

S.Pratt and J.V., arXiv:0809.0089  
J.V. and S.Pratt, arXiv:0810.4325  
S.Pratt, arXiv:0811.3363

# Universality in Early Stage Flow

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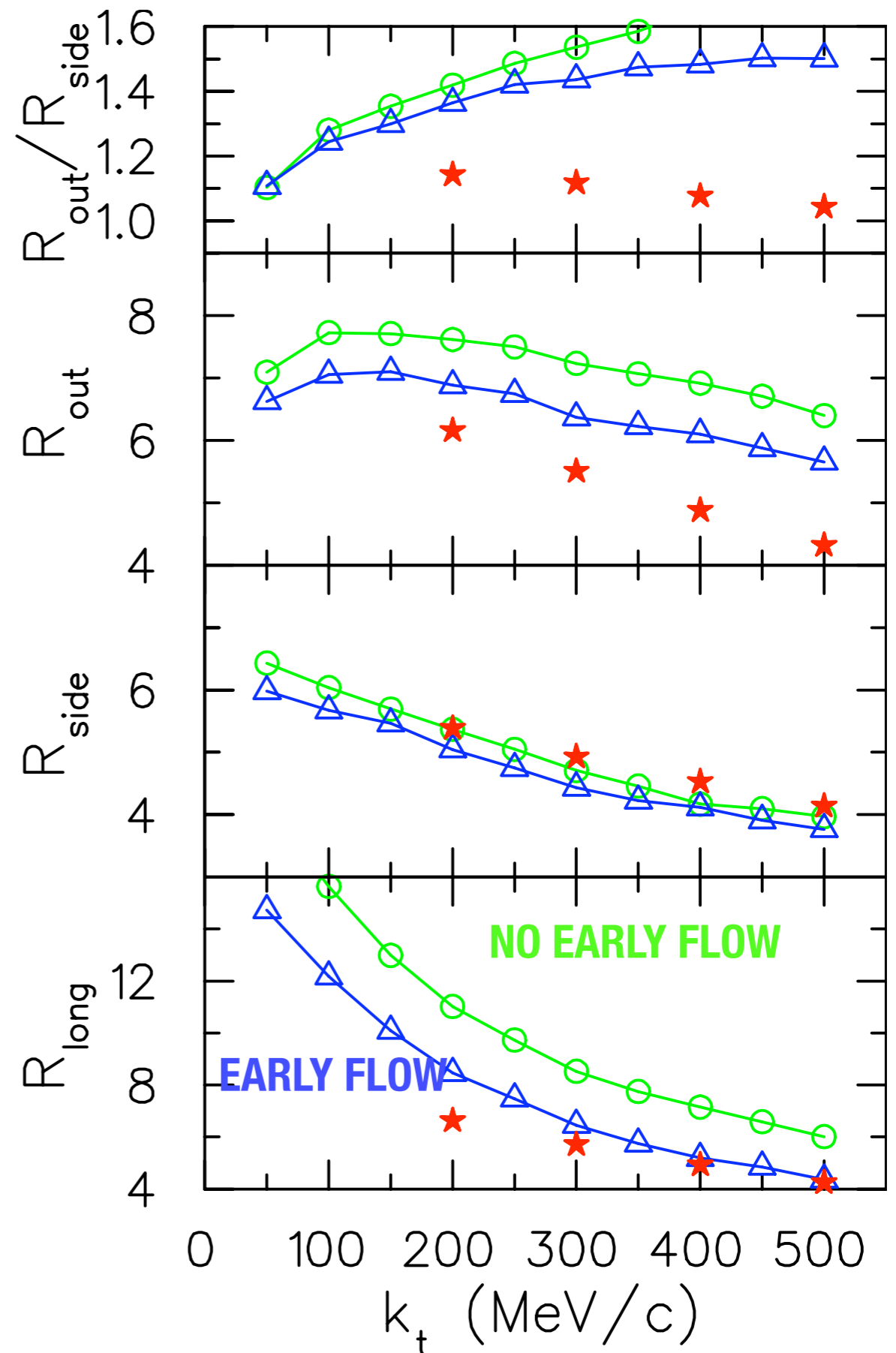
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# Early Acceleration

