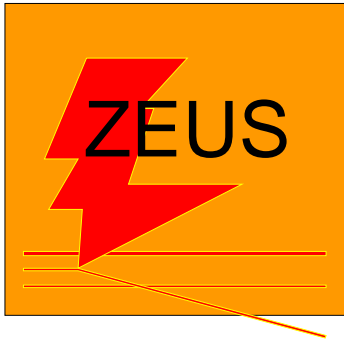


# ZEUS Parton Distribution Functions

## - Addition of Jet Data to ZEUS QCD Fit -



HERA-LHC PDF Working Group  
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- Introduction
- Putting Jet Data in the Fit
  - Procedure
  - Results
  - Extrapolation to LHC Scales
- Conclusions and Outlook

# ZEUS Parton Density Function Parameterisation

- Each parton momentum distribution is parameterised in  $x$  at the starting scale  $Q_0^2 = 7 \text{ GeV}^2$  using an expression of the form:

$$xf(x) = p_1 x^{p_2} (1-x)^{p_3} (1+p_5 x)$$

→ sensitive to low ( $p_2$ ), mid ( $p_5$ ) and high ( $p_3$ )  $x$  regions

- Parton densities are evolved in  $Q^2$  using the NLO DGLAP equations, and are convoluted with coefficient functions in the Roberts-Thorne Variable Flavour Number scheme  
 → List of parameters is fed to an evaluation function which calculates  $\chi^2$  based on the data and theory PDFs
- The following distributions are parameterised:

- |   |  |
|---|--|
| • $\underline{u\text{-valence } xu_v(x)}$ : | $p_{1u}, p_{2u}, p_{3u}, p_{5u}$                     |
| • $\underline{d\text{-valence } xd_v(x)}$ : | $p_{1d}, p_{2d}, p_{3d}, p_{5d}$                     |
| • $\underline{\text{total sea } xS(x)}$ :   | $p_{1S}, p_{2S}, p_{3S}, p_{5S}$                     |
| • $\underline{\text{gluon } xg(x)}$ :       | $p_{1g}, p_{2g}, p_{3g}, p_{5g}$                     |
| • $\underline{x\Delta = x(d - \bar{u})}$ :  | $p_{1\Delta}, p_{2\Delta}, p_{3\Delta}, p_{5\Delta}$ |

⇒  $4 \times 5 = 20$  possible free parameters !

# Parameter Constraints

- Fortunately, some parameters can be fixed ...

Parameter constraints in latest ZEUS-O (94-00) fit:

	$u_v$	$d_v$	<b>S</b>	<b>g</b>	$\Delta$
$p_1$	NO. SUM	NO. SUM	FREE	MOM. SUM	FIXED TO ZEUS-S
$p_2$	FREE	FIX TO $p_2u$	FREE	FREE	0.5
$p_3$	FREE	FREE	FREE	FREE	$p_3S + 2$
$p_5$	FREE	FREE	FIX TO 0	FREE	FIXED TO 0

- $p_1u, p_1d$  are fixed through number sum rules and  $p_1g$  through momentum sum rule
- $p_2\Delta = 0.5$ ,  $p_3\Delta (= p_3S + 2)$ ,  $p_5\Delta = 0$  as per MRST
- $p_2u$  is free BUT  $p_2u = p_2d$  for convergence of fit
- $p_5S = 0$  (simplifying form of sea) since little information above  $x > 0.4$

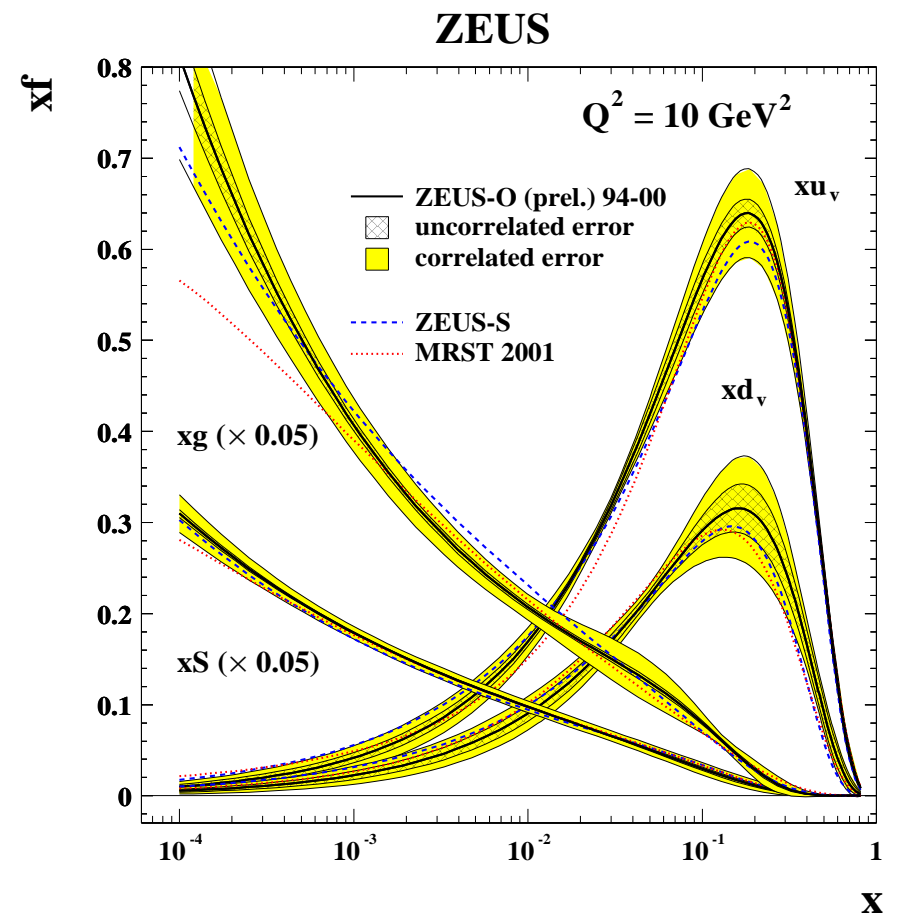
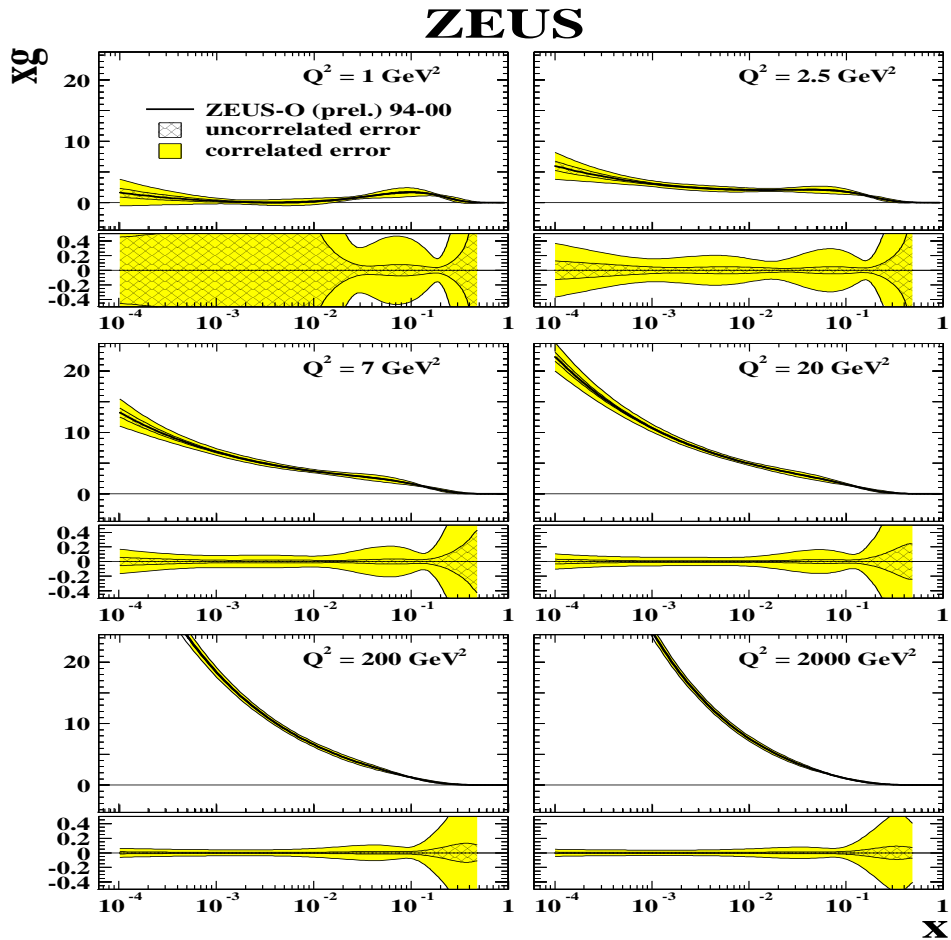
- ZEUS-O: 94-00 NC & CC DATA FROM ZEUS ONLY

