

Ultrahigh Energy Neutrino Nucleon Cross Sections

Jamal Jalilian-Marian
Institute for Nuclear Theory
University of Washington

Neutrino Nucleon Cross Sections

$$\sigma_{total}^{\nu N \rightarrow X}(s) = \int_0^1 dx \int_0^{xs} dQ^2 \frac{d\sigma^{\nu N \rightarrow X}}{dx dQ^2}$$

$$\frac{d\sigma^{\nu N \rightarrow X}}{dx dQ^2} = \frac{G_F^2}{\pi} \left(\frac{M_W^2}{Q^2 + M_W^2} \right)^2 [q(x, Q^2) + (1-y)^2 \bar{q}(x, Q^2)]$$

$q(x, Q^2), \bar{q}(x, Q^2)$ from DGLAP

$Q \sim M_W$ dominates the cross section

$$\sigma_{total}^{\nu N \rightarrow X}(s) \simeq \int_0^1 dx \left[\left(\frac{\hat{s}}{1 + \hat{s}} \right) q(x) + \left(1 + \frac{2}{\hat{s}} - 2 \left(\frac{1 + \hat{s}}{\hat{s}^2} \right) \ln(1 + \hat{s}) \right) \bar{q}(x) \right]$$

with $\hat{s} \equiv \frac{xs}{M_W^2}$

x dependence of PDF's determines the cross section

Neutrino Nucleon Cross Sections

- Contribution of small x partons

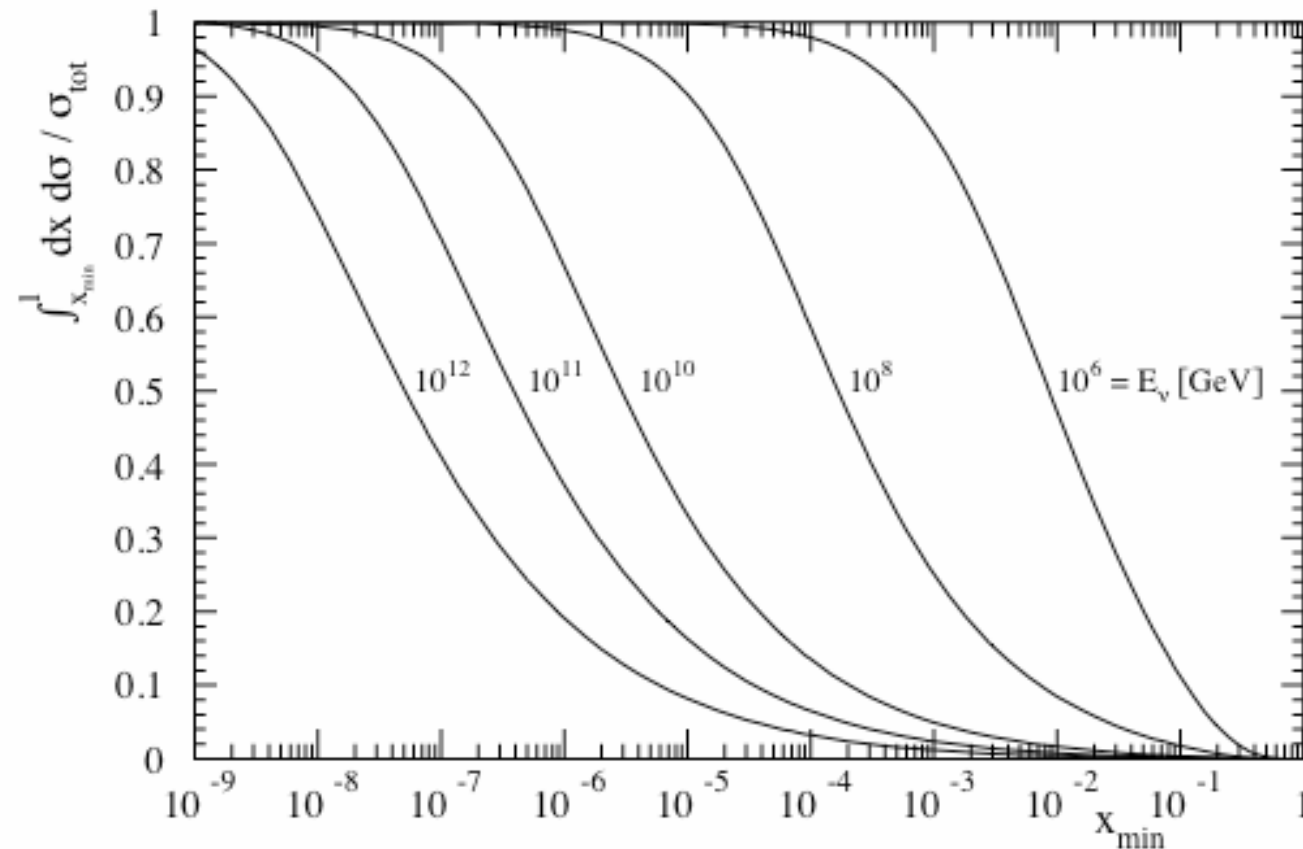
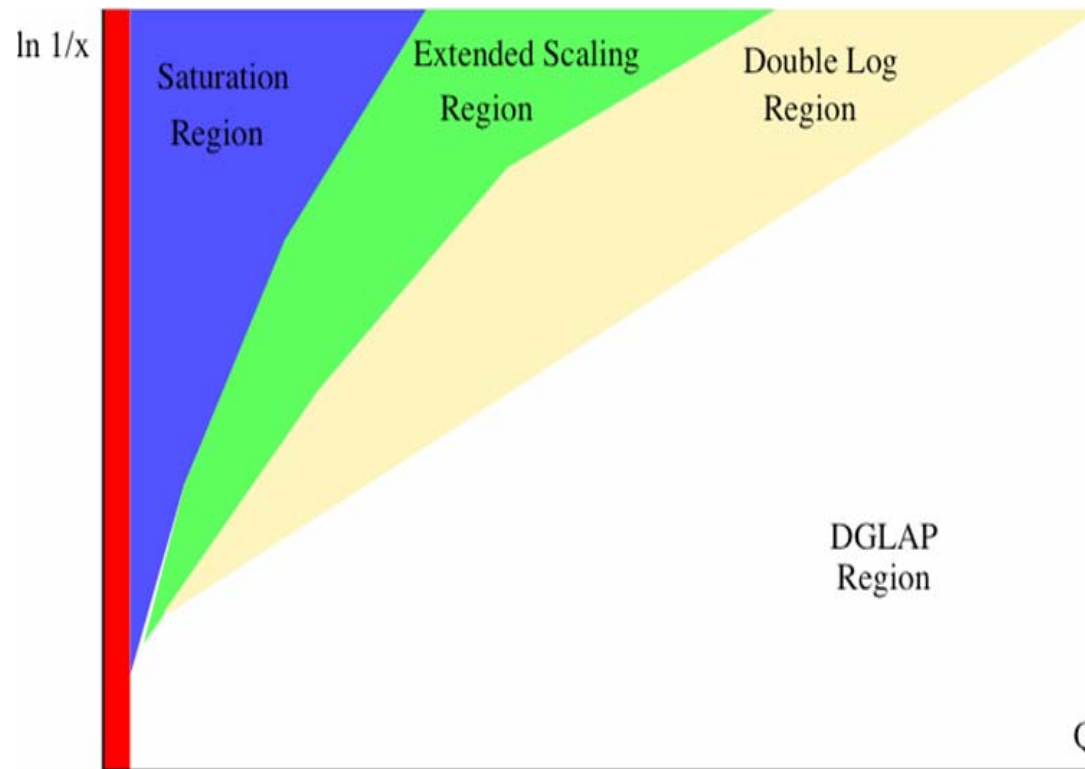
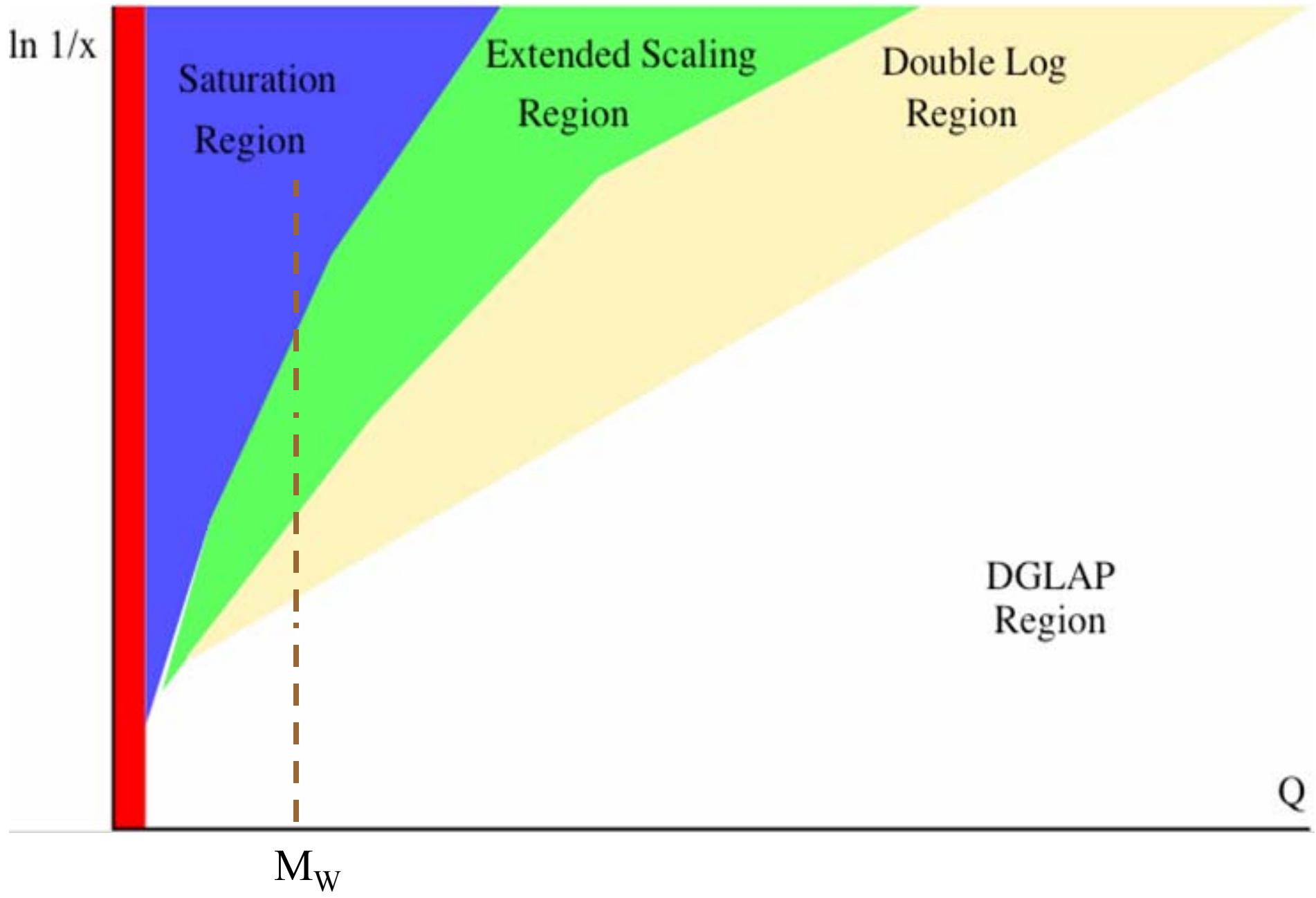


