



**Neutrino Oscillations:**

**Solar**

**and Atmospheric**

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# $\nu$ Oscillations In Two Domains: Atmospheric and Solar

$$|\nu_\alpha\rangle = \sum_i U_{\alpha i}^* |\nu_i\rangle \quad \nu \text{ mass eigenstates} \neq \text{flavor eigenstates}$$

$$U = \begin{bmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{bmatrix} \times \begin{bmatrix} c_{13} & 0 & s_{13}e^{-i\delta} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta} & 0 & c_{13} \end{bmatrix} \times \begin{bmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{bmatrix}$$

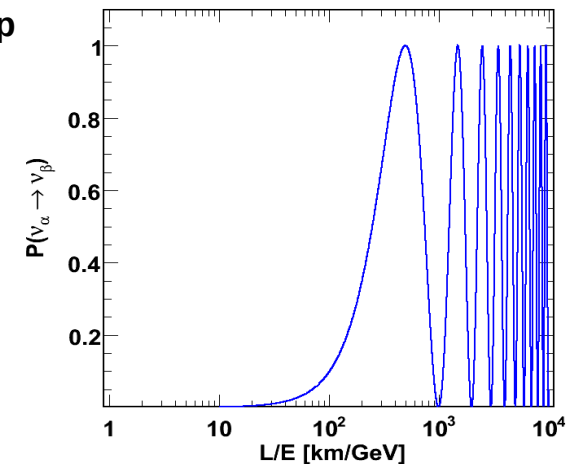
Atmospheric

Solar

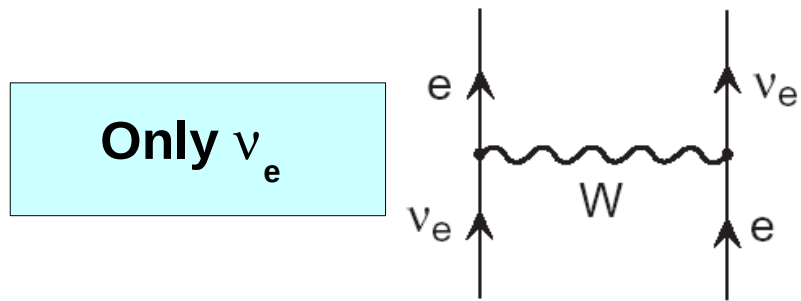
Additionally two mass splittings:  $\Delta m_{12}^2$ ,  $\Delta m_{13}^2$ ,  $\delta_{cp}$

To first order experiments are sensitive to oscillations between two active  $\nu$ 's:

$$P(\nu_\alpha \rightarrow \nu_\beta) = \sin^2 2\theta \sin^2 \left( \frac{1.27 \Delta m^2 L}{E} \right) \left[ \frac{eV^2 km}{GeV} \right]$$



# Matter Effects : Constant Density



⇒ Creates an effective potential

$$A = \sqrt{2} G_F N_e, \quad N_e = e^- \text{ density}$$

⇒ Alters  $\nu_e \leftrightarrow \nu_\alpha$  oscillations

Two- $\nu$  system can be expressed in “matter” variables:

$$P(\nu_e \rightarrow \nu_\alpha) = \sin^2 2\theta_M \sin^2 \left( \frac{1.27 \Delta M^2 L}{E} \right)$$

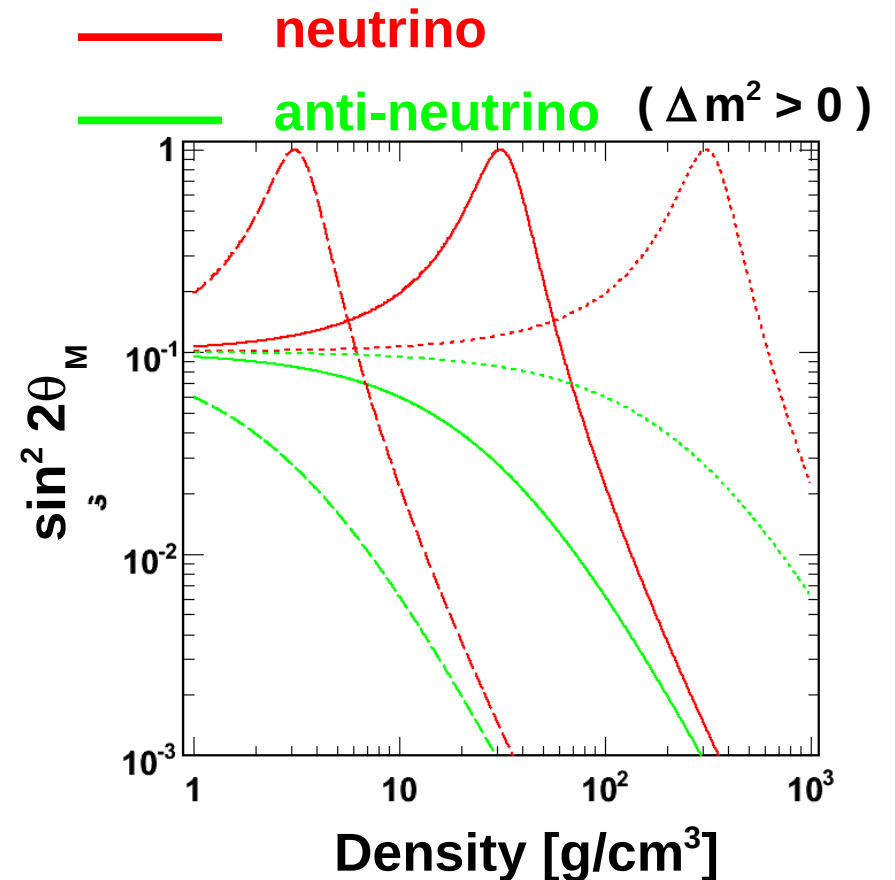
$$\Delta M^2 = \Delta m^2 \sqrt{\sin^2 2\theta + (\Gamma - \cos 2\theta)^2}$$

$$\sin^2 2\theta_M = \frac{\sin^2 2\theta}{\sin^2 2\theta + (\Gamma - \cos 2\theta)^2}$$

Leads to a resonance condition

$$\Gamma = \pm 2\sqrt{2}G_f N_e E / \Delta m^2$$

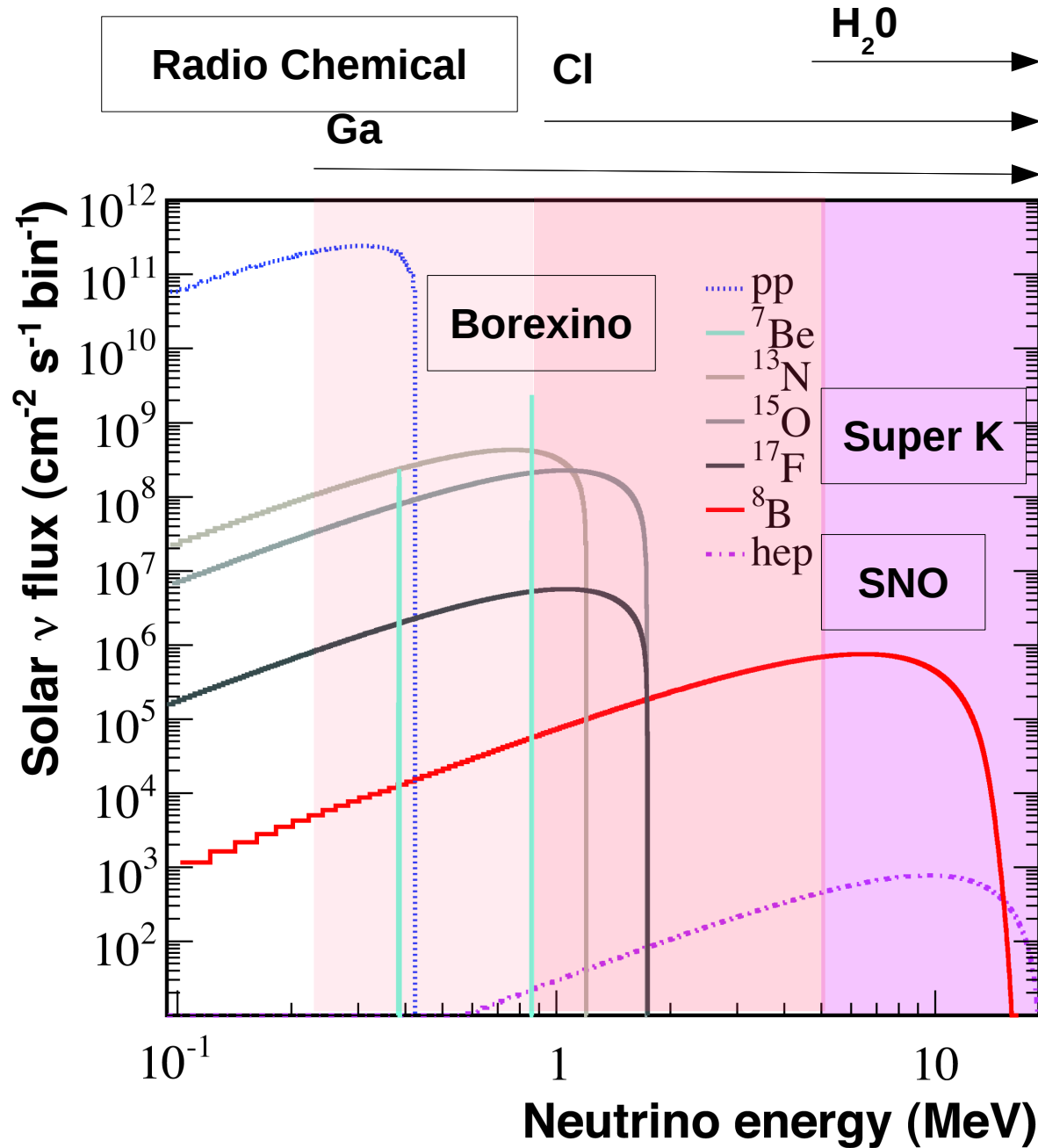
At low densities and energies vacuum oscillations are recovered





**Solar**

# Standard Solar Model



# Radio-Chemical Experiments and the Solar $\nu$ Problem

## Homestake experiment ( 1969- 1993)



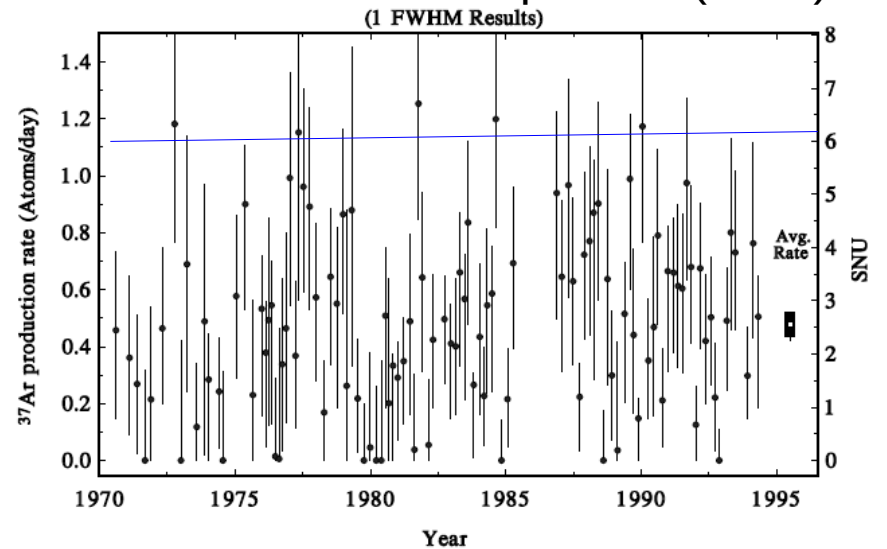
Measure:

2..56 SNU ,  
 SNU = 1 ev /s/  $10^{36}$ atoms

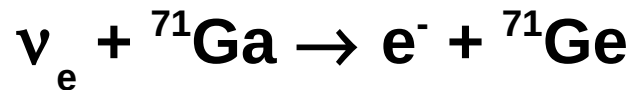
Solar Model Predictions:

9.3, Bahcall, , 6.3 Turk-Chieze, 7.6 Sacman

ApJ. 496 (1998) 505

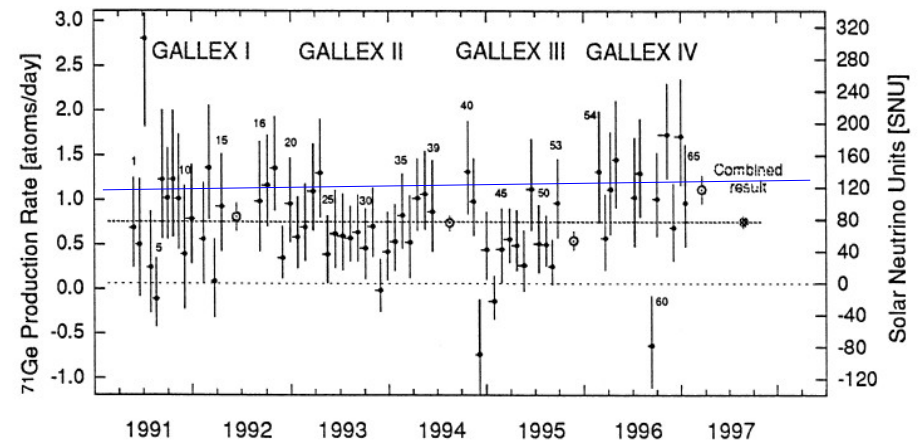


## Gallex / GNO



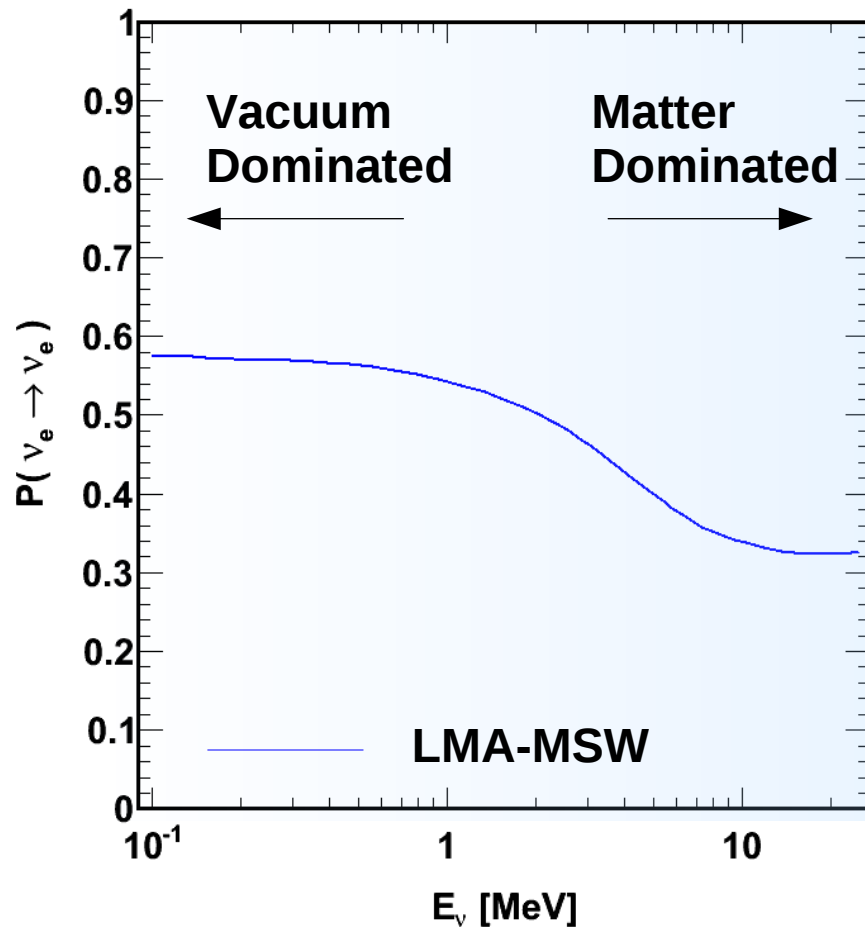
Observed rate :  $77.5 \pm 6.2$  SNU  
 vs. **130** from SSM

