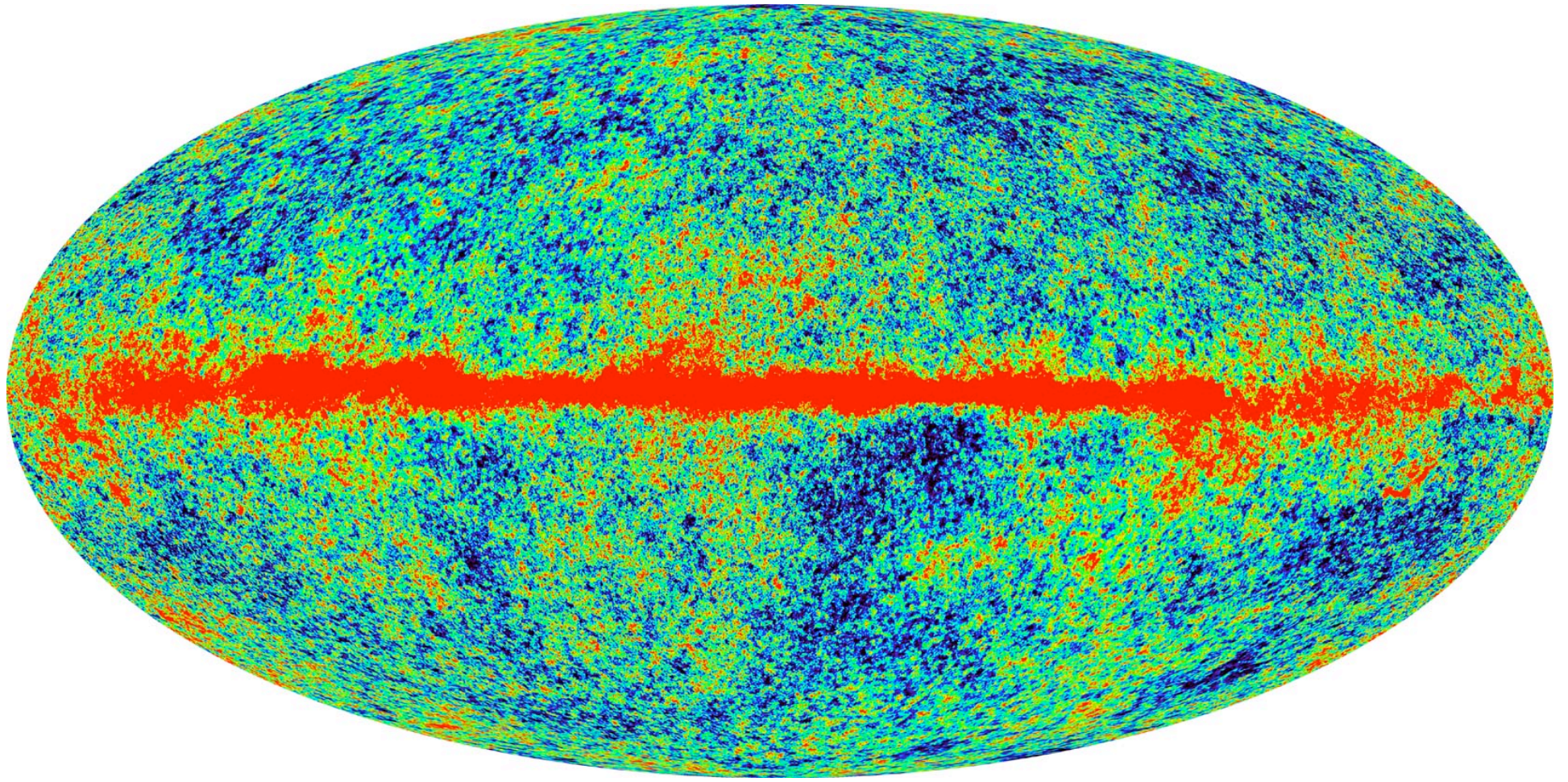
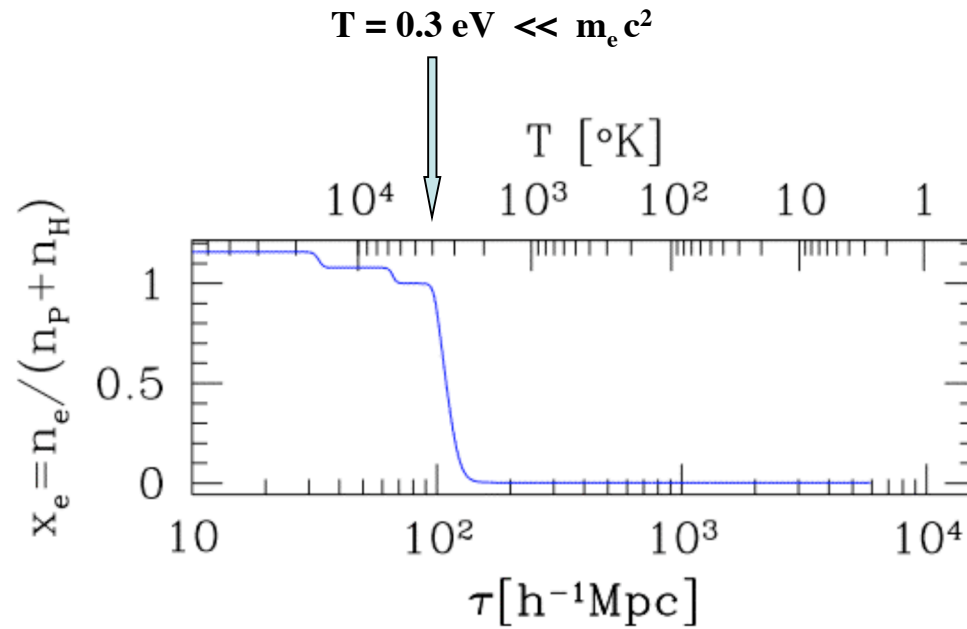


What creates the anisotropies?



