

# Herwig++

Stefan Gieseke

*Institut für Theoretische Physik  
Universität Karlsruhe (TH)*

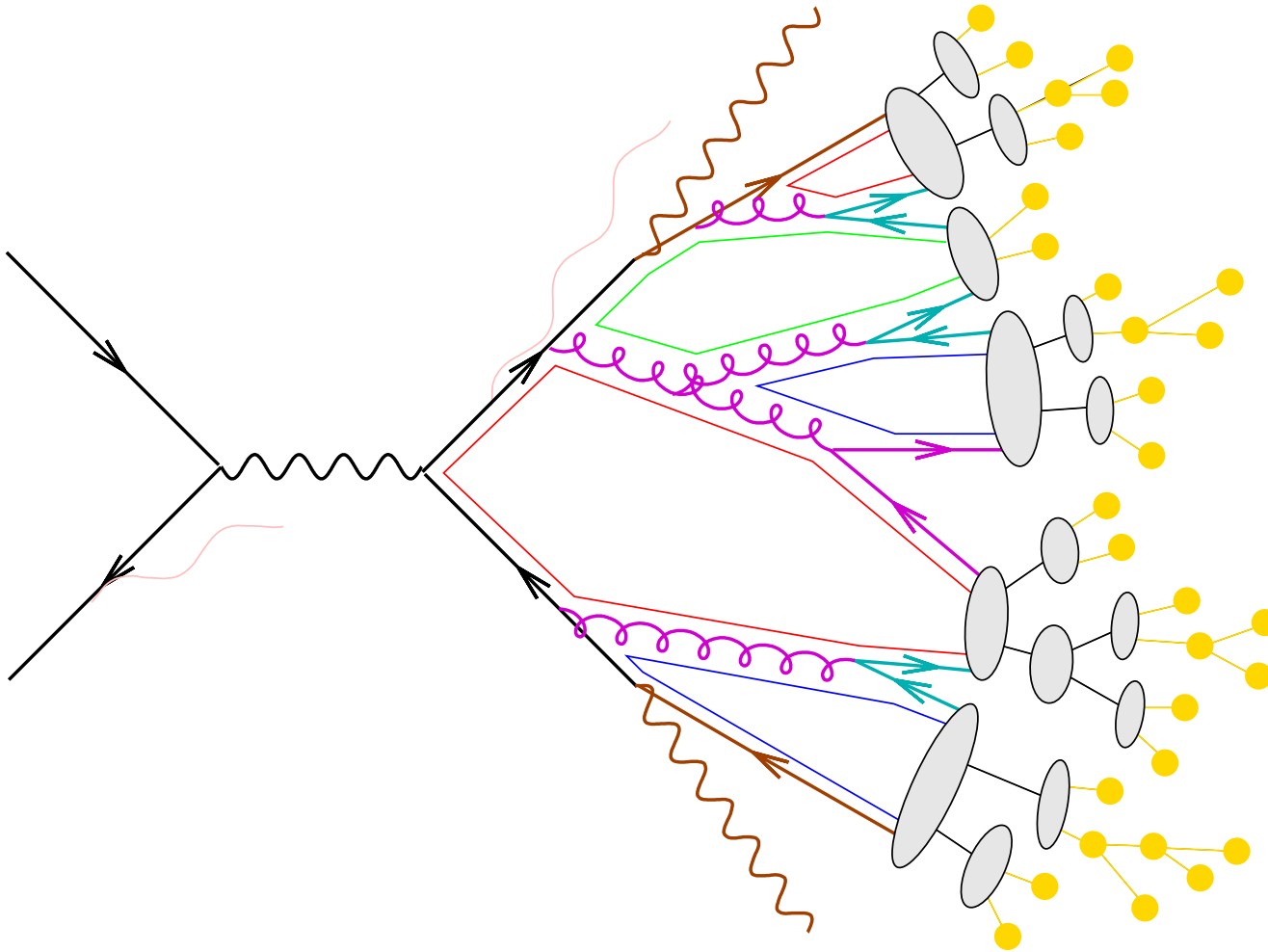
work with A Ribon, P Richardson, MH Seymour, P Stephens, BR Webber (Cambridge, Durham, CERN)

- Some features of Herwig++
- Results for  $e^+e^-$  Annihilation
- Outlook.

SG, P. Stephens and B. Webber, JHEP **0312** (2003) 045 [hep-ph/0310083]

SG, A. Ribon, M. H. Seymour, P. Stephens and B. Webber, JHEP **0402** (2003) 005 [hep-ph/0311208]

# $e^+e^-$ Event Generator

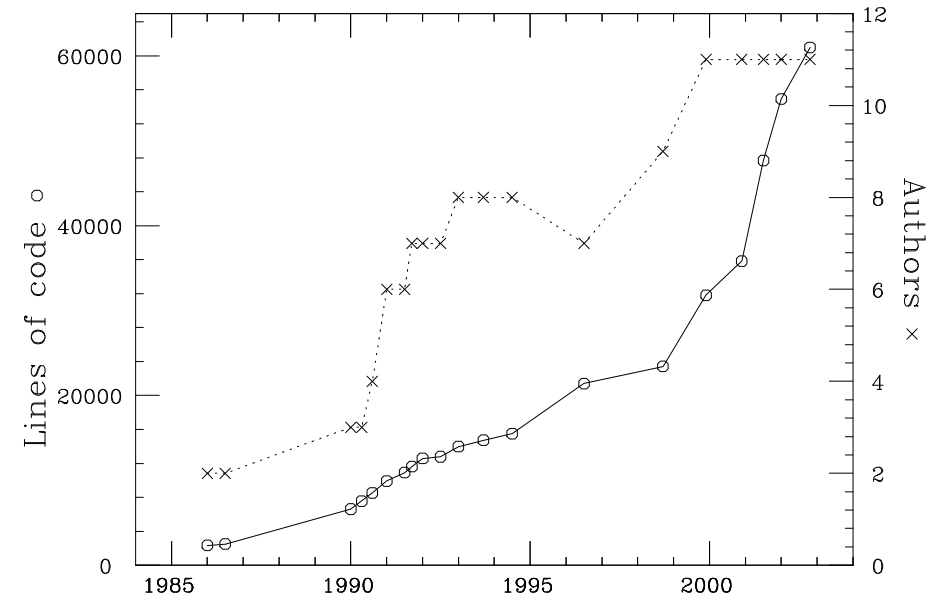


- hard scattering
- (QED) initial/final state radiation
- partonic decays, e.g.  $t \rightarrow bW$
- parton shower evolution
- nonperturbative gluon splitting
- colour singlets
- colourless clusters
- cluster fission
- cluster  $\rightarrow$  hadrons
- hadronic decays

# The new generator Herwig++

*Complete rewrite of HERWIG in C++*

- aiming at full multi-purpose generator for LHC and future colliders.
- Preserve main features of HERWIG such as
  - angular ordered parton shower
  - Cluster Hadronization
- New features and improvements
  - improved parton shower evolution for heavy quarks
  - consistent radiation from unstable particles



HERWIG's growth. . .

# Use of ThePEG in Herwig++

ThePEG = Toolkit for high energy Physics Event Generation



Won't re-invent the wheel

Share administrative overhead, common to event generators with Pythia7

Independent *physics* implementation

Large but very flexible implementation

Common basis for Pythia7/Herwig++:

- ✗ Lack of independence.
- ✗ Miss the possibility to test codes against each other.
- ✓ Physics, however, is still independent.
- ✓ Beneficial for the user to have the same framework.
- ✓ Running Herwig++ with the Lund String Fragmentation from Pythia7 is very simple!

## Hard interactions

- Basic ME's included in **ThePEG**, such as:

$$e^+e^- \rightarrow q\bar{q}, \text{ partonic } 2 \rightarrow 2,$$

we use them.

- Soft and hard **matrix element corrections** implemented for  $e^+e^- \rightarrow q\bar{q}g$ .
- **AMEGIC++** will provide arbitrary ME's for multiparton final states via **AMEGICInterface**.
- CKKW ME+PS foreseen.
- Other authors can easily include their own matrix elements ( $\rightarrow$  *safety* of OO code)

# Quasi-Collinear Limit (Heavy Quarks)

Sudakov-basis  $p, n$  with  $p^2 = M^2$  ('forward'),  $n^2 = 0$  ('backward'),

$$p_q = zp + \beta_q n - q_\perp$$

$$p_g = (1 - z)p + \beta_g n + q_\perp$$

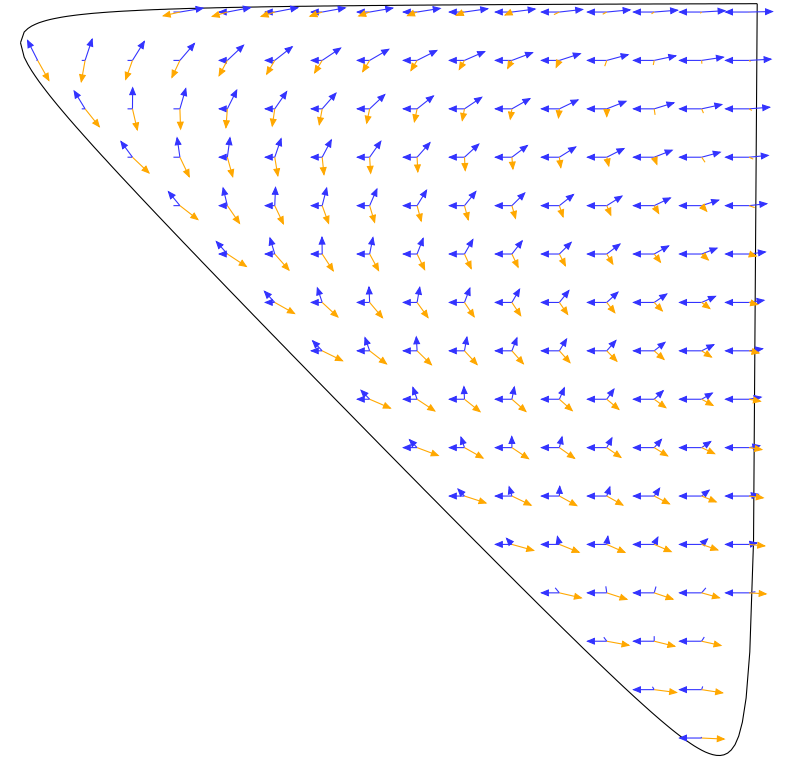
Collinear limit for radiation off heavy quark,

$$P_{gq}(z, \mathbf{q}^2, m^2) = C_F \left[ \frac{1 + z^2}{1 - z} - \frac{2z(1 - z)m^2}{\mathbf{q}^2 + (1 - z)^2 m^2} \right]$$

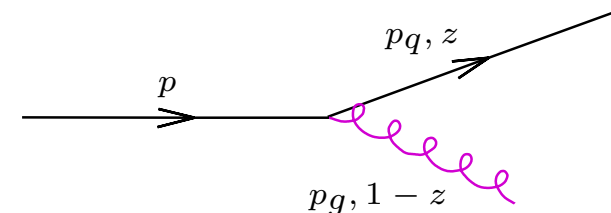
$$= \frac{C_F}{1 - z} \left[ 1 + z^2 - \frac{2m^2}{z\tilde{q}^2} \right]$$

→  $\tilde{q}^2 \sim \mathbf{q}^2$  may be used as evolution variable.

