

# Diffraction parton distributions and absorptive corrections to $F_2$

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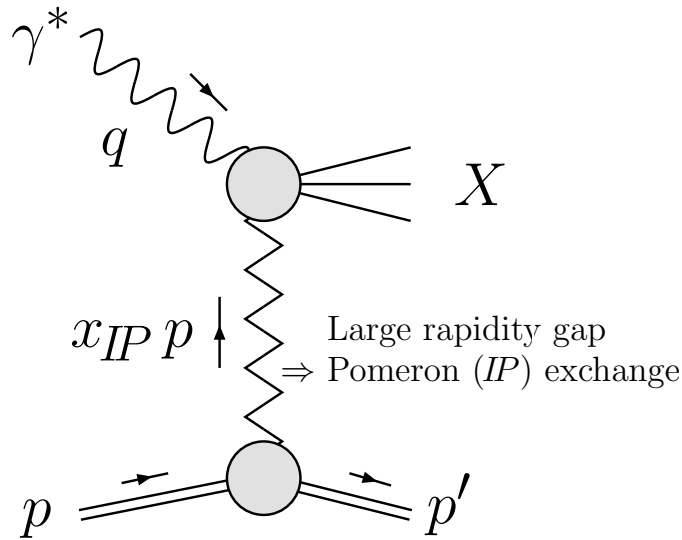
University of Durham, UK

# Outline of talk

- Diffractive structure function ( $F_2^{D(3)}$ ) at HERA
- ‘Traditional’ extraction of diffractive parton distributions from  $F_2^{D(3)}$
- **New** improved perturbative QCD approach
- *Application:* absorptive corrections to inclusive  $F_2$  from AGK cutting rules
- Simultaneous  $F_2 + F_2^{D(3)}$  analysis

In collaboration with A.D. Martin and M.G. Ryskin

# Diffractive DIS kinematics



- $q^2 \equiv -Q^2$

- $W^2 \equiv (q + p)^2 = -Q^2 + 2 p \cdot q$

$$\Rightarrow x_B \equiv \frac{Q^2}{2 p \cdot q} = \frac{Q^2}{Q^2 + W^2}$$

(fraction of proton's momentum carried by struck quark)

- $t \equiv (p - p')^2 \approx 0, (p - p') \approx x_{IP} p$

- $M_X^2 \equiv (q + p - p')^2 = -Q^2 + x_{IP}(Q^2 + W^2)$

$$\Rightarrow x_{IP} = \frac{Q^2 + M_X^2}{Q^2 + W^2} \text{ (fraction of proton's momentum carried by Pomeron)}$$

- $\beta \equiv \frac{x_B}{x_{IP}} = \frac{Q^2}{Q^2 + M_X^2}$  (fraction of Pomeron's momentum carried by struck quark)

# Diffractive structure function $F_2^{D(3)}$

- Diffractive cross section (integrated over  $t$ ):

$$\frac{d^3\sigma^D}{d\boldsymbol{x}_{\mathbb{P}} d\beta dQ^2} = \frac{2\pi\alpha_{\text{em}}^2}{\beta Q^4} [1 + (1 - y)^2] \sigma_r^{D(3)}(\boldsymbol{x}_{\mathbb{P}}, \beta, Q^2),$$

where  $y = Q^2/(x_B s)$ ,  $s = 4E_e E_p$ , and

$$\sigma_r^{D(3)} = F_2^{D(3)} - \frac{y^2}{1 + (1 - y)^2} F_L^{D(3)} \approx F_2^{D(3)}(\boldsymbol{x}_{\mathbb{P}}, \beta, Q^2),$$

for small  $y$  and/or small  $F_L^{D(3)}/F_2^{D(3)}$

- Measurements of  $F_2^{D(3)} \Rightarrow$  *diffractive* parton distributions (**D**PDFs)  $a^D(\boldsymbol{x}_{\mathbb{P}}, \beta, Q^2) = q^D$  or  $g^D$

# Collinear factorisation in DDIS

$$\frac{d\sigma^{\gamma^*p}}{dx_{IP}} = \sum_{a=q,g} \int_0^1 d\beta' a^D(x_{IP}, \beta', Q^2) \hat{\sigma}^{\gamma^*a}$$

- $a^D(x_{IP}, \beta', Q^2)$  satisfy **DGLAP** evolution in  $Q^2$
- $\hat{\sigma}^{\gamma^*a}$  **same** as in **inclusive** DIS
- **Proven** to hold for **all** diffractive DIS processes (Collins)
- Can extend to **hadron-hadron** collisions, but need rapidity gap ‘**survival probability**’ due to multi-Pomeron exchange (Kaidalov, Khoze, Martin, Ryskin)

# 'Traditional' extraction of DPDFs

- Assume Regge factorisation:

$$F_2^{D(3)}(x_{IP}, \beta, Q^2) = f_{IP}(x_{IP}) F_2^{IP}(\beta, Q^2)$$

- Pomeron flux factor from Regge phenomenology:

$$f_{IP}(x_{IP}) = \int_{t_{\text{cut}}}^{t_{\text{min}}} dt \frac{e^{B_{IP} t}}{x_{IP}^{2\alpha_{IP}(t)-1}} \quad (\alpha_{IP}(t) = \alpha_{IP}(0) + \alpha'_{IP} t)$$

Fits to  $F_2^{D(3)}$  data give  $\alpha_{IP}(0) > 1.08$  (value from soft hadron data)  
 $\implies$  *effective* Pomeron intercept

- Evaluate Pomeron structure function  $F_2^{IP}(\beta, Q^2)$  from quark singlet  $\Sigma^{IP}(\beta, Q^2)$  and gluon  $g^{IP}(\beta, Q^2)$  Pomeron PDFs DGLAP-evolved from *arbitrary polynomial input* at scale  $Q_0^2$

# New perturbative QCD approach

- Pomeron singularity not a *pole* but a *cut* (Lipatov)  
⇒ **continuous** number of components of **size**  $1/\mu$ :

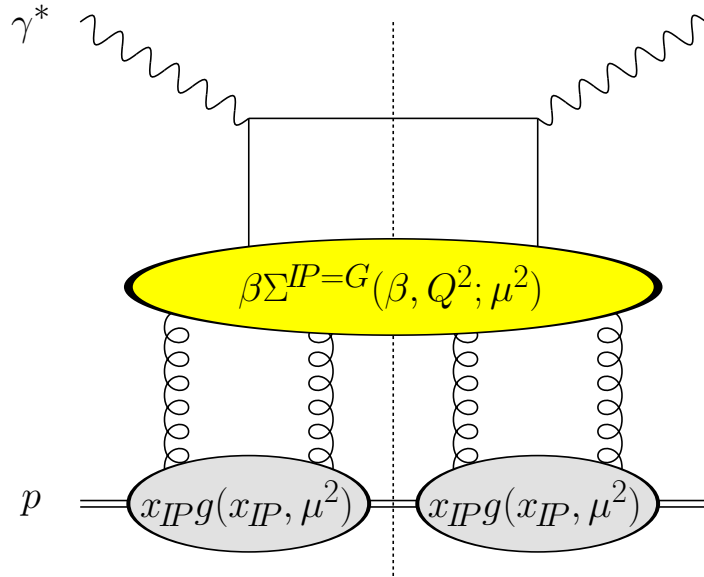
$$F_{2,P}^{D(3)}(x_{IP}, \beta, Q^2) = \int_{Q_0^2}^{Q^2} d\mu^2 f_{IP}(x_{IP}; \mu^2) F_2^{IP}(\beta, Q^2; \mu^2)$$

- Perturbative Pomeron represented by **two  $t$ -channel gluons** in colour singlet:

$$f_{IP=G}(x_{IP}; \mu^2) = \frac{1}{x_{IP}} \left[ \frac{\alpha_S(\mu^2)}{\mu^2} x_{IP} g(x_{IP}, \mu^2) \right]^2$$

where  $g(x_{IP}, \mu^2)$  is the (integrated) gluon distribution of the proton

# New perturbative QCD approach



- $F_2^{IP}(\beta, Q^2; \mu^2)$  calculated from quark singlet  $\Sigma^{IP}(\beta, Q^2; \mu^2)$  and gluon  $g^{IP}(\beta, Q^2; \mu^2)$  DGLAP-evolved from an input scale  $\mu^2$  up to  $Q^2$

- Get **input** Pomeron PDFs  $\Sigma^{IP}(\beta, \mu^2; \mu^2)$  and  $g^{IP}(\beta, \mu^2; \mu^2)$  from **leading-order Feynman diagrams**
- Calculate using light-cone wave functions of the photon (Wüsthoff):

