



# The Increased Biological Effectiveness of Heavy Charged Particle Radiation:

## From Cell Culture Experiments to Biophysical Modelling

Michael Scholz  
GSI Darmstadt

# Ion Beams for Tumor Therapy

Advantage of ion beams for therapy:

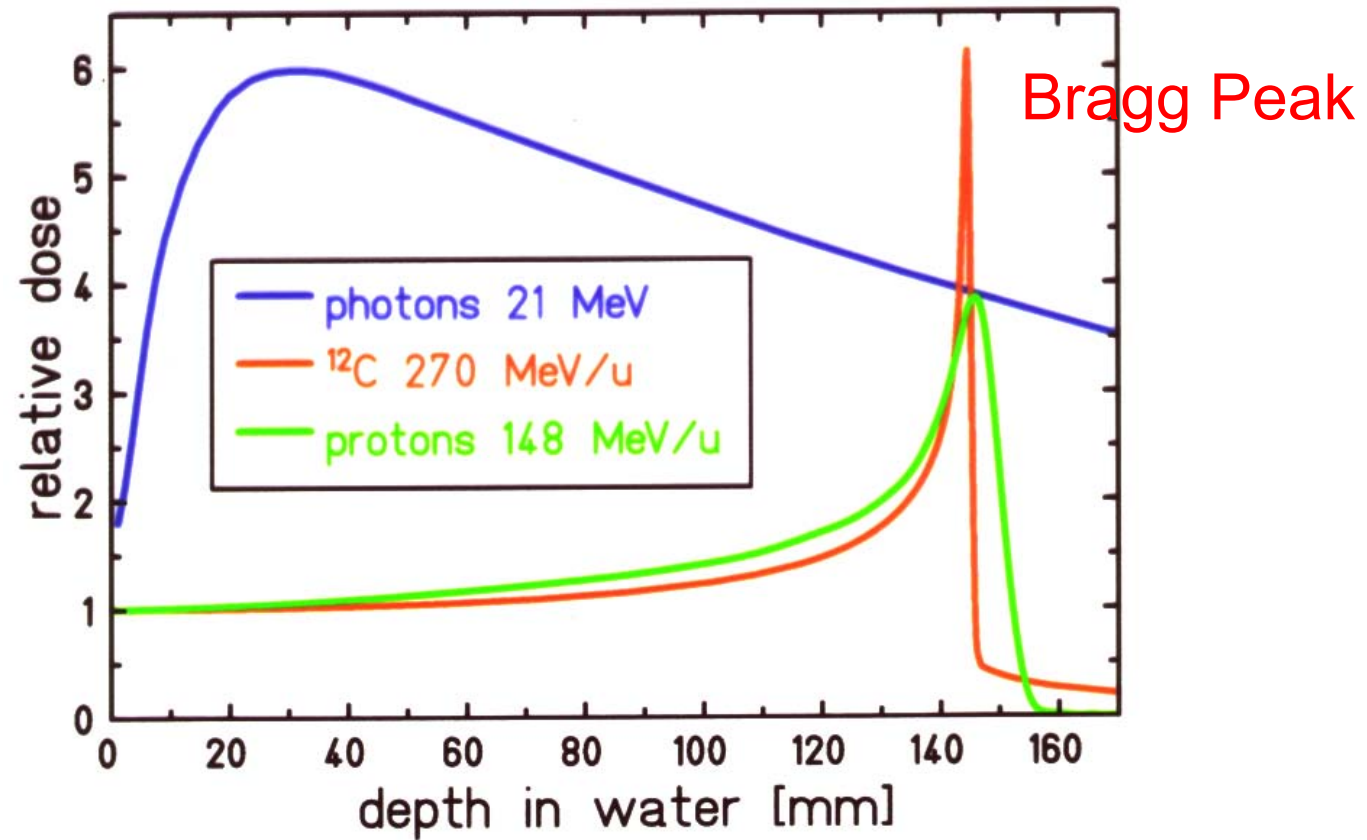
**Physical** aspects:

- Inverted depth dose profile
- Defined penetration depth
- Reduced lateral scattering

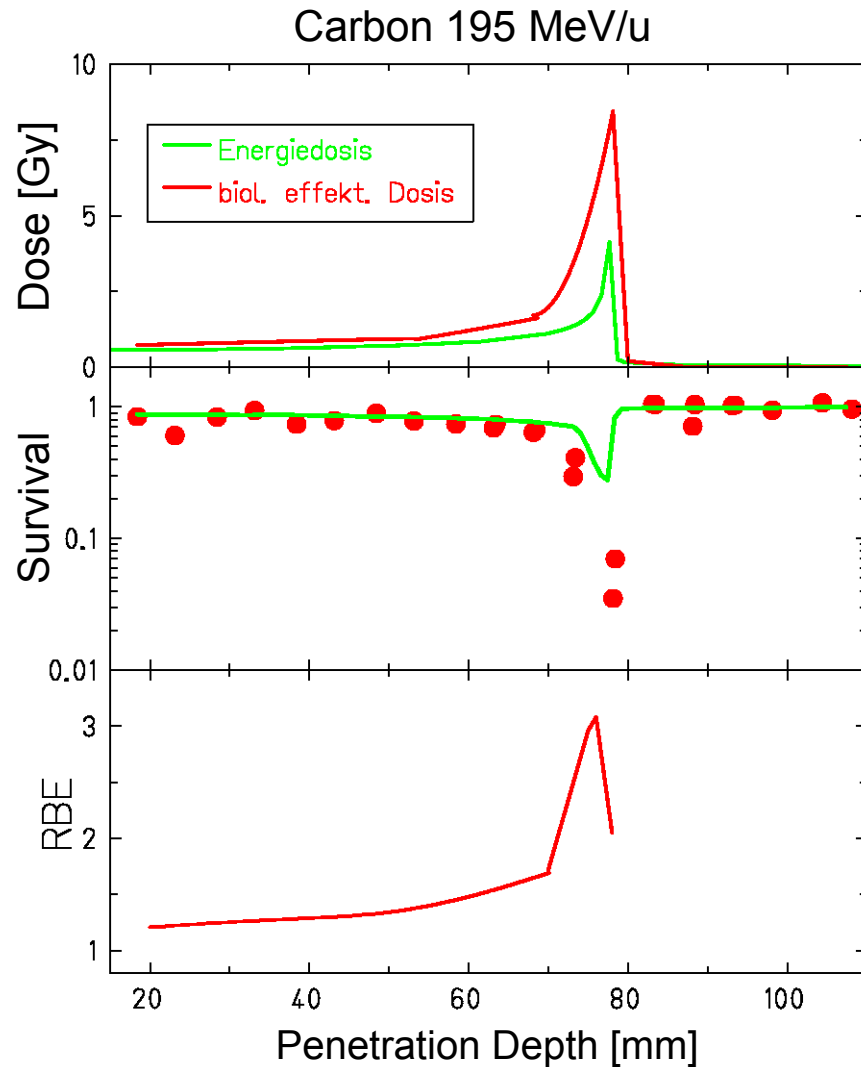
**Biological** aspects:

- Increased effectiveness
- Reduced oxygen effect

# Inverted Depth Dose Profile



# Biological Advantage: Increased Effectiveness



Differential Effect:

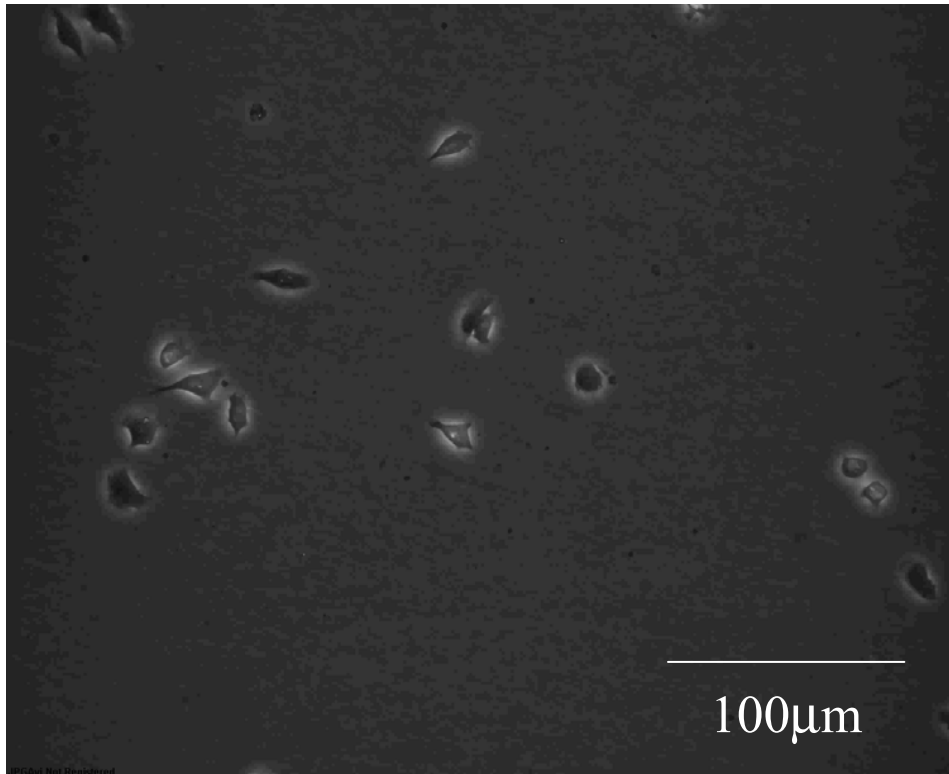
RBE(Depth)

>

RBE(Entrance)

# Cell Survival

## V79 Chinese Hamster Cells



G. Böhrensens/  
I. Katayama

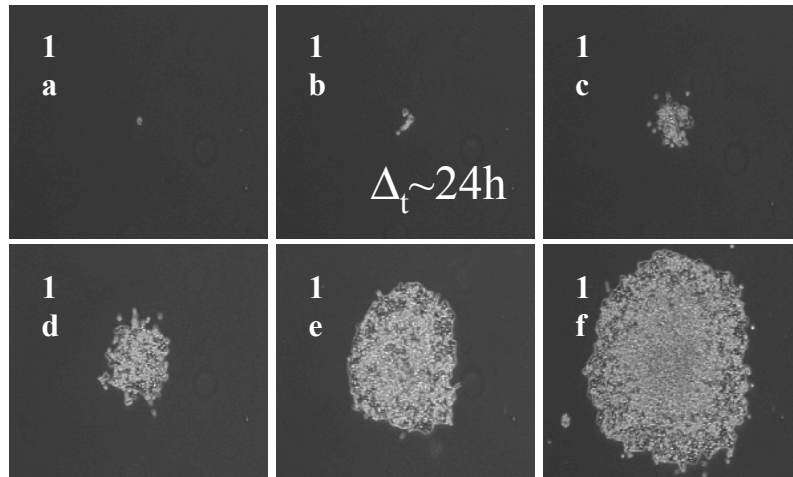
$\Delta t = 15 \text{ min}$   
 $T_{\text{ges}} = 85 \text{ h}$

Survivor:

1 cell  $\rightarrow$   $\geq 50$  cells  
(t=0) (t=7d)

