



Measurement of B_c properties at CDF

(mass, lifetime and cross section)

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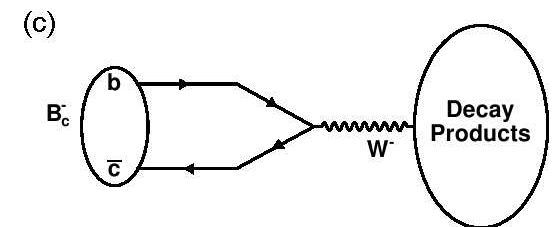
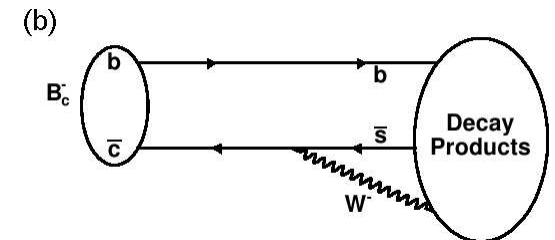
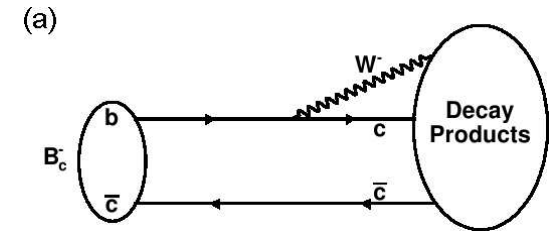
DPF 2009 WSU Detroit MI

July 26-31, 2009

introduction

B_c^+ meson is composed of a \bar{b} and c quarks

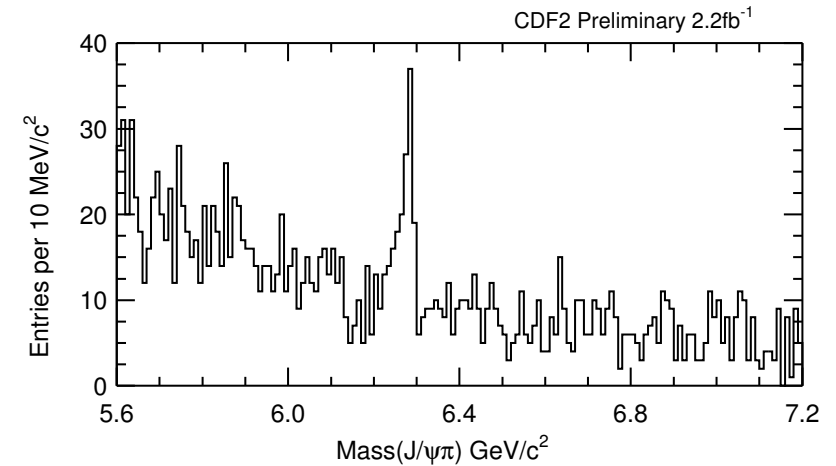
- Double heavy B_c^+ properties are interesting to compare with heavy-light mesons, such as B^+ , B^0 or B_s^0
- Partial width from decays of either quark (a,b), or annihilation (c) make significant contribution to the total width:
 - predicted lifetime for B_c^+ is 0.55 ± 0.15 ps (arXiv:hep-ph/0308214v1)
 - lifetimes of other B mesons are 3 times longer
- Rich spectroscopy. $B_c^+ \rightarrow J/\psi + \mu/e + \nu$ decay mode predicted to have a largest branching fraction:
 - used for lifetime and cross section measurements





B_c^+ mass measurements at CDF

- B_c^+ mass predictions:
 - nonrelativistic potential models: 6247-6286 MeV/c^2
 - lattice QCD calculations: $6304 \pm 12 \text{ MeV}/c^2$
- Precision measurements are needed to test these predictions
- B_c^+ is too heavy to be produced at e^+e^- colliders
- CDF has a capability to make most precise mass measurement of B_c^+ using hadronic decay mode: $B_c^+ \rightarrow J/\psi \pi^+$



- Integrated luminosity: 2.2 fb^{-1}
- A signal: 108 ± 15 candidates
- $m(B_c^+) = 6275.6 \pm 2.9(\text{stat}) \pm 2.5(\text{syst}) \text{ MeV}/c^2$
- [Phys.Rev.Lett. 100,182002, 2008](#)
- Studies are extended to higher luminosity