Recombination



Hydrogen is ionized

Hydrogen is neutral

Thomson Scattering

Orders of Magnitude:

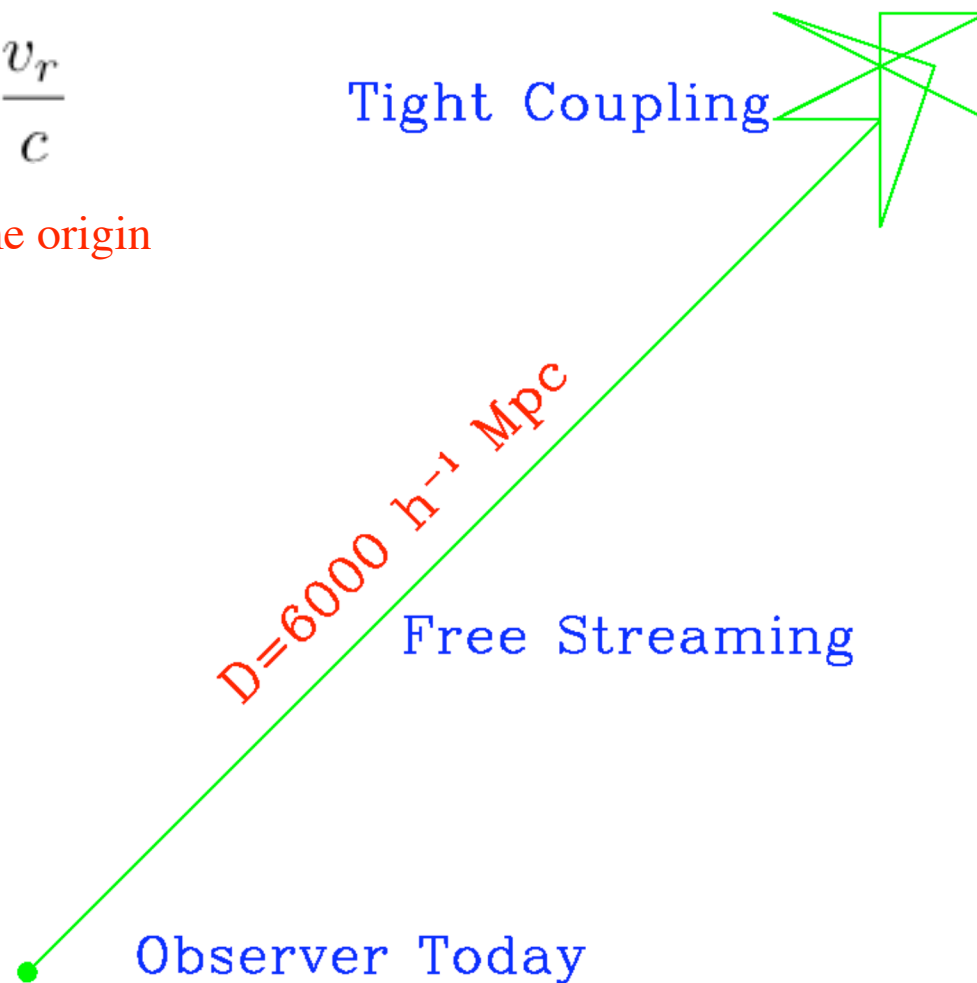
$$\begin{aligned}\lambda_T &= (a n_e \sigma_T)^{-1} \\ &= 2 \text{ Mpc } x_e^{-1} [(1+z)/1000]^{-2}\end{aligned}$$

$$\tau_R \approx 100 [\Omega h^2]^{-1/2} \text{ Mpc}$$

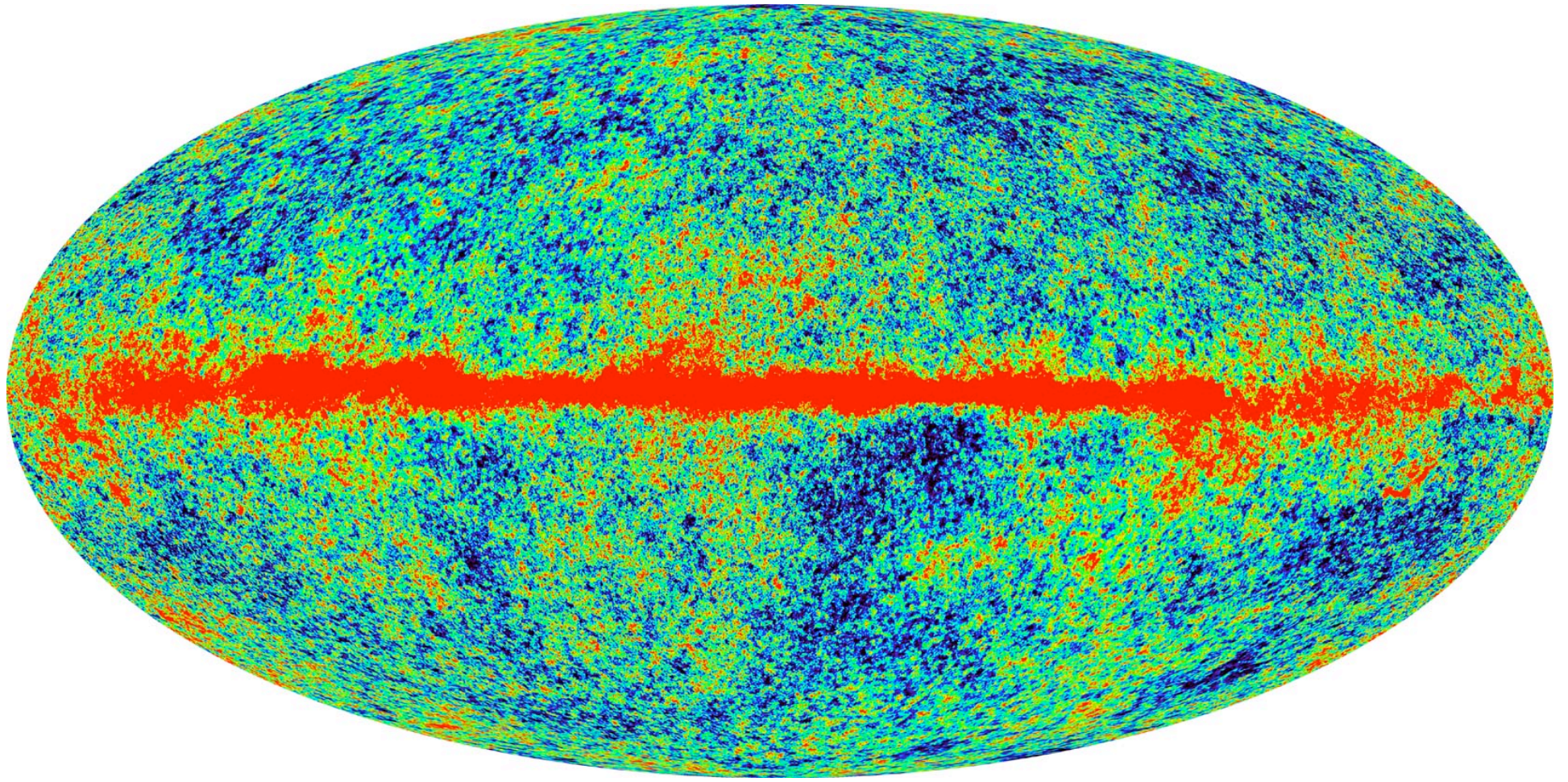
$$D = \tau_0 - \tau_R \approx 6000 [\Omega h^2]^{-1/2} \text{ Mpc}$$

