

# Dilepton low $p_T$ Suppression as an Evidence of the CGC

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Talk based on work with M. A. Betemps (hep-ph/0408097 *Phys. Rev. D* in press)

# Outline

- Motivation
- Color Glass Condensate
- Dilepton production in the Color Glass Condensate
- Saturation effects in the Dilepton  $p_T$  spectra
- Cronin effects in dilepton production
- Conclusions

# Motivation

- Gluon High Density  $\Rightarrow$  Saturation below a characteristic scale  $Q_s \Rightarrow$  Color Glass Condensate (CGC).
- Search for signatures of the CGC description of the saturated regime.
- **proton-nucleus** collisions  $\Rightarrow$  ideal experiment to investigate the saturation effects described by the CGC in the proton fragmentation region.
- Transverse momentum distribution  $p_T$  at high energies:
  - Hadron Production **measured** and **investigated**.
  - **dilepton production**  $\Rightarrow$  sensitive probe of the perturbative shadowing and saturation dynamics in **proton-proton**, **proton-nucleus** or **nucleus-nucleus** scattering (**needs measurements**).

# What we have

- Inclusive hadron production
  - To calculate the  $p_T$  and  $y$  (rapidity) distributions

$$\frac{d\sigma^{pA \rightarrow hX}}{dq_T^2 dy_h} = \frac{d\sigma^{ij \rightarrow kX}}{dq_T^2 dy_j} \otimes f_i(y_i, Q_h^2) \otimes f_j(y_j, Q_h^2) \otimes D_{k \rightarrow h}(z, Q_h^2).$$

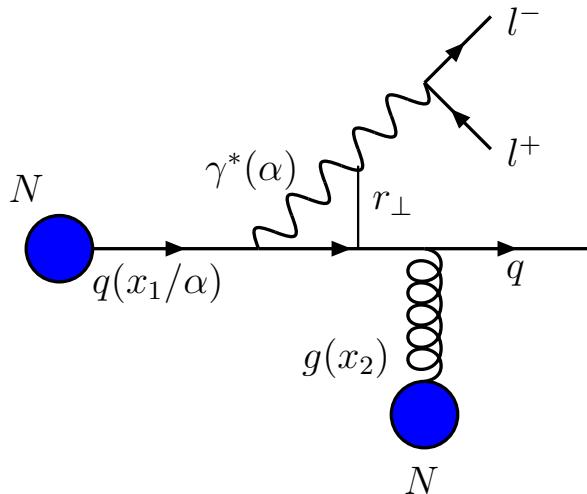
- Needs a fragmentation function  $\Rightarrow$  strongly dependent on the final state interactions
- dilepton production

$$\frac{d\sigma^{pA \rightarrow l^+ l^- X}}{dq_T^2 dy} = \frac{d\sigma^{ij \rightarrow kX}}{dq_T^2 dy} \otimes f_i(y_i, Q_h^2) \otimes f_j(y_j, Q_h^2).$$

- Final state interactions are disregarded (electromagnetic interaction).
- Cleaner analysis

# Perturbative Shadowing in $pp$ collisions

Investigated in the dipole picture



Dipole ?

- $r_{\perp} \rightarrow$  photon-quark transverse separation,
- $\alpha r_{\perp} \rightarrow q\bar{q}$  (dipole) transverse separation,
- $\alpha \rightarrow$  quark light-cone momentum fraction carried by the photon,
- $x_1/\alpha \rightarrow$  projectile momentum fraction carried by the quark,
- $x_2 \rightarrow$  target momentum fraction carried by the gluon.
- $p_T \rightarrow$  transverse momentum of the lepton pair.
- $M^2$  squared lepton pair mass.
- $x_F = x_1 - x_2$ .

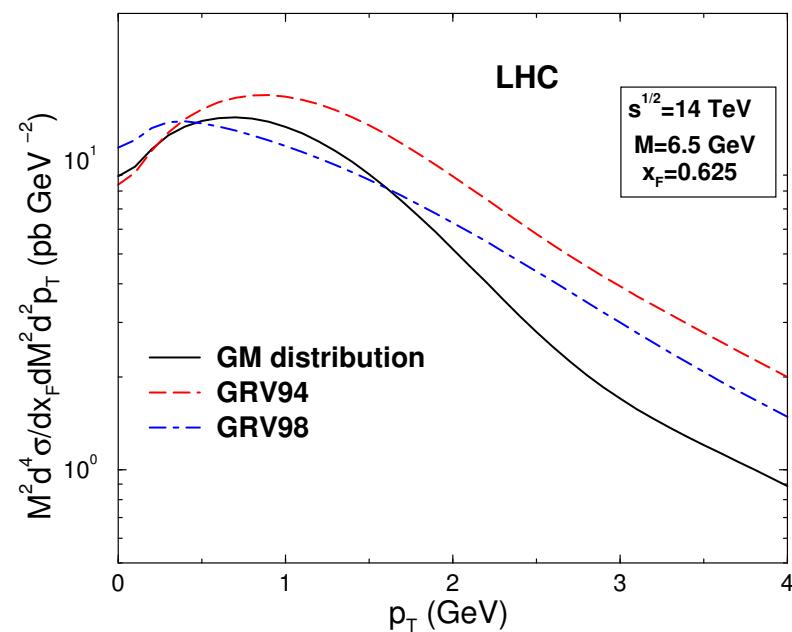
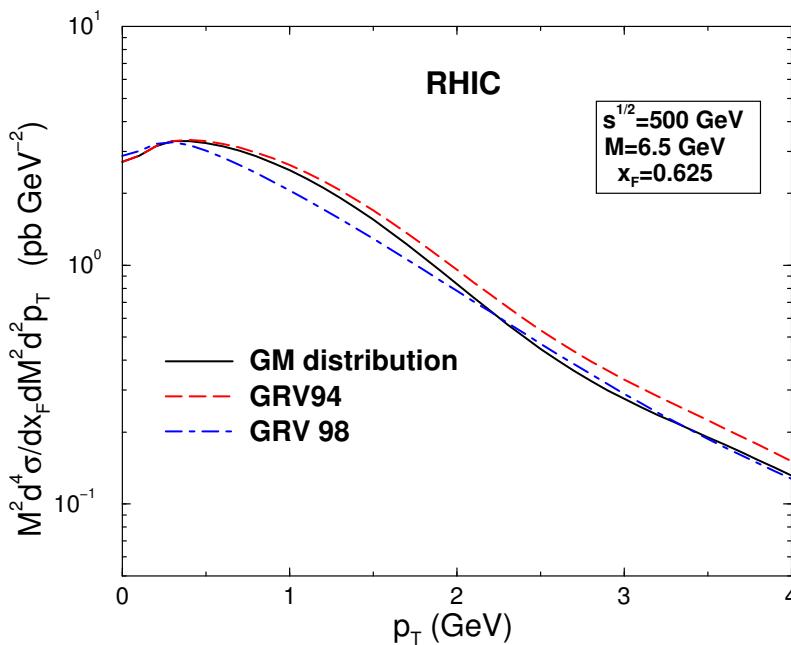
$$\frac{d\sigma_{T,L}(qN \rightarrow q\gamma^* N)}{d \ln \alpha} = \int d^2 \mathbf{r} |\Psi_{\gamma^* q}^{T,L}(\alpha, \mathbf{r})|^2 \sigma_{dip}^{q\bar{q}}(x_2, \alpha \mathbf{r})$$

