

Branching Fraction and CP asymmetry in $B^0 \rightarrow \pi^0 \pi^0$ Decays



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Overview

- Introduction & motivation $B^0 \rightarrow \pi^0 \pi^0$
- Analysis procedure
- Results
- Summary

The CKM matrix & CP violation

CKM matrix describes mixing between flavor and weak eigenstates in the Standard Model.

$$V_{CKM} = \begin{bmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{bmatrix}$$

3x3 unitary matrix:
3 real parameters,
1 phase: only source of CPV in SM

Unitarity implies

$$V_{ud} V_{ub}^* + V_{cd} V_{cb}^* + V_{td} V_{tb}^* = 0$$

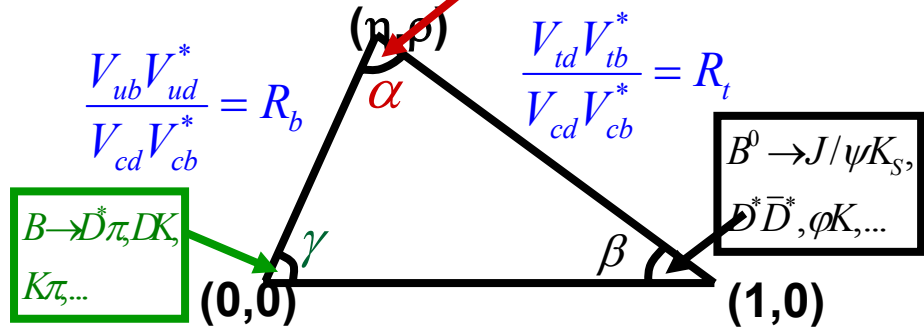
Wolfenstein parameterization

$$V_{CKM} \approx \begin{bmatrix} 1 - \frac{\lambda^2}{2} & \lambda & A\lambda^3(\rho - i\eta) \\ -\lambda & 1 - \frac{\lambda^2}{2} & A\lambda^2 \\ A\lambda^3(1 - \rho - i\eta) & -A\lambda^2 & 1 \end{bmatrix}$$

CP violating phases

$B \rightarrow \pi\pi, \rho\pi, \rho\rho$

This talk



Area of triangle is equivalent to the amount of CP violation in SM

Observing CP Violation at *BABAR*

Three observable effects in **B** decays to a final state **f**:

CP violation in mixing ($|q/p| \neq 1$)

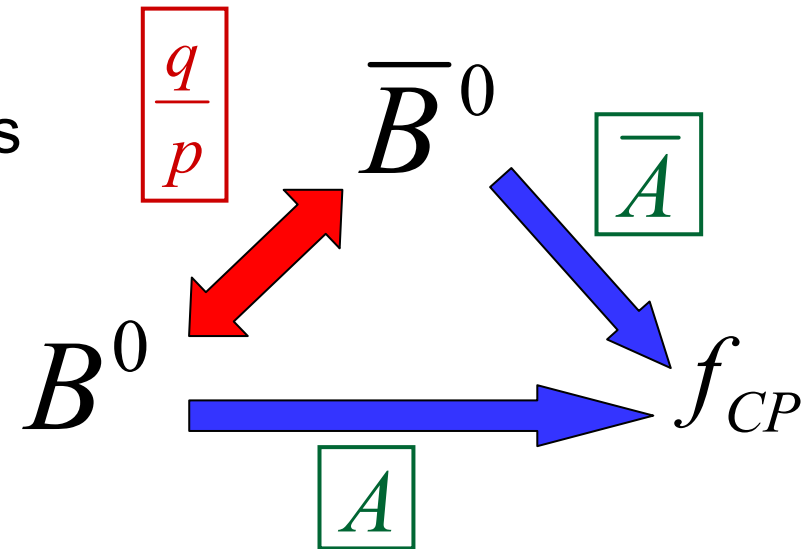
$$B^0 \rightarrow \bar{B}^0 \neq \bar{B}^0 \rightarrow B^0$$

(direct) CP violation in decay ($|\bar{A}/A| \neq 1$)

$$B^0 \rightarrow f \neq \bar{B}^0 \rightarrow \bar{f}$$

(indirect) CP violation in the interference between mixing and decay ($\text{Im}\lambda_{f_{CP}} \neq 0$)

Time dependent effect is sensitive to measure unitarity triangle angles



$$\lambda_{f_{CP}} = \frac{q}{p} \frac{\bar{A}}{A}$$

How to measure α from $B^0 \rightarrow \pi^+ \pi^-$ decays

Decays sensitive to α

$$B^0 \rightarrow \pi^+ \pi^-$$

Time dependent cp asymmetry:

$$a_{\pi\pi}(t) = \frac{\Gamma_{B^0 \rightarrow \pi\pi} - \Gamma_{\bar{B}^0 \rightarrow \pi\pi}}{\Gamma_{B^0 \rightarrow \pi\pi} + \Gamma_{\bar{B}^0 \rightarrow \pi\pi}}$$

Can be written as:

$$= S_{\pi\pi} \sin(\Delta m_B \Delta t) - C_{\pi\pi} \cos(\Delta m_B \Delta t)$$

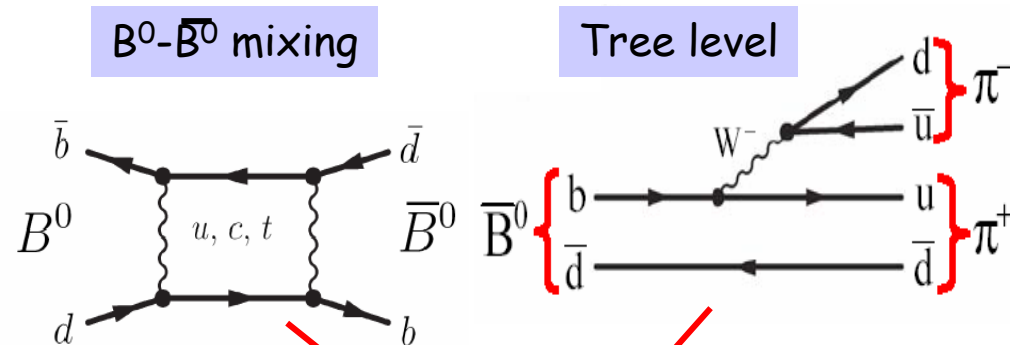
$$S \propto 2 \operatorname{Im} \lambda$$

Indirect CP

relevant to α

$$C \propto 1 - |\lambda|^2$$

Direct CP



$$\lambda = \frac{q}{p} \frac{\bar{A}}{A} = e^{i2\alpha}$$



$$S_{\pi\pi} = \sin 2\alpha$$

$$C_{\pi\pi} = 0$$

$$a_{\pi\pi}(t) = \sin(2\alpha) \sin(\Delta m_B \Delta t)$$

Measuring α in presence of penguins

Coefficients of time-dependent CP Asymmetry in $B^0 \rightarrow \pi^+\pi^-$ decays

Tree level



$$S_{\pi\pi} = \sin 2\alpha$$

$$C_{\pi\pi} = 0$$

But penguin diagrams are not negligible!!!