$$\frac{\delta T}{T} = \phi + \frac{\delta_\gamma}{4} + \frac{v_r}{c}$$

All 3 effects have the same origin

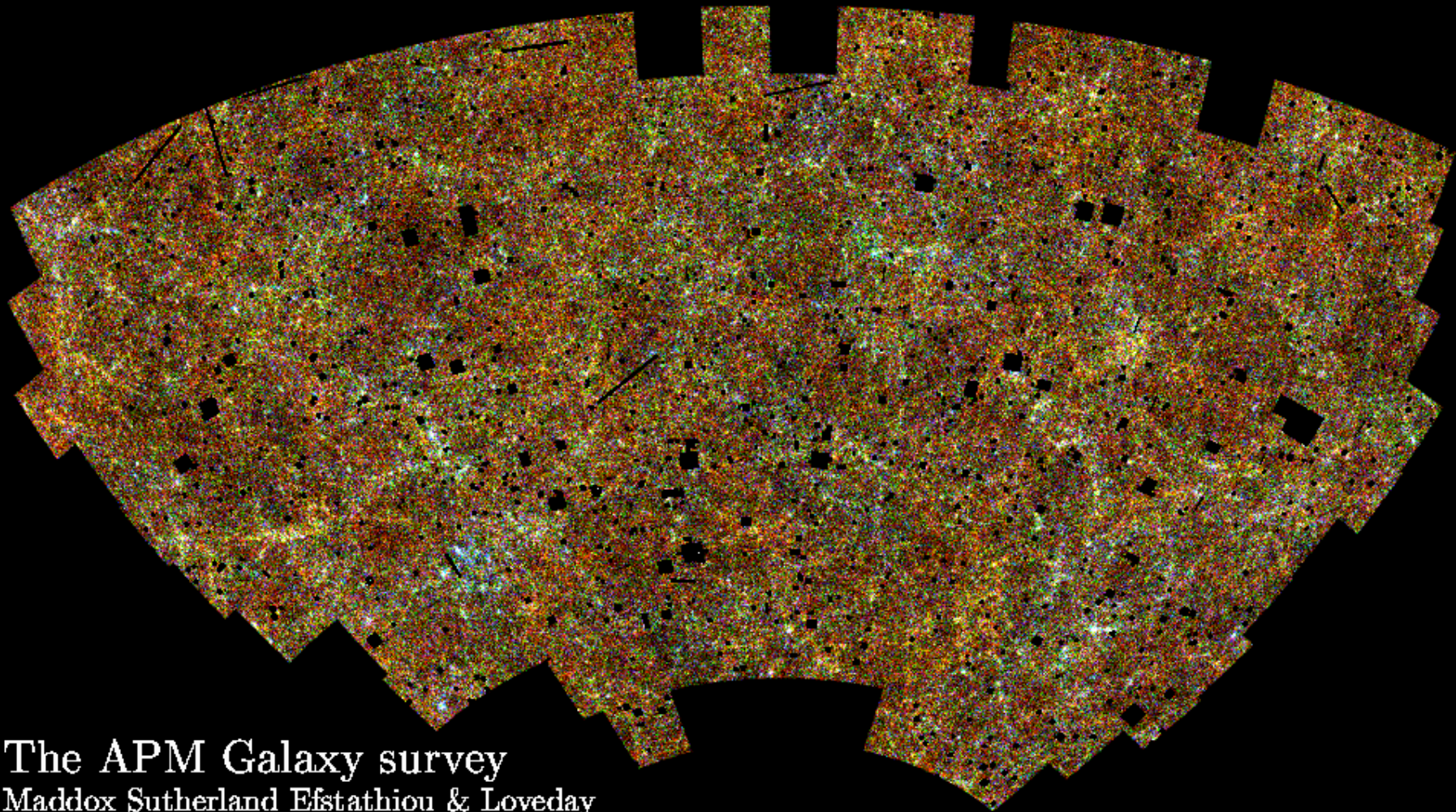


WMAP: level of structure at
recombination