- Uses some input from the ZEUS global (ZEUS-S) fit ( $p_1\Delta$ )
- Valence information comes mainly from high  $Q^2$  NC and CC data
- Low- $x$  sea and gluon comes from HERA  $F_2$  data

**BUT HIGH- $x$  GLUON IS VERY POORLY CONSTRAINED SINCE INFORMATION COMES ONLY FROM MOMENTUM SUM RULE**

# How Does This Show In The ZEUS-O Fits?

PUTTING JET DATA IN THE ZEUS QCD FIT, DESY, JUNE 2004



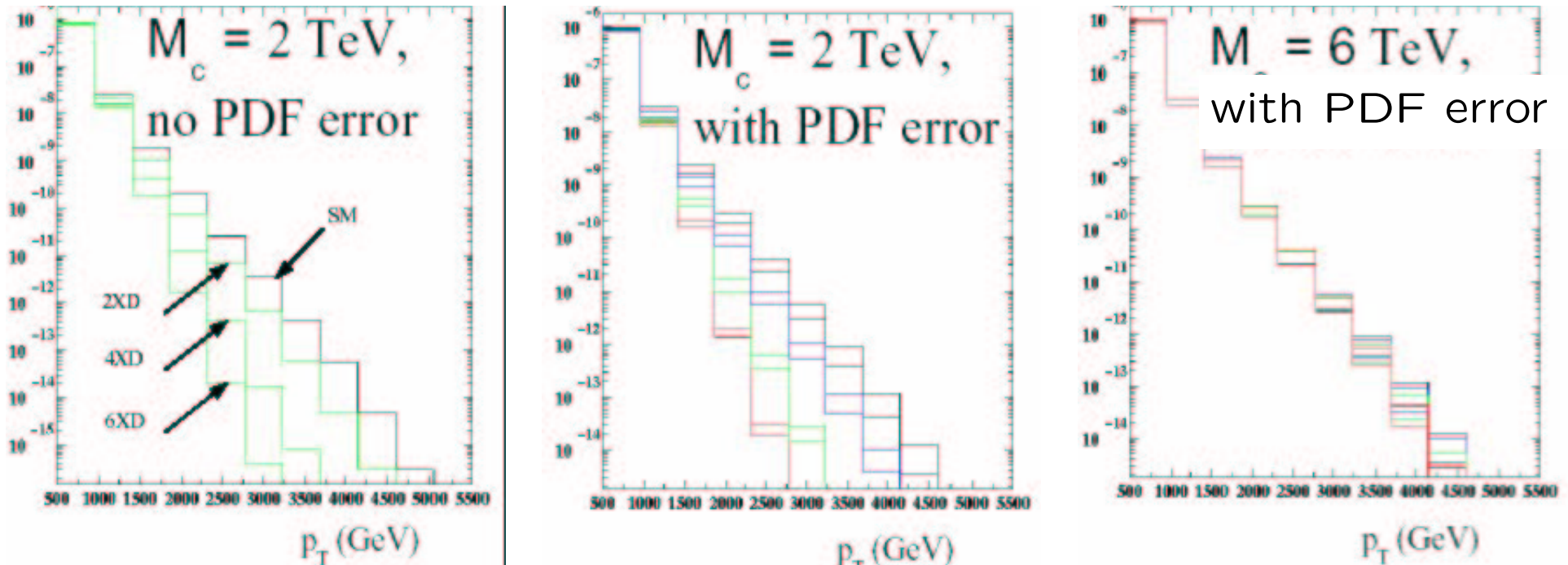
- Mid-to-high  $x$  gluon not well constrained  
 → because there is no data directly sensitive to high- $x$  gluon in ZEUS-O fit

# Effect of PDF Uncertainties on LHC Predictions

- Large PDF uncertainties (and in particular the gluon) has potentially serious consequences for the LHC

→ dominant uncertainty in production rates for many processes at LHC

EXAMPLE: Two-jet cross sections at the LHC sensitive to compactification scale of extra dimensions ( $M_C$ ) :- Ferrag et al.



- Discovery reach reduced from  $M_C \sim 5$  TeV  $\rightarrow \sim 2$  TeV
- PDF uncertainty comes mainly from large gluon uncertainty at high- $x$

# What Can We Do ?

## ADD JET DATA.....

We have added data from two distinct papers (both 1996-1997 data):

- INCLUSIVE JET DEEP INELASTIC SCATTERING  
(ZEUS Coll., Phys. Lett. B547 (2002) 164)

KINEMATIC REGION:  $\rightarrow Q^2 > 125 \text{ GeV}^2, E_T^B > 8 \text{ GeV}, -2 < \eta^B < 1.8$

- 9 cross sections available: differential in  $Q^2, E_T^B, \eta^B$  and double differential in  $E_T^B$  in 6 bins of  $Q^2$

- TWO-JET PHOTOPRODUCTION AT HIGH-ET  
(ZEUS Coll., Eur. Phys. J C23 (2002) 4)

KINEMATIC REGION:  $\rightarrow Q^2 < 1 \text{ GeV}^2, E_T^{jet1,2} > 14, 11 \text{ GeV}, -1 < \eta^{jet1,2} < 2.4$

- 12 cross sections available: double differential in  $E_T$  in 6 bins of  $\eta^{jet1,2}$   
(and for  $x_\gamma < 0.75$  and  $x_\gamma > 0.75$ )

