

**Rate asymmetries
in chargino and charged Higgs decays
as a probe of CP violation**

HELMUT EBERL

HEPHY Vienna



3rd meeting 24-25 March 2005 at SLAC

This talk is based on papers written with

E. Christova - INRNE, SOFIA

T. Gajdosik - INSTITUTE OF PHYSICS, VILNIUS

S. Kraml - HEPHY VIENNA/CERN

W. Majerotto and B. Schraußer - HEPHY VIENNA

- CP violating asymmetry in chargino decay into neutralino and W boson

H. E., T. Gajdosik, W. Majerotto, B. Schraußer

hep-ph/0502112

- CP violation in charged Higgs boson decays in the MSSM with complex parameters

E. Christova, H. E., S. Kraml, W. Majerotto

hep-ph/0205227

- CP violation in charged Higgs boson decays into tau and neutrino

E. Christova, H. E., S. Kraml, W. Majerotto

hep-ph/0211063

OUTLINE

- Introduction: MSSM, CP phases (mass matrices)
- Decay rate asymmetry
- **New:** $\tilde{\chi}_i^\pm \rightarrow \tilde{\chi}_j^0 W^\pm$
- Review of $H^\pm \rightarrow tb, \tau\nu_\tau$
- Conclusions

COMPLEX MSSM

- In the general MSSM **complex parameters** in Higgs potential and soft SUSY breaking terms
- Physical phases:
 - $|\mu|e^{i\phi_\mu}$: higgsino mass parameter
 - $|M_1|e^{i\phi_{M_1}}$: U(1) gaugino mass parameter
(M_2 is made real by field-redefinition)
 - $m_{\tilde{g}} e^{i\phi_3}$: SU(3) gaugino mass parameter
 - $|A_f|e^{i\phi_{A_f}}$: trilinear coupling of sfermions
- **CP violating MSSM**

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[see e.g. Dine, Kusenko, hep-ph/0303065]

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[see e.g. Dine, Kusenko, hep-ph/0303065]

- **but** constraints from electric dipole moments (EDMs) of e^- , n, Hg, Tl
[Ibrahim, Nath, '99; Barger, Falk, Han, Jiang, Li, Plehn, '01; Abel, Khalil, Lebedev, '01]

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- **CP-odd asymmetries** - already at tree-level (in $\tilde{\chi}^\pm$ and $\tilde{\chi}^0$ sectors)
 - formed by triple products asymmetries
 - full spin correlations between production and decay

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CPV asymmetry

$$A_{\text{CP}} = \frac{\Gamma(\text{decay}^+) - \Gamma(\text{decay}^-)}{\Gamma(\text{decay}^+) + \Gamma(\text{decay}^-)}$$

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$$A_{\text{CP}} \sim (\text{imaginary part of coupling}) \times (\text{absorptive part of loop-integral})$$

is a loop effect! "Optical theorem"

- The observable is the decay rate, significance $\sim A_{\text{CP}} \times \sqrt{\text{branching ratio}}$.
- If new channel opens: $A_{\text{CP}} \uparrow$, BR \downarrow .

\Rightarrow always work in opposite directions

- Two types of loop-diagrams: vertex and self-energy – contributions only from $\tilde{\chi}_1^\pm - \tilde{\chi}_2^\pm$ or $H^\pm - W^\pm$ transitions

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- No renormalization - A_{CP} - denominator approximated by Γ^{tree}

CPV asymmetry

$$A_{CP} \simeq \frac{\Gamma(\text{decay}^+) - \Gamma(\text{decay}^-)}{2\Gamma^{\text{tree}}(\text{decay}^+)}$$

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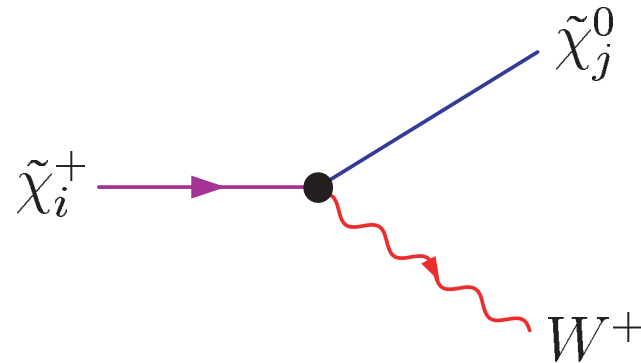
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$$\tilde{\chi}_i^+ \rightarrow \tilde{\chi}_j^0 W^+$$

tree-level:



$$\text{coupling} \sim \gamma^\mu (O_{ji}^R P_R + O_{ji}^L P_L)$$

$$O_{ji}^R = g Z_{j2}^* U_{i1} + \frac{g}{\sqrt{2}} Z_{j3}^* U_{i2}, \quad O_{ji}^L = g Z_{j2} V_{i1}^* - \frac{g}{\sqrt{2}} Z_{j4} V_{i2}^*$$

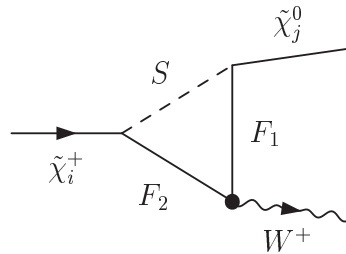
$$\Gamma^{\text{tree}} = \frac{\sqrt{\lambda}}{32\pi m_i^3} \left(\left(\frac{\lambda}{m_W^2} + 3X \right) (|O^R|^2 + |O^L|^2) - 12m_i m_j \text{Re}[O^{R*} O^L] \right)$$

$$X = m_i^2 + m_j^2 - m_W^2, \quad \lambda = \lambda(m_i^2, m_j^2, m_W^2) \text{ with } \lambda(x, y, z) = (x - y - z)^2 - 4yz$$

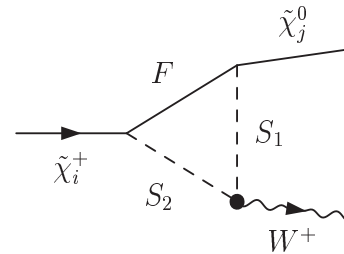
- dependence on ϕ_μ and ϕ_{M_1}
- no bino coupling - Γ^{tree} small for bino-like neutralino! \rightarrow BR to zero