Present day structure: the distribution of galaxies

The distribution of matter as traced by galaxies



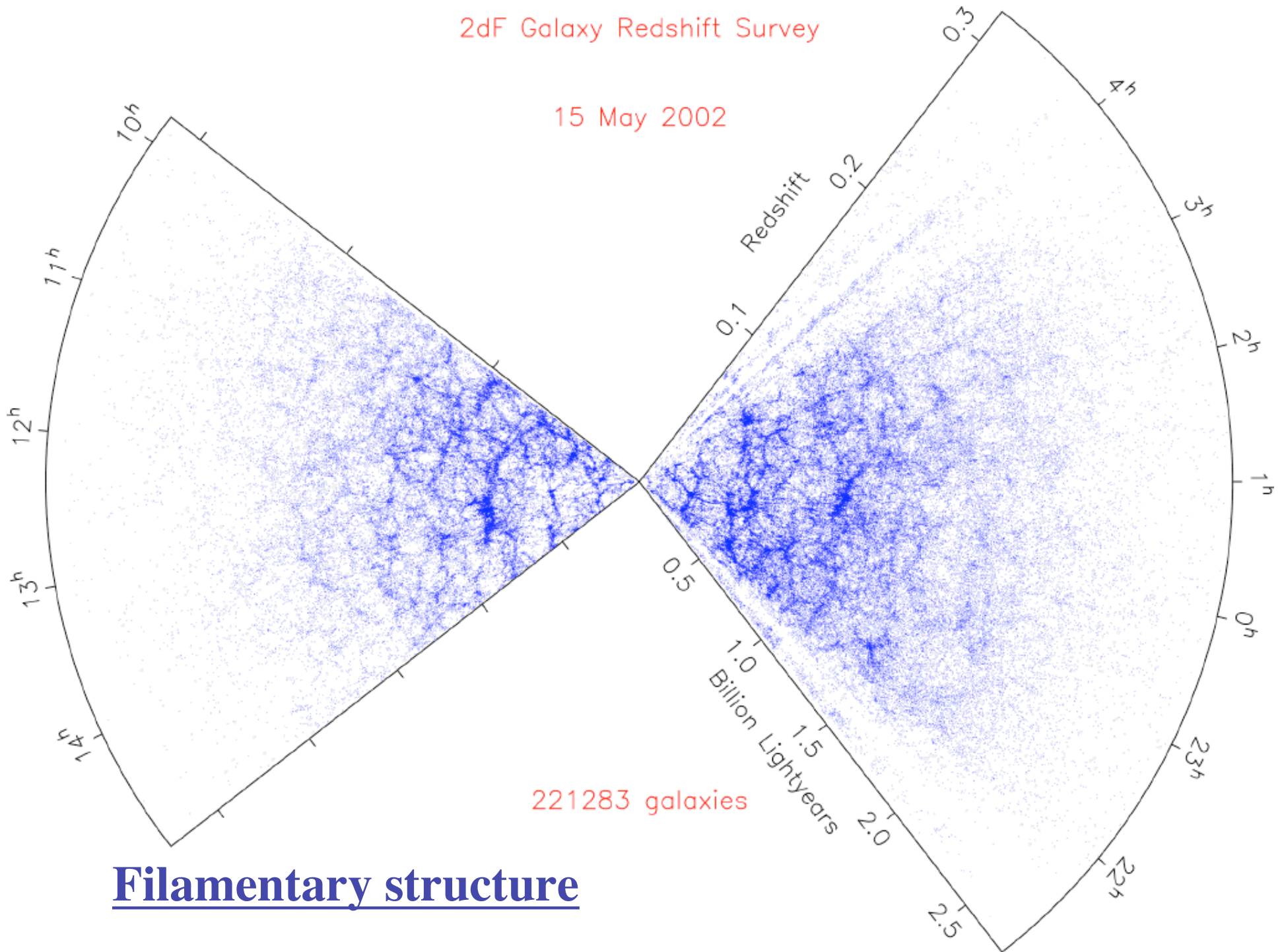
The APM Galaxy survey
Maddox Sutherland Efsthathiou & Loveday