**SAGE** :  $66 \pm 7$  SNU



Phys. Lett. B 447(1999) 127

# Solar MSW : LMA



$A_R$  = Matter potential at resonance

$A_0$  = Matter potential at creation

Three Domains for Solar  $\nu$ :  
“adiabatic regime”

i)  $A_0 \ll A_R$  : **low E or low  $\rho$**

Never cross resonance region,  
Vacuum oscillations dominant

$$P_{ee} = 1 - \frac{1}{2} \sin^2 2\theta > \frac{1}{2}$$

ii)  $A_0 < A_R$  :  **$\nu$  born near resonance**

Vacuum + Matter oscillation effects

$$P_{ee} = \frac{1}{2} [ 1 + \cos 2\theta_{m,0} \cos 2\theta ]$$

iii)  $A_0 > A_R$  :  **$\nu$  born above resonance**

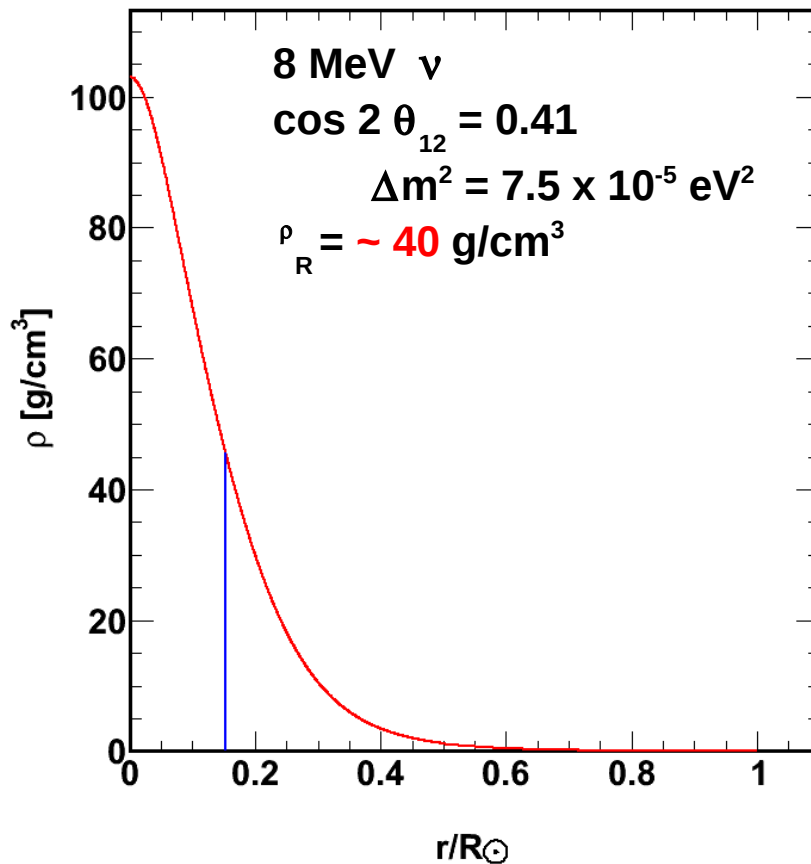
Cross resonance,  $\cos^2 \theta_{m,0} \sim -1$

Mixing at birth is suppressed

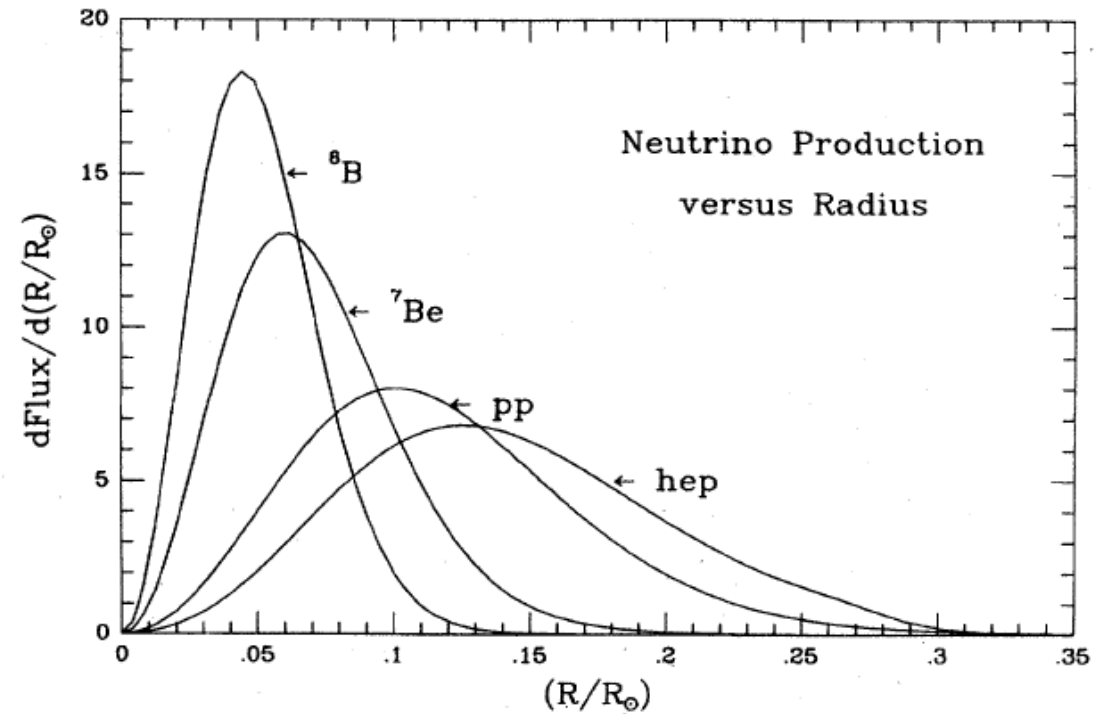
$$P_{ee} = \sin^2 2\theta = | \langle \nu_e | \nu_2 \rangle |^2$$

# Solar MSW : LMA (2)

Solar matter profile



Bahcall Rev. Mod. Phys 60 (1988)

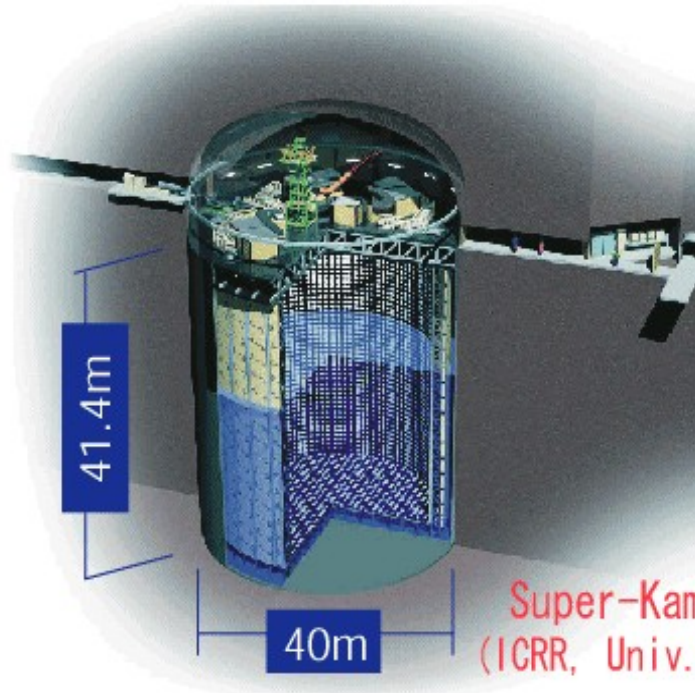


As a function of density the location of the matter resonance is inversely proportional to the  $\nu$  energy

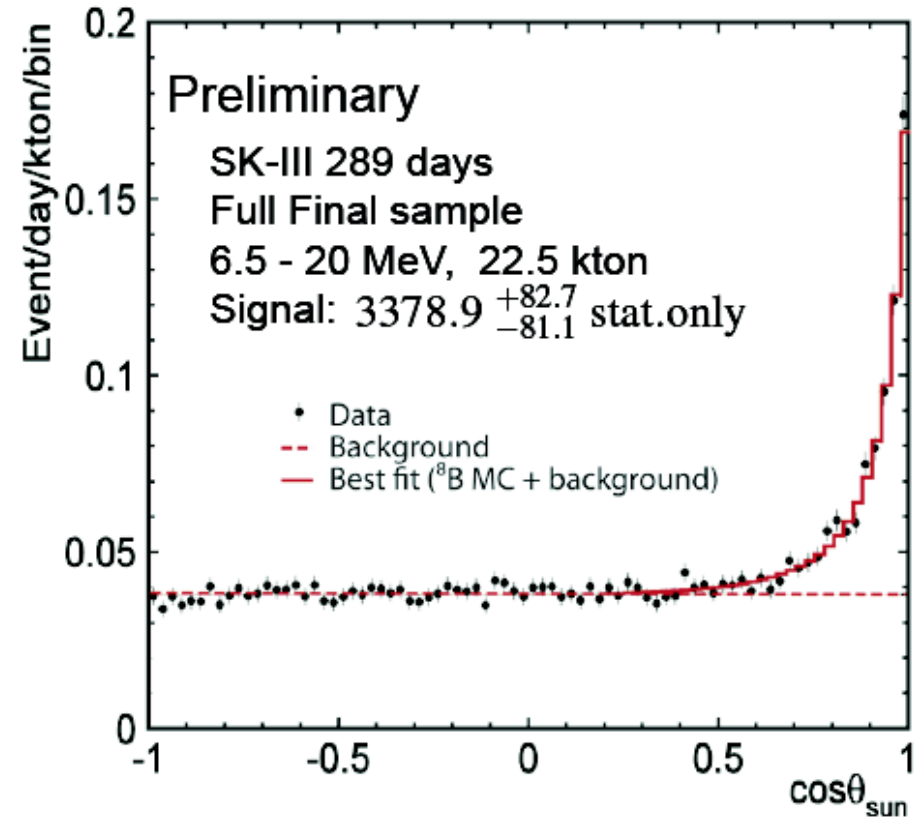
⇒ Solar  $\nu$ 's probe all of the MSW-LMA regions



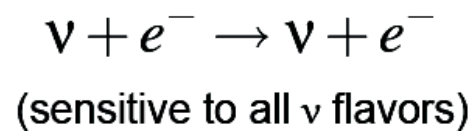
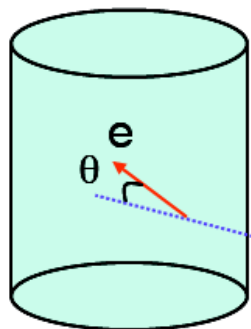
# Super-Kamiokande (Super-K): Solar $\nu$ 's



SK-III solar : see B. Yang



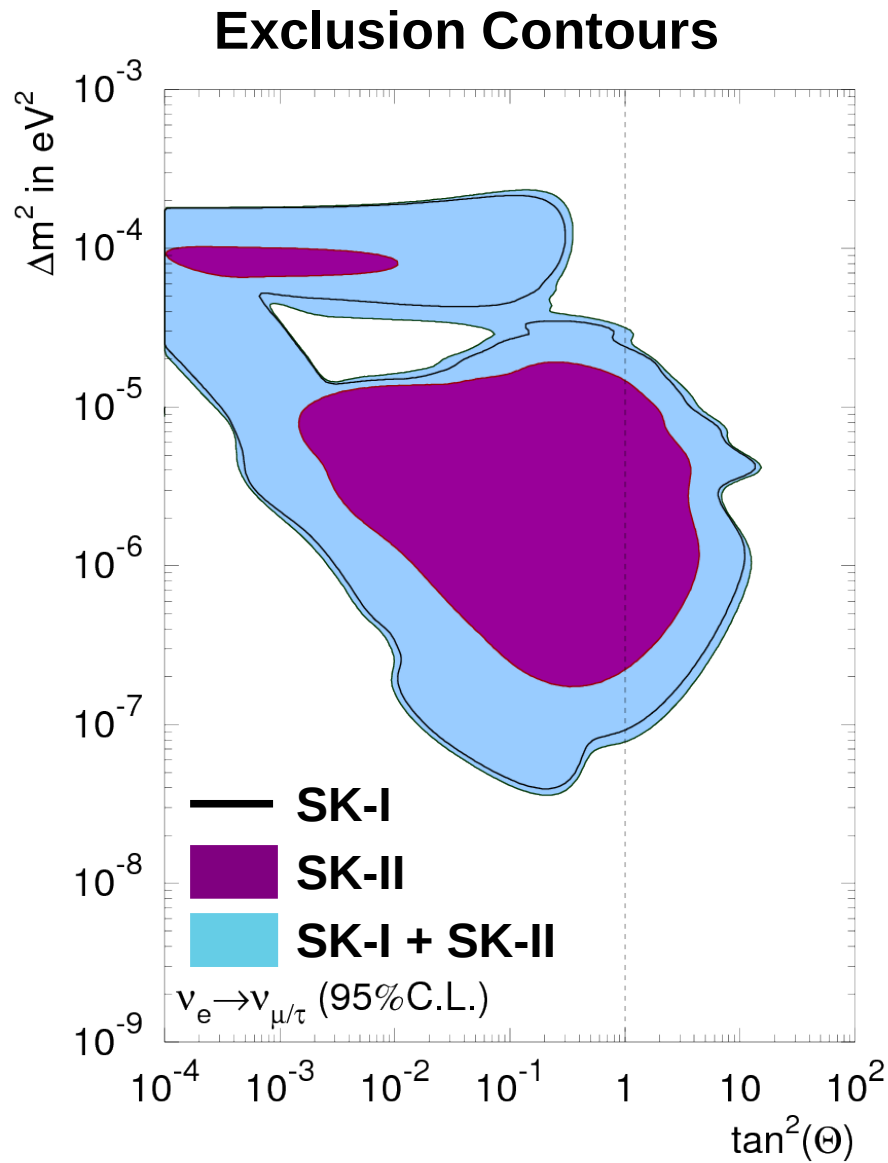
$^8\text{B}$  neutrino measurement  
by elastic scattering:



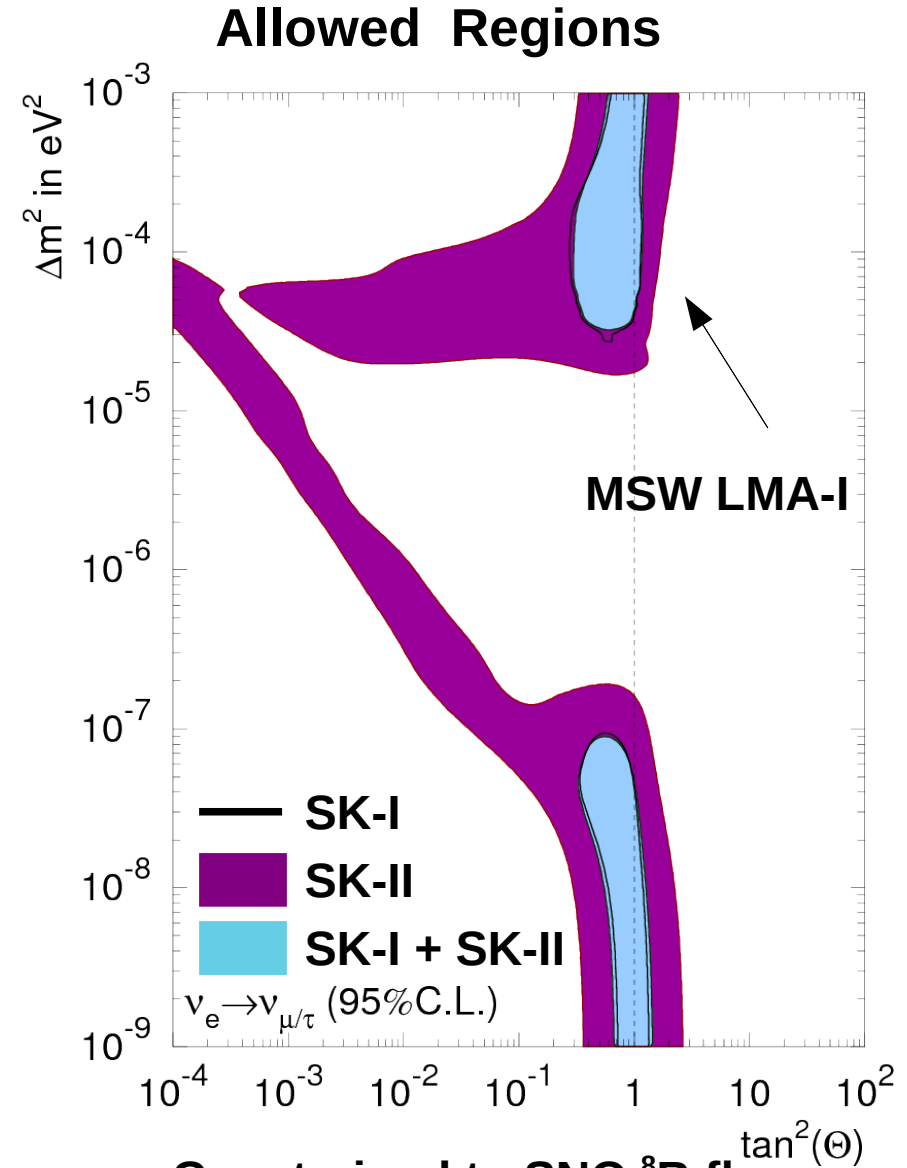
- Reconstruct direction to the sun
- Measure  $^8\text{B}$  flux
- Day / Night and Seasonal variations
- $2.38 \pm 0.05 \times 10^{-6} \text{ cm}^{-2} \text{ s}^{-1}$
- Data/ SSM =  $0.465 \pm 0.005$

# Super-Kamiokande ( SK Only )

Phys.Rev.D78:032002 (2008)



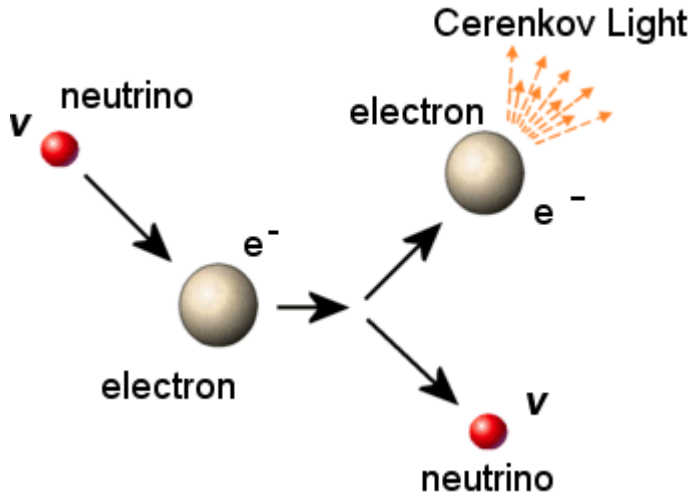
Best Fit::  $\tan^2 \theta = 0.4$   $\delta m^2 = 6.0 \times 10^{-5} eV^2$



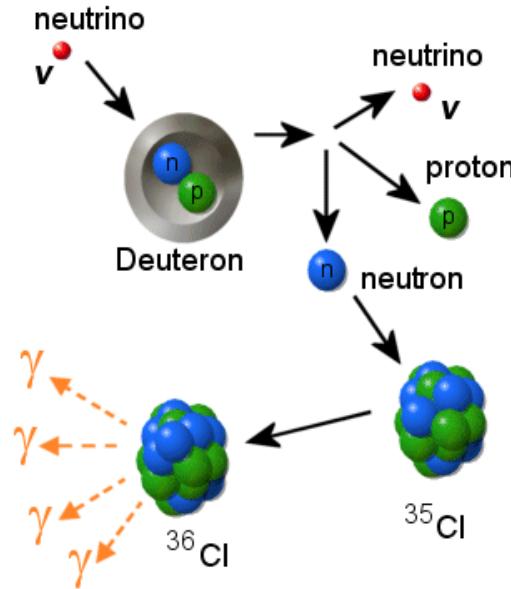
Constrained to SNO  $^8B$  flux  
(S.N. Ahmed et al., PRL92 (2004) 181301)

# Sudbury Neutrino Observatory - SNO

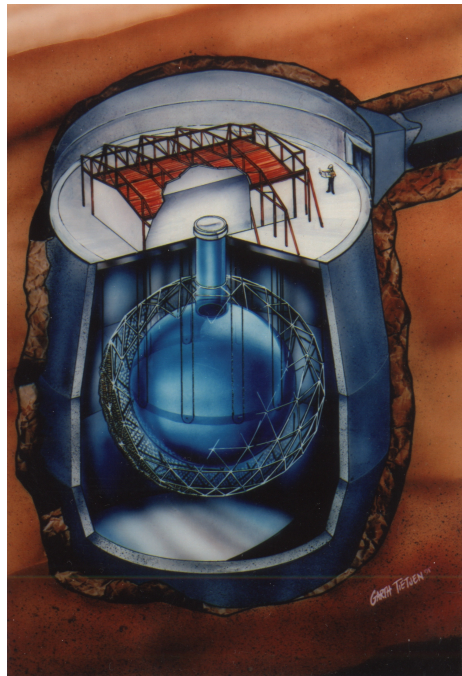
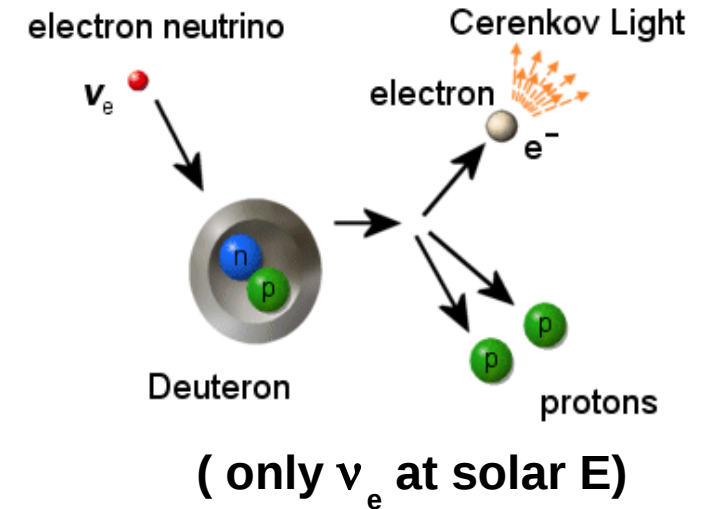
## Elastic Scattering (ES)



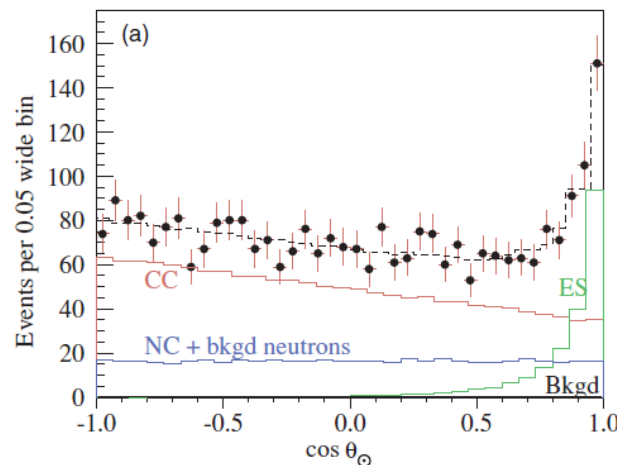
## Neutral Current (NC)



## Charged Current (CC)



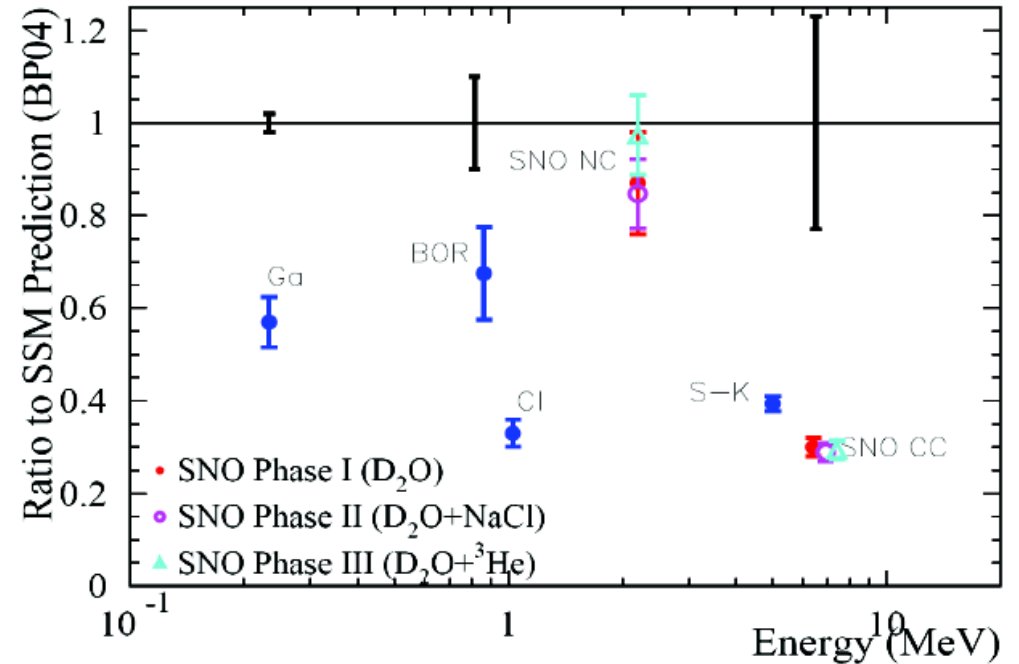
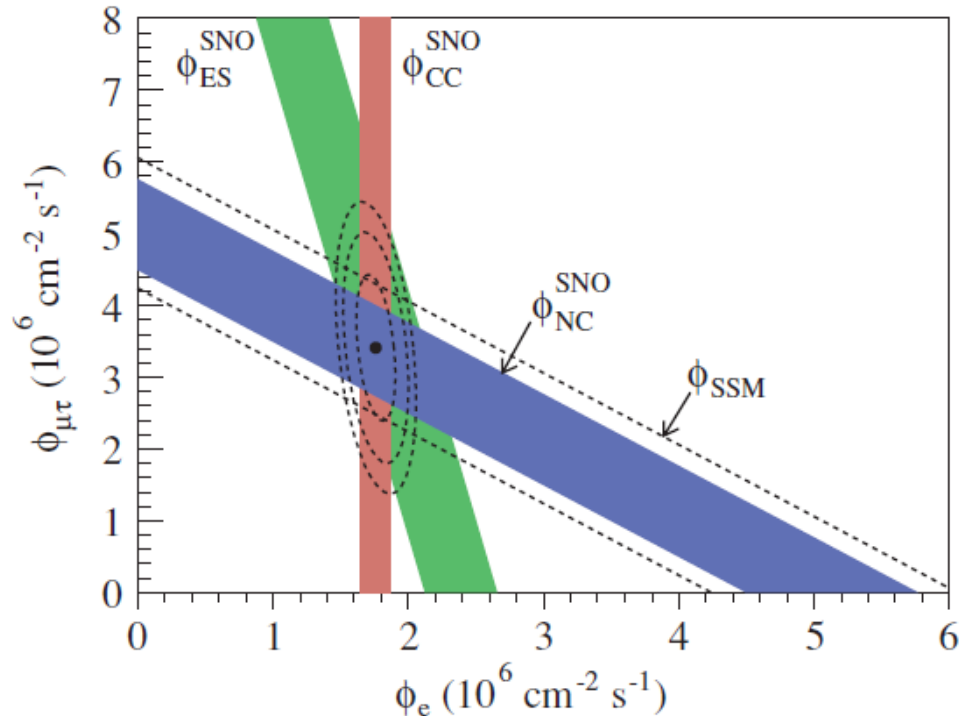
## Cherenkov imaging experiment using $\text{D}_2\text{O}$ (1 kton)



