

Phase diagram in a chiral hadronic model and implications on neutron stars and particle ratios

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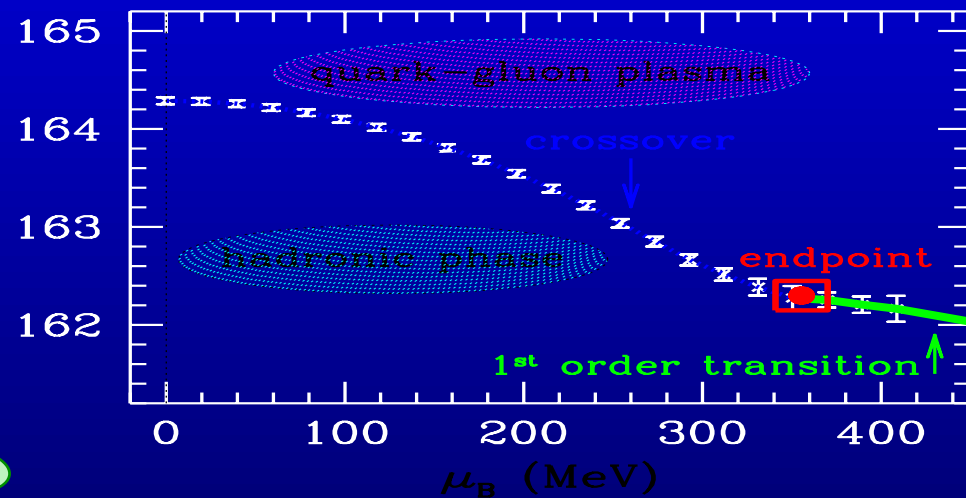
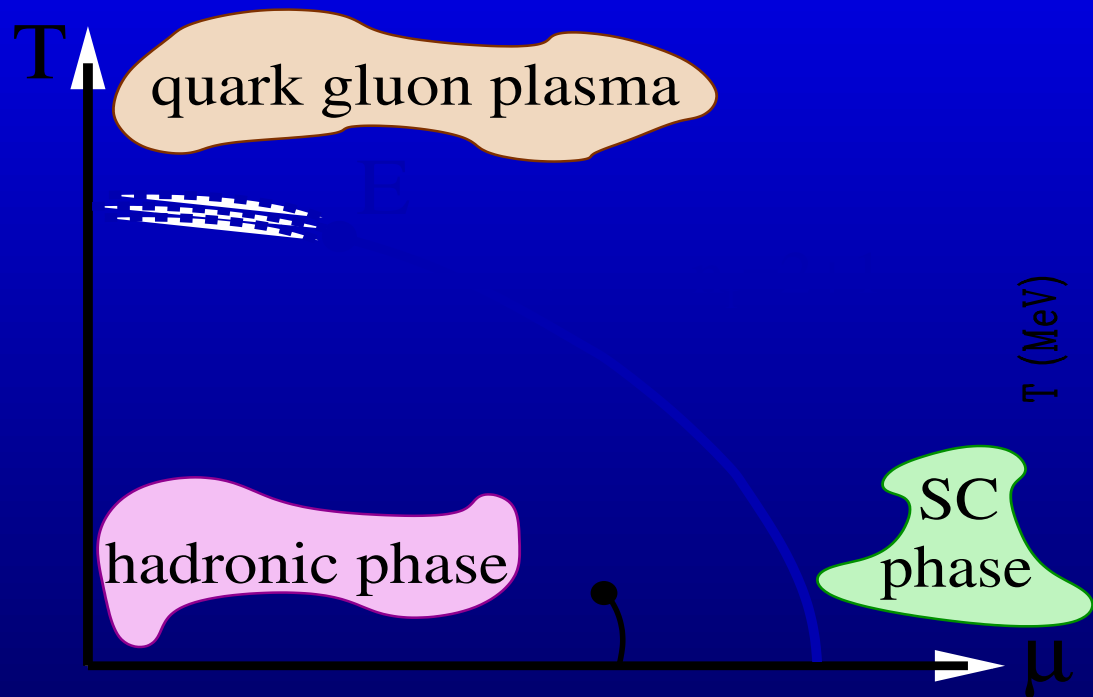
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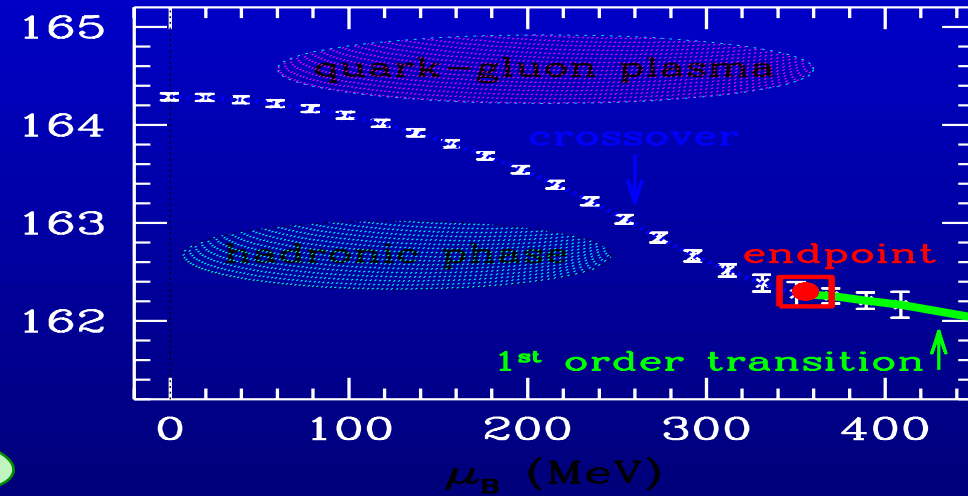
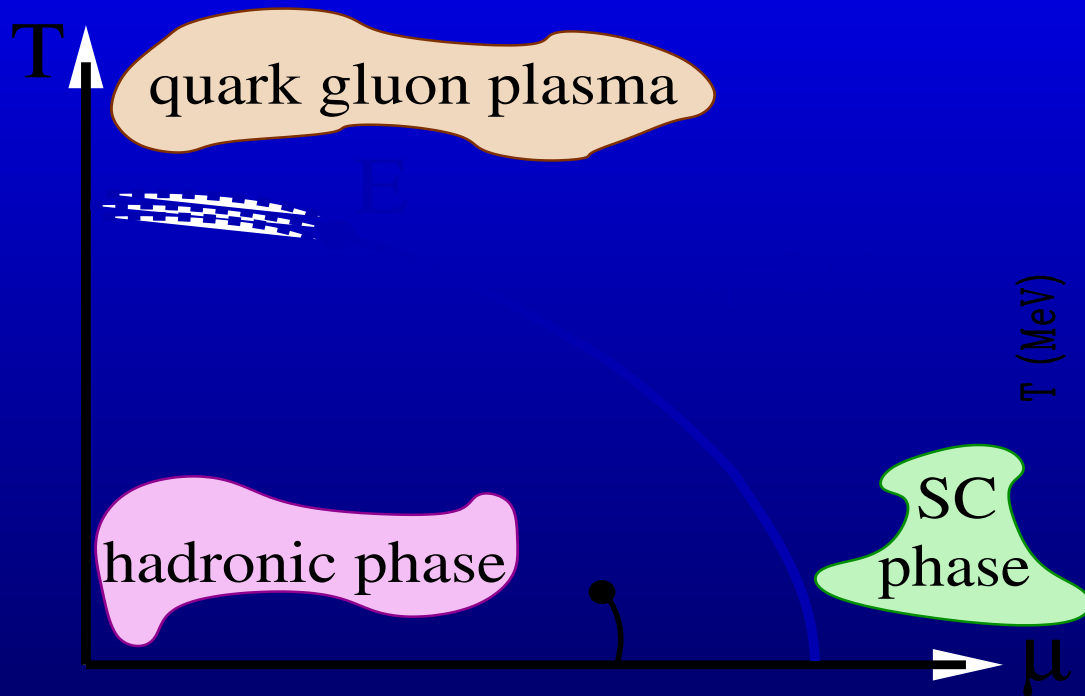
A. Dumitru, J. Schaffner-Bielich, S.Schramm, H. Stöcker, G. Zeeb, D.Z.

1. Motivation and general Ideas
2. The chiral $SU(3)_L \times SU(3)_R$ model
3. The phase diagram
4. Neutron stars
5. Particle ratios

Motivation



Motivation



Uncertainties in LQCD

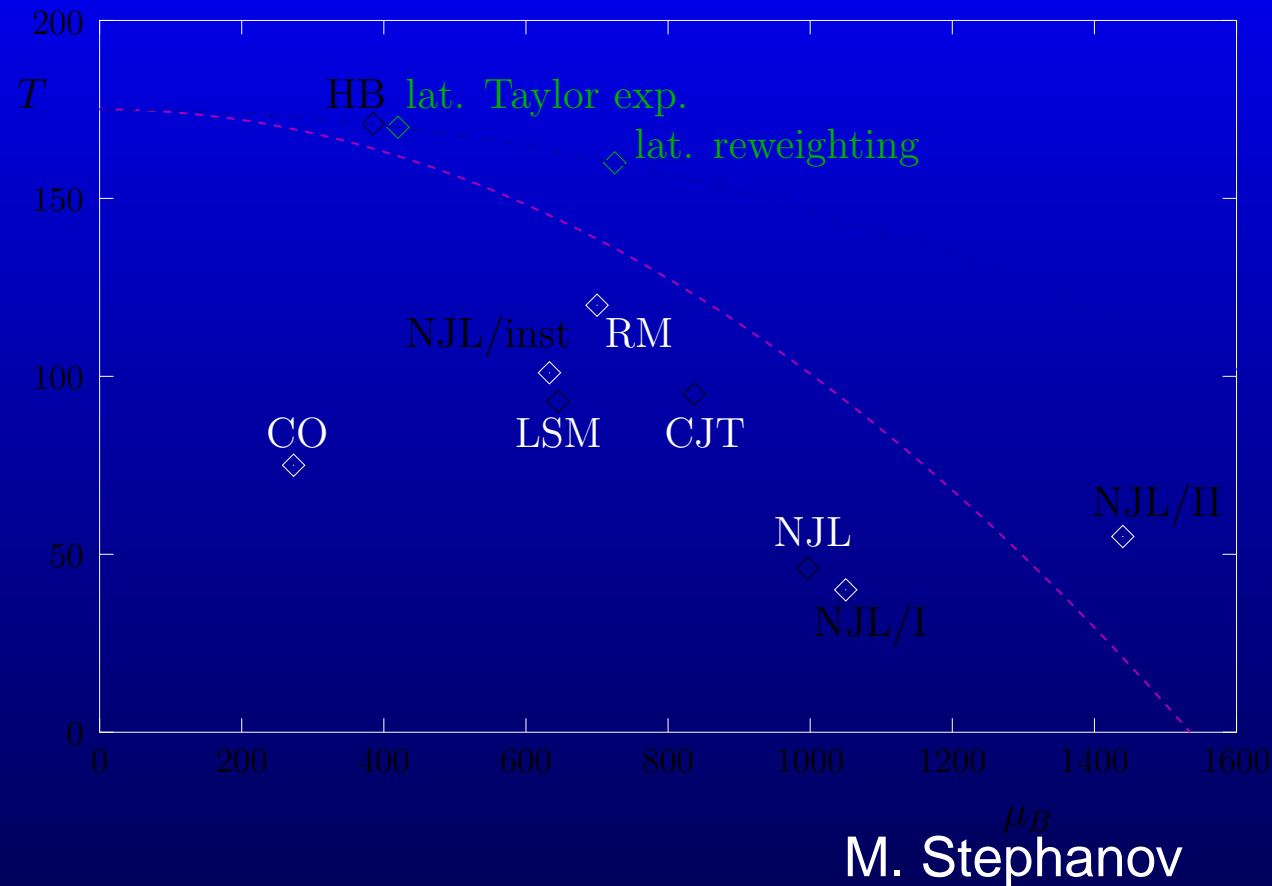
Need EoS at high μ for relativistic heavy ion collisions

Why does the phase diagram look as it does?

What 'drives' the phase transition?