Fig. from Gluck, Kretzer and Reya, Astropart. Phys.11 (1999) 327

QCD Kinematic Regions



- DGLAP ($\alpha_s \ln Q^2$) [leading twist, no Anomalous Dimension]
 - Double Log ($\alpha_s \ln Q^2 \ln 1/x$)
- Extended scaling ($\alpha_s \ln 1/x$) [leading twist, BFKL, Ano. Dim.]
- Saturation region ($\alpha_s \rho \ln 1/x$) [all twist, JIMWLK (BK)]



QCD Effective Action at Small x

McLerran & Venugopalan 93
JJM et al. 96

$$\begin{aligned} S = & -\frac{1}{4} \int d^4x G_a^{\mu\nu} G_{\mu\nu}^a \\ & + \frac{i}{N_c} \int d^2x_t dx^- \delta(x^-) \text{Tr} \rho(x_t) W_{-\infty, \infty} [A^-](x^-, x_t) \\ & + i \int d^2x_t F[\rho^a(x_t)] \end{aligned}$$

with

$$W_{-\infty, \infty} [A^-](x^-, x_t) = \hat{P} \exp \left[-ig \int_{-\infty}^{\infty} dx^+ A_a^-(x) T_a \right]$$

and

$$\langle O(A) \rangle \equiv \frac{\int [D\rho^a] [DA_a^\mu] O(A) \exp\{iS[\rho, A]\}}{\int [D\rho^a] [DA_a^\mu] \exp\{iS[\rho, A]\}}$$

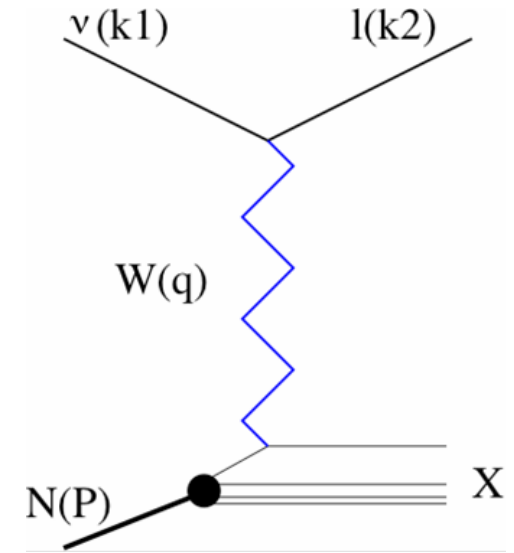
Neutrino-Nucleon DIS: Charged Current

$$\nu_l(k_1) N(P) \rightarrow l(k_2) X$$

$$s \equiv (k_1 + P)^2 \quad q \equiv k_1 - k_2$$

$$x \equiv -\frac{q^2}{2P \cdot q} \quad Q^2 \equiv -q^2$$

$$y \equiv \frac{P \cdot q}{P \cdot k_1} = \frac{Q^2}{xs}$$



McLerran & Venugopalan PRD99
JJM PRD03

$$\frac{d\sigma}{dx dQ^2} = \frac{1}{4\pi} \frac{y}{xs} \frac{G_F^2 M_W^4}{[Q^2 + M_W^2]^2}$$

