

## *Simulation of jet quenching in HIC at CMS*

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- Scientific interest in high- $p_T$  jets and heavy quarks, expected statistics
  - Monte-Carlo model for simulation of jet quenching
  - Example I:  
Medium-modified jet fragmentation in leading particles
  - Example II:  
Medium-modified heavy quark fragmentation in muons
  - Summary
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# *The interest in jet and heavy quark production in HIC*

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1. Detection and studies of properties of quark-gluon plasma.
2. Probing QCD production in media (not in vacuum as in  $pp!$ ).

## Jet observables:

- Jet & leading particle production vs. event centrality
- Jet & leading particle production vs. azimuthal angle
- Jet fragmentation function with leading hadrons
- Photon+jet and  $Z$ +jet correlations

*CMS will provide adequate reconstruction of*  
jets, photons, charged hadrons, centrality and event plane

## Heavy quark observables:

- $B\bar{B} \rightarrow \mu^+ \mu^-$ ,
- $B \rightarrow J/\psi \rightarrow \mu^+ \mu^-$
- $B$ -jet tagged by leading muon

*CMS will provide adequate dimuon reconstruction & primary and secondary vertices*

## *Expected statistics in CMS acceptance*

*(no trigger and reconstruction efficiencies are taken into account)*

Channels including jets  $|\eta^{\text{jet}}, \gamma| < 3, |\eta^h, \mu| < 2.4$

Channel	Observables	Expected 2 week rates, $\sigma_{AA} = A^2\sigma_{pp}, A=\text{Pb}$ (Pythia6.2, CTEQ5M) $L = 5 \times 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$	Shadowing (EKS98)	Jet quenching (in-medium energy loss)
jet+jet, $E_T^{\text{jet}} > 100 \text{ GeV}$	Spectrum suppression, azimuthal anisotropy in non-central collisions	$4 \times 10^6$	negligible	up to factor $\sim 10$
jet tagged by $h^\pm, \pi^0$ , $E_T^{\text{jet}} > 100 \text{ GeV}, z^{h^\pm, \pi^0} > 0.5$	Softening of jet fragmentation	$2 \times 10^5$	negligible	up to factor $\sim 5$
$B$ -jet tagged by $\mu$ , $E_T^{\text{jet}} > 100 \text{ GeV}, z^\mu > 0.3$ $E_T^{\text{jet}} > 50 \text{ GeV}, z^\mu > 0.3$	Softening of jet fragmentation	700 $2 \times 10^4$	negligible	up to factor $\sim 2$

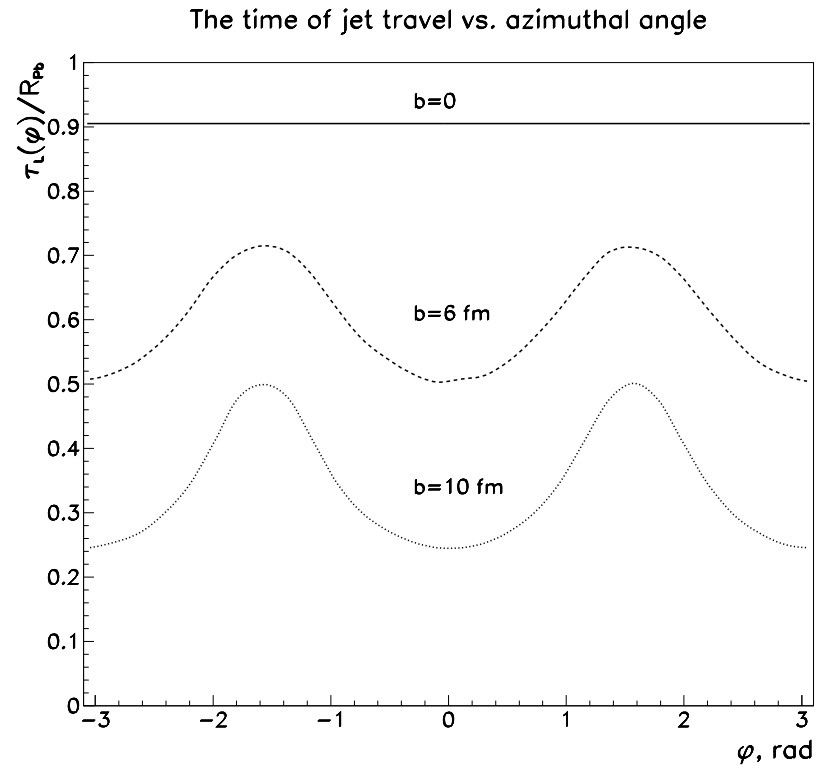
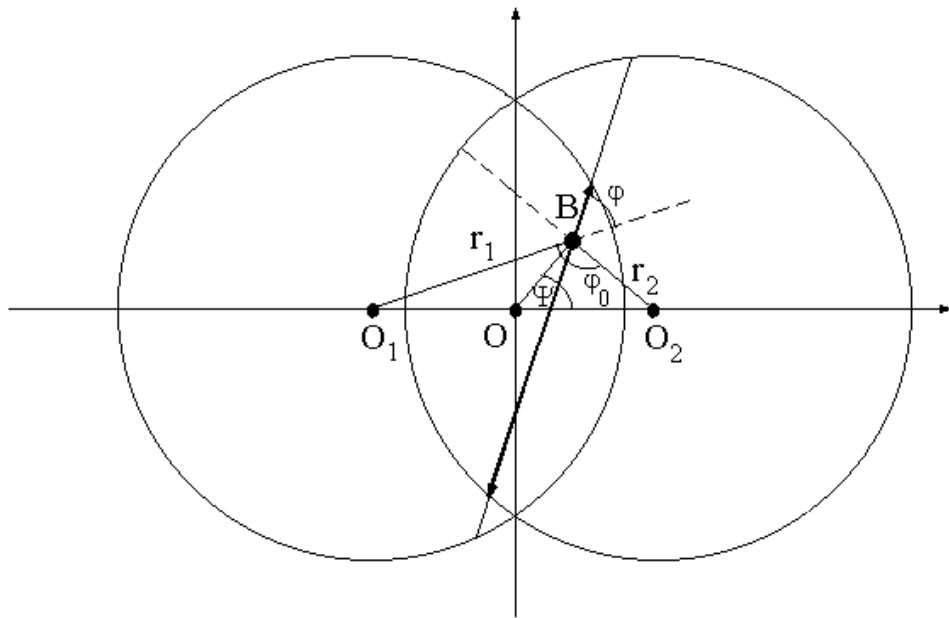
Channels including heavy quarks in dimuon modes  $|\eta^\mu| < 2.4$