- The differential Drell-Yan cross section can be written as

$$\frac{d\sigma^{DY}}{dM^2 dx_F d^2 p_T} = \frac{\alpha_{em}}{6\pi M^2} \frac{1}{(x_1+x_2)} \int_{x_1}^1 \frac{d\alpha}{\alpha} F_2^p \left( \frac{x_1}{\alpha} \right) \frac{d\sigma(qN \rightarrow q\gamma^* N)}{d \ln \alpha d^2 p_T}$$

# Perturbative Shadowing in $pp$ collisions

- Perturbative corrections in the dipole cross section by Glauber-Mueller approach (AGL evolution equations)
- Comparison with the GRV predictions
- $p_T$  distribution in  $pp$  collision (forward rapidities) at RHIC and LHC energies the DY

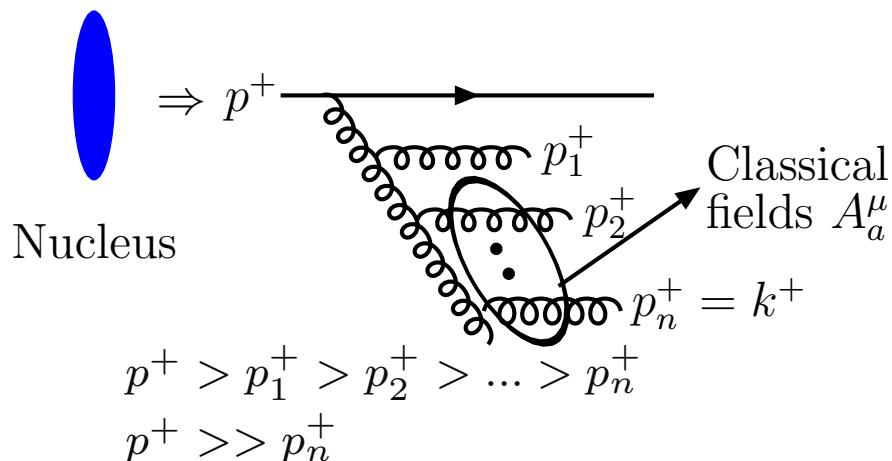


- Small corrections at RHIC energies
- Large unitarity effects at high  $p_T$  at LHC energies.
- Perturbative corrections appear at **large  $p_T$** .

# (Minimal) Color Glass Condensate

- Color  $\Rightarrow$  Gluonic field
- Glass  $\Rightarrow$  Internal dynamics evolves slowly
- Condensate  $\Rightarrow$  Dense and saturated gluon field

*Use of semi-classical techniques*



$A_a^\mu$  obeys Classical Yang-Mills equations,  
 $[D_{\mu\nu}, F_a^{\mu\nu}] = \delta^{\mu+} \rho_a(x^-, x_\perp)$ .

- color charge sources density.

- $x^-$  light-cone time.
- $\rho_a(x, x_\perp)$  stochastic variable with zero expectation value.
- average over all  $\rho_a$  configurations, with the gauge-invariant weight functional  $W_{\Lambda^+}[\rho_a]$
- $p^+ > \Lambda^+$  fast gluons,  $p^+ < \Lambda^+$  soft gluons.

# Color Glass Condensate

- Any observable is calculated by averaging over the sources configurations by means of

$$\langle A_a^i(x^+, \vec{x}) A_b^j(x^+, \vec{y}) \dots \rangle_{\Lambda^+} = \int \mathcal{D}_\rho W_{\Lambda^+}[\rho] \mathcal{A}_a^i(\vec{x}) \mathcal{A}_b^j(\vec{y}).$$

- Fundamental quantity in the CGC.
- Driven by the evolution equation JIMWLK.
- Phenomenology
  - Local Gaussian (can accommodate BFKL evolution and the gluon saturation)

$$W[x, \rho] = \exp \left\{ - \int dz_\perp \frac{\rho_a(z_\perp) \rho^a(z_\perp)}{2\mu^2(x)} \right\}$$

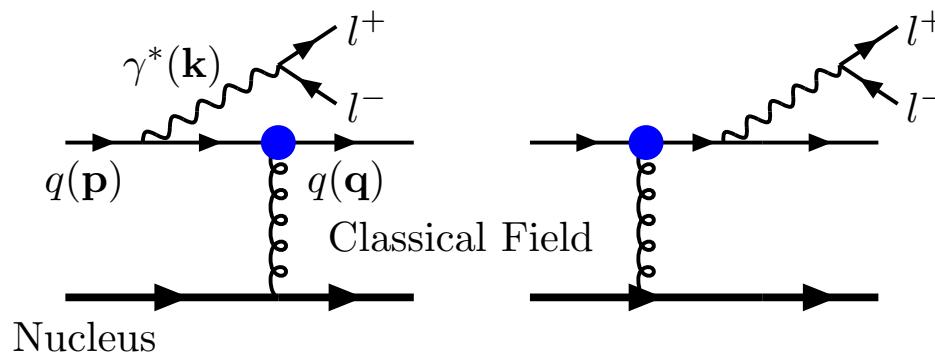
- Non local Gaussian (Predicted by the mean field asymptotic solution of the JIMWLK evolution equations)

$$W[x, \rho] = \exp \left\{ - \int dy_\perp dx_\perp \frac{\rho_a(x_\perp) \rho^a(y_\perp)}{2\mu^2(x)} \right\}$$

- $\mu^2(x)$  is related to the average of the color charge squared.

