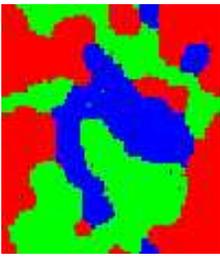


# Deconfinement and Quarkonium Suppression

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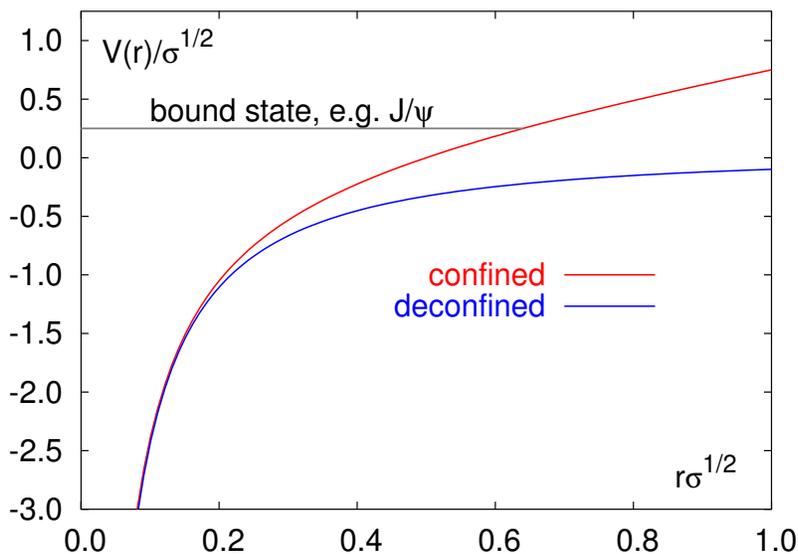
- Deconfinement, screening and asymptotic freedom
  - deconfinement is density driven
- Heavy quark free energies
  - screening sets in at short distances;  $1/r$  still dominant scale
- Potential models for quarkonium
  - dissociation may spoil sequential suppression pattern
- Spectral functions
  - (directly produced)  $J/\psi$  exist well above  $T_c$
- Charmonium in heavy ion collisions
  - sequential suppression pattern may be the smoking gun



# Deconfinement $\Rightarrow$ screening $\Rightarrow$ quarkonium suppression

The Matsui-Satz argument:

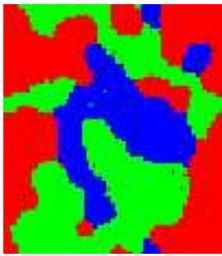
- deconfinement  $\Rightarrow$  screening  
 $\Rightarrow$  no heavy quark bound states in a QGP



$V_{\bar{q}q}(r, T) \rightarrow \infty$  confinement

$V_{\bar{q}q}(r, T) < \infty$  deconfinement

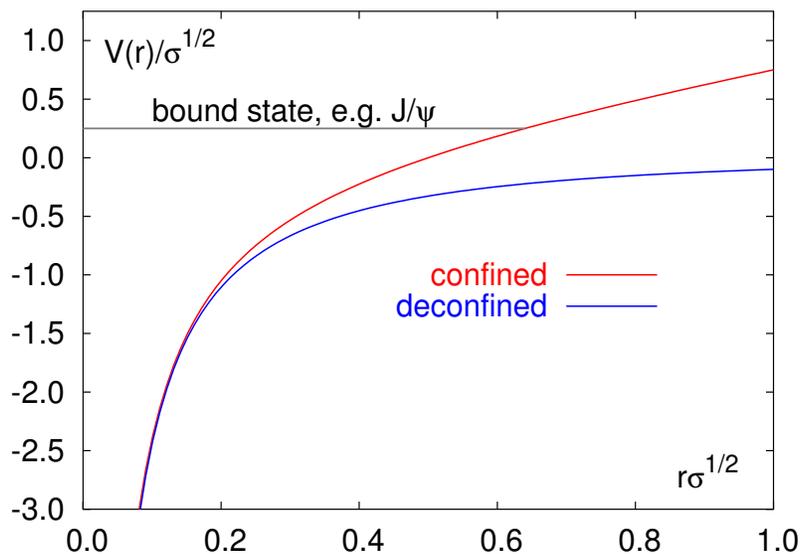
- heavy  $q\bar{q}$ -pairs are rare states in a QGP  
 $\Rightarrow$  dissolved pairs never recombine



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- deconfinement  $\Rightarrow$  screening  
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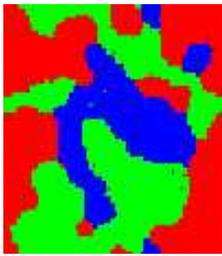


$V_{\bar{q}q}(r, T) \rightarrow \infty$  confinement

$V_{\bar{q}q}(r, T) < \infty$  deconfinement

**$J/\psi$  suppression**

- heavy  $q\bar{q}$ -pairs are rare states in a QGP  
 $\Rightarrow$  dissolved pairs never recombine



# Deconfinement

## and asymptotic freedom

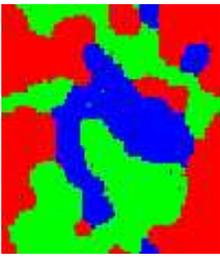
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asymptotic freedom  $\Rightarrow$  deconfinement (the original concept):

- N. Cabibbo, G. Parisi, Exponential Hadronic Spectrum and Quark Liberation, PL B59 (1975) 67;
- J.C. Collins, M.J. Perry, Superdense Matter: Neutrons and asymptotically free quarks? PRL 34 (1975) 1353

- deconfinement is a consequence of asymptotic freedom
- deconfinement  $\Leftrightarrow$  liberation of many new degrees of freedom, asymptotically free  $q\bar{q} + g$  gas
- deconfinement is density driven

↑ evidence from LGT



# Confinement and deconfinement



## confinement

- stick together, find a comfortable separation
- controlled by confinement potential

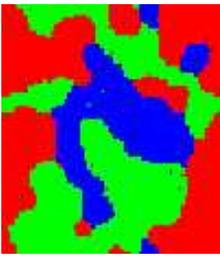
$$V(r) = -\frac{4}{3} \frac{\alpha(r)}{r} + \sigma r$$



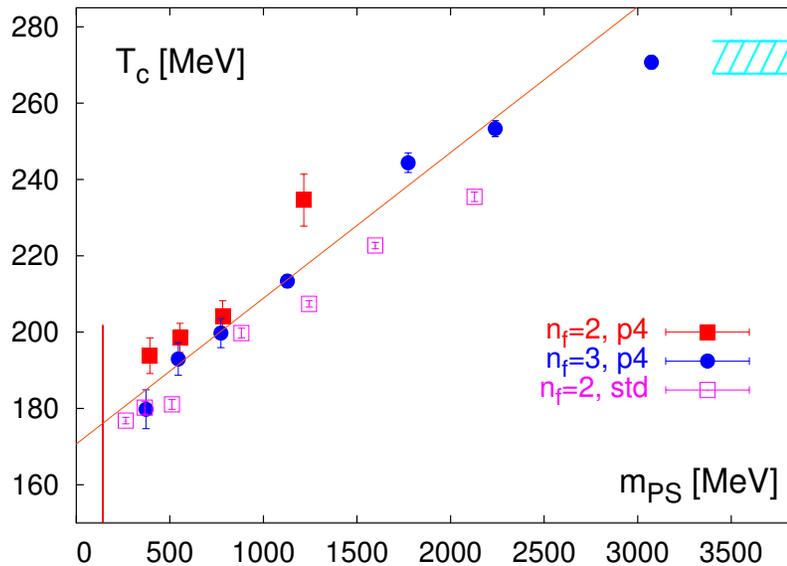
## deconfinement

- free floating in the crowd
- average distance always smaller than  $r_{af}$ :

$$r_{af} = \sqrt{\frac{4}{3} \frac{\alpha(r)}{\sigma}} \simeq 0.25 \text{ fm}$$



# Density driven transition: Critical temperature & EoS



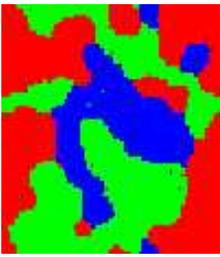
$m_{PS} \simeq 140 \text{ MeV} : T_c \simeq 175 \text{ MeV}$

$m_{GB} \simeq 1.5 \text{ GeV} : T_c \simeq 265 \text{ MeV}$

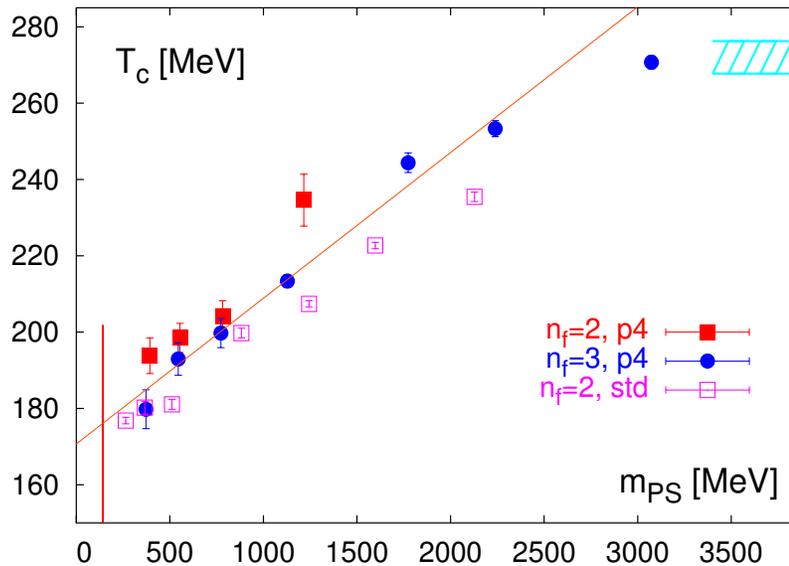
$(m_{PS} = \infty)$

lightest masses apparently do

not control the transition



# Density driven transition: Critical temperature & EoS

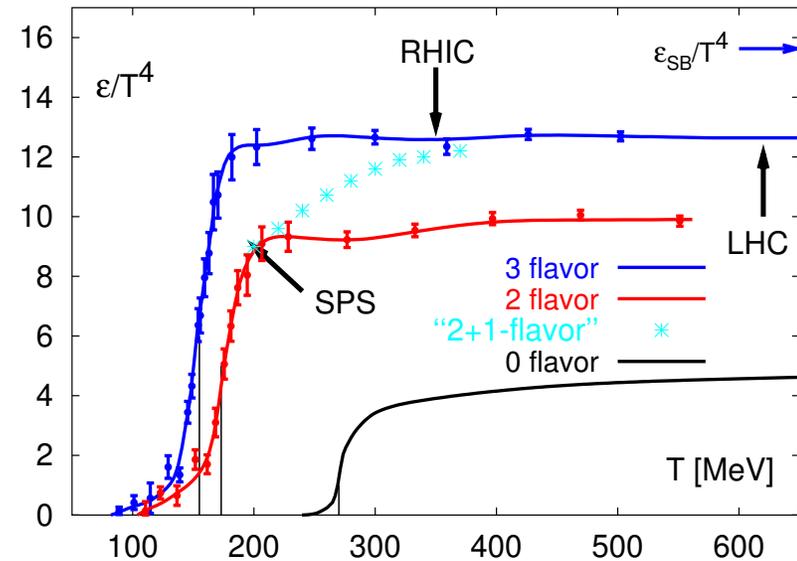


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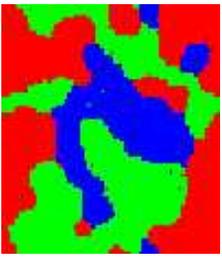
$$n_f = 2 : \epsilon_c \simeq (6 \pm 2) T_c^4$$

$$\simeq (0.3 - 1.3) \text{ GeV}/\text{fm}^3$$

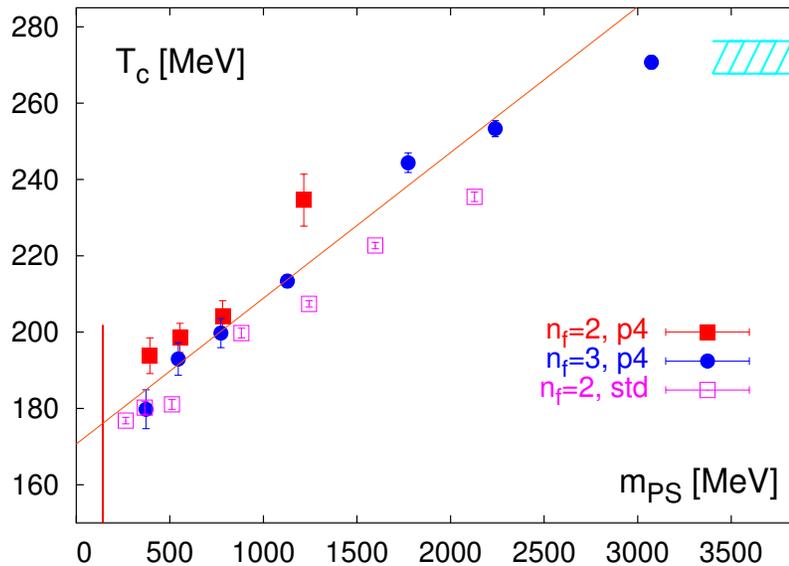
$$n_f = 0 : \epsilon_c \simeq (0.5 - 1) T_c^4$$

$$\simeq (0.3 - 0.7) \text{ GeV}/\text{fm}^3$$

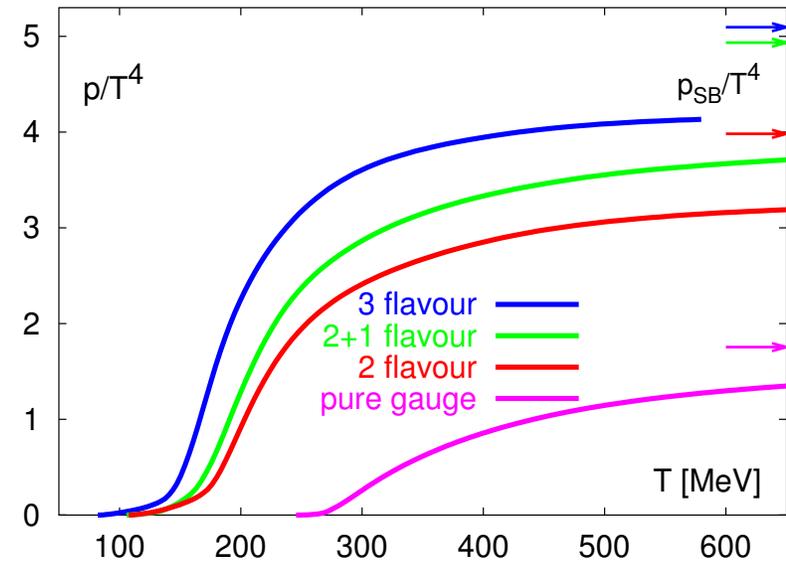
change in  $\epsilon_c/T_c^4$  compensated by shift in  $T_c$   
transition sets in at similar energy (or parton)  
densities  $\Rightarrow$  percolation



# Density driven transition: Critical temperature & EoS



$$m_{PS} \simeq 140 \text{ MeV} : T_c \simeq 175 \text{ MeV}$$

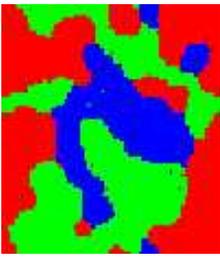


$$\text{parton density (ideal gas): } n \equiv p/T$$

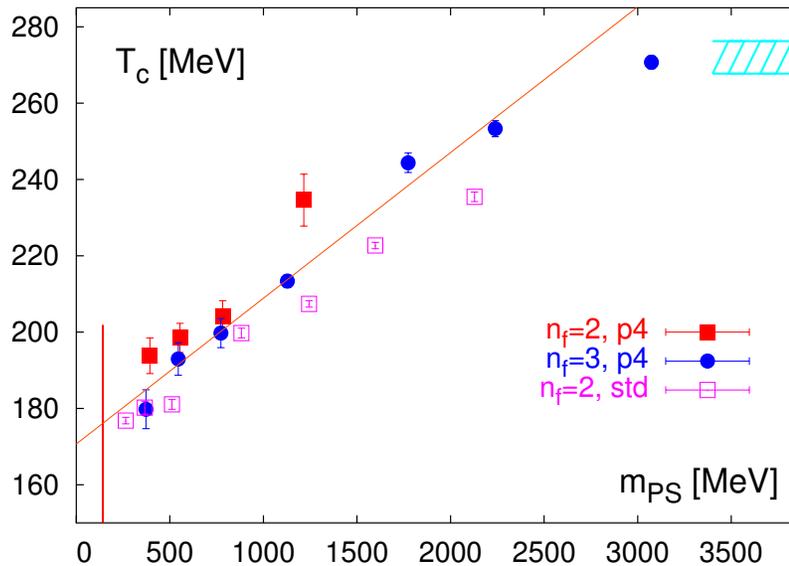
$$\text{Debye screening radius: } r_D \sim 1/g(T) \sqrt{n/T} \\ \sim 1/g T$$

rapid change across  $T_c$ :

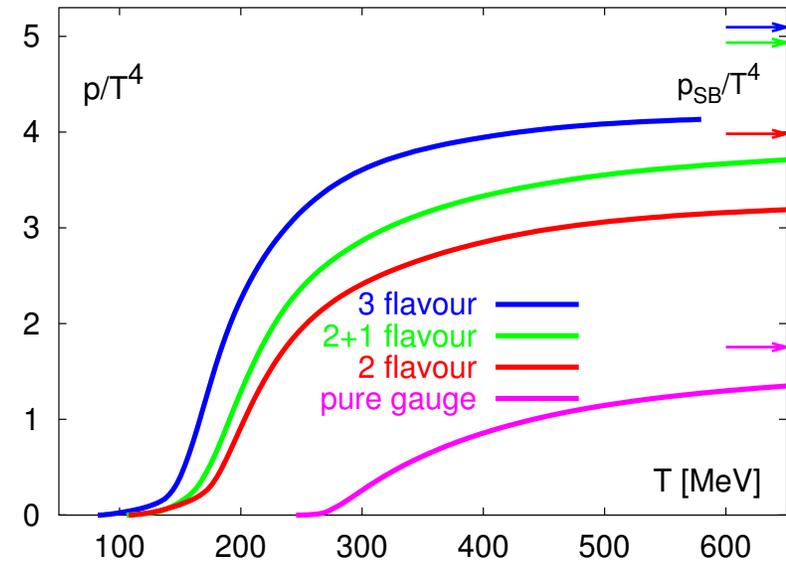
$$r_D/T \sim 1/g(T) \sqrt{p/T^4}$$



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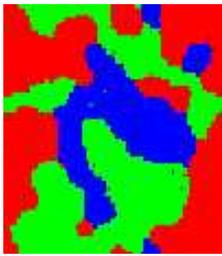


parton density (ideal gas):  $n \equiv p/T$

Debye screening radius:  $r_D \sim 1/g(T)\sqrt{n/T}$

constant parton density in an ideal gas:

$$\frac{T(m_\pi = \infty)}{T(m_\pi = 0)} = \left(1 + \frac{21}{4} \frac{n_f}{N_c^2 - 1}\right)^{1/3} \simeq 1.3 - 1.5$$