- ✦ HBT Radii and Early Acceleration
- ✦ Universality in a Class of Models
  - ✦ Why Microscopic Structure May Not Matter Much

# Early Acceleration

- Helps explain HBT radii
- With Hydro + Cascade
- Especially  $R_{\text{long}}$
- Early Thermalization?



# Early Acceleration

- ✦ Anisotropy Parameter  $k$ :  $T_{xx} = T_{yy} = kT_{00}$ .
  - ✦  $k(x,t) = k(t)$
- ✦ Traceless Stress Energy Tensor
- ✦ Boost Invariance (Bjorken Flow)

# Models in Class

Model	$T_{xx}, T_{yy}$	$T_{zz}$	$\text{Tr } T$
CGC	$\approx \epsilon$	$\approx -\epsilon$	0
Ideal Hydro	$\epsilon/3$	$\epsilon/3$	0
Free-Streaming	$\epsilon/2$	0	0
???	0	0	0

# Without Expansion...

$$T_{xx} = \kappa T_{00}$$

Transverse Pressure  
(1/3, 1/2, 1)

$$\frac{d}{dt} T_{0x} = -\partial_x T_{xx}$$

$$\frac{T_{0x}}{T_{00}} \approx -\kappa \frac{\partial_x T_{00}}{T_{00}} t$$

*Directly Depends on  $\kappa$*

# With Bjorken Expansion

$$T_{00} \sim \frac{1}{\tau^{2-2\kappa}}$$

Transverse Pressure  
(1/3, 1/2, 1)

$$\frac{d}{dt} T_{0x} = -\partial_x T_{xx} - \partial_z T_{xz} = -\partial_x T_{xx} - \frac{1}{\tau} T_{0x}$$

$$\frac{d}{dt} T_{00} = -T_{00} \frac{(2-2\kappa)}{\tau}$$

$$\frac{T_{0x}}{T_{00}} \approx -\frac{1}{2} \frac{\partial_x T_{00}}{T_{00}} t$$

*No k Dependence!*

# Early Acceleration

$$\mathbf{FLOW} \equiv \frac{T_{0x}}{T_{00}} = -\frac{1}{2} \frac{\partial_x T_{00}}{T_{00}} t$$