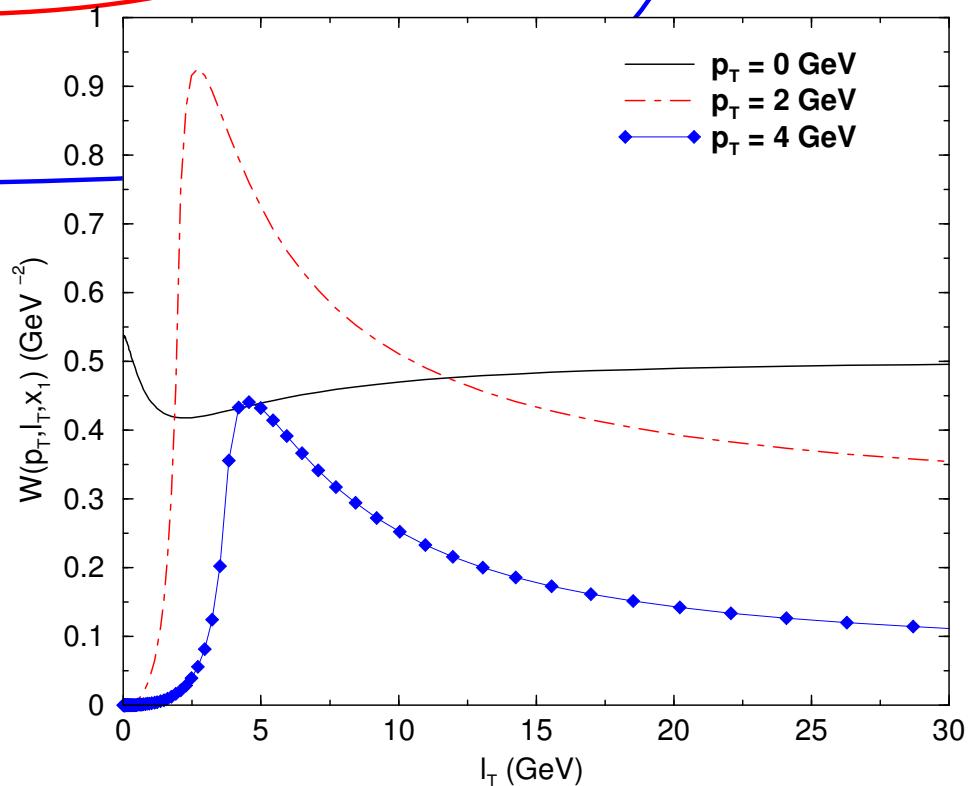
# Dilepton Production in CGC

The cross section is written as



$$\frac{d\sigma^{pA \rightarrow ql^+l^- X}}{dp_T^2 dM dx_F} = \frac{4\pi^2}{M} R_A^2 \frac{\alpha_{em}^2}{3\pi} \frac{1}{x_1 + x_2} \times \int \frac{dl_T}{(2\pi)^3} l_T W(p_T, l_T, x_1) C(l_T, x_2, A),$$

- $W(p_T, l_T, x_1)$  analytical calculations  $\Rightarrow$  select the values of  $l_T$  larger than  $p_T$ .
- $C(l_T, x_2, A)$  color field correlation  $\Rightarrow$  interaction of the quark with the condensated gluonic field (Classical field).



F. Gelis, J.Jalilian-Marian, *Phys. Rev. D* 66, 094014 (2002)

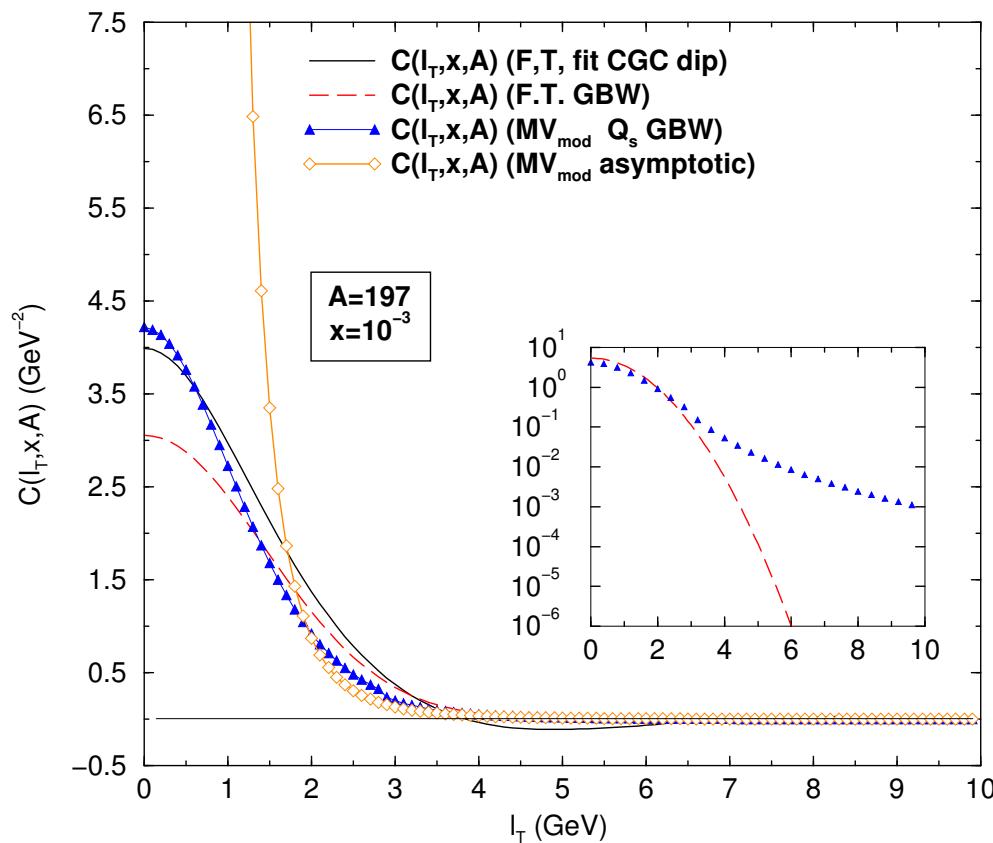
# Color Field Correlation

$$C(l_T) \equiv \int d^2x_\perp e^{il_T \cdot x_\perp} \langle U(0)U^\dagger(x_\perp) \rangle_\rho,$$

