

Update on MRST Parton Distributions

James Stirling
IPPP, University of Durham

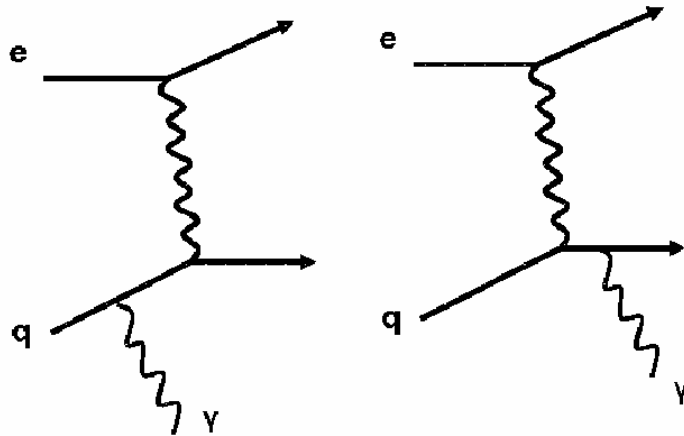
- QED-improved parton distributions
- a new approach to the high- x gluon distribution

(with Alan Martin, Dick Roberts and Robert Thorne)

QED effects in pdfs

De Rujula, Petronzio, Savoy-Navarro 1979
 Krifganz, Perlt 1988
 Bluemlein 1990
 Spiesberger 1994
 Roth, Weinzierl 2004

QED corrections to DIS include:

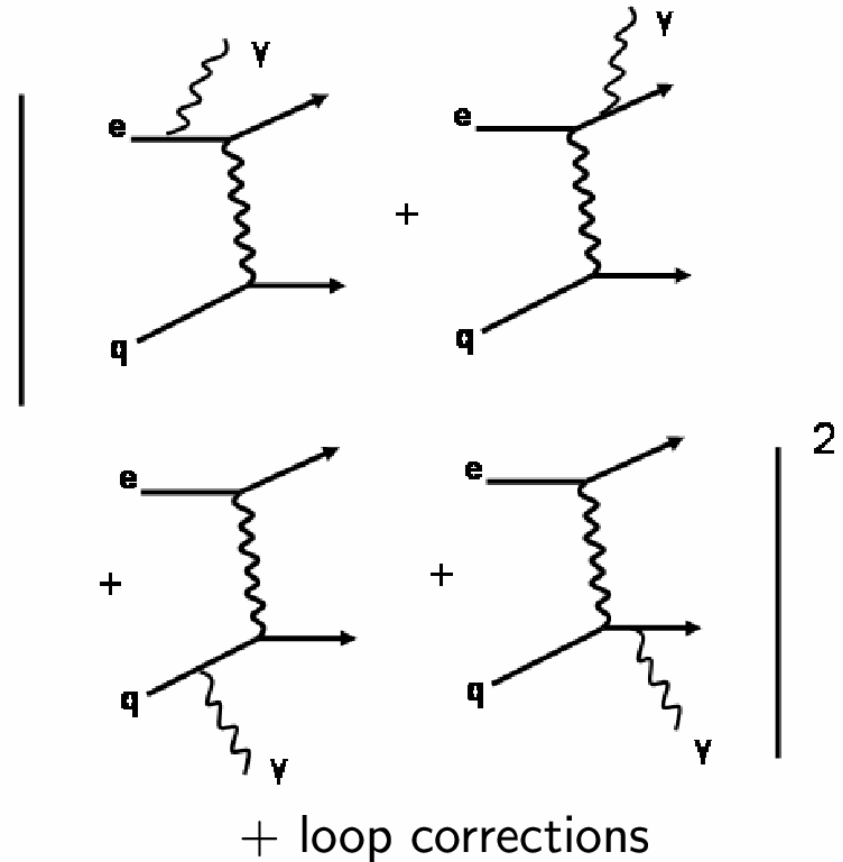


⇒ mass singularity when $\gamma \parallel q$

$$\frac{\alpha}{2\pi} \langle e_q^2 \rangle \ln \left(\frac{Q^2}{m_q^2} \right) \simeq 0.01$$

for $Q = 100 \text{ GeV}$, $m_q = 10 \text{ MeV}$, $\langle e_q^2 \rangle = 5/18$.

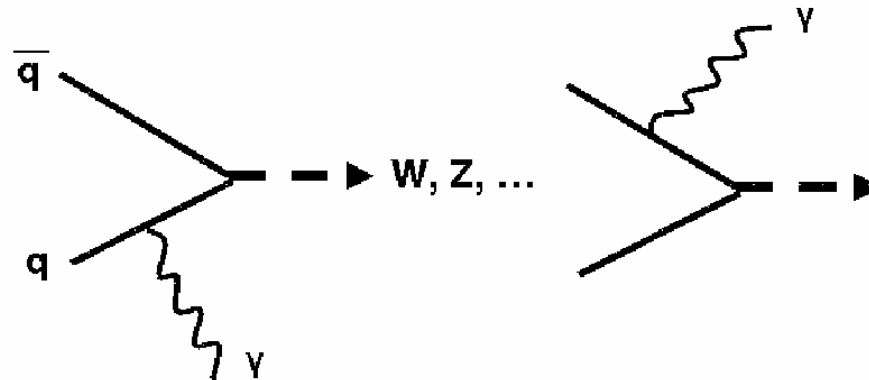
included in standard radiative correction packages (HECTOR, HERACLES)



$$\Rightarrow \frac{\alpha}{\pi} \left[C_{\text{lept}} + e_q^2 C_{\text{quark}} + e_q C_{\text{int}} \right]$$

Note: C_{int} finite as $m_q \rightarrow 0$

- above QED corrections are *universal* and can be absorbed into pdfs, exactly as for QCD singularities, leaving finite (as $m_q \rightarrow 0$) $O(\alpha)$ QED corrections in coefficient functions



- relevant for electroweak correction calculations for processes at Tevatron & LHC, e.g. W, Z, WH, ...
(see e.g. U. Baur et al, PRD 59 (2003) 013002)

QED-improved DGLAP equations

- at leading order in α and α_S

$$\frac{\partial q_i(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{qq}(y) q_i\left(\frac{x}{y}, \mu^2\right) + P_{qg}(y, \alpha_S) g\left(\frac{x}{y}, \mu^2\right) \right\}$$

$$+ \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left\{ \tilde{P}_{qq}(y) e_i^2 q_i\left(\frac{x}{y}, \mu^2\right) + P_{q\gamma}(y) e_i^2 \gamma\left(\frac{x}{y}, \mu^2\right) \right\}$$

$$\frac{\partial g(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{gq}(y) \sum_j q_j\left(\frac{x}{y}, \mu^2\right) \right.$$

$$\left. + P_{gg}(y) g\left(\frac{x}{y}, \mu^2\right) \right\}$$

$$\frac{\partial \gamma(x, \mu^2)}{\partial \log \mu^2} = \frac{\alpha}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{\gamma q}(y) \sum_j e_j^2 q_j\left(\frac{x}{y}, \mu^2\right) \right.$$

$$\left. + P_{\gamma\gamma}(y) \gamma\left(\frac{x}{y}, \mu^2\right) \right\}$$

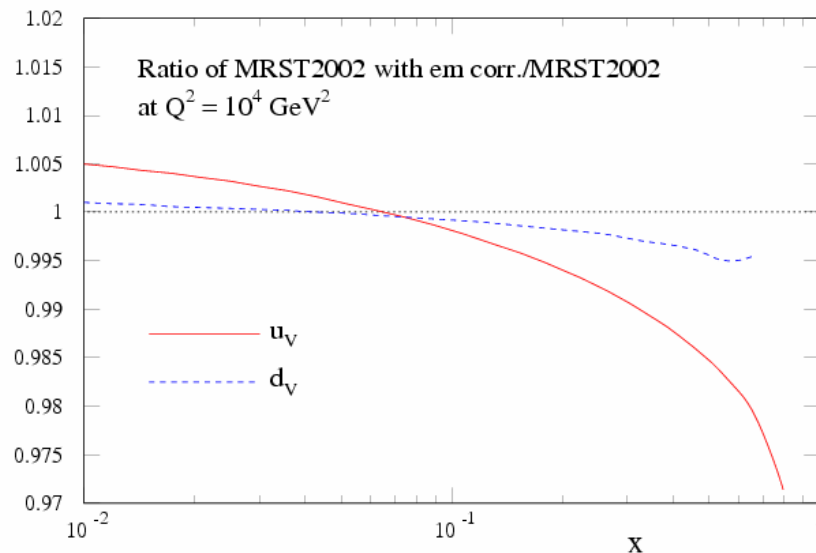
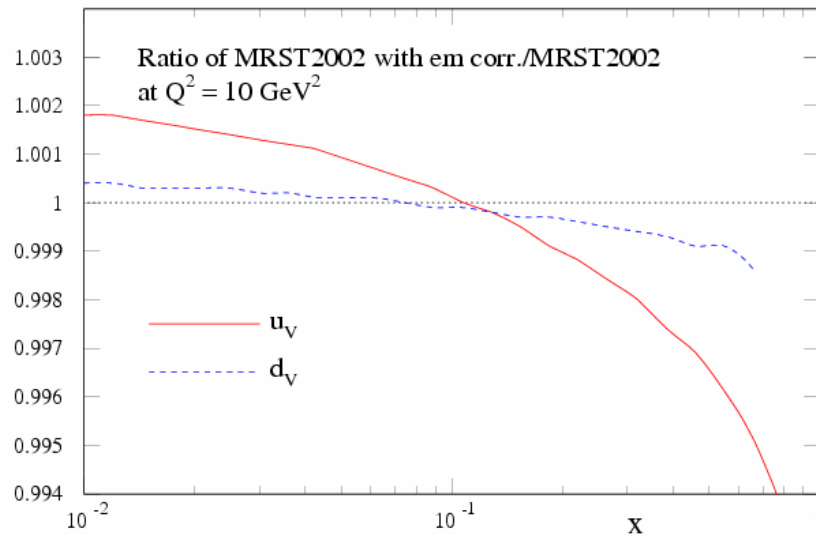
where

$$\begin{aligned} \tilde{P}_{qq} &= C_F^{-1} P_{qq}, & P_{\gamma q} &= C_F^{-1} P_{gq}, \\ P_{q\gamma} &= T_R^{-1} P_{qg}, & P_{\gamma\gamma} &= -\frac{2}{3} \sum_i e_i^2 \delta(1-x) \end{aligned}$$

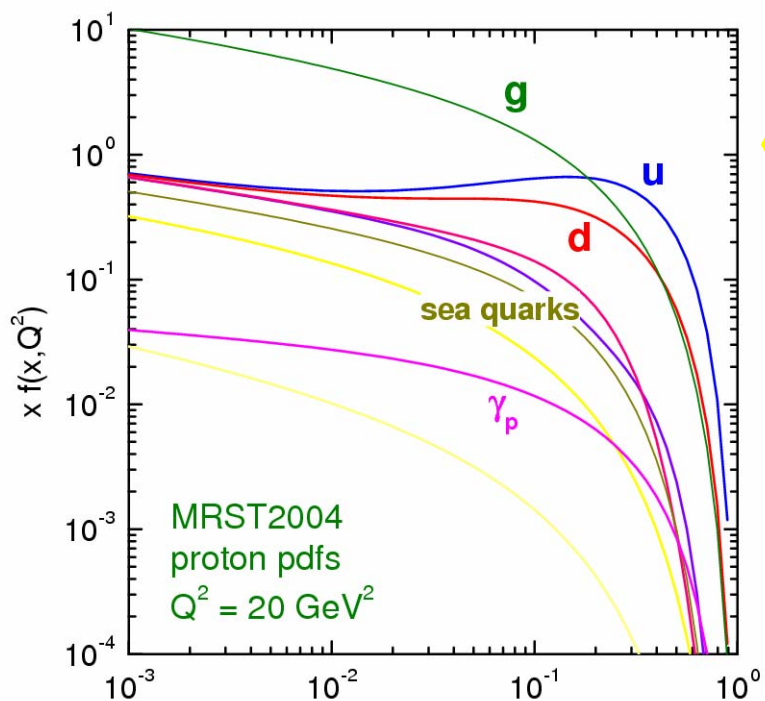
- momentum conservation: $\int_0^1 dx x \left\{ \sum_i q_i(x, \mu^2) + g(x, \mu^2) + \gamma(x, \mu^2) \right\} = 1$



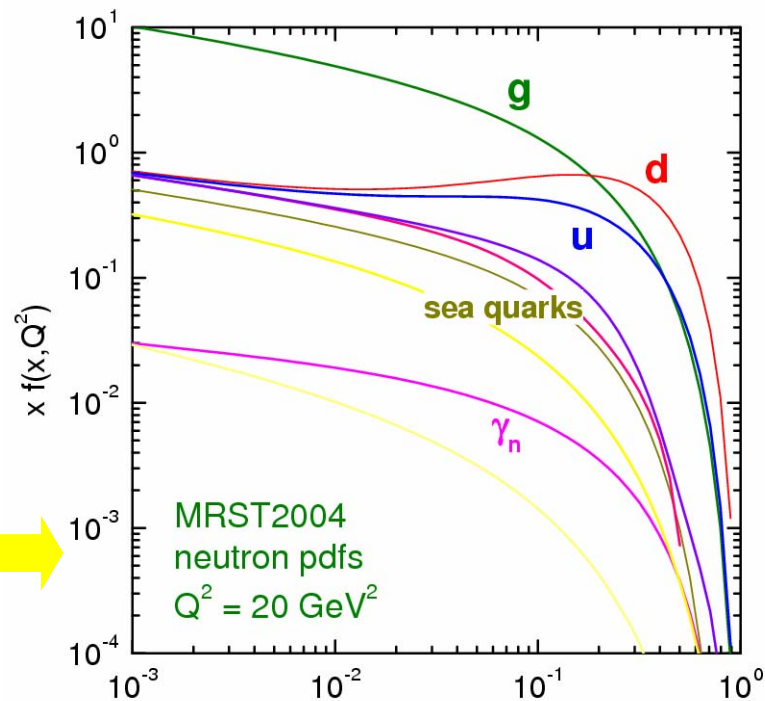
effect on valence quark evolution:



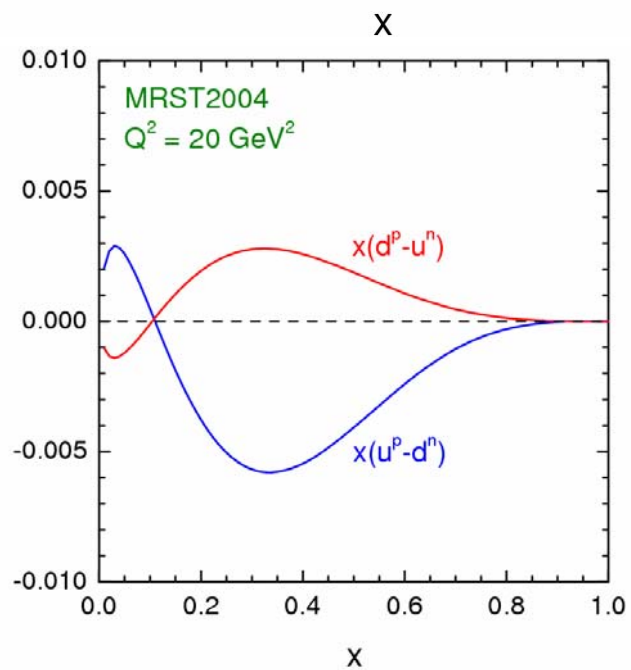
- effect on quark distributions negligible at small x where gluon contribution dominates DGLAP evolution
- at large x , effect only becomes noticeable (order percent) at very large Q^2 , where it is equivalent to a shift in α_s of $\Delta\alpha_s \approx 0.0003$
- dynamic generation of **photon parton distribution**
- isospin violation: $u^p(x) \neq d^n(x)$
- first consistent global pdf fit with QED corrections included (MRST2004QED @ NLO and NNLO QCD)
- QED fit is of very similar quality to standard global fit: improved fit to deuterium data balanced by overall deterioration due to smaller gluon



← proton



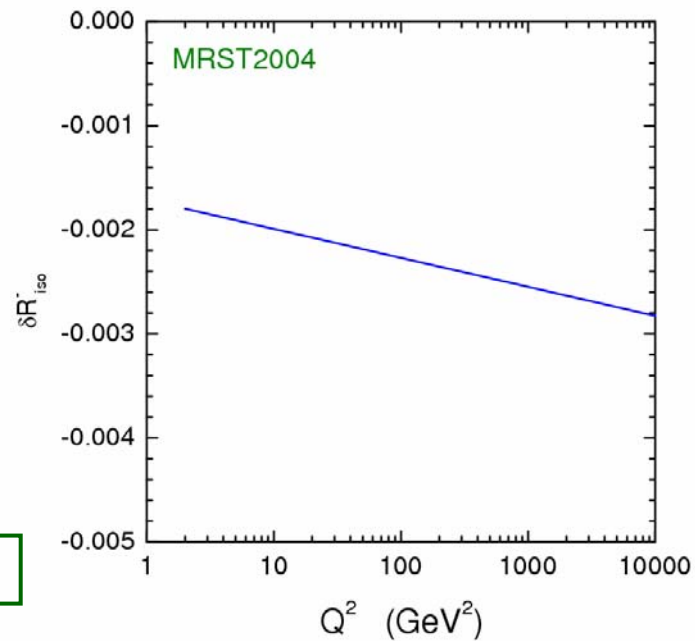
neutron →



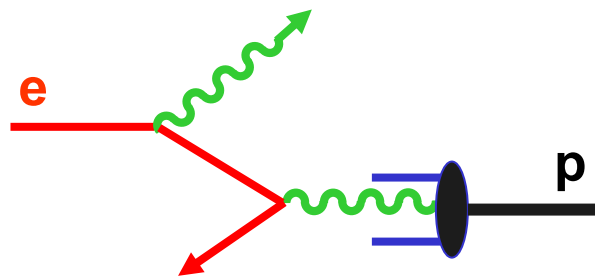
← valence difference

δR_{iso}^- →

MRST2004QED(NLO)



first measurement of $\gamma_p(x, Q^2)$?

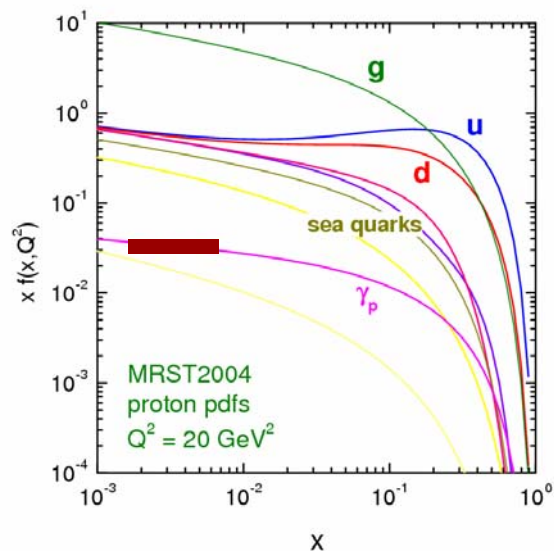


ZEUS: “Observation of high E_T photons in deep inelastic scattering”, hep-ex/0402019

$\sqrt{s} = 318 \text{ GeV}$, $Q^2 > 35 \text{ GeV}^2$, $E_e > 10 \text{ GeV}$

$139.8^\circ < \theta_e < 171.8^\circ$

$5 < E_T^\gamma < 10 \text{ GeV}$, $-0.7 < \eta^\gamma < 0.9$



$\sigma(ep \rightarrow e\gamma X) = 5.64 \pm 0.58 \text{ (stat.)} \pm \begin{matrix} 0.47 \\ 0.72 \end{matrix} \text{ (syst.) pb}$

prediction using MRST2004 QEDpdfs:

$\sigma(ep \rightarrow e\gamma X) = 6.2 \pm 1.2 \text{ pb}$

↑
scale dependence



$\sin^2\theta_W$ from νN

NuTeV (2001): $\sigma^{\nu N, \bar{\nu} N} \Rightarrow \sin^2 \theta_W = 0.2277 \pm 0.0016$

cf. world average: $\sin^2 \theta_W = 0.2227 \pm 0.0004$

\updownarrow 3σ
difference

Paschos-Wolfenstein ratio

$$R^- \equiv \frac{\sigma_{\text{NC}}^\nu - \sigma_{\text{NC}}^{\bar{\nu}}}{\sigma_{\text{CC}}^\nu - \sigma_{\text{CC}}^{\bar{\nu}}} \simeq \frac{1}{2} - \sin^2 \theta_W + \delta R_{\text{A}}^- + \delta R_{\text{EW}}^- + \delta R_{\text{NLO}}^- + \delta R_{\text{s}}^- + \delta R_{\text{iso}}^-$$

Global fit: $\delta R_{\text{iso}}^- = -0.002$

Lagrange Multiplier method: $-0.007 < \delta R_{\text{iso}}^- < +0.007$ at 90%cl

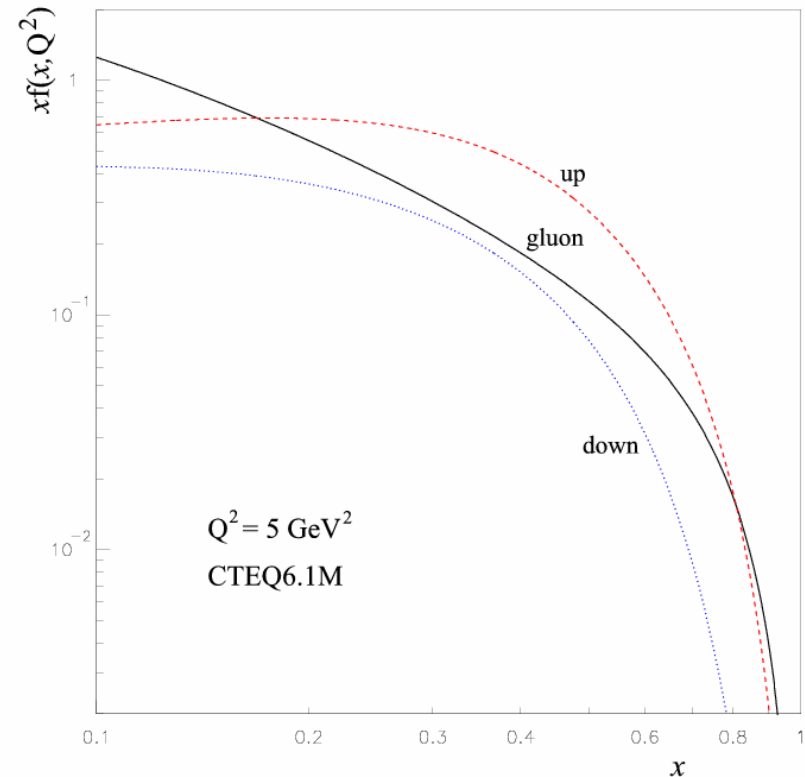
(MRST, hep-ph/0308087)

a new look at the high-x gluon distribution

- good fit to Tevatron high E_T jet data requires 'hard' gluon distribution
- **MRST** use traditional parametrisation $Ax^a(1-x)^n[1+b\sqrt{x}+cx]$, not quite as good a fit as **CTEQ**; note that $n_g = 2.98$ for the MSbar NLO global fit
- but recall dimensional counting arguments for $x \rightarrow 1$ behaviour of parton distributions

$$q_{val} \sim (1-x)^3, \quad g(x) \sim (1-x)^5$$

(but in what factorisation scheme, and at what Q^2 scale?)



the DIS-scheme gluon distribution

- Kramer and Klasen (1996) noticed that it was easier to get a good fit to the Tevatron high E_T jet data in the DIS scheme, schematically:

$$q^{\text{DIS}} = q^{\overline{\text{MS}}} + C_{2,q}^{\overline{\text{MS}}} \otimes q^{\overline{\text{MS}}} + C_{2,g}^{\overline{\text{MS}}} \otimes g^{\overline{\text{MS}}},$$

$$g^{\text{DIS}} = g^{\overline{\text{MS}}} - C_{2,q}^{\overline{\text{MS}}} \otimes q^{\overline{\text{MS}}} - \cancel{C_{2,g}^{\overline{\text{MS}}} \otimes g^{\overline{\text{MS}}}}. \quad \text{this term negligible}$$

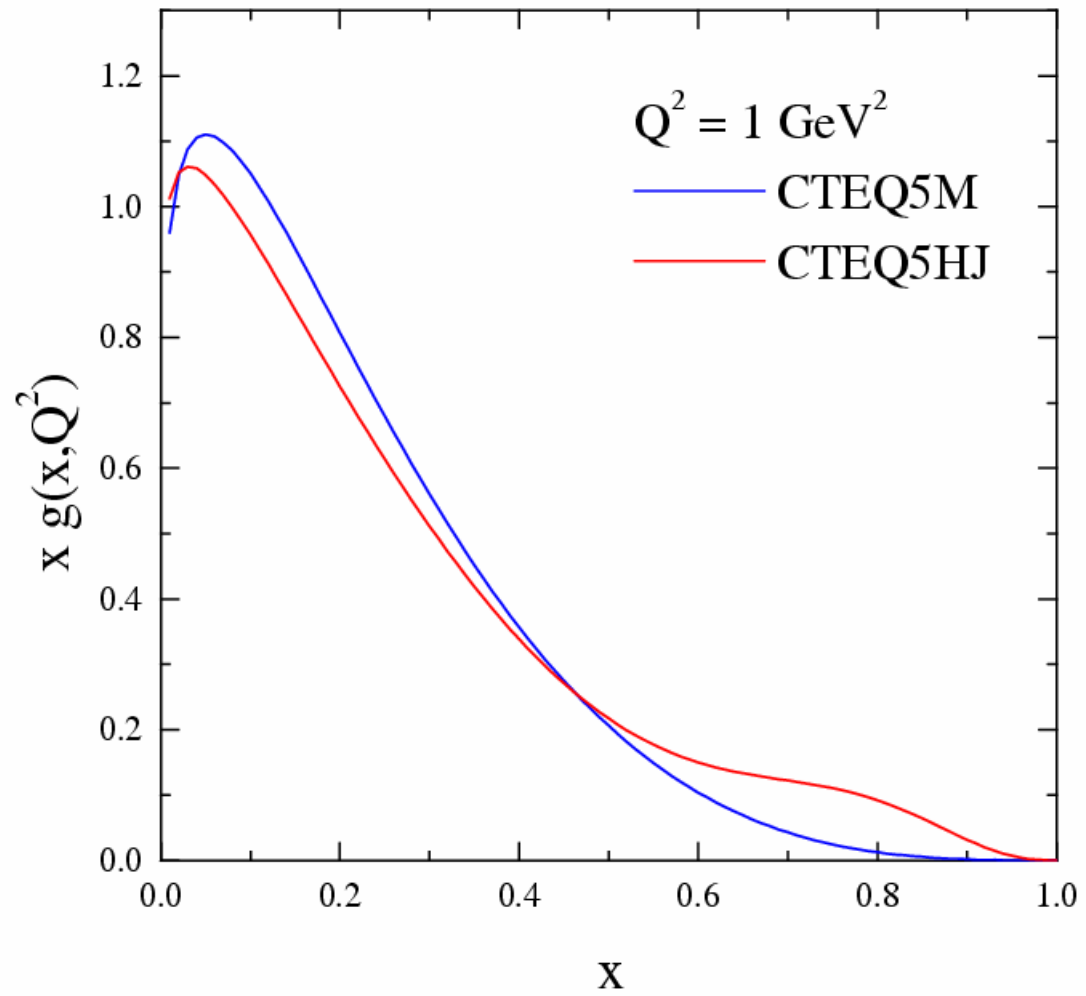
so that the DIS quarks (gluons) are harder (softer) at large x . (In fact the **MRST** g^{DIS} obtained from the above is negative at large x)

- Therefore, suppose we write

$$g^{\overline{\text{MS}}}(x, Q_0^2) = g^{\text{DIS}}(x, Q_0^2) + C_{2,\text{NS}}^{\overline{\text{MS}}} \otimes \sum_{q=u,d} q_{\text{val}}^{\overline{\text{MS}}}(x, Q_0^2),$$

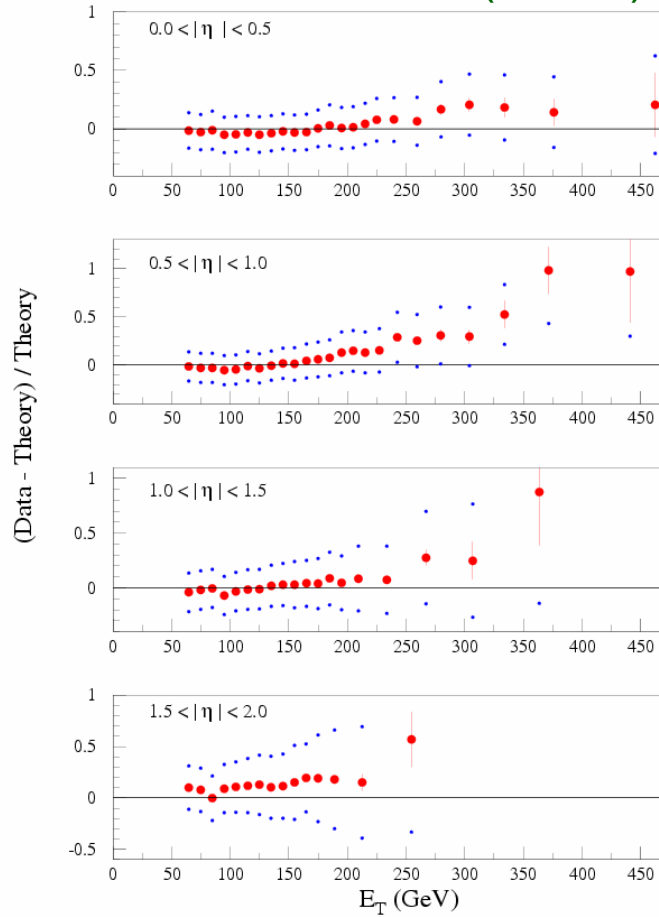
and use the canonical parametrisation for g^{DIS} (**Note: no new parameters!**)

- If g^{DIS} satisfies usual dimensional counting, then $g^{\overline{\text{MS}}}$ dominated by the second term, and will have non-trivial high- x structure as a result.