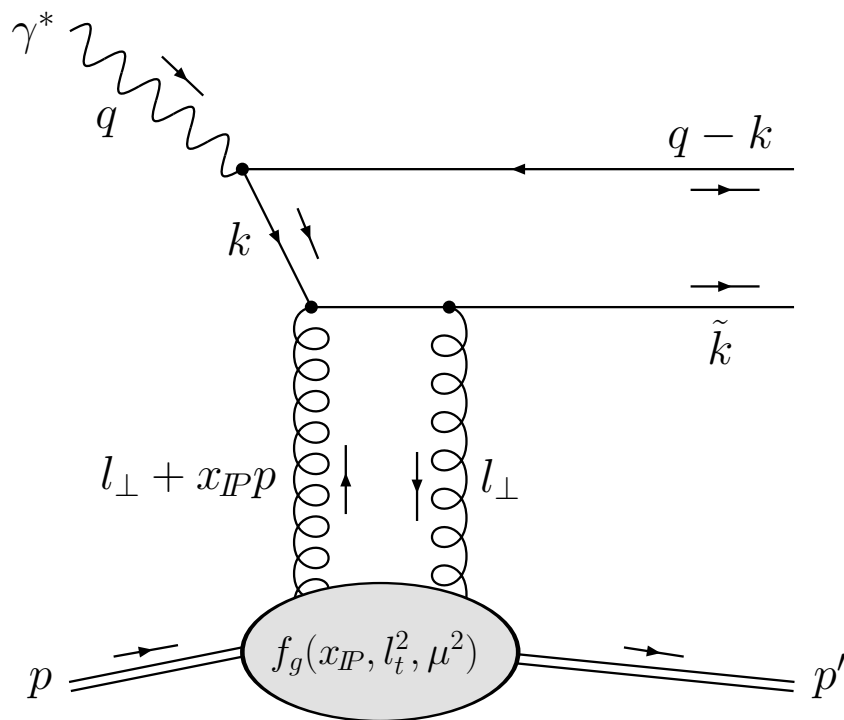
$$\sigma_{T,L}^{\gamma^* p} \sim \int d\alpha \int d^2 \mathbf{k}_t |\Psi_{T,L}(\alpha, \mathbf{k}_t)|^2 \hat{\sigma}^2$$



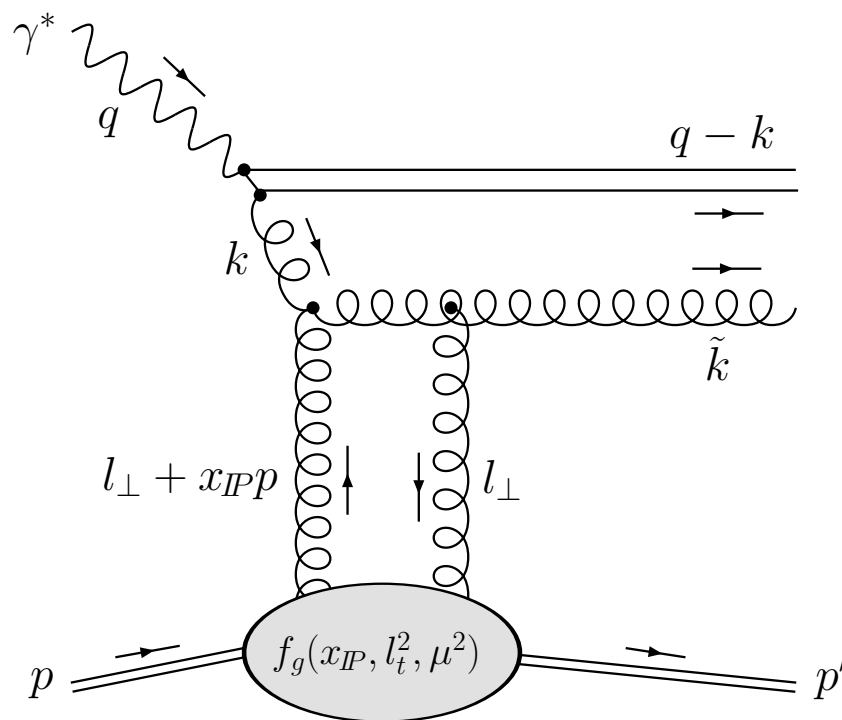
# Two-gluon Pomeron

- Work in strongly-ordered limit:  $l_t \ll k_t \ll Q$

Quark dipole



Effective gluon dipole



$$\beta \Sigma^{IP=G}(\beta, \mu^2; \mu^2) = c_{q/G} \beta^3 (1 - \beta)$$

$$\beta' g^{IP=G}(\beta', \mu^2; \mu^2) = c_{g/G} (1 + 2\beta')^2 (1 - \beta')^2$$

# Other contributions to $F_2^{D(3)}$

$$F_2^{D(3)} = F_{2,P}^{D(3)} + F_{2,NP}^{D(3)} + F_{L,P}^{D(3)} + F_{2,\mathcal{R}}^{D(3)}$$

- **Non-perturbative** contribution ( $\mu < Q_0$ ,  $\alpha_{IP}(0) = 1.08$ ):

$$F_{2,NP}^{D(3)} = f_{IP=NP}(x_{IP}) F_2^{IP=NP}(\beta, Q^2; Q_0^2)$$

- **Twist-four** contribution:

$$F_{L,P}^{D(3)} = \left( \int_{Q_0^2}^{Q^2} d\mu^2 \frac{\mu^2}{Q^2} f_{IP=G}(x_{IP}; \mu^2) \right) c_{L/G} \beta^3 (2\beta - 1)^2$$

- **Secondary Reggeon** contribution ( $\alpha_{\mathcal{R}}(0) = 0.50$ ):

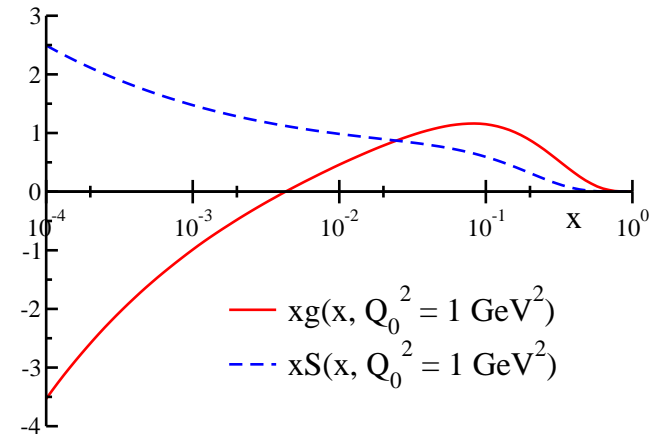
$$F_{2,\mathcal{R}}^{D(3)} = c_{\mathcal{R}} f_{\mathcal{R}}(x_{IP}) F_2^{\pi}(\beta, Q^2)$$

# Problem: $x_{IP} g(x_{IP}, \mu^2)$ at low $\mu^2$

- $f_{IP=G}(x_{IP}; \mu^2) \propto [x_{IP} g(x_{IP}, \mu^2) / \mu^2]^2$   
 $\Rightarrow$  dominant contribution from **low** scales  
 $\mu \sim Q_0 \sim 1 \text{ GeV}$
- $F_2^{D(3)}$  data need  $x_{IP} g(x_{IP}, \mu^2) \sim x_{IP}^{1-\alpha_{IP}(0)}$   
 with  $\alpha_{IP}(0) > 1.08$

● But ...

MRST2001 NLO proton PDFs



## Solutions:

1. Parameterise with simplified form:  $x_{IP} g(x_{IP}, \mu^2) \propto x_{IP}^{-\lambda}$
2. Introduce Pomeron composed of **two sea quarks** in a colour singlet:

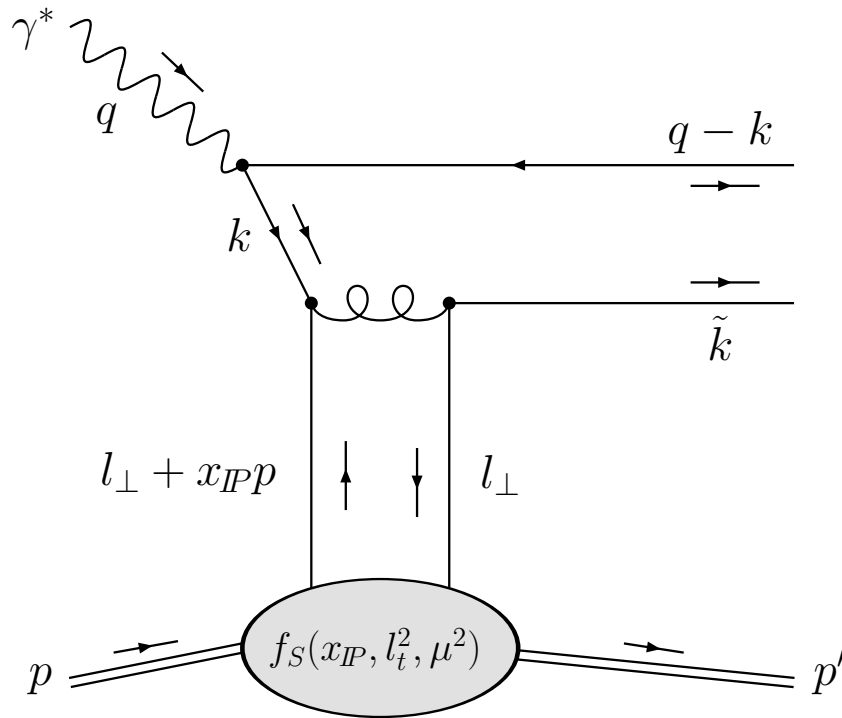
$$f_{IP=S}(x_{IP}; \mu^2) = \frac{1}{x_{IP}} \left[ \frac{\alpha_S(\mu^2)}{\mu^2} x_{IP} S(x_{IP}, \mu^2) \right]^2$$

and interference term with two-gluon Pomeron (set  $x_{IP} g = 0$  if -ve)

# Two-quark Pomeron

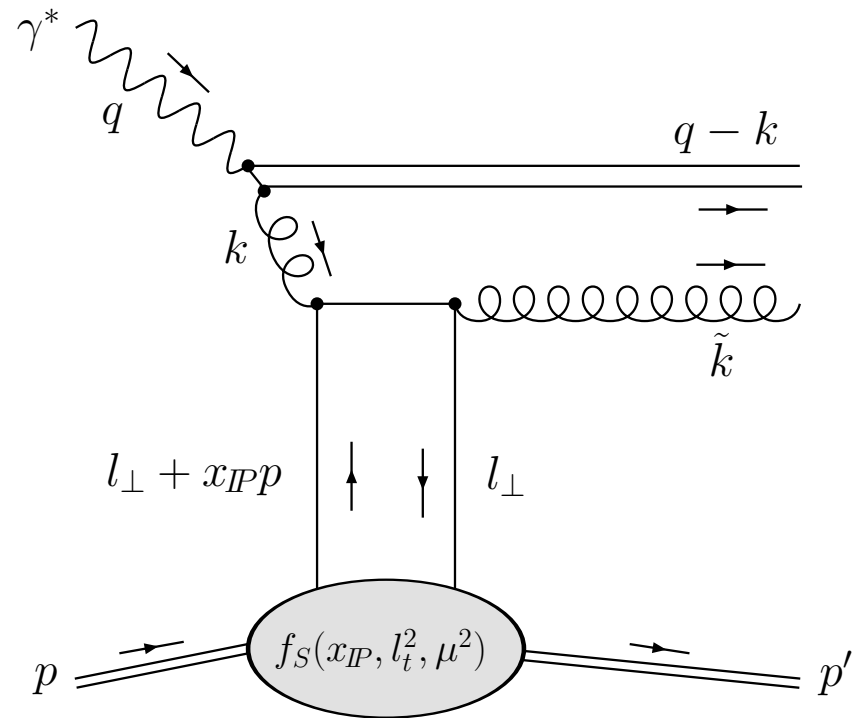
- Work in strongly-ordered limit:  $l_t \ll k_t \ll Q$

Quark dipole



$$\beta \Sigma^{IP=S}(\beta, \mu^2; \mu^2) = c_{q/S} \beta (1 - \beta)$$

Effective gluon dipole



$$\beta' g^{IP=S}(\beta', \mu^2; \mu^2) = c_{g/S} (1 - \beta')^2$$

# Description of $F_2^{D(3)}$ data

Data set	Points <sup>a</sup>	Proton dissociation	Normalisation
1997 ZEUS LPS (prel.)	69	none	1
1998/99 ZEUS (prel.)	121	$M_Y < 2.3 \text{ GeV}$	$\approx 1.5$
1997 H1 (prel.)	214	$M_Y < 1.6 \text{ GeV}$	$\approx 1.2$

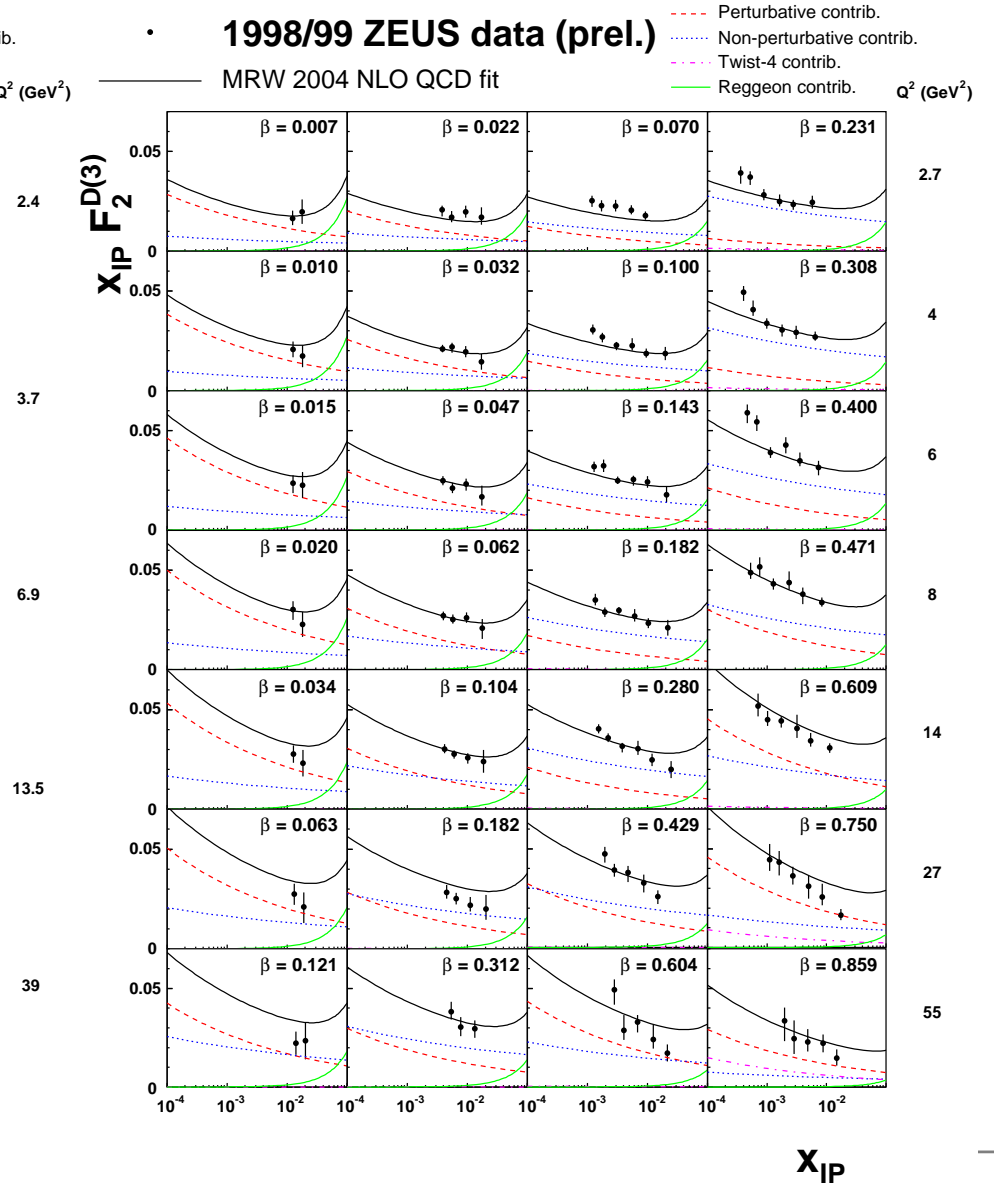
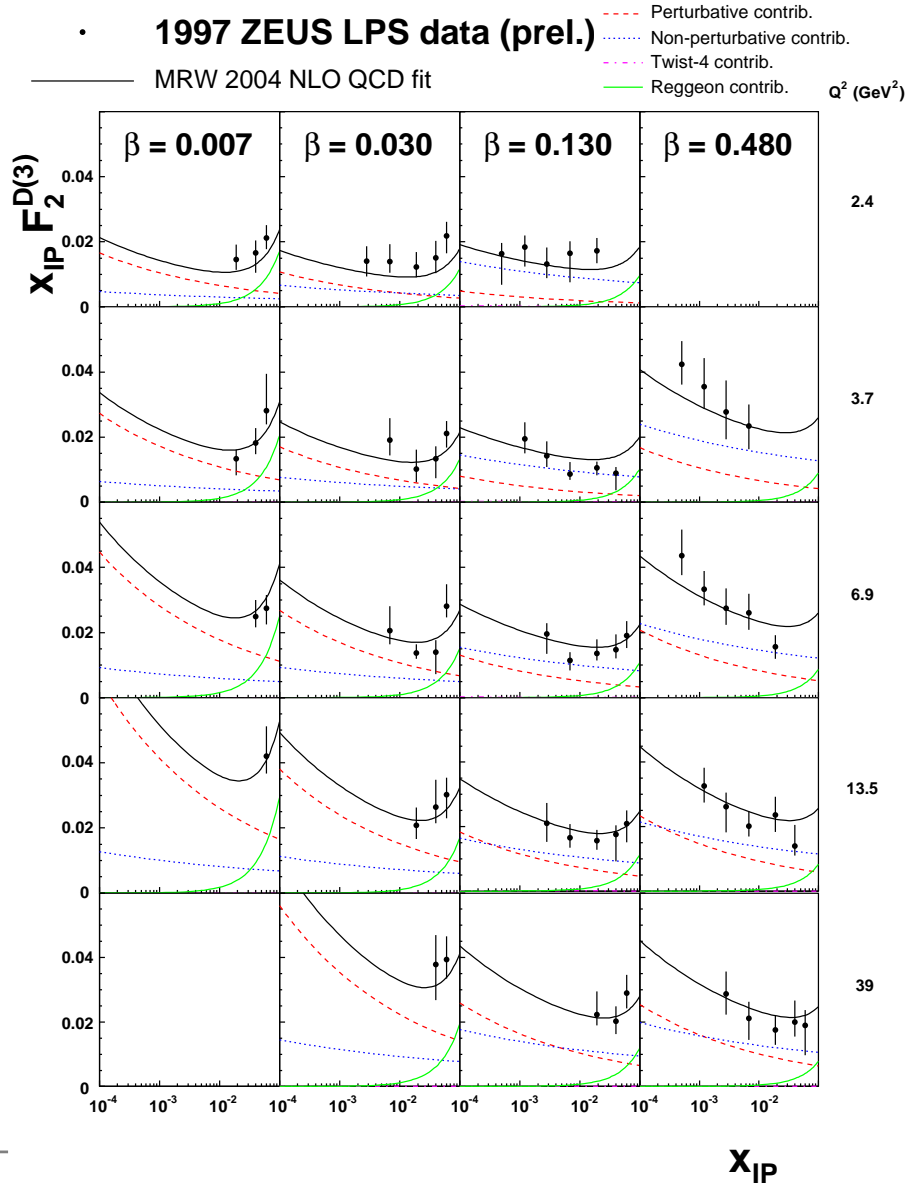
- Only free parameters are normalisation of each contribution to  $F_2^{D(3)}$  (effective  $K$ -factors):  $(Q_0 = 1 \text{ GeV})$

