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# **Search for the Lepton Flavor Violation in the Higgs Boson Decay at a Linear Collider**

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in collaboration with

S. Kanemura, K. Matsuda, T. Shindou, E. Takasugi, K. Tsumura

Osaka University

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- Introduction
  - Motivation
    - LFV via Higgs and LF violating Higgs decay

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  - Why linear collider?

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  - *Fake event*

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- Summary

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# Introduction

# Motivation

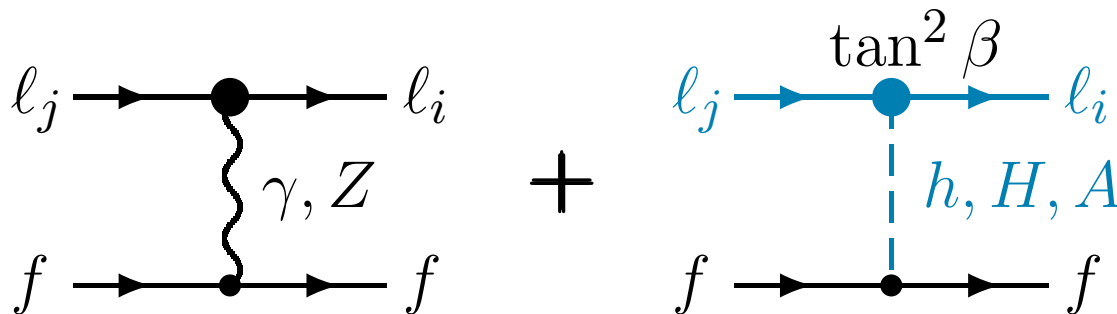
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- Lepton Flavor Violation (LFV) in the charged lepton sector  
— the signal of the new physics.

# Motivation

- Lepton Flavor Violation (LFV) in the charged lepton sector — the signal of the new physics.
- In MSSM with large  $\tan \beta$ , the Higgs bosons affect *the LFV processes*, such as,

$\tau \rightarrow 3\mu$ : K.Babu C.Kolda, PRL**89** 241802,  
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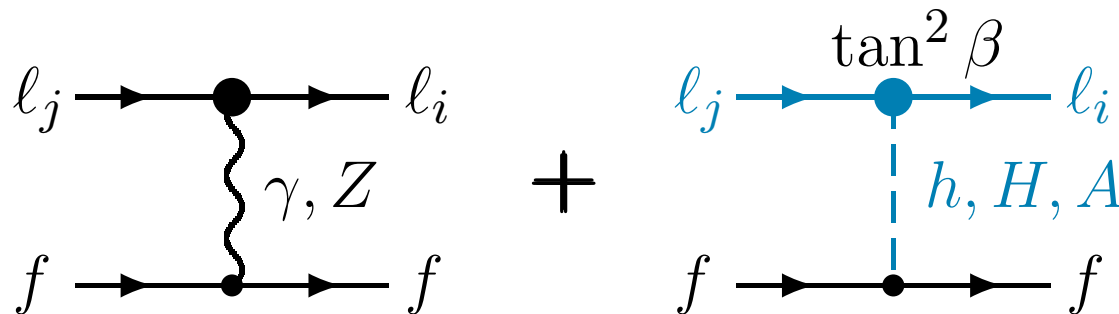




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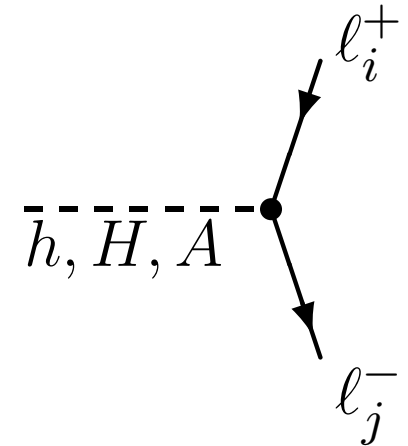


- The Higgs-contribution is important in  $m_{\text{SUSY}} \gg m_{\text{Higgs}}$ .

\*In such a case, the model below  $m_{\text{SUSY}}$  can be regarded effectively as the general 2HDM.

# Motivation

- We discuss *the LF violating Higgs boson decay*, expecting to get the information on the next energy scale by comparing between *the LFV processes* and *the LF violating Higgs decay*.



- **LFV processes**

- combination of the photon-mediation and the Higgs-mediation. indirect measurement.

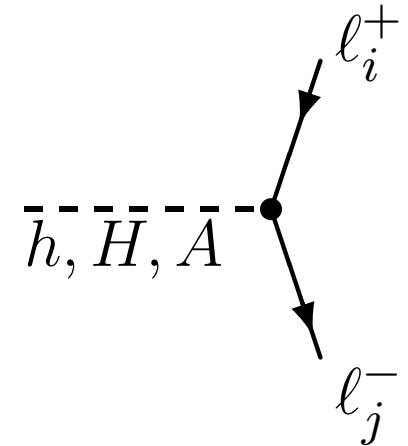
- **LF violating Higgs decay**

- direct measurement of the LF violating Higgs coupling.

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- We make a study on the detectability of the LF violating Higgs boson decay at a Linear Collider (LC).