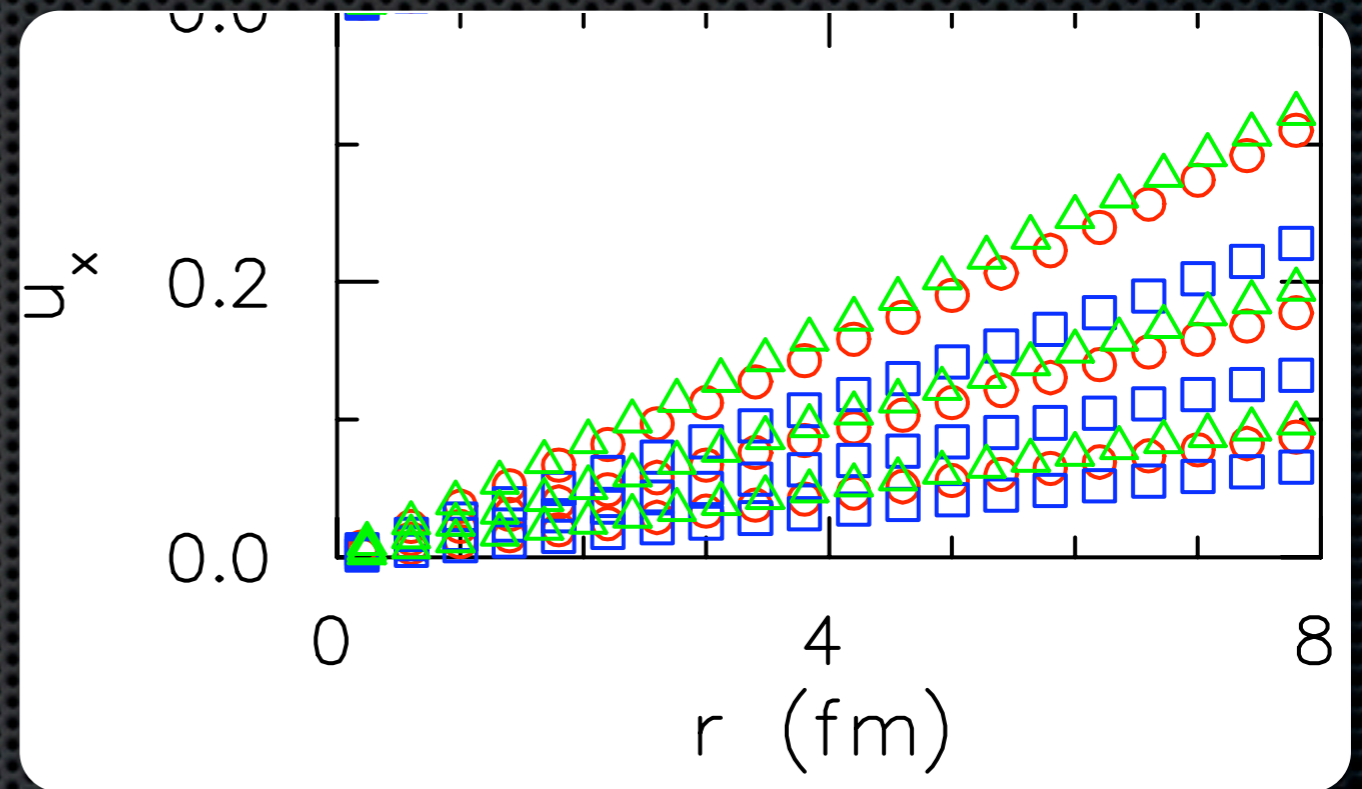
- ✦ Anisotropy Parameter  $k$ :  $kT_{00} = T_{xx} = T_{yy}$ 
  - ✦  $k(x,t) = k(t)$
- ✦ Traceless Stress Energy Tensor
- ✦ Boost Invariance (Bjorken Flow)

Initial flow for hydro depends only on initial profile,  
microscopic structure irrelevant.