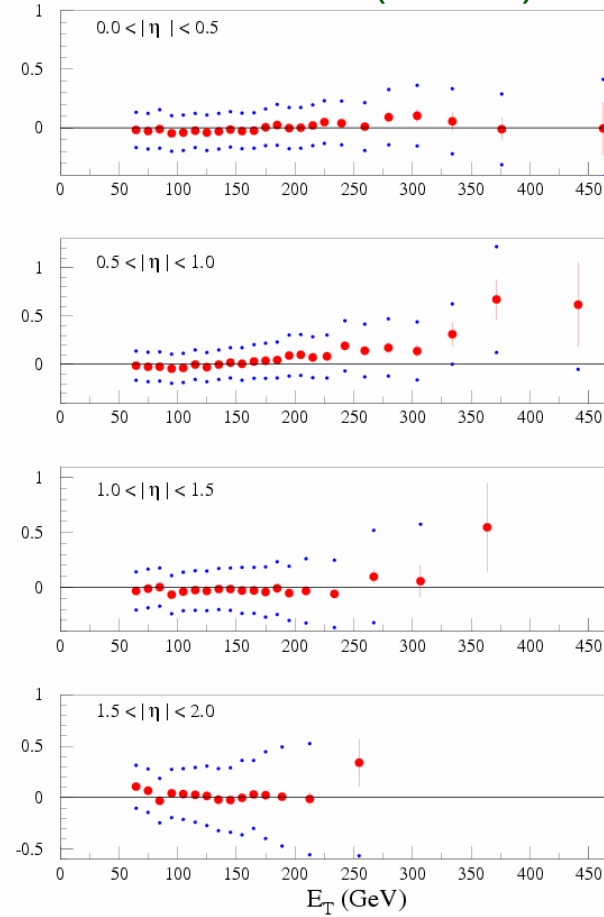


DZero
Run 1b
jet data

MRST2003(NNLO)



new (NNLO) fit



jet data only:
global fit:

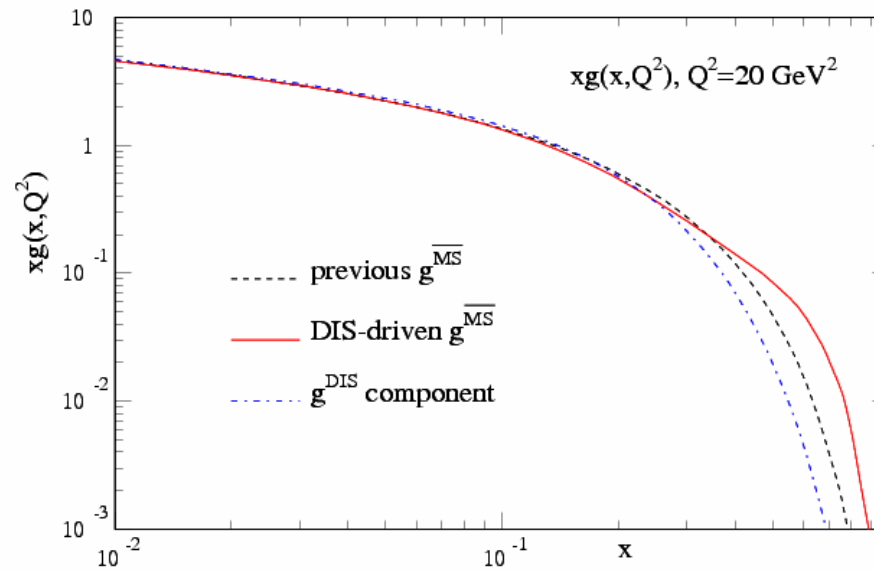
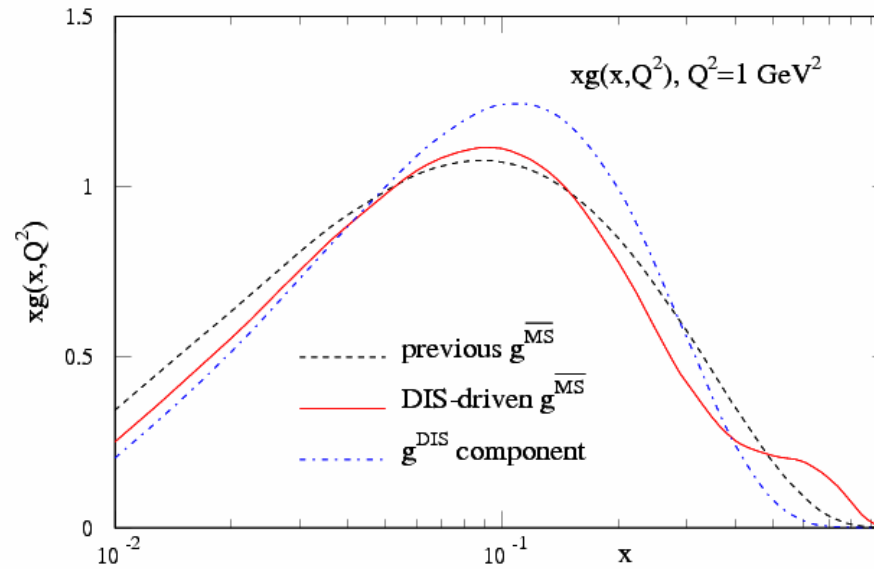
$$\chi^2 = 164 \rightarrow 117$$

$$\Delta\chi^2 = -79$$

same number of
parameters as before

... and now $n_g = 4.5$

sensitivity to x , Q^2 cuts reduced
but not eliminated – see next talk



MRST2004(NNLO)

summary

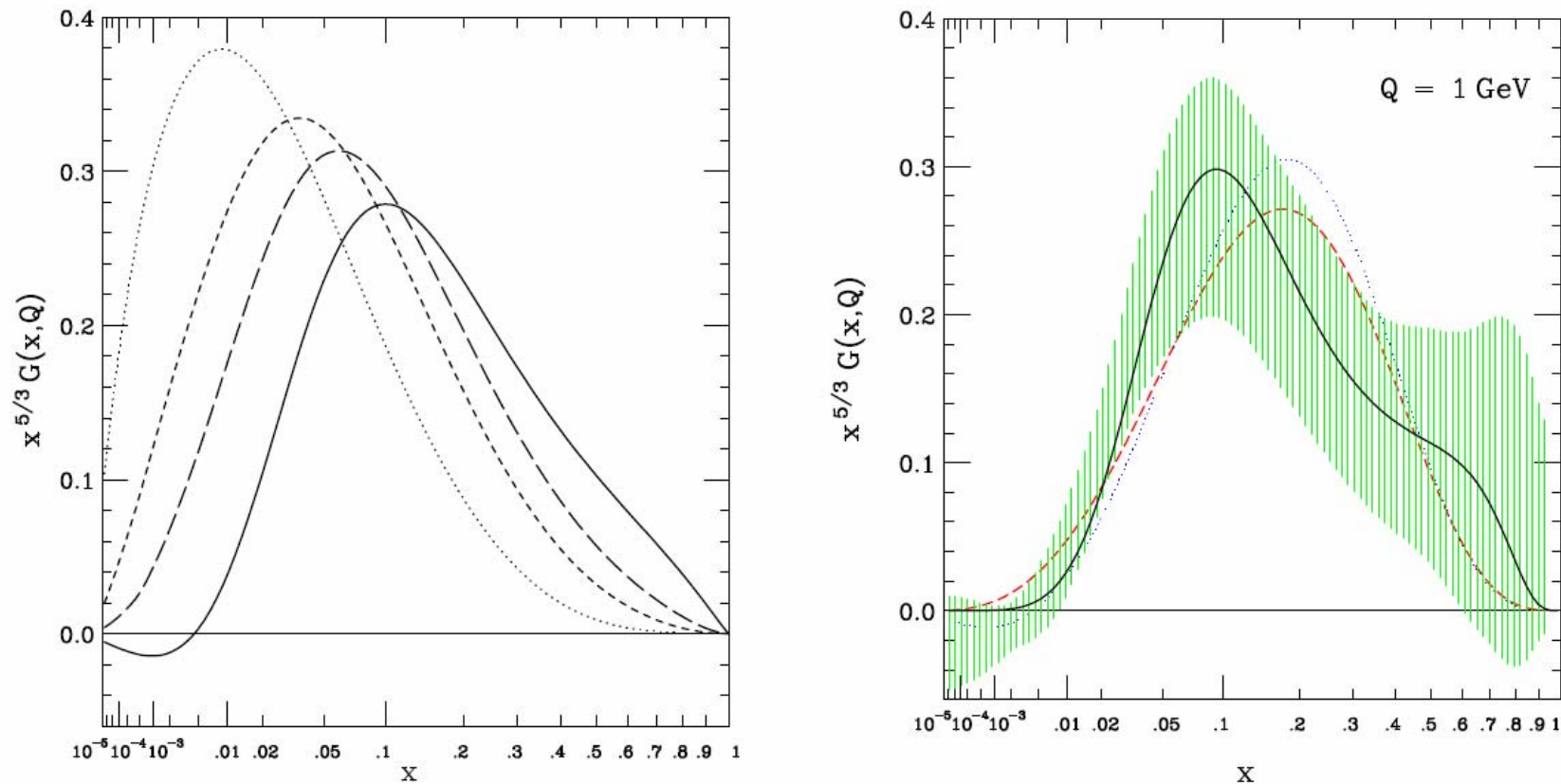
- pdf sets with $O(\alpha)$ QED effects are now available and allow pEW corrections at hadron colliders to be consistently included
- isospin violation arises naturally and reduces the NuTeV $\sin^2\theta_W$ 'anomaly'
- the structure in the *high-x* $\overline{\text{MS}}$ gluon distribution is explained as an artefact of the unphysical factorisation scheme
- dimensional counting behaviour is obtained in the DIS scheme at $Q^2 \sim 1 \text{ GeV}^2$
- at the very least, an efficient and well-motivated way of parametrising the starting gluon distribution

extra slides

the President tells me he doesn't allow negative gluons over there

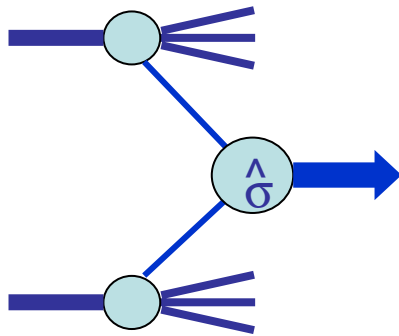


Fig. 24 : (a) The gluon distribution at $Q = 1, 2, 5, 100$ GeV obtained from a global fit in our parametrization, but allowing for negative gluon at small- x ; and (b) Gluon uncertainty band at $Q = 1$ GeV, covering both $+$ and $-$ regions. Dashed:CTEQ5, dotted:MRST2001.



precision QCD at hadron colliders

the QCD **factorization theorem** for hard-scattering (short-distance) inclusive processes:



$$\sigma_X = \sum_{a,b} \int_0^1 dx_1 dx_2 f_a(x_1, \mu_F^2) f_b(x_2, \mu_F^2) \times \hat{\sigma}_{ab \rightarrow X} \left(x_1, x_2, \{p_i^\mu\}; \alpha_S(\mu_R^2), \alpha(\mu_R^2), \frac{Q^2}{\mu_R^2}, \frac{Q^2}{\mu_F^2} \right)$$

where $X=W, Z, H, \text{high-}E_T \text{ jets, SUSY sparticles, ...}$ and Q is the ‘hard scale’ (e.g. $= M_X$), usually $\mu_F = \mu_R = Q$, and $\hat{\sigma}$ is known to some fixed order in pQCD and pEW (or to all orders in some LL approximation)

what limits the precision?

- the order of the perturbative expansion
- the uncertainty in the input parton distribution functions

example $\sigma(Z)$ @ LHC

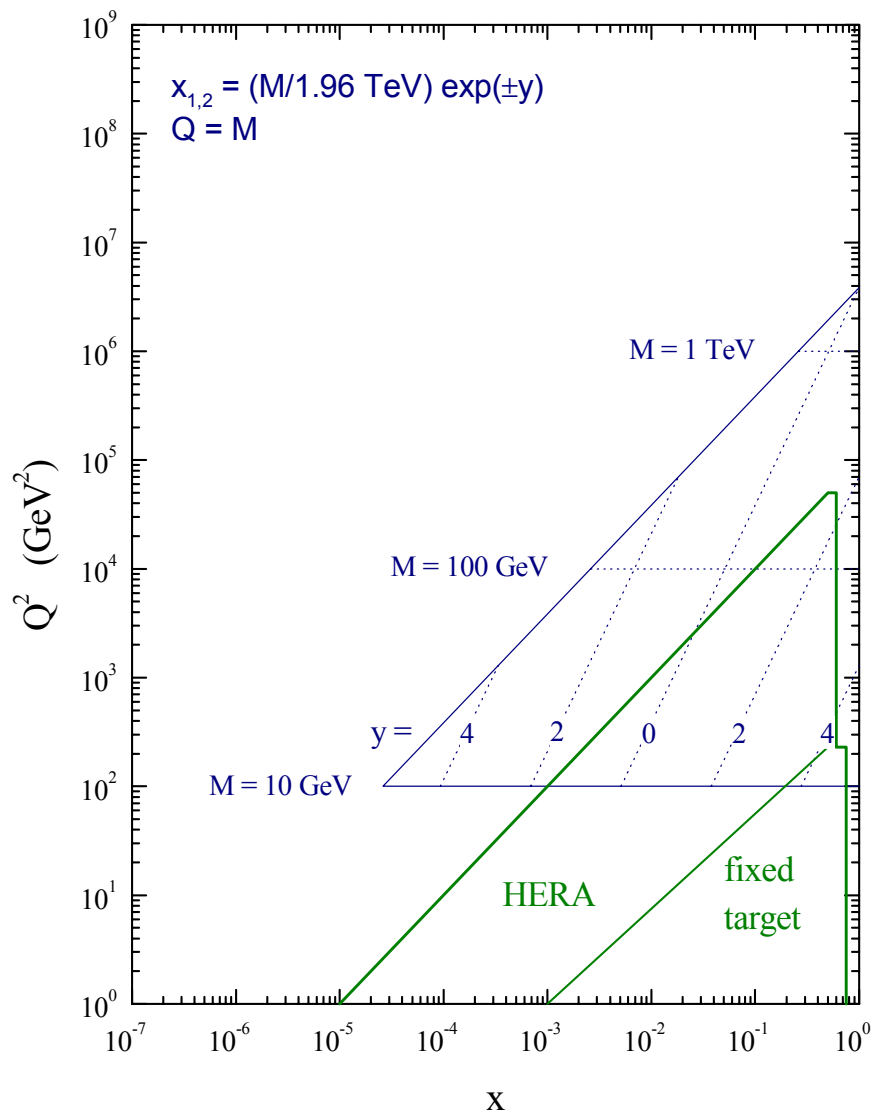
$$\delta\sigma_{\text{pdf}} \approx \pm 3\%, \quad \delta\sigma_{\text{pt}} \approx \pm 2\%$$

$$\rightarrow \delta\sigma_{\text{theory}} \approx \pm 4\%$$

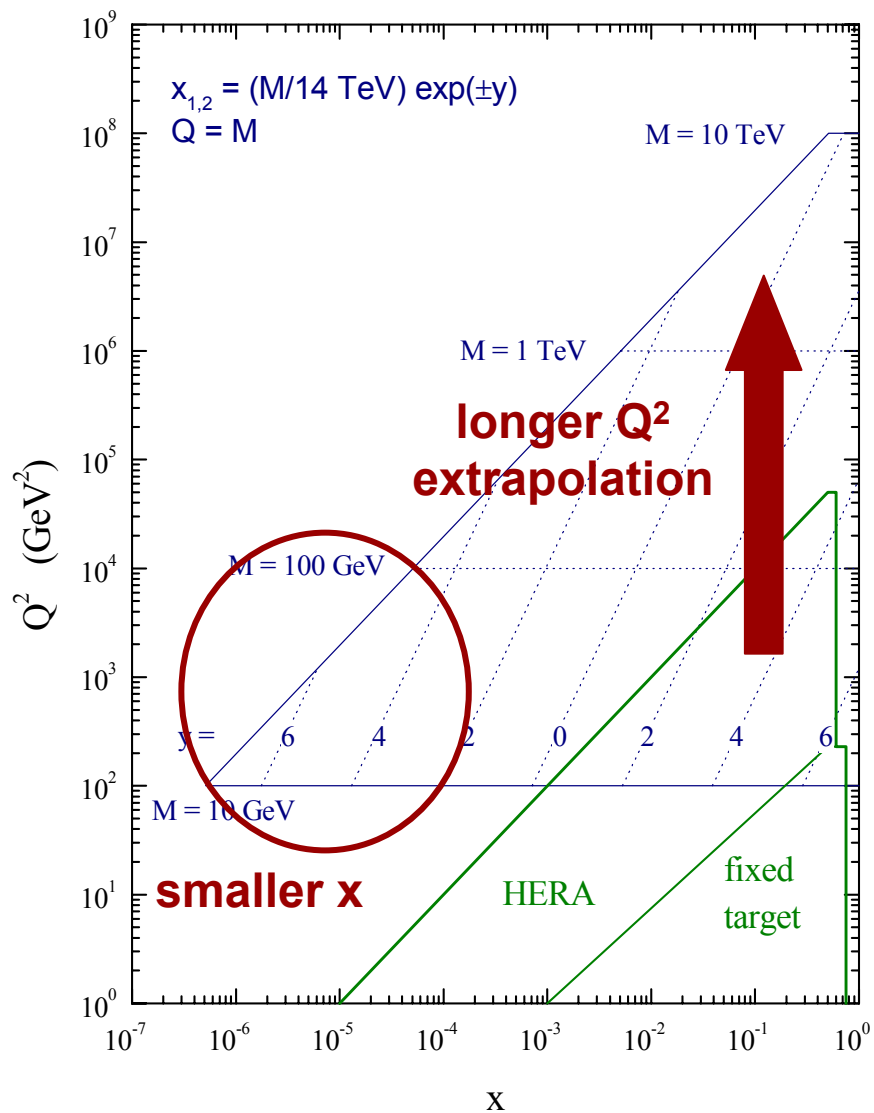
whereas for $gg \rightarrow H$:

$$\delta\sigma_{\text{pdf}} \ll \delta\sigma_{\text{pt}}$$

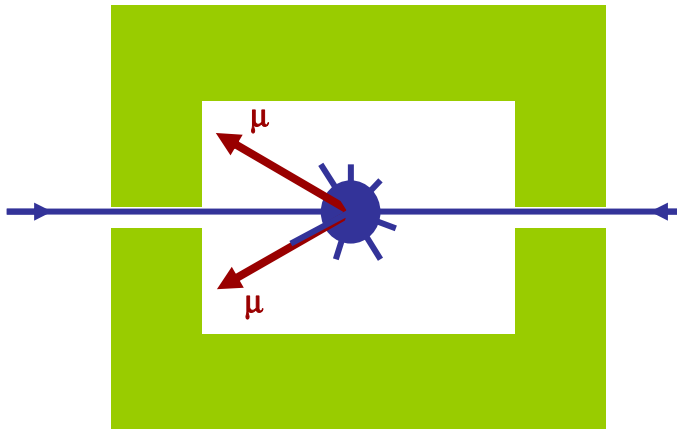
Tevatron parton kinematics



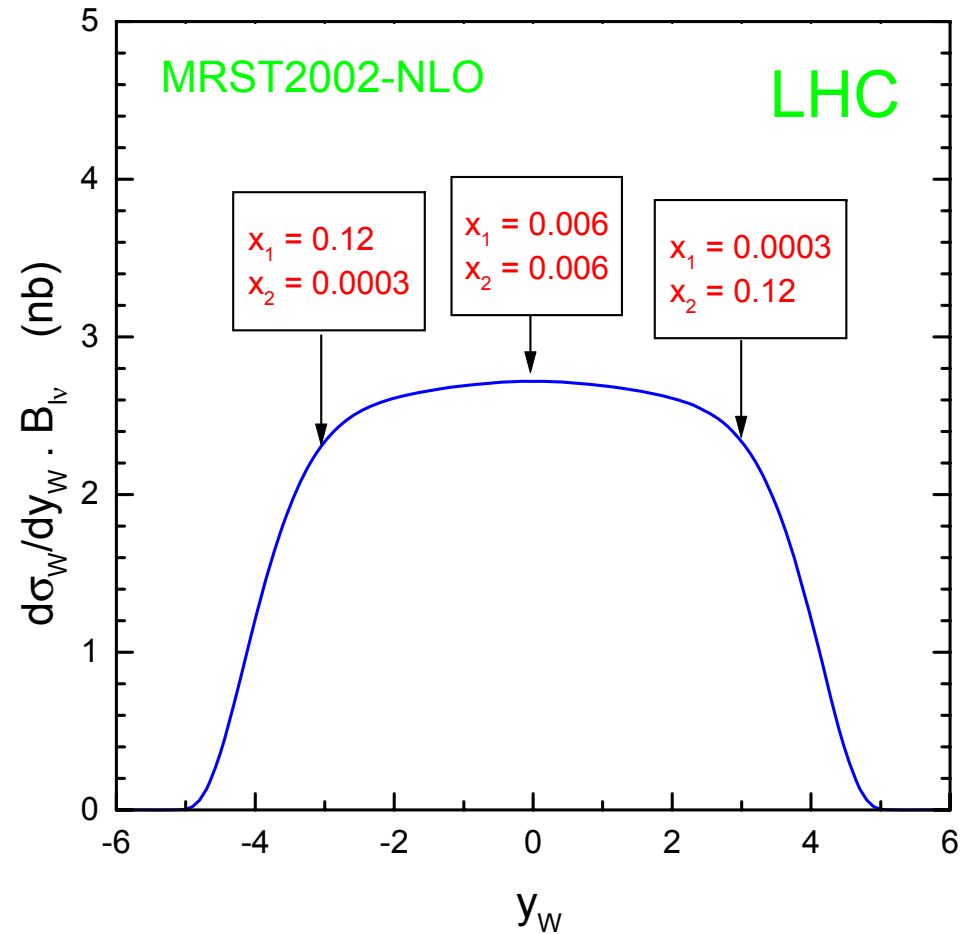
LHC parton kinematics



forward W, Z, dijet... production at LHC samples small and high x

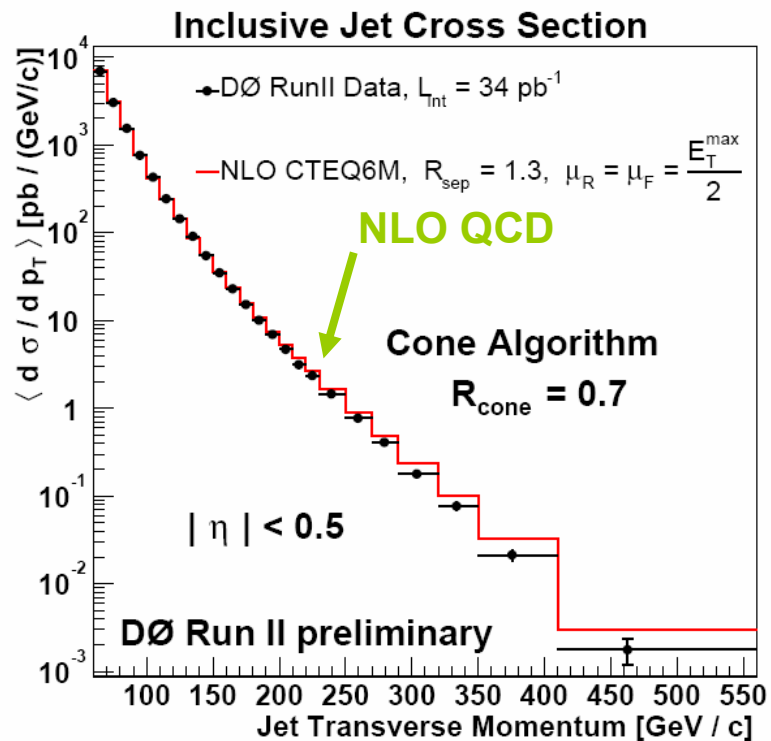


but no acceptance,
no triggers?!