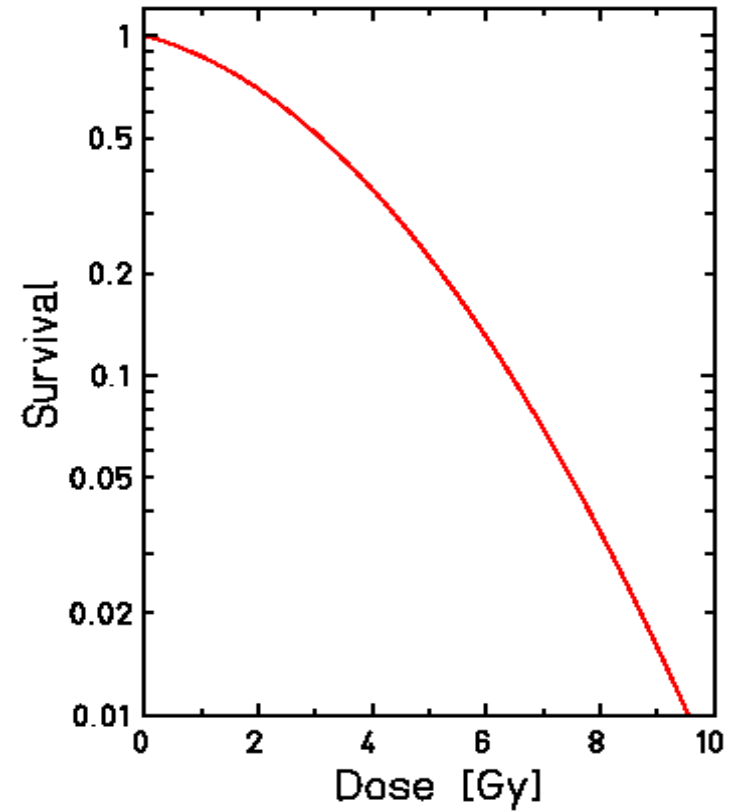
„Colony forming“

# Survival after Photon Irradiation



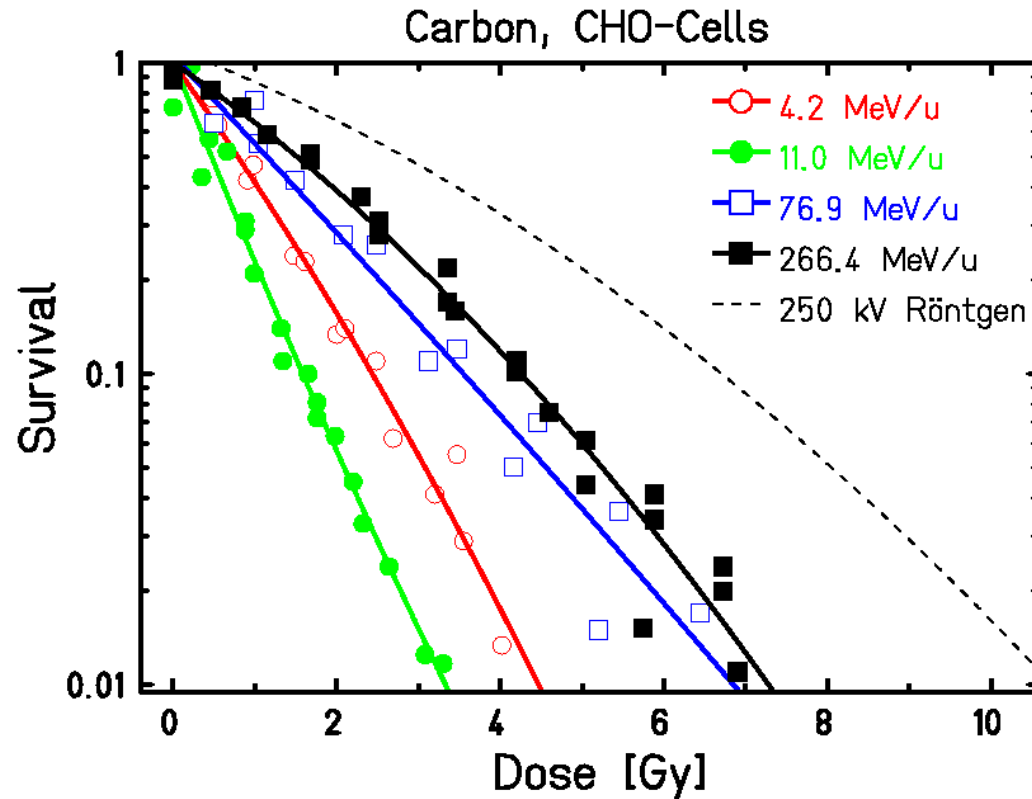
G. Böhrnsen

$$S = \frac{N_{col}}{N_{seed}} = e^{-(\alpha D + \beta D^2)}$$



Shoulder  $\leftrightarrow$  Repair

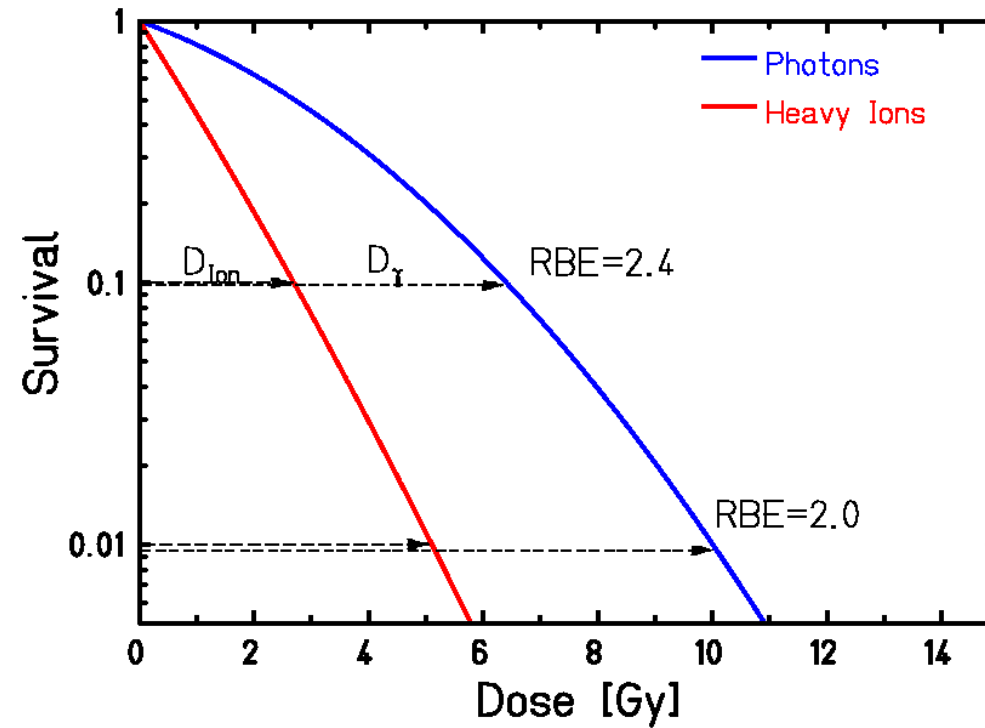
# Survival after Carbon Ion Irradiation



W. Kraft-Weyrather

- Increasing effectiveness with decreasing energy
- Saturation effects at very low energies (<10 MeV/u)
- Transition from shouldered to straight survival curves

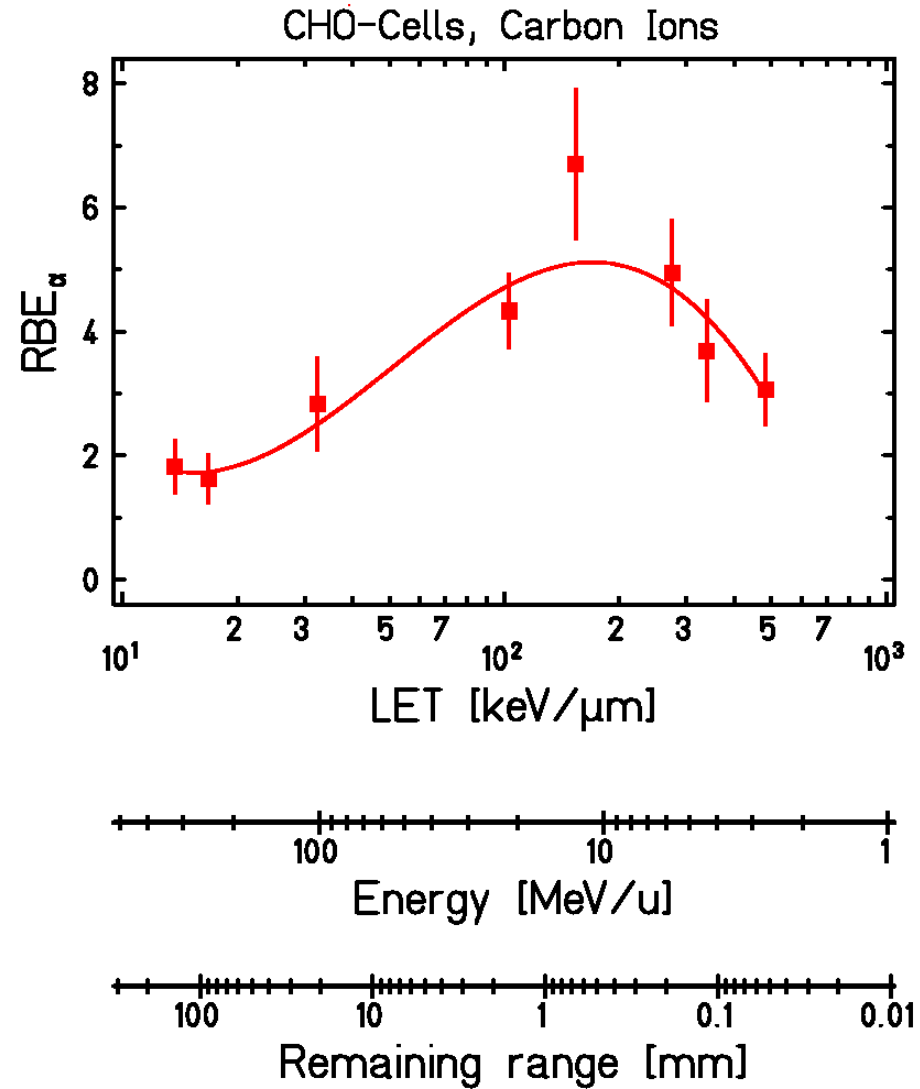
# Definition of Relative Biological Effectiveness



