Evolution Of Shell Structure, Shapes & Collective Modes

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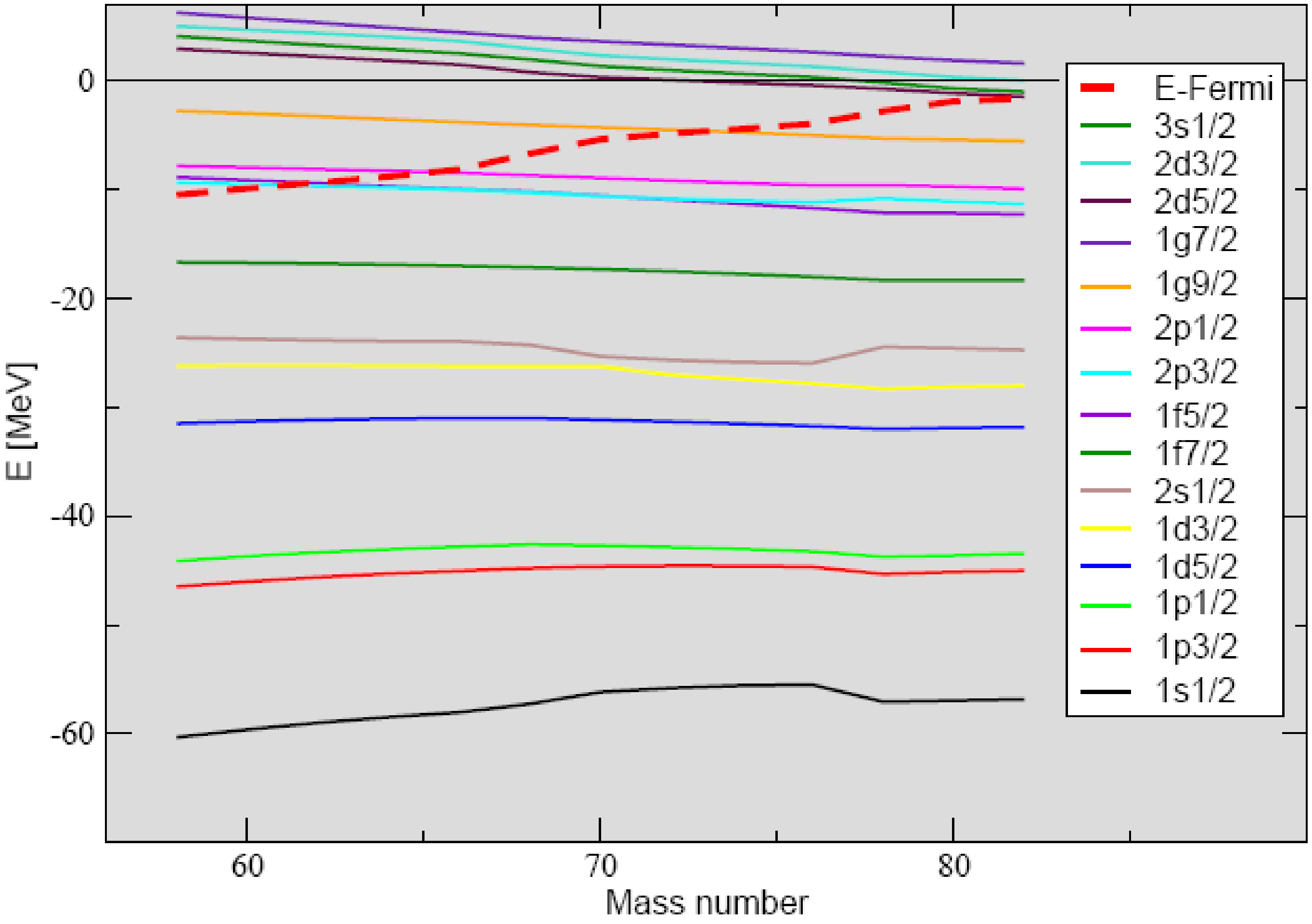
1. Evolution of shell structure with N and Z

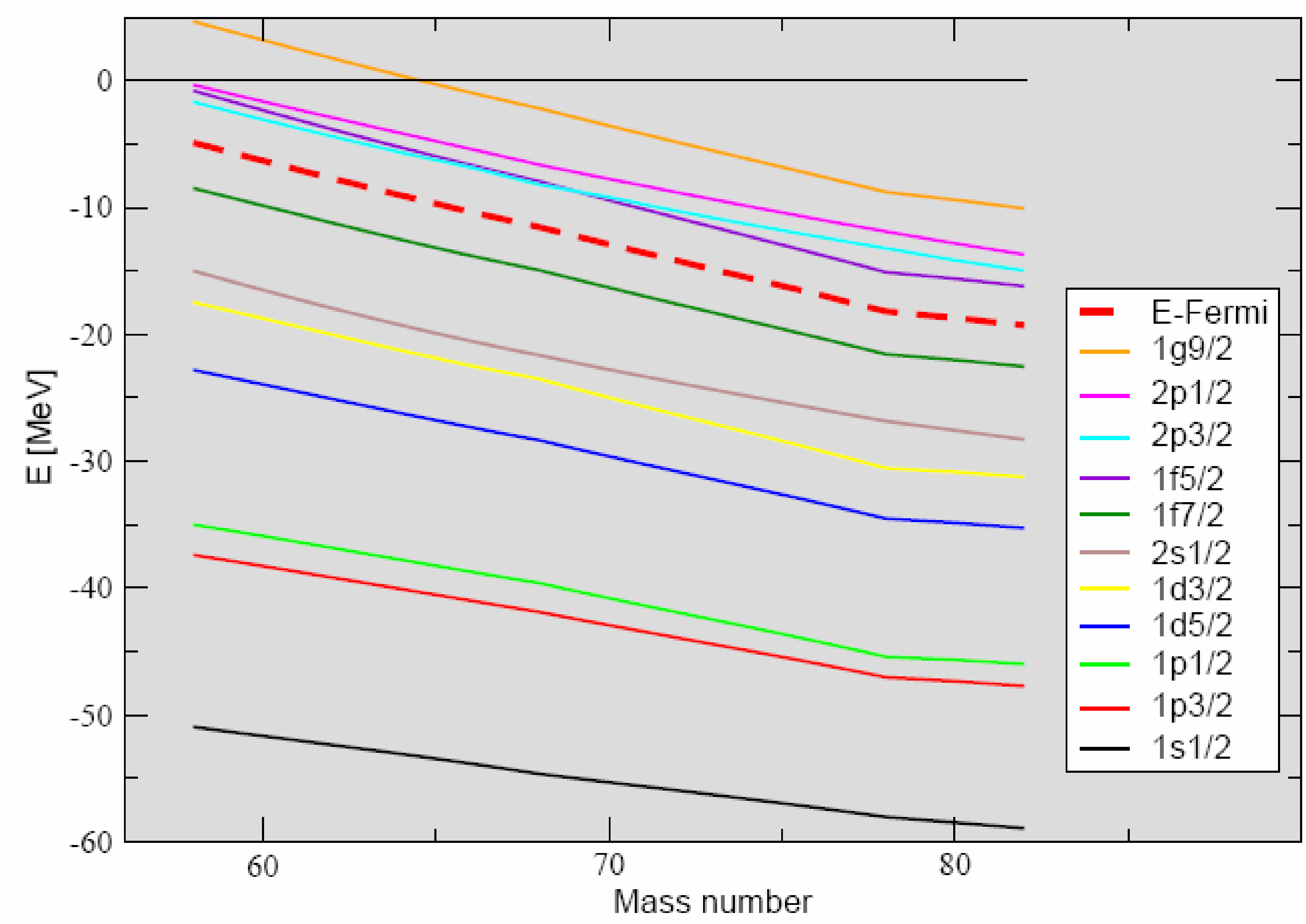
A. Modification of the effective single-nucleon potential

Relativistic Hartree-Bogoliubov calculation:
DD-ME1 effective interaction + Gogny D1S pairing

Neutron canonical single-particle levels in Ni isotopes.



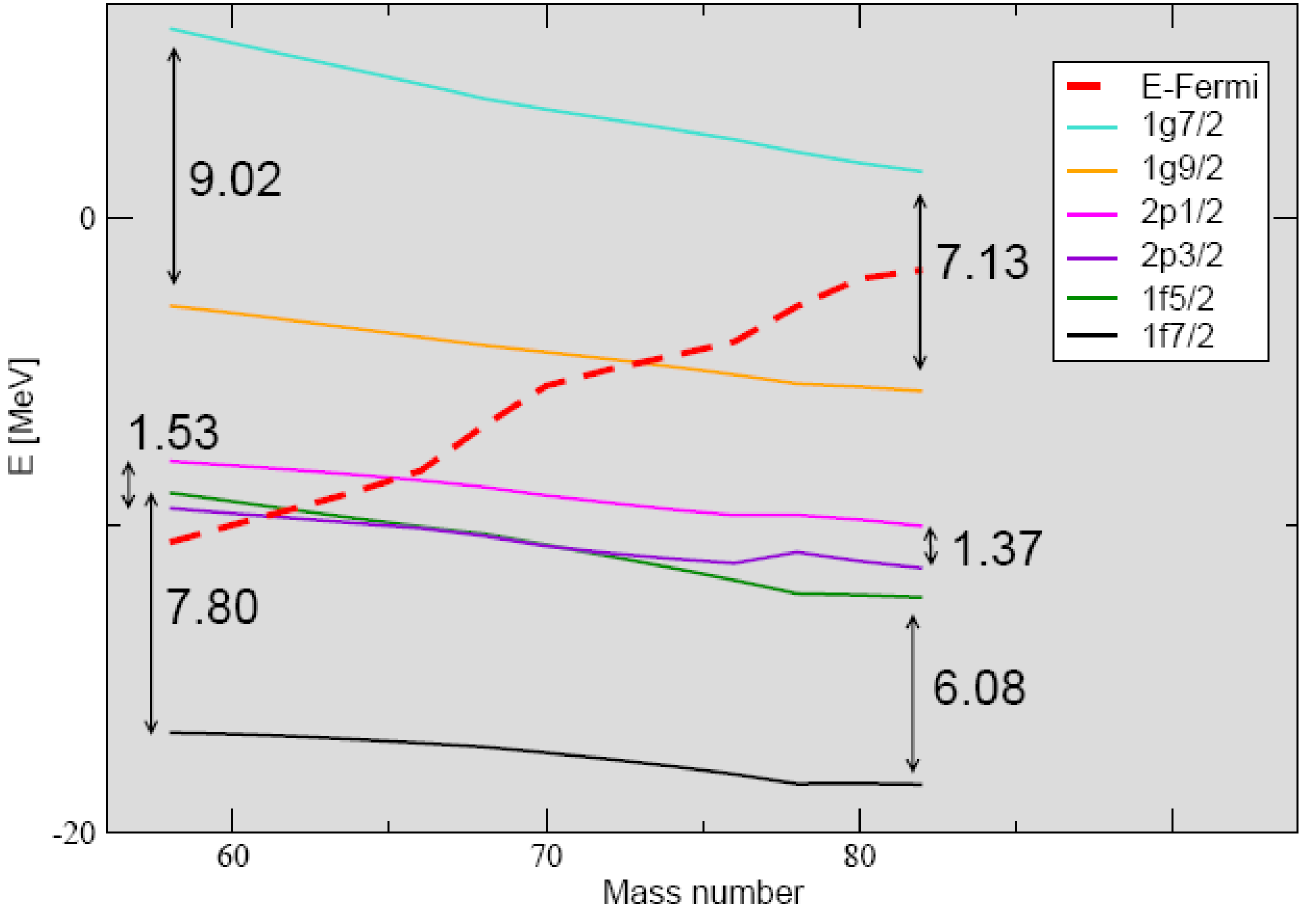
Proton canonical single-particle levels in Ni isotopes



Most of the single-nucleon levels evolve in parallel, keeping the level spacing essentially unchanged!

