



# Non-Supersymmetric Physics Beyond the Standard Model

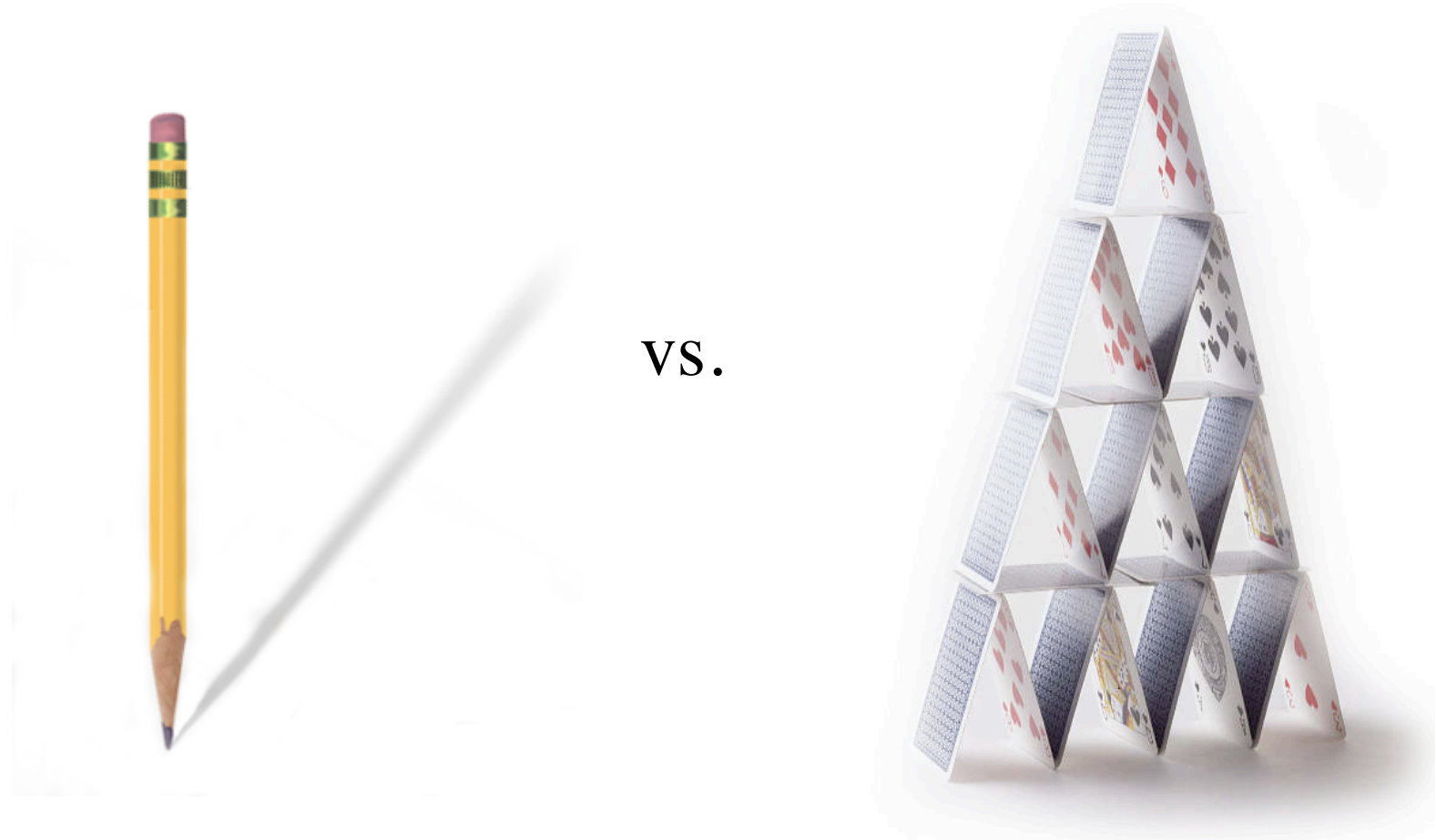
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# Introduction

After 35 years of building models, electroweak symmetry breaking remains a mystery...

