



HERA and the LHC  
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# New $p_{\perp}$ -ordered showers and Interleaved Multiple Interactions

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[hep-ph/0408302](https://arxiv.org/abs/hep-ph/0408302)

also [JHEP 03 \(2004\) 053 \[hep-ph/0402078\]](https://arxiv.org/abs/hep-ph/0402078)

# Transverse-momentum-ordered showers

1) Define  $p_{\perp\text{evol}}^2 = z(1-z)Q^2 = z(1-z)M^2$  for FSR  
 $p_{\perp\text{evol}}^2 = (1-z)Q^2 = (1-z)(-M^2)$  for ISR

2) Evolve all partons *downwards* in  $p_{\perp\text{evol}}$  from common  $p_{\perp\text{max}}$

$$d\mathcal{P}_a = \frac{dp_{\perp\text{evol}}^2}{p_{\perp\text{evol}}^2} \frac{\alpha_s(p_{\perp\text{evol}}^2)}{2\pi} P_{a \rightarrow bc}(z) dz \exp\left(-\int_{p_{\perp\text{evol}}^2}^{p_{\perp\text{max}}^2} \dots\right)$$

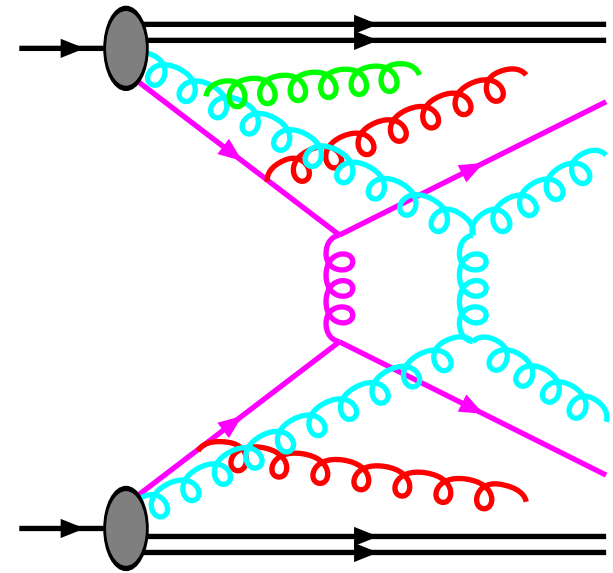
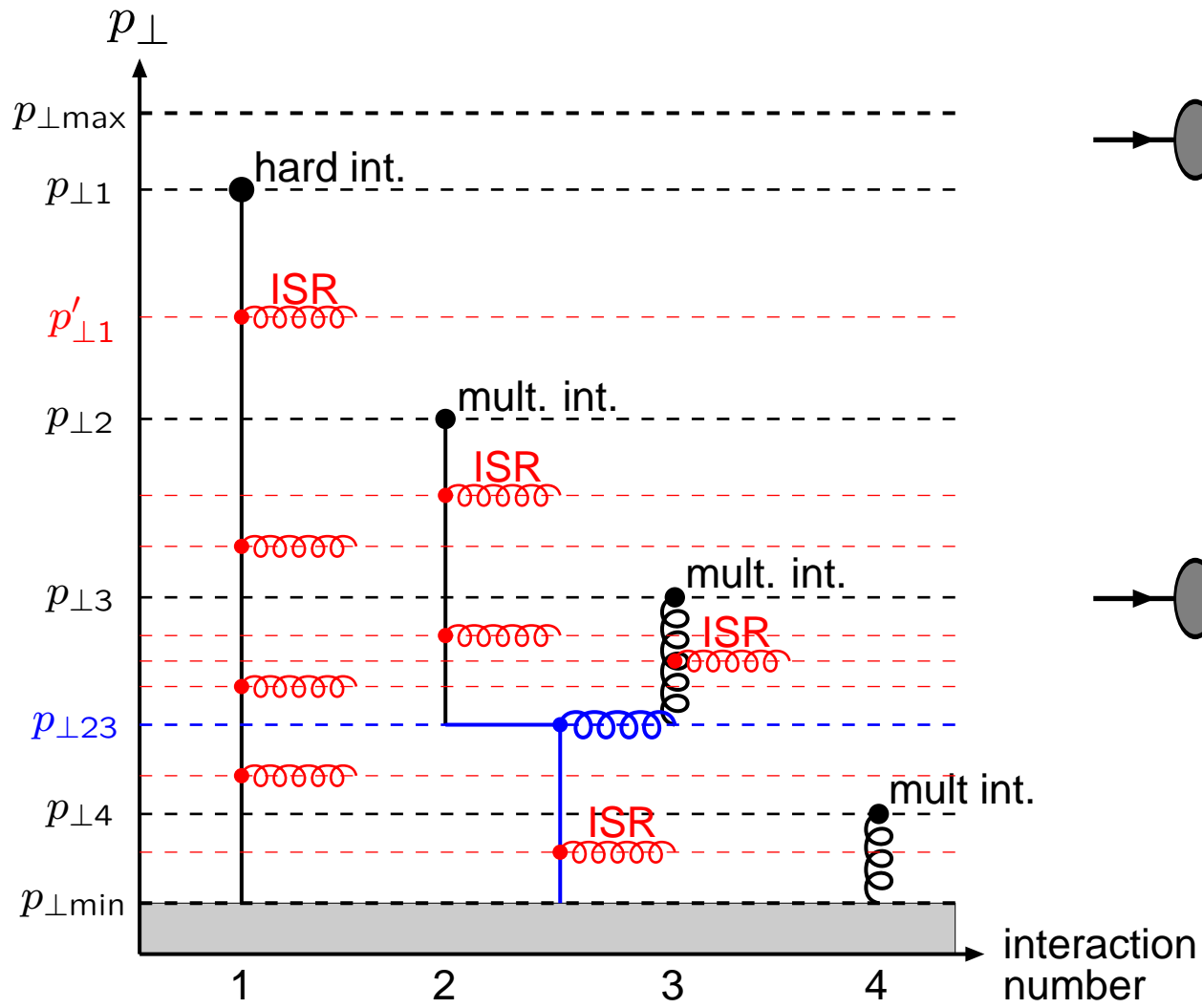
$$d\mathcal{P}_b = \frac{dp_{\perp\text{evol}}^2}{p_{\perp\text{evol}}^2} \frac{\alpha_s(p_{\perp\text{evol}}^2)}{2\pi} \frac{x' f_a(x', p_{\perp\text{evol}}^2)}{x f_b(x, p_{\perp\text{evol}}^2)} P_{a \rightarrow bc}(z) dz \exp(-\dots)$$

