

# Status of Hough Transform TPC Tracker



C.Cheshkov



# Outline

- Introduction
- Hough Transform (HT) approach:
  - Description of the algorithm
  - Practical implementation for fast filling of the Hough space
  - Hough space variables
- Recent improvements
- Results:
  - Efficiency, fakes
  - Resolution
  - Time consumption (!)
- Conclusions & Plans

# Introduction

- It has been already shown that the presented HT method:
  - Overcomes the common problems in high multiplicity PbPb events
  - Provides reasonably **high tracking efficiency and low fake tracks rate**
  - Can work not only as a seeding for consecutive cluster finder/fitter, but also as a **stand-alone tracking algorithm**
  - **Extremely fast**
- The recent developments were oriented towards:
  - Further **speeding up**  $\Rightarrow$  To be able to track central PbPb events **online**, by means of purely software version of HT
  - Adding **dEdx** reconstruction  $\Rightarrow$  **online PID**
  - Studies of the sources of inefficiencies and fakes

# Hough Transform method

- Hough Transform method:
  - Transformation of TPC Digit coordinates into curve in the track parameter space (Hough space). The curve corresponds to all possible tracks the digit can belong to
  - The transformation is done in  $\eta$  bins
  - Assume that the tracks are coming from the primary vertex
  - Neglect multiply scattering and energy losses
- Each space bin represents a track candidate  
⇒ one can define a certain "road" within a given TPC sector
- The approach consists simply in counting of the number of TPC rows without a digit inside the track "road" - #gaps

# Hough Transform method

- After the HT is finished, a simple peak finder runs over the Hough space in order to extract the track candidates
- The peak finder looks for **neighbor bins** with **#gaps < N** and identifies the peaks (track candidates)
- Track parameters are extracted by **averaging** the **peak edge points**  
⇒ track is guided by the **cluster borders**

# Hough Transform method

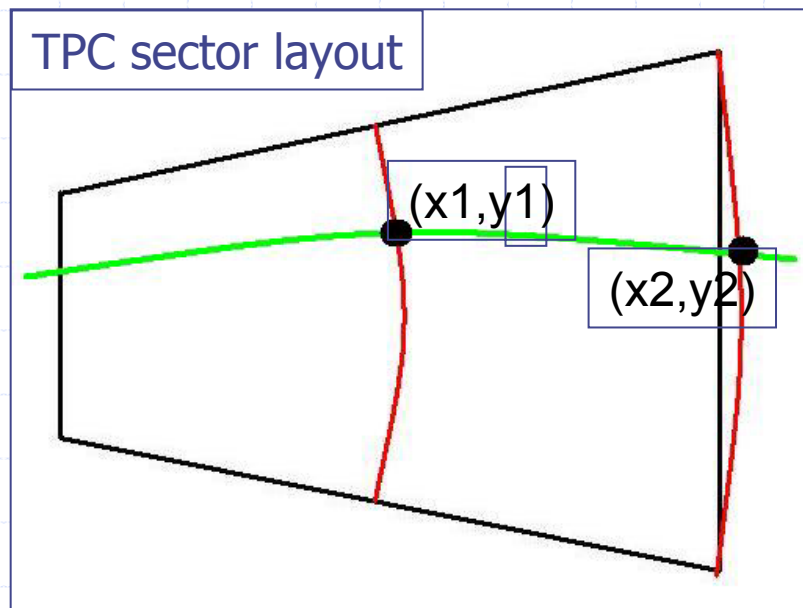
- Assuming **ordered TPC digits** (in time bins, pads, padrows)  
⇒ **the algorithm offers big space for speeding up!**
- HT is **monotonic** along the padrows  
⇒ do it only for the **first and last** (in pad index direction) digits which belong to a cluster and **fill at once the corresponding ribbon** in the HT space
- **Stopping rule** using already accumulated **#gaps**