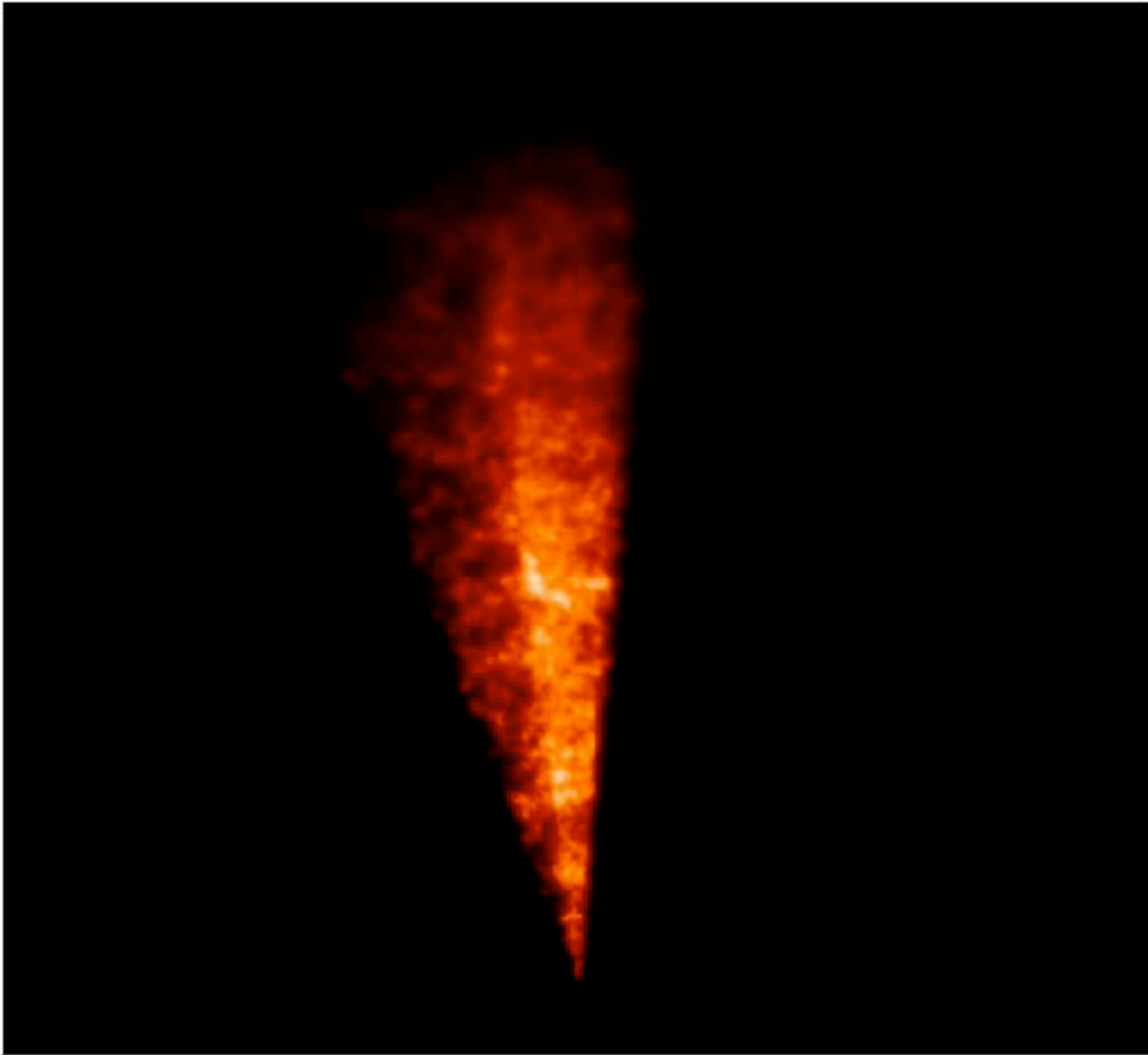
2dF Galaxy Redshift Survey

15 May 2002

221283 galaxies

Filamentary structure





<http://www.mso.anu.edu.au/2dFGRS/>

Gravitational Instability

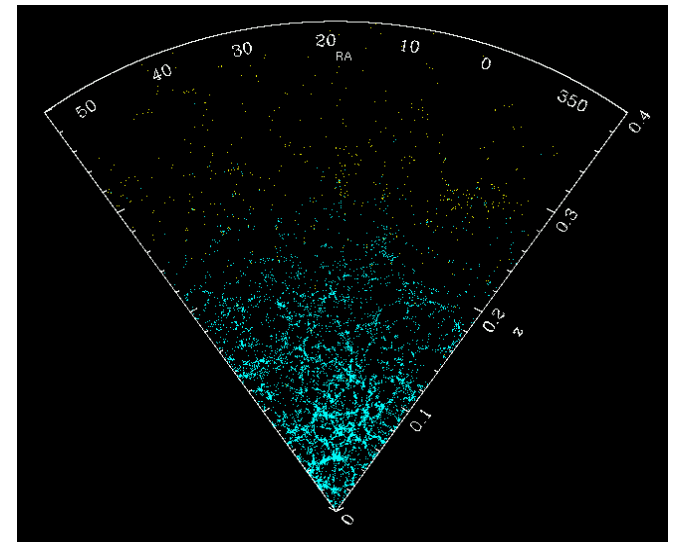
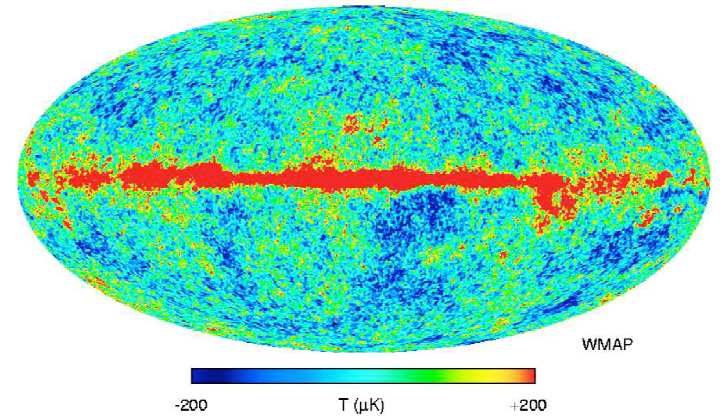
t_1



$t_2 > t_1$



$$t_g \sim (G\rho)^{-1/2}$$



Different constituents can be distinguished when studying the evolution of perturbations because of their different interactions.