$$RBE = \frac{D_\gamma}{D_{Ion}} \Big|_{Isoeffect}$$

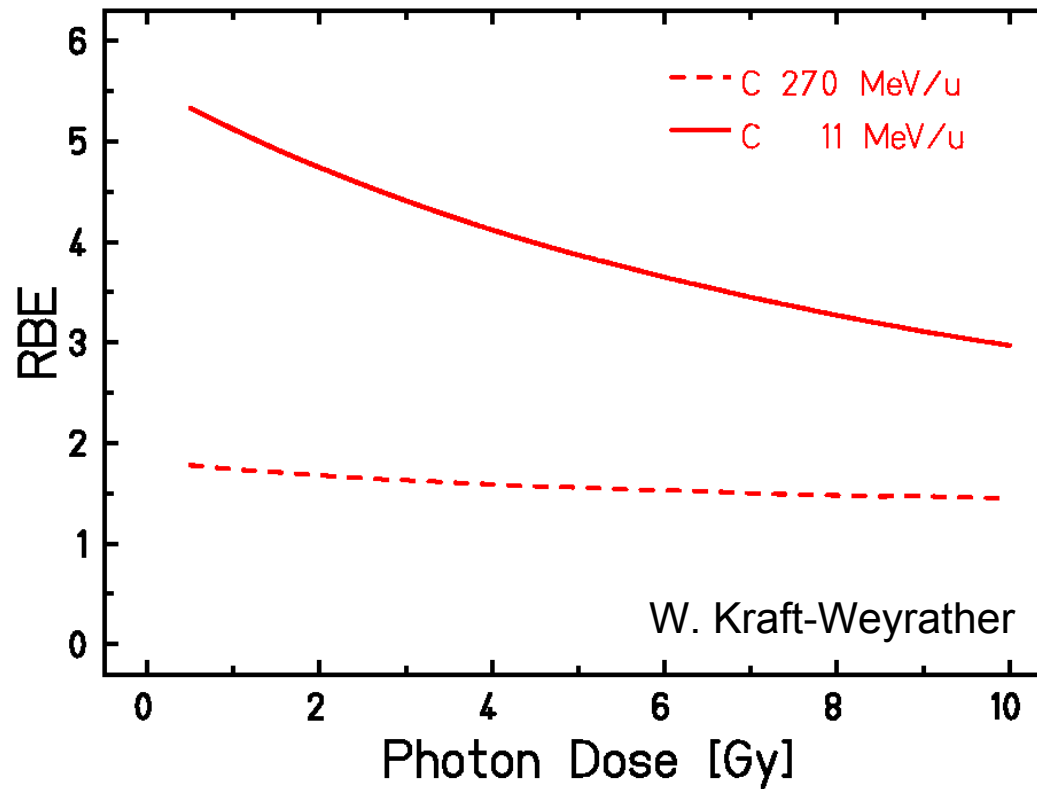


# RBE depends on LET



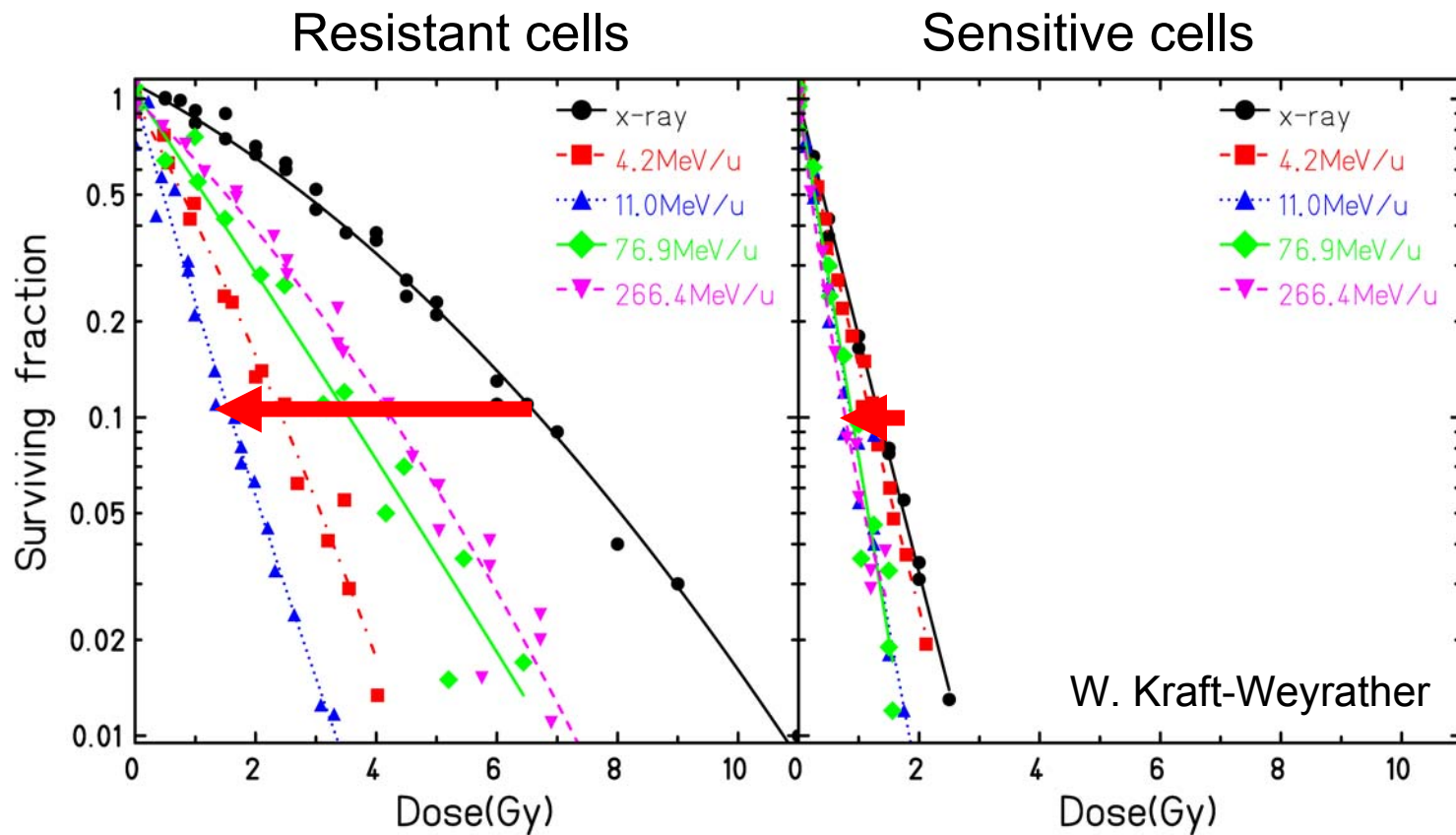
W. Kraft-Weyrather

# RBE depends on Dose



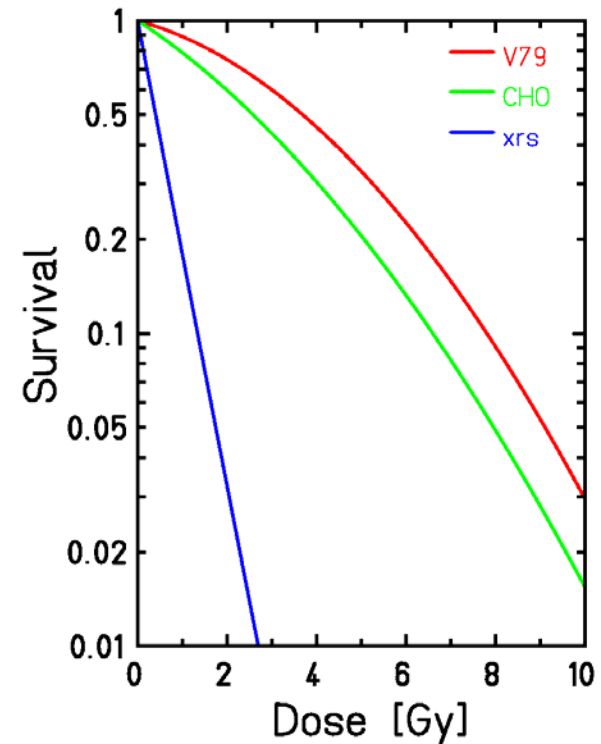
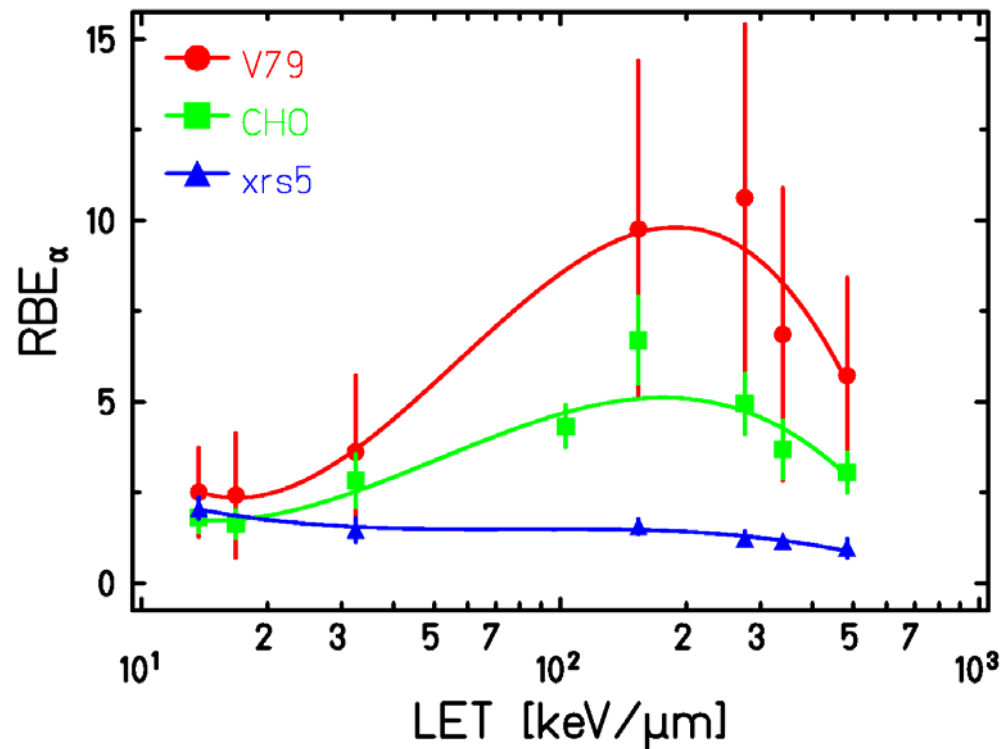
- RBE decreases with dose
- Dose dependence more pronounced for lower energies

# RBE depends on Cell Type



**Increase of effectiveness is more pronounced for resistant tumors compared to sensitive tumors**

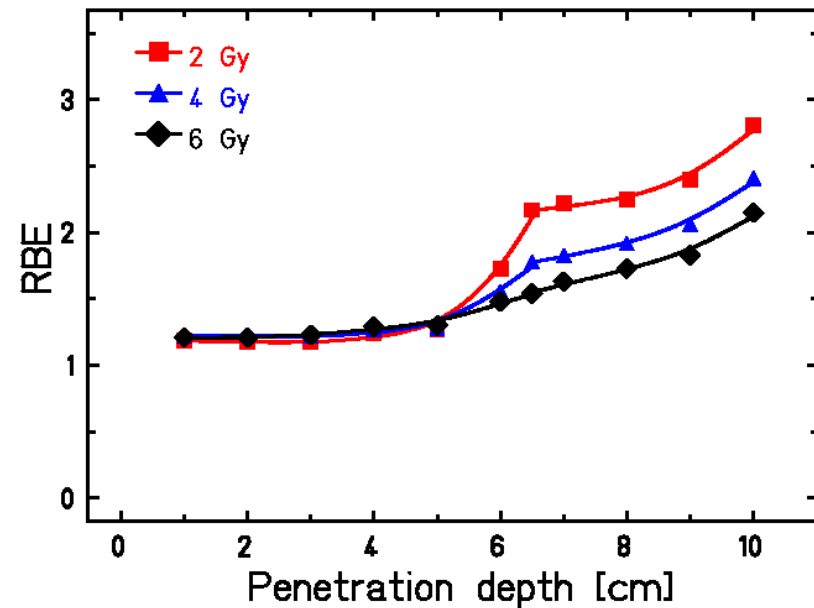
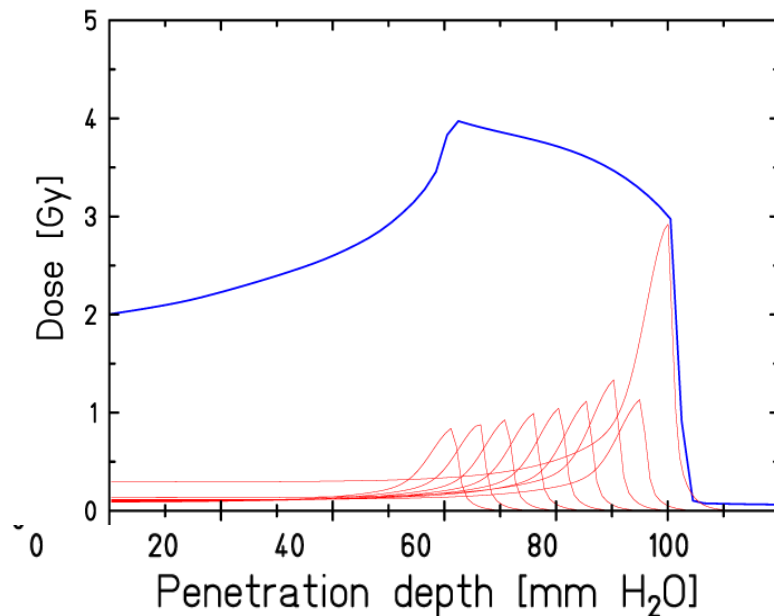
# RBE depends on Cell Type



