

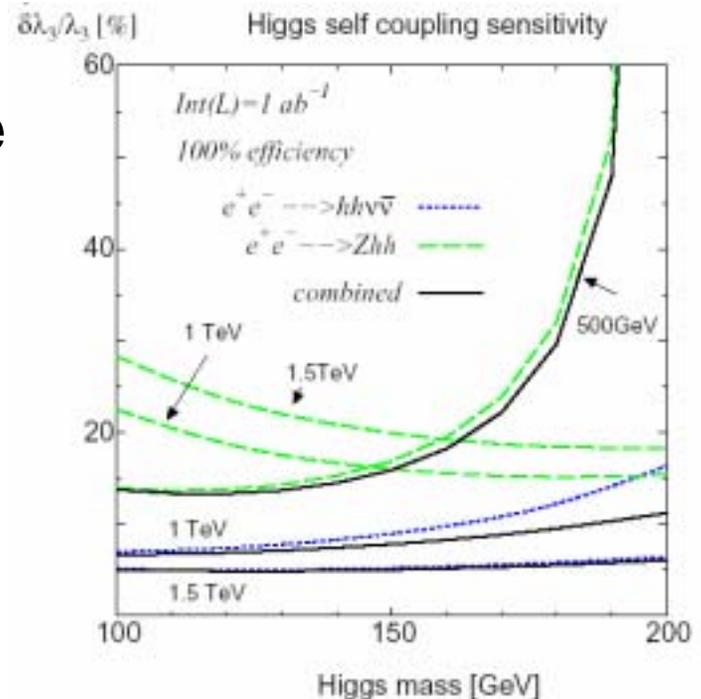
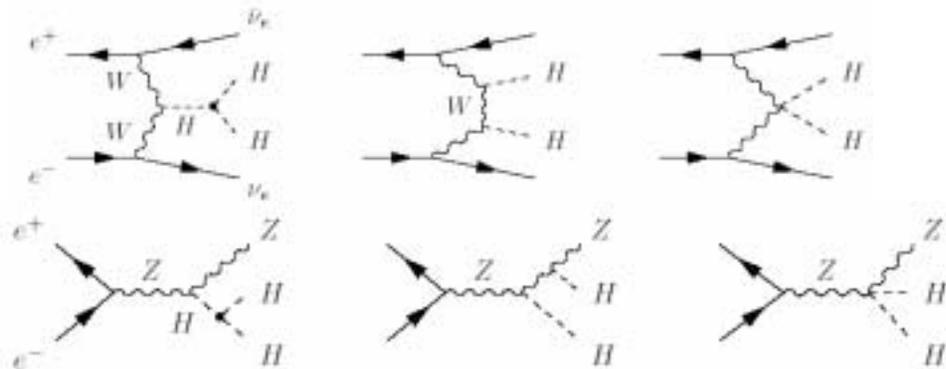
# New Physics from Higgs self-coupling measurement

Yasuhiro Okada (KEK)

LCWS 04, April 20, 2004, Paris

# Higgs self-coupling measurement

- Access to the Higgs potential.
- A few x10% determination of the triple Higgs coupling in the first stage of LC.  
( $e^+e^- \rightarrow ZHH, \gamma\gamma \rightarrow HH$ )
- Need a higher energy for precise determination.



Y. Yasui, et al, LCWS02

# New physics effect to the self-coupling

The self-coupling is sensitive to the tree level structure of the Higgs sector as well as loop effects.

Suppose that a light SM-like Higgs boson is found at LHC and LC. What will be impact of the self-coupling measurement?

We consider 2HDM as an example.

1. Relation between the corrections to  $hhh$  and  $hVV$  coupling constants.
2. Connection to the electroweak baryogenesis scenario.