$$L^{\mu\nu}(k_1, k_2) W_{\mu\nu}(q^2, P \cdot q)$$

Neutrino-Nucleon DIS: Charged Current

Leptonic part

$$L^{\mu\nu}(k_1, k_2) = 2[k_1^\mu k_2^\nu + k_1^\nu k_2^\mu - g^{\mu\nu} k_1 \cdot k_2 + i\epsilon^{\mu\nu\rho\sigma} k_{1\rho} k_{2\sigma}]$$

Hadronic part

$$W_{\mu\nu}(q^2, 2P \cdot q) = \frac{\sigma_h}{2\pi} \frac{P^+}{M_h} \text{Im} \int dx^- \int d^4z e^{iq \cdot z} \langle T J_\mu^\dagger(x^- + z/2) J_\nu(x^- - z/2) \rangle_\rho$$

with

$$J_\mu(x) = \bar{u}(x) \gamma_\mu (1 + \gamma_5) d(x)$$

σ_h, M_h are the nucleon size and mass

Neutrino-Nucleon DIS: Charged Current

$$\begin{aligned} \langle T J_\mu^\dagger(x) J_\nu(y) \rangle_\rho &= \text{Tr} \gamma_\mu (1 + \gamma_5) S_A(x, y) \gamma_\nu (1 + \gamma_5) S_A(y, x) \\ &\quad + \text{Tr} \gamma_\mu (1 + \gamma_5) S_A(x) \text{Tr} \gamma_\nu (1 + \gamma_5) S_A(y) \end{aligned}$$

where S_A is the quark propagator in the classical gluon field background

$$\begin{aligned} S_A(x, y) &= S_0(x, y) - i \int d^4r \delta(r^-) \\ &\quad \left[\theta(x^-) \theta(-y^-) [V^\dagger(r_t) - 1] - \theta(-x^-) \theta(y^-) [V(r_t) - 1] \right] \\ &\quad S_0(x - r) \gamma^- S_0(r - y) \end{aligned}$$

S_0 is the free quark propagator and

$$V(r_t) \equiv \hat{P} e^{-ig \int dz^- A^+(z^-, r_t)}$$

Neutrino-Nucleon DIS: Charged Current

$$2xF_1 = \frac{N_c Q^2}{4\pi^4} \int_0^1 dz \int d^2b_t d^2r_t \gamma(x, b_t, r_t) a^2 [z^2 + (1-z)^2] K_1^2(ar_t)$$

with $a^2 \equiv z(1-z)Q^2$

$$F_2 = \frac{N_c Q^2}{4\pi^4} \int_0^1 dz \int d^2b_t d^2r_t \gamma(x, b_t, r_t) \{4z(1-z)a^2 K_0^2(ar_t) + a^2 [z^2 + (1-z)^2] K_1^2(ar_t)\}$$

$$xF_3 = \frac{N_c Q^2}{4\pi^4} \int_0^1 dz \int d^2b_t d^2r_t \gamma(x, b_t, r_t) (1-2z)a^2 K_1^2(ar_t)$$

$$\frac{d\sigma}{dx dQ^2} = \frac{1}{2\pi} \frac{G_F^2}{x[1 + Q^2/M_W^2]^2} \left\{ y^2 xF_1 + (1-y)F_2 + y\left(1 - \frac{y}{2}\right)xF_3 \right\}$$

Dipole Cross Section

$$\gamma(x, r_t, b_t) \equiv \frac{1}{N_c} \text{Tr} \langle V(b_t + r_t/2) V^\dagger(b_t - r_t/2) - 1 \rangle$$

Solution of JIMWLK (BK) non-linear evolution equation:

Rumakainen & Weigert, NPA739 (2004)183

Golec-Biernat & Stasto, NPB668 (2003) 345

Mueller & Triantafyllopoulos NPB640 (2002) 331

Triantafyllopoulos NPB648 (2003) 293

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Phenomenological parameterizations:

Golec-Biernat and Wusthoff, PRD59 (1999) 014017

Iancu, Itakura and Munier, PLB590 (2004)199

Kharzeev, Kovchegov and Tuchin, hep-ph/0405045

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Probing the Dipole Cross Section

- Inclusive observables
 - Structure functions F_2, F_L
- Single inclusive observables
 - Hadron production in $p(d)A$
 - Photon, dilepton production in $p(d)A$
- Double inclusive observables
 - Photon + hadron (jet)
- Correlation studies are excellent probes of CGC but involve higher point functions (quark+gluon, two gluon, quark anti-quark production, ...)