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# Outline

- Standard model
- UV sensitivity
- Composite Higgs
  - Strong electroweak symmetry breaking
  - Pseudo-Nambu-Goldstone Higgs

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## Disclaimers

- No attempt at completeness
- Topics reflect personal interests

# Standard Model

	I	II	III	
Quarks	$u$	$c$	$t$	$\gamma$
	$d$	$s$	$b$	$g$
Leptons	$\nu_e$	$\nu_\mu$	$\nu_\tau$	$Z$
	$e$	$\mu$	$\tau$	$W$
				Force Carriers

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$+ h^0$

- Minimal model of electroweak symmetry breaking
- Agrees with all data
- Can't be the whole story, even at LHC energies



# Beyond the Standard Model

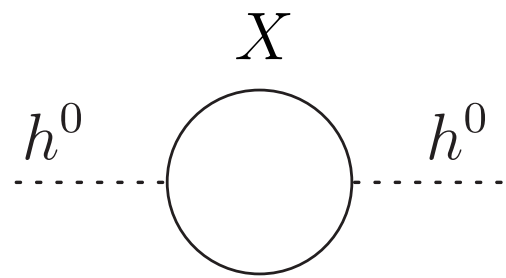
- Quantum gravity:  $M_{\text{Planck}} \sim 10^{19}$  GeV
- Grand unification:  $M_{\text{GUT}} \sim 10^{16}$  GeV
- Neutrino masses:  $M_{\nu_{\text{mass}}} \sim 10^{14}$  GeV
- Baryogenesis
- Origin of masses and mixing angles
- Strong  $CP$

⇒ Standard model is an effective low-energy theory

New physics may be beyond experimental reach, but...

# UV Sensitivity

Electroweak symmetry breaking is sensitive to UV physics in standard model



The diagram shows a circular loop labeled  $X$  at the top. Two dashed lines labeled  $h^0$  enter and exit the loop from the left and right respectively.

$$\Rightarrow \Delta V \sim \frac{g_{h^0 \bar{X} X}^2}{16\pi^2} M_X^2 |H|^2 + \dots$$
$$\Rightarrow v \sim M_X$$

**Note:** problem *worse* for larger  $M_X$ !

All UV sensitivity in one parameter  
(coefficient of  $|H|^2$  in effective potential)

$\Rightarrow$  can “fine-tune” away problem



# Supersymmetry

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	Force Carriers			

	I	II	III	
Squarks	$\tilde{u}$	$\tilde{c}$	$\tilde{t}$	$\tilde{\gamma}$
	$\tilde{d}$	$\tilde{s}$	$\tilde{b}$	$\tilde{g}$
Sleptons	$\tilde{\nu}_e$	$\tilde{\nu}_\mu$	$\tilde{\nu}_\tau$	$\tilde{Z}$
	$\tilde{e}$	$\tilde{\mu}$	$\tilde{\tau}$	$\tilde{W}$
	Gauginos			

Superpartners cancel UV sensitivity:

$$\Rightarrow \Delta V \sim \frac{g_{h^0 \tilde{X} X}^2}{16\pi^2} (M_X^2 - M_{\tilde{X}}^2) |H|^2$$

# Supersymmetric Fine Tuning

$$m_{h^0}^2 \simeq m_Z^2 \cos^2 2\beta + \frac{3y_t^4}{4\pi^2} \ln \frac{m_{\tilde{t}}}{m_t}$$

$$m_{h^0} > 114 \text{ GeV} \quad \Rightarrow \quad m_{\tilde{t}} \gtrsim \text{TeV}$$