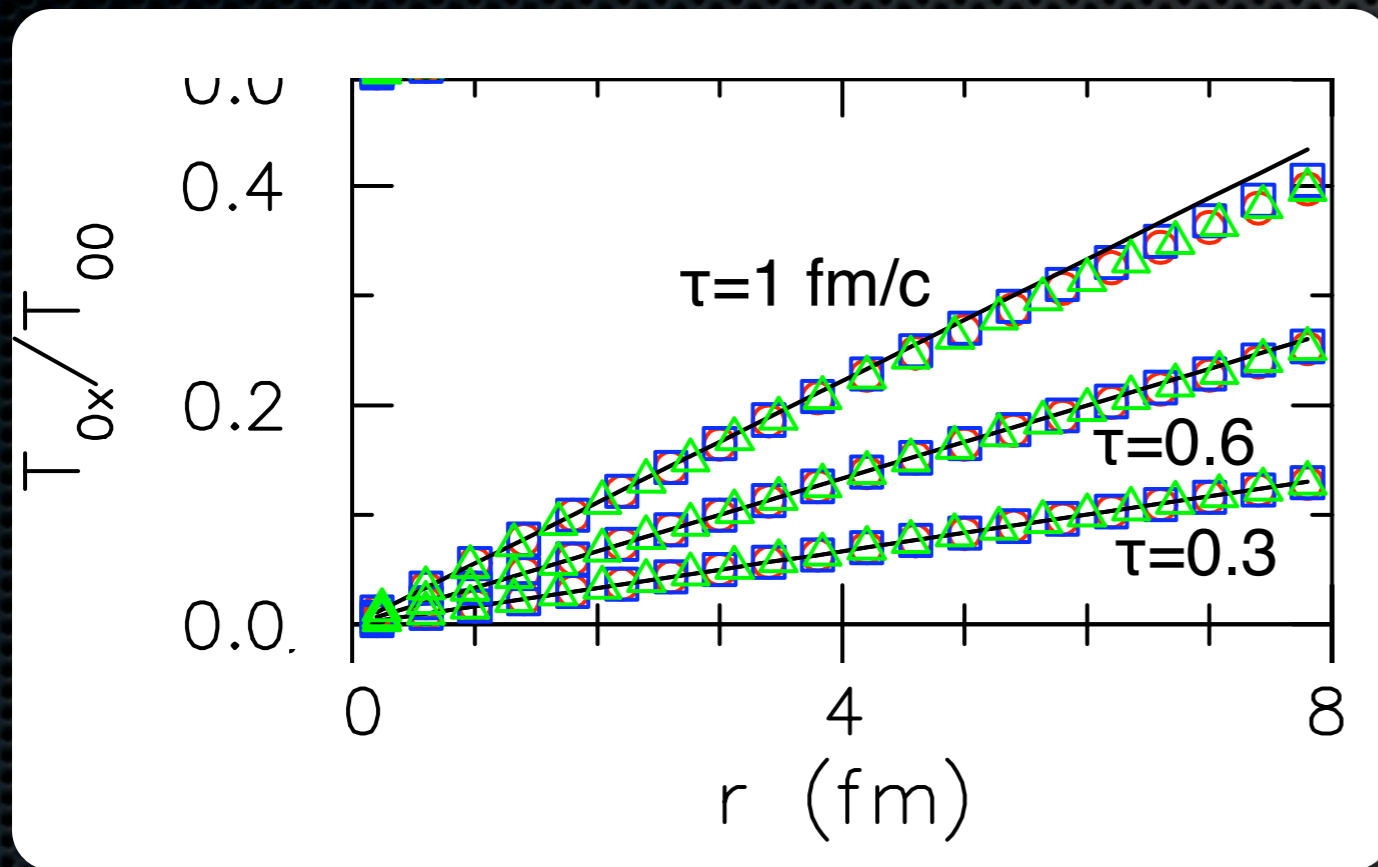
# Transverse Velocity

- ✦ Between models, transverse velocities differ.
- ✦ Is this still universal flow?



▲ IDEAL HYDRO  
■ COHERENT FIELDS  
● INCOHERENT FIELDS

# Transverse Velocity



- ✦ ‘Flow’ develops consistently.
- ✦ This ratio is conserved in a ‘sudden’ transition.