B. Isovector dependence of the effective spin-orbit interaction

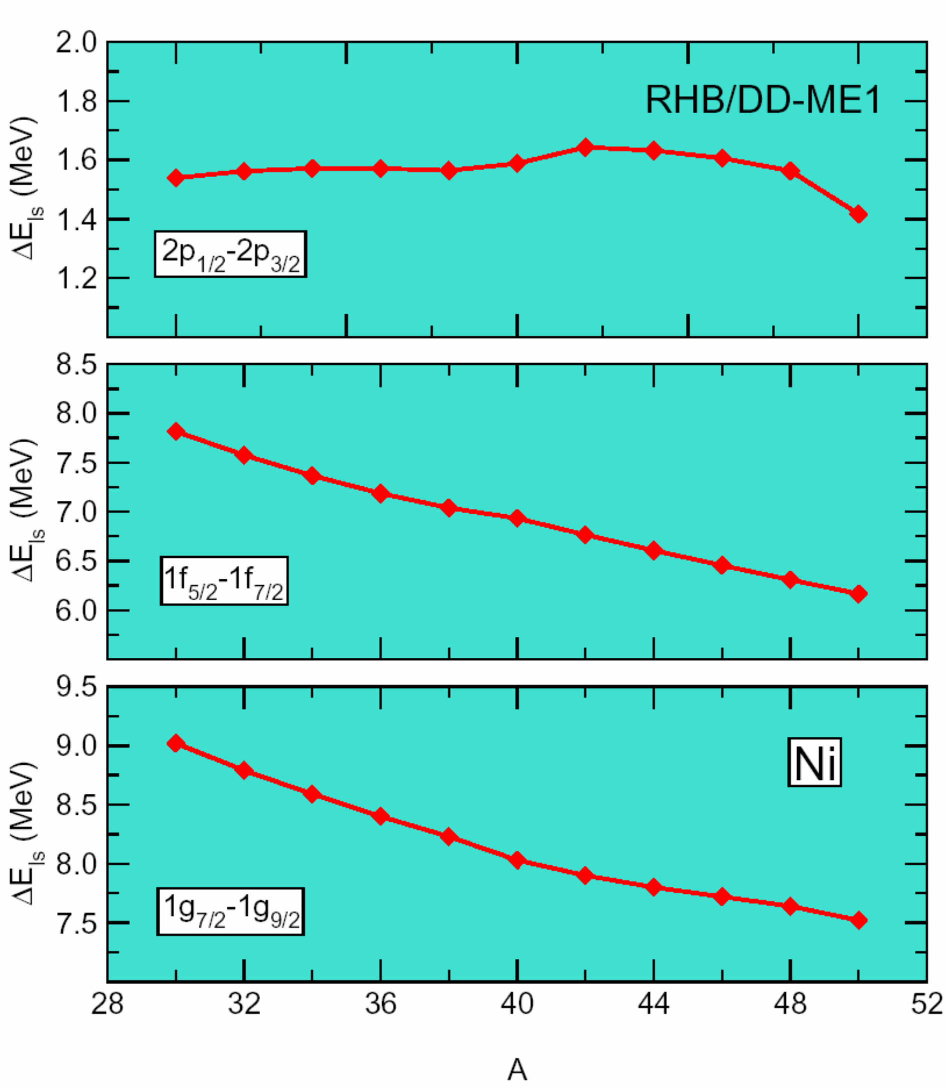
Neutron s.p. levels in Ni isotopes



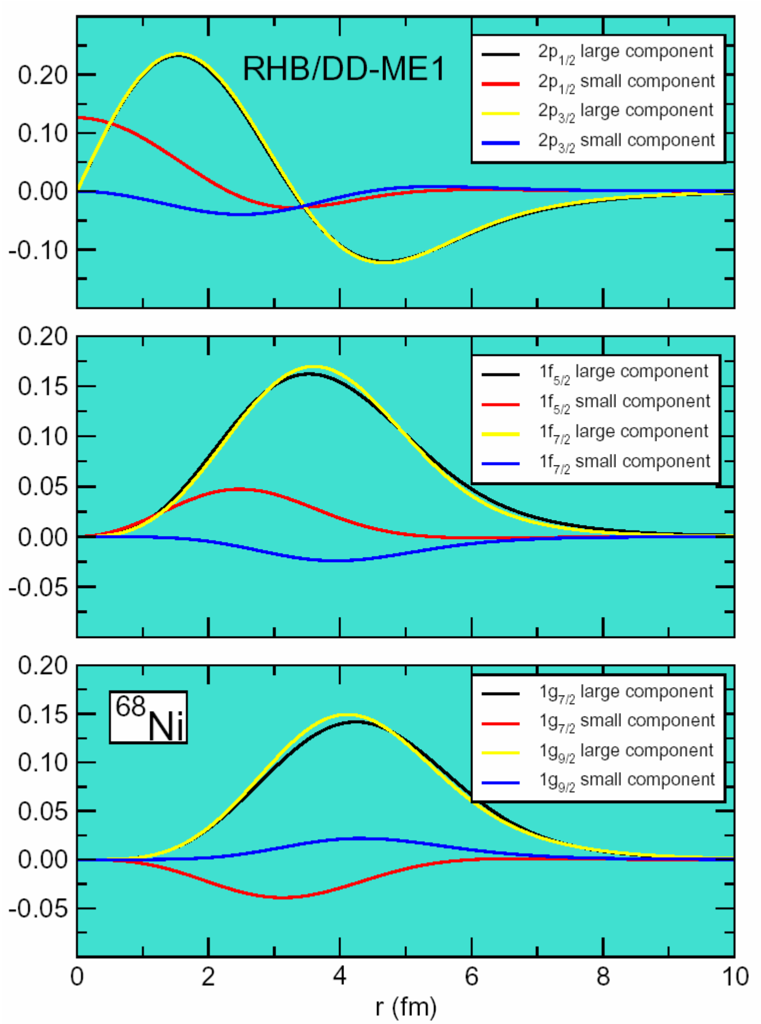
Relativistic Hartree-Bogoliubov calculation:
DD-ME1 effective interaction + Gogny D1S pairing

Reduction of the energy spacing between spin-orbit partner states.

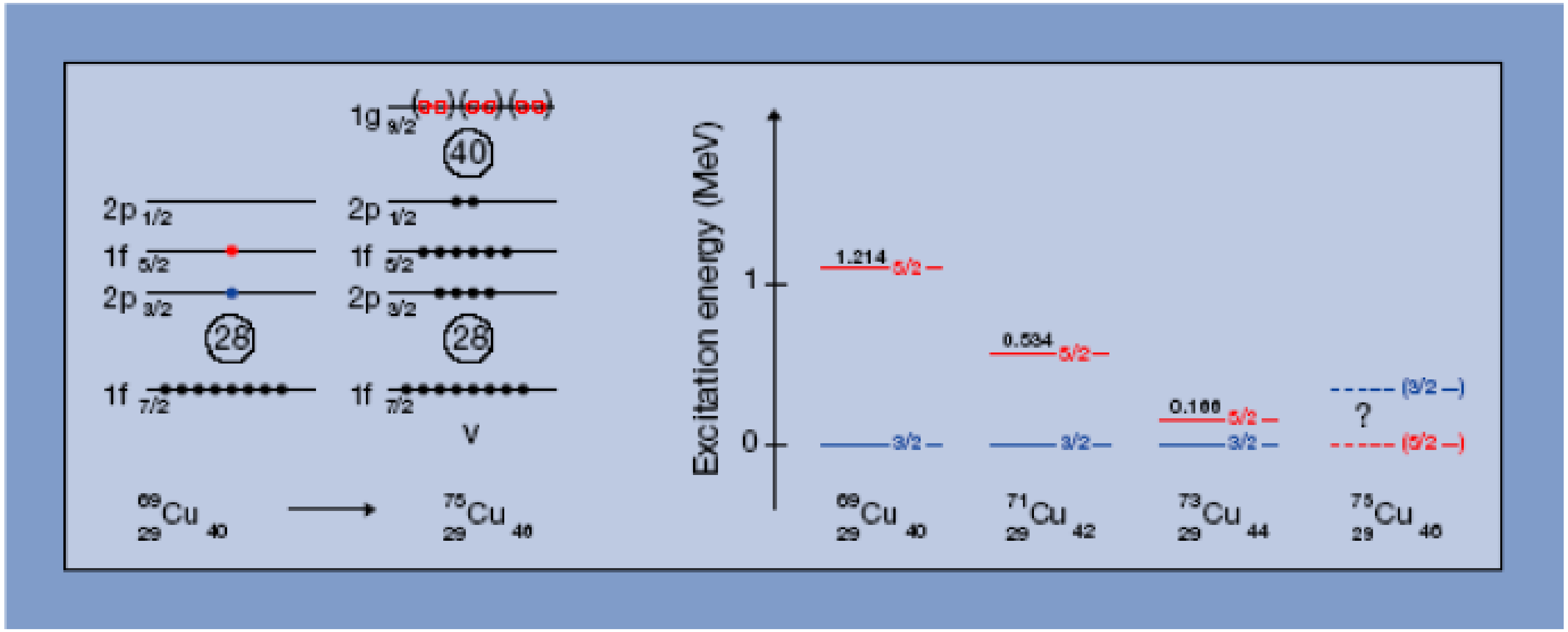
$$\Delta E_{ls} = E_{n,l,j=l-1/2} - E_{n,l,j=l+1/2}$$



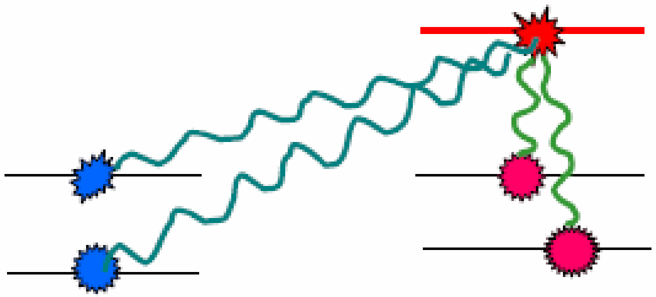
Radial Dirac wave-functions of spin-orbit doublets.



C. Monopole migration



Odd-A copper isotopes: migration of the 1f5/2 proton orbital as the 1g9/2 neutron orbital is being filled.



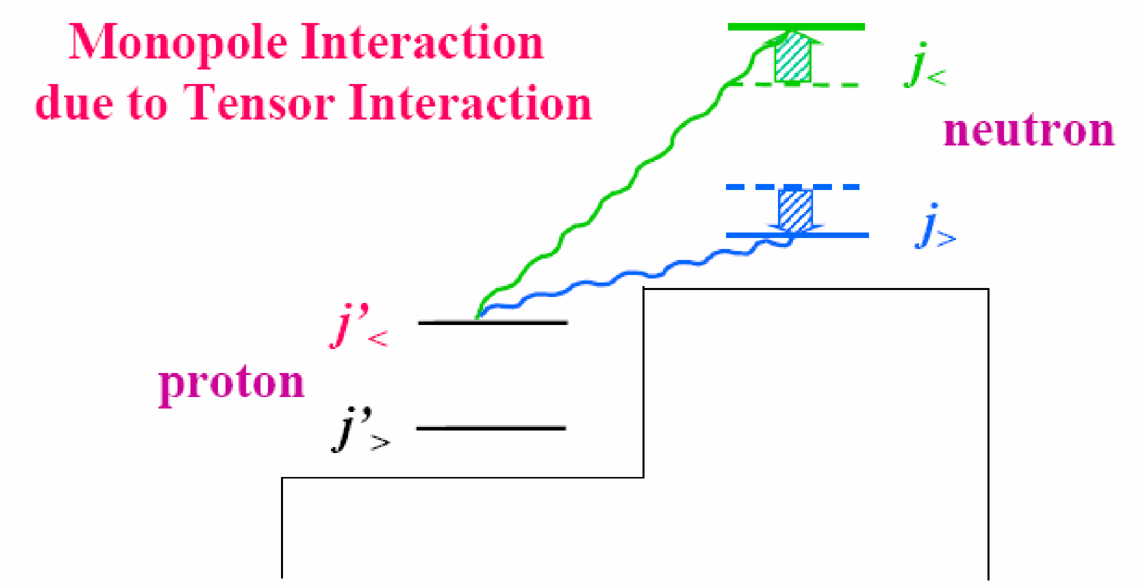
Monopole part of the NN interaction between valence protons and neutrons:

$$V_{ab}^{T} = \frac{\sum_J (2J+1) V_{abab}^{JT}}{\sum_J (2J+1)}$$

Effective Single-Particle Energies (ESPE) – depend on the monopole interaction between valence nucleons

What is the microscopic mechanism that determines the monopole migration of effective single-particle energies?

1)

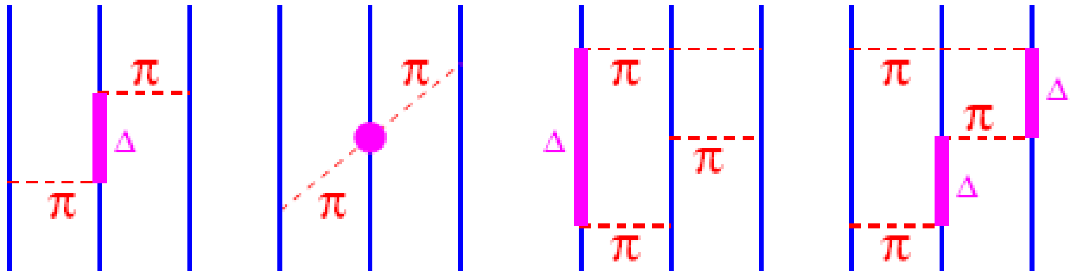


?

2)

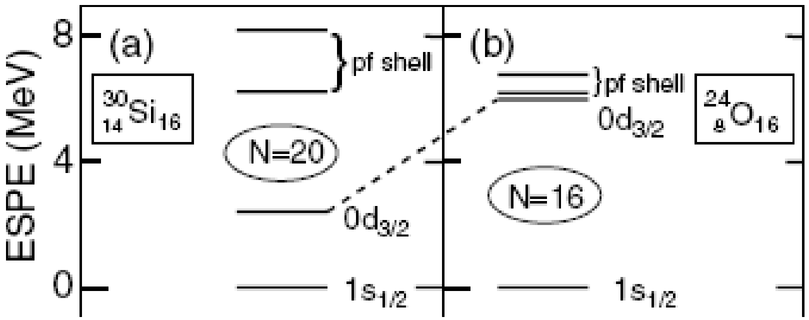
Monopole contribution from three-body forces?

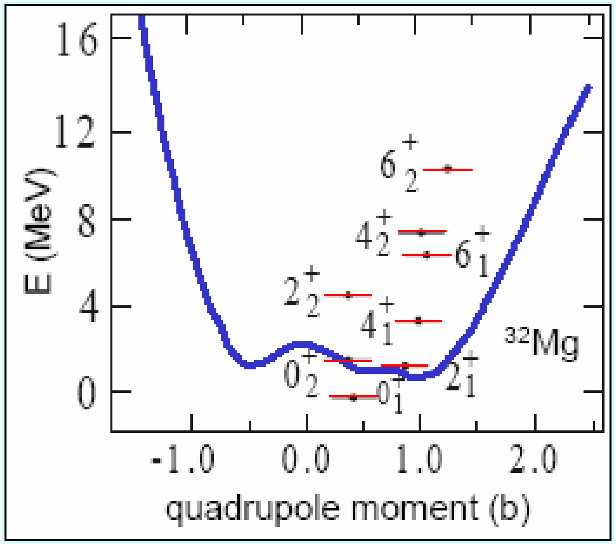
?