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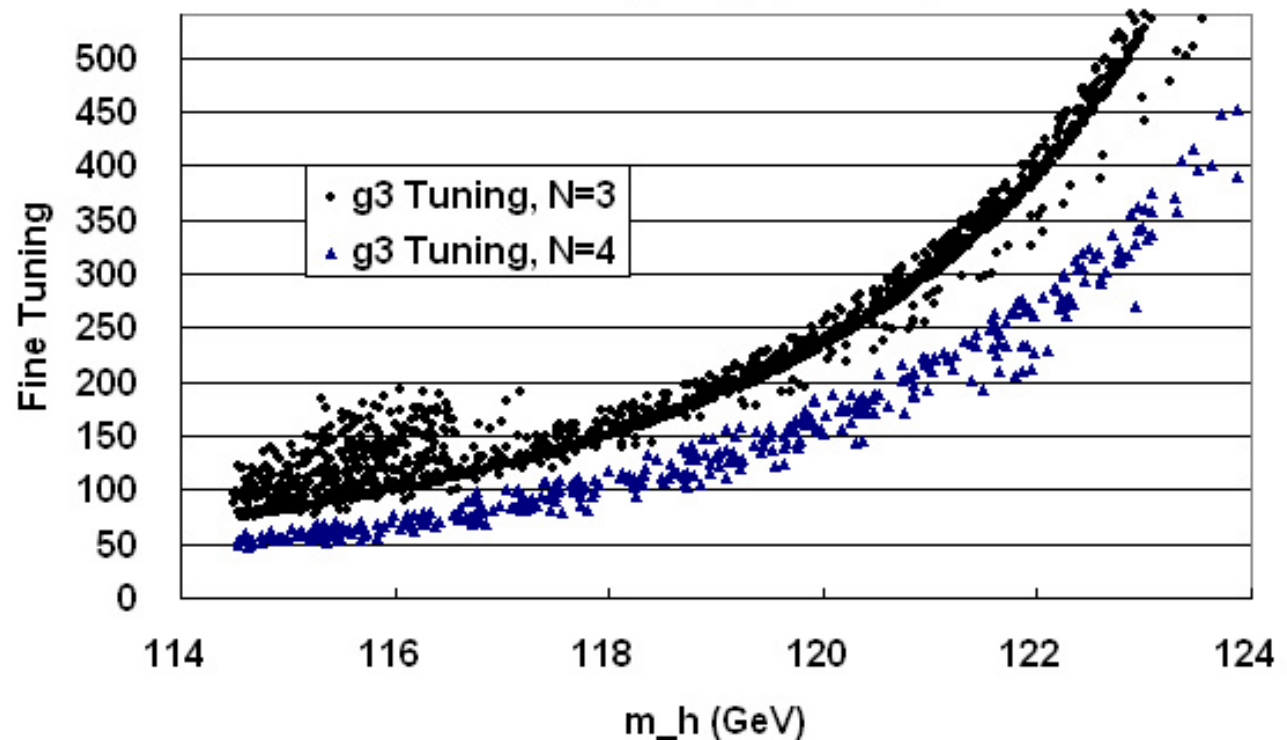
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$\Rightarrow$  1% tuning:

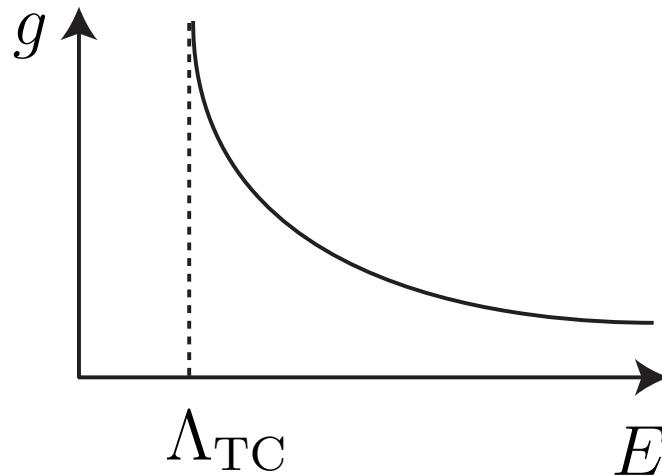




*“Magnificent! And to think that someday they’ll all be turned into supersymmetry phenomenology papers.”*

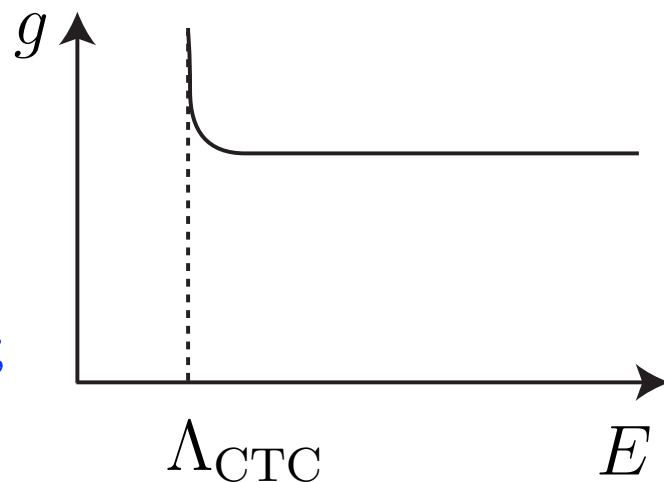
# Strong Electroweak Symmetry Breaking

Technicolor:  
(Susskind, 1979;  
Weinberg 1979)



$$\Lambda_{\text{TC}} \sim M_0 e^{-8\pi^2/g^2(M_0)}$$

Conformal  
Technicolor:  
(Luty, Okui 2004;  
Luty 2008)