Independent measurements of  $\nu_e$  component and total active  $\nu_x$  component of the solar  $^8\text{B}$  flux

# SNO $^8\text{B}$ Fluxes

B. Ahramin et al., Phys. Rev. C 75 04552 (2007)

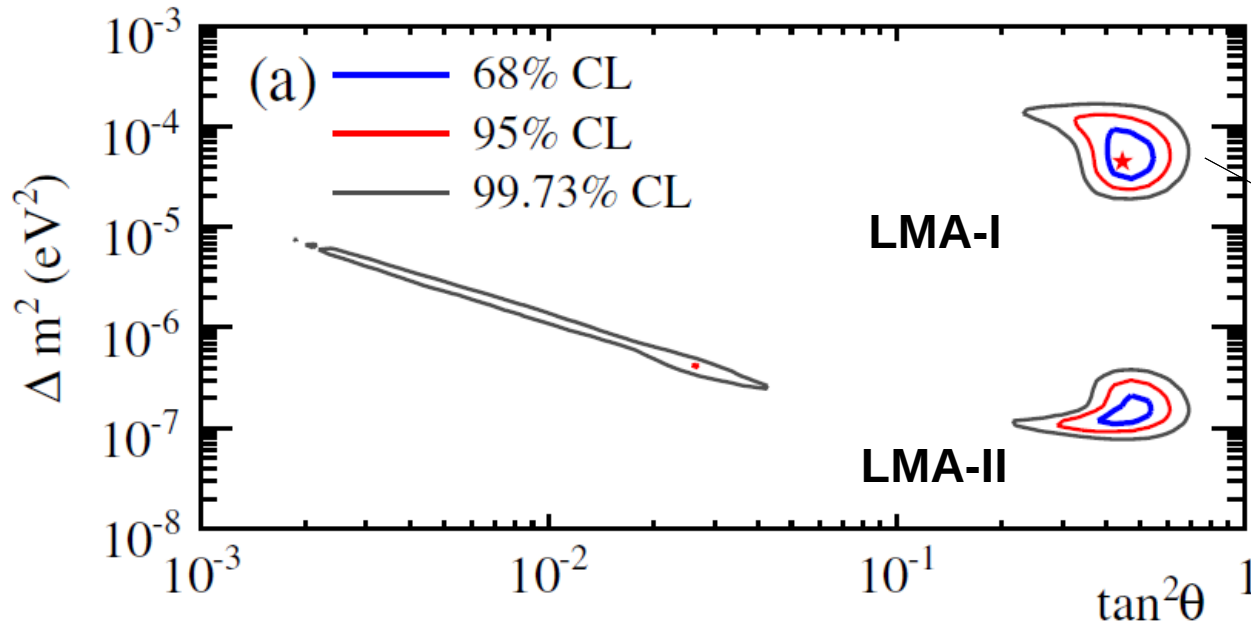


**ES flux is well below the standard solar model prediction**  
**Consistent with observations from other solar experiments**

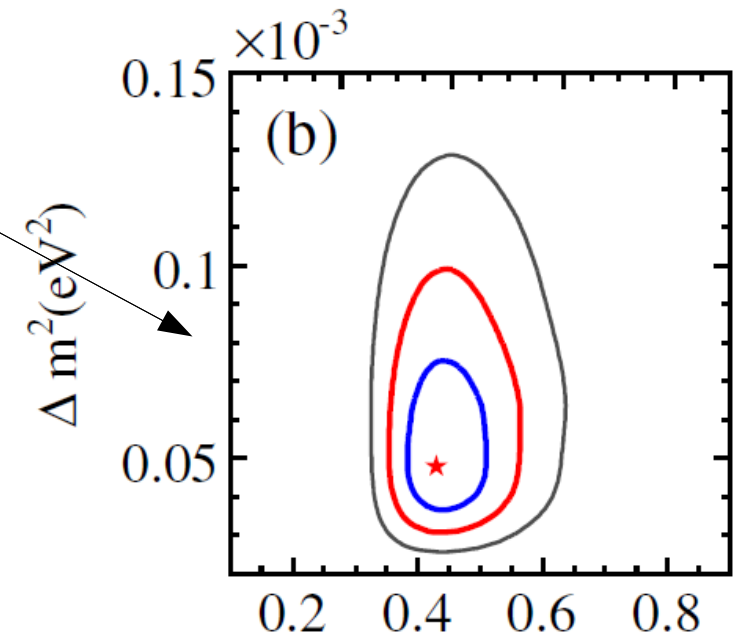
**NC flux agrees well with the SSM prediction**  
**Strong evidence that non- $\nu_e$  neutrinos make up solar flux...**

# SNO : Oscillation Contours

PRL 101, 111301 (2008)



SNO Only (D<sub>2</sub>O, salt, NCD)



SNO + Solar Experiments

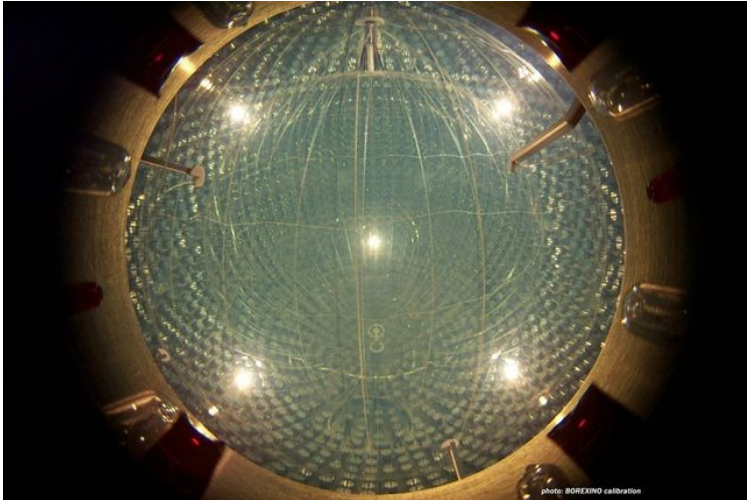
## Best Fit:

SNO Only:  $\tan^2\theta = 0.447$   $\delta m^2 = 4.57 \times 10^{-5}$  eV<sup>2</sup>

SNO + Solar:  $\tan^2\theta = 0.437$   $\delta m^2 = 4.90 \times 10^{-5}$  eV<sup>2</sup>

Global solar neutrino data favor the MSW-LMA solution to solar neutrino problem ... more precision with reactor experiments

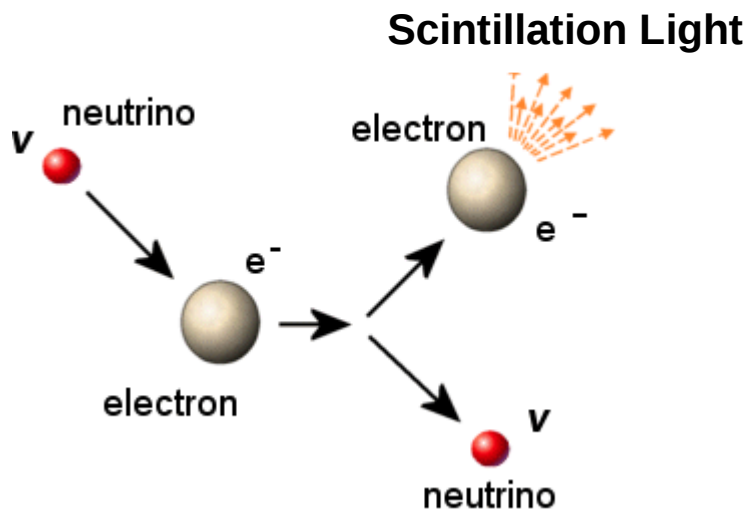
# Borexino : $^7\text{Be}$ Flux Measurement



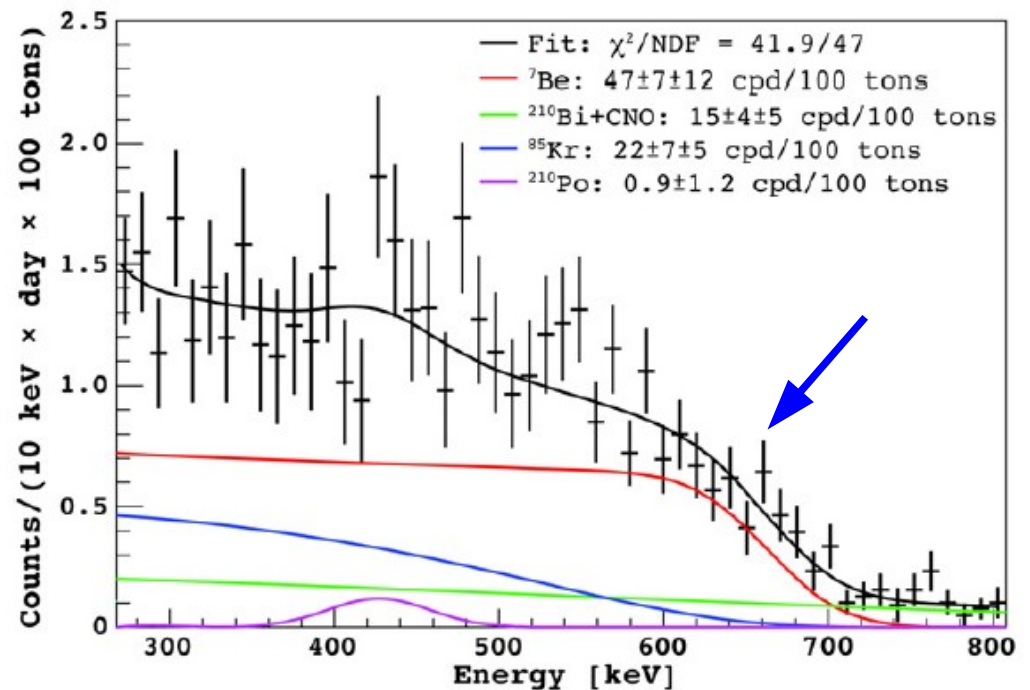
~ 300 ton liquid scintillator experiment  
No directionality: Scattered  $e^-$   
indistinguishable from BG  $e^-$   
low background essential

Measure  $^7\text{Be } \nu$  ( 865 KeV ) ~ 10% of flux  
Also sensitive to  $^8\text{B } \nu$