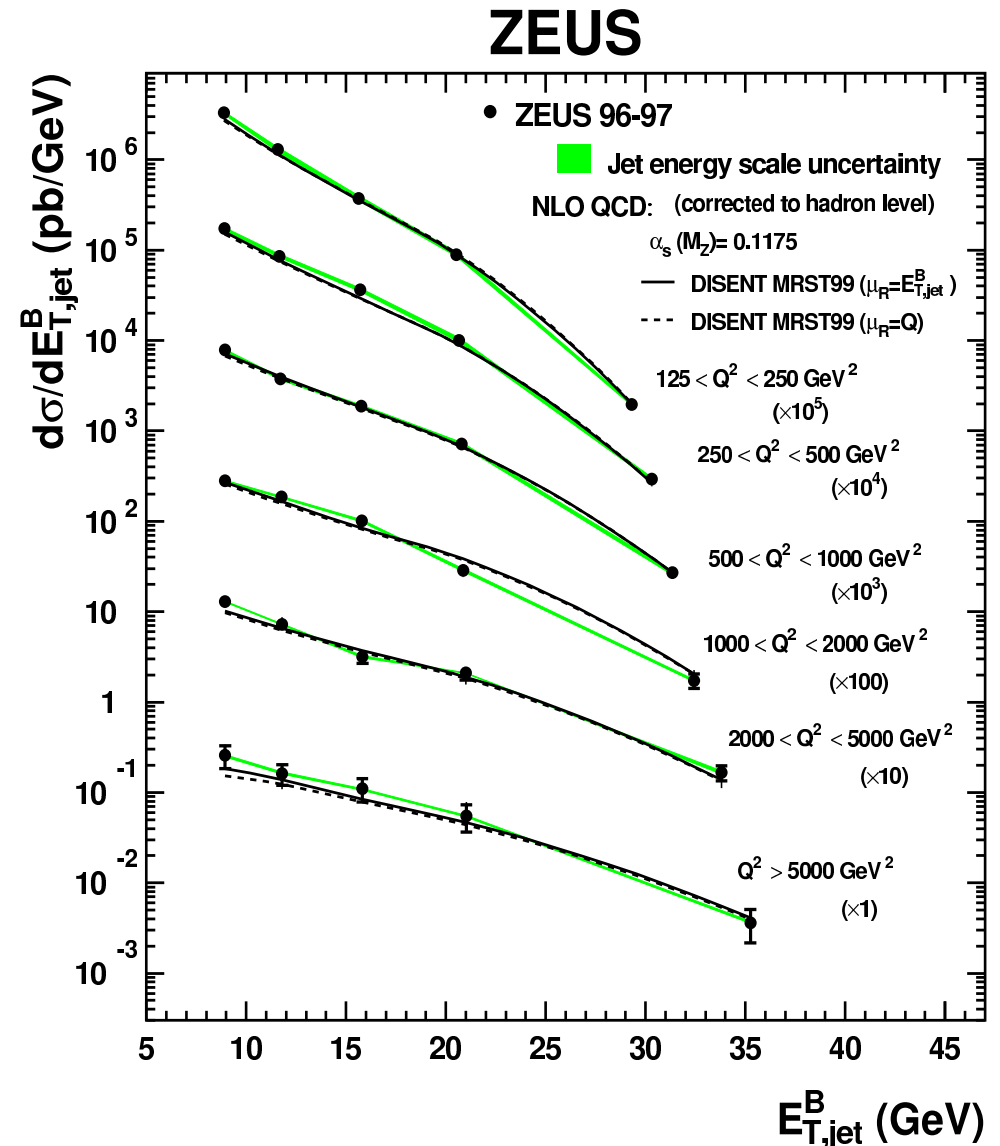
We have made a careful choice of cross sections most suitable for use in the ZEUS QCD fit  $\rightarrow$

# Inclusion of Inclusive DIS Jet Data

- INCLUSIVE JET DEEP INELASTIC SCATTERING  
(ZEUS Coll., Phys. Lett. B547 (2002) 164)

We have chosen to use only the 6 cross sections differential in  $E_{T,jet}^B$  in bins of  $Q^2$ . This avoids correlations between cross sections with same events

30 NEW DATA POINTS →

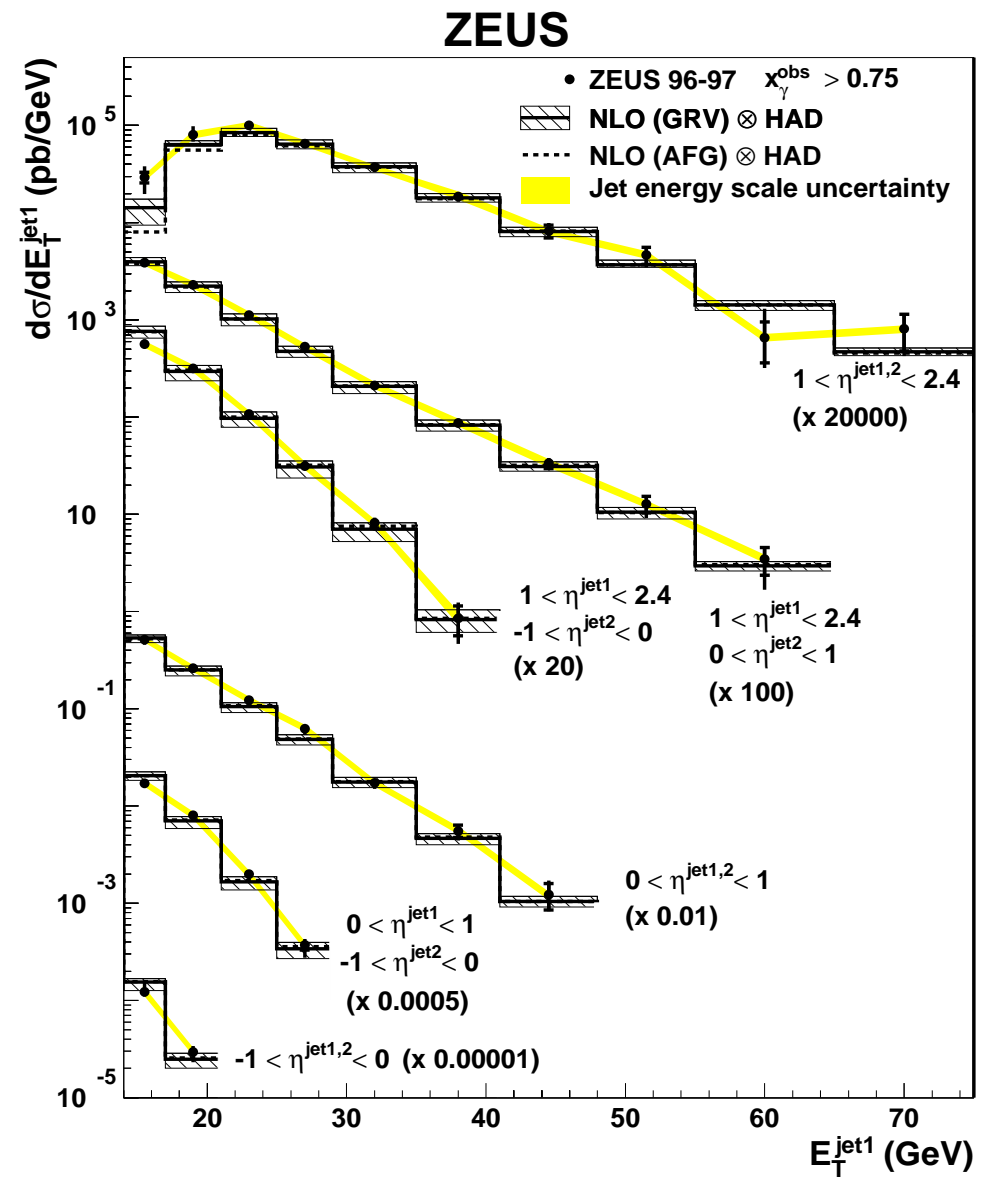
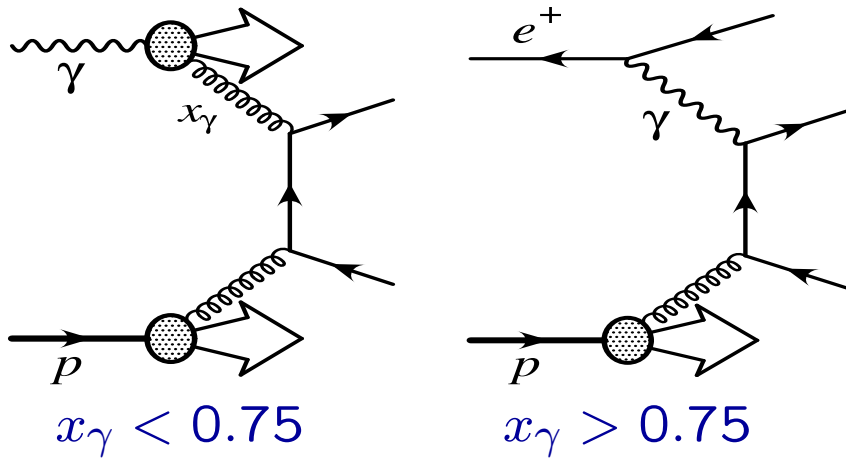