Models of the dipole cross section:

Iancu, Itakura and Munier PLB590 (2004) 199

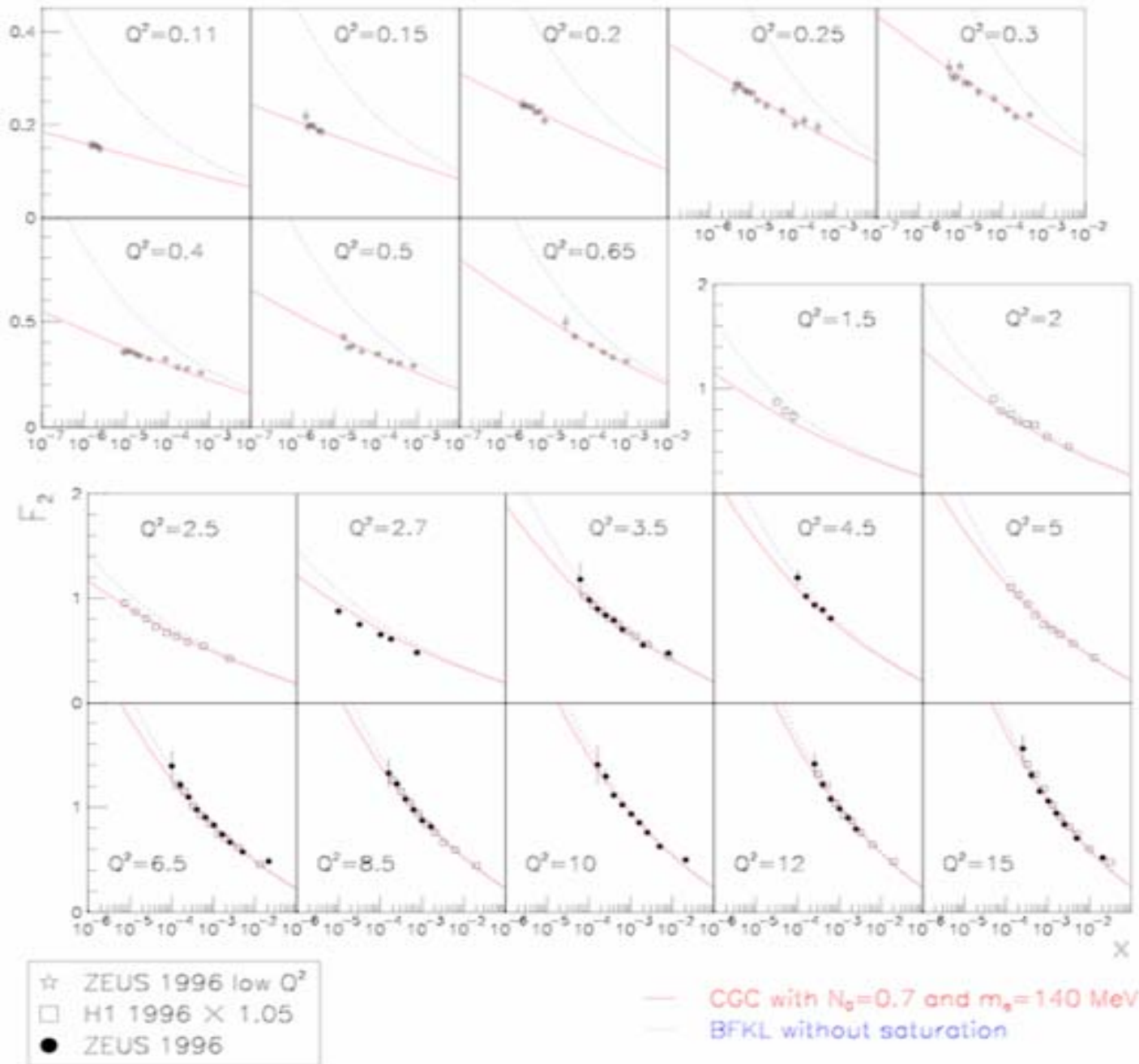
$$\gamma(x, r_t, b_t) \equiv \sigma_0 \mathcal{N}(r_t Q_s, x)$$