$$c_{q/G}, c_{g/G}, c_{L/G}, (c_{q/S}, c_{g/S}, c_{L/S}), c_{q/NP}, c_{IR}$$

	$x_{IP}g = x_{IP}^{-\lambda} (x_{IP}S = 0)$		$x_{IP}g, x_{IP}S = \text{MRST}$
Data sets fitted	$\lambda$	$\chi^2/\text{d.o.f.}$	$\chi^2/\text{d.o.f.}$
ZEUS	0.25	0.79	0.95
H1	0.13	1.08	0.71
ZEUS + H1	0.18	1.11	1.16

<sup>a</sup>Cuts:  $M_X > 2 \text{ GeV}, y < 0.45$

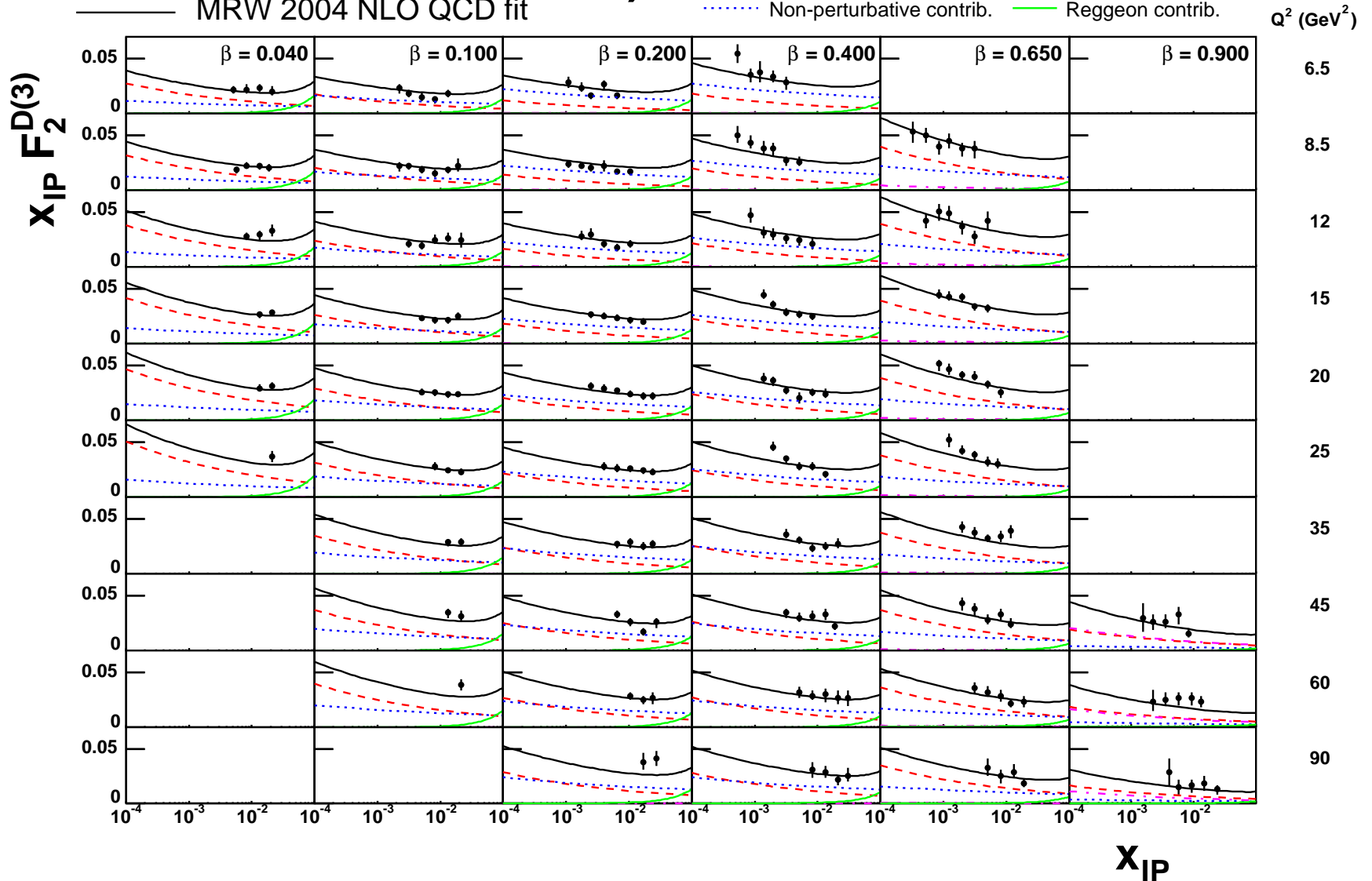
# Fit to ZEUS+H1 with $x_{IP}g = x_{IP}^{-\lambda}$