- related to the Fourier transform of non-integrated gluon distribution

$$C(l_T) = \frac{1}{\sigma_0} \int d^2r e^{il_T \cdot r} [\sigma_{dip}(r \rightarrow \infty) - \sigma_{dip}(r)],$$

- We have analyzed some models for the correlation function
  - McLerran-Venugopalan
  - GBW
  - Iancu, Itakura and Munier (CGCfit)
- We use McLerran-Venugopalan



# Local $\times$ Non-local

- We use McLerran-Venugopalan model with an energy dependence into the saturation scale

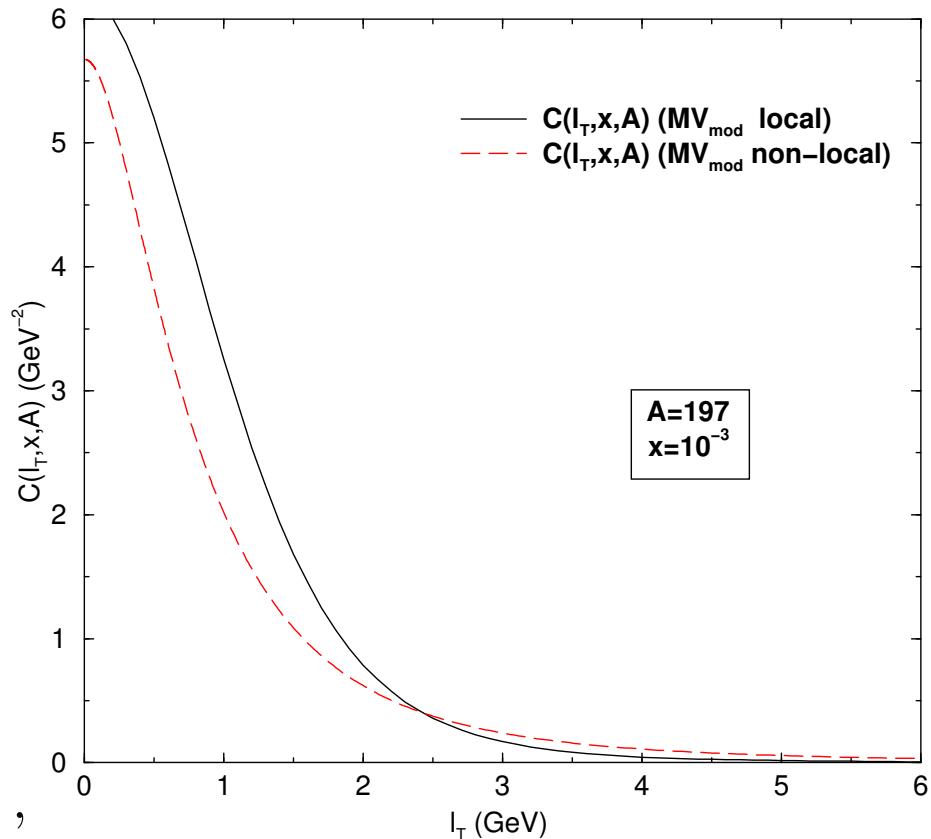
$$Q_s^2(x, A) = A^{1/3} \left( \frac{x_0}{x} \right)^\lambda \quad \text{parameters } \left\{ \begin{array}{l} x_0 \\ \lambda \end{array} \right.$$

- Local Gaussian

$$C_{MV_{mod}}(l_T, x, A) = \int d^2 x_\perp \times e^{il_T \cdot x_\perp} e^{-\frac{Q_s^2(x, A)}{\pi} \int \frac{dp}{p^3} (1 - J_0(px_\perp))}.$$