# Two Higgs doublet model

## Higgs potential

$$V_{2\text{HDM}} = m_1^2 |\varphi_1|^2 + m_2^2 |\varphi_2|^2 - m_3^2 (\varphi_1^\dagger \varphi_2 + \varphi_2^\dagger \varphi_1) + \frac{\lambda_1}{2} |\varphi_1|^4 + \frac{\lambda_2}{2} |\varphi_2|^4 \\ + \lambda_3 |\varphi_1|^2 |\varphi_2|^2 + \lambda_4 |\varphi_1^\dagger \varphi_2|^2 + \frac{\lambda_5}{2} \left\{ (\varphi_1^\dagger \varphi_2)^2 + (\varphi_2^\dagger \varphi_1)^2 \right\},$$

Physical Higgs bosons:  $h, H, A, H^\pm$

## Two cases

Heavy Higgs boson masses

$$m_\Phi^2 \simeq M^2 + \lambda_i v^2$$

$$M = m_3 / \sqrt{\cos \beta \sin \beta}$$

$$\tan \beta = \langle \phi_2 \rangle / \langle \phi_1 \rangle$$

(1) **Decoupling case:**  $M^2 \gg O(\lambda_i v^2)$

The couplings of hVV, hff, and hhh approach to the SM values.

Loop corrections are suppressed by  $1/M^2$ .

(2) **Non-decoupling case:**  $M^2 \leq O(\lambda_i v^2)$

Large loop corrections due to the self coupling constants are possible,

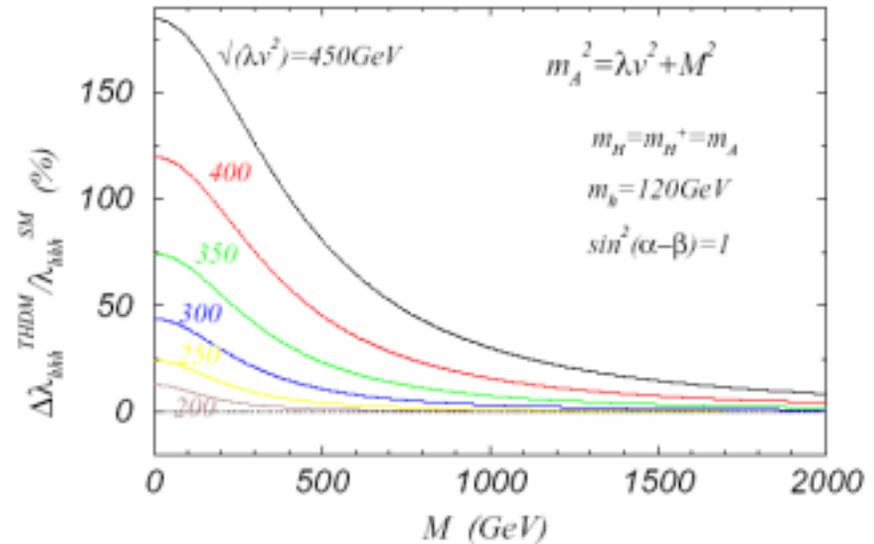
# Large loop correction to hhh coupling

In the limit that the tree level hVV coupling is the same as the SM value, the triple Higgs coupling can receive O(100%) radiative correction through heavy Higgs boson loop diagrams.

$$\sin(\beta - \alpha) \rightarrow 1$$

$\alpha$ : Mixing angle between neutral CP even Higgs bosons.

The decoupling behavior of  $\Delta\lambda_{hhh}^{THDM}$



S.Kanemura, S.Kiyoura, Y.O., E.Senaha, C.P.Yuan, 02

$$\lambda_{hhh}^{eff}(THDM) = \frac{3m_h^2}{v} \left\{ 1 + \frac{m_H^4}{12\pi^2 m_h^2 v^2} \left(1 - \frac{M^2}{m_H^2}\right)^3 + \frac{m_A^4}{12\pi^2 m_h^2 v^2} \left(1 - \frac{M^2}{m_A^2}\right)^3 + \frac{m_{H^\pm}^4}{6\pi^2 m_h^2 v^2} \left(1 - \frac{M^2}{m_{H^\pm}^2}\right)^3 - \frac{N_G m_t^4}{3\pi^2 m_h^2 v^2} + \dots \right\}$$

# Correction to hhh and hVV couplings

S.Kanemura, Y.O. ,E.Senaha,C.P.Yuan

$$(M = m_A/2)$$

We extend the analysis to  $\sin(\beta-\alpha) < 1$ .

