

Lecture # 3

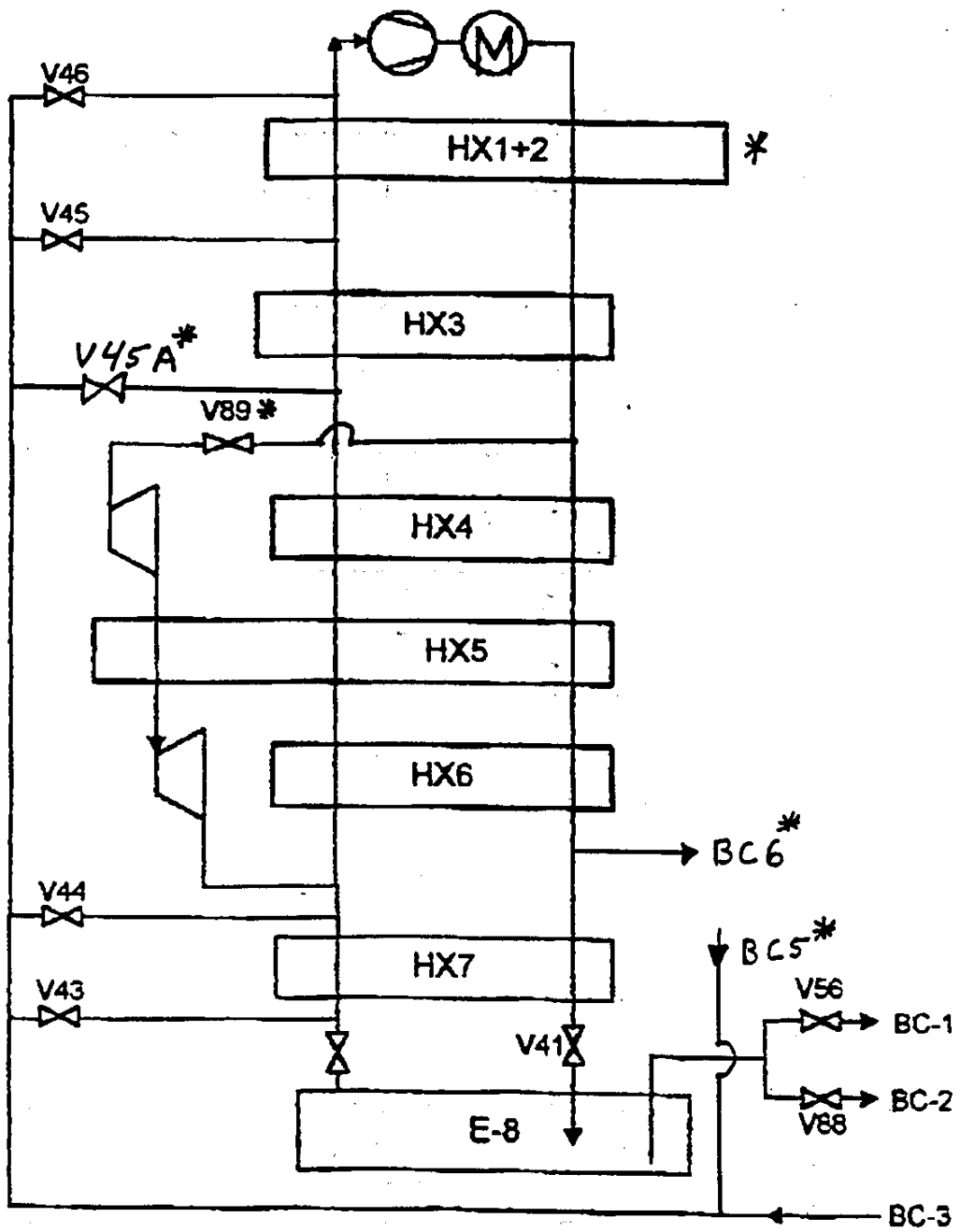
Refrigeration (Part II) & He II

I) Refrigeration

Collins Cycle

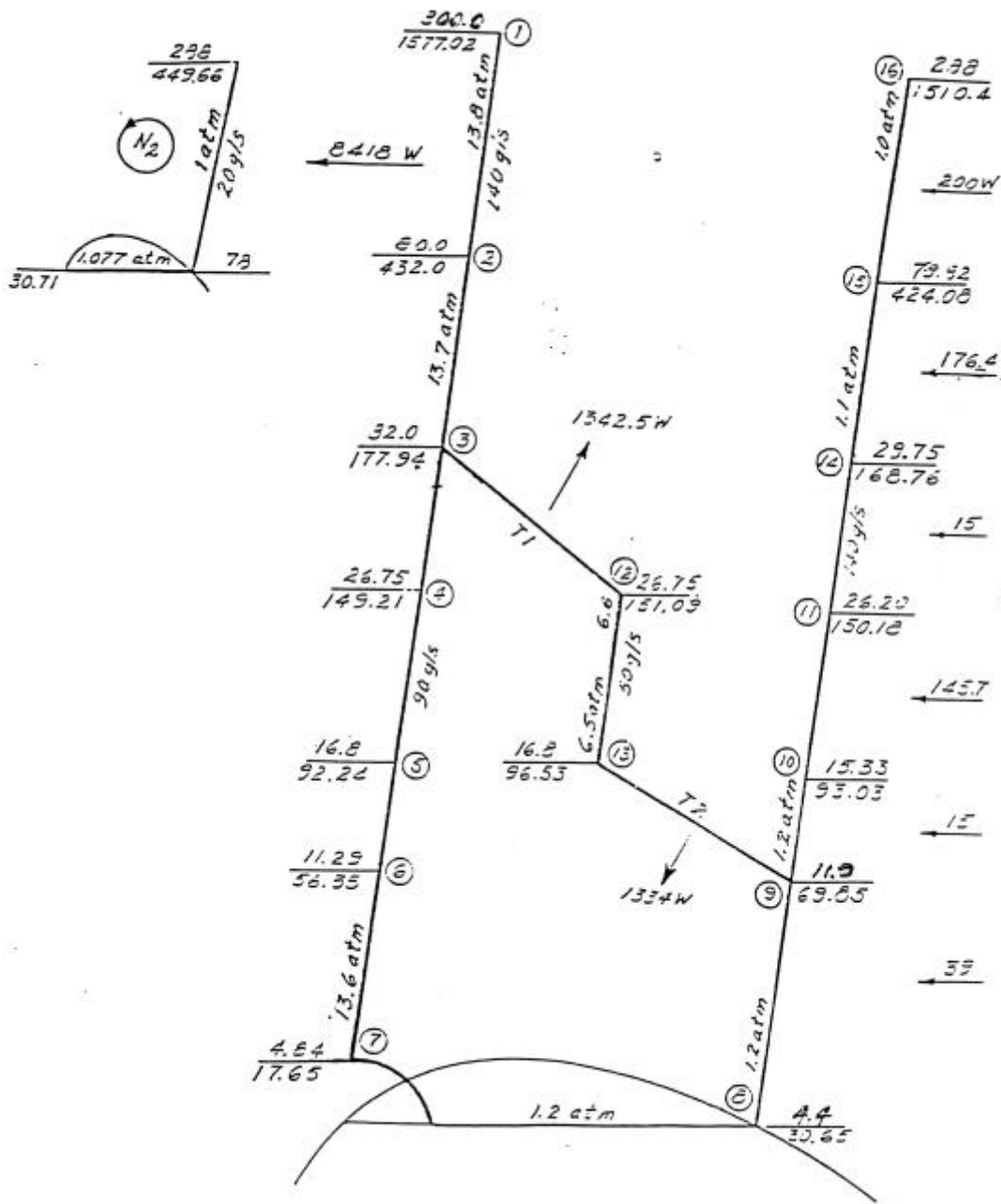
- Used in most large He refrigerator / liquefiers
- Cycle consists of :
 - 1) Compression to ~ 20 Bar with cooling back to 300 K + oil removal