# Hough Space variables

- Initially Hough space defined by track curvature  $k(=1/R)$  and emission angle  $\Psi$
- Two main problems:
  - The variables are **strongly correlated**  $\Rightarrow$  “Butterfly”-like shape of the peaks
    - complex peak finder
    - relatively high fake peak rate
  - **Non-linear** functions in the filling of HT space
    - Need in LUTs inside HT filling loop
    - “Time consuming” FP operations inside HT filling loop
- **Better solution was found**

# Hough Space variables

- **Conformal Map transformation variables were chosen:**
  - Variables connected to the **physical setup of the TPC**
  - Variables which lead to **linear HT**



- Lets define two curves inside a TPC sector by

$$x/R^2 = \text{constant} = \beta_1(\beta_2)$$

- Each primary track is represented by two points on these curves
- One can parameterize the track using:  
 $\alpha_1 = y_1/R_1^2$  and  $\alpha_2 = y_2/R_2^2$
- Conformal map coordinates of each space-point along the track trajectory are connected by linear expression



# Hough Space variables

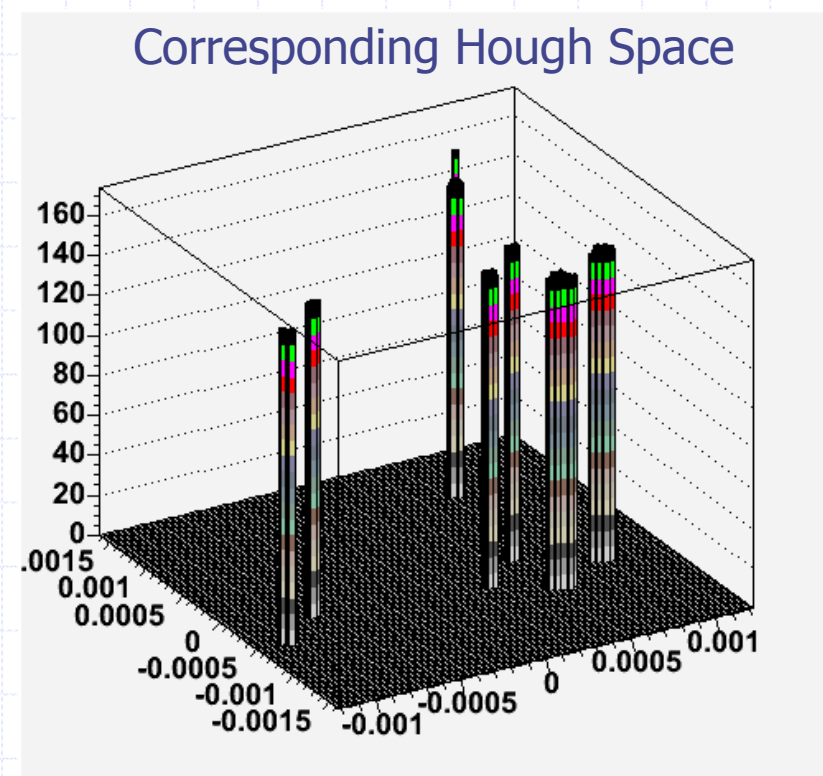
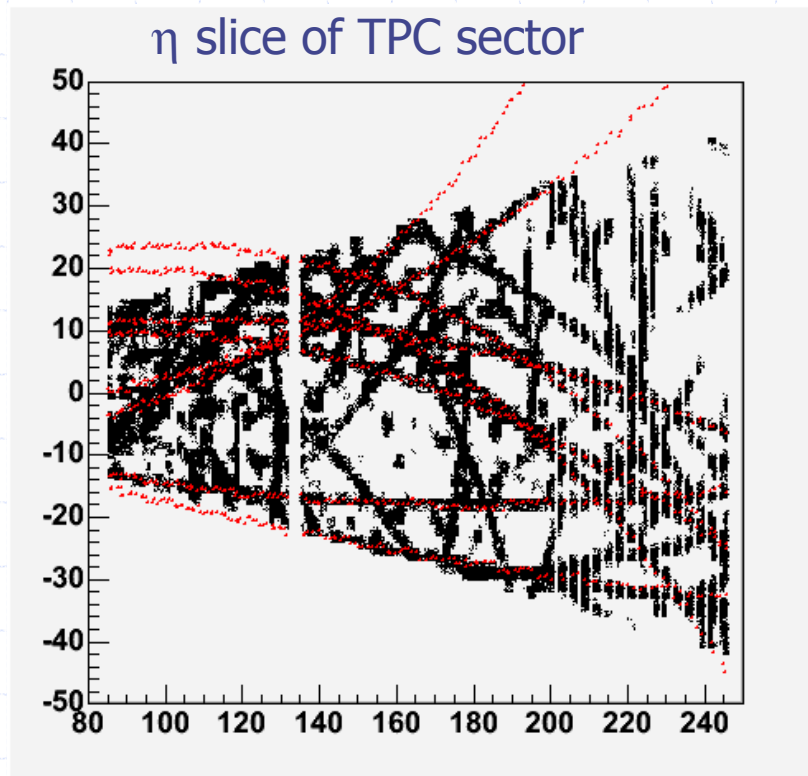
- One can use the variables  $\alpha_1$  and  $\alpha_2$  to define the Hough space
- In this way each space-point inside a TPC sector will be represented in the Hough space by a **straight line**:

$$\alpha_1 = A + B \alpha_2$$

## Linear filling of the Hough space

- The parameters A and B are calculated in advance and used via **LUTs**
- In order to keep HT monotonic and Hough peaks uncorrelated: curve  $\beta_1$  – in middle and curve  $\beta_2$  – at the outer edge of the TPC sector

# Example



- **Uncorrelated** and easily detectable Hough peaks
- Linear HT  $\Rightarrow$  Gain of **30-40%** in the time consumption

# Hough Space variables

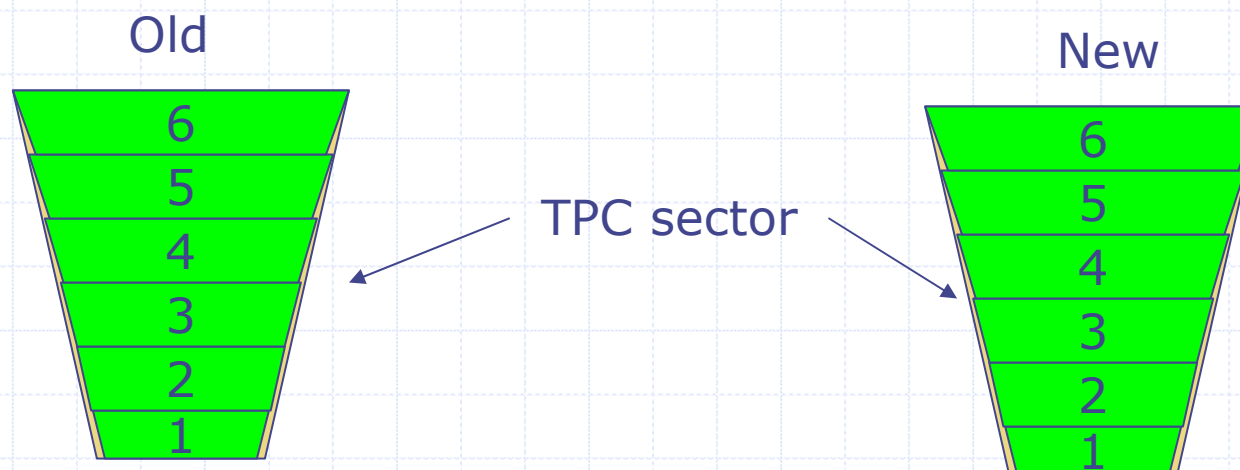
- Limits on Hough space variables correspond to a track with minimum  $P_t[\text{GeV}/c] = B_{\text{field}}[\text{T}]$  which crosses the middle of the TPC sector
- Hough space binning is fixed to  $\sim$  twice the pad size in the corresponding TPC rows  $\Rightarrow 80(\alpha 1) \times 120(\alpha 2) \times 100(\eta)$