→ Effective models

Modelling the QCD phase diagram



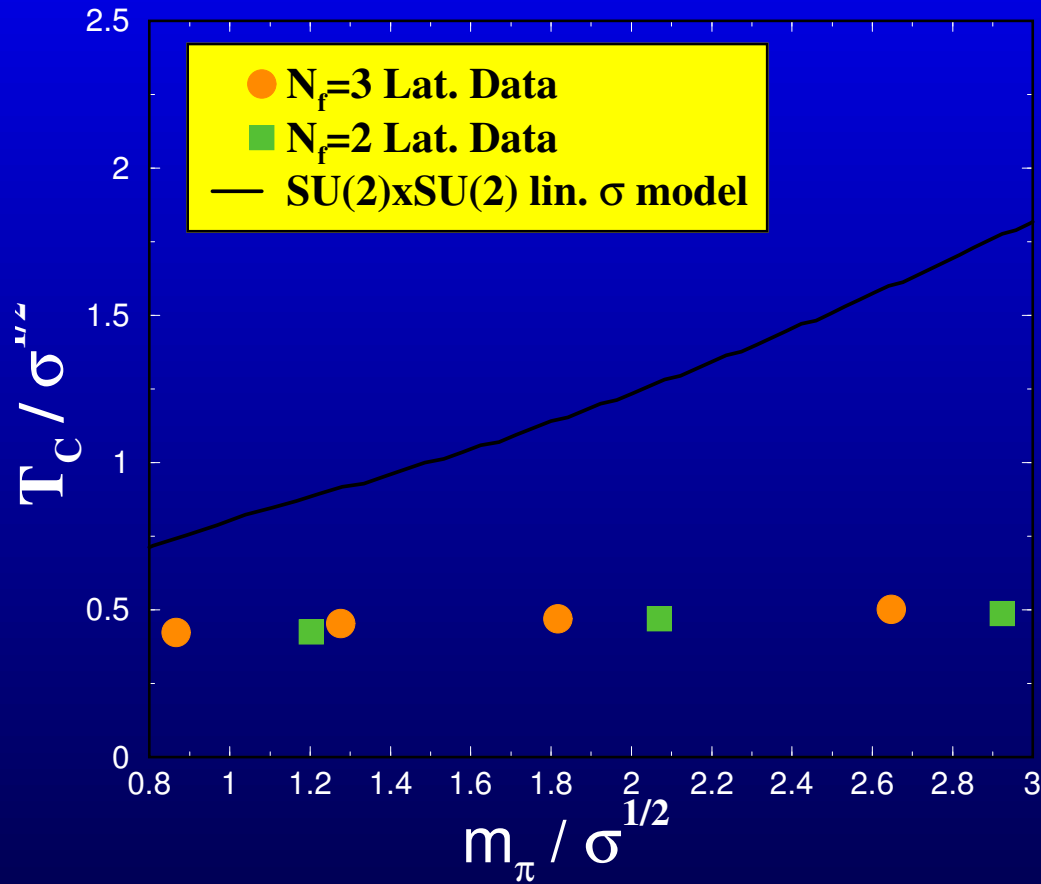
Many models have difficulties in getting T_c up

Many models do not describe nuclear matter/finite nuclei

High T: Hadron resonance gas good description

- Hagedorn limiting temperature - Bootstrap high T_c
- particle ratios well described
- mass-scaled version: good description of LQCD below T_c

The m_π -dependence of T_c



Dumitru, Roeder, Ruppert

T_c depends only weakly on m_π in LQCD but strongly in $L_\sigma M$
 Not only π s drive the transition but Baryon resonances are important!

Generalized Ansatz

- $\sigma - \omega$ model - successful for nuclear matter and finite nuclei
- chiral SU(3) symmetry
- include resonances - interacting hadron gas (phase transition, EoS at high T, particle ratios,..)

Hadronic, chiral $SU(3)\sigma - \omega$ model

- Degrees of freedom: Baryons und Mesons ($SU(3)$ -Multiplets)
- σ - ω -Model: Interactions induced by scalar and vector field
- Nonlinear realization of chiral symmetry
- Chiral symmetry spontaneously broken \Rightarrow dynamical mass generation
- Chiral symmetry explicitly broken \Rightarrow finite PS masses, PCAC relations
- scale breaking potential \Rightarrow mimics trace anomaly of QCD
- Mean-field approximation, i.e. mesons are treated as classical fields

Mean Field Lagrangian

$$\mathcal{L}^{\text{MF}} = \mathcal{L}_{\text{BM}} + \mathcal{L}_{\text{BV}} + \mathcal{L}_{\text{vec}} + \mathcal{L}_0 + \mathcal{L}_{\text{SB}}$$

Mean Field Lagrangian

$$\mathcal{L}^{\text{MF}} = \mathcal{L}_{\text{BM}} + \mathcal{L}_{\text{BV}} + \mathcal{L}_{\text{vec}} + \mathcal{L}_0 + \mathcal{L}_{\text{SB}}$$

- Baryon - scalar meson interaction und scalar potential
 \Rightarrow SSB, dynamical mass generation by scalar fields/ chiral condensates
 $\sigma \equiv \langle \bar{q}q \rangle, \zeta \equiv \langle \bar{s}s \rangle$

$$\begin{aligned} \mathcal{L}_{\text{BM}} &= - \sum_i \bar{B}_i m_i^* B_i \\ m_i^* &= g_{i\sigma} \sigma + g_{i\zeta} \zeta \\ i &= N, \Lambda, \Sigma, \Xi, \Delta, \Sigma^*, \Xi^*, \Omega \end{aligned}$$

$$\begin{aligned} \mathcal{L}_0 &= -\frac{1}{2} k_0 \chi^2 (\sigma^2 + \zeta^2) + k_1 (\sigma^2 + \zeta^2)^2 + k_2 \left(\frac{\sigma^4}{2} \right) \\ &\quad + k_3 \chi \sigma^2 \zeta - k_4 \chi^4 - \frac{1}{4} \chi^4 \ln \frac{\chi^4}{\chi_0^4} + \frac{\delta}{3} \chi^4 \ln \frac{\sigma^2 \zeta}{\sigma_0^2 \zeta_0} \end{aligned}$$

Mean Field Lagrangian

$$\mathcal{L}^{\text{MF}} = \mathcal{L}_{\text{BM}} + \mathcal{L}_{\text{BV}} + \mathcal{L}_{\text{vec}} + \mathcal{L}_0 + \mathcal{L}_{\text{SB}}$$

- Explicit Symmetry breaking
⇒ Finite π mass (pseudoscalar mesons)

$$\mathcal{L}_{\text{SB}} = - \left(\frac{\chi}{\chi_0} \right)^2 \left[m_\pi^2 f_\pi \sigma + (\sqrt{2} m_K^2 f_K - \frac{1}{\sqrt{2}} m_\pi^2 f_\pi) \zeta \right]$$

Mean Field Lagrangian

$$\mathcal{L}^{\text{MF}} = \mathcal{L}_{\text{BM}} + \mathcal{L}_{\text{BV}} + \mathcal{L}_{\text{vec}} + \mathcal{L}_0 + \mathcal{L}_{\text{SB}}$$

- baryon - vector meson interaction and vectormeson potential \Rightarrow saturation properties of nuclear matter

$$\mathcal{L}_{\text{BV}} = - \sum_i \bar{\text{B}}_i \gamma_0 [g_{i\omega} \omega_0 + g_{i\phi} \phi_0] \text{B}_i$$

$$\mathcal{L}_{\text{vec}} = \frac{1}{2} m_\omega^2 \frac{\chi^2}{\chi_0^2} \omega^2 + \frac{1}{2} m_\phi^2 \frac{\chi^2}{\chi_0^2} \phi^2 + g_4^4 (\omega^4 + 2\phi^4)$$

Description of excited hadronic matter

1. Grandcanonical potential $\Omega(T, V, \mu)$

$$\frac{\Omega}{V} = -\mathcal{L}_{vec} - \mathcal{L}_0 - \mathcal{L}_{SB} \mp T \sum_i \frac{\gamma_i}{(2\pi)^3} \int d^3k \left[\ln \left(1 \pm e^{-\frac{1}{T}[E_i^*(k) - \mu_i^*]} \right) \right]$$

$$E_i^*(\vec{k}) = \sqrt{\vec{k}_i^2 + m_i^{*2}} \quad \mu_i^* = \mu_i - g_{i\omega}\omega - g_{i\phi}\omega - g_{i\rho}\tau_3\rho^0$$

2. Fitting of parameters: vacuum, nuclear matter, finite nuclei

$$\text{Vacuum: } \frac{\partial(\mathcal{L}_0)}{\partial\sigma} + \frac{\partial(\mathcal{L}_{SB})}{\partial\sigma} = 0 \Rightarrow \sigma = \sigma_0 \neq 0 \Rightarrow \text{SSB, masses}$$

$$\frac{\chi}{\chi_0} m_\omega^2 \omega 4g_4^4 \omega^3 = 0 \Rightarrow \omega = 0$$

medium:

$$\frac{\partial(\mathcal{L}_0)}{\partial\sigma} + \frac{\partial(\mathcal{L}_{SB})}{\partial\sigma} = \sum_i \frac{\partial m_i^*}{\partial\sigma} \frac{\gamma_i}{(2\pi)^3} \int d^3k \frac{m_i^*}{E_i^*} (n_{k,i} - \bar{n}_{k,i}) \Rightarrow \sigma \text{ decreases}$$

$$\frac{\chi}{\chi_0} m_\omega^2 \omega + 4g_4^4 \omega^3 = \sum_i \frac{\gamma_i}{(2\pi)^3} \int d^3k (n_{k,i} - \bar{n}_{k,i}) \Rightarrow \omega \text{ increases}$$

Additional parameters: scalar and vector coupling of resonances

$$mR_i = g_{i\sigma}\sigma + g_{i\zeta}\zeta + m_{Dek}$$

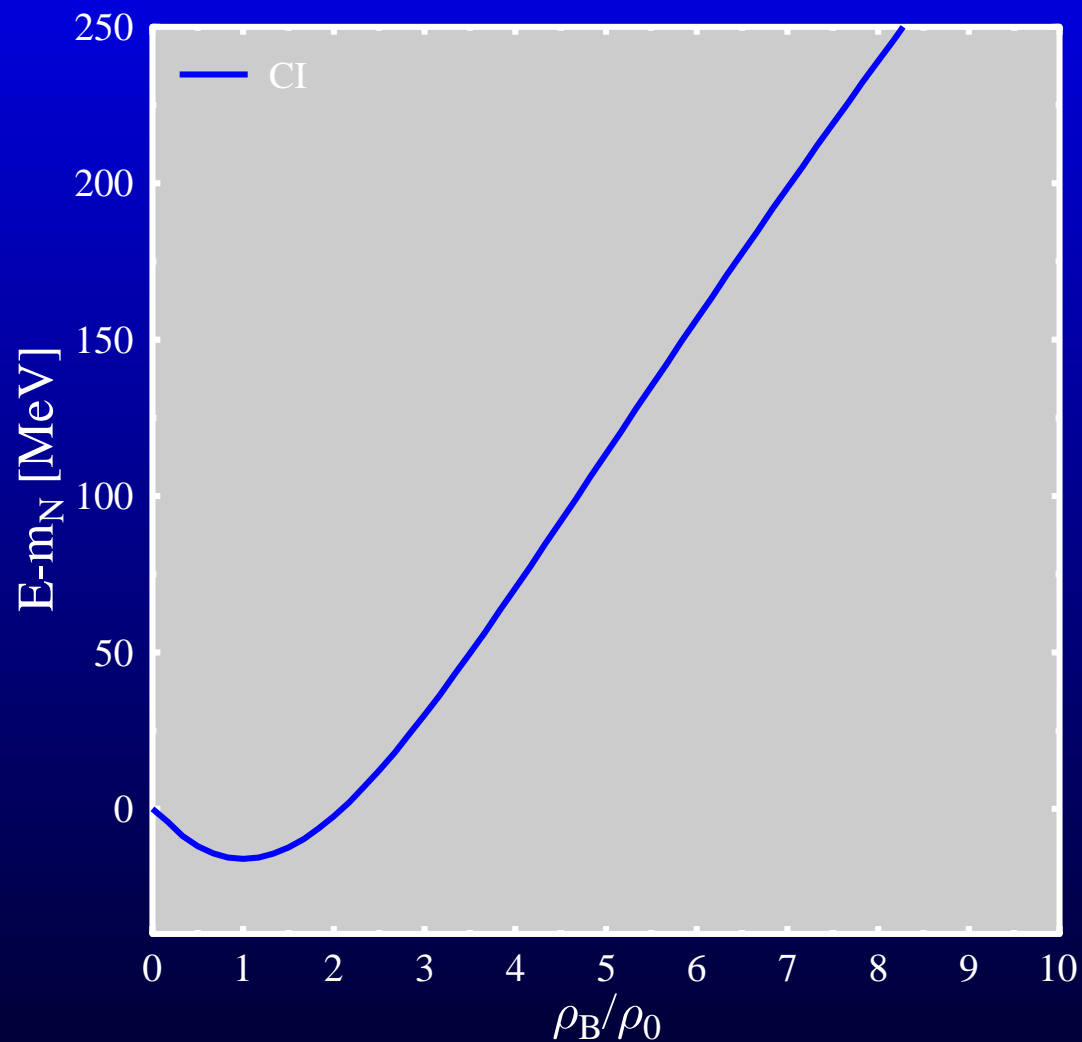
$$r_v = \frac{g_{\Delta\omega}}{g_{N\omega}}$$