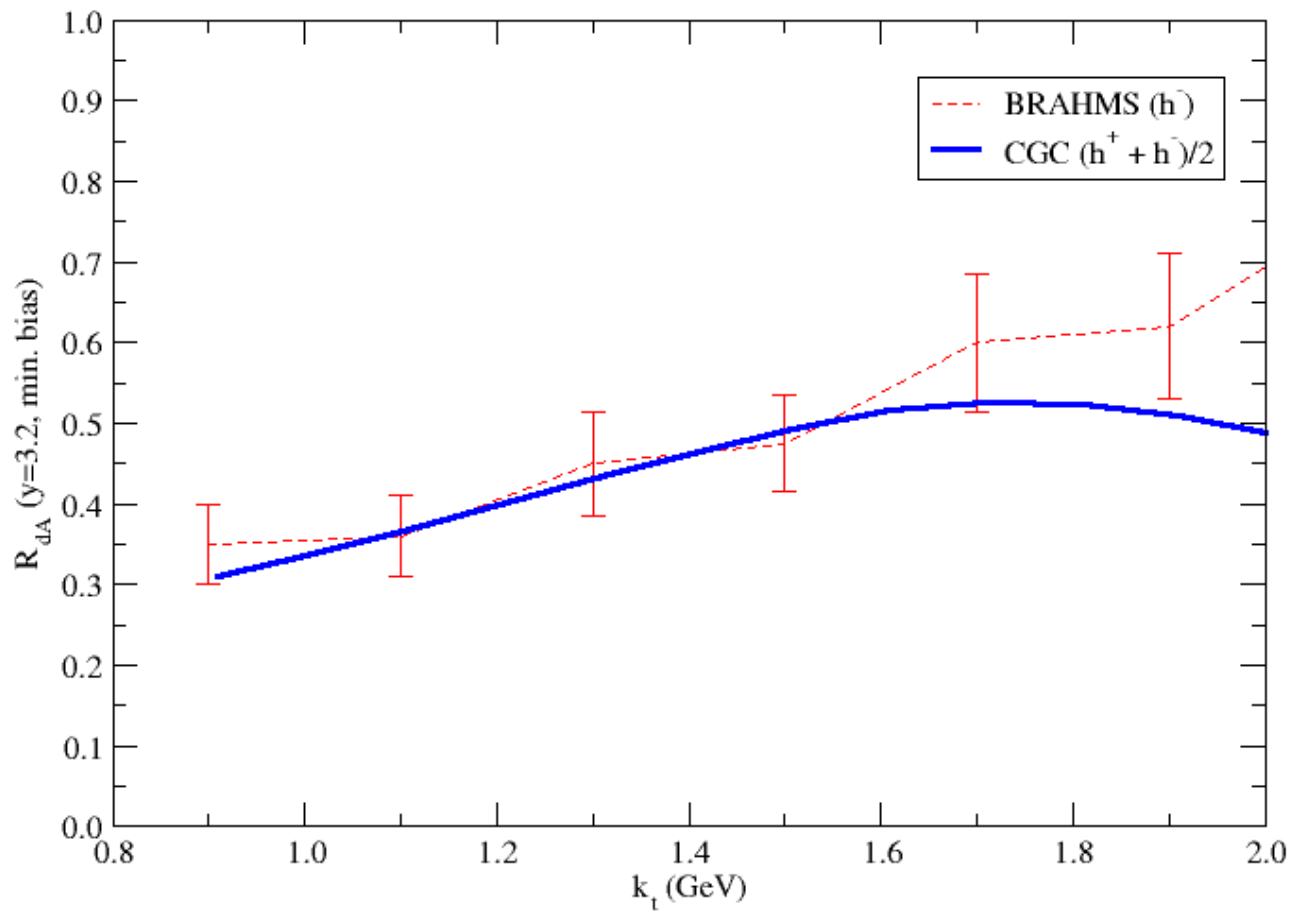
$$\mathcal{N}(r_t Q_s, x) = \mathcal{N}_0 \left[\frac{r_t Q_s}{2} \right]^{2\left(\gamma_s + \frac{\ln(2/R_t Q_s)}{\kappa \lambda y}\right)} \quad r_t Q_s \leq 2$$

$$\mathcal{N}(r_t Q_s, x) = 1 - e^{-a \ln^2(br_t Q_s)} \quad r_t Q_s \geq 2$$

$$Q_s^2(x) = (x_0/x)^\lambda \text{ GeV}^2$$

$$\lambda = 0.25 - 0.3$$





A. Dumitru & JJM 02
JJM 04

Models of the dipole cross section:

Kharzeev, Kovchegov and Tuchin hep-ph/0405045

$$\mathcal{N}(r_t, x) = 1 - e^{-\frac{1}{4} \left[\frac{C_F}{N_c} r_t^2 Q_s^2 \right] \gamma_s(x, r_t^2)}$$