One-loop graphs

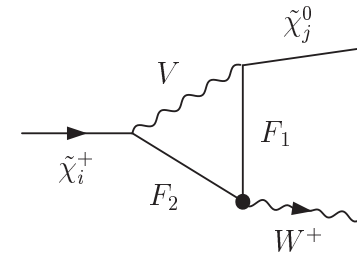
Sources for CP violation in $\tilde{\chi}_i^+ \rightarrow \tilde{\chi}_j^0 W^+$ decays at one-loop level in the MSSM with complex couplings



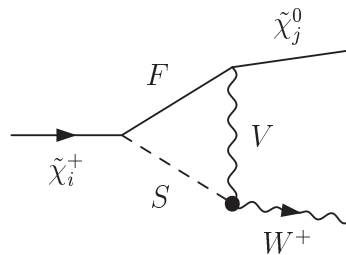
SF_1F_2 :
 $\tilde{f}ff', \phi^0\tilde{\chi}^0\tilde{\chi}^+, \phi^+\tilde{\chi}^+\tilde{\chi}^0$



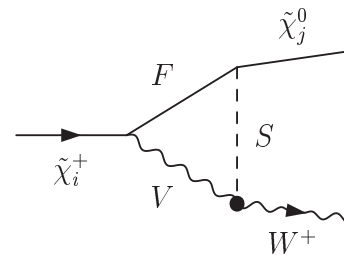
FS_1S_2 :
 $ff\tilde{f}', \tilde{\chi}^0\phi^0\phi^+, \tilde{\chi}^+\phi^+\phi^0$



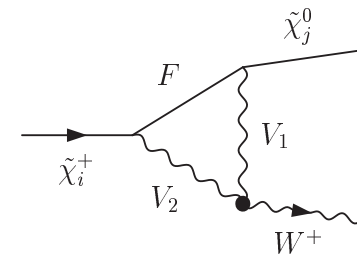
VF_1F_2 :
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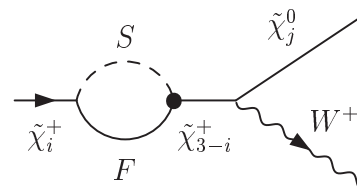
FVS :
 $\tilde{\chi}^0Z^0G^+, \tilde{\chi}^+W^+H_n^0$



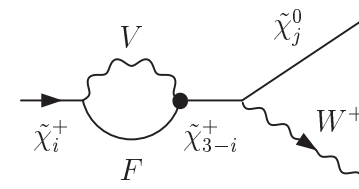
FSV :
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FV_1V_2 :
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SF :
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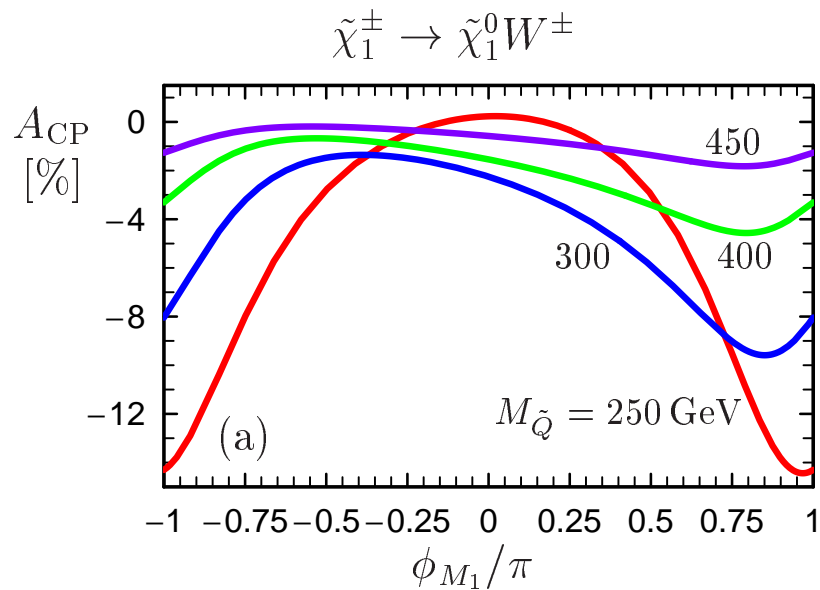