# Recent improvements

- All the recent changes are aimed to **speed up the code** and do not affect the algorithm efficiency
- There are no revolutionary improvement – all the changes give an **effect of 30-50%**
- The overall speed-up factor is  **$\sim 3$**

# Recent improvements

- Change in the order in which the readout patches are processed
- Choose an order which allows the **earliest possible removal of track candidates** (Hough space bins)
- Why **patches 6 and 3** before others? Digits in patch 6 – horizontal lines in the Hough Space, in patch 3 – vertical lines  
⇒ **the crossings of these lines gives sort of seeding**



# Recent improvements

- **Selective filling of the Hough space:**
  - For each bin of the hough space assign pointers to the closest possible track candidate (bin)
  - Update the pointers after each processed readout patch
  - Use the pointers to jump in the hough space during the filling process
- **Floating operations used to calculate the cluster properties in the hough space  $\Rightarrow$  pre-calculated LUTs**
  - Conformal mapper variables as a hough space variables
  - Therefore a TPC cluster is represented by 2 straight lines:  
 $\Rightarrow$  2 offsets and 2 slopes

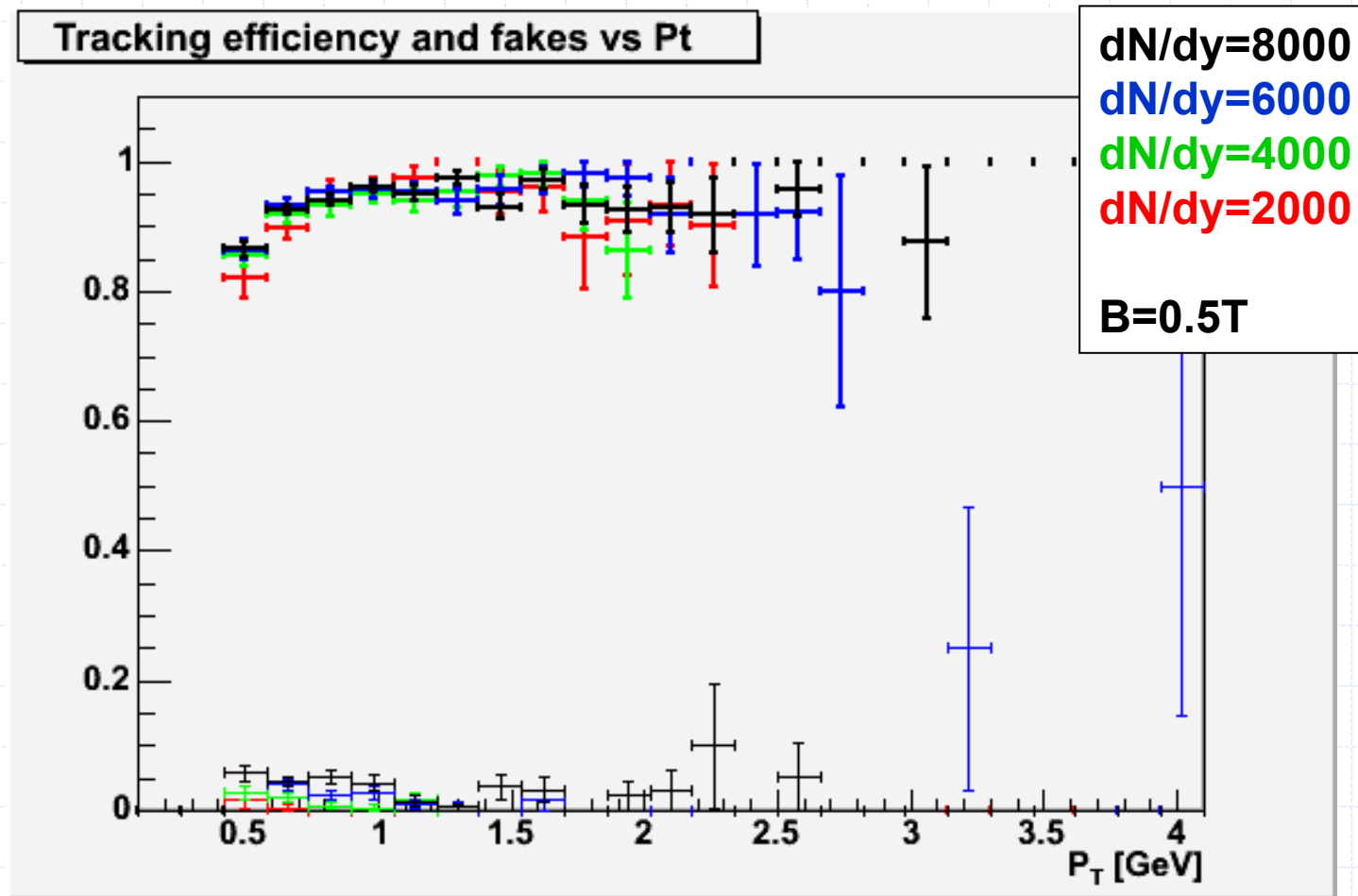
# Results: Efficiency, resolution and timings