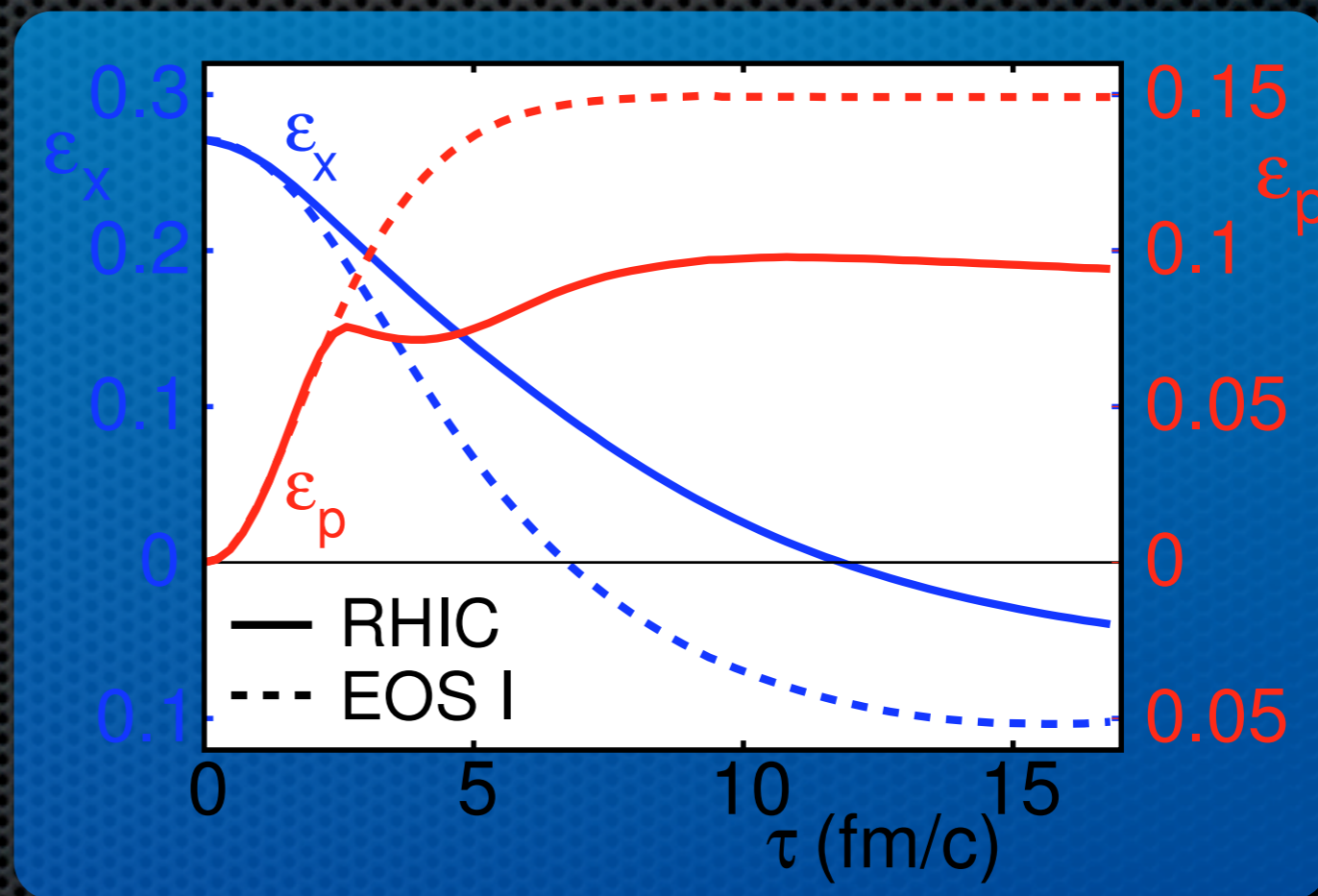
▲ IDEAL HYDRO  
■ COHERENT FIELDS  
● INCOHERENT FIELDS

# Developing Flow

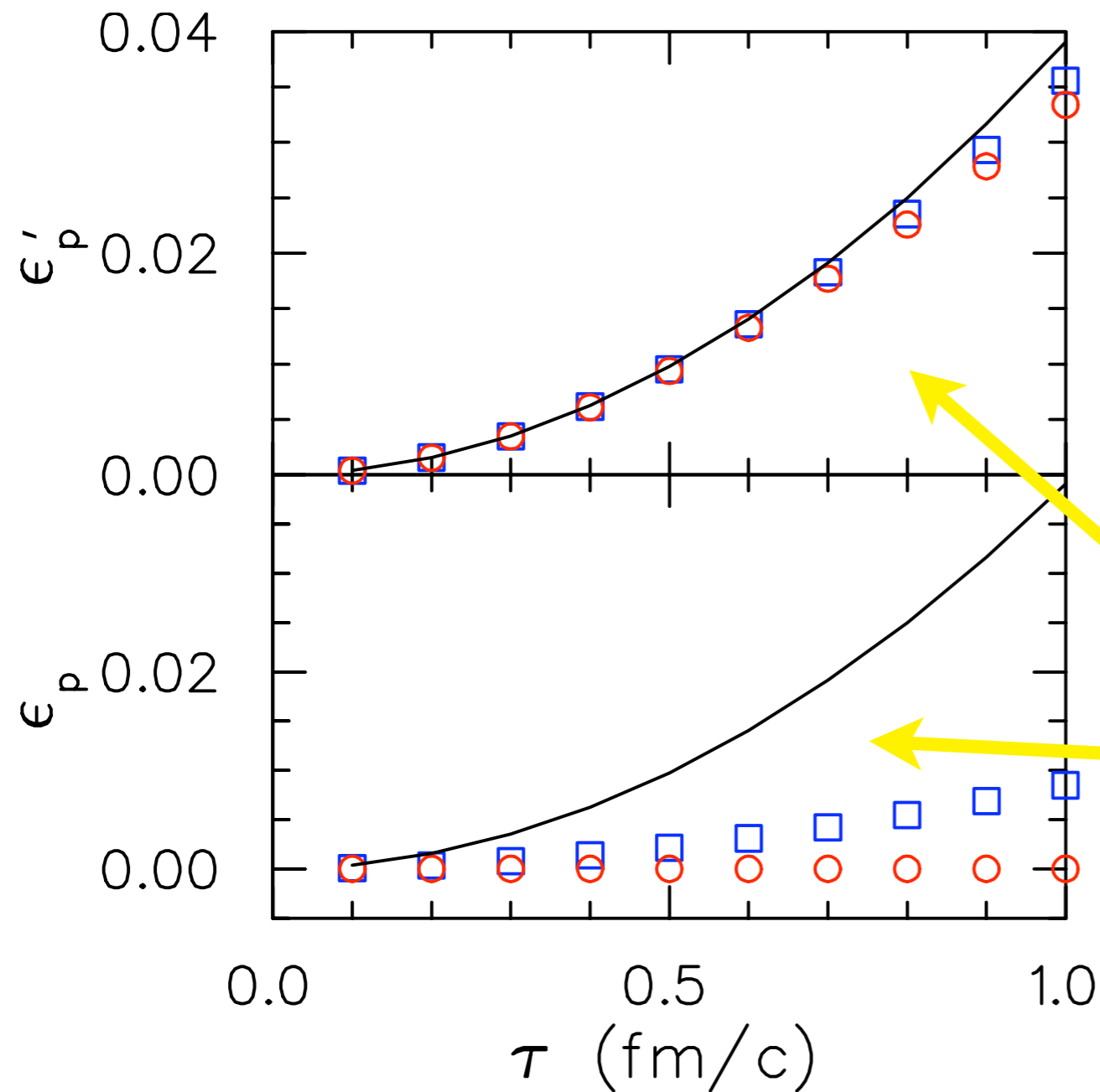
During thermalization,

$$\epsilon_p \equiv \frac{\int dx dy (T_{xx} - T_{yy})}{\int dx dy (T_{xx} + T_{yy})}$$

could change suddenly.