Evolution of shell structure in nuclei with N,Z < 40

Low-density of single-particle states!





-**reduced spherical shell gaps**

-**reordering of nucleonic shells (occurrence of islands of inversion!)**

-spherical magic gaps (N=8, 20, 28, ...) may disappear and new strong gaps can be found at N=6,16,32, ...)

-onset of deformation and shape coexistence (could extend the neutron drip line!)

Global Shell Model Description

Advantages:

-the ability to describe simultaneously all spectroscopic properties of low-lying states with very different structure within a nucleus

-effective interactions connected with both two- and three-nucleon bare forces

-a description of collective properties in the laboratory frame

Recent successful applications:

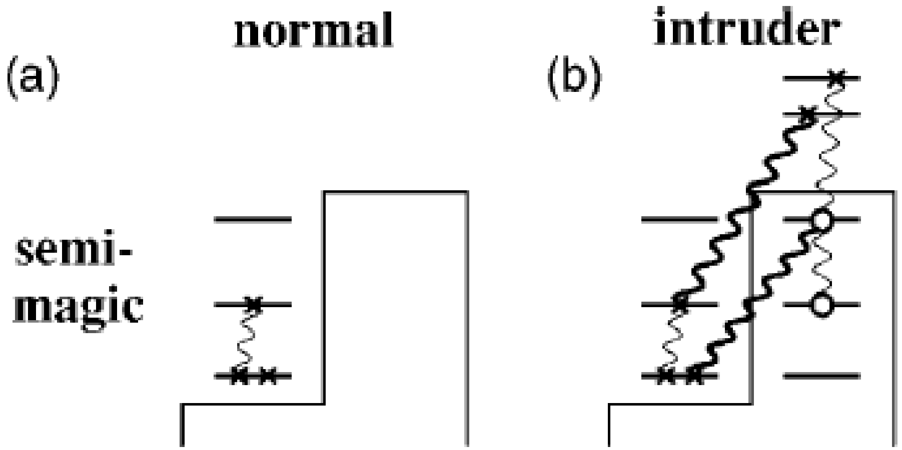
Standard large-scale shell model studies (Strasbourg-Madrid)

Shell-Model Monte Carlo

Quantum Monte Carlo diagonalization – MCSM (Tokyo)

No-core Shell Model

Island of inversion around Z≈11 and N=20



The ground states of these nuclei gain binding energy by promoting neutrons from the **sd-shell** to the **fp-shell** => gain in **deformation energy.**

Intruder configurations have lower energy than normal configurations.

Weakening of the shell closure and eventually the disappearance of the N=20 magic number!

Issues:

Boundary of the island of inversion?

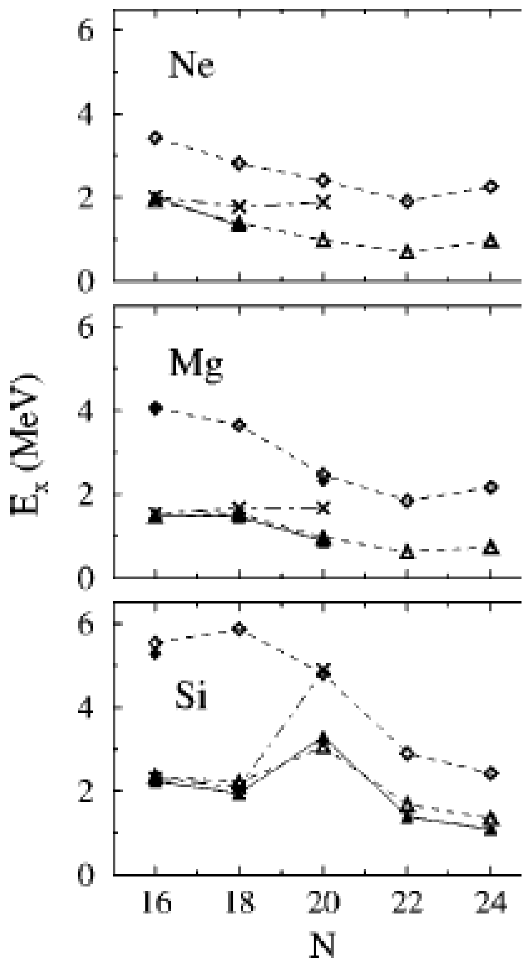
Degree of mixing between 0p0h and 2p2h configurations?

Unrestricted SM calculations in the sd + f7/2 and p3/2 shells

Quantum Monte-Carlo diagonalization based SM:

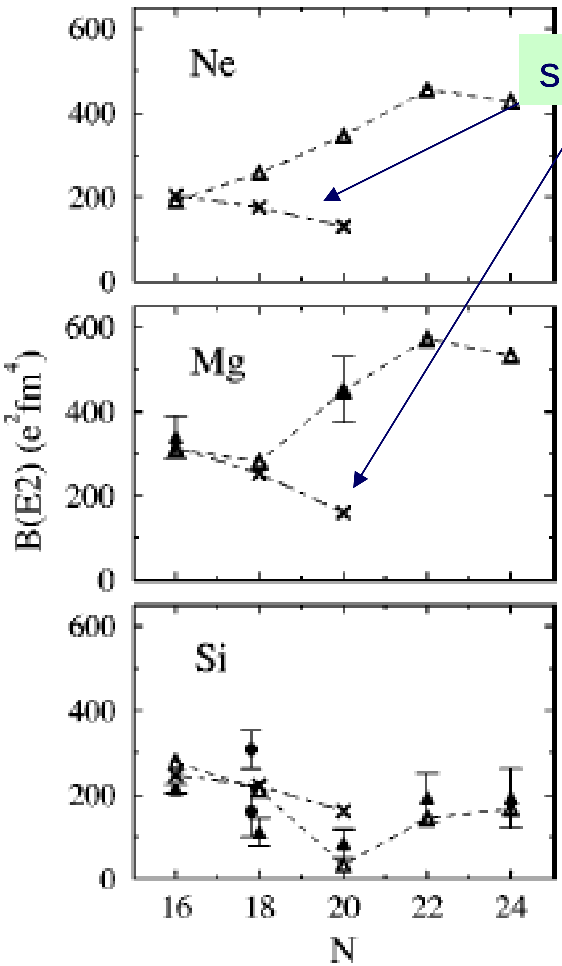
UTSUNO, OTSUKA, MIZUSAKI, AND HONMA
PHYSICAL REVIEW C **60** 054315

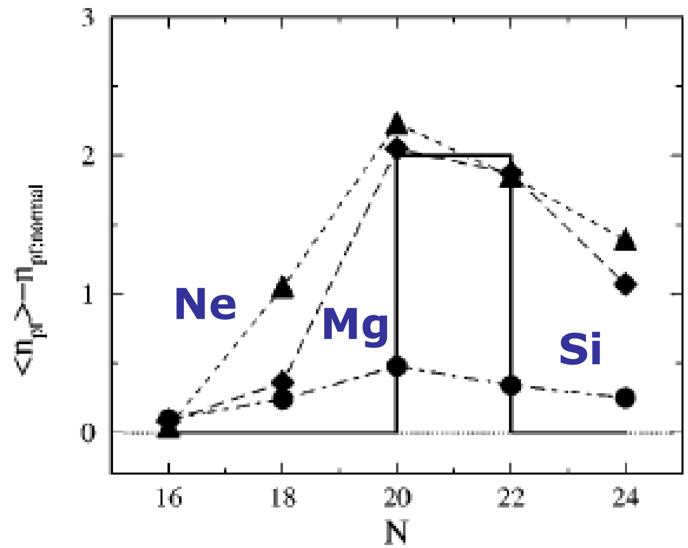
Yrast levels $0^+, 2^+, 4^+$



$B(E2; 0_1^+ \rightarrow 2_1^+)$

sd-shell only





Average number of neutrons in the pf-shell minus those in the normal configuration.

USD int. for the sd-shell

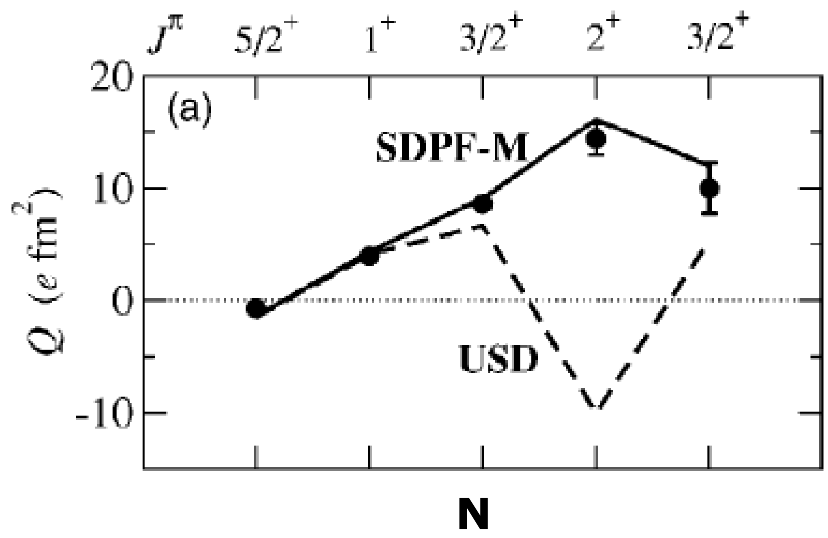
Kuo-Brown int. for the pf-shell

SDPF-M effective interaction

Modified Millener-Kurath int. for the cross-shell

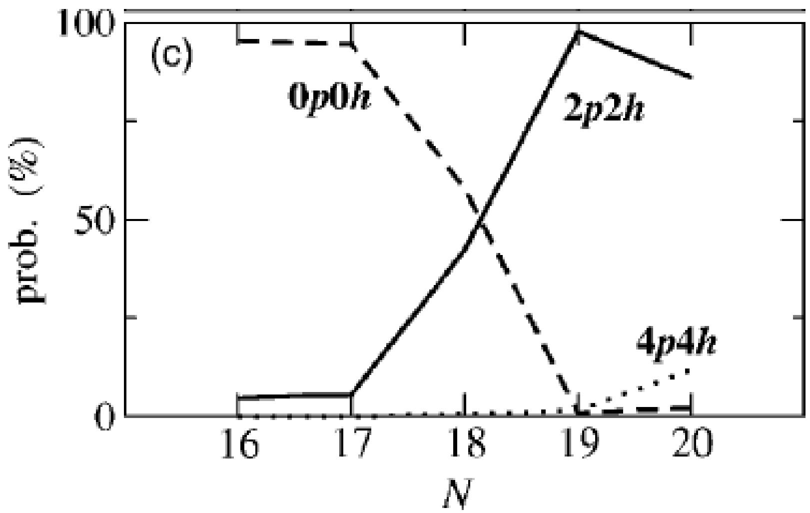
monopole shifts

Onset of intruder ground states in exotic Na isotopes

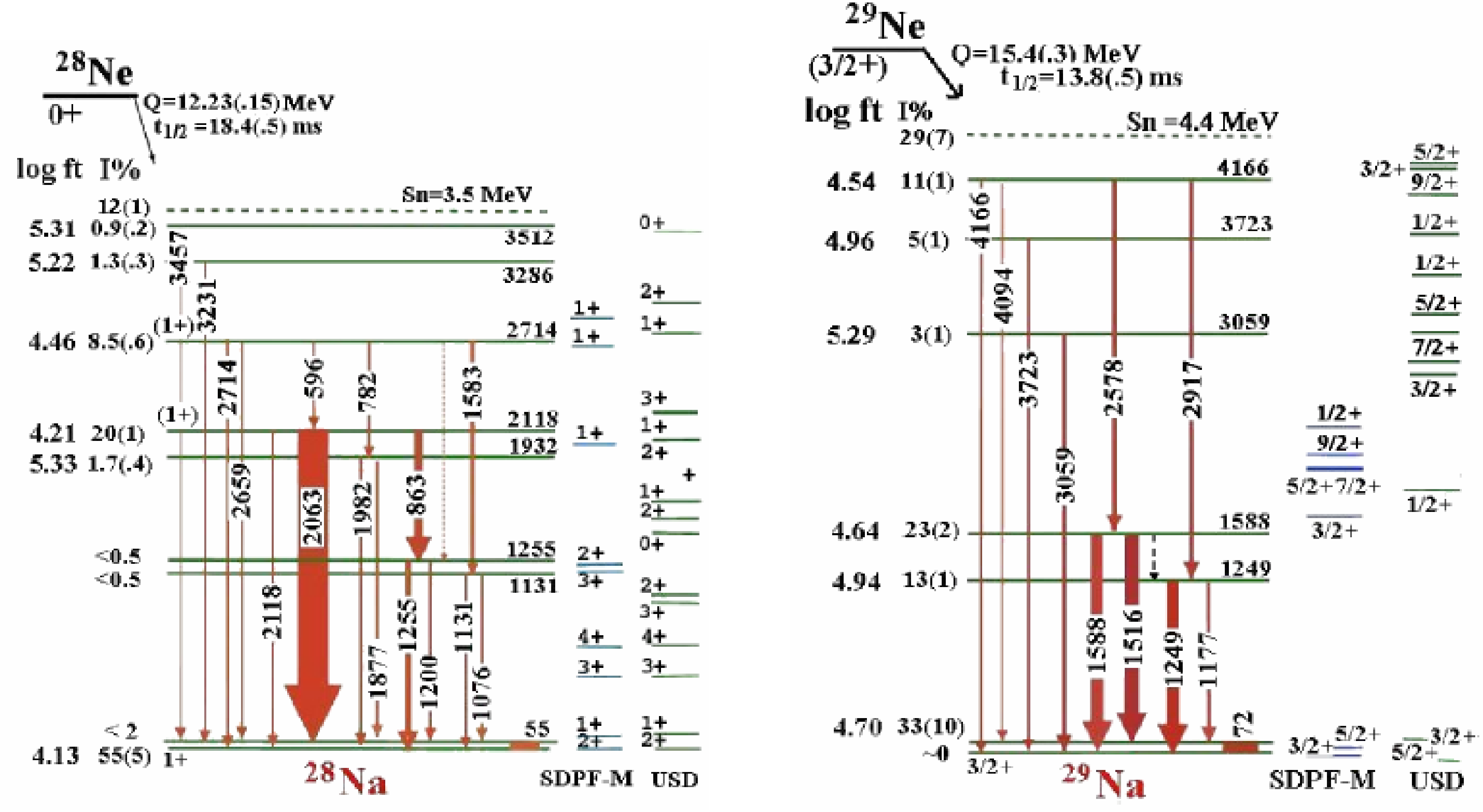


UTSUNO, OTSUKA, GLASMACHER, MIZUSAKI, AND HONMA
PHYSICAL REVIEW C 70, 044307 (2004)

The transition from normal to the intruder ground state: between N=18 and N=19.