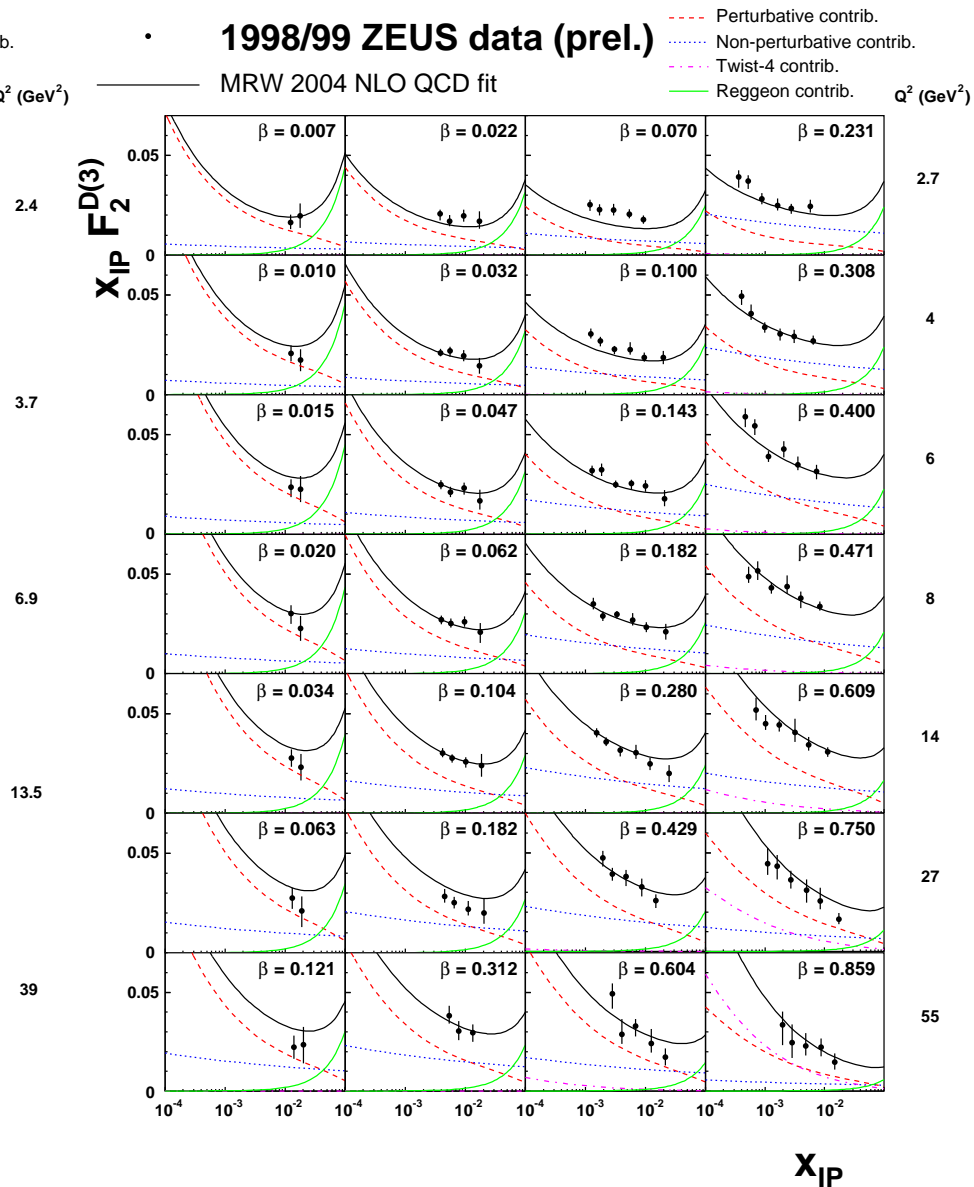
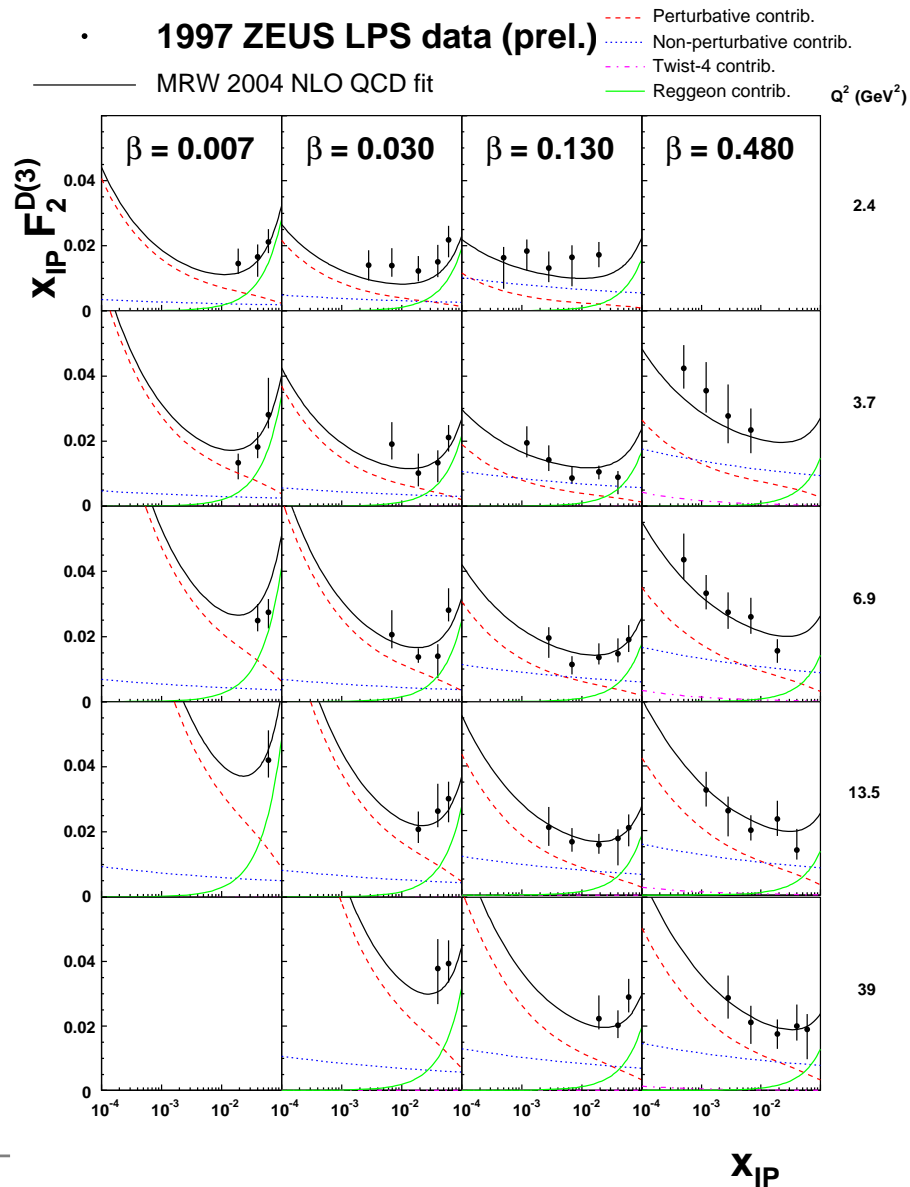
# Fit to ZEUS+H1 with $x_{IP}g = x_{IP}^{-\lambda}$

• **1997 H1 data (prel.)**  
MRW 2004 NLO QCD fit

- - - Perturbative contrib.     - - - Twist-4 contrib.  
⋯ Non-perturbative contrib.     — Reggeon contrib.