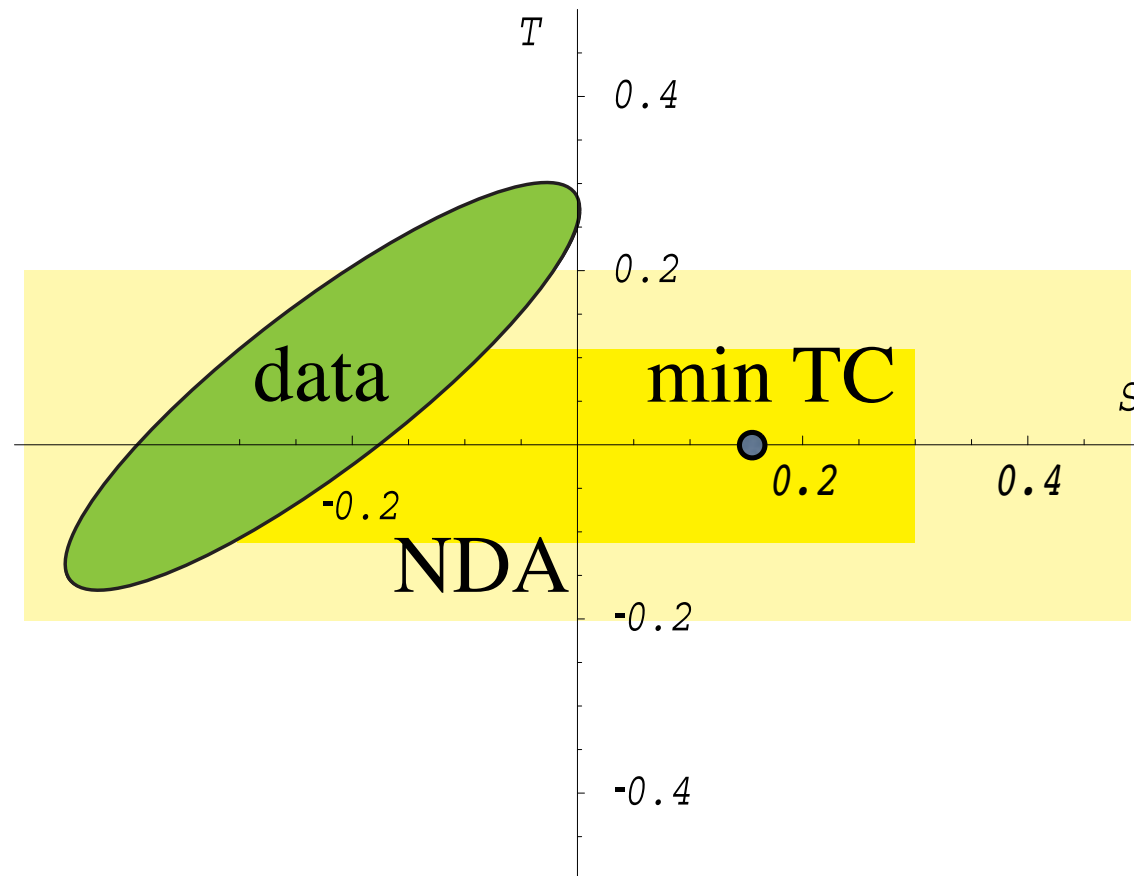
$$\Delta\mathcal{L} = m \bar{\psi}\psi$$