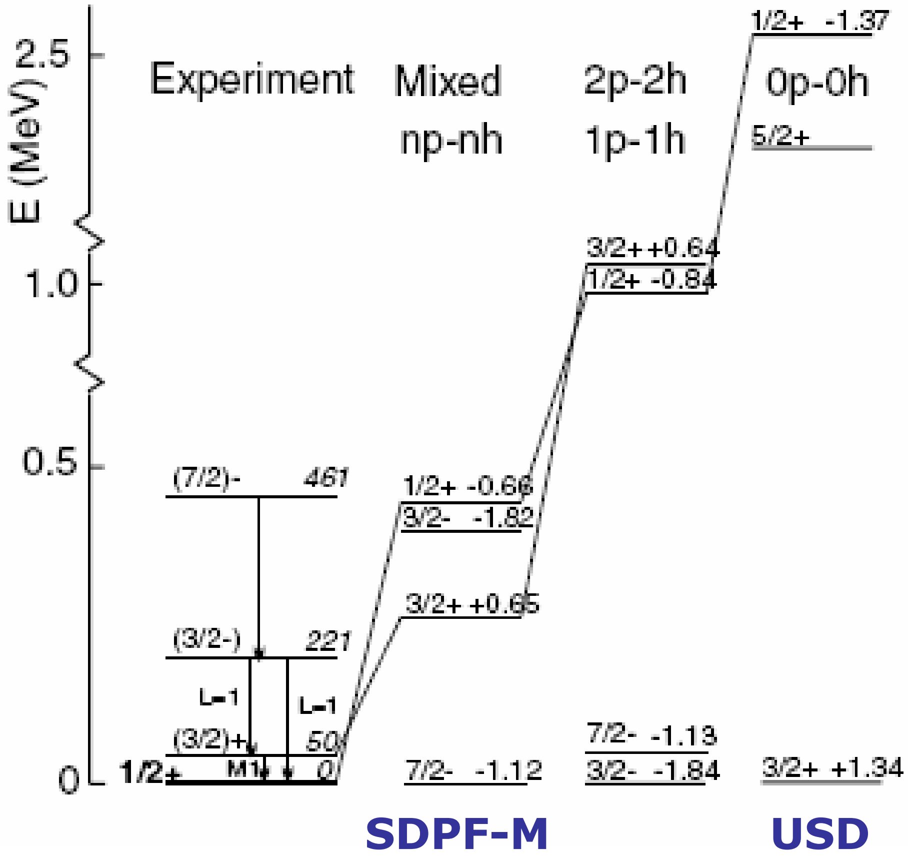
^{29}Na: Defining the Edge of the Island of Inversion for $Z=11$



PRL 94, 162501 (2005)

Measurement of the Spin and Magnetic Moment of ^{31}Mg: Evidence for a Strongly Deformed Intruder Ground State

PRL 94, 022501 (2005)



The calculations do not reproduce the correct ordering of intruder levels!

Large-scale shell-model calculation of the N=28 spin-orbit shell closure

USD for the proton-proton int.

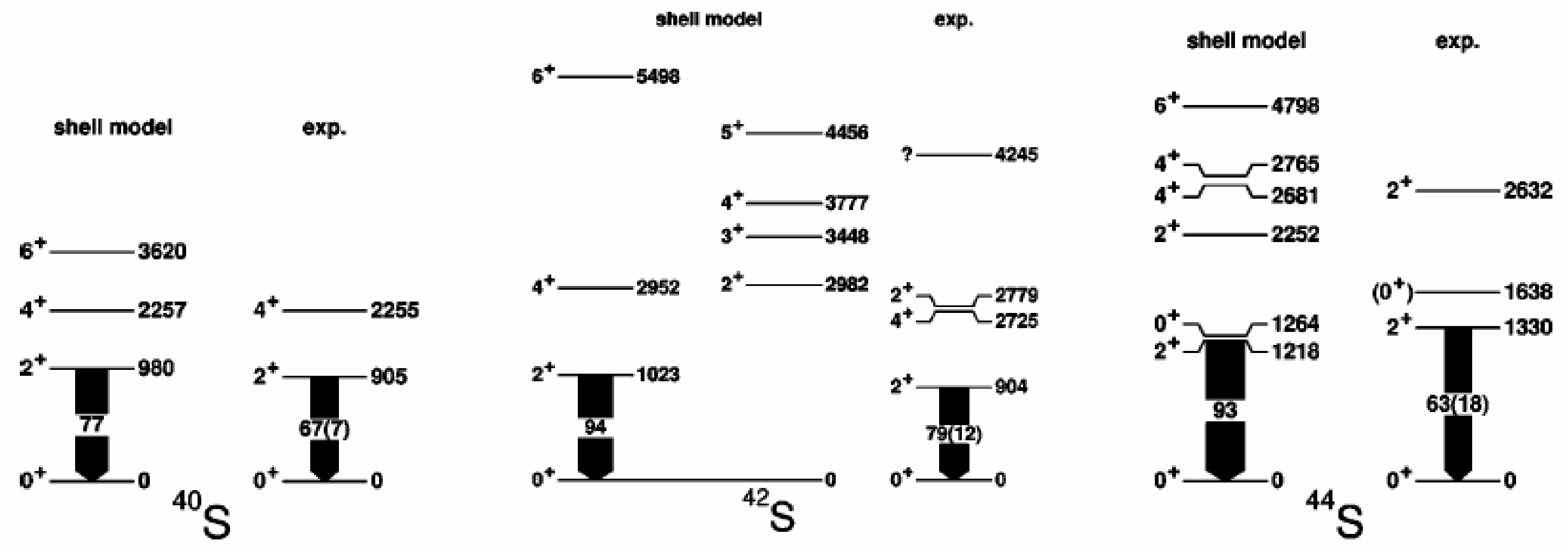
Kahana-Lee-Scott G-matrix for the cross-shell proton-neutron int.

SPDF-NR interaction

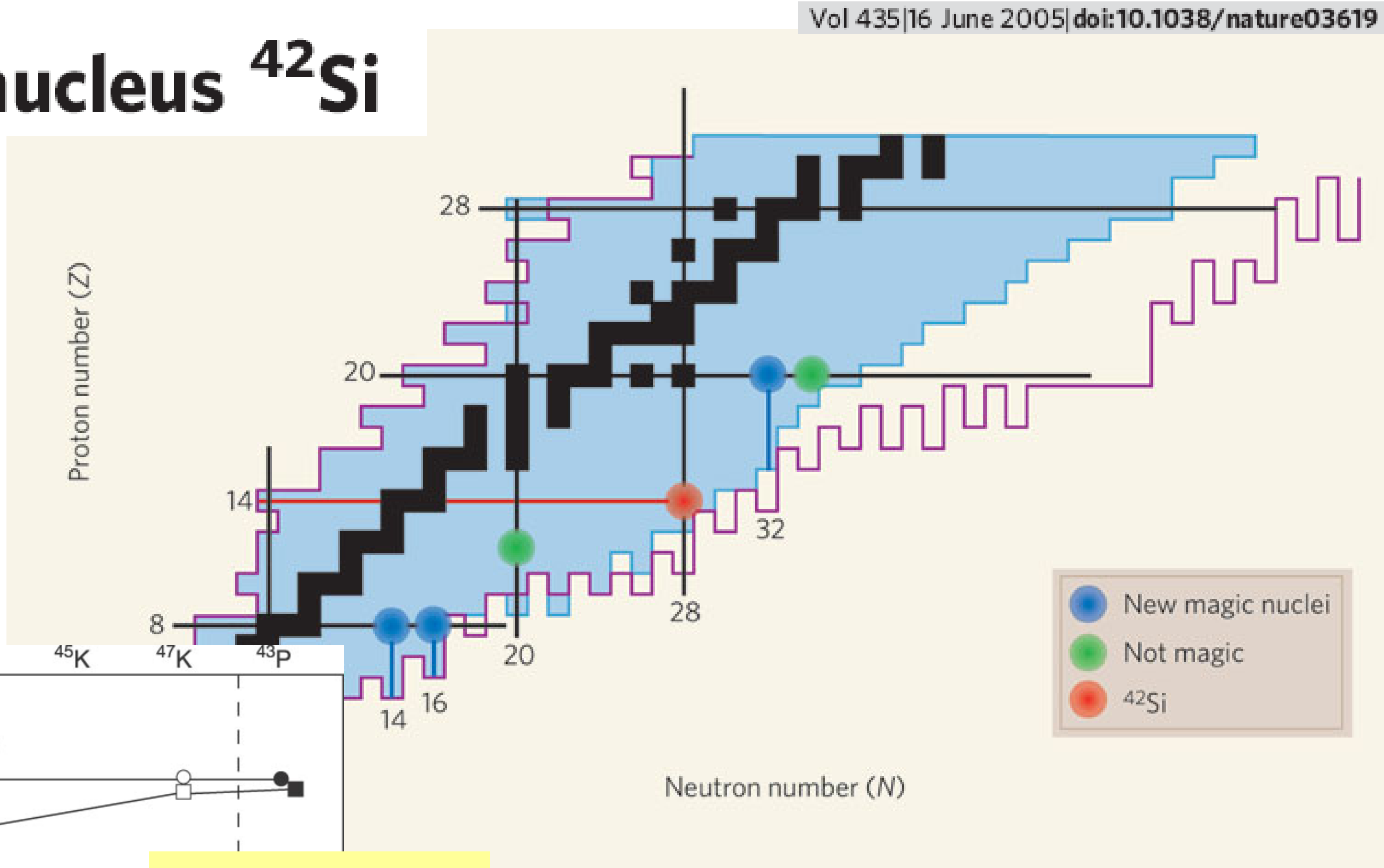
monopole adjustments

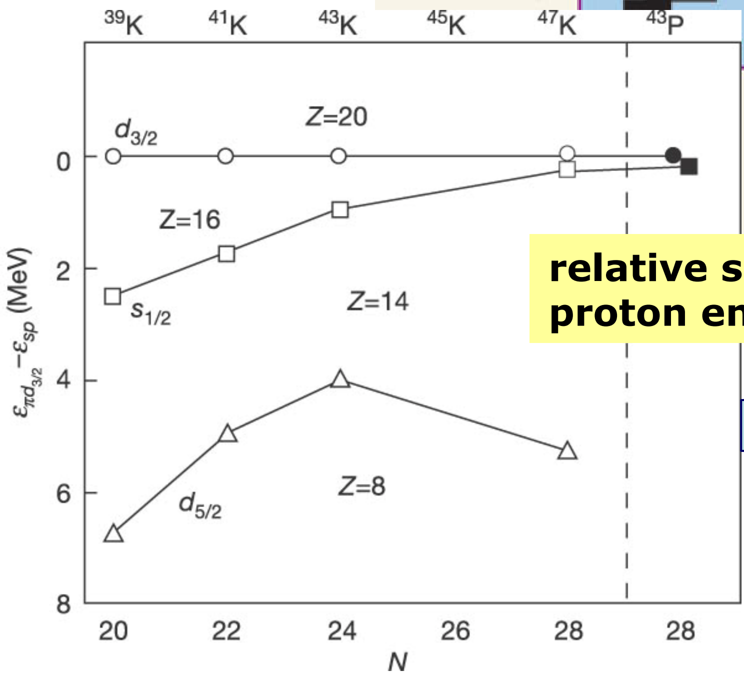
Kuo-Brown (modified) for the neutron-neutron int.

REVIEWS OF MODERN PHYSICS, VOLUME 77, APRIL 2005



'Magic' nucleus ^{42}Si





relative single proton energies

The magic number N=28 remains valid in this nucleus.
Proton shell closure at Z=14.

This Si isotope is doubly magic!

Microscopic description of weakly bound neutron-rich nuclei

consistent treatment of both the many-body correlations and the continuum of positive energy states and decay channels

GAMOW SHELL MODEL -> description of bound states and the particle continuum (resonances and the nonresonant scattering background).