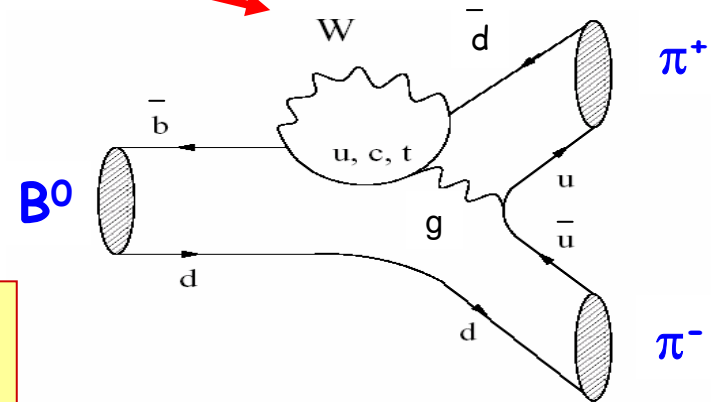
Penguin

- Carry a different phase compared to tree level
- Measure α_{eff}



$$S_{\pi\pi} = \sqrt{1 - C_{\pi\pi}^2} \sin 2\alpha_{\text{eff}}$$

$$C_{\pi\pi} \propto \sin \delta$$



Measure

$$\alpha_{\text{eff}} = \alpha + \delta\alpha_{\text{peng}}$$

need to bound

$$|\alpha - \alpha_{\text{eff}}|$$

Need Isospin analysis

Measuring α from $B \rightarrow \pi \pi$ Isospin

Isospin relates different amplitudes

Gronau-London: PRL **65**, 3381 (1990)

$$A^{+0} = \frac{1}{\sqrt{2}} A^{+-} + A^{00}$$

$$\bar{A}^{+0} = \frac{1}{\sqrt{2}} \bar{A}^{+-} + \bar{A}^{00}$$

Need to measure:

$$A^{+-} = A(B^0 \rightarrow \pi^+ \pi^-)$$

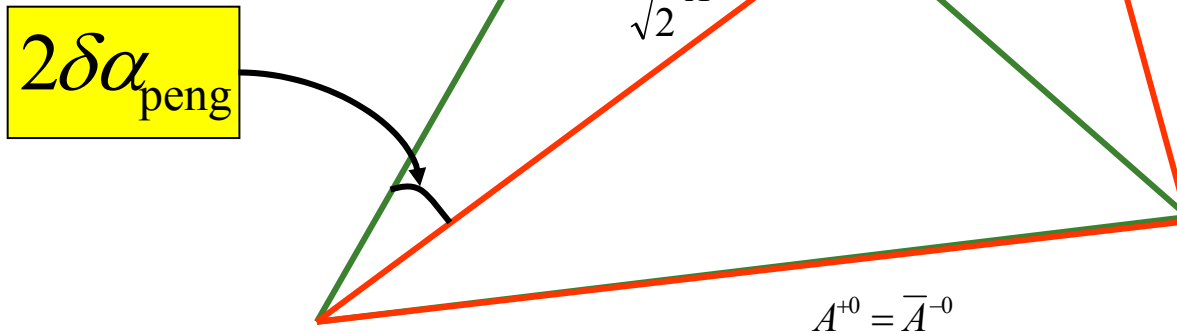
$$\bar{A}^{+-} = A(\bar{B}^0 \rightarrow \pi^+ \pi^-)$$

$$A^{00} = A(B^0 \rightarrow \pi^0 \pi^0)$$

$$\bar{A}^{00} = A(\bar{B}^0 \rightarrow \pi^0 \pi^0)$$

$$A^{+0} = A(B^+ \rightarrow \pi^+ \pi^0)$$

$$\bar{A}^{-0} = A(B^- \rightarrow \pi^- \pi^0)$$



BaBar has measured all BFs to carried out the isospin analysis

small A^{00} & \bar{A}^{00} \rightarrow small $\delta\alpha_{\text{peng}}$ $\sin^2(\alpha_{\text{eff}} - \alpha) < \frac{\langle \text{BF}(B^0 \rightarrow \pi^0 \pi^0) \rangle}{\text{BF}(B^+ \rightarrow \pi^+ \pi^0)}$ Grossman-Quinn bound PRD 58, 017504 (1998)

$B^0 \rightarrow \pi^0 \pi^0$ CP asymmetry

Time dependent CP asymmetry

$$a_{\pi^0 \pi^0}(t) = -C_{\pi^0 \pi^0} \text{Cos}(\Delta m_b t) + S_{\pi^0 \pi^0} \text{Sin}(\Delta m_b t)$$

Neutral B mixing probability

PDG 2004

Integrating
over time



$$A_{\pi^0 \pi^0} = -(1 - 2\chi)(1 - 2\omega)C_{\pi^0 \pi^0}$$

Need tagging to identify the B flavor

Mistag probability

**Time integrated
CP asymmetry**

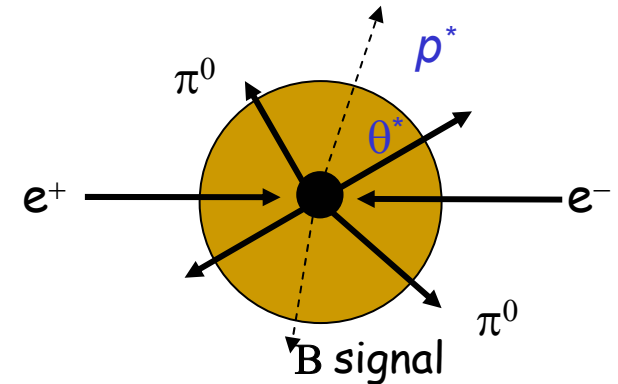


$$A_{\pi^0 \pi^0} = \frac{\bar{N}_{\pi^0 \pi^0} - N_{\pi^0 \pi^0}}{\bar{N}_{\pi^0 \pi^0} + N_{\pi^0 \pi^0}}$$

