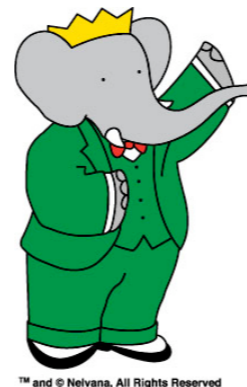


# Search for Lepton Flavor Violation at BABAR



Swagato Banerjee



University  
of Victoria

British Columbia  
Canada

DPF 2009



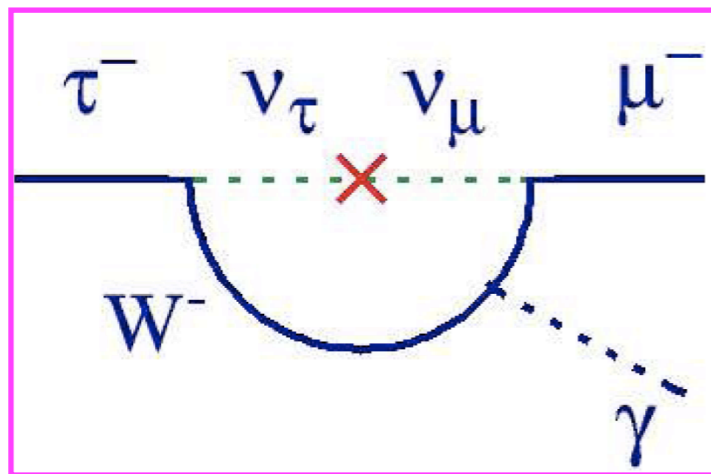
*2009 Meeting of the Division of Particles and  
Fields of the American Physical Society (DPF 2009)*

26-31 JULY 2009

Wayne State University, Detroit, MI

# Introduction

- Lepton flavor violation (LFV)
  - not forbidden by SM gauge symmetry
  - most new models naturally include LFV vertex
- In SM, LF is conserved for zero degenerate  $\nu$  masses
- Now we have clear indication that  $\nu$ 's have finite mass  
 $\Rightarrow$  Lepton Flavor is violated in Nature: but by how much?
- SM extended to include finite  $\nu$  mass and mixing predicts LFV



$$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) \text{ [Lee-Shrock, Phys. Rev. D 16, 1444 (1977)]}$$
$$= \frac{3\alpha}{128\pi} \left( \frac{\Delta m_{23}^2}{M_W^2} \right)^2 \sin^2 2\theta_{\text{mix}} \mathcal{B}(\tau \rightarrow \mu \bar{\nu}_\mu \nu_\tau)$$

With  $\Delta \sim 10^{-3} \text{ eV}^2$ ,  $M_W \sim \mathcal{O}(10^{11}) \text{ eV}$   
 $\approx \mathcal{O}(10^{-54})$  ( $\theta_{\text{mix}} : \text{max}$ )

... many orders below experimental sensitivity!

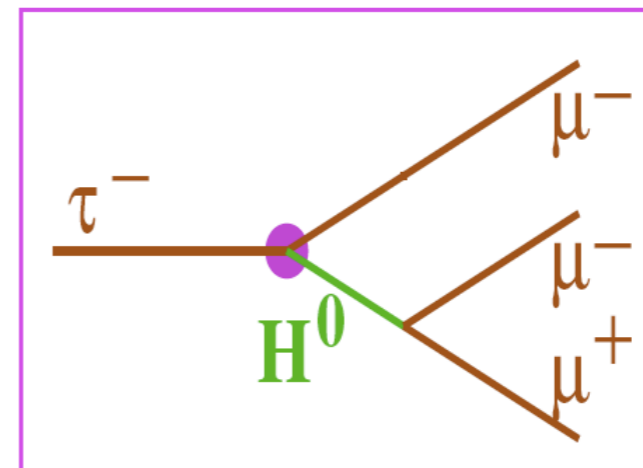
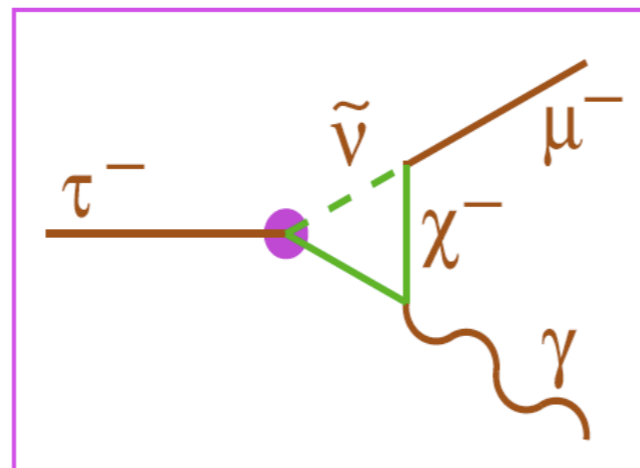
- Observation for LFV  $\Rightarrow$  unambiguous signature of new physics

# Lepton Flavor Violating Tau Decays

- Predicted by many beyond SM processes ...
  - SUSY models: non-diagonal slepton mass matrix  $\Rightarrow$  LFV
  - Normal (Inverted) slepton hierarchy  $\Rightarrow \tau^\pm \rightarrow \mu^\pm \gamma$  ( $\tau^\pm \rightarrow e^\pm \gamma$ )
- Some models: LFV upto existing experimental bounds

	$\mathcal{B}(\tau \rightarrow l\gamma)$	$\mathcal{B}(\tau \rightarrow lll)$
SUSY Higgs (PLB549(2002)159, PLB566(2003)217)	$10^{-10}$	$10^{-7}$
SM+Heavy Majorana $\nu_R$ (PRD66(2002)034008)	$10^{-9}$	$10^{-10}$
Non-Universal $Z'$ (PLB547(2002)252)	$10^{-9}$	$10^{-8}$
SUSY SO(10) (NPB649(2003)189, PRD68(2003)033012)	$10^{-8}$	$10^{-10}$
mSUGRA+seesaw (EPJC14(2000)319, PRD66(2002)115013)	$10^{-7}$	$10^{-9}$

Illustrations:



# Probing TeV scale via Upsilon Decays

## SUSY + Higgs

(A.Brignole, A.Rossi, PLB566(2003)217)

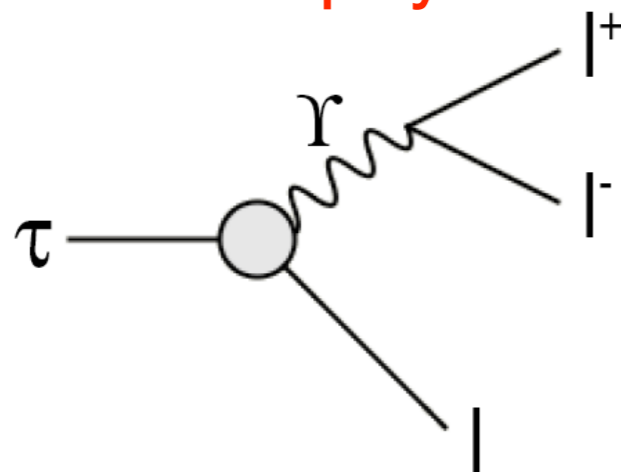
$$\bullet \mathcal{B}(\tau \rightarrow lll) \simeq 10^{-7} \times \left(\frac{\tan \beta}{50}\right)^6 \times \left(\frac{100 \text{ GeV}}{m_A}\right)^4 \times \left(\frac{|50\Delta_L|^2 + |50\Delta_R|^2}{10^{-3}}\right)$$

• If Higgs light, s-particles  $\sim \mathcal{O}(\text{TeV})$ ,  $\tan \beta \sim 50$

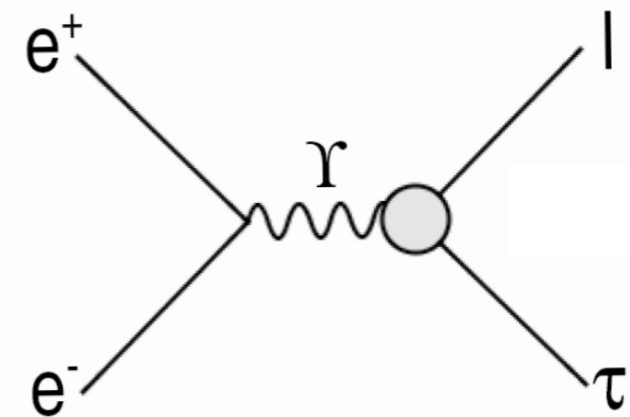
• No direct observation, but  $\tau \rightarrow \mu\mu\mu$  observable (?)

• Sensitivity  $\sim 10^{-8} - 10^{-10}$  at B-Factories, LHC

## Same new physics at TeV scale also predicts LFV Upsilon Decays



Re-ordering of  
incoming/outgoing  
particles



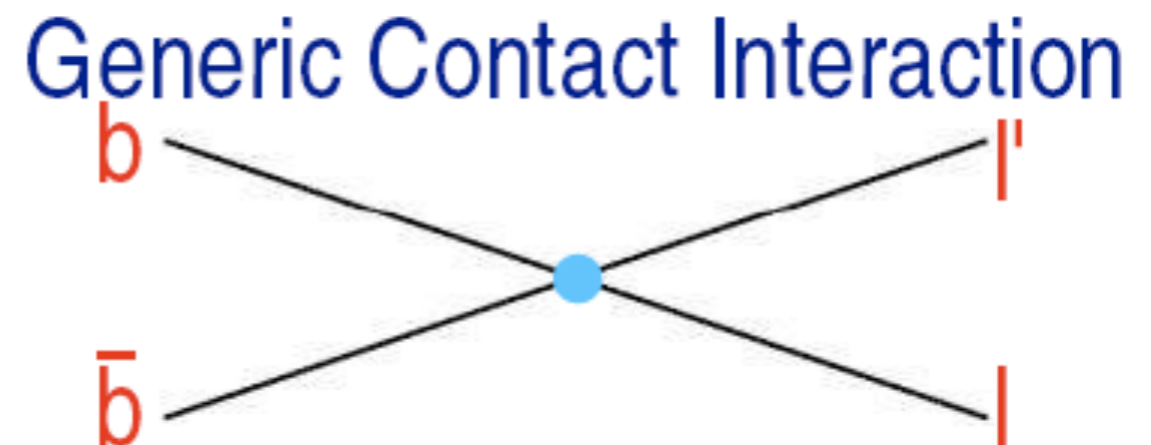
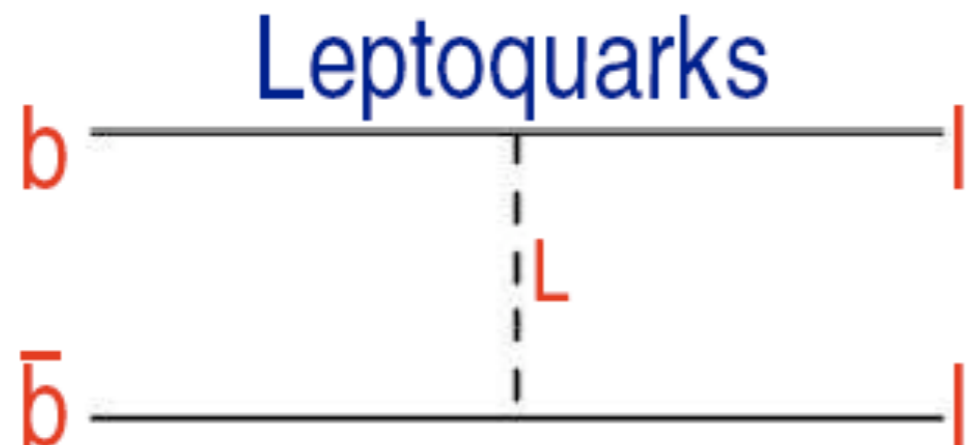
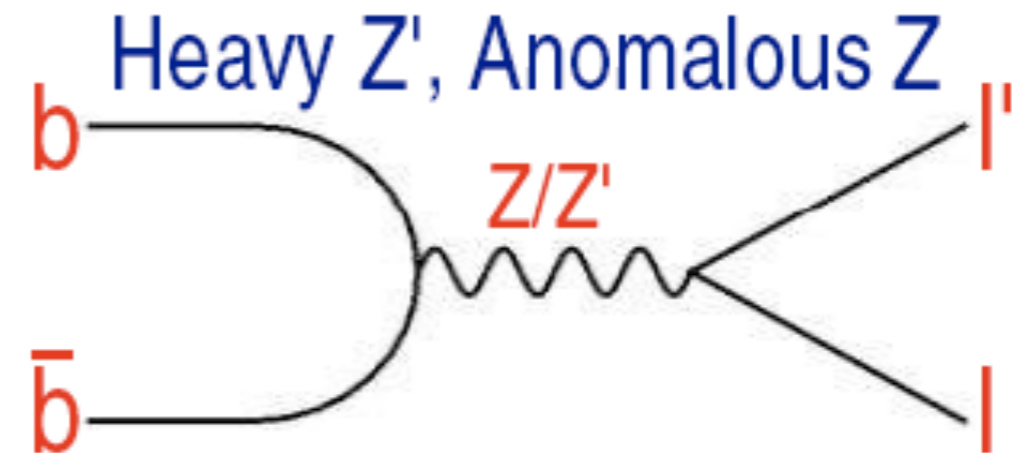
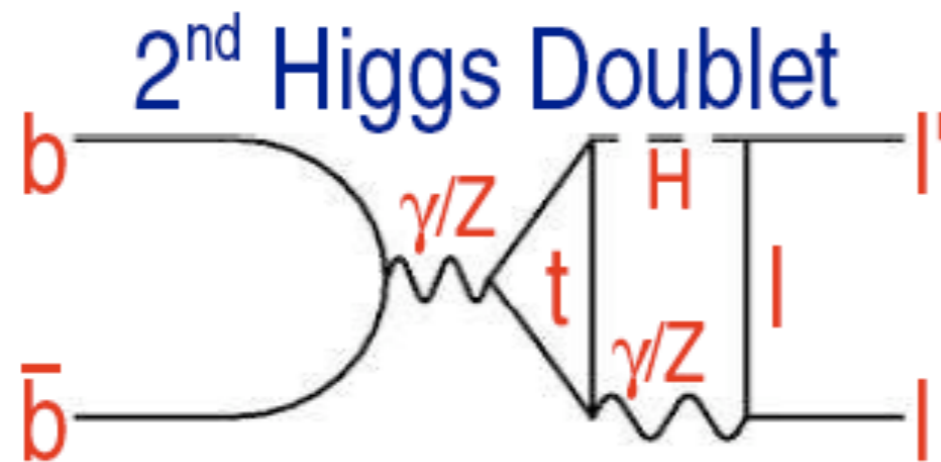
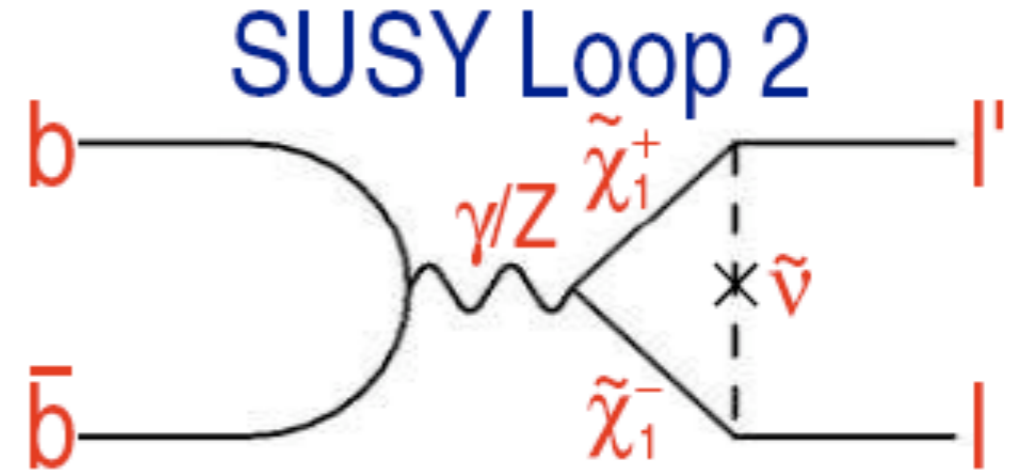
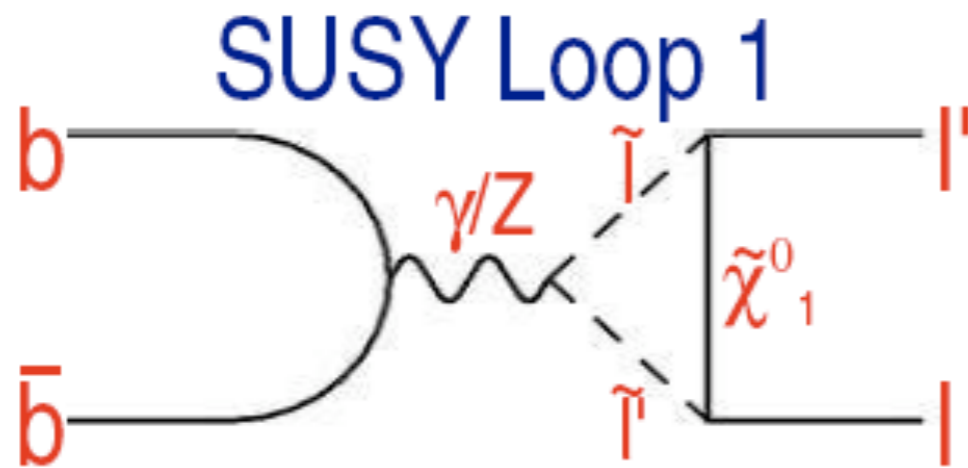
$$\mathcal{B}(\Upsilon \rightarrow l\tau) \sim \frac{\mathcal{B}(\tau \rightarrow lll)}{\mathcal{B}(\tau \rightarrow l\nu\bar{\nu})} \frac{\Gamma(W \rightarrow l\nu)^2}{\Gamma(\Upsilon)\Gamma(\Upsilon \rightarrow ll)} (M_\Upsilon/M_W)^6$$