- Lagrangian — leptonic Yukawa

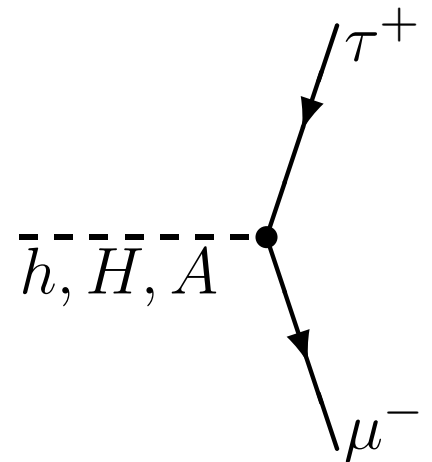
$$-\mathcal{L} \supset Y_{\ell_i} \overline{\ell_{Li}} (\delta_{ij} \Phi_1^0 + \epsilon_{ij} \Phi_2^0) \ell_{Rj} + \text{H.c.}$$

$\simeq$ (mass term) + (flavor diagonal interactions)

$$+ \frac{m_{\ell_i} \kappa_{ij}}{v \cos^2 \beta} \overline{\ell_{Li}} \ell_{Rj} [\cos(\beta - \alpha) h - \sin(\beta - \alpha) H - iA]$$

+ (charged Higgs term) + H.c.,

The LFV Higgs decay arise since two Yukawa matrices ( $Y_{\ell_i} \delta_{ij}$  and  $Y_{\ell_i} \epsilon_{ij}$ ) can not be diagonalized simultaneously.



# Bound on $|\kappa_{32}|^2$ from LFV processes

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- Branching ratio for  $h \rightarrow \tau^+ + \mu^-$  is estimated as

$$\text{Br}(h \rightarrow \tau^+ + \mu^-) \simeq \frac{1}{N_c} \frac{m_\tau^2}{m_b^2} \frac{\cos^2(\beta - \alpha)}{\sin^2 \alpha \cos^2 \beta} |\kappa_{32}|^2.$$

- Throughout this talk, we assume
  - Nearly *decoupling region*,  $h \simeq \Phi_{\text{SM}}$ ,  $\sin(\alpha - \beta) = -0.95$ .
  - Large  $\tan \beta$ ,  $\tan \beta = 60$ .

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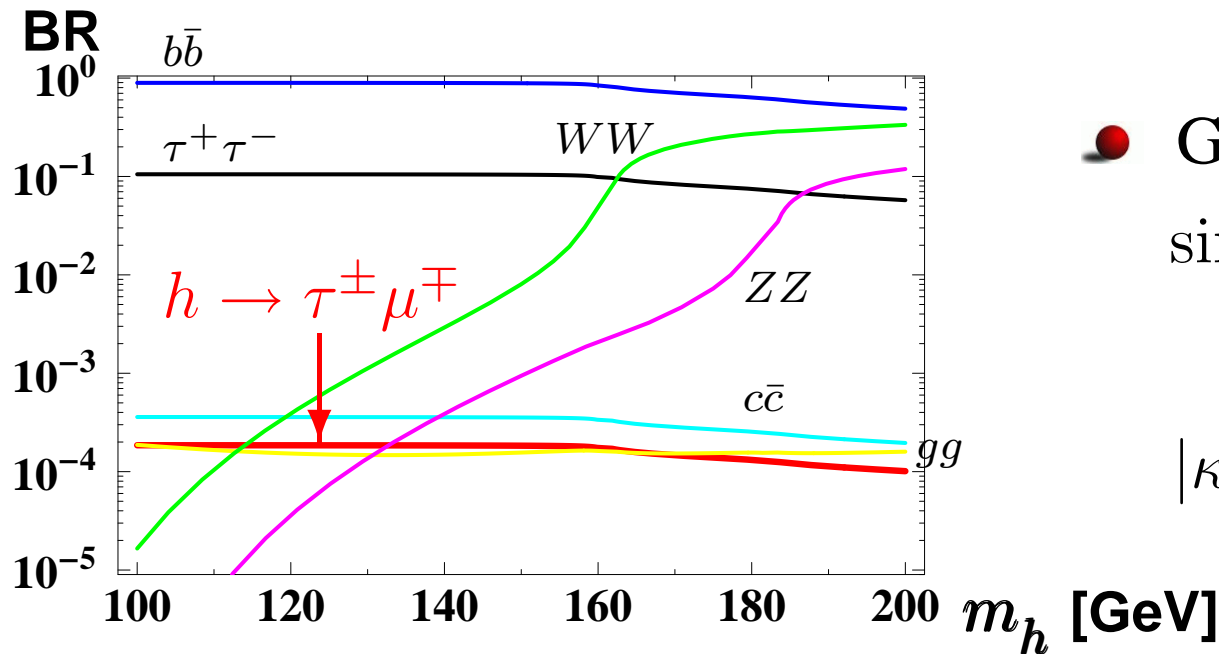
- Nearly *decoupling region*,  $h \simeq \Phi_{\text{SM}}$ ,  $\sin(\alpha - \beta) = -0.95$ .
- Large  $\tan \beta$ ,  $\tan \beta = 60$ .

