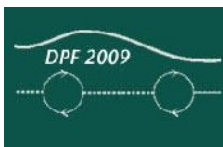


# Top Mass Measurements with the D0 Detector

Dan Boline  
On behalf of the D0 Colaboration

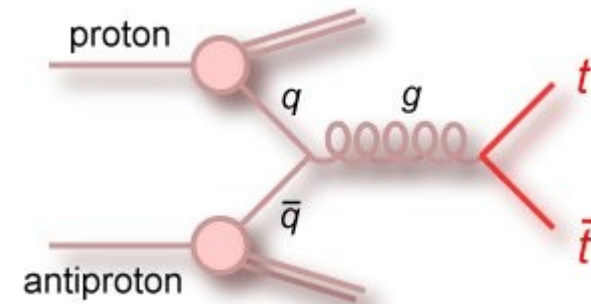
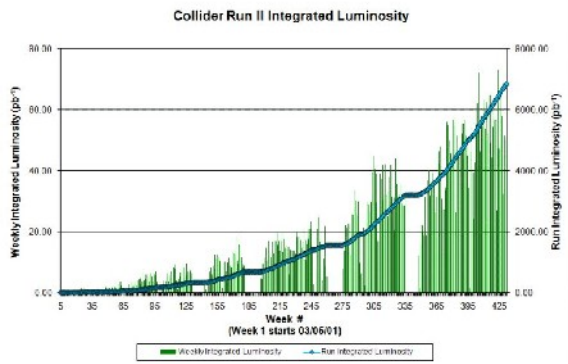
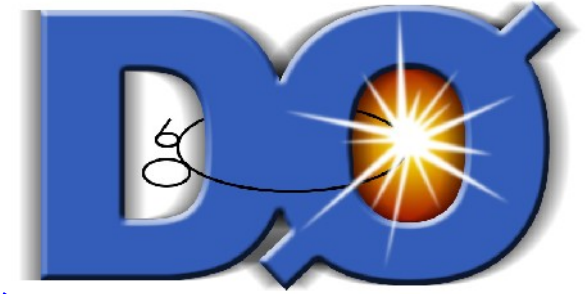


Wayne State University  
Detroit MI  
July 27-31



# Introduction

- Won't discuss D0 experiment, Tevatron, Top Pair production



Results with up to  $3.6 \text{ fb}^{-1}$  of data.

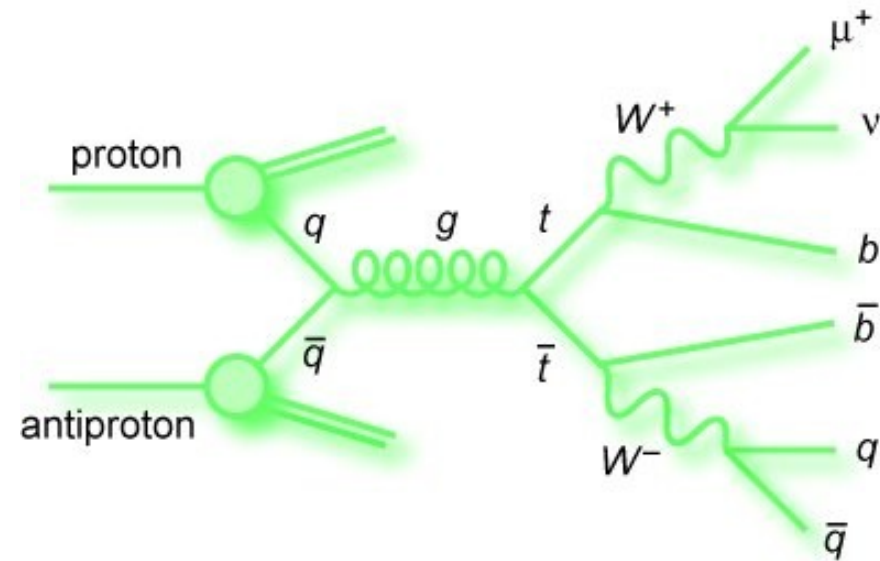
# Content of Talk

- Mass Measurement:
  - Lepton+Jets Channel:
    - First Top-antiTop Mass Difference ( $1.0 \text{ fb}^{-1}$ )
    - Matrix Element Mass in ( $3.6 \text{ fb}^{-1}$ )
  - Dilepton Channel:
    - Matrix Element Mass in  $e\mu$  ( $3.6 \text{ fb}^{-1}$ )
    - Template-Based Mass ( $1.0 \text{ fb}^{-1}$ )

# Event Selection : ljets channel

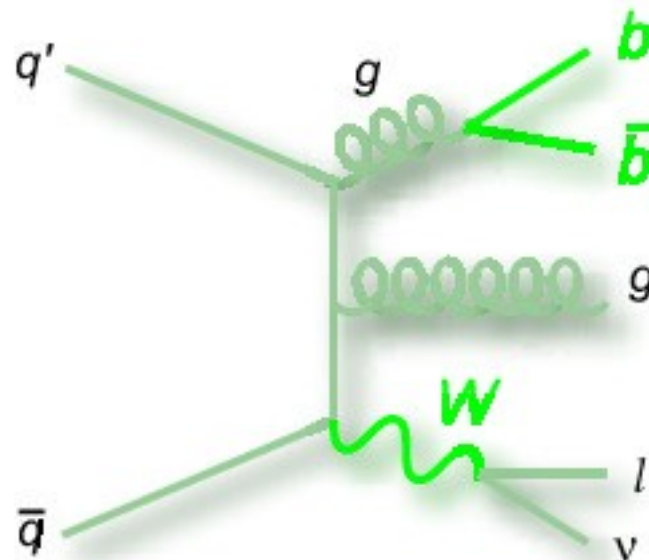
- Lepton+Jets Channel:

- 1 lepton
  - e or  $\mu$  ( $p_T > 15$  GeV)
- large MissingET
- 2 b-jets, 2 light jets



- Backgrounds:

- W+jets
- QCD



# Top Mass Difference

Top decays before it can hadronize

- > Can directly measure top quark mass
- > top anti-top assumed to have same mass
  - CPT invariance requires this
- > What happens if we drop the assumption?

# Matrix Element Method

$$\mathcal{L}(m_t, m_{\bar{t}}, f_t) = \prod_{i=1}^{N_{evt}} [f_t P_{sig}(x_i; m_t, m_{\bar{t}}) + (1 - f_t) P_{bkg}(x_i)]$$

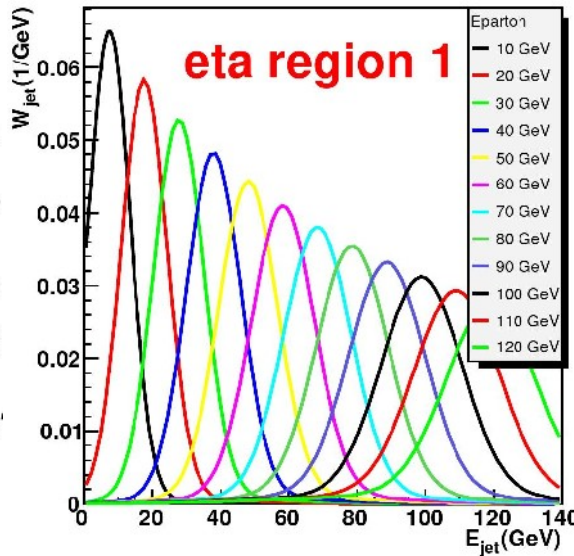
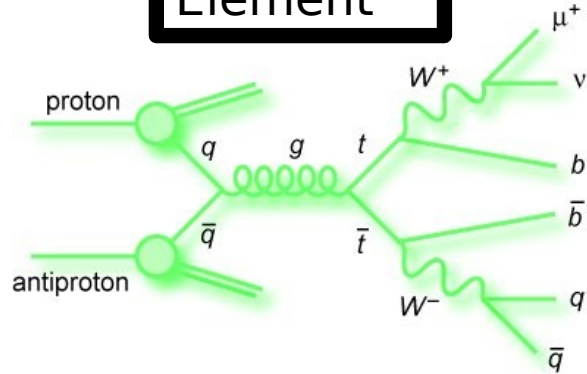
$$P_{sig}(x; m_t, m_{\bar{t}}) = Acc(x) \times \frac{1}{\sigma} \int d^n \sigma(y; m_t, m_{\bar{t}}) dq_1 dq_2 f(q_1) f(q_2) W(x, y)$$

Acceptance:  
selection  
efficiency

Transfer Function

Integrate over  
parton  
momenta

LO Matrix  
Element



Transform to convenient variables:

$$(m_t, m_{\bar{t}}) \rightarrow (\Delta m_t = (m_t - m_{\bar{t}}), m_{sum} = (m_t + m_{\bar{t}})/2)$$