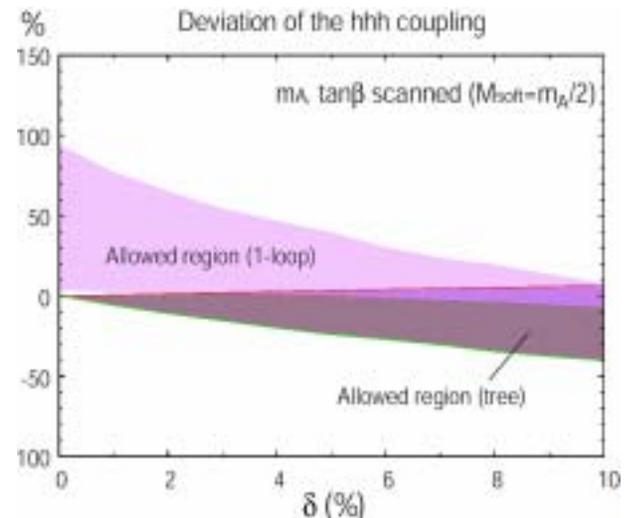
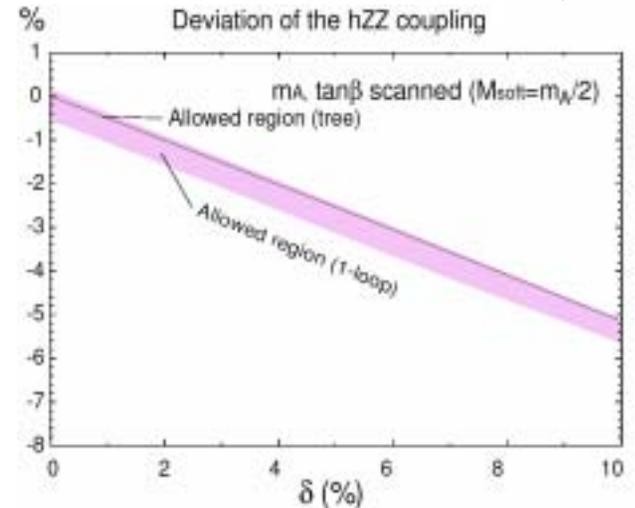
We consider :

- (1) loop corrections to the hVV vertex as well as the hhh vertex,
- (2) change of the hhh coupling from the tree level formula. J.F.Gunion, H.E.Haber,03

Possible range of the hhh and hVV couplings under the condition that perturbative unitarity of  $VV \rightarrow VV$  scattering amplitudes.  $(\lambda_i/4\pi \leq O(1))$

## Results

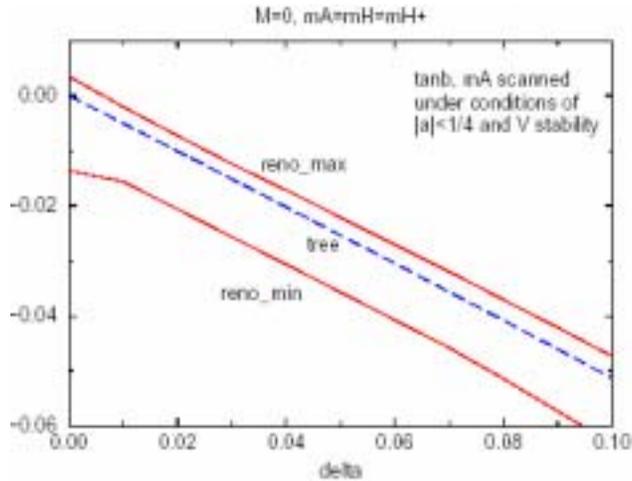
- One loop correction for hVV coupling is  $O(1\%)$ .
- Tree formula reduces the hhh coupling for  $\delta > 0$ , while one loop correction is mostly positive.