$c\tau$ and $\sigma(B_c)$ measurement concepts

Lifetime:

- Undetected ν lead to the missing momentum in B_c decays
- We measure a pseudo-decay length:

$$ct^* = \frac{M(B_c)L_{xy}(J/\psi+l)}{p_T(J/\psi+l)}$$

- Define K factor that relates ct of B_c system to ct^* :

$$Kct^* = ct, \text{ where } ct = \frac{mL_{xy}}{p_T}$$

- Obtain K distribution from Monte Carlo
- Write model for ct^* in terms of B_c lifetime, $c\tau$, and distributions of K, $H(K)$:

$$F_{B_c}(ct^*, \sigma) = \sum_i H(K_i) \frac{K_i}{c\tau} e^{-\frac{K_i ct^*}{c\tau}} \theta(ct^*) \otimes G(\sigma)$$

where σ is an error of ct^* in event-by-event base

Cross section:

- Perform measurements for both mesons: B_c and B^+ and calculate a ratio:

$$\frac{\sigma(B_c^+) * BR(B_c^+ \rightarrow J/\psi + \mu^+ + \nu)}{\sigma(B^+) * BR(B^+ \rightarrow J/\psi + K^+)} = \frac{N(B_c^+)}{N(B^+)} \times \epsilon_{rel}$$

- Advantages:

- $\sigma(B^+)$ and $BR(B^+ \rightarrow J/\psi K^+)$ are well measured
- Most of uncertainties for $J/\psi \rightarrow \mu^+ \mu^-$ and some for 3-rd track in $J\psi + Track$ system would be canceled

- For this analysis we use $B_c^+ \rightarrow J/\psi \mu^+ \nu$ where selection cuts require a high quality third muon

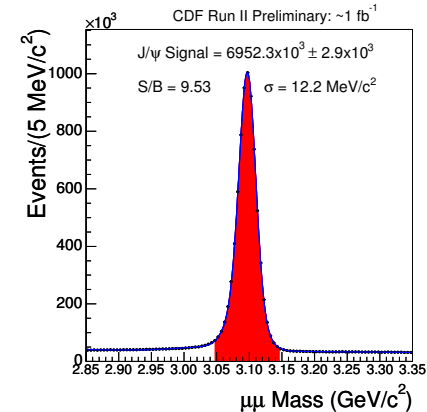


Analysis overview

Reconstruct $J/\psi \rightarrow \mu^+ \mu^-$ decays:

- Data: use an inclusive J/ψ trigger stream with integrated luminosity of 1 fb^{-1}
- Look for dimuons from $J/\psi \rightarrow \mu^+ \mu^-$ within of $|\eta| < 1.0$

Dimuons from red area used as an input for both analysis



Reconstruct:

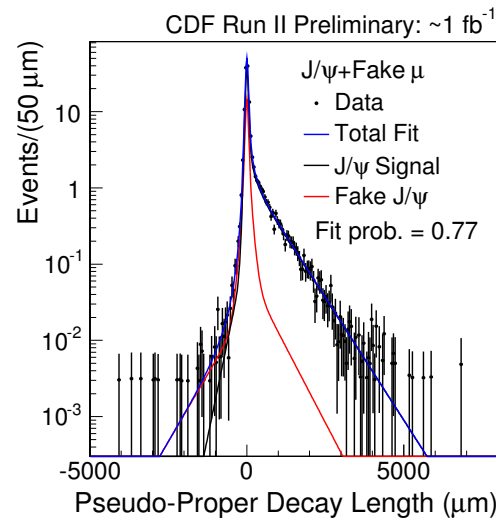
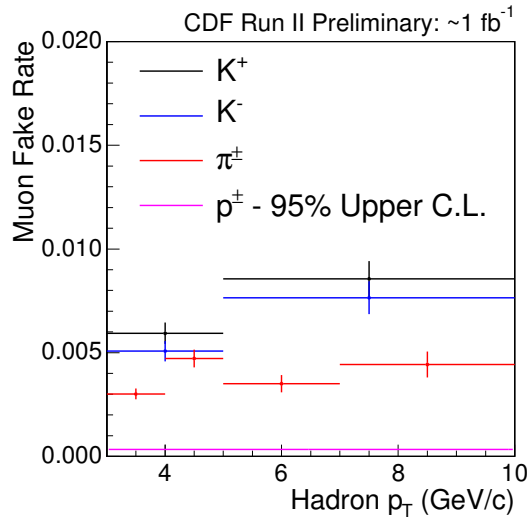
- $B^+ \rightarrow J/\psi + K^+$ (for both analysis: background normalization and ratio calculation)
- $B_c^+ \rightarrow J/\psi + l^+$ (where l either μ/e for lifetime and μ for cross section)