Analysis procedure

Data sample:

- 227 million B pairs collected at the Y(4S) energy
- 16 fb⁻¹ of data recorded 40 MeV below the Y(4S)

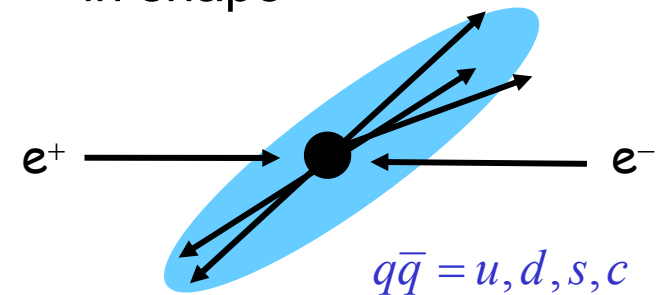


Event Selection:

- $B^0(\bar{B}^0)$ Decays from combination of 4 photons to make 2 π^0 s
- Photons not matched to any charged track in the detector
- π^0 mass required
- $110 < m_{\gamma\gamma} < 160$ (MeV/c²)

- **Event shape variables for background suppression (~80%)**

B events are **spherical** in shape



Background events from light quark production have **jet-like topology**

Backgrounds

Main Backgrounds

Continuum (u,d,s,c quarks)

B background

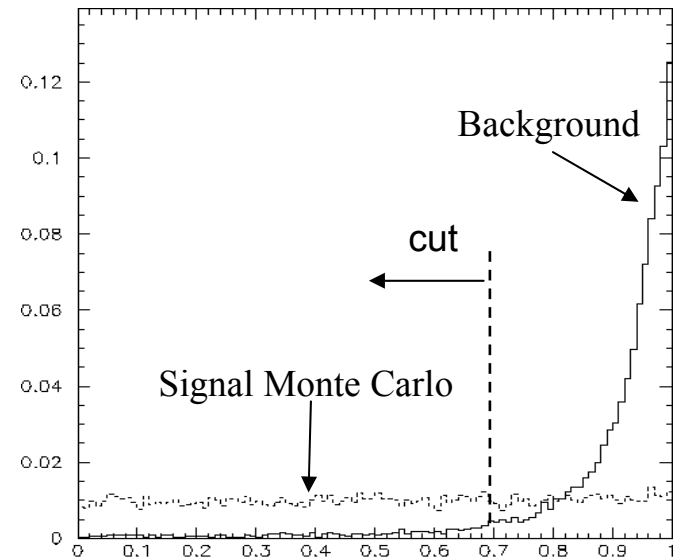
$$B^{\pm} \rightarrow \rho^{\pm} \pi^0$$

$$\rho^{\pm} \rightarrow \pi^{\pm} \pi^0$$

When charged π is missed

Final efficiency 1.3% and use world average BF to fix number of events in fit

Babar PRL 93, 051802 (2004), Belle hep-hex/0406006



Cosine of the angle between the sphericity axes of the B and of the rest of the event
 $|\cos(\theta_s)| < 0.7$

Analysis procedure

With a preselected sample of **8153** events

- Method

Extended ML fit simultaneously determines:

$$N_{\pi^0\pi^0}, N_{q\bar{q}}, A_{\pi^0\pi^0}, A_{q\bar{q}}$$

Yields & Asymmetries

and uses:

- **Kinematic variables for signal selection**
- **Event shape for signal-background separation**
- **Use of tagging information**

$$m_{ES}, \Delta E, Fisher$$

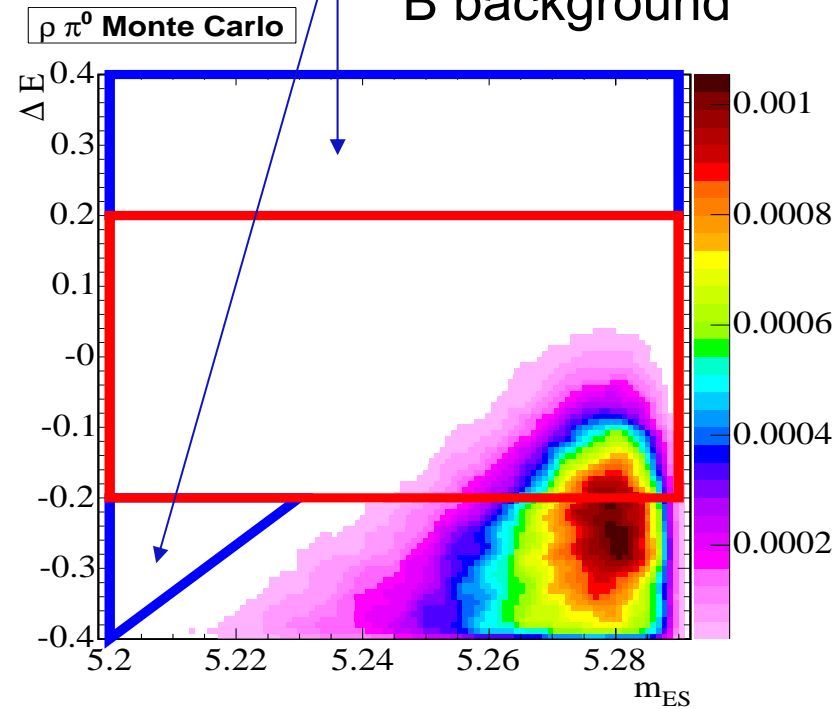
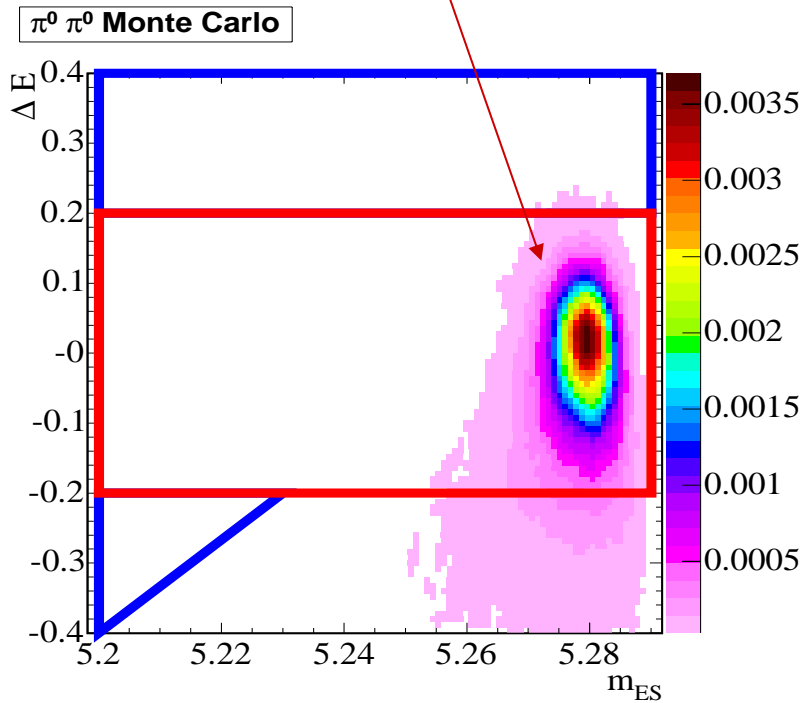
PDF Parameterization