$q\bar{q}g$ -Phase space  $(x, \bar{x})$



Single emission:



## New evolution variables

Kinematics to allow better treatment of heavy particles, avoiding overlapping regions in phase space, in particular for soft emissions

We choose  $\tilde{q}^2$  as new evolution variable,

$$\tilde{q}^2 = \frac{\mathbf{q}^2}{z^2(1-z)^2} + \frac{m^2}{z^2} \quad \text{for } q \rightarrow qg$$

and with the argument of running  $\alpha_S$  chosen according to

$$\alpha_S(z^2(1-z)^2\tilde{q}^2)$$

angular ordering

$$\tilde{q}_{i+1} < z_i \tilde{q}_i \quad \tilde{k}_{i+1} < (1-z_i) \tilde{q}_i$$

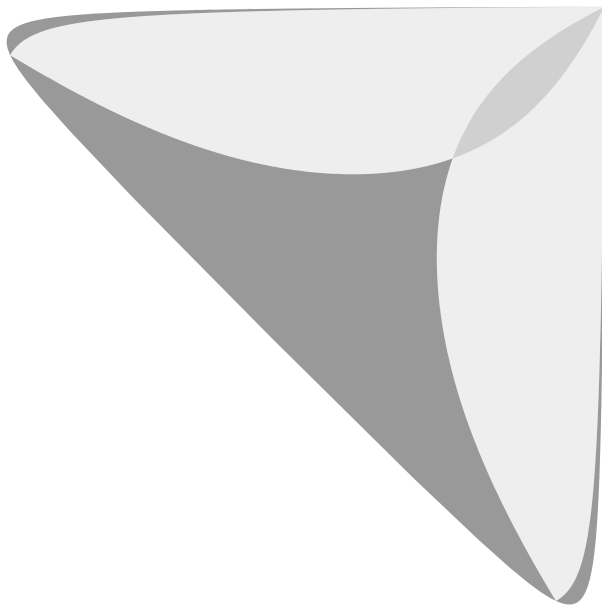
Technically: *reinterpretation* of known evolution variables, i.e. the branching probability for  $a \rightarrow bc$  still is

$$dP(a \rightarrow bc) = \frac{d\tilde{q}^2}{\tilde{q}^2} \frac{C_i \alpha_S}{2\pi} P_{bc}(z, \tilde{q}) dz$$

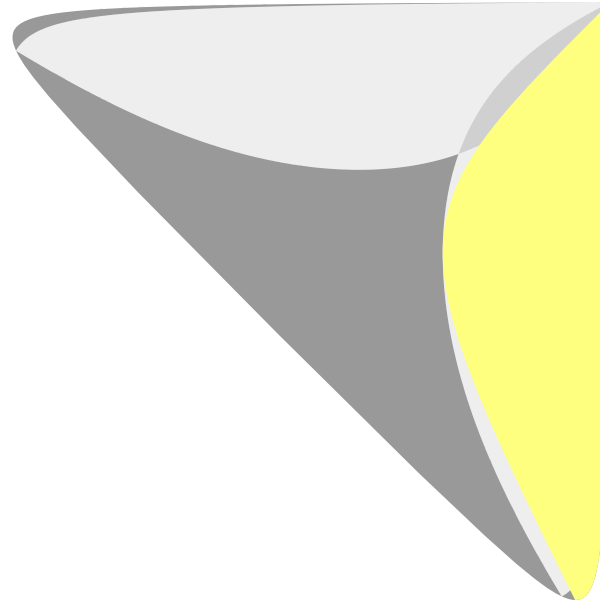
→ Sudakov's etc. technically remain the same!

## $q\bar{q}g$ Phase Space old vs new variables

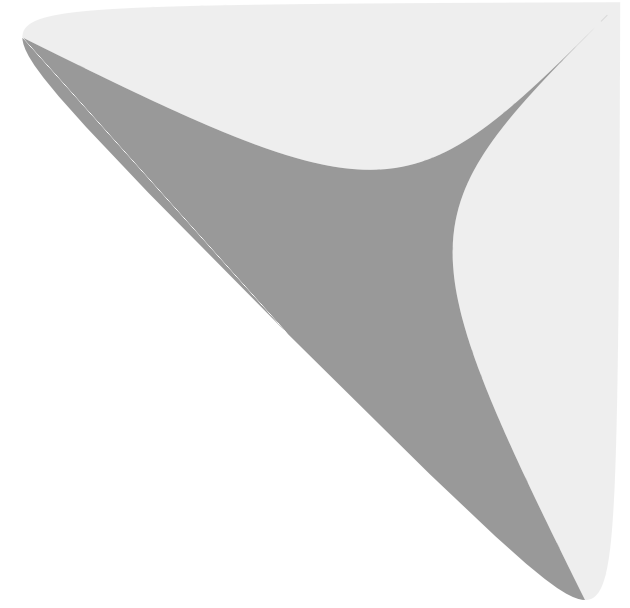
Consider  $(x, \bar{x})$  phase space for  $e^+e^- \rightarrow q\bar{q}g$



HERWIG



Comparison



Herwig++

- ✗ Larger dead region with new variables.
- ✓ Smooth coverage of soft gluon region.
- ✓ No overlapping regions in phase space.



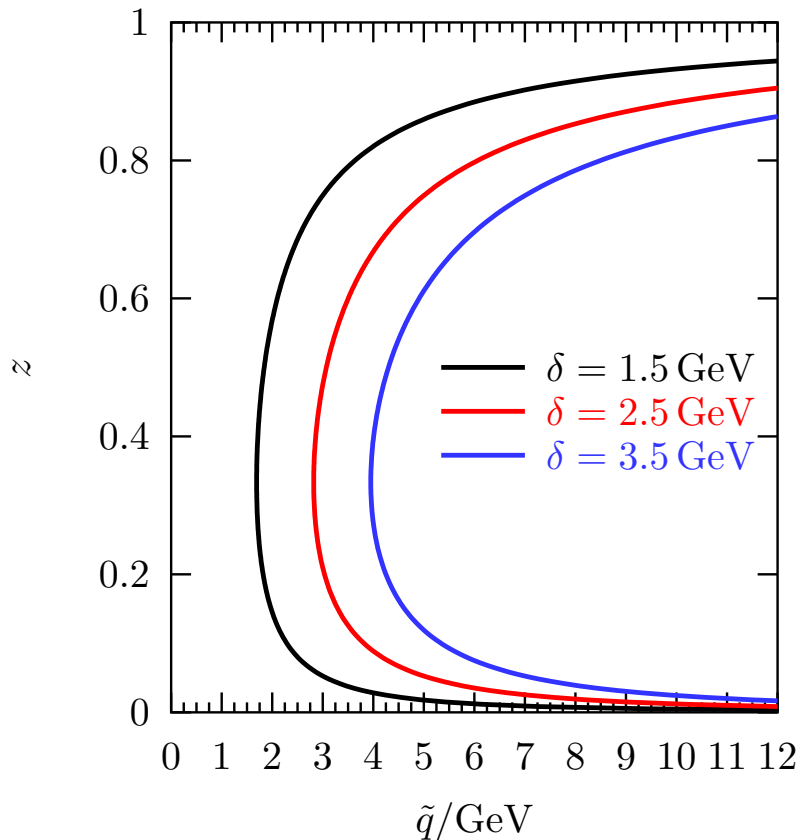
## Universal cutoff parameter $\delta$

- Parton shower termination determined by  $Q_g$ .
- $Q_g$  flavour dependent.
- Universal parameter  $\delta$  in configuration file.

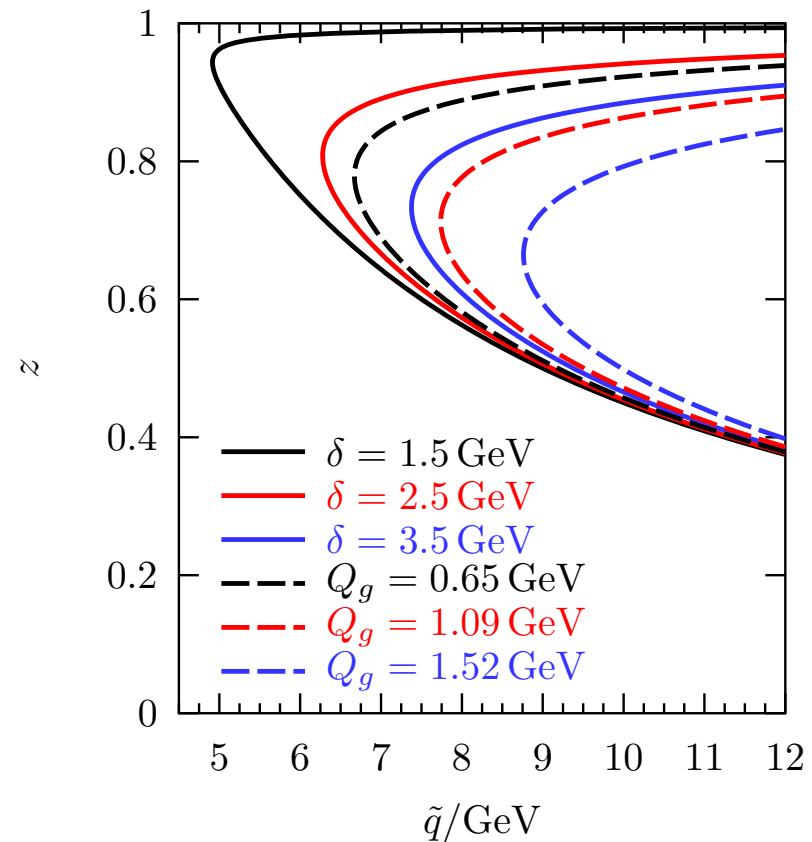
Parametrization of  $Q_g$  in terms of  $\delta, m_q$