VF :
 $Z^0\tilde{\chi}^+, W^+\tilde{\chi}^0$

$$\tan \beta = 10, m_{A^0} = 300 \text{ GeV}, \phi_\mu = \frac{\pi}{10}$$

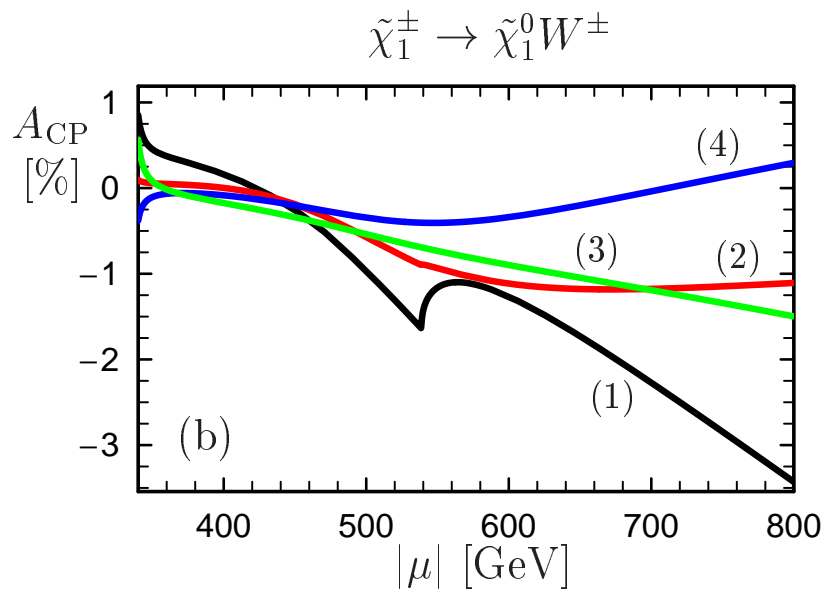
$$M_2 = 500 \text{ GeV},$$

$$|A| = 400 \text{ GeV}, \phi_A = -\frac{\pi}{4}$$



$$|\mu| = 600 \text{ GeV},$$

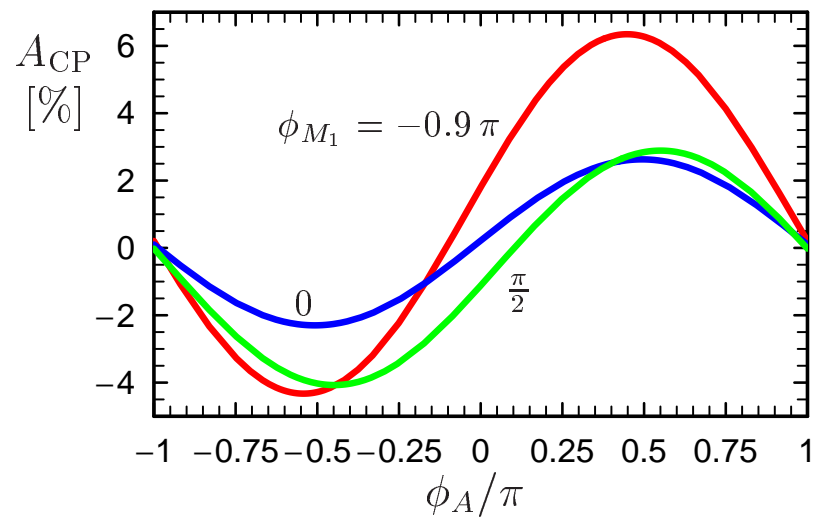
- (1) vertex contribution with third gen. (s)quarks
- (2) chargino selfenergy contribution with with third gen. (s)quarks
- (3) all other (s)fermions in the loop
- (4) remaining contributions



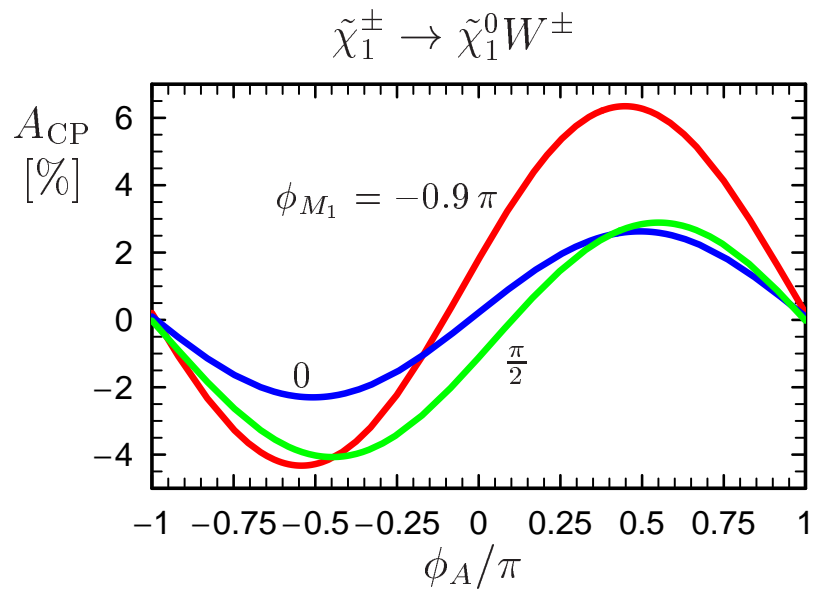
$$\phi_{M_1} = \frac{\pi}{4}, M_{\tilde{Q}} = 350 \text{ GeV}$$

$\tan \beta = 10, m_{A0} = 300 \text{ GeV}, \phi_\mu = \frac{\pi}{10}$
 $M_2 = 500 \text{ GeV}, |\mu| = 600 \text{ GeV}$
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$$\tilde{\chi}_1^\pm \rightarrow \tilde{\chi}_1^0 W^\pm$$

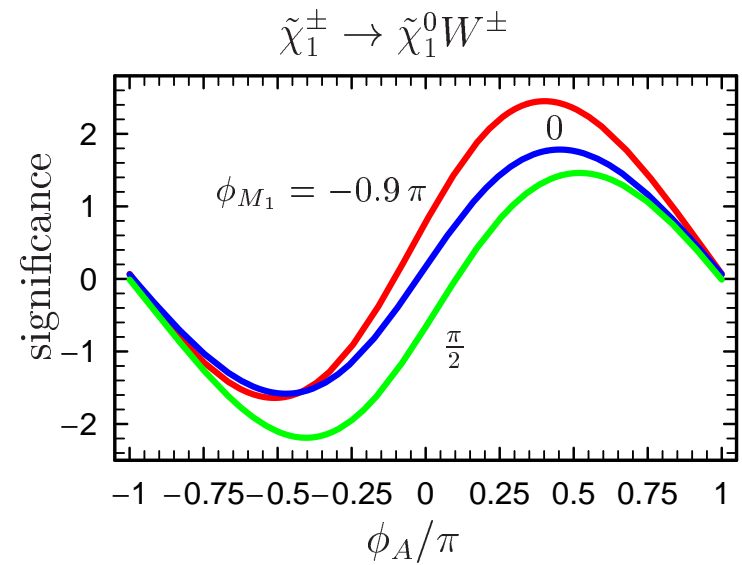
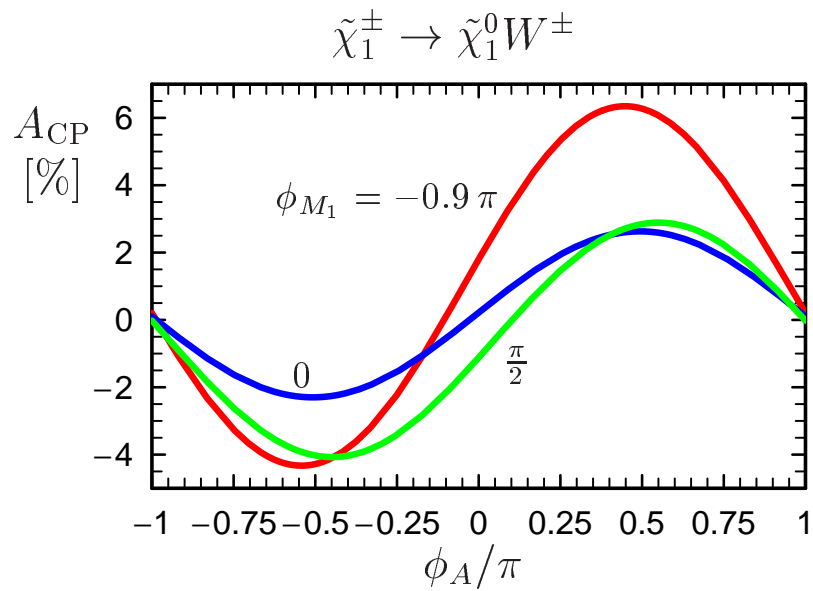