Channel	Observables	Expected 2 week rates, $\sigma_{AA} = A^2\sigma_{pp}, A=\text{Pb}$ (Pythia6.1, CTEQ5M) $L = 5 \times 10^{26} \text{ cm}^{-2} \text{ s}^{-1}$	Shadowing (EKS98)	Jet quenching (in-medium energy loss)
$BB \rightarrow \mu^+\mu^-$ , $M_{\mu^+\mu^-} > 20 \text{ GeV}$ , $p_t^\mu > 5 \text{ GeV}$	Spectrum suppression	$2.7 \times 10^4$	15%	up to factor $\sim 4$
$B \rightarrow J/\Psi \rightarrow \mu^+\mu^-$ , $p_t^\mu > 5 \text{ GeV}$	Spectrum suppression	$1.0 \times 10^4$	30%	up to factor $\sim 2$

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# *Nuclear geometry of jet quenching*

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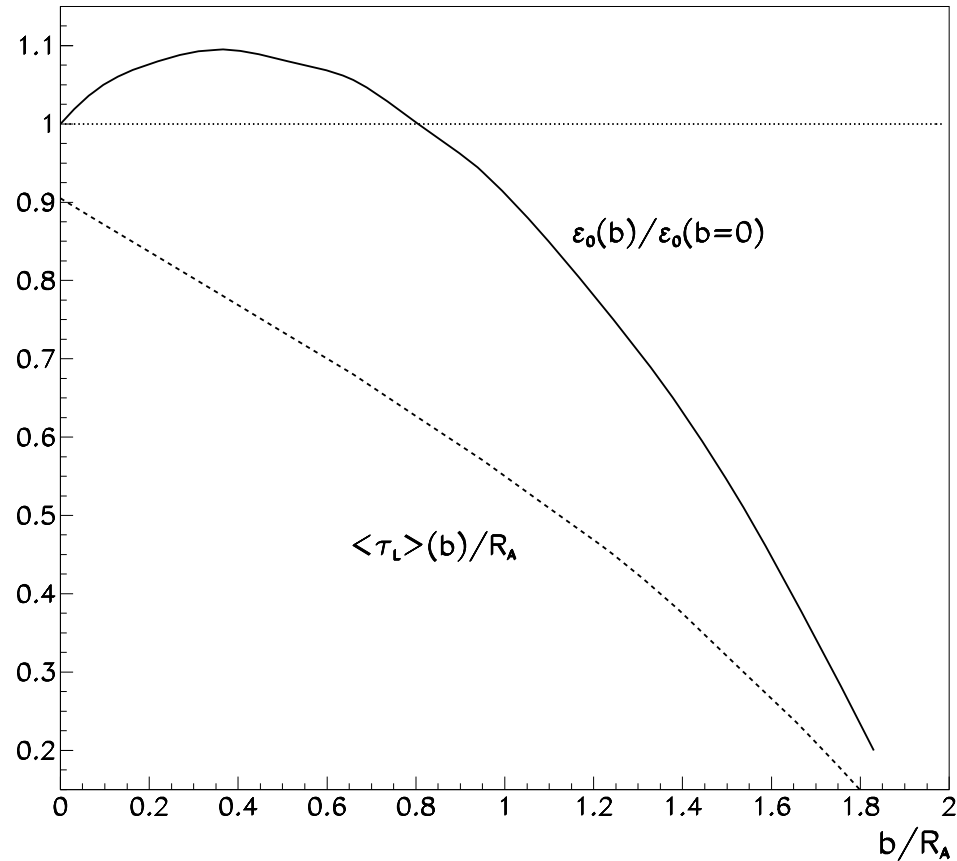
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**Jet partons lose energy in azimuthally asymmetric volume of quark-gluon plasma**