S.Nussinov, et. al.  
PRD 63, 016003 (2001)

$$\bullet \mathcal{B}(\tau \rightarrow lll) < 2 - 4 \times 10^{-8} \Rightarrow \mathcal{B}(\Upsilon \rightarrow l\tau) < 3 - 6 \times 10^{-3}$$

BaBar PRL 99, 251803 (2007), Belle PLB 660,154 (2008)

# Lepton Flavor Violating Upsilon Decays



# How small is the rate known to be?

## BaBar/Belle searches for LFV in $\tau \rightarrow e/\mu\gamma$ decays at $\sqrt{s} \approx \Upsilon(4S)$

●  $\mathcal{L} = 232 fb^{-1} \Rightarrow N_\tau \approx 4 \times 10^8 : \mathcal{B}(\tau \rightarrow e\gamma) < 11 \times 10^{-8} @ 90\% \text{ C.L.}$

BaBar Collab., PRL 96, 041801 (2006)

●  $\mathcal{L} = 232 fb^{-1} \Rightarrow N_\tau \approx 4 \times 10^8 : \mathcal{B}(\tau \rightarrow \mu\gamma) < 6.8 \times 10^{-8} @ 90\% \text{ C.L.}$

BaBar Collab., PRL 95, 041802 (2005)

●  $\mathcal{L} = 535 fb^{-1} \Rightarrow N_\tau \approx 1 \times 10^9 : \mathcal{B}(\tau \rightarrow e\gamma) < 12 \times 10^{-8} @ 90\% \text{ C.L.}$

●  $\mathcal{L} = 535 fb^{-1} \Rightarrow N_\tau \approx 1 \times 10^9 : \mathcal{B}(\tau \rightarrow \mu\gamma) < 4.5 \times 10^{-8} @ 90\% \text{ C.L.}$

Belle Collab., PLB 666, 16 (2008)

## CLEO search for $\Upsilon \rightarrow \mu\tau, \tau \rightarrow e\nu\nu$

CLEO Collab., PRL 101, 201601 (2008)

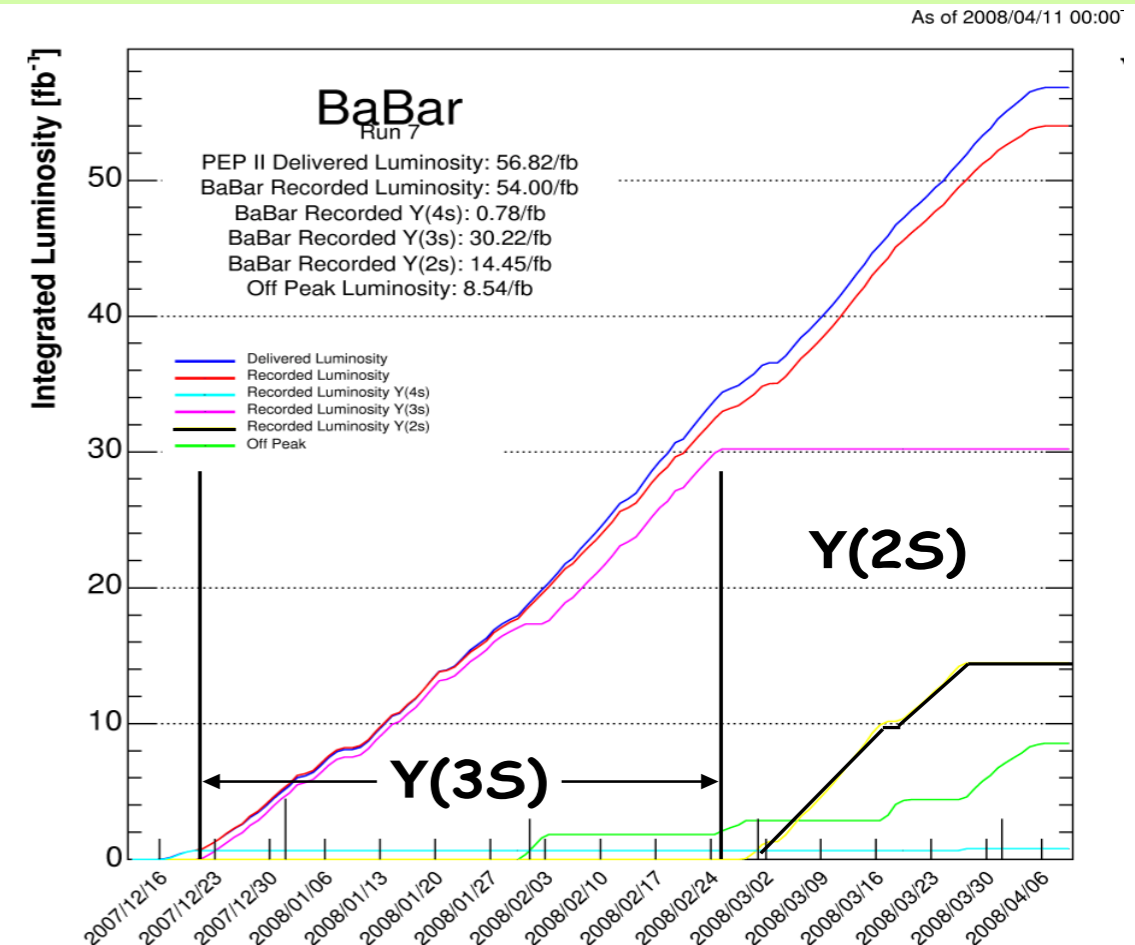
	$\Upsilon(1S)$	$\Upsilon(2S)$	$\Upsilon(3S)$
Mass (GeV/ $c^2$ )	9.46	10.02	10.36
$N$ decays (millions)	20.8	9.3	5.9
$\Gamma(\Upsilon \rightarrow \mu\mu)$ (keV)	1.252	0.581	0.413
$\Gamma(\Upsilon)$ (keV)	53.0	43.0	26.3
$\mathcal{B}(\mu\mu)$ ( $\times 10^{-3}$ )	23.6	13.5	15.7
$\mathcal{B}(\mu\tau)$ (95% CL UL, $\times 10^{-6}$ )	6.0	14.4	20.3
$\mathcal{B}(\mu\tau)/\mathcal{B}(\mu\mu)$ (95% CL UL, $\times 10^{-3}$ )	0.25	1.1	1.3
$\Lambda$ (95% CL LL, TeV, $\alpha_N = 1.0$ )	1.30	0.98	0.98

# How small a rate can BABAR measure?

Between Dec 2007 - Apr 2008,  
PEP II collected data below  $\Upsilon(4S)$ :  
 $\sim 30 \text{ fb}^{-1}$  @  $\Upsilon(3S)$  (122 M decays)  
 $\sim 15 \text{ fb}^{-1}$  @  $\Upsilon(2S)$  (100 M decays)

Dramatic increase in  
sensitivity to rare decays:

$$\Gamma_{\Upsilon(4S)} / \Gamma_{\Upsilon(nS)} \sim 10^3$$



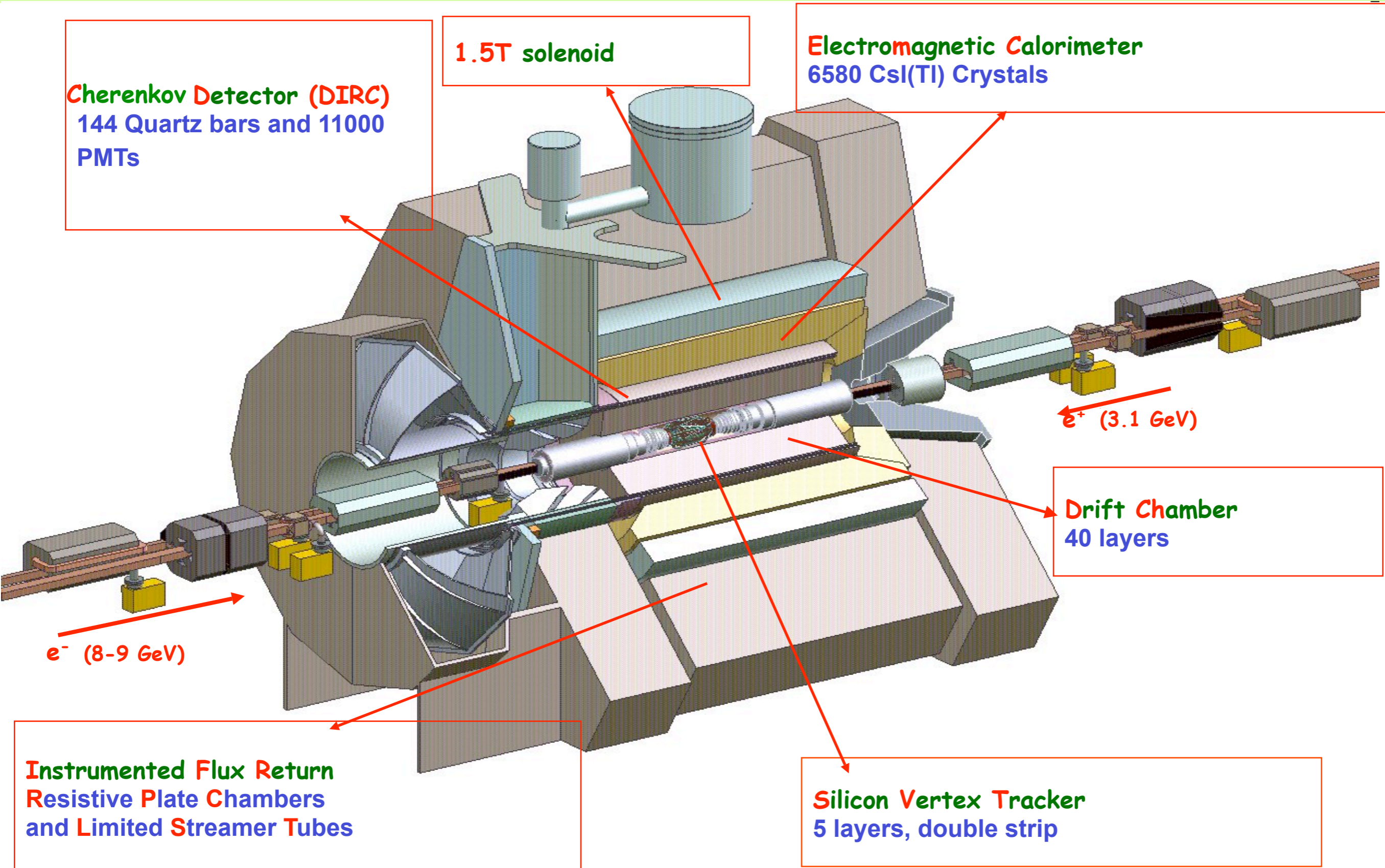
Improving Sensitivity for LFV discovery in  $\Upsilon$  Decays:

$\sim 20$  times more  $\Upsilon(3S)$  decays than CLEO  $\Rightarrow$  lower limits by  $\sim 4$

Improving Sensitivity for LFV discovery in  $\tau$  Decays:

$470 \text{ fb}^{-1}$  @  $\Upsilon(4S)$ ,  $30 \text{ fb}^{-1}$  @  $\Upsilon(3S)$ ,  $15 \text{ fb}^{-1}$  @  $\Upsilon(2S)$   $\Rightarrow N_{\tau} \sim 10^9$