W. Kraft-Weyrather

RBE is higher for resistant (repair proficient) cell types

# RBE depends on Depth



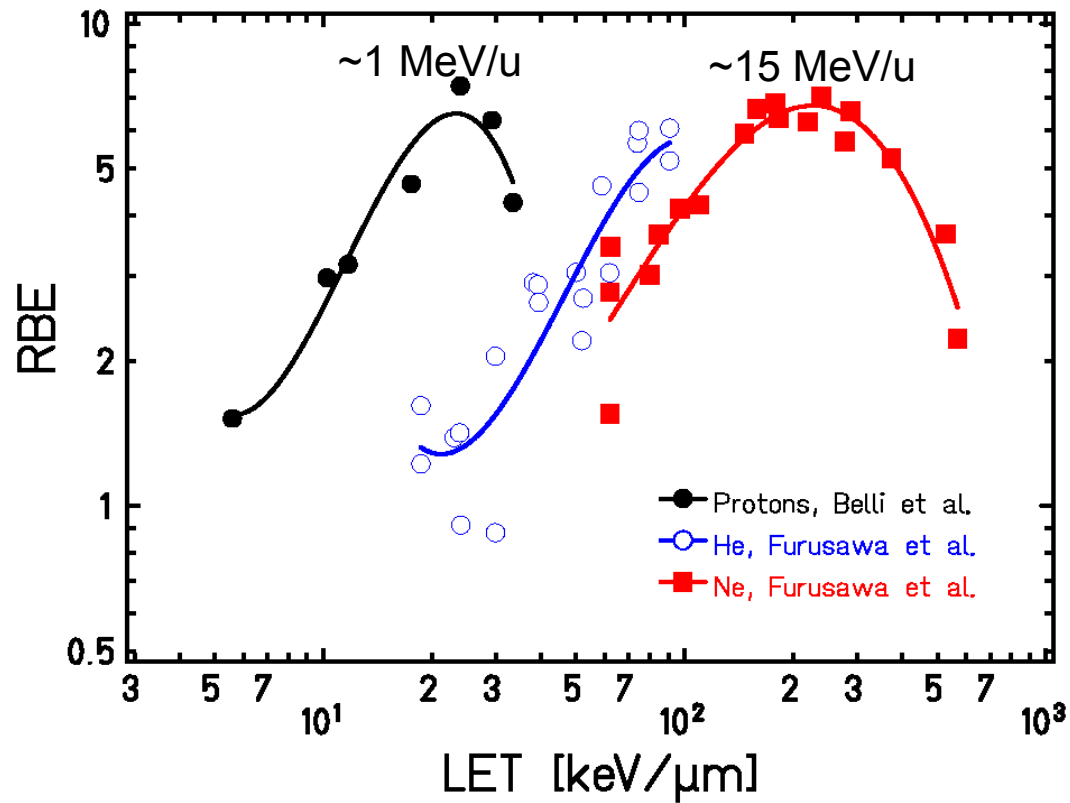
W. Weyrather et al.

Extended Bragg peak / SOBP irradiation:

Distal part: mainly Bragg peak ions  $\Rightarrow$  high RBE

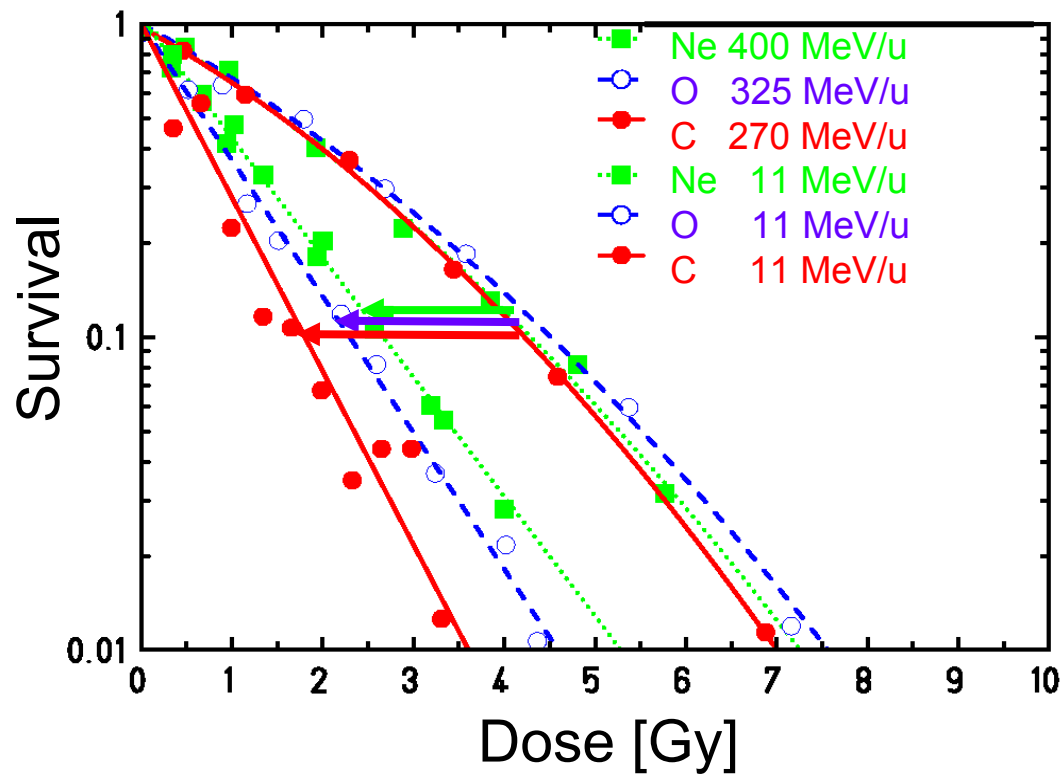
Proximal part: mix of Bragg peak and higher energies  $\Rightarrow$  moderate RBE

# RBE depends on Ion Species



- RBE maximum is shifted to higher LET for heavier particles
- The shift corresponds to a shift to higher energies

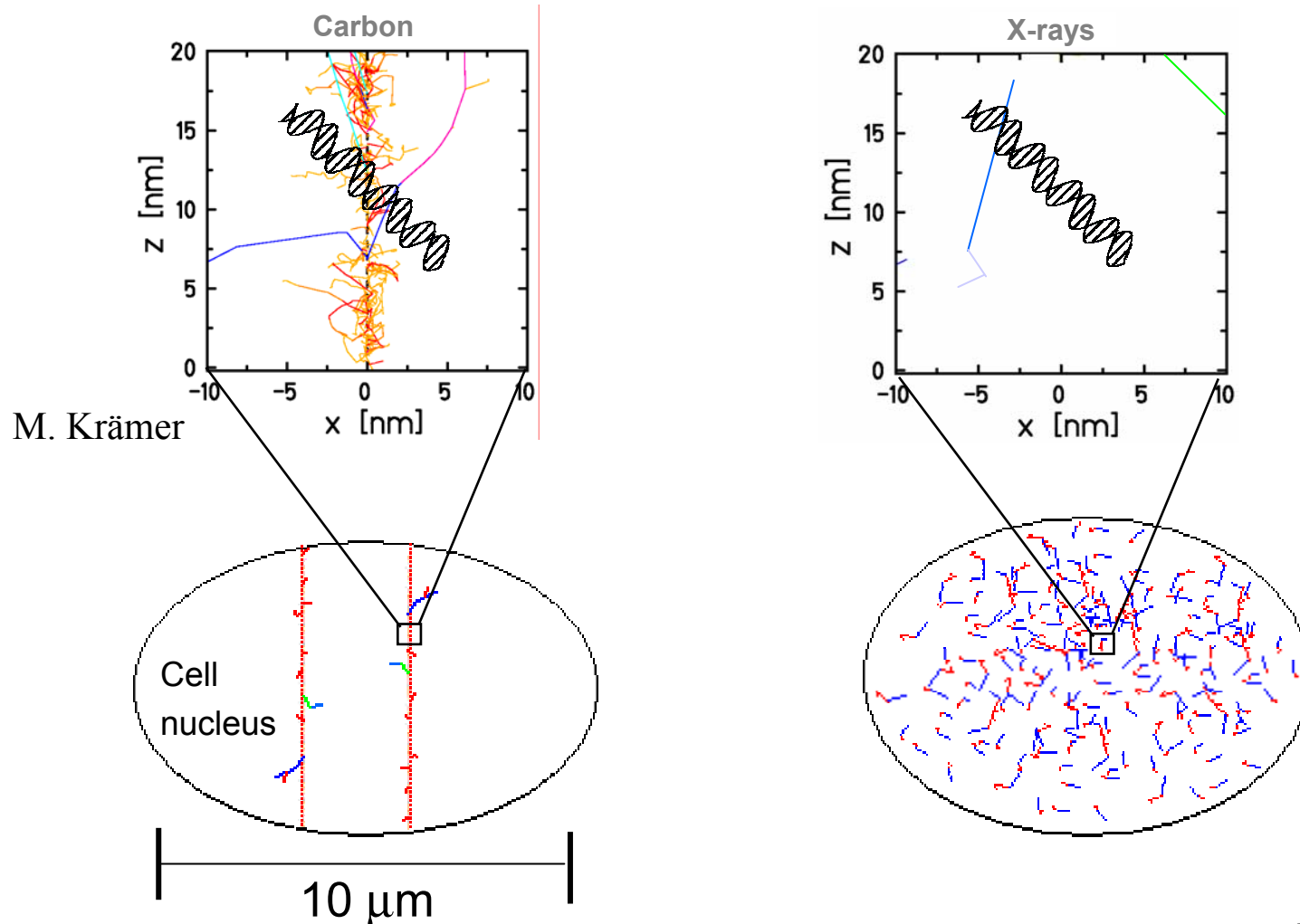
# Why Carbon Ions?