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# Initial energy density and jet path length vs. centrality

Initial energy density  $\epsilon_0$  and mean jet path length  $\langle \tau_L \rangle$



$$\epsilon_0(\mathbf{b}) \propto \mathbf{T}_{AA}(\mathbf{b})/\mathbf{S}_{AA}(\mathbf{b})$$

Nuclear overlap function:  $\mathbf{T}_{AA}(\mathbf{b}) = \int_0^{2\pi} d\psi \int_0^{r_{\max}} r dr \mathbf{T}_A(\mathbf{r}_1) \mathbf{T}_A(\mathbf{r}_2)$ ,  $\mathbf{T}_A(\vec{r}) = \int_{-\infty}^{+\infty} \rho_A(\vec{r}, z) dz$

Transverse area of dense zone:  $\mathbf{S}_{AA}(\mathbf{b}) = \int_0^{2\pi} d\psi \int_0^{r_{\max}} r dr = \left( \pi - 2 \arcsin \frac{b}{2R_A} \right) R_A^2 - b \sqrt{R_A^2 - \frac{b^2}{4}}$

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## *In-medium partonic energy loss*

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*General kinetic integral equation:*

$$\Delta E(L, E) = \int_0^L dx \frac{dP}{dx}(x) \lambda(x) \frac{dE}{dx}(x, E), \quad \frac{dP}{dx}(x) = \frac{1}{\lambda(x)} \exp(-x/\lambda(x))$$


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1. *Collisional loss*

$$\nu = \left\langle \frac{t}{2m_0} \right\rangle = \frac{1}{2} \left\langle \frac{1}{m_0} \right\rangle \cdot \langle t \rangle \simeq \frac{1}{4T\sigma_{ab}} \int_{\mu_D^2}^{t_{\max}} dt \frac{d\sigma_{ab}}{dt} t$$

$$\frac{d\sigma_{ab}}{dt} \simeq C_{ab} \frac{2\pi\alpha_s^2(t)}{t^2}, \quad \alpha_s = \frac{12\pi}{(33-2N_f) \ln(t/\Lambda_{\text{QCD}}^2)}, \quad C_{ab} = 9/4, 1, 4/9 - gg, gq, qq$$

2. *Radiative loss* (R. Baier, Yu.L. Dokshitzer, A. Mueller, D. Schiff. NPB 531 (1998) 403)

$$\left. \frac{dE}{dx} \right|_{m_q=0} = \frac{2\alpha_s C_F}{\pi\tau_L} \int_{E_{\text{LPM}} \sim \lambda_g \mu_D^2}^E d\omega \left[ 1 - y + \frac{y^2}{2} \right] \ln |\cos(\omega_1 \tau_1)|,$$

$$\omega_1 = \sqrt{i \left( 1 - y + \frac{C_F}{3} y^2 \right) \bar{\kappa} \ln \frac{16}{\bar{\kappa}}}, \quad \bar{\kappa} = \frac{\mu_D^2 \lambda_g}{\omega(1-y)}, \quad \tau_1 = \frac{\tau_L}{2\lambda_g}, \quad y = \frac{\omega}{E}, \quad C_F = \frac{4}{3}$$

Yu.L. Dokshitzer and D. Kharzeev, PLB 519 (2001) 199 (“dead cone” approximation) :

$$\left. \frac{dE}{dx} \right|_{m_q \neq 0} = \frac{1}{(1 + (l\omega)^{3/2})^2} \left. \frac{dE}{dx} \right|_{m_q=0}, \quad l = \left( \frac{\lambda}{\mu_D^2} \right)^{1/3} \left( \frac{m_q}{E} \right)^{4/3}$$


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## Simulation of parton rescattering in QGP

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- The initial parton spectrum is generated with **PYTHIA**
- The transverse distance between scatterings,  $l_i = (\tau_{i+1} - \tau_i)E/p_T$ :

$$\frac{dP}{dl_i} = \lambda^{-1}(\tau_{i+1}) \exp\left(-\int_0^{l_i} \lambda^{-1}(\tau_i + s) ds\right), \quad \lambda_a^{-1} = \sum_b \sigma_{ab} \rho_b$$

- The scattering cross section  $d\sigma/dt$ :

$$\frac{d\sigma_{ab}}{dt} \cong C_{ab} \frac{2\pi\alpha_s^2(t)}{t^2}, \quad \alpha_s = \frac{12\pi}{(33 - 2N_f) \ln(t/\Lambda_{\text{QCD}}^2)}, \quad C_{ab} = 9/4, 1, 4/9 - gg, gq, qq$$

- Radiative and collisional energy loss per scattering  $i$ :

$$\Delta E_{\text{tot},i} = \Delta E_{\text{rad},i} + \Delta E_{\text{col},i}$$

- Transverse momentum kick per scattering  $i$ :

$$\Delta k_{t,i}^2 = \left(E - \frac{t_i}{2m_{0i}}\right)^2 - \left(p - \frac{E}{p} \frac{t_i}{2m_{0i}} - \frac{t_i}{2p}\right)^2 - m_q^2$$