 - 2) Cooling of HP gas with LN₂
 - 3) Isentropic expansion via 2 or more expansion engines
 - 4) Cooling of HP gas by cold returning LP stream

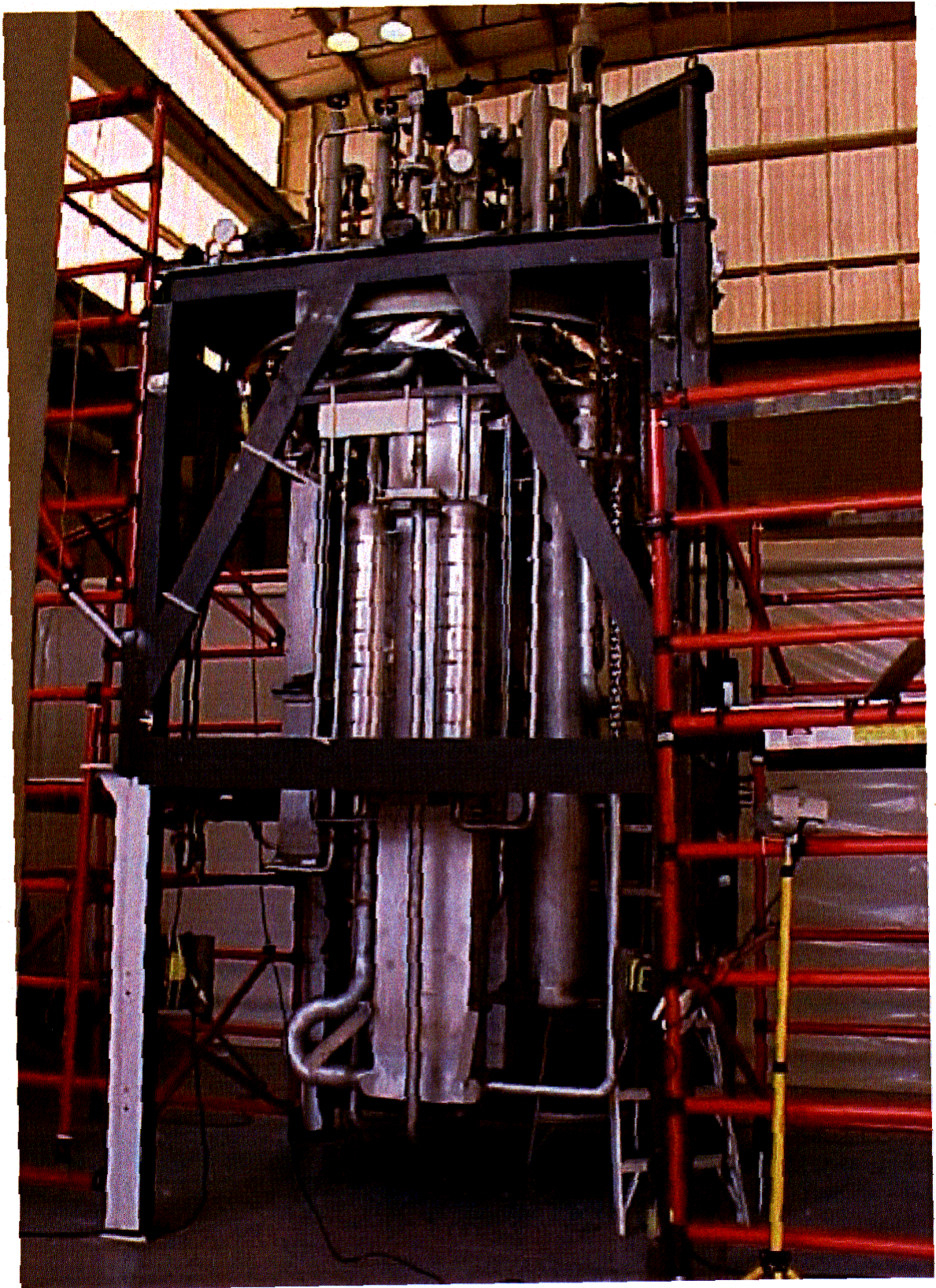
- 5) Isenthalpic expansion through JT valve**
- 6) Return of gas to compressors at just above 1 Bar pressure**



