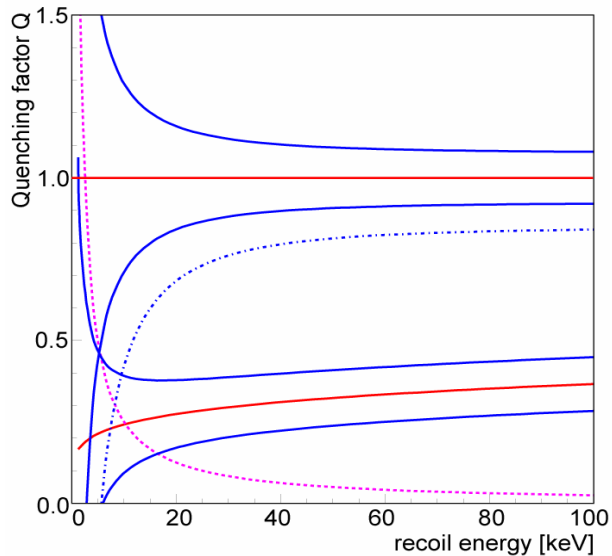


### exercise #1: Direct WIMP search with bolometers

a) explain the different curves of the plot

b) plot the  $1-\sigma$  contour of a population of events from a 60 keV „ $\gamma$  line“ with an experimental energy resolution of  $\sigma(E_{\text{recoil}})=10\%$  and  $\sigma(E_{\text{ionisation}})=2\%$

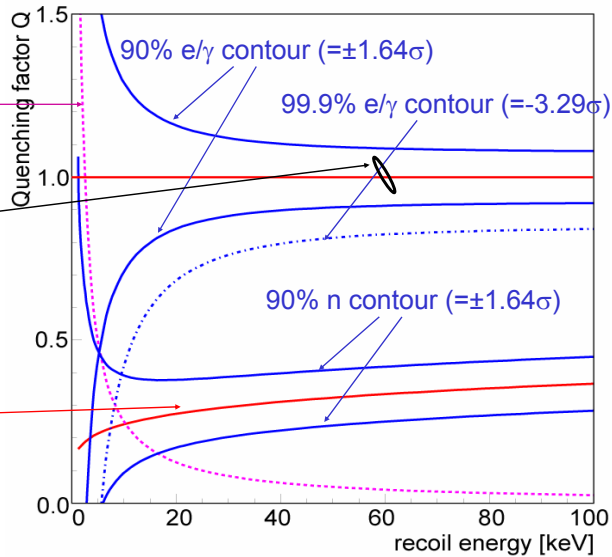


### exercise #1: Direct WIMP search with bolometers

ionization threshold of 3.7keV<sub>ee</sub>

60 keV  $\gamma$  „line“ population ( $\sim 1\sigma$ -contour)

central Q value for nuclear recoils



## exercise #2: Direct WIMP search with bolometers

In direct DM searches, WIMP's can be detected via elastic scattering off nuclei of the detector material. Assume a WIMP with  $m(\chi)=50\text{GeV}/c^2$  hitting a Ge nucleus with a relative velocity of  $v=300\text{km/s}$ .

In the case of a central collision, what is the transferred energy  $E_{\text{recoil}}$ ?

How does this compare to the energy transfer of a WIMP collision with an electron of the Ge atom?

## exercise #2: Direct WIMP search with bolometers

$m(\chi) = 50\text{GeV}/c^2$  with velocity of  $v(\chi) = 300\text{km/s}$   
 $\rightarrow E(\chi) = \frac{1}{2} m(\chi)c^2 (v/c)^2 = 25 \text{ keV}$

elastic collision: energy transfer

$$\Delta E = \frac{4m(\chi) \cdot m(\text{Ge})}{[m(\chi) + m(\text{Ge})]^2} \cdot E(\chi) \cdot \cos^2 \theta$$

with the scattering angle  $\theta$  in the lab system.