Pick the one with *largest*  $p_{\perp\text{evol}}$  to undergo branching; also gives  $z$ .

3) Kinematics: Derive  $Q^2 = \pm M^2$  by inversion of 1), but then interpret  $z$  as *energy fraction* (not lightcone) in “dipole” rest frame, so that *Lorentz invariant* and matched to matrix elements. Assume yet unbranched partons on-shell and shuffle  $(E, \mathbf{p})$  inside dipole.

4) *Iterate*  $\Rightarrow$  combined sequence  $p_{\perp\text{max}} > p_{\perp 1} > p_{\perp 2} > \dots > p_{\perp\text{min}}$ .

# Interleaved Multiple Interactions



- **Competition:** (for PDF and phase space)

$$\frac{d\mathcal{P}}{dp_{\perp}} = \left( \frac{d\mathcal{P}_{\text{MI}}}{dp_{\perp}} + \sum \frac{d\mathcal{P}_{\text{ISR}}}{dp_{\perp}} \right) \exp \left( - \int_{p_{\perp}}^{p_{\perp i-1}} \left( \frac{d\mathcal{P}_{\text{MI}}}{dp'_{\perp}} + \sum \frac{d\mathcal{P}_{\text{ISR}}}{dp'_{\perp}} \right) dp'_{\perp} \right)$$

⇒ one interleaved sequence of MI and ISR

FSR: no competition so not required (but nice for ME merging)

- **Regularization procedure:**

$$\alpha_s(p_{\perp}^2) \frac{dp_{\perp}^2}{p_{\perp}^2} \rightarrow \alpha_s(p_{\perp 0}^2 + p_{\perp}^2) \frac{dp_{\perp}^2}{p_{\perp 0}^2 + p_{\perp}^2}$$

common for MI (quadratically) and ISR by colour neutralization

$p_{\perp 0} \approx 2\text{--}3$  GeV energy-dependent (Tune A)