Signal region

Side band

B background

$$\Delta E = E_B^* - E_{\pi^0}^*$$



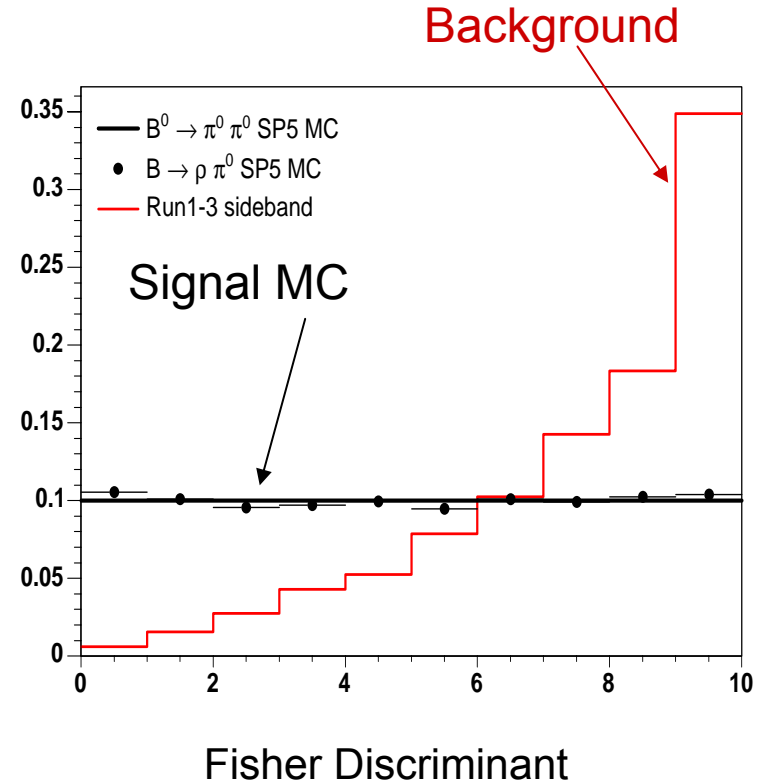
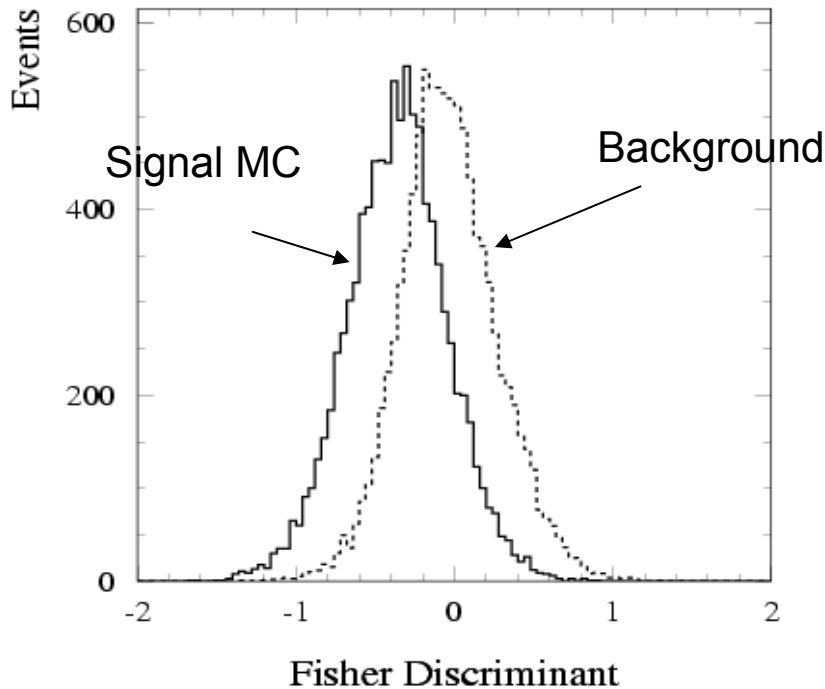
$$5.2 <$$

$$m_{ES} = \sqrt{E_{beam}^{*2} - P_B^{*2}}$$

(GeV/c^2)

Background suppression

- Continuum rejection using event shape variables



$$F = 0.53 - 0.60 \times \sum_i p_i^* + 1.27 \times \sum_i p_i^* |\cos(\theta_i^*)|^2$$

Parametric Step Function, 10 bins (9 free params.)