- The bound on  $|\kappa_{32}|^2$  from  $\tau \rightarrow \mu\eta$  (Belle)

$$\text{Br}(\tau \xrightarrow{h,H,A} \mu\eta) \simeq 8.4 \times \frac{G_F^2 m_\mu^2 m_\tau^7}{768\pi^3 m_A^4} |\kappa_{32}|^2 \tan^6 \beta < 3.4 \times 10^{-7},$$

$$|\kappa_{32}|^2 < 0.3 \times 10^{-6} \times \left( \frac{m_A}{150[\text{GeV}]} \right)^4 \times \left( \frac{60}{\tan \beta} \right)^6.$$

# Branching ratio



- General-2HDM with
 
$$\sin(\alpha - \beta) = -0.95,$$

$$\tan \beta = 60,$$

$$|\kappa_{32}|^2 = 0.3 \times 10^{-6}.$$

- The branching ratio for  $h \rightarrow \tau^\pm \mu^\mp$  with  $|\kappa_{32}|^2 = 0.3 \times 10^{-6}$  is constrained as  $\mathcal{O}(10^{-4})$ .

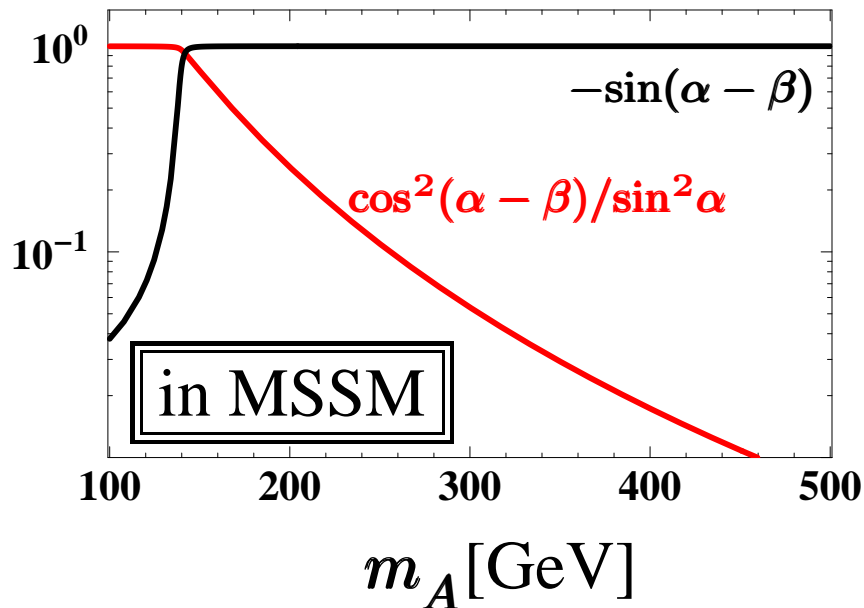
# Note on the bound and the signal

$$\text{signal event} = \sigma_h \times \text{Br}(h \rightarrow \tau^\pm + \mu^\mp),$$

$$\sigma_h \propto \sin^2(\alpha - \beta),$$

$$\text{Br}(h \rightarrow \tau^\pm + \mu^\mp) \simeq 7.2 \times 10^2 \frac{\cos^2(\alpha - \beta)}{\sin^2 \alpha} \left( \frac{m_A}{150[\text{GeV}] \tan \beta} \right)^4 \text{Br}(\tau \rightarrow \mu \eta).$$

- In MSSM,  $\alpha$  is the function of  $m_A$  and  $\tan \beta$  (and  $m_{\text{SUSY}}$ 's).



- $m_A \rightarrow$  large,

$$\frac{\cos^2(\alpha - \beta)}{\sin^2 \alpha} \rightarrow \text{small}$$

The  $\text{Br}(h \rightarrow \tau^\pm \mu^\mp)$  is constrained as  $\mathcal{O}(10^{-4})$ .



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- In the extended models, such as the general-2HDM,  $m_A$  and  $\alpha$  are independent parameters.
- In such a model, the bound from  $\tau \rightarrow \mu\eta$  can be relaxed.

large value of  $m_A$ ,

keeping the value of  $\cos^2(\alpha - \beta) / \sin^2 \alpha$ .

$\text{Br}(h \rightarrow \tau^\pm \mu^\mp)$  can be as large as  $\mathcal{O}(10^{-3})$ .

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- Why lightest Higgs?
  - First object to be found  
Its mass will be thoroughly determined.
  - Nealy decoupling region,  $\sigma \propto \sin^2(\alpha - \beta)$ .