Backgrounds, common for both analysis:

- Misidentified J/ψ : continuum J/ψ background from $J/\psi + \mu/e$ system.
- Misidentified third muon: it can be caused by π or K hadrons due to decays-in-flight or punch through calorimetry and a steel absorber of 3.3 interaction lengths.
- $b\bar{b}$ background. The J/ψ and l^+ originate from different b jets in same event.



Backgrounds, continue



Left: probabilities to mimic a μ

- $D^{*+} \rightarrow D^0 \pi^+ \rightarrow K^- \pi^+ \pi^+$ for π and K
- $\Lambda^0 \rightarrow p^+ \pi^-$ for protons

Right: ct^* model for misidentified third muon background

Backgrounds, specific for each analysis:

	lifetime	cross section
Other modes of B_c^+ with 3μ in final state: $\psi(2S)\mu^+ \dots \rightarrow J/\psi\mu$	included	subtracted
Misidentified e^\pm - if $\pi/K/\bar{p}$ satisfied e^\pm likelihood (calorimeter)	yes	n/a
Residual conversion - electrons from γ -conversion or $\pi^0 \rightarrow e^\pm + \dots$	yes	n/a
Prompt J/ψ - additional $J/\psi l^+$ that are not accounted above	yes	negligible

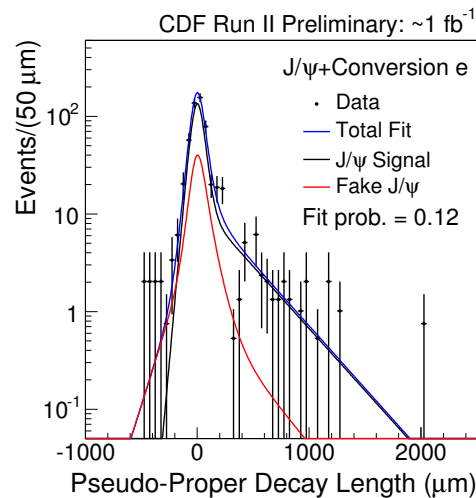
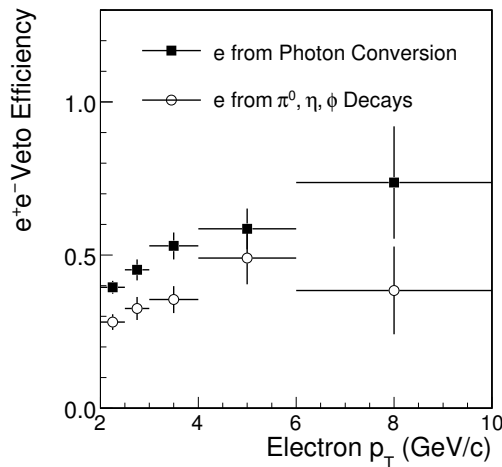


Systematic uncertainties for lifetime analysis

Apply veto if electron is part of e^+e^- pair.

Top: veto efficiency, determined with Pythia

Bottom: Fit ct^* of reweighted veto events



Lifetime systematic uncertainties:

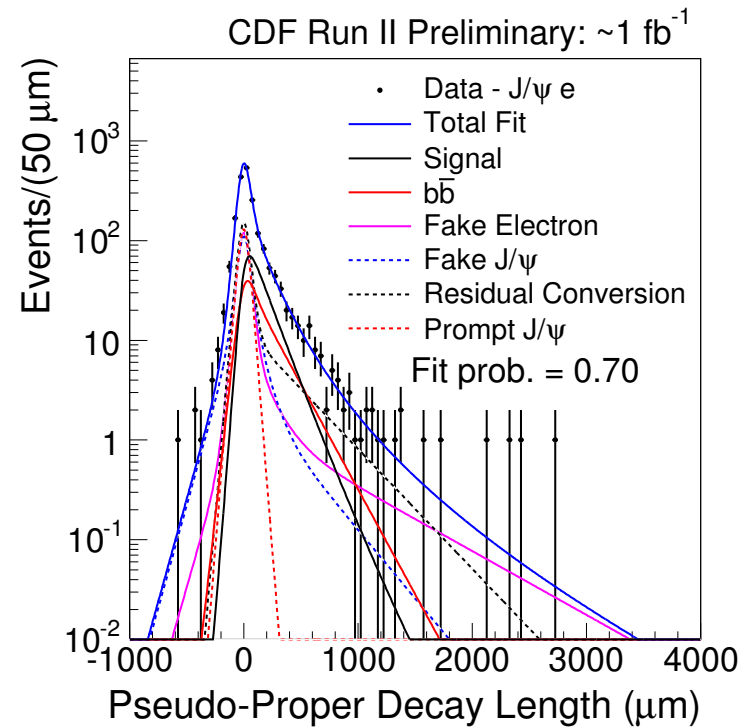
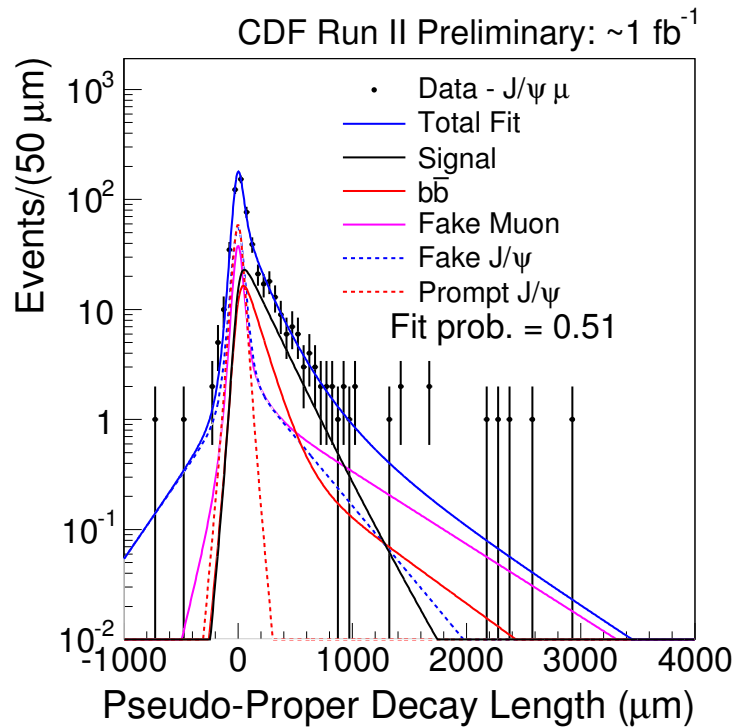
- Resolution function - choice of model for detector resolution: $3.8 \mu m$
- Pythia model for $b\bar{b}$ background - relative contribution of QCD processes: $2.4 \mu m$
- Vertex detector alignment - uncertainties in positions of silicon detectors: $2.0 \mu m$
- e^+e^- veto efficiency - uncertainties related to modeling e^+e^- veto efficiencies: $1.5 \mu m$
- B_c spectrum - variations of K factor distribution due to variations in B_c production spectrum: $1.3 \mu m$

Total uncertainty: ± 5.5 (syst) μm



B_c^+ lifetime fits

Background sizes were constrained to it's predicted values. Prompt J/ψ allowed to float.