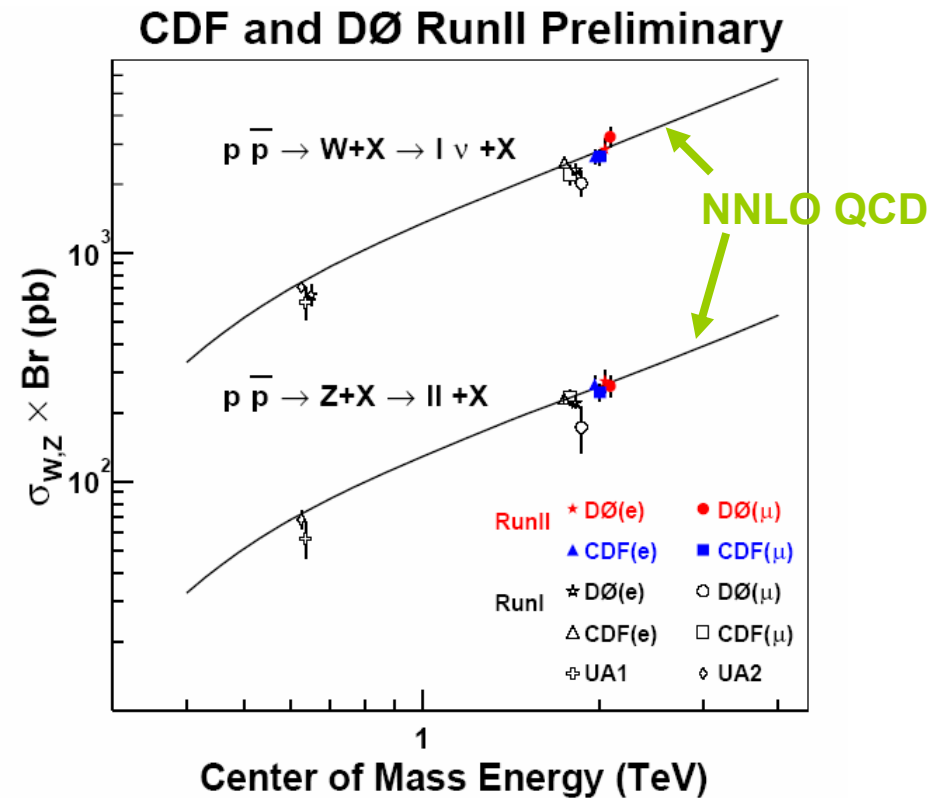


examples of 'precision' phenomenology

jet production



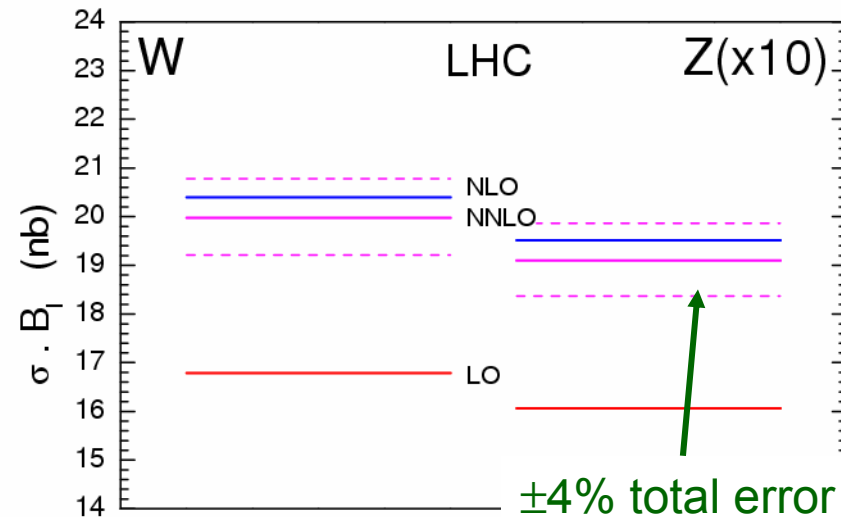
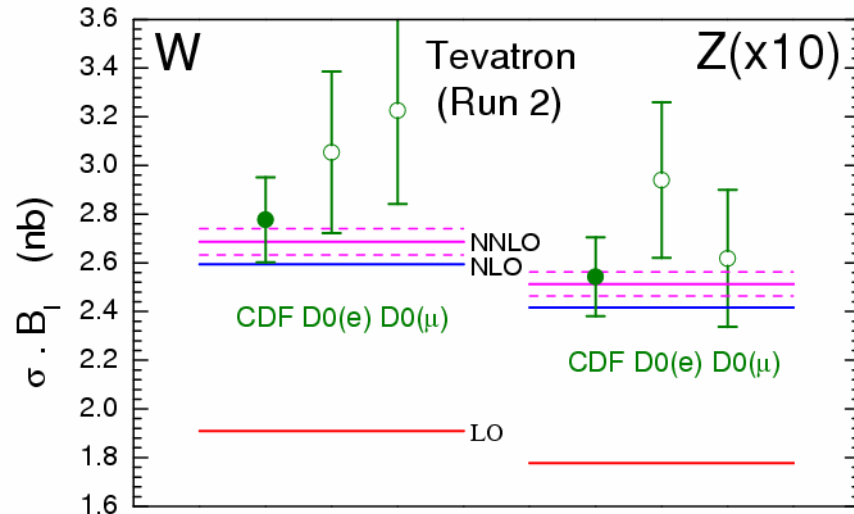
W, Z production



$\sigma(W)$ and $\sigma(Z)$: precision predictions and measurements at the Tevatron and LHC



- the pQCD series appears to be under control
- the EW corrections are known and can in principle be included (see below)
- with sufficient theoretical precision, these ‘standard candle’ processes can be used to measure *machine luminosity*



partons: MRST2002
 NNLO evolution: Moch, Vermaseren, Vogt
 NNLO W,Z corrections: van Neerven et al. with Harlander, Kilgore corrections

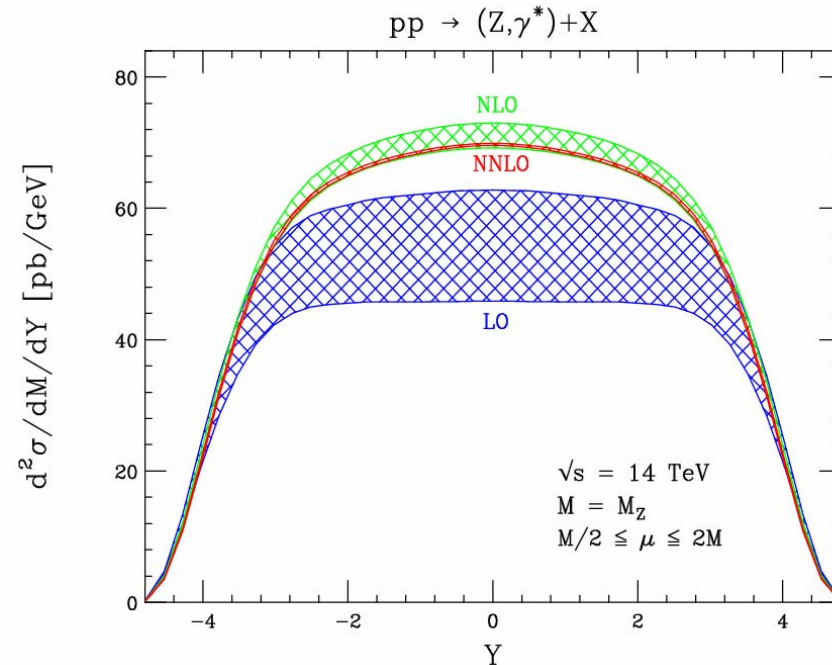
the rapidity distributions $d\sigma/dy$ are also known to NNLO \Rightarrow matching to experimental acceptance



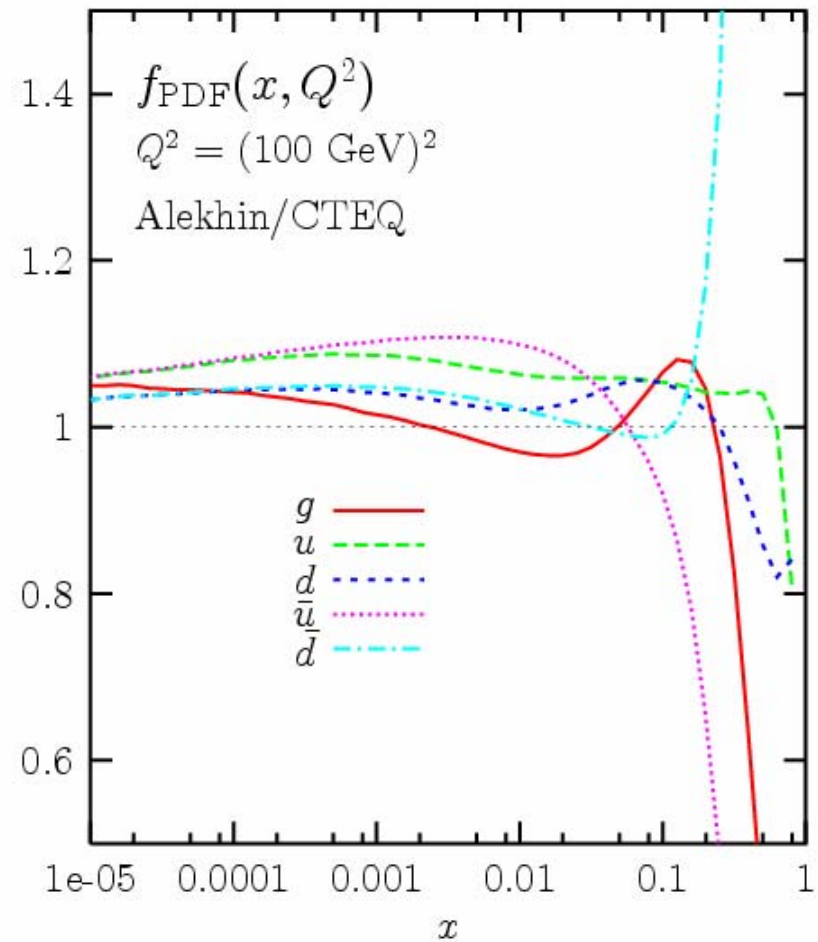
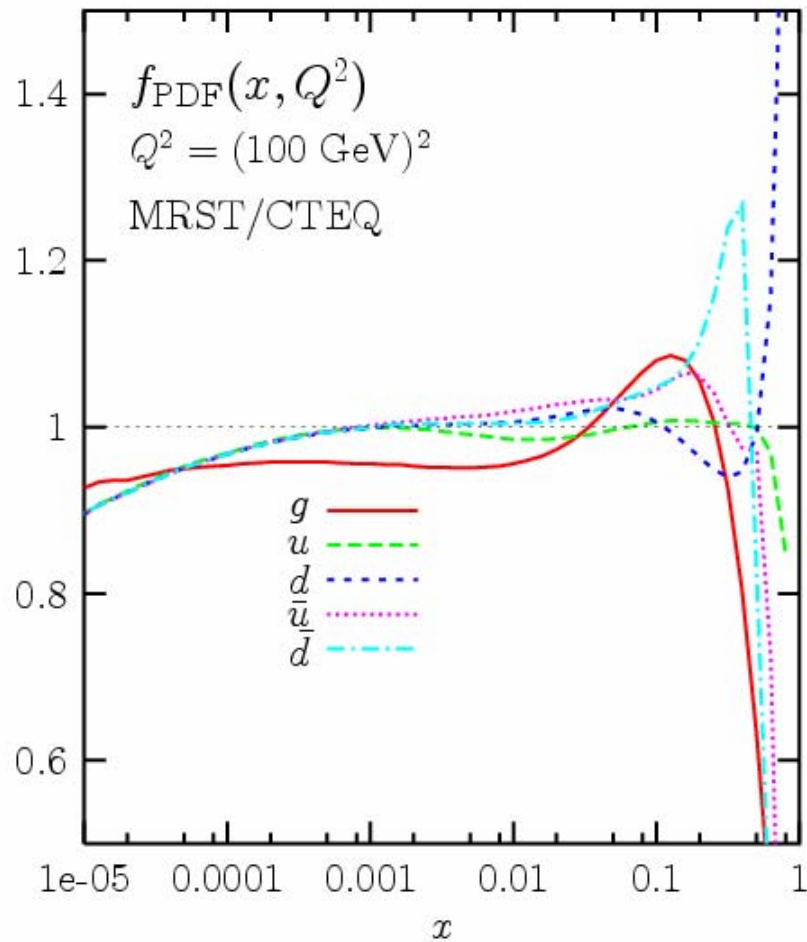
however...

LHC	$\sigma_{\text{NNLO}}(W)$ (nb)
MRST2002	204 ± 6 (expt)
CTEQ6	205 ± 8 (expt)
Alekhin02	215 ± 6 (tot)

similar partons
different partons
different $\Delta\chi^2$



Anastasiou et al.
[hep-ph/0306192](https://arxiv.org/abs/hep-ph/0306192)
[hep-ph/0312266](https://arxiv.org/abs/hep-ph/0312266)



the differences between pdf sets needs to be better understood!

Djouadi & Ferrag, hep-ph/0310209

why do 'best fit' pdfs and errors differ?

- different data sets in fit
 - different subselection of data
 - different treatment of exp. sys. errors
 - different choice of
 - tolerance to define $\pm \delta f_i$ (CTEQ: $\Delta\chi^2=100$, Alekhin: $\Delta\chi^2=1$)
 - factorisation/renormalisation scheme/scale
 - Q_0^2
 - parametric form $Ax^a(1-x)^b[..]$ etc
 - α_s
 - treatment of heavy flavours
 - theoretical assumptions about $x \rightarrow 0, 1$ behaviour
 - theoretical assumptions about sea flavour symmetry
 - evolution and cross section codes (removable differences!)
- see ongoing HERA-LHC Workshop PDF Working Group

- small **MRST** and **CTEQ** differences largely understood, see hep-ph/0211080

mainly: CTEQ gluon at Q_0^2 required to be positive at small x means $g_{\text{CTEQ}} > g_{\text{MRST}}$ there, also $\Delta\chi^2 = 50$ (MRST), 100 (CTEQ)

- **ALEKHIN** gluon smaller at high x (no Tevatron jet data in fit) and different content of sea at small x from different assumptions about *ubar-dbar* as $x \rightarrow 0$ and (ii) ratio of strange to non-strange pdfs. Also $\Delta\chi^2 = 1$ allowed by use of smaller overall data set.

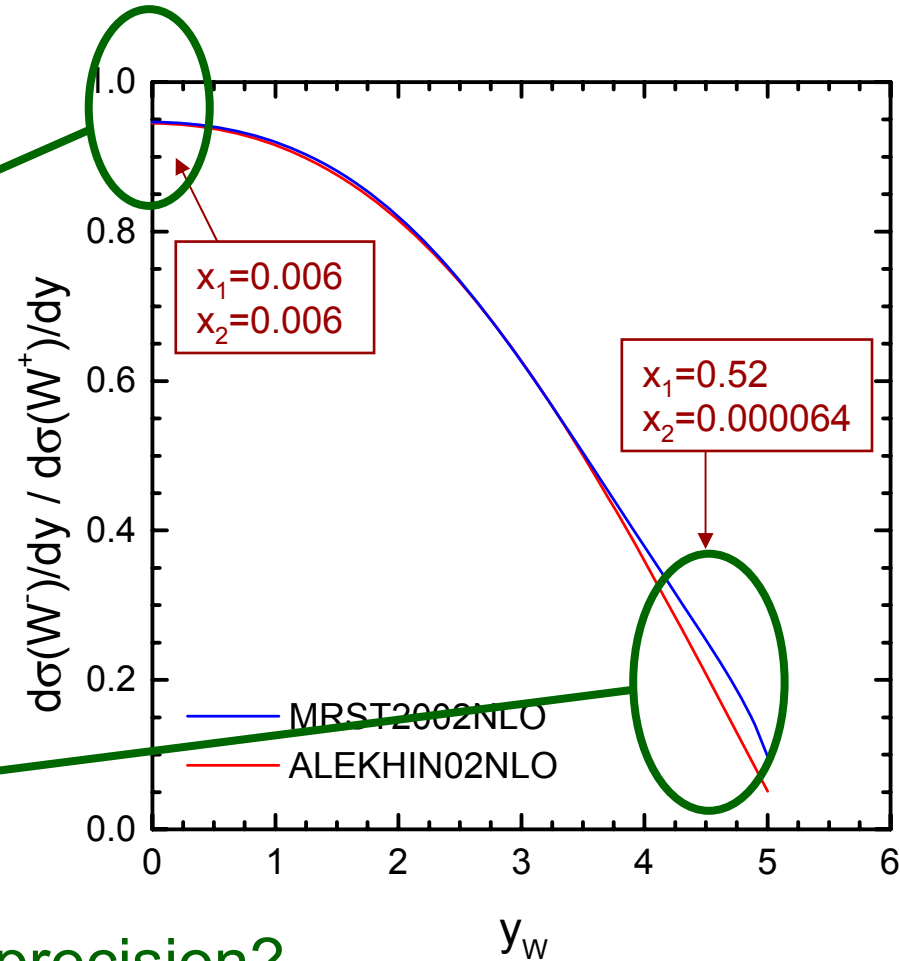
ratio of W^- and W^+ rapidity distributions

$$\frac{d\sigma(W^-)}{d\sigma(W^+)} = \frac{d(x_1) \bar{u}(x_2) + \bar{u}(x_1) d(x_2) + \dots}{u(x_1) \bar{d}(x_2) + \bar{d}(x_1) u(x_2) + \dots}$$

ratio close to 1 because $u \approx \bar{u}$ etc.
 (note: MRST error = $\pm 1\frac{1}{2}\%$)

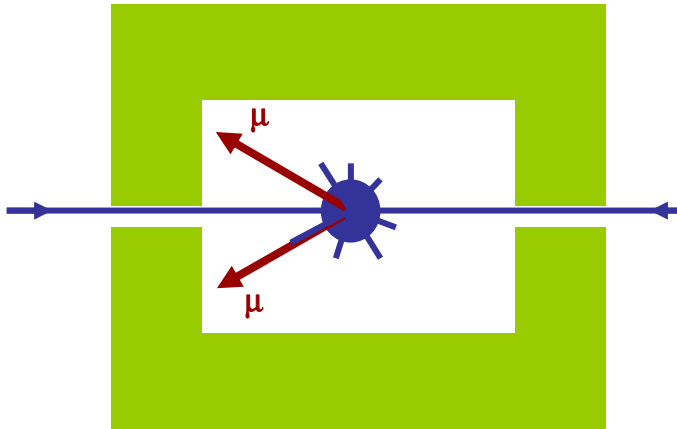
LHC	W^-/W^+
MRST2002	0.75
CTEQ6	0.75
Alekhin02	0.74

sensitive to large-x d/u
 and small x \bar{u}/\bar{d} ratios

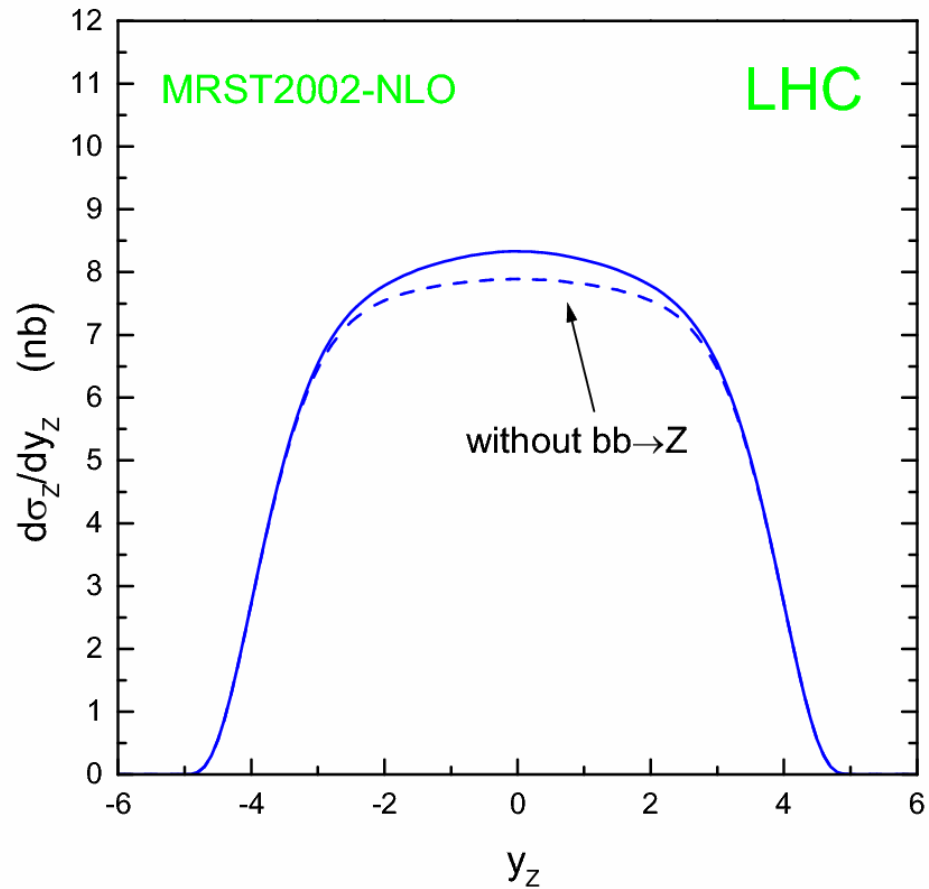


Q. What is the experimental precision?

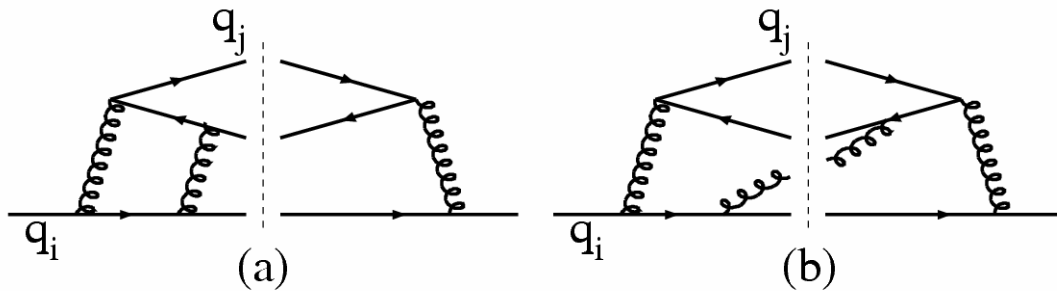
$bb \rightarrow Z$ contribution to Z production @ LHC



Note: much smaller effect at Tevatron



perturbative generation of $s(x) \neq \bar{s}(x)$



➔

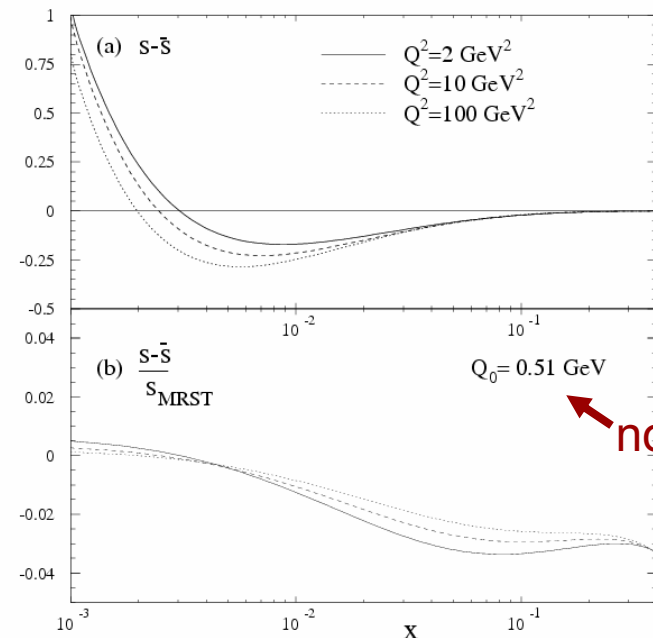
$P^{us}(x) \neq P^{\bar{u}s}(x)$
at $O(\alpha_s^3)$

Quantitative study by de Florian et al
[hep-ph/0404240](https://arxiv.org/abs/hep-ph/0404240)

⇒ $\langle x(s-\bar{s}) \rangle_{\text{pQCD}} \lesssim -0.0005$

cf. from global pdf fit
 (Olness et al, [hep-ph/0312322,3](https://arxiv.org/abs/hep-ph/0312322))

⇒ $-0.001 < \langle x(s-\bar{s}) \rangle_{\text{fit}} < +0.004$



note!



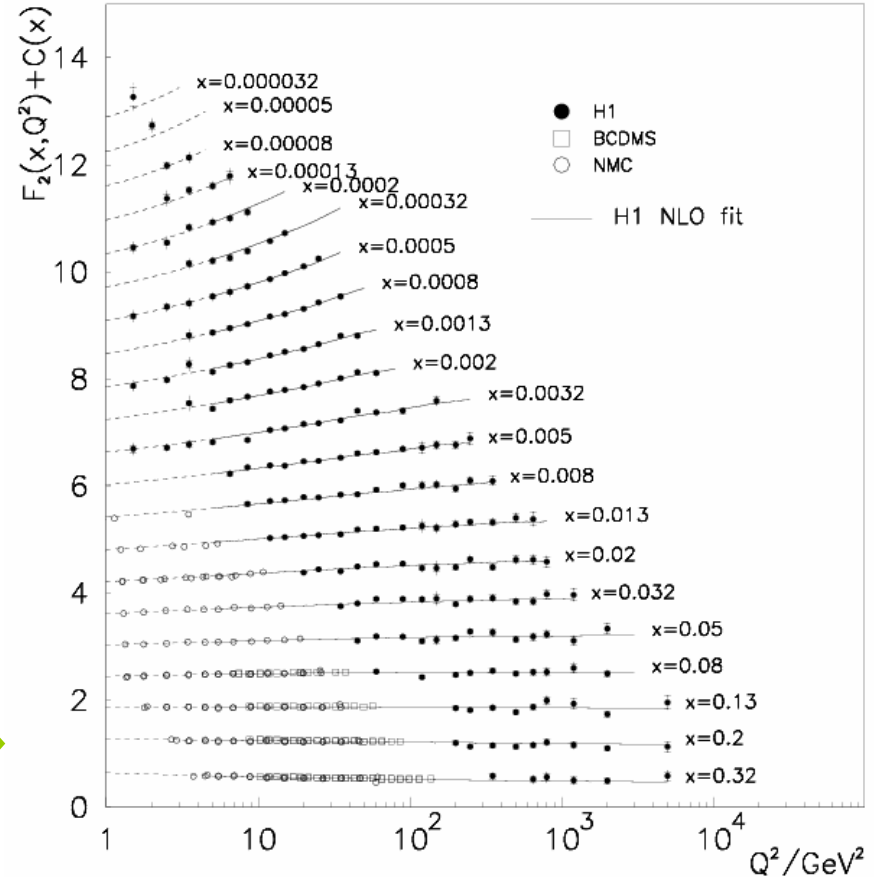
$$\frac{\partial q_i(x, Q^2)}{\partial \log Q^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{q_i q_j}(y, \alpha_S) q_j\left(\frac{x}{y}, Q^2\right) + P_{q_i g}(y, \alpha_S) g\left(\frac{x}{y}, Q^2\right) \right\}$$

$$\frac{\partial g(x, Q^2)}{\partial \log Q^2} = \frac{\alpha_S}{2\pi} \int_x^1 \frac{dy}{y} \left\{ P_{g q_j}(y, \alpha_S) q_j\left(\frac{x}{y}, Q^2\right) + P_{g g}(y, \alpha_S) g\left(\frac{x}{y}, Q^2\right) \right\}$$

DGLAP equations

$$F_2(x, Q^2) = \sum_q e_q^2 x q(x, Q^2) \text{ etc}$$

x dependence of $f_i(x, Q^2)$ determined by 'global fit' to deep inelastic scattering (H1, ZEUS, NMC, ...) and hadron collider data



pdfs from global fits

Formalism

NLO DGLAP
MSbar factorisation
 Q_0^2
functional form @ Q_0^2
sea quark (a)symmetry
etc.