$$\delta \equiv \cos^2(\beta - \alpha)$$

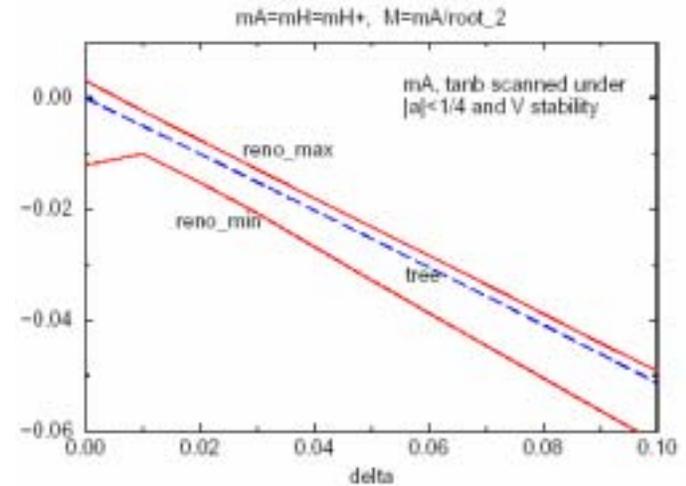
$$M = 0$$

Deviation of the hZZ coupling

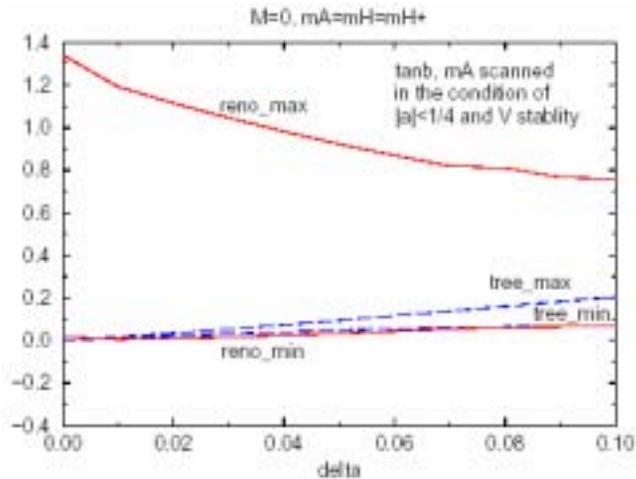


$$M = m_A/\sqrt{2}$$

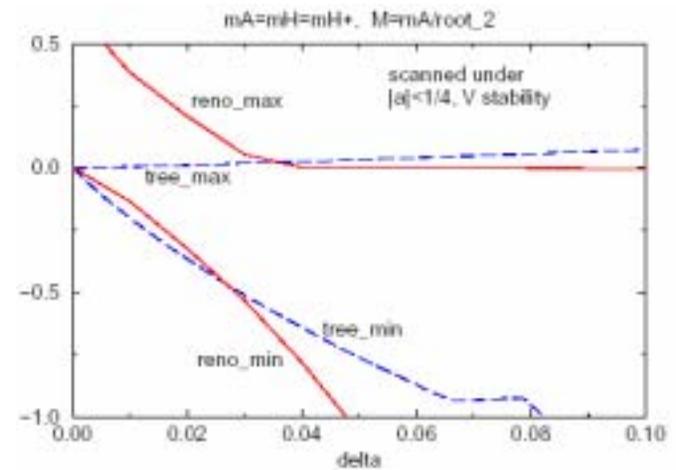
Deviation of the hZZ coupling



Deviation of the hhh coupling



Deviation of the hhh coupling



# Electroweak baryogenesis in 2HDM

- Baryogenesis: Explain the baryon-to-photon ratio from zero baryon number.  $n_B/s = 10^{-11} - 10^{-10}$
- A basic fact: B+L violation at high temperature in the SM.
- Two scenarios:
  - (1) B-L generation above the EW phase transition (leptogenesis, etc).
  - (2) Baryogenesis at the EW phase transition.
- EW baryogenesis is difficult in the minimal SM.
- 2HDM is a simple viable model. A.Nelson, D.B.Kaplan, A.G.Cohen, 91, M.Joyce, T.Prokopec, and N.Turok 91; J.M.Cline, K.Kainulainen, A.P.Vischer, 96