Integrate out  $M_{sum}$ :

$$\mathcal{L}(\Delta m_t) = \int dm_{sum} \mathcal{L}(\Delta m_t, m_{sum})$$





# Simulating

$$m_t \neq m_{\bar{t}}$$

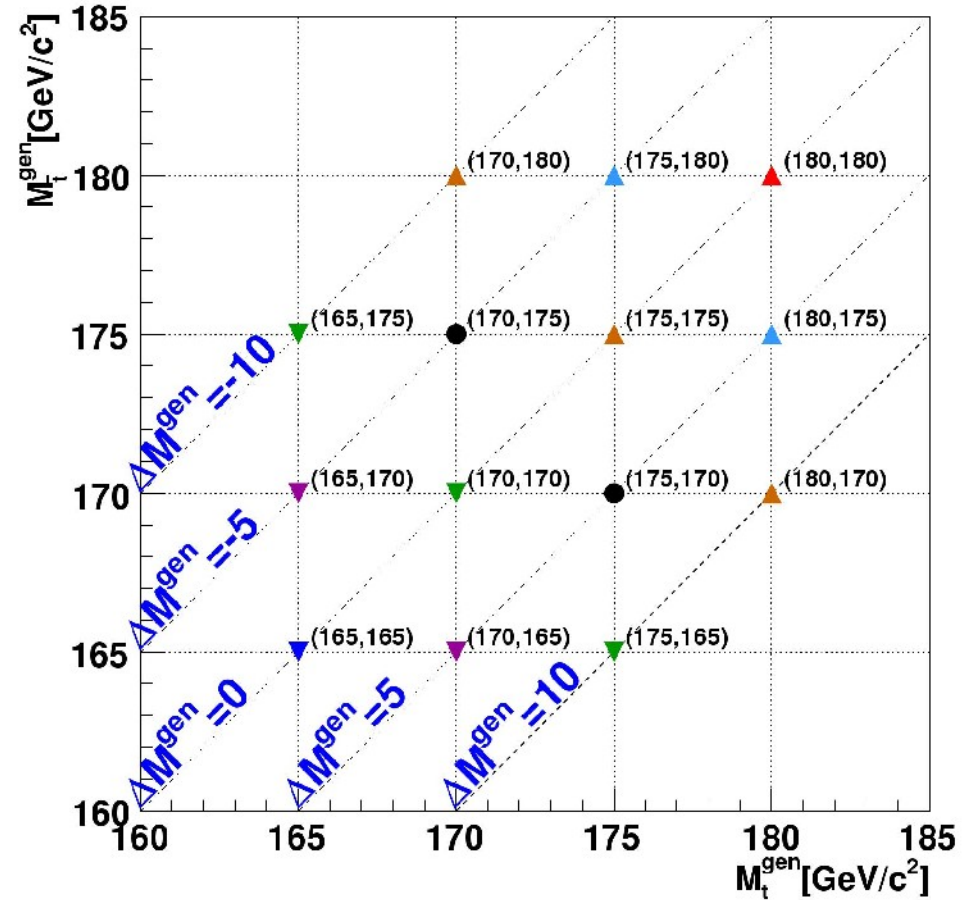
Samples generated with PYTHIA event generator

$m_t, m_{\bar{t}}$  set to different values.

Monte Carlo run through standard D0 Reconstruction (GEANT, etc)

W+jets background simulated with ALPGEN+PYTHIA

QCD Background taken from Data



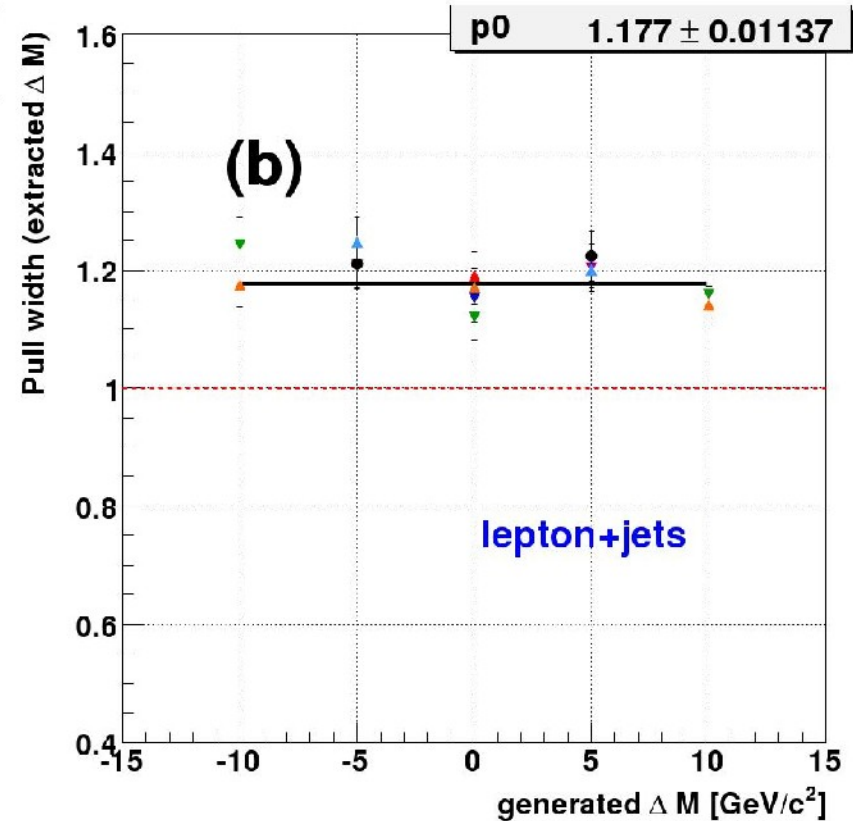
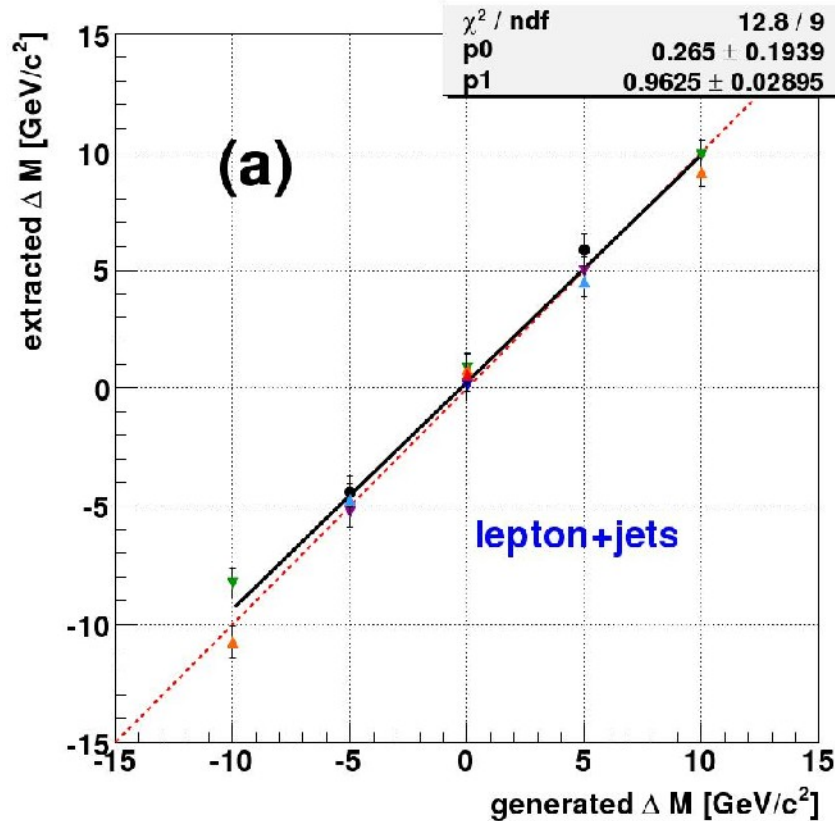
# Performance on Simulated Data

Remove bias on measured mass

$\langle \Delta m_t^{\text{measured}} \rangle$  vs  $\Delta m_t^{\text{true}}$

Remove bias on measured error

$$PULL = \frac{\Delta m_t^{\text{measured}} - \Delta m_t^{\text{true}}}{\delta(\Delta m_t)^{\text{measured}}}$$