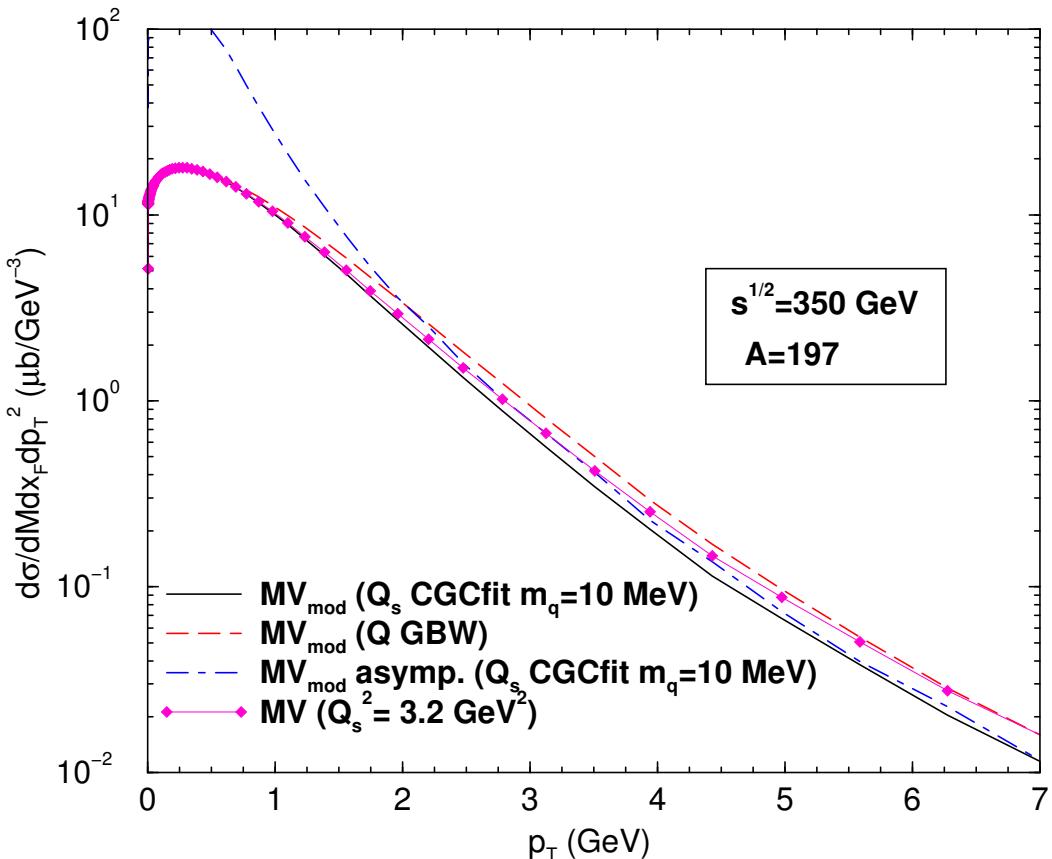
- Non-local Gaussian

$$C(l_T, x, A) \equiv \int d^2 x_\perp e^{il_T \cdot x_\perp} \times e^{-\frac{2}{\gamma_c} \int \frac{dp}{p} (1 - J_0(x_\perp p)) \ln \left( 1 + \left( \frac{Q_s^2(x, A)}{p^2} \right)^\gamma \right)},$$



# Dilepton $p_T$ spectra

RHIC



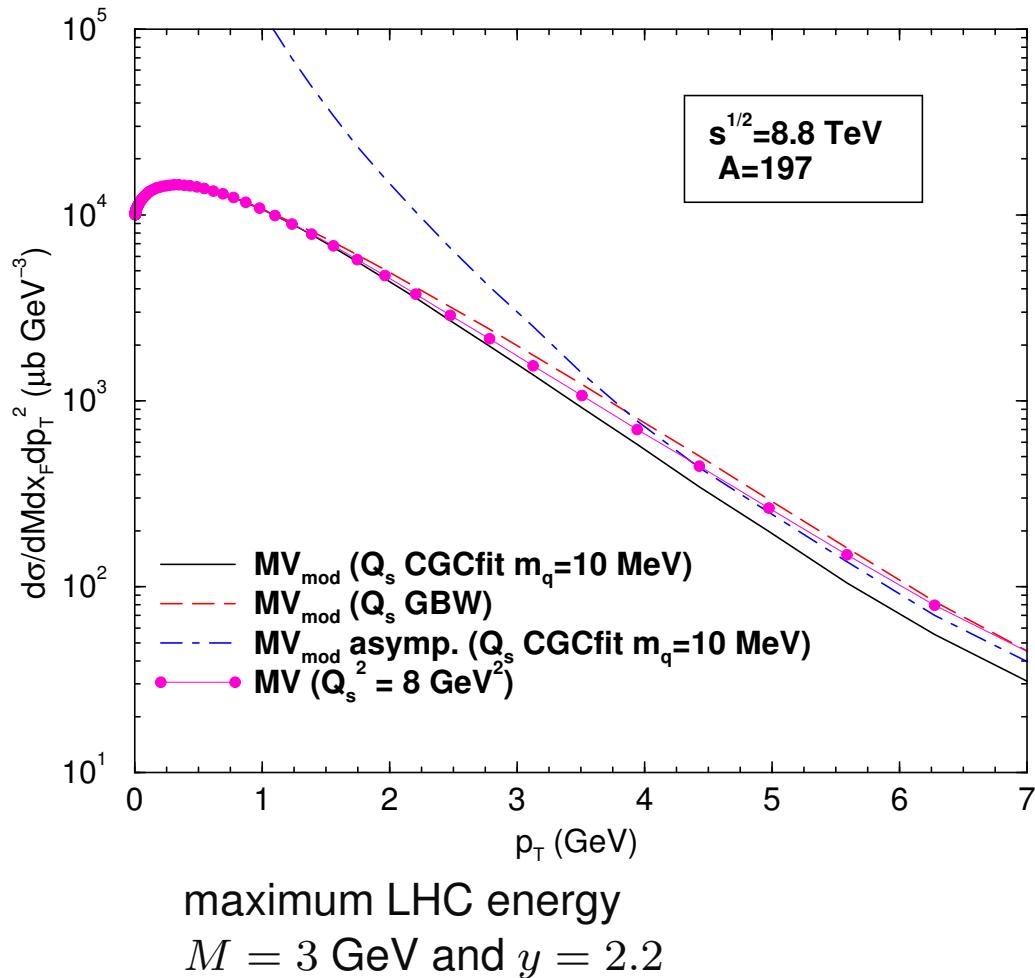
maximum RHIC energy  
 $M = 3 \text{ GeV}$  and  $y = 2.2$

fits	$Q_s^2 (x = 10^{-3})$ $A = 197$
GBW	$4.114 \text{ GeV}^2$
CGCfit	$3.069 \text{ GeV}^2$
$m_q = 10 \text{ MeV}$	

- Large suppression effects at small  $p_T$ ;
- Suppression below the saturation scale ( $Q_s$ );
- Dependence on the  $Q_s$  value at large  $p_T$ ;
- Large value of  $Q_s$  increases the spectra at large  $p_T$ ;
- $Q_s x$  evolution yields a reduction at large  $p_T$  in comparison with the no evolution case (Magenta line).

# Dilepton $p_T$ spectra

LHC



fits	$Q_s^2 (x = 10^{-3})$ $A = 197$
GBW	$4.114 \text{ GeV}^2$
CGCfit	$3.069 \text{ GeV}^2$
$m_q = 10 \text{ MeV}$	

- Large suppression effects at small  $p_T$ ;
- Suppression below the saturation scale (larger than at RHIC energies);
- Large value of  $Q_s$  increases the spectra at large  $p_T$ ;
- $Q_s$   $x$  evolution yields a reduction at large  $p_T$  in comparison with the no evolution case (**Magenta Line**).