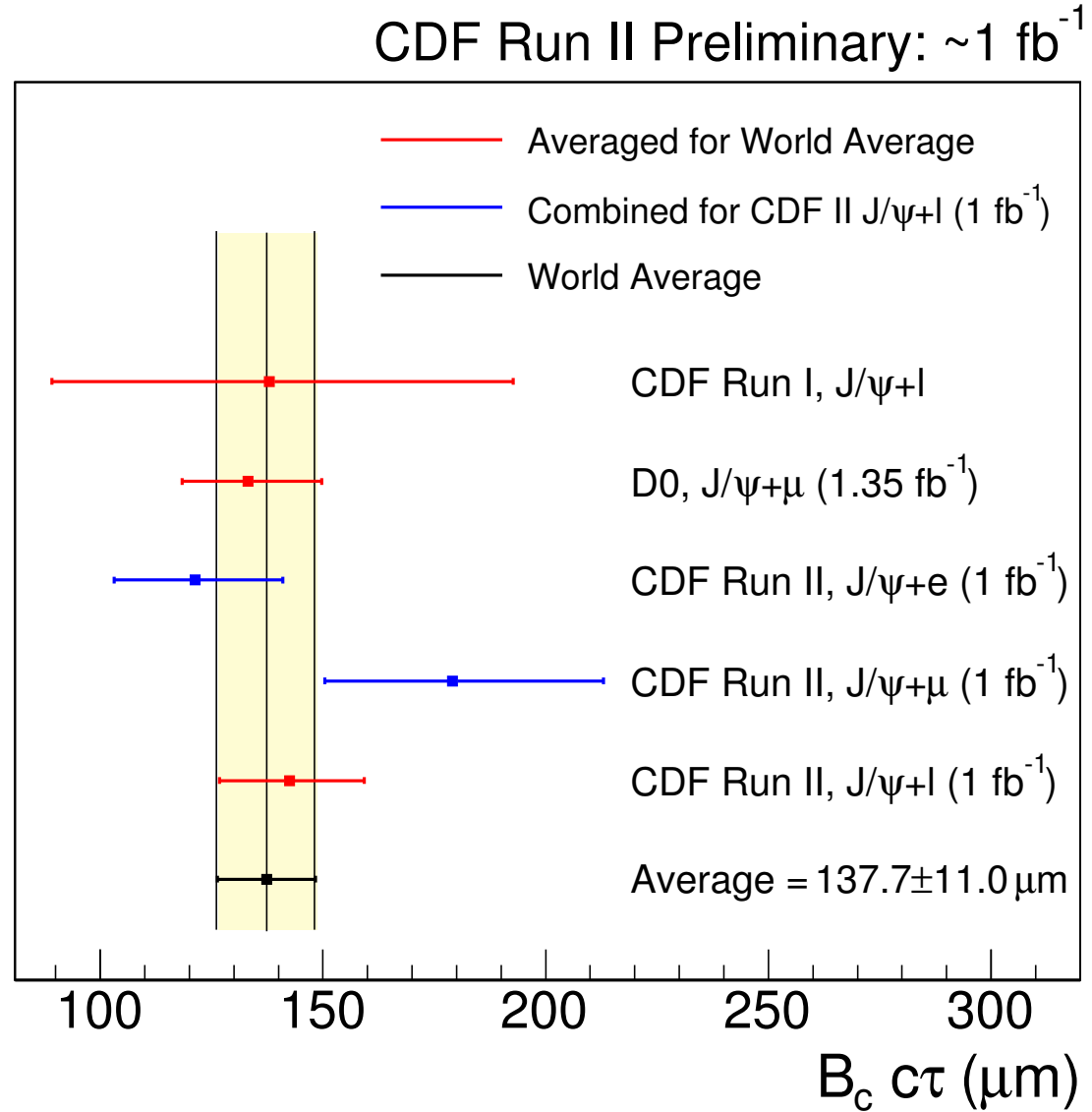
Fitted $c\tau^*$ for muon (on left) and electron (on right) channels.

$$c\tau_{\mu} = 179.1_{-27.2}^{+32.6} (stat) \mu\text{m} \quad c\tau_e = 121.7_{-16.3}^{+18.0} (stat) \mu\text{m}$$

$$\text{combined: } c\tau(B_c^+) = 142.5_{-14.8}^{+15.8} (stat) \pm 5.5 (syst) \mu\text{m}$$