- The final spectrum is generated after hadronization with **JETSET**
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## *Medium-modified jet fragmentation*

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*Experimentally observable jet fragmentation function:*

$$D(z) \equiv \int_{z p_{T,\min}^{\text{jet}}} d(p_T^h)^2 dy \frac{dN_{AA}^{h(k)}}{d(p_T^h)^2 dy dz} / \int_{p_{T,\min}^{\text{jet}}} dp_T^2 dy \frac{dN_{AA}^{\text{jet}(k)}}{dp_T^2 dy}$$

*Experimentally observable integrated jet suppression factor:*

$$Q^{\text{jet}}(p_{T,\min}^{\text{jet}}) \equiv \int_{p_{T,\min}^{\text{jet}}} dp_T^2 dy \frac{dN_{AA}^{\text{jet}(k)}}{dp_T^2 dy} / \int_{p_{T,\min}^{\text{jet}}} dp_T^2 dy \frac{dN_{AA}^{\text{jet}(k)}}{dp_T^2 dy} (\Delta p_T^{\text{jet}} = 0).$$

*Rate of jets of cone size  $\theta_0$  at impact parameter  $b$ :*

$$\frac{dN_{AA}^{\text{jet}(k)}}{dp_T^2 dy}(b) = \int_0^{2\pi} d\psi \int_0^{r_{\max}} r dr T_A(r_1) T_A(r_2) \frac{d\sigma^{\text{jet}(k)}(p_T + \Delta p_T^{\text{jet}}(r, \psi, \theta_0))}{dp_T^2 dy}$$

*Rate of “jet-induced” hadrons at impact parameter  $b$ :*

$$\frac{dN_{AA}^{h(k)}}{d(p_T^h)^2 dy dz}(b) = \int_0^{2\pi} d\psi \int_0^{r_{\max}} r dr T_A(r_1) T_A(r_2) \frac{d\sigma^{\text{jet}(k)}(p_T + \Delta p_T(r, \psi))}{dp_T^2 dy} \frac{1}{z^2} D_k^h(z, p_T^2)$$

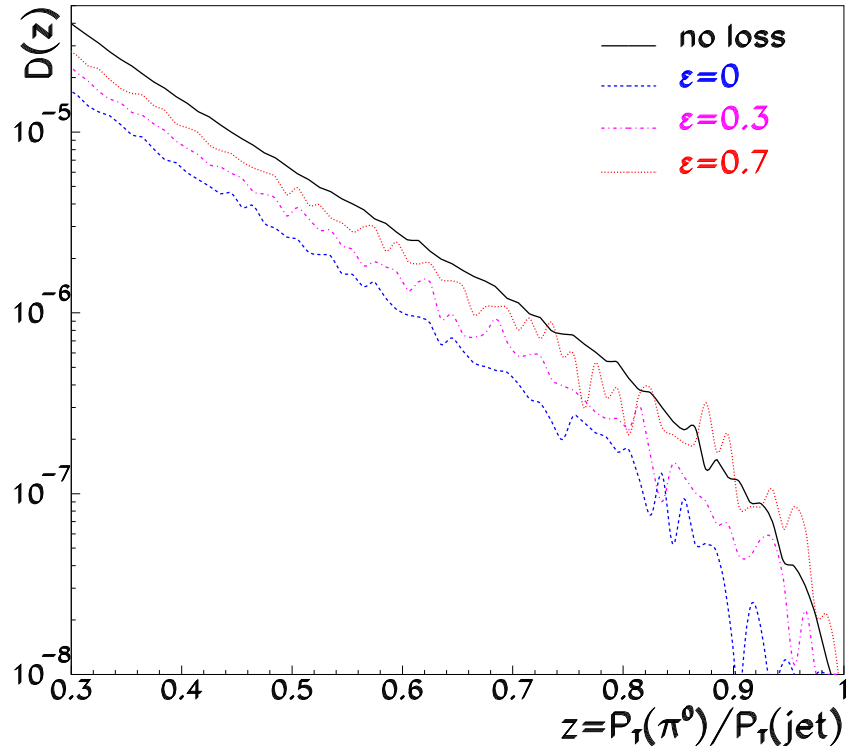
$D_k^h(z, Q^2)$  and  $\frac{d\sigma^{\text{jet}(k)}}{dp_T^2 dy}$  are fragmentation function and jet cross section in vacuum.

$\Delta p_T^{\text{jet}}(\theta_0)$  and  $\Delta p_T$  are medium-induced shifts of jet and hadron  $p_T$ -spectrum.