choose m_{Dek} and r_v , remaining couplings fixed by symmetry

the larger m_{Dek} the smaller $g_{i\sigma}$

the larger r_v the more repulsion feel the decuplet members

Cold dense hadronic matter



$$\rho_0 = 0.15 \text{ fm}^{-3}$$

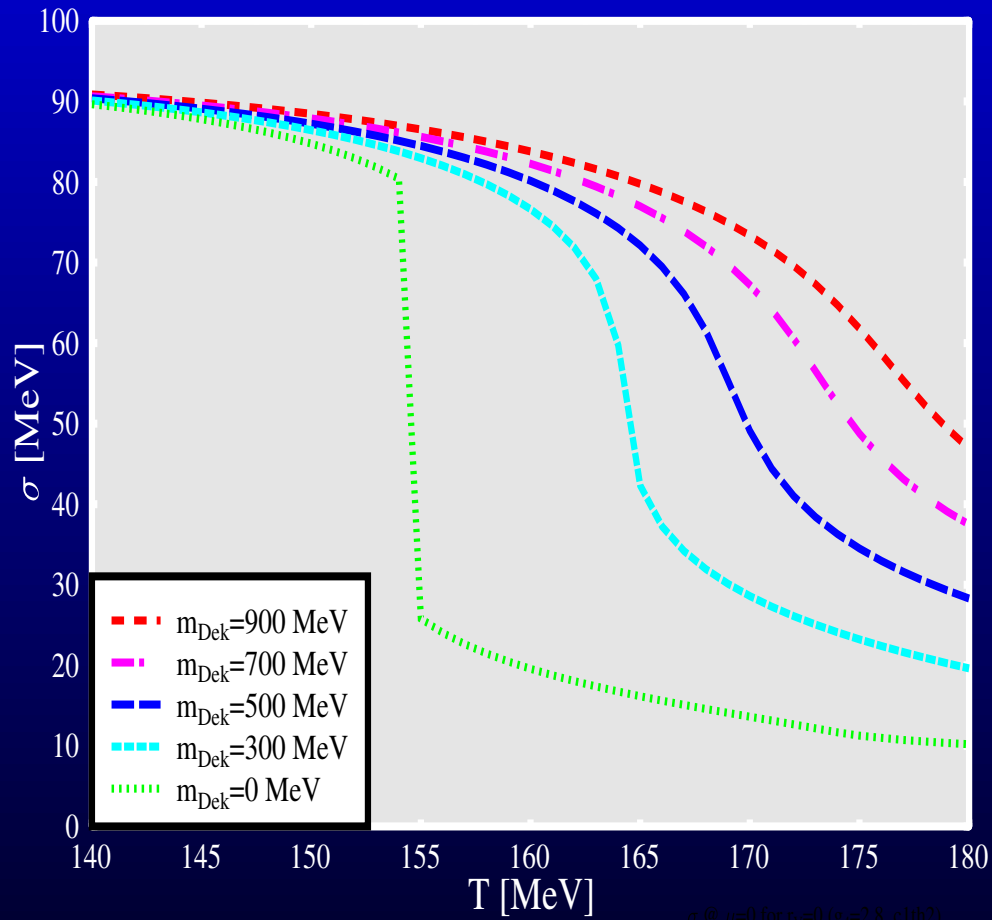
$$E/A - m_N = -16 \text{ MeV}$$

$$K = 276 \text{ MeV}$$

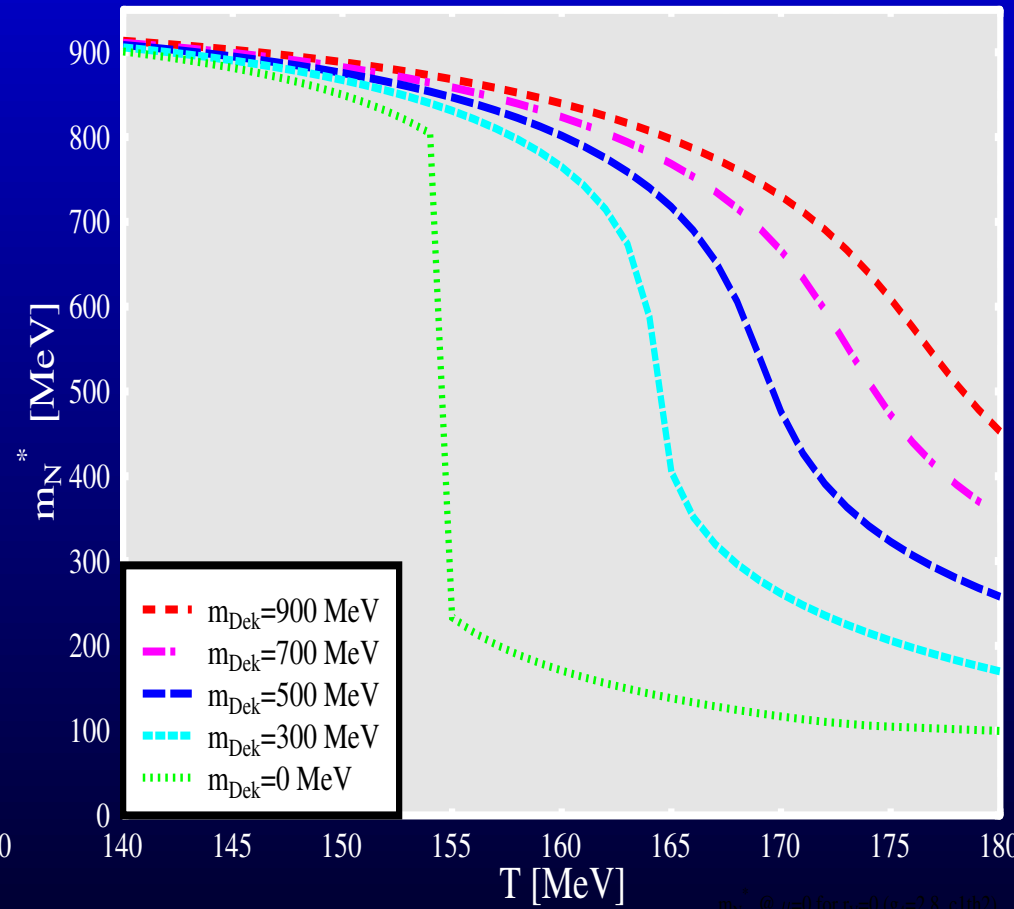
Finite nuclei and Hypernuclei also well described (Schramm et al, Beckmann et al)

Phase structure

Scalar condensate and effective masses at $\mu_q = 0$

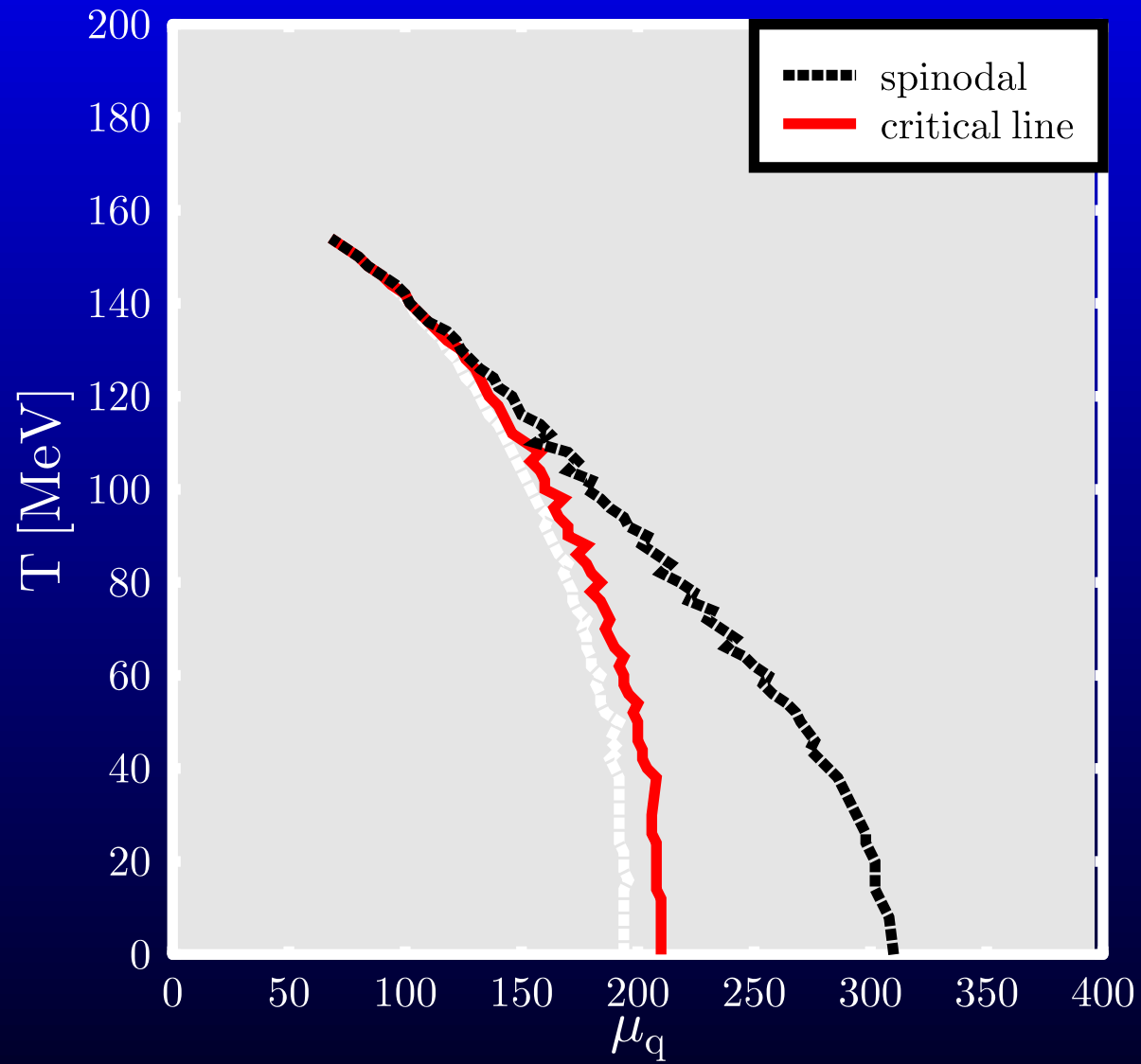


σ @ $\mu=0$ for $r_V=0$ ($g_V=2.8$, c1h2)

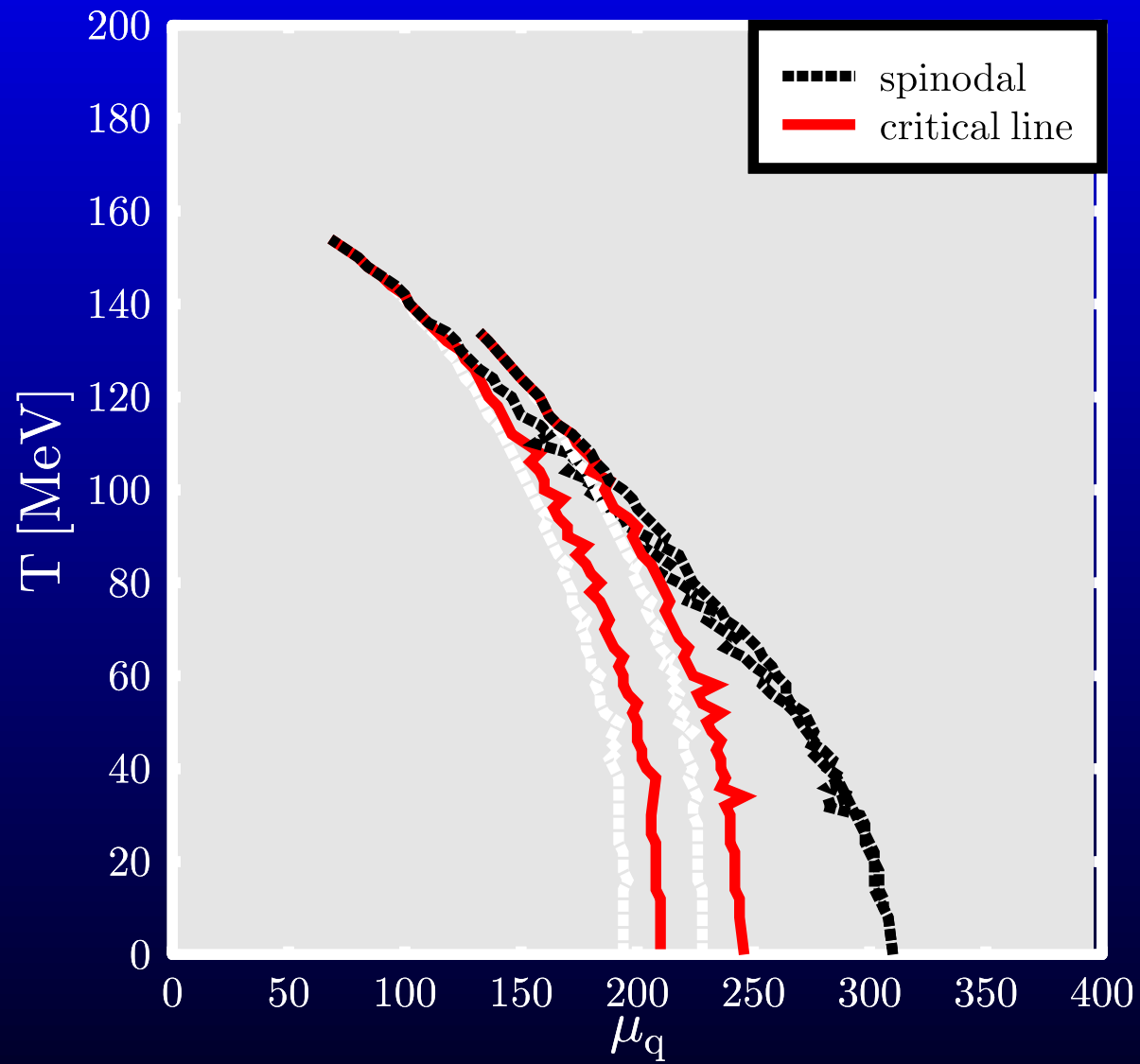


m_N^* @ $\mu=0$ for $r_V=0$ ($g_V=2.8$, c1h2)