Lifetime: comparison with other results





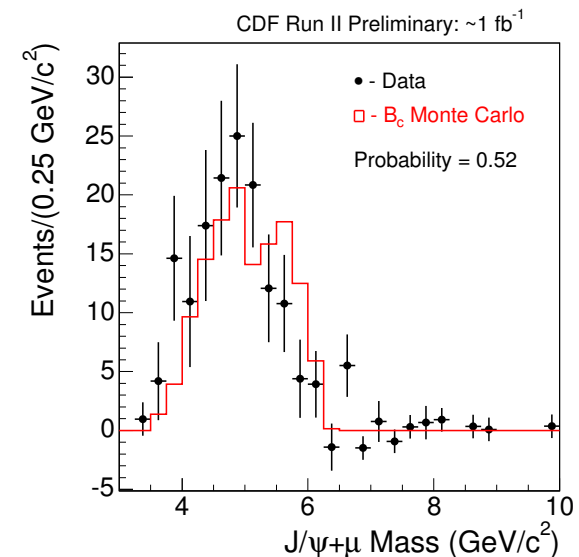
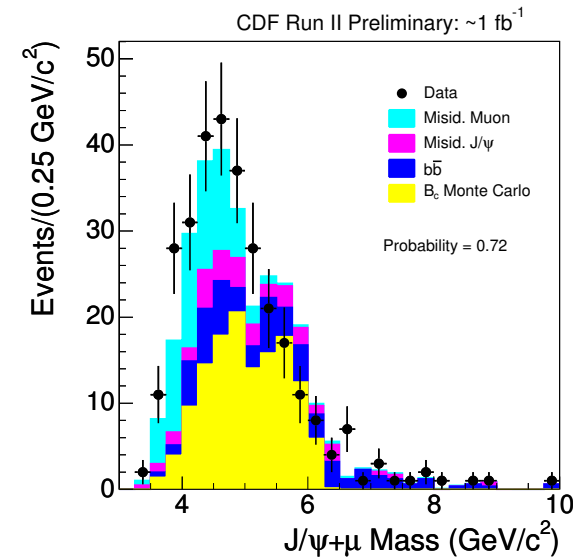
B_c^+ backgrounds for cross section

Backgrounds for $B_c^+ \rightarrow J/\psi \mu^+$ decays and B_c^+ excess with the $p_T(3\mu) > 4$ (6) GeV/c cuts.

	$p_T(B_c^+) > 4$ GeV/c	$p_T(B_c^+) > 6$ GeV/c
$N(B_c^+)$ observed	229 ± 15.1 (stat)	214 ± 14.6 (stat)
Misidentified J/ψ	21.5 ± 3.3 (stat)	20.5 ± 3.2 (stat)
Misid. third muon	55.8 ± 2.0 (stat)	53.6 ± 1.9 (stat)
Doubly misidentified	-8.8 ± 0.4 (stat)	-7.5 ± 0.3 (stat)
$b\bar{b}$ background	37.7 ± 7.3 (st+sys)	35.4 ± 7.0 (st+sys)
Other decay modes	5.2 ± 0.5 (stat)	4.8 ± 0.4 (stat)
Total background	111.4 ± 8.3 (stat)	106.9 ± 8.0 (stat)
B_c^+ signal	117.6 ± 17.2 (st)	107.1 ± 16.7 (st)

Note: "Doubly misidentified" is a subsample of misid. J/ψ and misid. muon samples, it needs to be subtracted once to avoid double counting.

Upper plot: $B_c^+ \rightarrow J/\psi \mu^+$ candidates. Monte Carlo sample and backgrounds are superimposed. Lower: backgrounds are subtracted.



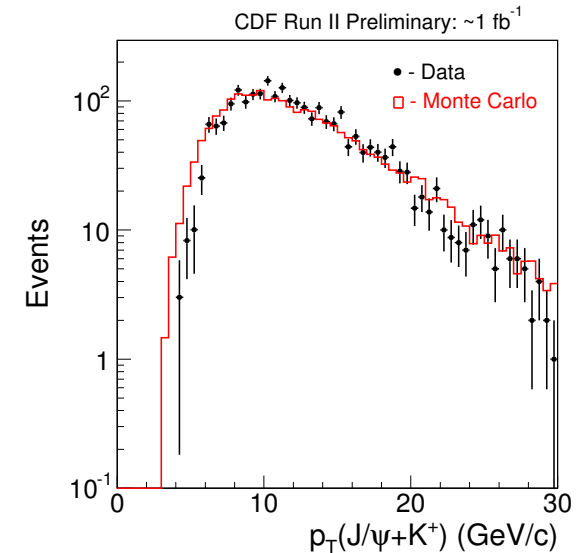
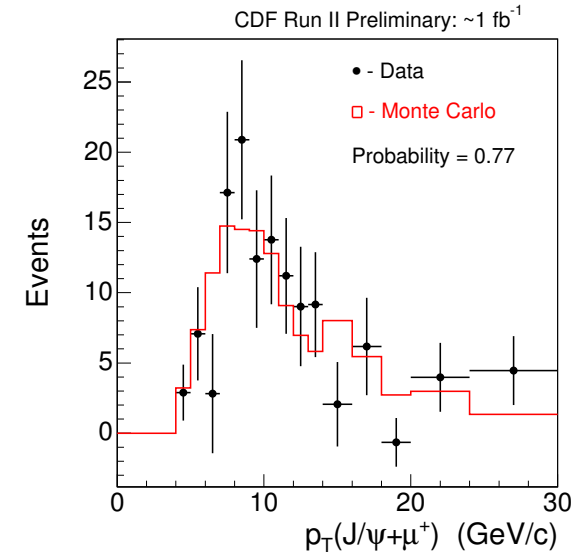