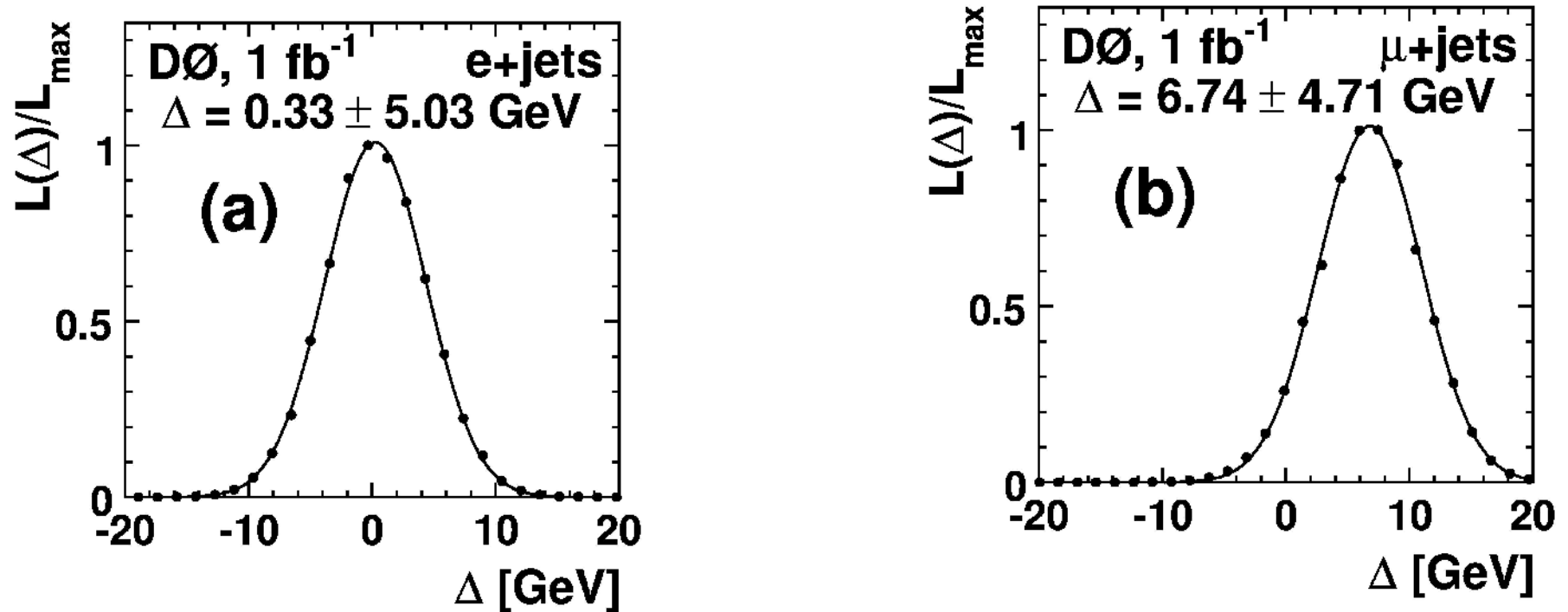


# Systematics

Source	Uncertainty
Statistical	$\pm 3.44$
<i>Physics modeling:</i>	
Signal modeling	$\pm 0.85$
Background modeling	$\pm 0.034$
<i>b</i> -fragmentation	$\pm 0.12$
PDF uncertainty	$\pm 0.26$
Heavy flavor scale factor	$\pm 0.067$
<i>Detector modeling:</i>	
Jet energy scale	$\pm 0.076$
Residual jet energy scale	$\pm 0.071$
<i>b</i> /light response ratio	$\pm 0.037$
Jet ID efficiency	$\pm 0.16$
Jet resolution	$\pm 0.39$
Trigger	$\pm 0.09$
Wrong sign leptons	$\pm 0.075$
<i>Method:</i>	
Signal fraction	$\pm 0.10$
QCD contamination	$\pm 0.40$
MC calibration	$\pm 0.25$
<i>b</i> -tagging efficiency	$\pm 0.25$
$\mu$ resolution	$\pm 0.09$
luminosity reweighting	$\pm 0.016$
Total systematic uncertainty	$\pm 1.15$
Total uncertainty	$\pm 3.63$

← Statistics Limited

# Measurement in Data

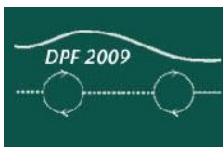


$$e + jets \quad \Delta m_t = 0.33 \pm 5.03(stat) \text{ GeV}$$

$$\mu + jets \quad \Delta m_t = 6.74 \pm 4.71(stat) \text{ GeV}$$

$$\boxed{\text{combined} \quad \Delta m_t = 3.75 \pm 3.44(stat) \pm 1.15(syst) \text{ GeV}}$$

First measurement of mass difference between quark and its antiquark partner



# Matrix Element Method I+jets

$$\mathcal{L}(m_{top}, JES, f_{top}) = \prod_{i=1}^{N_{evt}} [f_{top} P_{sig}(x_i; m_{top}, JES) + (1 - f_{top}) P_{bkg}(x_i)]$$

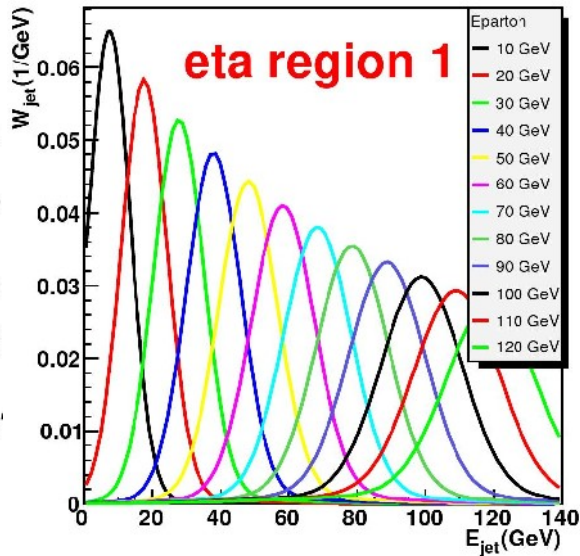
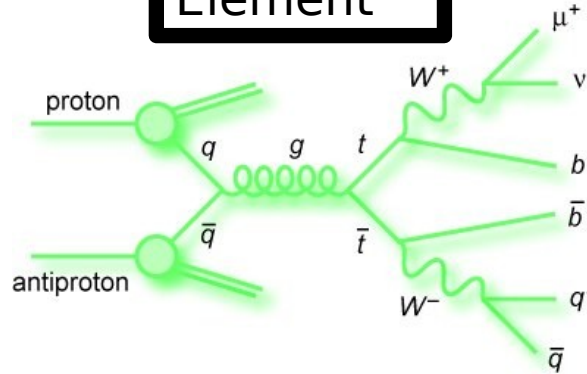
$$P_{sig}(x; m_t, JES) = Acc(x) \times \frac{1}{\sigma} \int d^n \sigma(y; m_t) dq_1 dq_2 f(q_1) f(q_2) W(x, y; JES)$$

Acceptance:  
selection  
efficiency

Integrate over  
parton  
momenta

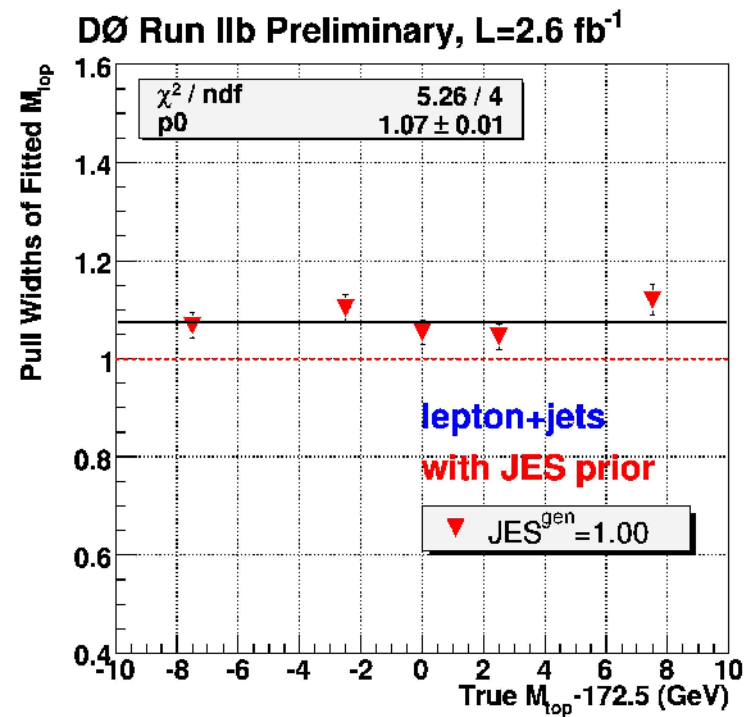
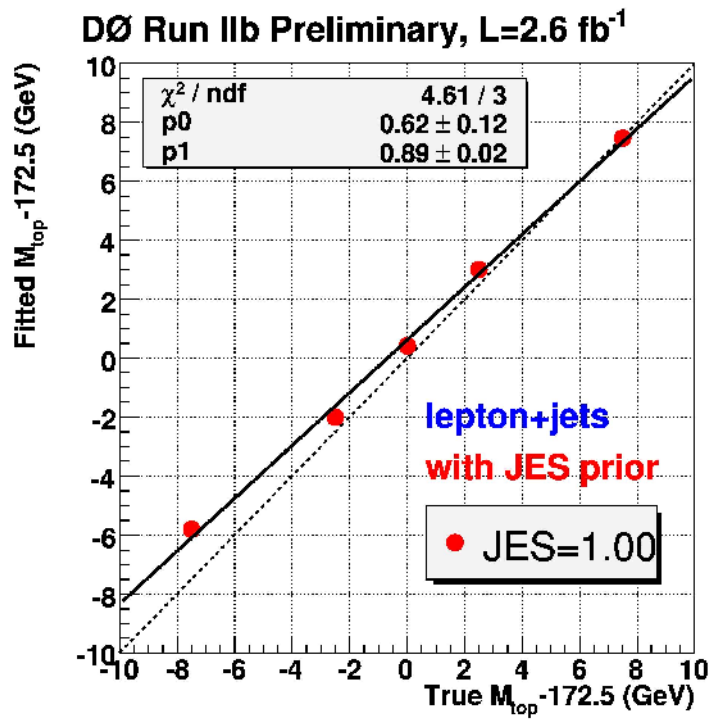
LO Matrix  
Element