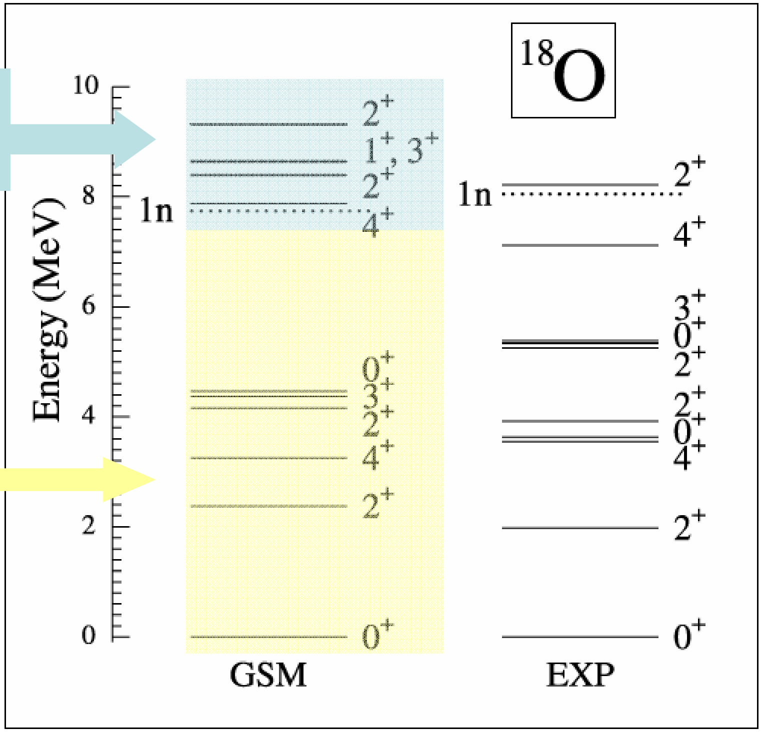
MICHEL, NAZAREWICZ, PŁOSZAJCZAK, AND OKOŁOWICZ

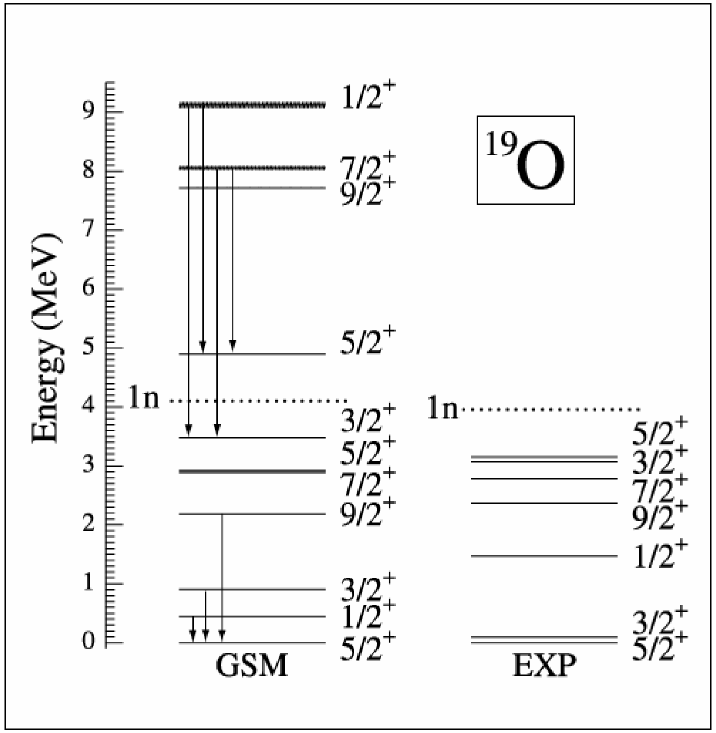
PHYSICAL REVIEW C 67, 054311 (2003)

Applications to systems with several valence neutrons!

resonant states

bound states





The shell model as a unified view of nuclear structure

REVIEWS OF MODERN PHYSICS, VOLUME 77, APRIL 2005

Problems:

-the effective interactions strongly depend on the choice of the configuration space (active shells and the truncation scheme): **there is no universal effective SM interaction that can be used for all nuclei!**

-the effective interactions are adjusted starting from microscopic two-body forces. **3-nucleon effects?**

-a large number of two-body matrix elements (10^2 – 10^3 ?) has to be adjusted to the data => **the effective interactions cannot be unique! Extrapolations to exotic nuclei not reliable!**

-nuclei very far from stability will require calculations with matrix dimension > 10^{10} => **far beyond the limits of current Shell Model variants!**

2. Evolution of shapes

High density of single-particle levels in medium-heavy and heavy nuclei

- -evolution of quadrupole collectivity
- -new regions of deformation: shape transitions and shape coexistence
- -nuclei with very diffuse neutron densities – neutron skin
- -exotic modes of collective excitations

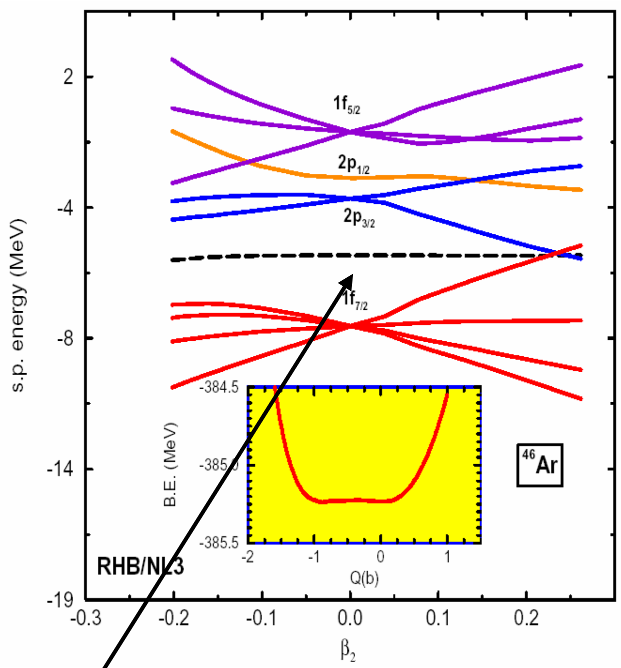
Self-consistent mean-field methods:

- -use of global effective nuclear interactions
- -description of arbitrarily heavy systems
- -intuitive picture of intrinsic shapes

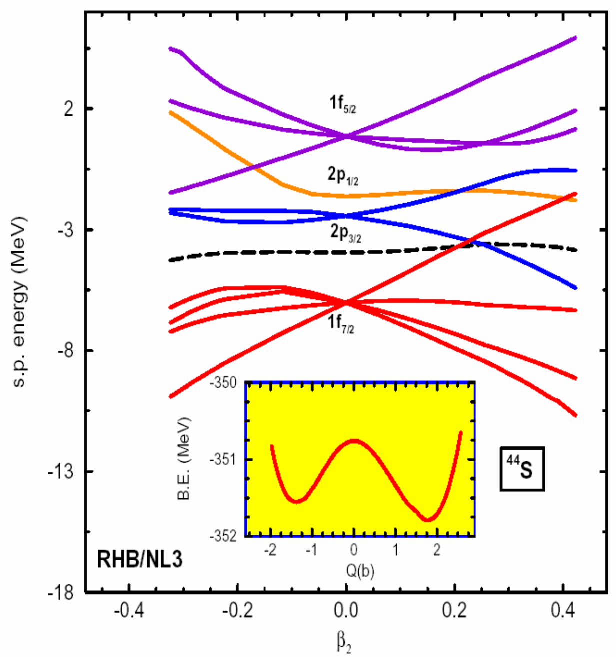
Non-relativistic HF/HFB based on Skyrme and Gogny interactions

Relativistic MF/HB finite-range meson-exhange and point-coupling models

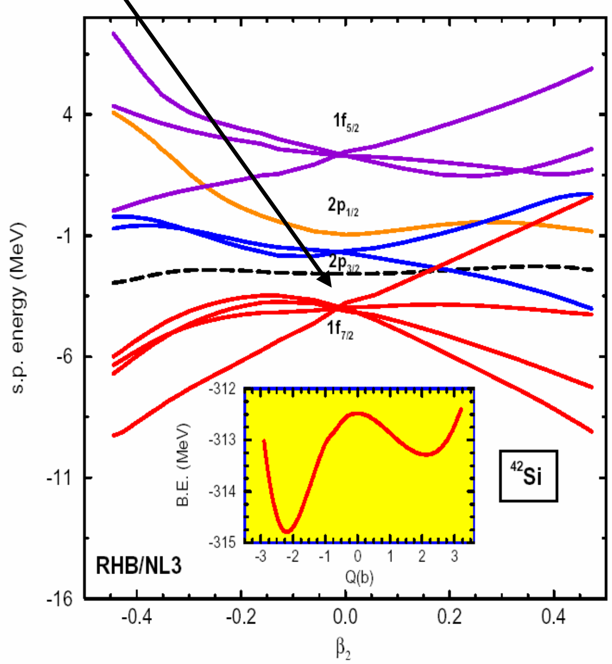
Neutron single-particle levels for ^{42}Si, ^{44}S, and ^{46}Ar (N=28) as functions of the quadrupole deformation (RHB/NL3 calculation).



large spherical gap



small spherical gap



For a quantitative description of shape transitions and shape coexistence => include correlations:

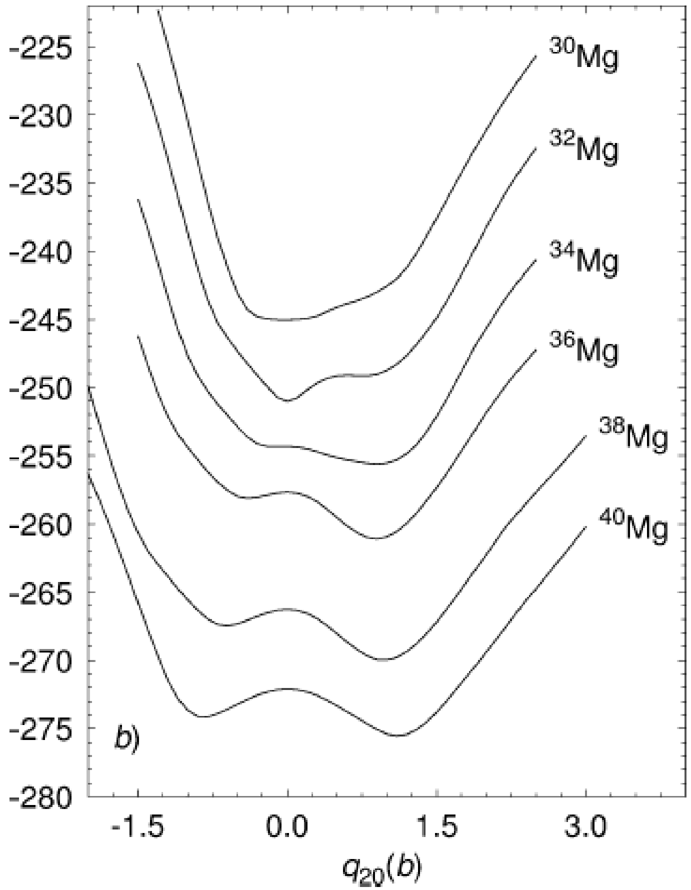
-angular momentum projection (rotational energy)
-quadrupole fluctuations (configuration mixing)
-particle number projection

...

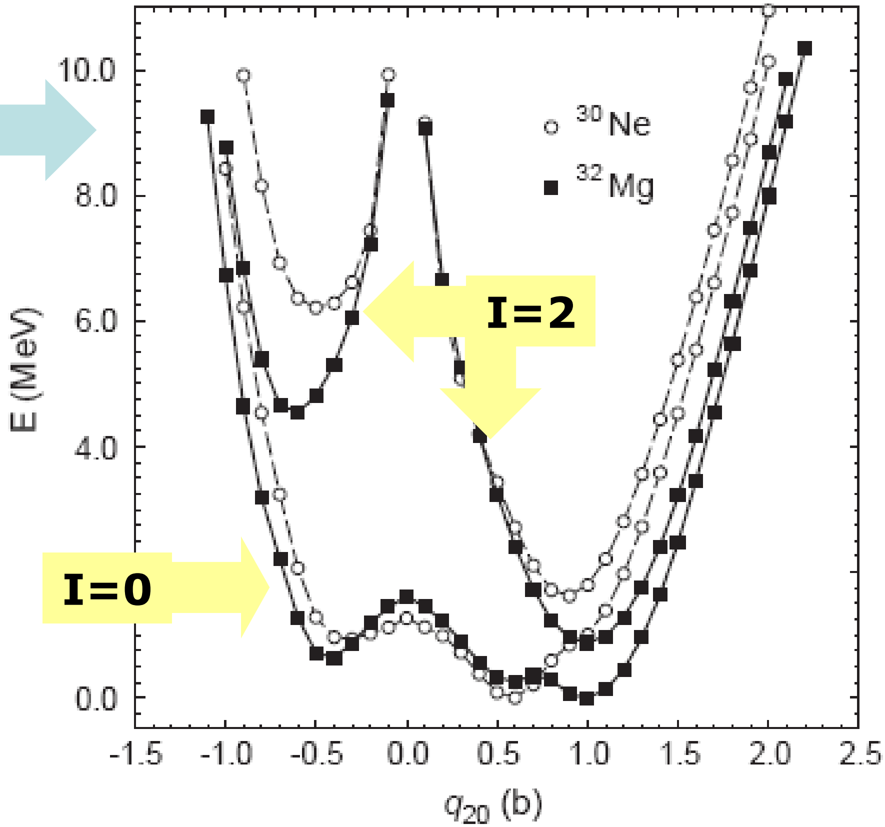
CORRELATIONS BEYOND MEAN-FIELD IN Mg NUCLEI