Maximal energy transfer  $\Delta E$  for central collision, assume  $m(\text{Ge})=72.6\text{GeV}$

$\rightarrow \Delta E = 0.966 E(\chi) = 24.15 \text{ keV}$

$\Delta E$  with collision on electron  $m(e^-)=0.511\text{MeV}$ :

$\rightarrow \Delta E = \{4 \times 0.000511 \times 50\} / \{50.000511\}^2 E(\chi) = 4.1 \cdot 10^{-5} E(\chi) \approx 1\text{eV} !!$

### exercise #3: Kinematics of $\beta$ decays

Determine the value of the retarding potential, at which the  $\beta$ -decay signal count rate  $\Gamma_{e^-}$  is twice the expected background rate of  $\Gamma_{e^-} = 2\Gamma_{bg} = 2 \times 0.01 \text{ counts/s} = 0.02 \text{ cts/s}$ .

The amount of  $T_2$  molecules in the source is  $N(T_2) = 3.2 \cdot 10^{19}$ , the Tritium half life is  $T_{1/2} = 12.3 \text{ years}$ , the endpoint energy is  $E_0 = 18575 \text{ eV}$ . Applying a retarding potential of  $V = E_0/q - 1V = 18574V$ , the measured signal rate is only  $\sim 10^{-13}$  of the total  $\beta$ -spectrum of the integrating spectrometer. To determine the spectral shape of the  $\beta$  electrons, assume a  $\beta$ -spectrum with vanishing neutrino mass near the endpoint  $E_0$ .

### exercise #3: Kinematics of $\beta$ decays

number of T nuclei in source:  $N(T) = 2 N(T_2) = 6.4 \cdot 10^{19}$

$T_{1/2} = 12.3 \text{ years} \rightarrow$  decay rate  $\Gamma = 1/\tau = 1/(\tau/\ln 2) = 1.8 \cdot 10^{-9} /s$

we simplify and assume ALL decay electrons going into the spec.:

$N(E=18547\text{eV})/N_{tot} = 10^{-13}$  with  $N(E) \sim (E_0 - E)^3$

so we get  $\Gamma_{e^-}(U=18547V) = 10^{-13} \times 6.4 \cdot 10^{19} \times 1.8 \cdot 10^{-9} = 0.01152 /s$

$\Gamma_{e^-} = 2\Gamma_{bg} = 0.02 /s$  for  $(0.02/0.01152)^{1/3} V$  below  $18575V \rightarrow 18573,8V$

(we also neglected the energy of the final states of  $(\text{He-T})^+$  molecules)

### exercise #4: neutrino mass from SN ToF

Discuss how a „time-of-flight“ measurement of Supernova neutrinos can be used to determine the neutrino mass. What are the difficulties?

Determine the time-of-flight  $T$  of a neutrino with mass  $m_\nu$  and energy  $E_\nu \gg m_\nu$  with a distance  $L$  of the source (emission time  $t_0$ ) and the detector (detection time  $t$ ).

Assume two neutrinos  $\nu_1$  and  $\nu_2$  emitted at times  $t_{01}$  and  $t_{02}$  with energies  $E_1$  and  $E_2$ . What is the difference of the arrival time  $\Delta t$ ?

Take Supernova SN1987A and the detection of  $\nu$ 's by Kamiokande:

$E_1=43.4\text{MeV}$ ,  $E_2=15.6\text{MeV}$ ,  $\Delta t=9\text{s}$ ,  $L=50\text{kpc}$

What upper limit on  $m_\nu$  can be extracted assuming  $\Delta t_0=0$ ?

### exercise #4: neutrino mass from SN ToF

$$T = t - t_0 = \frac{L}{v} = \frac{L}{c} \cdot \frac{E_\nu}{p_\nu c} = \frac{L}{c} \frac{E_\nu}{\sqrt{E_\nu^2 - m_\nu^2}} \approx \frac{L}{c} \left( 1 + \frac{m_\nu^2}{2E_\nu^2} \right)$$

$$\Delta t = t_2 - t_1 = \Delta t_0 + \frac{L m_\nu^2}{2c} \left( \frac{1}{E_2^2} - \frac{1}{E_1^2} \right)$$

$$m_\nu^2 = \frac{2c\Delta t}{L} \left( \frac{1}{E_2^2} - \frac{1}{E_1^2} \right)^{-1} = 0.39 \cdot \frac{\Delta t / \text{sec} \cdot (E_1 / \text{MeV})^2}{L / 50 \text{kpc}} \cdot \frac{1}{\alpha^2 - 1} \text{eV}^2$$

$$\text{with } \alpha = \frac{E_1}{E_2} > 1 \text{ we deduce } m(\nu_e) < 31 \text{eV}$$