$$Q_g = \frac{\delta - 0.3m_q}{2.3} .$$

*light quarks:*

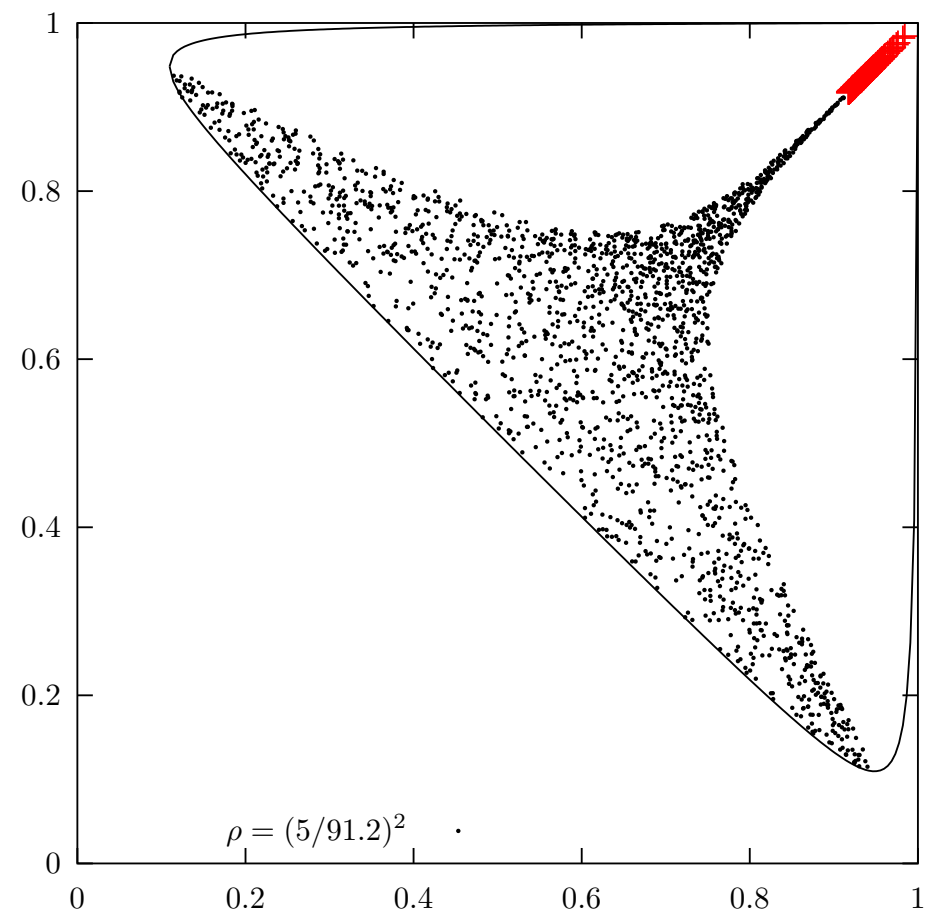


*b quarks:*



## Hard Matrix Element Corrections

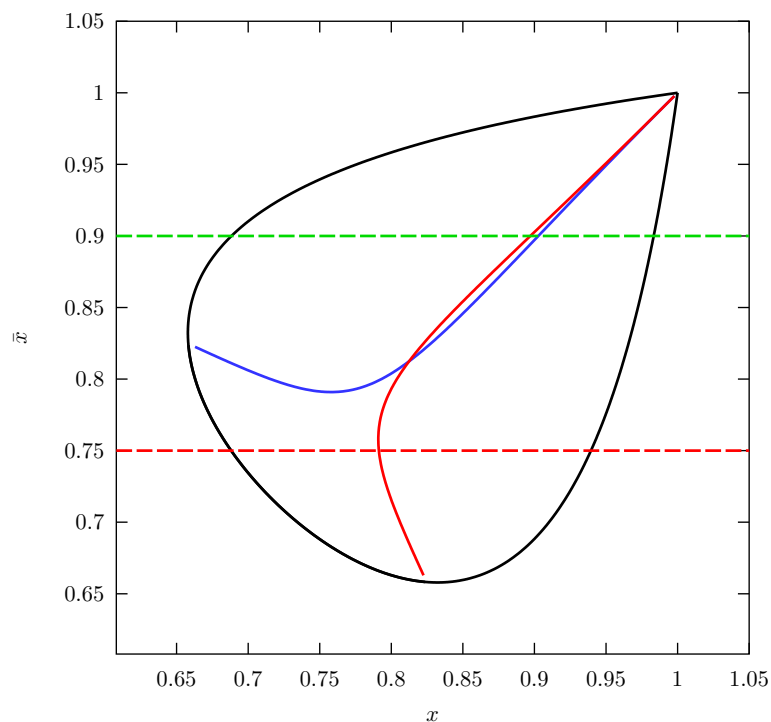
- Points  $(x, \bar{x})$  in **dead region** chosen acc to LO  $e^+e^- \rightarrow q\bar{q}g$  matrix element and accepted acc to ME weight.
- About **3%** of all events are actually hard  $q\bar{q}g$  events.
- Red points have **weight  $> 1$** , practically no error by setting weight to one.
- Event **oriented** according to given  $q\bar{q}$  geometry. Quark direction is kept with weight  $x^2/(x^2 + \bar{x}^2)$ .



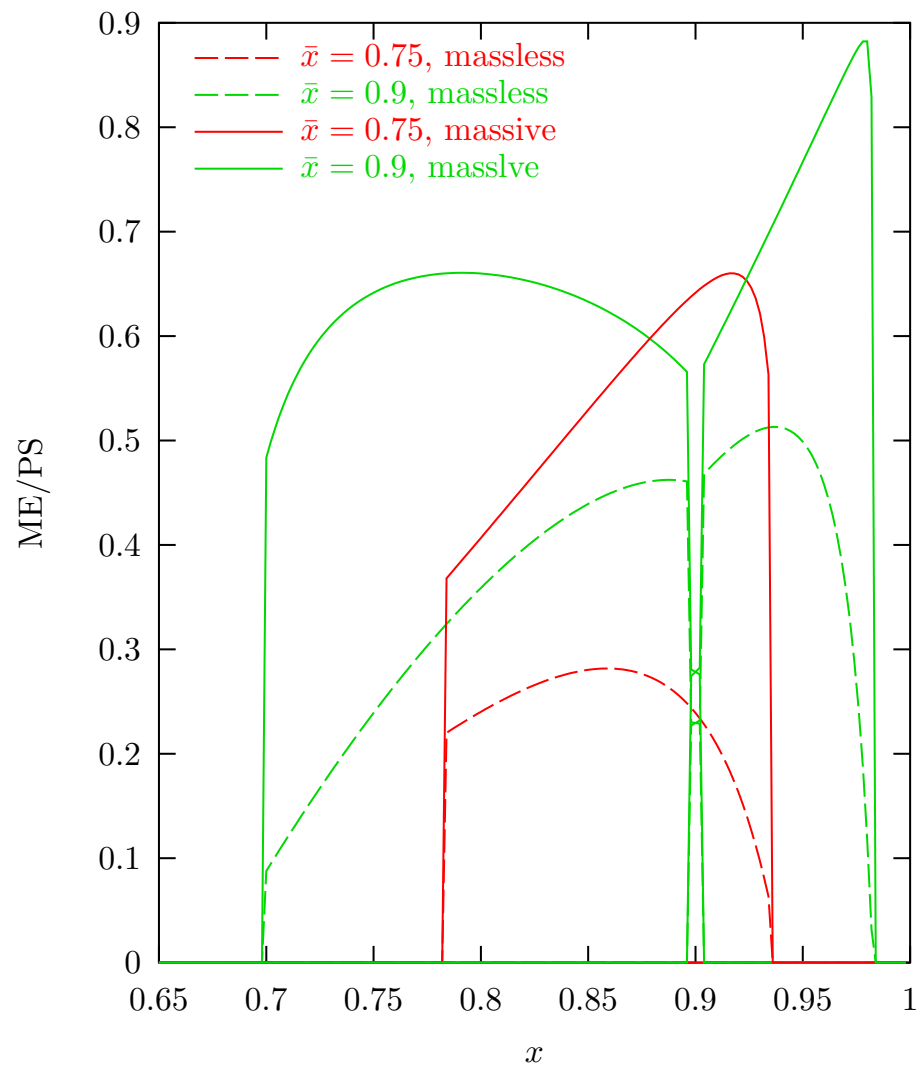
# Soft Matrix Element Corrections

- Ratio ME/PS compares emission with result from true ME if slightly away from soft/collinear region.
- **Veto** on 'hardest emission so far' in  $p_{\perp}$ .
- **Massive splitting function** *very important!*

Example with heavy quark,  $m^2/Q^2 = 0.1$ :



Comparison with massless splitting function



# Cluster hadronization in a nutshell

- **Nonperturbative  $g \rightarrow q\bar{q}$  splitting** ( $q = uds$ ) isotropically. Here,  $m_g \approx 750 \text{ MeV} > 2m_q$ .
- **Cluster formation**, universal spectrum (see below)
- **Cluster fission**, until

$$M^P < M_{\text{max}}^P + (m_1 + m_2)^P$$

where masses are chosen from

$$M_i = \left[ \left( M^P - (m_i + m_3)^P \right) r_i + (m_i + m_3)^P \right]^{1/P},$$

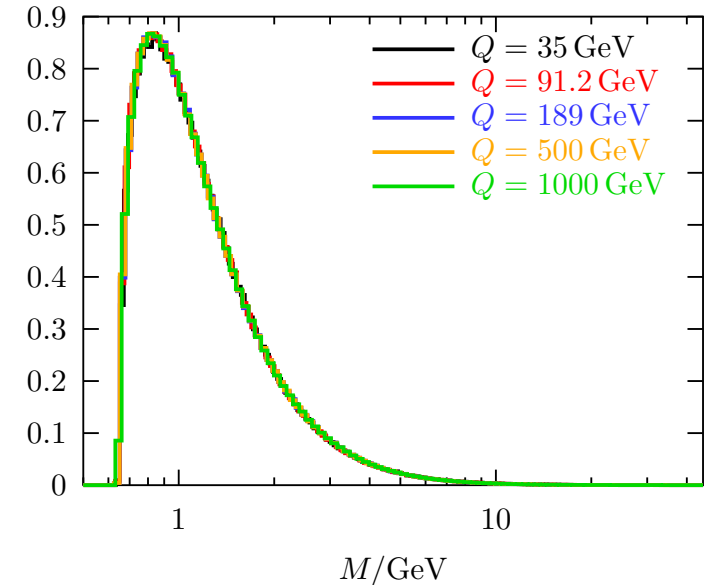
with additional phase space constraints. Constituents keep moving in their original direction.

- **Cluster Decay**

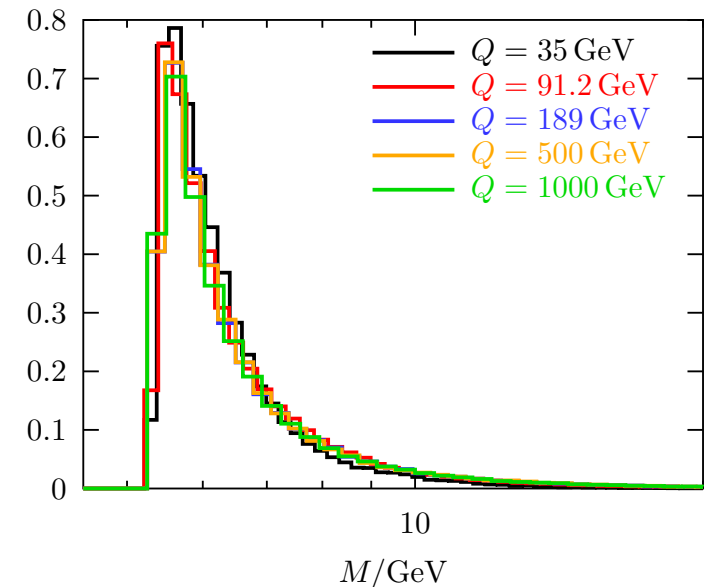
$$P(a_{i,q}, b_{q,j} | i, j) = \frac{W(a_{i,q}, b_{q,j} | i, j)}{\sum_{M/B} W(c_{i,q'}, d_{q',j} | i, j)}.$$

**New!** Meson/Baryon ratio is parametrized in terms of diquark weight. In HERWIG the sum ran over all possible hadrons.

Primary Light Clusters

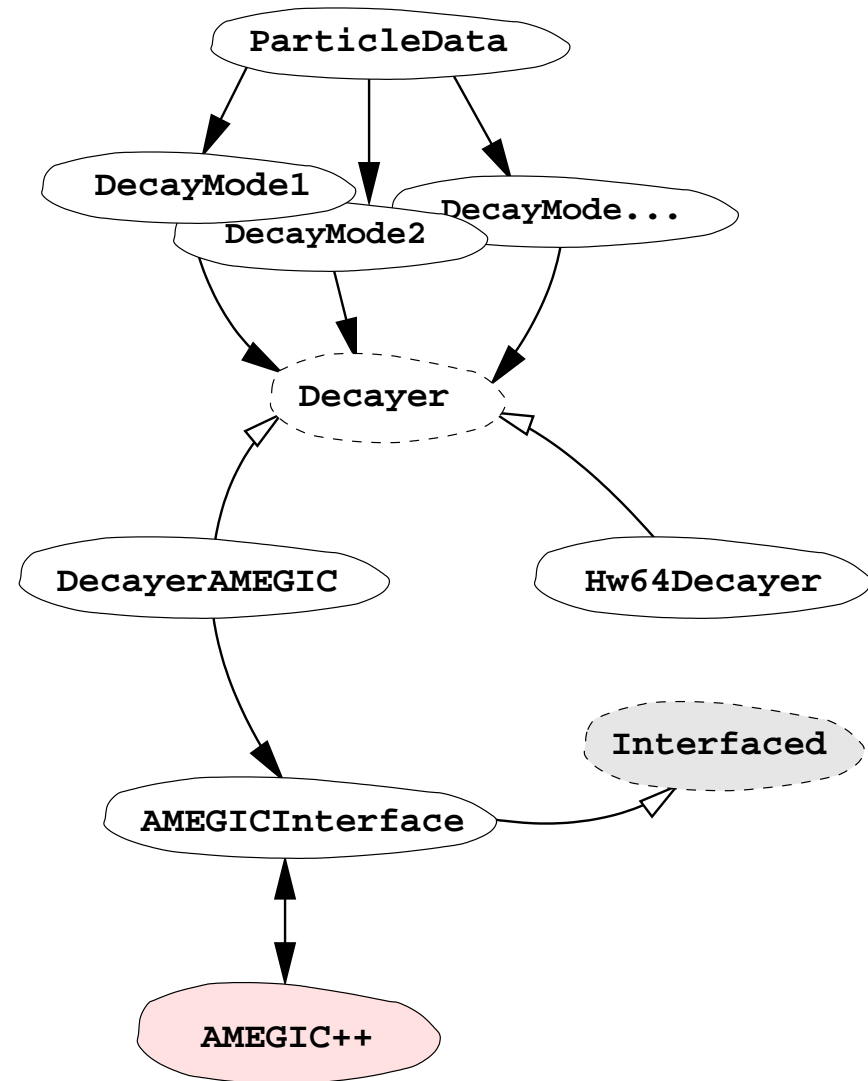


Primary  $b$ -Clusters



# Decays

- FORTRAN HERWIG is reproduced with **Hw64Decayer** using the same Matrix element codes as before (will be used for hadronic decays right now)
- **DecayerAMEGIC** gets final states for a perturbative decay mode directly from **AMEGIC++**
- Better hadronic decayers are currently being developed for particular decay modes.
- Status: 448 particles with a total of 2607 decay modes. . .
- Spin correlations.
- —→ Peter Richardson's talk.