# Inclusion of Photoproduction Jet Data

- TWO-JET PHOTOPRODUCTION AT HIGH-ET  
 (ZEUS Coll., Eur. Phys. J C23 (2002) 4)

We have chosen only the 6 cross sections at high  $x_\gamma$  (to avoid complications from uncertainty in photon structure)

38 NEW DATA POINTS →





# Addition of Jet Data

## FIRST STAGE:

- Use NLO program to produce grid (in  $x, \mu_F^2$ ) of weights giving the perturbatively calculable part of cross section
  - Each weight is uniquely identified by  $x, \mu_F^2$  and  $\sigma$  bins as well as parton ID

## INCLUSIVE DEEP INELASTIC SCATTERING JET DATA

- NLO PROGRAM: DISENT
  - SCALES:  $\mu_R = E_T^{jet}, \mu_F = Q$
- Grids are  $200 \times 200$  in  $(x, Q^2)$

## TWO-JET PHOTOPRODUCTION DATA

- NLO PROGRAM: FRIXIONE-RIDOLFI
  - SCALES:  $\mu_R = \mu_F = E_T/2$  where  $E_T$  is summed transverse energy of final state partons
  - PHOTON PDF: AFG-MC PH
- Grids are  $200 \times 200$  in  $(x, (E_T/2)^2)$

# GRID Reproduction of the NLO Predictions

- We placed on ourselves, the requirement that the cross sections from the NLO programs should be reproducible to within  $\sim 1\%$

## DIS INCLUSIVE JET CROSS SECTIONS

→ All six double differential cross sections are reproducible to within 0.05% !!!

THIS IS A FACTOR OF 20 BETTER THAN WE ORIGINALLY REQUIRED!

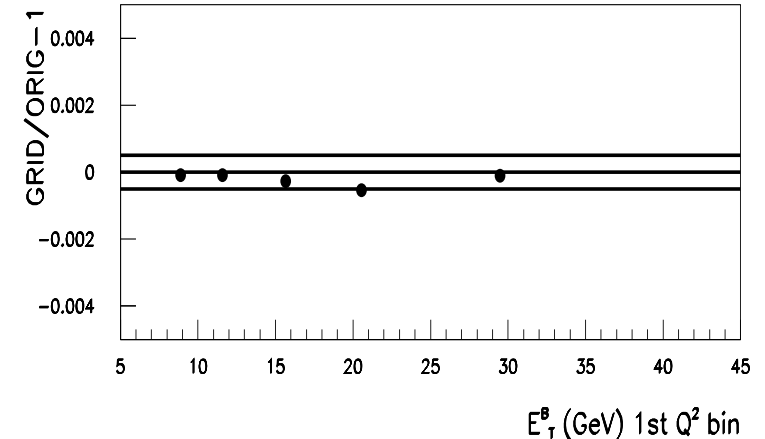
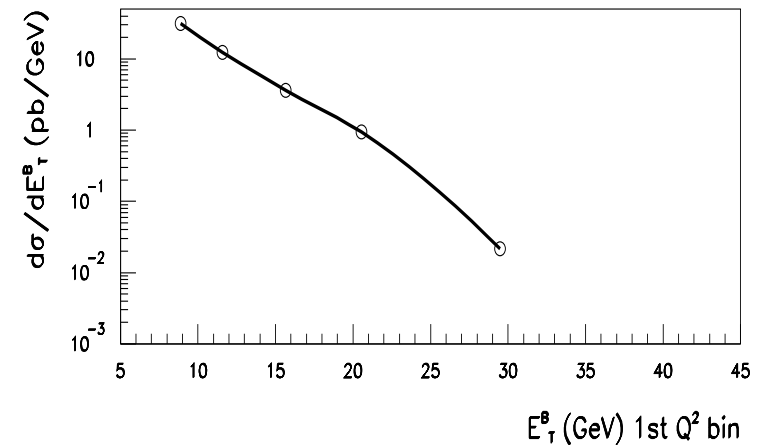
Typical example is shown opposite →

## $\gamma p$ TWO-JET CROSS SECTIONS

→ All high- $x_\gamma$  cross sections reproducible to within  $\sim 1\%$  (& usually within 0.5%)

SATISFIES OUR REQUIREMENT

Incl. Jet XSections Parton Level CTEQ6 (Gridnew/Orig,50M)  $Q^2 > 125 \text{ GeV}^2$



# Addition of Jet Data

## SECOND STAGE:

- In the QCD fit program, convolute NLO weights with ZEUS PDFs (evaluated using the evolution program QCDNUM) to give predicted cross sections according to:

$$d\sigma_{\text{jet}} = \sum_{a=q,\bar{q},g} \int dx f_a(x, \mu_F^2) d\hat{\sigma}_a(x, \alpha_s(\mu_R), \mu_F^2) \times (1 + \delta_{had})$$

→ where  $\hat{\sigma}_a(x, \alpha_s(\mu_R), \mu_F^2)$  is the weight

→ where  $f_a(x, \mu_F^2)$  is the PDF for parton  $a$  at  $x$  and scale  $\mu_F$

NOTE that the parton-level predictions were multiplied by the hadronisation corrections quoted in the relevant papers. The inclusive DIS jet cross sections were also multiplied by correction factors for  $Z^0$  exchange.

- Add relevant terms to the  $\chi^2$
- Treatment of uncertainties (see “correlated systematics” talk):
  - UNCORRELATED: statistical and uncorrelated systematic
  - CORRELATED: calorimeter energy scale and luminosity determination

# Where Might These Data Have An Impact?

- Both the inclusive jet DIS and the two-jet photoproduction data have Bjorken- $x$  values of  $\sim 0.01 - 0.1$ 
  - expect some impact on the mid-to-high- $x$  gluon
  - may also expect some impact on the mid-to-high- $x$  sea ?