# Definitions

- The method requires **new definitions** in order to determine the performance:
  - No clusters associated
    - ⇒ assign **only 1** MC label to each track
  - High occupancy (and therefore overlapping clusters) in general **does not affect** the track parameters, but cause **appearance of “ghosts”**
    - ⇒ fakes tracks → ghost tracks
  - If more than 1 track with the same MC label, take **randomly** one as good and second as fake (or ghost)
- Good tracks – from offline comparison macro



# Tracking Efficiency

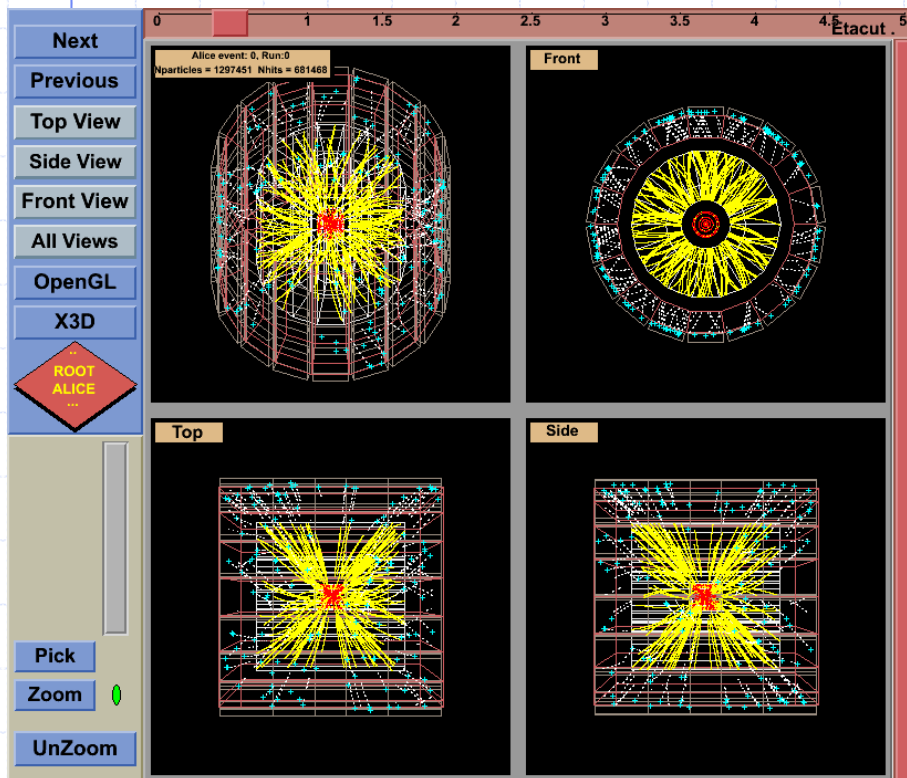