# Seeking Cronin effect in Dilepton

- Nuclear modification factor

$$R_{pA} = \frac{\frac{1}{R_A^2} \frac{d\sigma^{pA \rightarrow l^+ l^- X}}{dp_T^2 dM dy}}{A^{1/3} \frac{1}{R_p^2} \frac{d\sigma^{pp \rightarrow l^+ l^- X}}{dp_T^2 dM dy}}$$

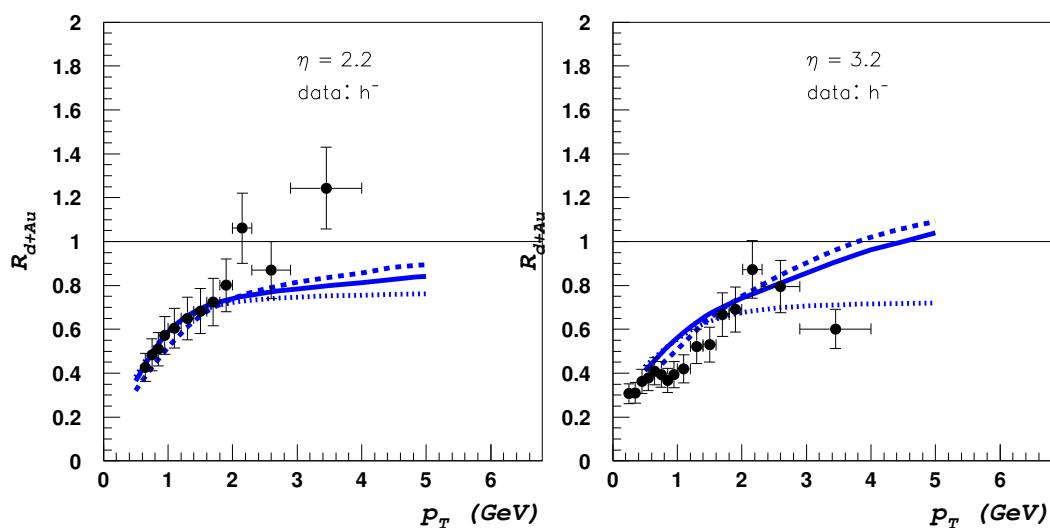
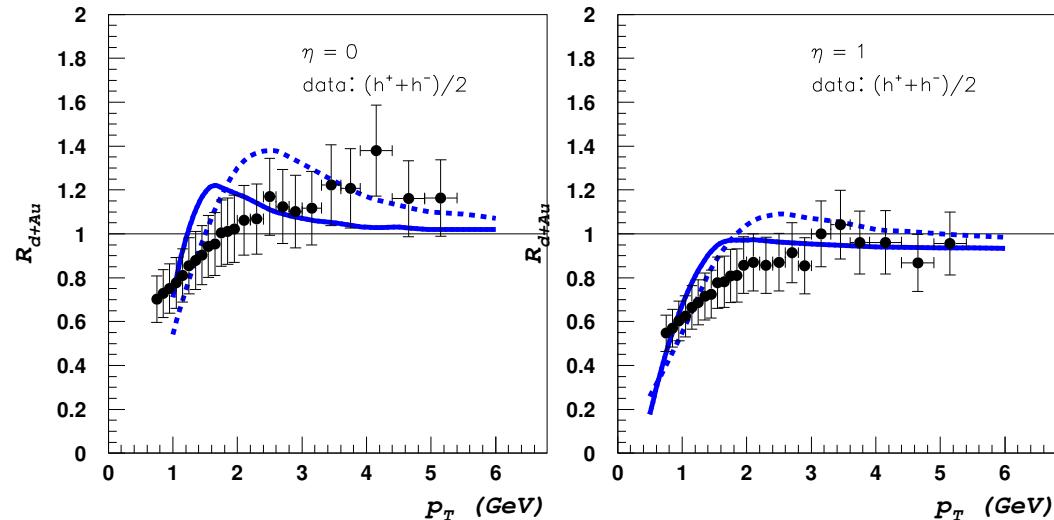
- Using the expressions to the cross section,

$$R_{pA}(y, p_T) = \frac{\int d^2 l_T W(p_T, l_T, x_1) C_A(l_T, x_2, A)}{A^{1/3} \int d^2 l_T W(p_T, l_T, x_1) C_p(l_T, x_2)},$$

- ratio between color field correlation weighted by the function  $W(p_T, l_T, x_1)$ ;
- Similar ratio used to investigate the Cronin effect in the hadron production;