## Elastic Scattering (ES)

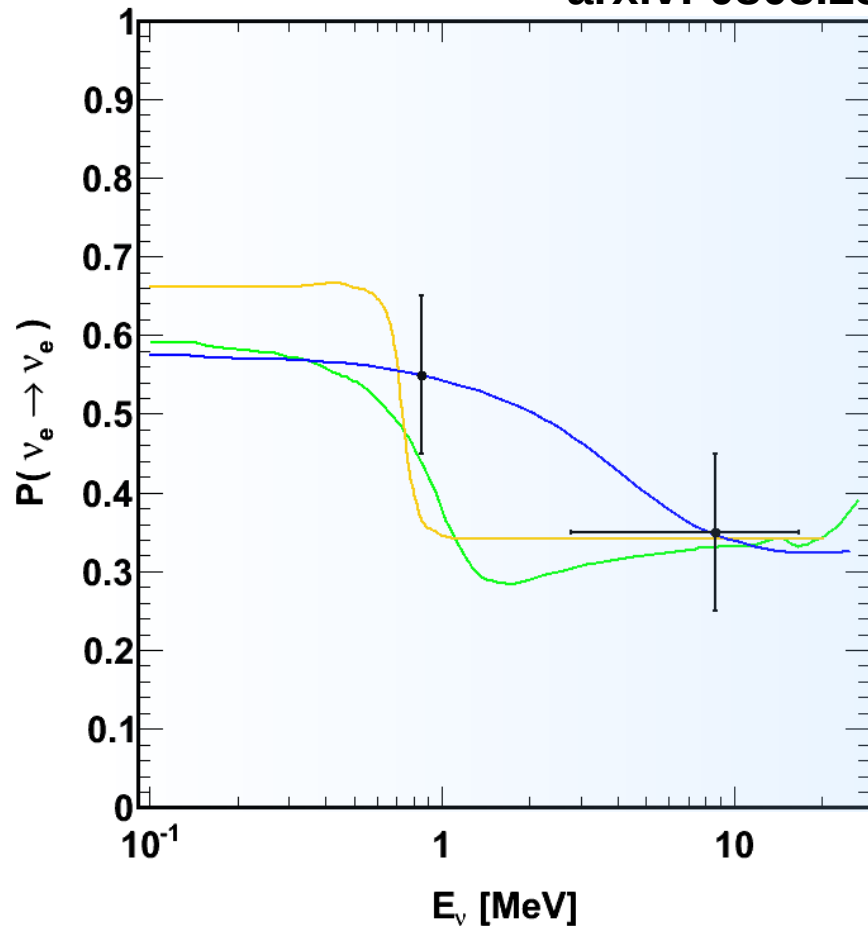


Physics Letters B 658 (2008) 101-108



# Borexino Results

arxiv: 0808.2868v11



- Borexino
- LMA-MSW
- NSI Friedland PLB594
- MaVan Barger et. al, PRL 95

$$P_{ee}({}^7\text{Be}) / P_{ee}({}^8\text{B}) = 1.8 \sigma$$

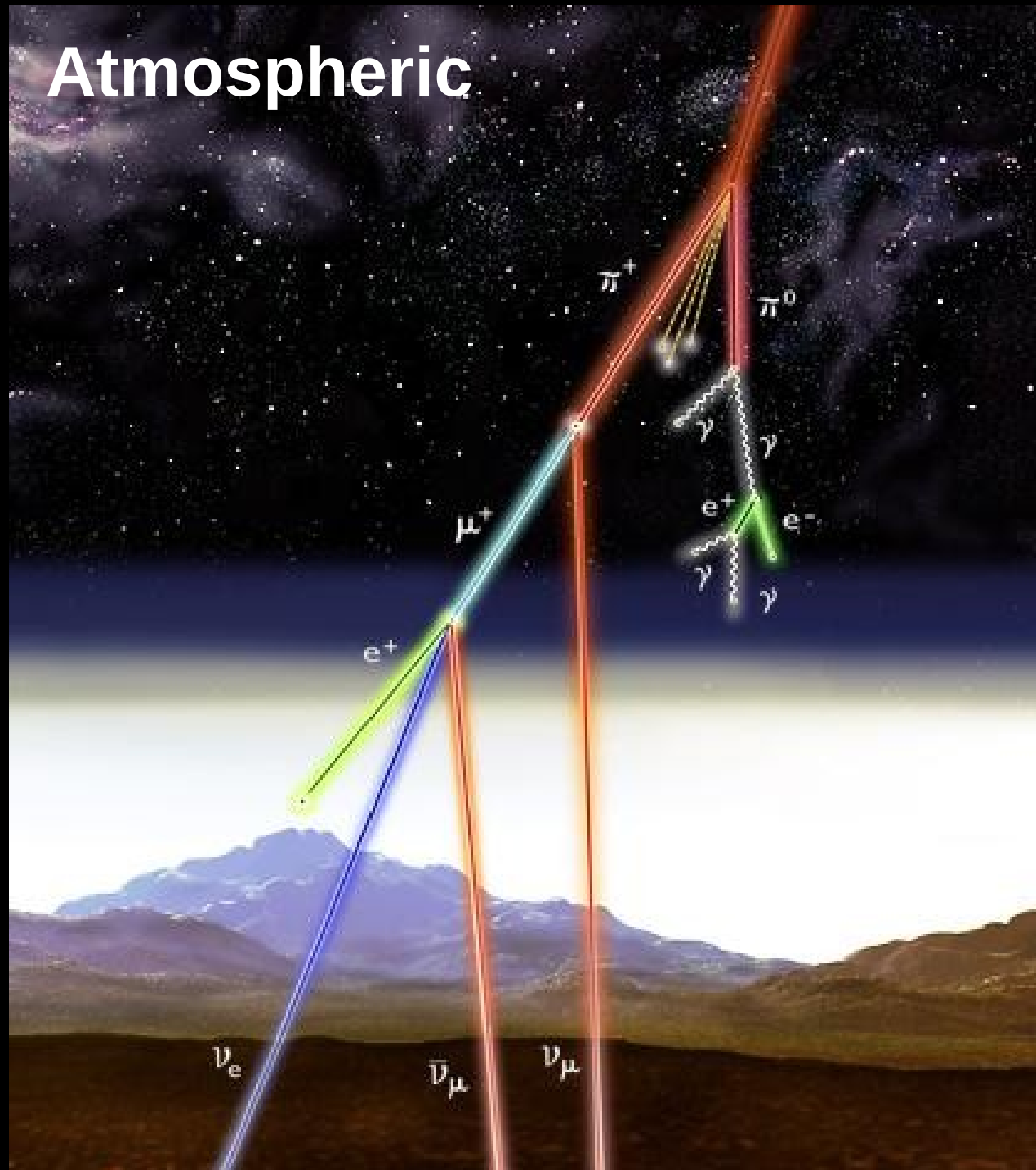
Physics Letters B 658 (2008) 101-108

${}^7\text{Be} \Phi : 47 \pm 7 \pm 12 \text{ ev / d / 100t}$  vs: unosc  $74 \pm 4 \text{ ev/d/100t}$

${}^8\text{B} \Phi (> 2.8 \text{ MeV}) : 2.65 \pm 0.44 \pm 0.18 \times 10^{-6} \text{ cm}^{-2} \text{ s}^{-1}$

**Borexino data is consistent with the MSW-LMA parameter space**

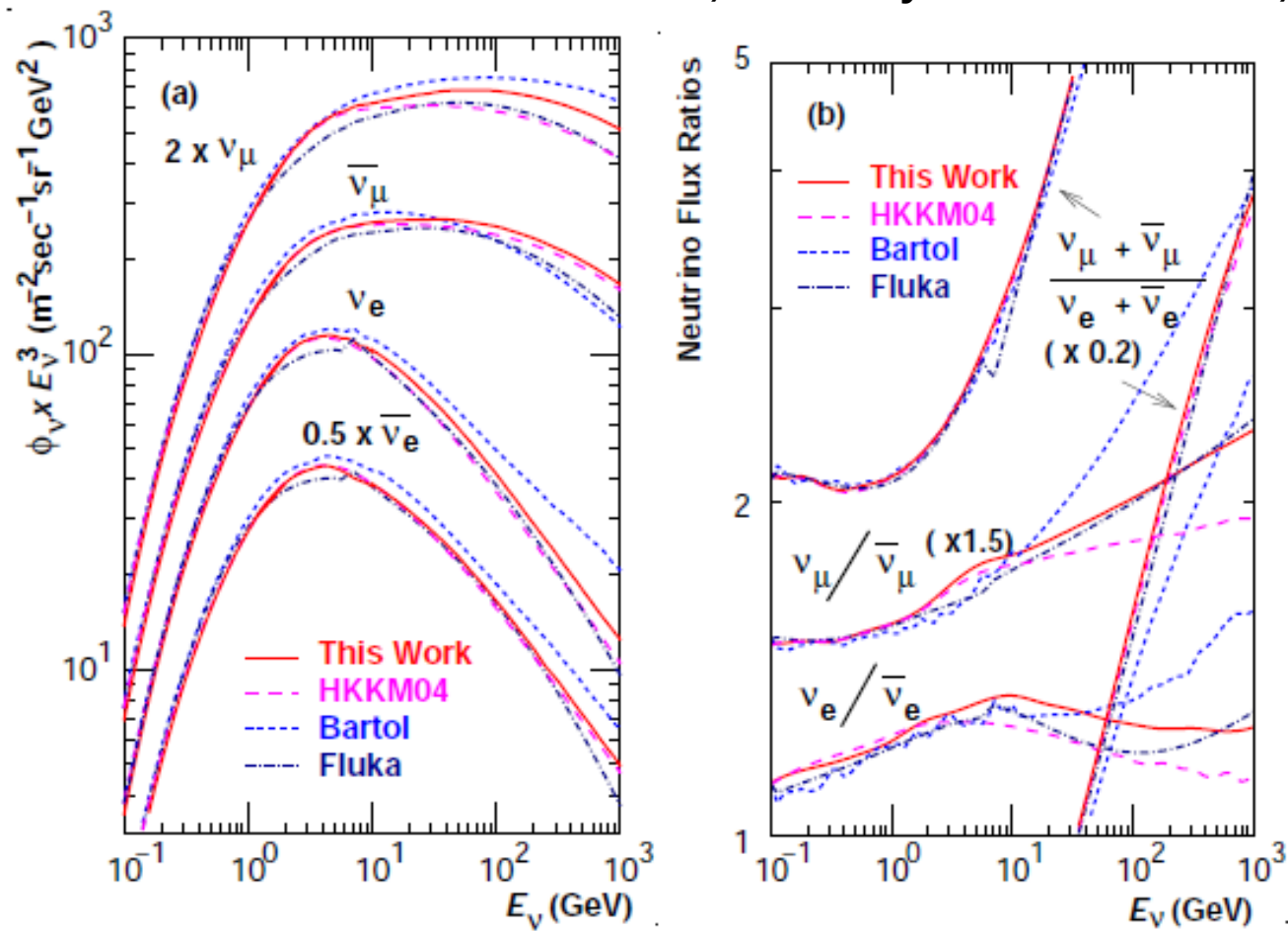
# Atmospheric





# Atmospheric $\nu$ Fluxes

M. Honda, et. al Phys.Rev.D75:043006,2007



Flux is isotropic about the Earth

- Large variation in  $\nu$  pathlength  $\sim 10 - 10^4$  km

Spanning several energy decades

At energies  $E < 10$  GeV flux ratio  $\nu_{\mu} / \nu_e \sim 2$



Large Variation  
in  $L/E$   
Good for osc.  
studies

# Atmospheric $\nu$ Anomaly

Taken from Fogli PhysRevD.52.2775

Experiment	Refs.	Total exposure (kt yr)	Simulated exposure (kt yr)	$\mu$ -like events		$e$ -like events		
				Data	BGS	Data	BGS	
H <sub>2</sub> O	Kamiokande sub-GeV	[3]	7.7	43	234	396.0	248	257.2
	Kamiokande multi-GeV (FC)	[3]	8.2	51	31	40.4	98	70.8
	Kamiokande multi-GeV (FC+PC)	[3]	8.2+6.0	51+40	135	165.8	98	70.8
Fe	IMB	[4],[5]	7.7	33	182	344.5	325	339.4
	Fréjus (FC)	[6],[7]	1.56	10	66	90.0	56	66.8
	Fréjus (all)	[6],[7]	1.56	10	108	125.8	57	70.6
	NUSEX	[8]	0.74	~15	32	36.8	18	20.5

Detectors with a water target saw evidence for  $\nu_{\mu}$  disappearance

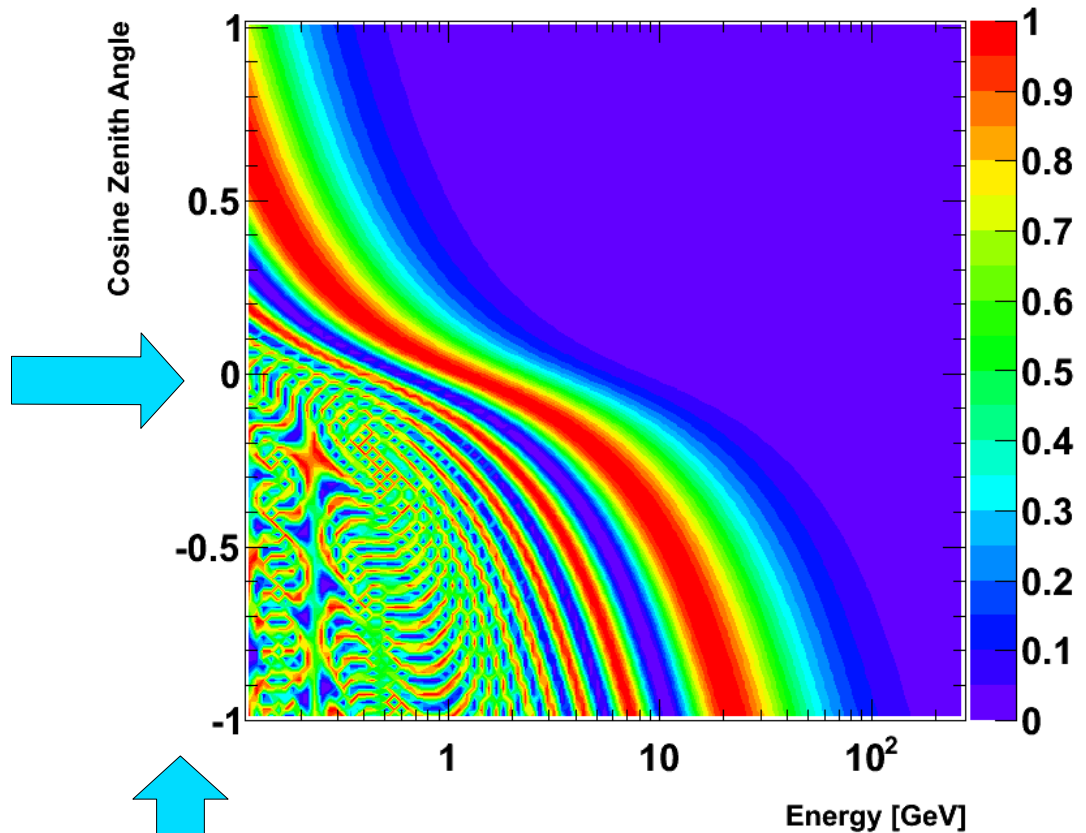
Iron based detector signatures were more consistent with no oscillation

