

# Small- $x$ and heavy flavor effects in $Z/W/H$ production at Tevatron and LHC

Small  $x$ : S. B., P. Nadolsky, F. Olness, C.-P. Yuan, hep-ph/0410375

Heavy flavor: S. B., P. Nadolsky, F. Olness (paper in preparation)

Stefan Berge, SMU, Dallas, TX

TeV4LHC, 29 April '05, CERN

1. Introduction
2. Small- $x$  effects in  $W/Z/H$  production
3. Heavy Flavor effects in  $W/Z/H$  production
4. Conclusion

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Small- $x$  grid files for  $W$  and  $Z^0$  boson production at Tevatron Run II can be downloaded from:

<http://hep.pa.msu.edu/people/nadolsky/ResBos/grids/tev1960/rap/>

[www.physics.smu.edu/~berge/small-x/](http://www.physics.smu.edu/~berge/small-x/)

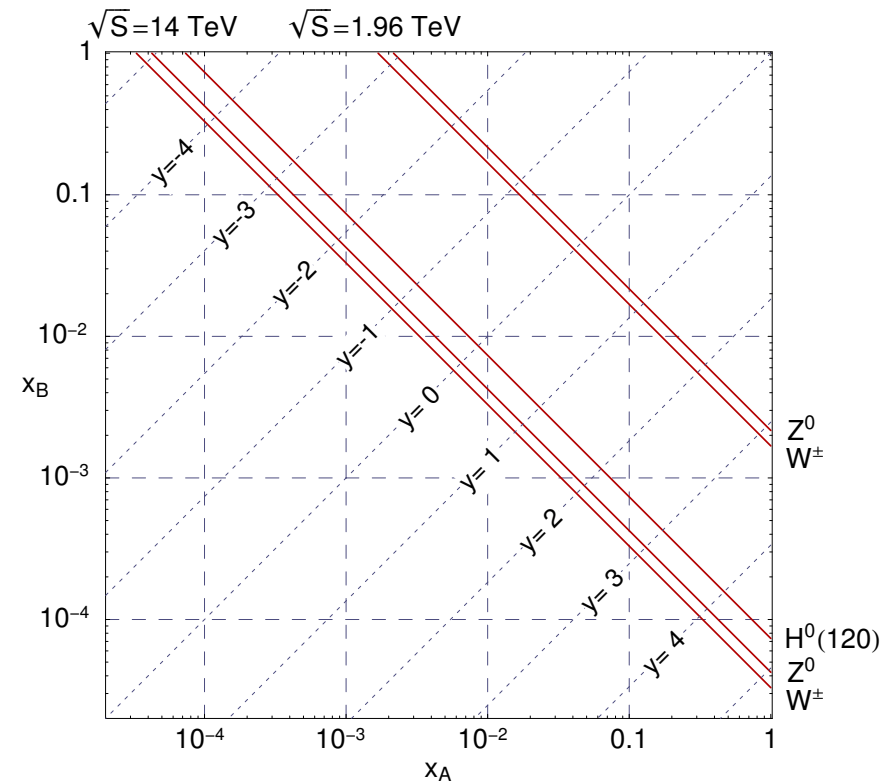
# 1. Introduction

Want to measure boson production ( $Z/W^\pm/H$ ) at Tevatron and LHC:

i) E.g. Measurement of  $W$ -boson mass  $M_W$  and width  $\Gamma_W$  in  $pp/p\bar{p} \rightarrow WX \rightarrow l\nu X$

Important for precision tests of SM

- ✓ Consistency between different experiments and SM
- ✓ Together with Top quark mass, constraint on Higgs boson mass



Tevatron Run-2 goal: reduce  $\delta M_W$  to **30 MeV** (present error 59 MeV)