Relative efficiency, ϵ_{rel}

Relative efficiency $\epsilon_{rel} = \epsilon_{B^+} / \epsilon_{B_c^+}$

- MC simulations of $B_c^+ \rightarrow J/\psi \mu^+ \nu$, $B_c^* \rightarrow B_c^+ \gamma$ and $B^+ \rightarrow J/\psi K^+$ decays need as input:
 - p_T dependence of B_c^+ production spectrum, we used it from PRD 72,114009(2005)
 - p_T dependence of B^+ production spectrum, we used it as at JHEP07,033(2004), good agreement with CDF measurements

	$p_T(B) > 4 \text{ GeV}/c$	$p_T(B) > 6 \text{ GeV}/c$
$\epsilon_{B_c^+}$ (%)	0.0551	0.1232
ϵ_{B^+} (%)	0.3231	0.6005
ϵ_{rel}	$5.867 \pm 0.068(st)$	$4.873 \pm 0.060(st)$





B_c^+ systematic uncertainty for cross section

- Misidentified J/ψ : as this is derived from data, we do not assign a systematic uncertainty.
- Misidentified muon: we calculate the uncertainties by varying the proton fraction in the $J/\psi + track$ sample. This is a dominant source of uncertainty.
- $b\bar{b}$ background: we combine statistical and systematic uncertainties in the fit of the scale factors and their correlations. It included in the B_c^+ statistical uncertainty.
- Other decay modes: we calculate the uncertainty by varying the branching ratios of the non-exclusive $B_c^+ \rightarrow J/\psi + \mu^+ + X$ decays.

	$p_T(B) > 4 \text{ GeV}/c$	$p_T(B) > 6 \text{ GeV}/c$
Misidentified muon	± 5.7	± 5.5
Doubly misidentified	± 0.9	± 0.8
$b\bar{b}$ (illustration)	± 7.3 (st+sys)	± 7.0 (st+sys)
Other decay modes	+6.0 -2.8	+5.6 -2.5
Total	+8.3 -6.4	+7.9 -6.1



ϵ_{rel} systematic uncertainty for cross section

- B_c^+ lifetime: it was estimated by varying the B_c^+ lifetime within $\pm 14\mu\text{m}$ ($\sim 1\sigma$) relative to the nominal value
- B_c^+ spectrum: we estimate variations due to of three different theoretical approaches
- B^+ spectrum: re-weight the simulated spectrum below 10 GeV/c to bring it into agreement with the data
- μ, K simulation: re-weighting the transverse momentum of the kaon and muon according to the measured differences in data

	$p_T(B) > 4 \text{ GeV/c}$	$p_T(B) > 6 \text{ GeV/c}$
B_c^+ lifetime	+0.393 -0.223	+0.354 -0.160
B_c^+ spectrum	± 0.720	± 0.298
B^+ spectrum	± 0.340	± 0.161
μ, K simulation	± 0.192	± 0.160
ϵ_{rel} total systematics	+0.554 -0.450 ± 0.720 (spectrum)	+0.420 -0.278 ± 0.298 (spectrum)



B_c^+ to B^+ ratio results

	$p_T(B) > 4 \text{ GeV}/c$	$p_T(B) > 6 \text{ GeV}/c$
$N(B_c^+)$	$117.6 \pm 17.2(\text{stat})_{-6.4}^{+8.3}(\text{sys})$	$107.1 \pm 16.7(\text{stat})_{-6.1}^{+7.9}(\text{sys})$
$N(B^+)$	$2333 \pm 55(\text{stat})$	$2299 \pm 53(\text{stat})$
ϵ_{rel}	$5.867 \pm 0.068(\text{stat})$ $+0.554(\text{sys}) \pm 0.720(\text{spectrum})$ -0.450	$4.872 \pm 0.060(\text{stat})$ $+0.420(\text{sys}) \pm 0.298(\text{spectrum})$ -0.278
$\frac{N(B_c^+)}{N(B^+)} \times \epsilon_{rel}$	$0.295 \pm 0.040(\text{stat})$ $+0.033(\text{sys}) \pm 0.036(\text{spectrum})$ -0.026	$0.227 \pm 0.033(\text{stat})$ $+0.024(\text{sys}) \pm 0.014(\text{spectrum})$ -0.017