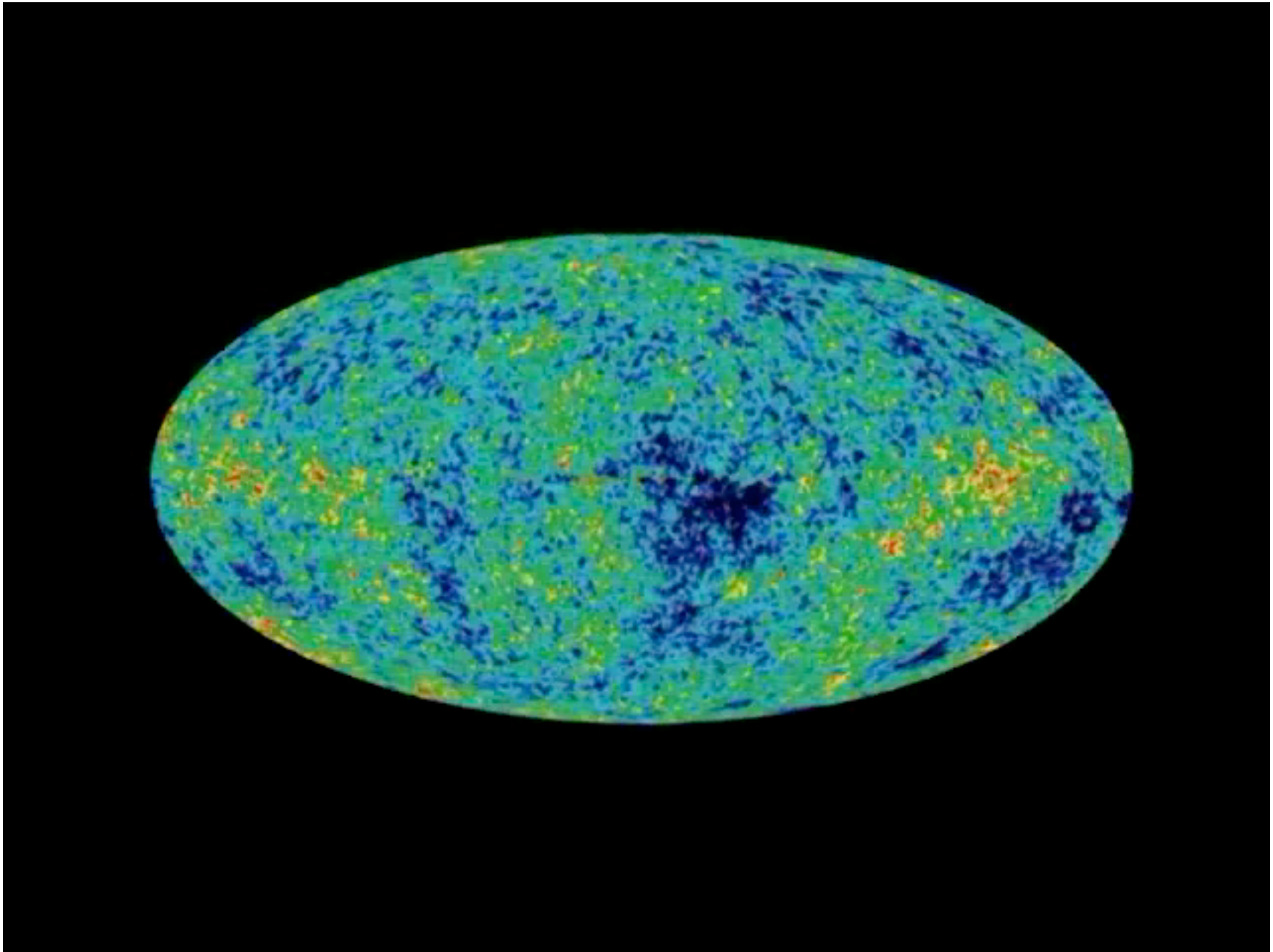
Baryons are coupled to the CMB before recombination.

CDM only interacts with the rest through gravity but can cluster.

A cosmological constant is spatially constant so it only affects the evolution of the expansion factor.

“Best” Cosmological Parameters:
Table 3 from ***Wilkinson Microwave Anisotropy Probe (WMAP) Observations:
Preliminary Maps and Basic Results***,
C. L. Bennett et al. (2003), accepted by the *Astrophysical Journal*;
available at <http://lambda.gsfc.nasa.gov/>

Description	Symbol	Value	+ uncertainty	– uncertainty
Total density	Ω_{tot}	1.02	0.02	0.02
Equation of state of quintessence	w	< -0.78	95% CL	—
Dark energy density	Ω_{Λ}	0.73	0.04	0.04
Baryon density	$\Omega_b h^2$	0.0224	0.0009	0.0009
Baryon density	Ω_b	0.044	0.004	0.004
Baryon density (cm^{-3})	n_b	2.5×10^{-7}	0.1×10^{-7}	0.1×10^{-7}
Matter density	$\Omega_m h^2$	0.135	0.008	0.009
Matter density	Ω_m	0.27	0.04	0.04
Light neutrino density	$\Omega_{\nu} h^2$	< 0.0076	95% CL	—
CMB temperature (K) ^a	T_{cmb}	2.725	0.002	0.002
CMB photon density (cm^{-3}) ^b	n_{γ}	410.4	0.9	0.9
Baryon-to-photon ratio	η	6.1×10^{-10}	0.3×10^{-10}	0.2×10^{-10}
Baryon-to-matter ratio	$\Omega_b \Omega_m^{-1}$	0.17	0.01	0.01
Fluctuation amplitude in $8h^{-1}$ Mpc spheres	σ_8	0.84	0.04	0.04
Low- z cluster abundance scaling	$\sigma_8 \Omega_m^{0.5}$	0.44	0.04	0.05
Power spectrum normalization (at $k_0 = 0.05 \text{ Mpc}^{-1}$) ^c	A	0.833	0.086	0.083
Scalar spectral index (at $k_0 = 0.05 \text{ Mpc}^{-1}$) ^c	n_s	0.93	0.03	0.03
Running index slope (at $k_0 = 0.05 \text{ Mpc}^{-1}$) ^c	$dn_s/d \ln k$	-0.031	0.016	0.018
Tensor-to-scalar ratio (at $k_0 = 0.002 \text{ Mpc}^{-1}$)	r	< 0.90	95% CL	—



<http://lambda.gsfc.nasa.gov/>

Gravitational instability
amplifies fluctuations but it
does not create them.