# The BABAR Detector

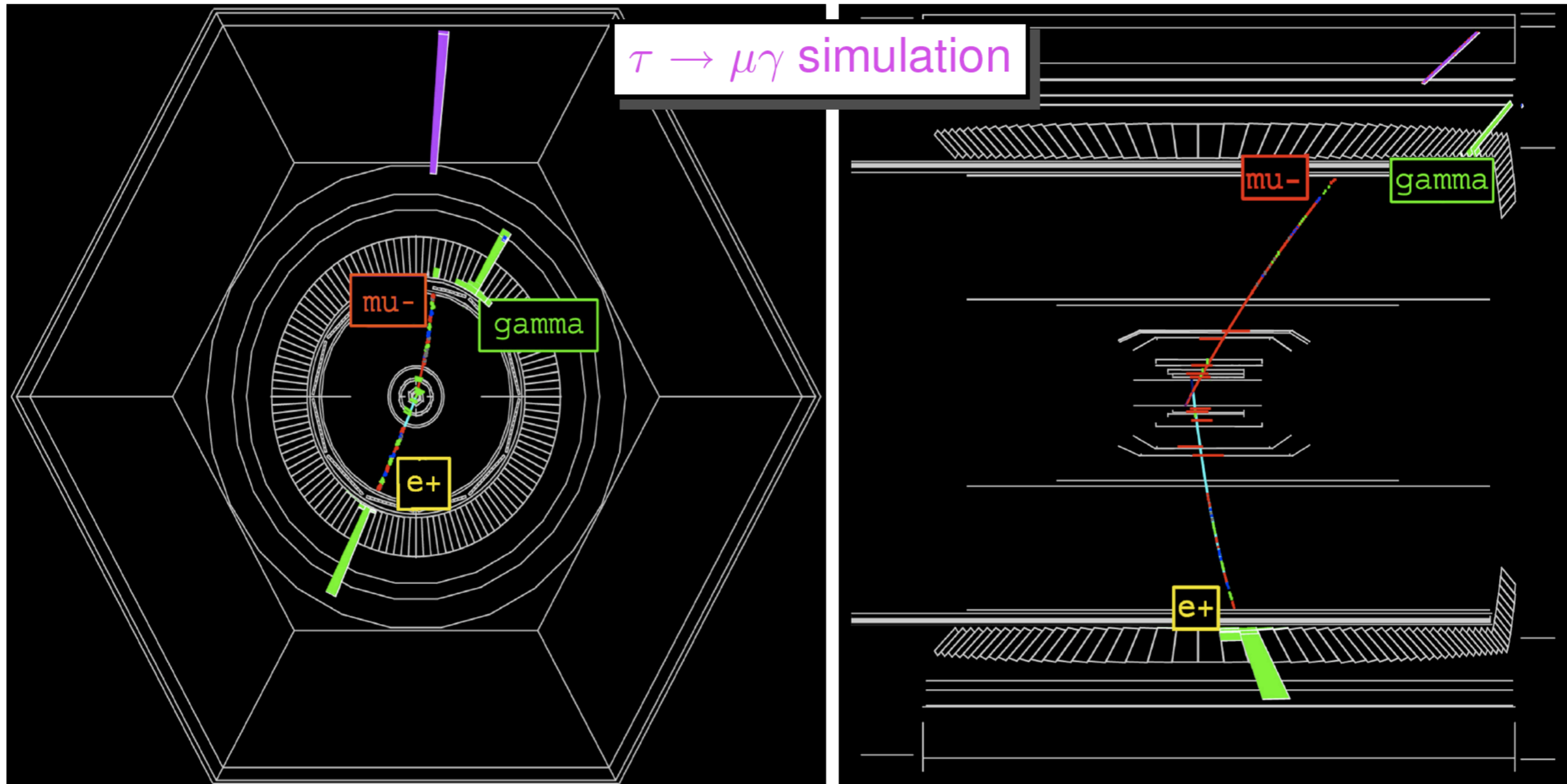




# $\tau \rightarrow \mu \gamma$ : Signal Characteristics

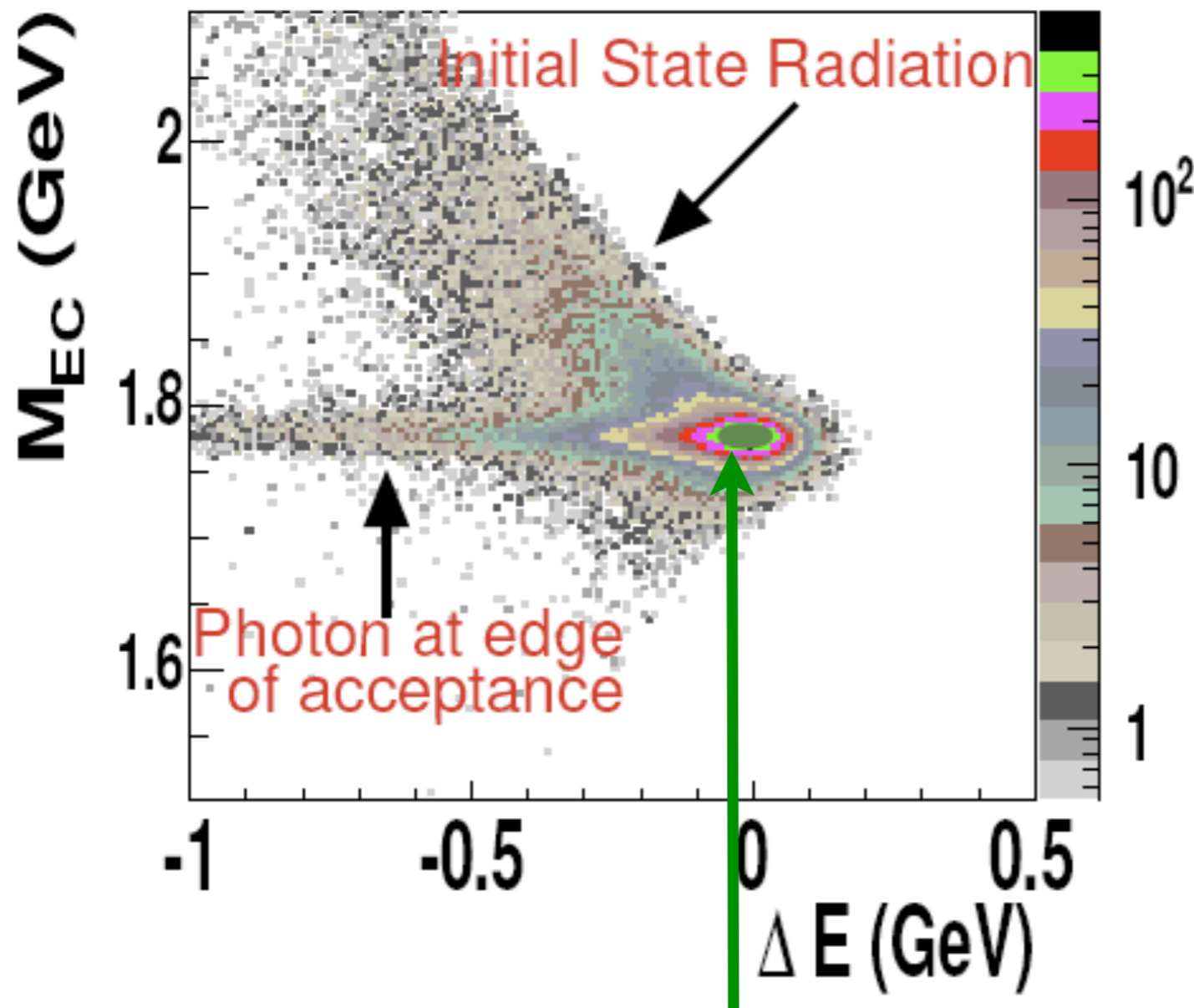
$m_{\mu\gamma} \sim m_\tau$

CM Frame:  $\Delta E = \sqrt{P_\mu^2 + m_\mu^2} + E_\gamma - \sqrt{s}/2 \sim 0$



# $\tau \rightarrow \mu \gamma$ : Signal Characteristics

- (Energy, Mass)<sub>daughters</sub>  $\sim (\frac{\sqrt{s}}{2}, m_\tau)$  (upto resolution & radiation)



$\tau \rightarrow \mu \gamma$  simulation

$$\Delta E = E_{rec} - \frac{\sqrt{s}}{2} \sim 0$$

$$\sigma(\Delta E) \sim 42 \text{ MeV}$$

$M_{EC}$  ( $\sigma \sim 8.3 \text{ MeV}$ )

Beam energy  
constrained mass  
after vertexing

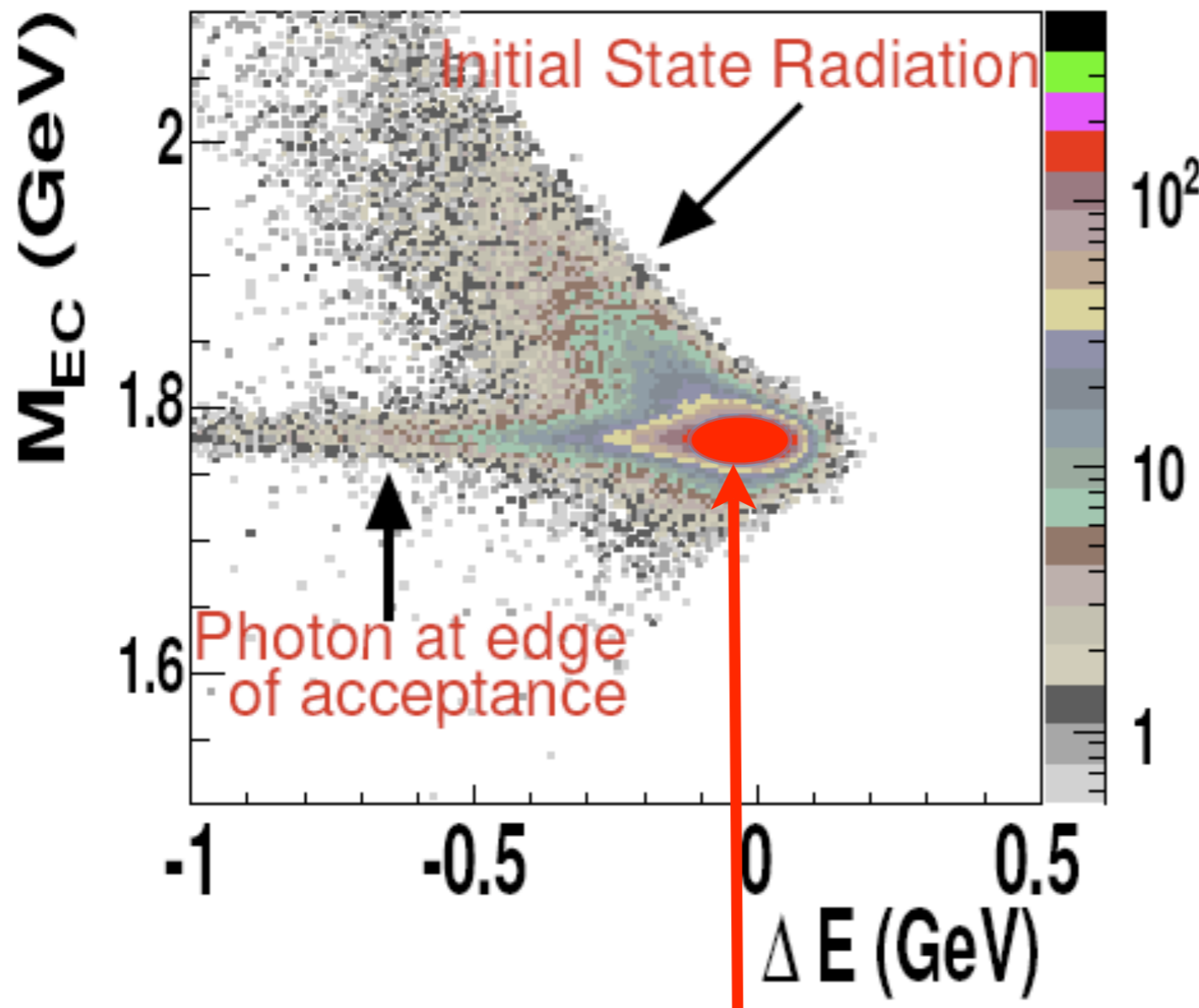
$\gamma$  at  $\mu$  POCA(XY)

[Inv. mass:  $\sigma \sim 18 \text{ MeV}$ ]

Signal Region:  $\pm 2 \sigma$  around  $(\langle \Delta E \rangle, \langle M_{EC} \rangle)$

# $\tau \rightarrow \mu \gamma$ : Signal Characteristics

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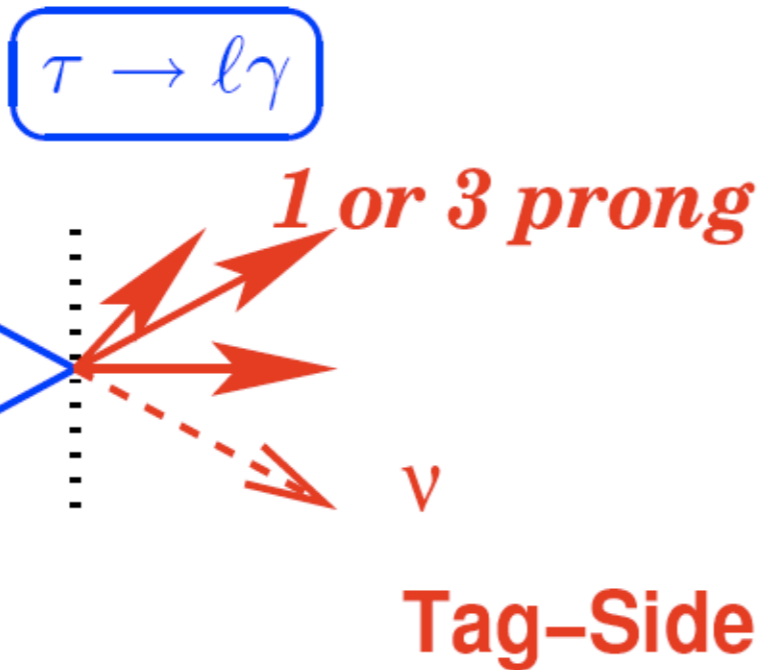
Beam energy  
constrained mass  
after vertexing

$\gamma$  at  $\mu$  POCA(XY)

[Inv. mass:  $\sigma \sim 18 \text{ MeV}$ ]

Blinded Region:  $\pm 3 \sigma$  around ( $\langle \Delta E \rangle, \langle M_{EC} \rangle$ )

# Analysis Strategy in a clean $e^+e^- \rightarrow \tau^+\tau^-$ environment



Backgrounds:

- $\tau \rightarrow e\gamma$  ( $\tau \rightarrow \mu\gamma$ ):
- Radiative Bhabha (di-muon)
- $\tau^+\tau^-\gamma$  ( $\tau \rightarrow \ell\nu\bar{\nu}$ )
- $q\bar{q}$  ( $\gamma$ )

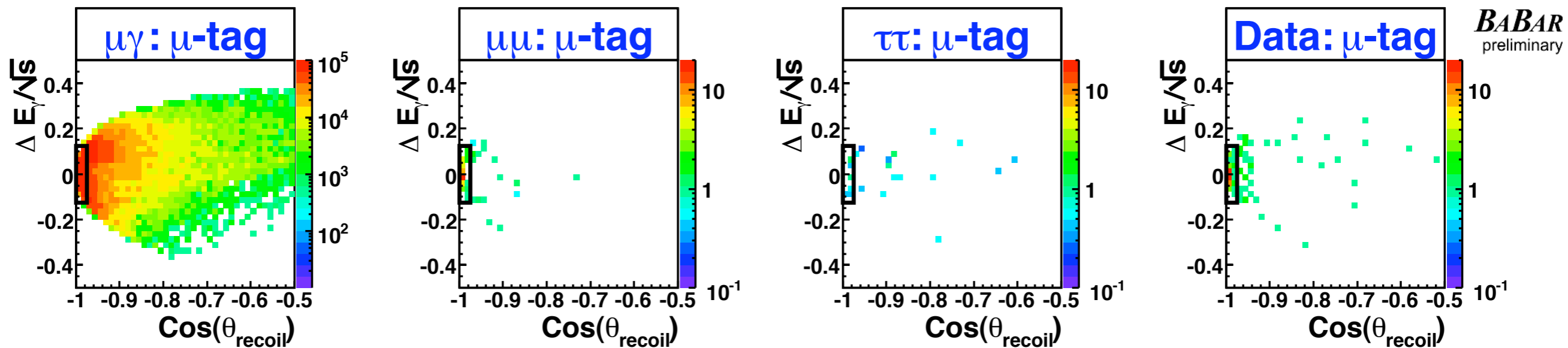
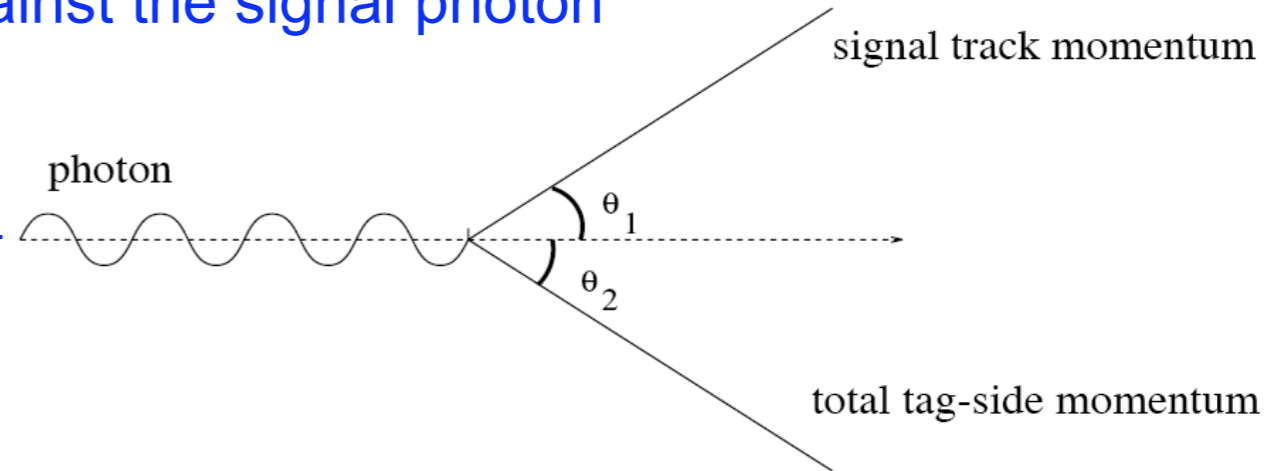
- Reconstruct final state from two or four charged tracks with zero total charge
- Divide event into signal-side and tag-side hemispheres perpendicular to Thrust axis
- Classify tag-side as e,  $\mu$ ,  $\pi$ ,  $\rho$ , 3h tags
- For  $\tau \rightarrow e\gamma$  search, veto e-tag because of very large radiative Bhabha cross-section
- For leptonic tags, reduce QED backgrounds characterized by zero missing momentum
- For hadronic tags, reduce backgrounds using cuts on tag-side missing mass
- Finally reduce remaining backgrounds using Neural Net based discriminators, tuned for each tag and at each center-of-mass energy
- Study backgrounds in Grand Signal Box (GSB)
  - $1.55 \text{ GeV}/c^2 < m_{\text{EC}} < 2.05 \text{ GeV}/c^2$
  - $-1.0 \text{ GeV} < \Delta E < 0.5 \text{ GeV}$ .

# QED Backgrounds in Leptonic Tags

Exploit correlation between 2 kinematic variables:

cosine of the opening angle  $\cos(\theta_{\text{recoil}})$  between the signal-track and the total observed tag-side momentum in the reference frame recoiling against the signal photon

$$\frac{\Delta E_\gamma}{\sqrt{s}} \equiv \frac{E_\gamma^{CM}}{\sqrt{s}} - \frac{|\sin(\theta_1 + \theta_2)|}{\sin \theta_1 + \sin \theta_2 + |\sin(\theta_1 + \theta_2)|}$$



In both  $e$  and  $\mu$  tags in  $\tau \rightarrow \mu \gamma$  search, remove events passing

$$|\Delta E_\gamma| < 0.125\sqrt{s} \text{ and } \cos \theta_{\text{recoil}} < -0.975$$

In  $\tau \rightarrow e \gamma$  search, not enough background events in  $\mu$  tag  $\Rightarrow$  so no additional cut needed