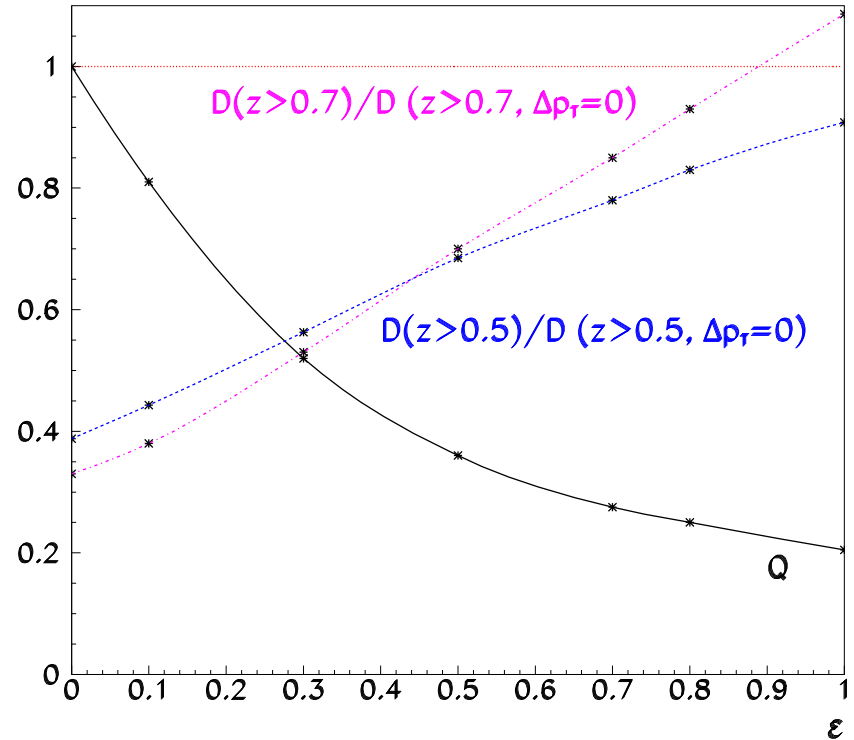


# Jet fragmentation function with leading $\pi^0$ , $h^\pm$

JFF in Pb–Pb at  $\sqrt{s}=5.5A$  TeV,  $E_T > 100$  GeV



JFF in Pb–Pb at  $\sqrt{s}=5.5A$  TeV,  $E_T > 100$  GeV

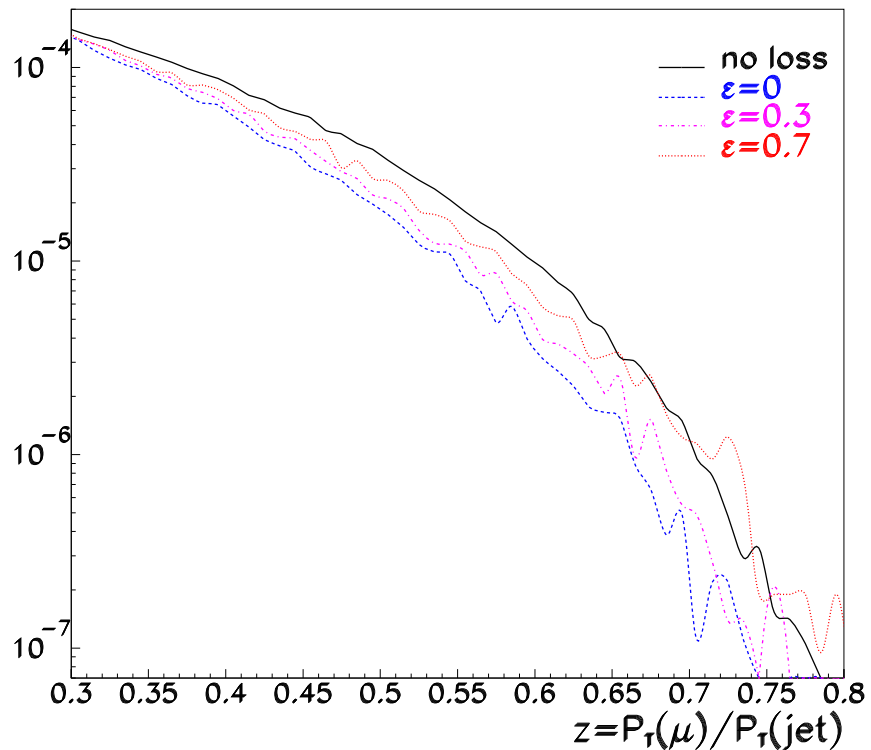


I.P. Lokhtin and A.M. Snigirev, hep-ph/0303121, Phys. Lett. B, in press

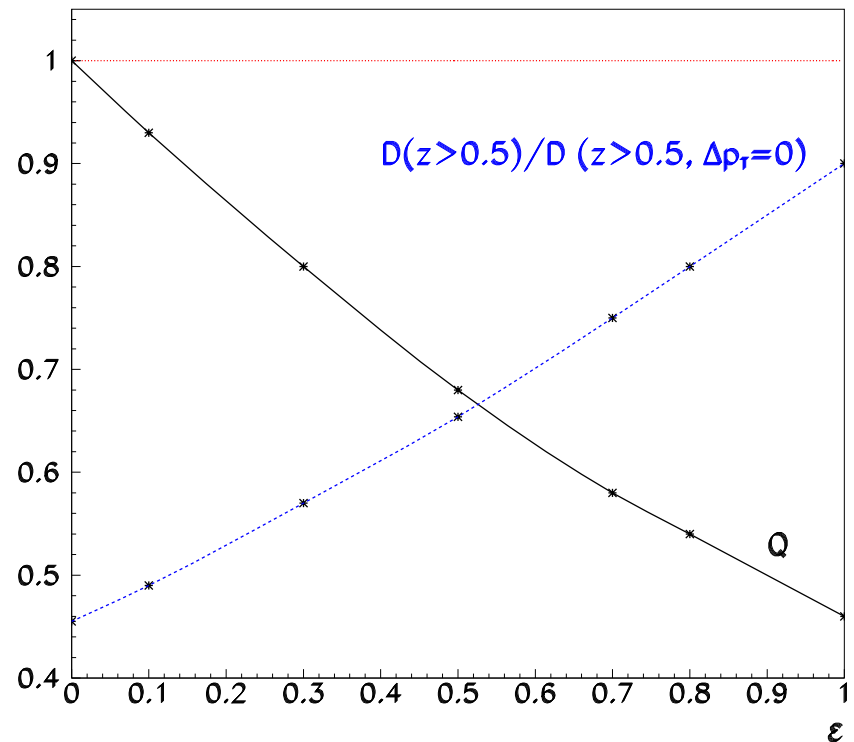
modification of jet fragmentation function crucially depends on the fraction  $\epsilon$  of jet energy loss falling outside the typical jet cone (and being truly lost to the jet).

# *B-jet fragmentation function with leading $\mu$*

B JFF in Pb–Pb at  $\sqrt{s}=5.5A$  TeV,  $E_T > 50$  GeV



B JFF in Pb–Pb at  $\sqrt{s}=5.5A$  TeV,  $E_T > 50$  GeV



modification of  $\mu$ -tagged B-jet fragmentation function also depends on the fraction  $\varepsilon$  of jet energy loss falling outside the typical jet cone.

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# Heavy quark fragmentation effects on dimuon spectra

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## Signal I:

$$b\bar{b} \rightarrow B\bar{B} \rightarrow \mu^+\mu^-X \quad (c\tau_{B^\pm} = 496\mu\text{m}, \quad c\tau_{B^0} = 464\mu\text{m})$$