$$\Lambda_{\text{CTC}} \sim M_0 \left( \frac{m(M_0)}{M_0} \right)^{1/(4-d)}$$

$$d = \dim(\bar{\psi}\psi)$$

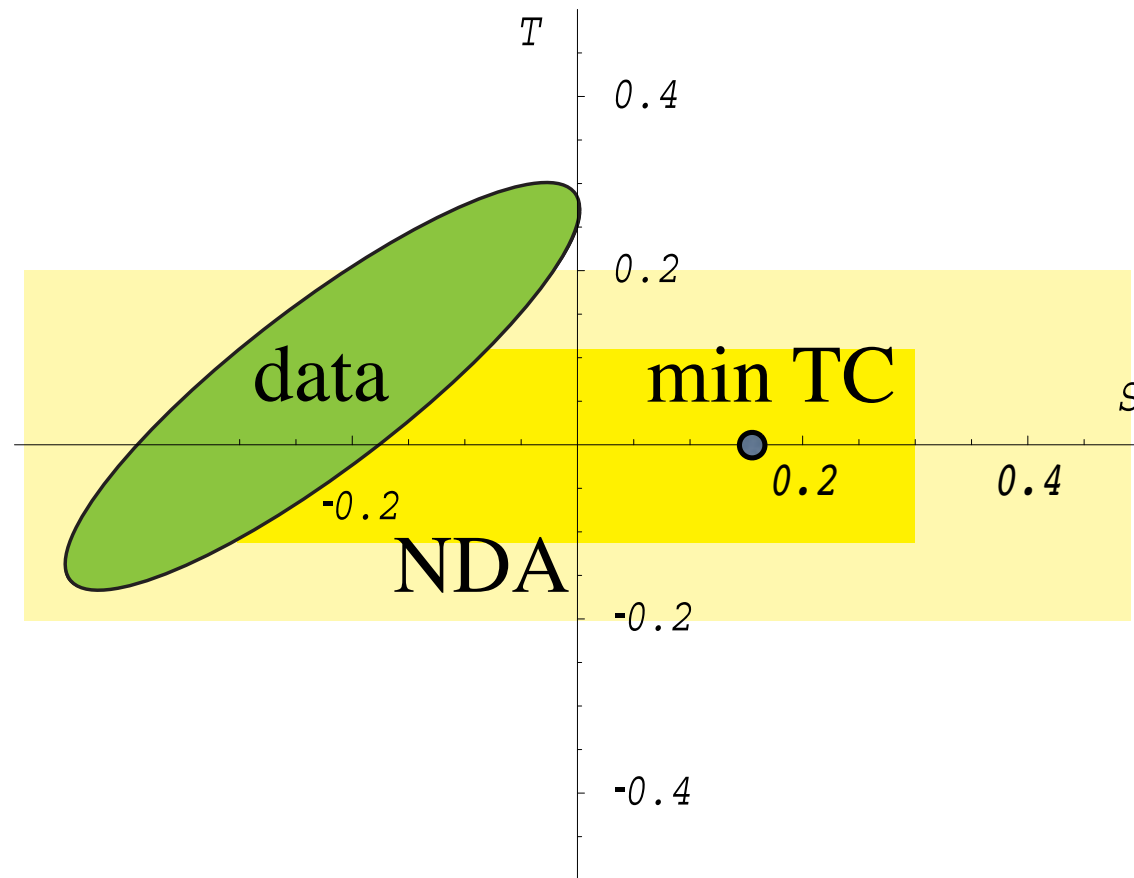


# Precision Electroweak Data



Good electroweak fit may be due to non-QCD dynamics and/or accidental cancelations

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“Little hierarchy problem”  $\rightarrow S < 0$  problem

# Origin of Flavor

$$\Delta\mathcal{L} \sim \frac{1}{\Lambda_t^{d-1}} (\bar{Q}_{L3} t_R) (\bar{\psi}_L \psi_R) \quad d = \dim(\bar{\psi}_L \psi_R)$$

$d > 1 \Rightarrow$  requires new physics at scale  $\Lambda_t$

Technicolor:  $d = 3 \Rightarrow \Lambda_t \sim 3 \text{ TeV}$

Conformal technicolor:  $d > 1$  (CFT unitarity bound)

$$\Rightarrow \Lambda_t \sim 10^{1/(d-1)} \text{ TeV}$$

(“Walking” technicolor: Holdom 1981,...)

E.g.  $d = 1.3 \Rightarrow \Lambda_t \sim 10^3 \text{ TeV}$

# Minimal Conformal Technicolor

$$SU(N)_{\text{CTC}} \times SU(2)_W \times U(1)_Y$$

$$\left. \begin{aligned} \psi_L &\sim (N, 2)_0, \\ \psi_{R1} &\sim (N, 1)_{\frac{1}{2}}, \\ \psi_{R2} &\sim (N, 1)_{-\frac{1}{2}}, \end{aligned} \right\} \text{minimal technicolor}$$
$$\left. \begin{aligned} \chi_L &\sim (N, 1)_0, \\ \chi_R &\sim (N, 1)_0 \end{aligned} \right\} \times K$$

$$\Delta\mathcal{L} = m_\chi \bar{\chi}_L \chi_R$$

$m_\chi =$  soft breaking of conformal symmetry

Triggers  $\langle \bar{\psi}_L \psi_R \rangle \neq 0 \Rightarrow$  electroweak breaking