angular momentum projection and configuration mixing

HFB mean-field PES Gogny D1S interaction



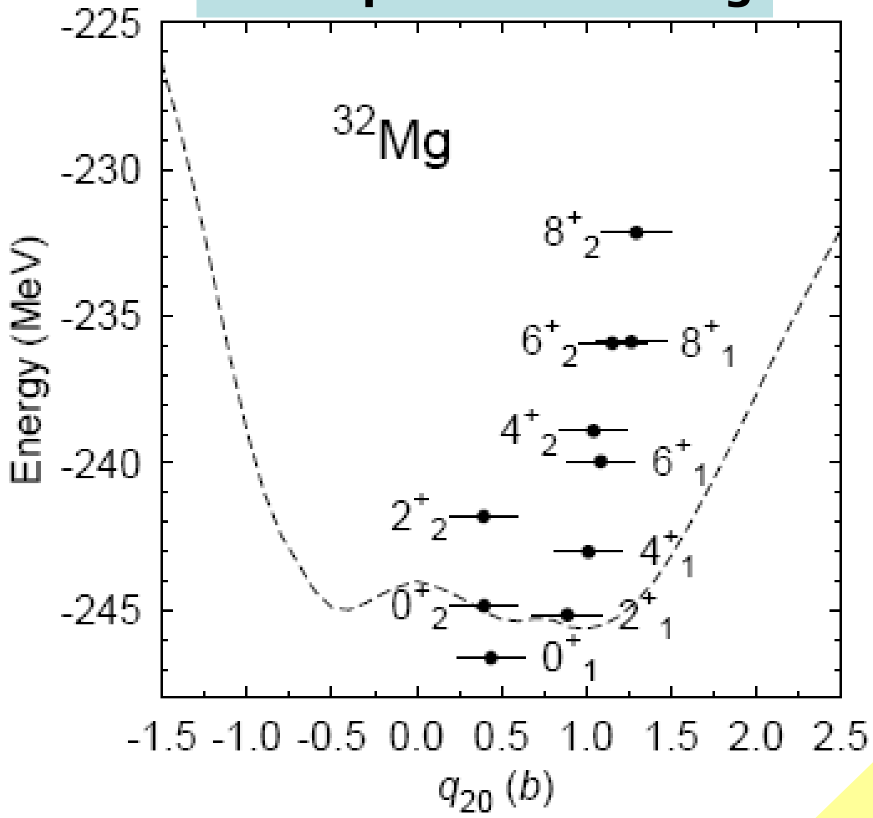
Nuclear Physics A 709 (2002) 201–235



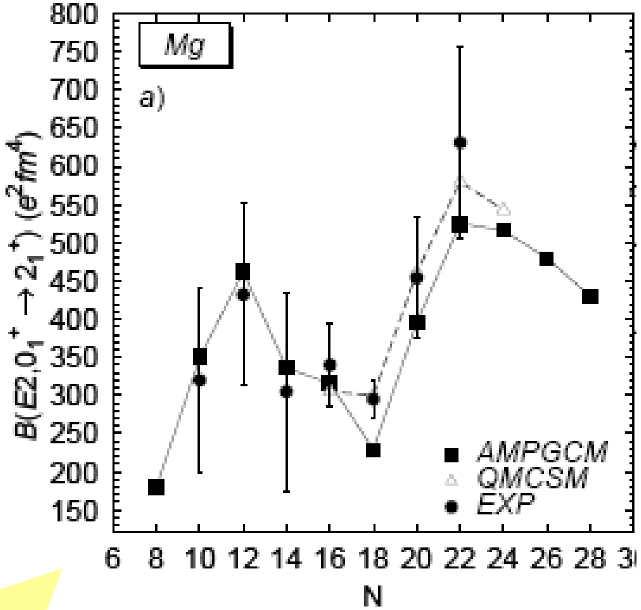
Small energy differences between coexisting minima: correlation effects beyond the mean-field level are important!

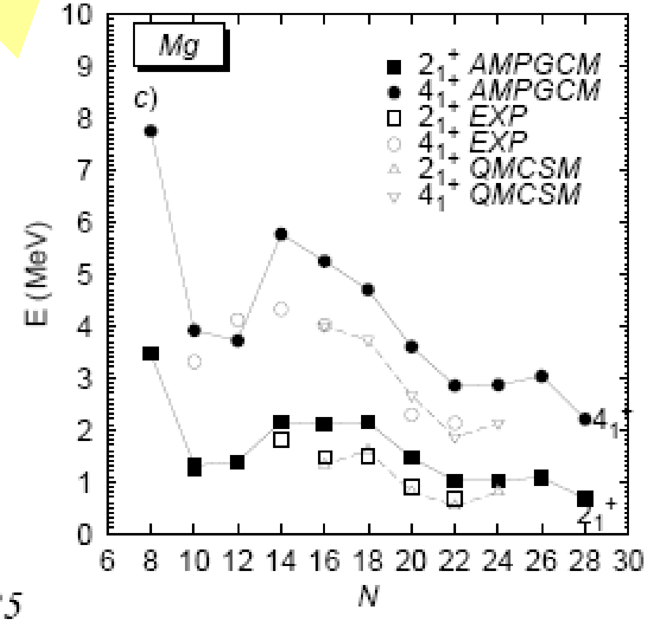
Angular momentum projected potential energy surfaces.

GCM spectrum of ^{32}Mg



B(E2, 0_1^+ -> 2_1^+) in $^{20\text{-}40}$Mg





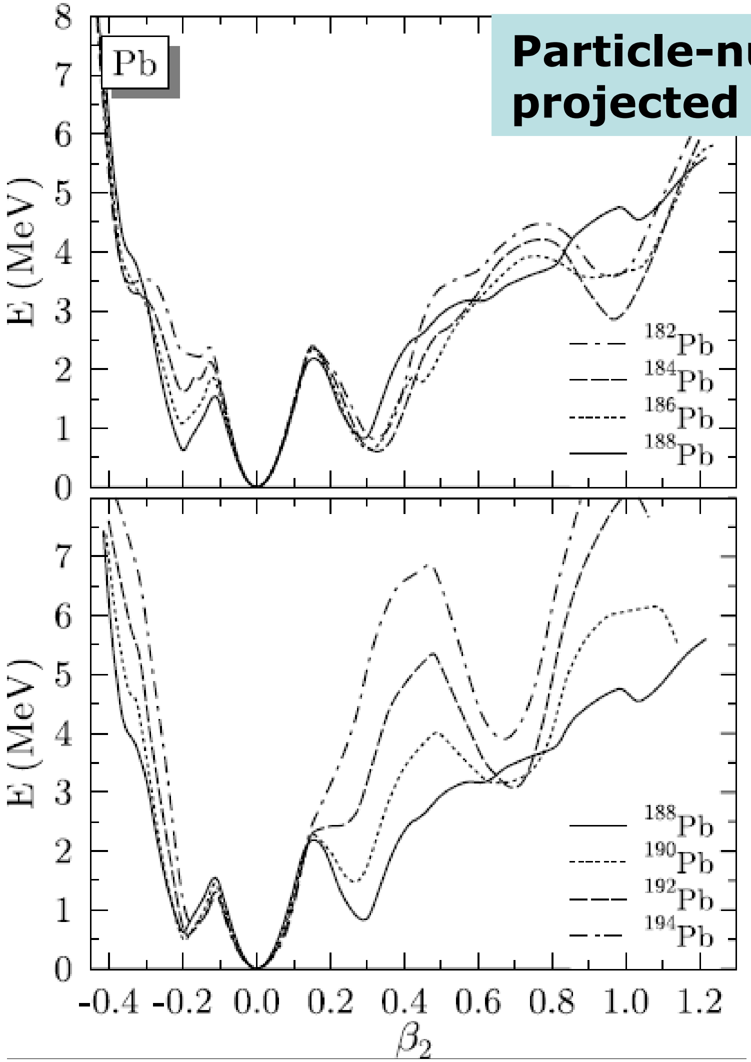
Good agreement with exp. data and QMCSM calculations.

The effective interaction (Gogny) has not been adjusted to this mass region!
No effective charges in the calculation of transition probabilities!

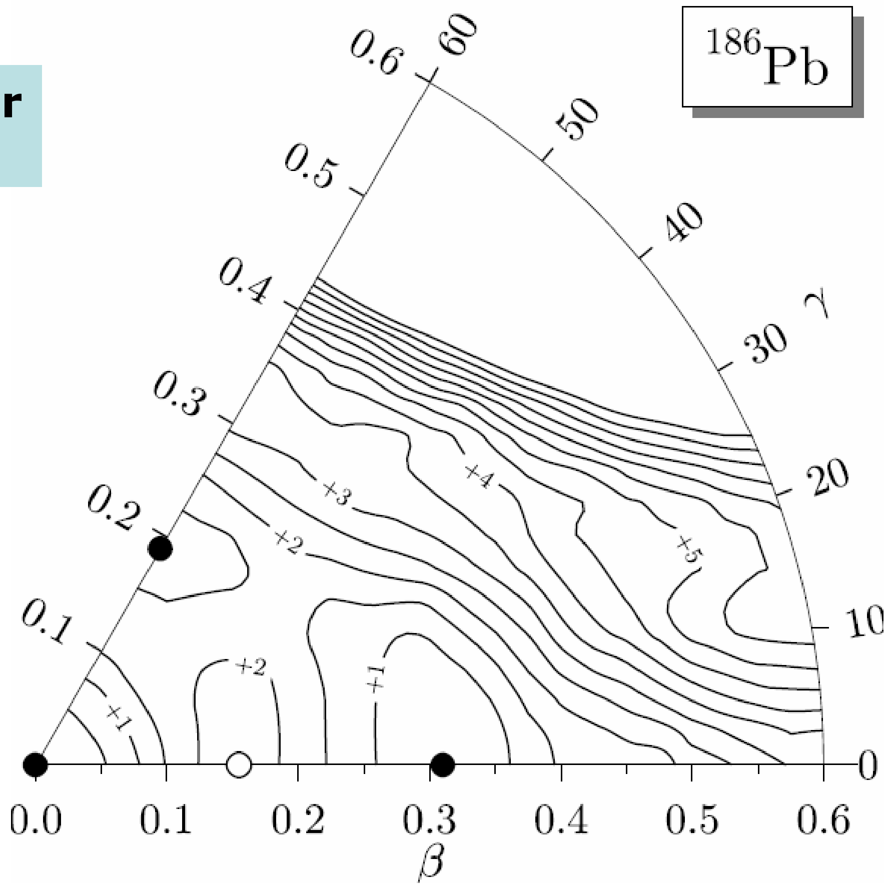
R. Rodríguez-Guzmán et al. / Nuclear Physics A 709 (2002) 201–235

SHAPE COEXISTENCE IN NEUTRON-DEFICIENT Pb ISOTOPES

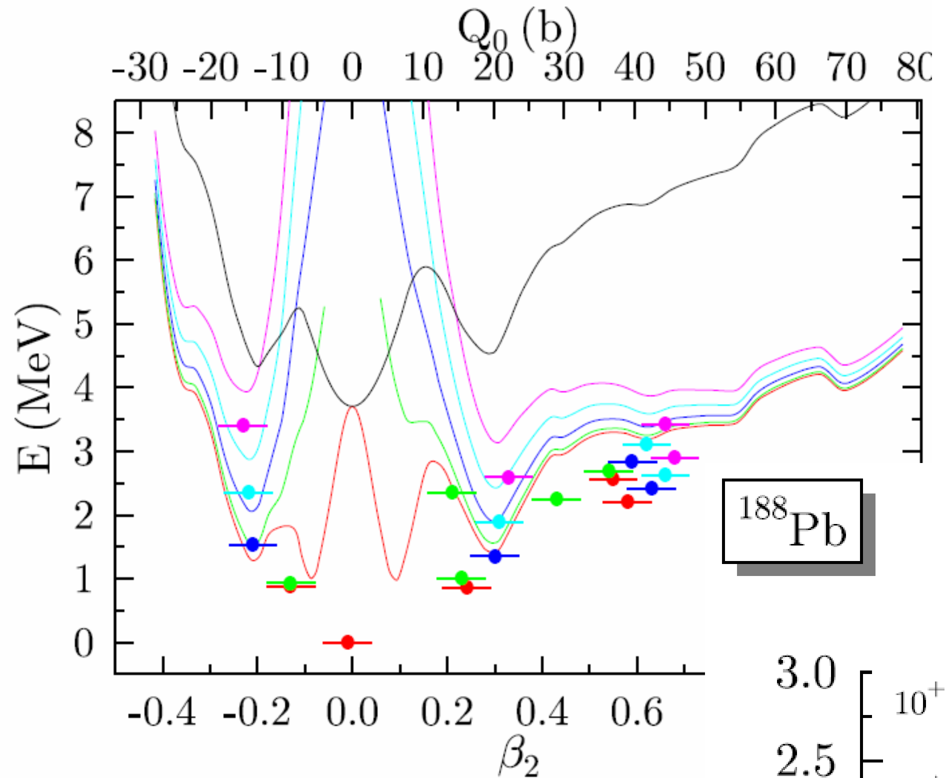
GCM configuration mixing of angular-momentum and particle-number projected self-consistent HF+BCS states. Skyrme SLy6 interaction. Density-dependent zero-range pairing.



Particle-number projected PES.