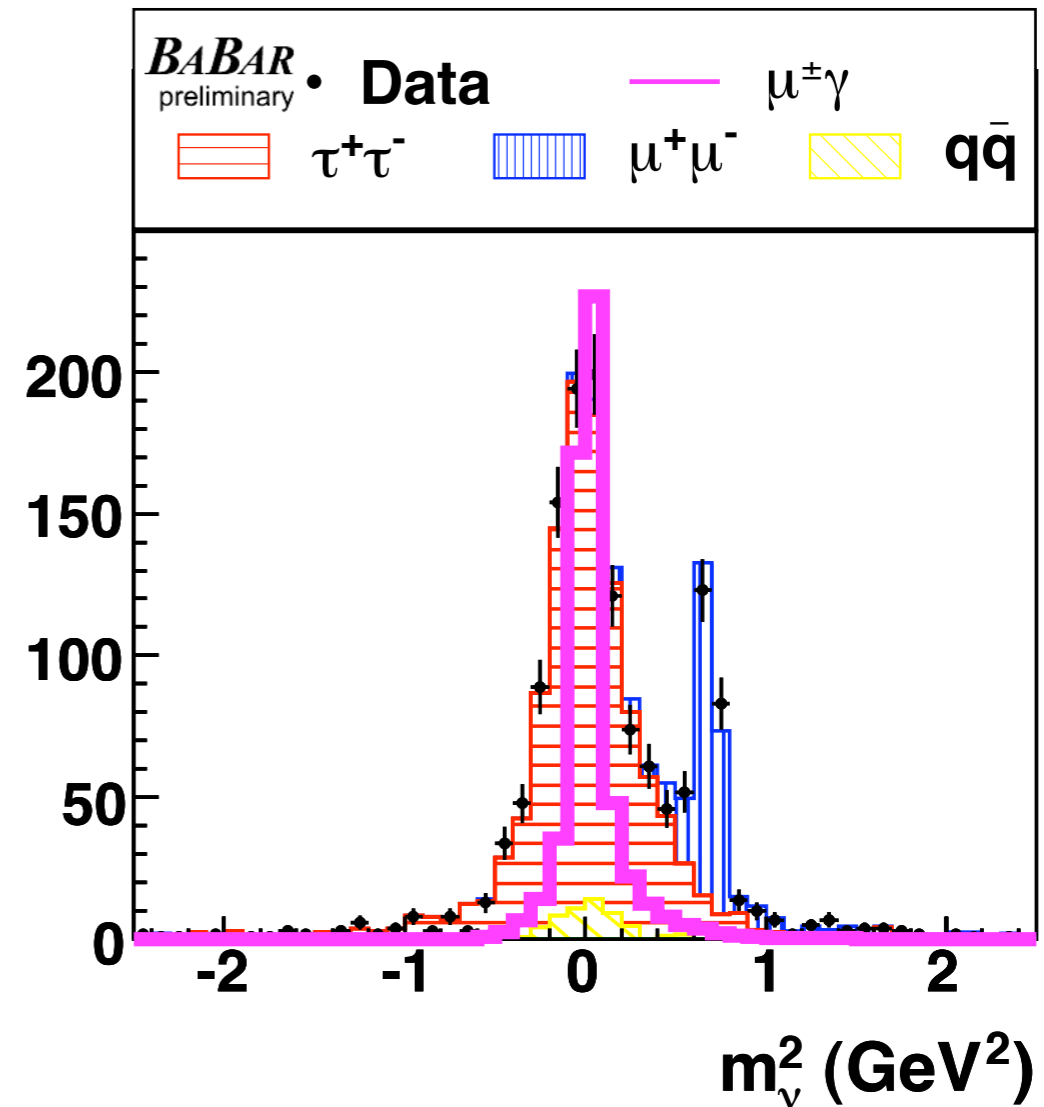
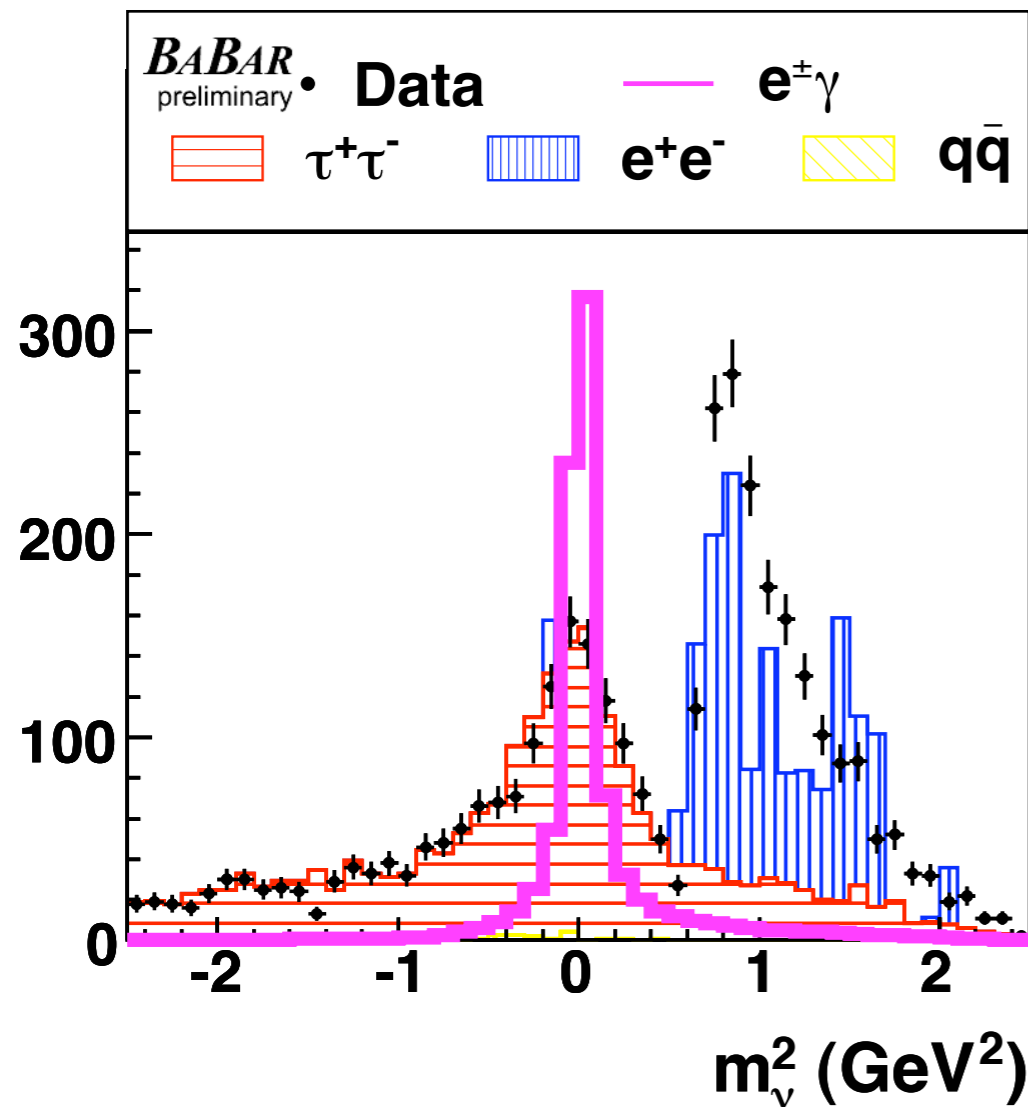
*BABAR*  
preliminary

# Tag-side Missing Mass for Hadronic Tags

- Exploit the unique feature that signal-side  $\tau$  decay is neutrino-less  
 $\Rightarrow$  fully reconstruct the direction of tag-side  $\tau$  assumed to be  $\sqrt{s}/2$  in CM frame

$$\tau^\pm \rightarrow e^\pm \gamma:$$

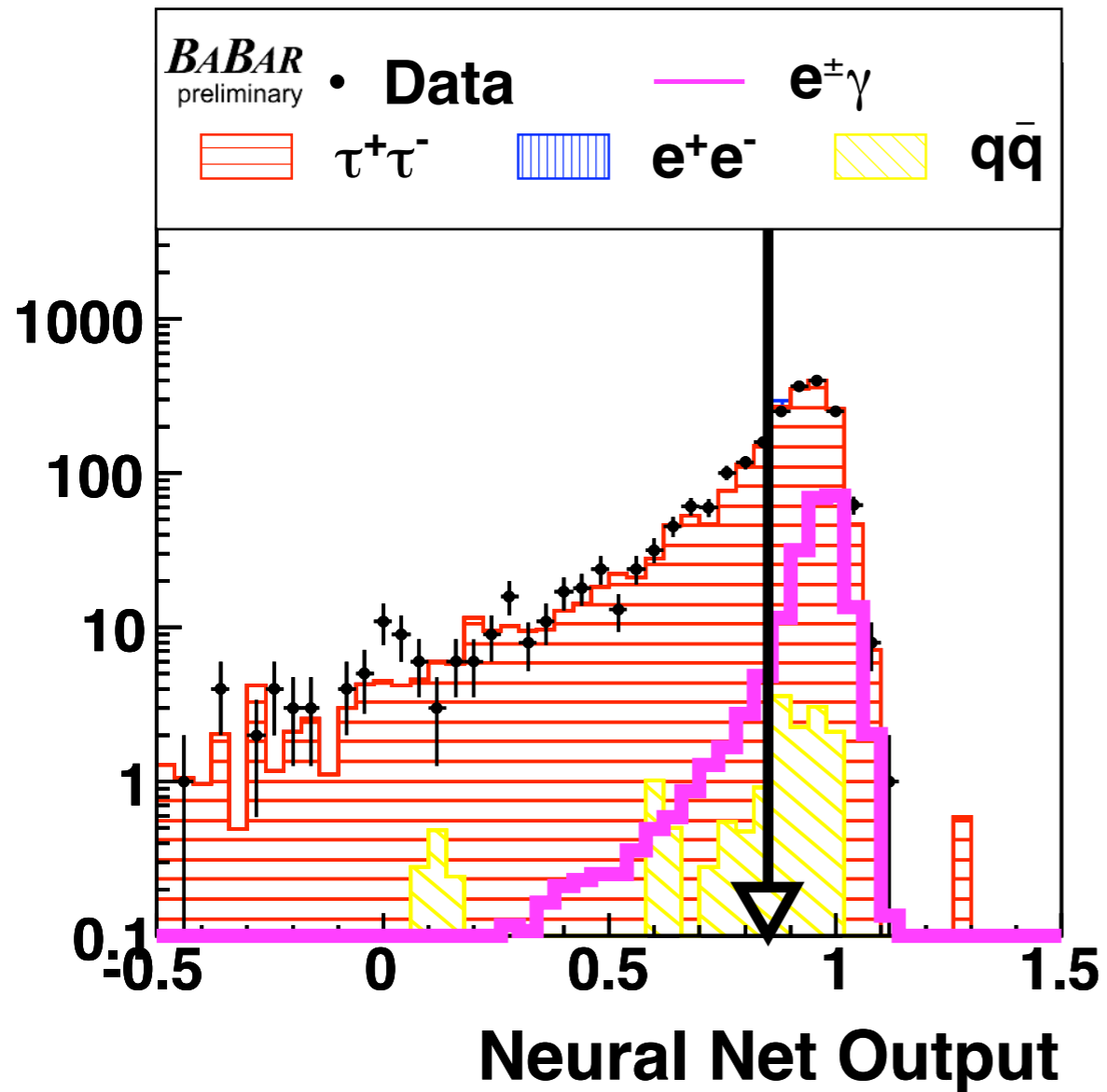
$$\tau^\pm \rightarrow \mu^\pm \gamma:$$



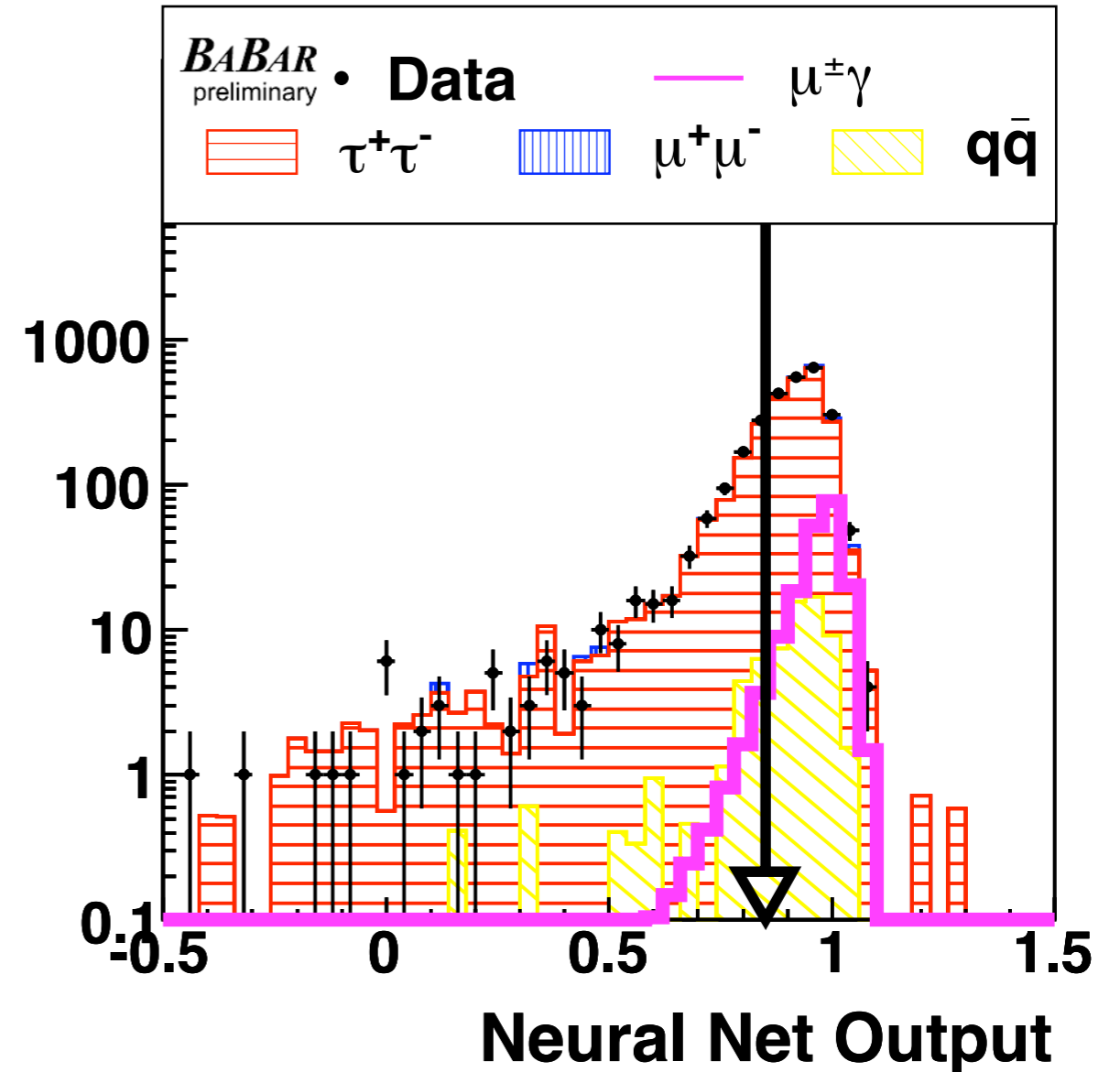
Require:  $|m_\nu^2| < 0.25 \text{ GeV}^2$  for  $\pi^-$ - and  $3h$ -tags, and  $|m_\nu^2| < 0.50 \text{ GeV}^2$  for  $\rho$ -tag.

# Neural Net Based discriminator

$$\tau^\pm \rightarrow e^\pm \gamma:$$



$$\tau^\pm \rightarrow \mu^\pm \gamma:$$



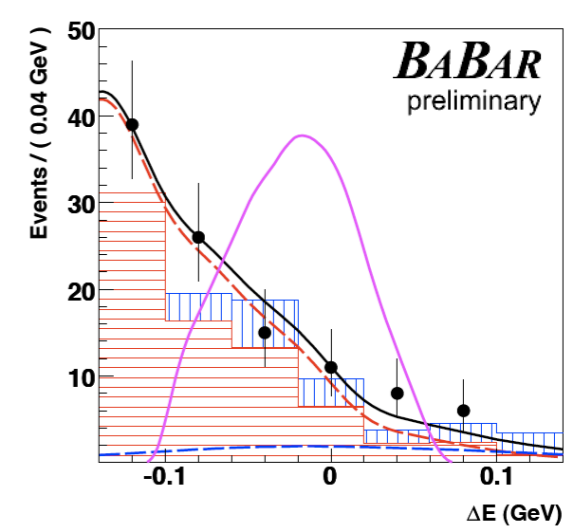
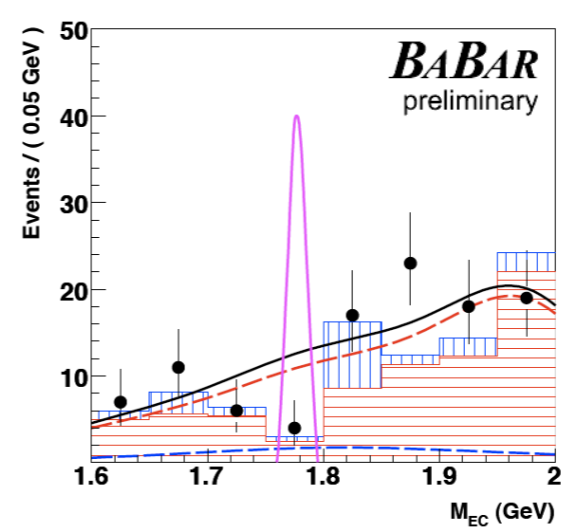
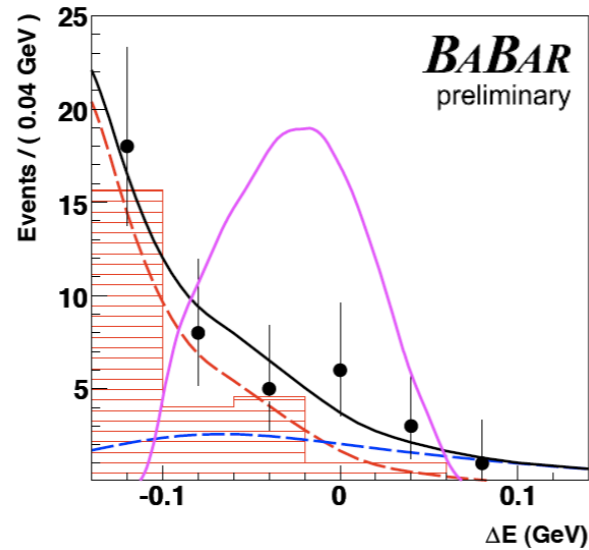
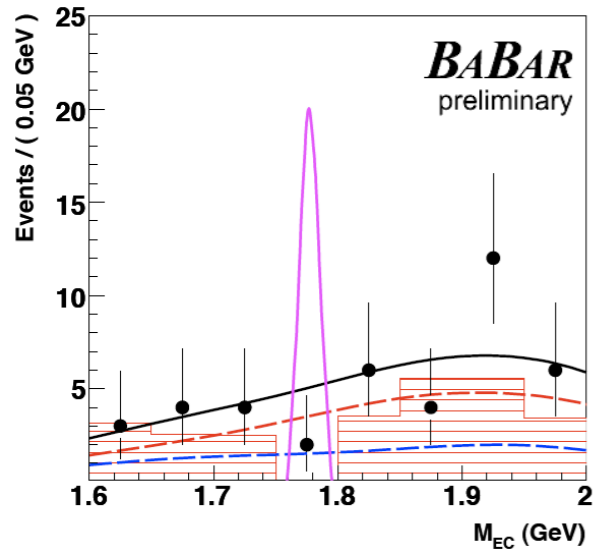
*A cut of NN output  $> .85$  improves Signal/Background by 40% for  $\tau \rightarrow e \gamma$  search and by 30% for  $\tau \rightarrow \mu \gamma$  search*