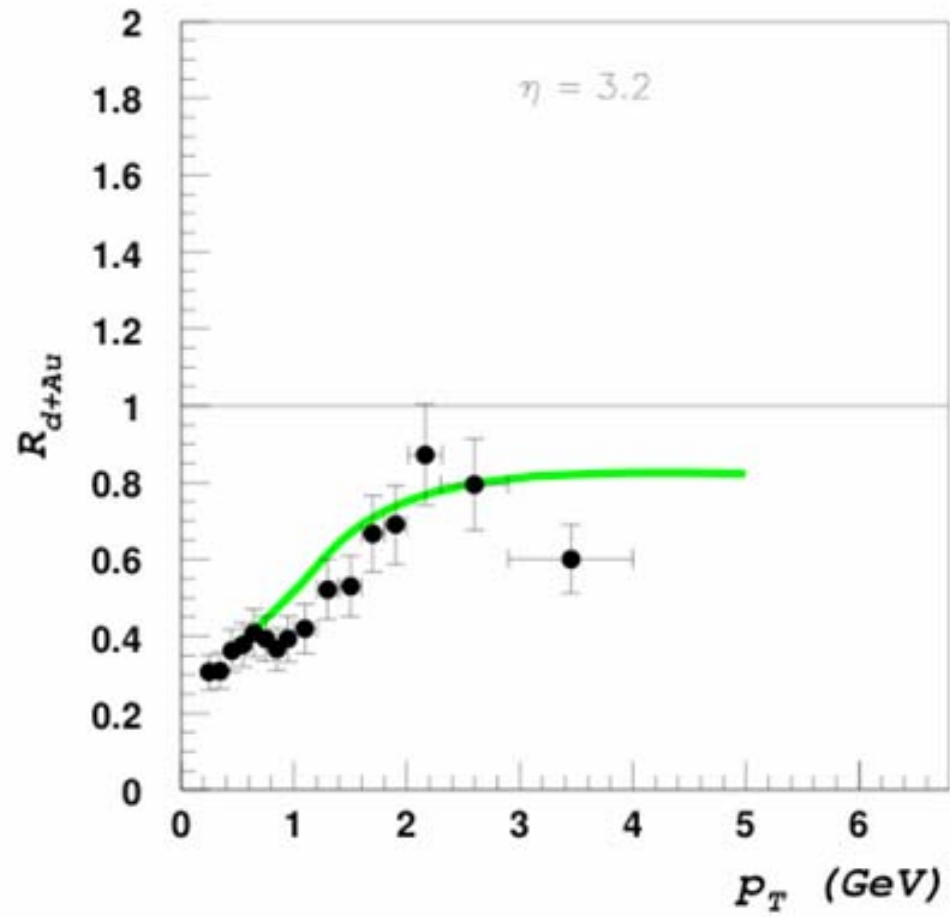
$$\gamma_s(x, r_t) = \frac{1}{2} \left[1 + \frac{\xi(x, r_t)}{\xi(x, r_t) + \sqrt{2\xi(x, r_t)} + 7c\zeta(3)} \right]$$