# Constraints on $d$

$$H = \bar{\psi}_L \psi_R = \text{Higgs operator} \quad d = \dim(H)$$

$$\Delta \mathcal{L} \sim M_X^{4-\Delta} H^\dagger H \quad \Delta = \dim(H^\dagger H)$$

$\Delta < 4 \Rightarrow$  UV sensitivity  $\Rightarrow$  fine tuning

- Large  $N \Rightarrow \Delta = 2d + \mathcal{O}(1/N)$

(explains “gap equation” result)

- $d \rightarrow 1 \Rightarrow \Delta \rightarrow 2$

In fact,  $d = 1 + \epsilon \Rightarrow \Delta = 1 + \mathcal{O}(\epsilon^{1/2})$

(Rattazzi, Rychkov, Tonni, Vichi 2007)

Rigorous bounds do not apply to singlet  $H^\dagger H$

$\Rightarrow d \simeq 1.3, \Delta > 4$  compatible with all constraints

# Lattice

Lattice can “easily” measure  $d$ : (Luty, 2008)

QCD in conformal window (e.g.  $N_c = 3, N_f = 12$ )

Hadron masses  $\propto \Lambda \sim m^{1/(4-d)}$        $m =$  quark mass  
 $d = \dim(\bar{\psi}\psi)$

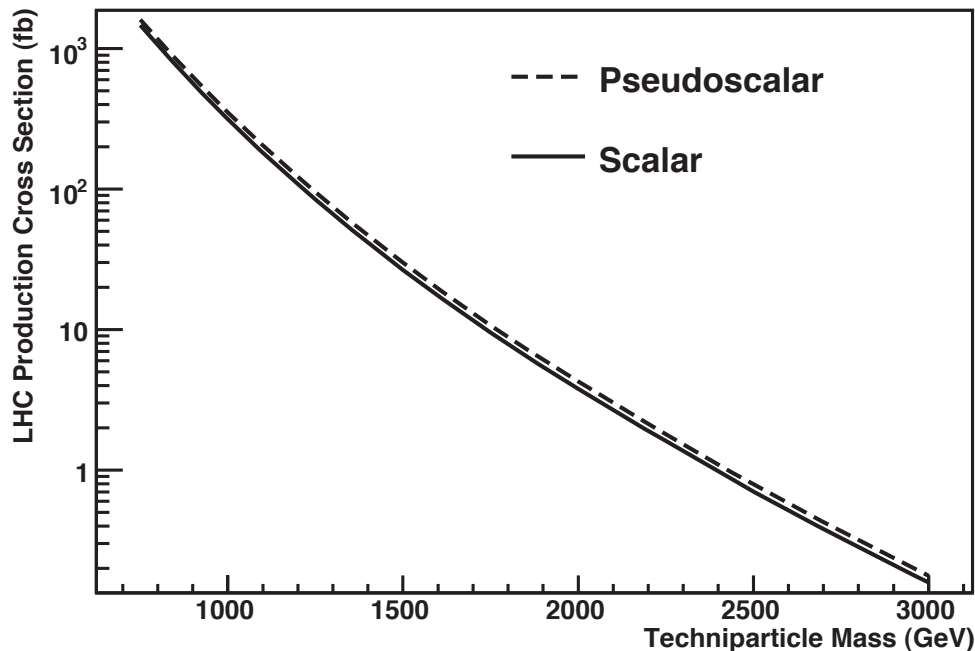
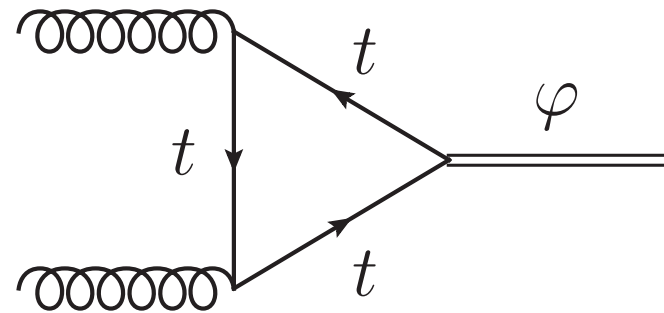
Measure scaling of hadron masses with  $m$

# LHC Phenomenology

Strong  $W_L W_L$  scattering requires  $100 \text{ fb}^{-1} \dots$

Spin 0 resonances from top couplings (Evans, Luty 2009)

$$\Delta\mathcal{L} \sim \frac{1}{\Lambda_t^{d-1}} (\bar{Q}_L t_R) (\bar{\psi}_L \psi_R) \Rightarrow$$



(Note: 14 TeV!)