# Heavy quark free energies: Testing $\bar{q}q$ interactions in matter

- Static quark and anti-quark sources in a thermal heat bath

↗ change in free energy due to presence of external sources

L.G. McLerran, B. Svetitsky, Phys. Rev. D24 (1981) 450

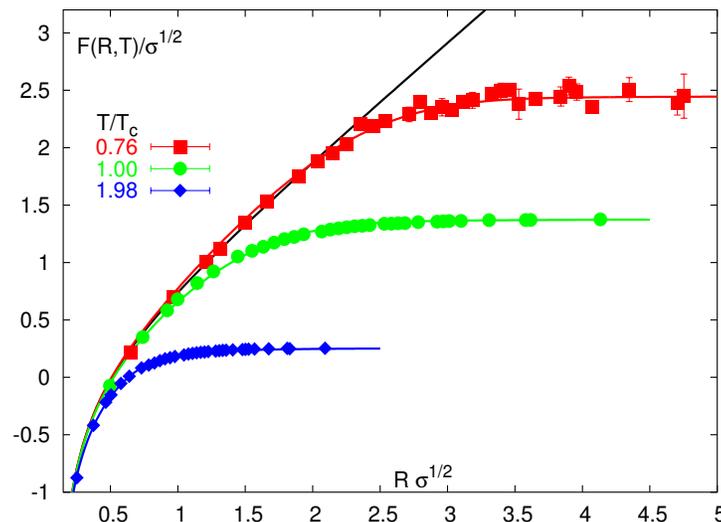
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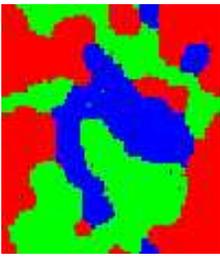
- asymptotic freedom, screening, string breaking

singlet free energy  
in 2-flavor QCD  
( $m_q/T = 0.4$ )

O.Kaczmarek, F. Zantow;  
similar:

P.Petreczky, K. Petrov





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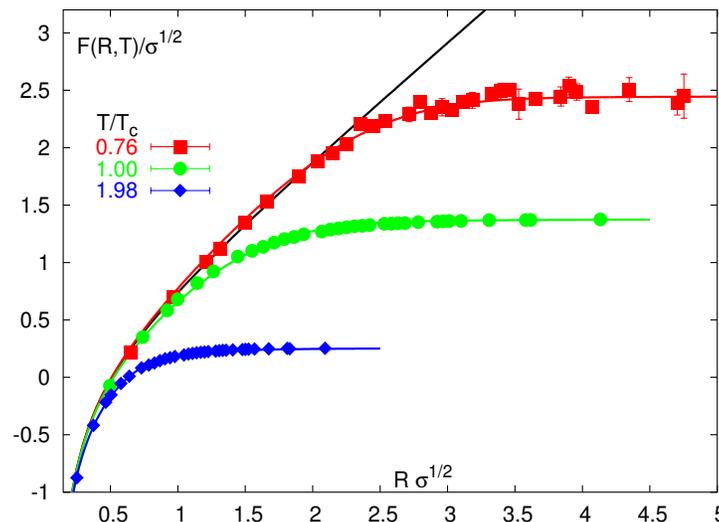
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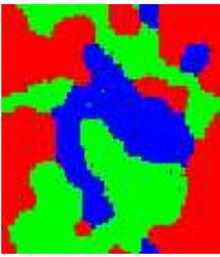
P.Petreczky, K. Petrov



$T \lesssim 0.75 T_c$ :

string breaking

$F(r, T) \simeq V(r, T = 0)$



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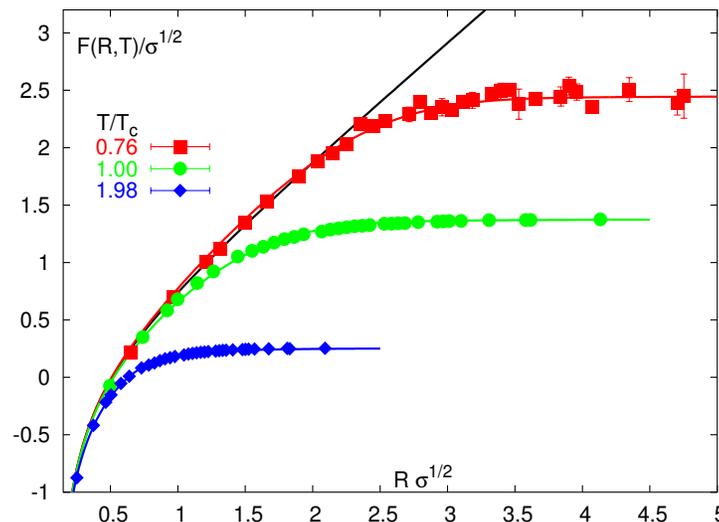
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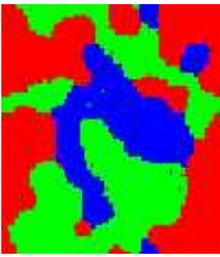
$T \simeq T_c$ :

screening sets in at

$r \simeq 0.3$  fm;

significant r-dep. upto

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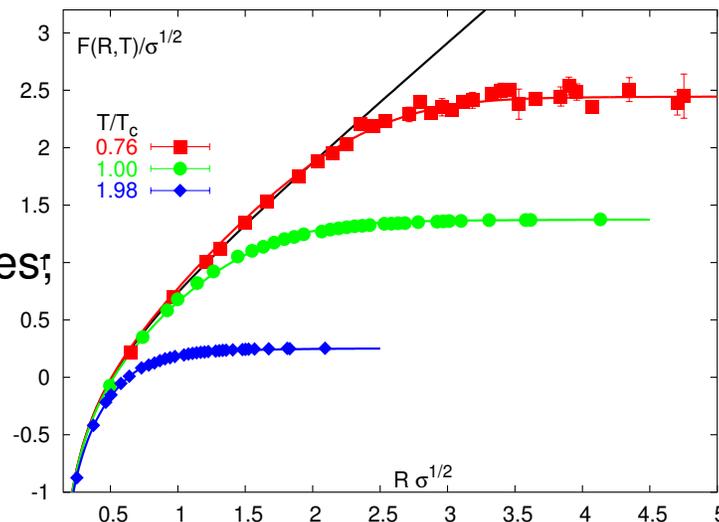
$T \gtrsim 2 T_c$ :

asymptotic freedom;

screening at short distances;

$F(r,T) \sim \text{const.}$  for

$r \lesssim r_{af}$



$T \lesssim 0.75 T_c$ :

string breaking

$F(r,T) \simeq V(r, T=0)$

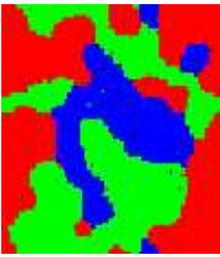
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$$e^{-F_{\bar{q}q}(r,T)/T} = \frac{1}{9} \langle \text{Tr} L_{\vec{x}} \text{Tr} L_{\vec{0}}^\dagger \rangle$$

- $3 \times \bar{3} = 1 + 8$ ;  $(q\bar{q})$ -pair can be in a singlet or octet state

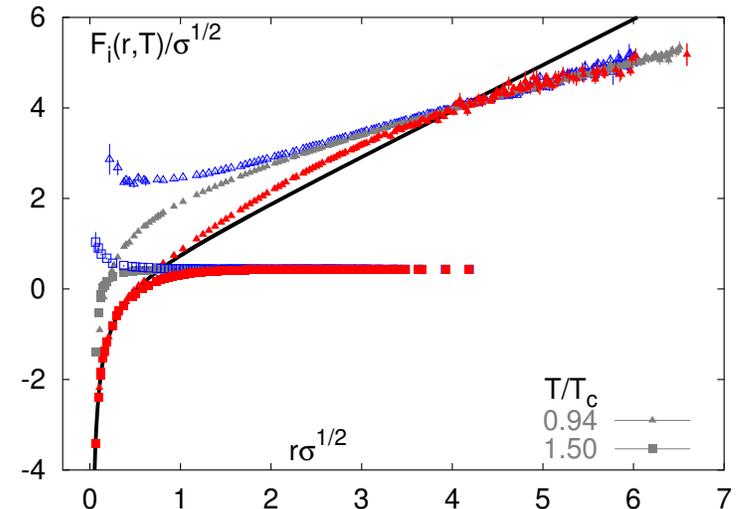
$$e^{-F_{\bar{q}q}(r,T)/T} = \frac{1}{9} e^{-F_1(r,T)/T} + \frac{8}{9} e^{-F_8(r,T)/T}$$

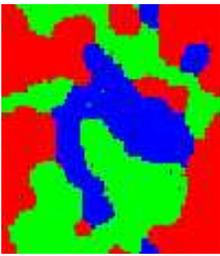
$$e^{-F_1(r,T)/T} = \frac{1}{3} \langle \text{Tr} L_{\vec{x}} L_{\vec{0}}^\dagger \rangle$$

- $F_1$ ,  $F_8$  require gauge fixing:  
Coulomb gauge; gauge invariant interpretation:  
O. Philipsen, PLB 535 (2002) 138

⇒  $F_1, F_8$  are not unique;

**BUT:** short and large distance behaviour are!!



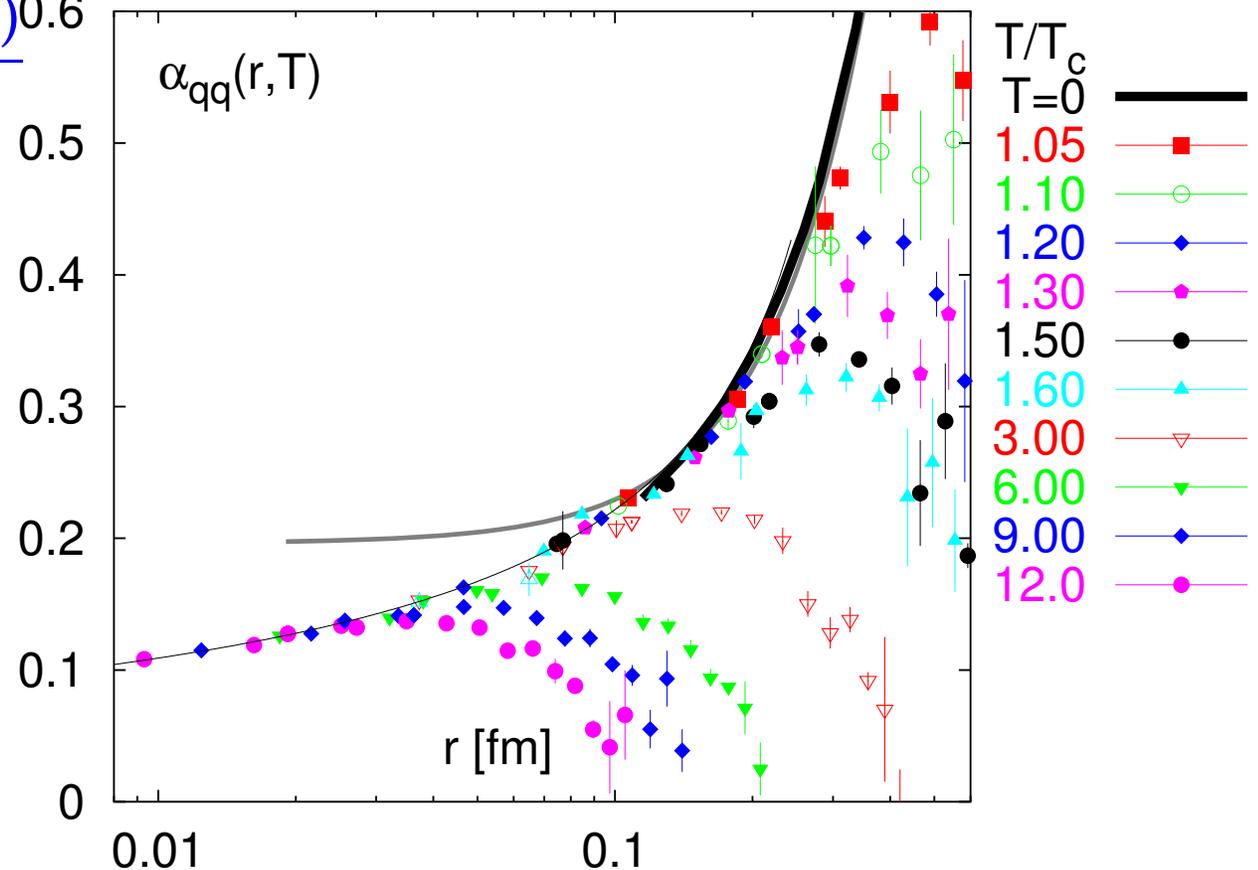


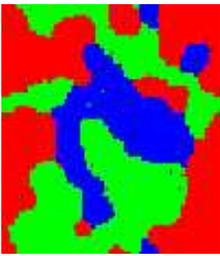
# Singlet free energy and asymptotic freedom

O.Kaczmarek, FK, P. Petreczky, F. Zantow (2004)

- singlet free energy defines a running coupling:

$$\alpha_{\text{eff}} = \frac{3r^2}{4} \frac{dF_1(r, T)}{dr}$$





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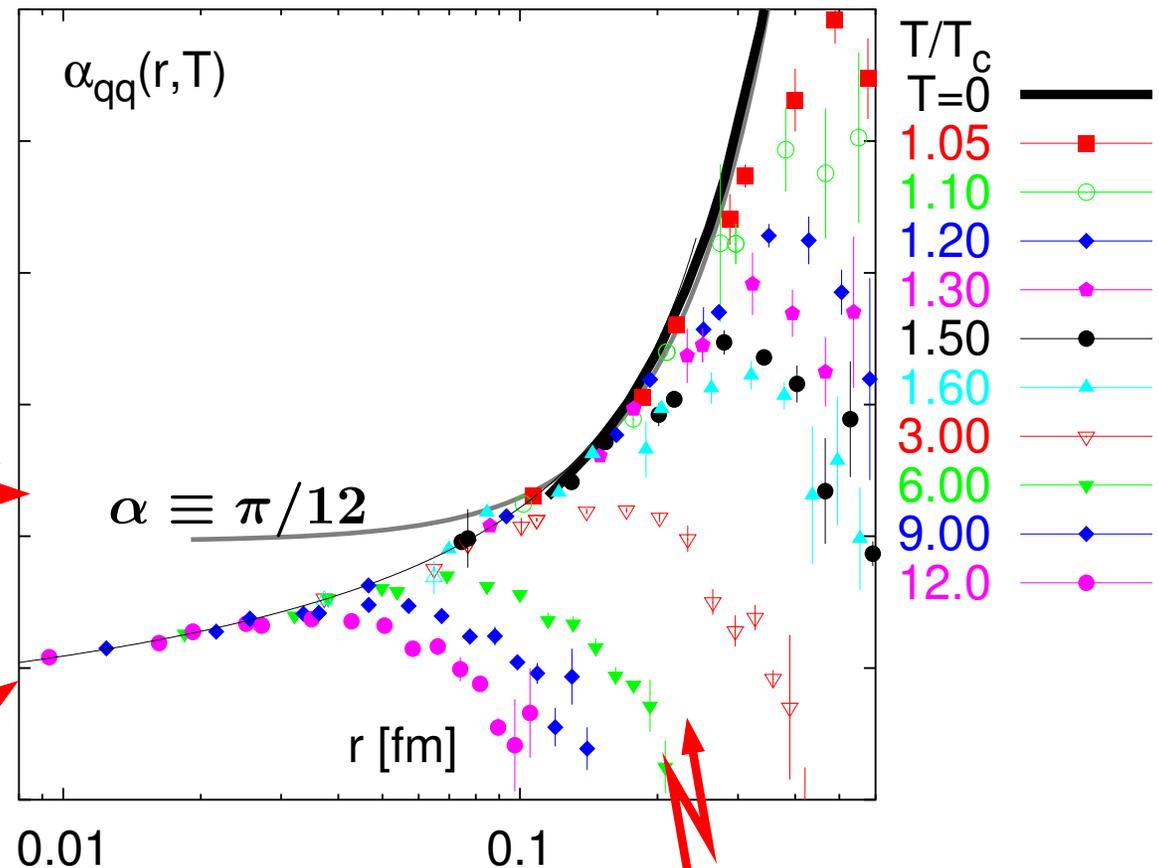
$$\alpha_{\text{eff}} = \frac{3r^2}{4} \frac{dF_1(r, T)}{dr}$$

large distance: constant

Coulomb term (string model)

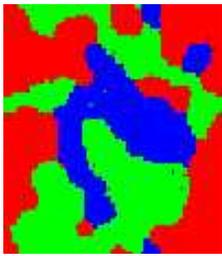
short distance: running coupling  
 $\alpha(r)$  from ( $T = 0$ ), 3-loop

(S. Necco, R. Sommer,  
 Nucl. Phys. B622 (2002) 328)



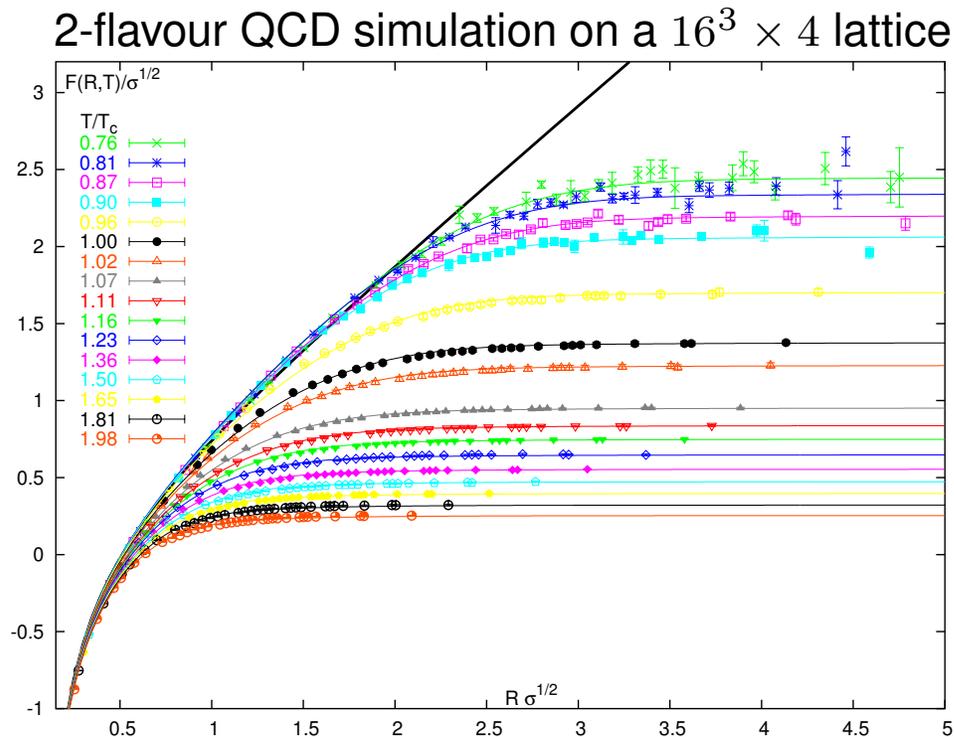
T-dependence starts in non-perturbative regime for  $T \lesssim 3 T_c$

- short distance physics  $\leftrightarrow$  vacuum physics



# Heavy quark free energy: screening and string breaking

string breaking  $\Leftrightarrow$  screening with  $q\bar{q}$  pairs from the vacuum