Transfer Function



# Performance on Simulated Data Top Mass

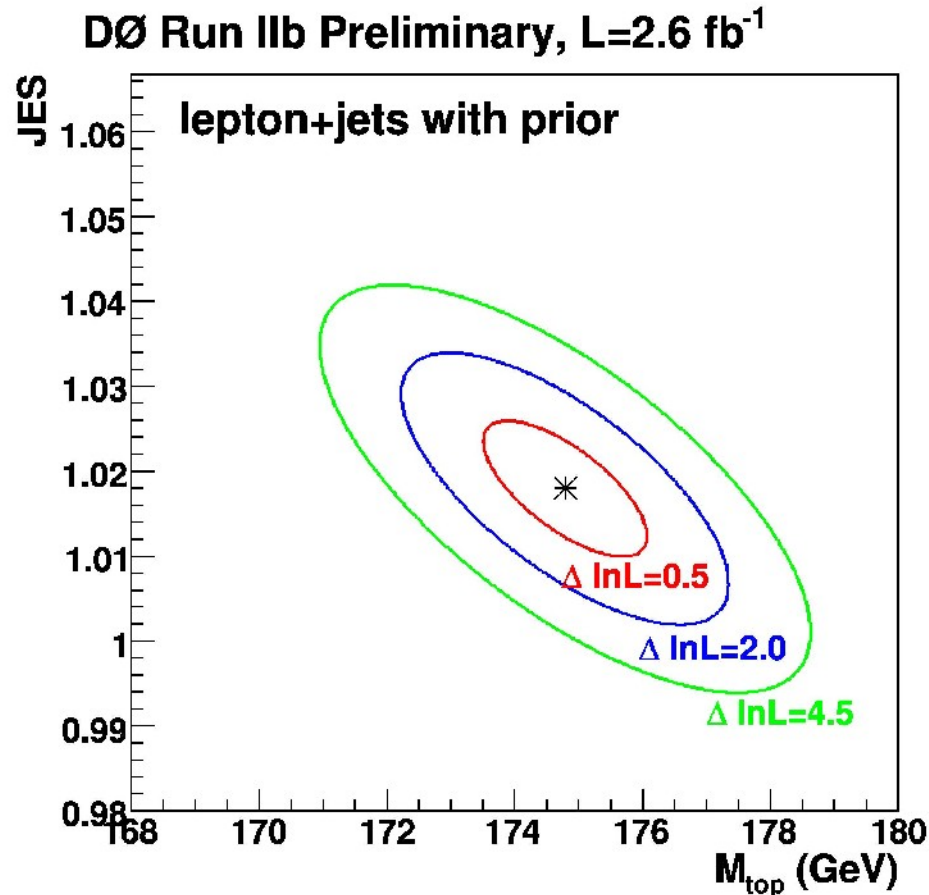
Need to remove bias on measured mass and statistical error



# Systematics

Source	Uncertainty on top mass in Run IIb (GeV)	Uncertainty on top mass in Run IIa (GeV)
Higher Order Effects	$\pm 0.25$	$\pm 0.25$
ISR/FSR	$\pm 0.26$	$\pm 0.40$
Hadronization and UE	$\pm 0.58$	$\pm 0.58$
Color Reconnection	$\pm 0.40$	$\pm 0.40$
Multiple Hadron Interactions	$\pm 0.07$	$\pm 0.01$
Background Modeling	$\pm 0.03$	$\pm 0.04$
W IIF factor	$\pm 0.07$	$\pm 0.09$
<b>b</b> -Modeling	$\pm 0.09$	$\pm 0.03$
PDF Uncertainty	$\pm 0.24$	$\pm 0.14$
Residual JES Uncertainty	$\pm 0.21$	$\pm 0.10$
Relative <i>b</i> /Light Response	$\pm 0.81$	$\pm 0.83$
Sample-Dependent JES	$\pm 0.56$	$\pm 0.56$
<b>b</b> -Tagging Efficiency	$\pm 0.08$	$\pm 0.15$
Trigger Efficiency	$\pm 0.01$	$\pm 0.19$
Lepton Momentum Scale	$\pm 0.17$	$\pm 0.17$
Jet Identification Efficiency	$\pm 0.26$	$\pm 0.26$
Jet Energy Resolution	$\pm 0.32$	$\pm 0.03$
QCD Background	$\pm 0.14$	$\pm 0.14$
Signal Fraction	$\pm 0.10$	$\pm 0.09$
Muon Resolution	-	$\pm 0.10$
Signal Contamination	-	$\pm 0.13$
MC Calibration	$\pm 0.20$	$\pm 0.26$
Total	$\pm 1.41$	$\pm 1.43$

# Measurement in Data



PRL 101, 182001  
(2008)

RunIIa 1.0 fb<sup>-1</sup>

RunIIb 2.6 fb<sup>-1</sup>

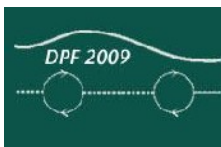
Combined

$$m_t = 171.5 \pm 1.4(\text{stat}) \pm 1.8(\text{syst}) \text{ GeV}$$

$$m_t = 174.8 \pm 1.0(\text{stat}) \pm 1.6(\text{syst}) \text{ GeV}$$

$$m_t = 173.8 \pm 0.8(\text{stat}) \pm 1.6(\text{syst}) \text{ GeV}$$

Systematically Limited





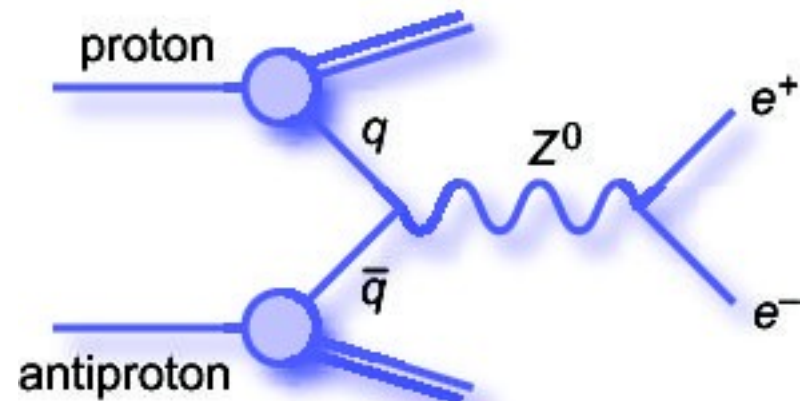
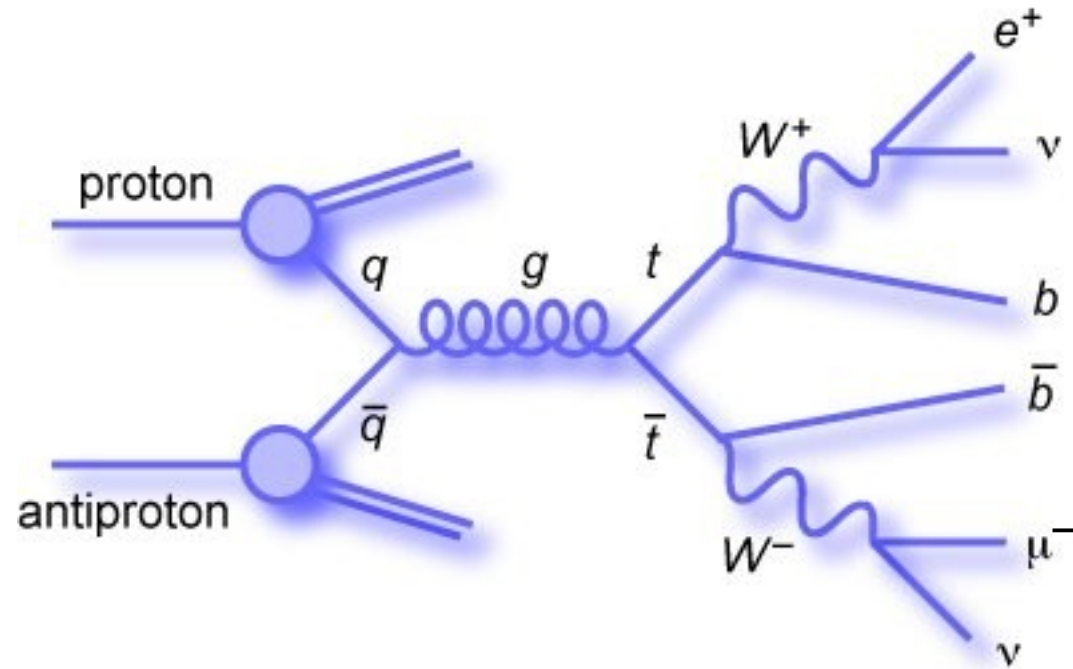
# Event Selection : II channel

