Shell model for weakly bound and unbound nuclear states: Bound and continuum states in one framework

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Spectra and matter distribution are modified by the proximity of scattering continuum

New exotic phenomena in weakly bound nuclei:

- continuum anti-odd-even staggering effect
- modification of 'magic numbers' and spin-orbit splitting
- halos and correlations, continuum anti-halo effect
- symmetry-breaking effects induced by the coupling to decay channels
- correlated continuum in reactions with multiple weakly bound/unstable subsystems
- influence of the poles of S-matrix on spectra and wave functions
- (e.g. spectroscopic factors, pair amplitudes, mirror nuclei, etc.)
- new kinds of natural radioactivity (e.g. 2p radioactivity, etc.)
- etc. .....



Continuum (real-energy) Shell Model (1977 - 1999 - 2005) Gamow (complex-energy) Shell Model (2002 -)

H.W.Bartz et al, NP A275 (1977) 111 R.J. Philpott, NP A289 (1977) 109 K. Bennaceur et al, NP A651 (1999) 289 J. Rotureau et al, PRL 95 (2005) 042503 N. Michel et al, PRL 89 (2002) 042502
R. Id Betan et al, PRL 89 (2002) 042501
N. Michel et al, PRC 70 (2004) 064311
G. Hagen et al, PRC 71 (2005) 044314

New paradigm is born!

#### Rigged Hilbert space formulation : Gamow Shell Model (2002)



complex-symmetric eigenvalue problem for hermitian Hamiltonian



Interaction of nucleons in the continuum states is an essential element of binding mechanism in helium isotopes

### Hilbert space formulation : Shell Model Embedded in the Continuum (1999)



Incompatible symmetries of  $H_{QQ}$  and  $H_{QQ}^{eff}(E)$ 

#### Reduction of the odd-even staggering close to the drip-line



Continuum correction to the binding energy of closed QS stronger for :

$$\begin{bmatrix} A \end{bmatrix} \rightarrow \begin{bmatrix} A - 1 \end{bmatrix} \otimes \begin{bmatrix} 1 \end{bmatrix}$$
$$\begin{bmatrix} \text{odd-N} \end{bmatrix} \rightarrow \begin{bmatrix} \text{even-N} \end{bmatrix} \otimes \begin{bmatrix} 1 \end{bmatrix}$$

Incompatible symmetries of a state  $\Phi_{\alpha}^{(A)}$ and decay channels:  $\Phi_{\beta}^{(A-1)} \otimes \phi_{\gamma}^{(n)}$  Continuum couplings are essential in the overlapping regime: failure of RMT! How important are continuum couplings for isolated states (low-density regime)?



Opening of cavit



### 2p decay from the ground state of ${}^{45}Fe$ , ${}^{48}Ni$ and ${}^{54}Zn$

M. Pfutzner et al, Eur. Phys. J. A14 (2002) 279; J. Giovinazzo et al, Phys. Rev. Lett. 89 (2002) 102501



B. Blank et al, Phys. Rev. Lett. 94 (2005) 232501



## Two-proton emission

J. Rotureau et al., PRL 95 (2005) 042503



 $H_{QQ}^{eff}(E) = H_{QQ} + H_{QP}G_P^{(+)}(E)H_{PQ} + [H_{QP}G_P^{(+)}(E)H_{PT}]\tilde{G}_T^{(+)}(E)[H_{TP}G_P^{(+)}(E)H_{PQ}]$ 

#### Direct 2p emission

+ final state interaction in terms of  $(l_x = 0)$  s-wave phase shift

Diproton emission channel:

$$c = \left(\theta_{J_f^{(A-2)}}^{(\text{int})}, l_x = 0, S = 0, L = 0\right)$$

$$\Gamma = \int_{0}^{Q_{2p}} \Gamma(U)\rho(U)dU$$
$$\Gamma(U) = -2Im\left[\left\langle \omega_{i,U}^{T,(+)} \middle| w_{i}^{T} \right\rangle\right]$$





$$^{45}_{26}Fe \rightarrow ^{43}_{24}Cr + 2p$$



Precise knowledge of  $Q_{2p}, Q_{1p}$  is indispensable!

# Conclusions

- Continuum shell model : Gamow (complex-energy) Shell Model or Shell Model Embedded in the Continuum, provide a consistent description of the of weakly bound nuclei
- -Priorities (personal choice):
  - \* study of pairing correlations via final state pp correlations in 2p decays (masses!)
  - \* exotic decays (2n, neutron droplets,  ${}^{3}He$ , ...) and exotic clustering phenomena
  - \* 2p-capture via correlated continuum
  - \* reactions with multiple (n > 1) weakly bound partners: dynamics in (multiple) correlated continua vs structure of weakly bound systems and resonances
  - \* new 'magic' nuclei & spin-orbit splitting: 3-body & tensor forces vs continuum coupling correlations
  - \* effective symmetries in weakly bound/unbound nuclei (open quantum systems)
  - \* strong NN correlations beyond mean-field :  $S_{n,p} \rightarrow 0 \Leftrightarrow \lambda_{n,p} \Delta_{n,p} \rightarrow 0$ 
    - → new limit of nuclear mean-field
  - \* .... ...

Nuclear structure enters in a new, exciting era!