# Our Points

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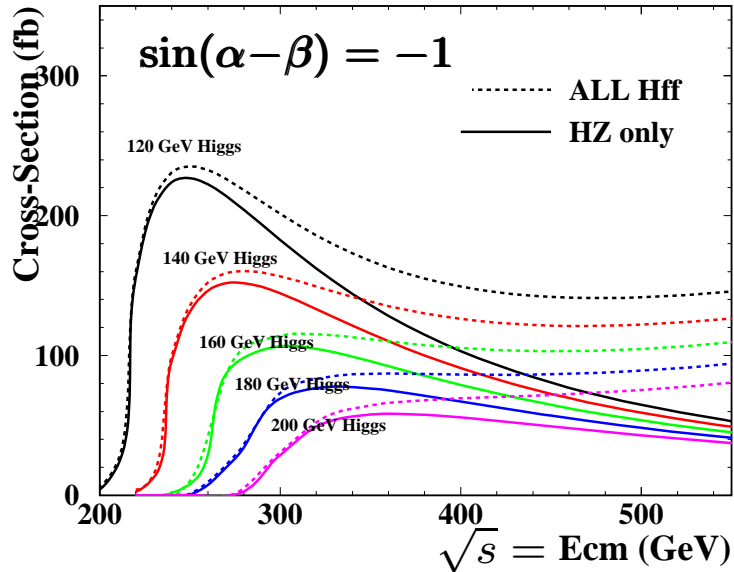
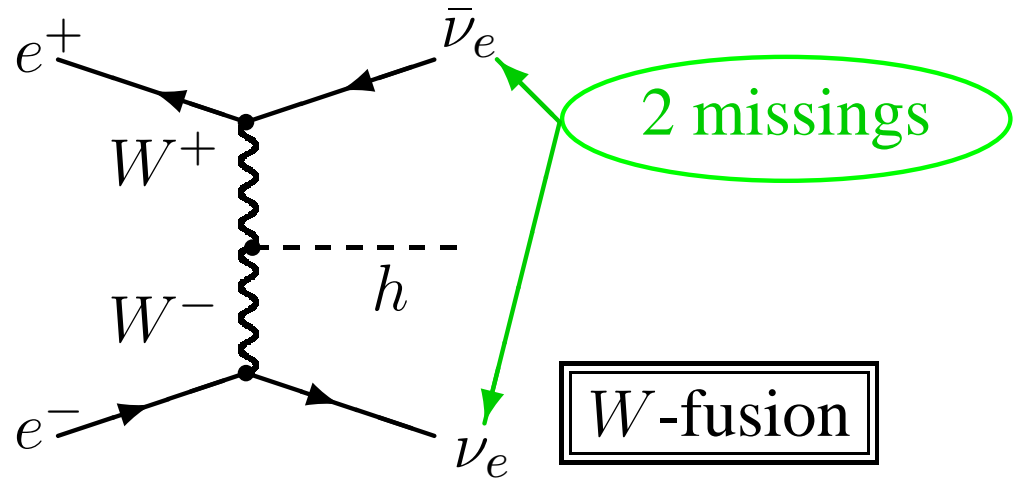
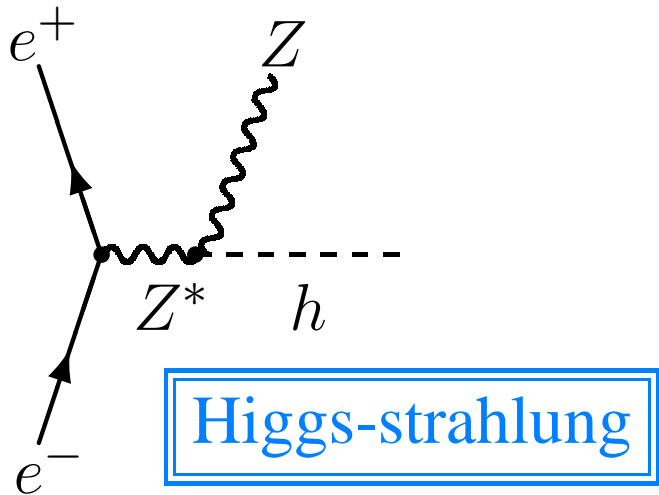
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- Why lightest Higgs?
  - First object to be found  
Its mass will be thoroughly determined.
  - Nealy decoupling region,  $\sigma \propto \sin^2(\alpha - \beta)$ .
- Why linear collider?
  - Clear signal, Precision measurement

It is important to reduce the backgrounds.

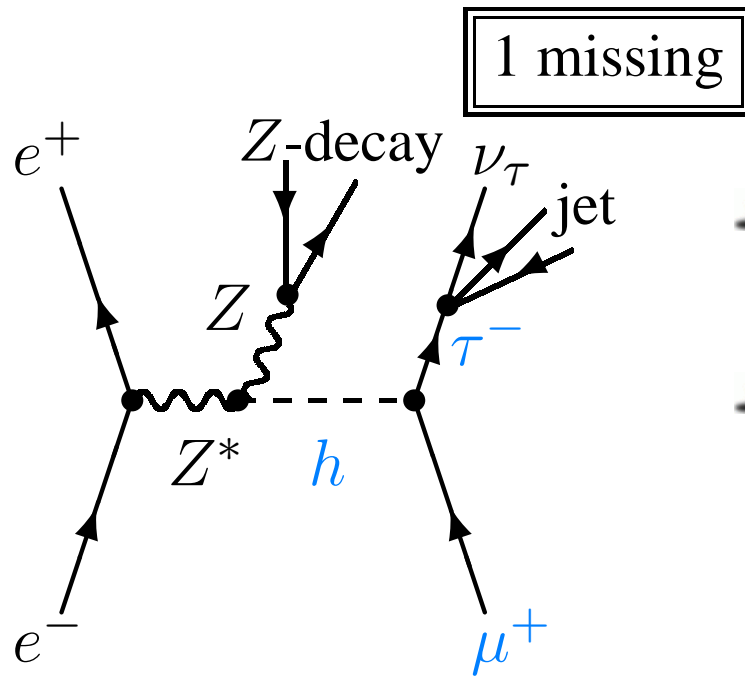
The Higgs-strahlung is preferable in the Higgs production processes to determine  $m_h$  and  $\sqrt{s}$  with high precision.

# Higgs production process



- In low  $\sqrt{s}$  region, the Higgs-strahlung is dominant.
- In 2HDM,  $\sigma \propto \sin^2(\alpha - \beta)$ .