No strong deviation found in  $\nu_e$  samples

# Oscillation interpretation

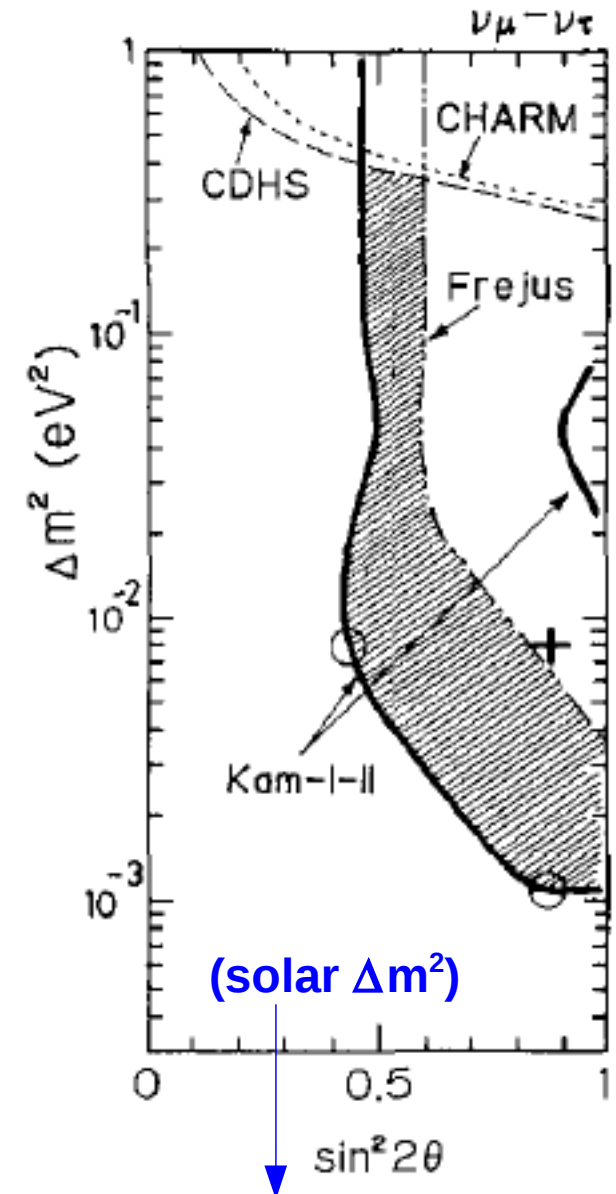
Two flavor oscillations:  $\nu_\mu \rightarrow \nu_\tau$

$$P(\nu_\mu \rightarrow \nu_\tau)$$



Upward going events have opportunity to oscillate away

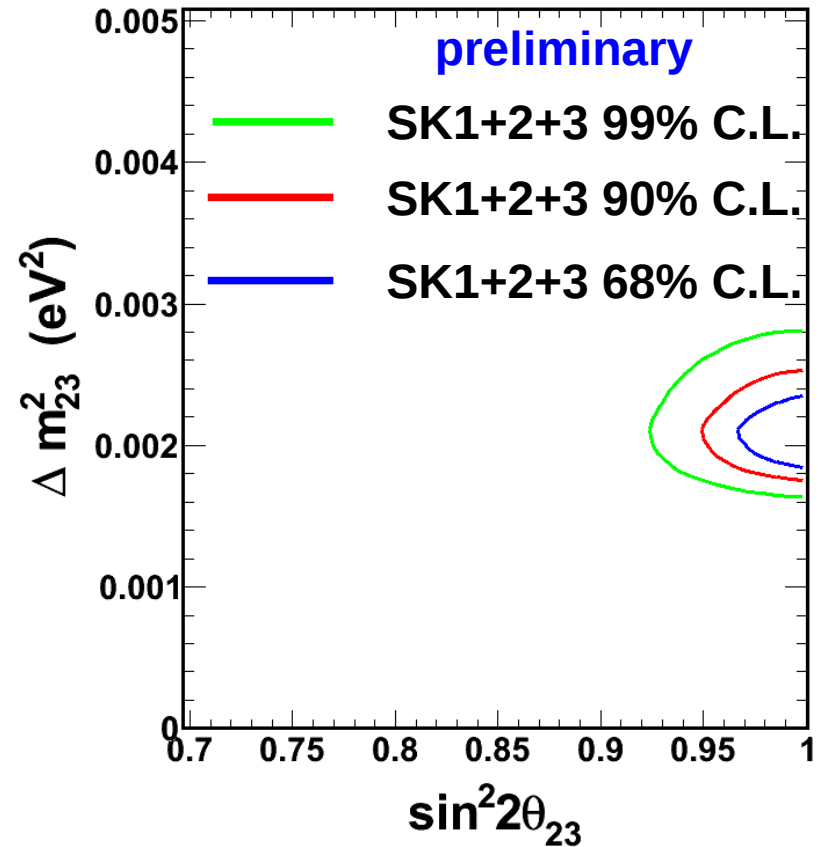
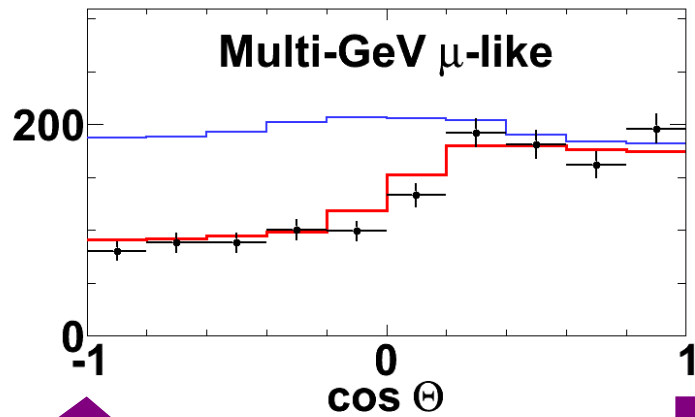
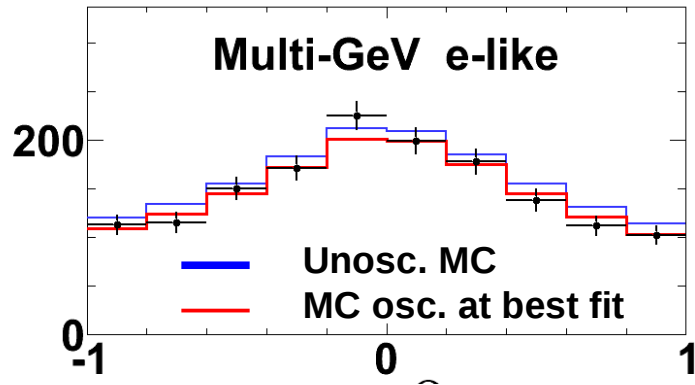
Phys. Lett. B 280 (1992) 146



# Super-Kamiokande: Atmospheric $\nu$

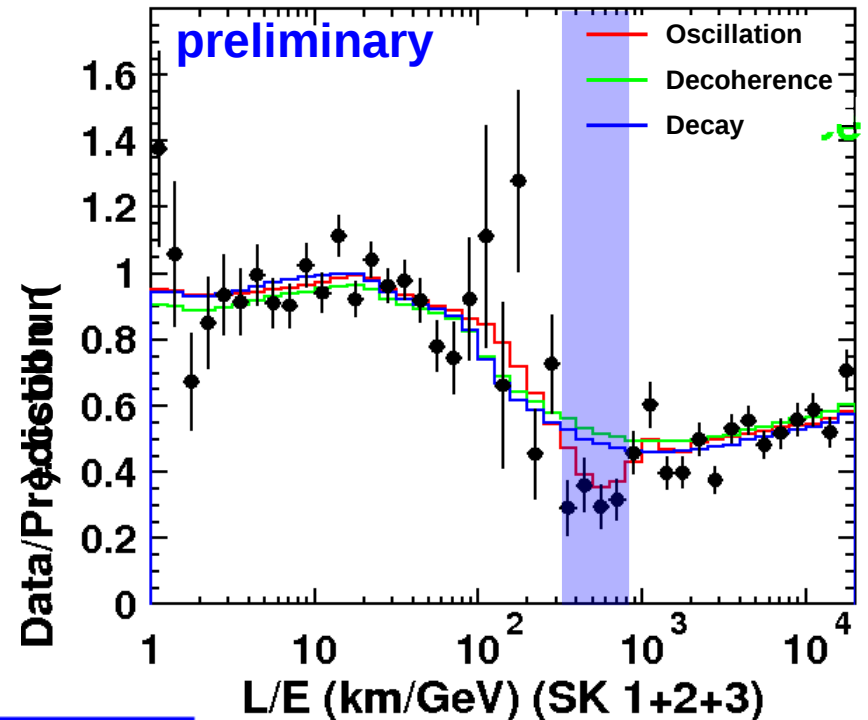
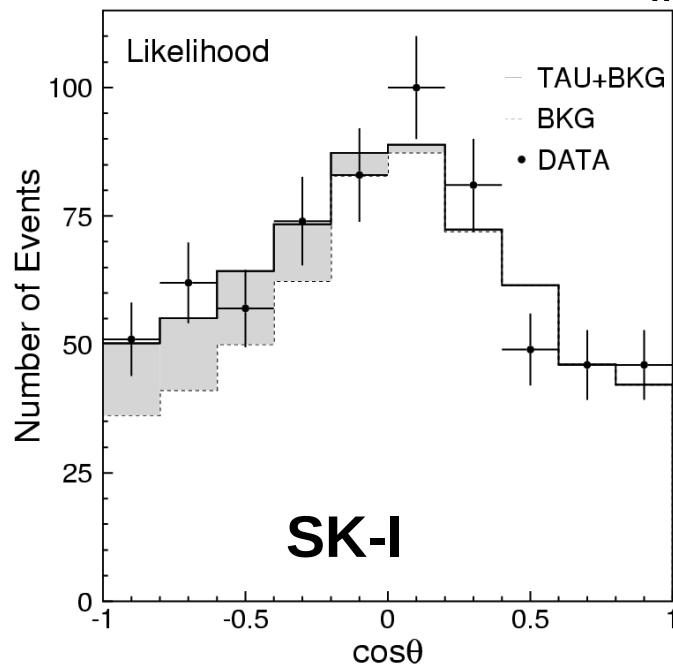
- High statistics
  - > 28,000  $\nu$  events

SK-I + II + III 2806 days



Best Fit: (physical):  
 $\Delta m^2 = 2.1 \times 10^{-3} \text{ eV}^2$   
 $\sin^2 2\theta = 1.0$   
 $\chi^2 = 468 / 418\text{d.o.f}$

# Where are the Super-K $\nu_{\mu}$ going?



Model	Limit / Exclusion
$\nu_{\mu} \rightarrow \nu_s$	7.2 $\sigma$ (SK-I + SK-II)
Sterile admixture (2+2)	23% allowed
Decay ( $\sin^4\theta + \cos^4\theta e^{-\alpha L/E}$ )	17 $\sigma$
Decay ( $\sin^2\theta + \cos^2\theta e^{-\alpha L/E}$ ) <sup>2</sup>	3.9 $\sigma$
Decoherence	4.4 $\sigma$
LIV Limit	$1.2 \times 10^{-24}$
CPTV Limit (GeV)	$0.9 \times 10^{-23}$
MaVaNs	3.5 – 3.8 $\sigma$ (SK-I)

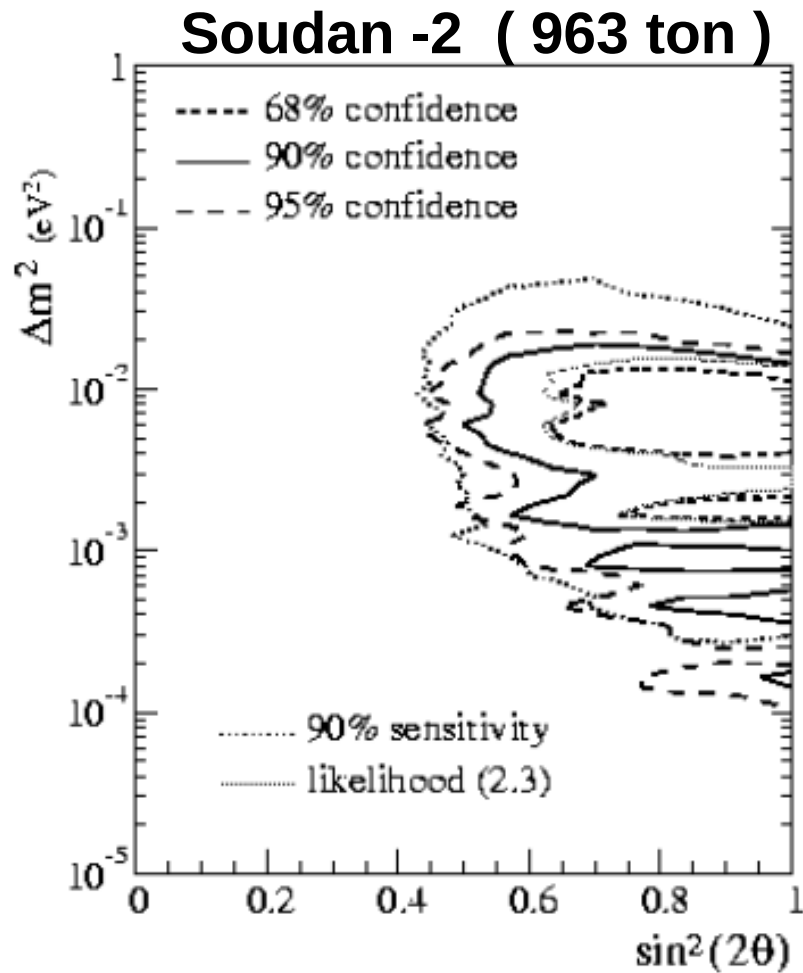
← No pure sterile

What about  $\theta_{13}$  ?

What about  $\theta_{23}$  's octant?