$$\xi(x, r_t) = \frac{2 \ln[1/(r_t^2 Q_{s0}^2)]}{\lambda(y - y_0)}$$

$$Q_s^2 \sim (x_0/x)^\lambda \text{GeV}^2$$

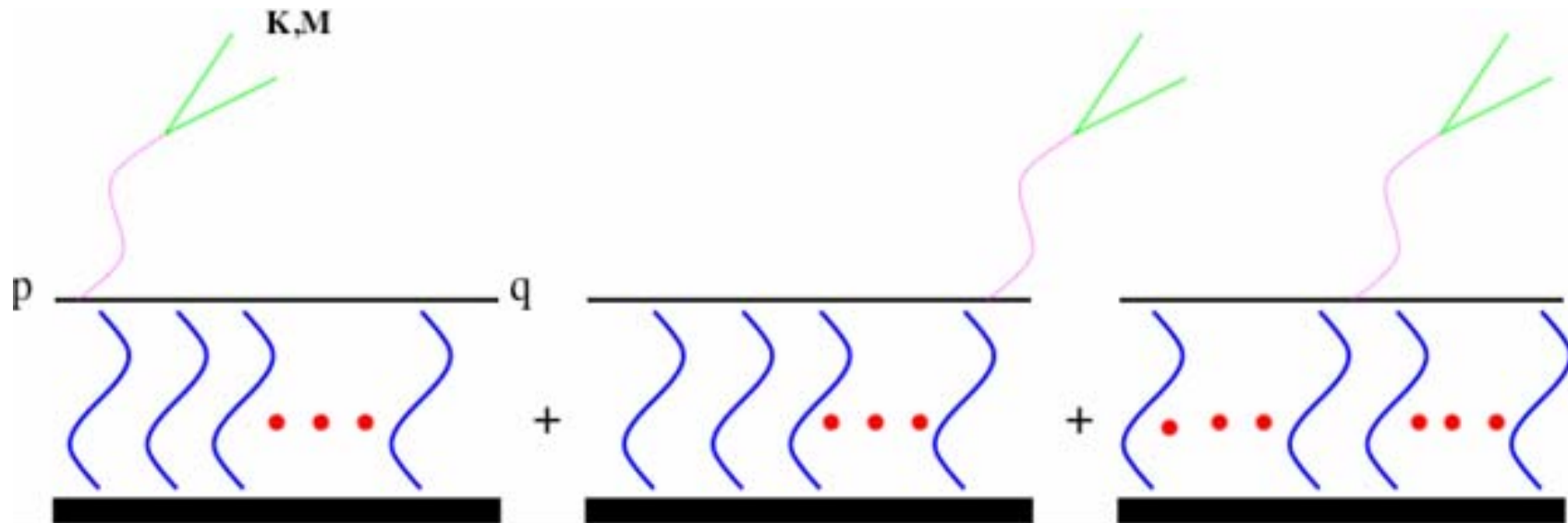
$$\lambda = 0.3$$

KKT04



Probing the Dipole Cross Section

- Electromagnetic signatures: **photons and dileptons**
 - Cleaner than hadrons but lower rates
- Photon and dilepton production in p(d)A



Probing the Dipole Cross Section: Dileptons

F. Gelis & JJM 02

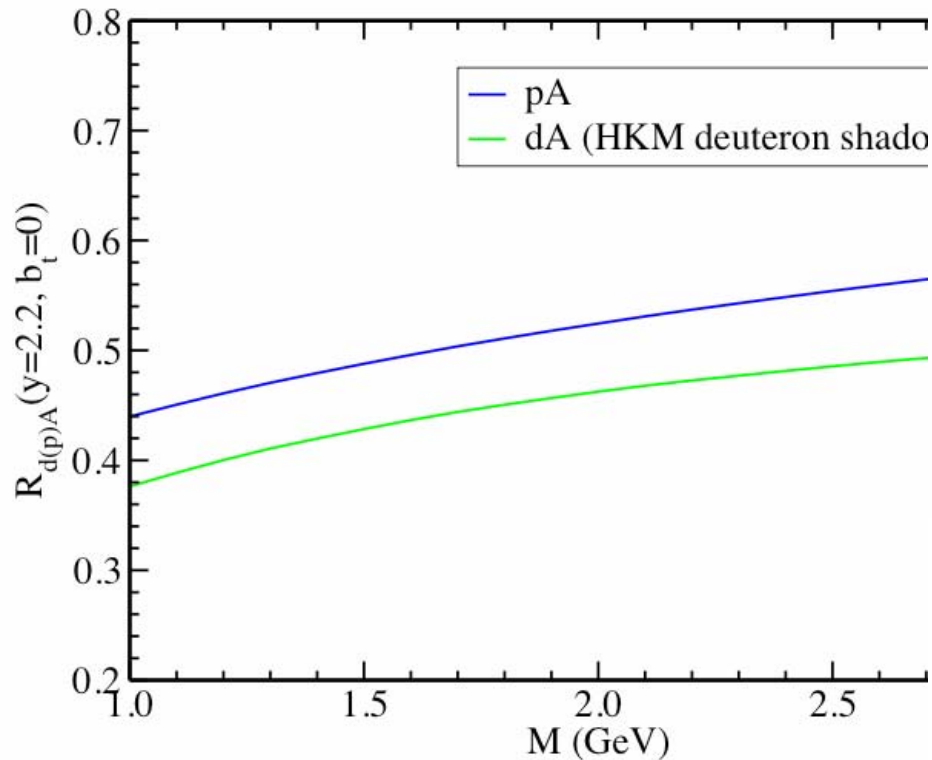
JJM 04

Baier & Mueller & Schiff 04

Kopeliovich et al

$$\frac{d\sigma^{d(p) A \rightarrow l^+ l^- X}}{d^2 b_t dM^2 dx_F} = \frac{\alpha_{em}^2}{6\pi^2} \frac{1}{x_q + x_g} \int_{x_q}^1 dz \int dr_t^2 \frac{1-z}{z^2}$$

$$F_2^{d(p)}(x_q/z) \gamma(x_g, b_t, r_t)$$



$$\left[[1 + (1-z)^2] K_1^2 \left[\frac{\sqrt{1-z}}{z} M r_t \right] + 2(1-z) K_0^2 \left[\frac{\sqrt{1-z}}{z} M r_t \right] \right]$$

$$x_F \equiv \frac{M}{\sqrt{s}} [e^y - e^{-y}]$$

Summary

- QCD at high energy ----> CGC
- CGC provides a systematic method to calculate observables at high energies
 - Universal ingredients: Wilson lines
- CGC domain of applicability: need experiments
 - Evidence from forward rapidity region at RHIC?
- CGC wishes/requests for forward rapidity LHC
 - At fixed rapidity: measure p_t spectra of hadrons, photons, dileptons
 - At fixed p_t : measure rapidity spectra
 - Measure correlations: same rapidity, different rapidity
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