# Inefficiency Sources

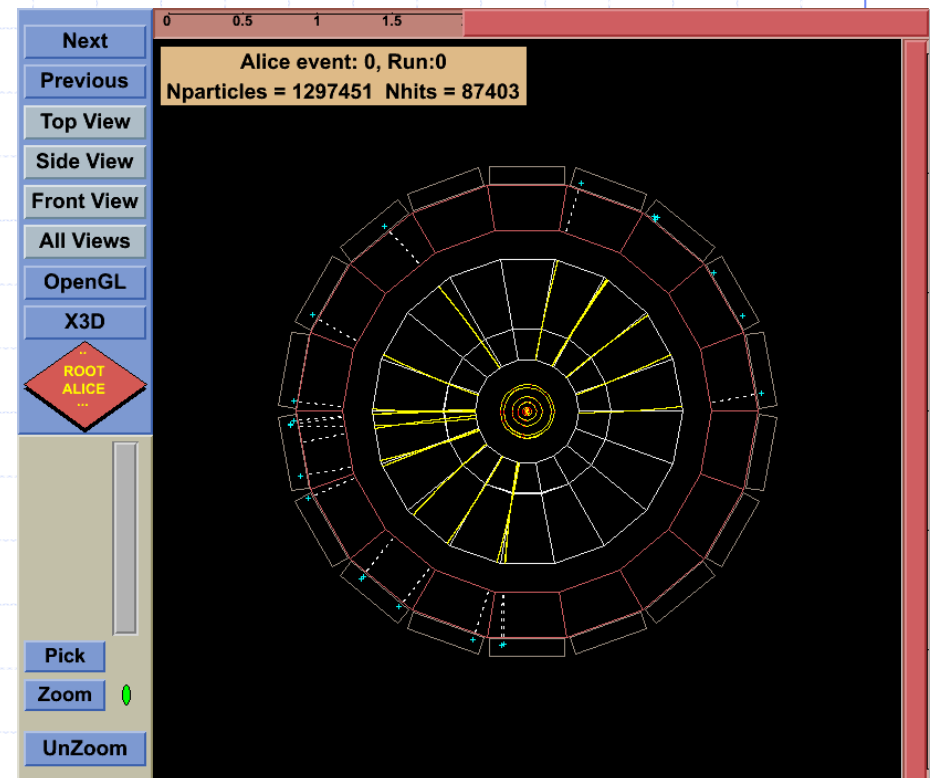
1. **Merging** of the tracks (**1-2%** for  $dN/dy=8000$ ,  $0.4T$ ) when:
  - they **overlap** in the hough space
  - they are **close to each other** and one is removed during the track merging (**both in hough space and  $\eta$  bins**)
2. **Low pt tracks at high  $\eta$**  ( $\rightarrow 1$ ).
  - The  $\eta$  bins efficiently get narrower
  - Mult.scat. in ITS & dead zone
  - $\eta$  binning (during binning we assume straight tracks)
3. Tracks **close to the TPC sector borders** (affects mainly tracks with  $Pt > 1-1.5\text{GeV}/c$ )