# Strategy

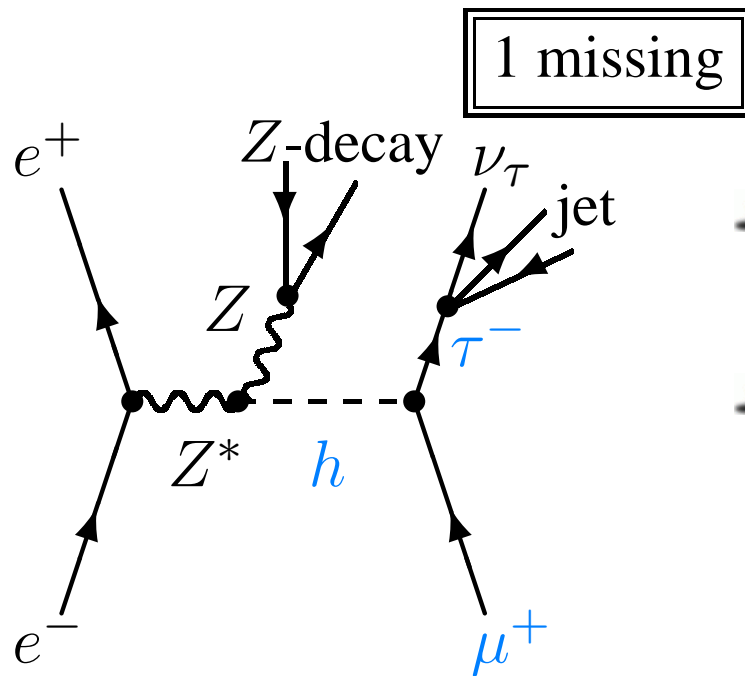


- Using  $Z$ -recoil, we can identify the process as the Higgs-mediated one.
- $p_\tau$  is reconstructed by using  $\sqrt{s}$ ,  $m_h$ ,  $m_Z$  and  $p_\mu$ .

It is not necessary to measure  $p_\tau$ .



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It is not necessary to measure  $p_\tau$ .

- We assume  $L = 1,000 \text{ fbarn}^{-1}$ , optimally tuned  $\sqrt{s}$ .
- The number of event for  $|\kappa_{32}|^2 = 0.3 \times 10^{-6}$  is estimated as

$$N_{\text{signal}} = L \times \sigma_{Zh} \times \text{Br}(h \rightarrow \tau + \mu) \times \epsilon \sim 30 \text{ events,}$$

$$\epsilon \equiv \text{Br}(Z \rightarrow jj, ee, \mu\mu) \times \text{Br}(\tau \rightarrow j + \nu_\tau) \simeq 0.5.$$

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# Feasibility Study

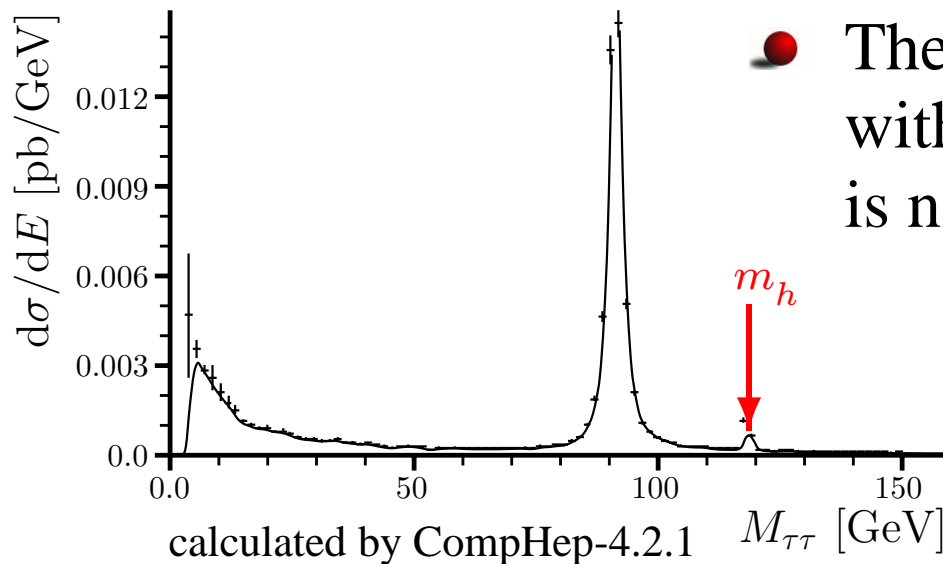
# Backgrounds

- We introduce the invariant mass cut to reduce the backgrounds which do not include the lightest Higgs boson.