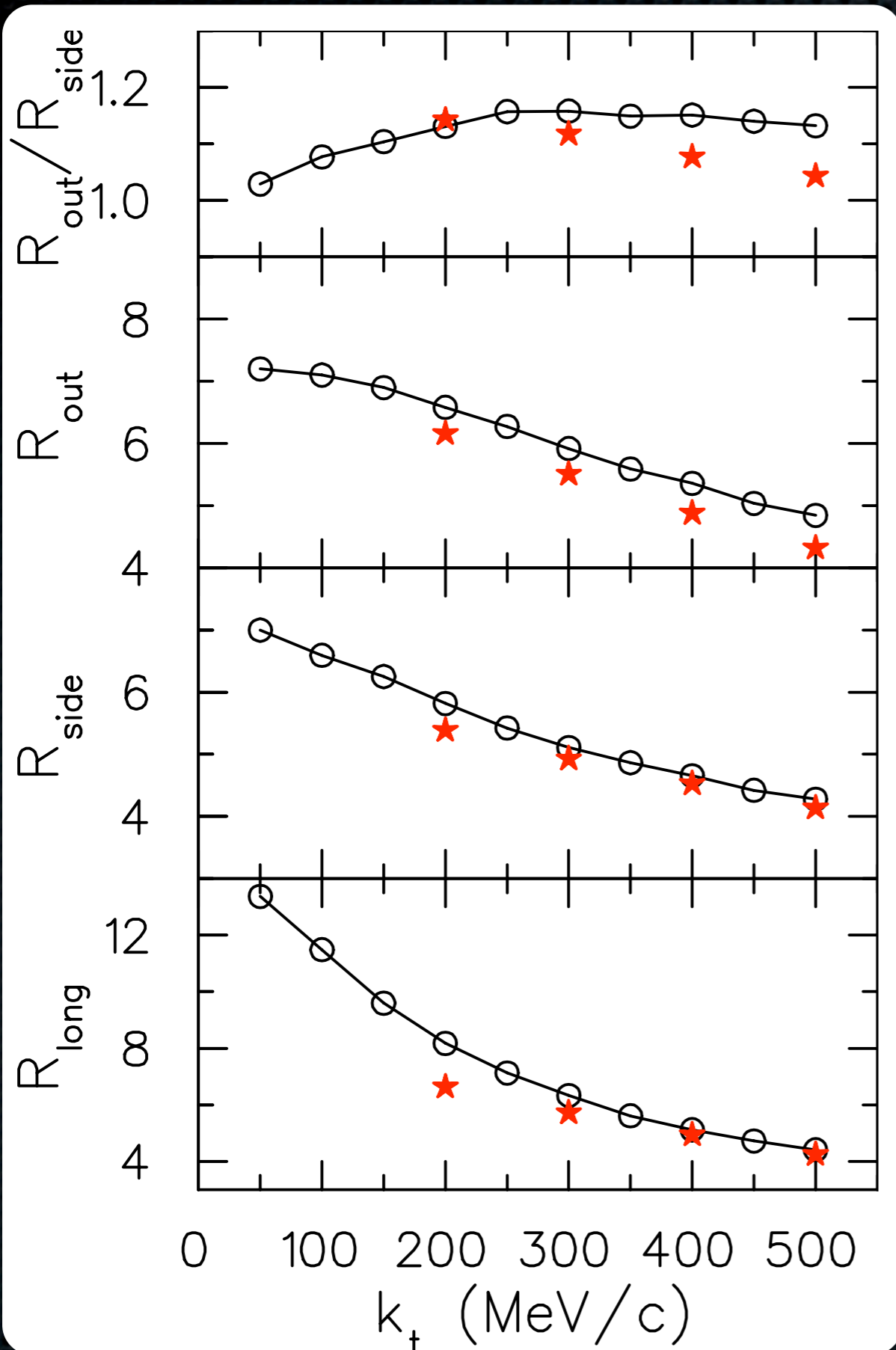
# Developing Flow



✦ System thermalizes.

after thermalization  
before thermalization

# Dying HBT?



- ✦ No definitive early model.
- ✦ But *existence* of early acceleration.
- ✦ Source size described at  $\sim 10\%$

# Remarks

- ✦ Flow develops before thermalization.
- ✦ Early Flow leads to significant improvements in HBT description, especially  $R_{\text{long}}$ .