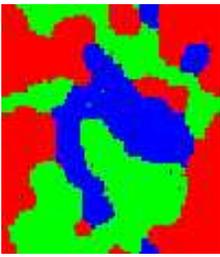
temperature dependence of  
heavy quark free energy

$$(m_q/T = 0.4)$$

rapid drop of  $F(\infty, T)$  across  $T_c$   
reflects rapid rise of (parton) density

fit: 
$$F(r, T) = \frac{\sigma r}{x} \left[ \frac{\Gamma(1/4)}{2^{3/2}\Gamma(3/4)} - \frac{\sqrt{x}}{2^{3/4}\Gamma(3/4)} K_{1/4}(x^2) \right] - \frac{4}{3} \frac{\alpha}{r} [e^{-x} + x], \quad x = \mu(T)r$$

see talks by S. Digal and O. Kaczmarek



# From heavy quark free energies to heavy quark potentials

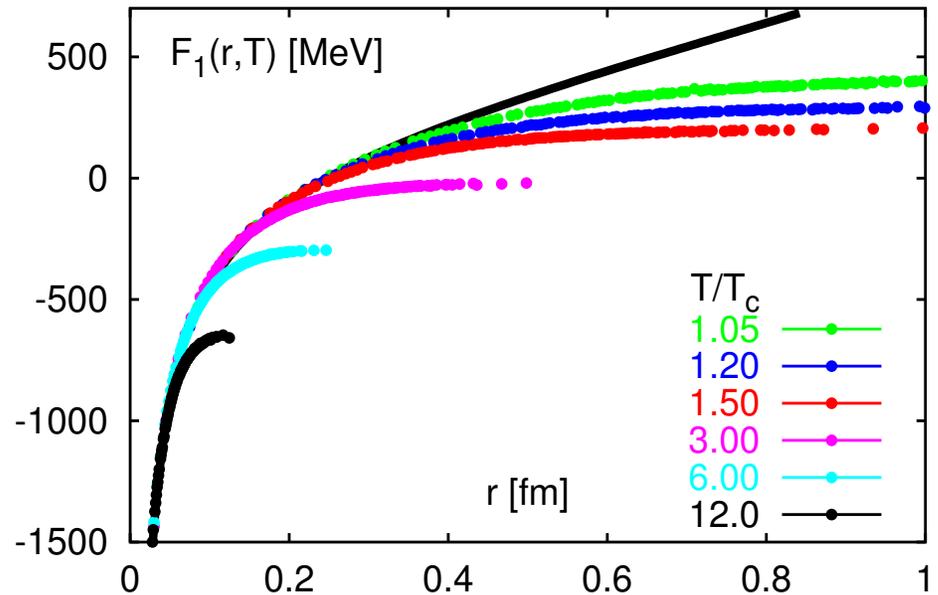
$$\lim_{T \rightarrow \infty} F(r, T) = -\infty !!$$



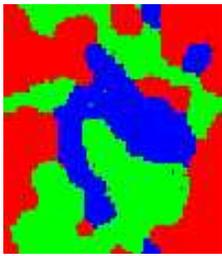
$$F = E - T \cdot S$$



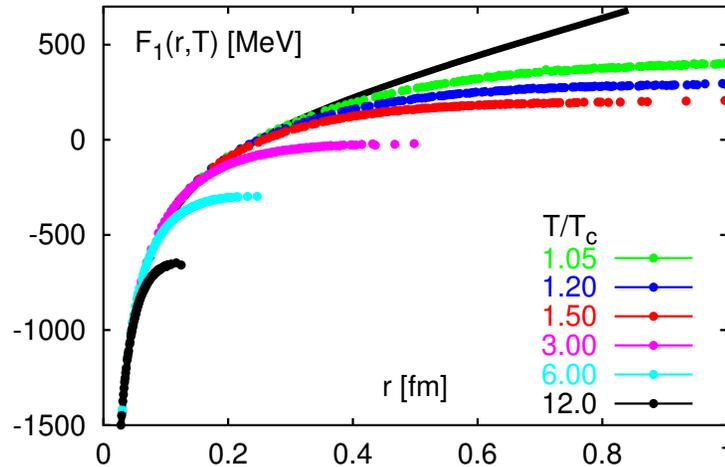
$$E(r, T) = -T^2 \frac{\partial F(r, T)/T}{\partial T}, \quad S(r, T) = -\frac{\partial F(r, T)}{\partial T}$$



- reconstruct energies from free energies;
- approximate derivatives through finite differences at  $T_1$ ,  $T_2$  and fixed  $r$
- requires good control over scaling behaviour of the cut-off "a" (complicated!)



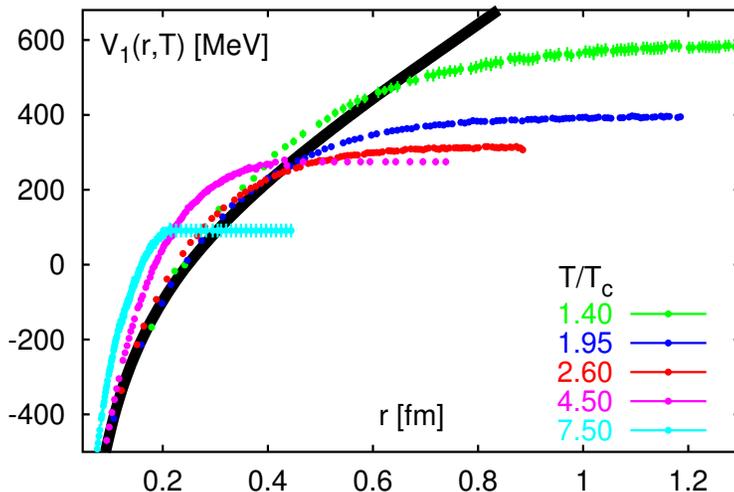
# From heavy quark free energies to heavy quark potentials



i) singlet free energy

$$\exp(-F_1(r, T)/T) = \frac{1}{3} \langle \text{Tr} L_{\vec{x}} L_0^\dagger \rangle$$

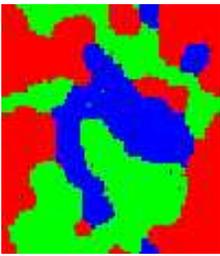
(Coulomb gauge)



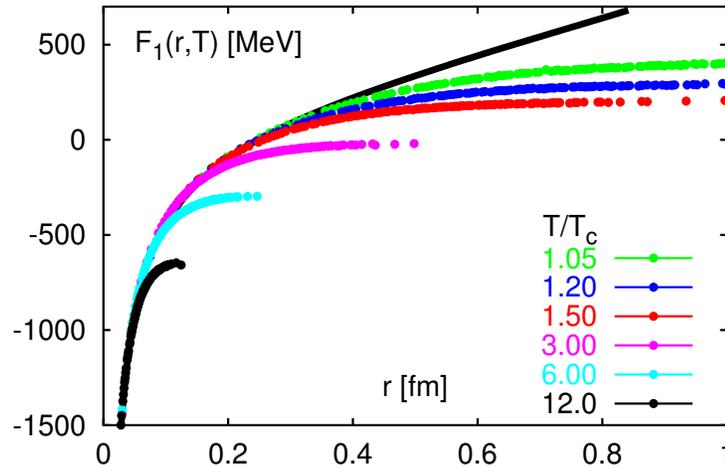
ii) singlet energy  $\Leftrightarrow$  "potential" energy

$$V_1(r, T) \equiv -T^2 \frac{\partial F_1(r, T)/T}{\partial T}$$

- potential is "deeper":  $V(r, T) > F(r, T)$
- potential "barrier" high also well above  $T_c$
- "potential" screened at short distances



# From heavy quark free energies to heavy quark potentials

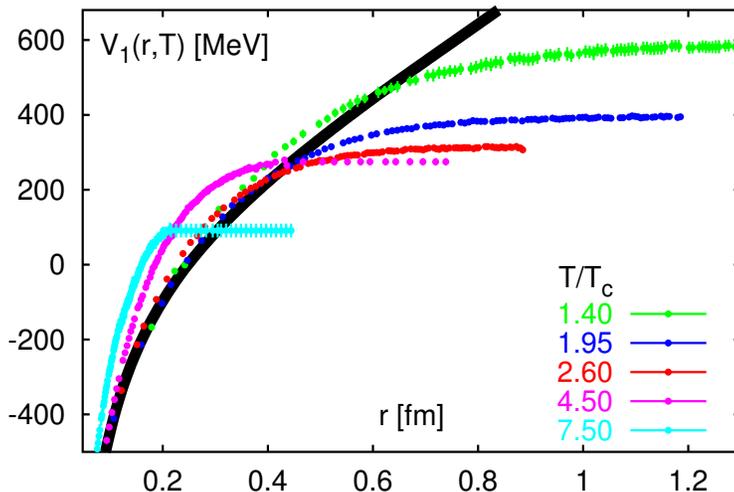


i) singlet free energy

**NOTE:**

$F_{\bar{q}q}(r, T)$  decreases with increasing  $T$  and fixed  $r \Rightarrow$  **positive entropy**

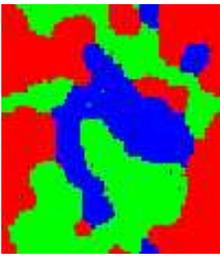
$$S = - \left( \frac{\partial F}{\partial T} \right)_V \geq 0$$



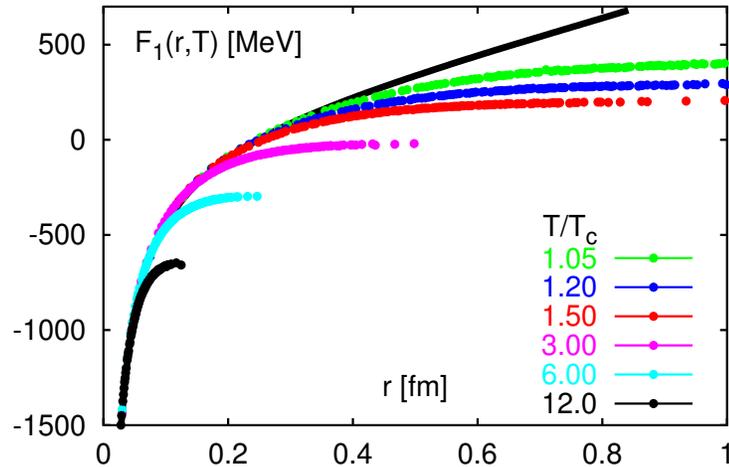
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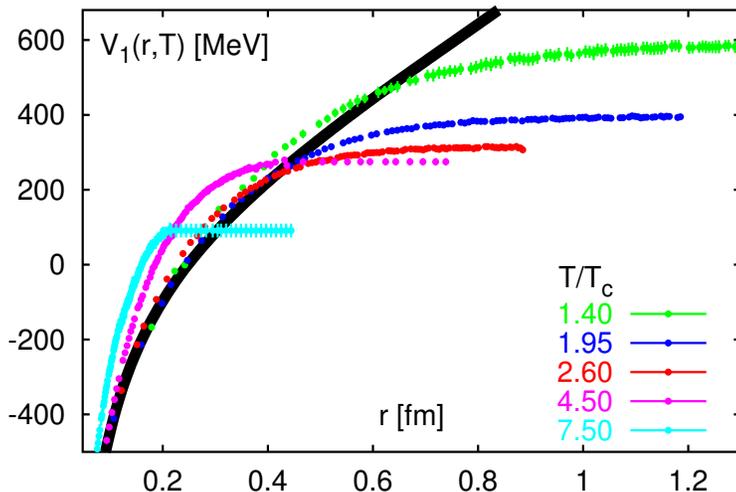


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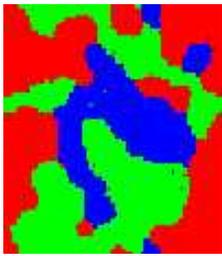
$$\Rightarrow V(r, T) > F(r, T)$$



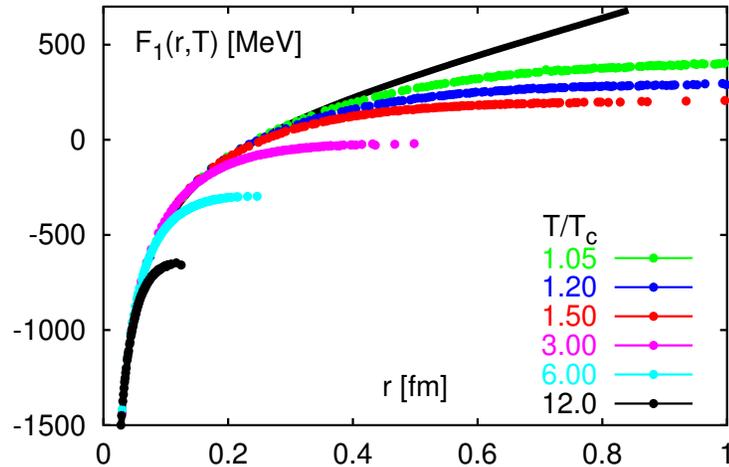
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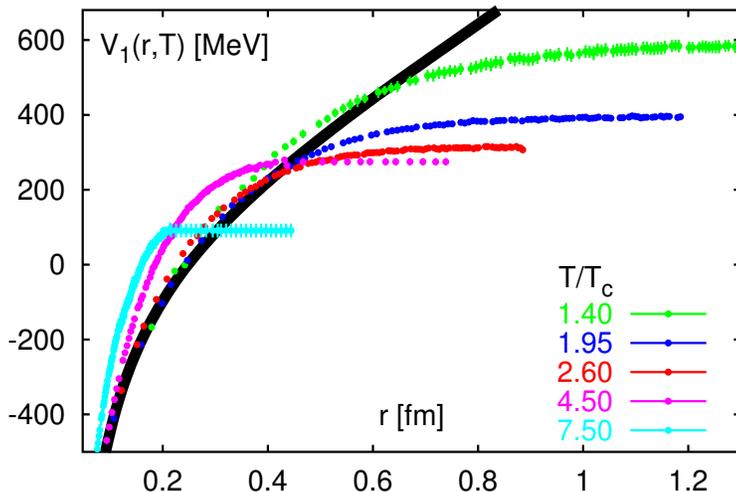
i) singlet free energy

**NOTE:**

$F_{\bar{q}q}(r, T)$  decreases with increasing  $T$  and fixed  $r \Rightarrow$  **positive entropy**

$$F_1(\infty, 1.4T_c) \simeq 200 \text{ MeV}$$

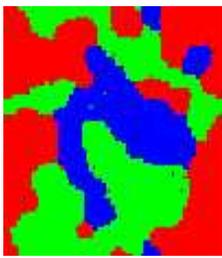
$$V_1(\infty, 1.4T_c) \simeq 600 \text{ MeV}$$



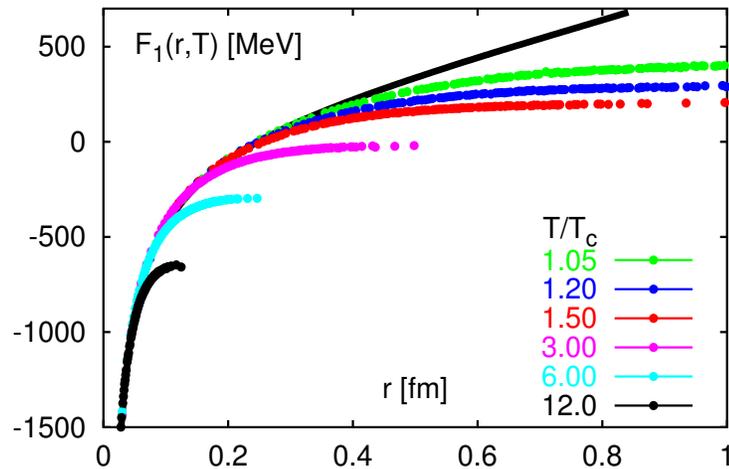
ii) singlet energy  $\Leftrightarrow$  "potential" energy

$$V_1(r, T) \equiv -T^2 \frac{\partial F_1(r, T)/T}{\partial T}$$

- potential is "deeper":  $V(r, T) > F(r, T)$
- potential "barrier" high also well above  $T_c$
- "potential" screened at short distances



# From heavy quark free energies to heavy quark potentials



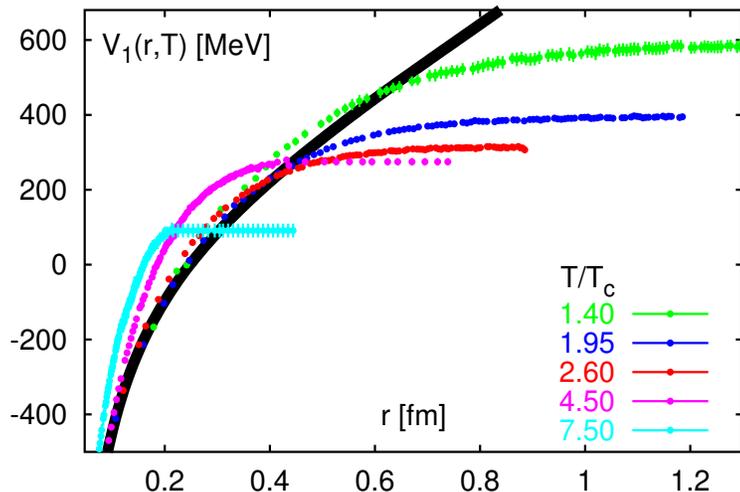
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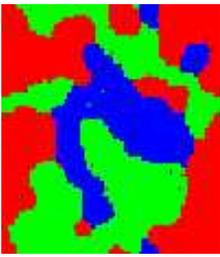
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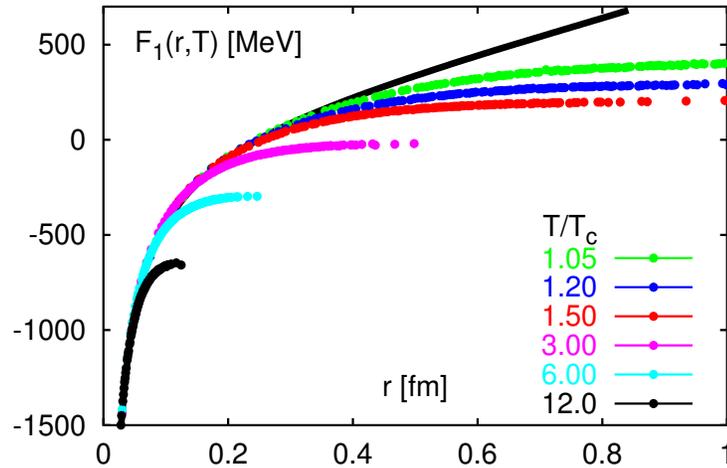


ii) singlet energy  $\Leftrightarrow$  "potential" energy

**When do heavy quark bound states  
really disappear?**



# From heavy quark free energies to heavy quark potentials



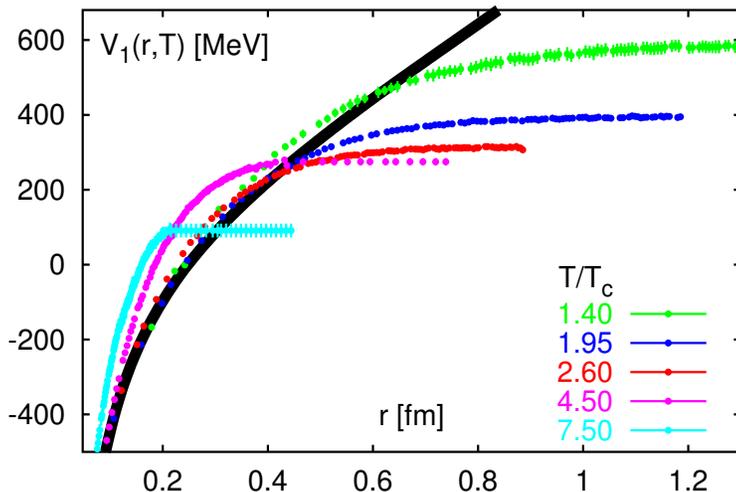
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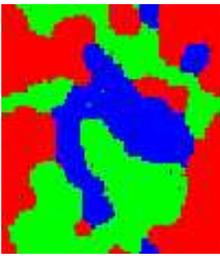
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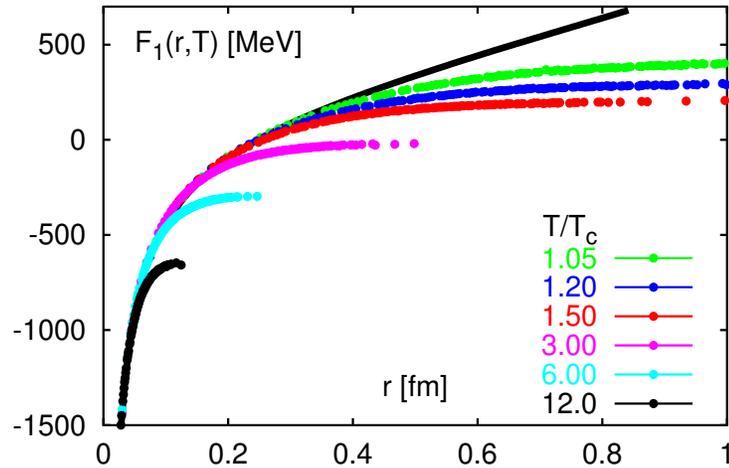
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When do heavy quark bound states  
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i) neither  $V_1$  nor  $F_1$  are "potentials"