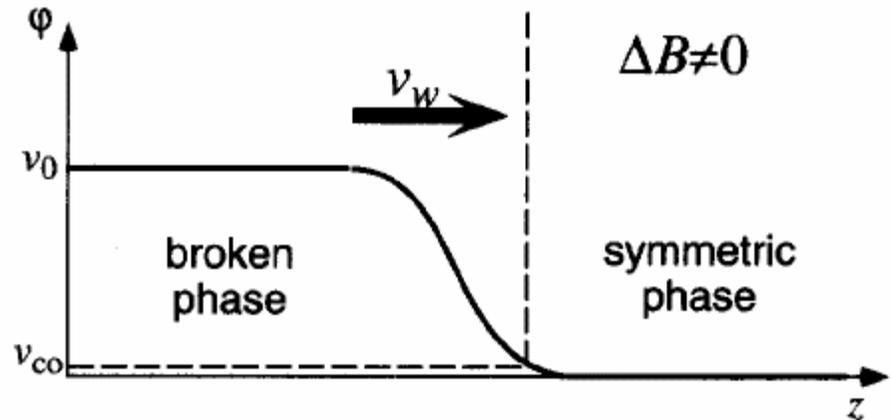
Connection between collider physics and cosmology

$$V_{eff}(\phi) \leftrightarrow V_T(\phi, T)$$

# Baryon number generation at the electroweak phase transition

- Strong first order phase transition.
- Expansion of a bubble.
- Charge flow of fermions due to CP violation at the wall.
- Baryon number violation in the symmetric phase.

In the minimal SM, the phase transition is not a strong first order, and CP violation from the Kobayashi-Maskawa phase is too small.



In 2HDM, we consider the following simplified case.

$$m_1^2 = m_2^2, \lambda_1 = \lambda_2, \leftrightarrow (\sin(\beta - \alpha) = \tan \beta = 1)$$

Vacuum expectation values at a finite temperature

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi(x) [i\theta(x)/2] \end{pmatrix} \quad \Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} 0 \\ \phi(x) [-i\theta(x)/2] \end{pmatrix}$$

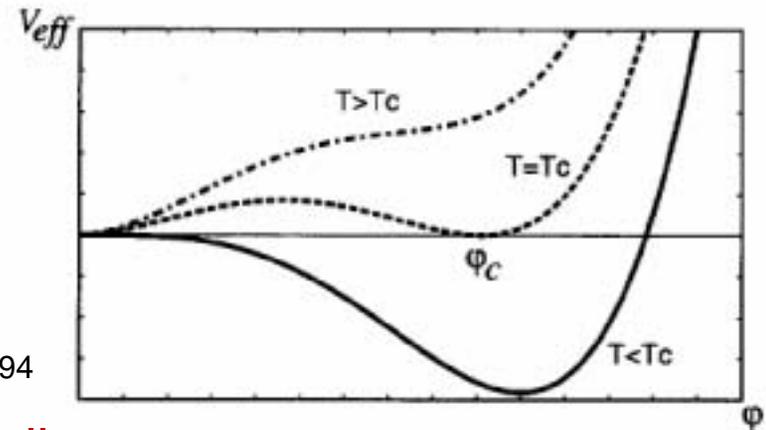
## Conditions for successful baryogenesis

### (1) Strong first order phase transition.

Not to erase the baryon number after the transition by the sphaleron process.

$$\phi_c/T_c > 1.4$$

K.Funakubo, A.Kakuto, K.Takenaga, 94,  
A.T.Davies, C.D.Froggatt, G.Jenkins, R.G.Moorhouse 94



### (2) Non-trivial phase rotation in the bubble wall.

Various possibilities:

Spontaneous CP violation only at finite temperature, explicit CP violation.