$$c\bar{c} \rightarrow D\bar{D} \rightarrow \mu^+\mu^-X \quad (c\tau_{D^\pm} = 300\mu\text{m}, \quad c\tau_{D^0} = 124\mu\text{m})$$

## Background I: ( $M_{\mu^+\mu^-} \gtrsim 10 \text{ GeV}/c^2$ )

$$q\bar{q} \rightarrow \mu^+\mu^-$$

Drell-Yan

$$\pi^\pm, K^\pm \rightarrow \mu^\pm\nu(\bar{\nu}) \quad \text{Combinatorial background (subtracted using like-sign spectra)}$$

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## Signal II:

$$b\bar{b} \rightarrow BX \rightarrow J/\psi X \rightarrow \mu^+\mu^-X$$

## Background II: ( $M_{\mu^+\mu^-} \sim 3.1 \text{ GeV}/c^2$ )

$$gg \rightarrow J/\psi \rightarrow \mu^+\mu^- \quad \text{primary } J/\psi$$

$$\pi^\pm, K^\pm \rightarrow \mu^\pm\nu(\bar{\nu}) \quad \text{Combinatorial background (subtracted using like-sign spectra)}$$

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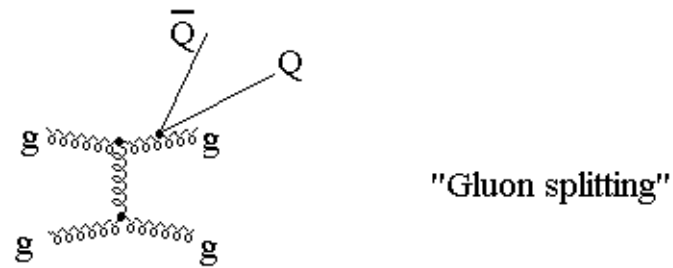
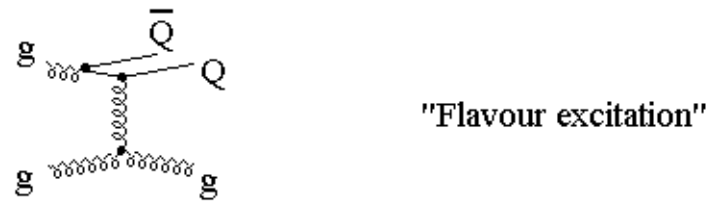
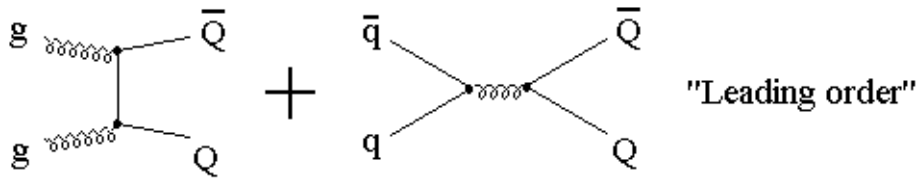
*Linear superposition of independent nucleon-nucleon sub-collisions (no collective effects):*

$$\sigma_{AA}^h = A^2\sigma_{pp}^h$$

**Nuclear collective effects (initial and final state) will modify dimuon rates & spectra**

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# Heavy quark production at very high energies