Data

DIS (SLAC, BCDMS, NMC, E665,
CCFR, H1, ZEUS, ...)
Drell-Yan (E605, E772, E866, ...)
High E_T jets (CDF, D0)
W rapidity asymmetry (CDF)
vN dimuon (CCFR, NuTeV)
etc.

$$f_i(x, Q^2) \pm \delta f_i(x, Q^2)$$

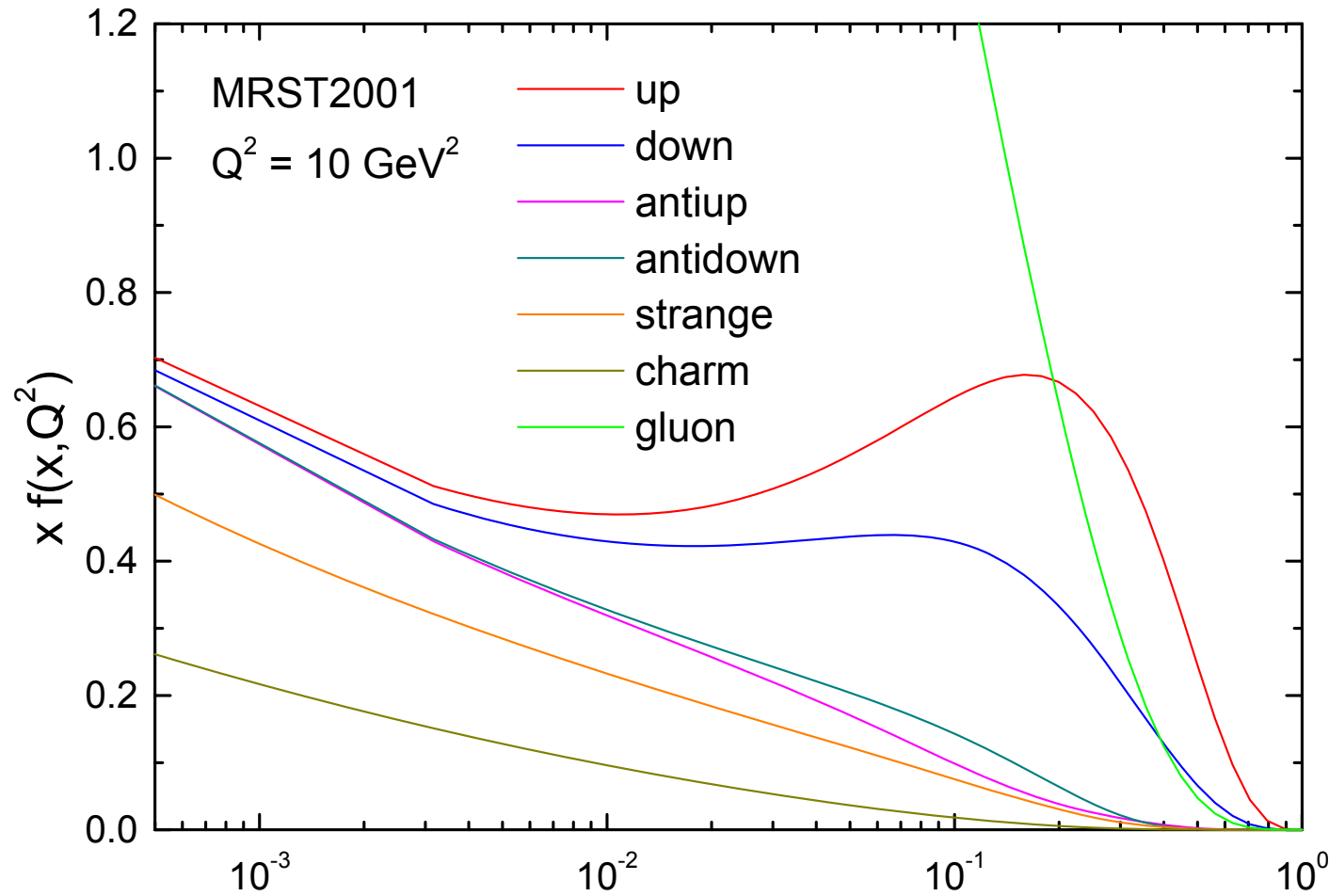
$$\alpha_s(M_Z)$$

Who?

Alekhin, CTEQ, MRST,
GKK, Botje, H1, ZEUS,
GRV, BFP, ...

<http://durpdg.dur.ac.uk/hepdata/pdf.html>

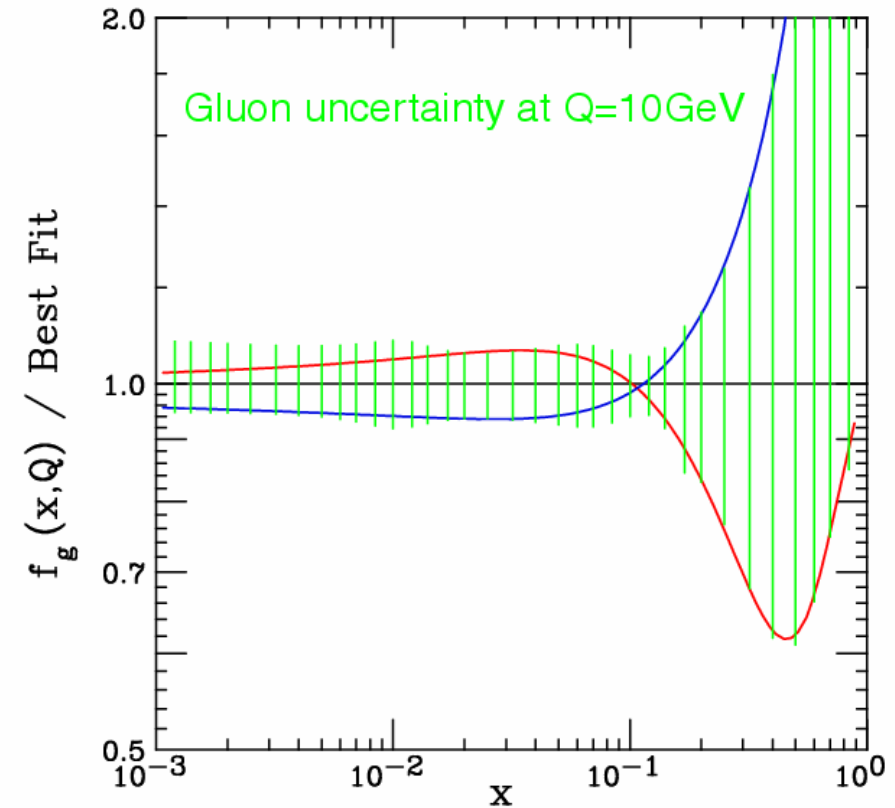
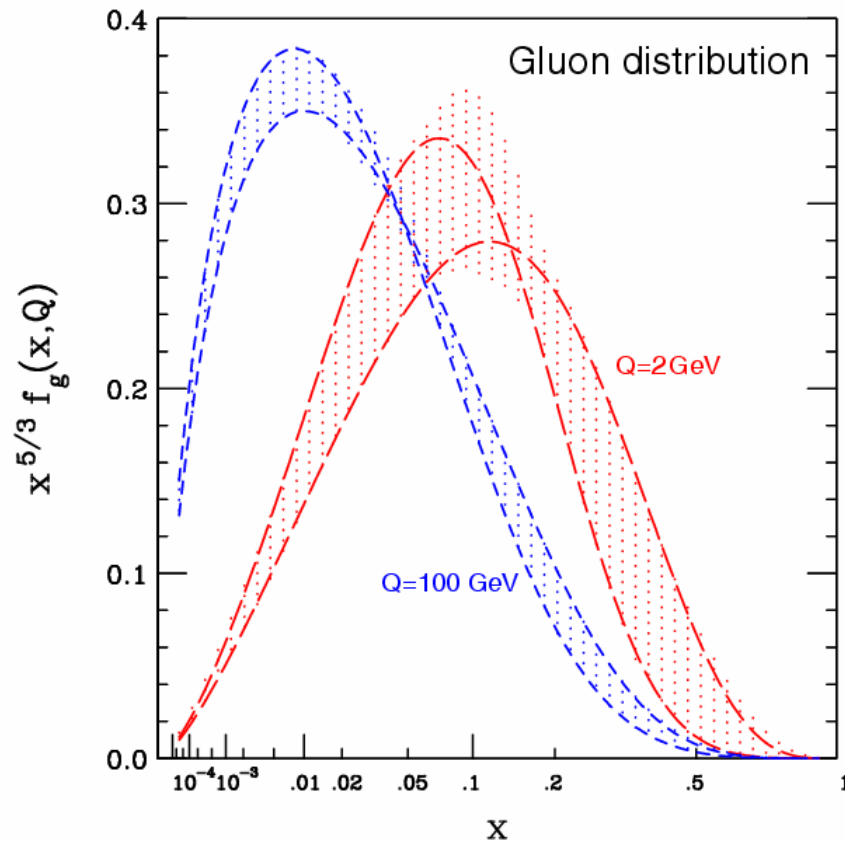
(MRST) parton distributions in the proton



Martin, Roberts, S, Thorne



uncertainty in gluon distribution (CTEQ)



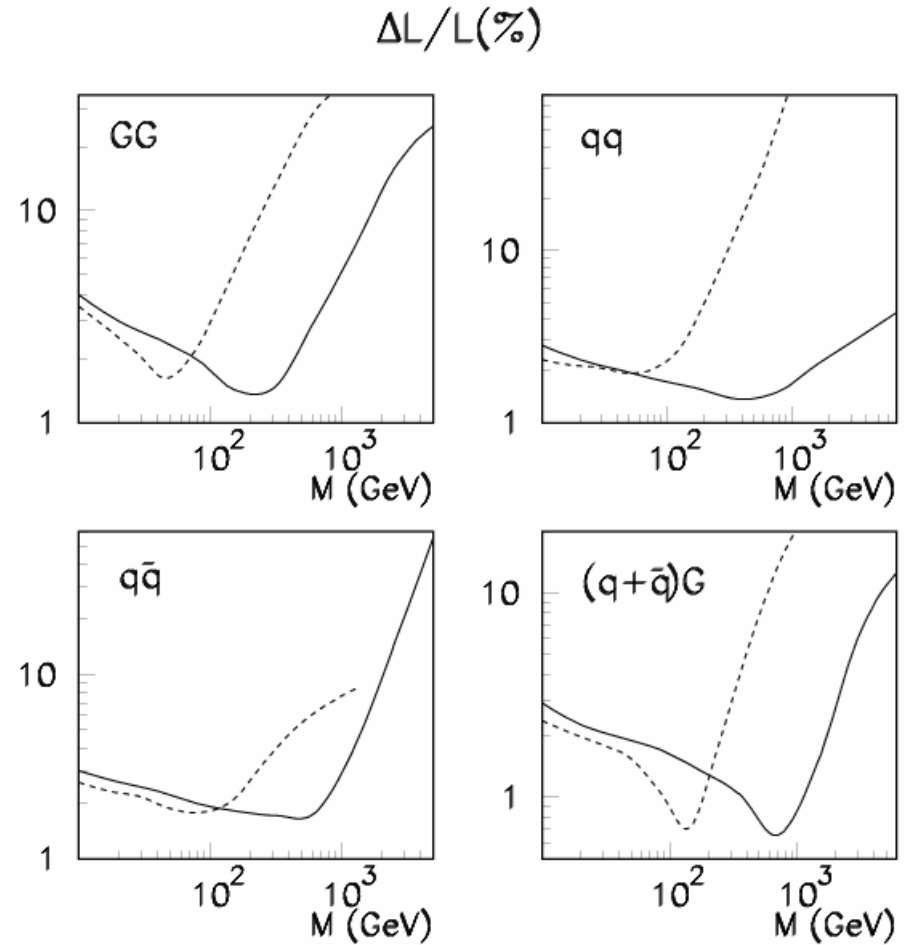
then $\delta f_g \rightarrow \delta \sigma_{gg \rightarrow X}$ etc.

pdf uncertainties
 encoded in parton-parton
luminosity functions:

$$\frac{\partial \mathcal{L}_{ab}}{\partial \tau} = \int_{\tau}^1 \frac{dx}{x} f_a(x, Q^2) f_b(\tau/x, Q^2)$$

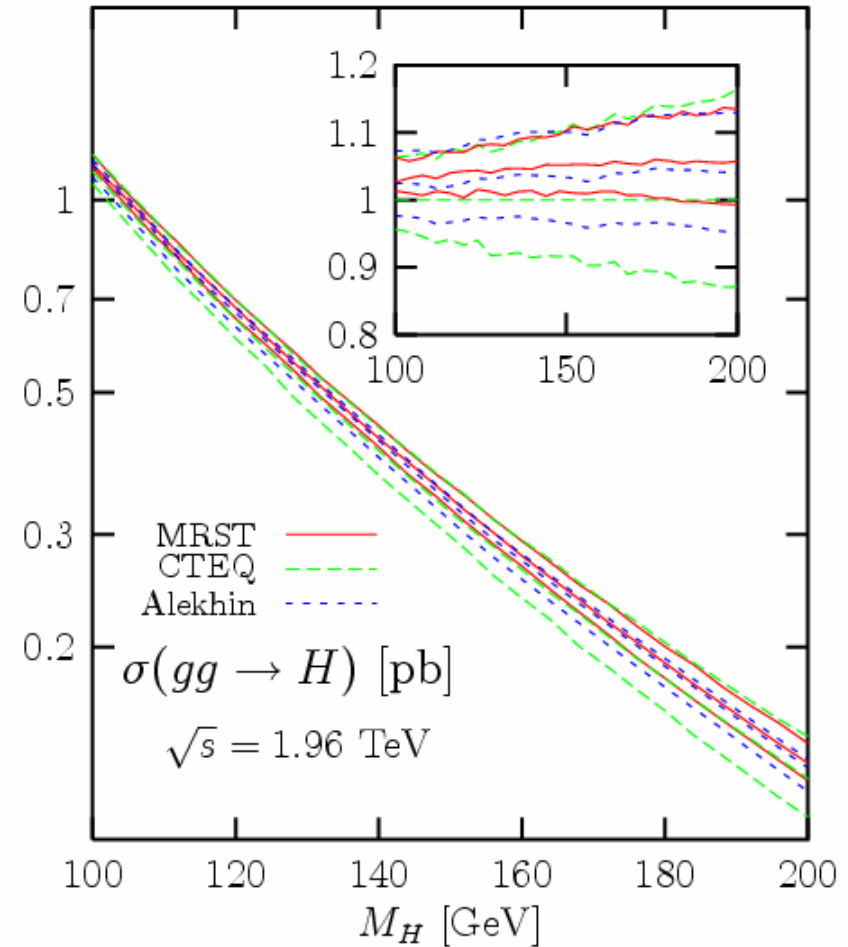
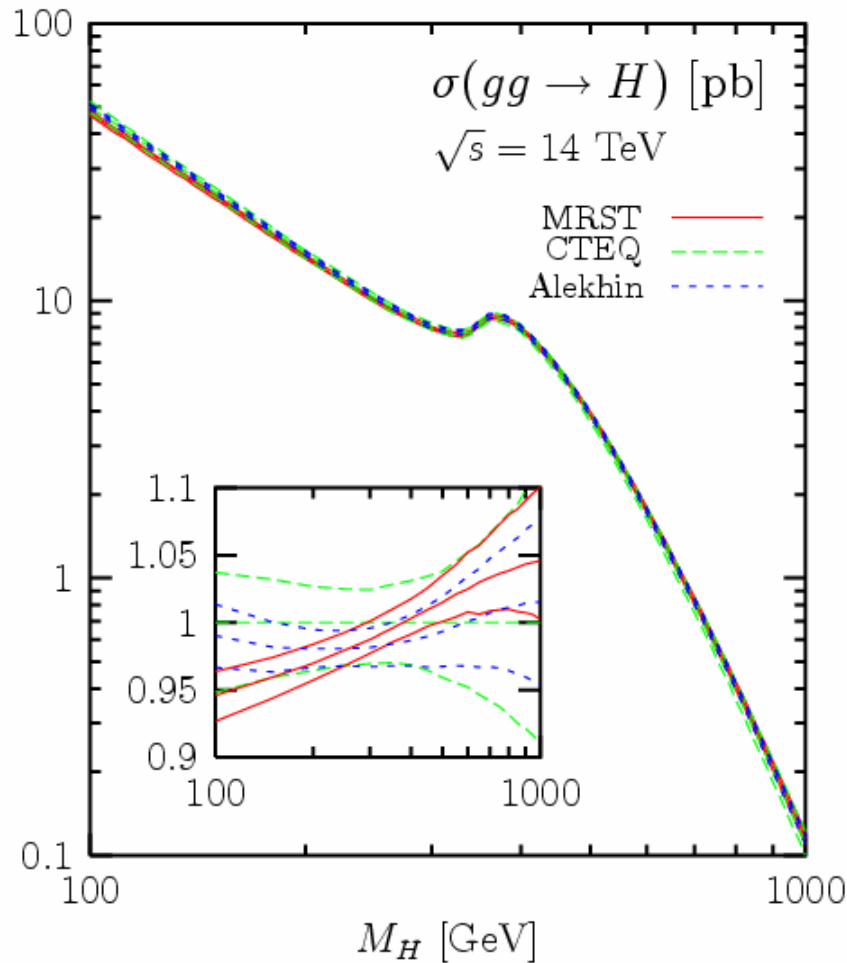
with $\tau = M^2/s$, so that for
 $ab \rightarrow X$

$$\sigma_X \propto \frac{1}{s} \frac{\partial \mathcal{L}_{ab}}{\partial \tau}$$

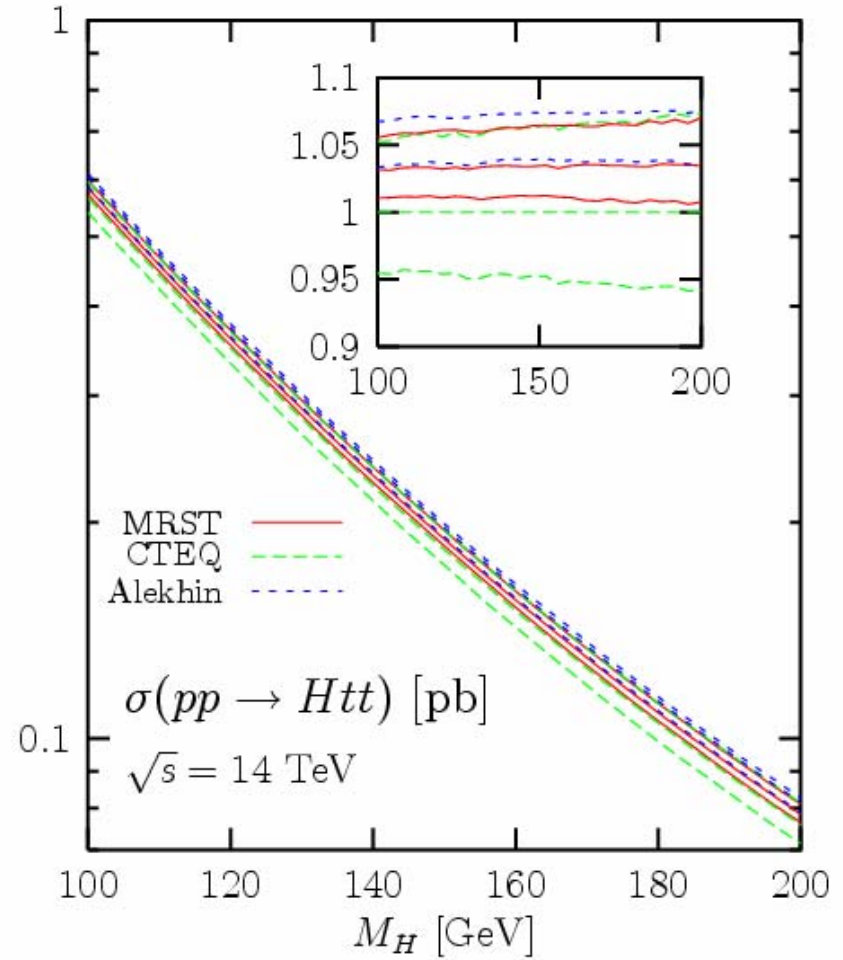
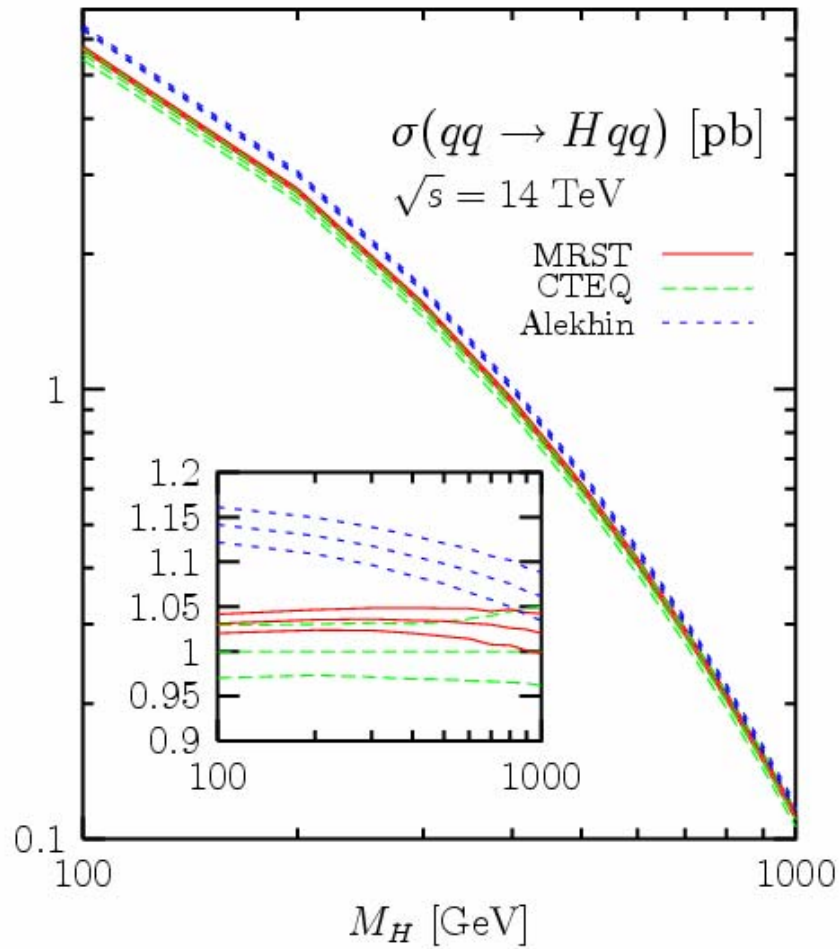


solid = LHC
 dashed = Tevatron
 Alekhin 2002

Higgs cross section: dependence on pdfs



Djouadi & Ferrag, hep-ph/0310209



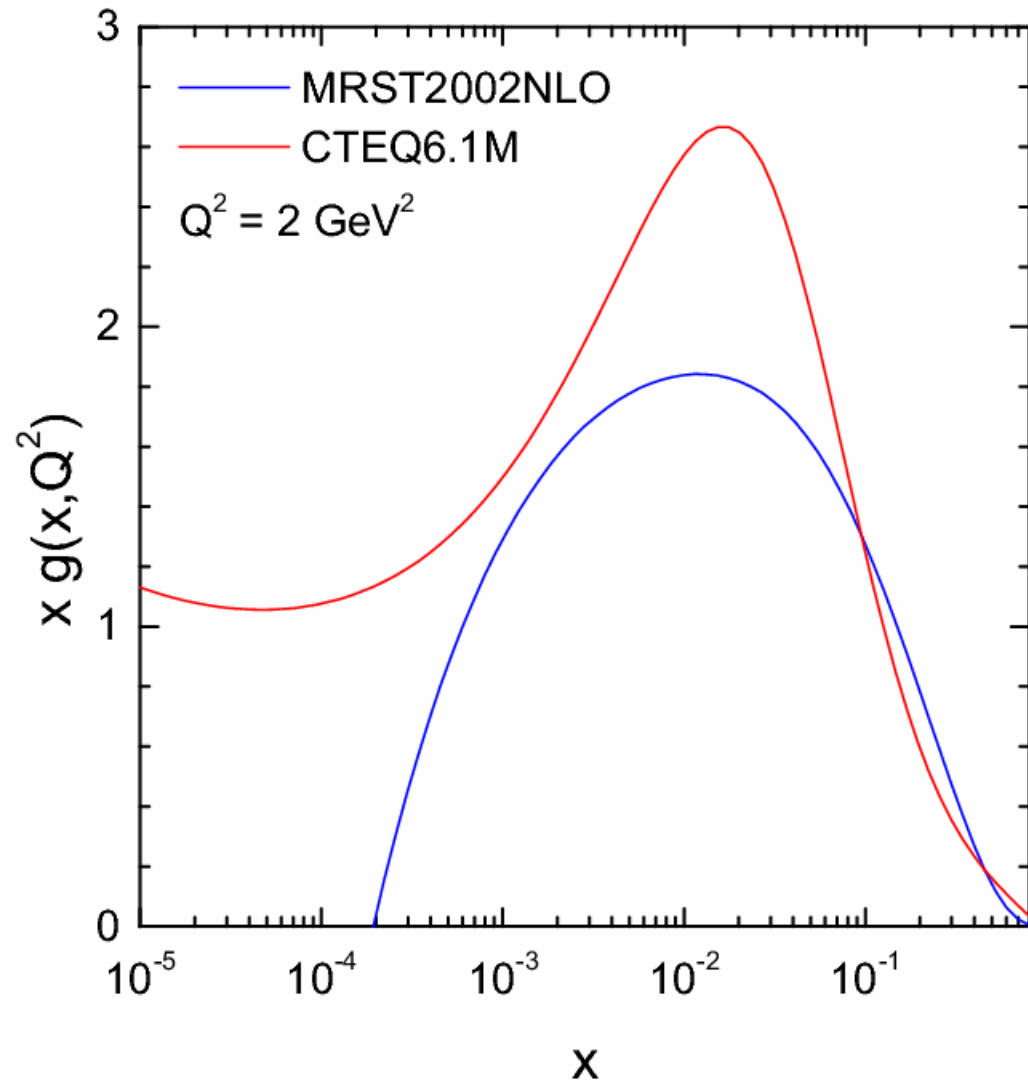
Djouadi & Ferrag, hep-ph/0310209

- MRST: $Q_0^2 = 1 \text{ GeV}^2$, $Q_{\text{cut}}^2 = 2 \text{ GeV}^2$

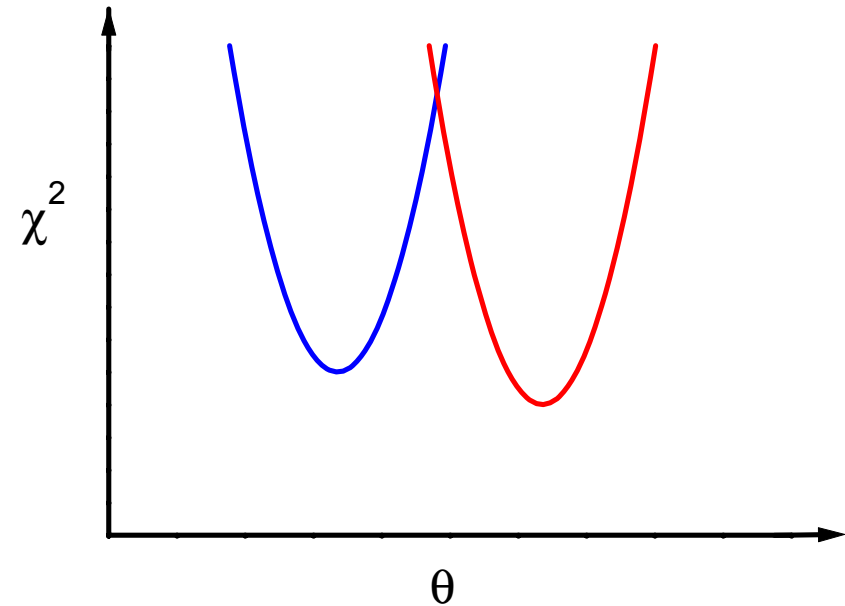
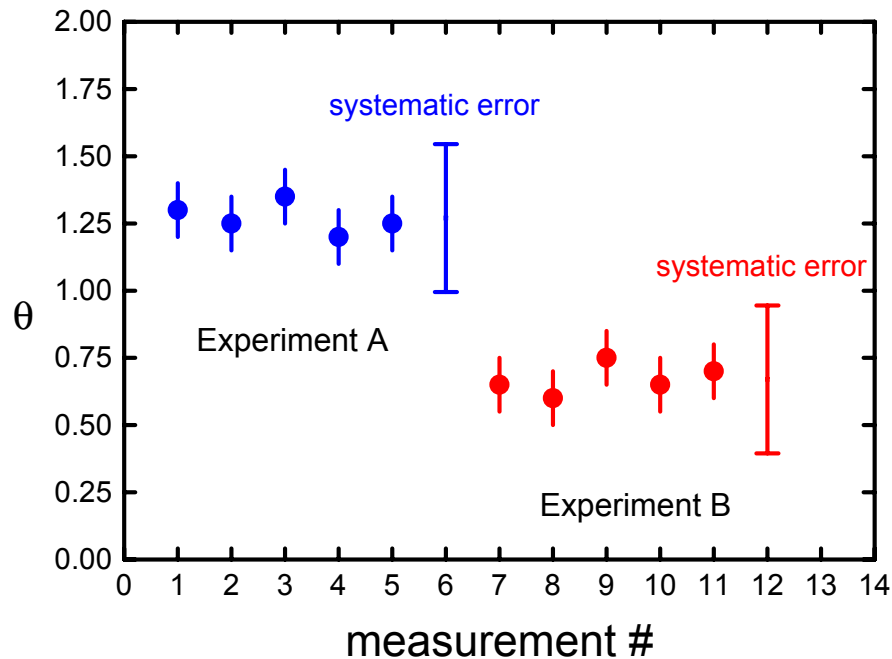
$$xg = Ax^a(1-x)^b(1+Cx^{0.5}+Dx) - Ex^c(1-x)^d$$