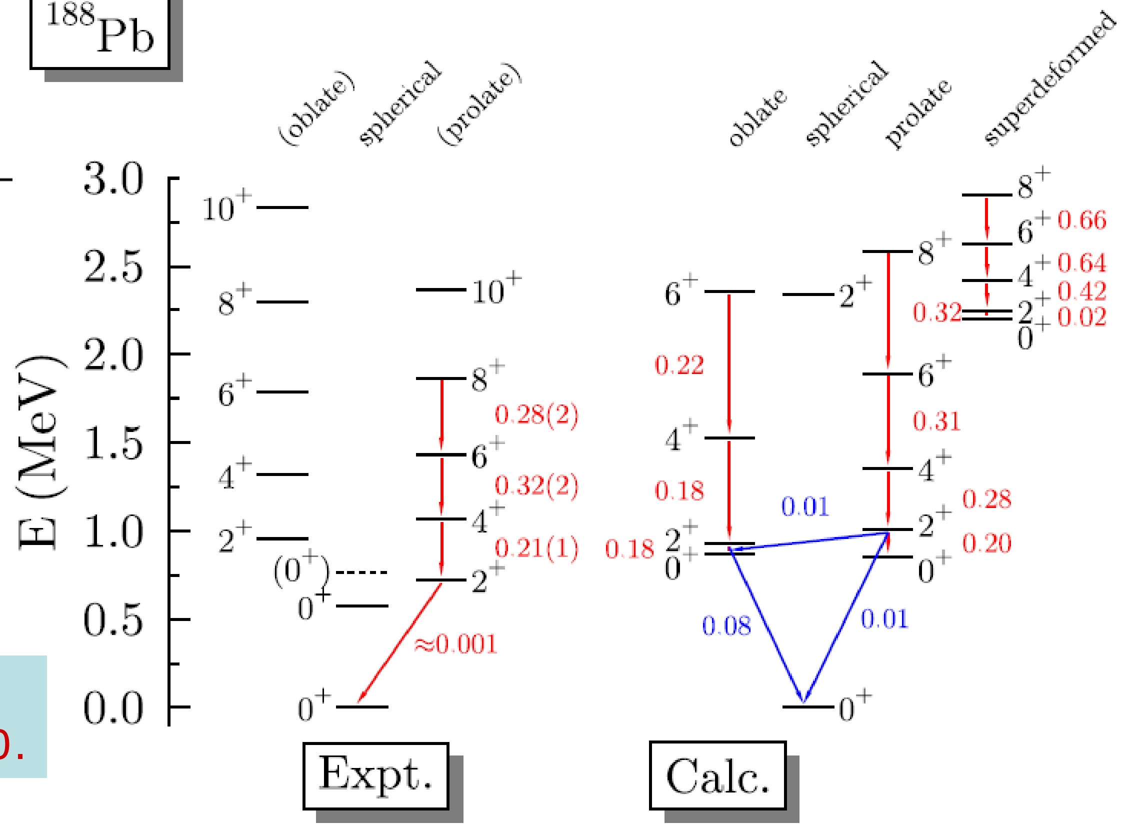


Unique example of a fermion system with the two lowest excited levels being 0^+ states!



Particle-number and angular-momentum projected PES for I=0$^+$, 2$^+$, 4$^+$, 6$^+$, 8$^+$.

PHYSICAL REVIEW C **69**, 064303 (2004)



GCM spectrum of the lowest positive parity bands with K=0.

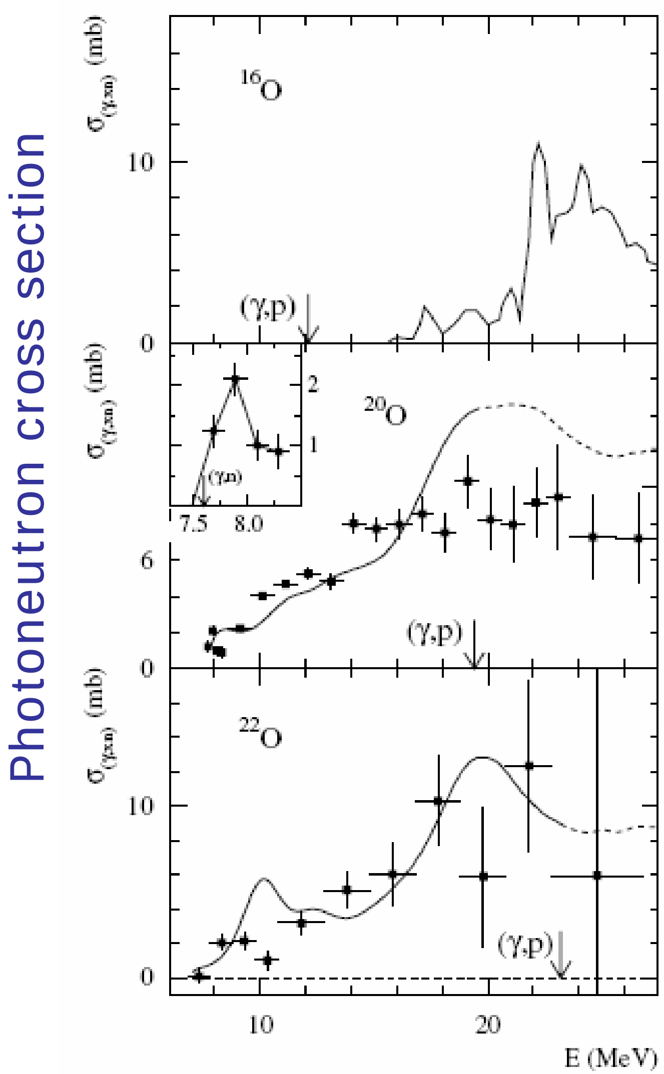
M. BENDER, P. BONCHE, T. DUGUET, AND P.-H. HEENEN

3. Evolution of low-lying collective modes

Low-lying dipole strength in neutron-rich nuclei

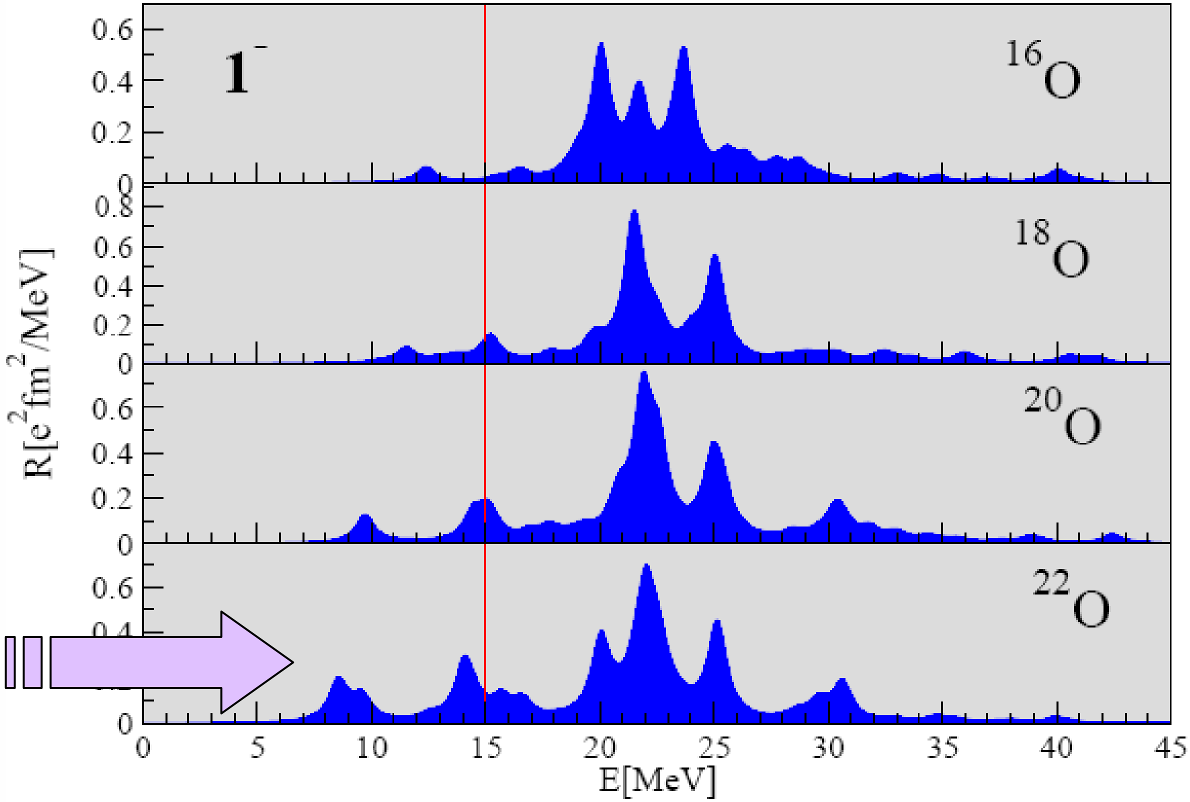
Evolution of low-lying E1 strength in oxygen isotopes

Phys. Rev. Lett. 86, 5442 (2001)



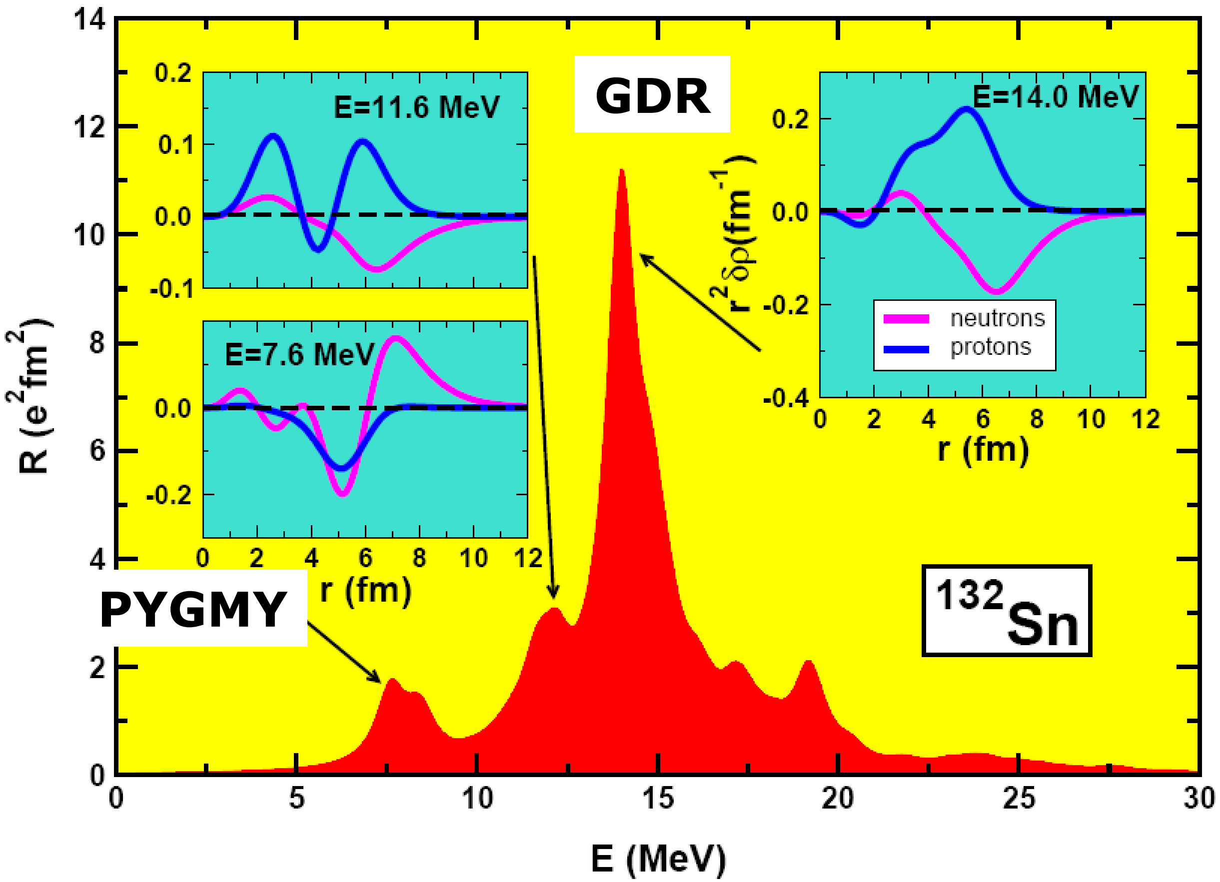
What is the structure of the low-lying strength below 15 MeV ?

The dipole strength in the low-energy region is caused by non-resonant independent single particle excitations of the loosely bound neutrons!