# From heavy quark free energies to heavy quark potentials



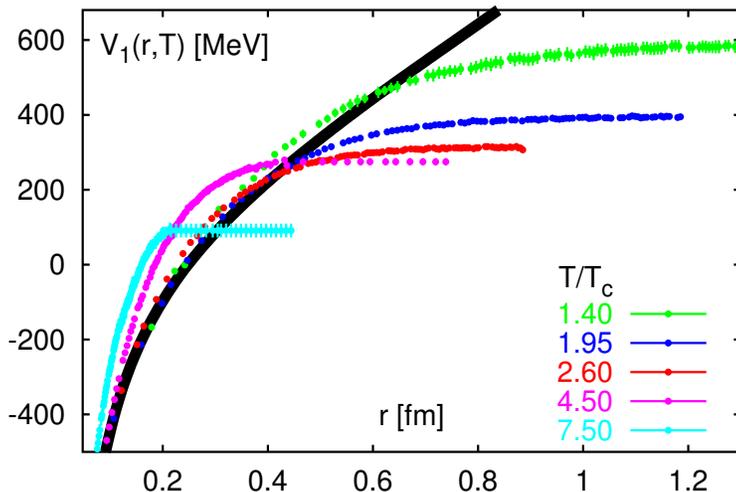
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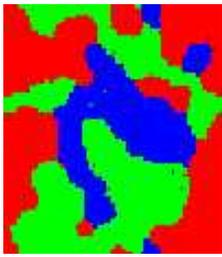


ii) singlet energy  $\Leftrightarrow$  "potential" energy

When do heavy quark bound states really disappear?

i) neither  $V_1$  nor  $F_1$  are "potentials"

ii) potential models are MODELS!



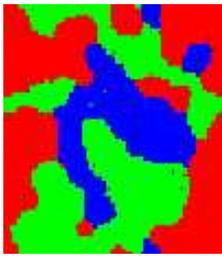
# Heavy quark bound states from Schrödinger-Equation

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- Schrödinger equation for heavy quarks:

$$\left[ 2m_a + \frac{1}{m_a} \nabla^2 + V_1(r, T) \right] \Phi_i^a = M_i^a(T) \Phi_i^a, \quad a = \text{charm, bottom}$$

- T-dependent color singlet heavy quark potential mimics in-medium modification of  $q\bar{q}$  interaction
  - reduction to 2-particle interaction clearly too simple, in particular close to  $T_c$
- recent analyses:
- using  $F_1$ : S. Digal, P. Petreczky, H. Satz, Phys. Lett. B514 (2001) 57;
  - using  $V_1$ : C.-Y. Wong, hep-ph/0408020;



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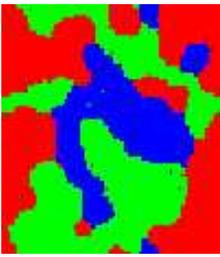
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state	$J/\psi$	$\chi_c$	$\psi'$	$\Upsilon$	$\chi_b$	$\Upsilon'$	$\chi'_b$	$\Upsilon''$
$E_s^i$ [GeV]	0.64	0.20	0.05	1.10	0.67	0.54	0.31	0.20
$T_d/T_c$	1.1	0.74	0.1 - 0.2	2.31	1.13	1.1	0.83	0.74
$T_d/T_c$	$\sim 2.0$	$\sim 1.1$	$\sim 1.1$	$\sim 4.5$	$\sim 2.0$	$\sim 2.0$	—	—

$V_1$  leads to dissociation temperatures consistent with spectral function analysis



# Heavy quark bound states from Schrödinger-Equation

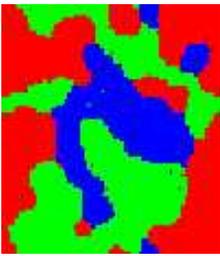
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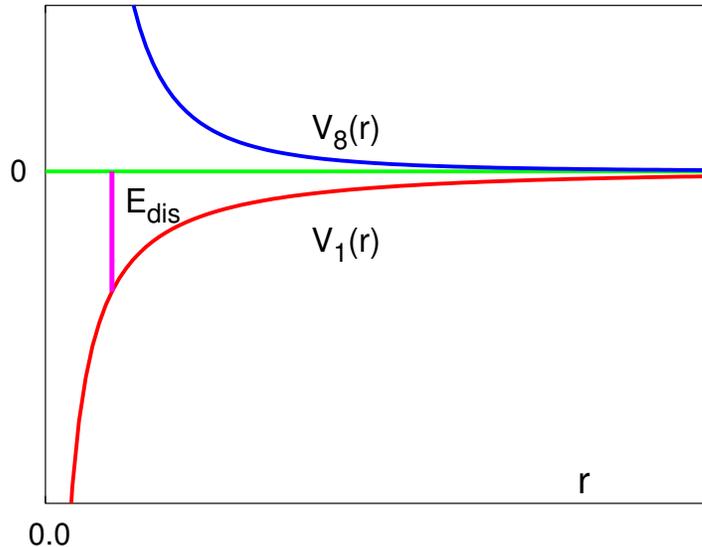
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- Schrödinger-eq. yields  $T_\chi > T_{\psi'}$   
 - collision with thermal gluons,  $\langle p \rangle \sim 3T$  can lead to earlier dissolution:  $dn_{J/\psi}/dt = -n_g \langle \sigma_{dis} \rangle$

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# Heavy quark bound states from Schrödinger-Equation



collisional dissociation

D. Kharzeev, H. Satz, PL B334 (1994) 155

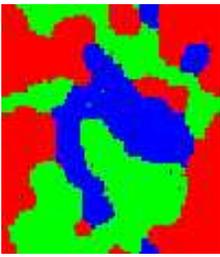


$$T = 1.1 T_c : E_{dis,\chi} \simeq 50 \text{ MeV}$$

$$E_{dis,J\psi} \simeq 500 \text{ MeV}$$

- Schrödinger-eq. yields  $T_\chi > T_{\psi'}$
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# Time dependence of $J/\psi$ dissolution

---

## ● Kinetic Formation

- dissolution and recombination may occur during cooling of the deconfined medium

R.L. Thews et al, PRC63 (2001) 054905

## ● Statistical Hadronization

quarkonium formation follows same statistical pattern as light quark bound states

P. Braun-Munzinger, J. Stachel, PLB490 (2000) 196

- produced  $c\bar{c}$ -pairs "separate" in QGP phase
- quarkonium and open charm bound states form at freeze out according to thermal hadronization rules

## ● possibility for $J/\psi$ enhancement (RHIC/LHC)

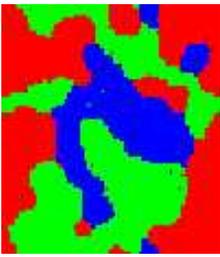
$$N_{J/\psi} \sim N_{c\bar{c}}^2$$



no sequential suppression pattern



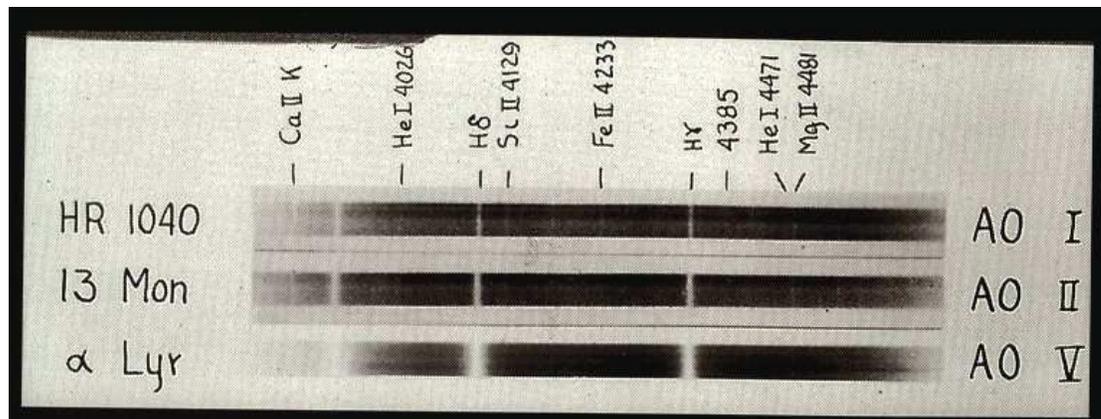
thermal excitation, collision broadening (in spectral functions)

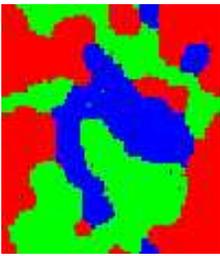


# Spectral lines emitted by stars: pressure broadening

screening, collision/pressure broadening:  $\Delta\lambda = \frac{\lambda^2 n \sigma}{\pi c} \left( \frac{2kT}{m} \right)^{1/2}$

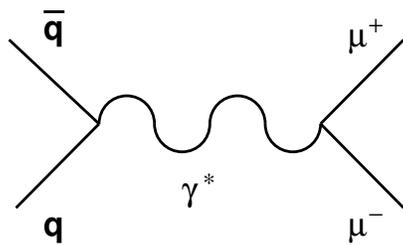
- spectral functions incorporate excitation, dissolution and recombination of states
- stellar atmosphere modifies electric field of an emitting atom





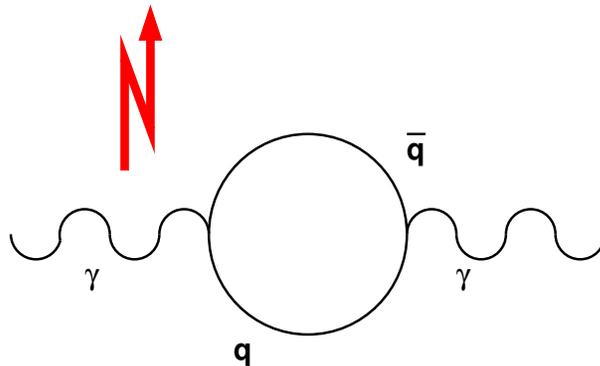
# Spectral functions and Dilepton rates

Thermal dilepton rate and **vector spectral function**



L.D. McLerran, T. Toimela, PR D31 (85) 545.

$$\text{rate} \sim |q\bar{q} \rightarrow \gamma^*|^2 \cdot |l^+l^- \rightarrow \gamma^*|^2$$



photon self-energy

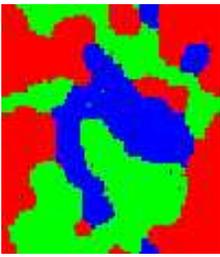


propagation of a  $q\bar{q}$ -pair with  
the quantum numbers of a vector meson

**spectral representation of dilepton rate**



$$\frac{dW}{d\omega d^3p} = \frac{5\alpha^2}{27\pi^2} \frac{1}{\omega^2 (e^{\omega/T} - 1)} \sigma_V(\omega, \vec{p}, T)$$



# Euclidean two-point functions: $T > 0$

thermal averages over states

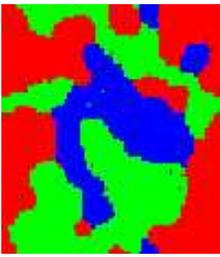
● Hamiltonian  $\hat{H}$ ; temperature  $T \equiv \beta^{-1}$ ;

partition function  $Z(\beta) = \text{Tr} e^{-\beta \hat{H}}$ ; expectation values  $\langle O \rangle_\beta = \frac{1}{Z(\beta)} \text{Tr} O e^{-\beta \hat{H}}$

$$\begin{aligned} G_\phi^\beta(\tau) &\equiv \langle 0 | \hat{\phi}^\dagger(\tau) \hat{\phi}(0) | 0 \rangle_\beta \\ &= \frac{1}{Z(\beta)} \sum_{k,l} |\langle l | \hat{\phi} | k \rangle|^2 e^{-\beta E_k} e^{-\tau(E_l - E_k)} \\ &= \int_{-\infty}^{\infty} \frac{d\omega}{2\pi} \sigma_\phi(\omega, T) \frac{\cosh(\omega(\tau - 1/2T))}{\sinh(\omega/2T)} \end{aligned}$$

with spectral function

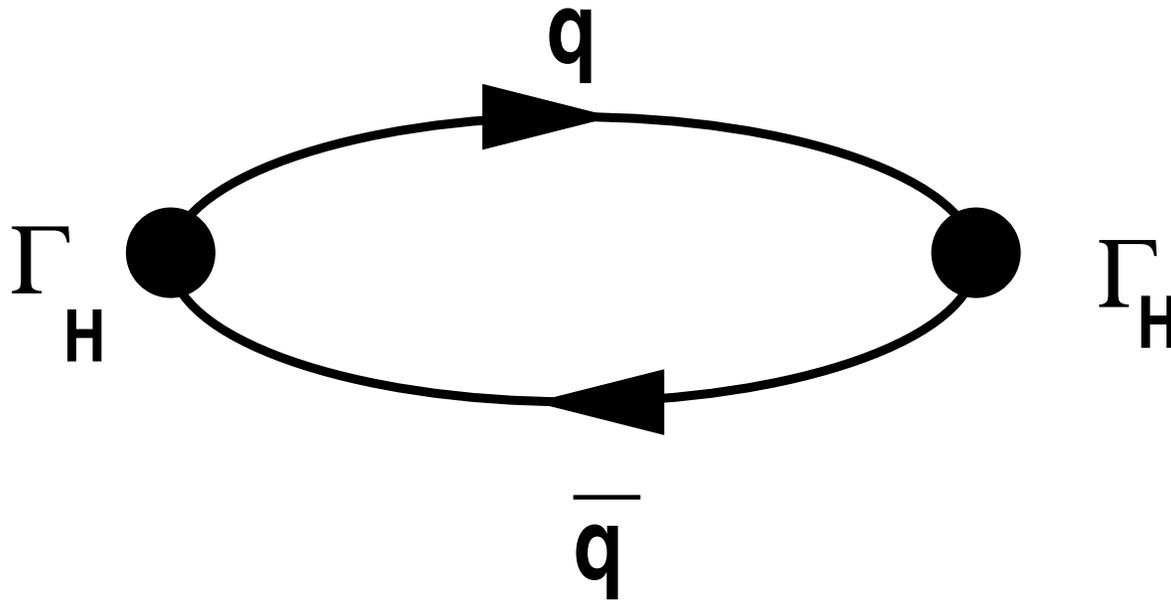
$$\sigma_\phi(\omega, T) = \frac{2\pi}{Z(\beta)} \sum_{k,l} |\langle k | \hat{\phi} | l \rangle|^2 e^{-\beta E_k} (1 - e^{-\beta\omega}) \delta(\omega - (E_k - E_l))$$



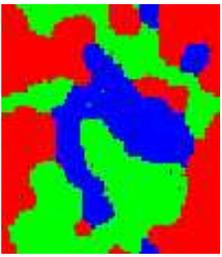
# Thermal meson correlation functions and spectral functions

Thermal correlation functions: 2-point functions which describe propagation of a  $\bar{q}q$ -pair

spectral representation of correlator  $\Rightarrow$  in-medium properties of hadrons;  
thermal dilepton (photon) rates



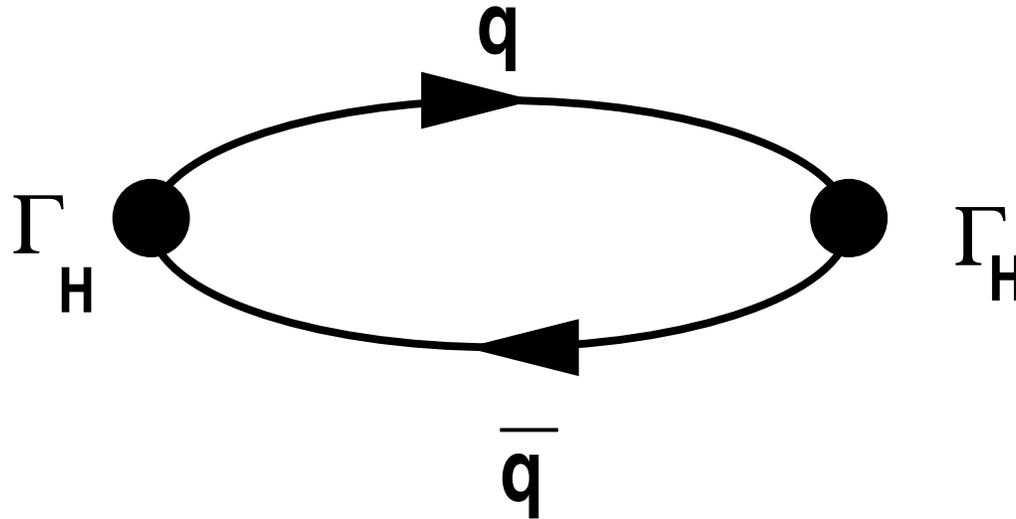
$$G_H^\beta(\tau, \vec{r}) = \langle J_H(\tau, \vec{r}) J_H^\dagger(0, \vec{0}) \rangle; \quad J_H(\tau, \vec{r}) = \bar{q}(\tau, \vec{r}) \Gamma_H q(\tau, \vec{r})$$



# Thermal meson correlation functions and spectral functions

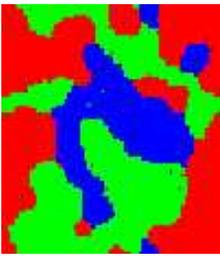
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spectral representation of  
Euclidean correlation functions