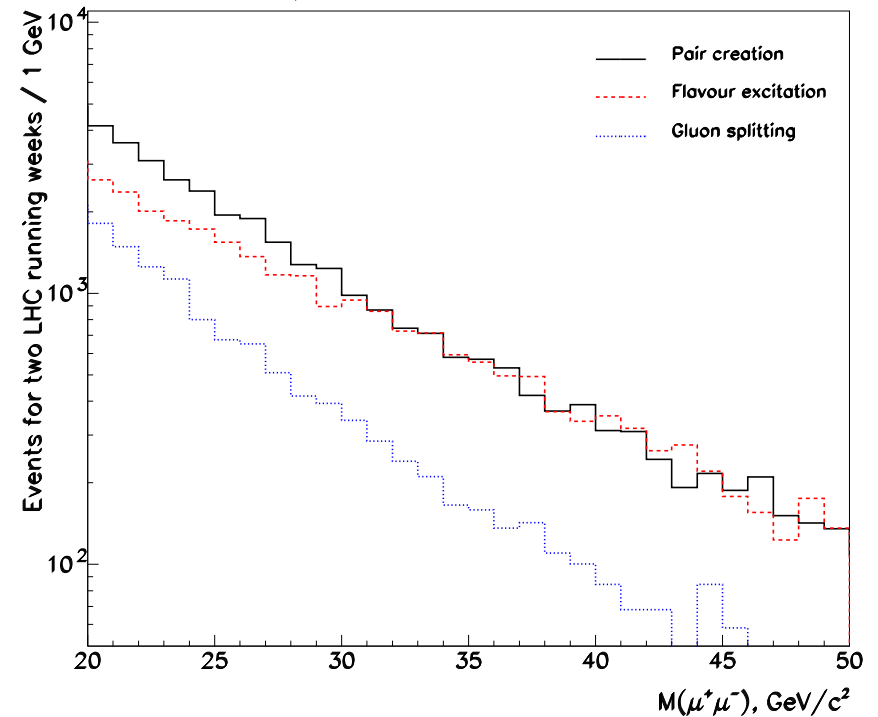


E. Norrbin, T. Sjöstrand, EPJ C 17 (2000) 137:

1. The "flavour excitation" and "gluon splitting" contributions in PYTHIA important and can dominate at LHC;
2. The single quark spectra are similar for all three contributions but the  $Q\bar{Q}$  correlations are different.

Invariant mass distribution of  $\mu^+\mu^-$  pairs in Pb-Pb,  $\sqrt{s}=5.5A$  TeV

Initial production from b bbar



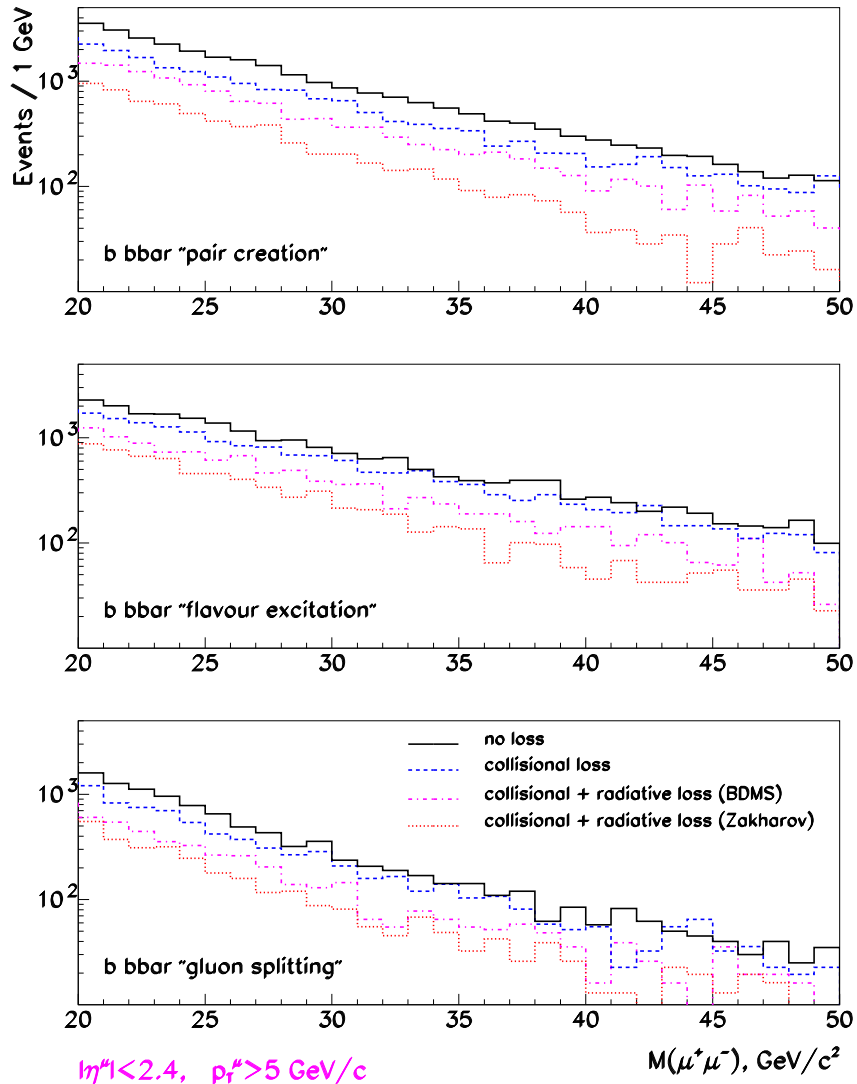
$|\eta^*| < 2.4, p_T^* > 5 \text{ GeV}/c$