- Dilepton Channel:

- 2 leptons
  - $ee, e\mu, \mu\mu, e\text{trk}, \mu\text{trk}$
- large MissingET
- 2 b-jets

- Backgrounds:

- $Z \rightarrow ee/\mu\mu/\tau\tau + \text{jets}$
- $WW \rightarrow ee/e\mu/\mu\mu + \text{jets}$
- Fake leptons ( $W + \text{jets}$ , QCD)



# Matrix Element Method ( $e_\mu$ )

$$\mathcal{L}(m_t, f_t) = \prod_{i=1}^{N_{evt}} [f_t P_{sig}(x_i; m_t) + (1 - f_t) P_{bkg}(x_i)]$$

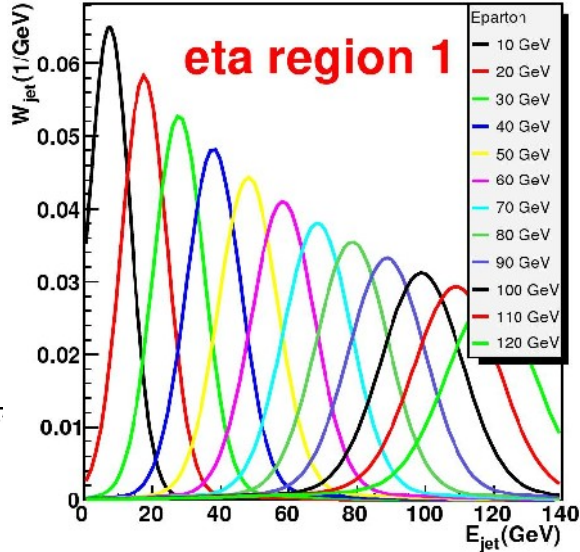
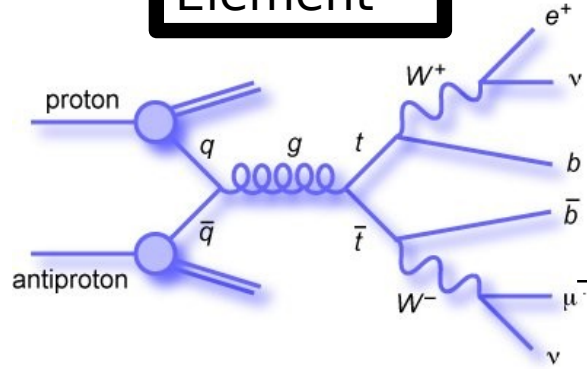
$$P_{sig}(x; m_t) = Acc(x) \times \frac{1}{\sigma} \int d^n \sigma(y; m_t) dq_1 dq_2 f(q_1) f(q_2) W(x, y)$$

Acceptance:  
selection  
efficiency

Integrate over  
parton  
momenta

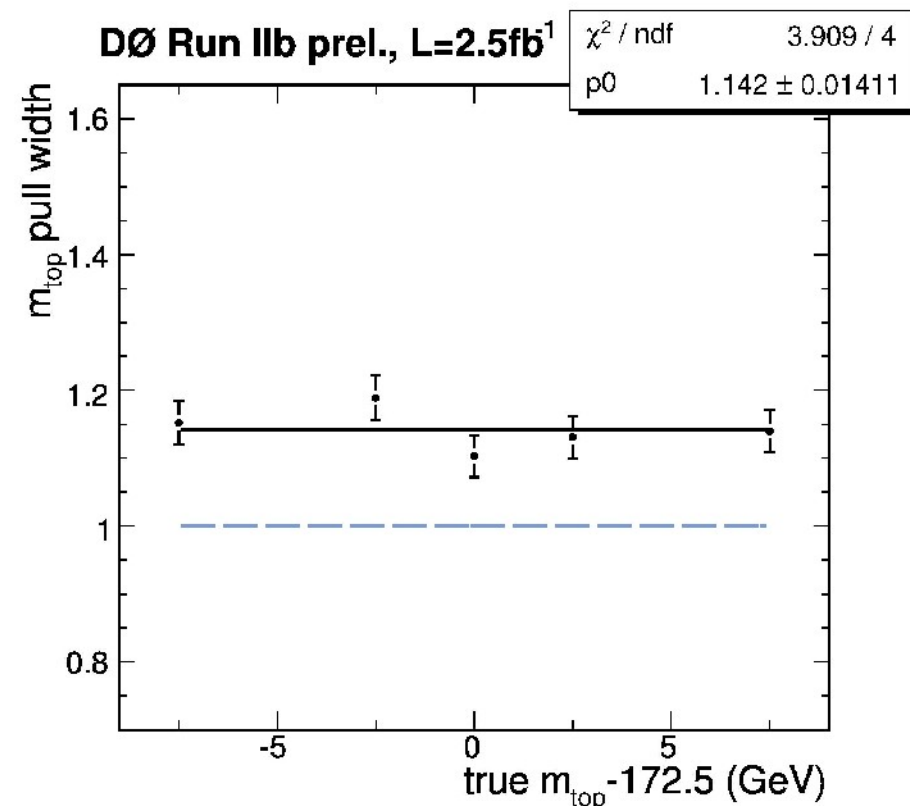
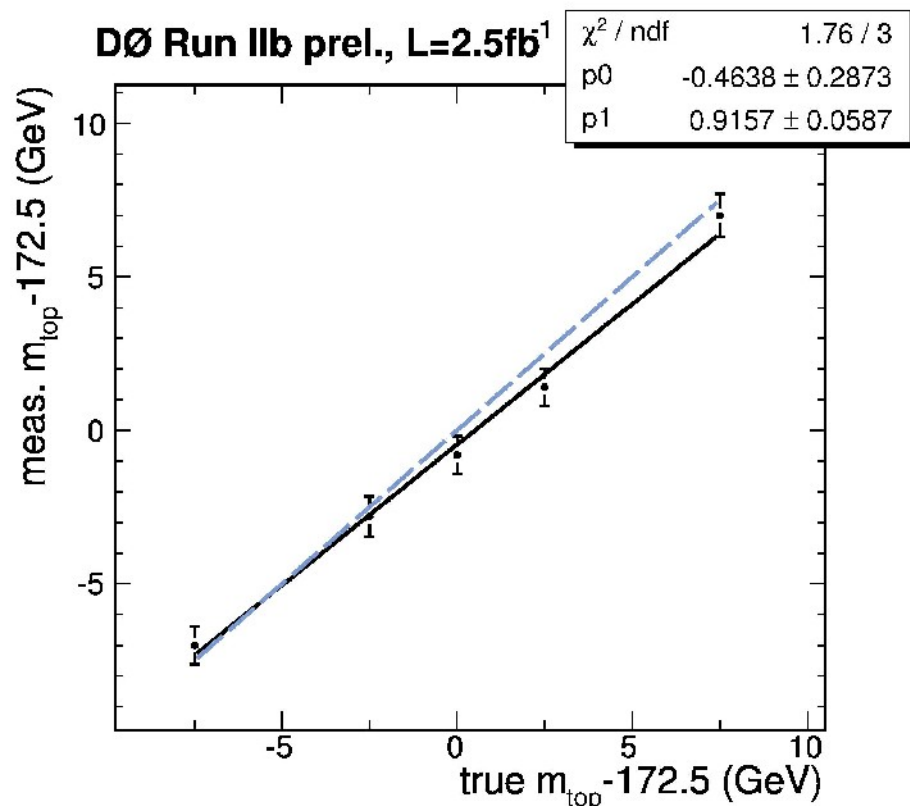
LO Matrix  
Element