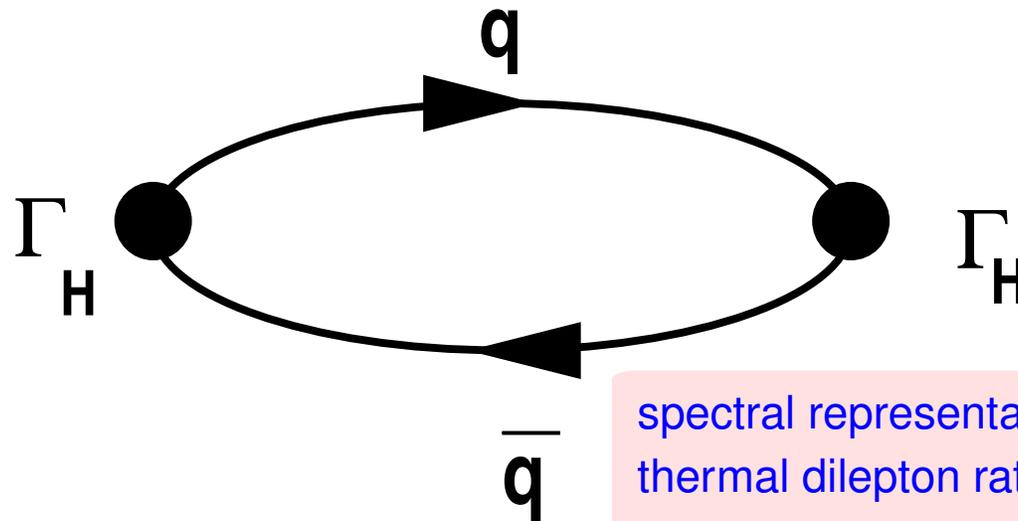
$$G_H^\beta(\tau, \vec{r}) = \int_0^\infty d\omega \int \frac{d^3\vec{p}}{(2\pi)^3} \sigma_H(\omega, \vec{p}, T) e^{i\vec{p}\vec{r}} \frac{\cosh(\omega(\tau - 1/2T))}{\sinh(\omega/2T)}$$



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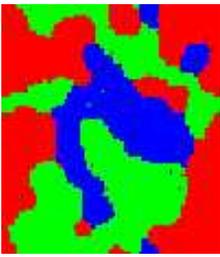


spectral representation of  
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spectral representation of  
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# Thermal correlation functions for hadronic excitations in QCD

thermal modifications of the hadron spectrum is encoded in **finite temperature**

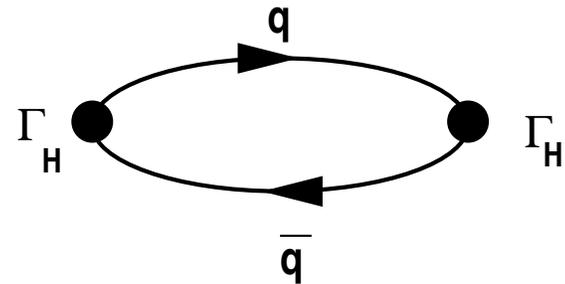
**Euclidean correlation functions**

- hadronic (mesonic) currents, composite  $q\bar{q}$ -operators

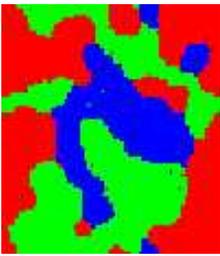
$$J_H = \bar{\psi}(\tau, \vec{r}) \Gamma_H \psi(\tau, \vec{r})$$

- $G_H^\beta(\tau, \vec{r}) \equiv \langle J_H(\tau, \vec{r}) J_H^\dagger(0, \vec{0}) \rangle_\beta$

- quantum numbers ( $H$ ) fixed through  $\Gamma_H$ :



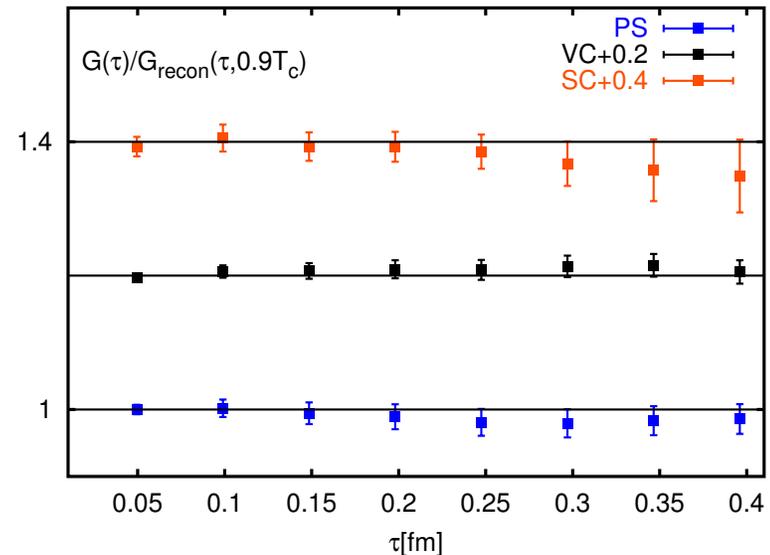
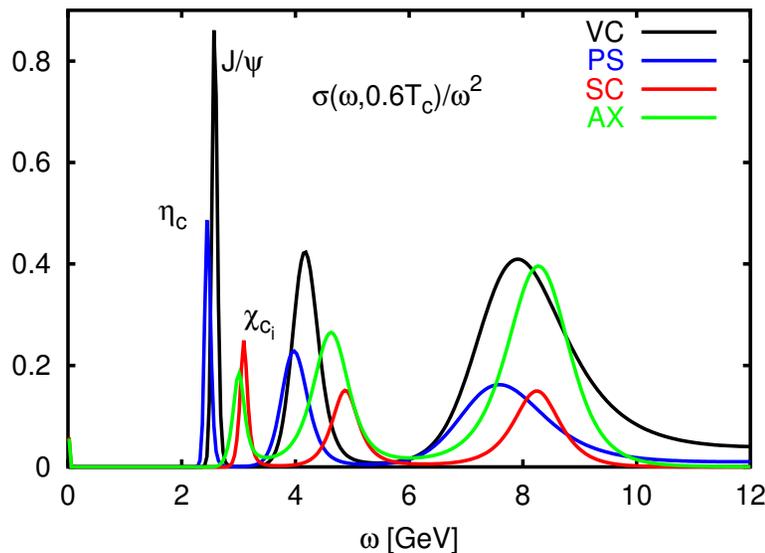
state		$J^{PC}$	$\Gamma_H$	$(u, d)$ -states	$c\bar{c}$ -states
scalar	${}^3P_0$	$0^{++}$	1	$\sigma$	$\chi_{c0}$
pseudo-scalar	${}^1S_0$	$0^{-+}$	$\gamma_5$	$\pi$	$\eta_c$
vector	${}^3S_1$	$1^{--}$	$\gamma_\mu$	$\rho$	$J/\psi$
axial-vector	${}^3P_1$	$1^{++}$	$\gamma_\mu \gamma_5$	$\delta$	$\chi_{c1}$



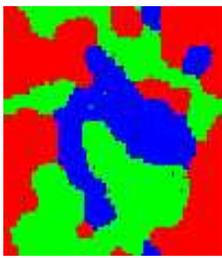
# Heavy quark spectral functions and correlation functions

- left: charmonium spectral functions below  $T_c$ , *i.e.* at  $T \simeq 0.6 T_c$ , lattice size  $48^3 \times 24$
- right: correlation function at  $T = 0.9T_c$  over reconstructed correlation function at  $T \simeq 0.9 T_c$  using the spectral function generated at  $T \simeq 0.6 T_c$ , *i.e.*

$$G_{recon}(\tau, 0.9T_c) = \int d\omega \sigma(\omega, 0.6T_c) \frac{\cosh(\omega(\tau - 1/2T))}{\sinh(\omega/2T)}$$



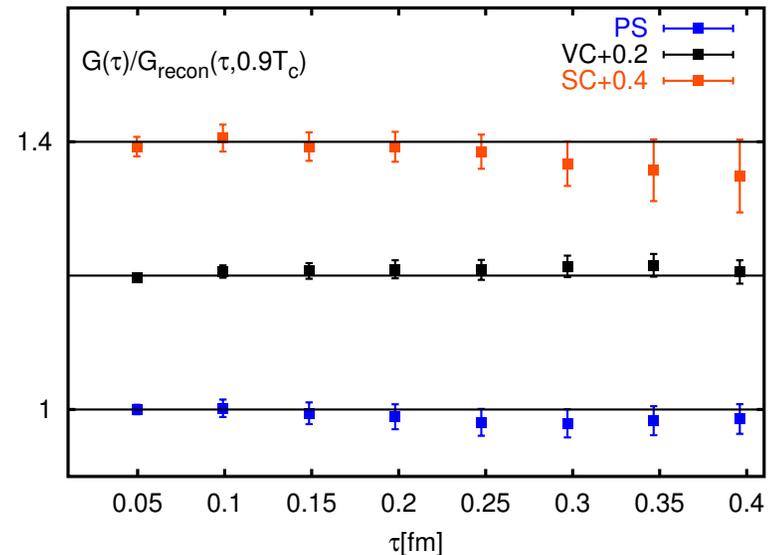
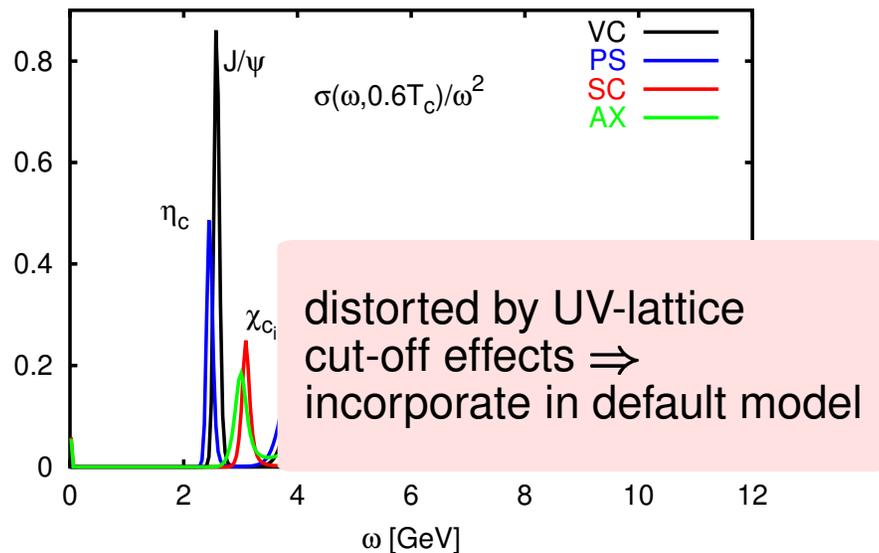
no significant temperature dependence below  $T_c$



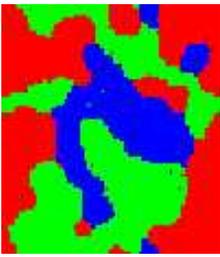
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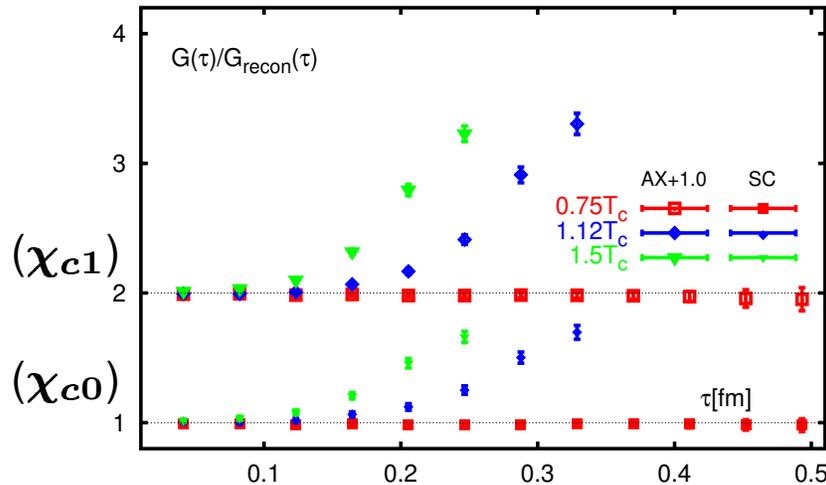


 no significant temperature dependence below  $T_c$



# Heavy quark spectral functions and correlation functions

data for  $G_H(\tau, T)$  over reconstructed correlation functions at  $T$  from data below  $T_c$

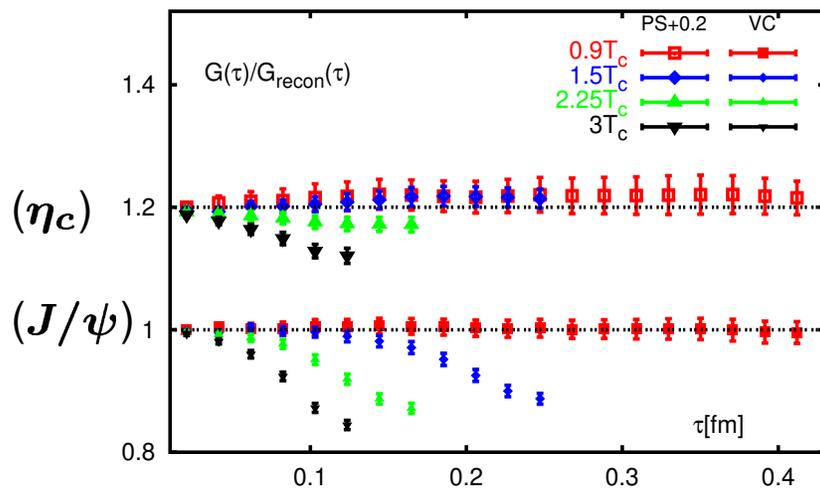


scalar and axial-vector correlation functions:

strong temperature dependence just above  $T_c$   
for  $\chi_c$  states

(normalized at  $T < T_c$ )

( $48^3 \times N_\tau$ ,  $N_\tau = 12, 16, 24$ ,  $a = 0.04$  fm)



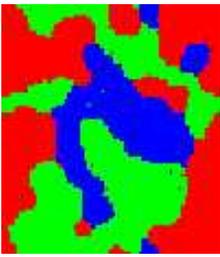
vector and pseudoscalar correlation functions:

no temperature dependence for  $\eta_c$  up to  $1.5 T_c$ ;  
only mild but systematic temperature dependence  
of  $J/\psi$

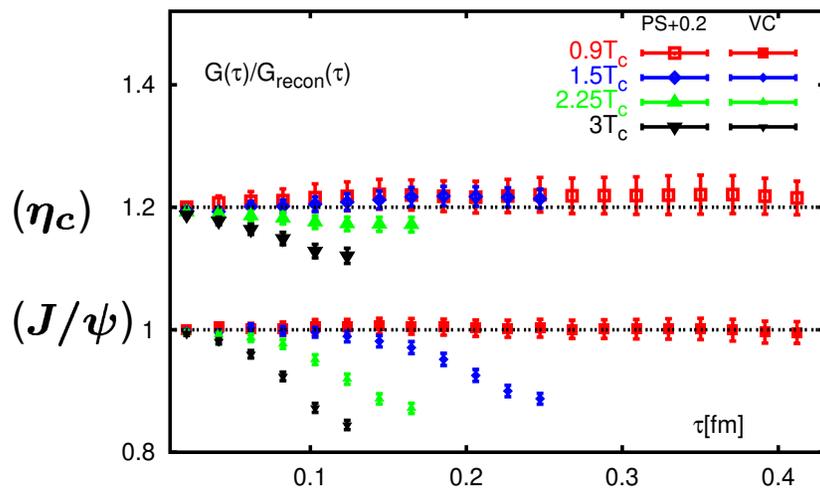
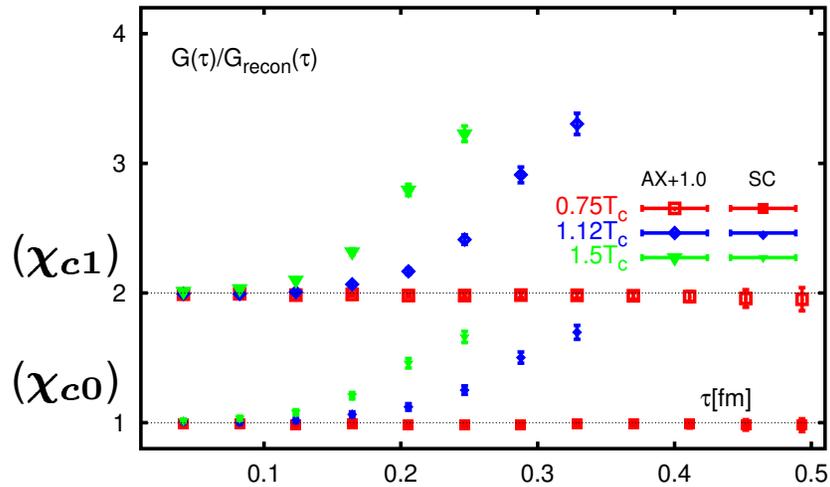
(normalized at  $T < T_c$ )

( $N_\sigma = 40, 48, 64$ ,

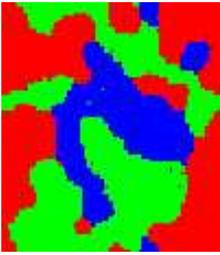
$N_\tau = 12, 16, 24, 40$ ,  $a = 0.02$  fm)