W. Kraft-Weyrather

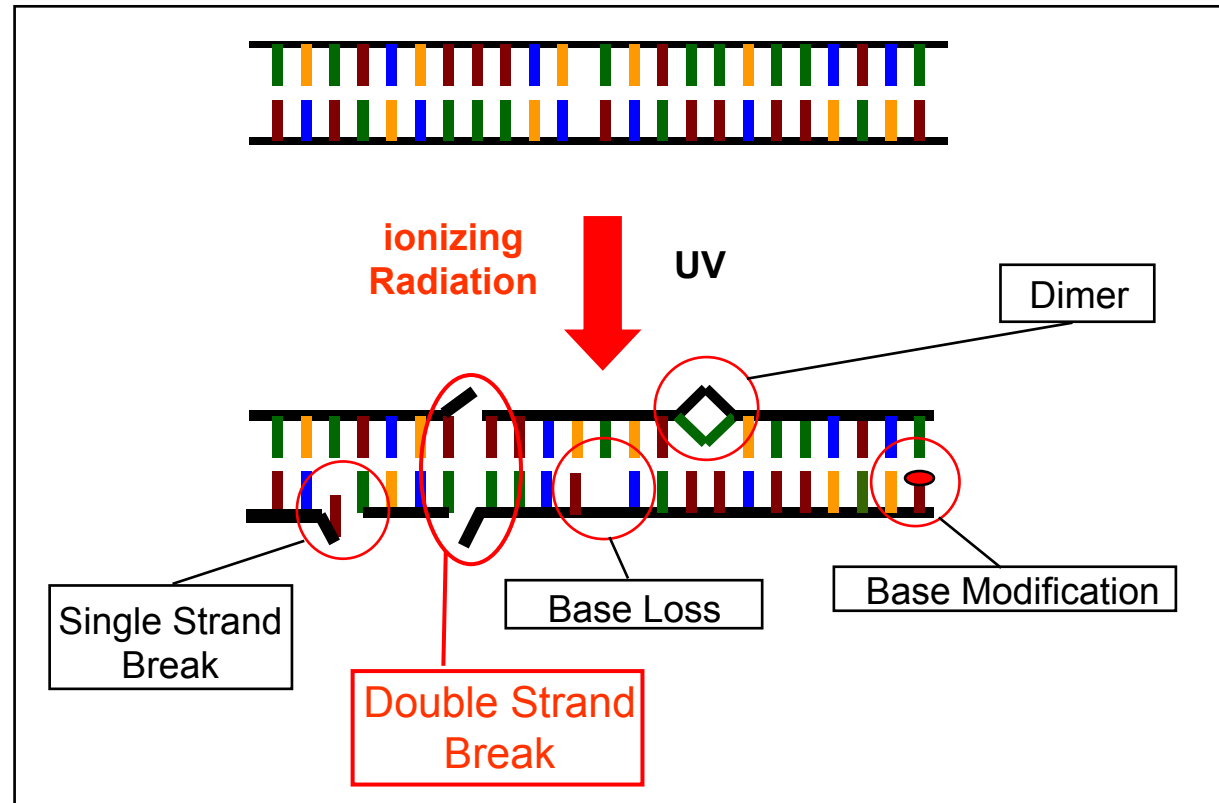
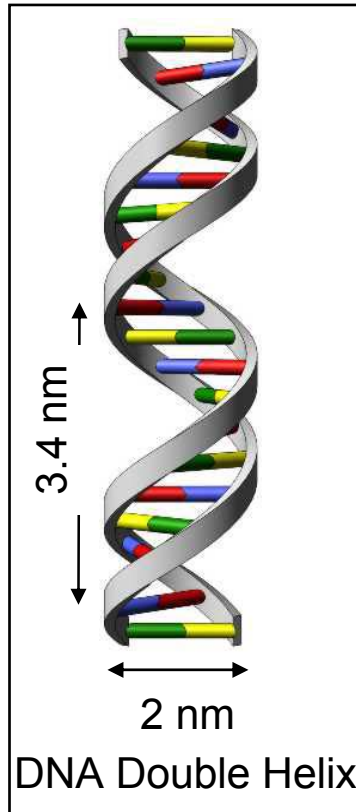
**Increase of RBE from entrance channel to Bragg peak region is most pronounced for carbon ions**

# Explanation of increased effectiveness



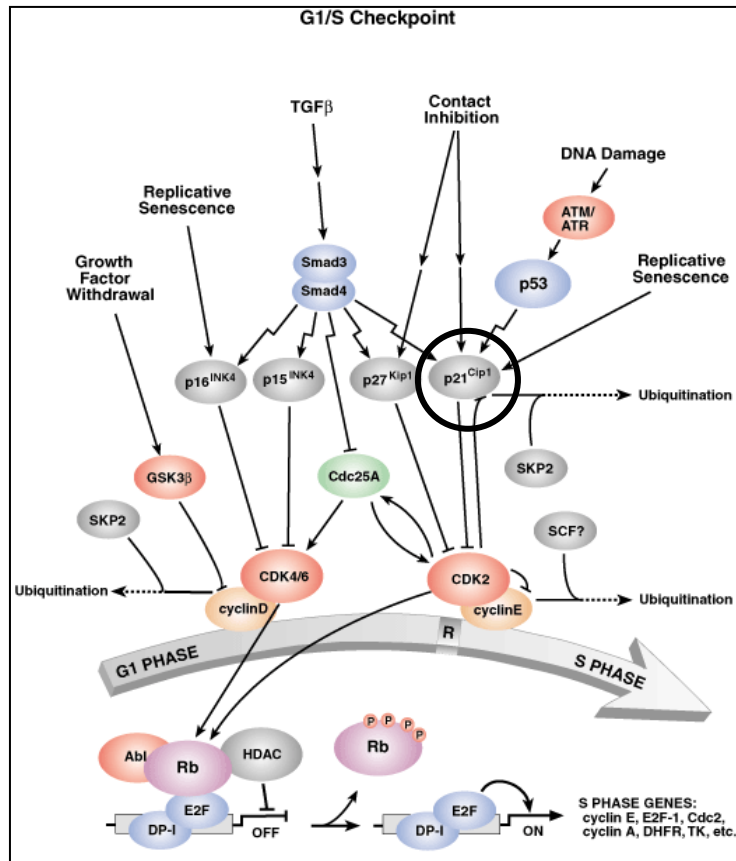


# Radiation induced DNA damage

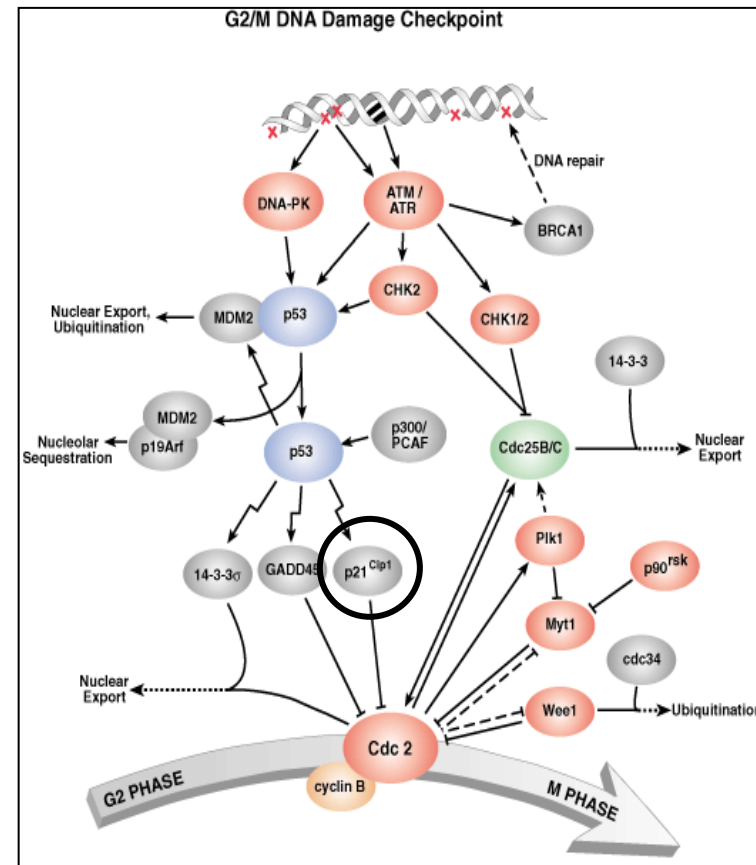


Cells are able to repair radiation induced DNA damage

# Cellular Repair Pathways

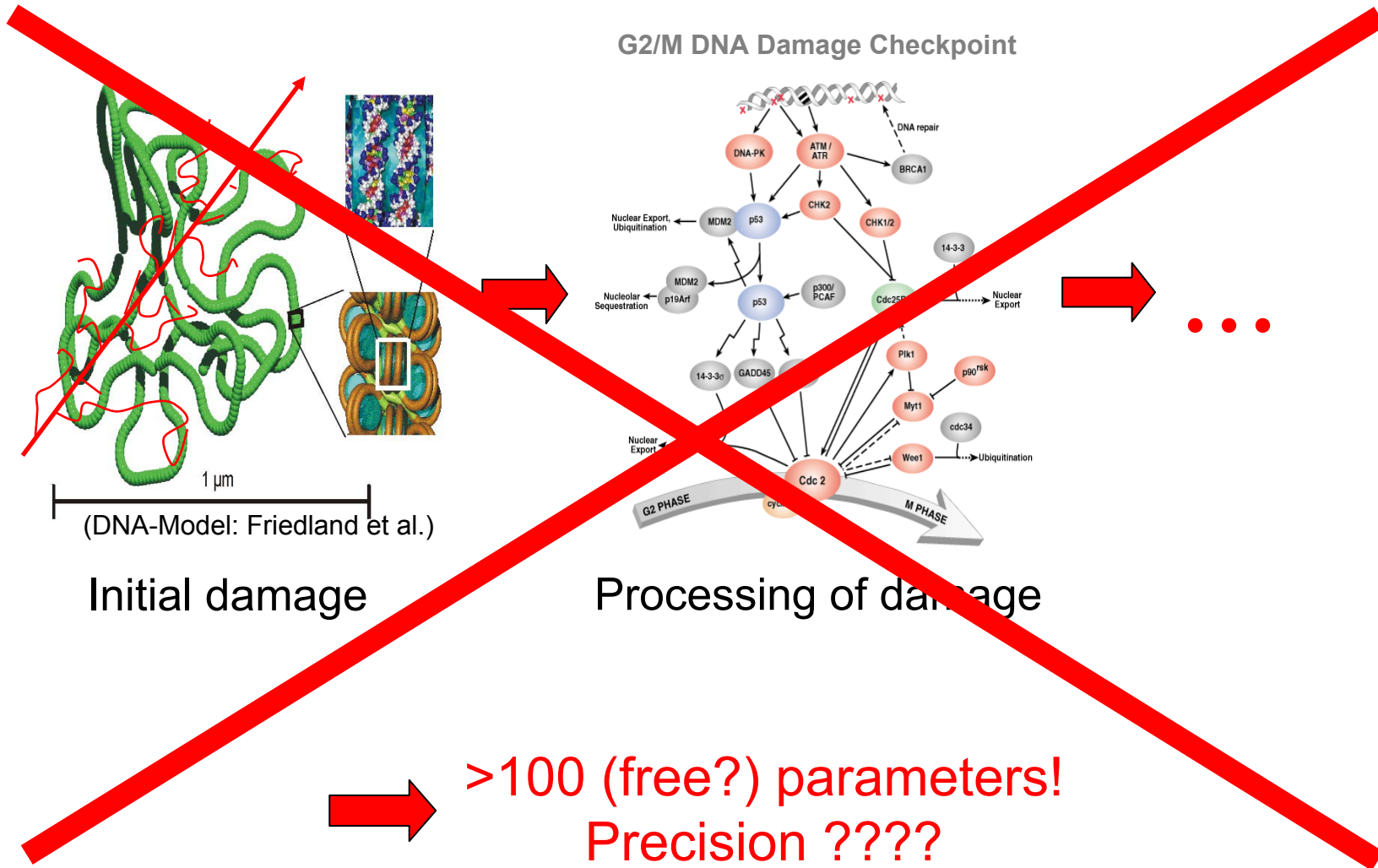


Transition  $G_1 \rightarrow S$ -Phase

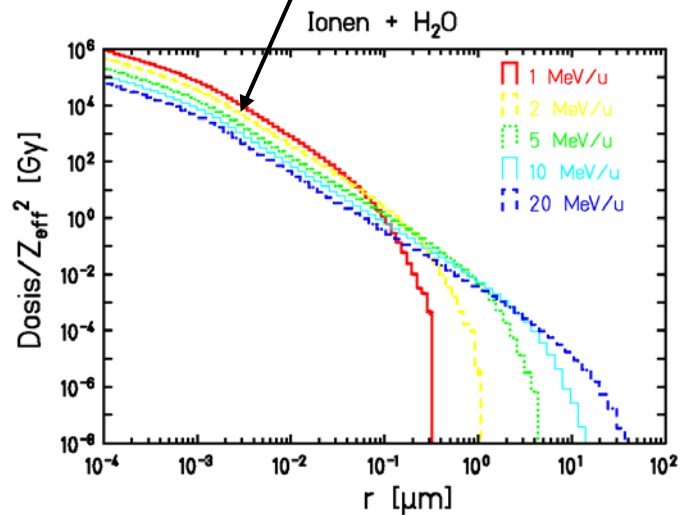
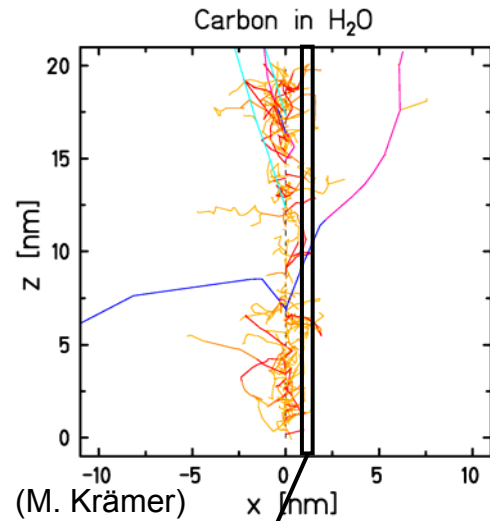