Parameterized for each tagging category

Results

Events

$$N_{\pi^0\pi^0} = 61 \pm 17$$

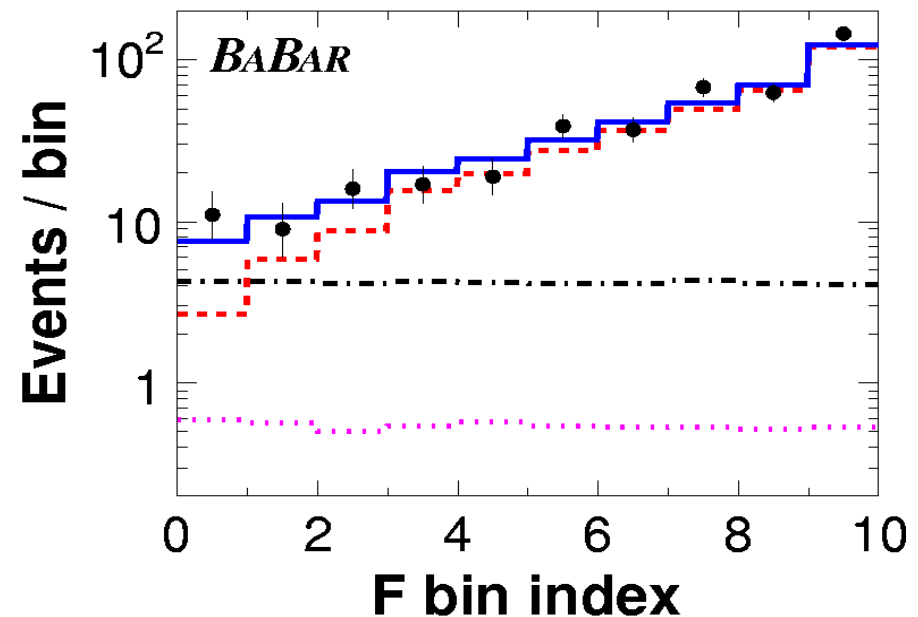
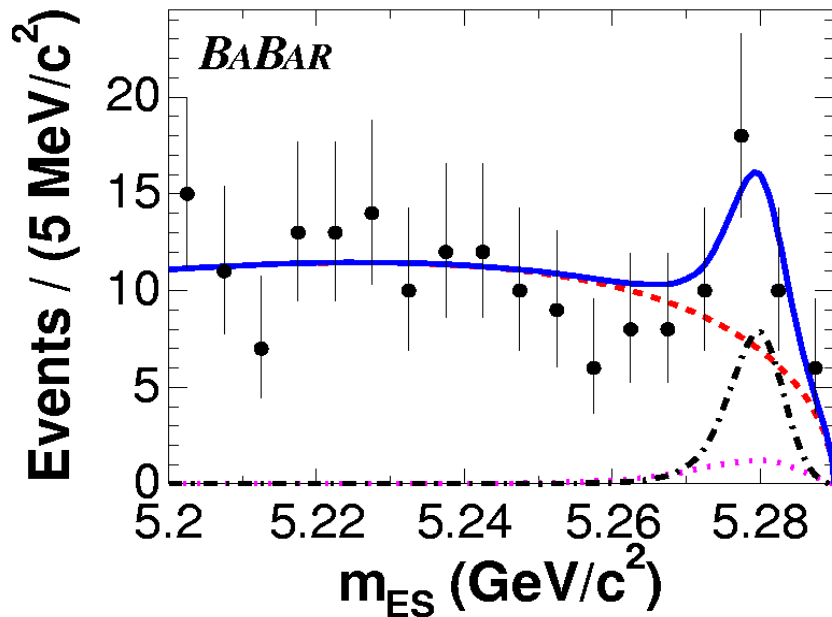
Reconstruction
efficiency

$$\varepsilon(23.5\%)$$

significance 5.2σ

$$BF_{\pi^0\pi^0} = (1.17 \pm 0.32 \pm 0.10) \times 10^{-6}$$

$$C_{\pi^0\pi^0} = -0.12 \pm 0.56 \pm 0.06$$



$$\text{Fit} = q\bar{q} \text{ bkgd} + B^{\pm} \rightarrow \rho^{\pm}\pi^0 + \text{signal}$$

Systematic errors and checks

Main sources of systematic errors

Source	ΔN_{00}	ΔC_{00}
Uncertainty in $\rho\pi$ BF	+2.12	+0.012
Uncertainty in $\rho\pi$ Asymmetry	+0.4	+0.051
π reconstruction	+4.45	+0.014
ΔE -Mes Monte Carlo corrections	+1.12	+0.015
Tagging efficiencies	+0.01	+0.032