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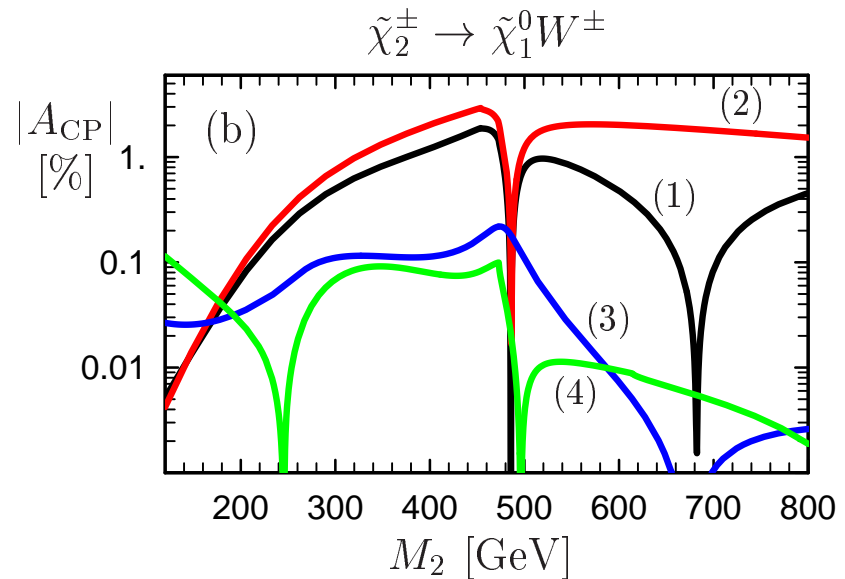
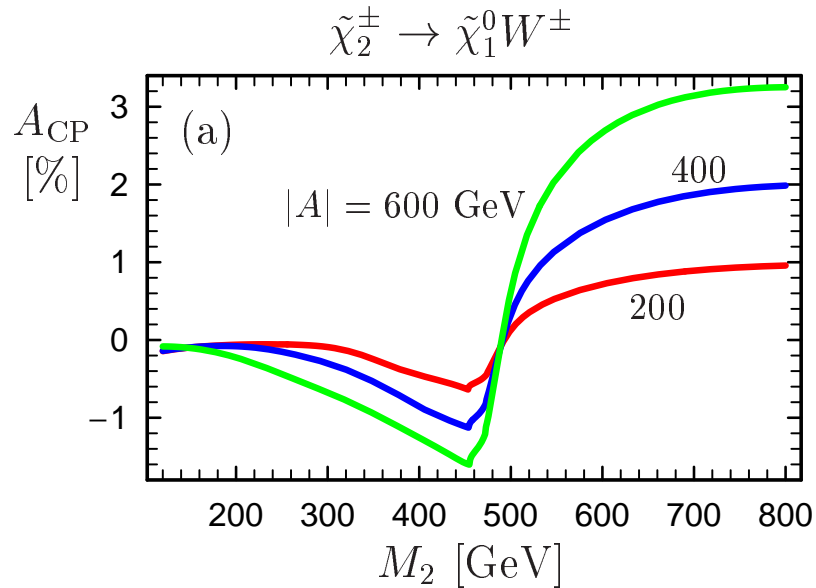
Assuming at LHC $n = \sim 2.4 \times 10^5$ of $\tilde{\chi}_1^\pm$
 (40% of gluinos decay into a $\tilde{\chi}_1^+$ or $\tilde{\chi}_1^-$)
 significance := $A_{CP} \times \sqrt{n BR}$

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$$\tan \beta = 10, m_{A^0} = 300 \text{ GeV}, \phi_\mu = \frac{\pi}{10}$$

$$|\mu| = 200 \text{ GeV}, \phi_{M_1} = \pi, M_{\tilde{Q}} = 300, \phi_A = -\frac{\pi}{4}$$

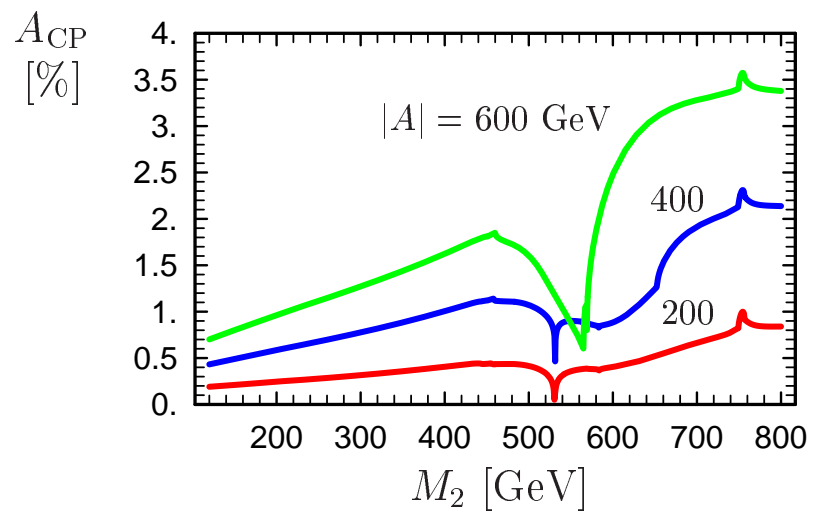


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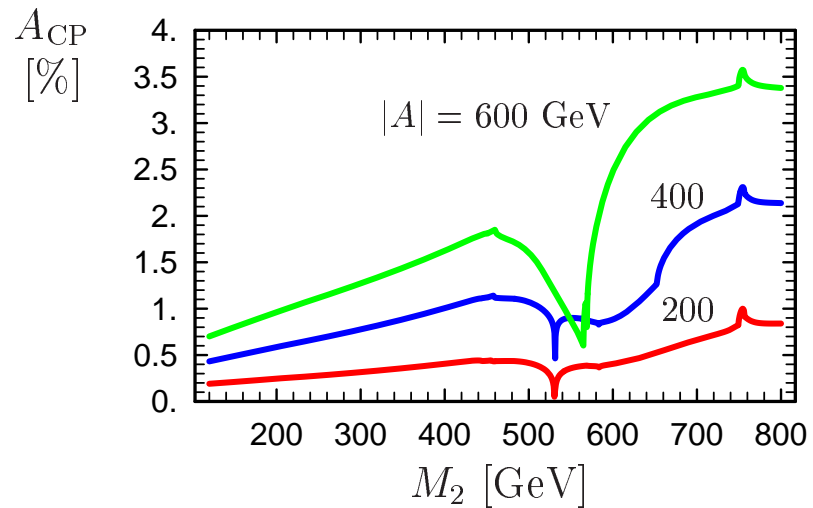
$$\tilde{\chi}_2^\pm \rightarrow \tilde{\chi}_2^0 W^\pm$$