Transition  $G_2 \rightarrow M$ -Phase

# Can we model it from first principles?



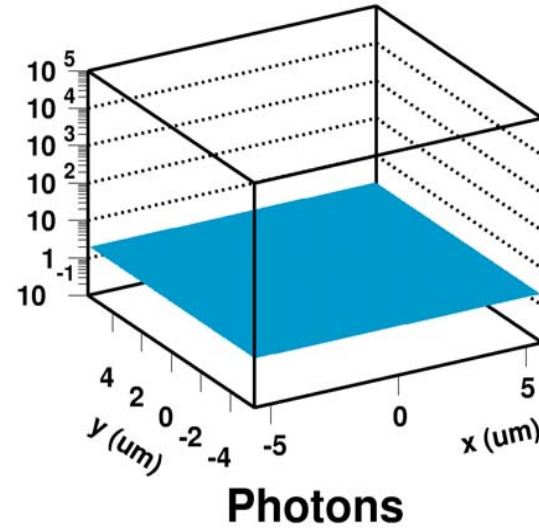
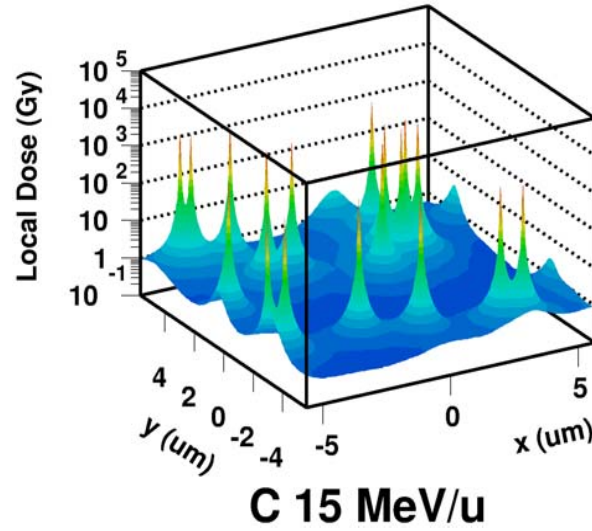
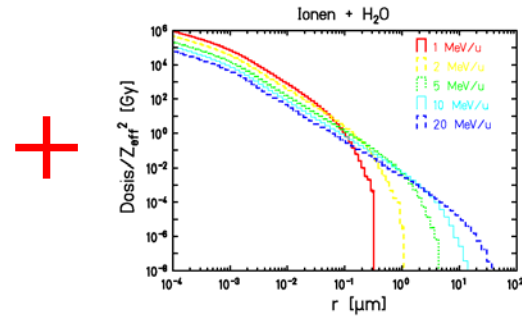
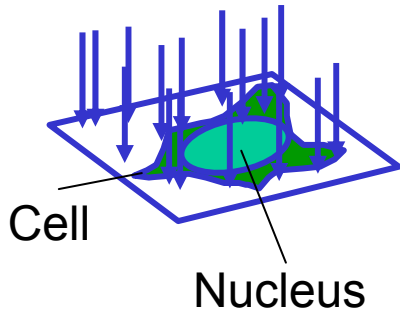
# Radial Dose Profile of Particle Tracks



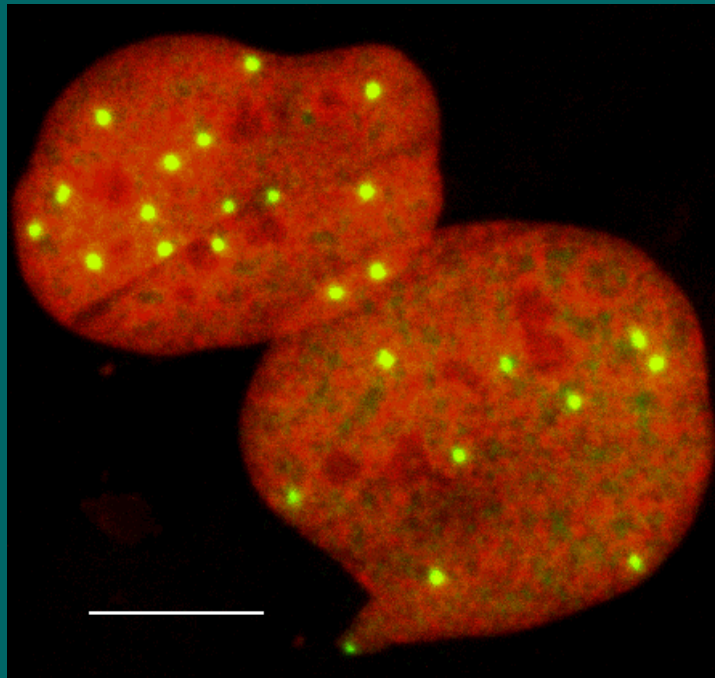
Radial Dose Profile:  
D(r): Expectation value

$$D(r) \sim 1/r^2$$
$$R_{\text{Track}} \sim E^c$$

# Microscopic Local Dose Distribution



# Visualization of Local Biological Effect

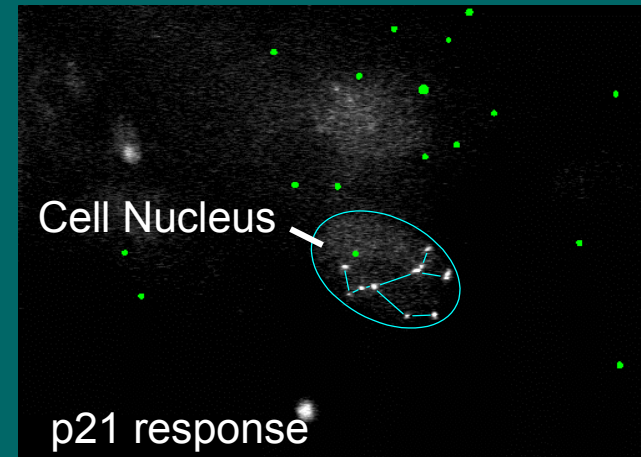


CDKN1A/p21: green

DNA: red

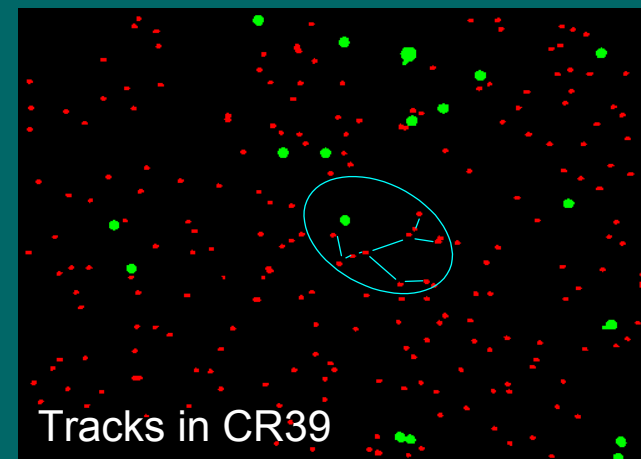
Pb-ions, 3.1 MeV/u,  $3 \times 10^6/\text{cm}^2$

B. Jakob et al.



Cell Nucleus

p21 response



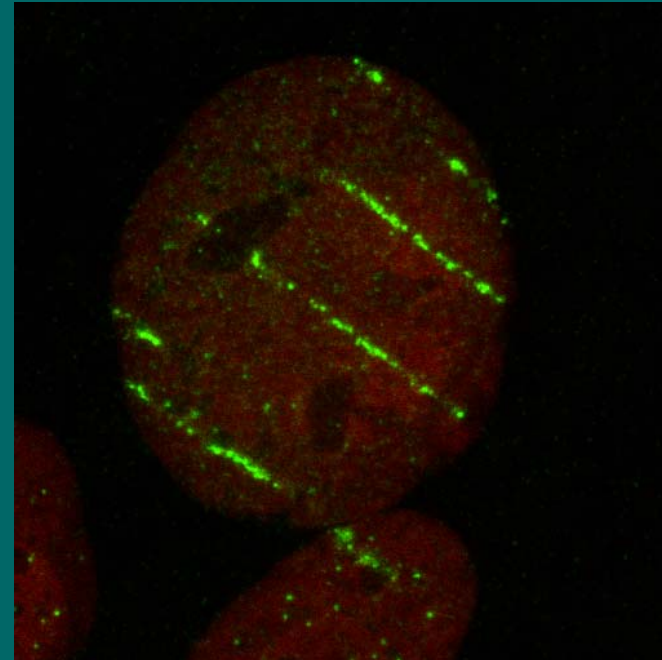
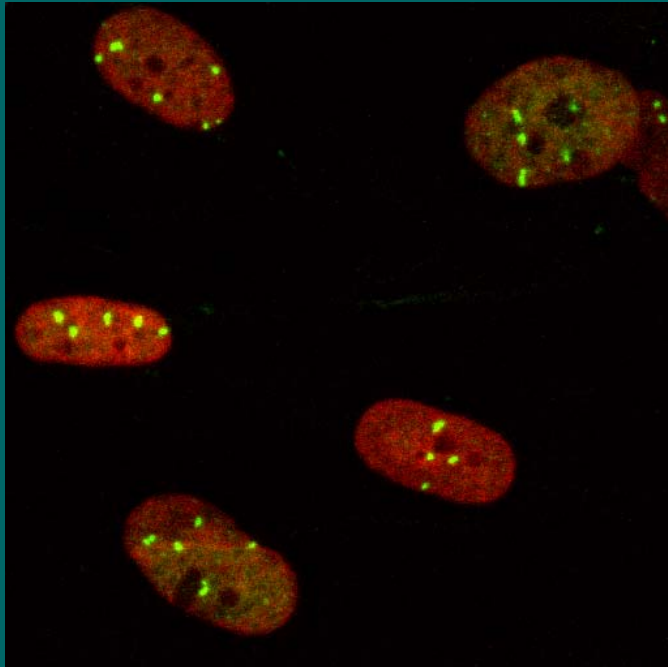
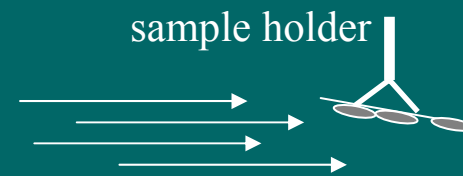
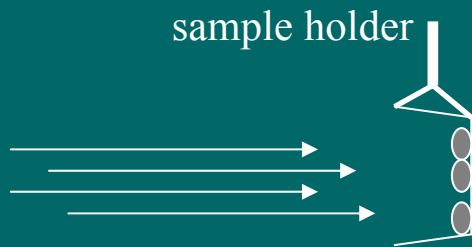
Tracks in CR39

Ca-ions, 10.1 MeV/u,  $2 \times 10^6/\text{cm}^2$

M. Scholz et al.



# Biological Visualization of Particle Tracks

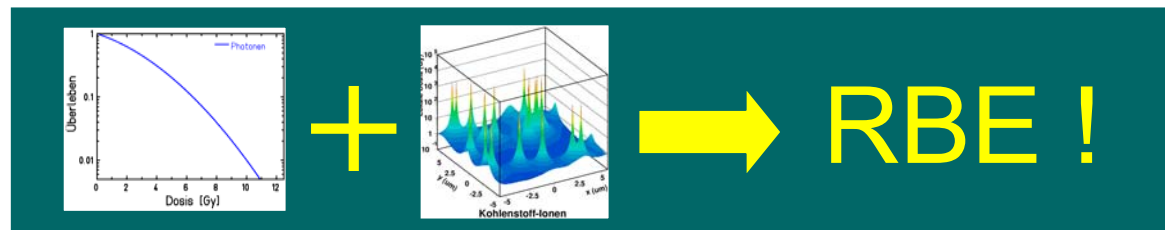


B. Jakob et al.

# Amorphous Track Structure Models

## Basic Assumption:

Increased effectiveness of particle radiation  
can be described by a combination of the  
photon dose response and microscopic dose distribution