# Spin 0 Resonances

$\varphi \rightarrow W_L W_L$  may be forbidden by strong symmetries  
(e.g. isospin,  $P$ ,  $C$ , ...)  $\Rightarrow$  narrow resonances!

(Resonances in  $W_L W_L$  scattering have strong 2-body decays  
 $\Rightarrow$  broad)

$$\frac{\Gamma(\varphi \rightarrow \bar{t}t)}{m_\varphi} \sim 10\% \quad \Rightarrow \bar{t}t \text{ resonances}$$

QCD extrapolation:  $\frac{\Gamma(\varphi \rightarrow W_L W_L W_L)}{m_\varphi} \sim 1\%$

$\Rightarrow$  large cross section for resonant multi-W production

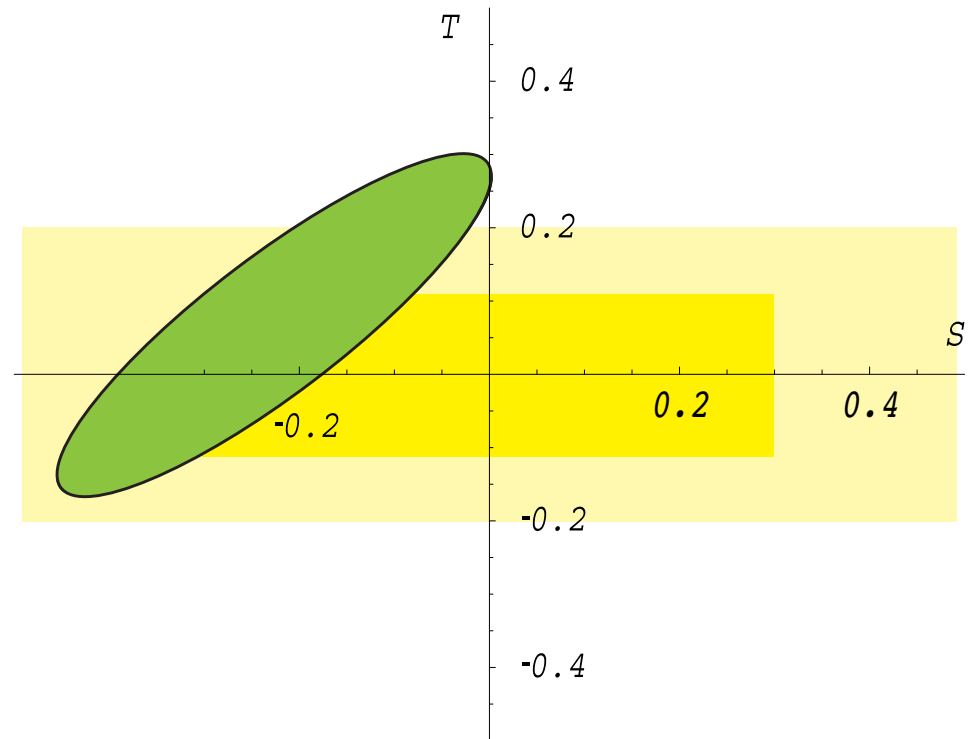
May be “smoking gun” of strong dynamics



# Precision Electroweak Again

Experience with QCD and 5D “holographic” models suggests  $S > 0$

(Agashe, Csaki, Grojean, Reece 2007)



Motivates models in which  $S$  is an adjustable parameter...