$$e^+ + e^- \rightarrow Z\tau\tau \rightarrow Z\tau\mu + \nu_\mu\nu_\tau$$

$$e^+ + e^- \rightarrow ZWW \rightarrow Z\tau\mu + \nu_\mu\nu_\tau$$

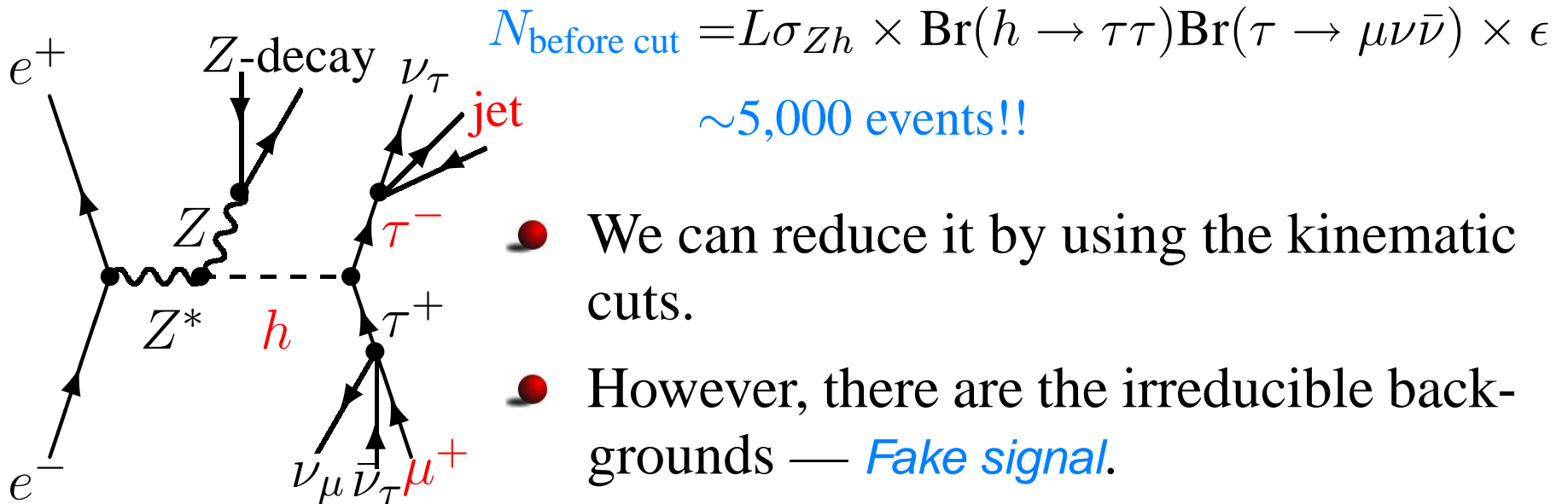
$$e^+e^- \rightarrow Z\tau^+\tau^-$$



- The number of backgrounds with  $M_{\tau\mu} \neq m_h$  is huge but it is not serious.

# Backgrounds — Fake signal —

- The most serious background is induced by the tau-pair production through the Higgs decay.



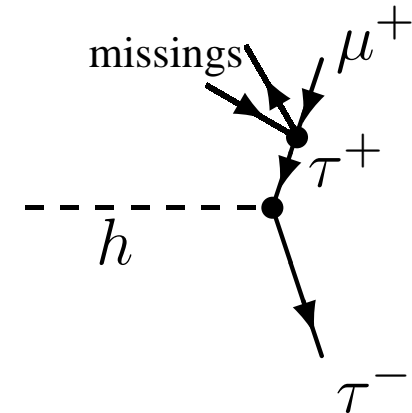
- We can reduce it by using the kinematic cuts.
- However, there are the irreducible backgrounds — *Fake signal*.

Fake signal condition:  $p_{\mu^+} \simeq p_{\tau^+}$

# Estimation of the number of the fake event

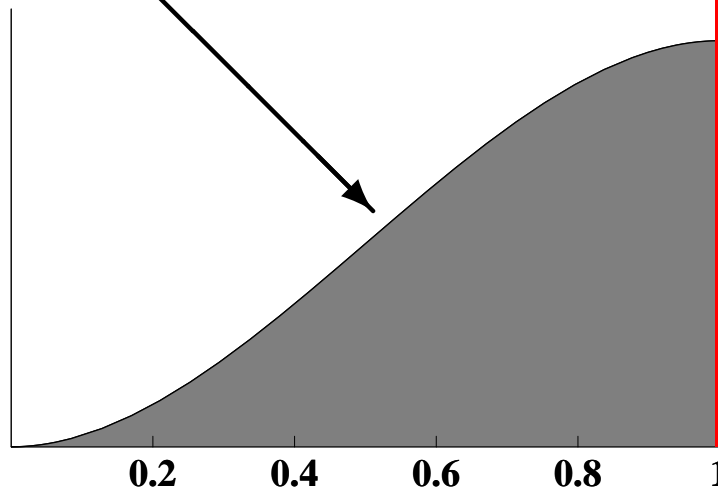
Fake signal condition:  $p_{\mu^+} \simeq p_{\tau^+}$

- The muon from tau tends to be emitted to the same direction of the parent tau.
- The energy of muon tends to distribute around the parent tau's.