## PARAMETER SUMMARY

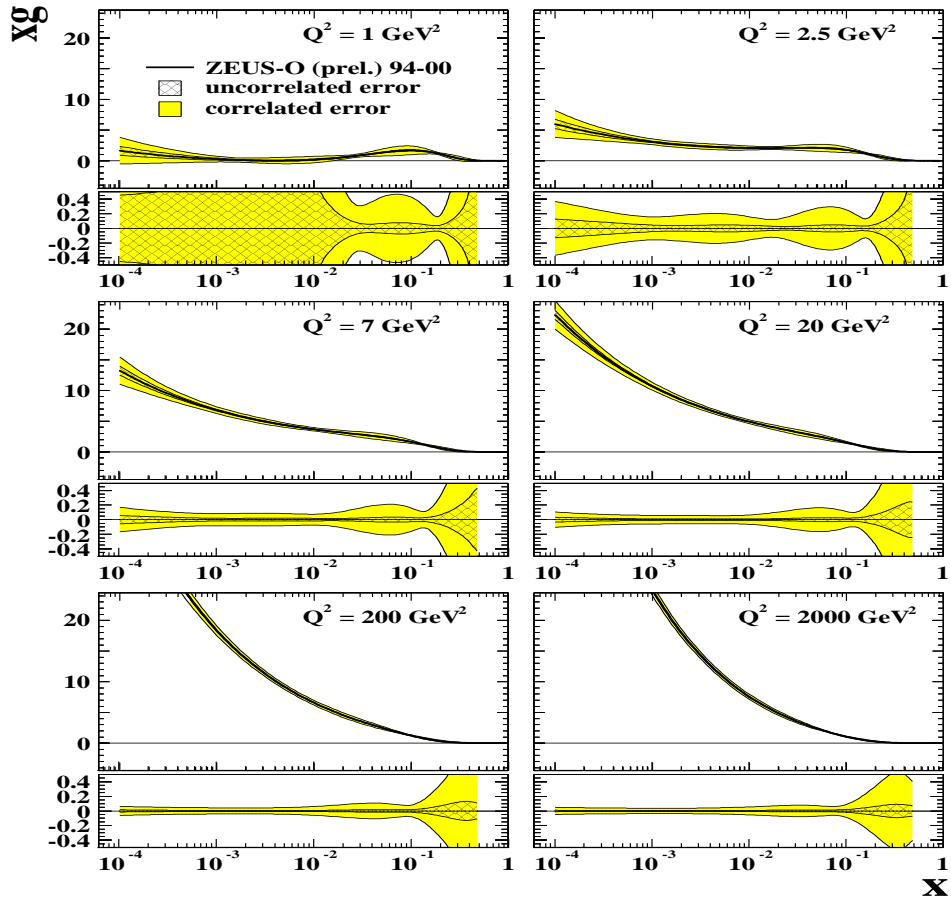
	$u_v$	$d_v$	<b>S</b>	<b>g</b>	$\Delta$
$p_1$	NO. SUM	NO. SUM	FREE	MOM. SUM	FIXED TO ZEUS-S
$p_2$	FREE	$p_2 d = p_2 u$	FREE	FREE	0.5
$p_3$	FREE	FREE	FREE	FREE	$p_3 S + 2$
$p_5$	FREE	FREE	FIXED = 0	FREE	FIXED TO 0