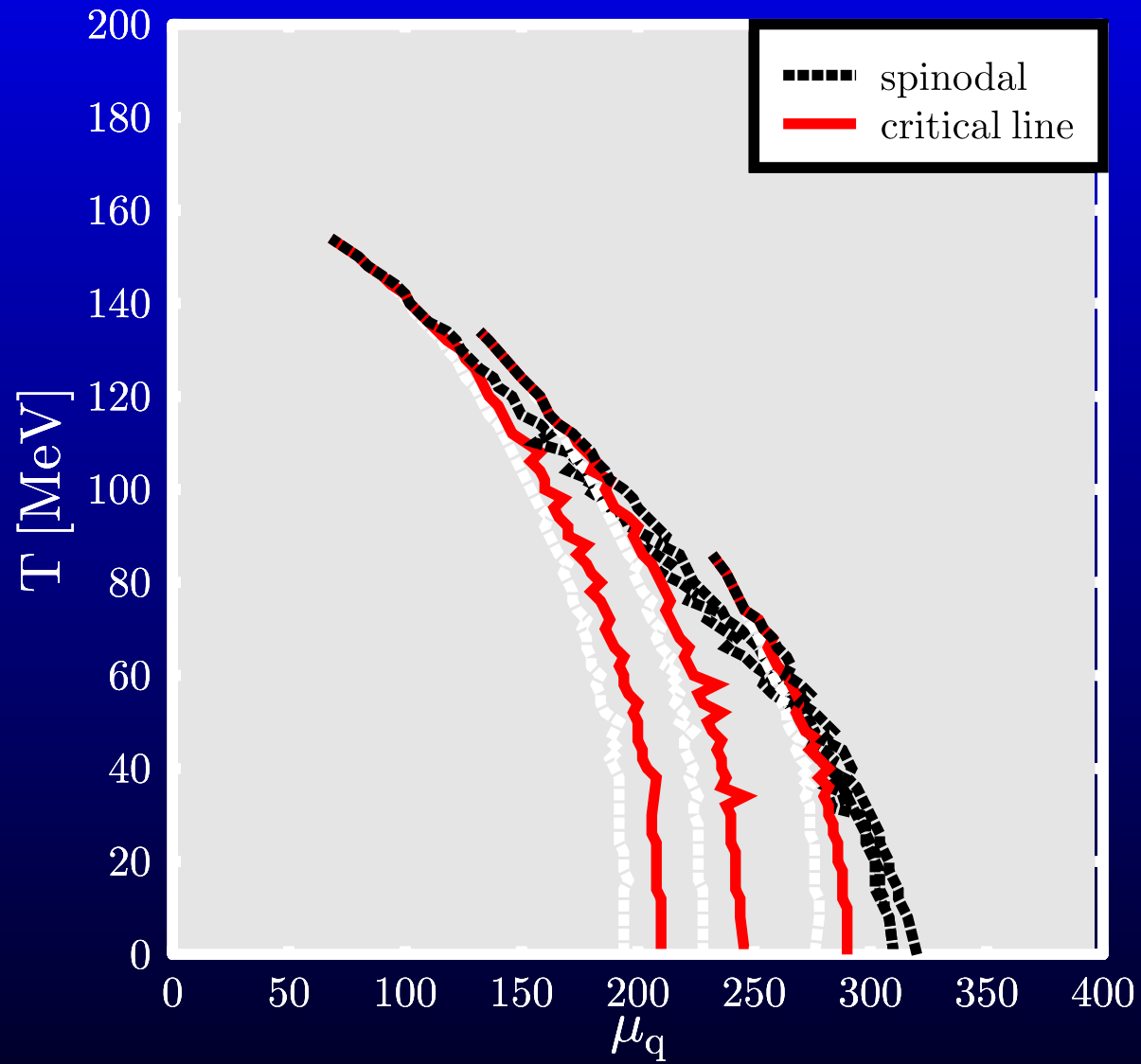
The Phase diagram I



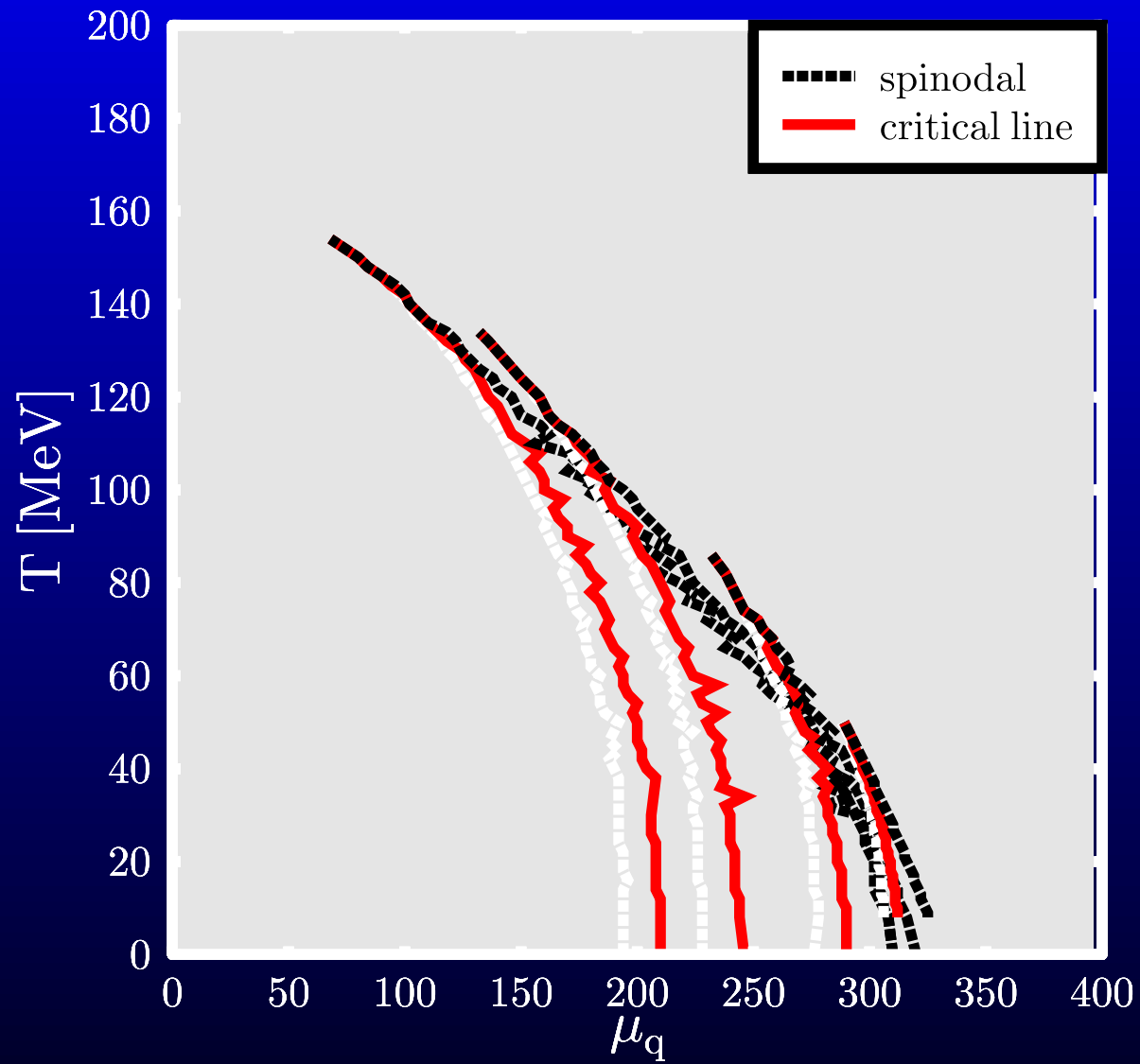
The Phase diagram I



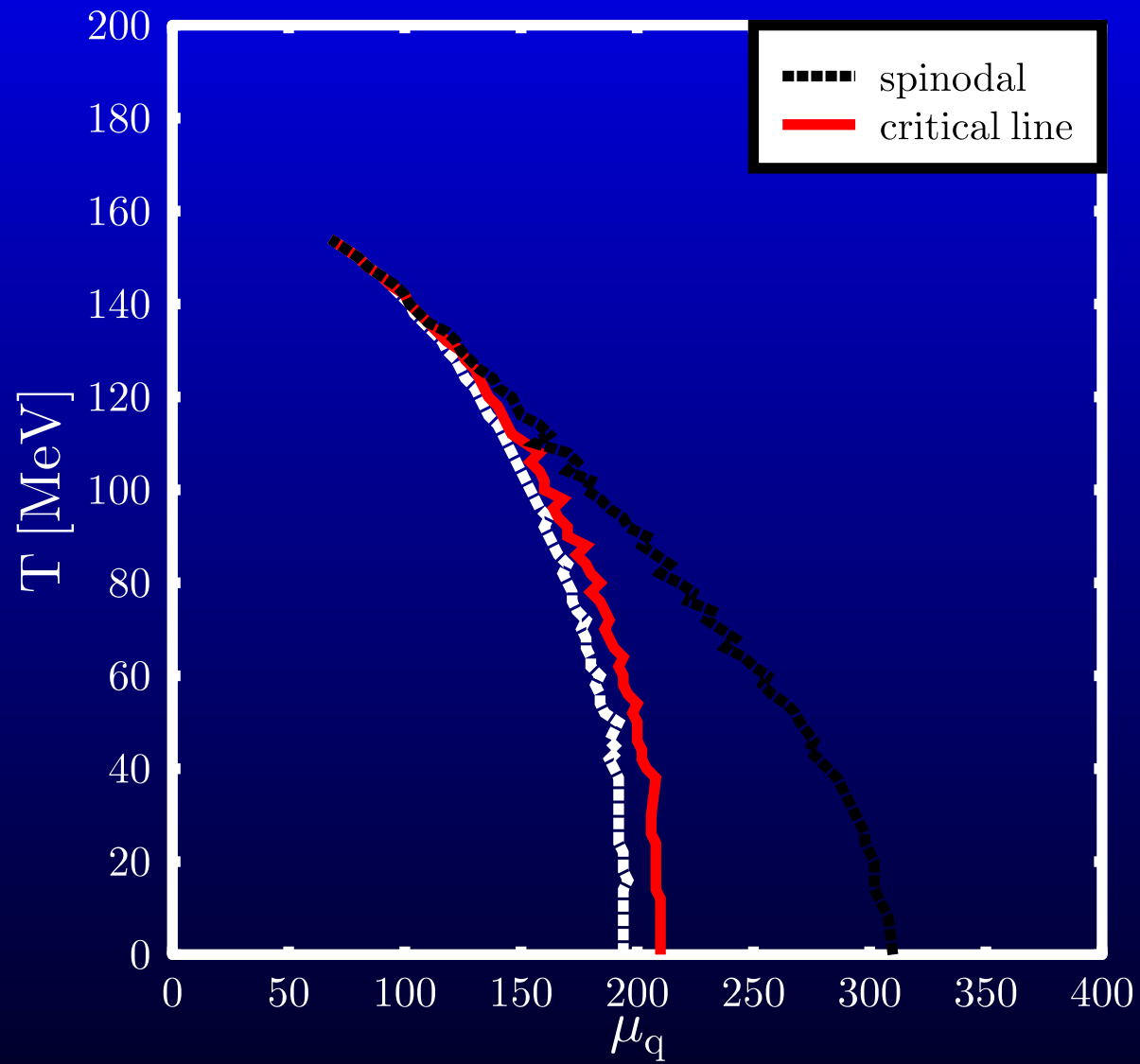
The Phase diagram I



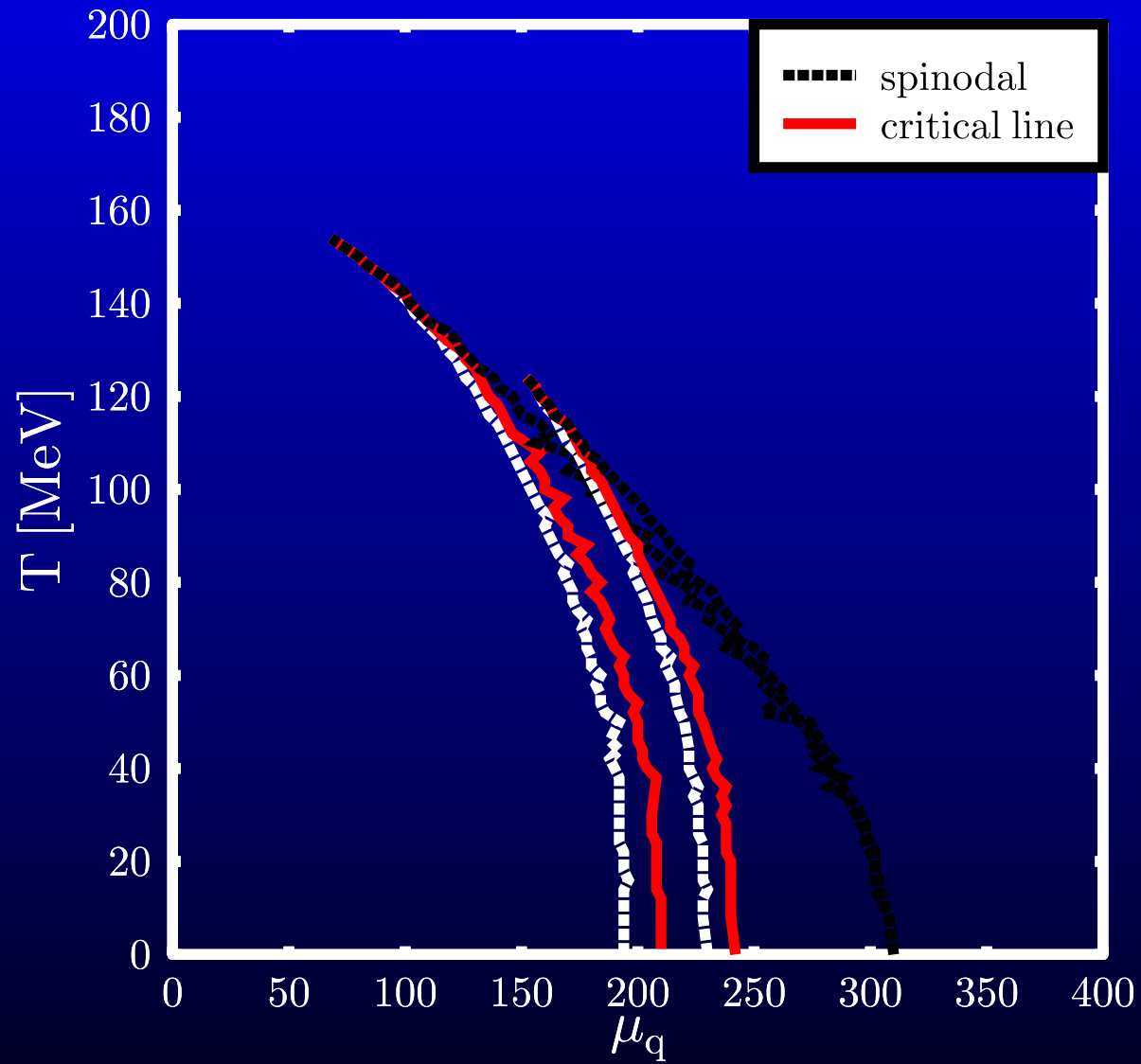
The Phase diagram I



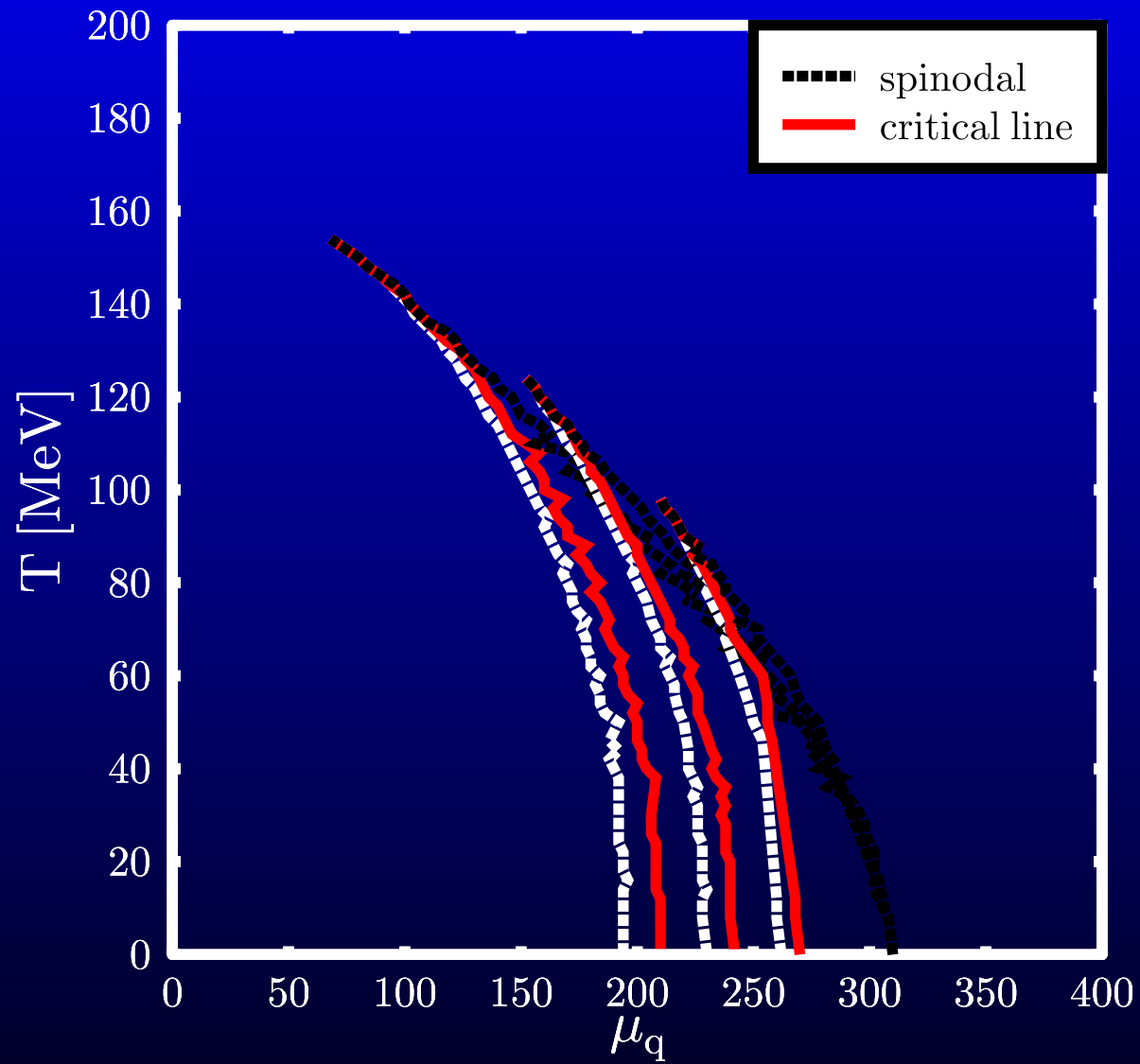