LHC goal:  $\delta M_W \simeq 15 \text{ MeV}$

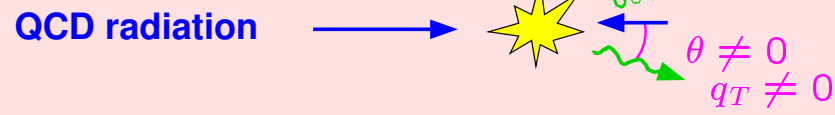
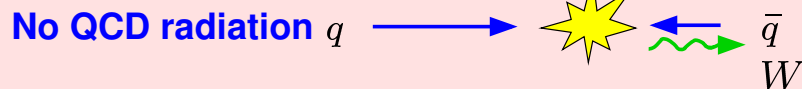
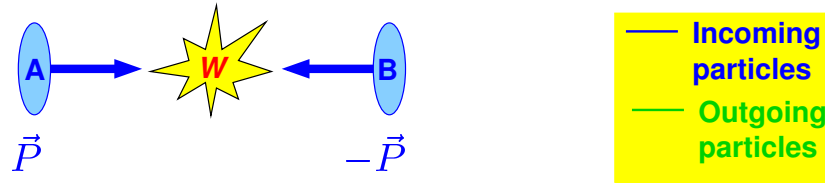
How is such accuracy achieved given that the  $W$ -bosons are not observed directly

1. Measure the lepton transverse mass distribution
2. Measure  $d\sigma/dq_T^l$ -distribution  $\rightarrow$  determine  $p_T$  distribution for  $W$ -bosons

ii) Need consistent theoretical predictions for small  $x$  ( $5 \cdot 10^{-4} \leq x \leq 0.01$ )

# 1. Introduction

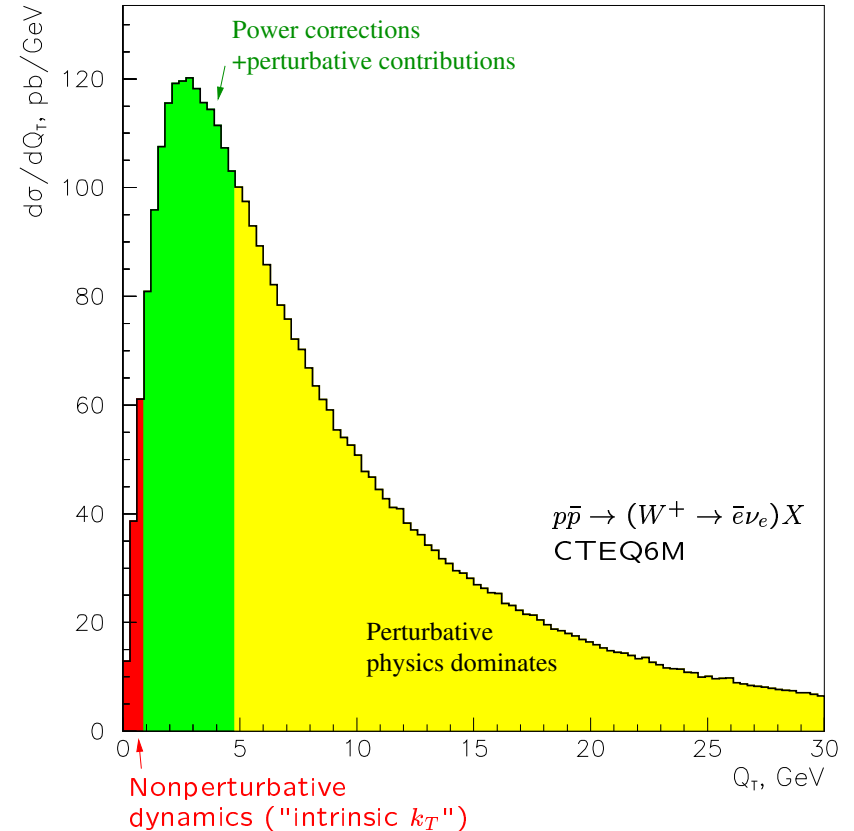
## Vector boson production at hadron-hadron colliders



$\rightarrow z$

Resummation needed to describes the whole  $q_T$  range

Important to precisely measure  $W$ -boson mass



NLO; calculated using ResBos (Balazs, Nadolsky, Yuan)