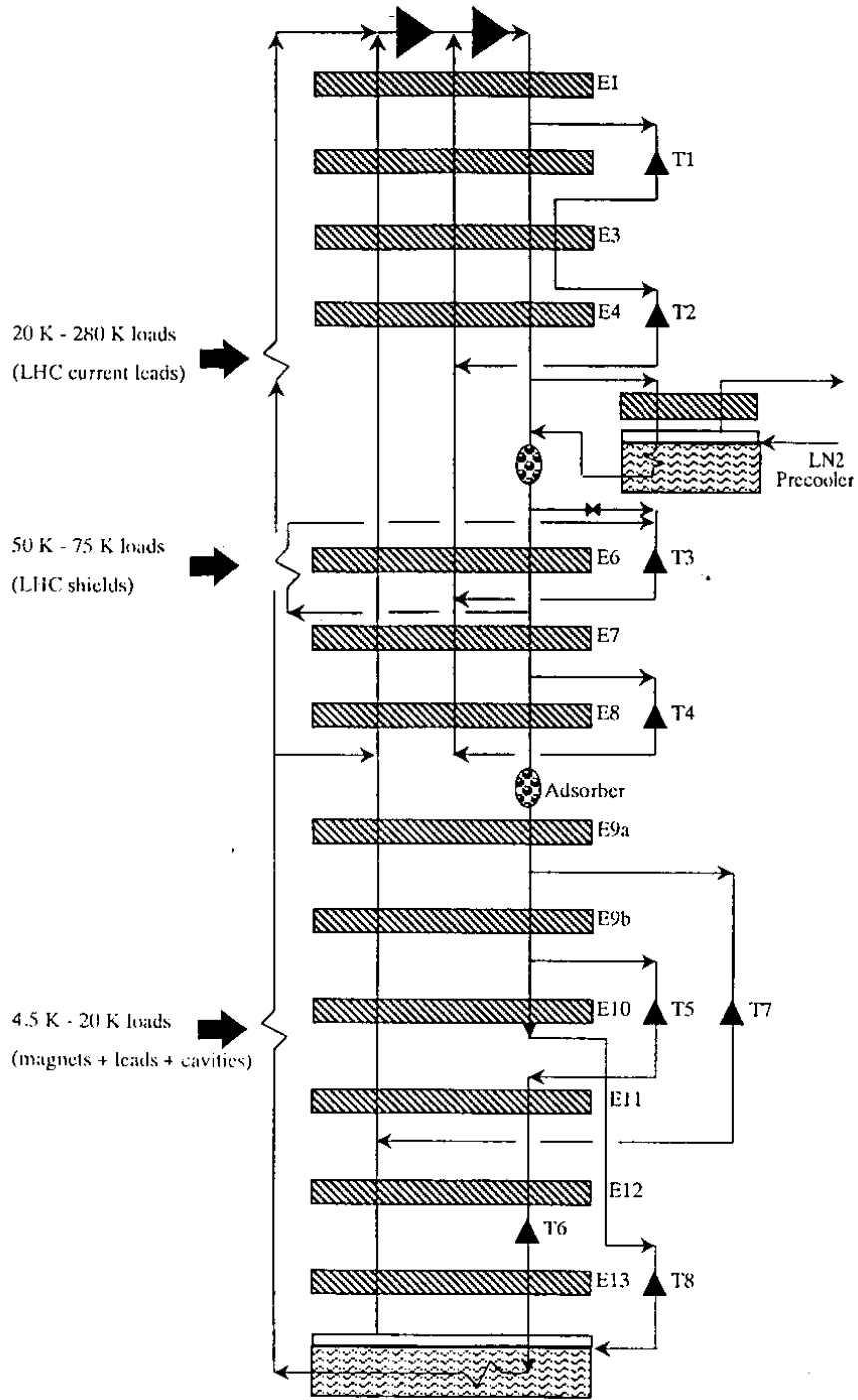
CTI 4000 Upgrade 12 / 2 / 99

* Indicates new or changed component



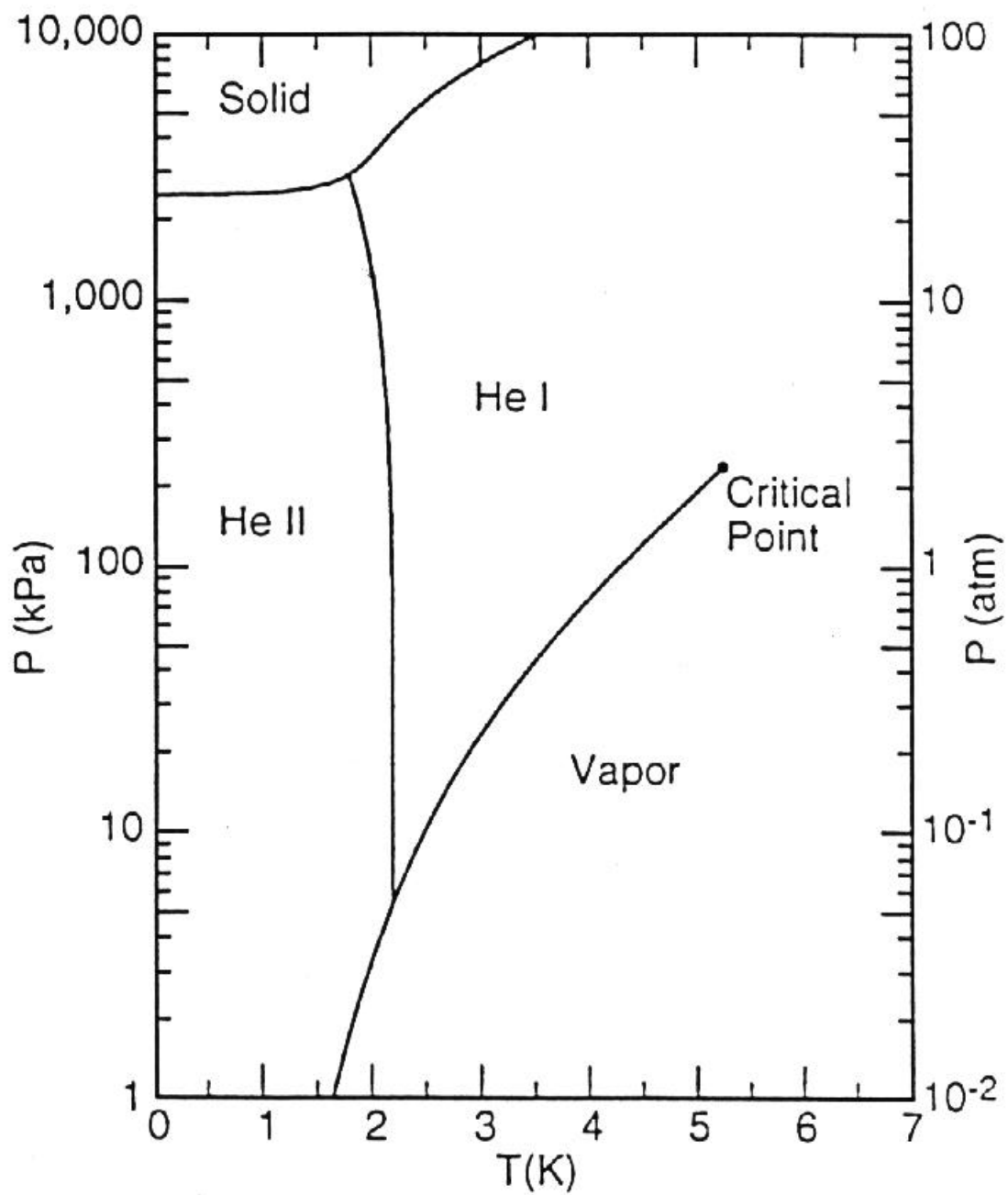






II) He II (Superfluid Helium)