- CTEQ6: $Q_0^2 = 1.69 \text{ GeV}^2$, $Q_{\text{cut}}^2 = 4 \text{ GeV}^2$

$$xg = Ax^a(1-x)^b e^{cx}(1+Cx)^d$$

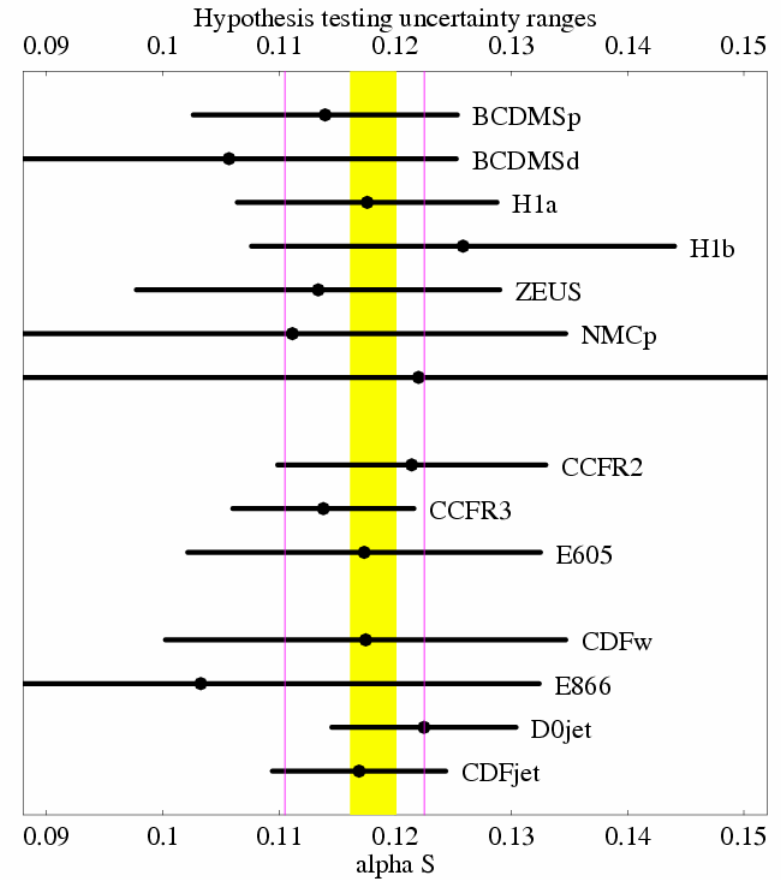
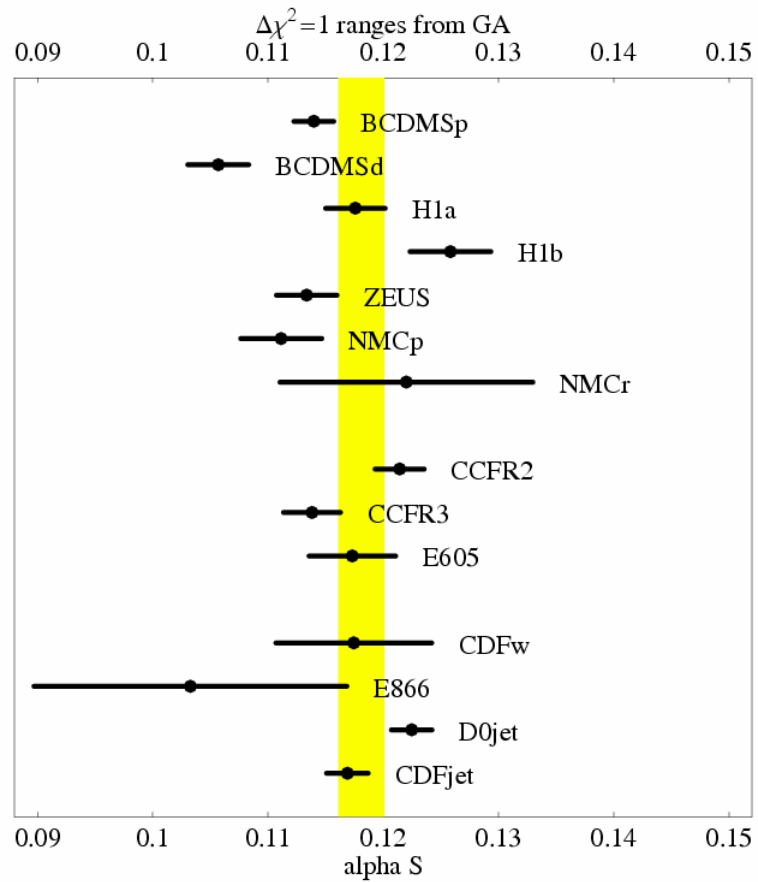


tensions within the global fit?

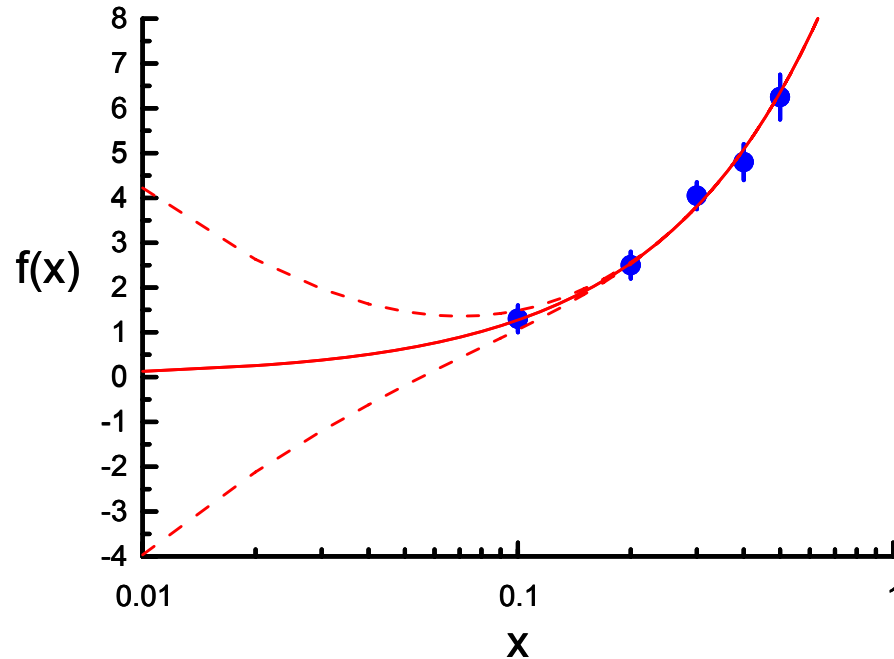


- with dataset A in fit, $\Delta\chi^2=1$; with A and B in fit, $\Delta\chi^2=?$
- 'tensions' between data sets arise, for example,
 - between DIS data sets (e.g. $\mu\mathbf{H}$ and $\nu\mathbf{N}$ data)
 - when jet and Drell-Yan data are combined with DIS data

CTEQ $\alpha_s(M_Z)$ values from global analysis with $\Delta\chi^2 = 1, 100$



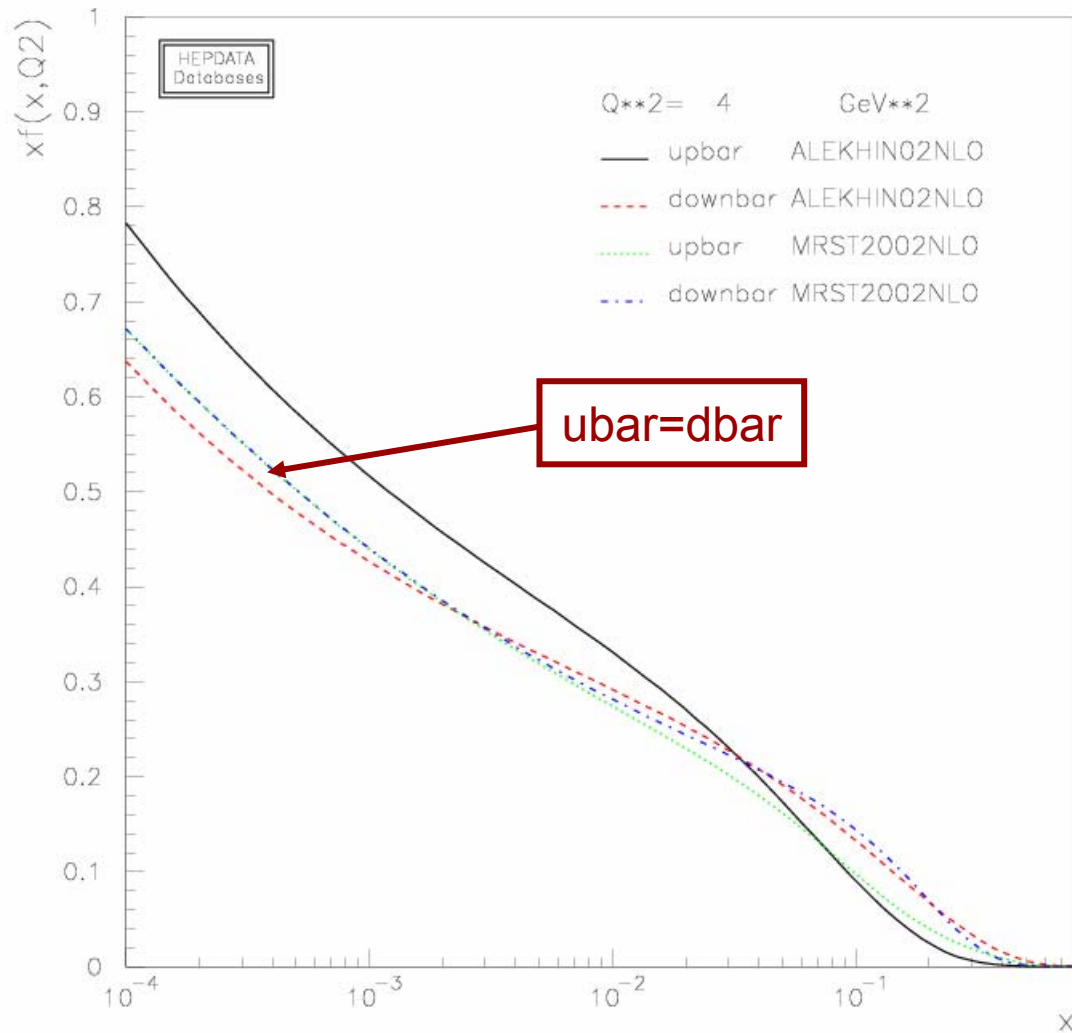
extrapolation errors

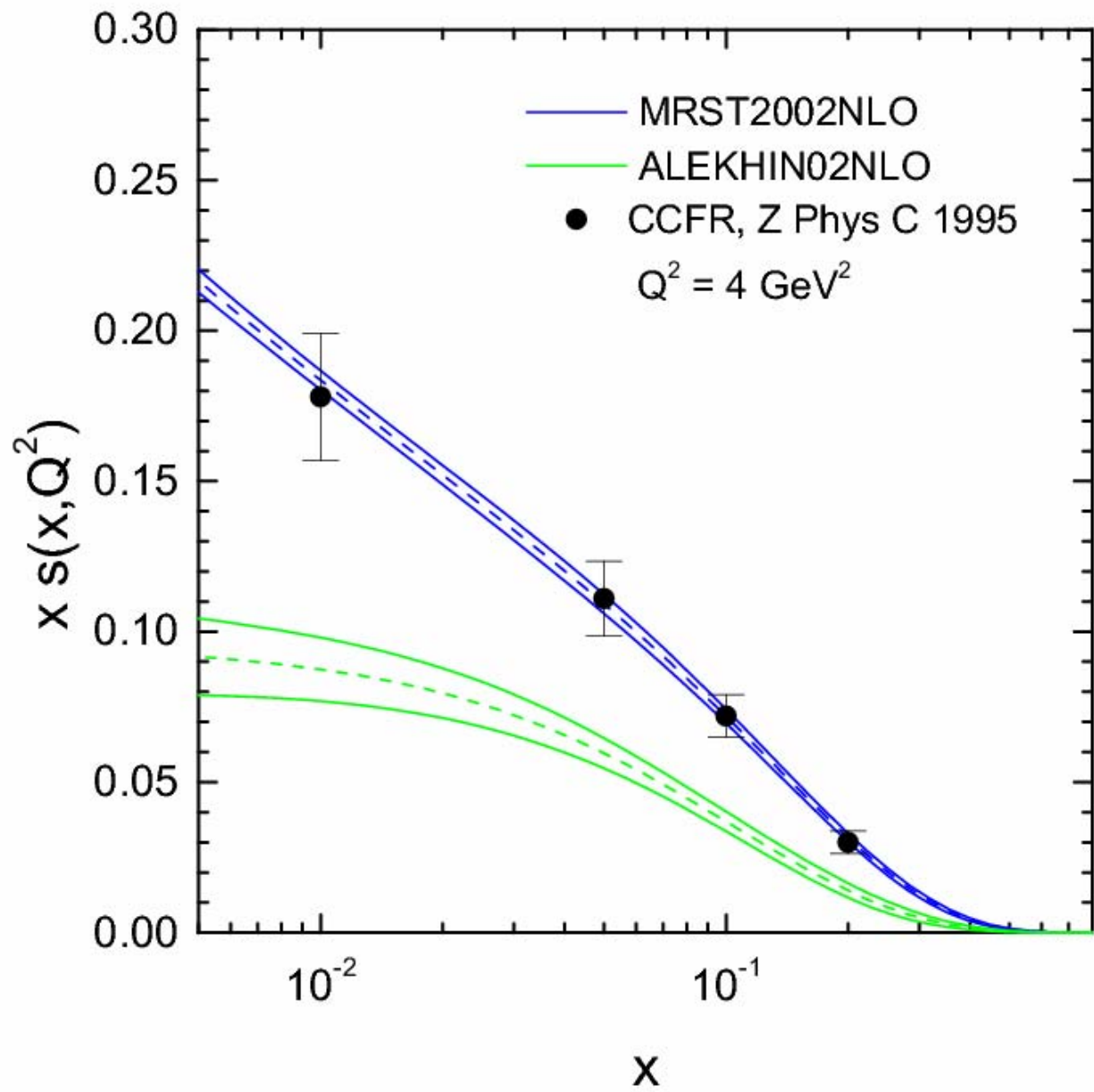


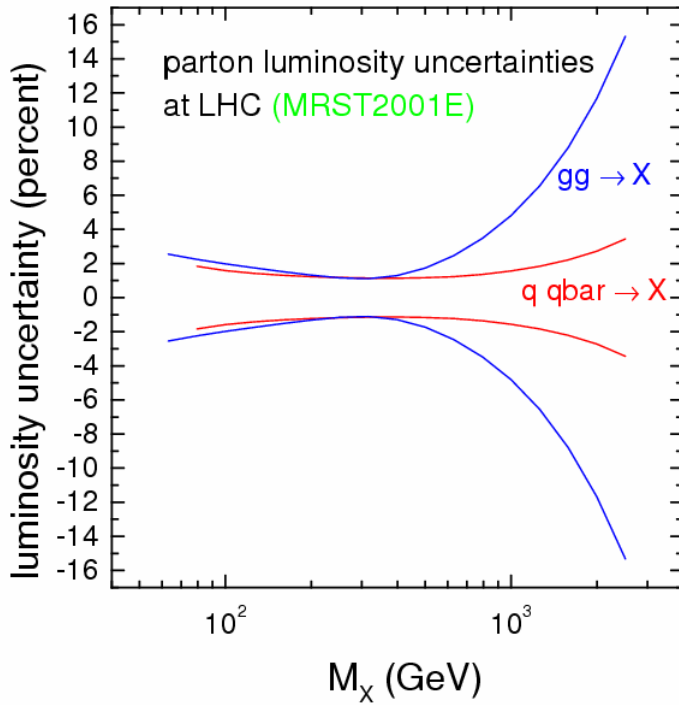
theoretical insight/guess: $f \sim A x$ as $x \rightarrow 0$

theoretical insight/guess: $f \sim \pm A x^{-0.5}$ as $x \rightarrow 0$

differences between the MRST and Alekhin u and d sea quarks near the starting scale

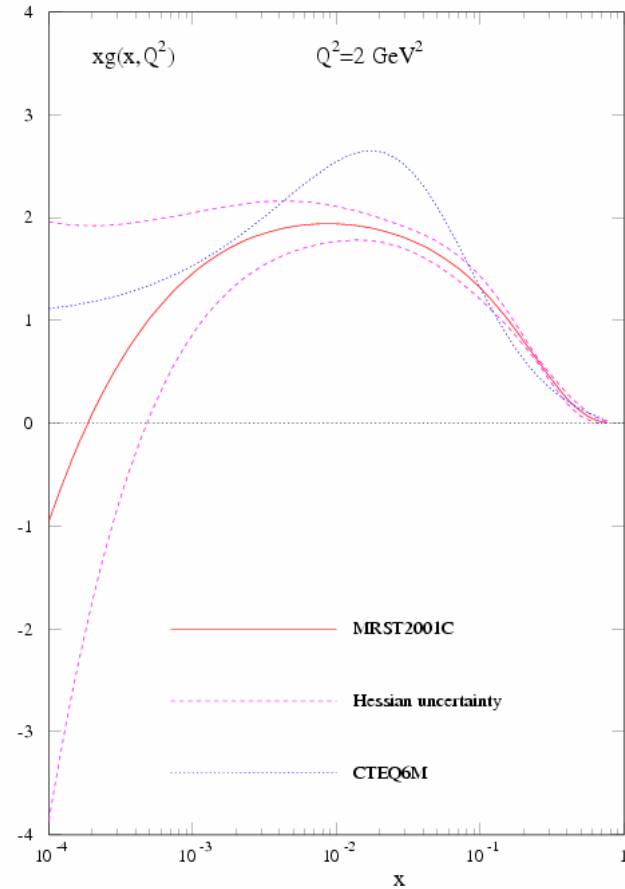






Note: high-x gluon should become better determined from Run 2 Tevatron data Q . by how much?

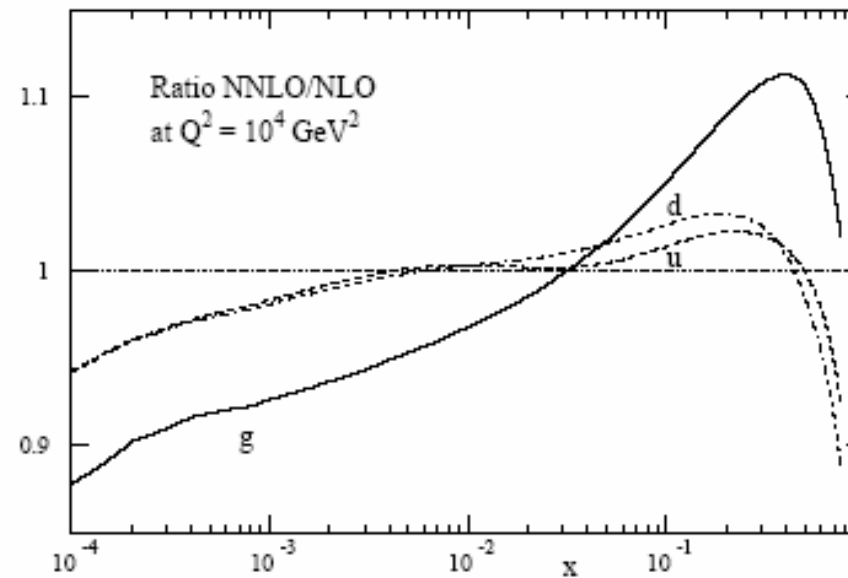
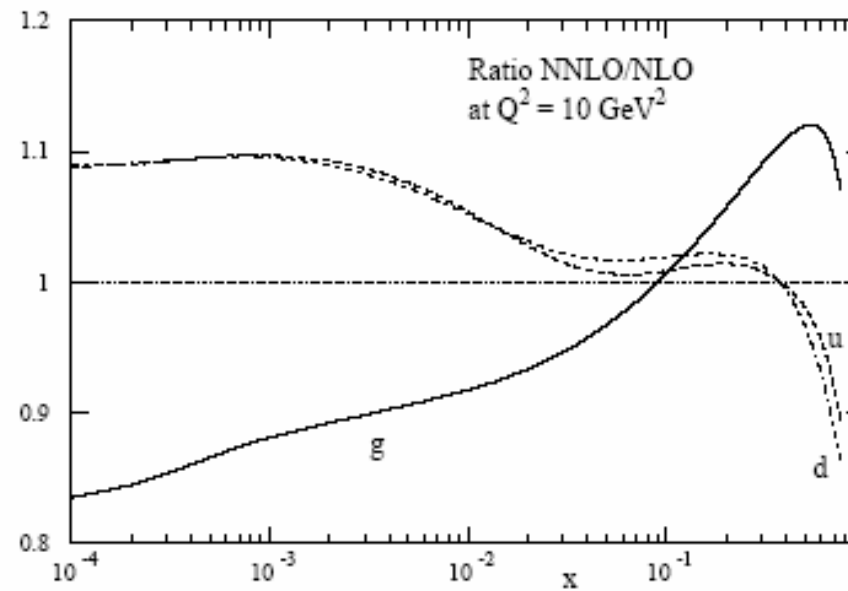
Note: CTEQ gluon 'more or less' consistent with MRST gluon



comparison with existing approximate NNLO fits? (MRST, Alekhin)

- exact NNLO splitting functions are very close to approximate splitting functions (van Neerven, Vogt) based on moments & known small- and large-x behaviours...
- ... and therefore the corresponding pdfs are almost identical
- **Note:**
 - the **full** NNLO pdf fit awaits calculation of the inclusive high E_T jet cross section at NNLO
 - including NNLO (splitting & coefficient functions) gives a **slight** improvement in overall fit quality, and reduction in $\alpha_s(M_Z)$ from 0.119 to 0.116

ratio of MRST2001 NLO and 'NNLO' parton distributions



summary of NNLO collider calculations

- $p + p \rightarrow jet + X$ *; in progress
- $p + p \rightarrow \gamma + X$; in principle, subset of the jet calculation but issues regarding photon fragmentation, isolation etc
- $p + p \rightarrow QQbar + X$; requires extension of above to non-zero fermion masses
- ☺ • $p + p \rightarrow (\gamma^*, W, Z) + X$ *; van Neerven et al, Harlander and Kilgore corrected (2002)
- ☺ • $p + p \rightarrow (\gamma^*, W, Z) + X$ differential rapidity distribution *; Anastasiou, Dixon, Melnikov (2003)
- ☺ • $p + p \rightarrow H + X$; Harlander and Kilgore, Anastasiou and Melnikov (2002-3)

Note: knowledge of processes * needed for a full NNLO global parton distribution fit

pdfs from global fits

Formalism

LO, NLO, NNLO DGLAP
MSbar factorisation
 Q_0^2
functional form @ Q_0^2
sea quark (a)symmetry
etc.

Data

DIS (SLAC, BCDMS, NMC, E665,
CCFR, H1, ZEUS, ...)
Drell-Yan (E605, E772, E866, ...)
High E_T jets (CDF, D0)
W rapidity asymmetry (CDF)
 νN dimuon (CCFR, NuTeV)
etc.

$$f_i(x, Q^2) \pm \delta f_i(x, Q^2)$$

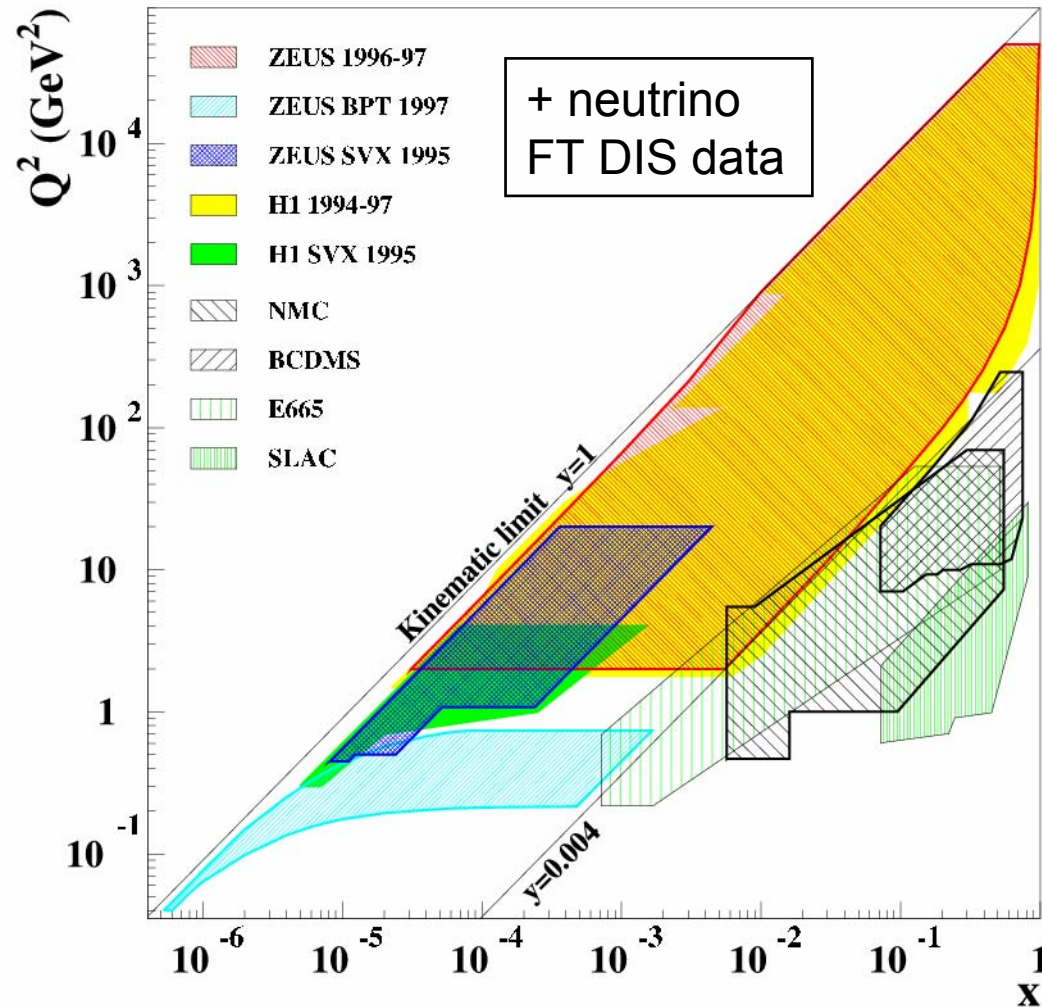
$$\alpha_s(M_Z)$$

Who?