Transfer Function



# Performance on Simulated Data

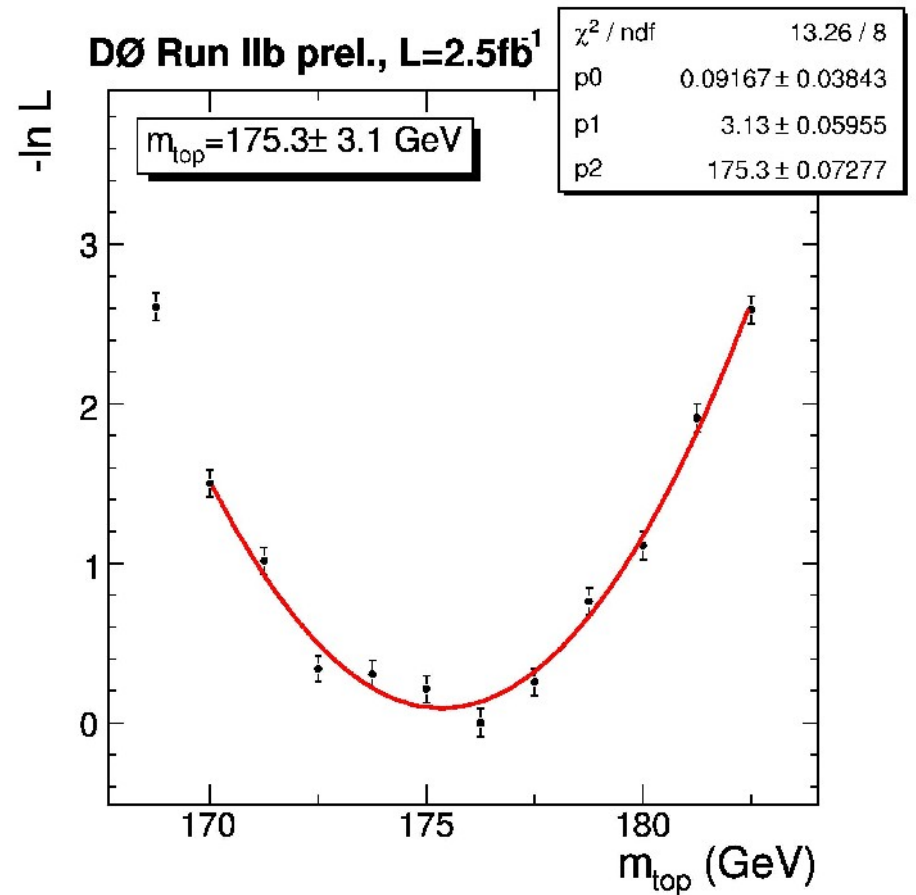
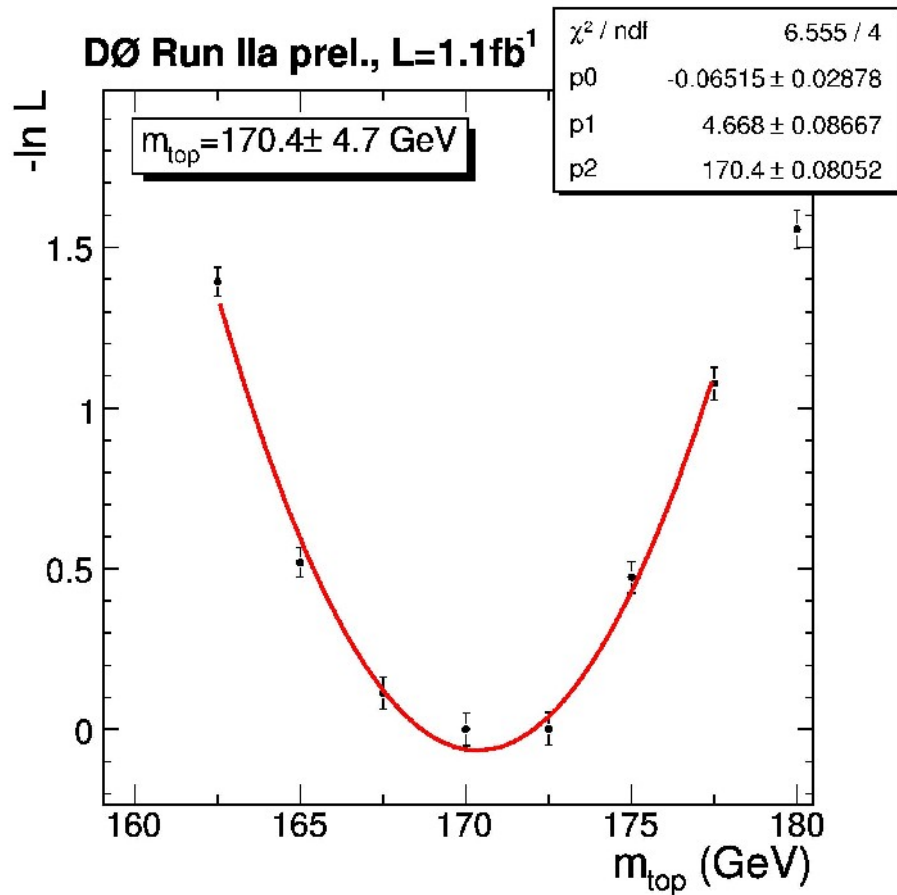
- Need to remove bias on measured mass and statistical error
- Includes events with 2 or more jets



# Systematics ( $e\mu$ )

Uncertainty	$e\mu$ Run IIa [GeV]	$e\mu$ Run IIb [GeV]
JES	+1.2 -1.3	+1.5 -1.6
b/light quark response	$\pm 1.4$	$\pm 1.6$
jet resolution	+0.6 -0.6	+0.2 -0.3
sample-dependent JES	$\pm 0.2$	$\pm 0.1$
muon smearing	+0.3 -0.0	$\pm 0.3$
b quark modeling	$\pm 0.1$	$\pm 0.3$
PDF uncertainty	+0.3 -0.0	+0.1 -0.2
MC calibration	$\pm 0.4$	$\pm 0.4$
signal fraction	+0.2 -0.0	$\pm 0.3$
QCD background modeling	$\pm 0.6$	$\pm 0.6$
electron energy scale	$\pm 0.1$	$\pm 0.1$
muon momentum scale	$\pm 0.2$	$\pm 0.2$
hadronization and UE	$\pm 1.0$	$\pm 1.0$
ISR/FSR	$\pm 0.6$	$\pm 0.6$
Color reconnection	$\pm 0.4$	$\pm 0.4$
TOTAL	$\pm 2.4$	$\pm 2.6$

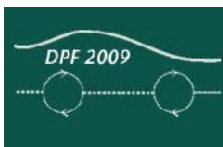
# Result on Data ( $e\mu$ )



RunIIa  $m_t = 171.7 \pm 6.4(\text{stat}) \text{ GeV}$

RunIIb  $m_t = 176.1 \pm 3.9(\text{stat}) \text{ GeV}$

Combined  $m_t = 174.8 \pm 3.3(\text{stat}) \pm 2.6(\text{syst}) \text{ GeV}$



# Dilepton Mass with Templates

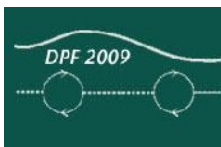
- Kinematic Reconstruction (2 neutrinos)
- Two Methods:
  - Neutrino Weighting
    - Sample neutrino eta's from expected distributions
    - Compare reconstructed MET to real MET:

$$w = \exp \left[ \frac{-(\cancel{E}_x^{\text{calc}} - \cancel{E}_x^{\text{obs}})^2}{2(\sigma_x^u)^2} \right] \exp \left[ \frac{-(\cancel{E}_y^{\text{calc}} - \cancel{E}_y^{\text{obs}})^2}{2(\sigma_y^u)^2} \right]$$

- Matrix Weighting

- Use Measured Missing  $E_T$
- Construct weight:  $w = f(x)f(\bar{x})p(E_\ell^*|m_t)p(E_{\bar{\ell}}^*|m_t)$

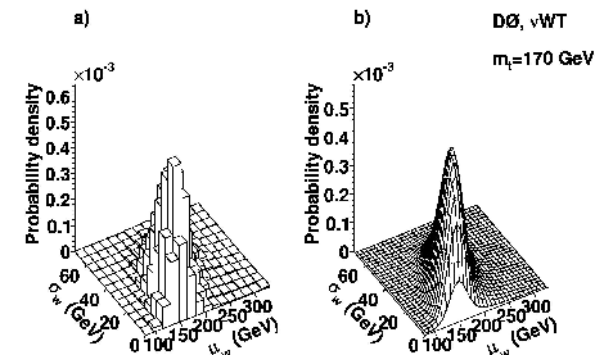
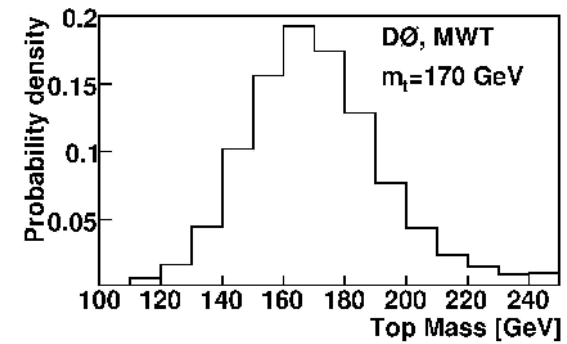
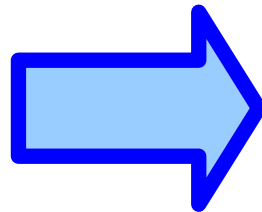
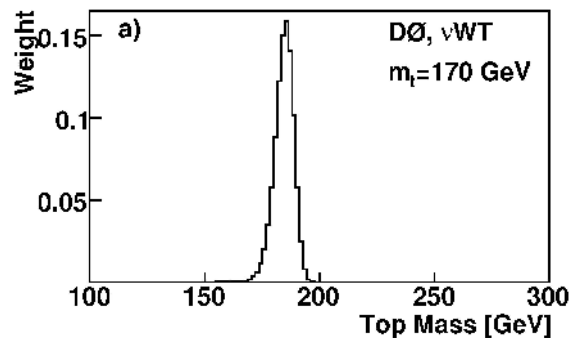
$$p(E_\ell^*|m_t) = \frac{4m_t E_\ell^* (m_t^2 - m_b^2 - 2m_t E_\ell^*)}{(m_t^2 - m_b^2)^2 + M_W^2 (m_t^2 - m_b^2) - 2M_W^4}$$