$h \rightarrow \tau\tau \rightarrow \tau\mu + \text{missings}$

event number



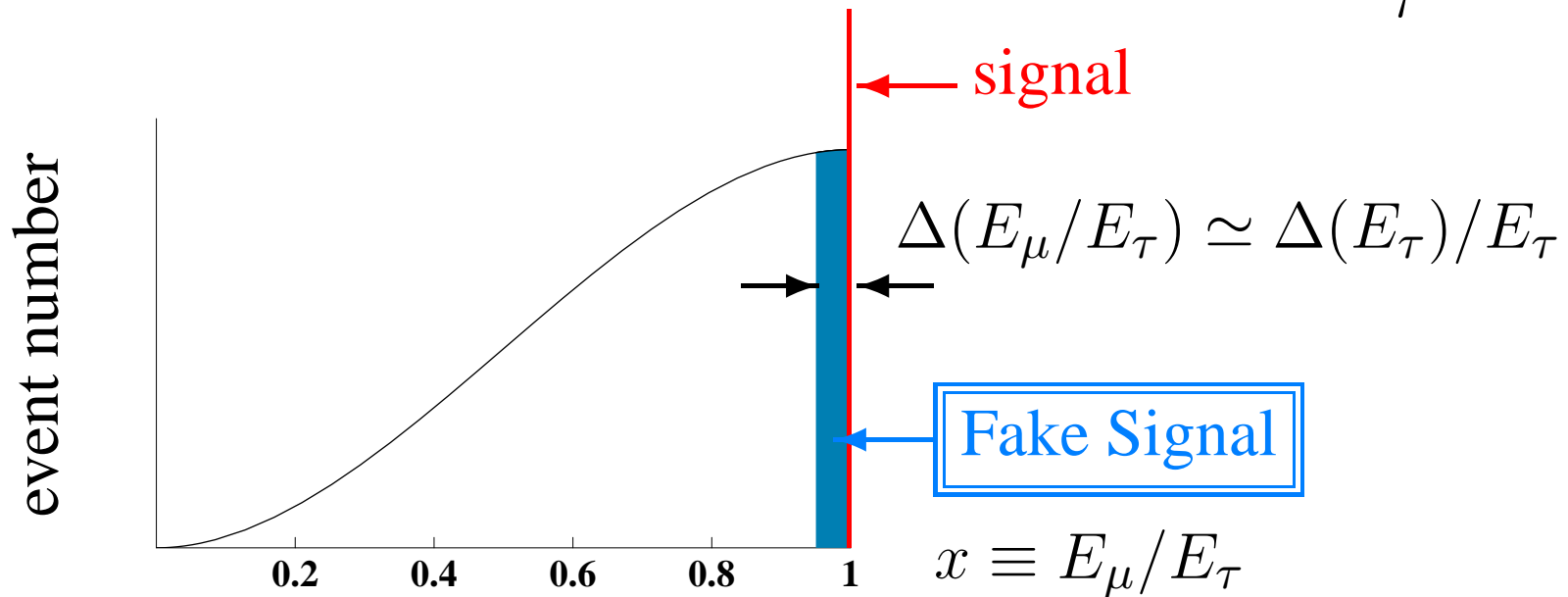
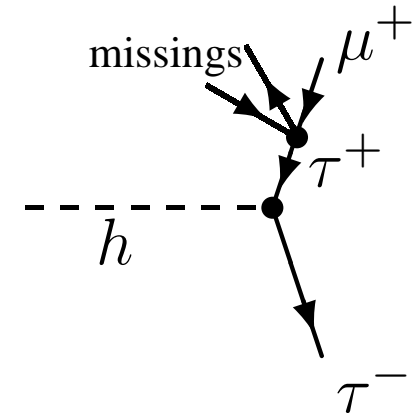
← signal,  $h \rightarrow \tau\mu$

$$x \equiv E_{\mu} / E_{\tau}$$

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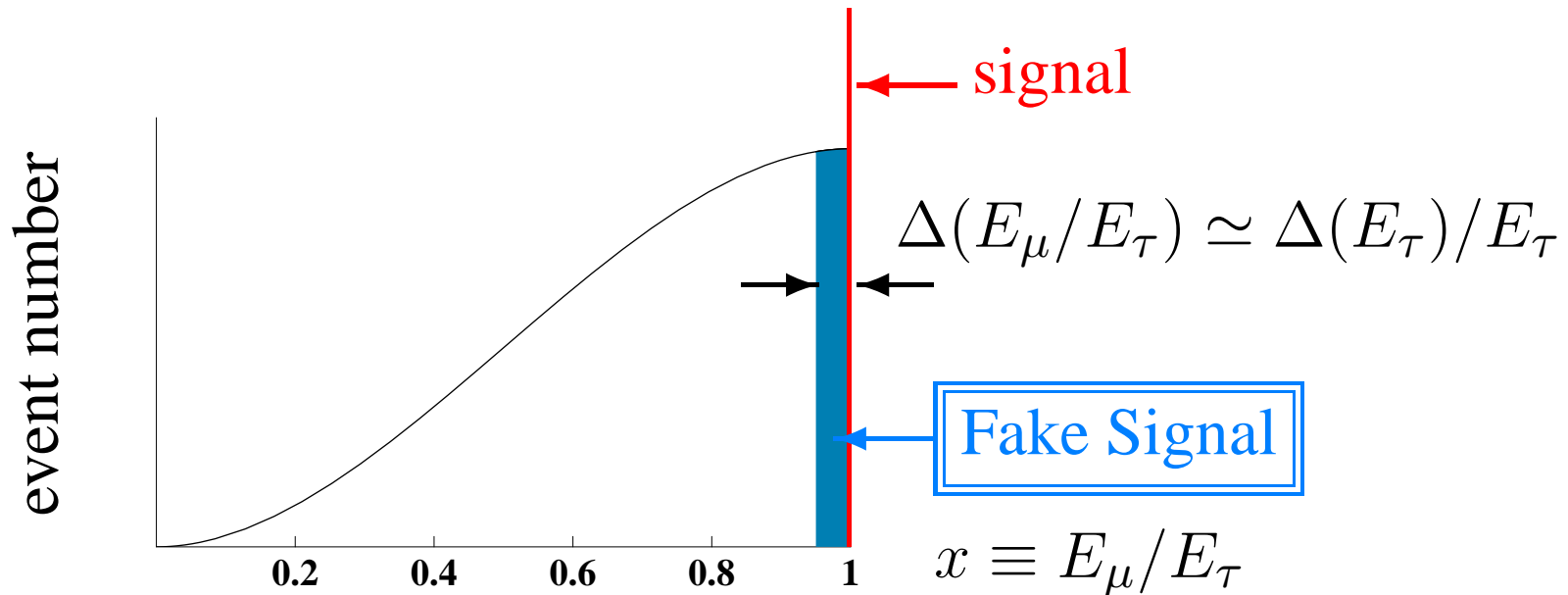