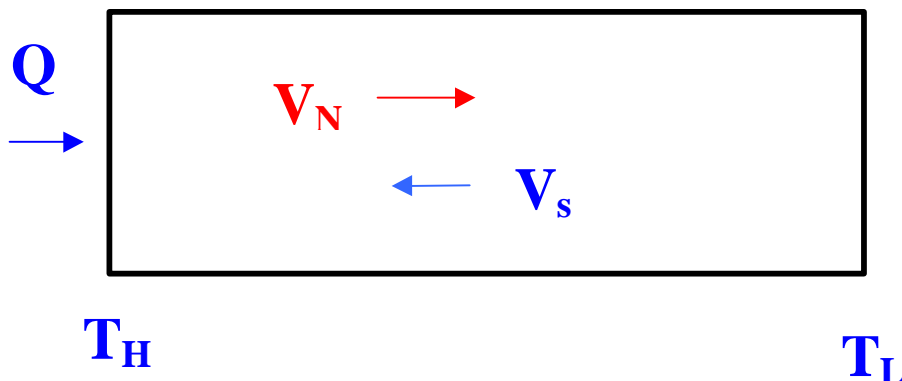
- **2nd liquid phase of helium**
- **Phase transition is 2nd order (no latent heat) but discontinuity in specific heat hence lambda transition**
- **$T_{1 \text{ max}} = 2.2 \text{ K}$**
- **Has unique thermal and fluid properties**
- **Lower temperature means:**
 - **Higher Field s/c magnets : LHC, Tore Supra**
 - **Lower BCS losses in RF s/c : TESLA, CEBAF**
 - **Lower background temperatures for IR observation : COBE, SIRTF**



- **Two Fluid Model**

- **He II results from Bose-Einstein condensation**
- **Model He II as two completely interpenetrating fluids**
- **Some fluid in ground state: $S=0$, $m=0$ (superfluid component)**
- **Some fluid in excited : S and m finite (normal fluid component)**

- **Internal Convection**



- **No net mass flow**
- **Extremely effective heat transfer mechanism**
- **Quantized Vortices**
 - **In the superfluid component:**

$$\mathbf{C} = \oint \mathbf{V}_s \times d\mathbf{l} = \mathbf{n} \frac{\mathbf{h}}{\mathbf{m}}$$
 - **Solves rotating bucket paradox**

$$\tilde{\mathbf{N}}^2 \mathbf{V}_s = \mathbf{0} \text{ in body of fluid}$$

$$\tilde{\mathbf{N}}^2 \mathbf{V}_s \cdot \mathbf{n} = \mathbf{0} \text{ at container wall}$$
 - **Have been experimentally observed**

- **Heat Transfer in He II**

2 Regimes:

$$V_s < V_{sc}$$

$$q = \frac{(r s d^2) T dT}{b h_n dx}$$

$$V_s > V_{sc}$$

- **Mutual Friction regime**
- **As $V_{sc} \sim d^{1/4}$ (cgs units) this regime is most applicable in engineering applications of He II**

$$q = \frac{\epsilon}{\epsilon_0} f^{-1}(P, T) \frac{dT}{dx} \dot{\epsilon}^{1/3}$$

Heat Transfer Limits

- In Pressurized He II ($T_h < T_1$)

Thus the peak heat flux q^* is:

$$q^* L^{1/3} = \left(\int_{T_b}^{T_1} \dot{q}^{-1}(T) dt \right)^{1/3}$$

At 1.9 K and 1 bar :