# Gluon Distribution

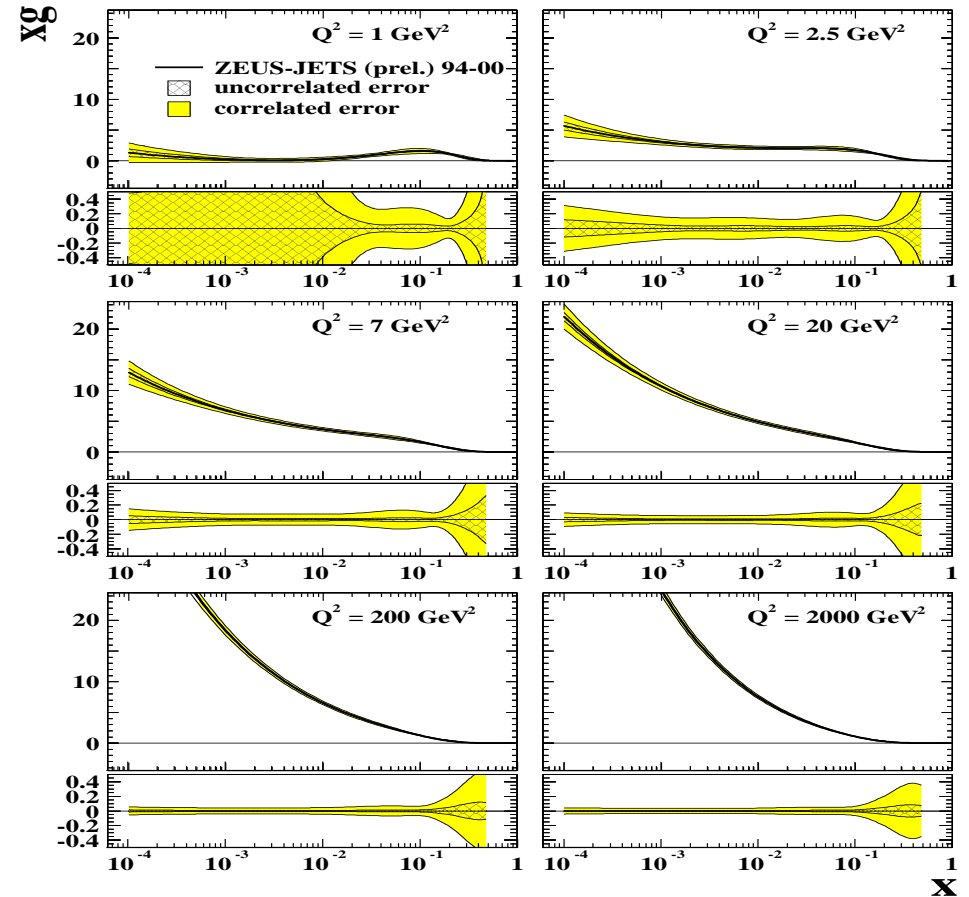
WITHOUT JETS

WITH JETS

**ZEUS**



**ZEUS**

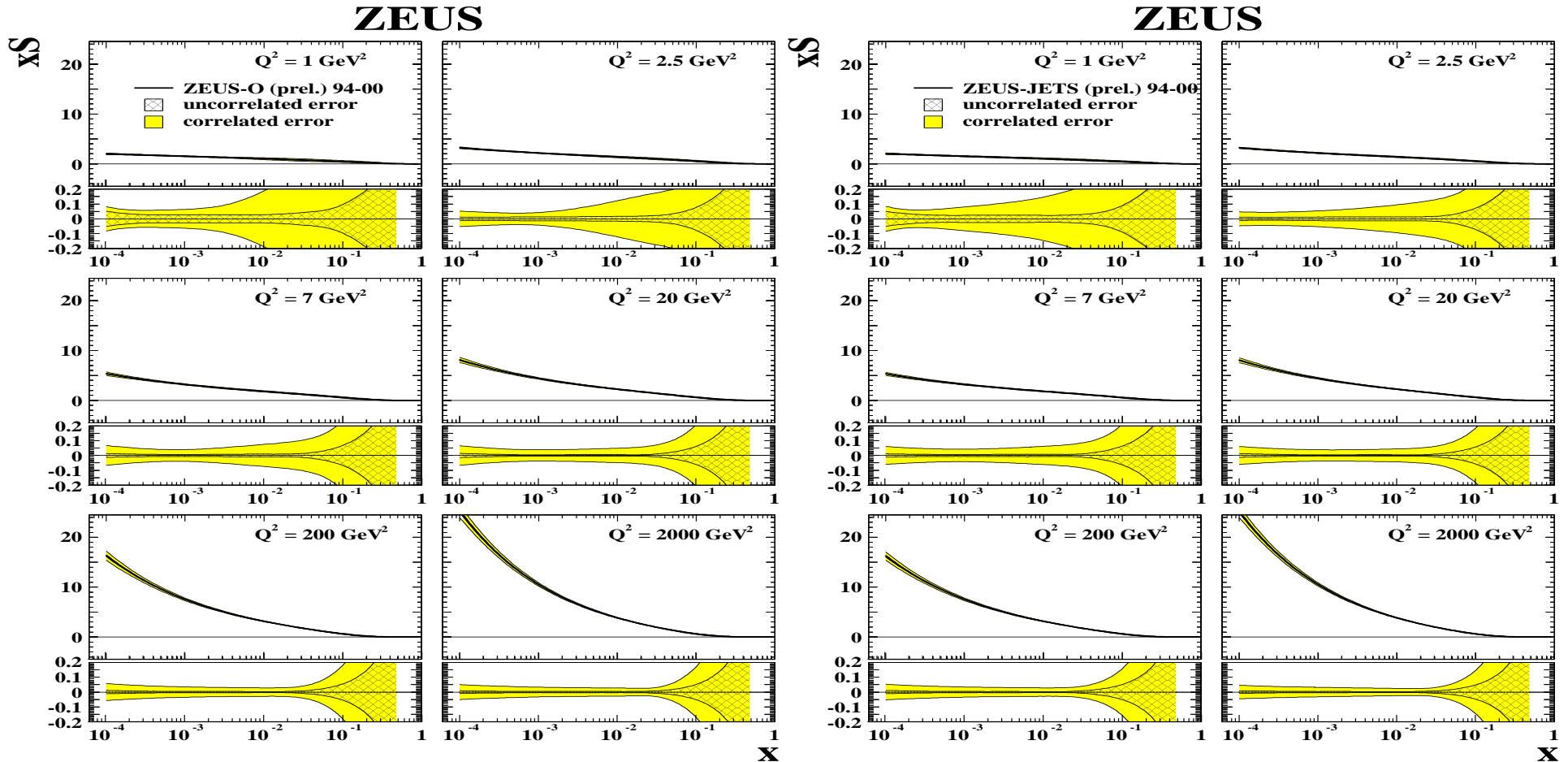


- Significant improvement to constraint on gluon PDF at mid-to-high- $x$  when jet data added!!!

# Sea Distribution

WITHOUT JETS

WITH JETS



- Some effect on the sea distribution also  $\rightarrow$  only really noticeable at low  $Q^2$

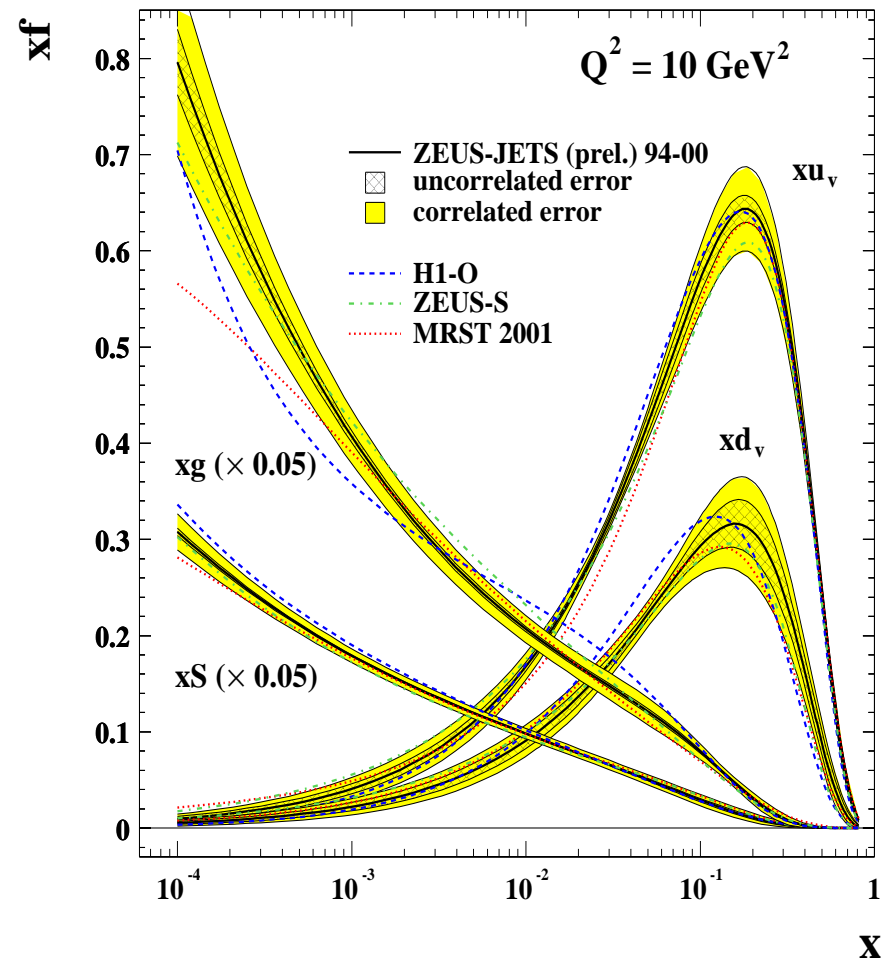
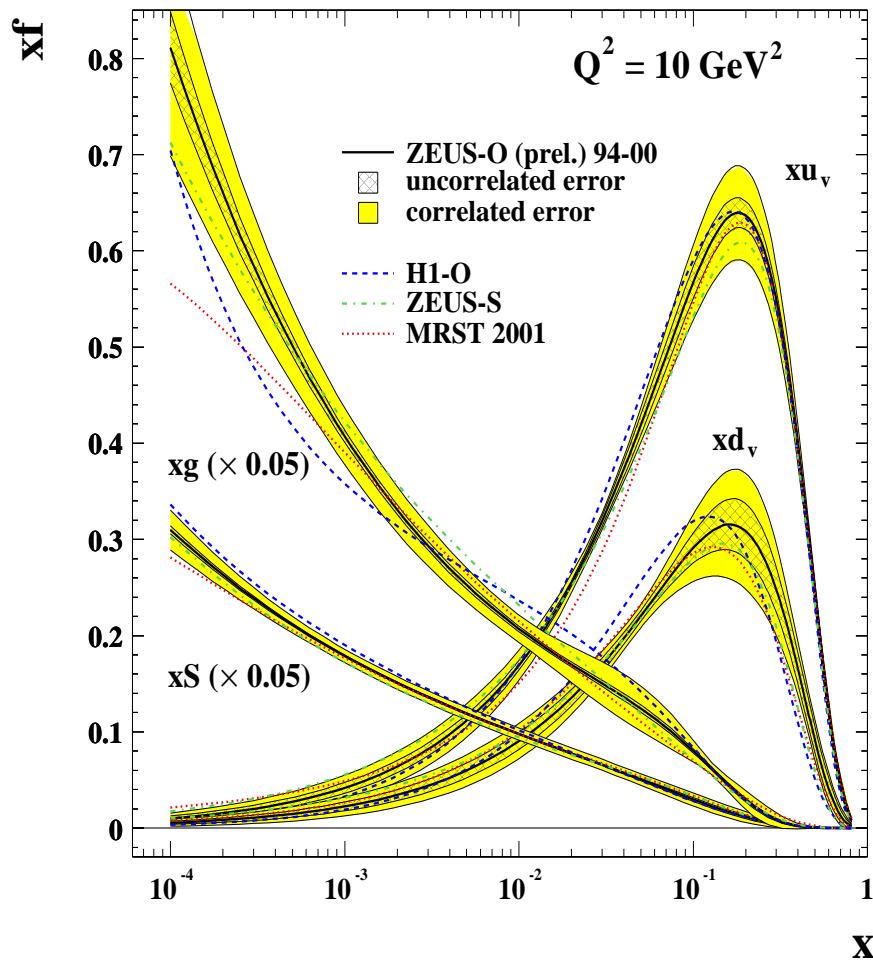
# ZEUS Fit - vs MRST/ZEUS-S/H1