# Cronin effect in the CGC approach

charged hadrons



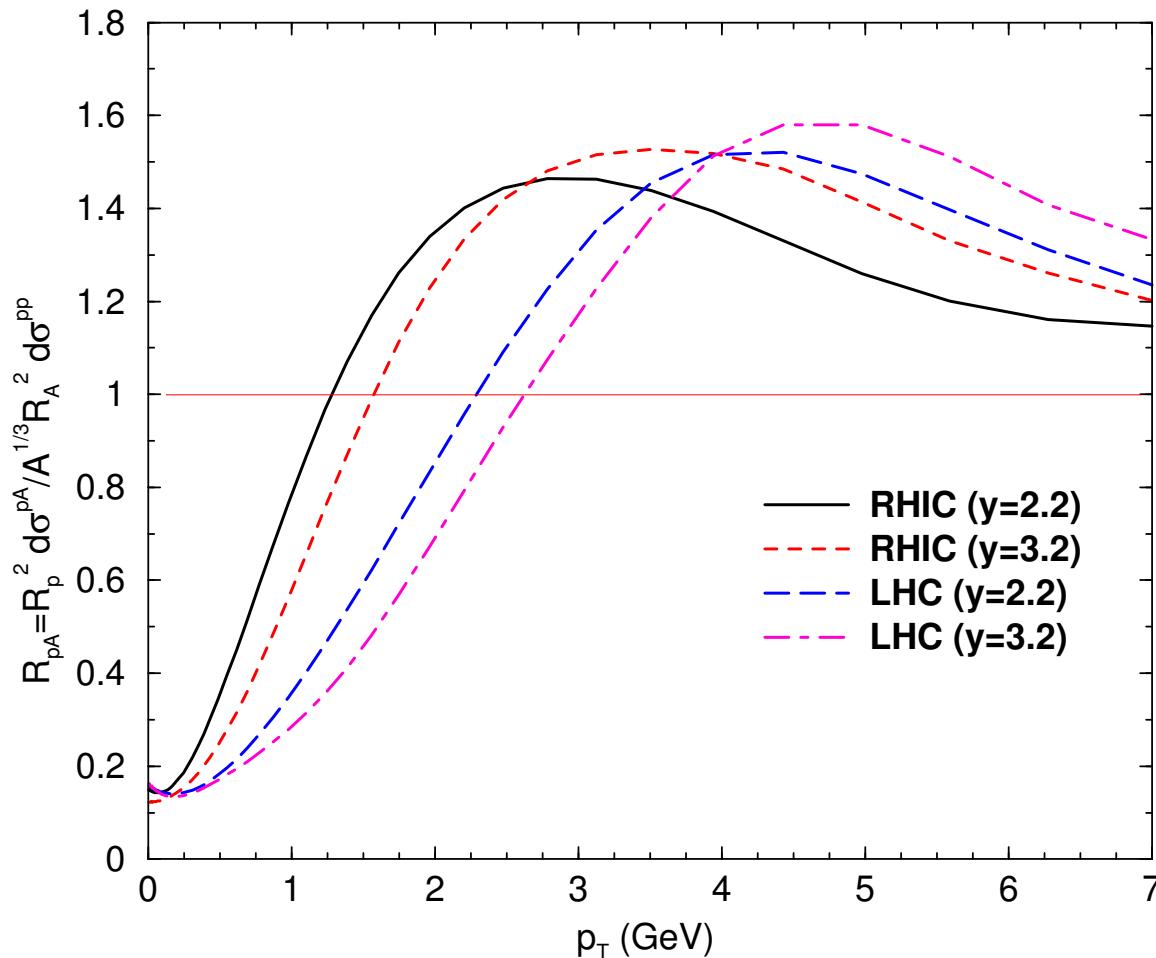
- Nuclear modification factor  $R_{dA}$ .

$$R_{dA} = \frac{\frac{d\sigma^{dA \rightarrow hX}}{dp_T^2 dy}}{\mathcal{N}_{coll} \frac{d\sigma^{pp \rightarrow hX}}{dp_T^2 dy}}$$

- data from  $dA$  collisions at  $\sqrt{s} = 200$  GeV.
- BRAHMS data.
- KKP fragmentation function
- Consider valence quarks
- Introduce a function to take into account large  $x$  gluon behavior

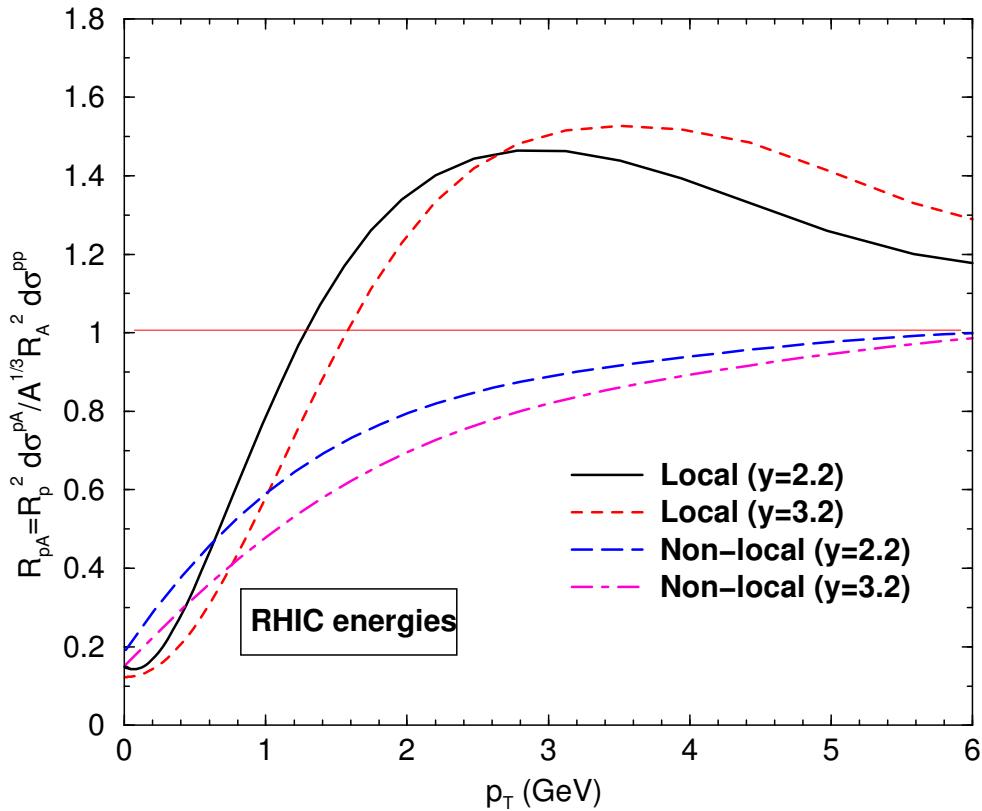
D. Kharzeev, Y. V. Kovchegov, K. Tuchin,  
[hep-ph/0405045](https://arxiv.org/abs/hep-ph/0405045).