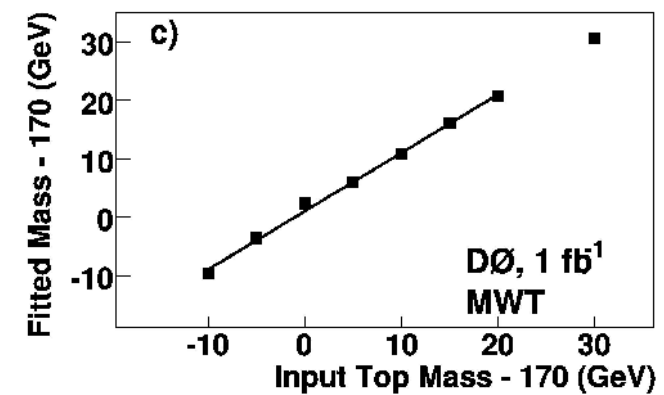
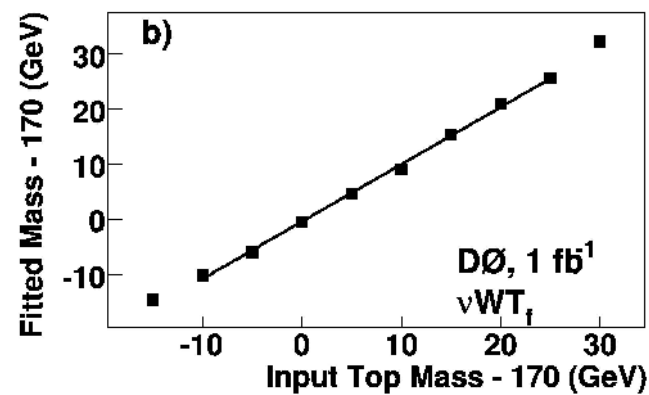
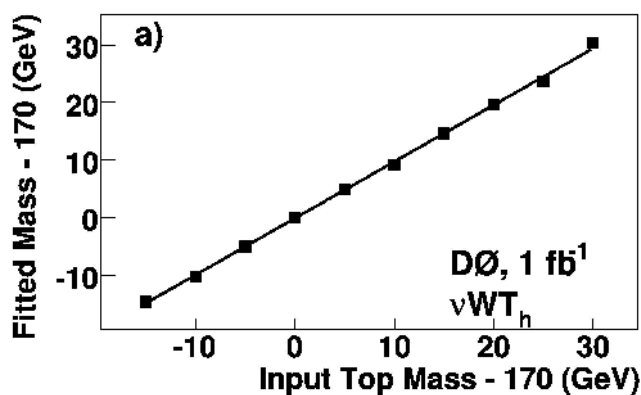
# Dilepton Mass with Templates

- Use weight distribution, Form Templates
  - MWT uses  $m_t$  with maximum weight
  - NuWT uses 2D templates
    - mean and RMS of weight distribution



# Performance on Simulated Data

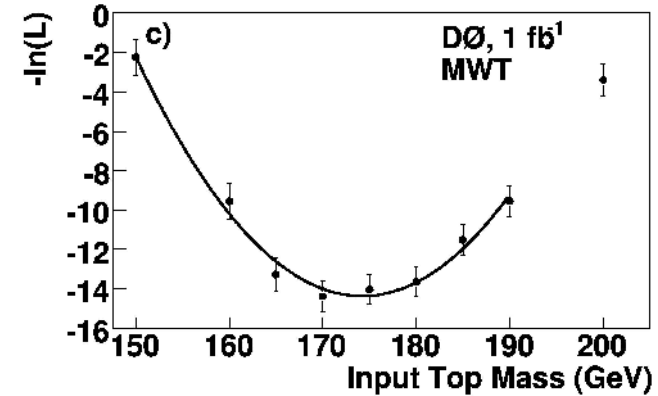
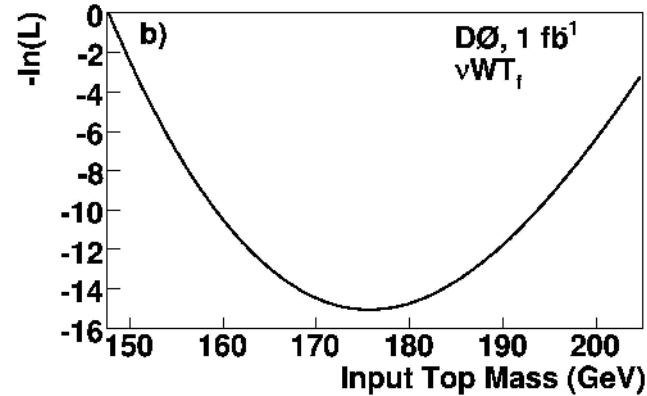
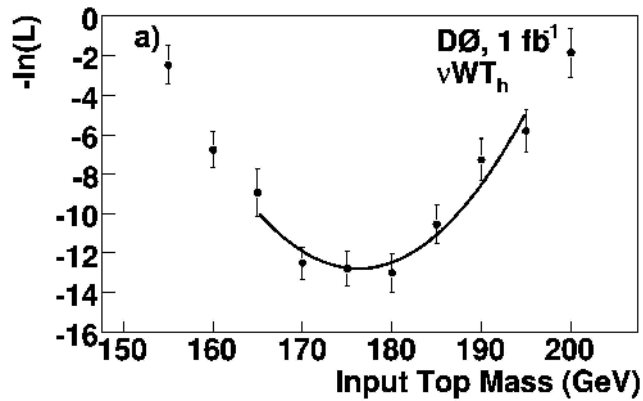
Method	Channel	Slope: $\alpha$	Offset: $\beta$ [GeV]	Pull width	Expected statistical uncertainty [GeV]
$\nu$ WT <sub>h</sub>	2 $\ell$	$0.98 \pm 0.01$	$-0.04 \pm 0.11$	$1.02 \pm 0.02$	5.8
$\nu$ WT <sub>h</sub>	$\ell$ +track	$0.92 \pm 0.02$	$2.28 \pm 0.27$	$1.04 \pm 0.02$	13.0
$\nu$ WT <sub>h</sub>	combined	$0.99 \pm 0.01$	$-0.04 \pm 0.11$	$1.03 \pm 0.02$	5.1
$\nu$ WT <sub>f</sub>	2 $\ell$	$1.03 \pm 0.01$	$-0.32 \pm 0.15$	$1.06 \pm 0.02$	5.8
$\nu$ WT <sub>f</sub>	$\ell$ +track	$1.07 \pm 0.03$	$-0.04 \pm 0.37$	$1.07 \pm 0.02$	12.9
$\nu$ WT <sub>f</sub>	combined	$1.04 \pm 0.01$	$-0.45 \pm 0.13$	$1.06 \pm 0.02$	5.3
MWT	2 $\ell$	$1.00 \pm 0.01$	$0.95 \pm 0.05$	$0.98 \pm 0.01$	6.3
MWT	$\ell$ +track	$0.99 \pm 0.01$	$0.64 \pm 0.12$	$1.06 \pm 0.01$	13.8
MWT	combined	$0.99 \pm 0.01$	$0.97 \pm 0.05$	$0.99 \pm 0.01$	5.8



# Systematics

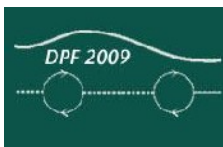
Source of uncertainty	$\nu W T_h$ [GeV]	$\nu W T_f$ [GeV]	MWT [GeV]
<i>b</i> fragmentation	0.4	0.5	0.4
Underlying event modeling	0.3	0.1	0.5
Extra jets modeling	0.1	0.1	0.3
Event generator	0.6	0.8	0.5
PDF variation	0.2	0.3	0.5
Background template shape	0.4	0.3	0.3
Jet energy scale (JES)	1.5	1.6	1.2
<i>b</i> /light response ratio	0.3	0.4	0.6
Sample dependent JES	0.4	0.4	0.1
Jet energy resolution	0.1	0.1	0.2
Muon/track $p_T$ resolution	0.1	0.1	0.2
Electron energy resolution	0.1	0.2	0.2
Jet identification	0.4	0.5	0.5
MC corrections	0.2	0.3	0.2
Background yield	0.0	0.1	0.1
Template statistics	0.8	1.0	0.8
MC calibration	0.1	0.1	0.1
Total systematic uncertainty	2.1	2.3	2.0