## 2. Semi-inclusive DIS

2000: Nadolsky, Stump, Yuan, hep-ph/0012261

Analysed semi-inclusive production of hadronic final states. Transverse energy flow using the CSS (Collins, Soper, Sterman, 1985) formalism:

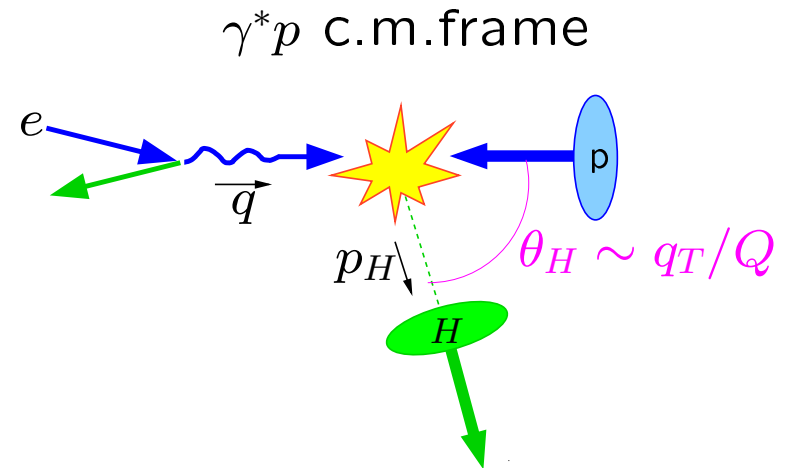
$$\frac{d\Sigma_z}{dx dQ^2 dq_T^2} = \int_0^\infty \frac{bdb}{2\pi} J_0(q_T b) \widetilde{W}_z(b, Q, x) + Y_z(q_T, Q, x).$$

using the  $b_*$  prescription:

$$\widetilde{W}_z(b, Q, x) = \frac{\pi}{S_{eA}} \sum_{j=u,\bar{u},\dots} \sigma_j^{(0)} C_z^{out}(b_*) \overline{\mathcal{P}}_j^{(S)}(x, b) e^{-S_P(b_*, Q) - S_{NP}(b, Q, x; b_*)}$$

$S(b, Q)$ : soft (Sudakov) factor

$$\overline{\mathcal{P}}_j^{(S)}(x, b) = \left[ C_{j/a}^{in(S)} \otimes f_a \right] (x, b_*): b\text{-dependent parton distribution}$$



## 2. Semi-inclusive DIS

2000: Nadolsky, Stump, Yuan, hep-ph/0012261

From the fit of the  $\mathcal{O}(\alpha_s)$  resummed z-flow to the Hera H1 data:

→ small-x behaviour is only consistent with the data if an  $q_T$ -broadening factor

$$\sim \exp\left\{-c_0 \frac{b^2}{x^p}\right\}$$

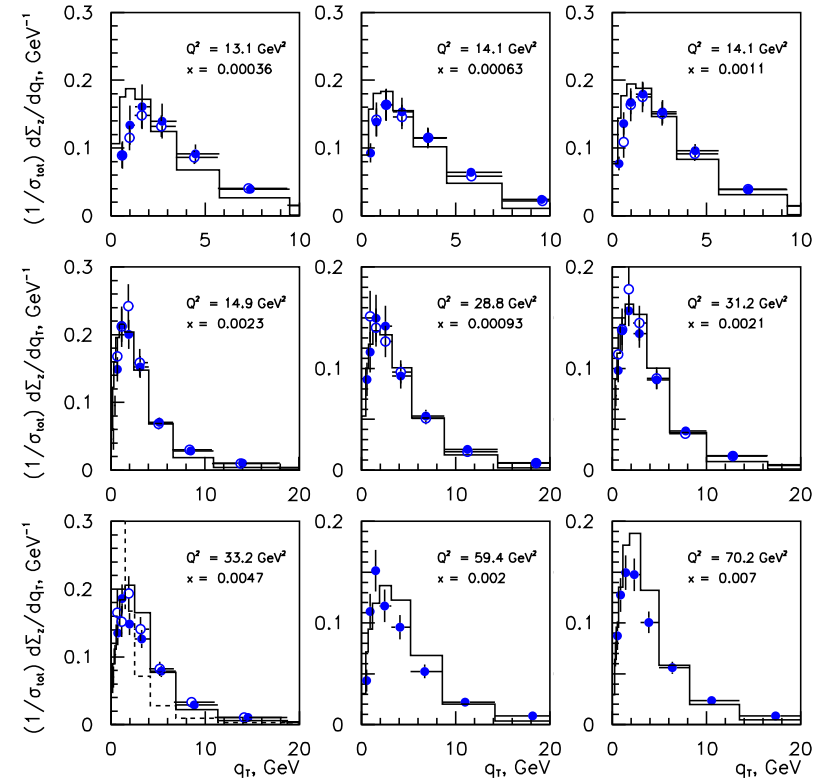
was introduced. Best fit for  $p=1$  and  $c_0 = 0.013$ .  
Identify:

$$\overline{\mathcal{P}}_j^{(S)}(x, b) = \left[ \mathcal{C}_{j/a}^{in(S)} \otimes f_a \right] (x, b_*) e^{-0.013 \frac{b^2}{x}}$$

Assumption supported by recent perturbative higher order calculations:

(Maniatis et al. hep-ph/0411300, Daleo et al. hep-ph/0411212, Fontannaz hep-ph/0410021, Aurenche et al. 2004)

Data from H1 Collaboration



$$8 \times 10^{-5} < \langle x \rangle < 7 \times 10^{-3}$$

## 2. Boson production at Hadron Collider

Use HERA results as a phenomenological approach for  $x \ll 10^{-2}$  to predict boson production at Hadron Colliders:

$$\frac{d\sigma_{AB \rightarrow VX}}{dQ^2 dy dq_T^2} = \int \frac{d^2b}{(2\pi)^2} e^{-i\vec{q}_T \cdot \vec{b}} \sum_{a,b} \frac{\sigma_{ab}^0}{S} \left[ \mathcal{C}_{a/c}^{in} \otimes f_c \right] \left( x_A, \frac{b_0}{b_*} \right) \left[ \mathcal{C}_{b/d}^{in} \otimes f_d \right] \left( x_B, \frac{b_0}{b_*} \right) \\ \times e^{-S_P(b_*, Q) - S_{NP}^{BLNY}(b, Q) - b^2 \rho(x_A) - b^2 \rho(x_B)} + Y$$