Cross checks

Fit compatible with 2003 result

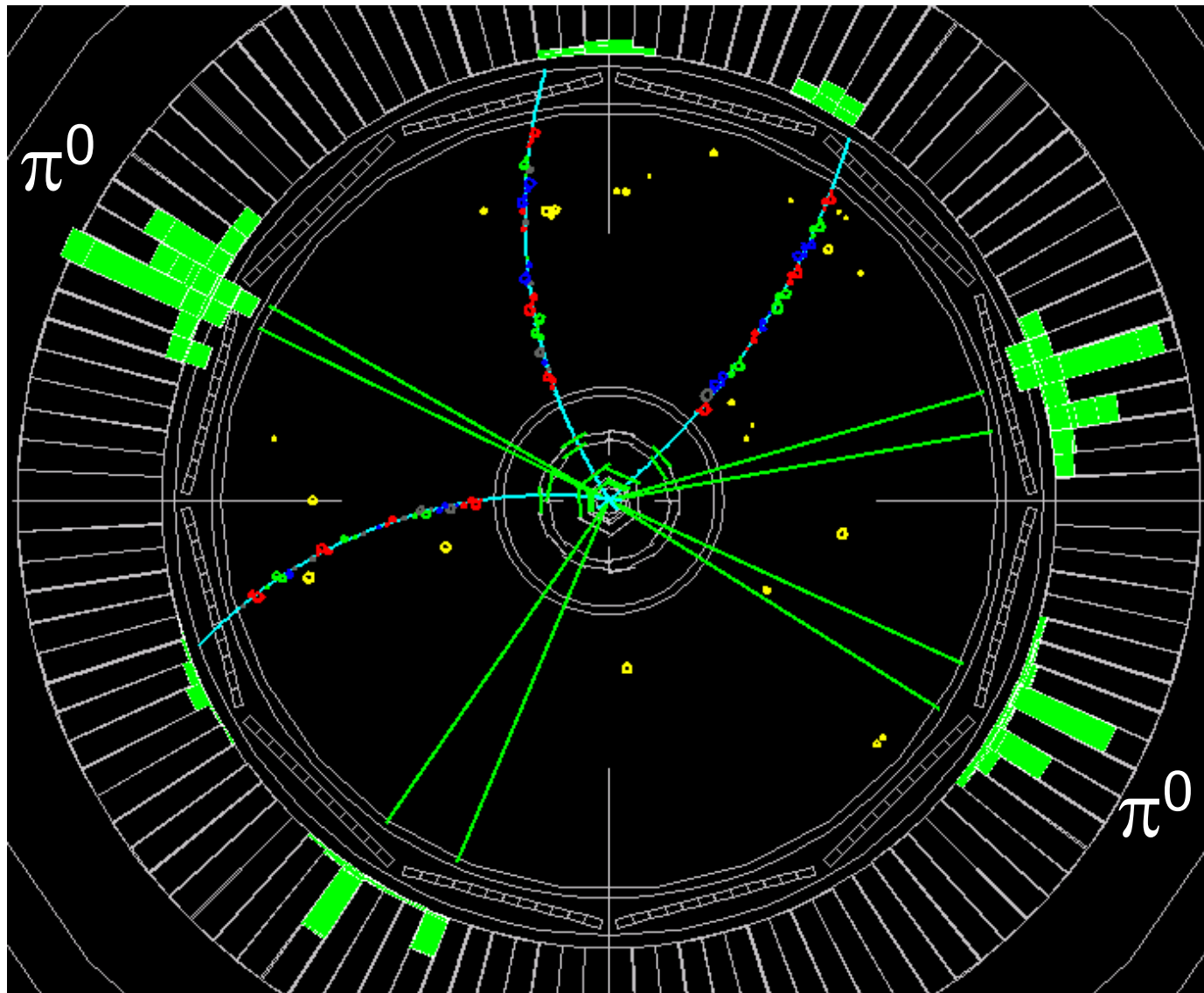
Fit performed on different data samples are consistent

Toy MC studies to look for potential fit bias

Cut & Count analysis compatible with Likelihood fit result

Using MC, check for crosstalk
Between different species, minimal

Signal
Event



Summary $B^0 \rightarrow \pi^0 \pi^0$

$$BF_{\pi^0 \pi^0} = (1.17 \pm 0.32 \pm 0.10) \times 10^{-6}$$

$$C_{\pi^0 \pi^0} = -0.12 \pm 0.56 \pm 0.06 \quad [-0.88, 0.64] \quad 90\% \text{ C.L.}$$

significance 5.0σ Including systematics

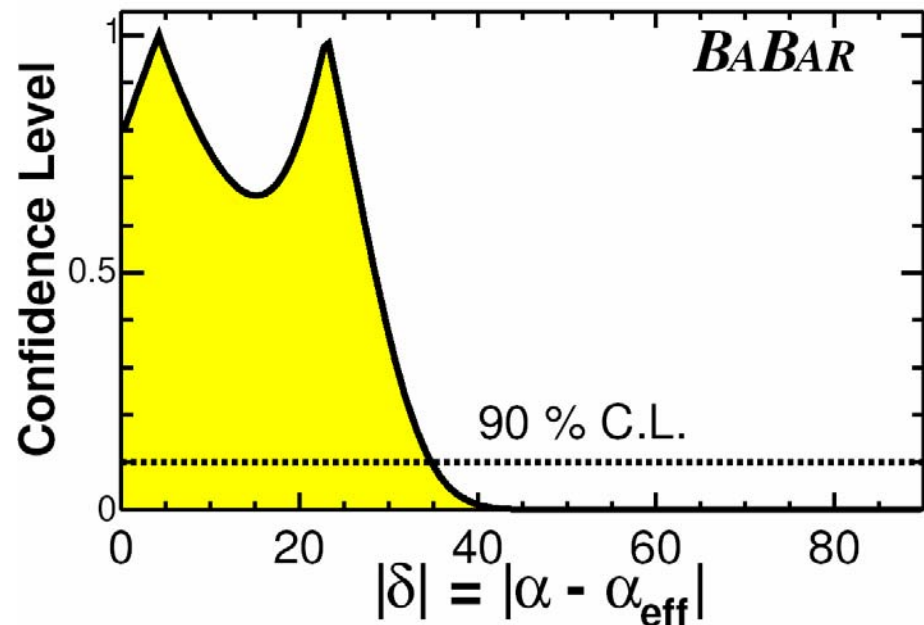
Hep-ex/0408081, submitted to PRL

Isospin analysis

$$|\alpha - \alpha_{\text{eff}}| < 35^\circ$$

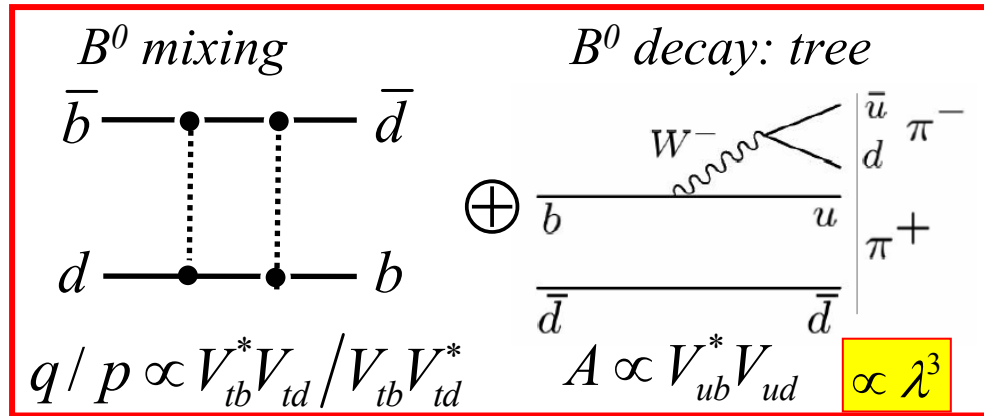
90% C.L.