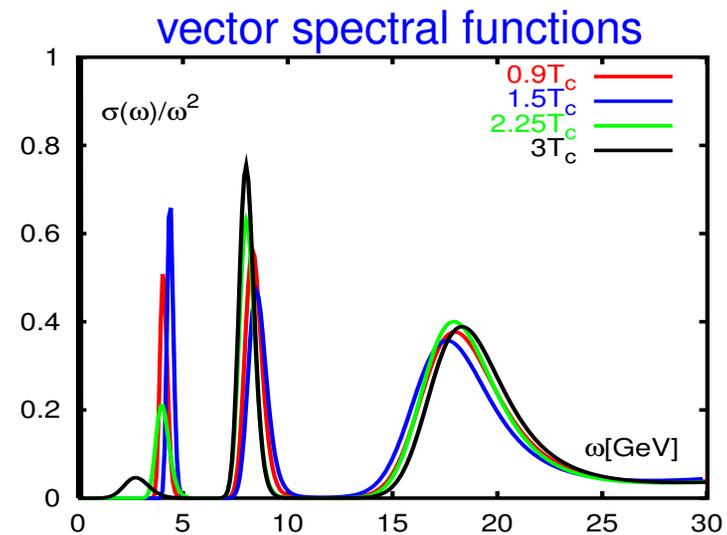
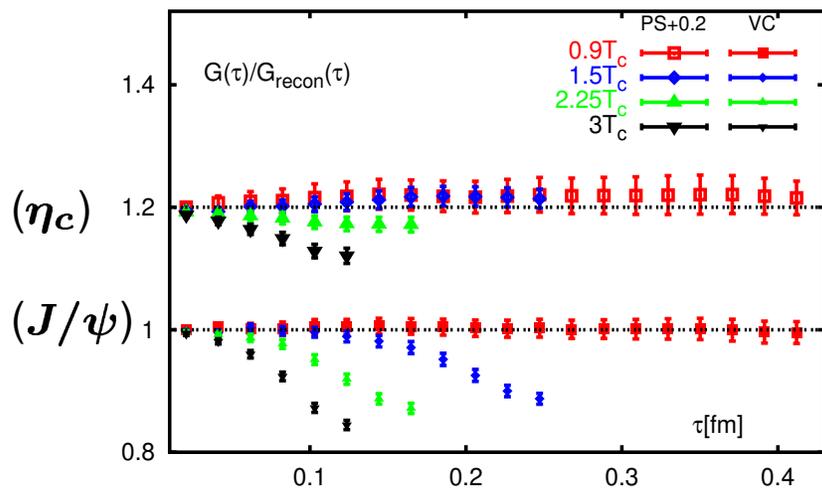
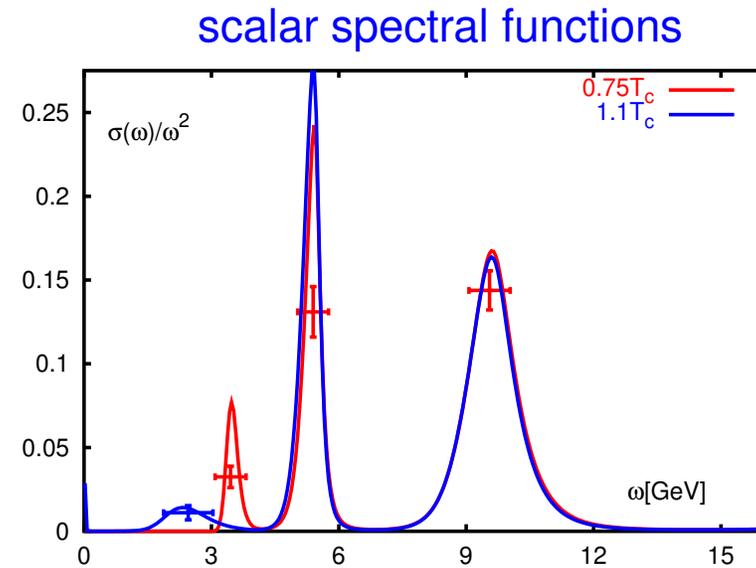
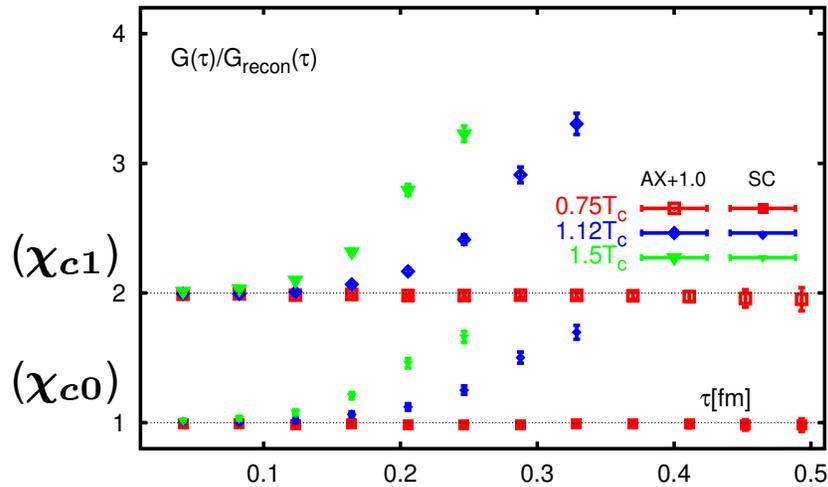
# Heavy quark spectral functions and correlation functions

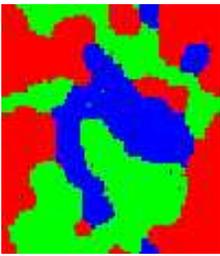


pattern seen in  
correlation functions  
also visible in  
spectral functions

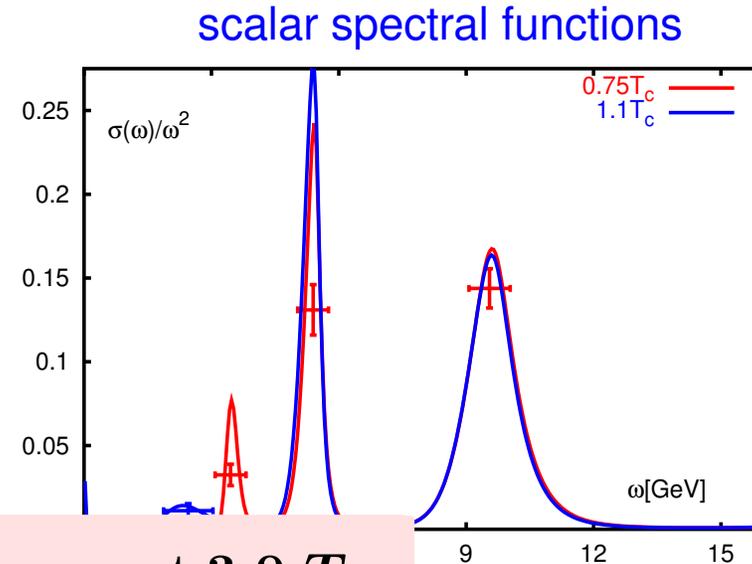
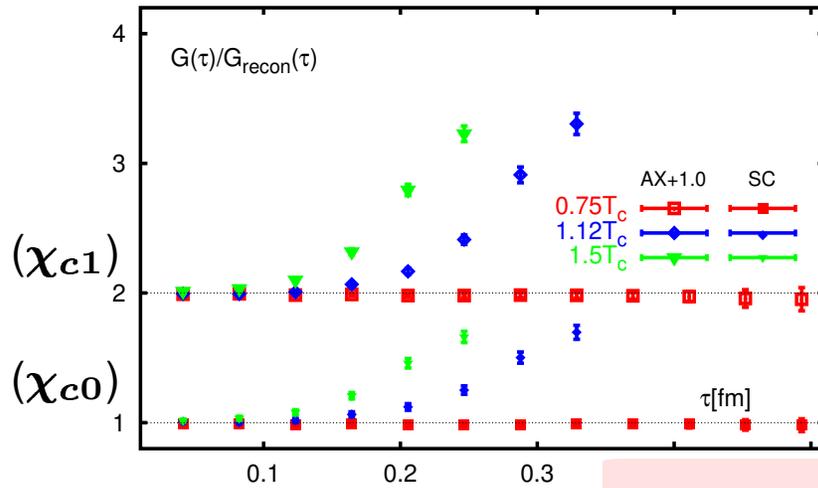


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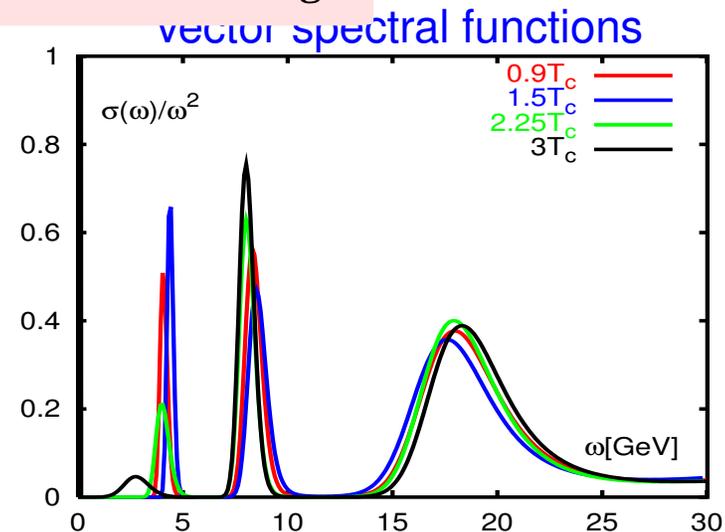
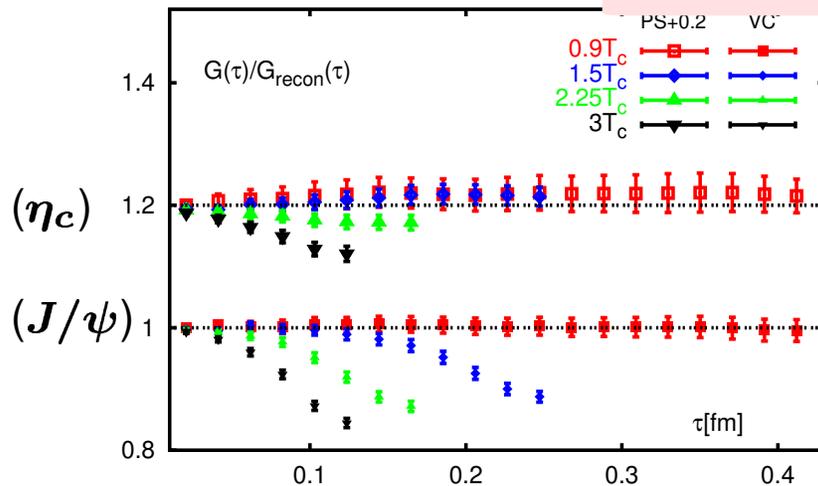


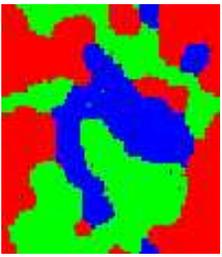


# Heavy quark spectral functions and correlation functions



*$J/\psi$  and  $\eta_c$  gone at  $3.0 T_c$*



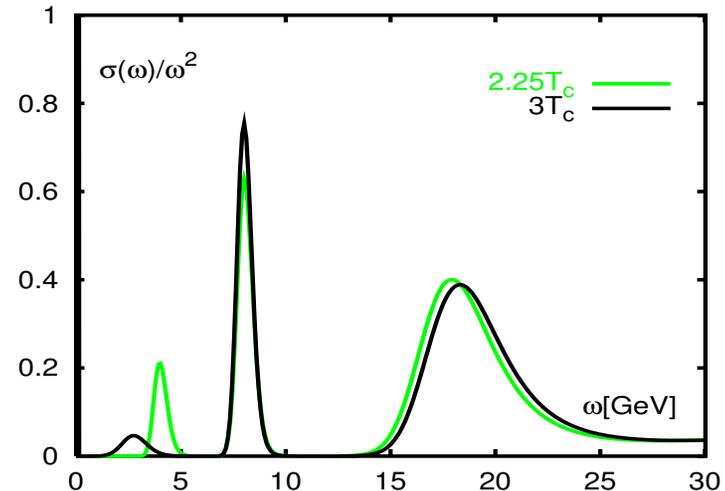
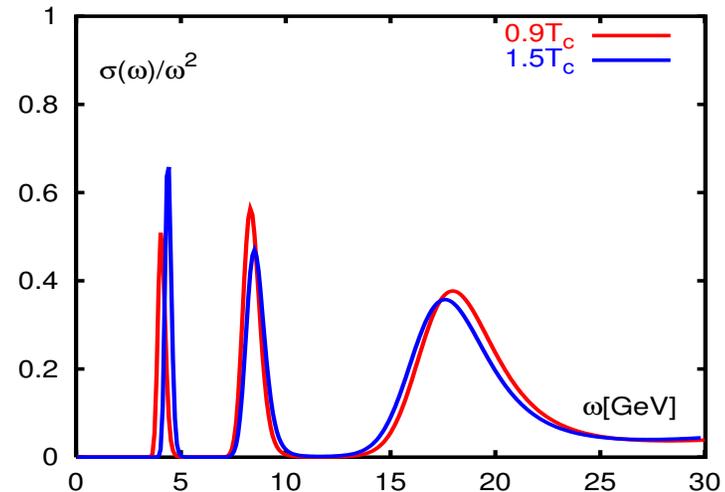
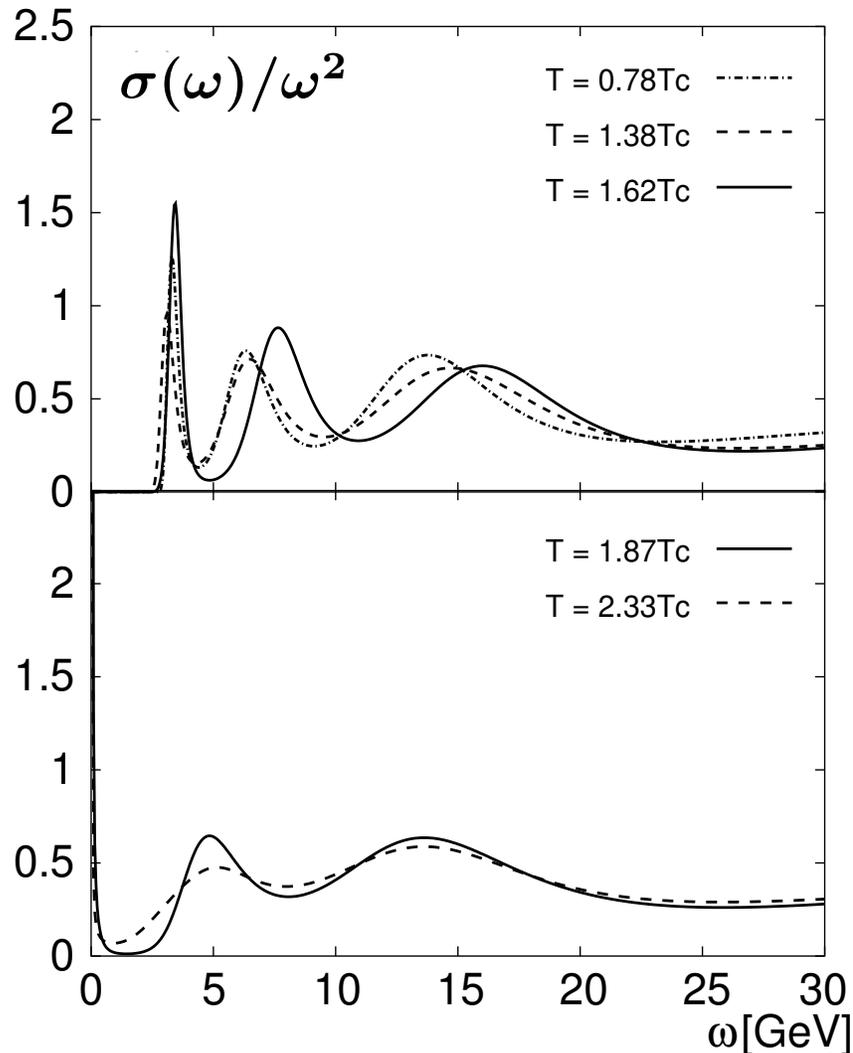


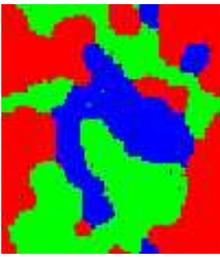
# Heavy quark spectral functions comparison of different approaches

M. Asakawa, T. Hatsuda, hep-lat/0308034

S. Datta et al., hep-lat/0312037

$J/\psi$  spectral function



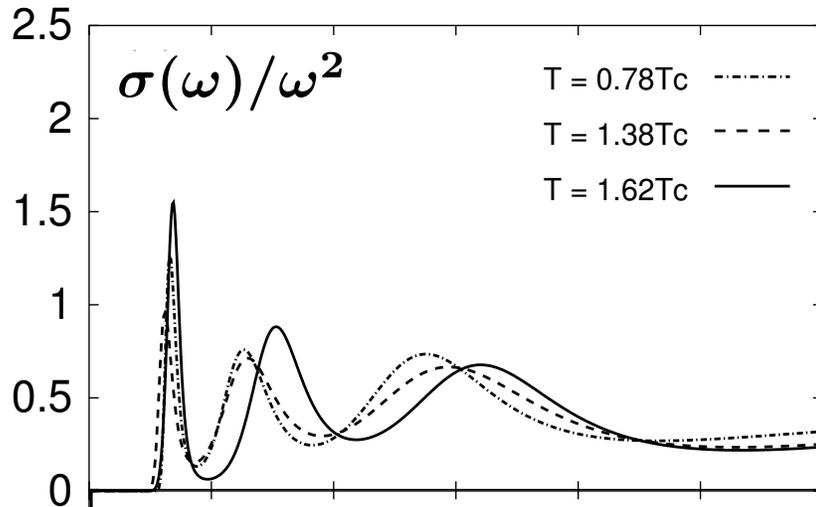


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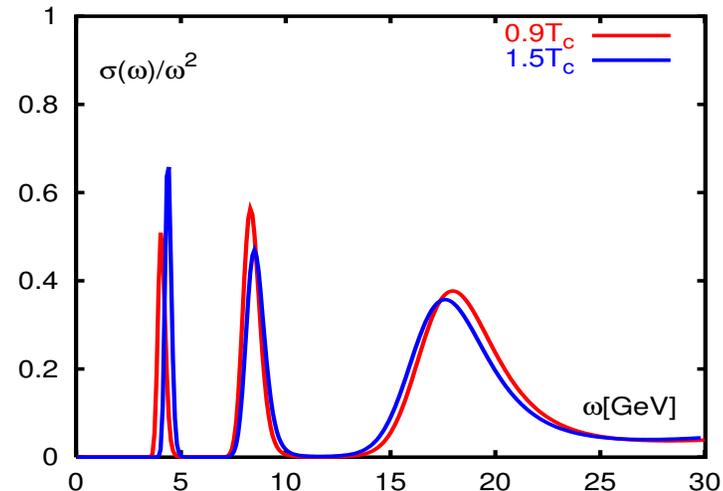
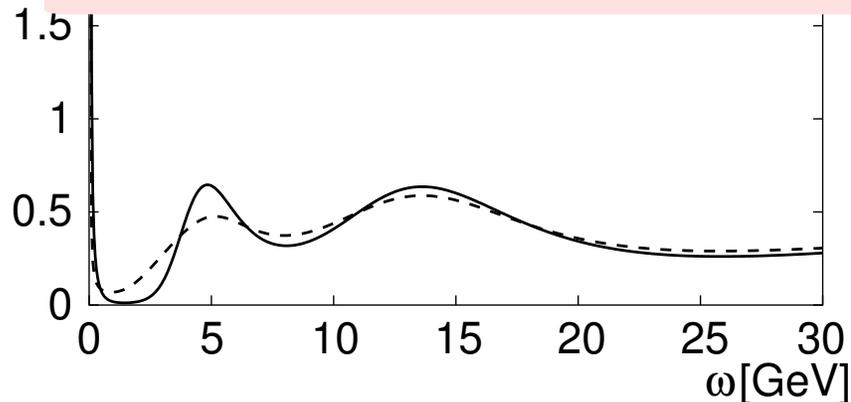
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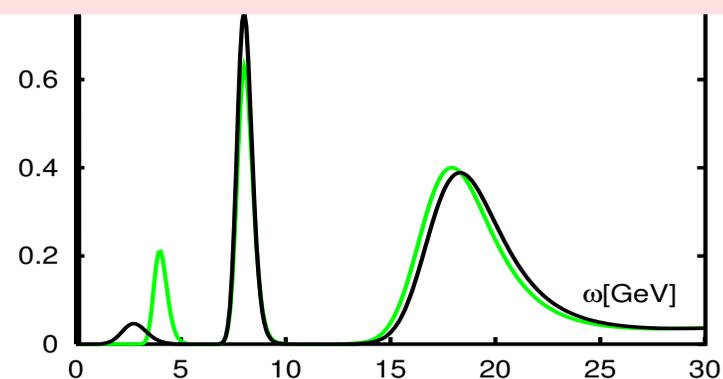
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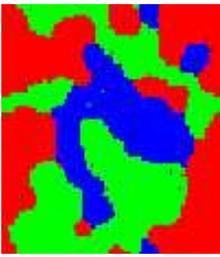