- **Availability:**

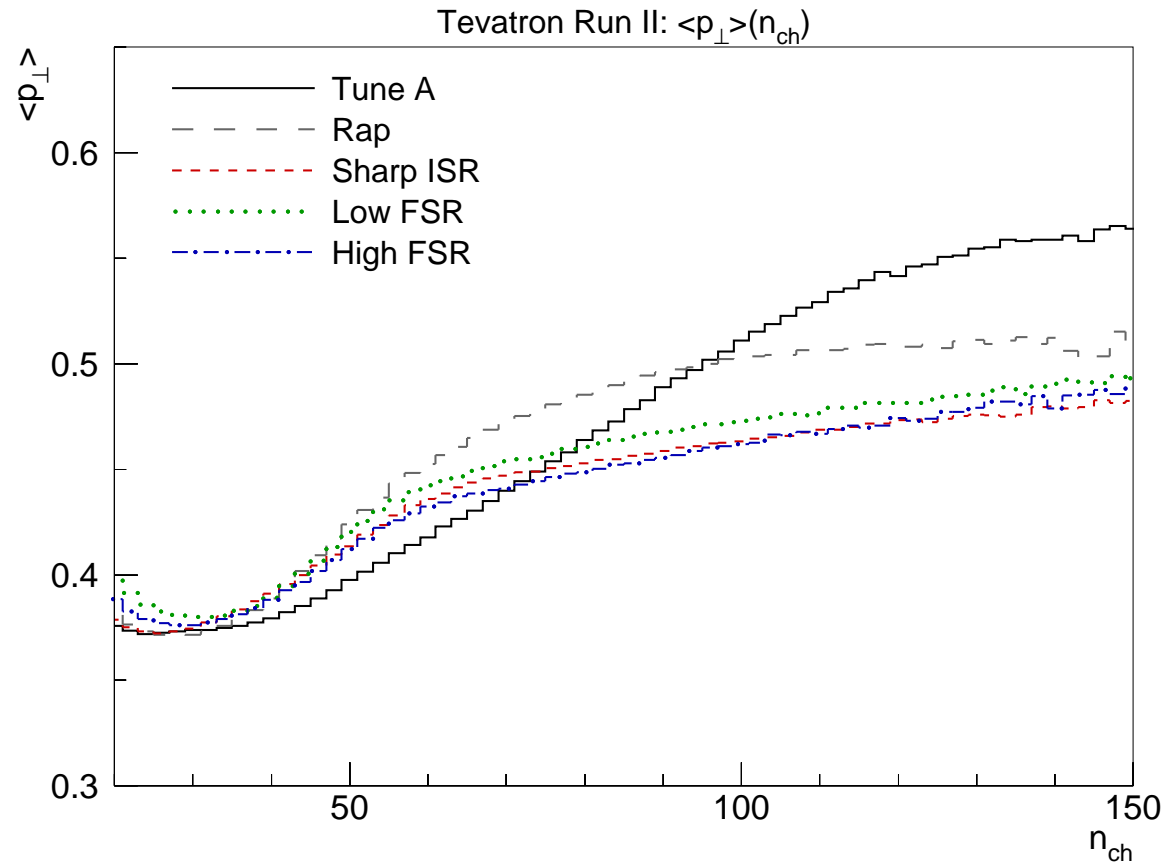
in PYTHIA 6.312 on [www.thep.lu.se/~torbjorn/Pythia.html](http://www.thep.lu.se/~torbjorn/Pythia.html)

**but pp/p $\bar{p}$  only** (technical + physics reasons)

- **Data comparisons:**

usually comparable with Tune A (for better or worse), but still in need of good tuning and detailed tests, and ...

...  $\langle p_{\perp} \rangle (n_{ch})$  problematical



⇒ how are final-state colours correlated?

• **Next steps:**

test and tune, especially colour flow

interleave FSR

intertwine =  $(3 \rightarrow 3) + 2$  interacting partons with same ancestry