# Principle of Local Effect Model

Local biological effect:

$$S = e^{-\bar{N}_{lethal}}$$

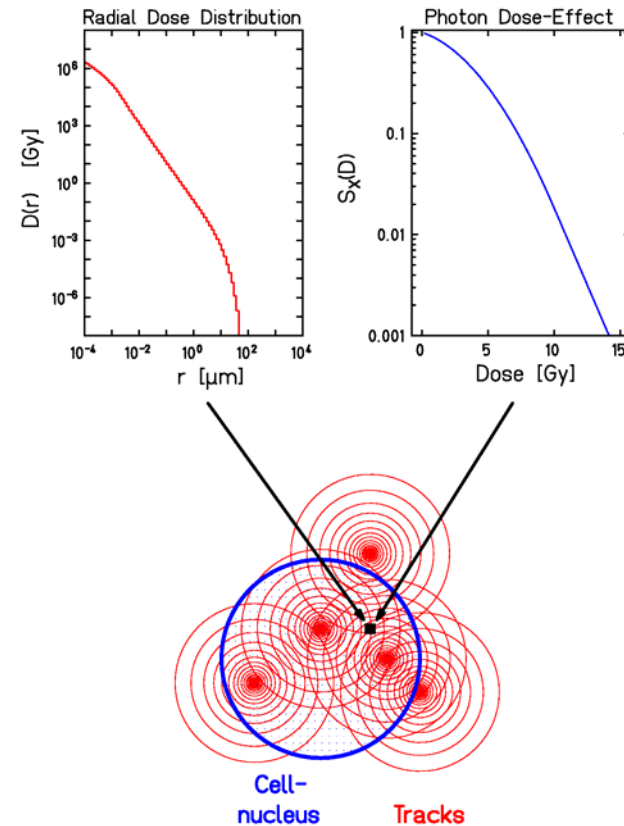
Low-LET dose response:

$$\bar{N}_{lethal}(D) = -\ln S_X(D) = \alpha D + \beta D^2$$

Event density:

$$v(D) = \bar{N}_{lethal}(D) / V_{Nucleus}$$

M. Scholz et al.



$$\bar{N}_{lethal} = \int \frac{-\ln S_X(d(x, y, z))}{V_{Nucleus}} dV_{Nucleus}$$

# Input Parameters

- Radial Dose Distribution:  
Monte-Carlo (M. Krämer), Analytical Models (Katz, Kiefer),  
Experimental Data

$$D(r) \propto \frac{1}{r^2} \quad R_{Track} \propto E^{1.7}$$

- X-ray Survival Curves:  
Experimental data according to LQ; additional assumption:  
Transition from shoulder to exponential shape at high doses

$$S = e^{-(\alpha D + \beta D^2)}, \quad D < D_t$$

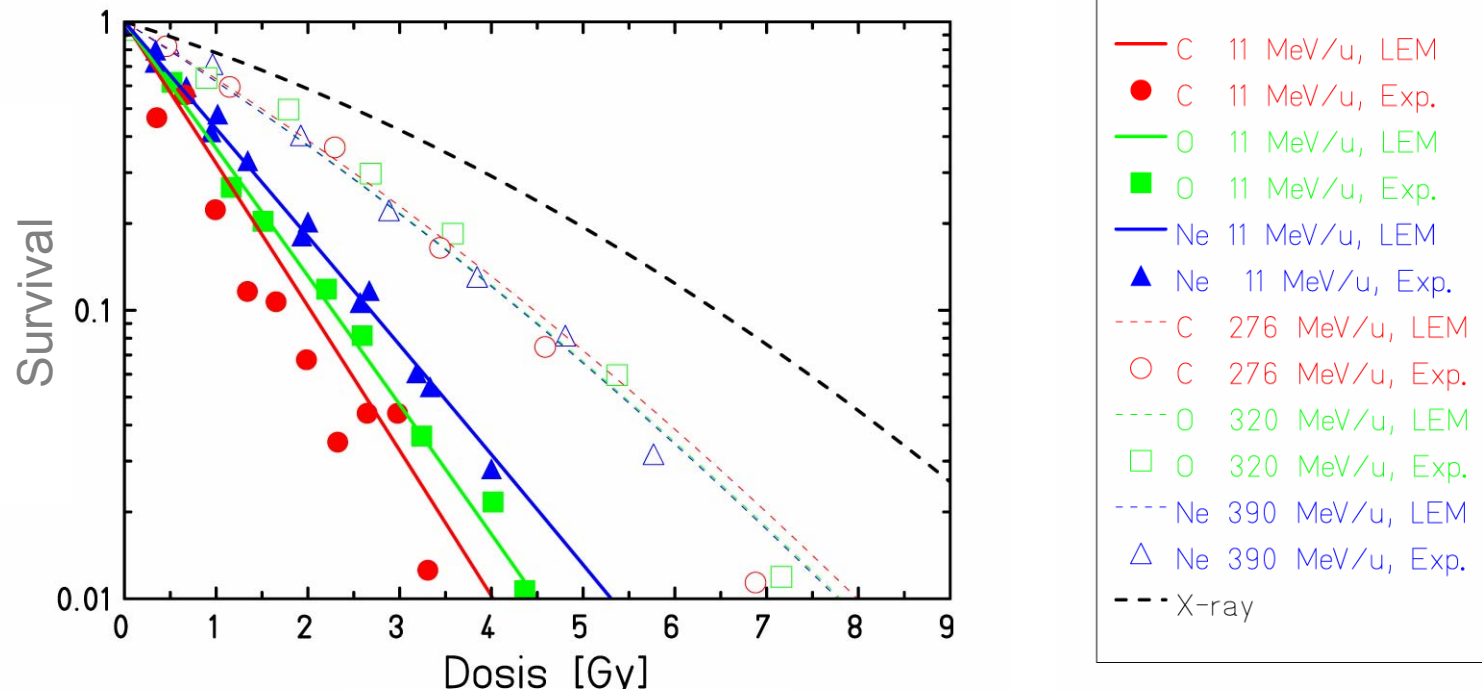
$$S = e^{-s_{\max}(D - D_t)}, \quad D \geq D_t$$

- Target Size (Nuclear Size):  
Experimental Data

# Algorithms

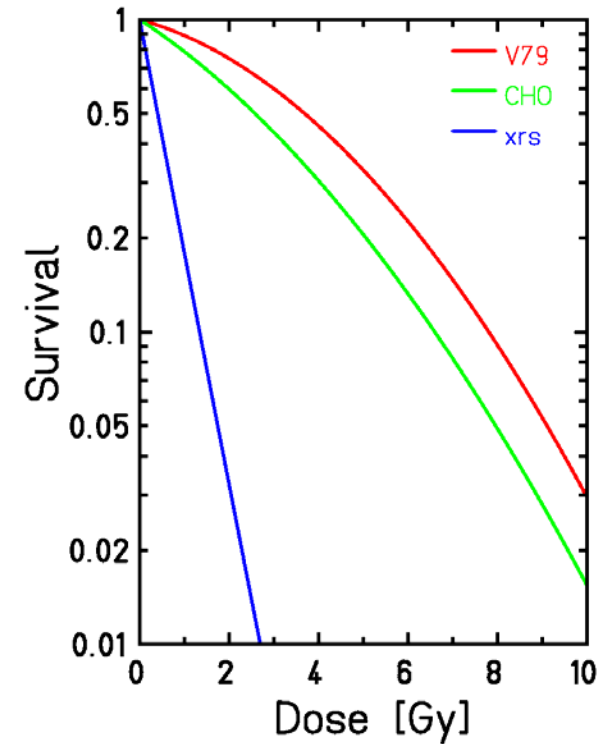
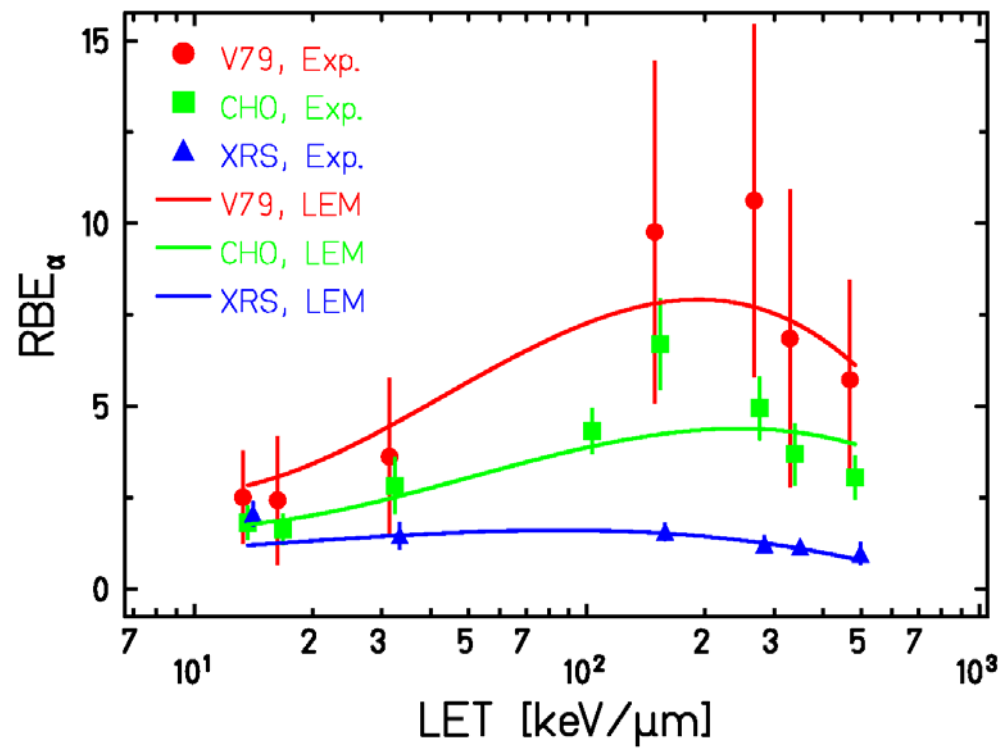
- Exact calculation:
  - Monte-Carlo method for determination of ion impact parameters
  - Numerical integration (taking into account overlapping tracks in detail)
- Approximation:
  - Exact calculation of single particle effects (corresponding to initial slope of survival curve)
  - Estimation of  $\beta$ -term from boundary condition:  
Max. slope of HI curve = max. slope of photon dose response curve