We need some “seeds”



Inflation

Summary of model parameters

- | | | | |
|----|--|---|---|
| 1. | Dark matter density | } | Matter budget: affects the physics of perturbations |
| 2. | Baryon density | | |
| 3. | Radiation density | | |
| 4. | Neutrino fraction | | |
| 5. | Curvature | } | Affect the evolution of $a(t)$ |
| 6. | Cosmological “constant” | | |
| 7. | Initial spectrum of scalar perturbations | } | Properties of the initial seeds |
| 8. | Initial spectrum of gravity waves | | |



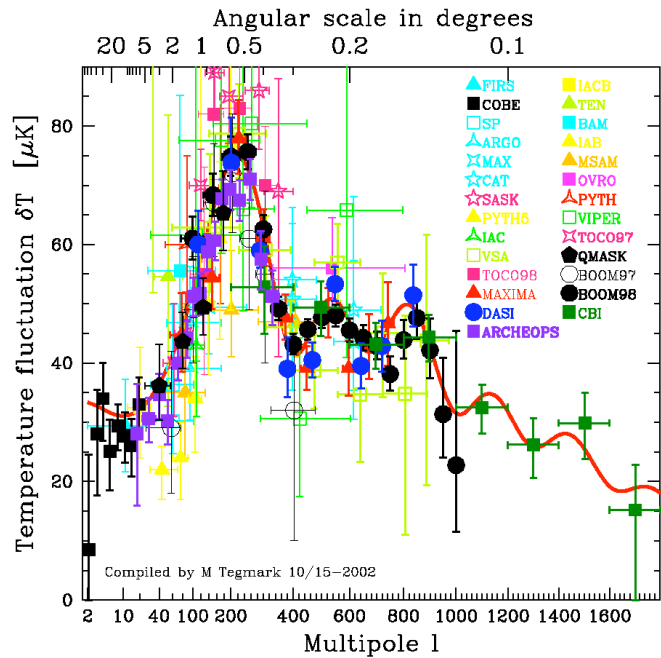
Objective: Invert the physics of the perturbations to get at properties of the seeds and hopefully to the mechanism that created the seeds

Anisotropies in the CMB Temperature

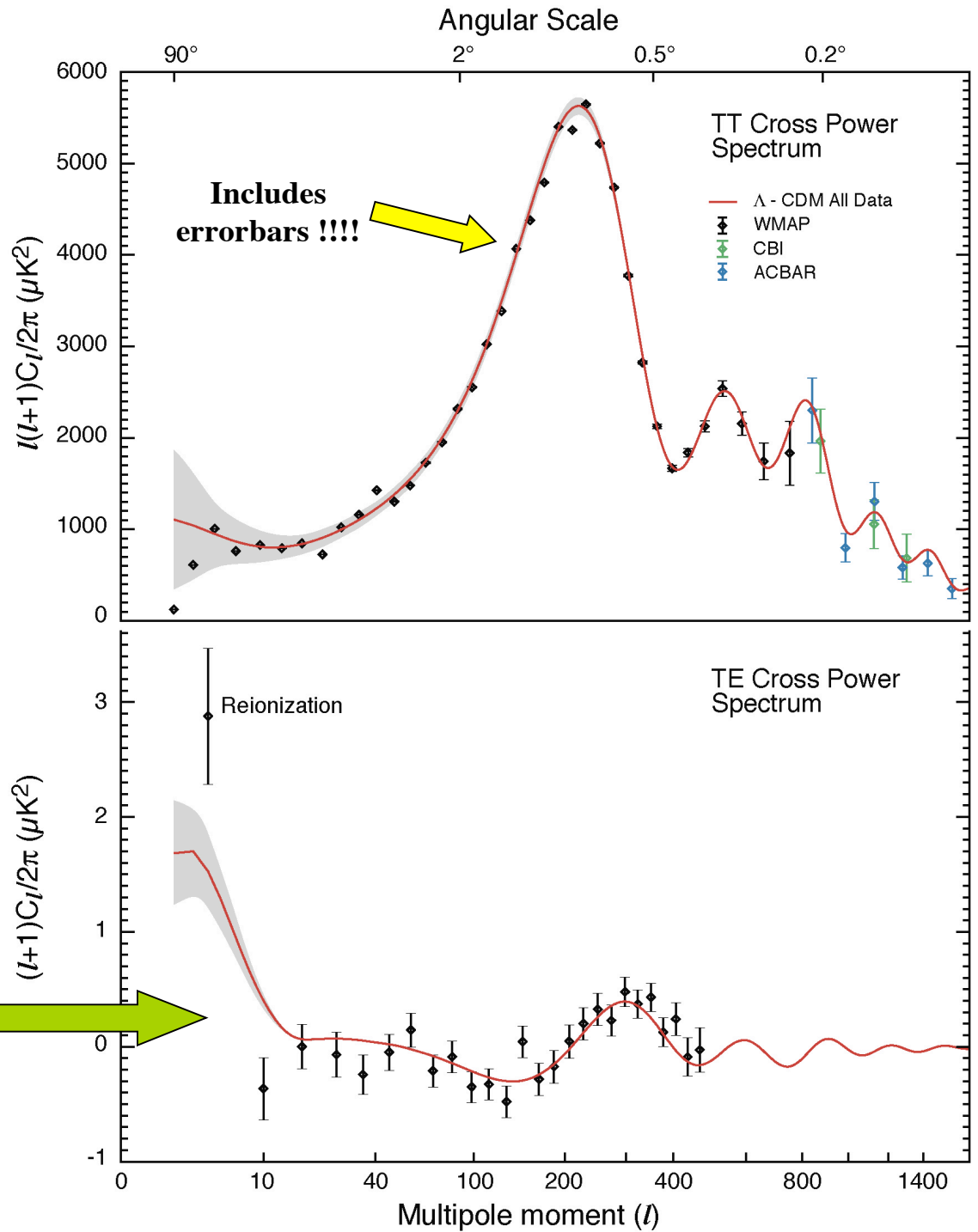
Outline

- Basic equations
- Solution under some simplifying assumption
- Basic parameter dependences
- Some effects left out