Alekhin, CTEQ, MRST,
GGK, Botje, H1, ZEUS,
GRV, BFP, ...

<http://durpdg.dur.ac.uk/hepdata/pdf.html>

summary of DIS data



Note: must impose cuts on DIS data to ensure validity of leading-twist DGLAP formalism in the global analysis, typically:

$$Q^2 > 2 - 4 \text{ GeV}^2$$

$$W^2 = (1-x)/x Q^2 > 10 - 15 \text{ GeV}^2$$

typical data
ingredients of
a global pdf fit

H1, ZEUS $F_2^{e^+p}(x, Q^2), F_2^{e^-p}(x, Q^2)$

BCDMS $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2)$

NMC $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2), (F_2^{\mu n}(x, Q^2)/F_2^{\mu p}(x, Q^2))$

SLAC $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2)$

E665 $F_2^{\mu p}(x, Q^2), F_2^{\mu d}(x, Q^2)$

CCFR $F_2^{\nu(\bar{\nu})p}(x, Q^2), F_3^{\nu(\bar{\nu})p}(x, Q^2)$

→ q, \bar{q} at all x and g at medium, small x

H1, ZEUS $F_{2,c}^{e^+p}(x, Q^2) \rightarrow c$

E605, E772, E866 Drell-Yan $pN \rightarrow \mu\bar{\mu} + X \rightarrow \bar{q}(g)$

E866 Drell-Yan p,n asymmetry → \bar{u}, \bar{d}

CDF W rapidity asymmetry → u/d ratio at high x

CDF, D0 Inclusive jet data → g at high x

CCFR, NuTeV Dimuon data constrains strange sea s, \bar{s}

Note: nowadays, no prompt photon data included in fits



recent global fit work

- **H1, ZEUS**: ongoing fits for pdfs + uncertainties from HERA and other DIS data
- **Martin, Roberts, WJS, Thorne (MRST)**: updated 'MRST2001' global fit (hep-ph/0110215); LO/NLO/NNLO' comparison (hep-ph/0201127); pdf uncertainties: from experiment (hep-ph/0211080) and theory (hep-ph/0308087)
- **Pumplin et al. (CTEQ)**: updated 'CTEQ6' global fit (hep-ph/0201195), including uncertainties on pdfs; dedicated study of high E_T jet cross sections for the Tevatron (hep-ph/0303013); strangeness asymmetry from neutrino dimuon production (hep-ph/0312323)
- **Giele, Keller, Kosower (GKK)**: restricted global fit, focusing on data-driven pdf uncertainties (hep-ph/0104052)
- **Alekhin**: restricted global fit (DIS data only), focusing on effect of both theoretical and experimental uncertainties on pdfs and higher-twist contributions (hep-ph/0011002); updated and including 'NNLO' fit (hep-ph/0211096)

HEPDATA pdf server

Comprehensive repository of past and present polarised and unpolarised pdf codes (with online plotting facility) can be found at the HEPDATA pdf server web site:

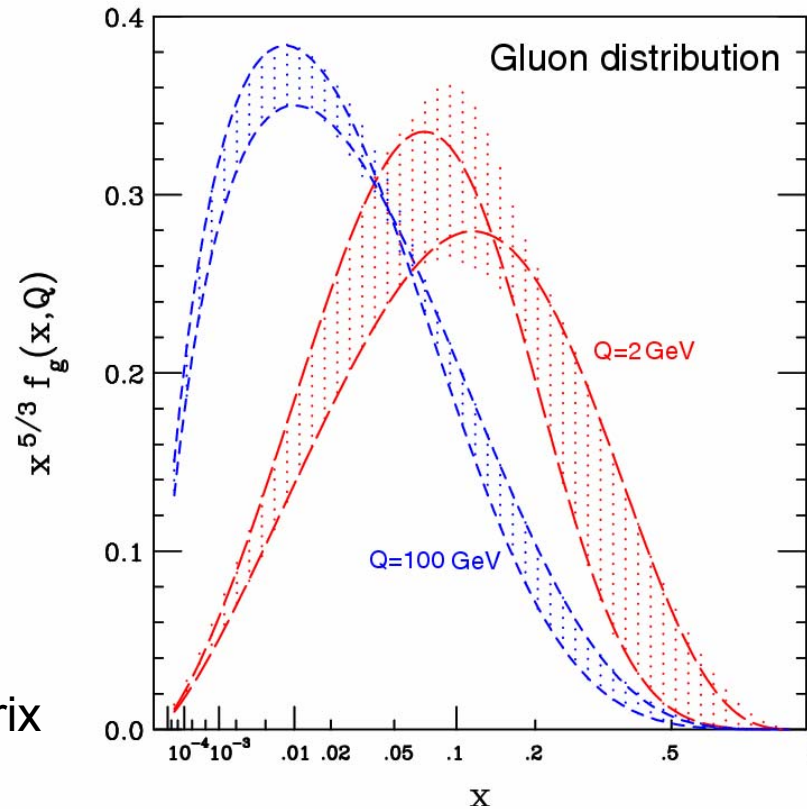
<http://durpdg.dur.ac.uk/hepdata/pdf.html>

... this is also the home of the LHAPDF project

pdfs with errors....

CTEQ gluon
distribution
uncertainty using
Hessian Method

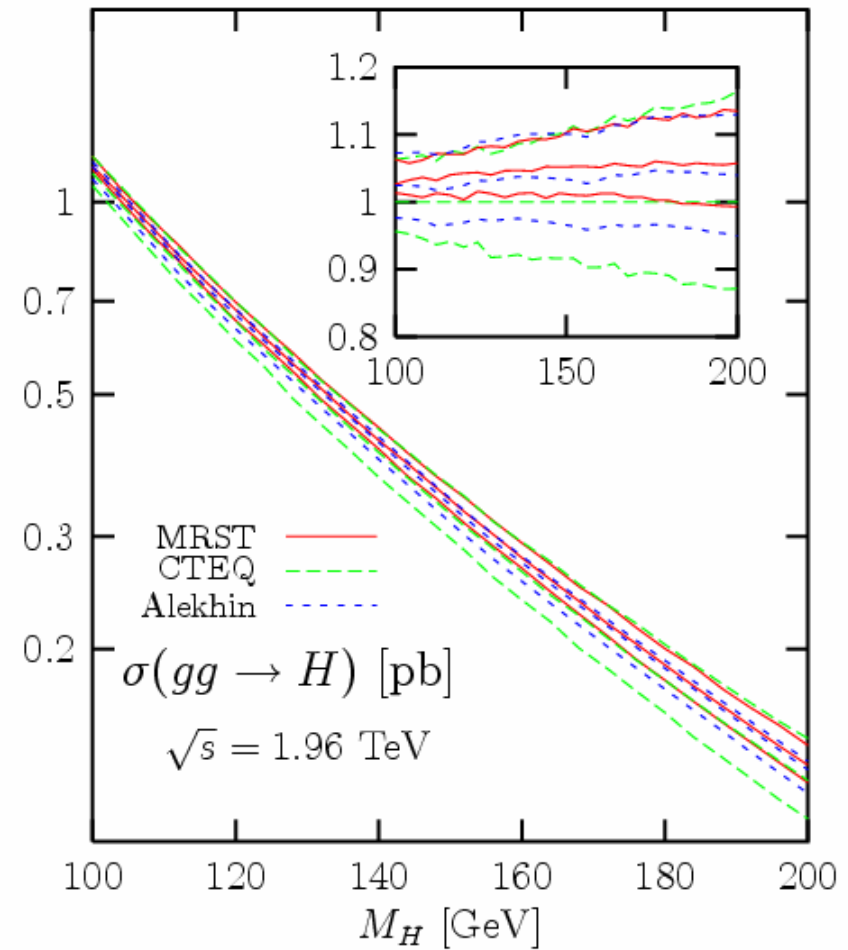
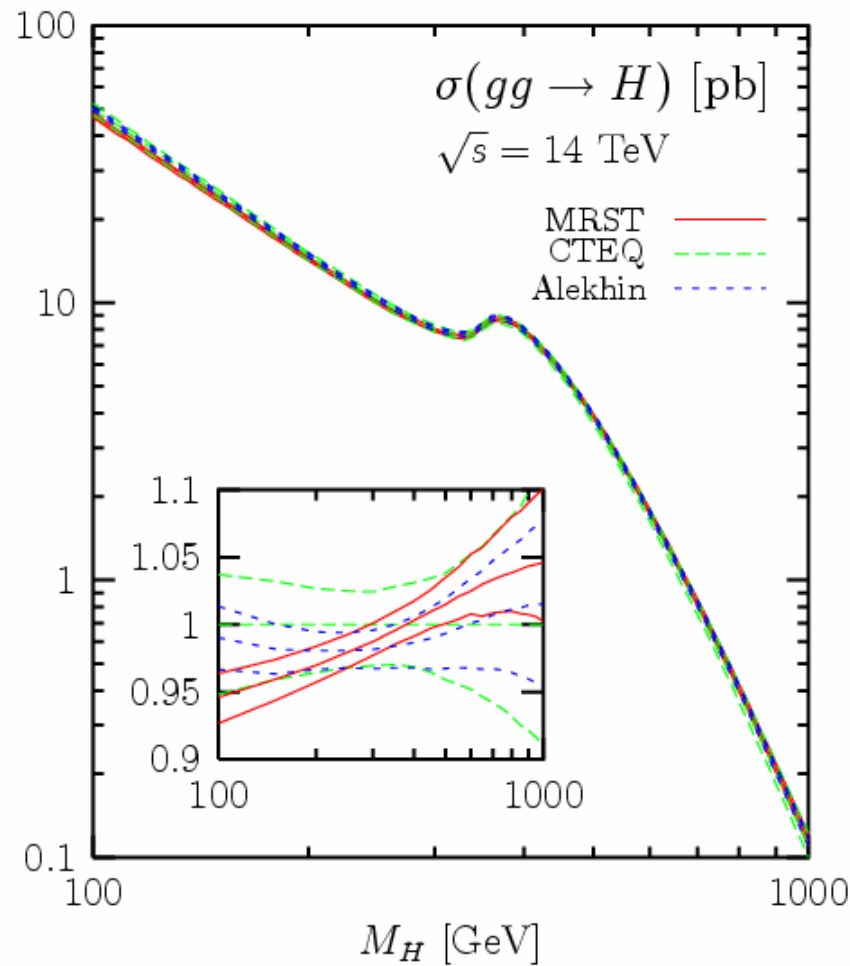
output = best fit set
+ $2N_p$ error sets



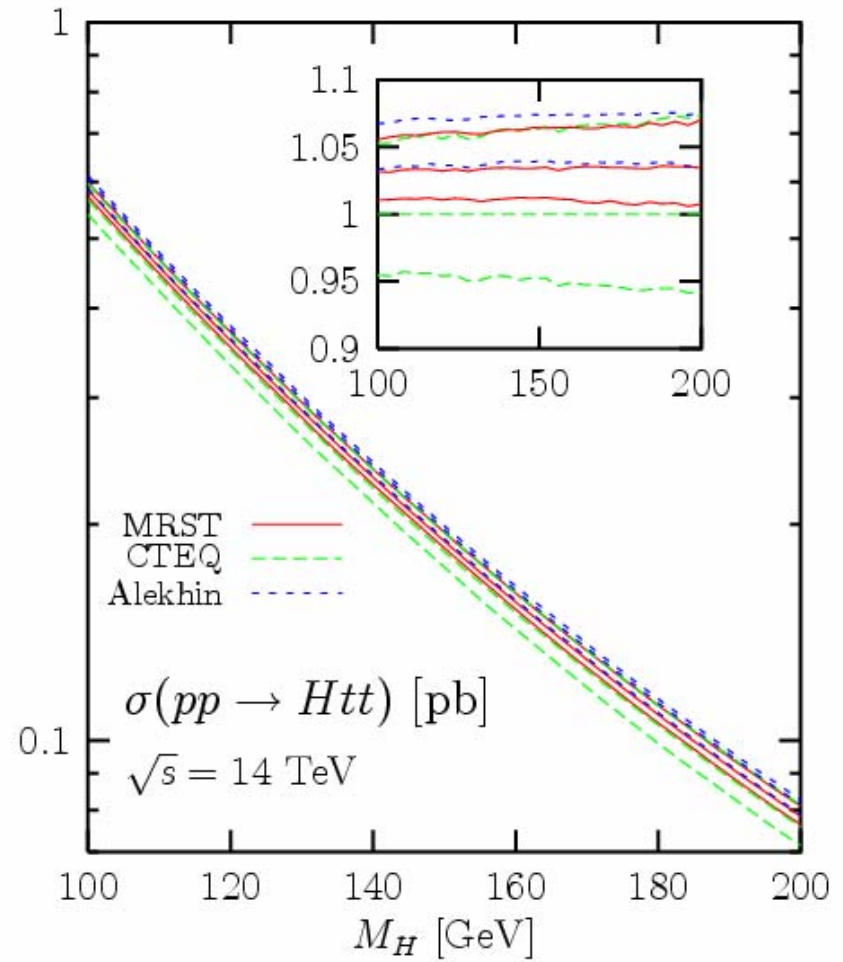
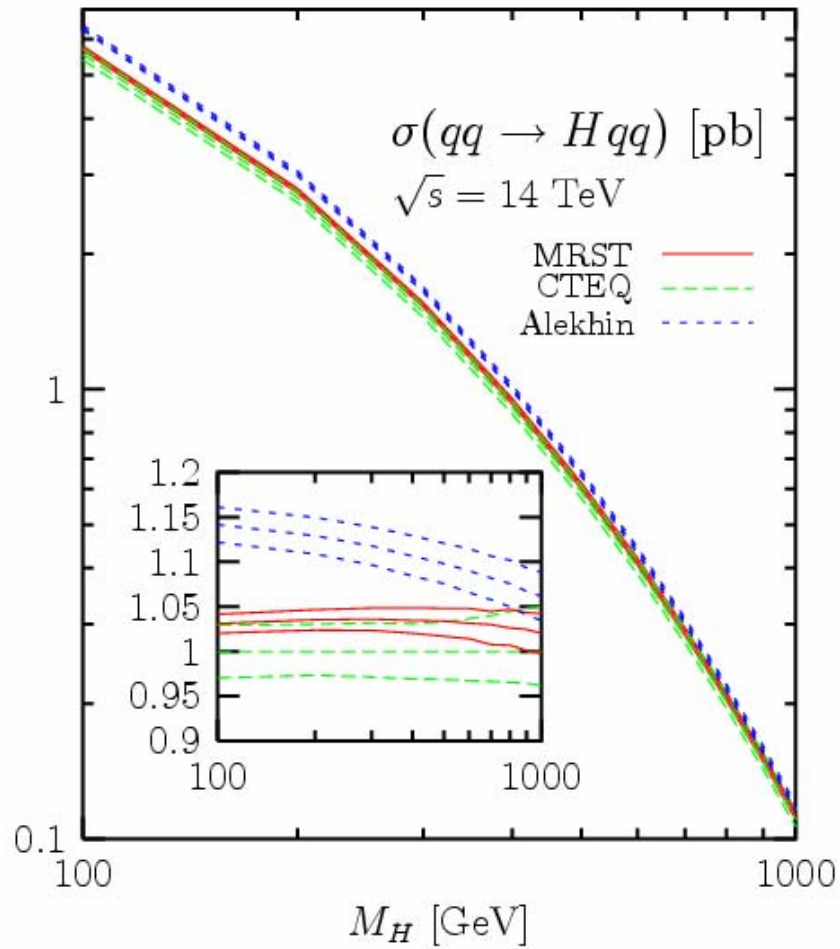
Hessian Matrix

$$\chi^2 - \chi_{min}^2 \equiv \Delta\chi^2 = \sum_{i,j} H_{ij} (a_i - a_i^{(0)}) (a_j - a_j^{(0)})$$

“best fit” parameters



Djouadi & Ferrag, hep-ph/0310209



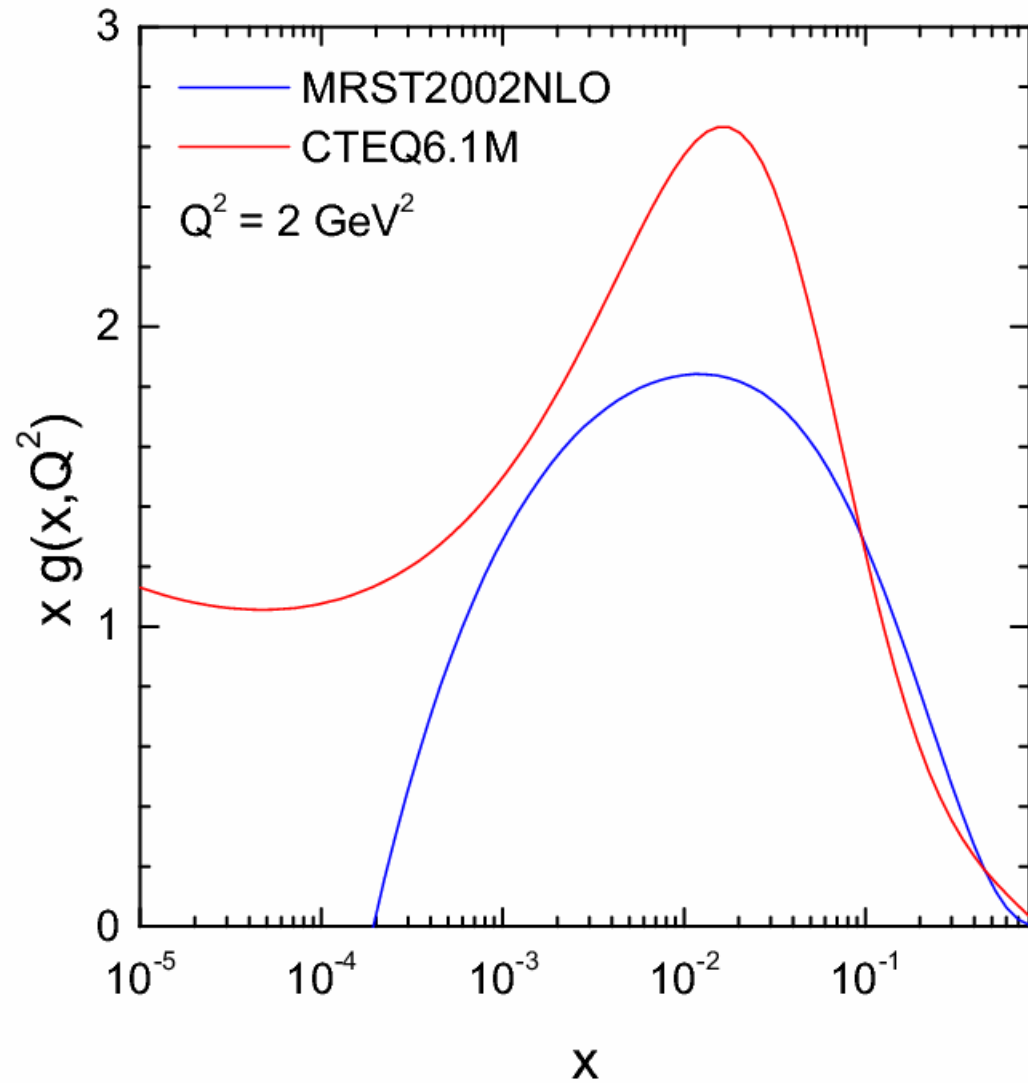
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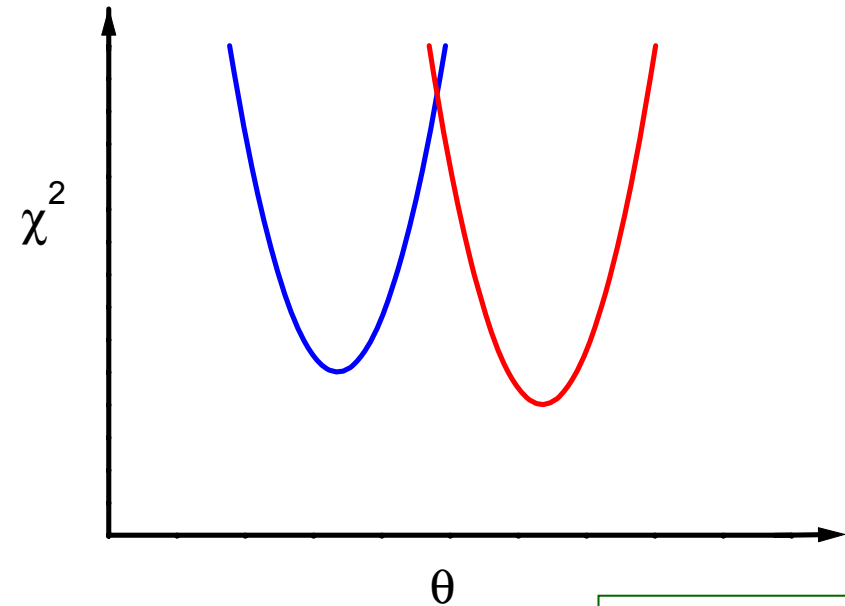
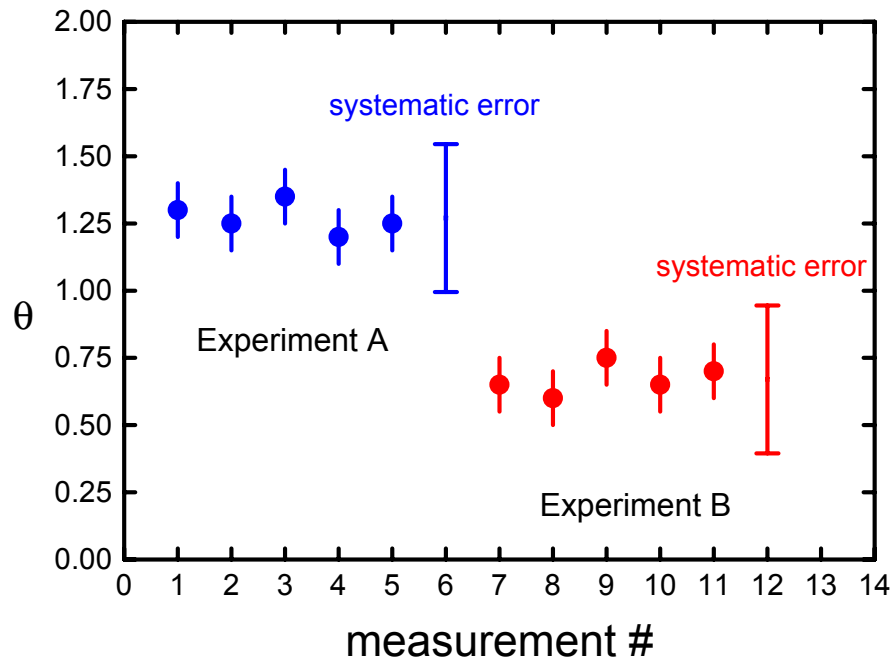
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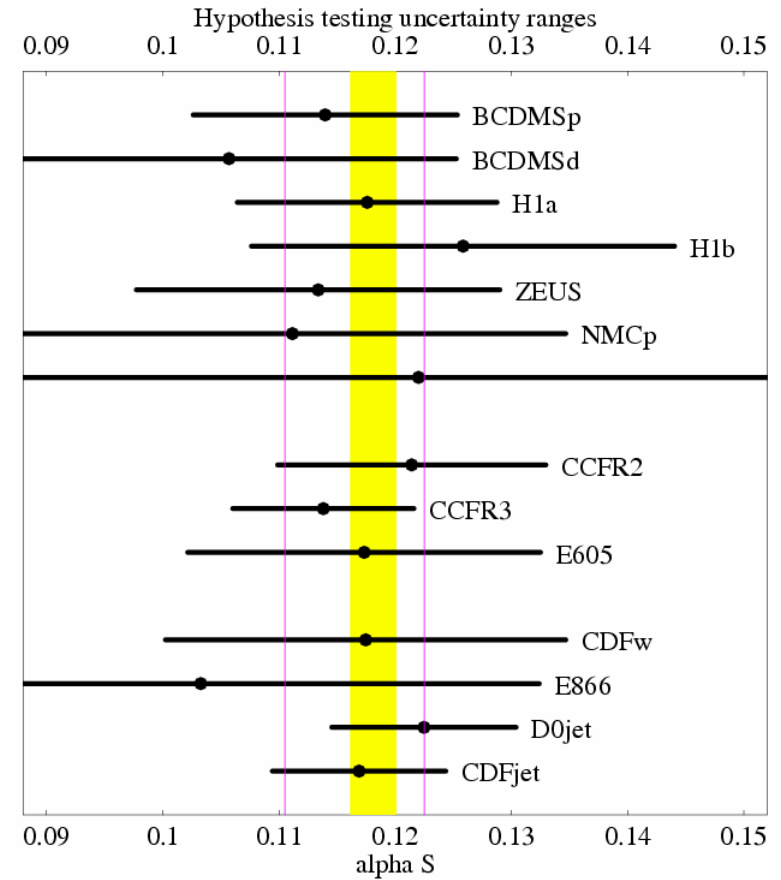
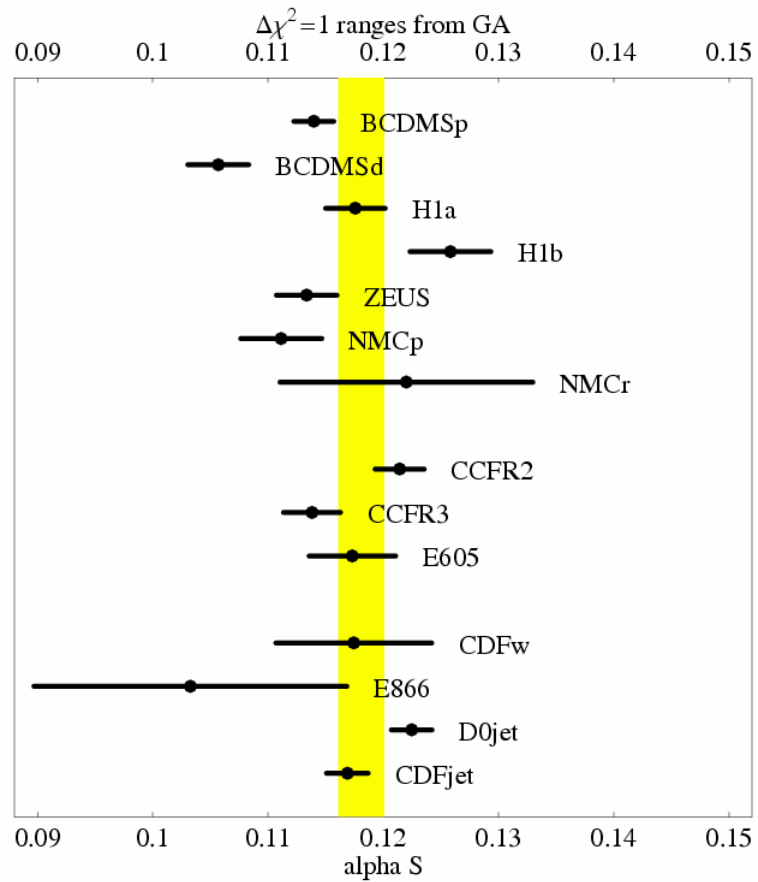
tensions within the global fit?