Need Super B-factory
to get useful bound

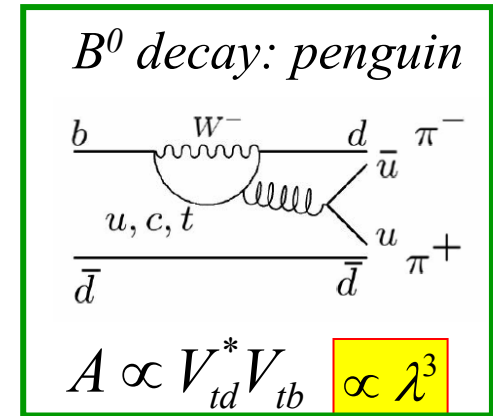


Backup slides

Interference of suppressed
 $b \rightarrow u$ “tree” decay with mixing



but: “penguin”
 is sizeable!



$$\lambda_{\pi\pi} = \frac{q}{p} \frac{\bar{A}_{\pi\pi}}{A_{\pi\pi}} = e^{-i2\beta} e^{-i2\gamma} = e^{i2\alpha}$$

$$\lambda_{\pi\pi} = e^{i2\alpha} \frac{T + P e^{+i\gamma} e^{i\delta}}{T + P e^{-i\gamma} e^{i\delta}}$$

Coefficients of time-dependent CP Asymmetry

With no penguins

$$\begin{aligned} S_{\pi\pi} &= \sin 2\alpha \\ C_{\pi\pi} &= 0 \end{aligned}$$

With large penguins
 and $|P/T| \sim 0.3$

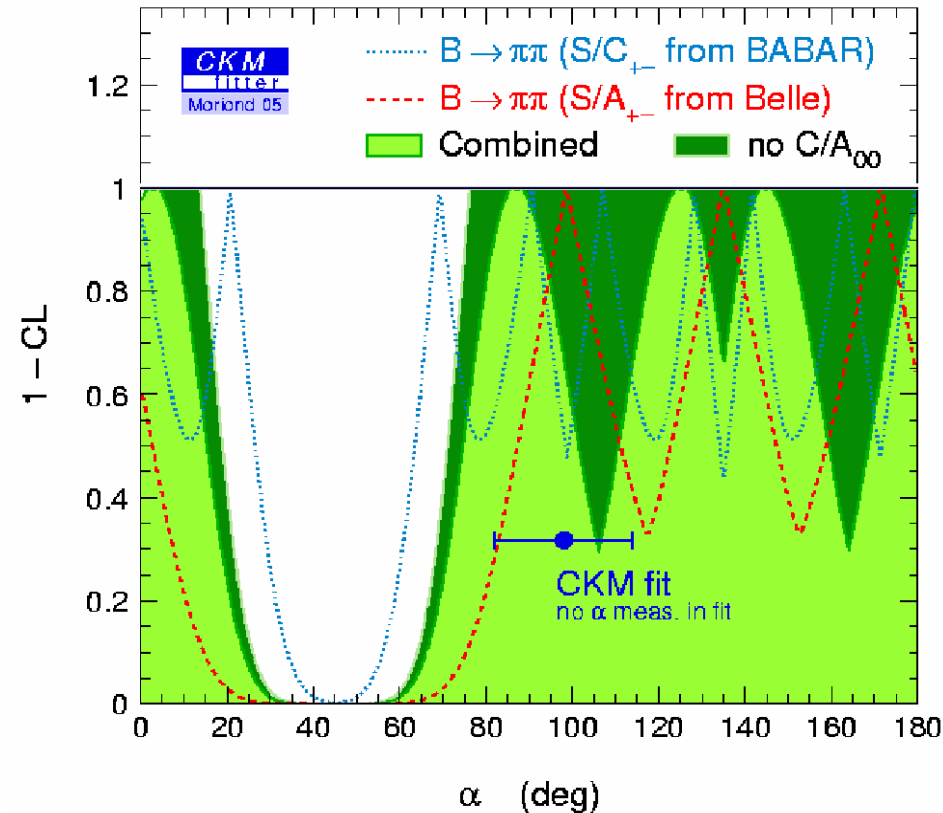
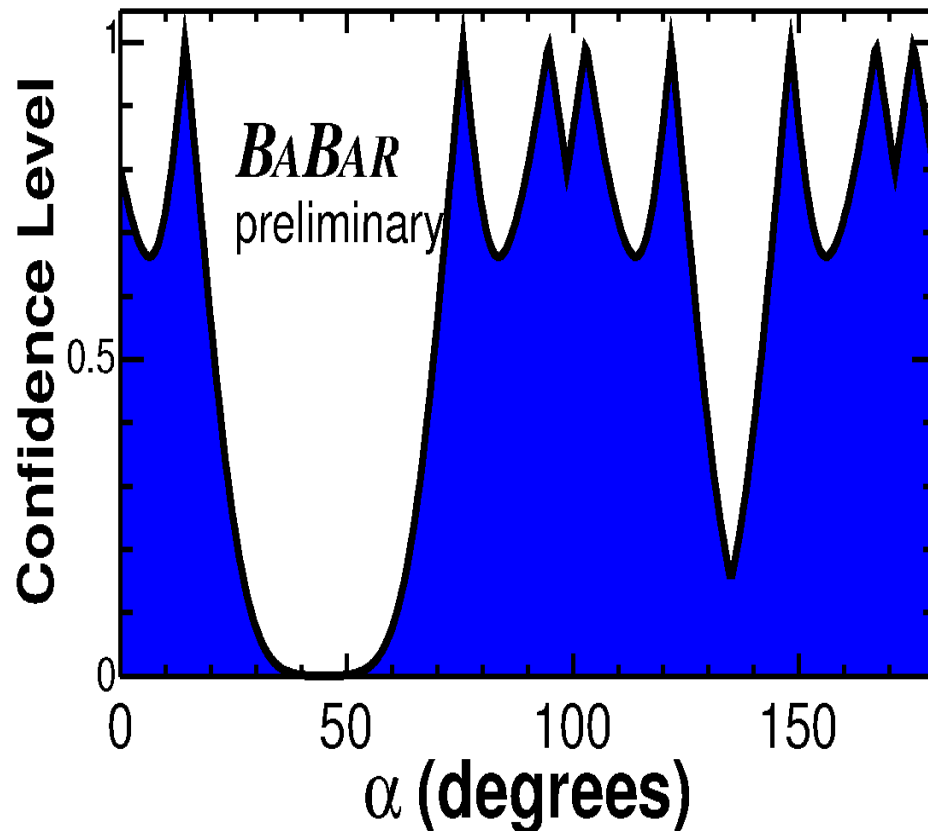
$$\begin{aligned} S_{\pi\pi} &= \sqrt{1 - C_{\pi\pi}^2} \sin 2\alpha_{\text{eff}} \\ C_{\pi\pi} &\propto \sin \delta \end{aligned}$$