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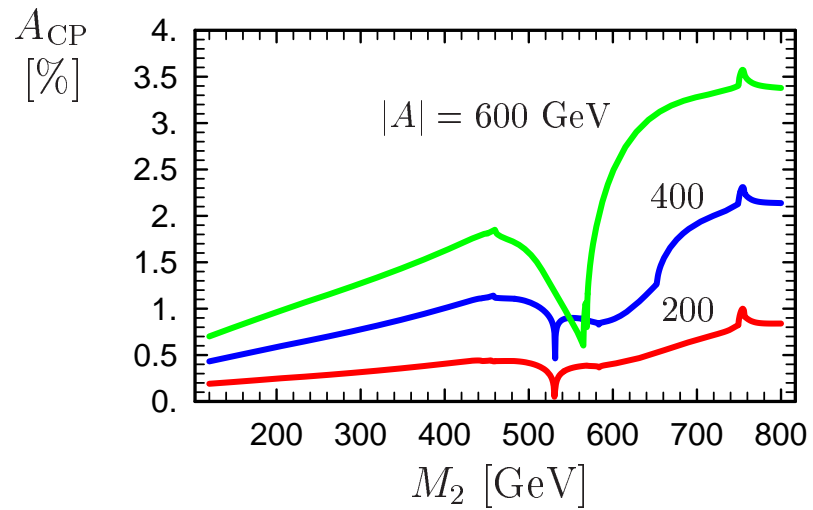


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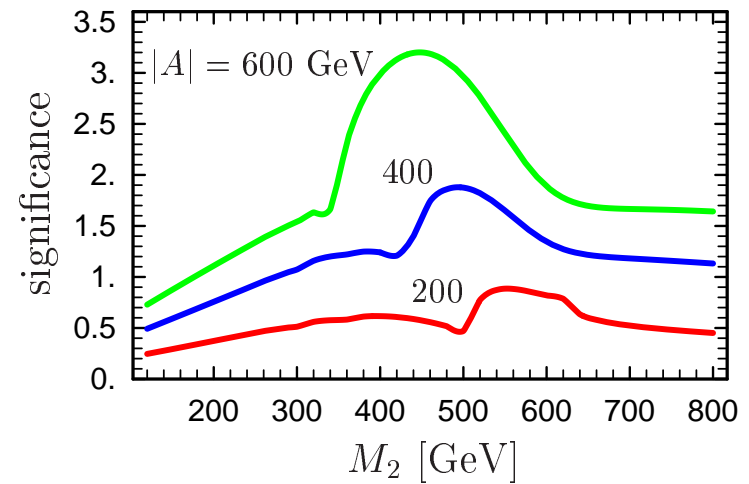
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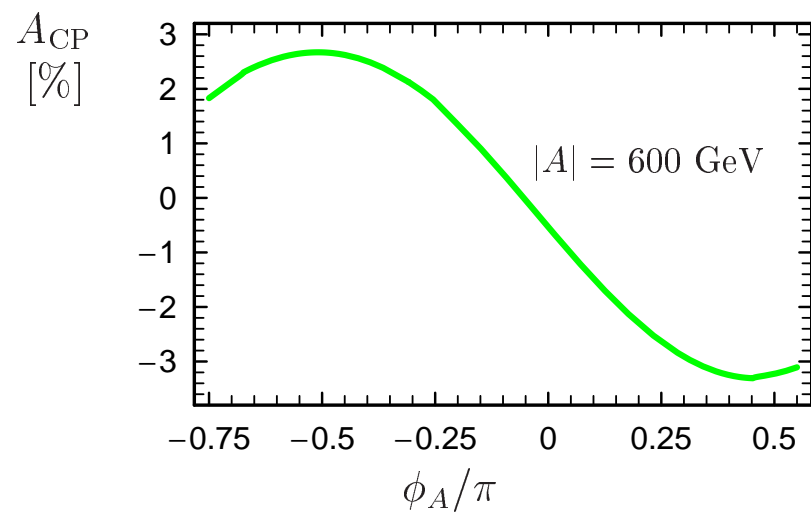


$$\tilde{\chi}_2^\pm \rightarrow \tilde{\chi}_2^0 W^\pm$$



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 $M_2 = 450 \text{ GeV}, \phi_{M_1} = 0, |\mu| = 600 \text{ GeV}, M_{\tilde{Q}} = 300 \text{ GeV}$