(PYTHIA prediction)

I. Lokhtin, A. Snigirev, NPA 702 (2002) 346

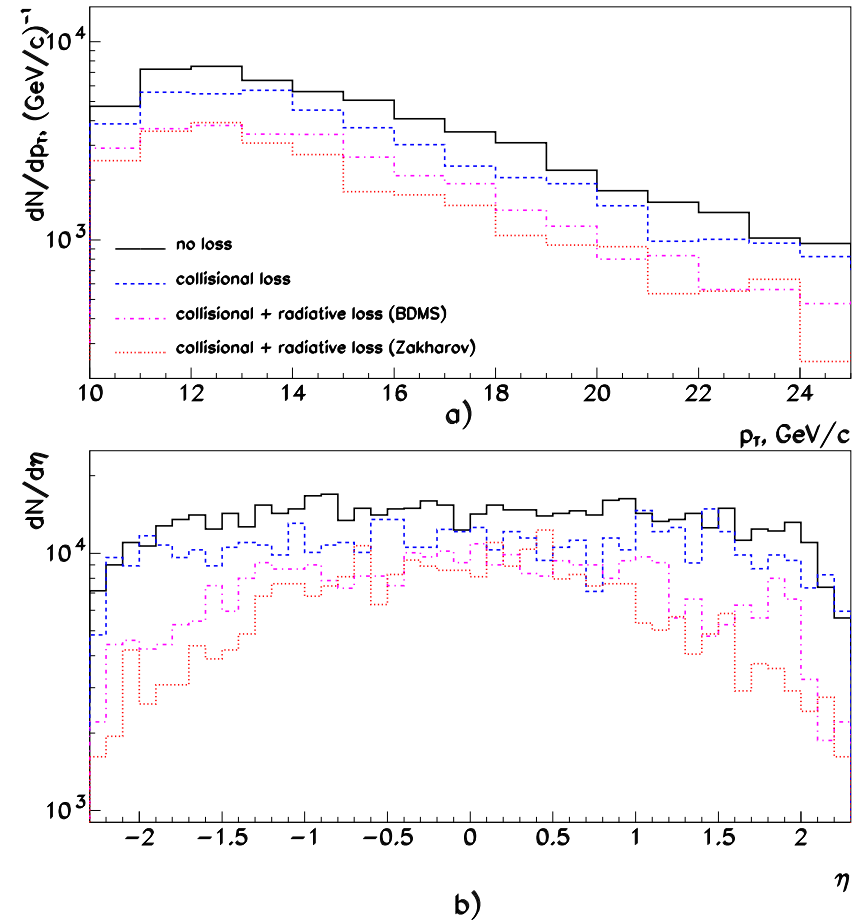
# B-fragmentation: $B\bar{B} \rightarrow \mu^+\mu^-$ and $B \rightarrow J/\psi \rightarrow \mu^+\mu^-$

Invariant mass distribution of  $\mu^+\mu^-$  in Pb–Pb,  $\sqrt{s}=5.5A$  TeV

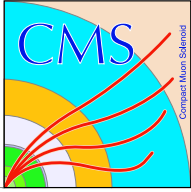


$p_T$  and  $\eta$  distributions of  $J/\psi (\rightarrow \mu^+\mu^-)$  from B-decay in Pb–Pb

## NUCLEAR SHADOWING + ENERGY LOSSES



I. Lokhtin, A. Snigirev, EPJ C 21 (2001) 155; JPG 27 (2001) 2365; CERN CMS Note 2001/008; NPA 702 (2002) 346 – see for details.



## *Jet quenching in HIC at CMS: Summary*

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Monte-Carlo studies show that CMS is well suited to observe and analyze jet quenching in various channels

### Leading particles in jet:

- medium-modified jet fragmentation function can be measured (with fine jet,  $\pi^0$  and charged hadron reconstruction)
- medium-modified  $b$ -quark fragmentation function can be measured (with fine jet and single muon reconstruction)

### Heavy quarks:

- medium-modified spectra of high-mass dimuons from semileptonic  $B\bar{B}$  decays and secondary  $J/\psi$ 's from single  $B$  can be observed (with fine dimuon and event vertex reconstruction)