# Inefficiency Sources

## Low Pt tracks



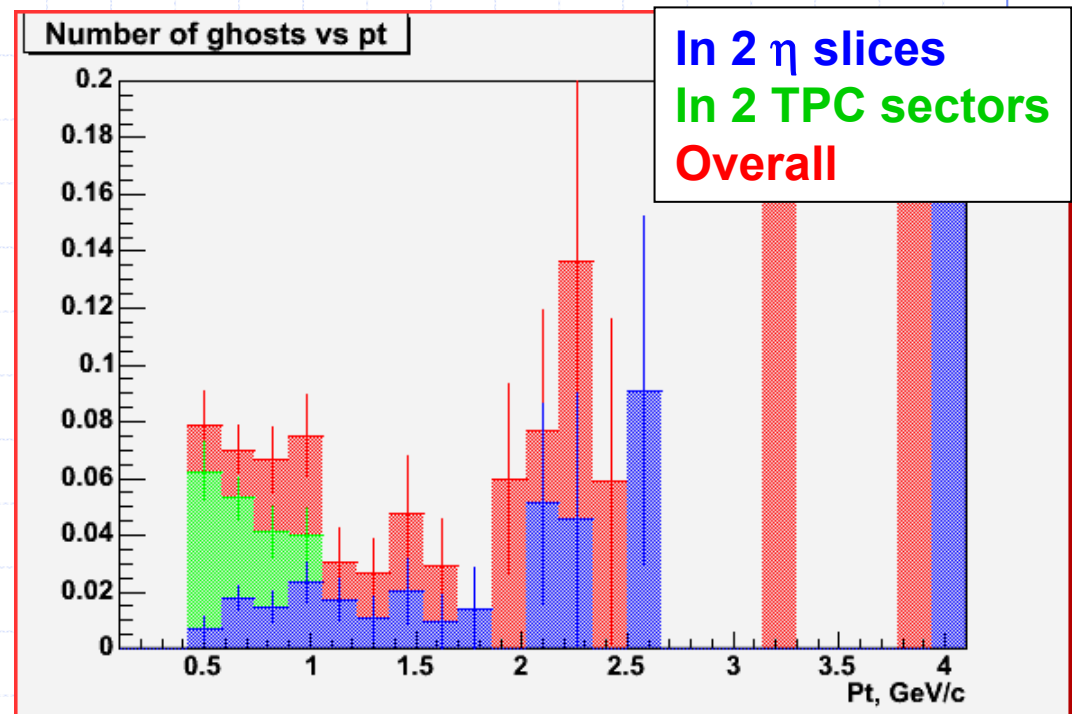
## Tracks with $1.5 < Pt < 2$ GeV/c



# Ghost Tracks

- Tracks found in 2  $\eta$  slices or 2 neighbor sectors can be further suppressed by more complex track merging procedure
- However ITS tracking "removes" almost completely these ghosts  $\Rightarrow$  no real need in further merging

$dN/dy=8000, 0.5T$



# Resolution

- Since the Hough space bin size  $\sim 1/Pt$   
 $\Rightarrow \Delta Pt/Pt \sim Pt + \text{const. (mult.scatt.)}$
- **$\Delta Pt/Pt = (1.8xPt + 1.0)\%$  (B=0.5T)**
- **$\sigma(\Psi) = 6.1\text{mad}$ ;  $\sigma(\eta) = 5.5 \times 10^{-3}$**
- No significant dependency on the event multiplicity can be seen – need more statistics

# Timing performance

- The benchmarks were done on Itanium II machines ( $\sim 1300$  SpecInt's) – the present Alice GDCs
- Code compiled with icc8.0 with  $-O3$
- Almost a factor of 3 improvement due to the latest improvements in the filling of the Hough space
- LUT initialization is done of event-by-event basis  $\Rightarrow$  more flexibility if one wants to adapt the HT resolution depending on the trigger

dN/dy	$\sim 0$	2000	4000	6000	8000
LUT Init	120ms				
Hough Transform	0.7s (3ms/patch)	3.3s (15ms/patch)	5.9s (27ms/patch)	8.7s (40ms/patch)	11.3s (53ms/patch)

# Conclusion and Outlook

- Hough Transform tracker shows very good efficiency and resolution (see also Constantin's transparencies on jet analysis)
- Taking into account the presented timing performance, one should consider seriously HT as a possible online tracking for HLT (details in my talk on online monitoring)
- The work on adding dEdx reconstruction is underway (see tomorrow's talk)
- Important feedback expected from the physics analysis of PDC'04 data
- The algorithm (together with HLT ITS tracker) will be tested in close to real conditions during the Alice computing DC in 2005