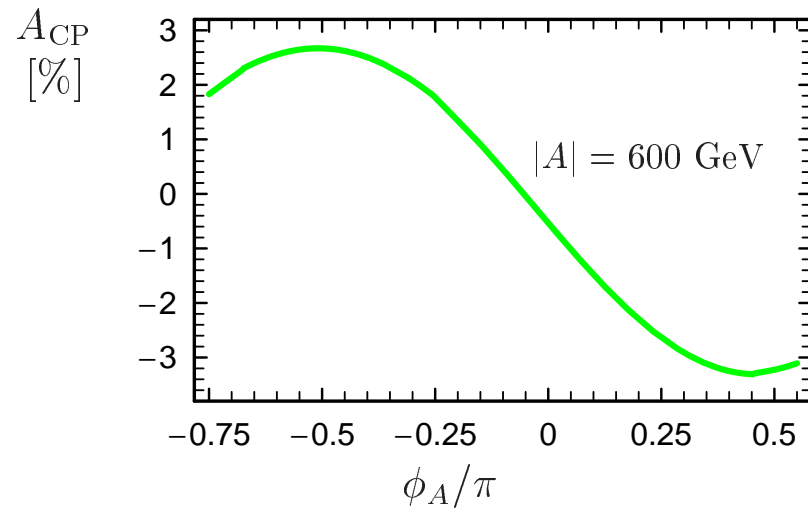
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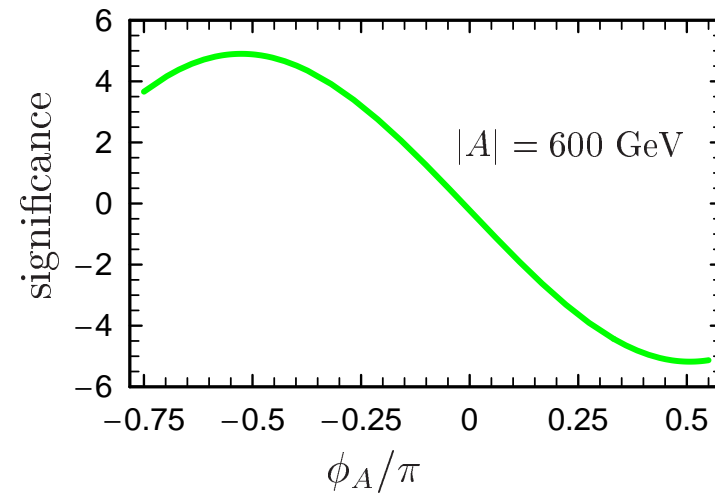
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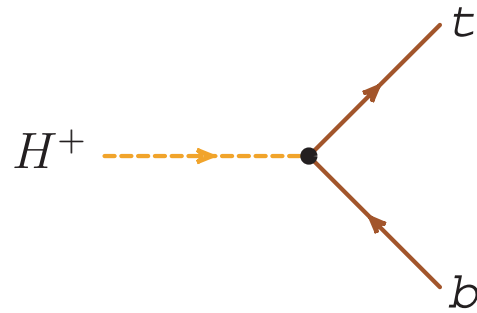
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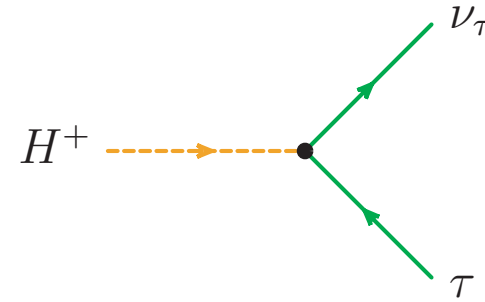
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$$H^+ \rightarrow t\bar{b}, \nu_\tau \tau^+$$



tree-level:



$$\sim \underbrace{h_t \cos \beta P_R}_{y_t} + \underbrace{h_b \sin \beta P_L}_{y_b}$$

$$\sim \underbrace{h_\tau \sin \beta P_L}_{y_\tau}$$

$$\Gamma^{\text{tree}}(H^+ \rightarrow t\bar{b}) = \frac{3\sqrt{\lambda}}{16\pi m_{H^+}^3} \left((m_{H^+}^3 - m_t^2 - m_b^2)(y_t^2 + y_b^2) - 4m_t m_b y_t y_b \right)$$

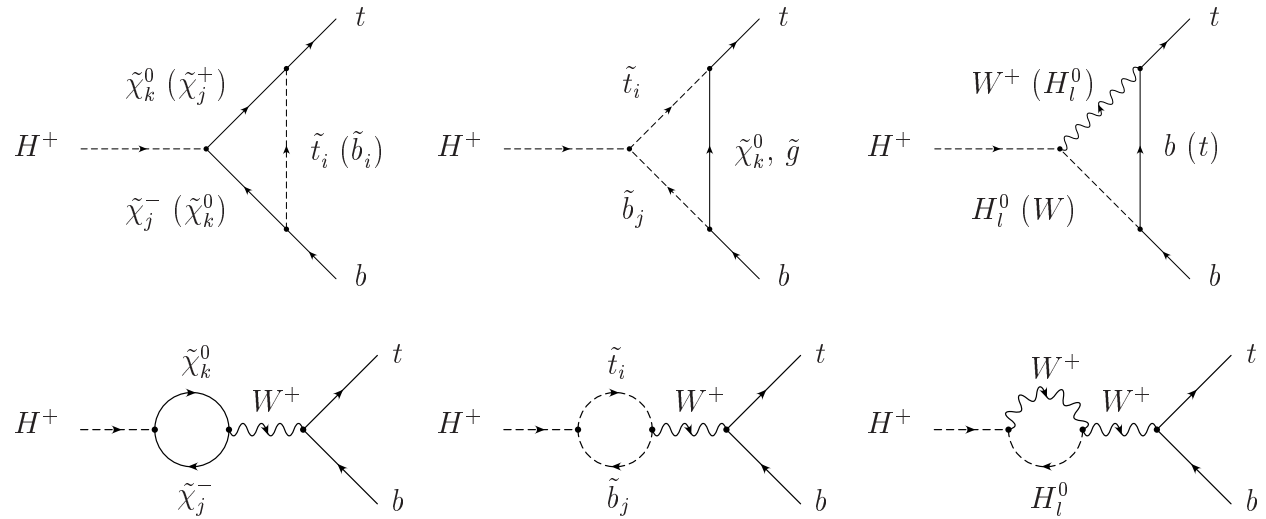
$$\Gamma^{\text{tree}}(H^+ \rightarrow \nu_\tau \tau^+) = \frac{\sqrt{\lambda}}{16\pi m_{H^+}^3} (m_{H^+}^3 - m_\tau^2) y_\tau^2$$

$$h_t = gm_t / (\sqrt{2}m_W \sin \beta), h_{b,\tau} = gm_{b,\tau} / (\sqrt{2}m_W \cos \beta)$$