# 2-dim Fit with Background PDFs only

$$PDF_{tot} = (f_{e^+e^-/\mu^+\mu^-} \times PDF_{e^+e^-/\mu^+\mu^-}) + ([1 - f_{e^+e^-/\mu^+\mu^-}] \times PDF_{\tau})$$

$$\tau^{\pm} \rightarrow e^{\pm}\gamma:$$

$$\tau^{\pm} \rightarrow \mu^{\pm}\gamma:$$



The number of background events ( $N_{2\sigma}^{data}$ ) inside the  $\pm 2\sigma$  ellipse is estimated as:

$$N_{2\sigma}^{data} = \frac{\int_{2\sigma} PDF_{tot}}{\int_{FitBox-3\sigma} PDF_{tot}} \times N_{FitBox-3\sigma}^{data}$$

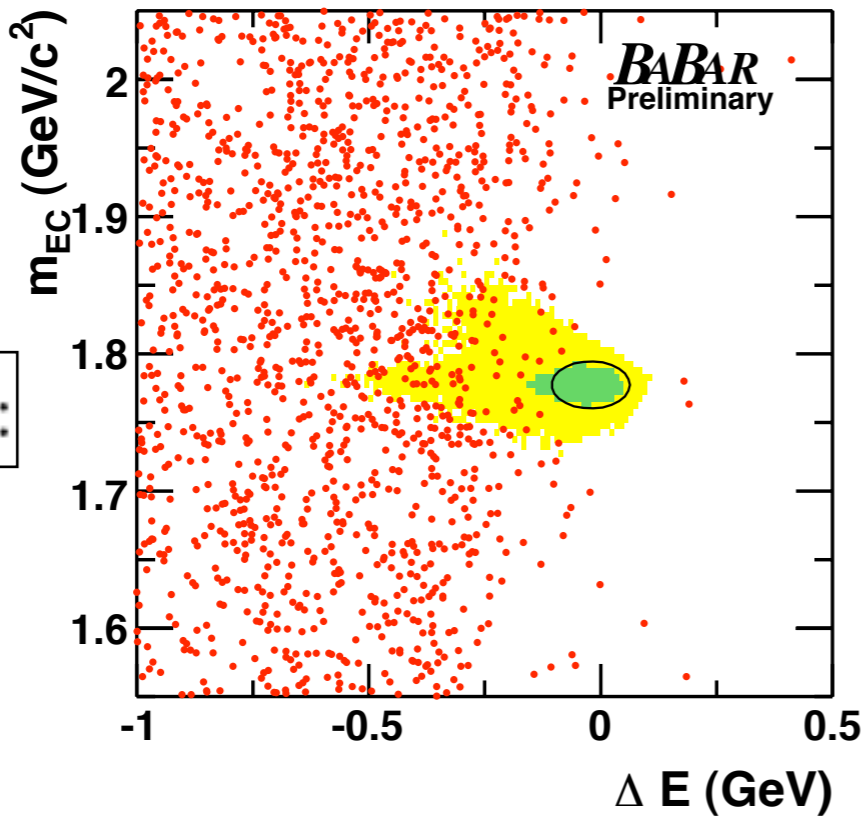
**Cross-check neighbouring ellipses shifted in the mass variable:**

Decay modes	# of events	-9 $\sigma$	-5 $\sigma$	0	+5 $\sigma$	+9 $\sigma$
$\tau^{\pm} \rightarrow e^{\pm}\gamma$	Observed	2	1	?	2	2
	Expected	$1.2 \pm 0.2$	$1.4 \pm 0.2$	$1.6 \pm 0.3$	$1.9 \pm 0.3$	$2.1 \pm 0.3$
$\tau^{\pm} \rightarrow \mu^{\pm}\gamma$	Observed	3	1	?	4	6
	Expected	$2.8 \pm 0.3$	$3.1 \pm 0.3$	$3.6 \pm 0.4$	$4.2 \pm 0.4$	$4.8 \pm 0.5$

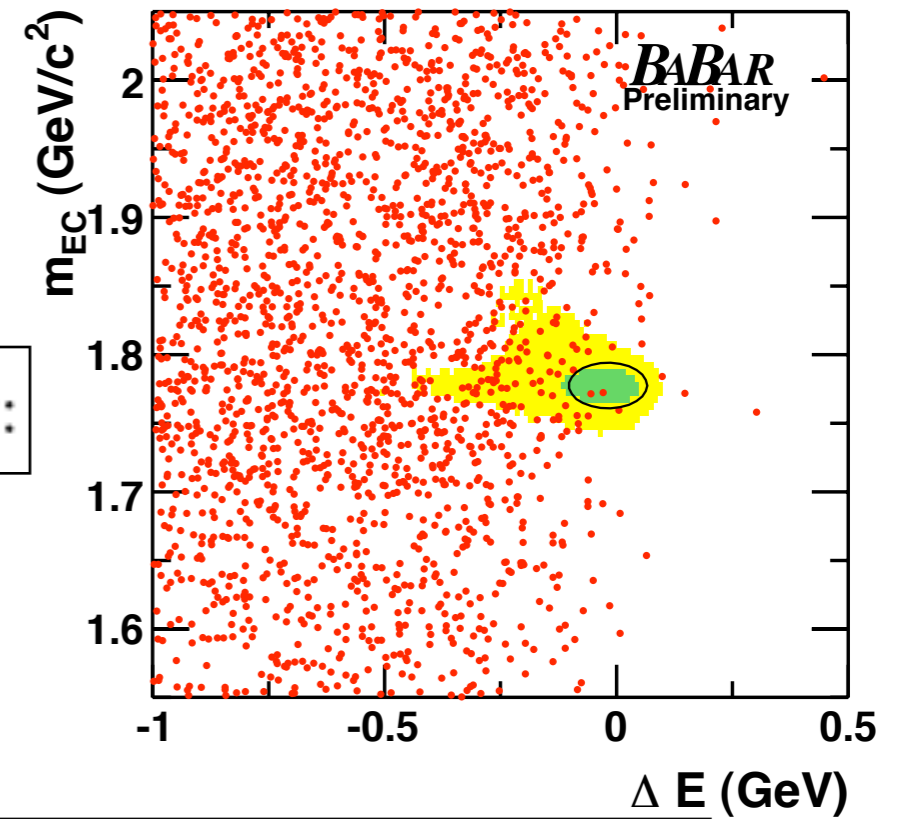


# Results

$$\tau^\pm \rightarrow e^\pm \gamma$$



$$\tau^\pm \rightarrow \mu^\pm \gamma$$



$N_\tau$

$(963 \pm 7) \times 10^6$

$\tau^\pm \rightarrow e^\pm \gamma$  search

Number of background events expected in  $2\sigma$  signal ellipse

$(1.6 \pm 0.4)$

Efficiency in  $2\sigma$  signal ellipse

$(3.9 \pm 0.3)\%$

Expected Feldman & Cousins Upper Limit (w/o systmatics)

$\mathcal{B}(\tau^\pm \rightarrow e^\pm \gamma) < 9.8 \times 10^{-8}$  at 90% CL

Expected Feldman & Cousins Upper Limit (with systmatics)

$\mathcal{B}(\tau^\pm \rightarrow e^\pm \gamma) < 9.8 \times 10^{-8}$  at 90% CL

Numbers of events observed in  $2\sigma$  signal ellipse

0

Observed Feldman & Cousins Upper Limit

$\mathcal{B}(\tau^\pm \rightarrow e^\pm \gamma) < 3.3 \times 10^{-8}$  at 90% CL



$\tau^\pm \rightarrow \mu^\pm \gamma$  search

Number of background events expected in  $2\sigma$  signal ellipse

$(3.6 \pm 0.7)$

Efficiency in  $2\sigma$  signal ellipse

$(6.1 \pm 0.5)\%$

Expected Feldman & Cousins Upper Limit (w/o systmatics)

$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) < 7.9 \times 10^{-8}$  at 90% CL

Expected Feldman & Cousins Upper Limit (with systmatics)

$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) < 8.2 \times 10^{-8}$  at 90% CL

Numbers of events observed in  $2\sigma$  signal ellipse

2

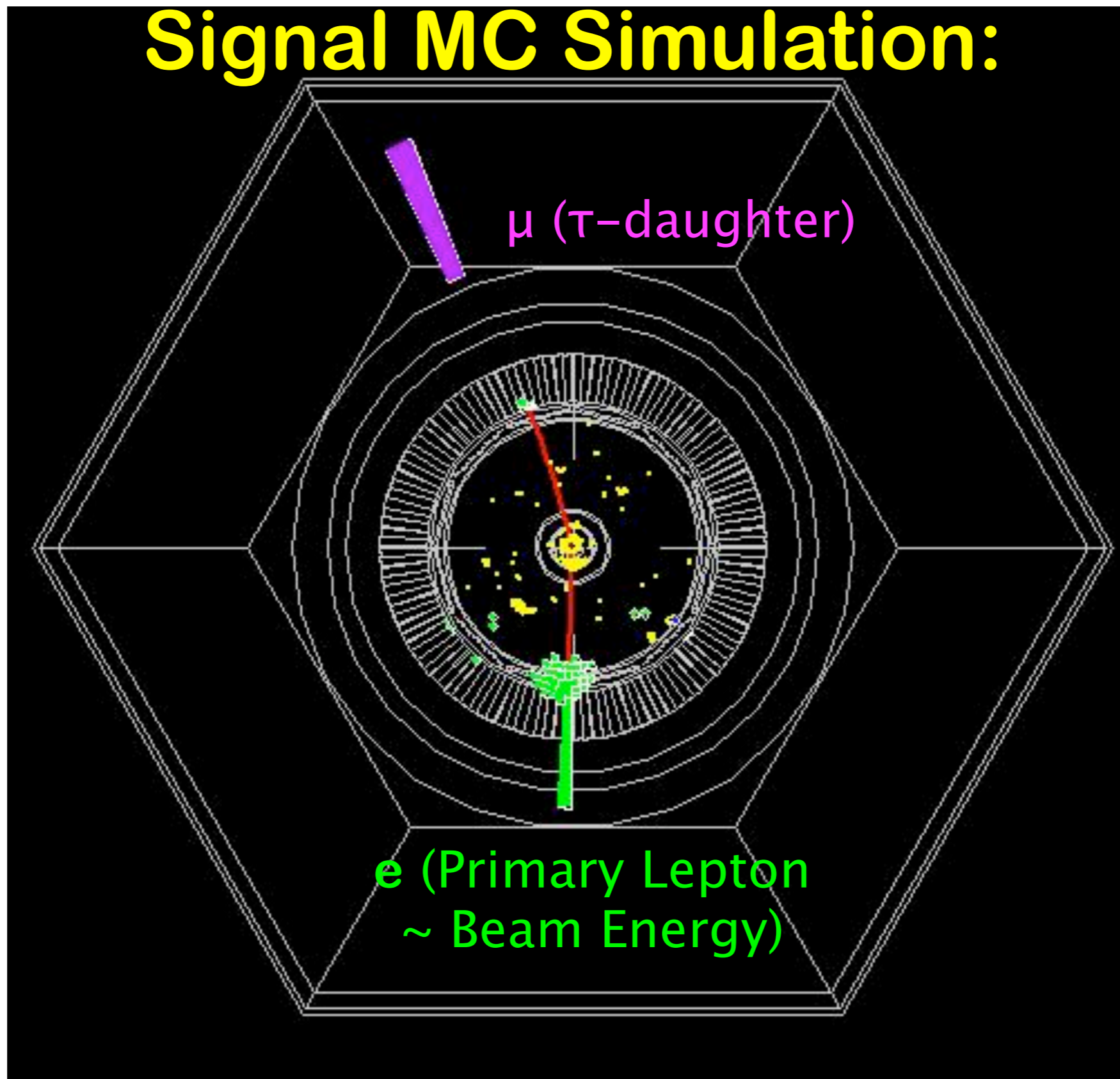
Observed Feldman & Cousins Upper Limit

$\mathcal{B}(\tau^\pm \rightarrow \mu^\pm \gamma) < 4.4 \times 10^{-8}$  at 90% CL