# Comparison with experimental data



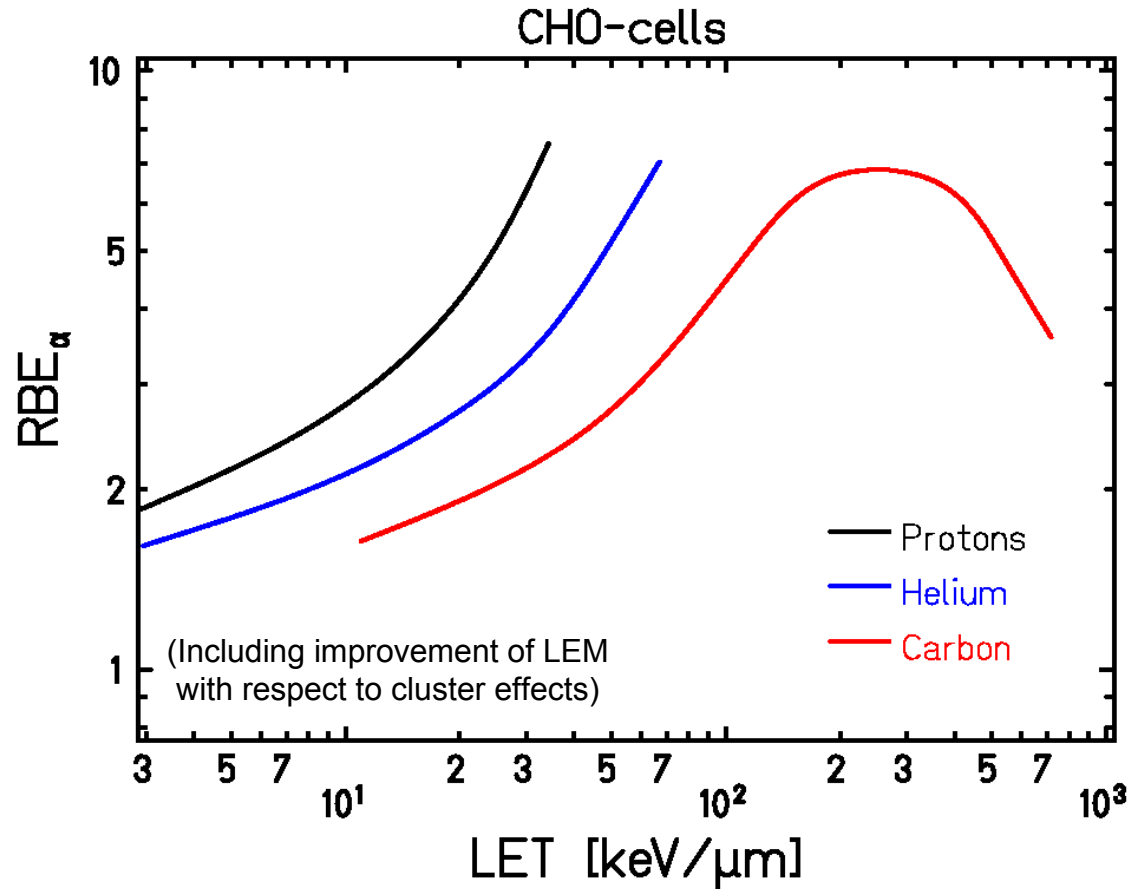
Data: Kraft-Weyrather et al.

# Comparison with experimental data



Data: Weyrather et al., IJRB 1999

# Dependence on Particle Species



Influence of track structure; for given LET:

$$E(C) > E(He) > E(p) \quad \rightarrow \quad R_{\text{track}}(C) > R_{\text{track}}(He) > R_{\text{track}}(p)$$

# Application to Tissue Effects

Tissues show complex response to radiation



Correlation with cell survival?

Nerve tissue: non proliferating cells

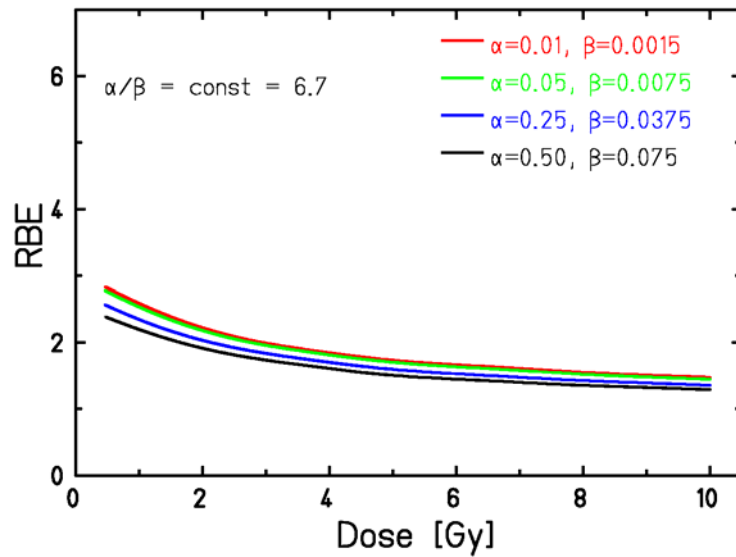


Clonogenic survival not defined

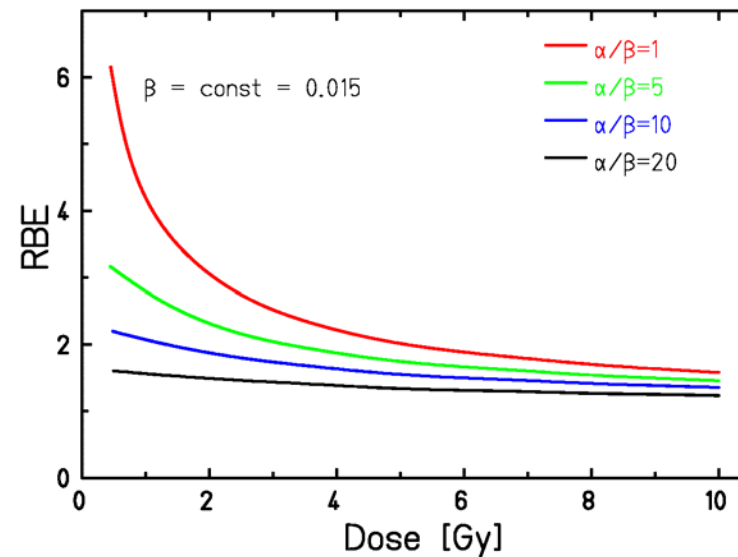
Which parameters of photon dose response  
define RBE?

# Correlation Shoulder – RBE: Theory

## Calculation of mid peak RBE Carbon 6-10cm SOBP



Constant  $\alpha_X/\beta_X$ -ratio  
Varying absolut  $\alpha_X, \beta_X$  values



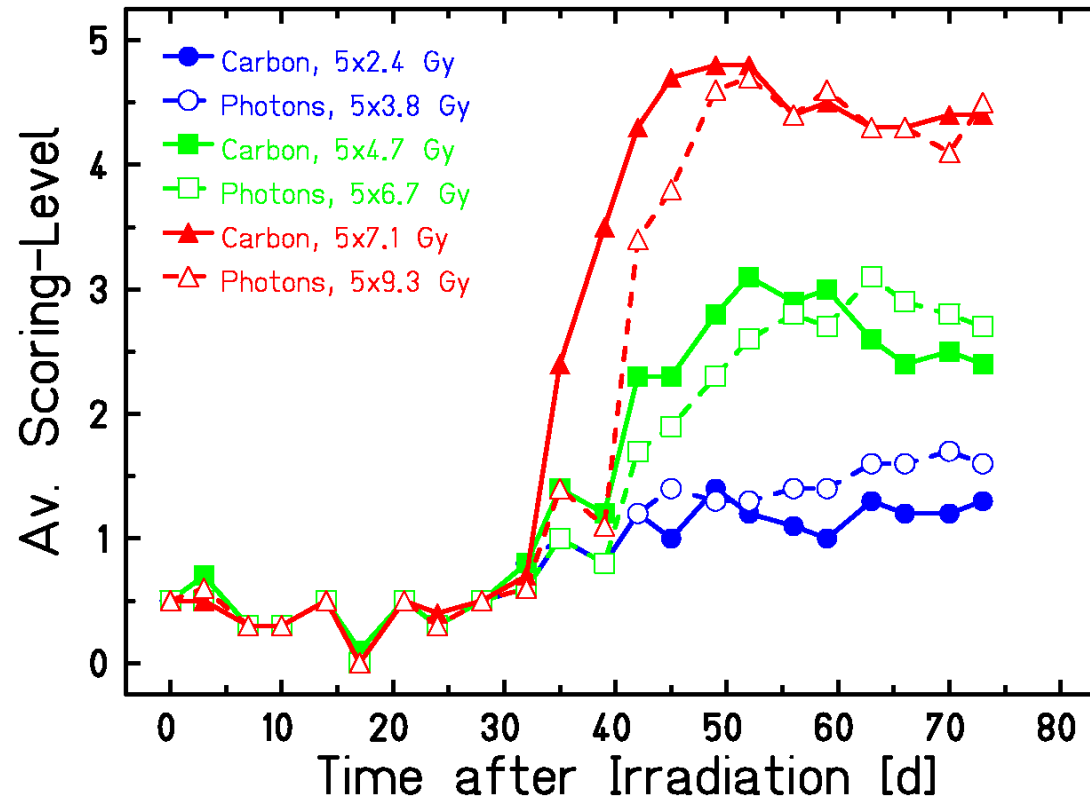
Constant  $\beta_X$ -value  
Varying  $\alpha_X/\beta_X$ -ratios

➔  $\alpha_X/\beta_X$ -ratio determines RBE



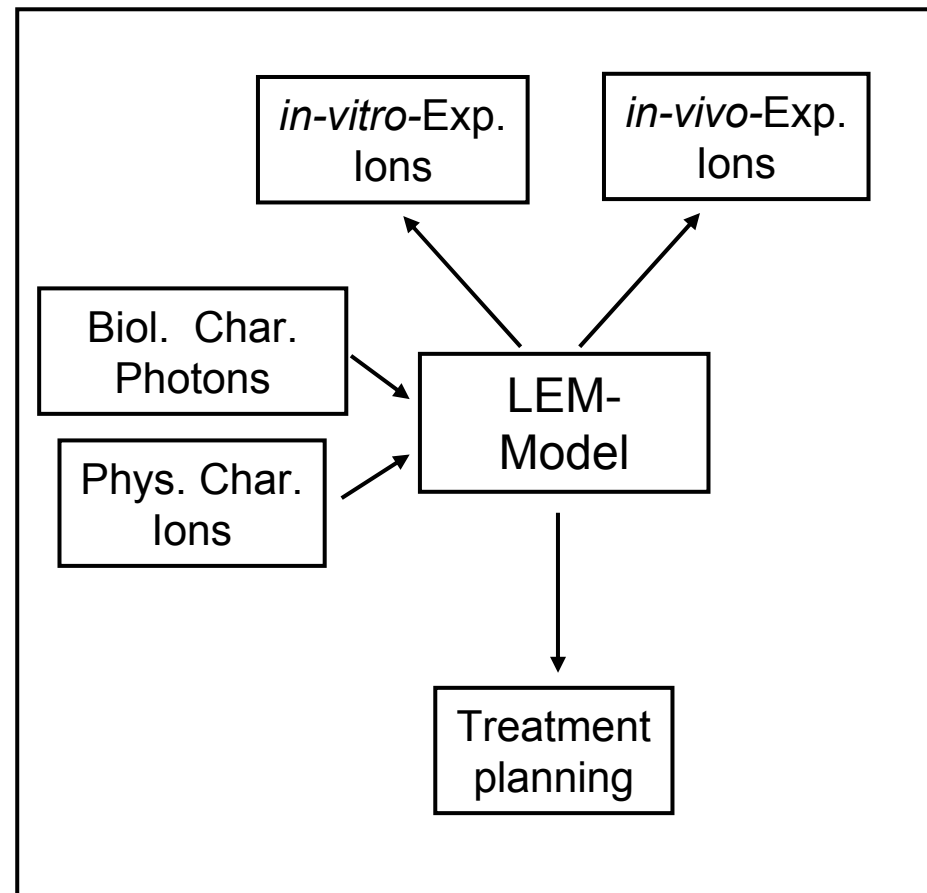
# Application to Normal Tissue Effects

## Skin reaction in minipigs



Zacharias et al., *Acta Oncol.* 1997

# Role of Modeling for Treatment Planning in Heavy Ion Tumor Therapy





## Summary

- Biological advantage of ion beams in tumor therapy: increased effectiveness in Bragg peak region
- Increased effectiveness depends on factors like dose, ion species & energy, cell type, ...
- Complex dependencies require modeling for treatment planning in ion tumor therapy
- Modeling cannot be based on first principles
- Empirical approaches based on a link to the photon dose response curves allow high quantitative precision