SK-I+II+III in detail:  
see: J.L. Raaf talk

# Soudan and MACRO Atmospheric $\nu$



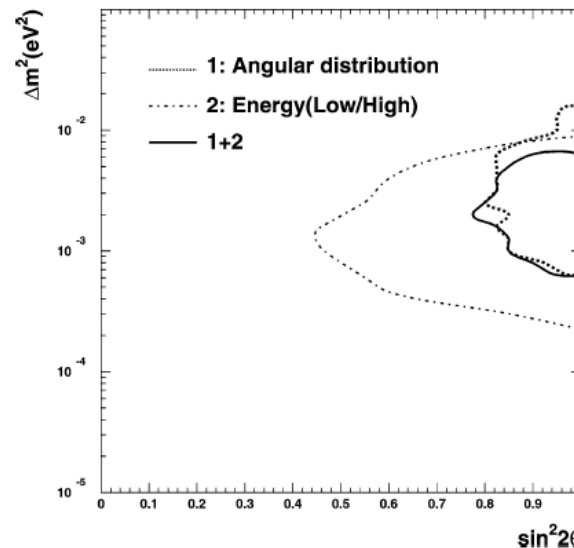
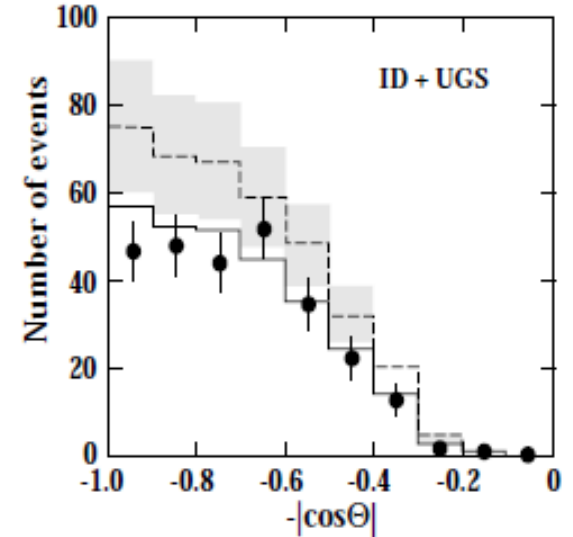
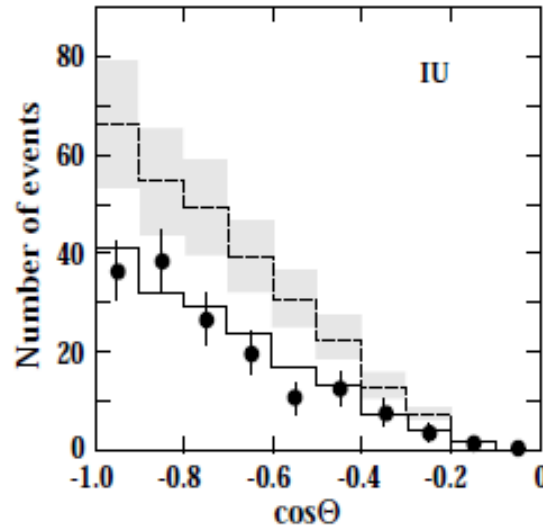
M. Sanchez Ph1ys. Rev. D68 (2003) 113004

**Best Fit::**

$$\Delta m^2 = 5.2 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta = 0.97$$

### MACRO



**Best Fit: :**

$$\Delta m^2 = 2.3 \times 10^{-3} \text{ eV}^2$$

$$\sin^2 2\theta = 1.0$$

**Confirmation of a consistent oscillation picture  
 ⇒ more precision with beam experiments**

# MINOS – Atmospheric $\nu$ 's

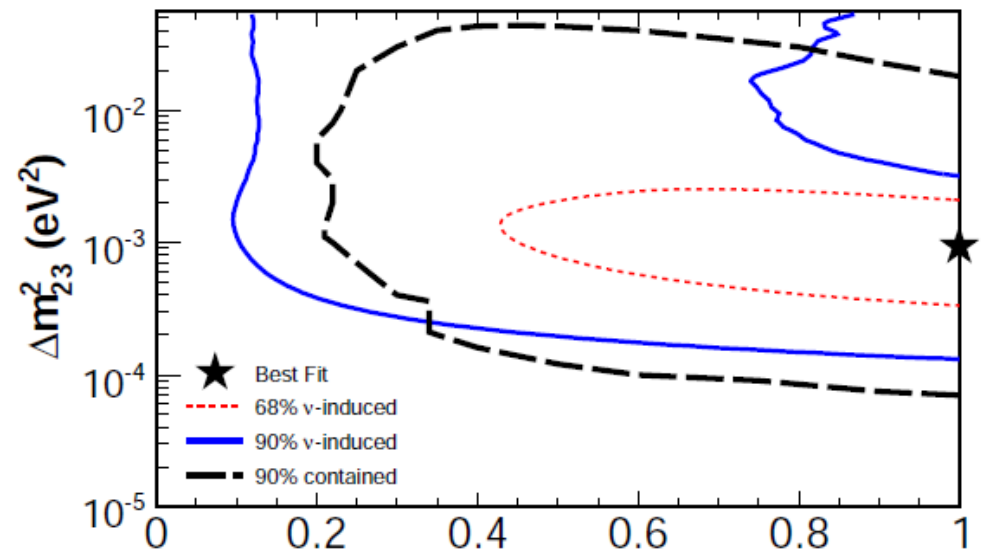
Search for  $\nu$ -induced muon events  
in the MINOS far detector

Magnetized: event by event  
separation of  $\mu^-$  and  $\mu^+$

Total : 140 events in 854 d



Phys.Rev.D75:092003,2007



Double Ratio:

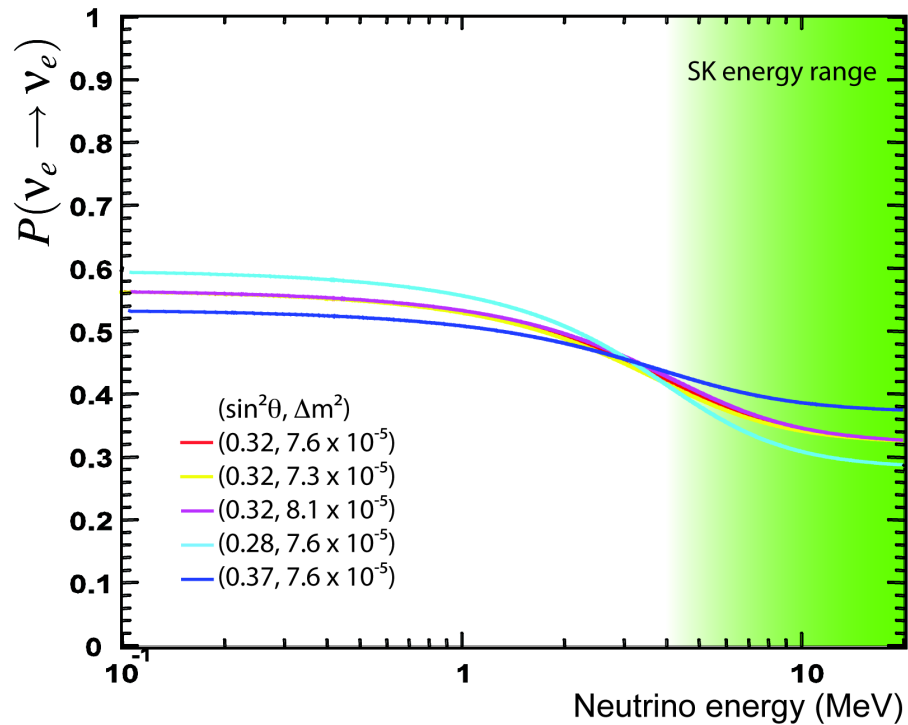
$$R = 0.65 \pm 0.09 \text{ (sys)}$$

CPT Double Ratio:

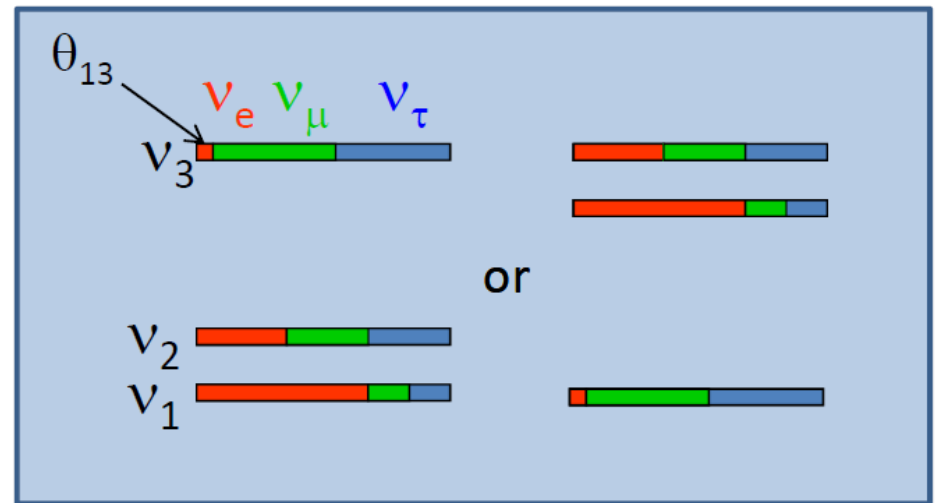
$$R_{cpt} = (\mu^-/\mu^+)_{\text{data}} / (\mu^-/\mu^+)_{\text{MC}} = 0.72^{+0.24}_{-0.18} \text{ (stat.) } +^{0.08}_{-0.04}$$

Consistent with no CPT Violation

# The Future



**Solar upturn?**  
**Earth regeneration effects?**  
**Day/Night ?**



$\theta_{13} > ?$

**Mass Hierarchy ?**

$\theta_{23}$  Octant



**Future : Observe all effects !**

## **SNO**

Low Energy Threshold analysis (**3.5 MeV** )

Improved oscillation parameters?

Solar upturn?

## **Super-Kamiokande**

Low energy solar upturn?

Earth regeneration effects and Day / Night asymmetry ?

Continued atmospheric running...

## **SNO+**

Observe pep and CNO neutrinos : Probe intermediate MSW region ?

## **LENS , CLEAN (others )**

Observe pp neutrinos : see M. Pitt's LENS talk in Neutrinos IV

## **INO**

Sensitivity to mass hierarchy ?

$\theta_{13} > 0$  ?

... and more ...

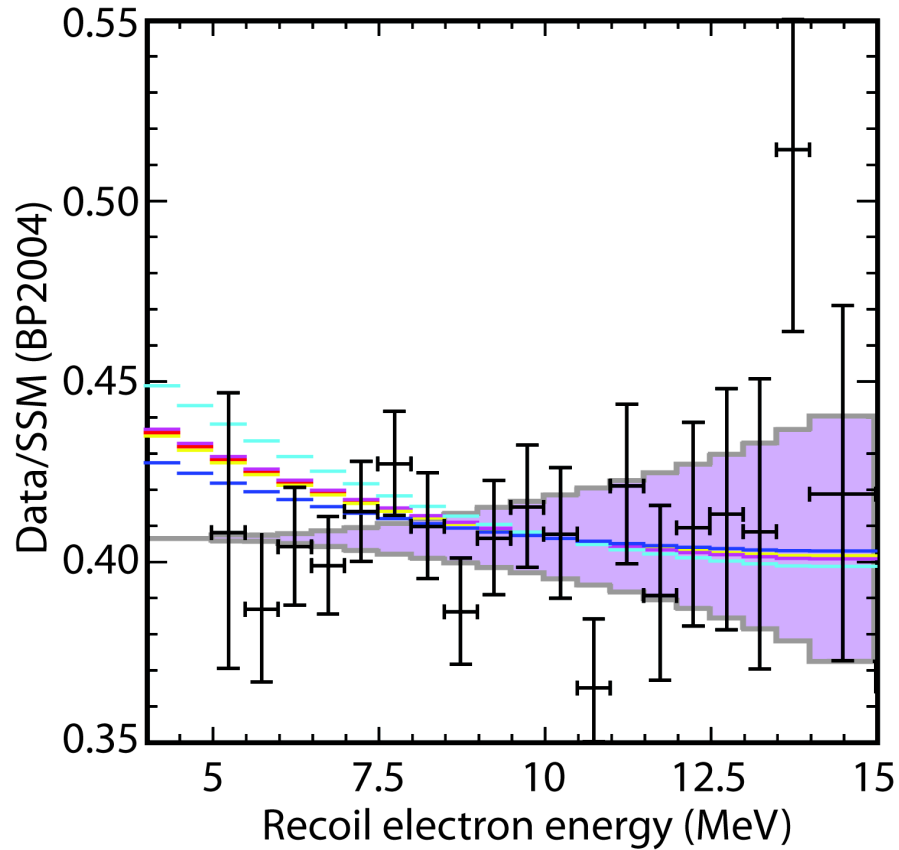
# Summary

- Observations of natural  $\nu$  sources have consistently yielded fewer events than would be expected in models where  $\nu$  mass is zero
  - across various  $\nu$  energies and detector targets
- Resolving these discrepancies lead to the discovery of  $\nu$  mass and  $\nu$  oscillations in two different regimes “solar” and “atmospheric”
  - $\Delta m^2_{\text{atm}} / \Delta m^2_{\text{solar}} = \sim 30 - 40$
  - Large angle mixing
- The observations of solar and atmospheric neutrinos have confirmed  $\nu$  oscillation scenarios and are increasingly constraining the values of these oscillation parameters
  - Additional information from reactor and accelerator experiments further improves these measurements ( see M.Bishai, other talks here)
  - Still plenty of questions remain to be explored