Evolution of isovector dipole strength in Sn isotopes

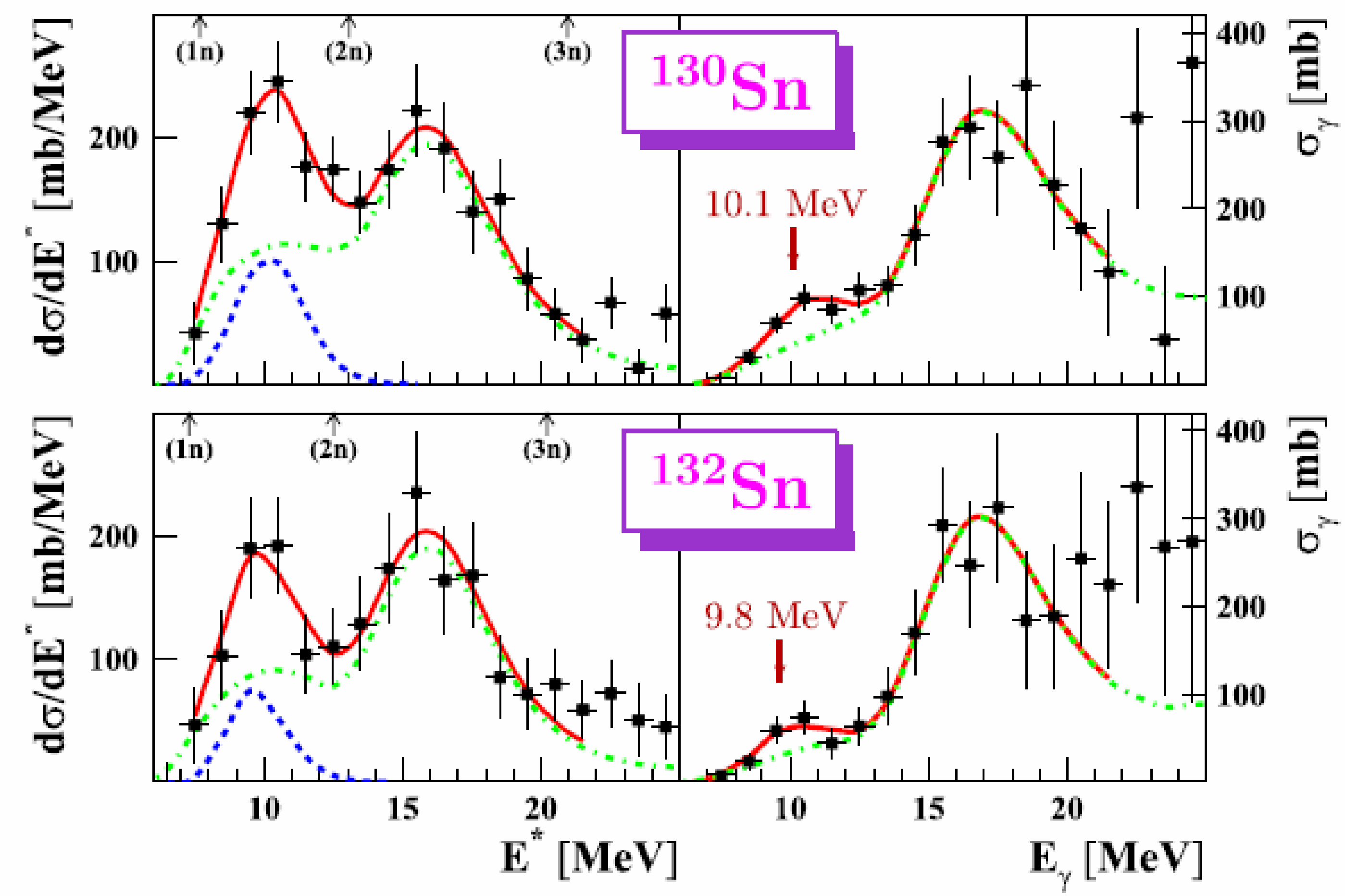
In heavier nuclei low-lying dipole states appear that are characterized by a more distributed structure of the QRPA amplitude.



Among several single-particle transitions, a single collective dipole state is found below 10 MeV and its amplitude represents a coherent superposition of many neutron particle-hole configurations → **PYGMY RESONANCE**

Evidence for Pygmy and Giant Dipole Resonances in ^{130}Sn and ^{132}Sn

P. Adrich *et al.* (LAND-FRS Collaboration) Phys. Rev. Lett. 95, 132501 (2005)

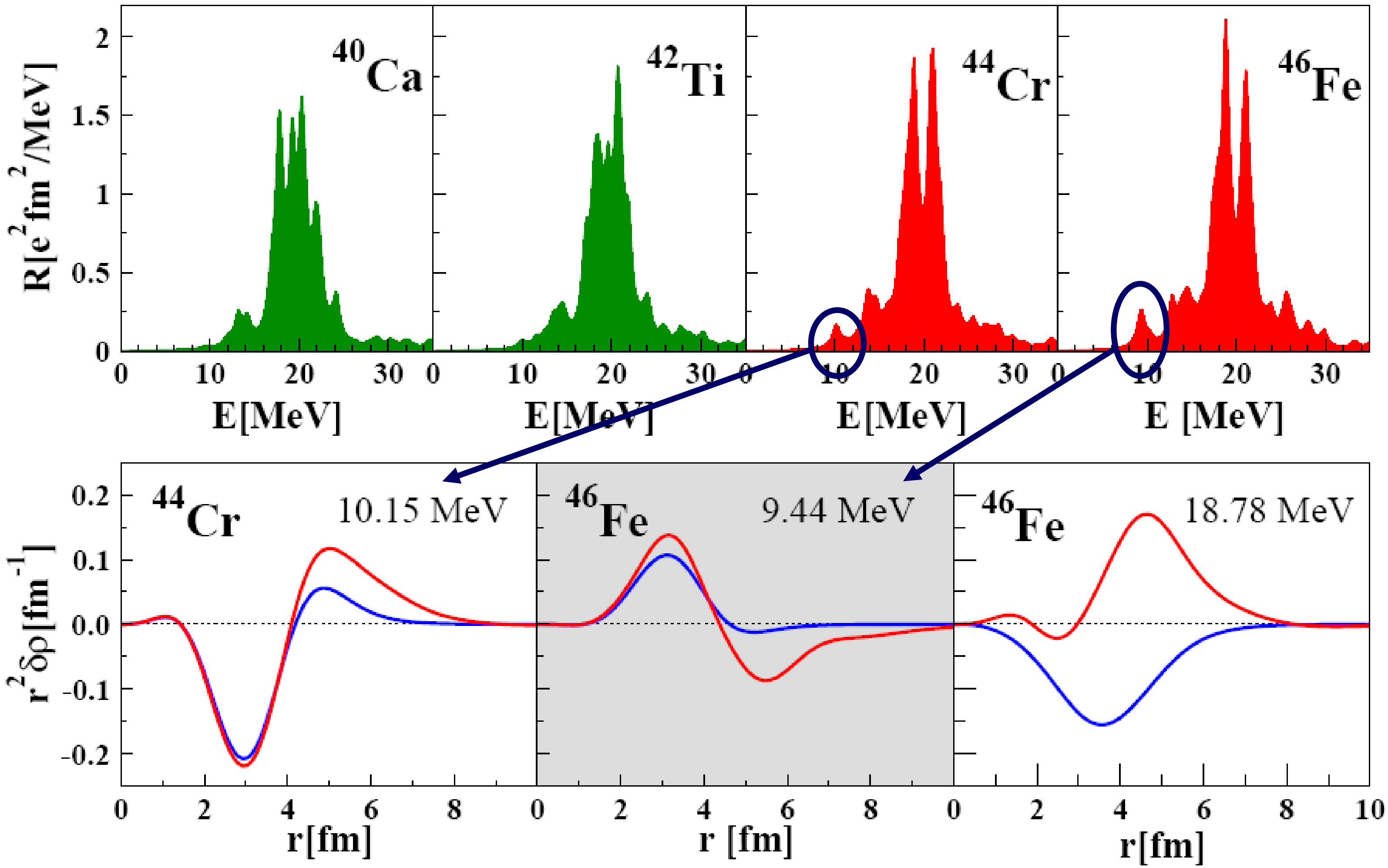


Energy differential electromagnetic dissociation cross section measured in $^{130,132}Sn$.	Deduced photo-neutron cross section.

Evolution of low-lying E1 strength in proton-rich nuclei

Paar, Vretenar, Ring, Phys. Rev. Lett. 94, 182501 (2005)

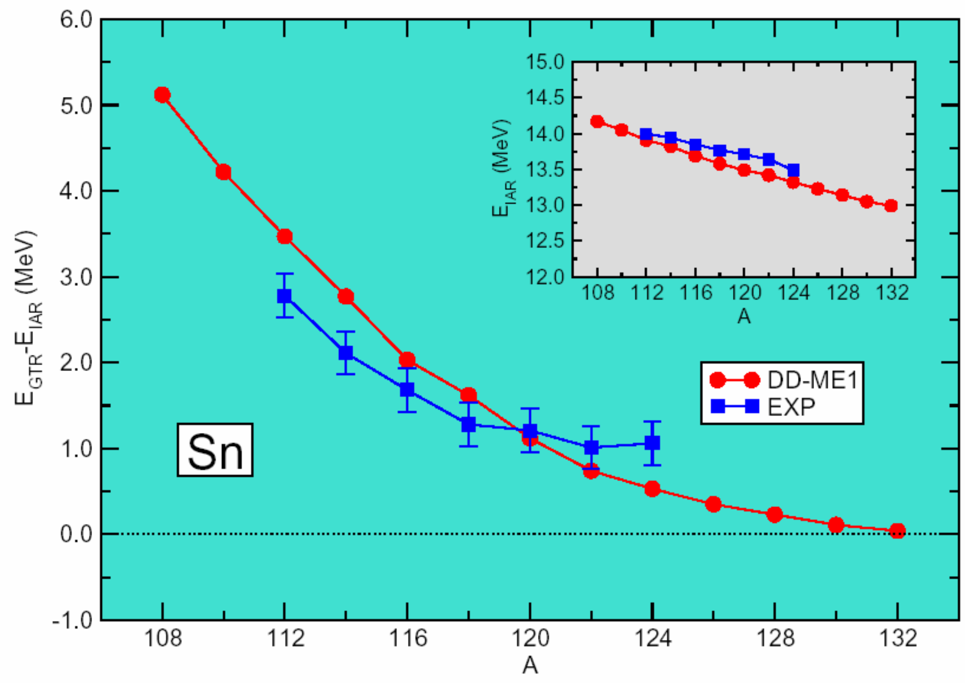
RHB+RQRPA isovector dipole strength distribution in the N=20 isotones.
DD-ME1 effective interaction + Gogny pairing.

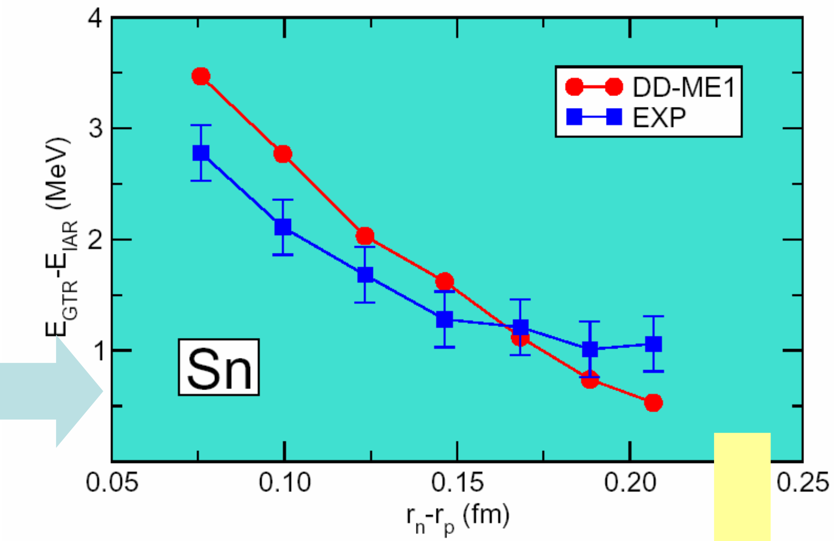


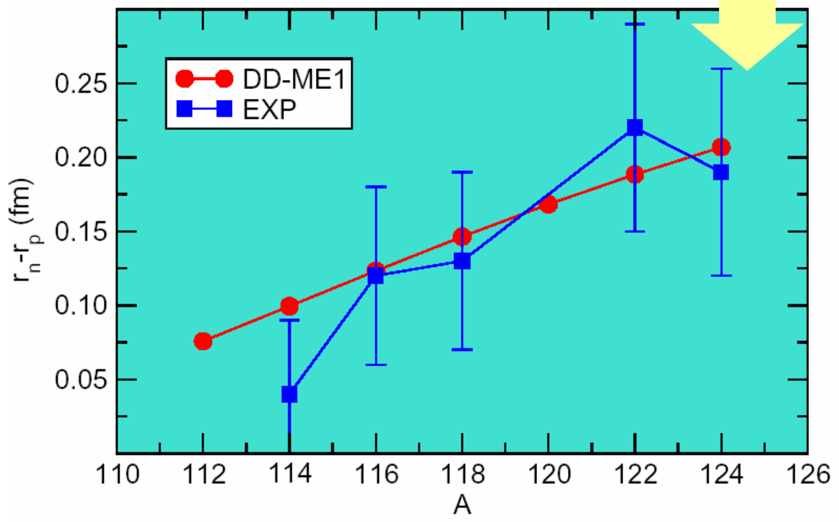
Spin-Isospin Resonances and the Neutron Skin of Nuclei

The isotopic dependence of the energy spacings between the GTR and IAS

Proton-neutron RQRPA calculation







Information on the evolution of the neutron skin thickness along the Sn isotopic chain.

D. Vretenar, N. Paar, T. Nikšić, and P. Ring, Phys. Rev. Lett. **91**, 262502 (2003).

Modern Nuclear Structure Theory:

Unified microscopic description of structure and reactions for nuclei far from stability and reliable extrapolations toward the drip lines.

Microscopic global predictions for astrophysical applications: characteristics of strong, electromagnetic and weak interaction processes.

Next generation universal energy density functionals and effective shell model interactions -> based on the EFT representation of low-energy QCD.

Stringent constraints on the microscopic approach to nuclear dynamics, effective nuclear interactions, and nuclear energy density functionals, are obtained from studies of the structure and stability of exotic nuclei with extreme isospin values.