The Phase diagram II



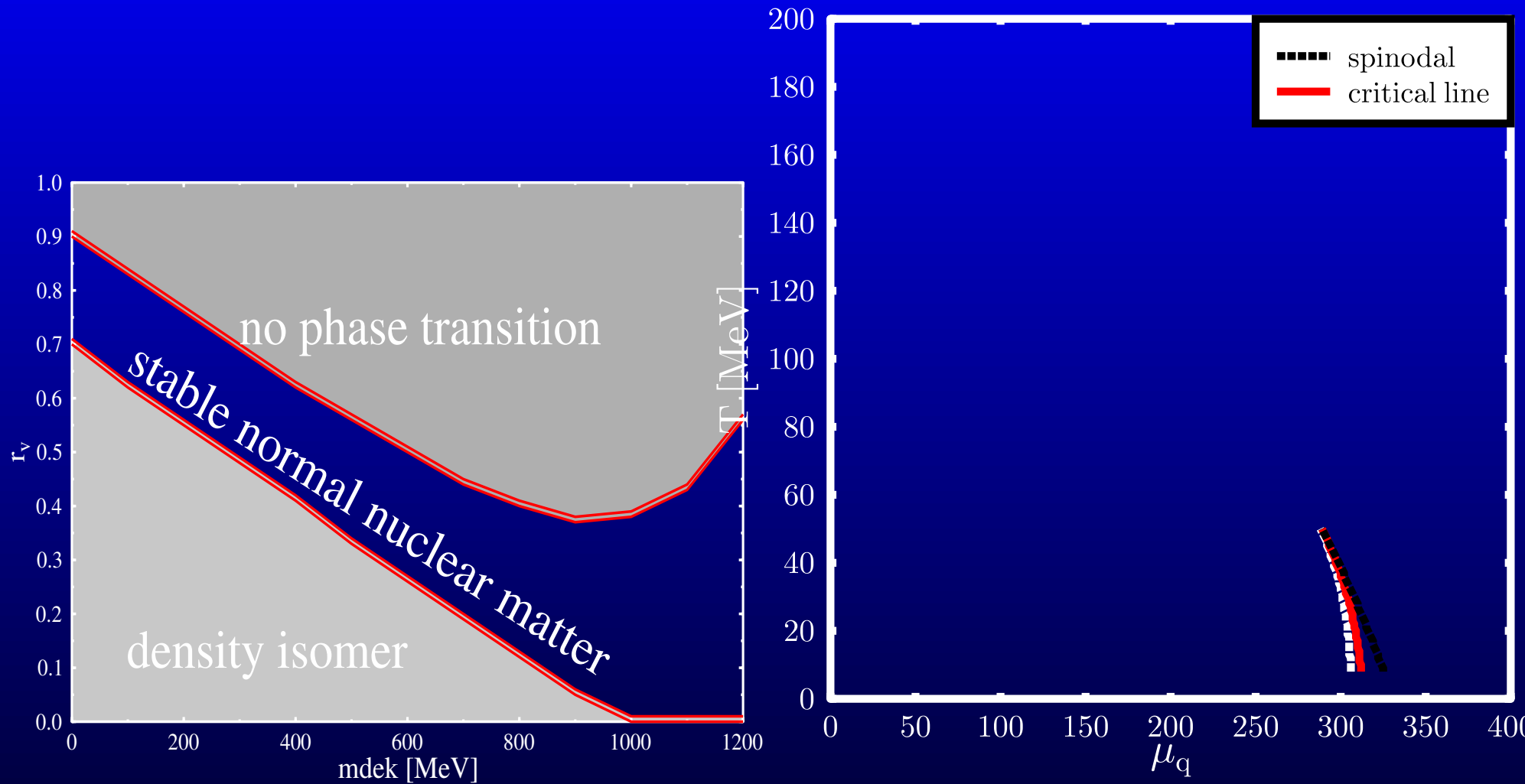
The Phase diagram II



The Phase diagram II

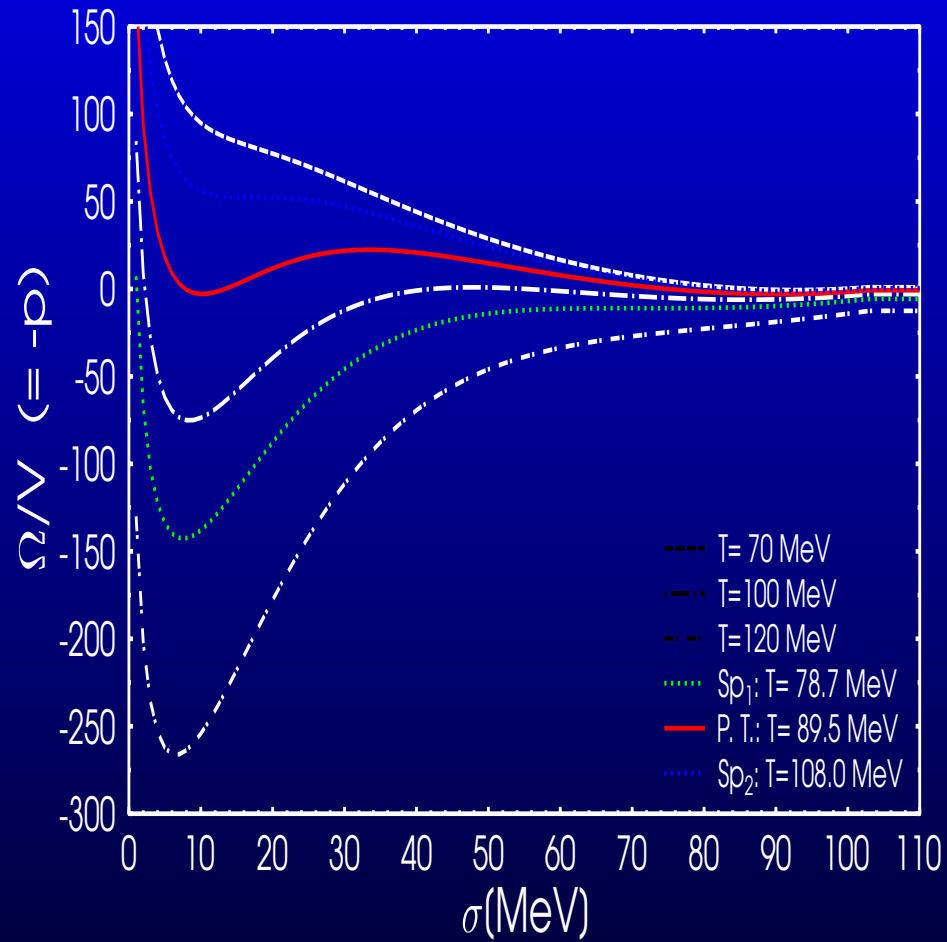


Phase structure at $T=0$ and T_c prediction

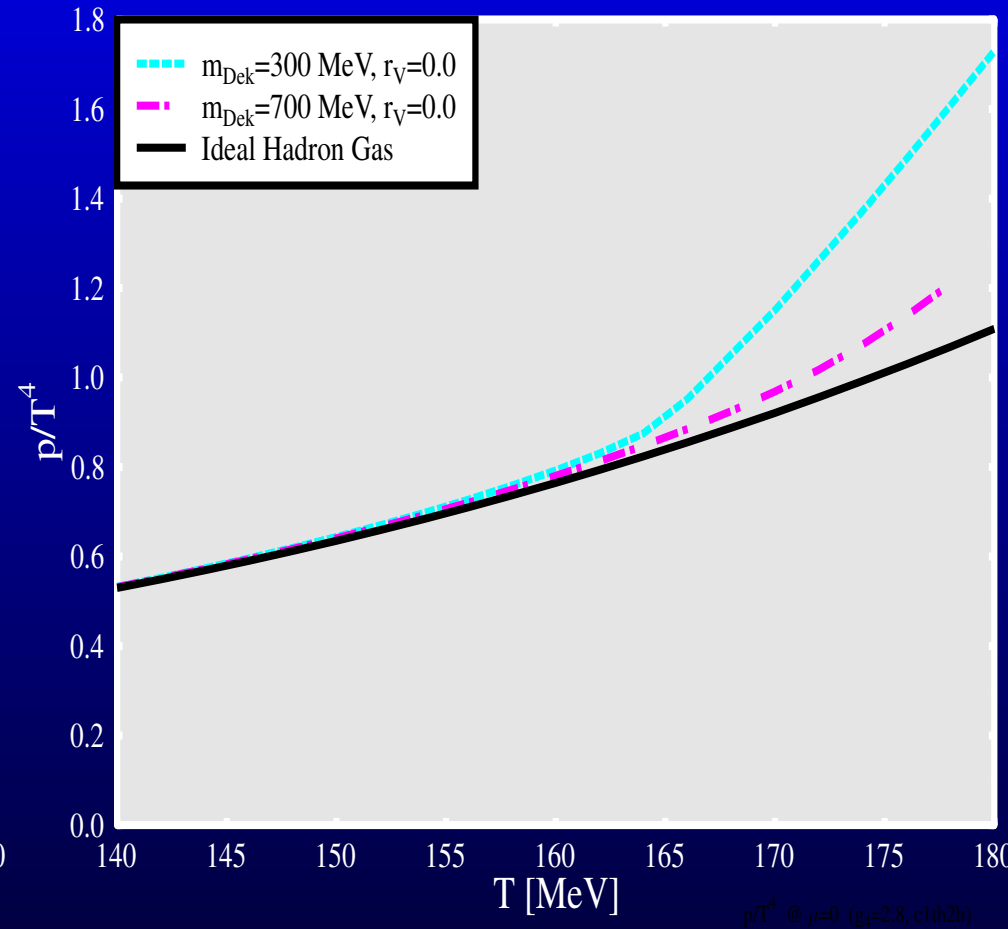
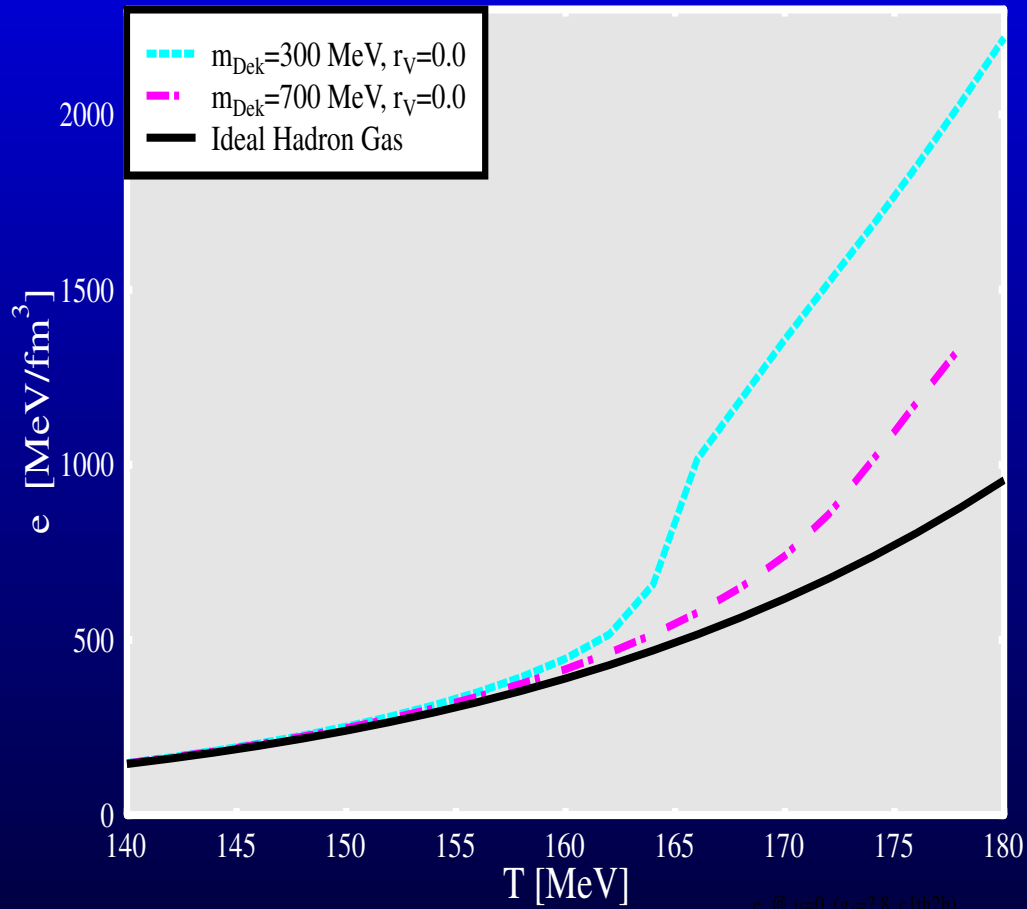


