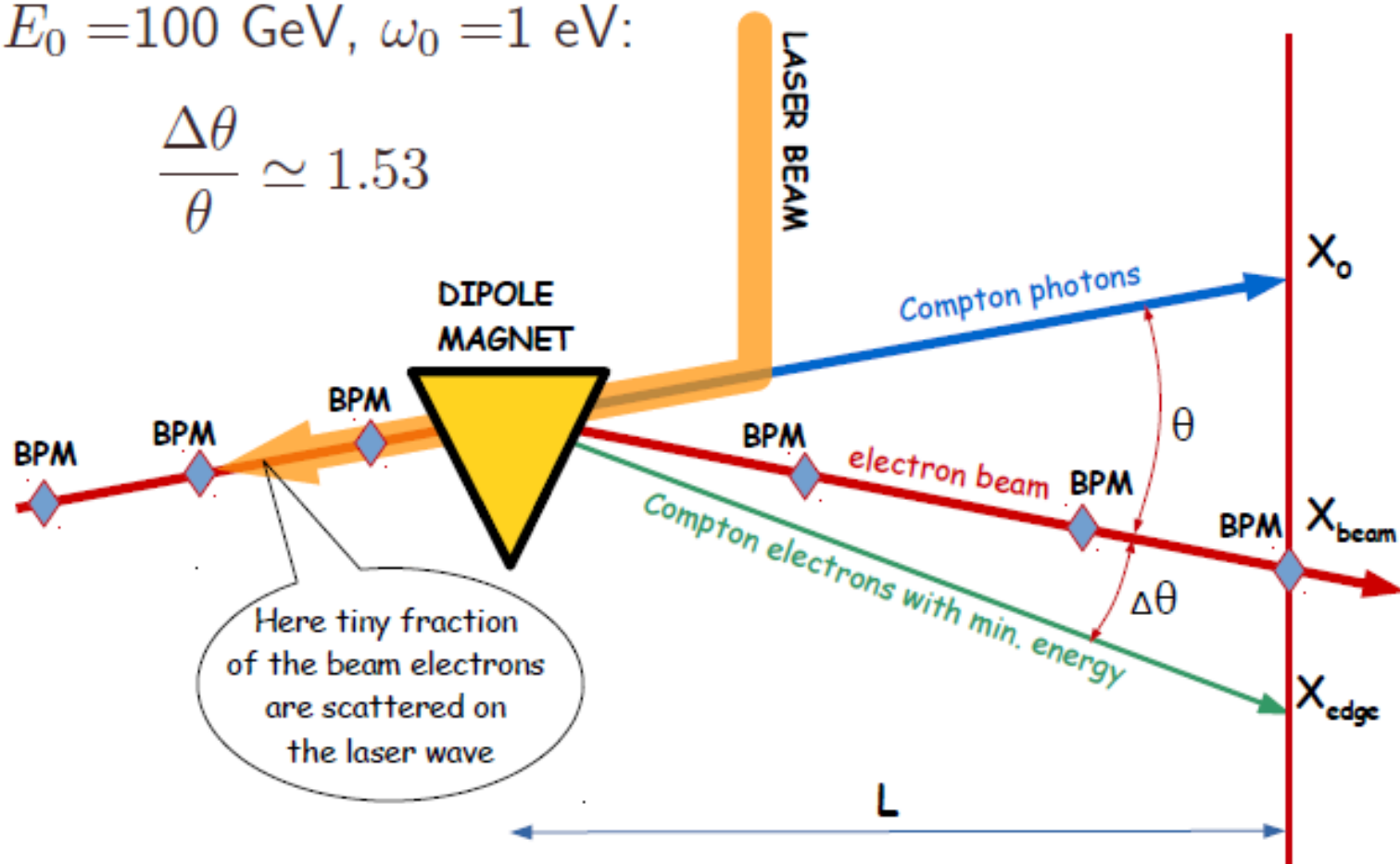
R. Assmann & K. Cornelis, EPAC2000



spectrometer with Compton scattering

$$E_0 = 100 \text{ GeV}, \omega_0 = 1 \text{ eV:}$$

$$\frac{\Delta\theta}{\theta} \simeq 1.53$$



$$\text{Access to the beam energy: } E_0 = \frac{\Delta\theta}{\theta} \times \frac{m^2}{4\omega_0}$$