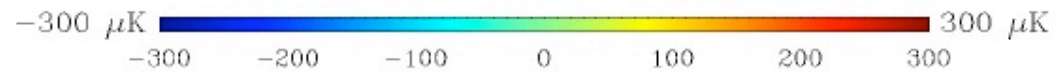
WMAP Spectra



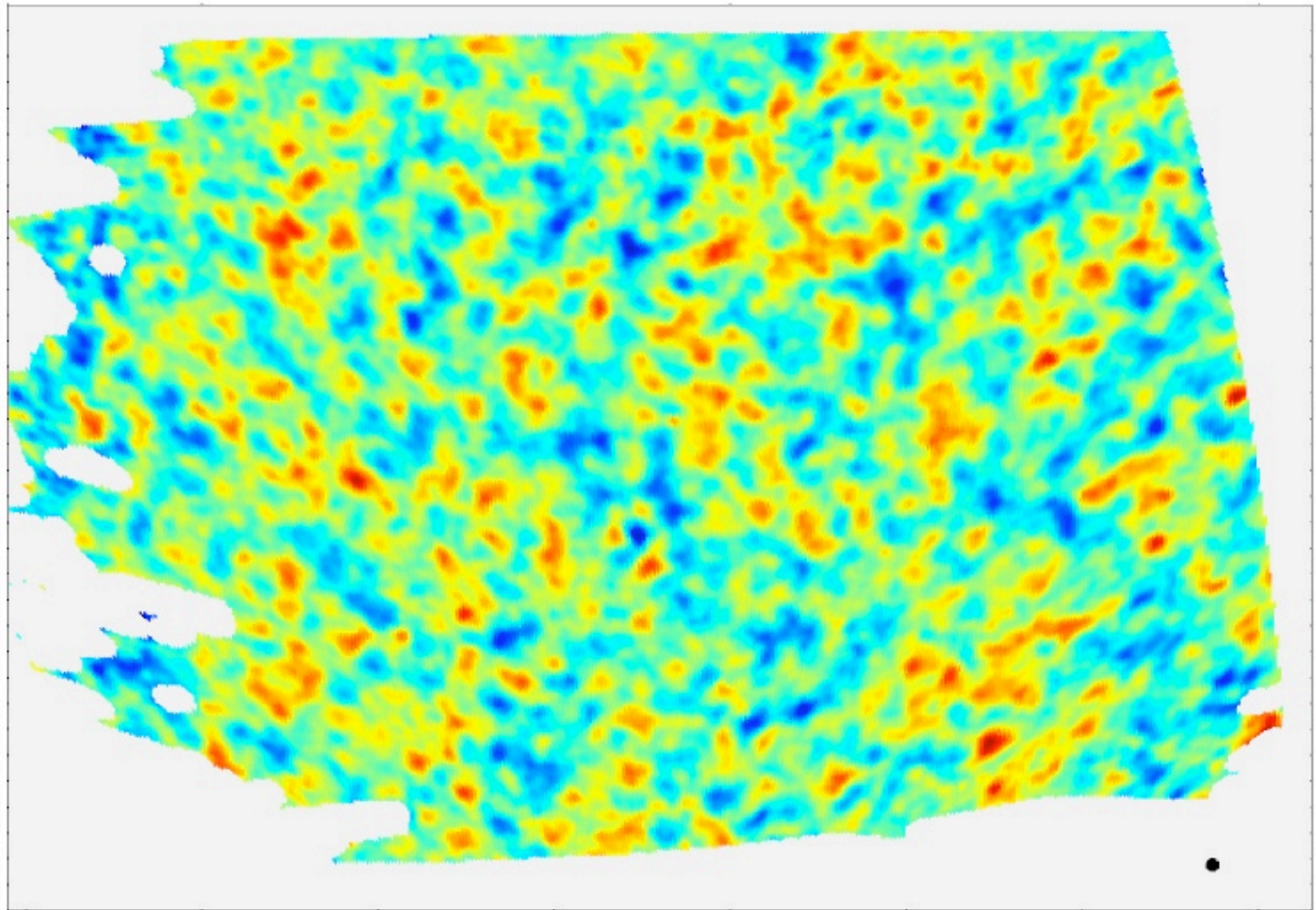
Temperature and polarization patterns are correlated



Anisotropies as seen by Boomerang

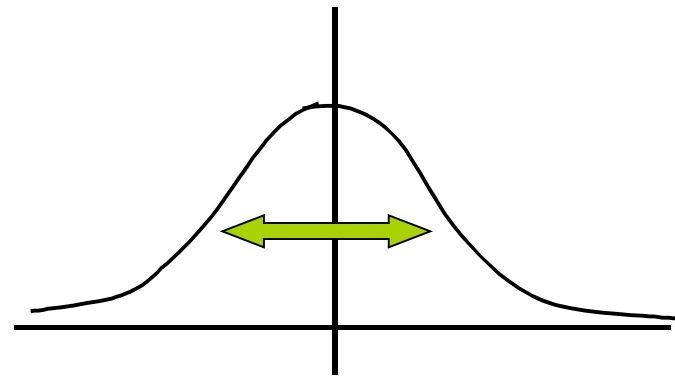


Flight: 10 days
1800 deg^2
3 % of the Sky
Resolution 0.2°



Definition of C_1

a_{lm} ← Gaussian Random Variable

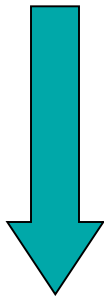


$$\langle a_{lm}^* a_{lm} \rangle = C_1$$

There are only $(2l+1)$ multipoles of a given l on the sky → **COSMIC VARIANCE**

WMAP Spectra

Fluctuations are small of
order 10^{-5}



We can use linear theory