# Hadron Multiplicities

Particle	Experiment	Measured	Old Model	Herwig++	Fortran
All Charged	M,A,D,L,O	$20.924 \pm 0.117$	20.22*	20.814	20.532*
$\gamma$	A,O	$21.27 \pm 0.6$	23.032	22.67	20.74
$\pi^0$	A,D,L,O	$9.59 \pm 0.33$	10.27	10.08	9.88
$\rho(770)^0$	A,D	$1.295 \pm 0.125$	1.235	1.316	1.07
$\pi^\pm$	A,O	$17.04 \pm 0.25$	16.30	16.95	16.74
$\rho(770)^\pm$	O	$2.4 \pm 0.43$	1.99	2.14	2.06
$\eta$	A,L,O	$0.956 \pm 0.049$	0.886	0.893	0.669*
$\omega(782)$	A,L,O	$1.083 \pm 0.088$	0.859	0.916	1.044
$\eta'(958)$	A,L,O	$0.152 \pm 0.03$	0.13	0.136	0.106
$K^0$	S,A,D,L,O	$2.027 \pm 0.025$	2.121*	2.062	2.026
$K^*(892)^0$	A,D,O	$0.761 \pm 0.032$	0.667	0.681	0.583*
$K^*(1430)^0$	D,O	$0.106 \pm 0.06$	0.065	0.079	0.072
$K^\pm$	A,D,O	$2.319 \pm 0.079$	2.335	2.286	2.250
$K^*(892)^\pm$	A,D,O	$0.731 \pm 0.058$	0.637	0.657	0.578
$\phi(1020)$	A,D,O	$0.097 \pm 0.007$	0.107	0.114	0.134*
$p$	A,D,O	$0.991 \pm 0.054$	0.981	0.947	1.027
$\Delta^{++}$	D,O	$0.088 \pm 0.034$	0.185	0.092	0.209*
$\Sigma^-$	O	$0.083 \pm 0.011$	0.063	0.071	0.071
$\Lambda$	A,D,L,O	$0.373 \pm 0.008$	0.325*	0.384	0.347*
$\Sigma^0$	A,D,O	$0.074 \pm 0.009$	0.078	0.091	0.063
$\Sigma^+$	O	$0.099 \pm 0.015$	0.067	0.077	0.088
$\Sigma(1385)^\pm$	A,D,O	$0.0471 \pm 0.0046$	0.057	0.0312*	0.061*
$\Xi^-$	A,D,O	$0.0262 \pm 0.001$	0.024	0.0286	0.029
$\Xi(1530)^0$	A,D,O	$0.0058 \pm 0.001$	0.026*	0.0288*	0.009*
$\Omega^-$	A,D,O	$0.00125 \pm 0.00024$	0.001	0.00144	0.0009

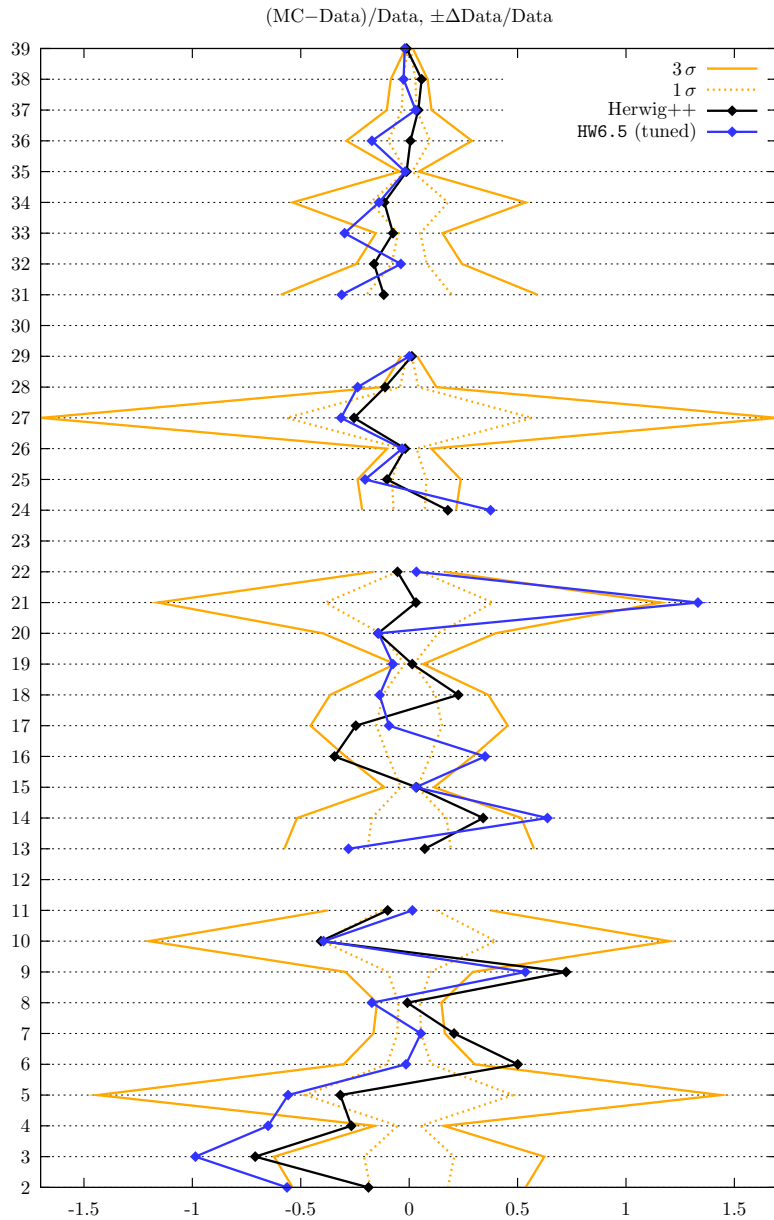
## Hadron Multiplicities (ctd')

Particle	Experiment	Measured	Old Model	Herwig++	Fortran
$f_2(1270)$	D,L,O	$0.168 \pm 0.021$	0.113	0.150	0.173
$f_2'(1525)$	D	$0.02 \pm 0.008$	0.003	0.012	0.012
$D^\pm$	A,D,O	$0.184 \pm 0.018$	0.322*	0.319*	0.283*
$D^*(2010)^\pm$	A,D,O	$0.182 \pm 0.009$	0.168	0.180	0.151*
$D^0$	A,D,O	$0.473 \pm 0.026$	0.625*	0.570*	0.501
$D_s^\pm$	A,O	$0.129 \pm 0.013$	0.218*	0.195*	0.127
$D_s^{*\pm}$	O	$0.096 \pm 0.046$	0.082	0.066	0.043
$J/\Psi$	A,D,L,O	$0.00544 \pm 0.00029$	0.006	0.00361*	0.002*
$\Lambda_c^+$	D,O	$0.077 \pm 0.016$	0.006*	0.023*	0.001*
$\Psi'(3685)$	D,L,O	$0.00229 \pm 0.00041$	0.001*	0.00178	0.0008*

# of \*'s = observables with more than  $3\sigma$  deviation:

OldModel : Herwig++ : Fortran = 9 : 7 : 13

# Hadron Multiplicities (ctd')



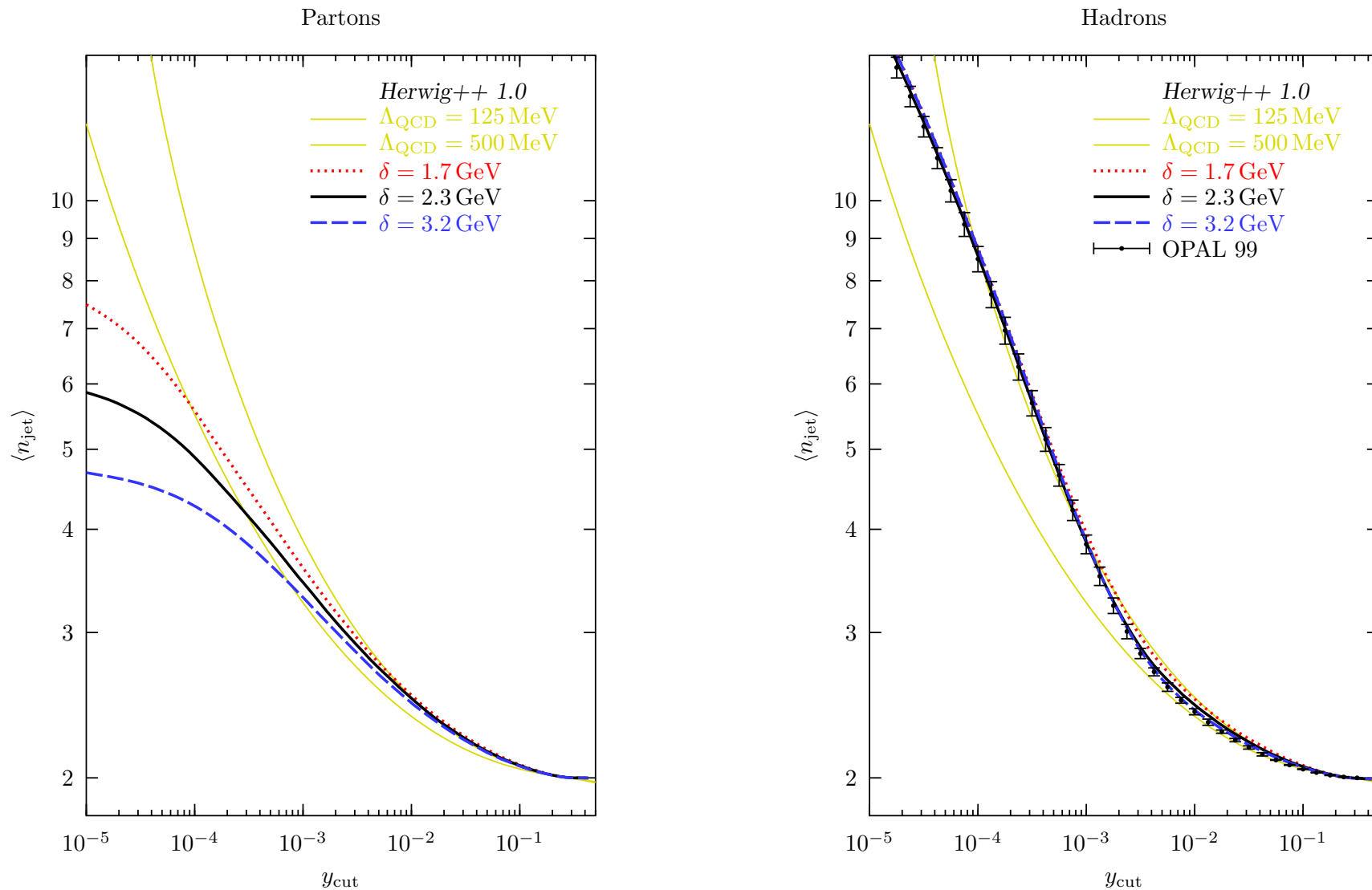
We can compare  $\chi^2$ 's:

model	$\sum \chi^2 / \text{dof} =$
DKMode 0:	543.84/35 = 15.54
DKMode 1:	3644.33/35 = 104.12
Herwig++:	277.16/35 = 7.92
no $D^\pm$ :	= 6.54
HW65d:	7151.13/35 = 204.32
HW65t:	490.52/35 = 14.01
no $J/\psi$ :	= 4.38