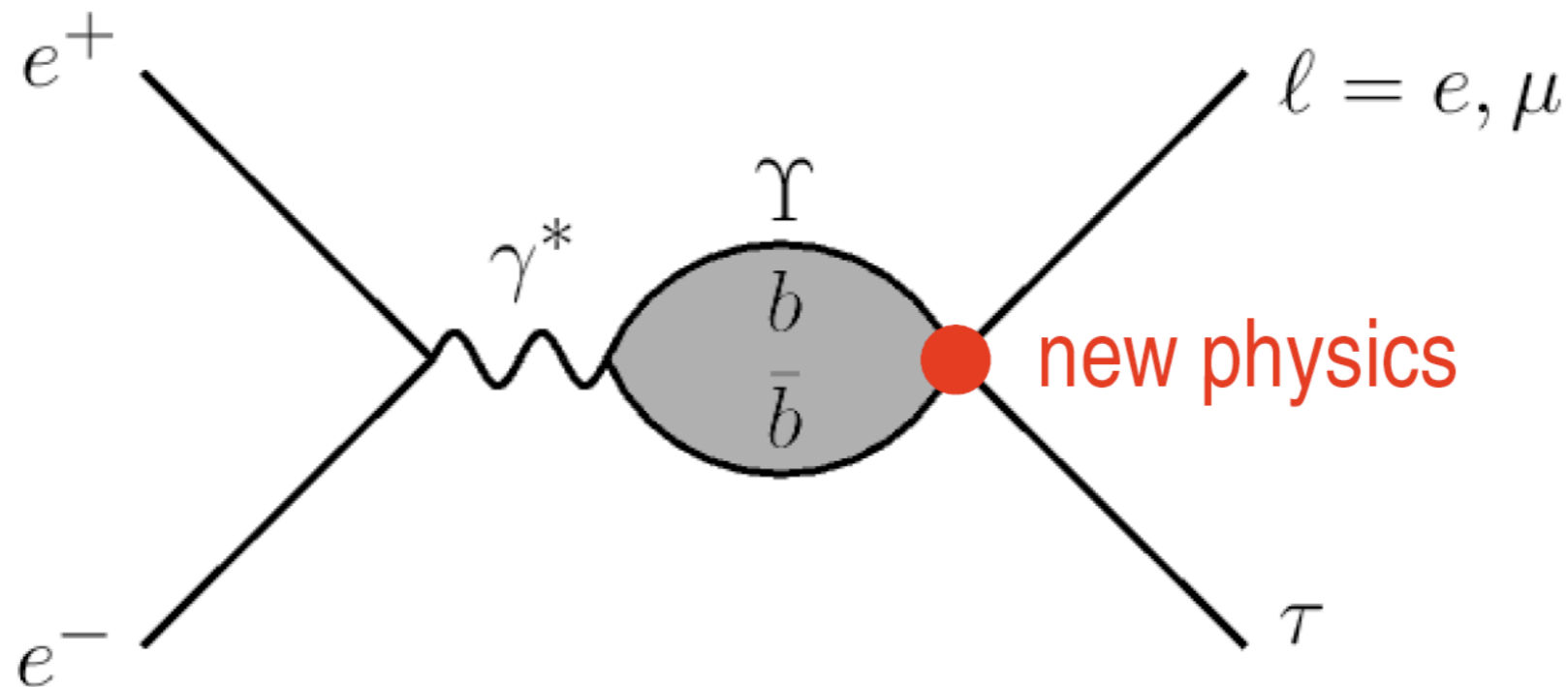


# $\Upsilon \rightarrow e\tau, \tau \rightarrow \mu\nu\nu$ : Signal Characteristics

## Signal MC Simulation:



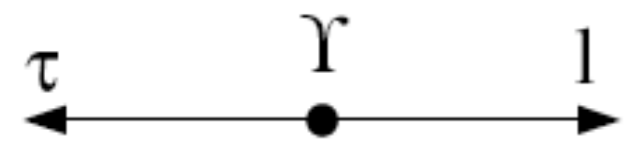
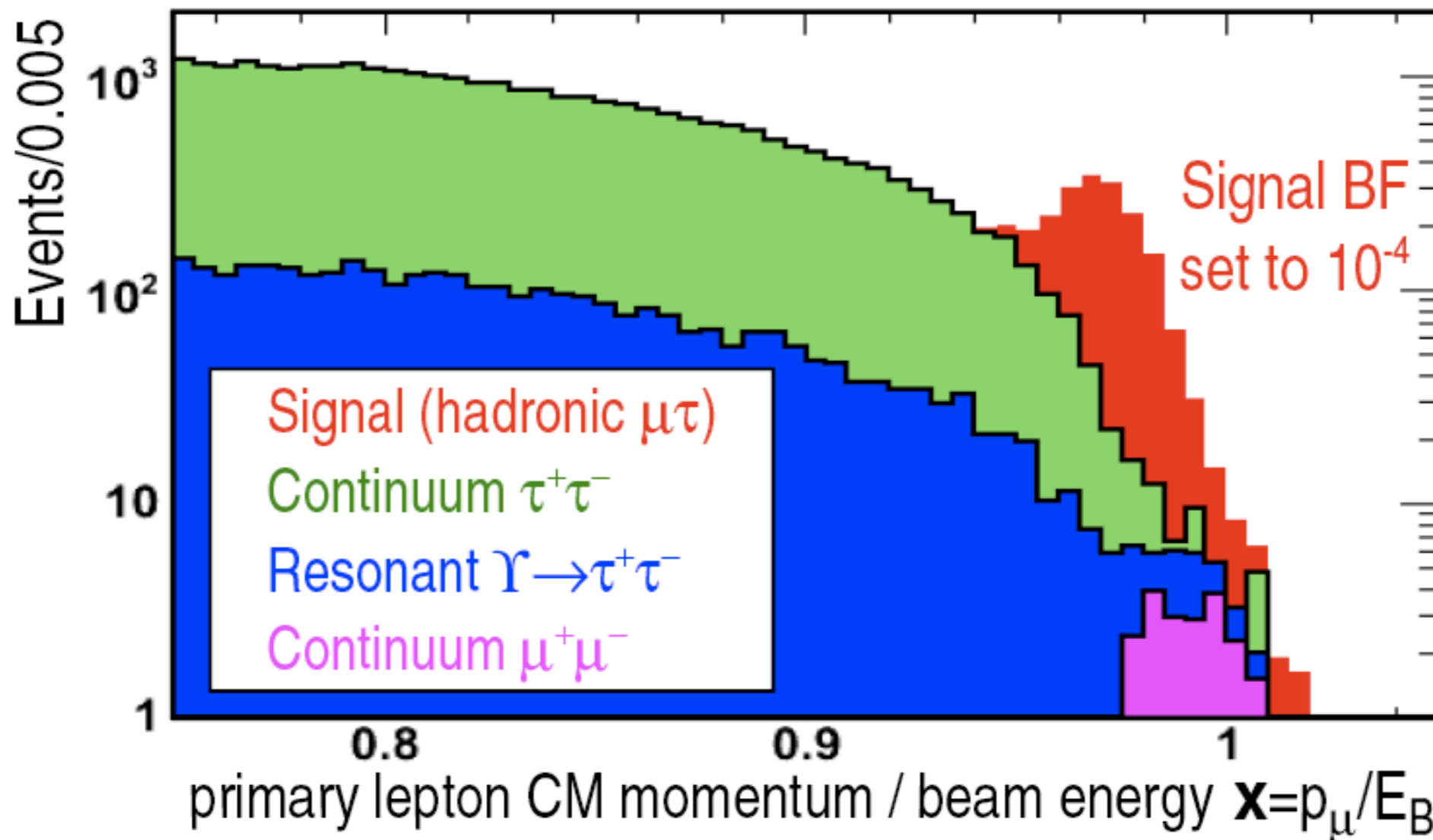
# Event Selection



- Reconstruct final state from
  - two oppositely charged tracks
  - one or two additional neutral pions
- Primary lepton ( $e/\mu$ ) near beam energy
- $\tau$  decay with missing energy in other hemisphere decaying into a lepton with opposite flavor or  $\rho/a_1$
- $\tau$  decay with same flavor lepton or a single  $\pi$  vetoed to reduce QED bkgd.

Process	$\tau$ Decay	Channel
$\Upsilon(3S) \rightarrow e\tau$	$\tau \rightarrow \mu\nu\nu$	leptonic $e\tau$
$\Upsilon(3S) \rightarrow e\tau$	$\tau \rightarrow \pi^\pm \pi^0 \nu / \pi^\pm \pi^0 \pi^0 \nu$	hadronic $e\tau$
$\Upsilon(3S) \rightarrow \mu\tau$	$\tau \rightarrow e\nu\nu$	leptonic $\mu\tau$
$\Upsilon(3S) \rightarrow \mu\tau$	$\tau \rightarrow \pi^\pm \pi^0 \nu / \pi^\pm \pi^0 \pi^0 \nu$	hadronic $\mu\tau$

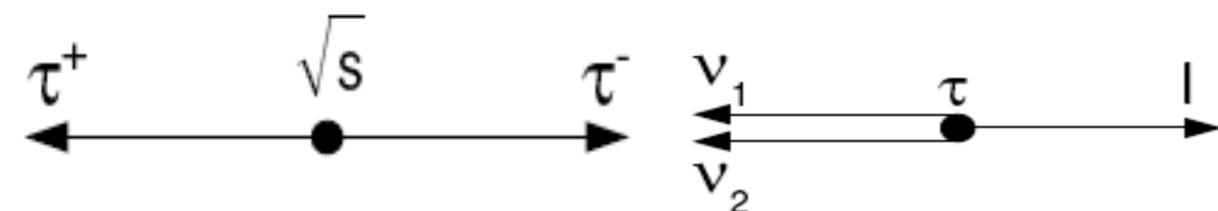
# The discriminating variable



$$E_l = (m_\Upsilon^2 - m_\tau^2 + m_l^2) / (2m_\Upsilon) \quad p_l / E_B = \sqrt{4(E_l^2 - m_l^2) / m_\Upsilon^2}$$

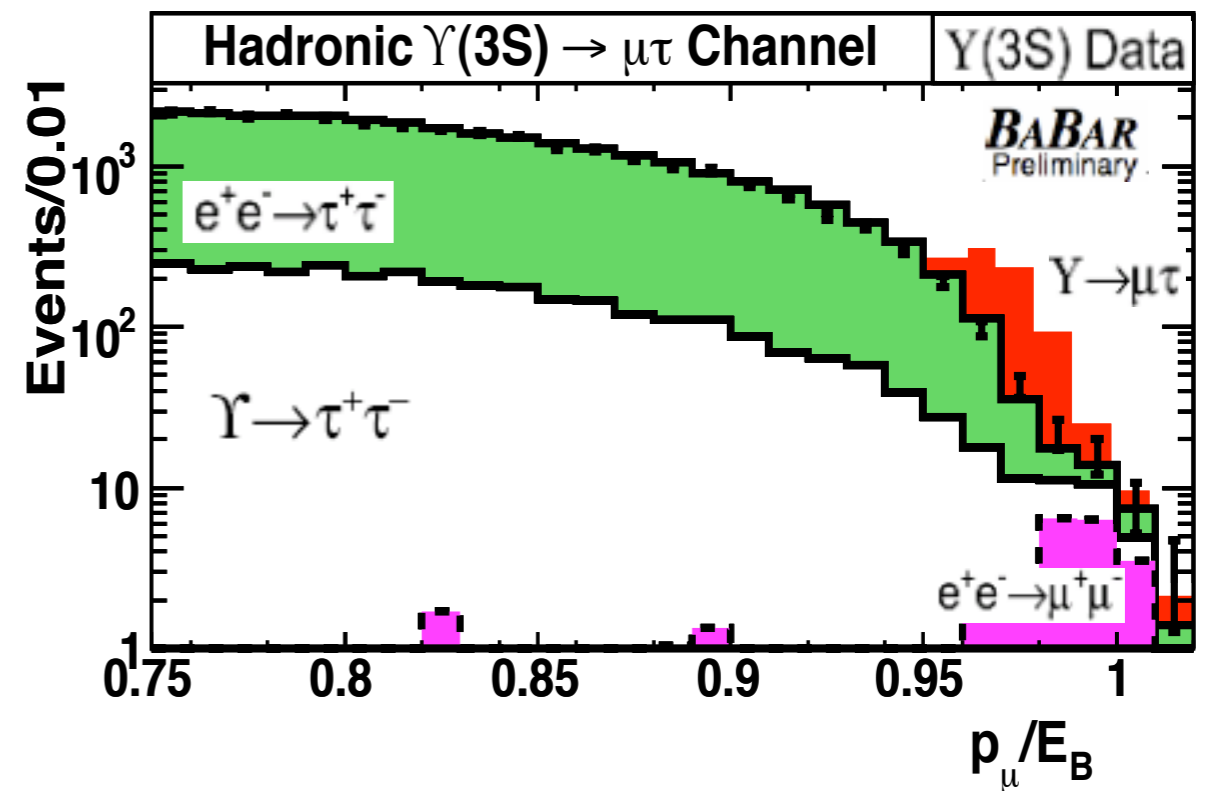
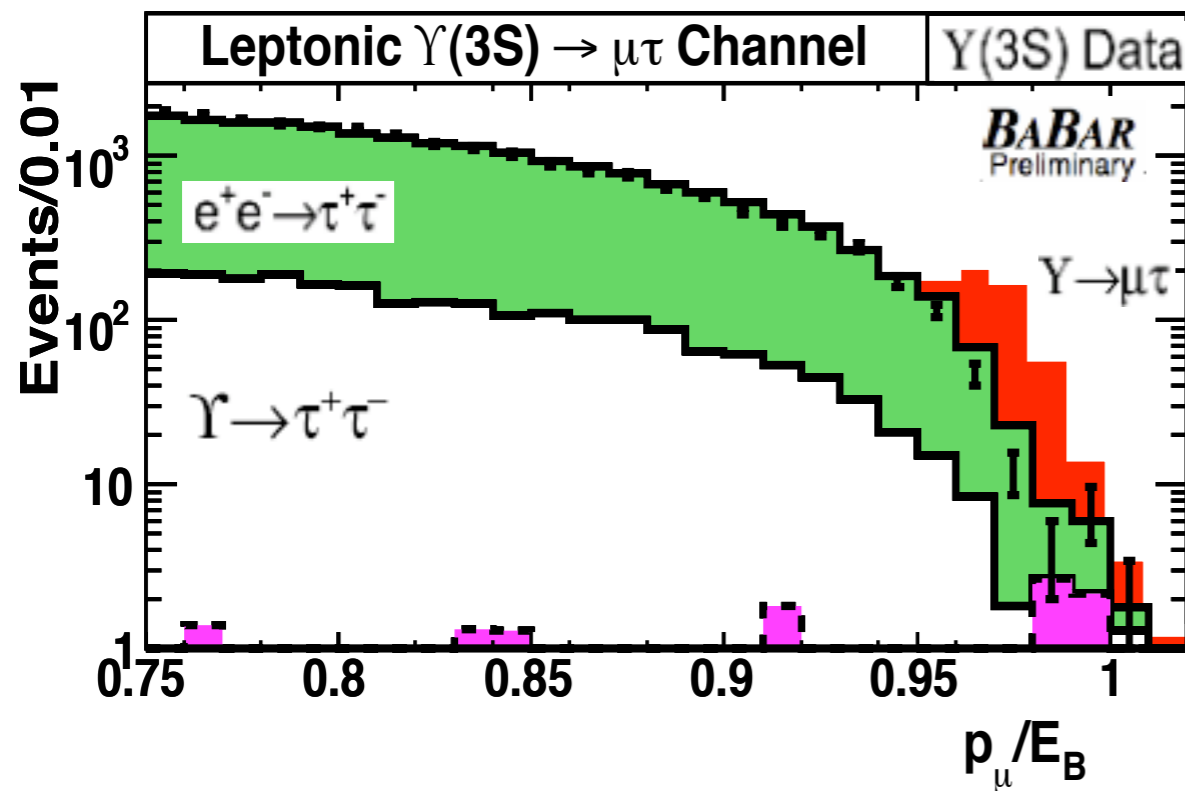
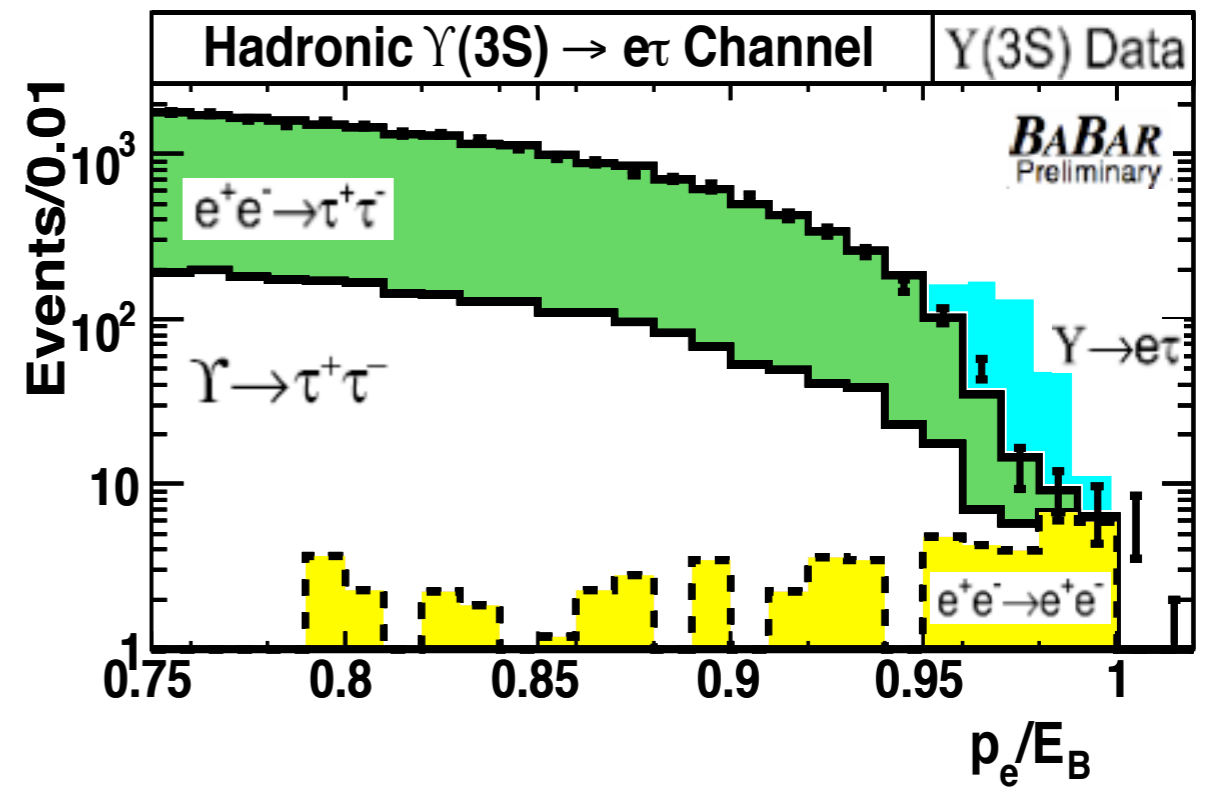
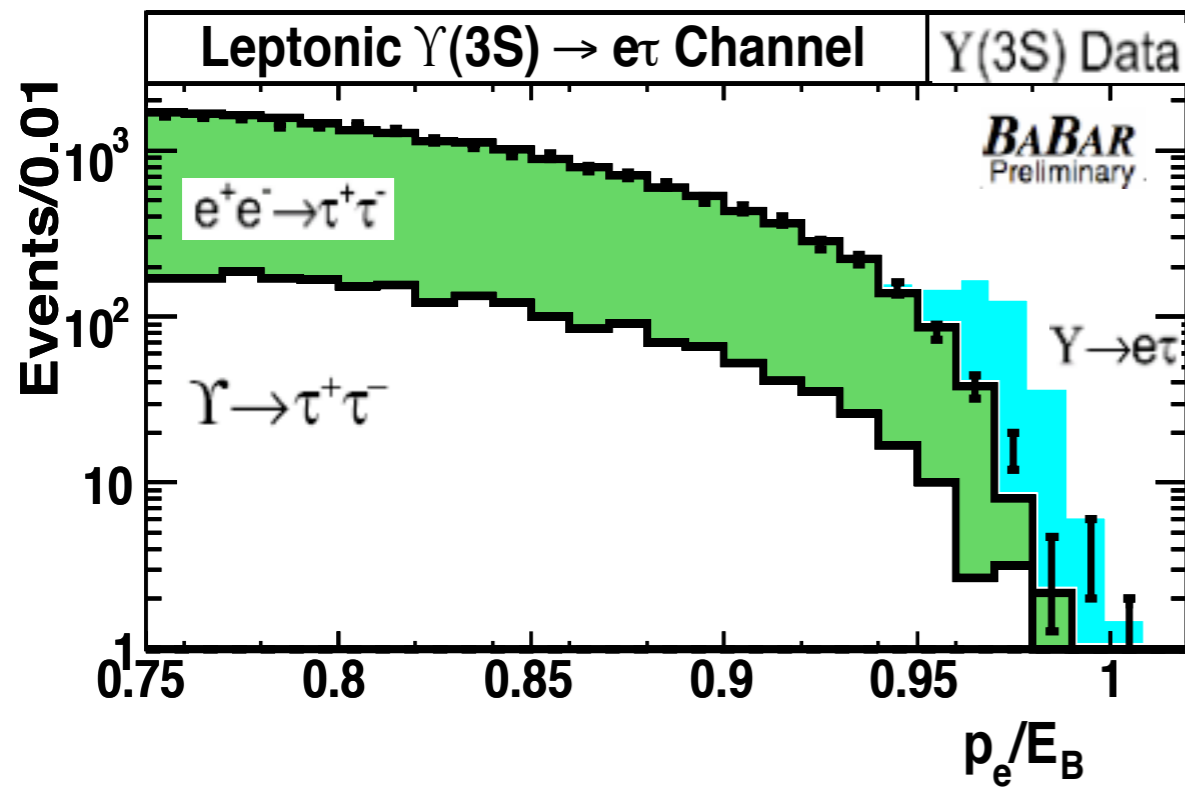
**Signal: peak ~ 0.97**