Previous CDF measurements:

	L, pb^{-1}	$p_T(B) \text{ value}$	$R = \frac{\sigma(B_c^+) \cdot BR(B_c^+ \rightarrow J/\psi + l^+ + \nu)}{\sigma(B^+) \cdot BR(B^+ \rightarrow J/\psi + K^+)}$
<i>Run I, e + μ</i>	110	$p_T(B) > 6 \text{ GeV}/c$	$0.132_{-0.037}^{+0.041}(\text{st}) \pm 0.031(\text{sys})_{-0.020}^{+0.032}(\text{lt})$
<i>Run II, μ</i>	360	$p_T(B) > 6 \text{ GeV}/c$	$0.245 \pm 0.045(\text{st}) \pm 0.066(\text{sys})_{-0.032}^{+0.080}(\text{lt})$
<i>Run II, e</i>	360	$p_T(B) > 4 \text{ GeV}/c$	$0.282 \pm 0.038(\text{st}) \pm 0.035(\text{y}) \pm 0.065(\text{a})$



B_c^+ total cross section

Available quantities:

Predicted $BR(B_c^+ \rightarrow J/\psi + l^+ + \nu) = 2.07 \times 10^{-2}$, PRD 73 054024 (2006)

$BR(B^+ \rightarrow J/\psi + K^+) = (1.007 \pm 0.035) \times 10^{-3}$ PDG, 2008

$\sigma(B^+) = 2.78 \pm 0.24 \mu\text{b}$ for $p_T(B^+) > 6 \text{ GeV}/c$ by CDF PRD 75:012010,2007

Then we might calculate followings:

$\sigma(B_c^+) \cdot BR(B_c^+ \rightarrow J/\psi + l^+ + \nu) = 0.64 \pm 0.20 \text{ nb}$ ($p_T(B_c^+) > 6 \text{ GeV}/c$)

$\sigma(B_c^+) = \frac{0.227 \times 2.78 \mu\text{b} \times 1.007 \times 10^{-3}}{2.07 \times 10^{-2}} = 31 \pm 10 \text{ nb}$ ($p_T(B_c^+) > 6 \text{ GeV}/c$)

Predicted $\sigma(B_c^+ + B_c^*)$:

	\sqrt{s} , TeV	$ y $	p_T , GeV/c	$\sigma(B_c^+ + B_c^*)$
Chao-Hsi Chang ¹	1.96	< 0.6	> 4	23.3 nb
Phys.Lett.B605(2005)311	1.8	< 1	> 6	$7.4 \pm 5.4 \text{ nb}$

¹Chao-Hsi Chang, "Bc Production at Hadron Colliders" Sino-German Workshop, Sept. 20-23, 2006, DESY



conclusions

Prior to LHC data CDF is a major contributor to B_c^+ property studies:

- mass measurements

$$m(B_c^+) = 6275.6 \pm 2.9(\text{stat}) \pm 2.5(\text{syst}) \text{ MeV}/c^2, \text{ PRL } 100, 182002, 2008$$

- decay properties:

$$c\tau(B_c^+) = 142.5_{-14.8}^{+15.8}(\text{stat}) \pm 5.5(\text{syst}) \mu\text{m}$$

- production properties (for $p_T(B) > 6 \text{ GeV}/c$):

$$- \frac{\sigma(B_c^+) \cdot BR(B_c^+ \rightarrow J/\psi + \mu^+ + \nu)}{\sigma(B^+) \cdot BR(B^+ \rightarrow J/\psi + K^+)} = 0.227 \pm 0.033(\text{stat})_{-0.017}^{+0.024}(\text{sys}) \pm 0.014(\text{spectrum})$$

$$- \sigma(B_c^+) \cdot BR(B_c^+ \rightarrow J/\psi + l^+ + \nu) = 0.64 \pm 0.20 \text{ nb} \text{ (free from predictions)}$$