Effective potential at $\mu = 170$ MeV

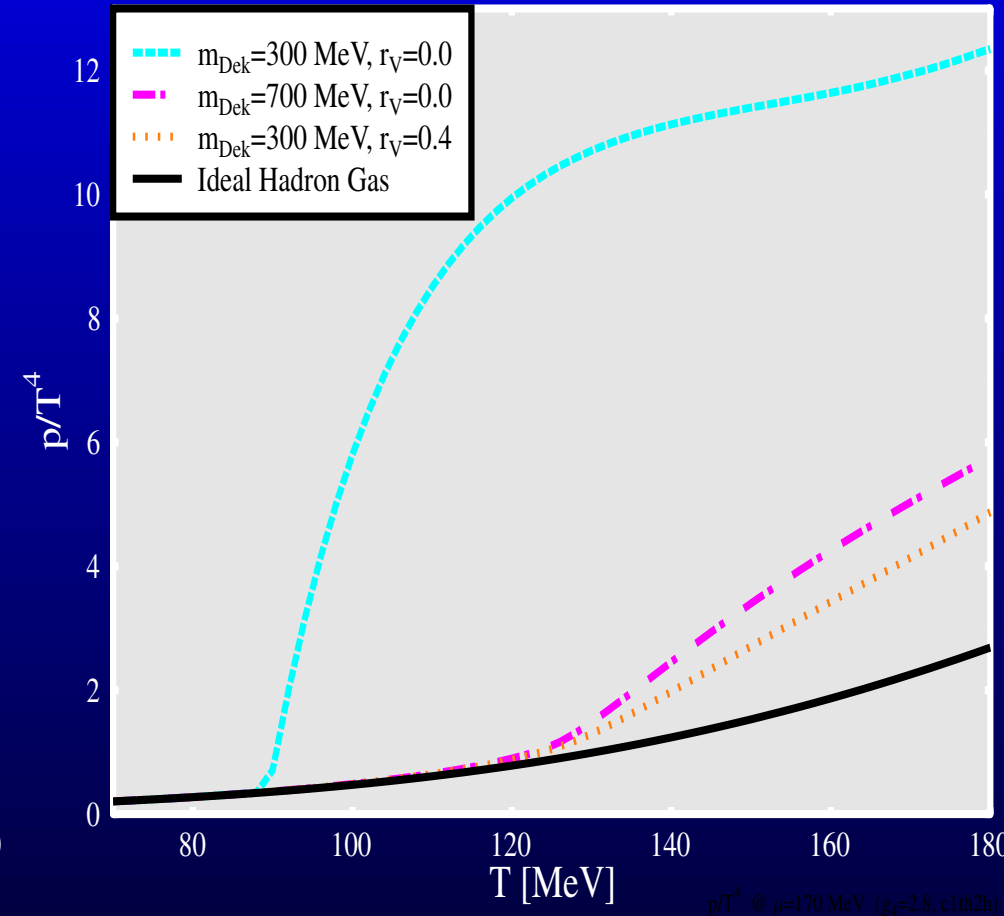
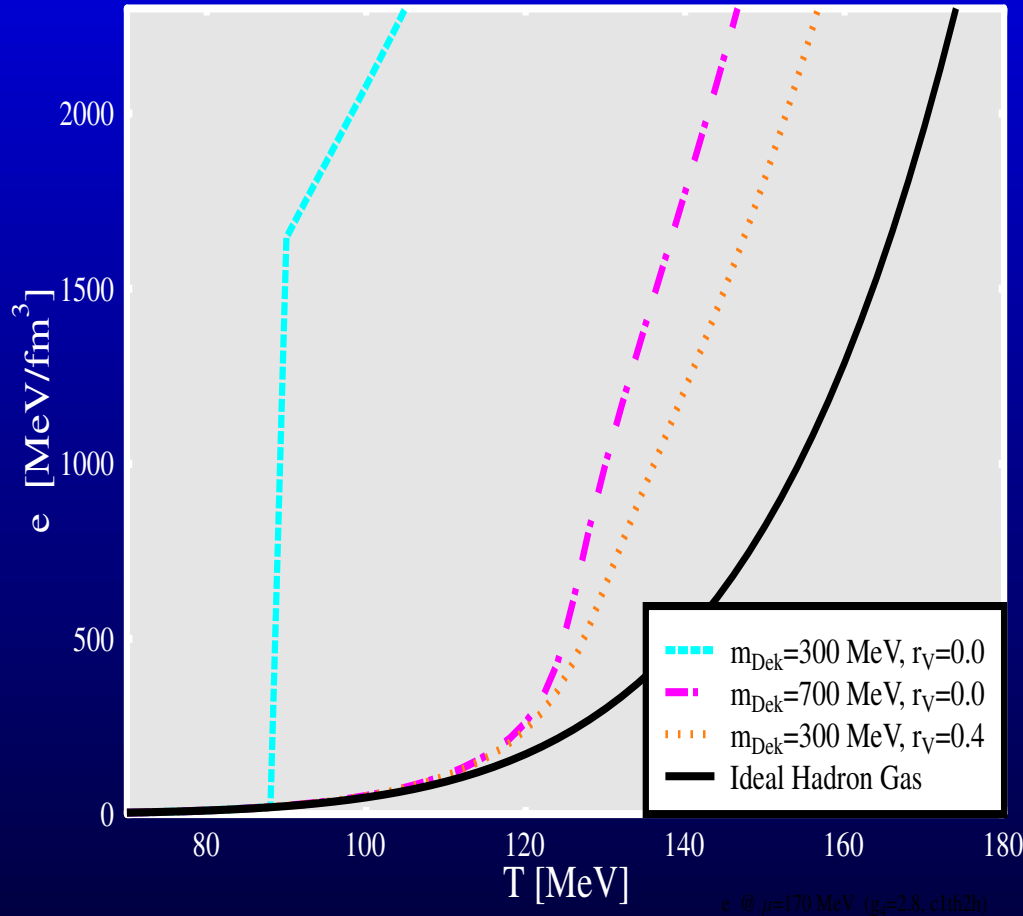
$g_4=2.8, r_V=0, m_{\text{Dek}}=300$ MeV, $\mu=170$ MeV



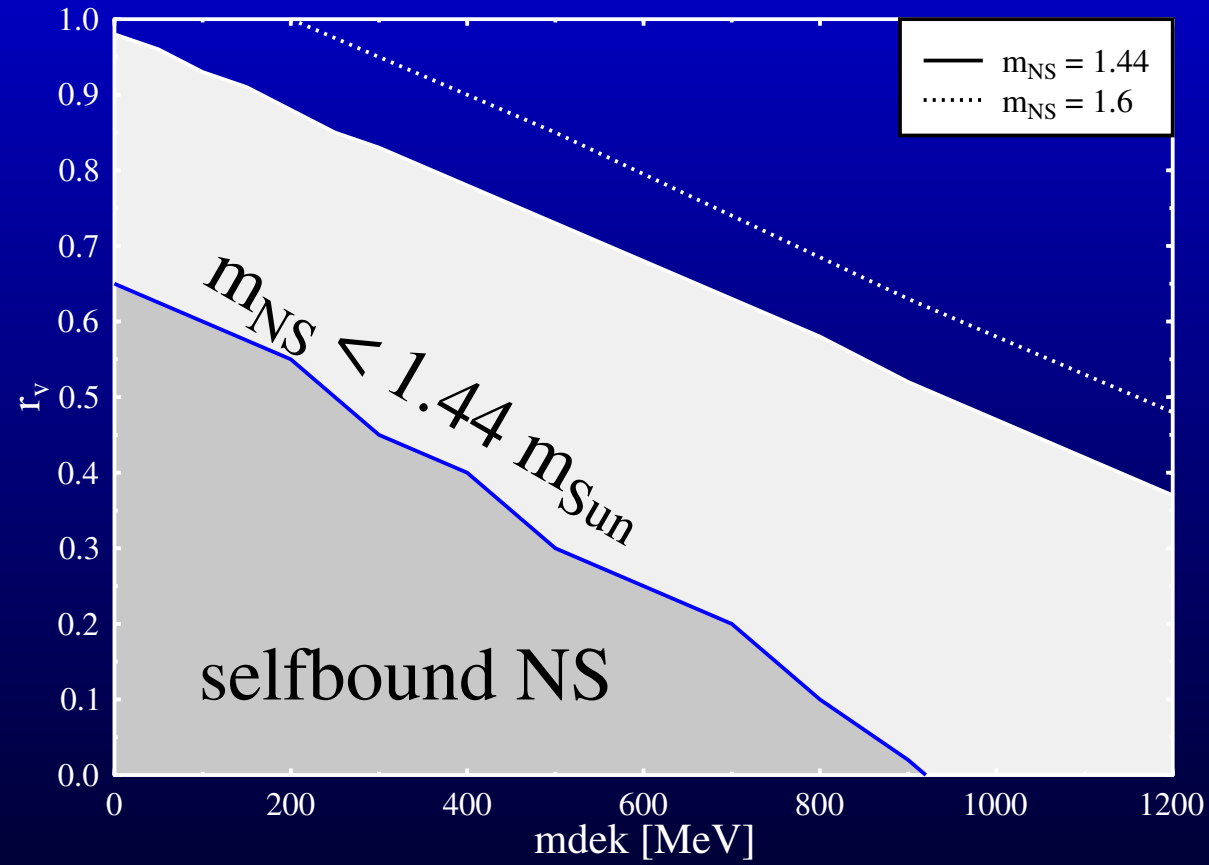
Pressure and energy density at $\mu = 0$