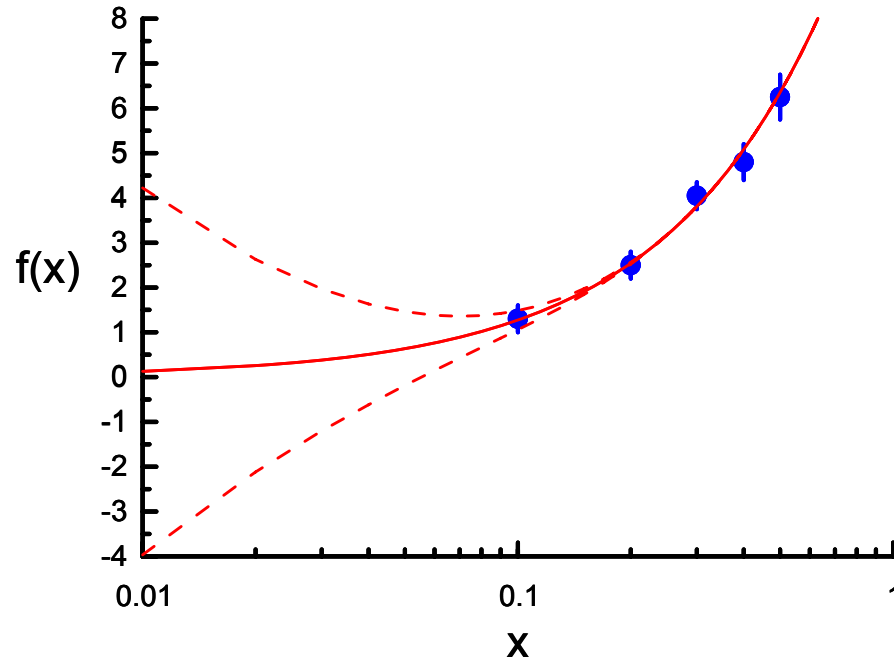
pictures from
W-K Tung

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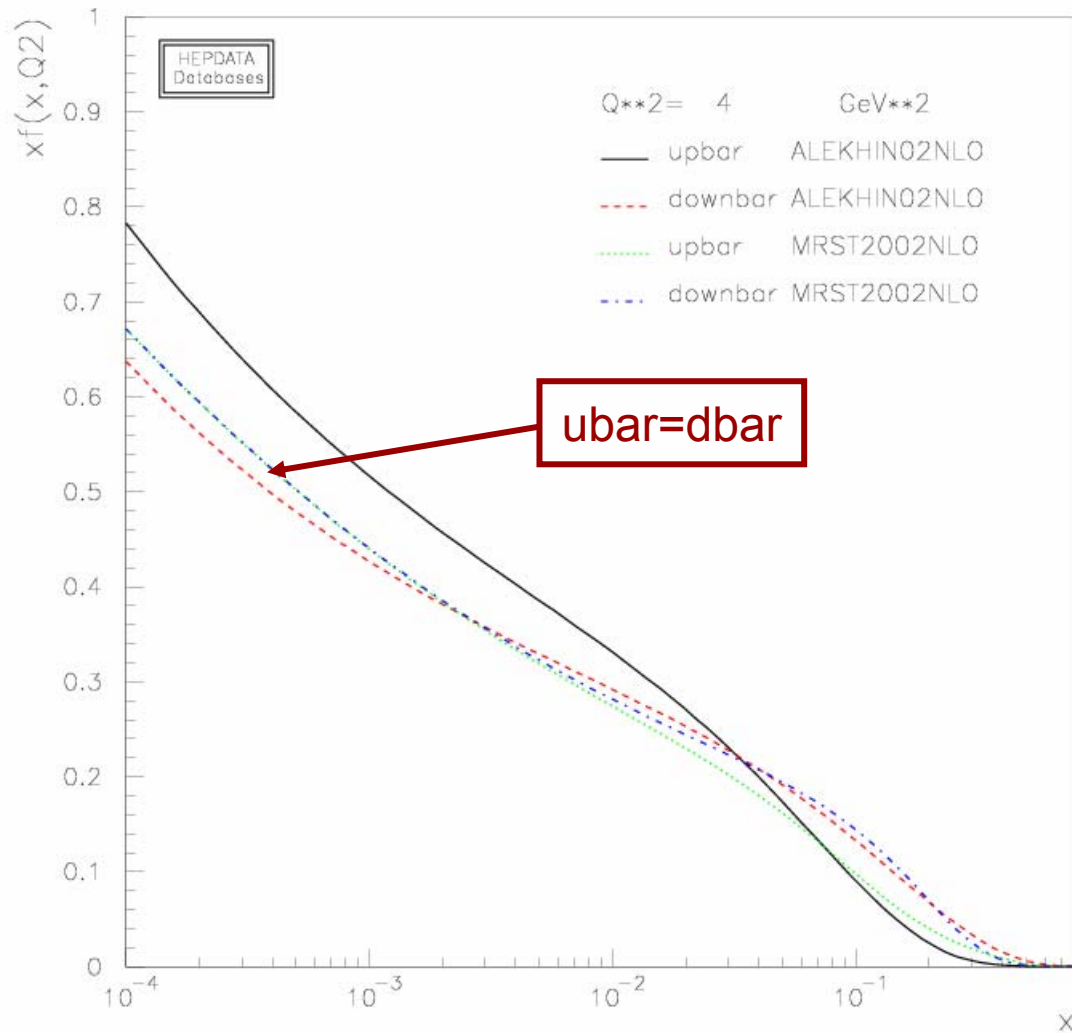
extrapolation errors

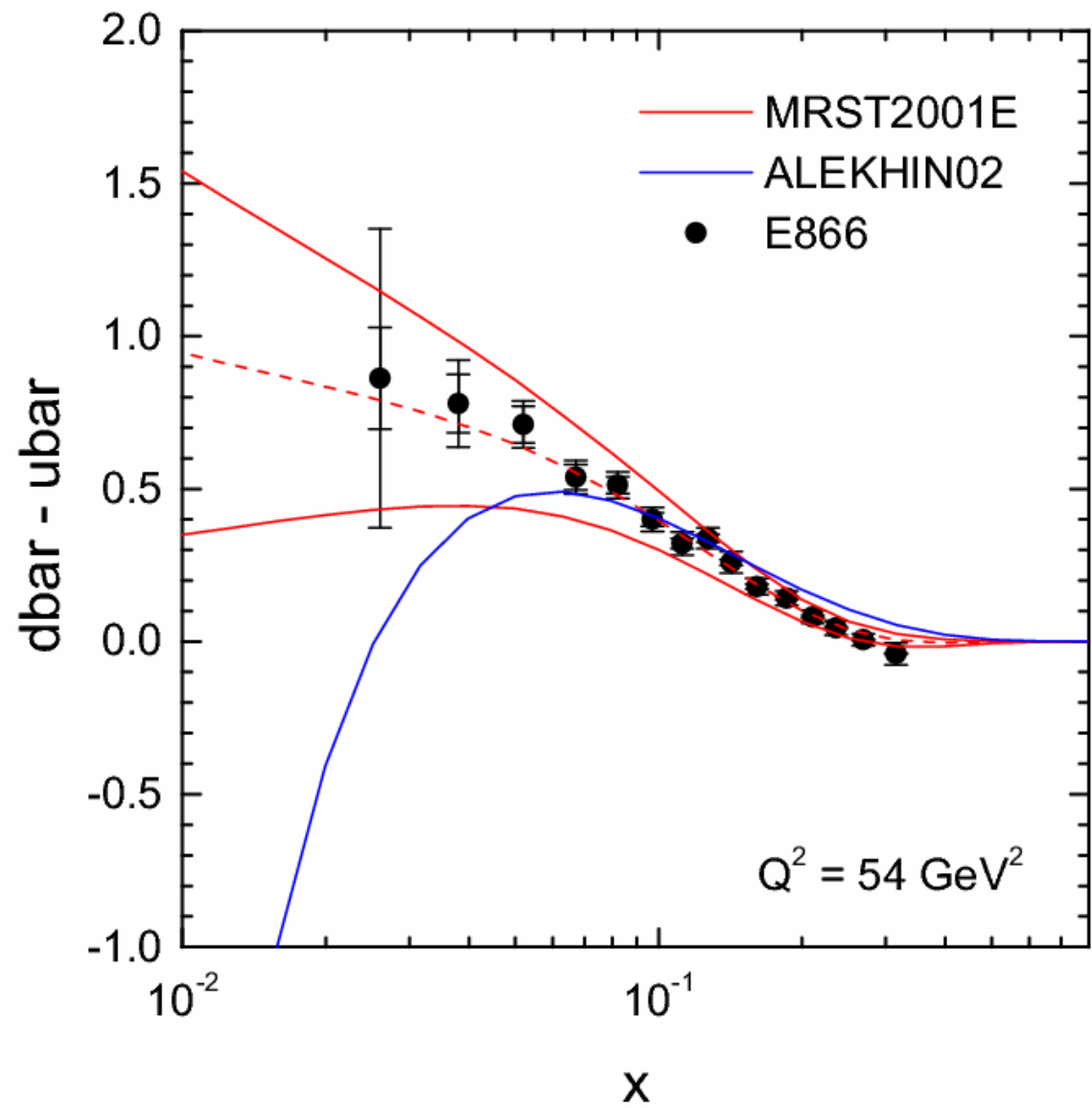


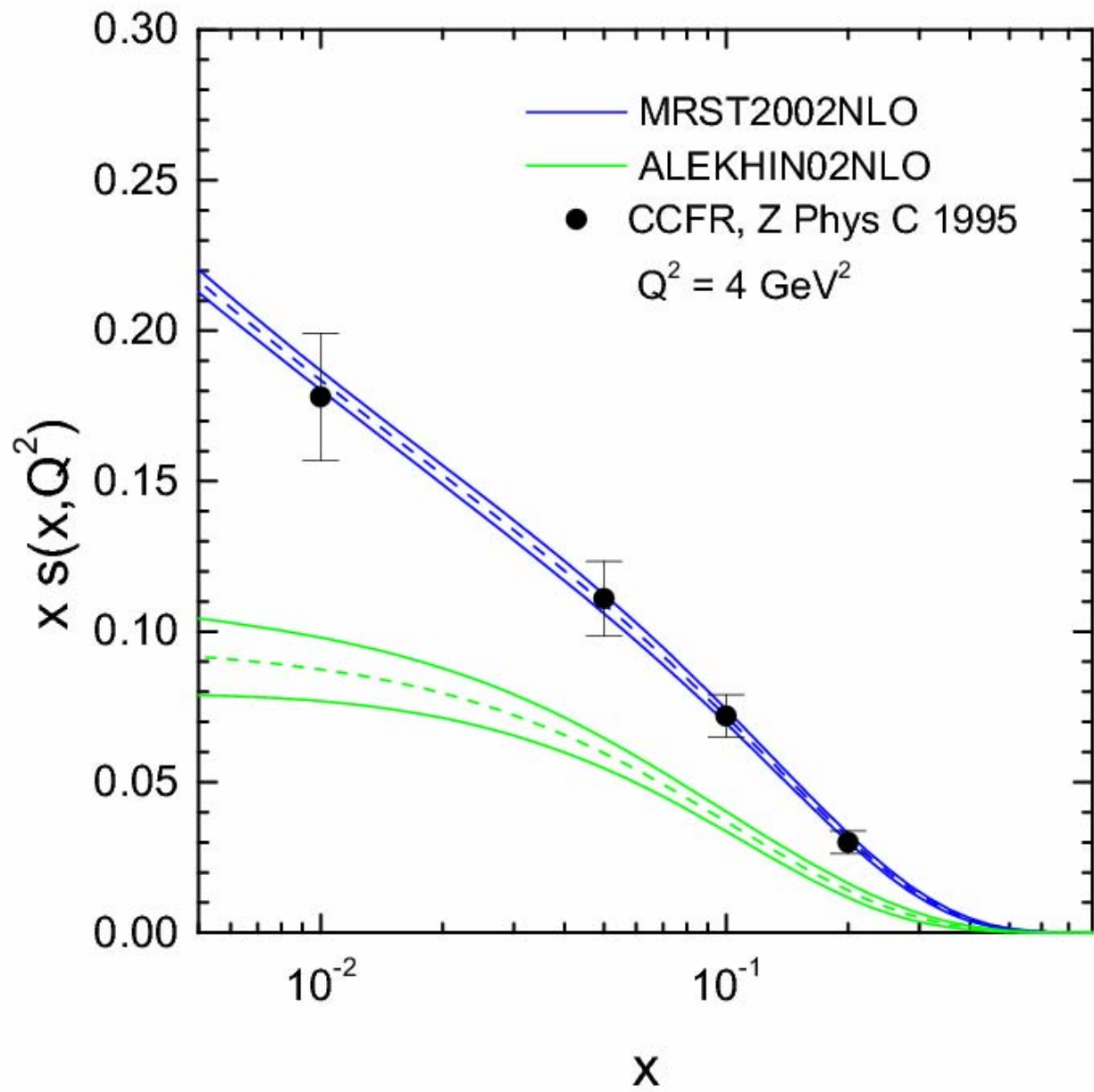
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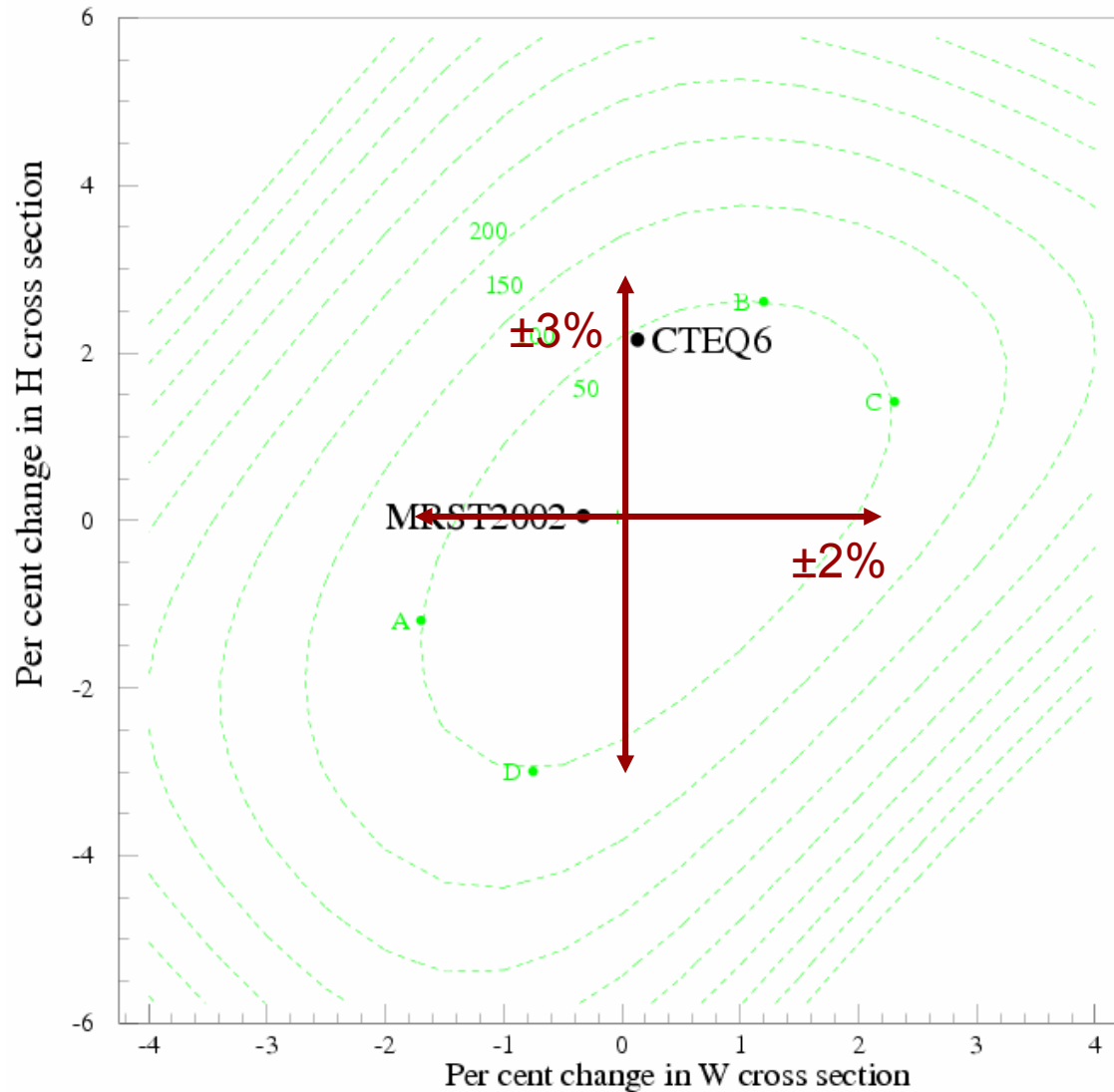
differences between the MRST and Alekhin u and d sea quarks near the starting scale





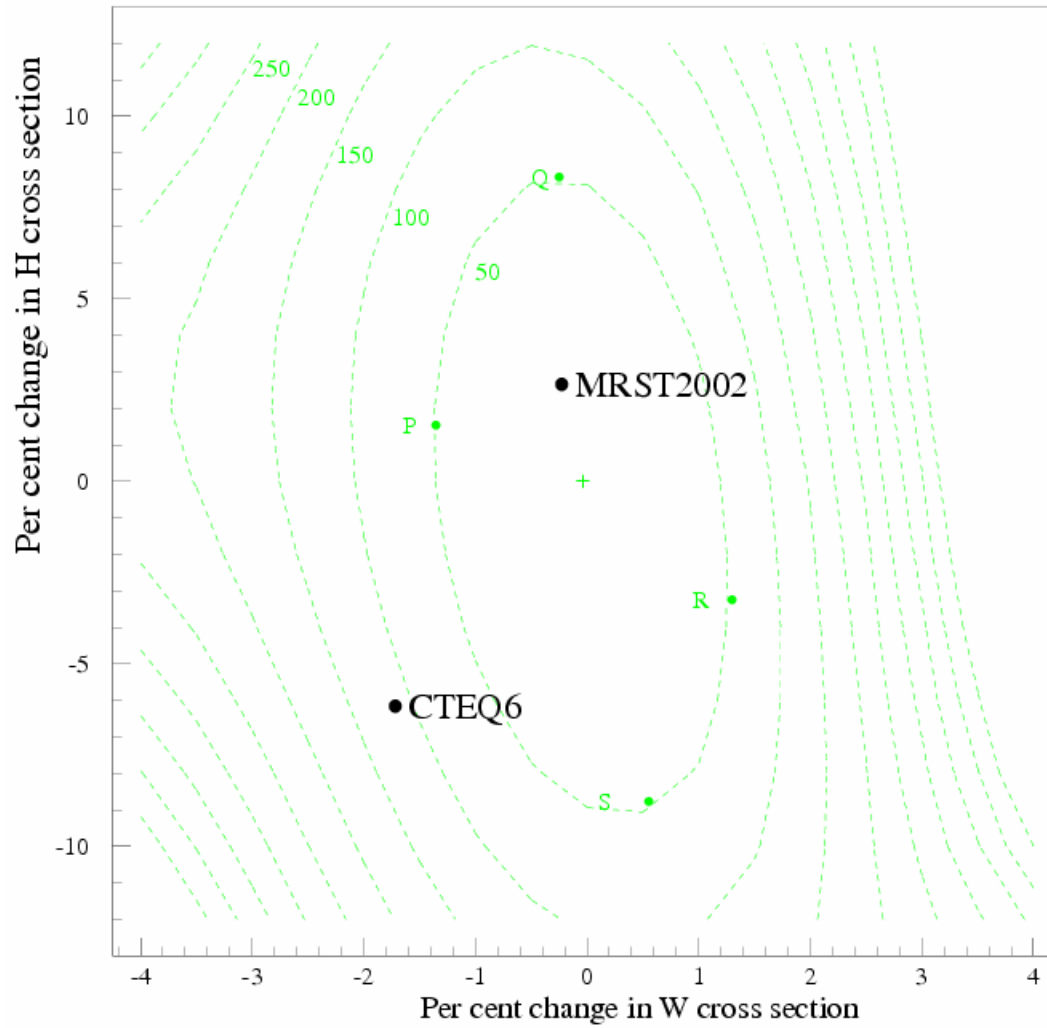


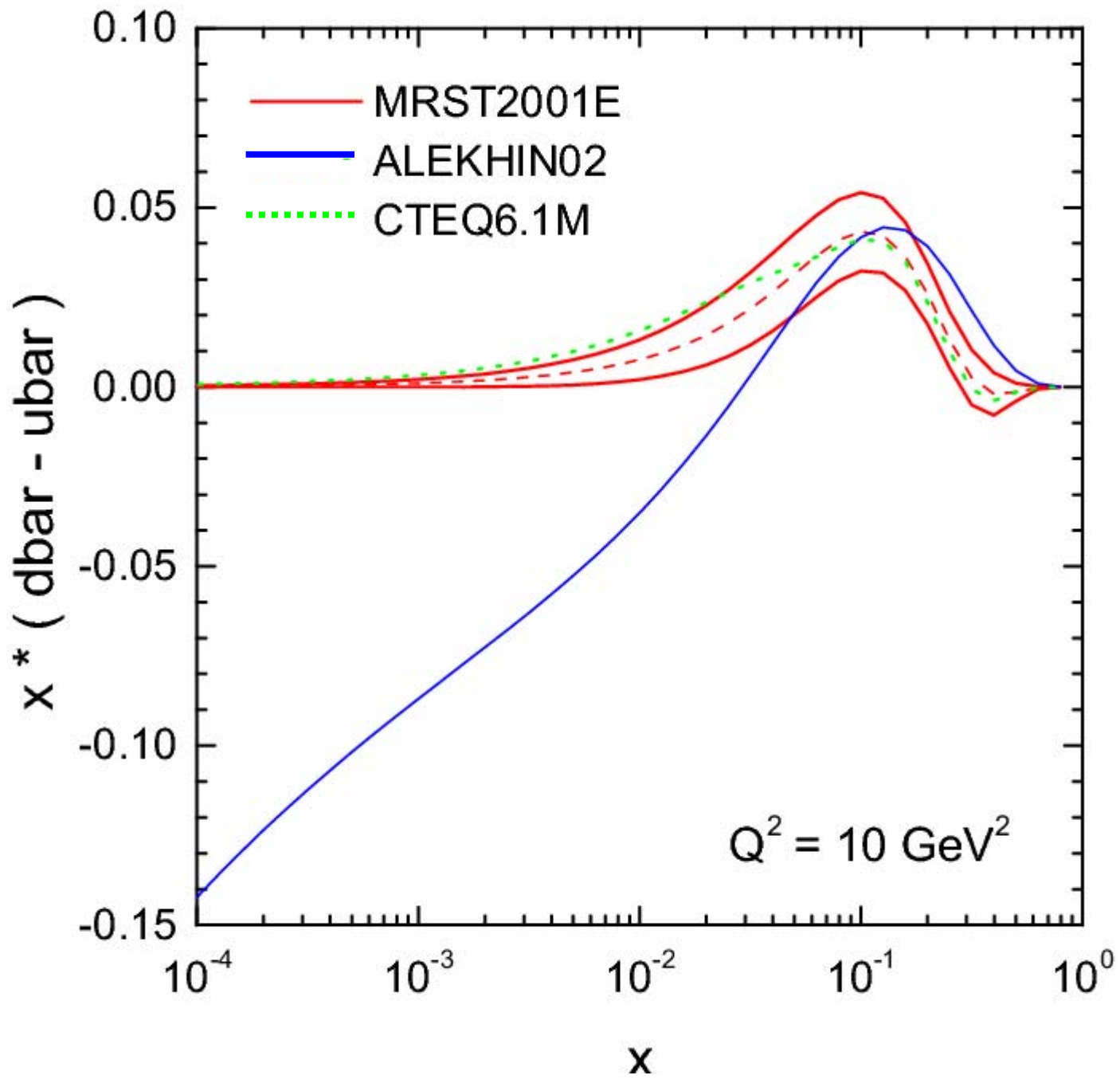
χ^2 increase in global analysis as the
W and H cross sections are varied at the LHC



contours correspond
to 'experimental'
pdf errors only; shift
of prediction using
CTEQ6 pdfs shows
effect of 'theoretical'
pdf errors

χ^2 increase in global analysis as the
W and H cross sections are varied at the TEVATRON





as small x data are systematically removed from the MRST global fit, the quality of the fit improves until stability is reached at around $x \sim 0.005$ (MRST hep-ph/0308087)

Q. Is fixed-order DGLAP insufficient for small- x DIS data?!

Δ = improvement in χ^2 to remaining data / # of data points removed

x_{cut} :	0	0.0002	0.001	0.0025	0.005	0.01
# data points	2097	2050	1961	1898	1826	1762
$\alpha_S(M_Z^2)$	0.1197	0.1200	0.1196	0.1185	0.1178	0.1180
$\chi^2(x > 0)$	2267					
$\chi^2(x > 0.0002)$	2212	2203				
$\chi^2(x > 0.001)$	2134	2128	2119			
$\chi^2(x > 0.0025)$	2069	2064	2055	2040		
$\chi^2(x > 0.005)$	2024	2019	2012	1993	1973	
$\chi^2(x > 0.01)$	1965	1961	1953	1934	1917	1916
Δ_i^{i+1}		0.19	0.10	0.24	0.28	0.02

the stability of the small- x fit can be recovered by adding to the fit empirical contributions of the form

$$P_{gg} \rightarrow P_{gg}^{\text{NLO}} + A\bar{\alpha}_S^4 \left(\frac{\ln^3 1/x}{3!} - \frac{\ln^2 1/x}{2!} \right)$$