# $R_{pA}$ Local Gaussian (dileptons)



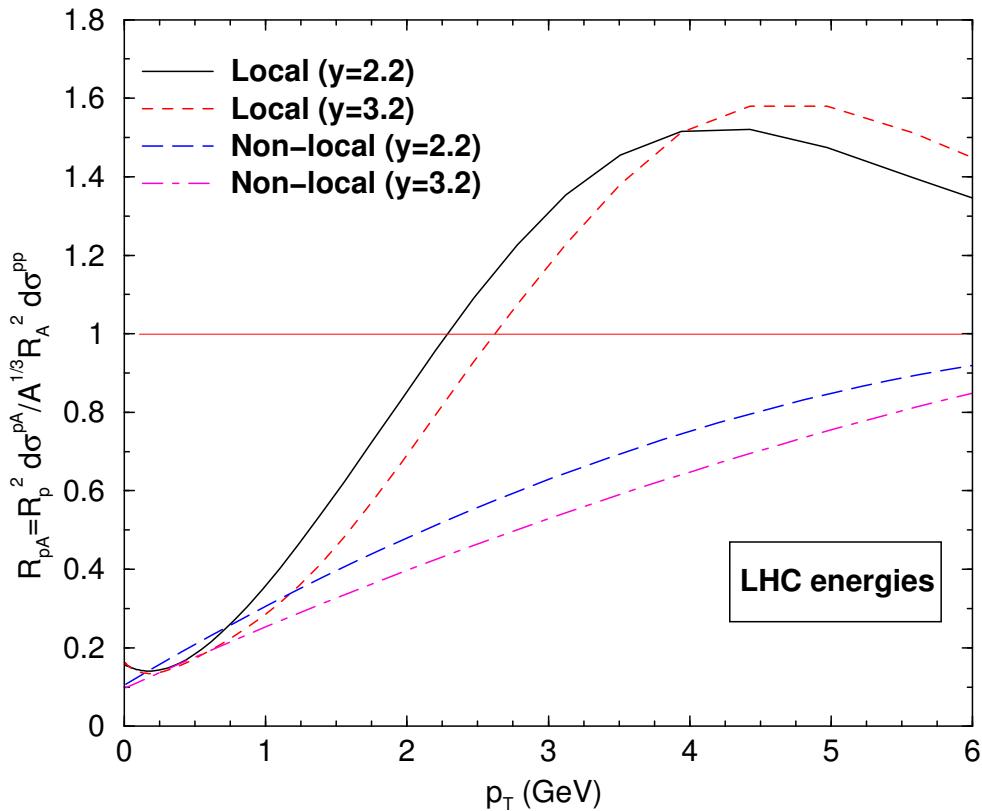
- ➊ Suppression at small  $p_T$ ;
- ➋ Cronin peak appears at intermediated  $p_T$ ;
- ➌ The peak increases and is shifted to large  $p_T$  with the increment in the rapidity;
- ➍ Disagreement with the suppression presented in the RHIC data on inclusive hadron sector

# Local $\times$ Non-local Gaussian



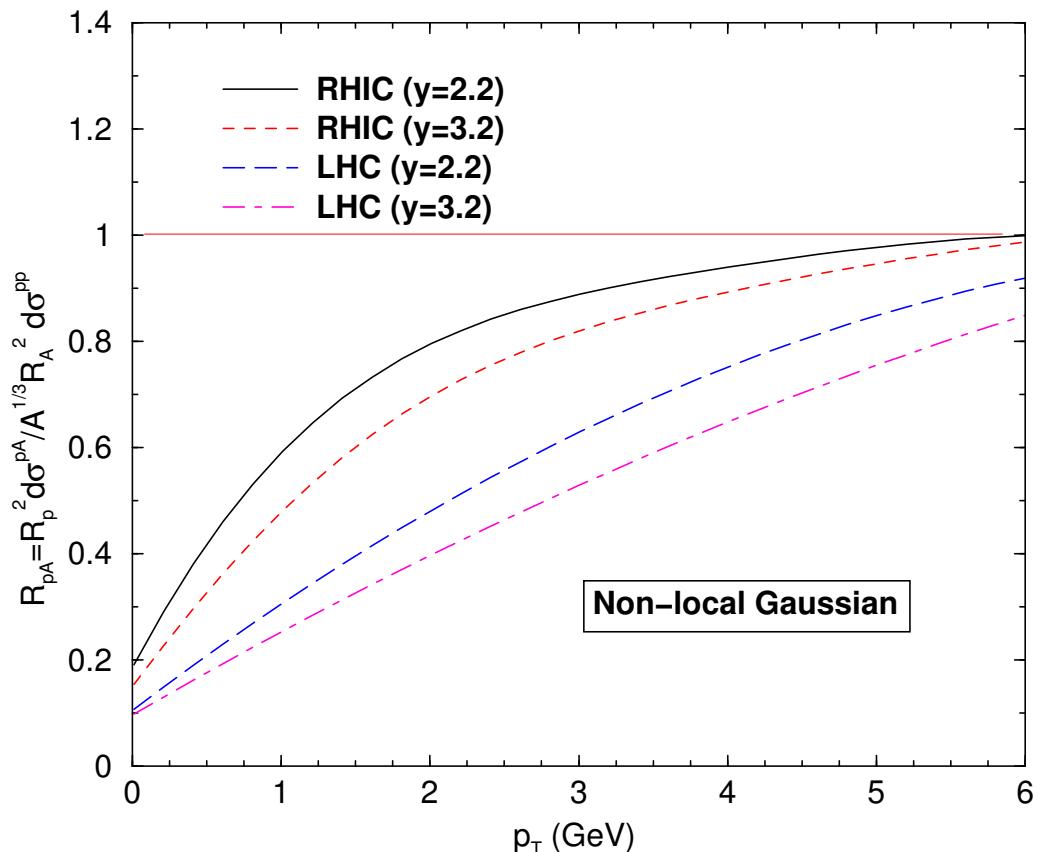
- The suppression of the Cronin peak is reached;
- The suppression is enlarged for large values of rapidity;
- RHIC data present the suppression of the Cronin peak at large rapidities;
- Effect of the evolution [Albacete, Armesto, Kovner, Salgado, Wiedemann, *Phys. Rev. D* 92, 082001 (2004)].

# Local $\times$ Non-local Gaussian



- The suppression of the Cronin peak is reached;
- The suppression is intensified for large values of rapidity;
- Simulation of the quantum evolution.

# Non-local Gaussian



- The suppression is intensified for large energies;
- Measurements on dilepton sector are needed.

# Conclusions

- The suppression at small and moderated  $p_T$  is an evidence of the saturation effects (CGC).
- The ratio  $R_{pA}$  shows a Cronin type peak with local Gaussian and presents a suppression with a non-local Gaussian, considering the dilepton  $p_T$  spectra.
- The dilepton  $p_T$  distribution indicates the Cronin effect as an initial state effect.
- Measurements on the dilepton  $p_T$  distribution at high energies are required.