**Bhabha/Mu-pair Background: peak ~ 1.0**

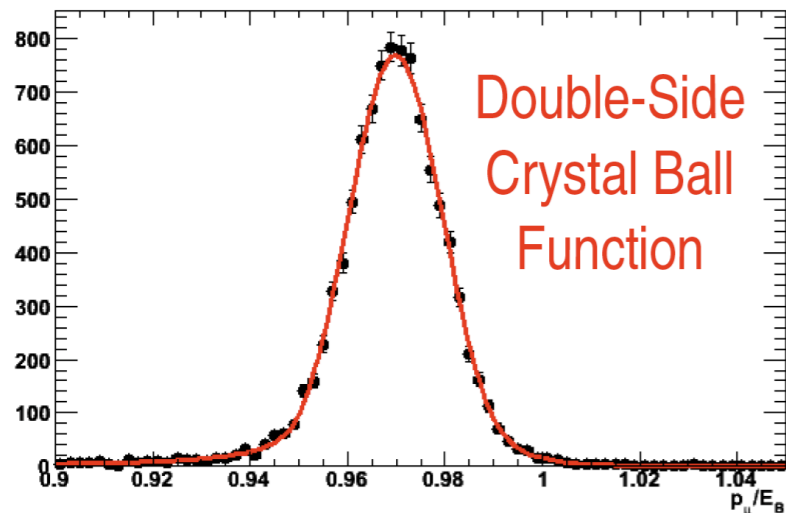


**Tau-pair Background: Kinematic cut-off ~ 0.97**

# The primary lepton momentum spectrum

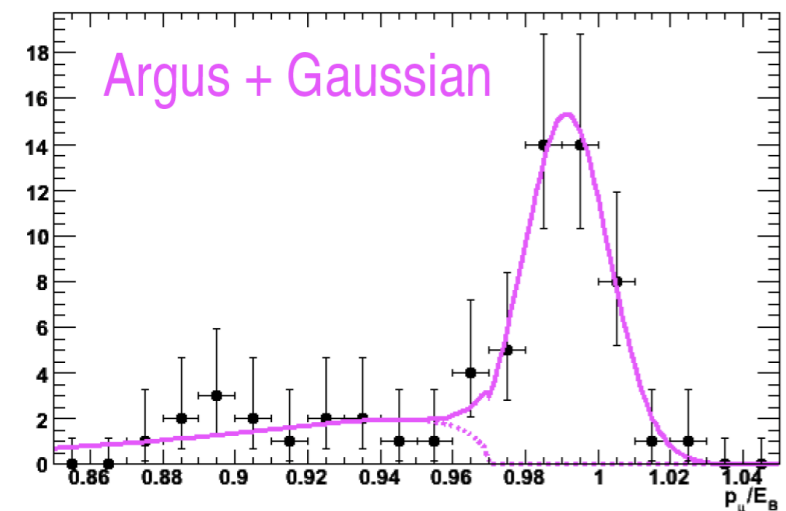


# Signal and background shapes



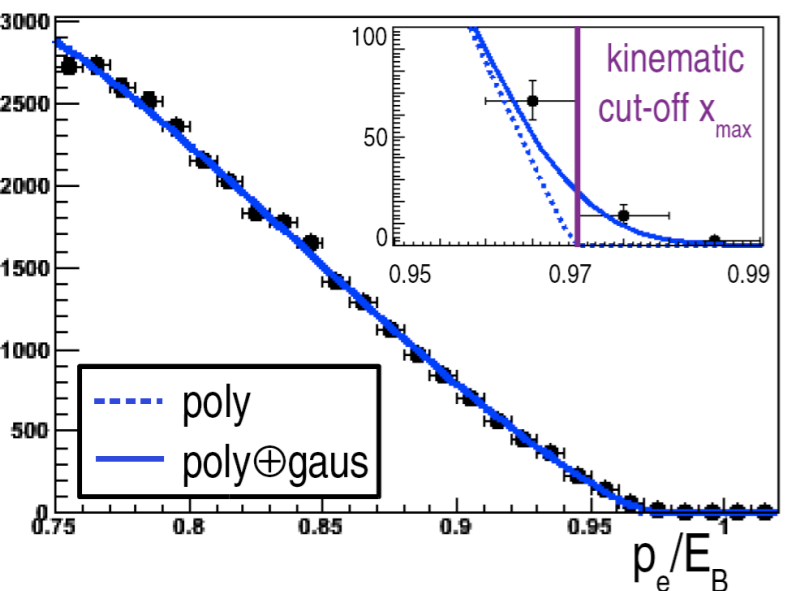
← • Signal PDF: double-sided CB function peaked at  $x=p_1/E_B = 0.97$

– Extract shape from fits to signal MC



← • Bhabha/m-pair Background PDF: Argus threshold function + Gaussian peaked at  $x \approx 1$

– Extract shape from fits to signal MC



← •  $\tau$ -Pair Background PDF: 3rd-order poly  $\oplus$  detector resolution function

–  $\text{poly}(x) = (1-x/x_{\text{MAX}}) + c_2(1-x/x_{\text{MAX}})^2 + c_3(1-x/x_{\text{MAX}})^3$

•  $x_{\text{MAX}}$  = kinematic cutoff parameter: extracted from fit to  $\Upsilon(4S)$  data control sample

•  $c_2, c_3$  = polynomial shape parameters: floated in fit to  $\Upsilon(3S)$  data

– detector resolution function extracted from MC

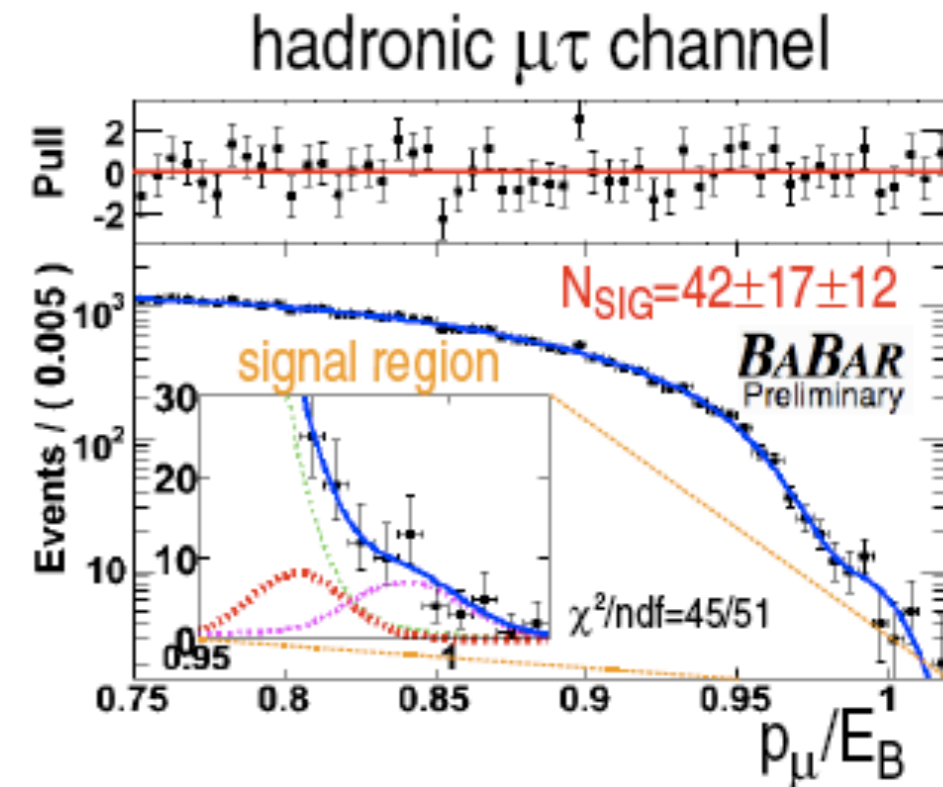
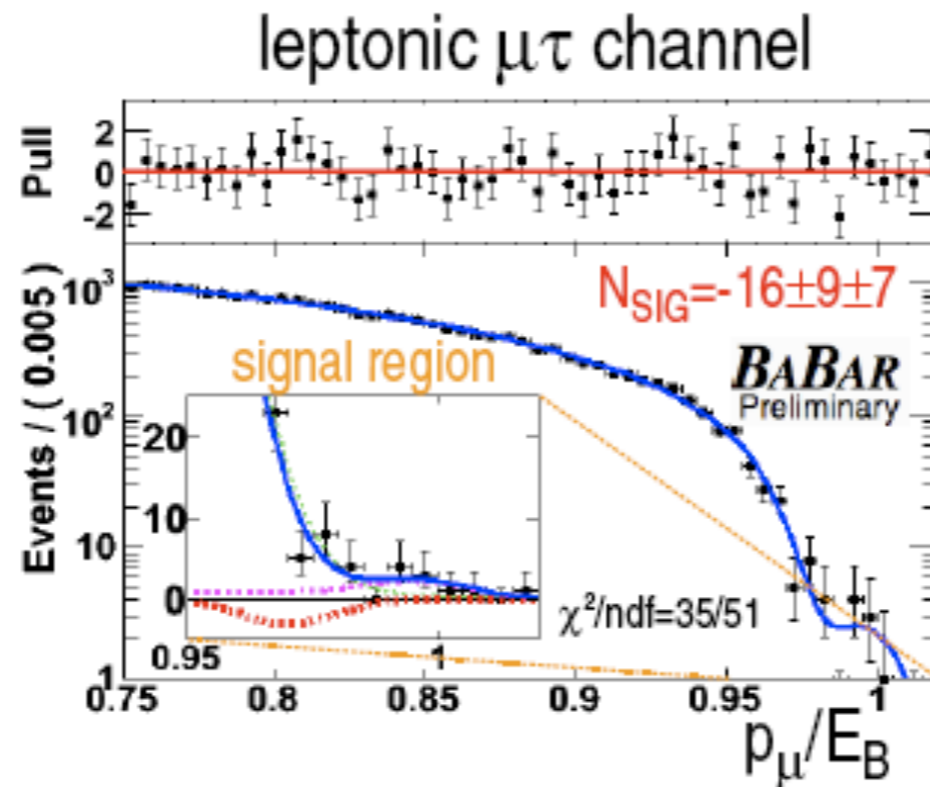
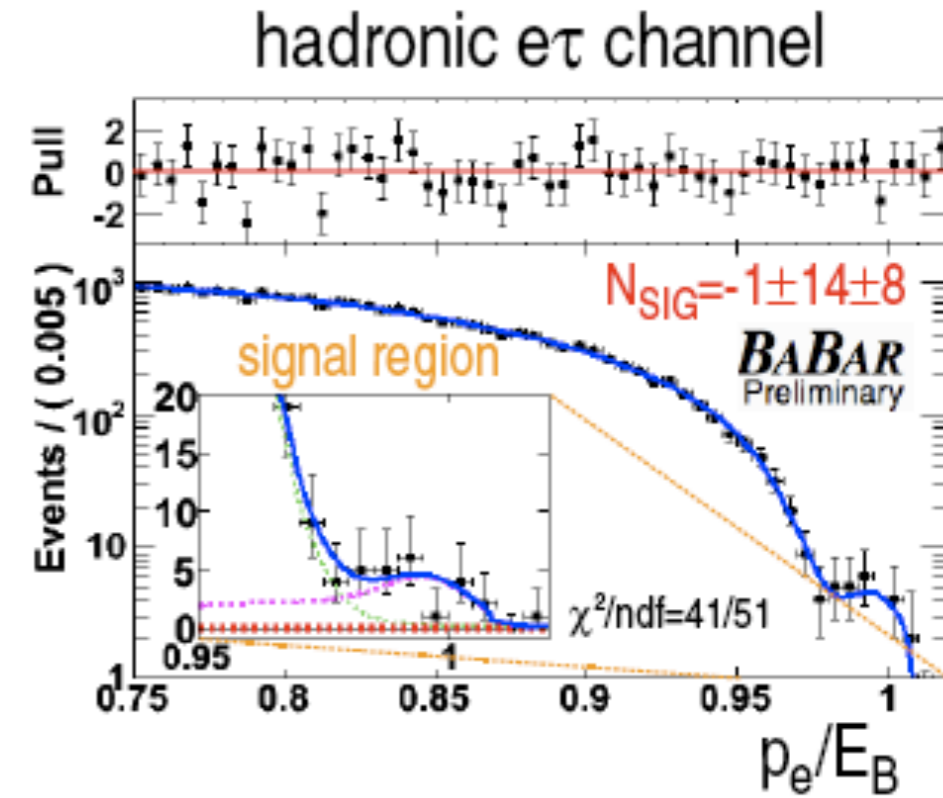
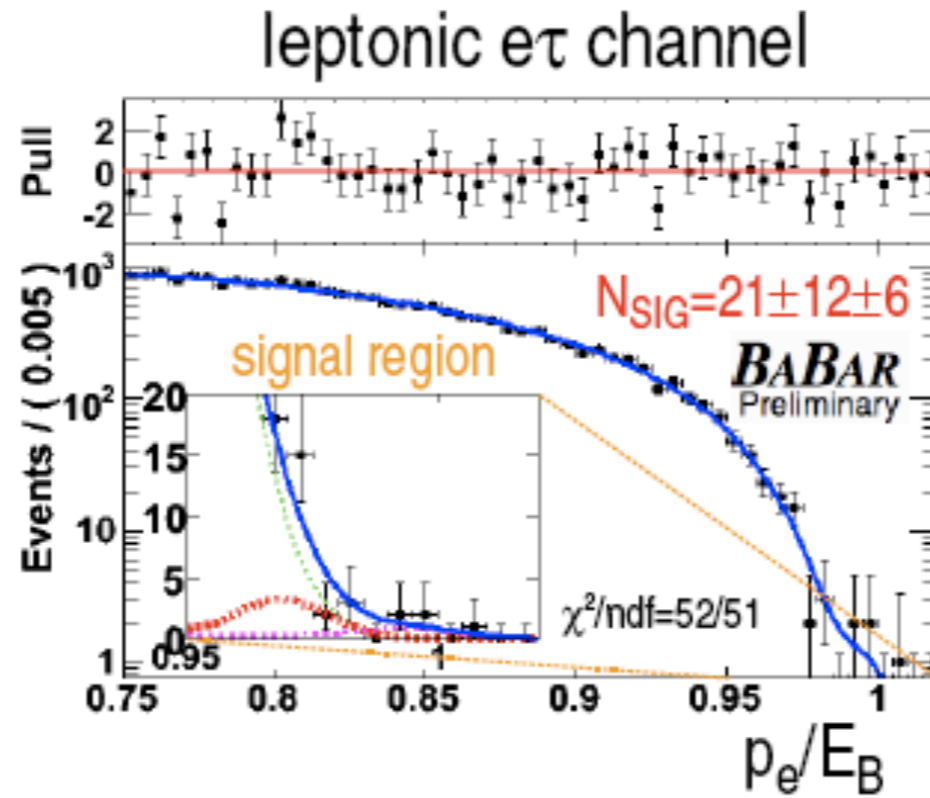
• Global PDF = signal + bhabha ( $\mu$ -pair) +  $\tau$ -Pair components for  $e\tau$  ( $\mu\tau$ ) channels

– Float component yields and polynomial shape parameters in fit to  $\Upsilon(3S)$  data