WITHOUT JETS

WITH JETS

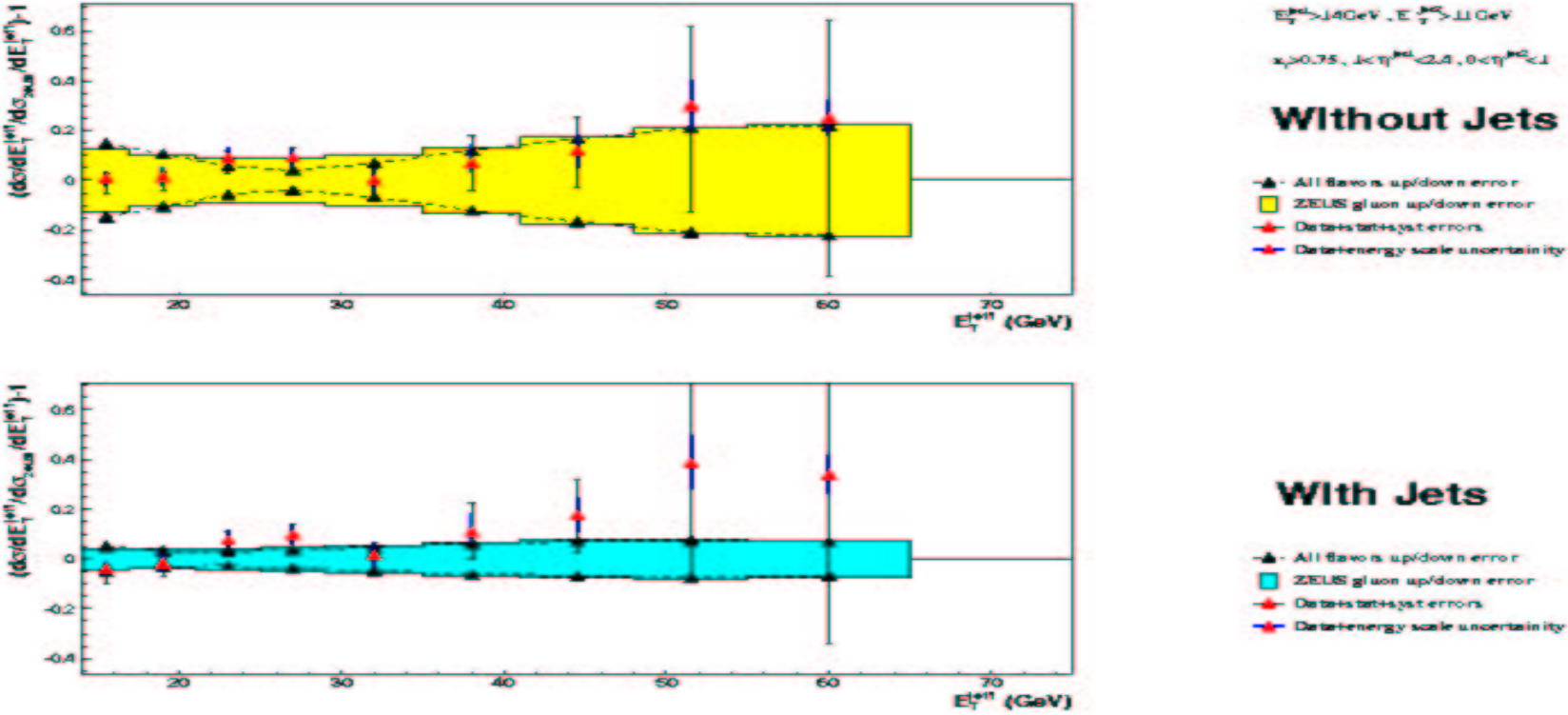
ZEUS

ZEUS



# Uncertainty on Cross Section Measurement

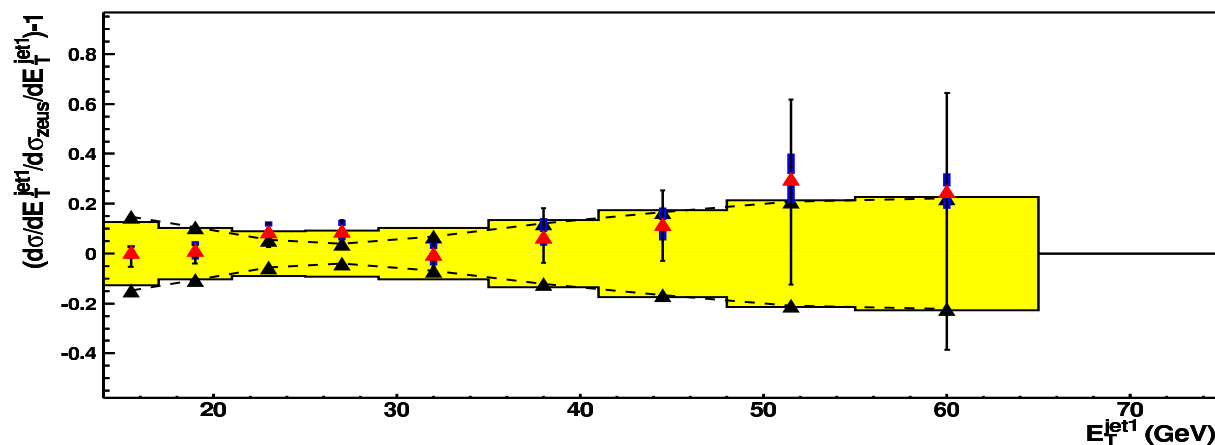
EXAMPLE:  $1 < \eta^{jet1} < 2.4, 0 < \eta^{jet2} < 1, x_\gamma > 0.75$



- Prediction for a typical high- $E_T$  two-jet photoproduction cross section included in the ZEUS-JETS fit, from ZEUS-O and ZEUS-JETS PDFs  
 → Reduction in uncertainty on cross section (from gluon PDF) is significant !



# Potential for Further Improvement

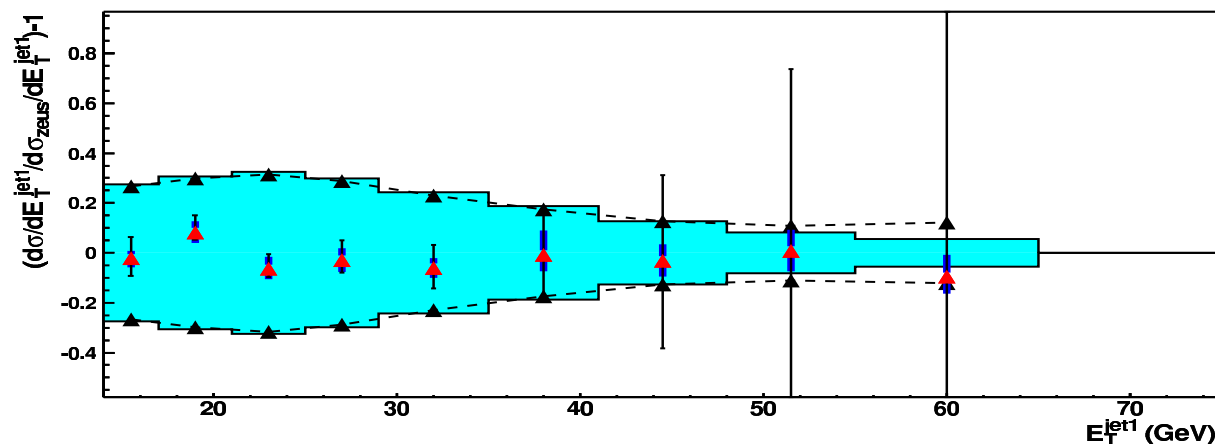


$E_T^{jet1} > 14 \text{ GeV}, E_T^{jet2} > 11 \text{ GeV}$

$x_\gamma > 0.75, 1 < \eta^{jet1} < 2.4, 0 < \eta^{jet2} < 1$

## Published

- ▲ All flavors up/down error
- ZEUS gluon up/down error
- ▲ Data+stat+syst errors
- ▲ Data+energy scale uncertainty