- independent of phases.
- only two SUSY parameters: m_{H^+} and $\tan \beta$

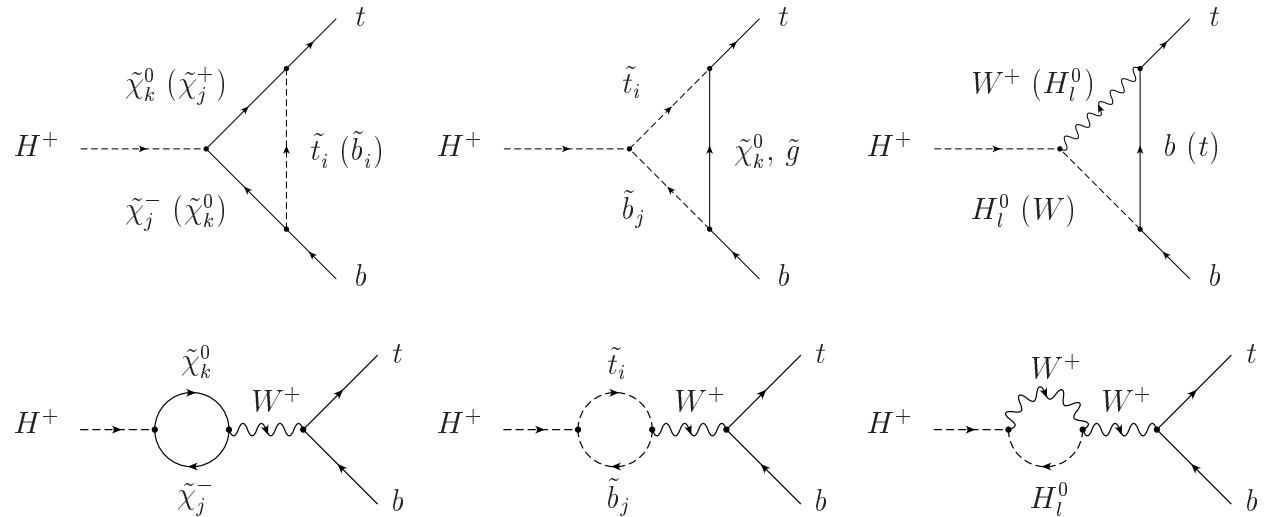
One-loop graphs

Sources for CP violation in $H^+ \rightarrow t\bar{b}$ decays at one-loop level in the MSSM with complex couplings

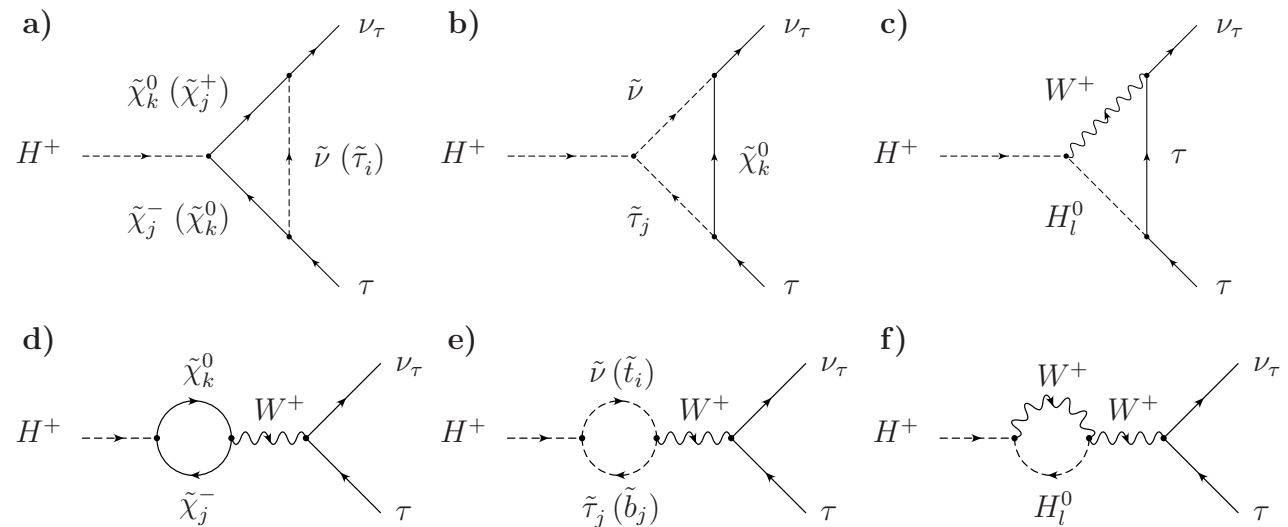


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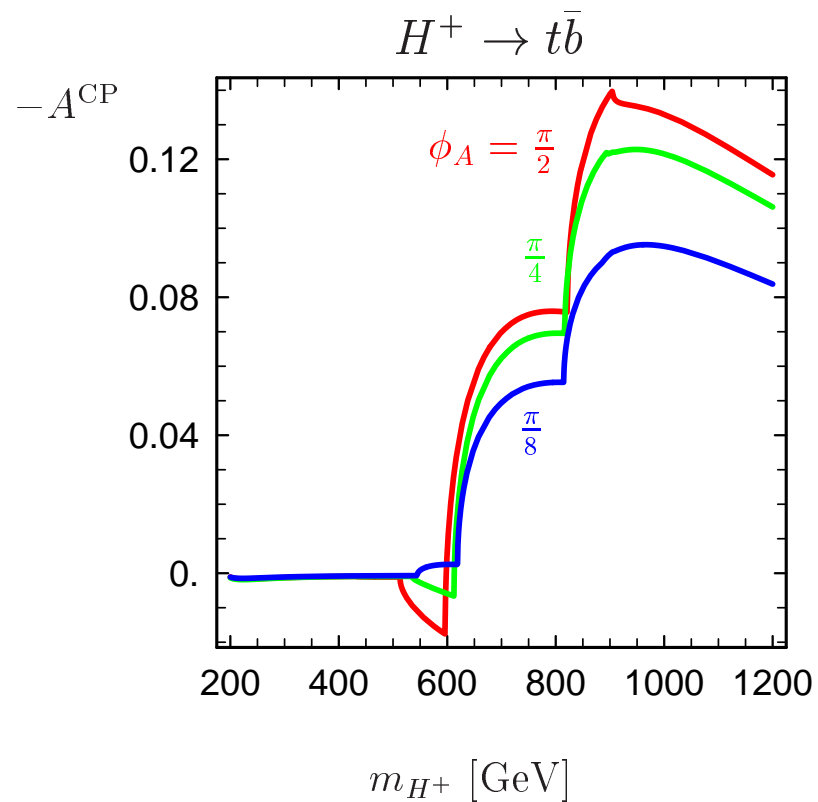
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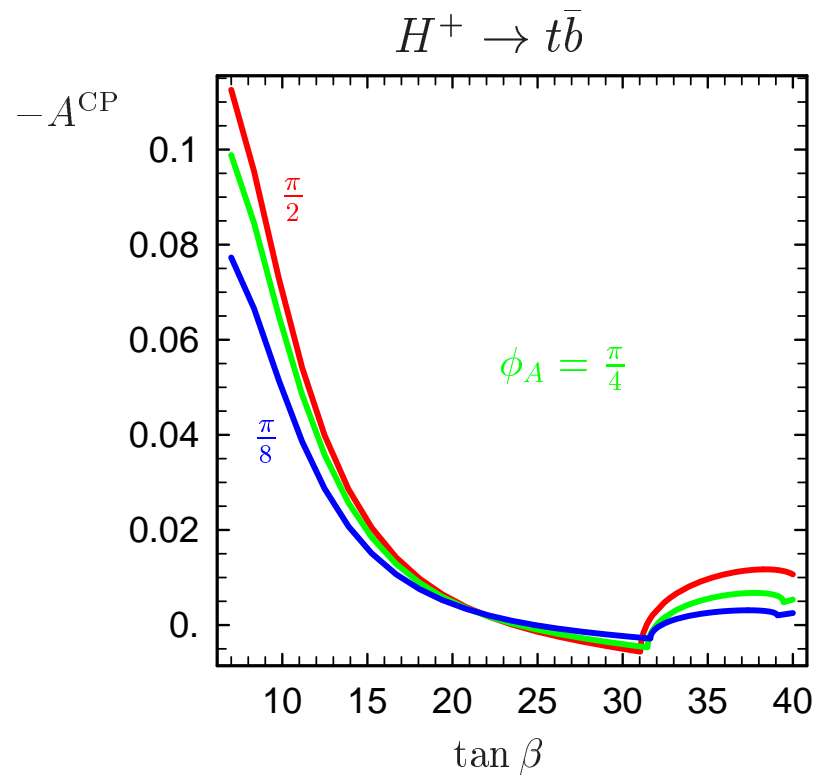
Sources for CP violation in $H^+ \rightarrow \tau\bar{\nu}_\tau$ decays at one-loop level in the MSSM with complex couplings