$J/\psi$  dissociates for  $1.6T_c \lesssim T \lesssim 1.9T_c$   
rather abrupt disappearance of  $J/\psi$



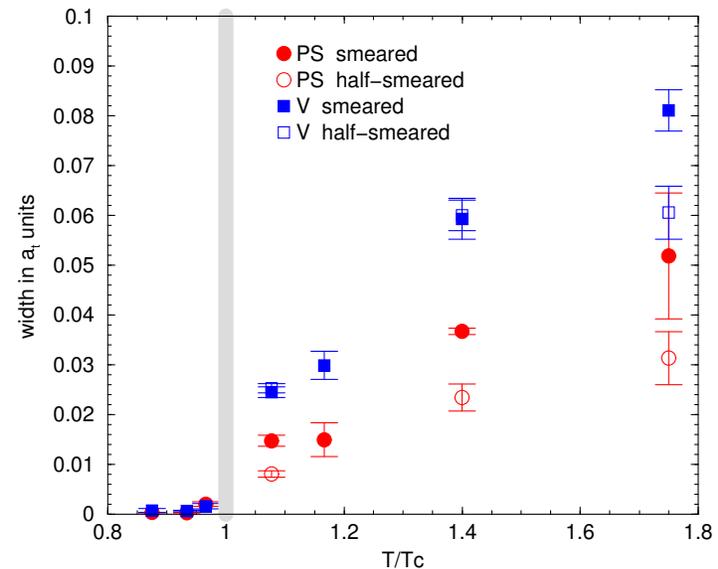
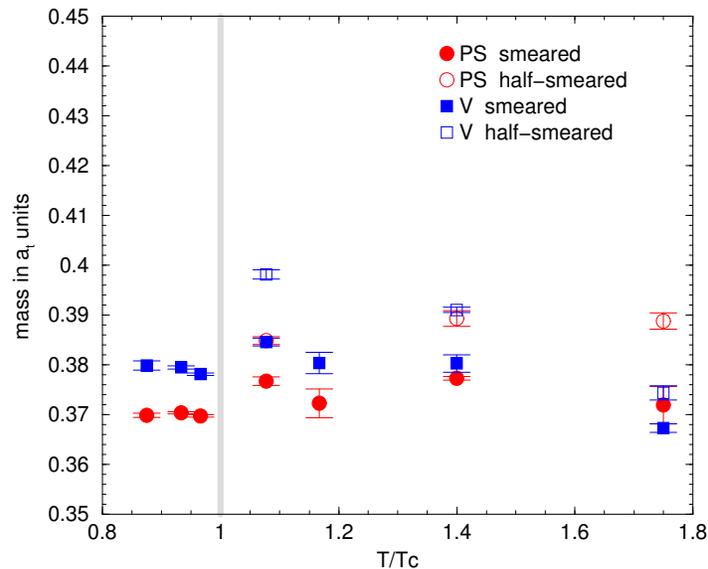
$J/\psi$  gradually disappears for  $T \gtrsim 1.5T_c$   
 $J/\psi$  strength reduced by 25% at  $T = 2.25T_c$



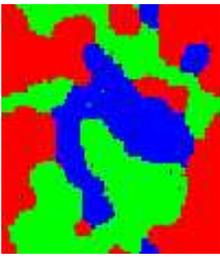


# Heavy quark spectral functions pressure broadening

- thermal broadening of charmonium spectral functions?
- no "first principle" evidence, **BUT** some evidence using resonance ansatz that incorporates a thermal width



T. Umeda, Proceedings of the RIKEN-BNL workshop on Lattice QCD at finite temperature and density, BNL-72083-2004

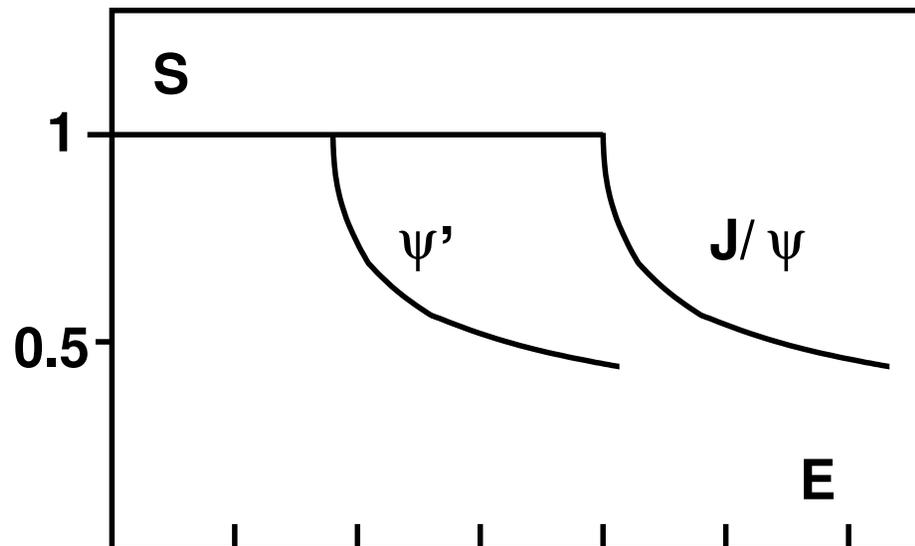


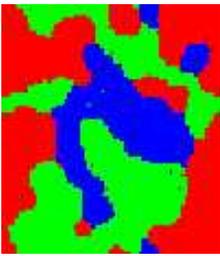
# Lattice QCD and Quarkonium Suppression in HI Collisions

---

- the original Matsui-Satz concept:
  - check whether medium supports existence of bound states under given thermal conditions: yes/no decision
  - fold with nuclear density and  $T(\tau)$  cooling profile

⇒ "abnormal" suppression pattern

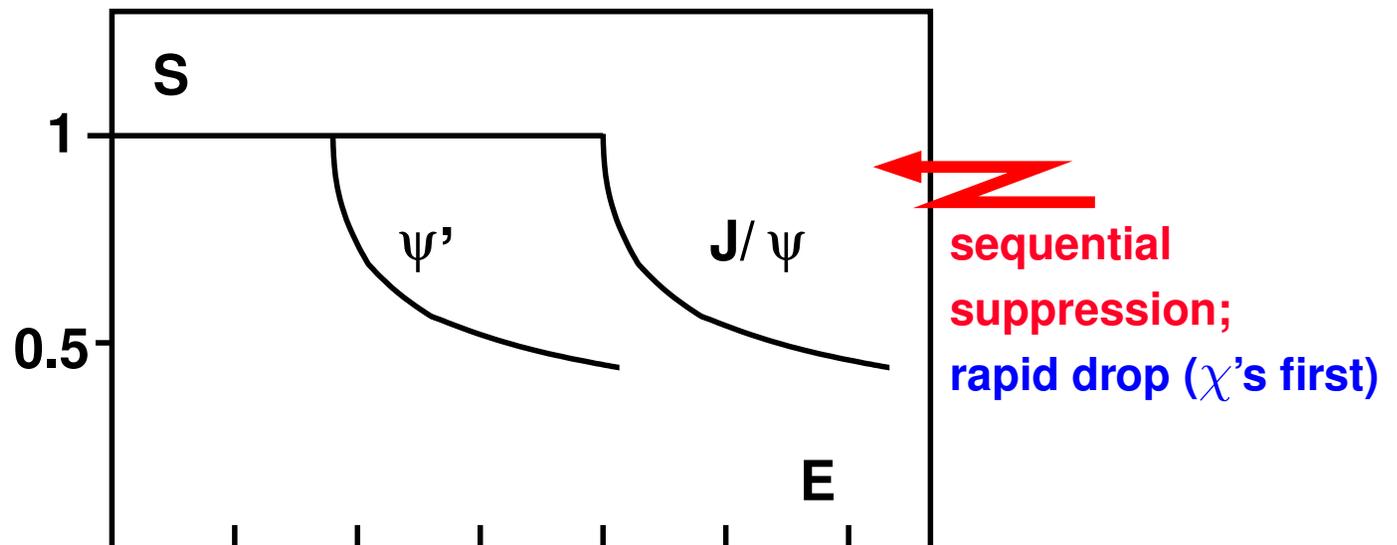


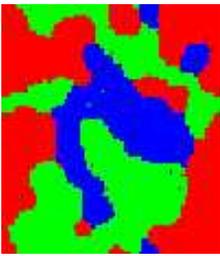


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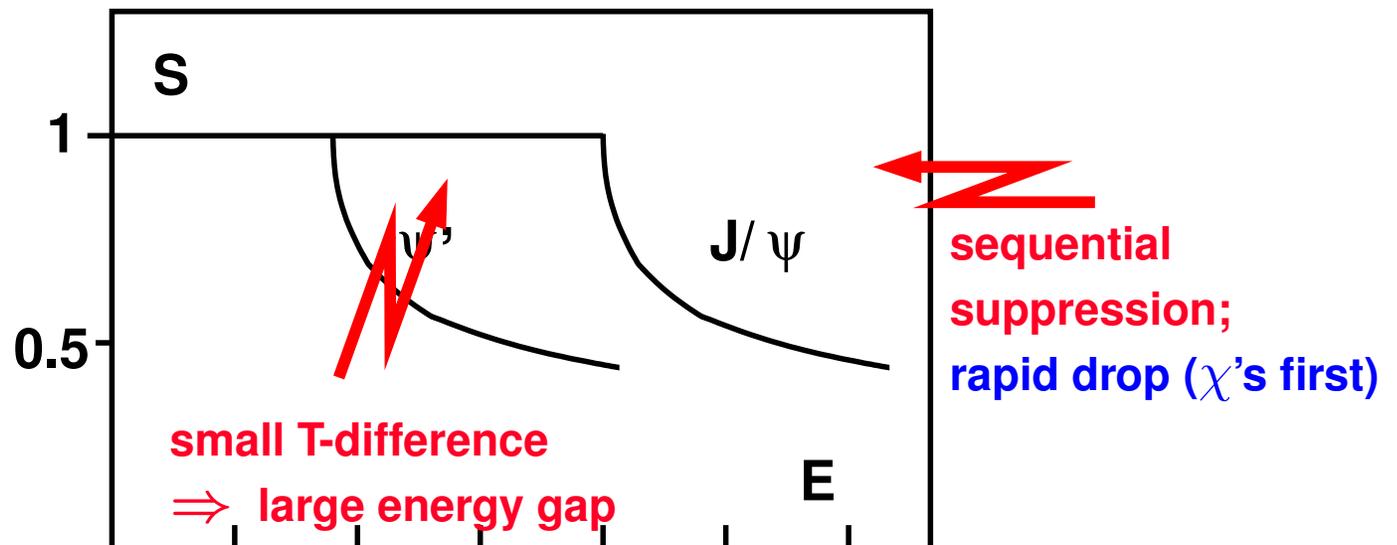


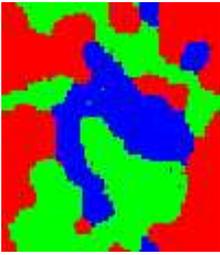


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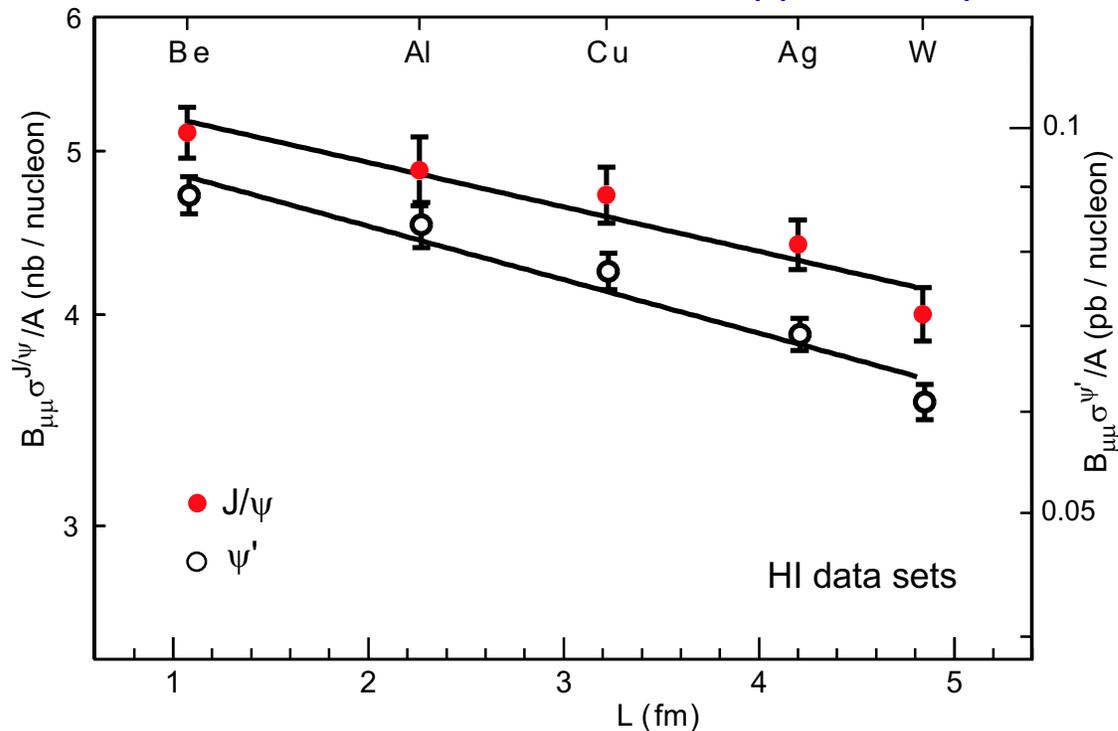
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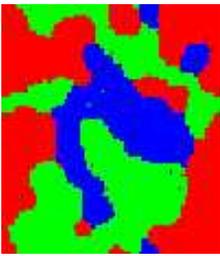
- "conventional complications": nuclear absorption
  - absorption in p-A collisions well analyzed

NA50, EPJC33 (2004) 31

$$\sigma_{pA} = \sigma_0 \cdot A \exp(-\sigma_{abs}L)$$

⇒ "normal" suppression pattern





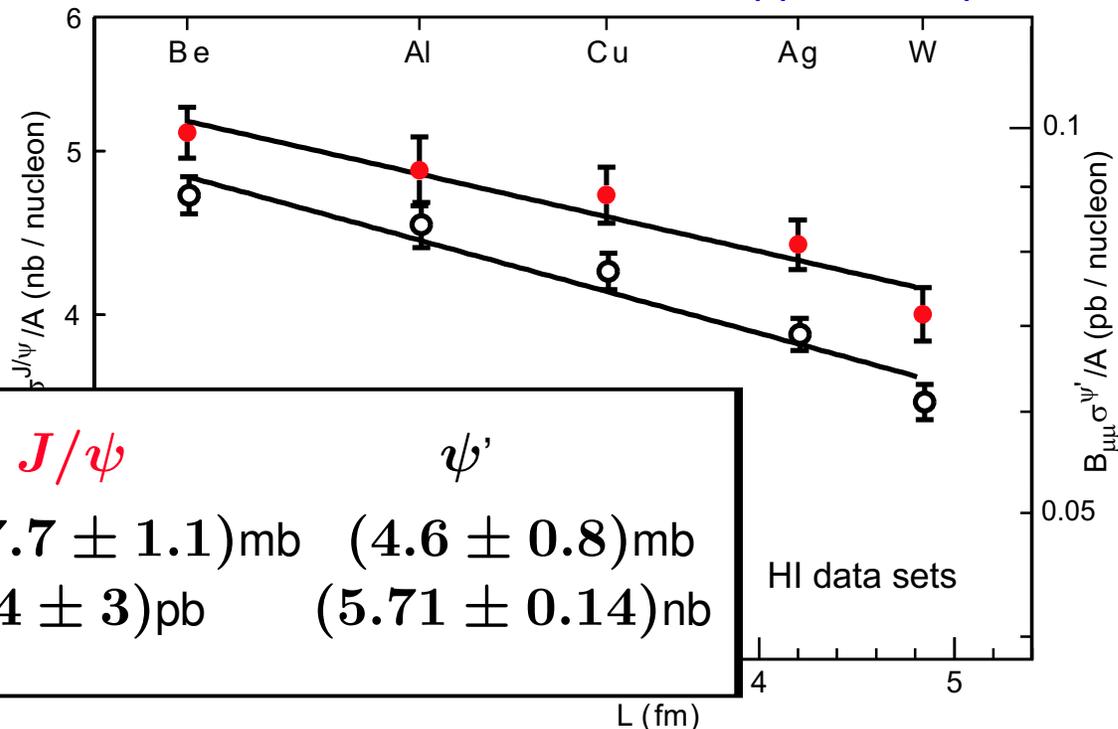
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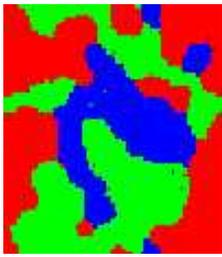
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# Lattice QCD and Quarkonium Suppression in HI Collisions

---

- Matsui-Satz: dissolved  $c\bar{c}$  never recombine again;  
potential model approach suggests sequential suppression pattern

- details depend on "potential" used in Schrödinger equation
- generic features consistent with spectral function studies

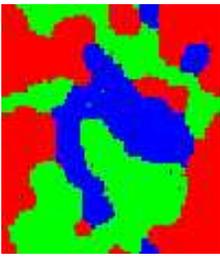
- $J/\psi$  survives the deconfinement transition and melts only at

$$T_{J/\psi}/T_c \sim (1.5 - 2.5)$$

- $\psi'$  and  $\chi_c$  dissolve at (or close to)  $T_c$

$$T_{\psi'} < T_{\chi} \text{ and } T_{\chi} \gtrsim T_c \text{ ???}$$

If so: small variations in dissociation temperature close to  $T_c$  will have significant effect on suppression pattern (large changes in density)