# Pseudo Nambu-Goldstone Higgs

Toy model:  $\Phi \sim 3$  of  $SU(3)_{\text{glob}}$  symmetry

$$\langle \Phi \rangle^\dagger \langle \Phi \rangle = f^2 \Rightarrow SU(3)_{\text{glob}} \rightarrow SU(2)_{\text{glob}}$$

Weakly gauge  $SU(2)_W \subset SU(3)_{\text{glob}} : T_a = \begin{pmatrix} \sigma_a & 0 \\ 0 & 0 \end{pmatrix}$

$$\langle \Phi \rangle = \begin{pmatrix} 0 \\ f \sin \theta \\ f \cos \theta \end{pmatrix} = \text{general VEV}$$

$v = f \sin \theta =$  scale of  $SU(2)_W$  breaking

$\theta \ll 1 \Rightarrow$  separation of scales

$\Rightarrow SU(2)_W$  broken by pseudo Nambu-Goldstone “Higgs”

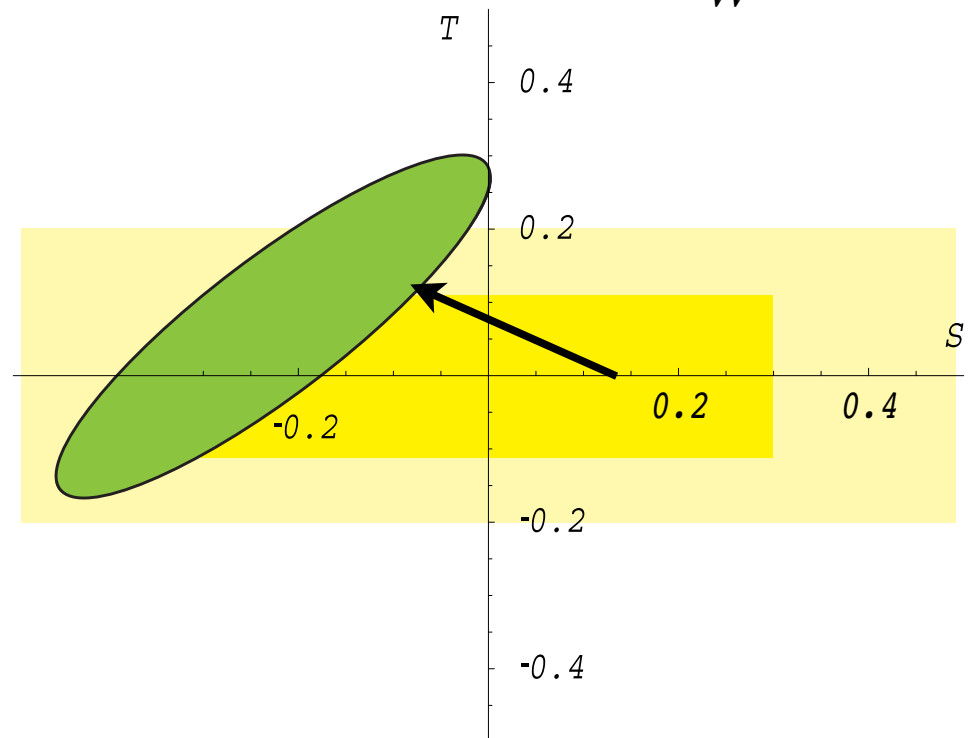
# Pseudo Nambu-Goldstone Higgs

$\theta \ll 1$  requires tuning  $\sim \sin^2 \theta \sim \frac{v^2}{f^2}$

But: a little tuning goes a long way

$$S = S_0 \sin^2 \theta + \frac{1}{12\pi} \ln m_h^2 \quad T = T_0 \sin^2 \theta - \frac{3}{16\pi c_W^2} \ln m_h^2$$

Recover electroweak fit with  $\sim 10\%$  tuning



# Models

Most literature based on 5D “holographic” models  
(Contino, Nomura, Pomarol 2004, Agashe, Contino,  
Pomarol 2004,...)

$$\Leftrightarrow 1/N \text{ expansion} \quad N \sim \frac{\Lambda}{m_{\text{KK}}}$$

$S_0 \sim +N \Rightarrow$  tune away expansion parameter

Or: composite Higgs from small  $N$  strong dynamics  
(Galloway, Evans, Luty, Tacchi, in preparation)

$$\Lambda_{\text{TC}} \sim \frac{\text{TeV}}{\sin \theta} \Rightarrow \text{strong dynamics signals still possible}$$

# Little Higgs?

- Aim to explain away 10% tuning required to get good electroweak fit
- Requires clever model building (“collective symmetry breaking”)
- Good precision electroweak fit requires residual tuning or model-building (“ $T$  parity”)



# Conclusions

- No perfect models
- Strong electroweak symmetry breaking may be a reasonable compromise between tuning and excessive model-building
- Testable at LHC
- Let the data-driven LHC era begin (please)!