Thank you

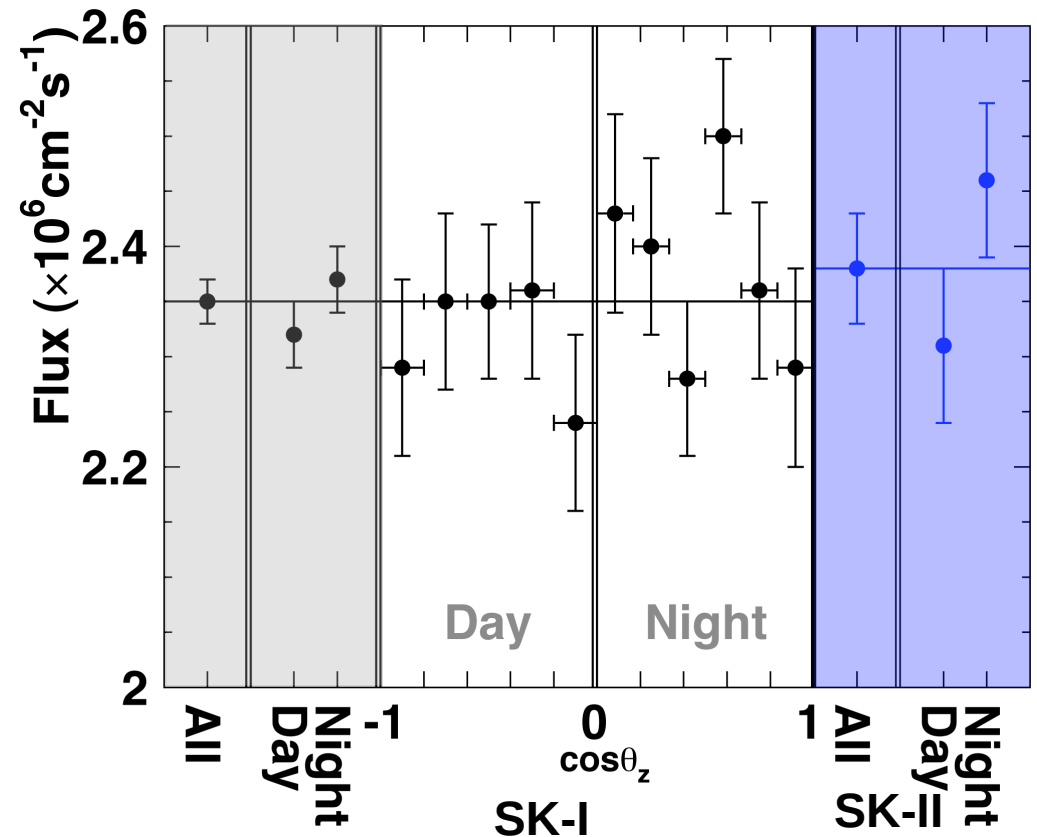
# Supplements

# The Future of Super-K Solar $\nu$ studies

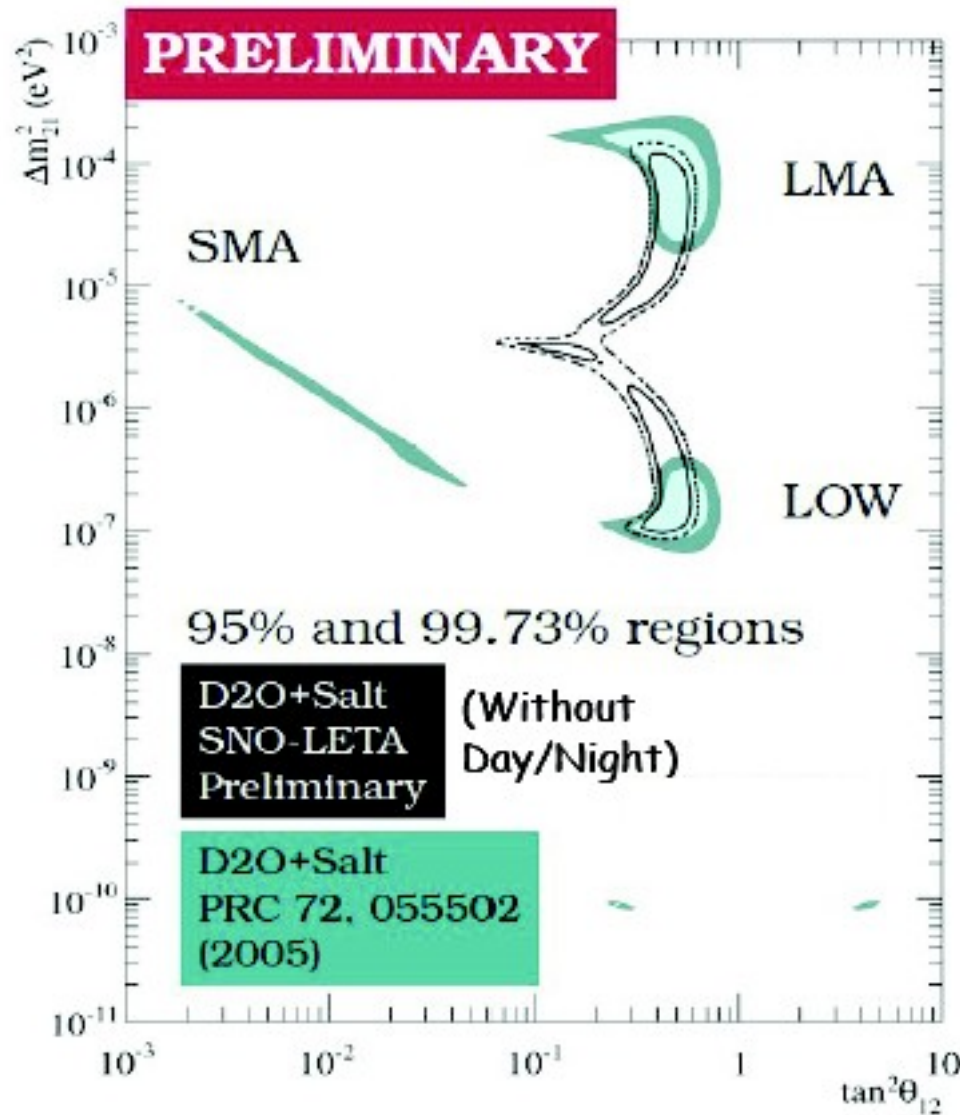


- Low energy upturn should be visible in the SK data ?

- Regeneration effects, Day/Night asymmetry



# SNO - Low Energy Threshold Analysis



- Reduce backgrounds and lower analysis threshold to **3.5 MeV**
- Two and Three flavor contours with KamLAND data
  - Improved solar parameters?
  - Information on  $\theta_{13}$  ?
- Direct extraction of survival probability
  - MSW upturn effects?

# SNO+

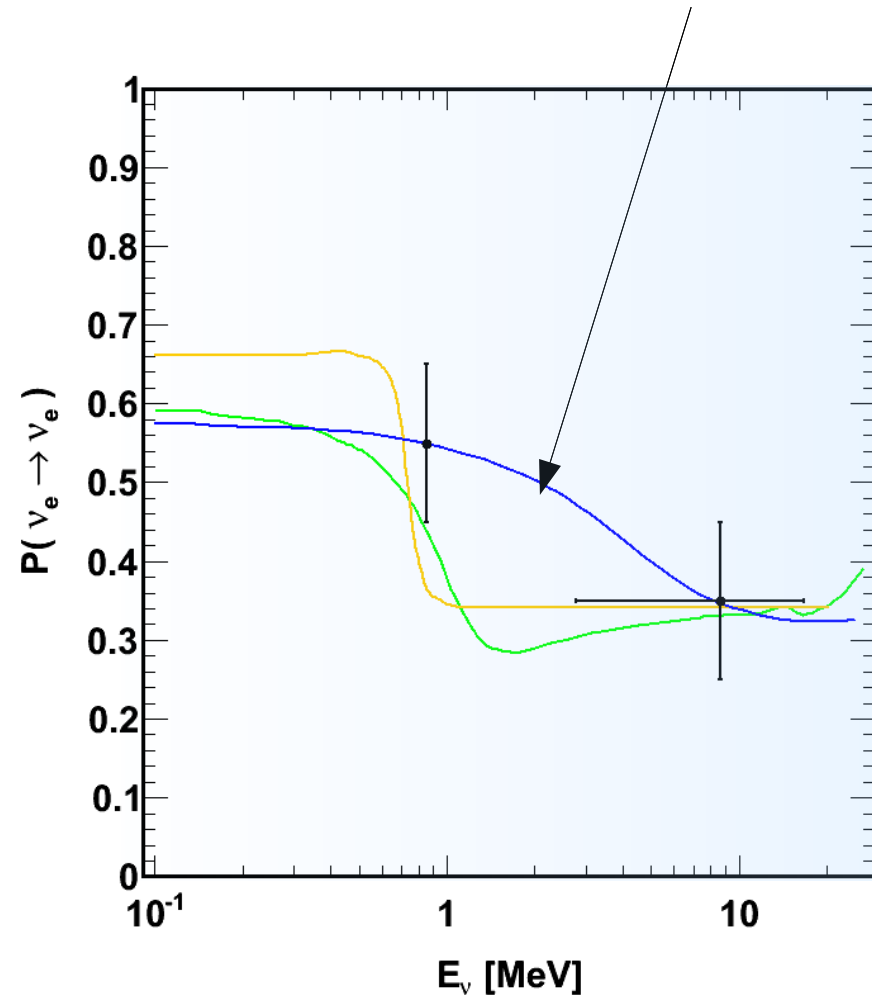
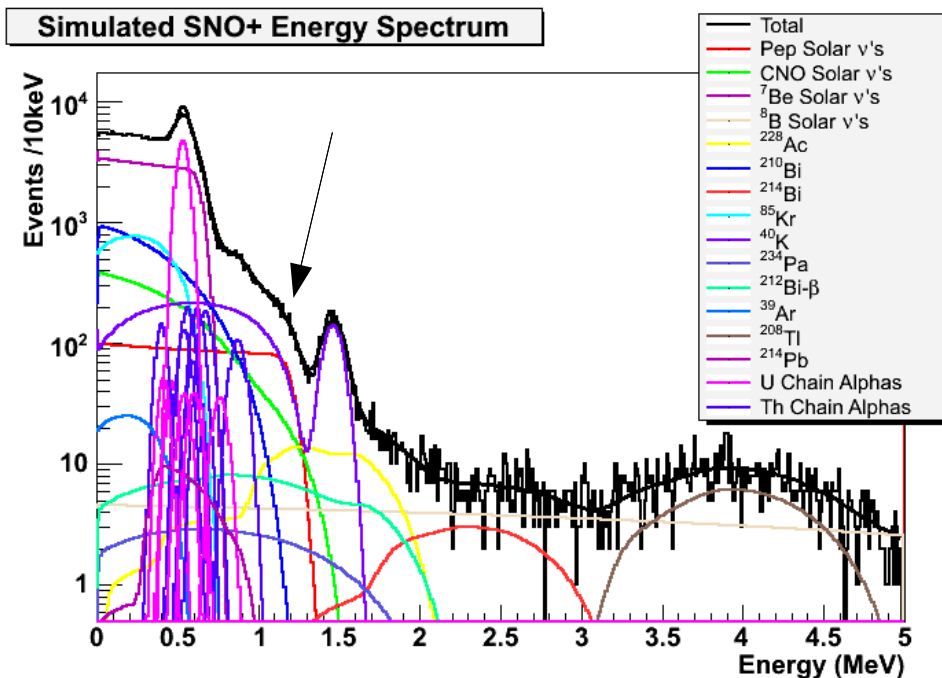
An experiment to fill the SNO acrylic vessel with liquid scintillator to study:

Geo- $\nu$ ,  $0\nu \beta$ -decay

pep and CNO  $\nu$  - Energy shoulder 1.4 MeV

→ Probe MSW transition region

SNO+ ??



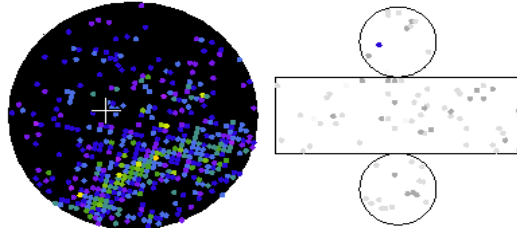
See Also : Precision Measurement of the Low Energy Solar Neutrino Spectrum with the LENS Experiment : M. Pitt neutrino-IV

# Two Fully Contained events from the SK-I Data

e-like

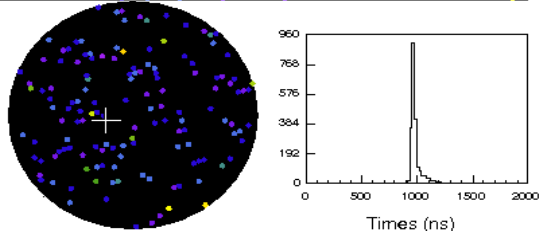
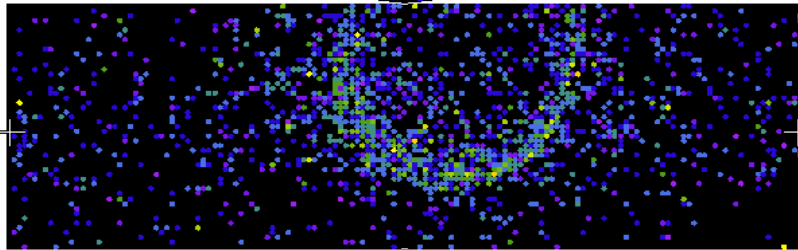
## Super-Kamiokande I

Run 3142 Sub 21 Ev 126426  
 96-11-24:19:52:45  
 Inner: 2700 hits, 3826 pE  
 Outer: 2 hits, 1 pE (ln-time)  
 Trigger ID: 0x03  
 D wall: 1219.5 cm  
 FC e-like,  $p = 442.0 \text{ MeV}/c$



### Charge (pe)

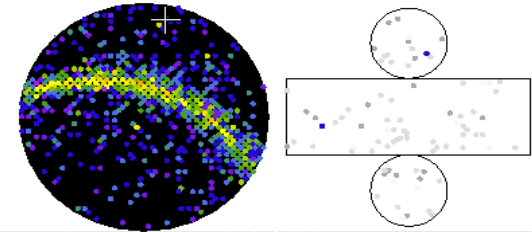
- >26.7
- 23.3-26.7
- 20.2-23.3
- 17.3-20.2
- 14.7-17.3
- 12.2-14.7
- 10.0-12.2
- 8.0-10.0
- 6.2- 8.0
- 4.7- 6.2
- 3.3- 4.7
- 2.2- 3.3
- 1.3- 2.2
- 0.7- 1.3
- 0.2- 0.7
- < 0.2



$\mu$ -like

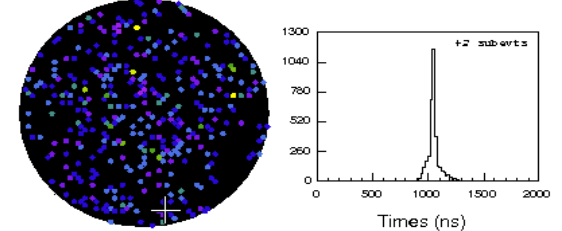
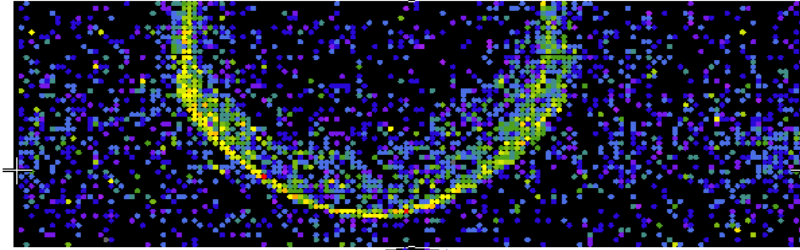
## Super-Kamiokande I

Run 3138 Sub 40 Ev 248548  
 96-11-23:04:00:25  
 Inner: 3587 hits, 5809 pE  
 Outer: 4 hits, 3 pE (ln-time)  
 Trigger ID: 0x03  
 D wall: 238.1 cm  
 FC  $\mu$ -like,  $p = 1205.3 \text{ MeV}/c$



### Charge (pe)

- >26.7
- 23.3-26.7
- 20.2-23.3
- 17.3-20.2
- 14.7-17.3
- 12.2-14.7
- 10.0-12.2
- 8.0-10.0
- 6.2- 8.0
- 4.7- 6.2
- 3.3- 4.7
- 2.2- 3.3
- 1.3- 2.2
- 0.7- 1.3
- 0.2- 0.7
- < 0.2



# SK-I + SK-II + SK-III Data (preliminary)