$$q^* L^{1/3} \sim 15 \text{ kW/m}^{5/3}$$

- In Saturated He II the limit is given by the local saturation temperature

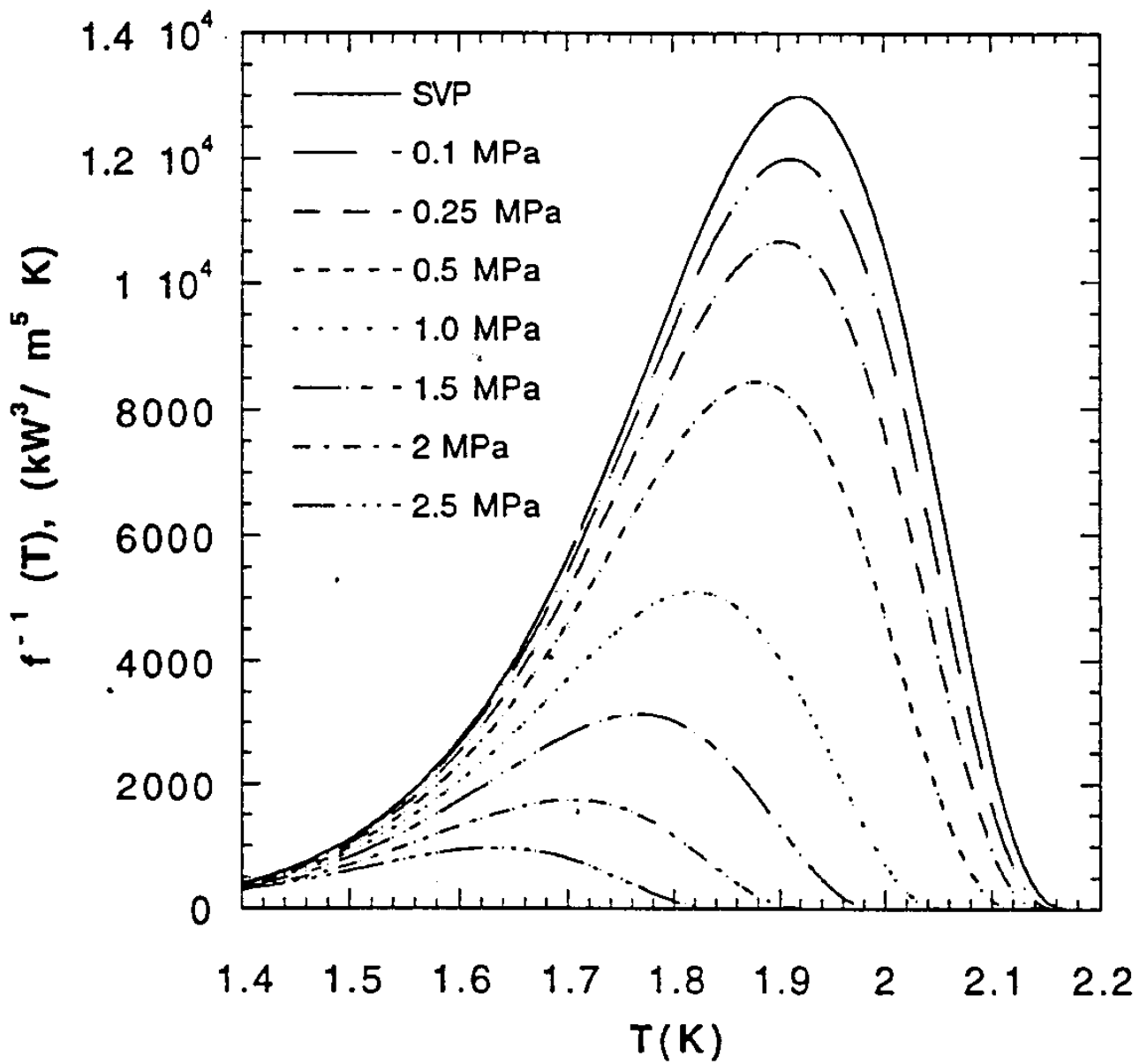
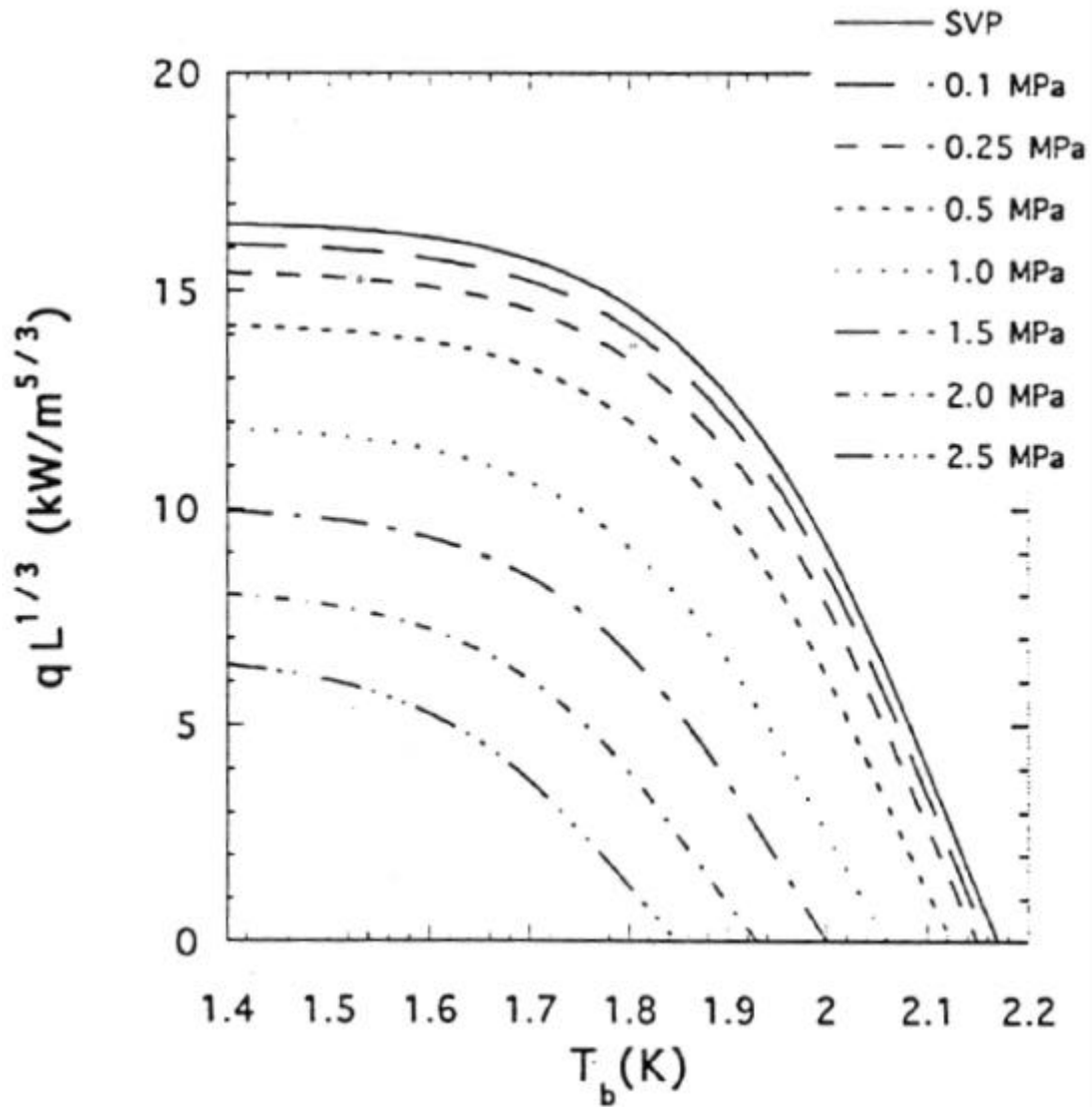