# Fit to ZEUS+H1 with $x_{IP}g, x_{IP}S = \text{MRST}$

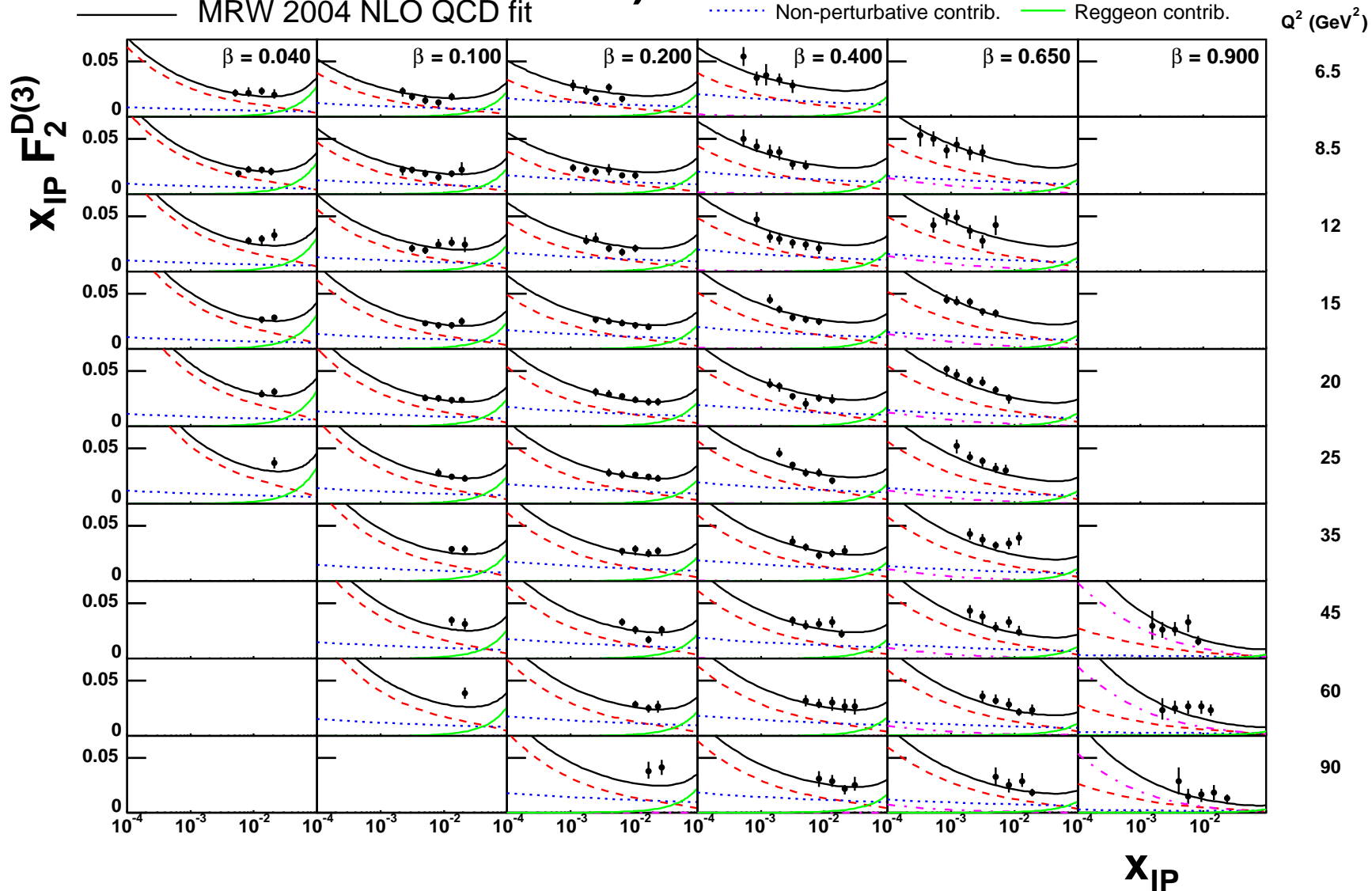




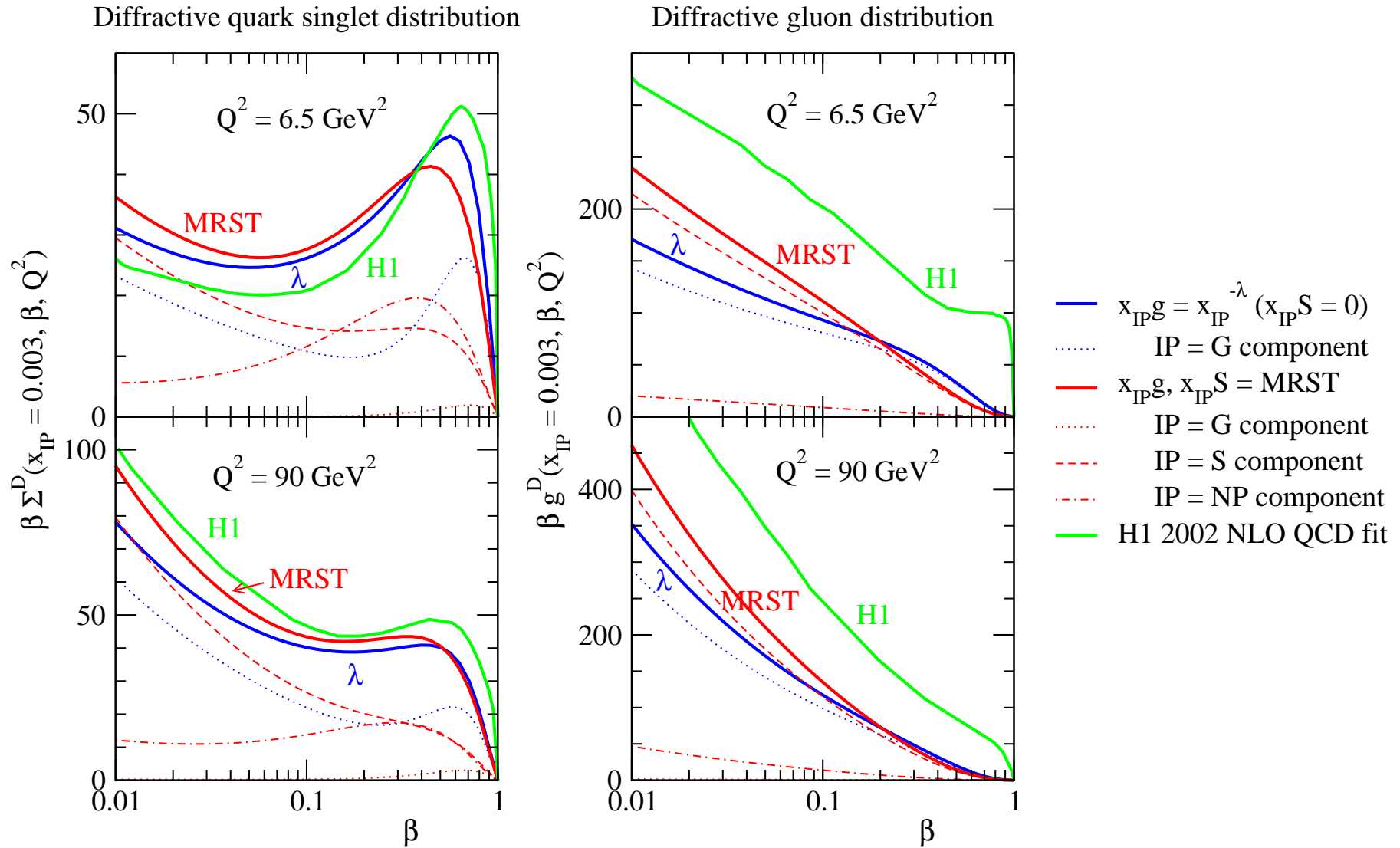
# Fit to ZEUS+H1 with $x_{IP}g$ , $x_{IP}S = \text{MRST}$


• **1997 H1 data (prel.)**  
MRW 2004 NLO QCD fit

--- Perturbative contrib.    - - - Twist-4 contrib.  
 ····· Non-perturbative contrib.    — Reggeon contrib.



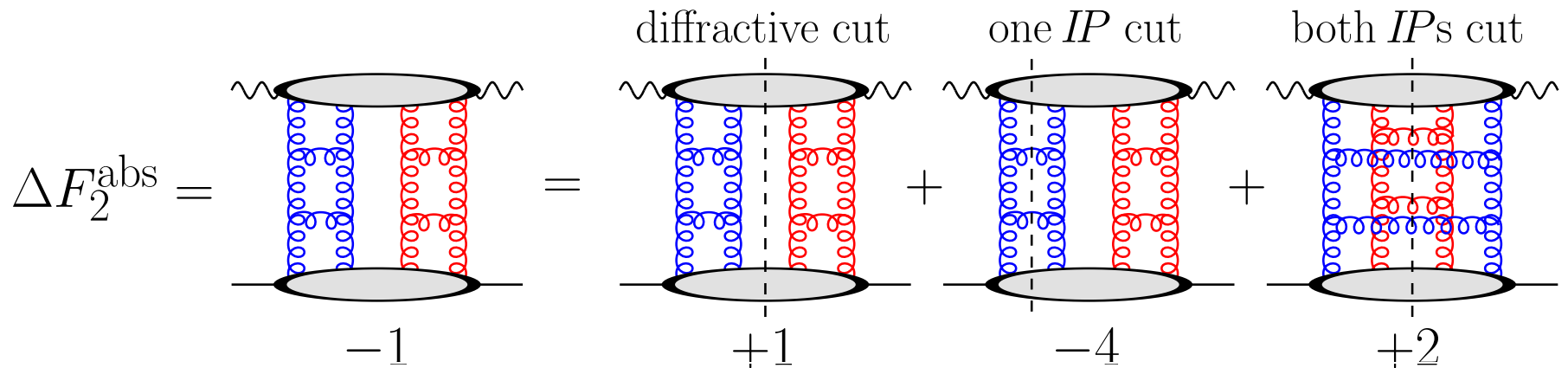
# DPDFs compared to H1 fit



 H1 use a smaller  $\alpha_S$  and have no twist-four contribution

# Absorptive corrections to $F_2$

- **AGK cutting rules**<sup>a</sup>  $\implies$  **diffractive** events are intimately related to **absorptive corrections** to the **inclusive** structure function  $F_2$ :



- **Aside:** absorptive corrections  $\sim$  non-linear effects, screening, shadowing, unitarity corrections, recombination, multiple scattering, multiple interactions, (saturation effects), ...