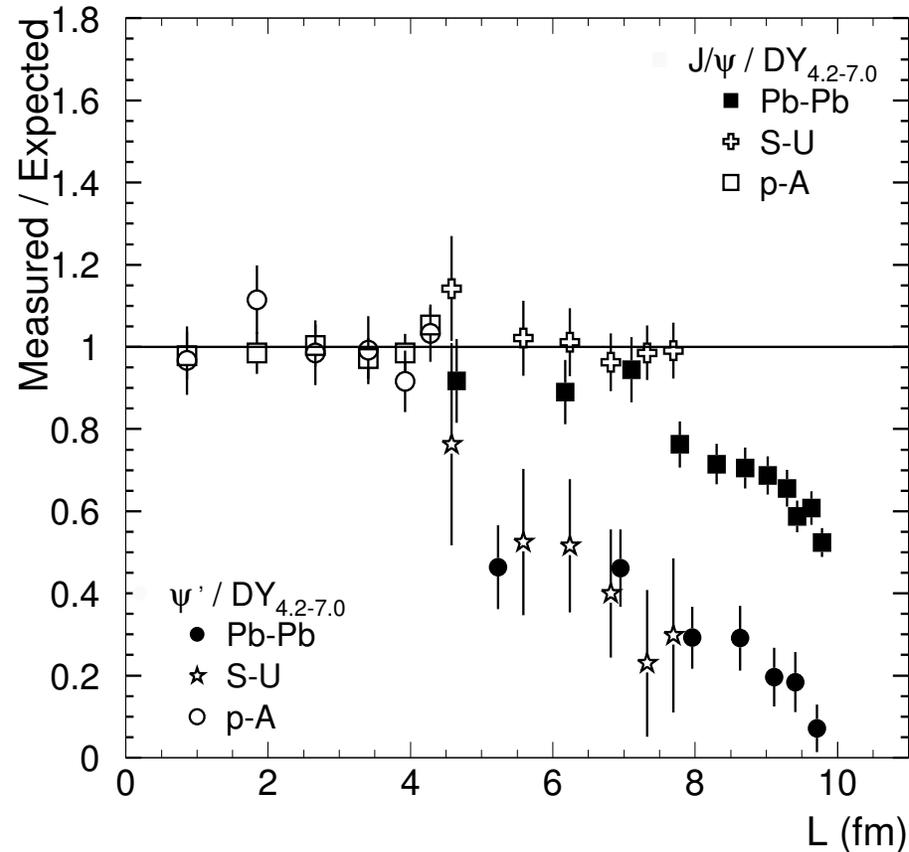


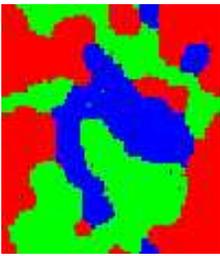
# Quarkonium suppression in HI collisions

- SPS data on charmonium suppression:

NA50, hep-ex/0405056

- may support sequential suppression pattern (or not)



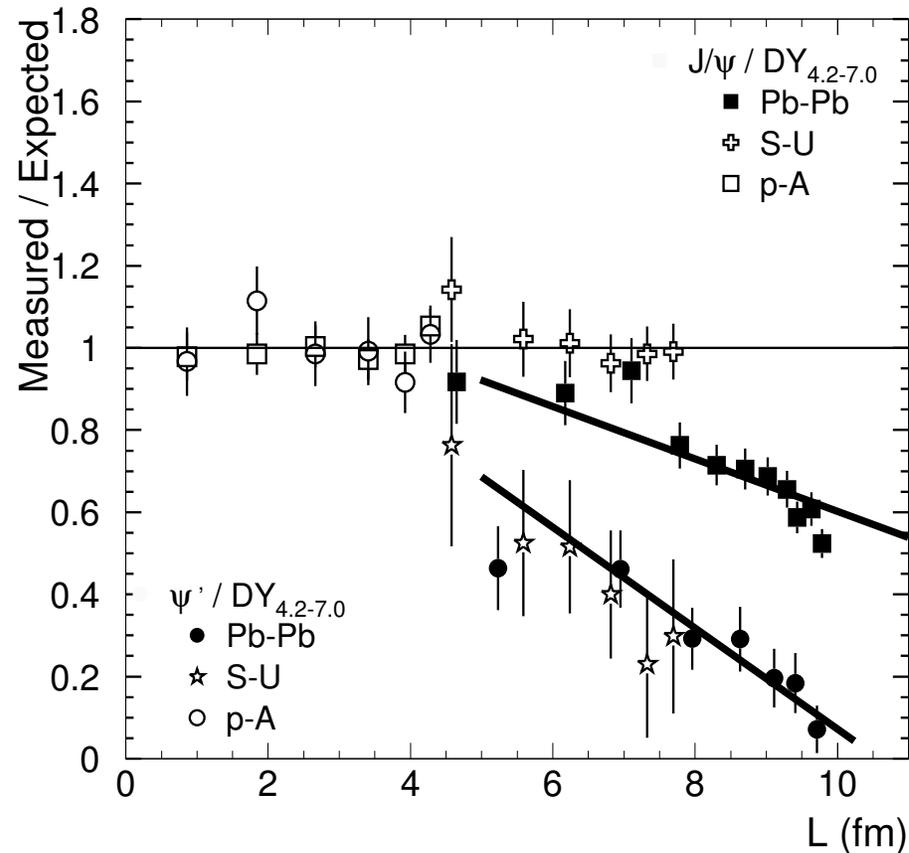


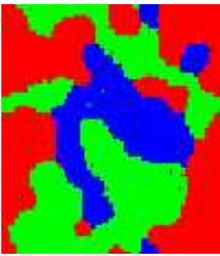
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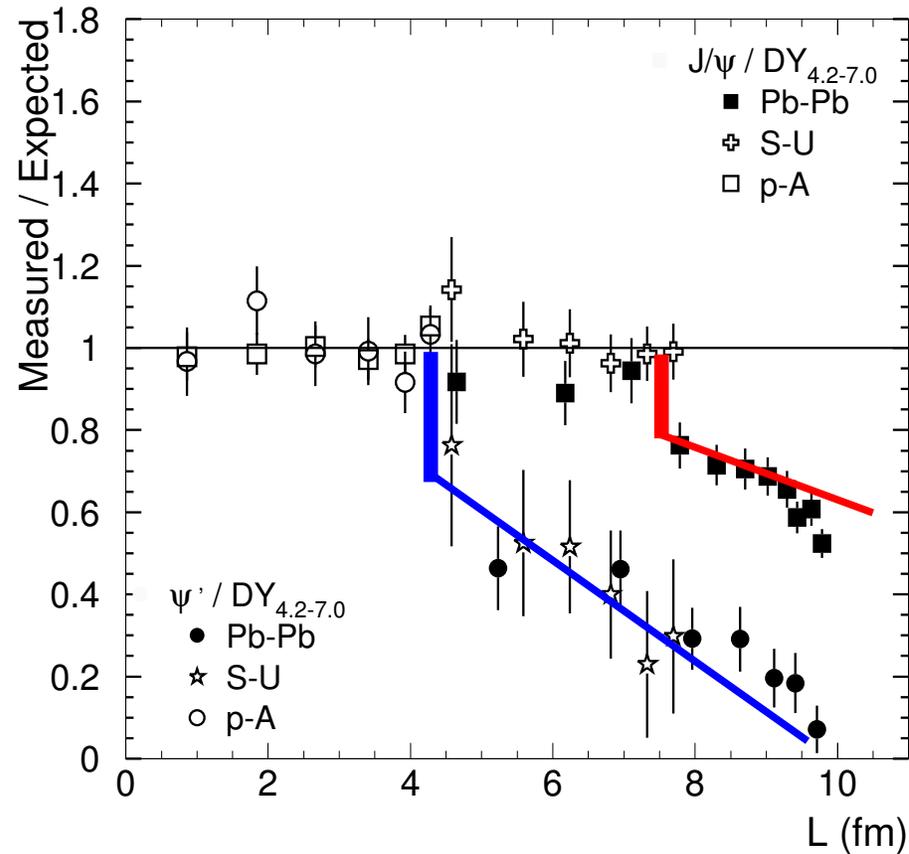
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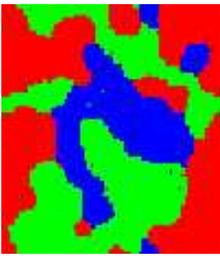




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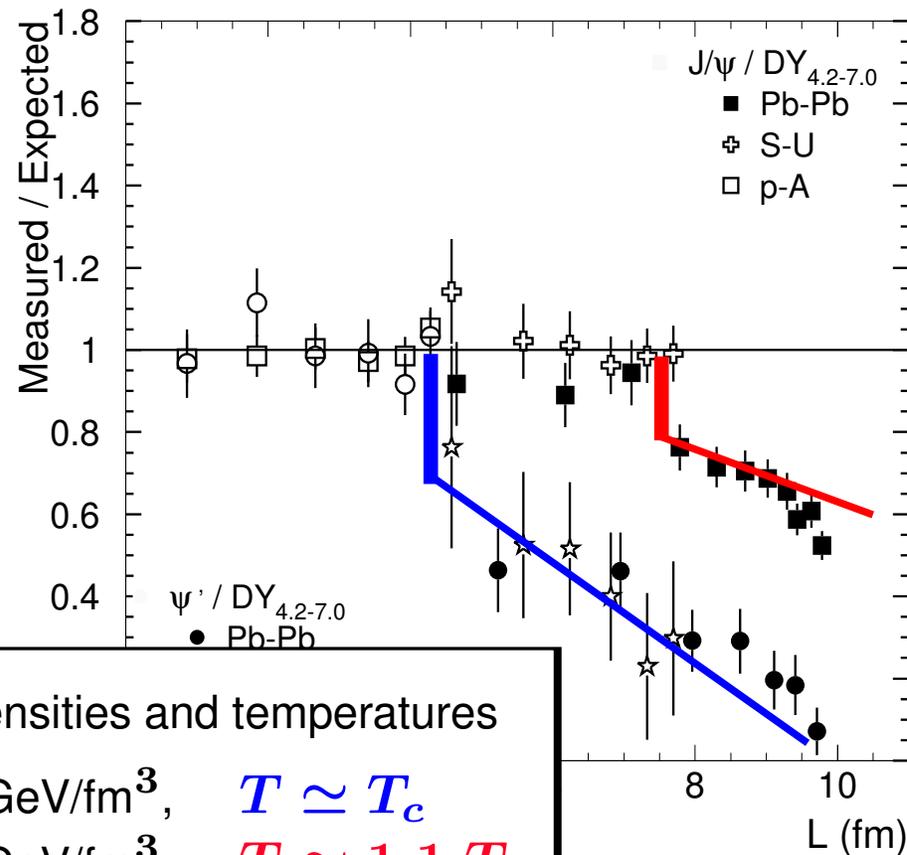
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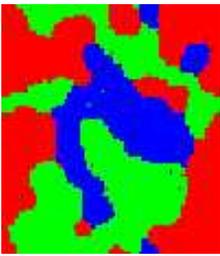
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"critical" energy densities and temperatures

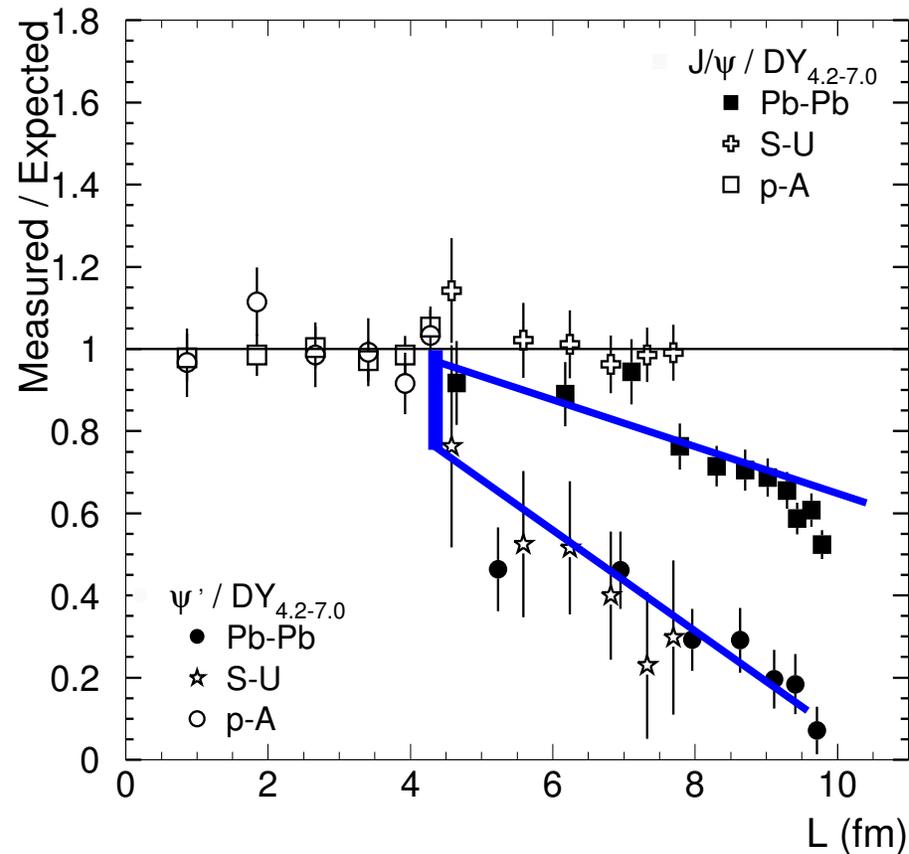
$$L=4 \text{ fm: } \epsilon \simeq 1.1 \text{ GeV/fm}^3, \quad T \simeq T_c$$

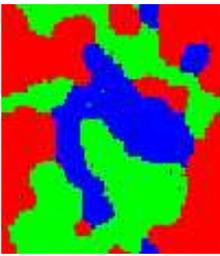
$$L=8 \text{ fm: } \epsilon \simeq 2.2 \text{ GeV/fm}^3, \quad T \simeq 1.1 T_c$$



# Quarkonium suppression in HI collisions

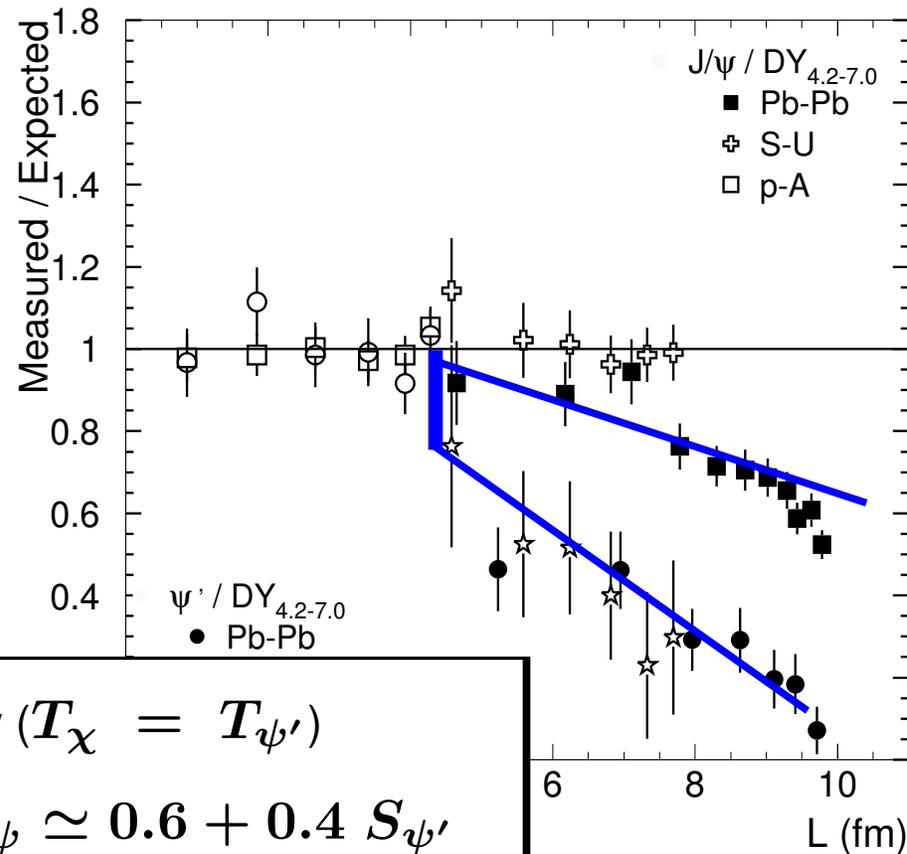
- SPS data on charmonium suppression:
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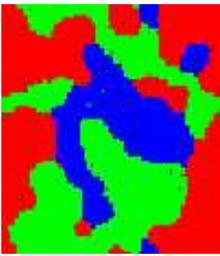
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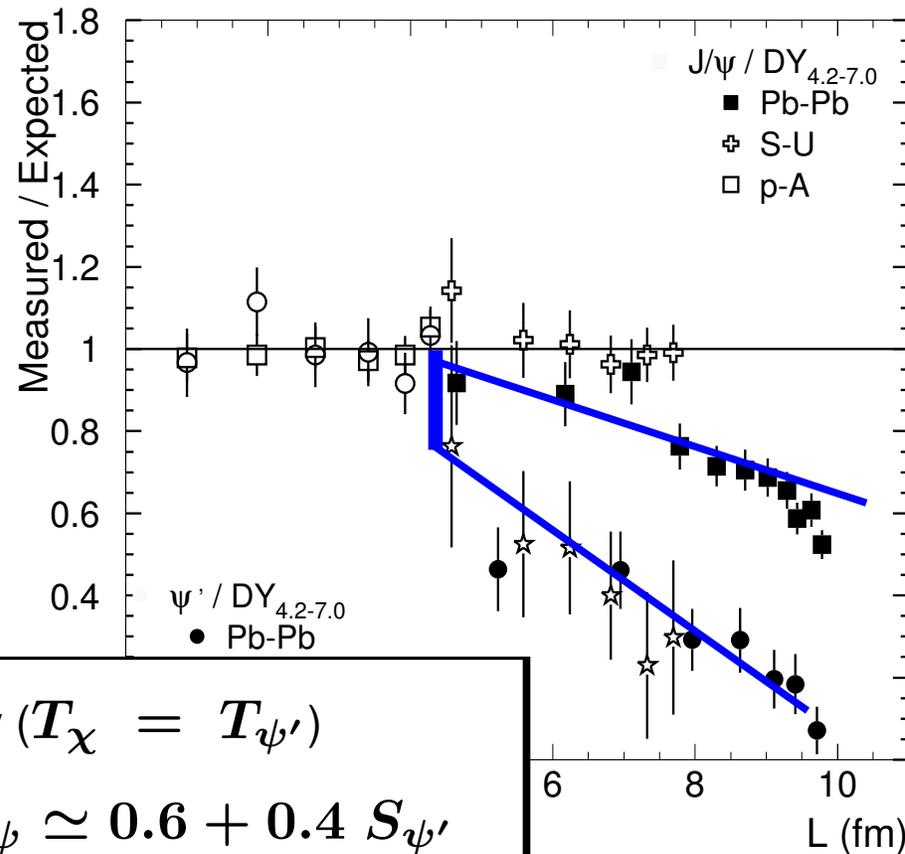
survival probability ( $T_\chi = T_{\psi'}$ )

$$\epsilon \gtrsim \epsilon_c : S_{J/\psi} \simeq 0.6 + 0.4 S_{\psi'}$$



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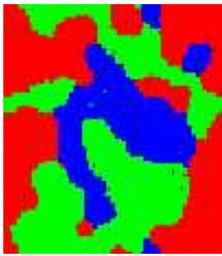


in conflict  
with S-U data

suggests:  
only  $\psi'$ ,  $\chi$  suppression  
up to  $\epsilon \simeq 3.5 \text{ GeV/fm}^3$   
or  $T \simeq 1.3 T_c$

survival probability ( $T_\chi = T_{\psi'}$ )

$$\epsilon \gtrsim \epsilon_c : S_{J/\psi} \simeq 0.6 + 0.4 S_{\psi'}$$



# Deconfinement and Quarkonium Suppression

---

- Deconfinement, screening and asymptotic freedom
  - deconfinement is density driven
- Heavy quark free energies
  - screening sets in at short distances;  $1/r$  still dominant scale
- Potential models for quarkonium
  - dissociation may spoil sequential suppression pattern
- Spectral functions
  - (directly produced)  $J/\psi$  exist well above  $T_c$
- Charmonium in heavy ion collisions
  - sequential suppression pattern may be the smoking gun