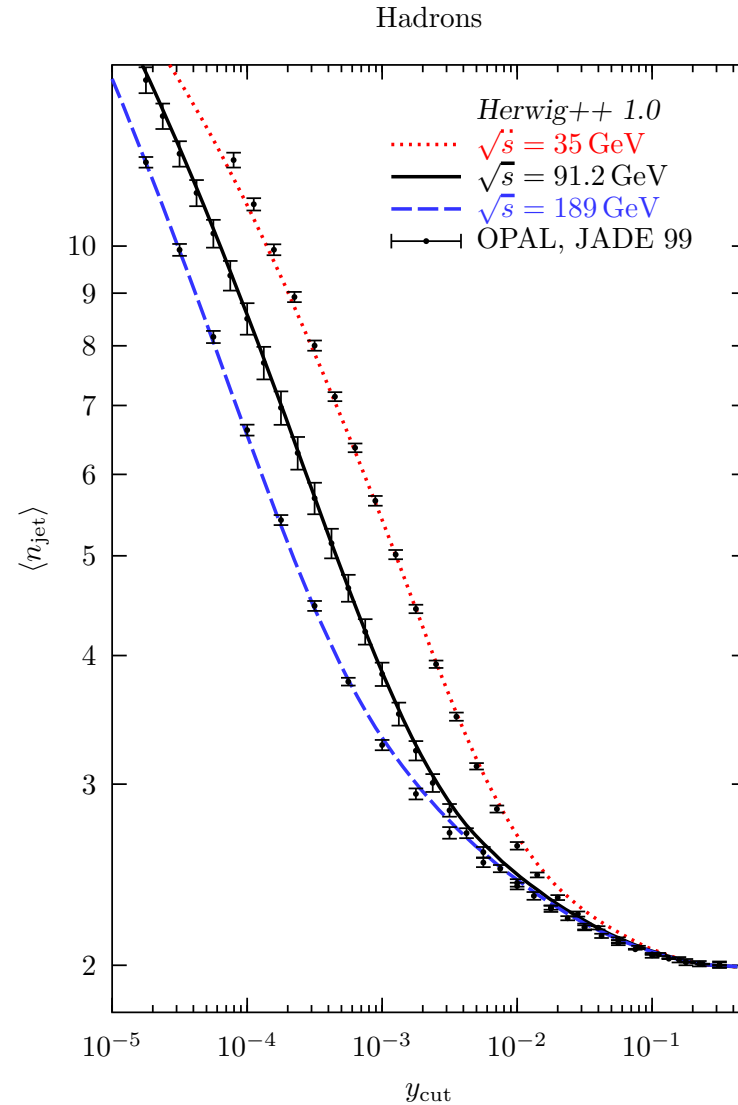
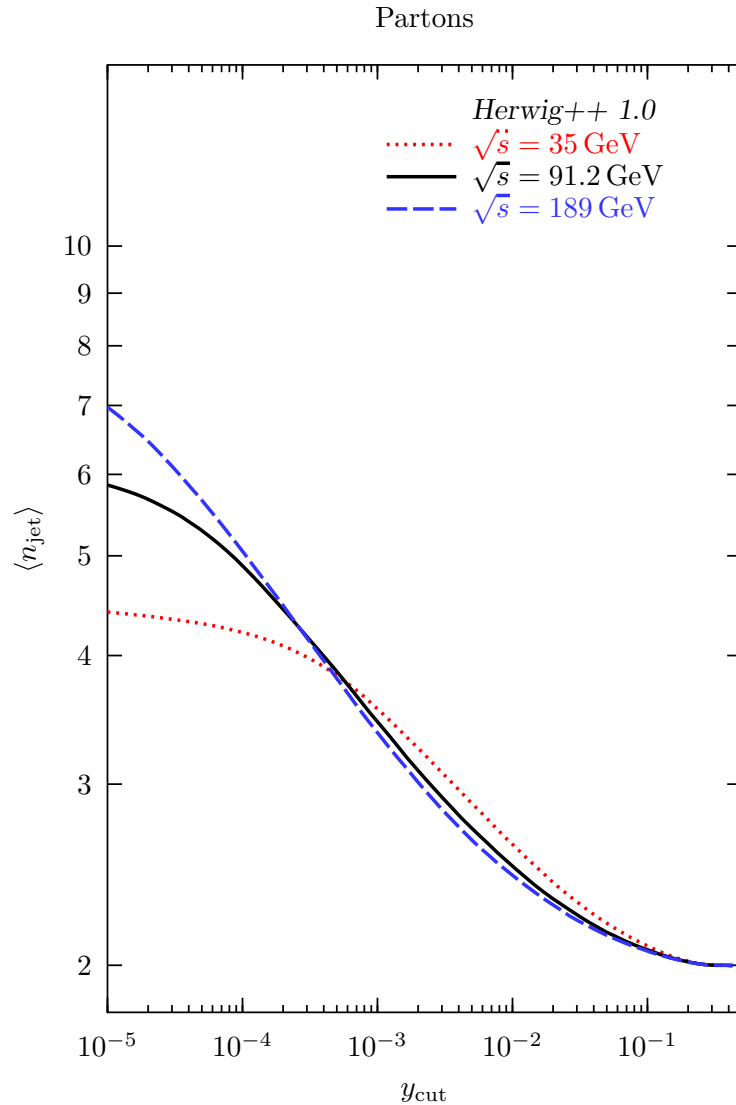
# Jet Multiplicity

Durham algorithm. Smooth interplay between shower and hadronization.



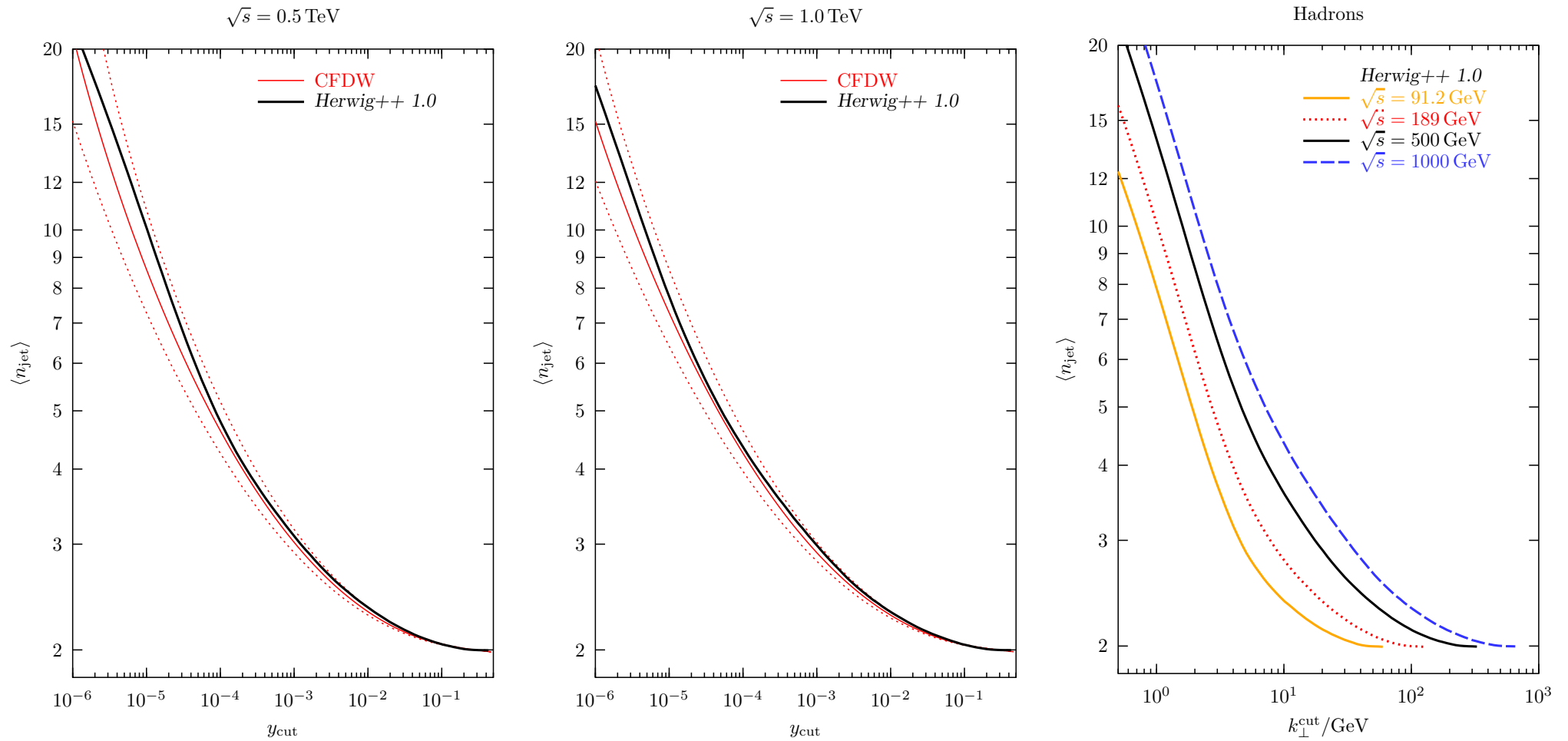
# Jet Multiplicity (PETRA, LEP, LEP II)