Figure 3-7

He II Heat Conductivity Function

He II (Superfluid Helium) S. W. Van Sciver, in Handbook of Cryogenic Engineering, J. G. Weisend II Ed., Taylor & Francis (1998)



He II Peak Heat Flux

He II (Superfluid Helium) S. W. Van Sciver, in Handbook of Cryogenic Engineering, J. G. Weisend II Ed., Taylor & Francis (1998)

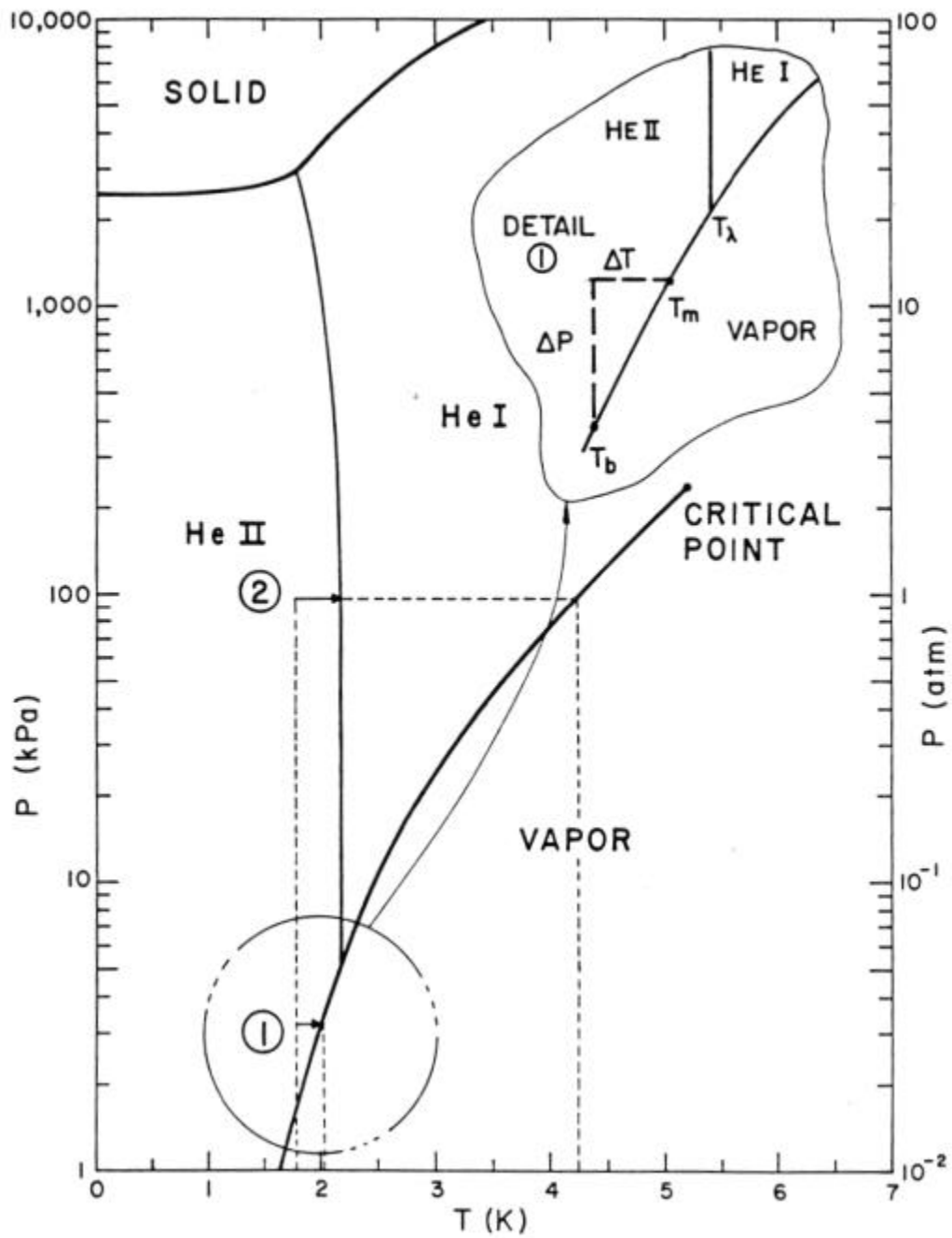


Figure3-9 Illustration of Saturated He II heat Transfer Limit

Helium Cryogenics ,S. W. Van Sciver, Plenum Press, (1986)