# Estimation of the number of the fake event

- In order to reduce the fake events, it is important to determine  $E_\tau$  with high precision.
- If we can determine  $\Delta(E_\tau)$  within 1 GeV, then

$$N_{\text{fake}} \sim 120 \text{ events !!}$$

$$N_{\text{signal}} \sim 30 \text{ events}$$



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$$N_{\text{signal}} \sim 30 \text{ events}$$

- When we assume  $|\kappa_{32}|^2 = 0.3 \times 10^{-6}$ ,  $\sin(\alpha - \beta) = -0.95$ , and  $\Delta(E_\tau) = 1 \text{ GeV}$ ,

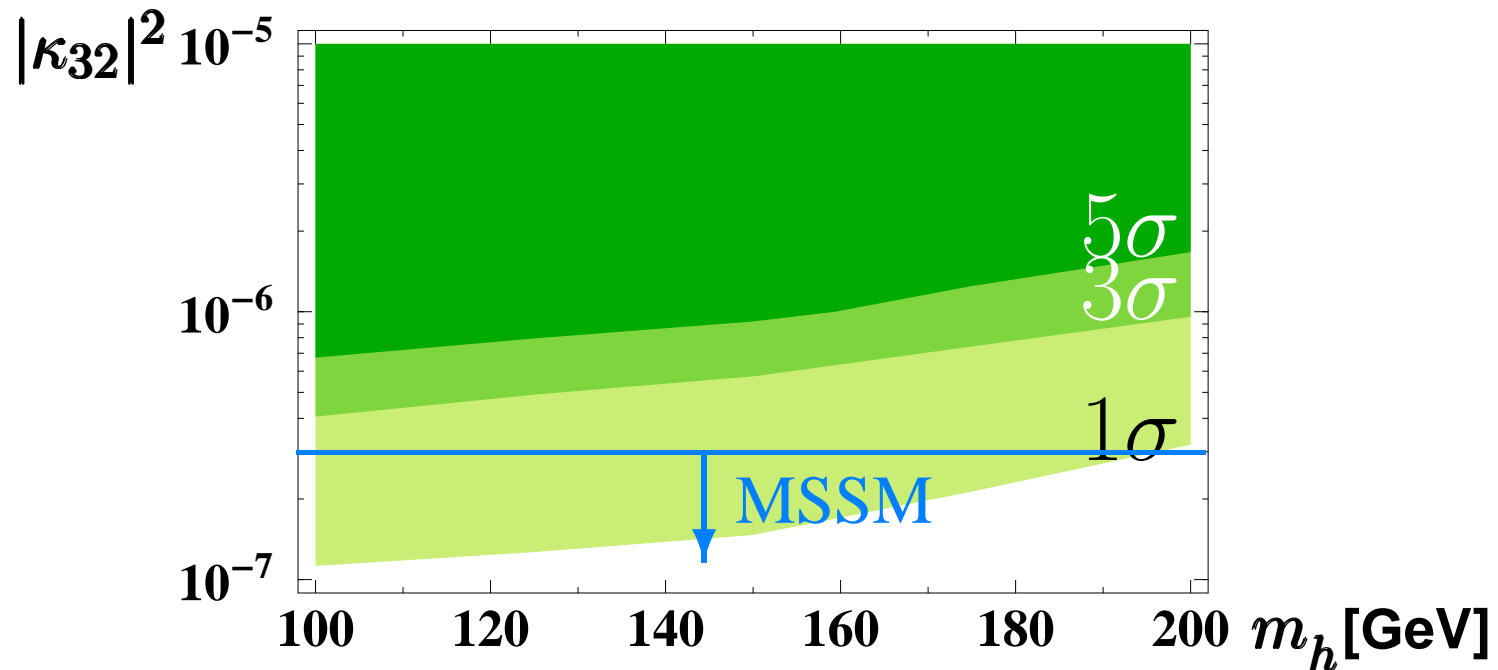
$$\frac{N_{\text{signal}}}{\sqrt{N_{\text{fake}}}} \sim 2.7\sigma.$$

In MSSM, the feasibility of observing  $h \rightarrow \tau\mu$  is marginal.



# Discovery contour

- We assume
  - $\sin(\alpha - \beta) = -0.95$ ,  $\tan \beta = 60$ ,
  - $1,000 \text{ fbarn}^{-1}$ ,  $\Delta(E_\tau) = 1 \text{ GeV}$



**Note:** When we assume the non-minimal models,  
we can take  $|\kappa_{32}|^2 \sim \mathcal{O}(10^{-6})$ .

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  - However, in the general model with the extended Higgs sector, we have a chance to find it at a linear collider.

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- It is constrained by  $\tau \rightarrow \mu\eta$  search.
  - In MSSM, the feasibility is marginal.
  - However, in the general model with the extended Higgs sector, we have a chance to find it at a linear collider.
- The direct measurement of the LF violating Higgs coupling and the indirect measurement of it should be complementary to each other.