$$\sqrt{s} = \{35, 91.2, 189\} \text{ GeV}$$

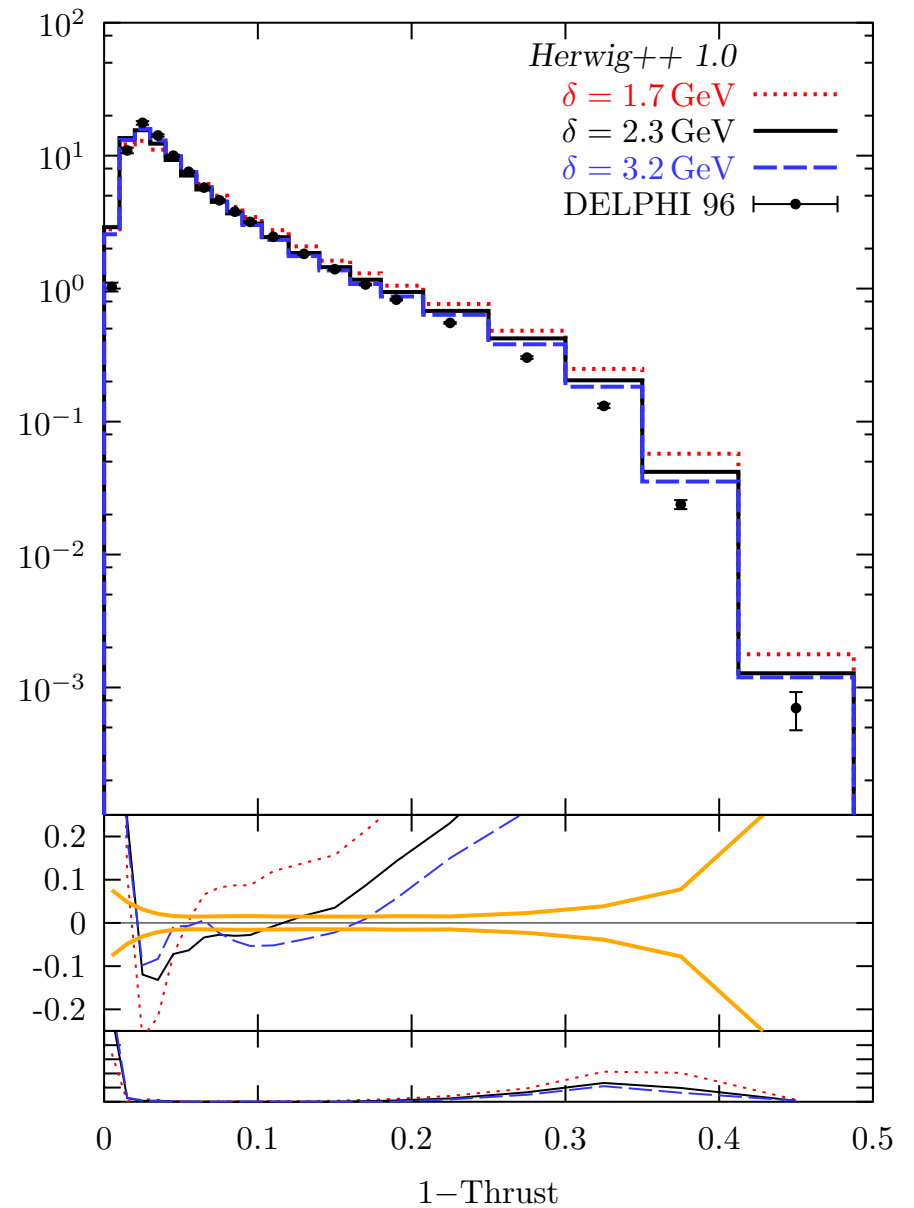
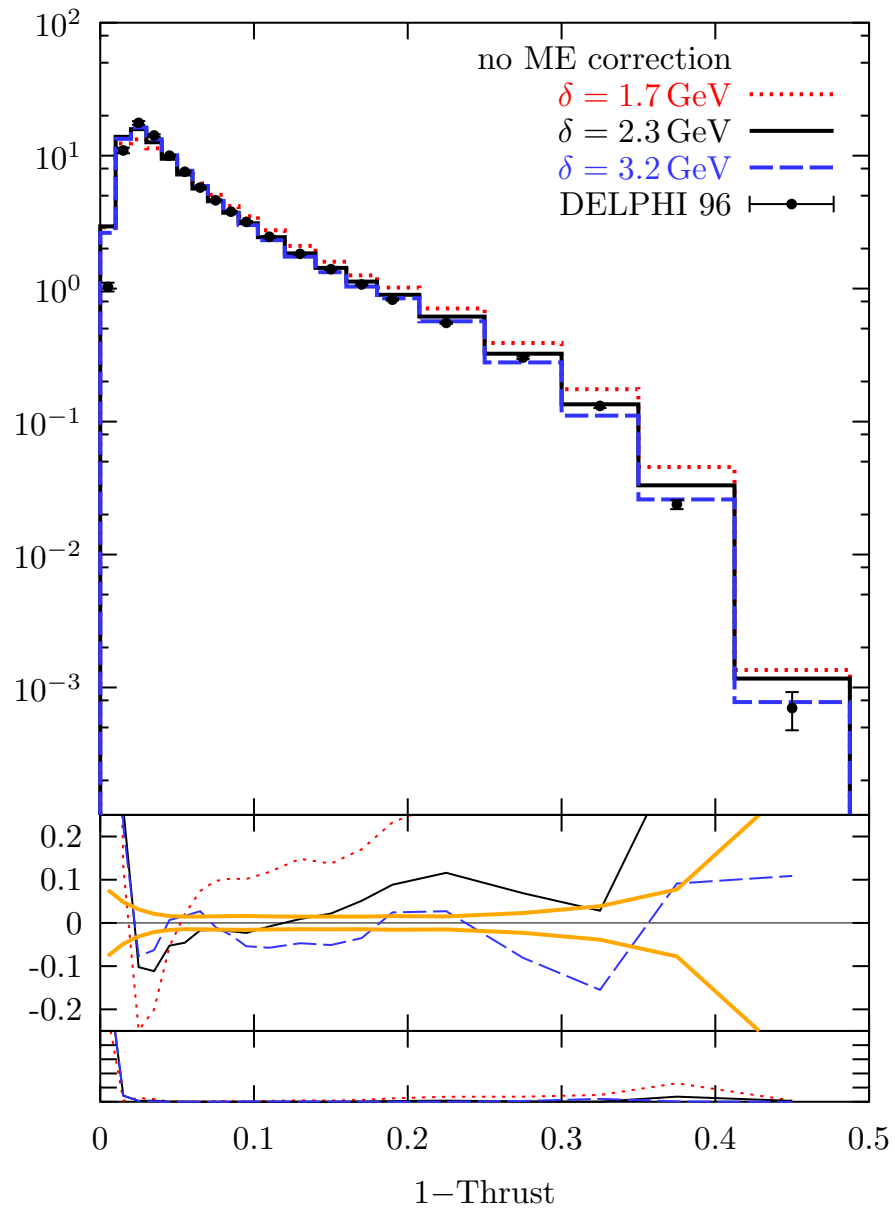


# Jet Multiplicity @ Next Linear Collider

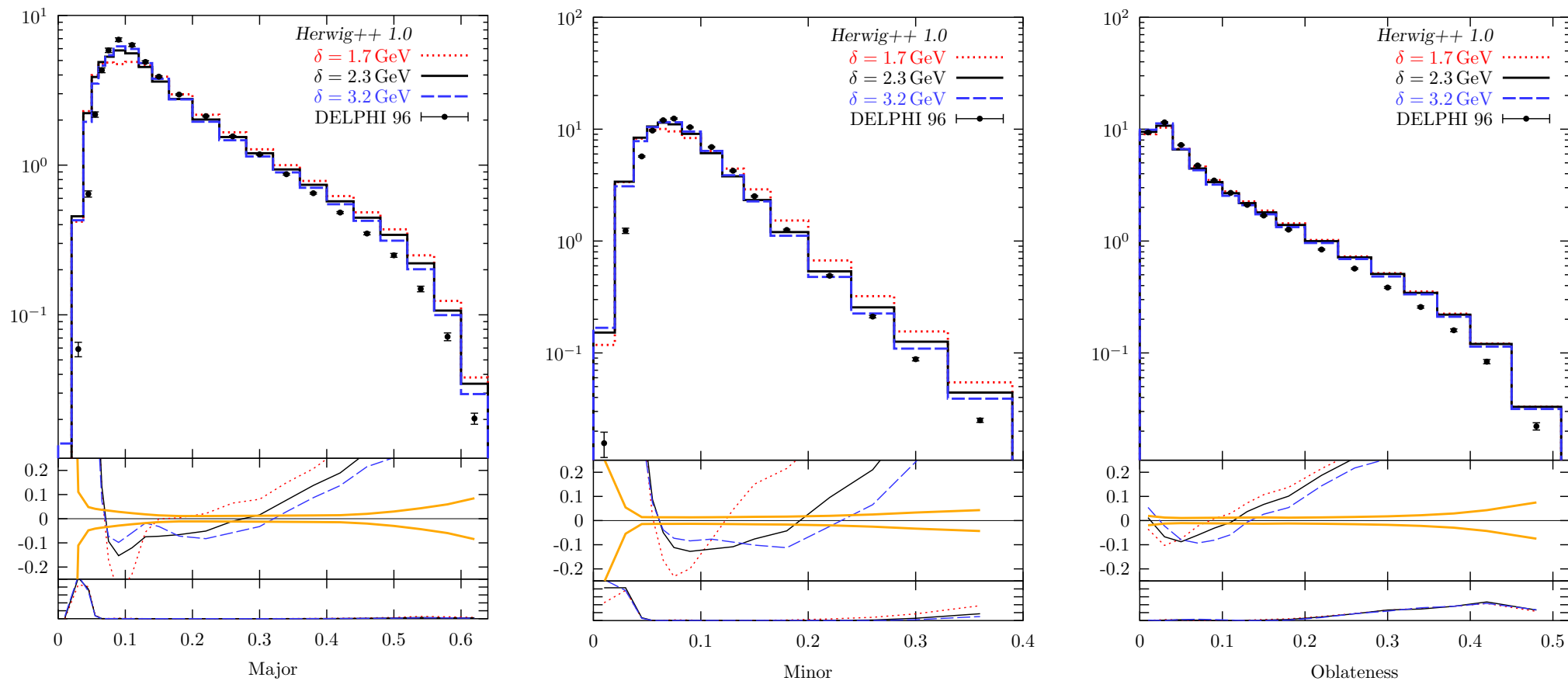
Herwig++ and NLLA pQCD (Catani, Fiorani, Dokshitzer, Webber, 1992); jet events with  $n_f = 5$ .



# Thrust — ME Corrections off/on

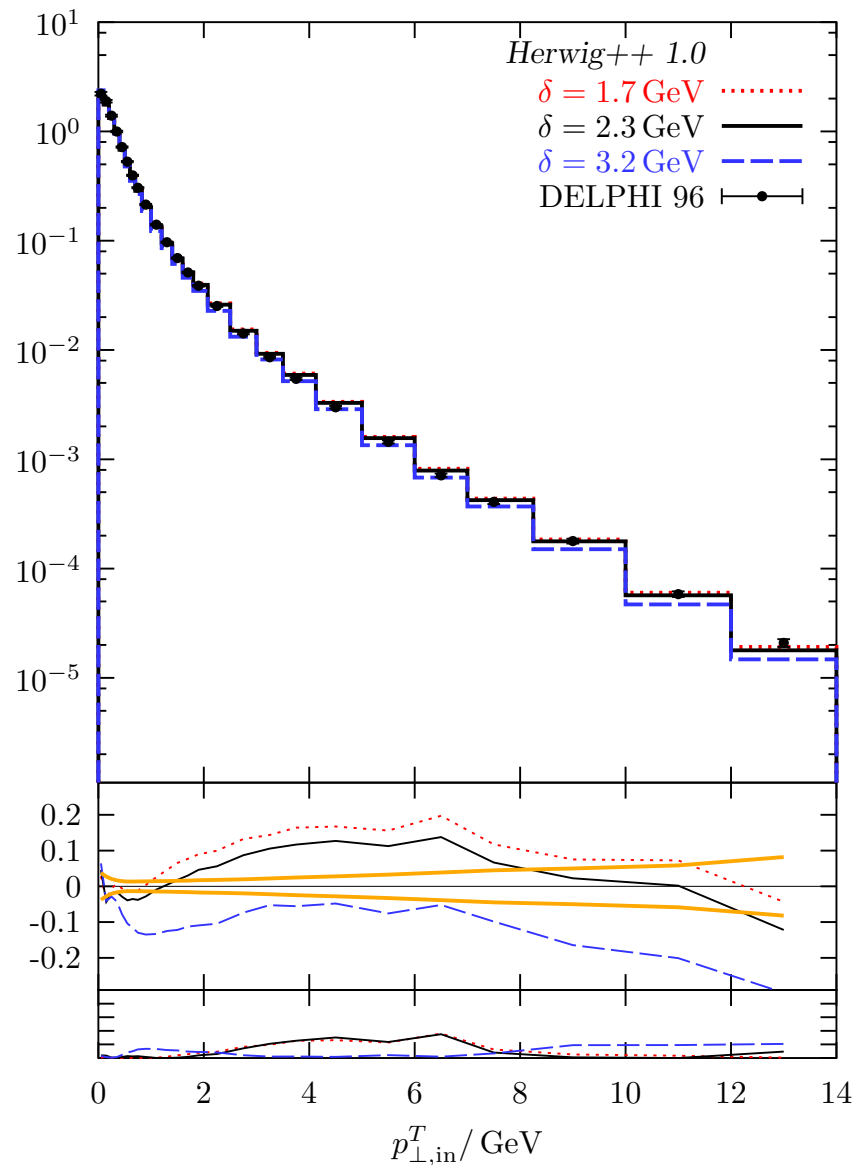
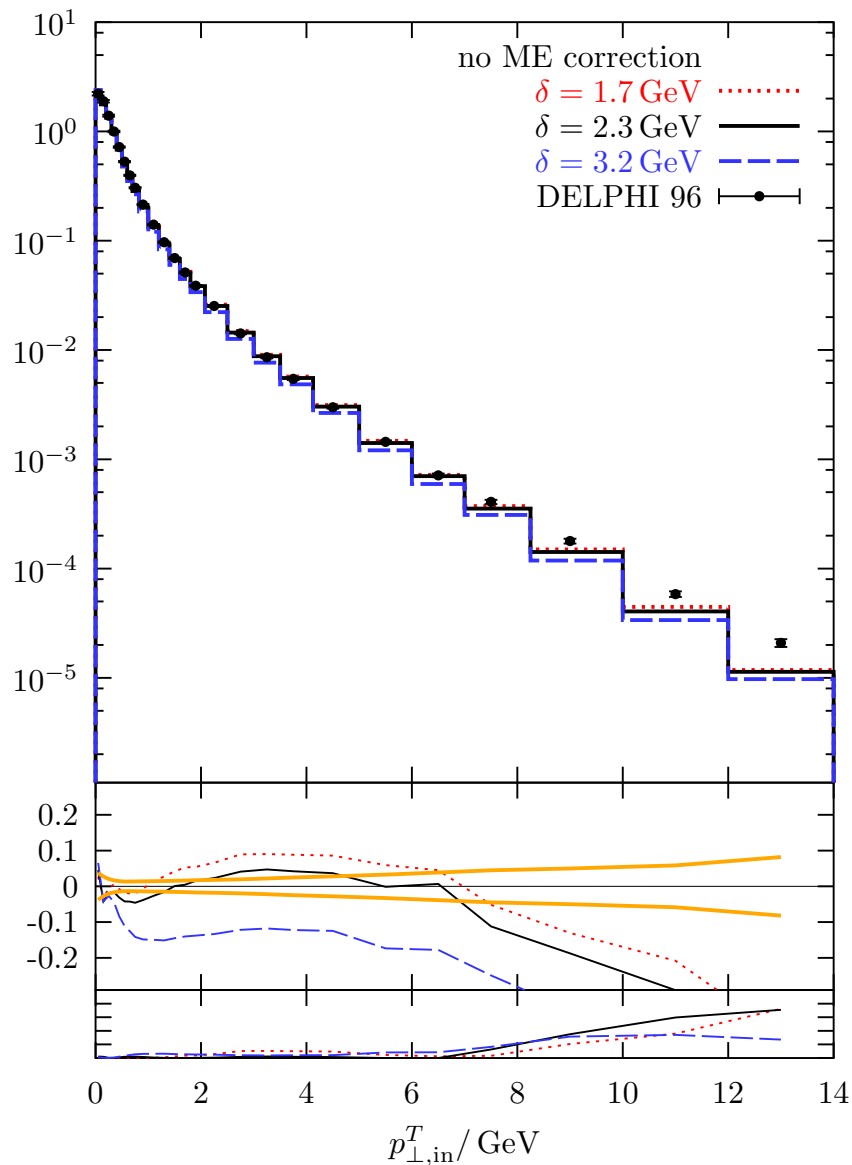