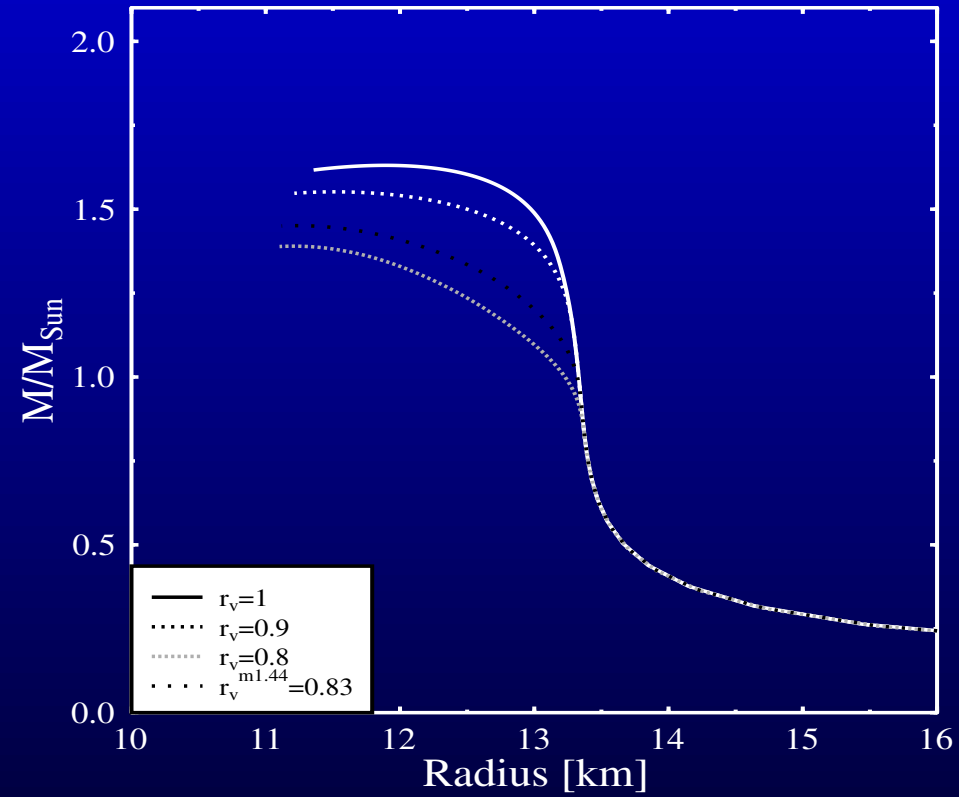
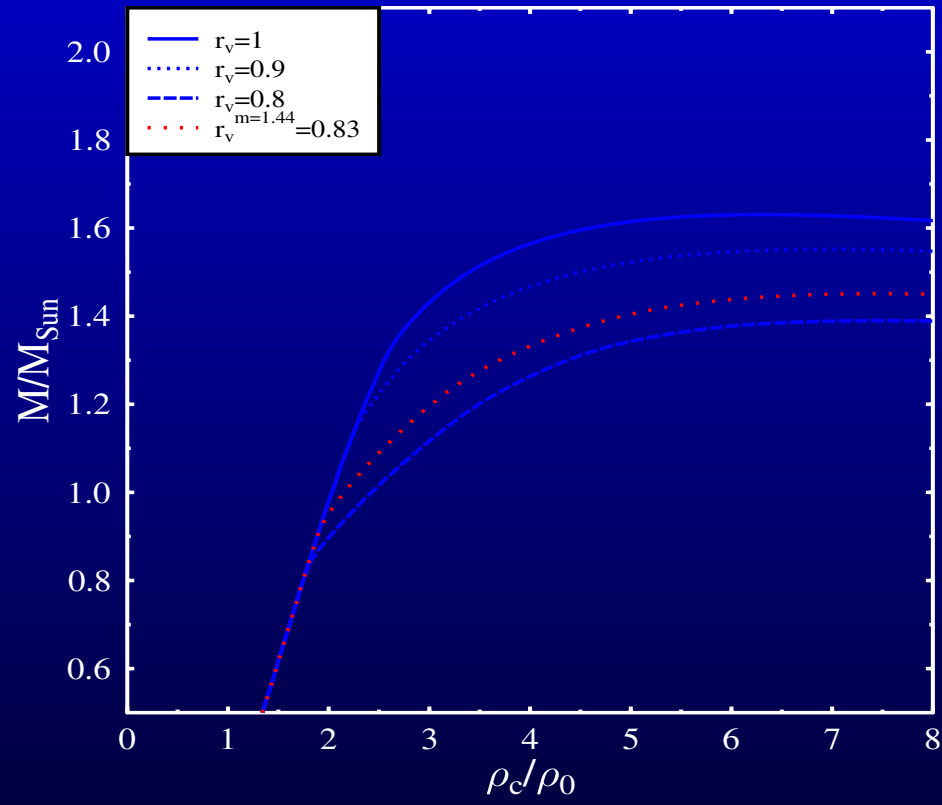
Pressure and energy density at $\mu = 170$ MeV



Neutron stars I - Parameter scan



Neutron stars II



Particle ratios in relativistic heavy ion collisions

Global "Freeze-out" of an interacting hadron gas in thermal and chemical equilibrium.

$$\rho_i = \gamma_i \int_0^\infty \frac{d^3k}{(2\pi)^3} \left[\frac{1}{\exp [(E_i^* - \mu_i^*)/T] \pm 1} \right] + \text{decays}$$

Particle ratios in relativistic heavy ion collisions

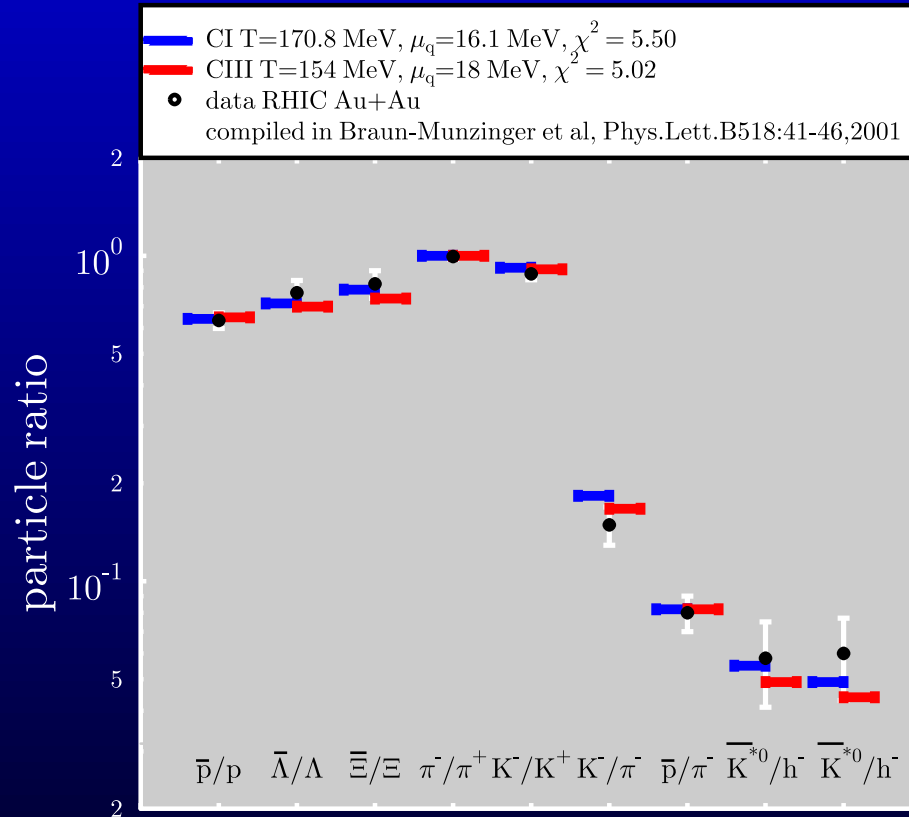
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choose T, μ such that

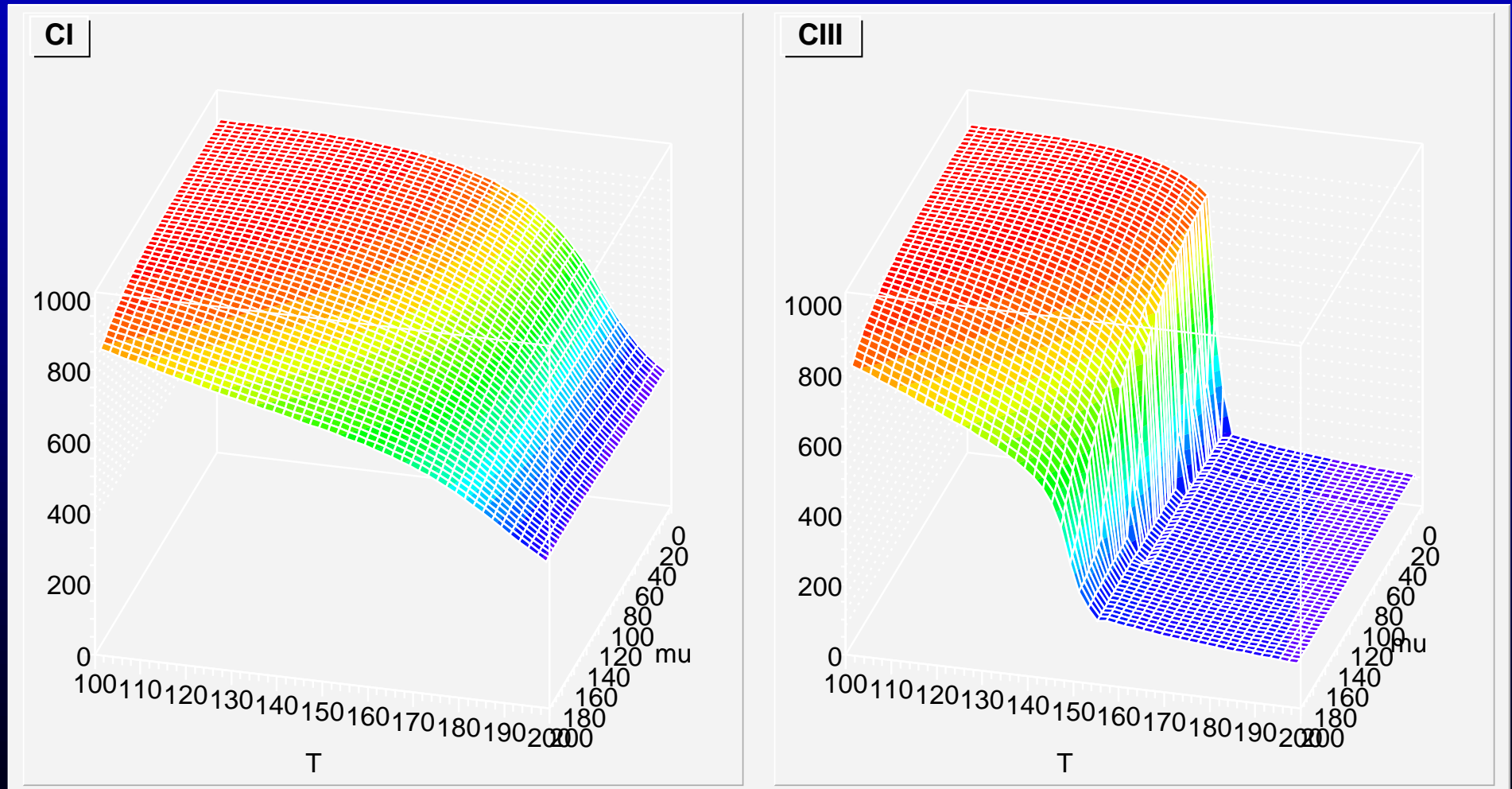
$$\chi^2 = \sum_n \frac{(r_n^{\text{exp}} - r_n^{\text{model}})^2}{\sigma_n^2}$$