<sup>a</sup>Abramovsky, Gribov, Kancheli ( $\rightarrow$  QCD: Bartels, Ryskin)

# Absorptive corrections to $F_2$

$$F_2^{\text{data}}(x_B, Q^2) = F_2^{\text{DGLAP}}(x_B, Q^2) + \Delta F_2^{\text{abs}}(x_B, Q^2)$$

$$\Delta F_2^{\text{abs}}(x_B, Q^2) \simeq - \int_{x_B}^{0.1} dx_{\text{IP}} \left[ F_{2,P}^{D(3)}(x_{\text{IP}}, \beta, Q^2) + F_{L,P}^{D(3)}(x_{\text{IP}}, \beta, Q^2) \right]$$

- Only  $\mu > Q_0$  contribution of  $F_2^{D(3)}$  in  $\Delta F_2^{\text{abs}}$ ;  $\mu < Q_0$  contribution already included in input parameterisations to  $F_2$  fit
- **Reminder:**  $F_{2,P}^{D(3)}$  = leading-twist,  $F_{L,P}^{D(3)}$  = twist-four
- To fit  $F_2$  using the **DGLAP** equation, first need to ‘correct’ the **data** for absorptive corrections:

$$F_2^{\text{DGLAP}} = F_2^{\text{data}} - \Delta F_2^{\text{abs}} = F_2^{\text{data}} + \left| \Delta F_2^{\text{abs}} \right|$$

# Simultaneous $F_2 + F_2^{D(3)}$ analysis

- Procedure:

1. Start by fitting ZEUS + H1  $F_2$  data (279 points) <sup>a</sup> with **no absorptive corrections**  $\sim$  MRST2001 NLO
  2. Fit ZEUS + H1  $F_2^{D(3)}$  data, using  $x_{IP}g$  and  $x_{IP}S$  from previous  $F_2$  fit
  3. Fit  $F_2^{DGLAP} = F_2^{\text{data}} + |\Delta F_2^{\text{abs}}|$ , with  $\Delta F_2^{\text{abs}}$  from **previous  $F_2^{D(3)}$  fit** (normalised to  $2 \times$  ZEUS LPS data: account for proton dissociation with  $M_Y \lesssim 5$  GeV)
  4. Go to 2.
- Only a few iterations needed for convergence

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<sup>a</sup>Cuts:  $x_B < 0.01, 2 < Q^2 < 500 \text{ GeV}^2, W^2 > 12.5 \text{ GeV}^2$ ; match to MRST  $xg, xS$  at  $x = 0.2$

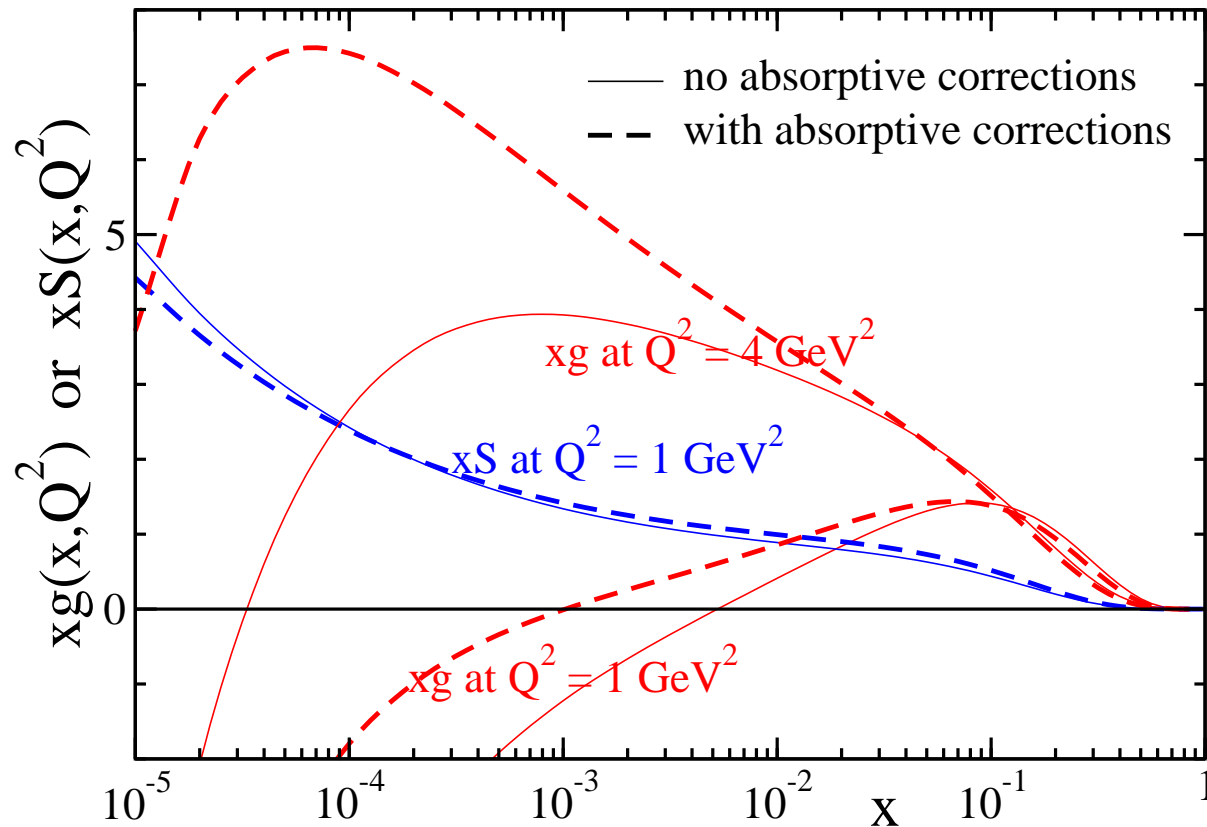
# Gluon and sea quark PDFs

$$xg(x, Q^2=1 \text{ GeV}^2) = A_g x^{-\lambda_g} (1-x)^{3.7} (1 + \epsilon_g x^{0.5}) - A_- x^{-\delta} (1-x)^{10}$$

$$xS(x, Q^2=1 \text{ GeV}^2) = A_S x^{-\lambda_s} (1-x)^{7.1} (1 + \epsilon_s x^{0.5})$$

$$\chi^2/\text{d.o.f.}$$

$F_2$	$F_2^{D(3)}$
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1.15	1.16
1.09	1.17

● Take +ve input gluon parameterisation ( $A_- = 0$ ):

● no absorptive corrections  $\chi^2/\text{d.o.f.} = 1.57$

● with absorptive corrections  $\chi^2/\text{d.o.f.} = 1.10$

# Multi-*IP* exchange (approximately)

- *s*-channel unitarity relation:

$$2 \operatorname{Im} T_{\text{el}}(s, b_t) = |T_{\text{el}}(s, b_t)|^2 + G_{\text{inel}}(s, b_t)$$

- Assume  $\operatorname{Re} T_{\text{el}} \ll \operatorname{Im} T_{\text{el}}$ , then  $T_{\text{el}} = i(1 - \exp(-\Omega/2))$  where  $\Omega(s, b_t)$  is the **opacity** (optical density) or eikonal
- Let  $F_2^D \equiv |\Delta F_2^{\text{abs}}|$  ( $\mu > Q_0$ ), then, for some average  $b_t$ :

$$\boxed{\frac{F_2^D}{F_2^{\text{data}}} = \frac{|T_{\text{el}}|^2}{2\operatorname{Im} T_{\text{el}}} = \frac{1}{2}(1 - \exp(-\Omega/2))} \quad \Rightarrow \text{Solve for } \Omega/2$$

- To fit  $F_2$  with **DGLAP** equation, need **one-*IP*** exchange:

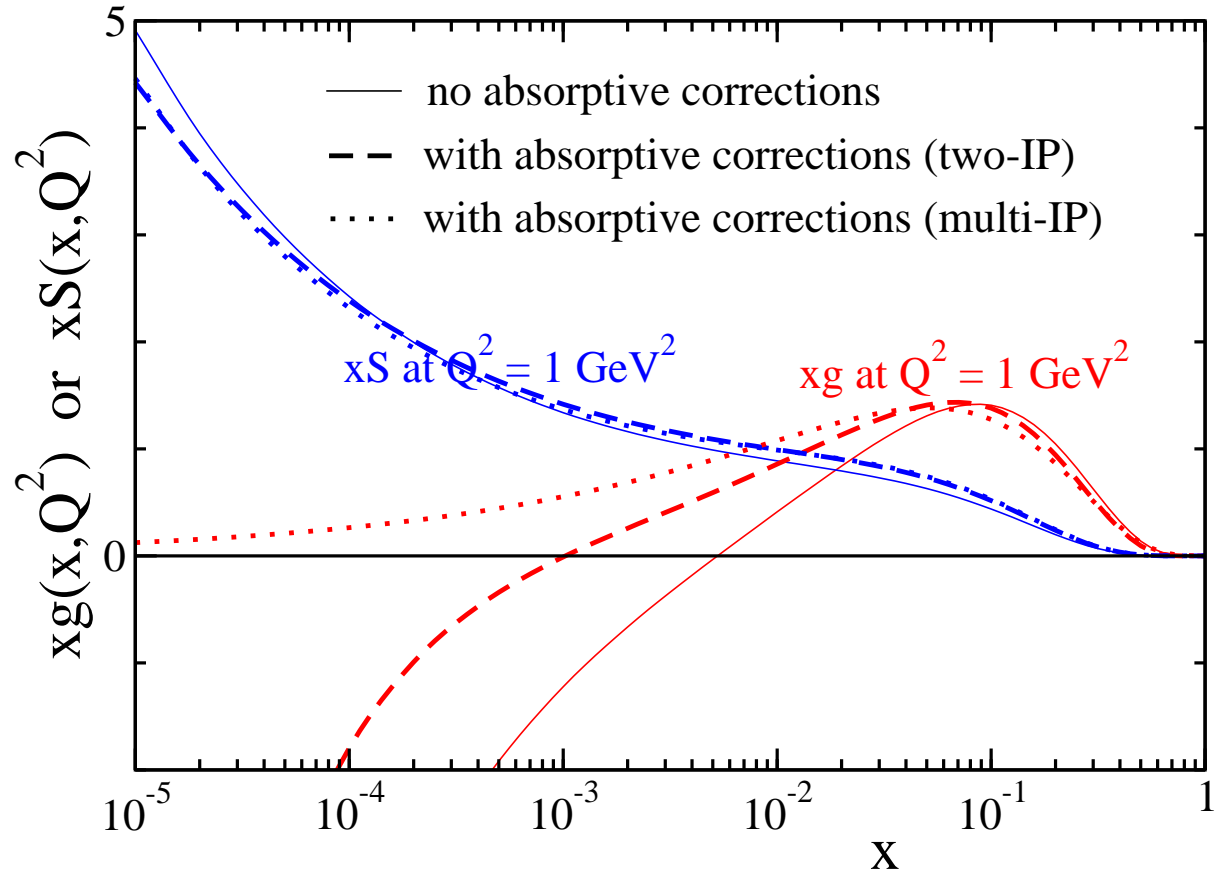
$$\boxed{F_2^{\text{DGLAP}} = F_2^{\text{data}} \frac{\Omega/2}{(1 - \exp(-\Omega/2))}}$$

# Gluon and sea quark PDFs

$$xg(x, Q^2=1 \text{ GeV}^2) = A_g x^{-\lambda_g} (1-x)^{3.7} (1 + \epsilon_g x^{0.5}) - A_- x^{-\delta_-} (1-x)^{10}$$

$$xS(x, Q^2=1 \text{ GeV}^2) = A_S x^{-\lambda_S} (1-x)^{7.1} (1 + \epsilon_S x^{0.5})$$

$\chi^2/\text{d.o.f.}$   
 $F_2$     $F_2^{D(3)}$



1.15	1.16
1.09	1.17
1.05	1.17

● Multi-Pomeron exchange  $\implies A_- \rightarrow 0$



# ‘Pomeron-like’ $xS$ but ‘valence-like’ $xg$ ?

- **Good news:** Absorptive corrections **remove** the need for a **negative input gluon** distribution
- **Bad news:** Still have ‘**Pomeron-like**’ sea quarks but ‘**valence-like**’ gluons at small- $x$  and low  $Q^2$ :

$$xg \sim x^{-\lambda_g}, xS \sim x^{-\lambda_S} \quad \text{with} \quad \lambda_g < 0 \text{ and } \lambda_S > 0$$

- **Reminder:**
  - Regge theory  $\implies \lambda_g = \lambda_S$
  - Resummed NLL BFKL  $\implies \lambda_g = \lambda_S \simeq 0.3$
  - Soft hadron data  $\implies \lambda \simeq 0.08$
- Must be some **large non-perturbative effect** causing the observed behaviour. One possibility: mimic unknown **power corrections** by **shifting scale** in  $F_2$  and  $F_2^{D(3)}$  fits by  $\approx 1 \text{ GeV}^2$ . Fix  $\lambda_g = \lambda_S = 0$

# Shift scale by 1 GeV<sup>2</sup> ?

$$xg(x, Q^2=1 \text{ GeV}^2) = A_g x^0 (1-x)^{3.7} (1 + \epsilon_g x^{0.5} + \gamma_g x)$$

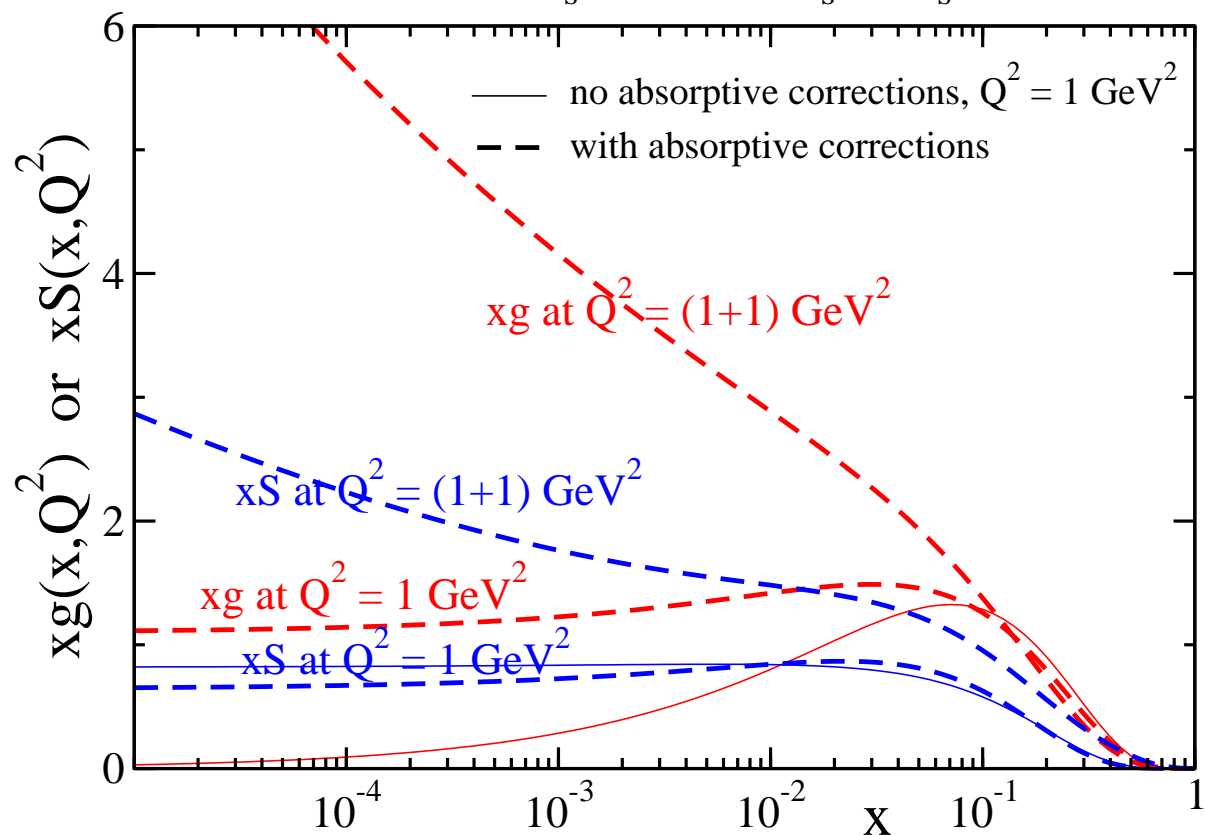
$$xS(x, Q^2=1 \text{ GeV}^2) = A_S x^0 (1-x)^{7.1} (1 + \epsilon_S x^{0.5} + \gamma_S x)$$

$\chi^2/\text{d.o.f.}$

$F_2$   $F_2^{D(3)}$

1.45 1.12

1.22 1.11



- Satisfactory description of  $F_2$  and  $F_2^{D(3)}$  data with 'flat' asymptotic behaviour ( $x \rightarrow 0$ ) of input  $xg$ ,  $xS$

# Conclusions

- **New perturbative QCD description of  $F_2^{D(3)}$** 
  - Pomeron singularity not a *pole* but a *cut*  
⇒ **Integral over Pomeron scale  $\mu$**
  - **Input Pomeron PDFs from leading-order QCD diagrams**
  - **Two-quark Pomeron** in addition to two-gluon Pomeron
- **Absorptive corrections to  $F_2$  from AGK cutting rules**
  - **Good news:** remove need for **negative gluon input**
  - **Dilemma:** still have ‘**Pomeron-like**’ sea quarks but ‘**valence-like**’ gluons at small- $x$  and low  $Q^2$ 
    1. Non-perturbative Pomeron **doesn't couple** to gluons, secondary Reggeon **couples more** to gluons than sea quarks ?
    2. Unknown non-perturbative power corrections **slow down DGLAP evolution** at low  $Q^2$  ?