# Major, Minor, Oblateness

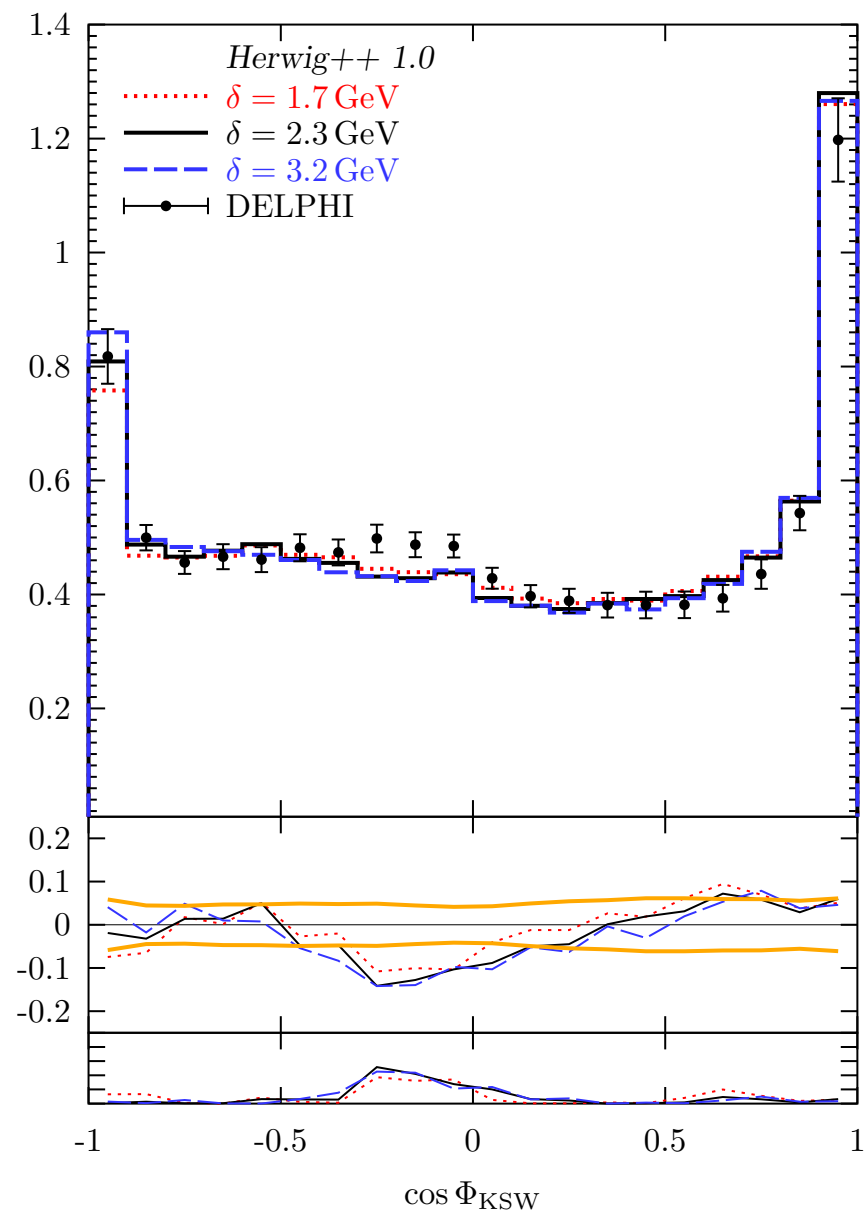
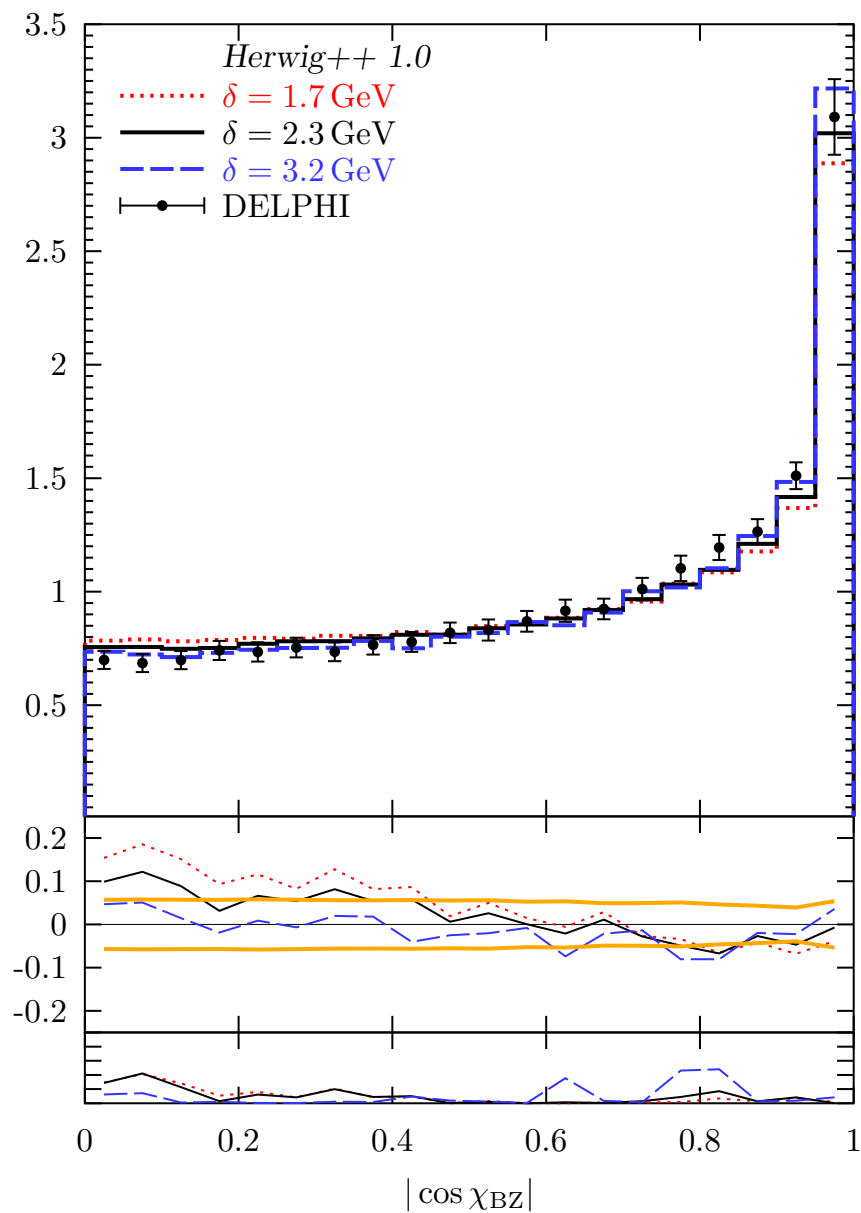


All Thrust-related distributions slightly wide, ie too many 2-jet like on one side and too many spherical events on the other side.