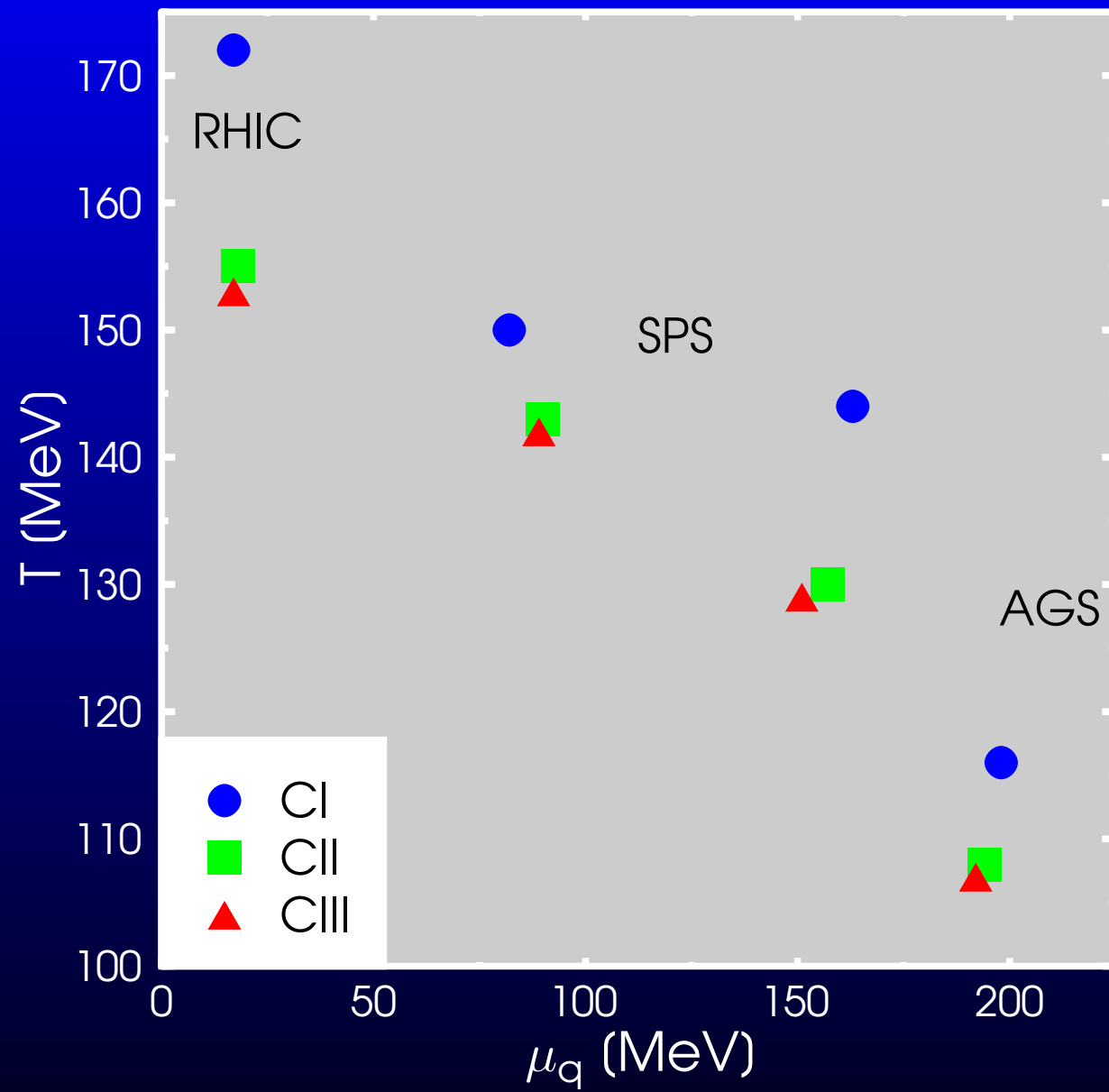
minimal

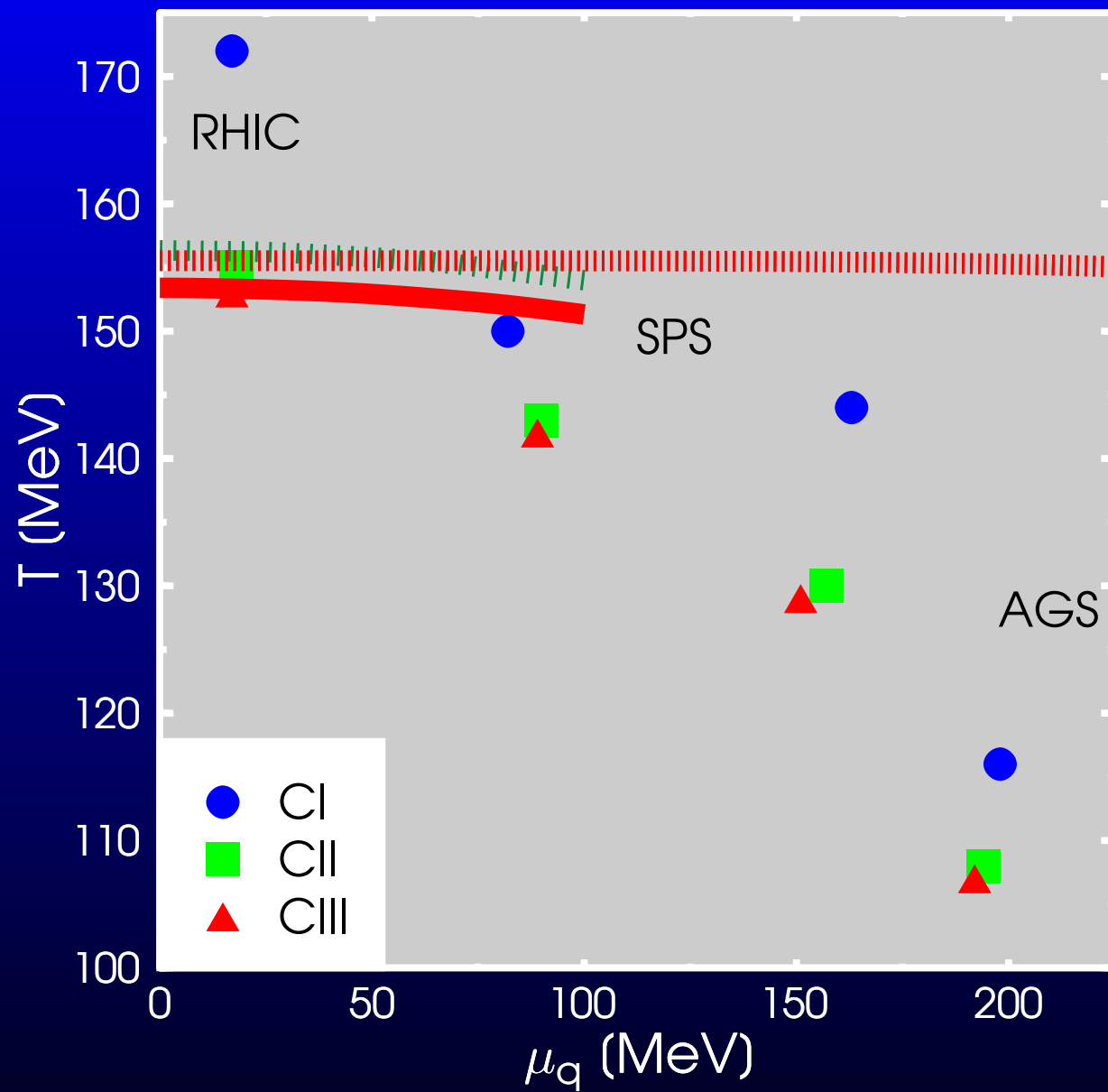


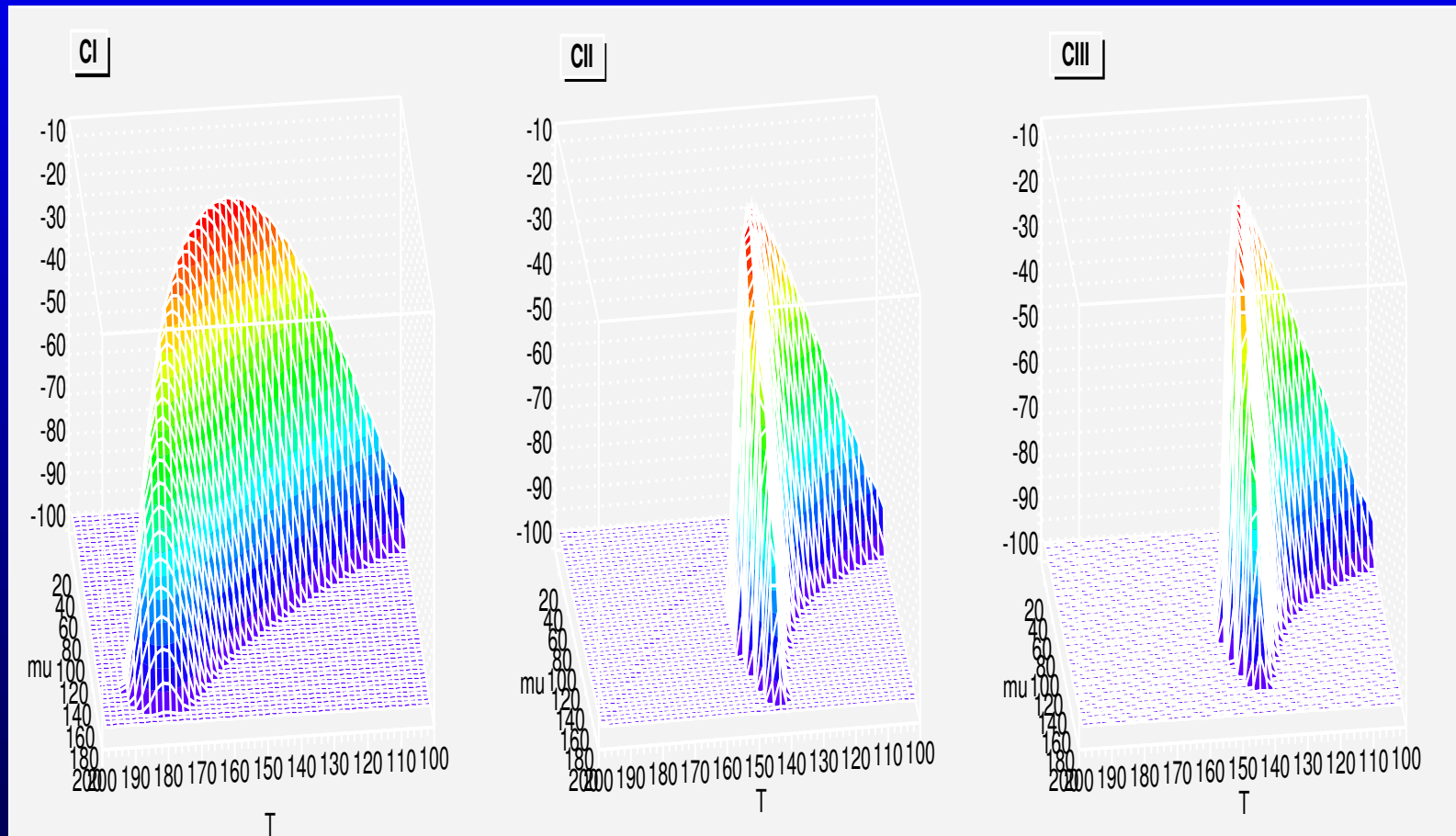
RHIC @ 130 AGeV

Effective nucleon mass in hot and dense matter

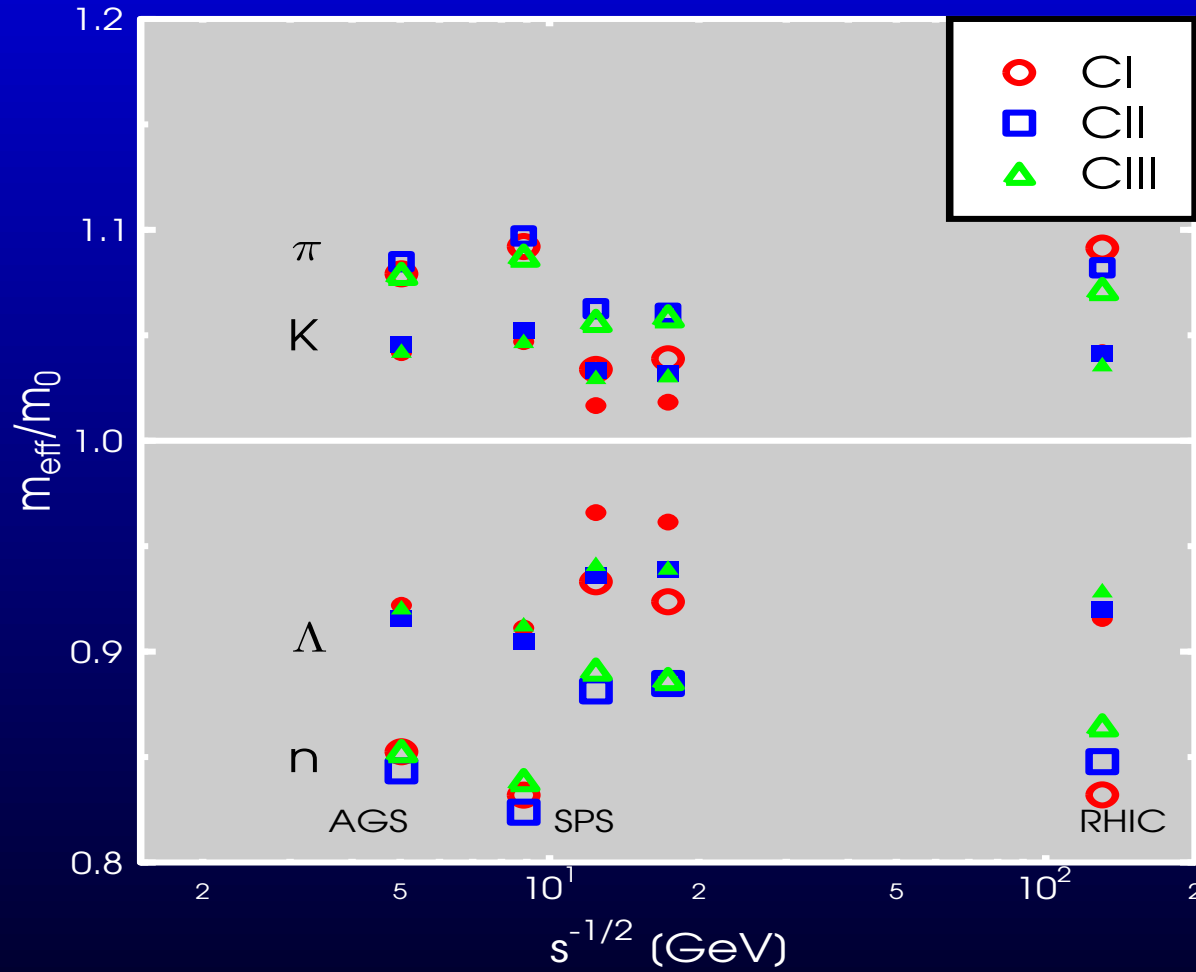






χ^2 at SPS 160 AGeV

Effective Masses at freeze-out



Summary

- Baryon resonances drive the chiral phase transition
- hadron/energy density 'explodes' - deconfinement
- T_c may be around 150 MeV - BUT then nuclear matter wrong
- stable nuclear matter: $T_c \approx 50$ MeV
- Phase diagram, particle ratios, nuclear matter and neutron stars give strong constraints on hadronic models (depend on reliable lattice results)
- can give prediction on difference between T_c and T_f in for specific phase diagram in single approach !!!

Outlook

A lot of work to do...

- consider coupling of whole resonance spectrum
- work on model (potentials, meson fluctuations,...)
- compare to lattice EoS, ratios..