$E_T^{jet1} > 15 \text{ GeV}, E_T^{jet2} > 10 \text{ GeV}$

$x_\gamma < 0.75, 2 < \eta^{jet1} < 3, 2 < \eta^{jet2} < 3$

## Optimised

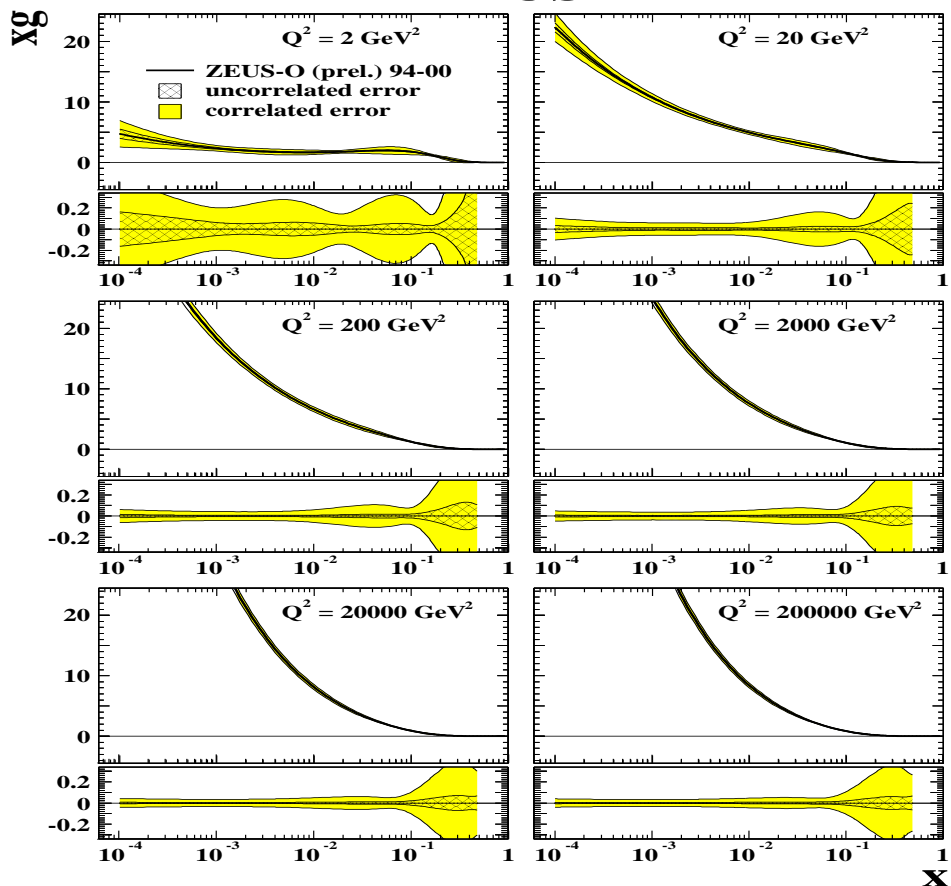
- ▲ All flavors up/down error
- ZEUS gluon up/down error
- ▲ Data+stat+syst errors (est)
- ▲ Data+energy scale uncertainty (est)

- So far, have only used 1996-1997 data → statistically limited at high- $E_T$  (high- $x$ )
- With rest of HERA I and HERA II data, potential to measure cross sections where sensitivity to high- $x$  gluon is significant

# Extrapolation to LHC Energies

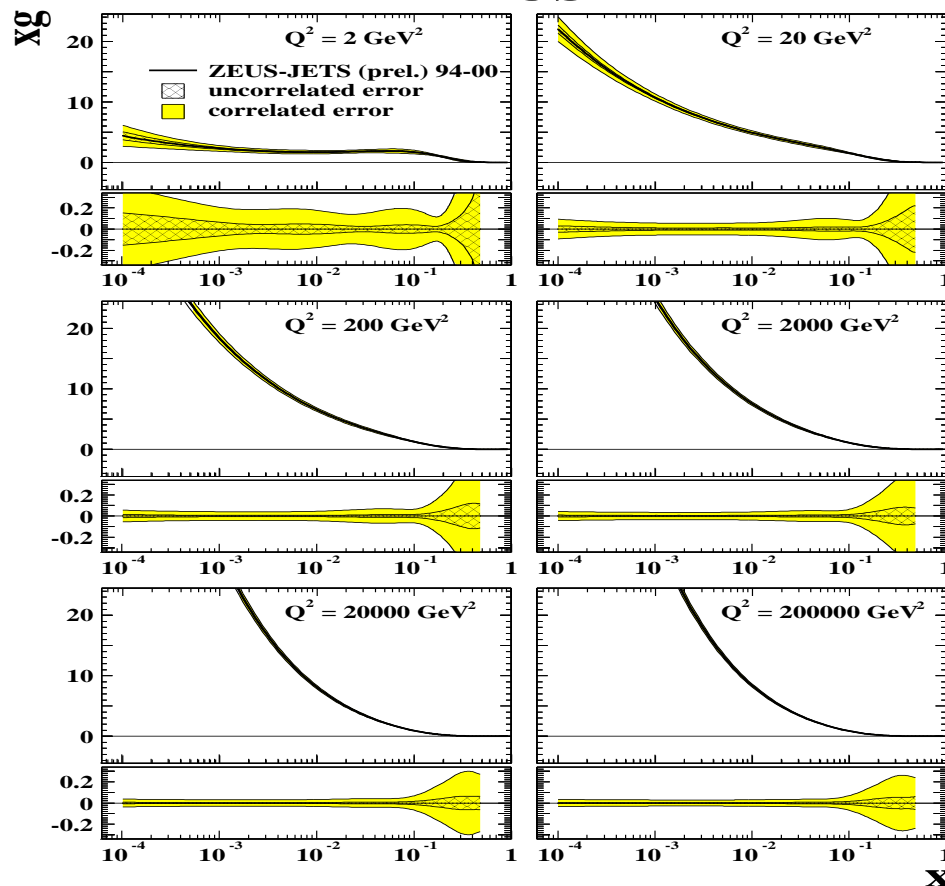
WITHOUT JETS

ZEUS



WITH JETS

ZEUS



- Uncertainty in high- $x$  ( $> 0.1$ ) gluon can still be large, even at LHC scales  
 → dominant uncertainty in production rates for many processes at LHC
- Addition of HERA jet data provides visible improvement even at LHC energies

# Conclusions and Outlook

- Jet data from DIS and  $\gamma p$  have been added to the ZEUS QCD fit
  - This is the first time that jet data has been rigorously added in any QCD fit!
  - The mid-to-high- $x$  gluon is now measured using HERA data, rather than being set only by the momentum sum rule
- Addition of ZEUS jet data constrains high- $x$  gluon significantly (PLUS a visible improvement even at LHC energies)
  - LHC predictions become less uncertain and things will only get better!!!
- Still many interesting avenues to explore
  - We still have more HERA I jet data to add
  - Potential for measurement of optimised cross sections
  - HERA II DATA !!!
- In principle, this method (modified!) can be used for LHC (and Tevatron !) jet data
  - Inclusion of LHC high- $E_T$  jet data in QCD fits !!!