# $p_{\perp, \text{in}}^T$ — ME corrections off/on

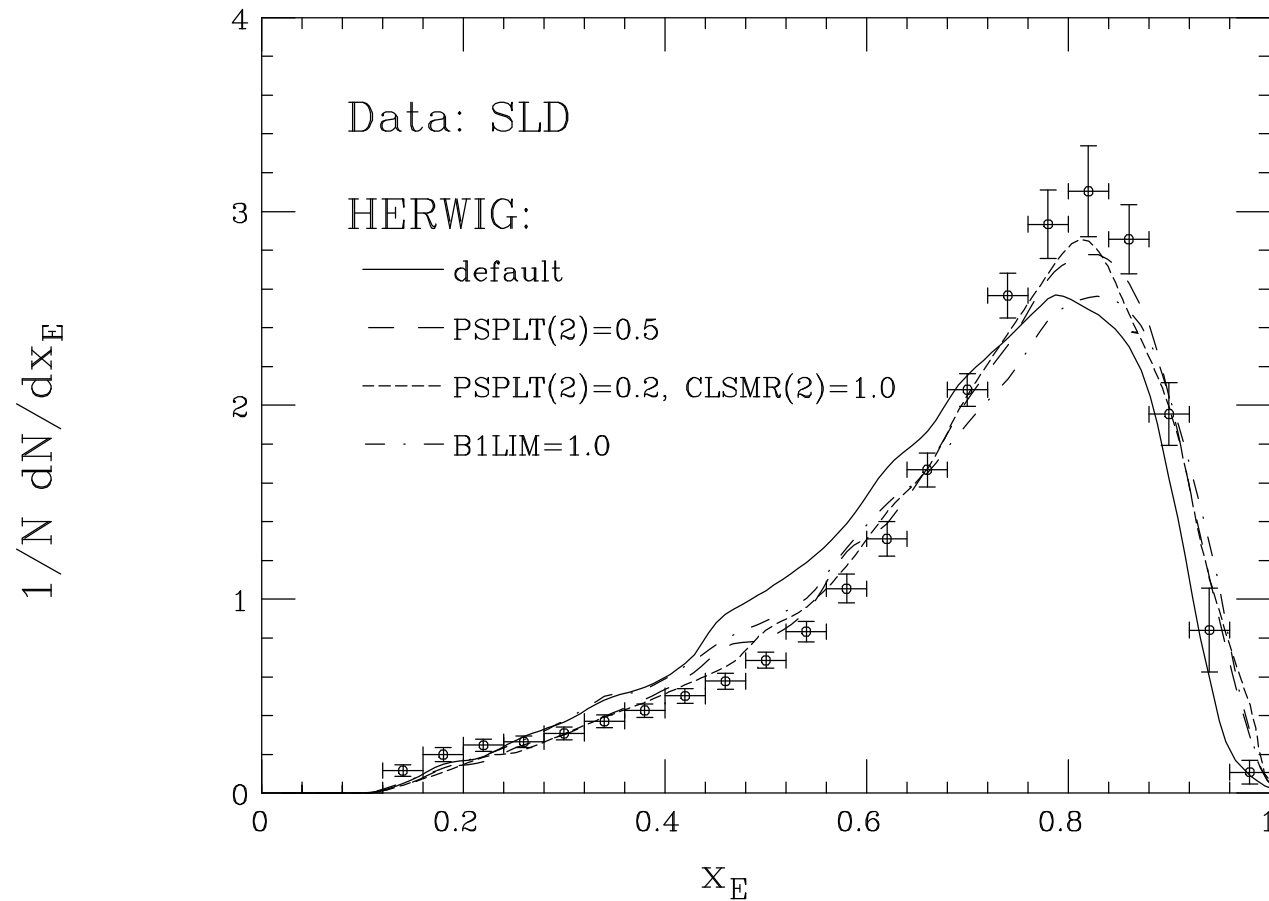


# Four Jet Angles I



# *B*-fragmentation function

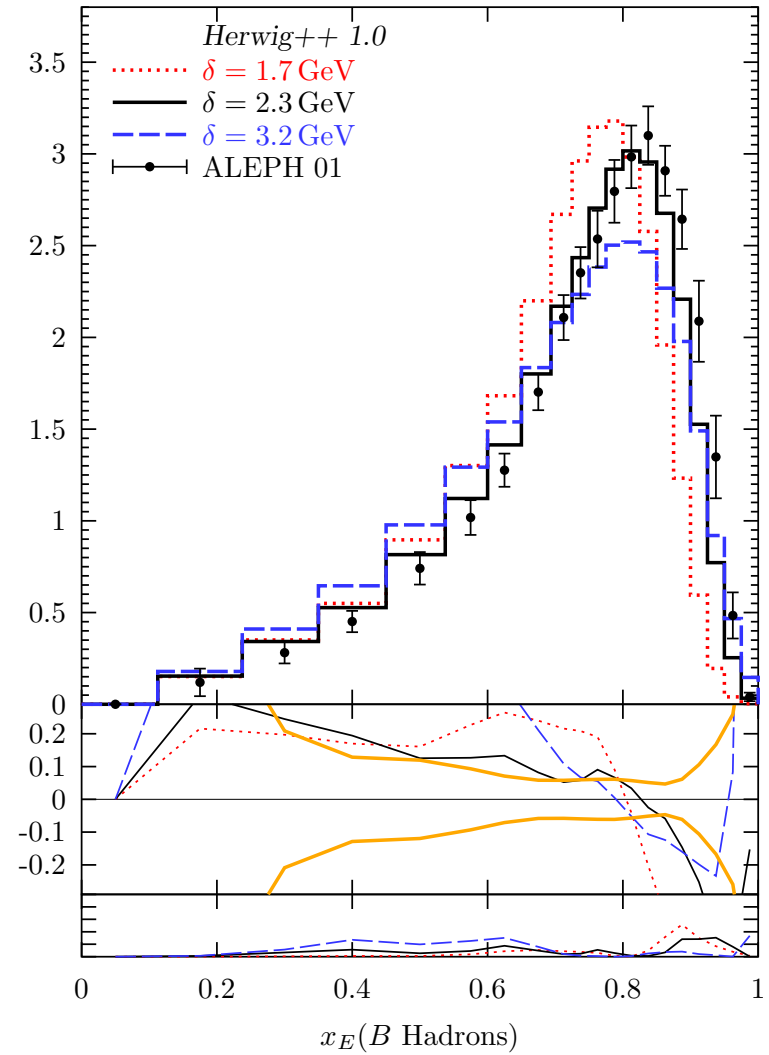
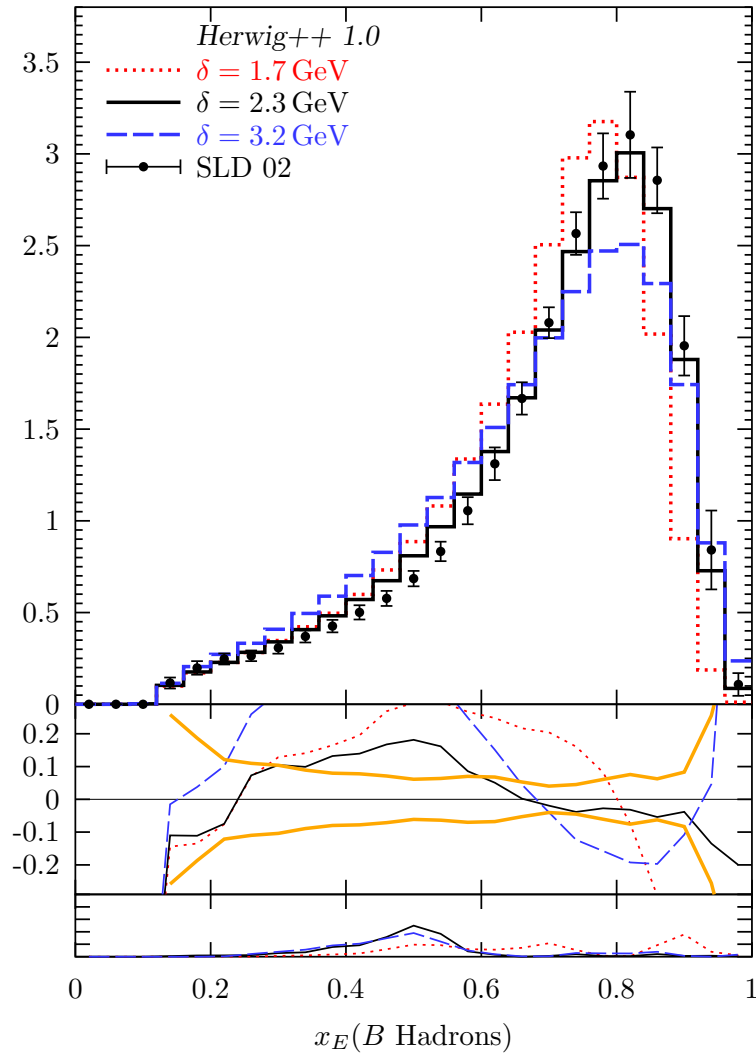
Weakly decaying *b* hadrons



HERWIG 6.4, very sensitive on hadronization!



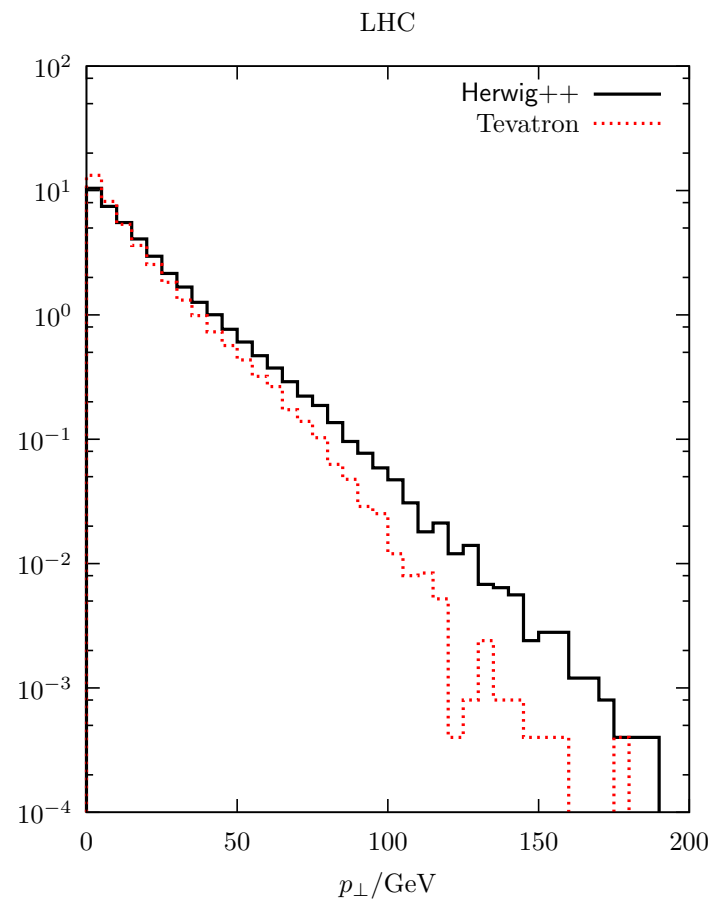
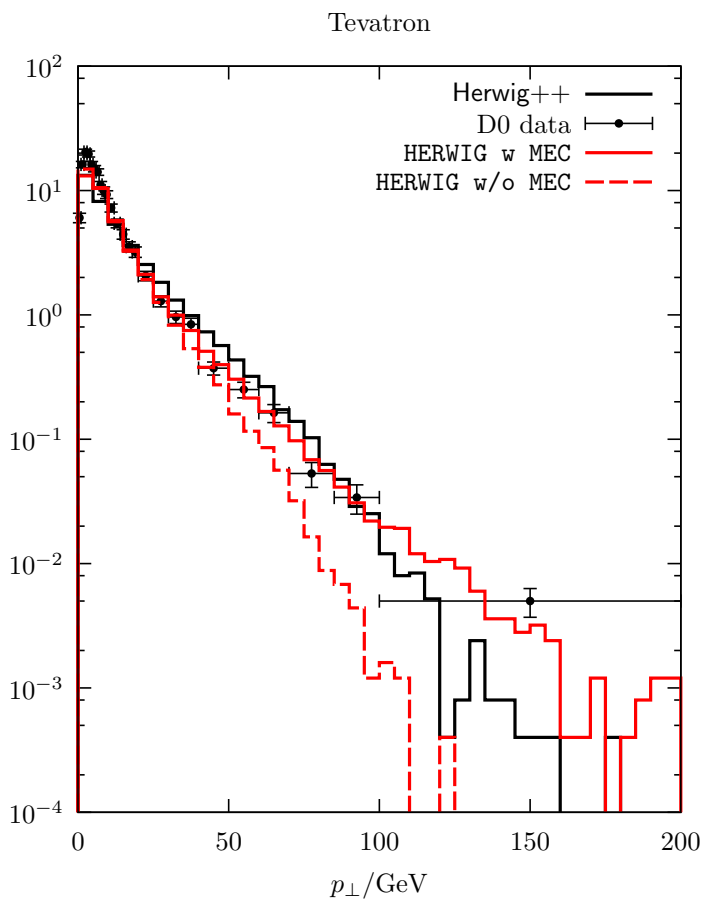
# B-fragmentation function



Only parton shower parameters varied!

## Currently. . .

- Parton shower implementations of evolution in our 'new variables' (hep-ph/0310083) ongoing.
- First results for Drell Yan coming up.
- Decays.



# What's next?

## Near Future. . .

- ★ Initial state shower:
  - Complete implementation and tests.
- ★ Refine  $e^+e^-$ :
  - Full CKKW ME+PS matching.
  - Precision tune to LEP data should be possible.
- ★ with IS and FS showers running:
  - Jets and shapes in DIS would be next logical step.
  - We can start to test Drell–Yan and jets in pp collisions.
  - Cross check with Tevatron data and finally make predictions for the LHC.
- ★ Underlying Event.
- ★ Hadronic Decays: *NEW!* many decays improved, spin correlations (P Richardson).
- ★ New Ideas: . . . .

## Conclusion

We have completed a new event generator for  $e^+e^-$  Annihilation:

**Herwig++ 1.0**

Next version for hadronic collisions in progress.