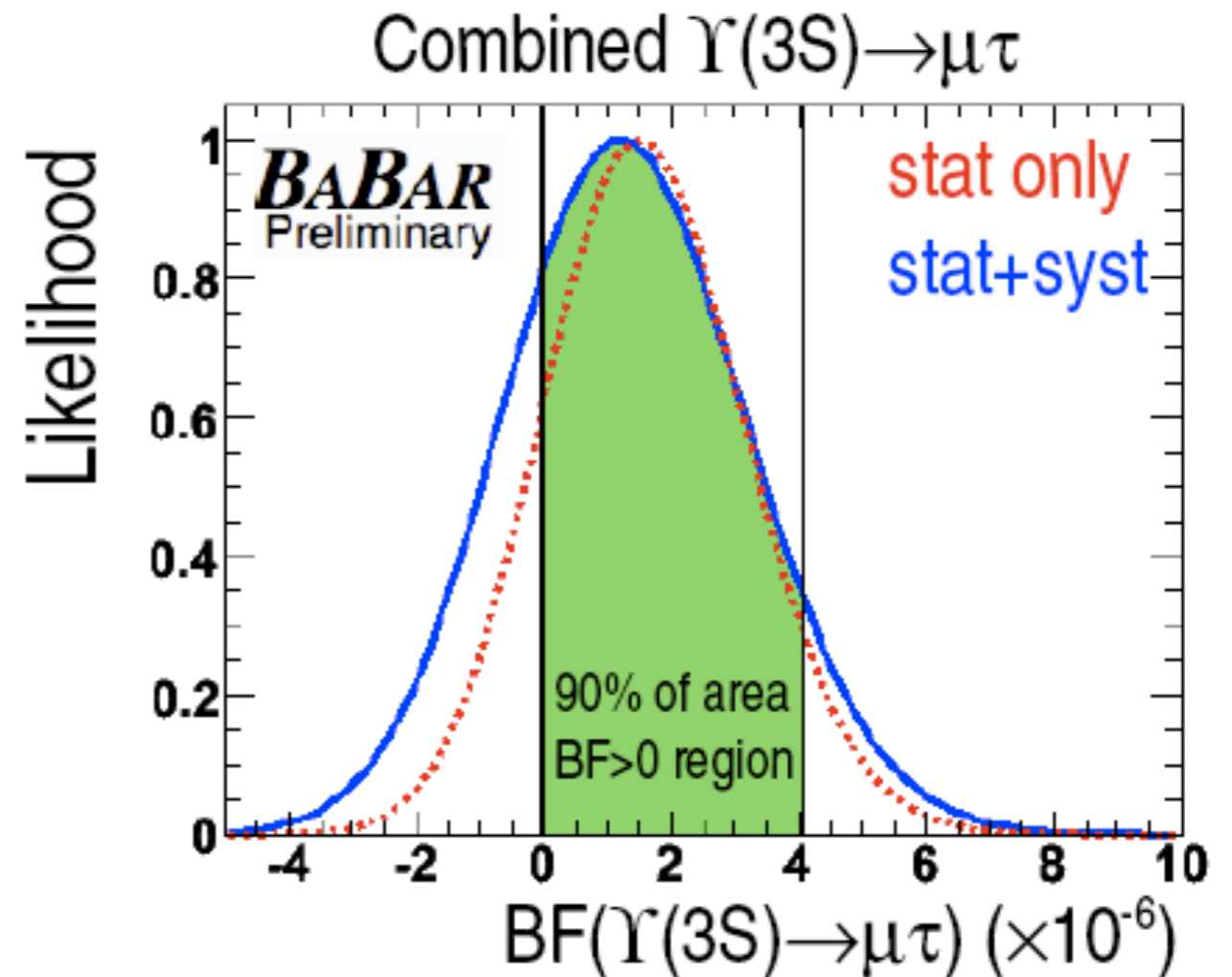
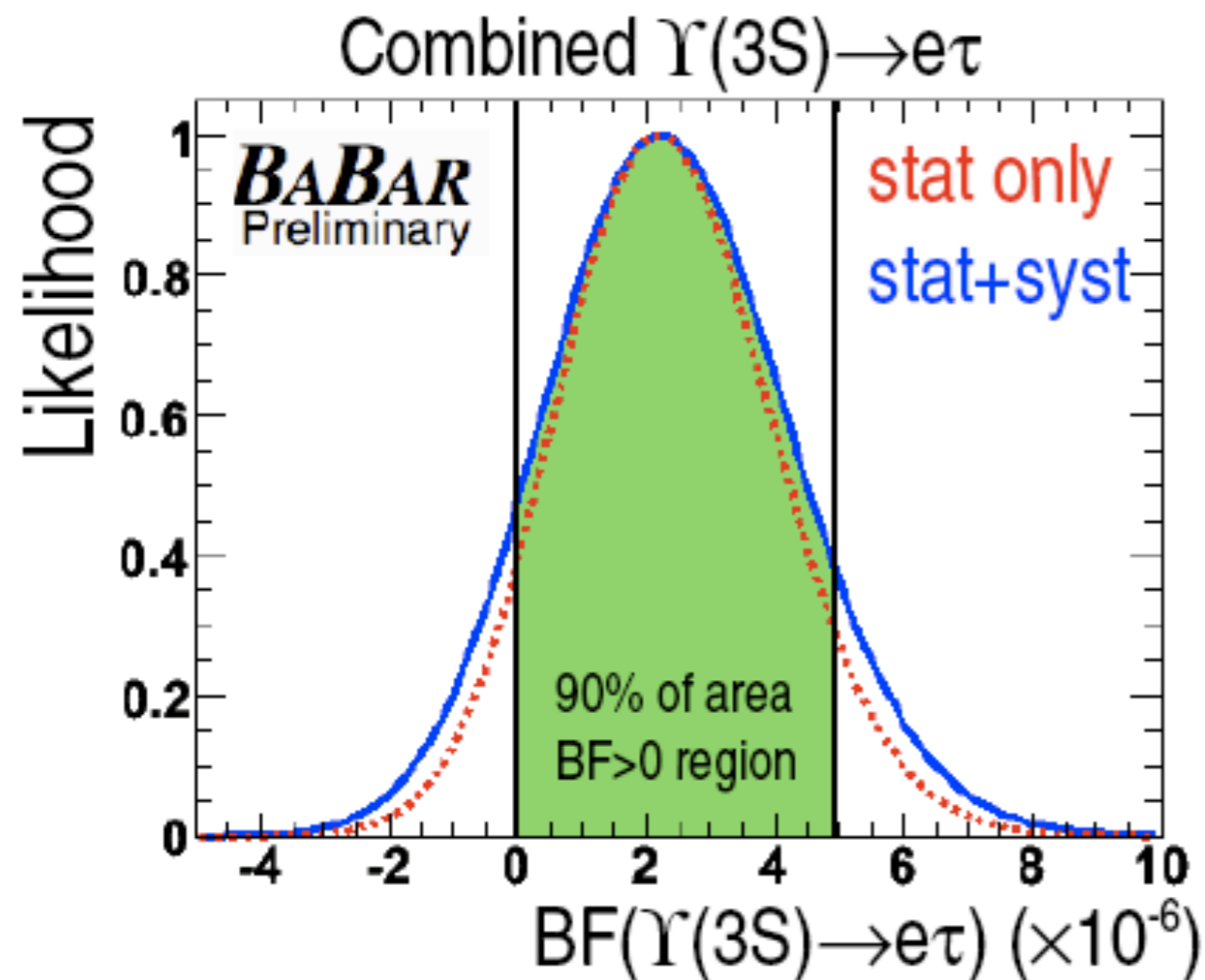
# Fit Results

Global PDF  
 Signal  
 $\tau$ -pair Bkg  
 Bhabha/  
 $\mu$ -pair Bkg

All channels  
give signal  
yield within  
 $\pm 2.1\sigma$  of zero



# BF( $\Upsilon(3S) \rightarrow e\tau, \mu\tau$ ) Upper Limits @ 90% CL



$$\text{BF}(\Upsilon(3S) \rightarrow e\tau) < 5.0 \times 10^{-6}$$

(first upper limit)

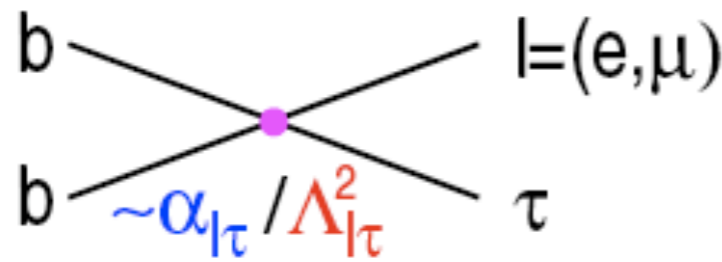
$$\text{BF}(\Upsilon(3S) \rightarrow \mu\tau) < 4.1 \times 10^{-6}$$

(>4x better than previous UL)

BaBar Collab., arXiv: 0812.1021 [hep-ex]

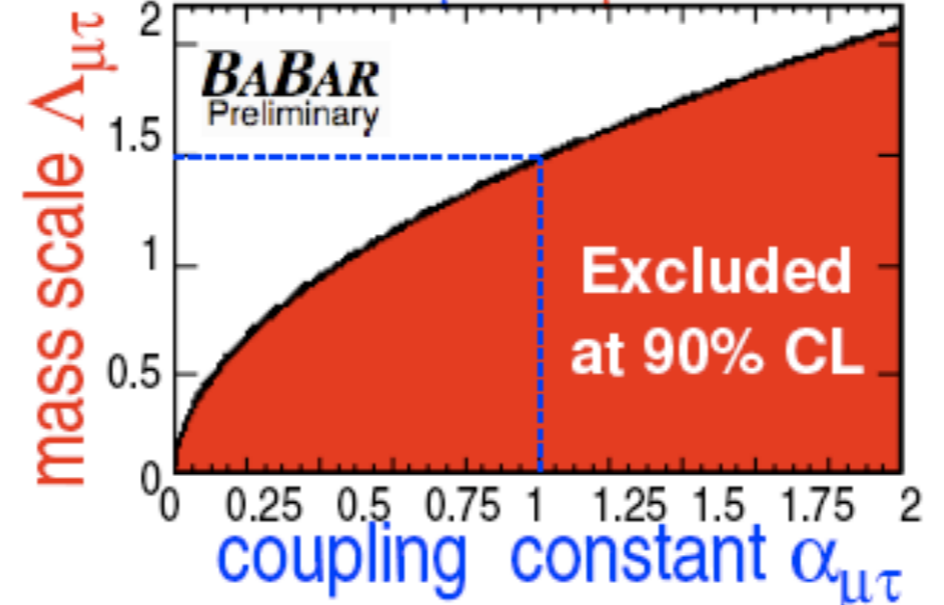
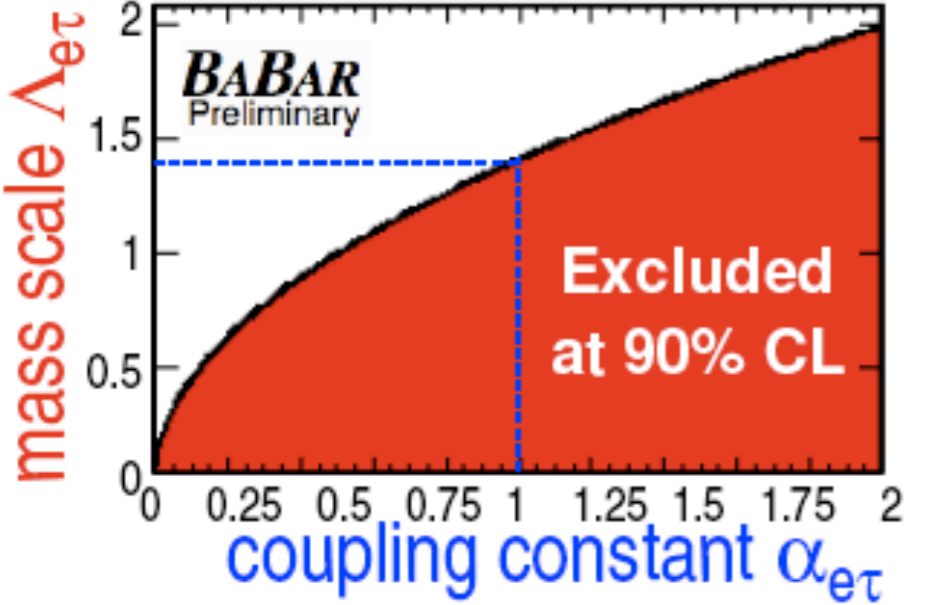
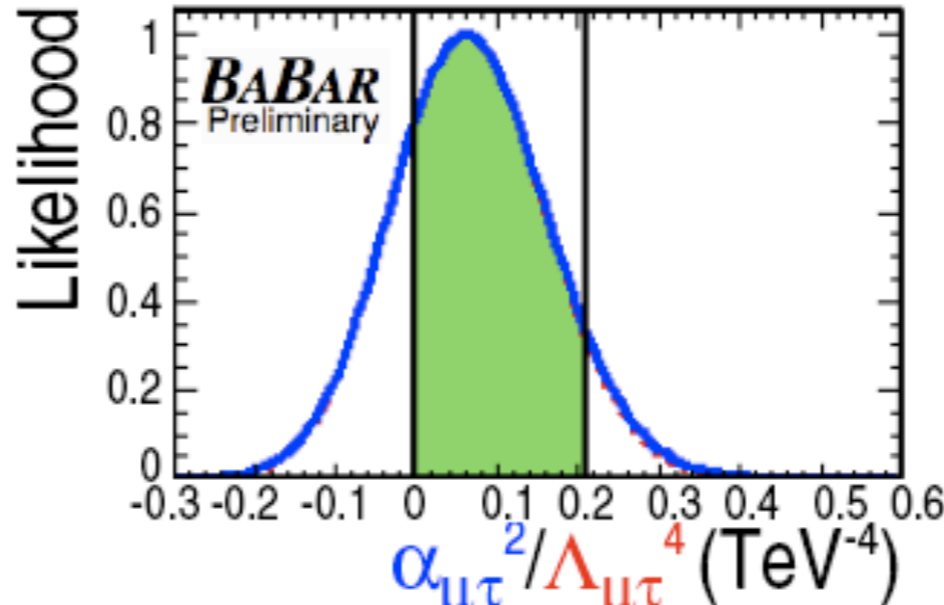
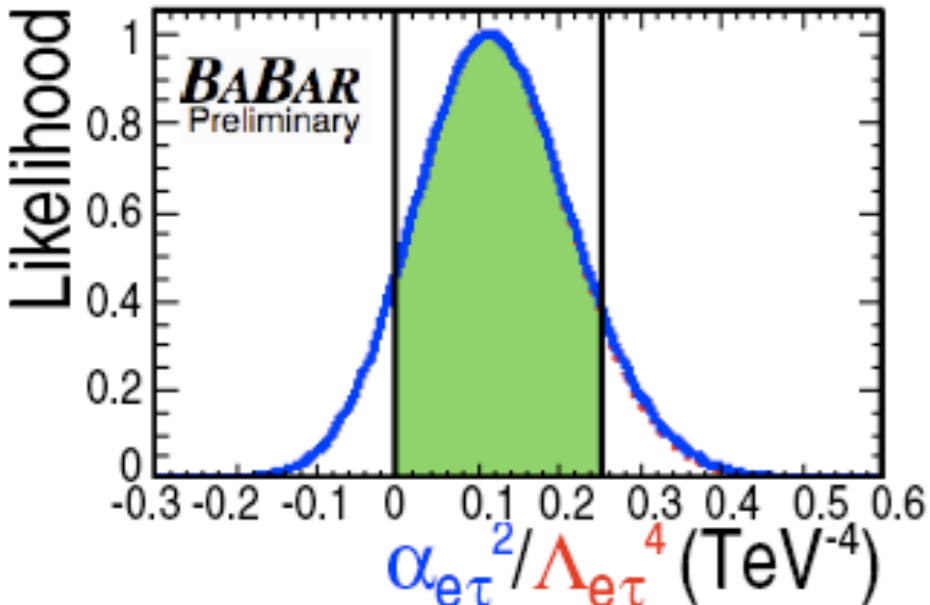


# Limits on Generic Contact Interaction



$$\frac{\Gamma(\Upsilon(3S) \rightarrow l^\pm \tau^\mp)}{\Gamma(\Upsilon(3S) \rightarrow l^+ l^-)} = \frac{1}{2q_b^2} \left( \frac{\alpha_N^{(l\tau)}}{\alpha} \right)^2 \left( \frac{M_{\Upsilon(3S)}}{\Lambda^{(l\tau)}} \right)^4 \quad (l = e, \mu)$$

$q_b = b$  quark charge  
 $\alpha =$  fine structure constant  
 assumes vector coupling  
 Silagadze Phys. Scripta 64.128  
 Black et al. PRD 66.053002



Assume strong coupling  
 $\alpha_{e\tau} = \alpha_{\mu\tau} = 1:$

$$\Lambda_{e\tau} > 1.4 \text{ TeV}$$

$$\Lambda_{\mu\tau} > 1.5 \text{ TeV}$$

# Conclusions

- No evidence of LFV  $\tau$  decays with  $N_\tau \approx 1 \times 10^9$  decays
  - $\mathcal{B}(\tau \rightarrow e\gamma) < 3.3 \times 10^{-8}$  @ 90% C.L.
  - $\mathcal{B}(\tau \rightarrow \mu\gamma) < 4.4 \times 10^{-8}$  @ 90% C.L.
- No evidence of LFV  $\Upsilon$  decays with  $N_{\Upsilon(3S)} \approx 1 \times 10^8$  decays
  - $\mathcal{B}(\Upsilon(3S) \rightarrow e\tau) < 5.0 \times 10^{-6}$  @ 90% C.L.
  - $\mathcal{B}(\Upsilon(3S) \rightarrow \mu\tau) < 4.1 \times 10^{-6}$  @ 90% C.L.
- More results to be available soon with  $\Upsilon(2S)$  decays