Scan on α

Babar 2004

$$S = -0.30 \pm 0.17 \pm 0.02$$

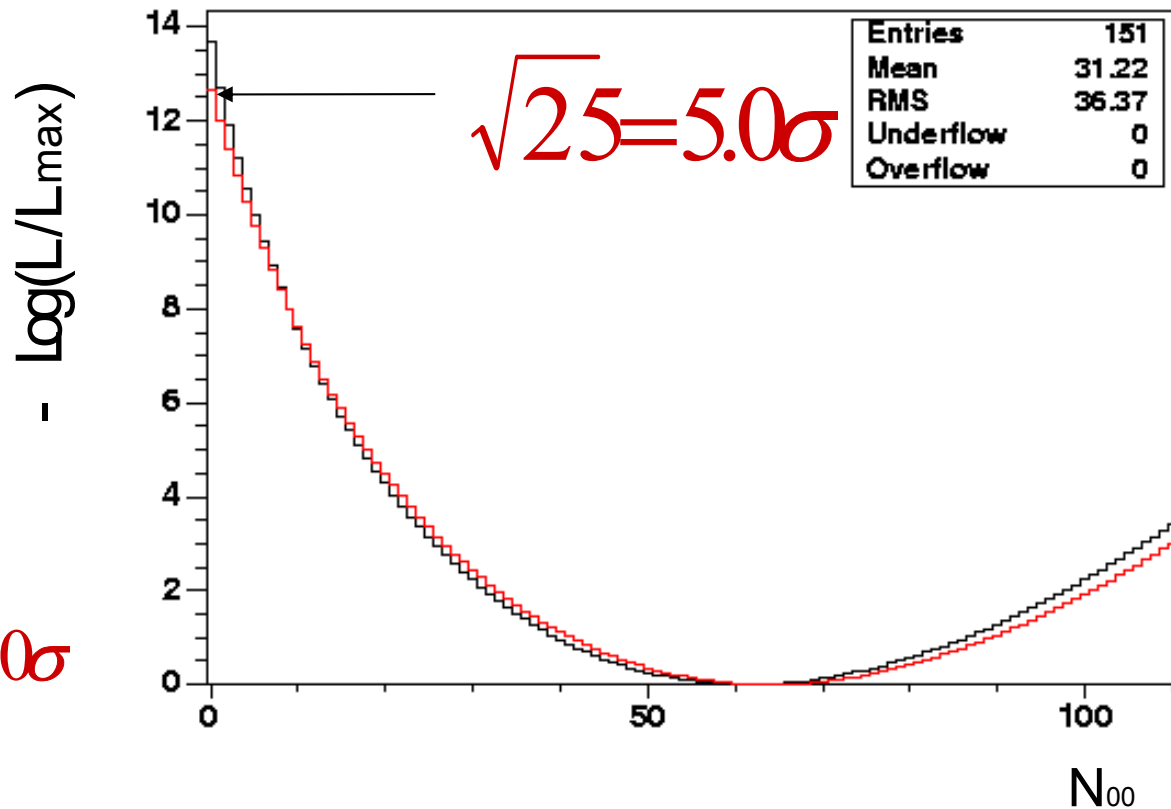
$$C = -0.09 \pm 0.15 \pm 0.03$$



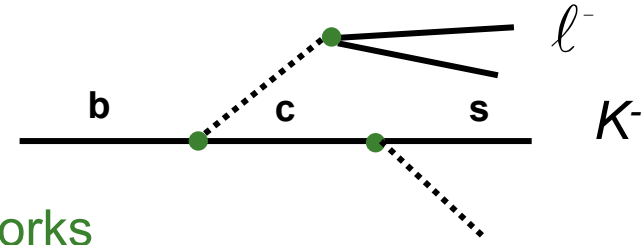
Significance calculation

The significance is defined as root square of the change in the log likelihood when the asymmetry is fixed to zero.

$$\sqrt{\Delta(-2\log L)_0} = 5.0\sigma$$



B Flavour Tagging



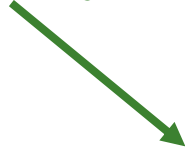
- Tagging algorithm with physics-based neural networks
 - Inputs include leptons, kaons, slow- π (from D^*), and high-momentum tracks
 - Outputs combined and categorized by mistag probability (w)
- 5 mutually exclusive hierarchical categories:
 - **Lepton** – isolated high-momentum leptons
 - **Kaon I** – high quality kaons or correlated K^+ and slow- π^-
 - **Kaon II** – lower quality kaons, or slow- π^-
 - **Inclusive** – unidentified leptons, poor-quality kaons, high-momentum tracks
 - **Untagged** – no flavour information is used

cleaner
signal



larger
mistag prob

efficiency



mistag probability



Category	ϵ_c (%)			ω_c (%)			$\Delta\omega_c$ (%)			Q_c (%)		
Lepton	9.1	\pm	0.2	3.3	\pm	0.7	-1.6	\pm	1.3	8.0	\pm	0.3
Kaon I	16.6	\pm	0.2	9.5	\pm	0.7	-2.8	\pm	1.3	10.7	\pm	0.4
Kaon II	19.8	\pm	0.3	20.6	\pm	0.8	-5.3	\pm	1.3	6.7	\pm	0.4
Inclusive	20.1	\pm	0.3	31.7	\pm	0.9	-2.6	\pm	1.4	2.7	\pm	0.3
Untagged	34.4	\pm	0.5									
Total Q										28.4	\pm	0.7

67% of events have some flavour information

$$Q = \epsilon(1 - 2\omega)^2 = (28.4 \pm 0.7)\%$$

PDF Parameterization

Variable	Signal PDF	Background PDF
m_{ES}	2-D smoothed hist.	Argus
ΔE	2-D smoothed hist.	Poly2
Fisher	Steep function (10 bins)	Steep function (10 bins)