Surface Heat Transfer

- Dominated by Kapitza conductance
- For $q < 1 \text{ kW/m}^2$

$$q = h_k DT_s$$

- For $q > 1 \text{ kW/m}^2$

$$q = a(T_s^m - T_b^m)$$

- h_k a and m are empirical and dependent on material, temperature and surface condition
- $m \sim 3$
- Kapitza conductance is not dependent on helium flow rate

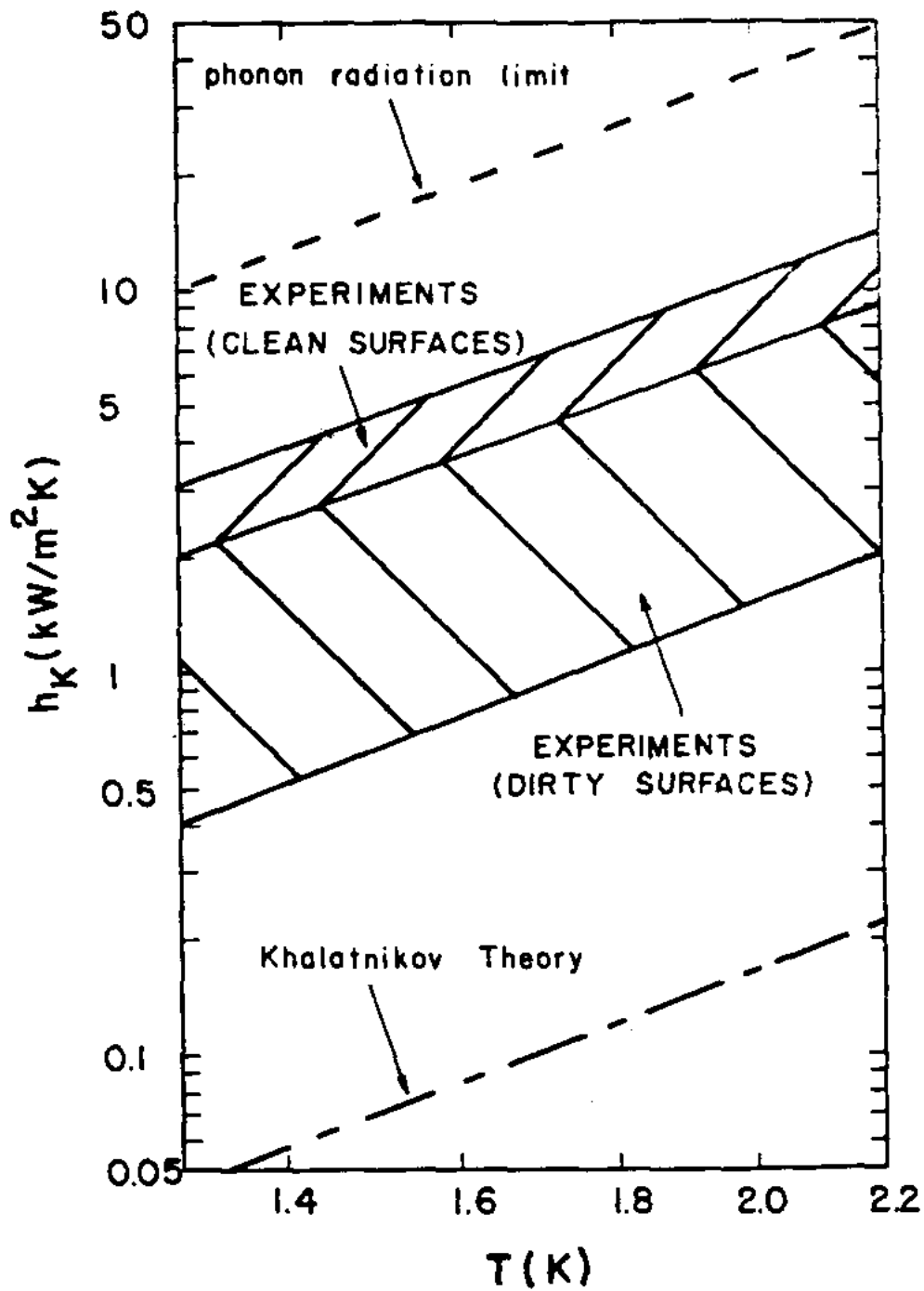


Figure 3-10
 Kapitza Conductance for Copper
 Helium Cryogenics, S. W. Van Sciver, Plenum Press, (1986)

- **Fluid dynamics**

- **Despite the presence of the superfluid component, in almost all engineering applications He II behaves as a classical fluid. This includes :**

- ◆ **Pump performance**

- ◆ **Pressure drop in tubes, valves, bellows and fitting**

- ◆ **Flowmetering techniques**

- **Not true for**

- ◆ **Film flow**

- ◆ **Porous plugs**

- ◆ **Hot wire anemometers**

- **He II Heat Exchangers**

- **Must take into account unique He II heat transfer properties**
- **Must allow for rapidly changing specific heat with temperature**
- **Handbook methods e.g. e - NTU are not suitable**