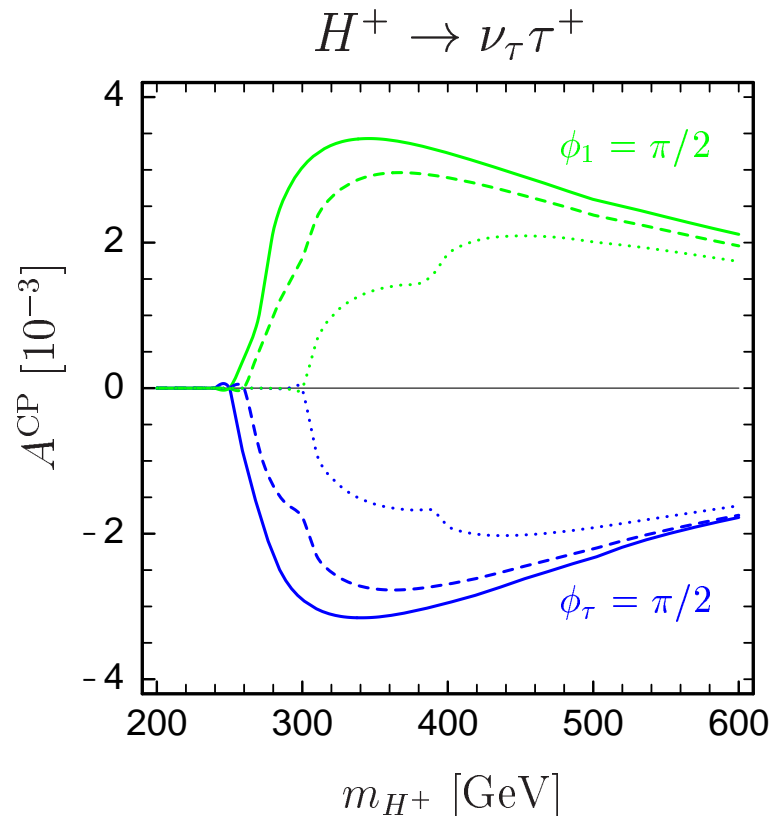
$\tan \beta = 10, M_2 = 300 \text{ GeV}, \phi_{M_1} = 0, |\mu| = 600 \text{ GeV}, \phi_\mu = \frac{\pi}{10},$
 $M_{\tilde{Q}} = 350 \text{ GeV}, |A| = 600 \text{ GeV}$



$M_{H^+} = 700 \text{ GeV}$, $M_2 = 300 \text{ GeV}$, $\phi_{M_1} = 0$, $|\mu| = 600 \text{ GeV}$, $\phi_\mu = \frac{\pi}{10}$,
 $M_{\tilde{Q}} = 350 \text{ GeV}$, $|A| = 600 \text{ GeV}$



$M_2 = 200 \text{ GeV}$, $\mu = 300 \text{ GeV}$, $M_{\tilde{E}} = M_{\tilde{L}} - 5 \text{ GeV} \rightarrow m_{\tilde{\tau}} = 135 \text{ GeV}$,
 $|A_\tau| = 400 \text{ GeV}$, $M_{\tilde{Q}} = 500 \text{ GeV}$, $M_{\tilde{U}} = 450 \text{ GeV}$, $M_{\tilde{D}} = 550 \text{ GeV}$, $A_t = A_b = -500 \text{ GeV}$.



$\phi_\tau = \pi/2$, $\phi_1 = 0$ ($A_{\text{CP}} < 0$), and for $\phi_1 = \pi/2$, $\phi_\tau = 0$ ($A_{\text{CP}} > 0$),
 $\tan \beta = 5$ (full), 10 (dashed), 30 (dotted).

Conclusions

- A_{CP} - simple measurement - only total decay rates
- SUSY loop effect – vertex and selfenergy contributions
- $\tilde{\chi}_i^\pm \rightarrow \tilde{\chi}_j^0 W^\pm$: A_{CP} order of several percent. $\tilde{\chi}_1^0$ must not be very bino like.
- $H^\pm \rightarrow tb$: A_{CP} up to $\sim 10\%$, high m_{H^\pm} necessary (> 500 GeV), $\tan \beta \uparrow \rightarrow A_{CP} \downarrow$ and BR \downarrow , stop-bottom channel, gluino exchange important.
- $H^\pm \rightarrow \nu_\tau \tau^\pm$: A_{CP} smaller than 0.5%, rel. low m_{H^\pm} (~ 300 GeV), $\tan \beta \uparrow \rightarrow A_{CP} \downarrow$ but BR \uparrow , stau-snu channel important.
- If A_{CP} becomes large, total (renormalized) one-loop result is maybe necessary.
- Combined study with production, BR and A_{CP} necessary.