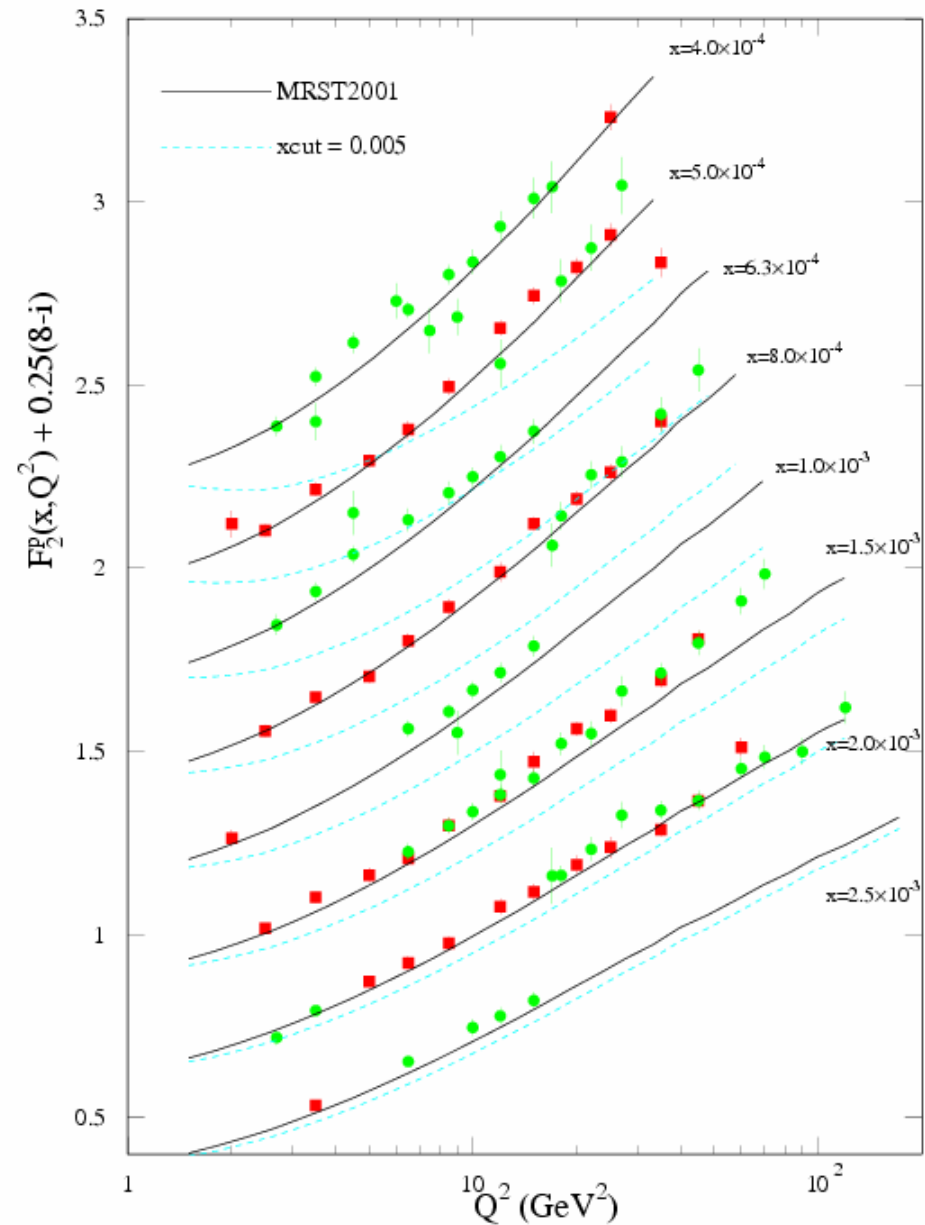
$$P_{qg} \rightarrow P_{qg}^{\text{NLO}} + B\alpha_S \frac{n_f}{3\pi} \bar{\alpha}_S^4 \left(\frac{\ln^3 1/x}{3!} - \frac{\ln^2 1/x}{2!} \right)$$

... with coefficients A , B found to be $O(1)$ (and different for the NLO, NNLO fits); the starting gluon is still very negative at small x however

the 'conservative' pdfs (blue lines) do not describe the very low x DIS data not included in the fit

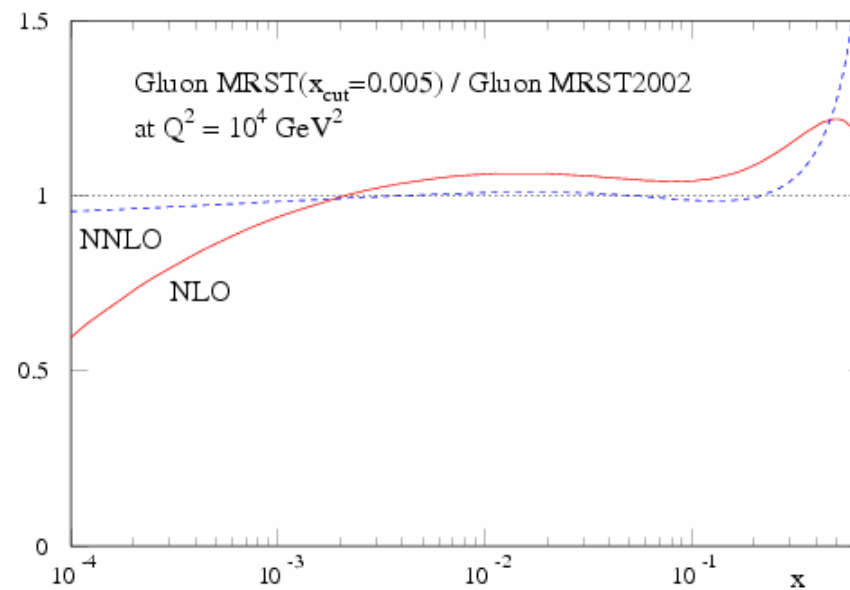
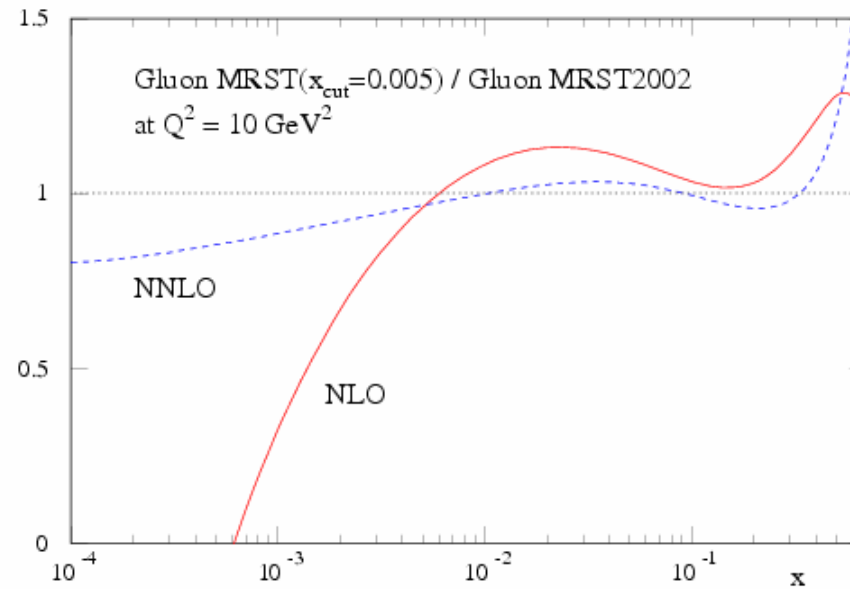
MRST, hep-ph/0308087

MRST(2001) NLO fit , $x=0.0004 - 0.0025$



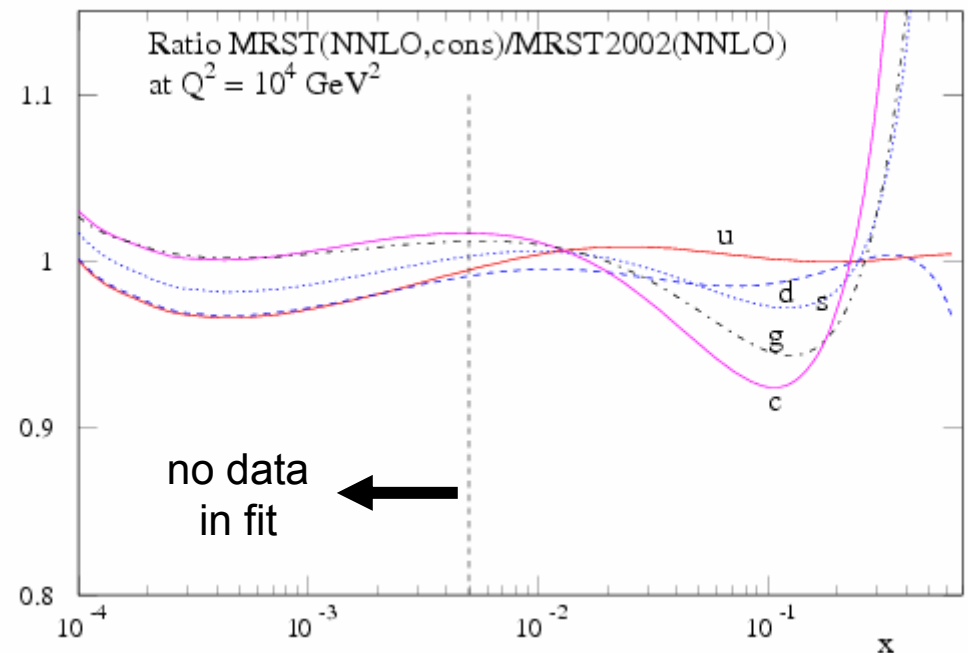
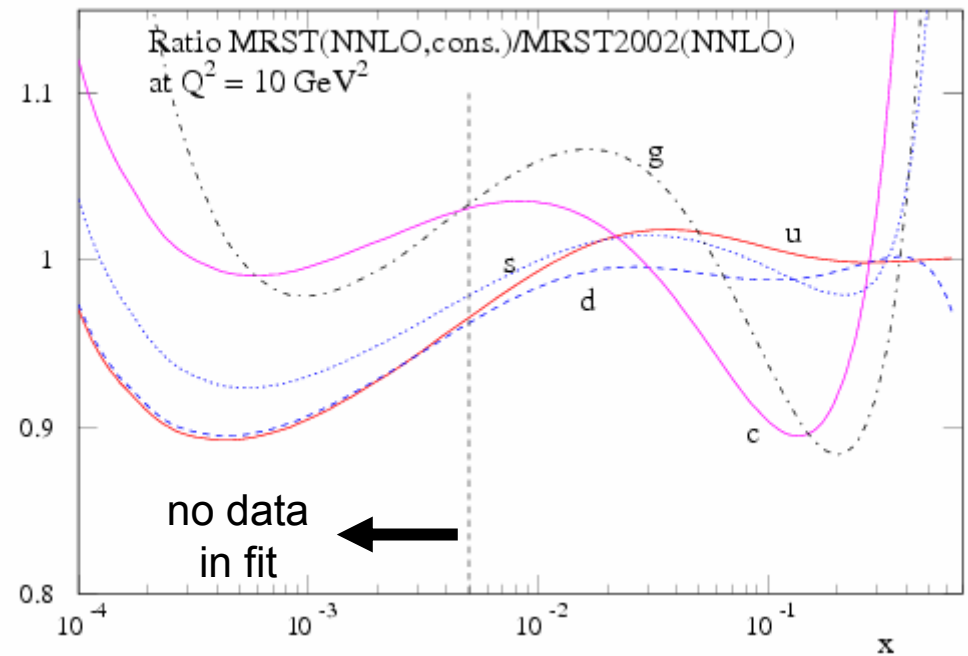
the change in the
NLO and **NNLO**
gluons when DIS
data with $x < 0.005$
are removed from
the global fit

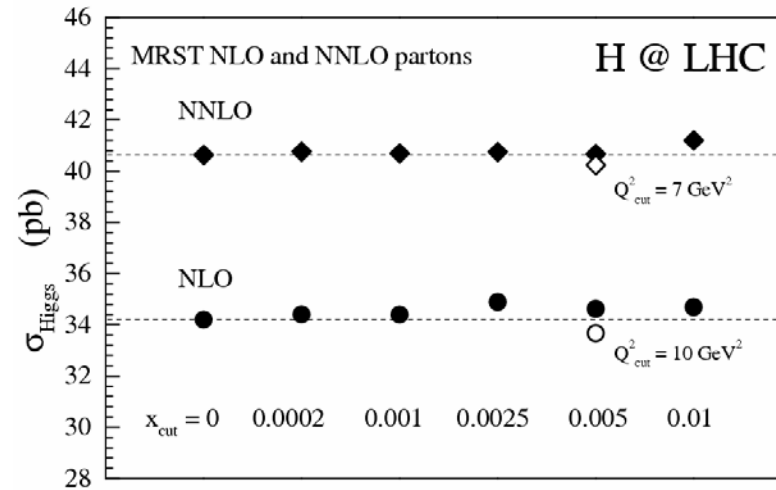
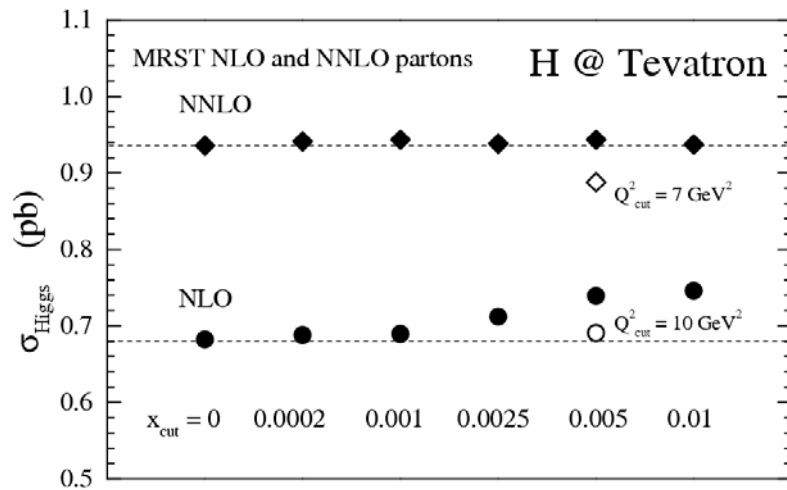
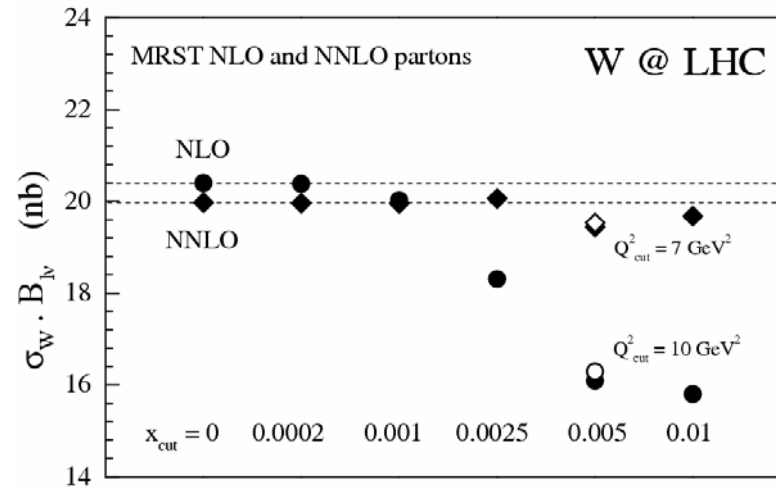
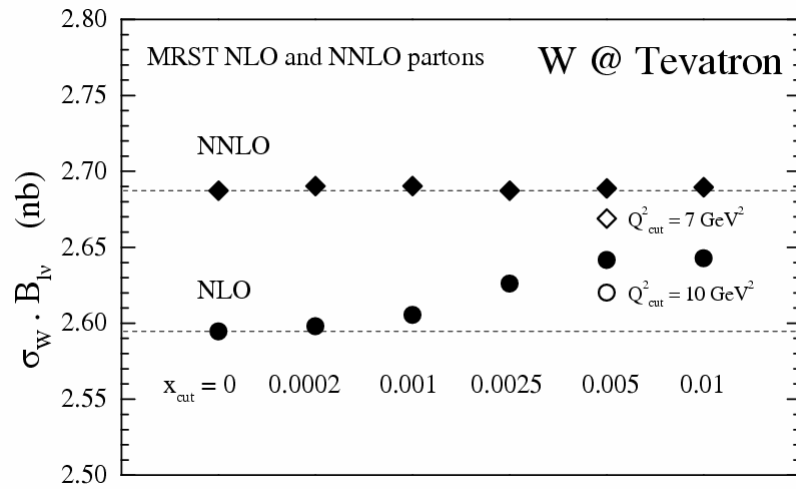
MRST, hep-ph/0308087



comparison of the standard MRST and 'conservative' NNLO pdfs

MRST, hep-ph/0308087





(LO) W cross sections
at the Tevatron and
LHC using (NLO)
partons from MRST,
CTEQ and Alekhin

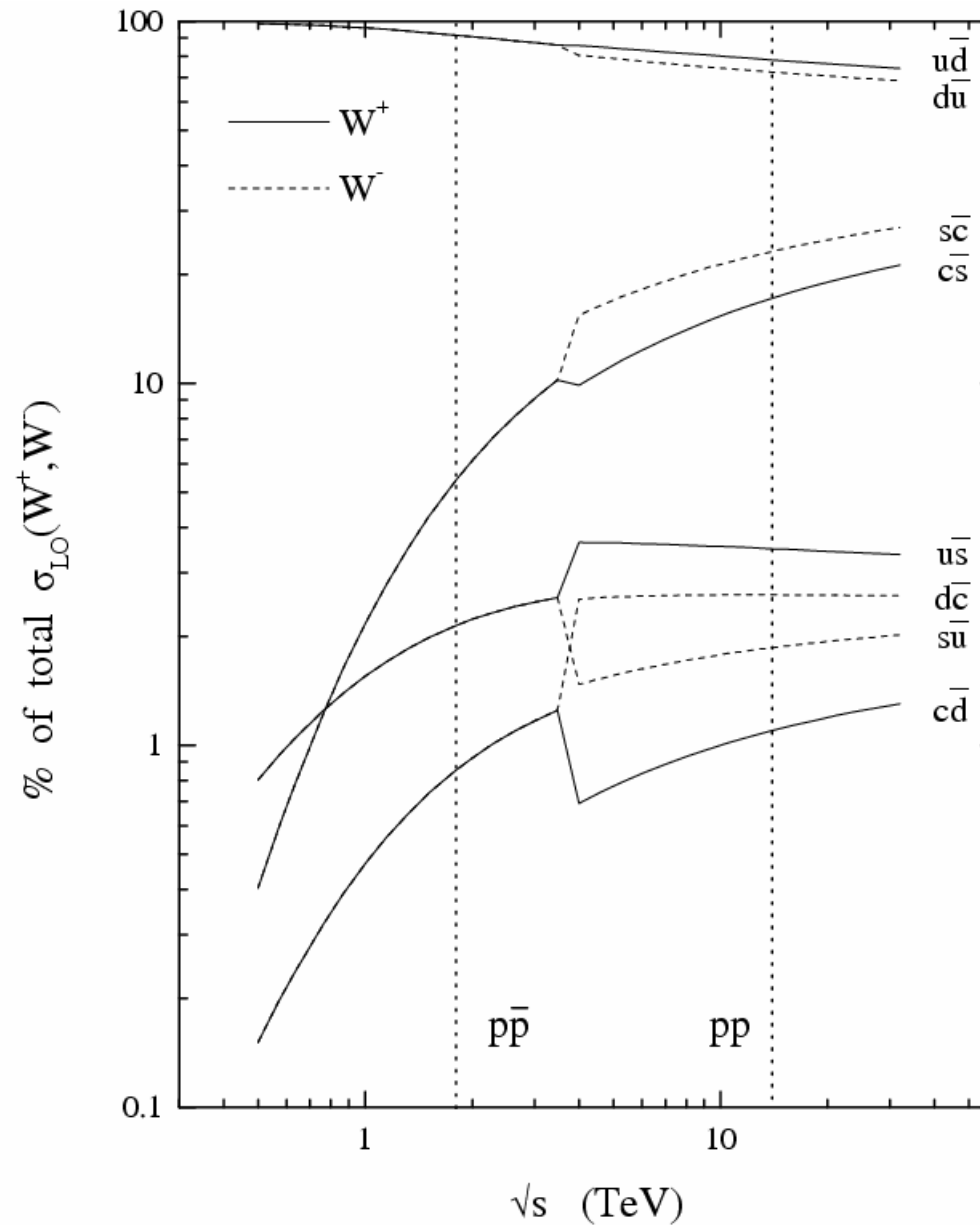
Tevatron	B. $\sigma(W)$ (nb)
MRST2002	2.14
CTEQ6	2.10
Alekhin02	2.22

LHC	B. $\sigma(W^+)$ (nb)	B. $\sigma(W)$ (nb)	W^+/W^-
MRST2002	10.1	7.6	1.33
CTEQ6	10.2	7.6	1.34
Alekhin02	10.7	7.9	1.35

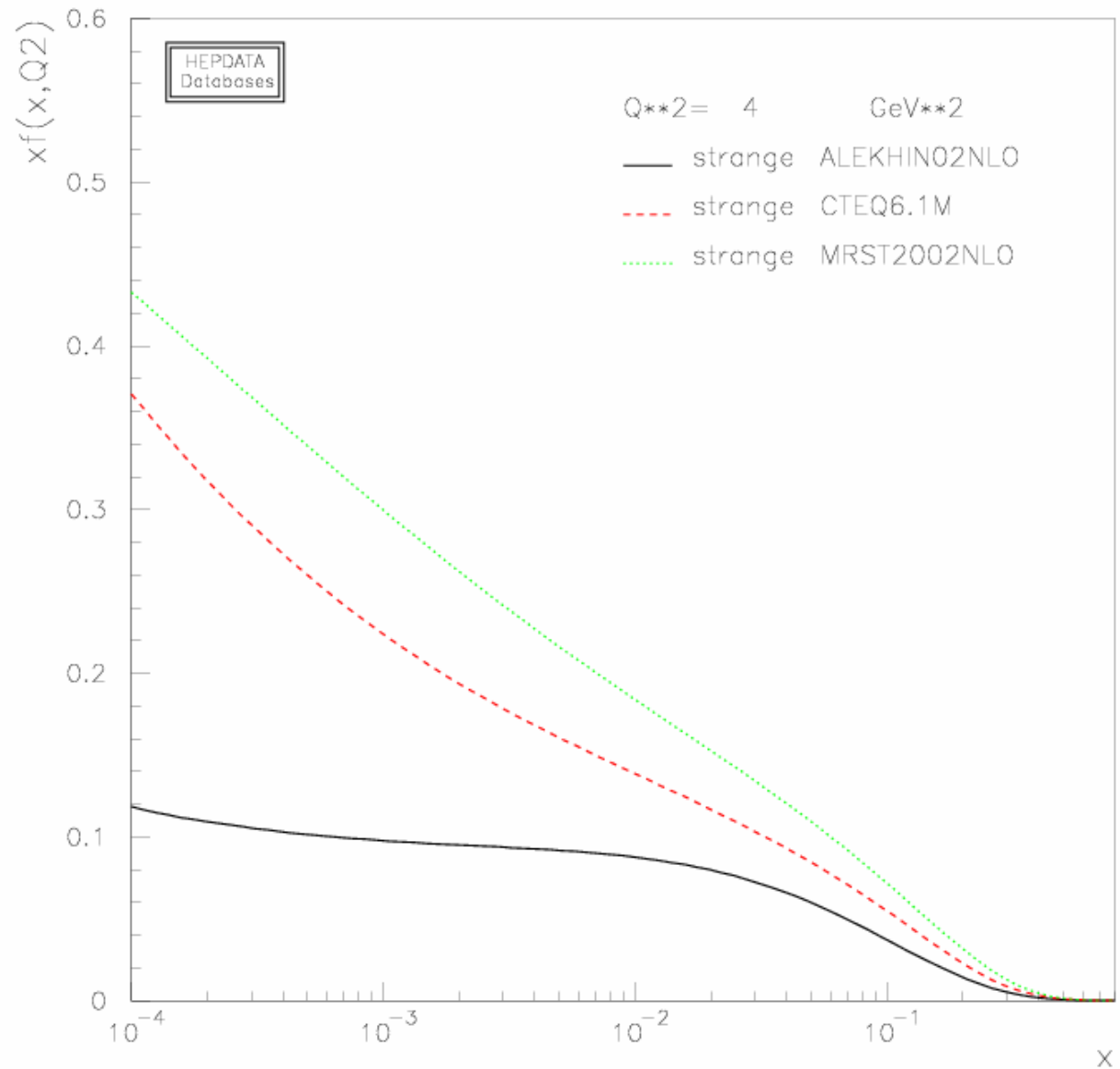
flavour decomposition of W cross sections at hadron colliders

recall that the only constraint on very small x quarks from inclusive DIS (F_2^{ep}) data is on the combination


$$\frac{4}{9} [u+c+u\bar{c}+c\bar{u}] + \frac{1}{9} [d+s+d\bar{s}+s\bar{d}]$$

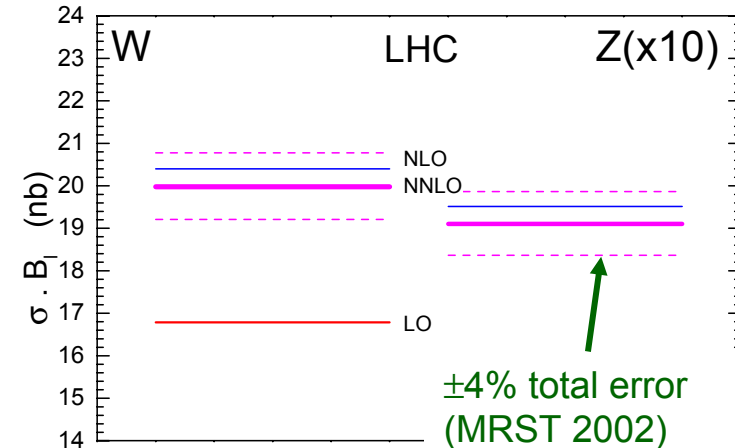
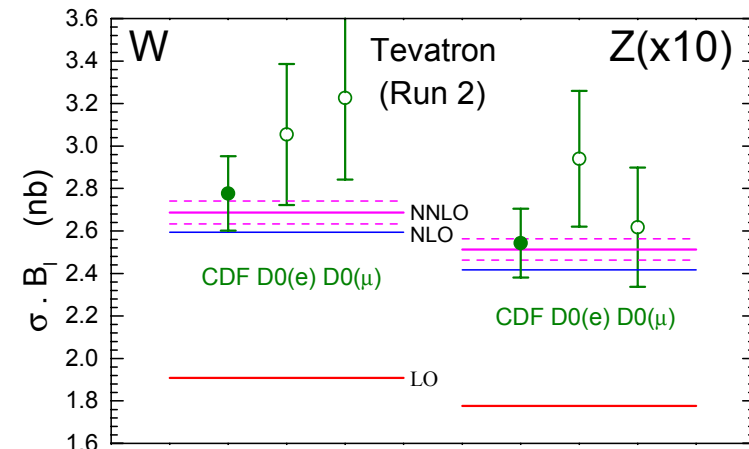


differences between the MRST, CTEQ and Alekhin strange quarks near the starting scale



NNLO precision phenomenology

- predictions calculated (MRST 2002) using 'old' approximate two-loop splitting functions
- width of  shows uncertainty from $P^{(2)}$ (biggest at small x)
- this uncertainty now removed, NNLO prediction unchanged



partons: MRST2002

NNLO evolution: van Neerven, Vogt approximation to Vermaseren et al. moments

NNLO W,Z corrections: van Neerven et al. with Harlander, Kilgore corrections