# Finite temperature effective potential in 2HDM

We calculate the finite temperature effective potential for the  $\phi$  direction to determine the first order phase transition.

For example, in the case of  $M=0$  and high temperature expansion,

$$V_T(\phi, T) = D(T^2 - T_0^2)\phi^2 - ET\phi^3 + \frac{\lambda_T}{4}\phi^4 + \dots$$

$$E = \frac{1}{12\pi v^3} (6m_W^3 + 3m_Z^3 + m_h^3 + m_H^3 + m_A^3 + 2m_{H^\pm}^3)$$

$$\phi_c/T_c = 2E/\lambda_{T_c}$$

Strong first order phase transition

<-> “Non-decoupling” effects of heavy Higgs bosons

<-> Correlation with a large corrections to the hhh coupling at zero temperature

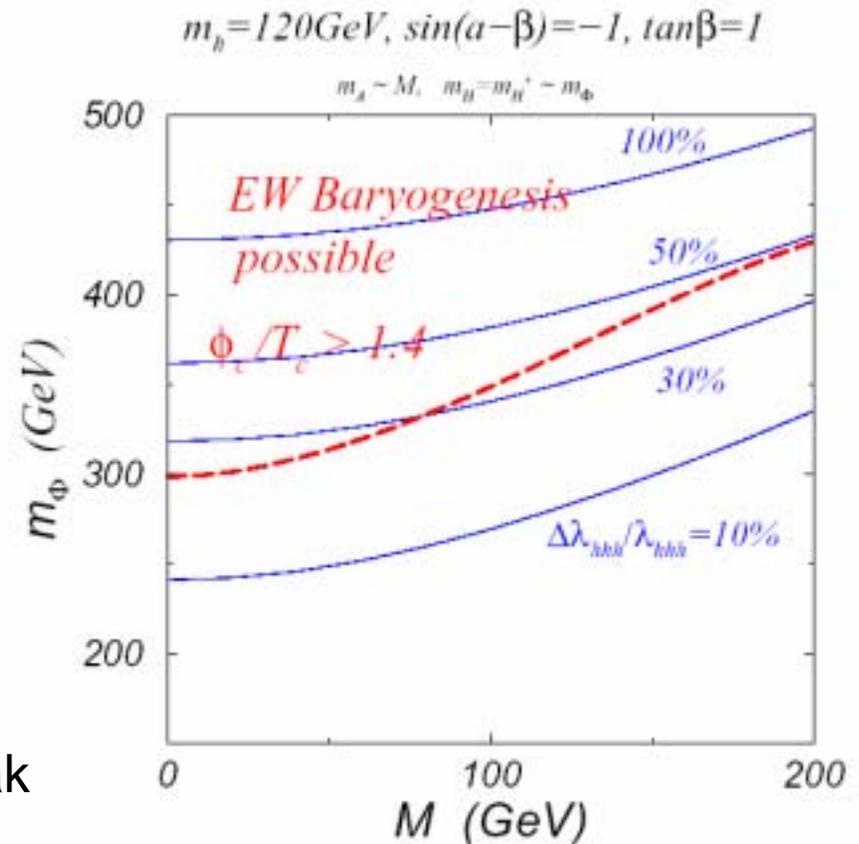
# Numerical calculation

S.Kanemura, Y.O., E.Senaha

We calculate the finite temperature effective potential without the high temperature expansion for  $M > 0$ .

We also study the loop correction to the hhh coupling constant.

The Higgs self-coupling receives correction of more than 30 % in the parameter region where the electroweak baryogenesis is possible.



Correlation between zero temperature and finite temperature potentials.  
Connection between cosmology and collider signals.

# Summary

- The triple Higgs coupling can receive  $O(1)$  radiative correction due to non-decoupling effects of heavy Higgs boson loops in 2HDM.
- A large correction to the self-coupling is expected, if the electroweak baryogenesis is realized in 2HDM.