# Result in Data



$\nu$ WT	$m_t = 176.2 \pm 4.8(stat) \pm 2.1(syst) \text{ GeV}$
MWT	$m_t = 173.2 \pm 4.9(stat) \pm 2.0(syst) \text{ GeV}$
Combined	$m_t = 174.7 \pm 4.4(stat) \pm 2.0(syst) \text{ GeV}$

arXiv:0904.3195 Submitted to PRD

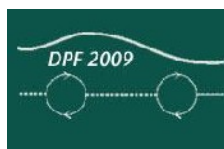
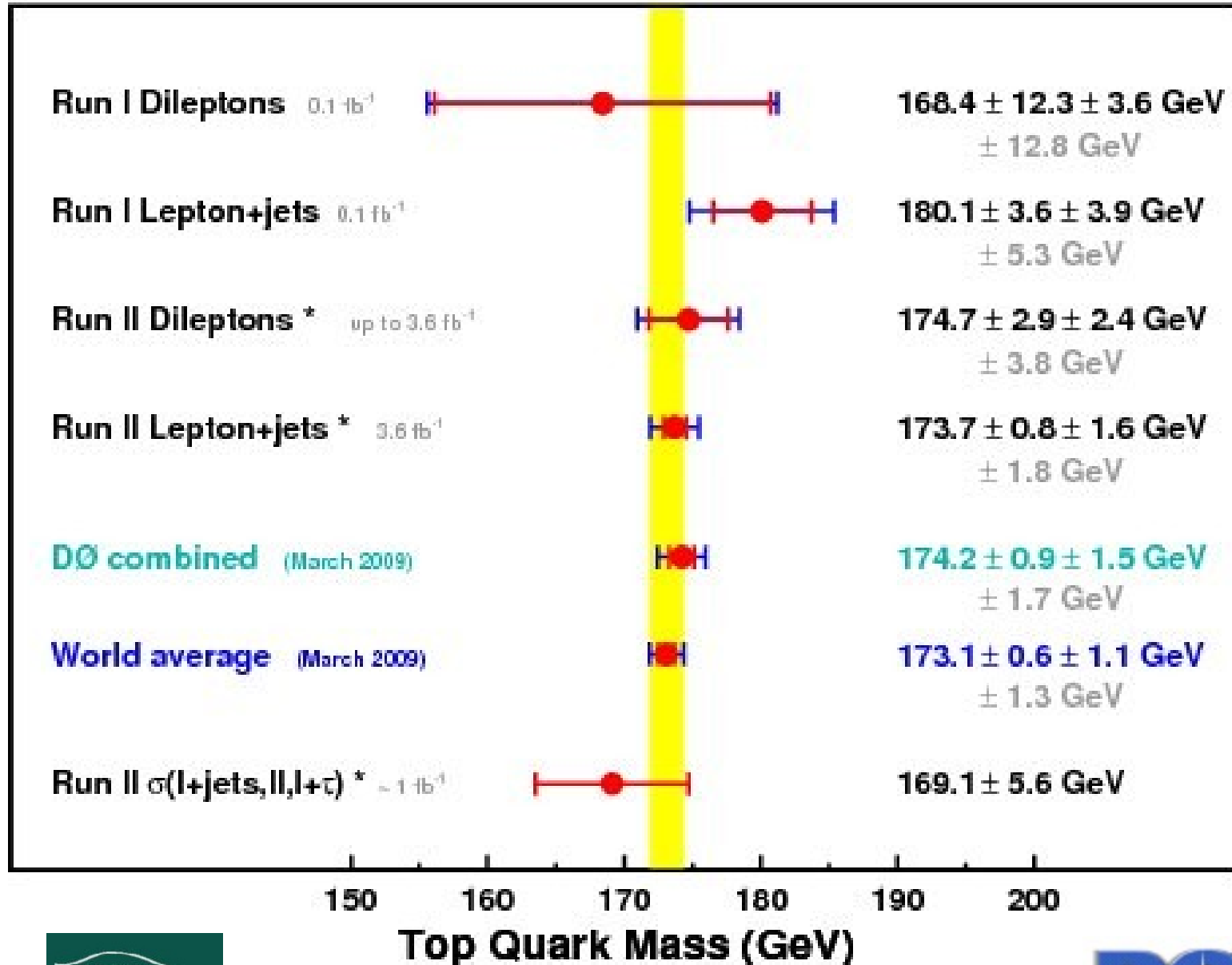


# Combination D0 Mass Results

**DØ**

\*=preliminary

Winter 2009



# Conclusion

- Lepton+jets:
  - First Measurement of Top Anti-top Mass Difference
    - First time quark and anti-quark mass compared
  - High precision measurement of  $l+jets$ 
    - measurement systematically limited
- Dilepton Channels
  - Matrix Element, Template based
    - measurement statistically limited
    - important consistency check

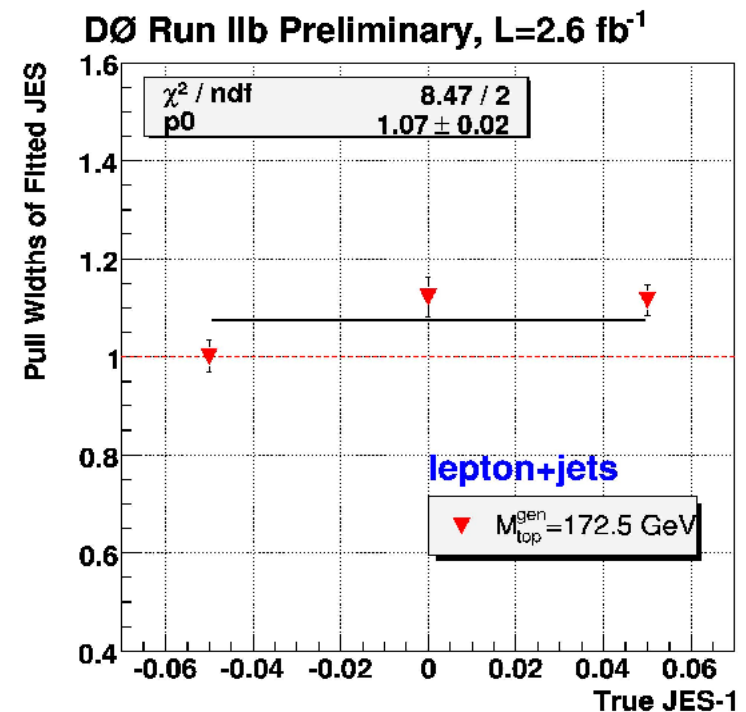
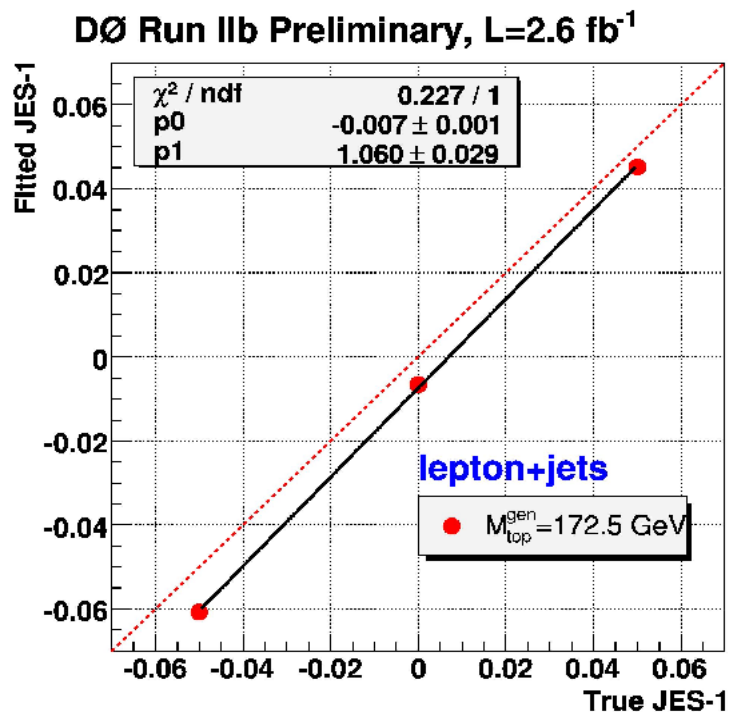


# Backup



# Performance on Simulated Data Jet Energy Scale

$M_W$  Constraint  $\rightarrow$  In-situ Jet Energy Calibration



# Top Mass Difference

Transform to convenient variables:

$$(m_t, m_{\bar{t}}) \rightarrow (\Delta m_t = (m_t - m_{\bar{t}}), m_{sum} = (m_t + m_{\bar{t}})/2)$$

Integrate out  $M_{sum}$ :

$$\mathcal{L}(\Delta m_t) = \int dm_{sum} \mathcal{L}(\Delta m_t, m_{sum})$$