with

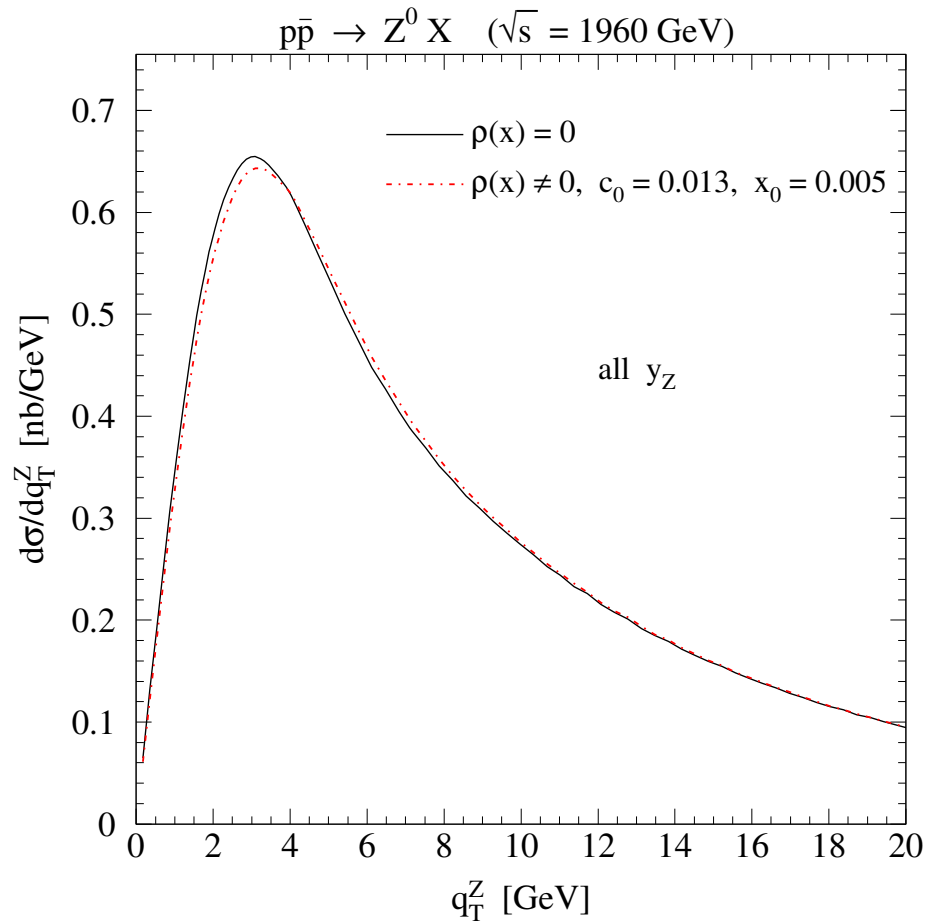
$$\rho(x) = c_0 \left( \sqrt{\frac{1}{x^2} + \frac{1}{x_0^2}} - \frac{1}{x_0} \right), \quad \begin{cases} x \ll x_0 : \rho(x) \sim c_0/x & \text{fits to SIDIS data} \\ x \gg x_0 : \rho(x) \rightarrow 0 & \text{fits to Run I, BLNY} \end{cases}$$

$$c_0 = 0.013, \quad x_0 = 0.005$$

$b_* = b / \sqrt{1 + b^2/b_{max}^2}$ . Above equation reduces to the conventional CSS cross section at large  $x$  and includes sources of additional  $q_T$  broadening at small  $x$  ( $x \lesssim 10^{-2}$ ).

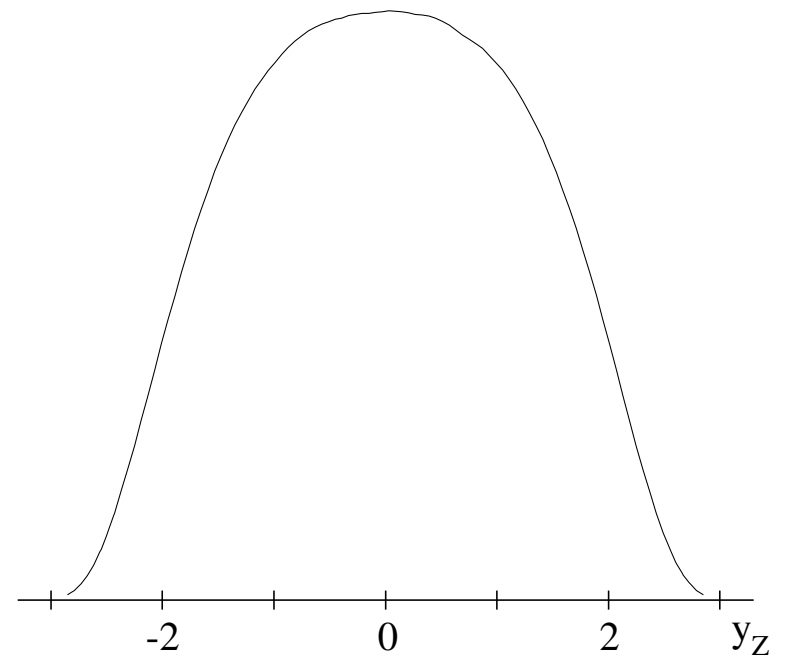
## 2. Small $x$ : Numerical Results

Small  $x$  broadening in  $p\bar{p} \rightarrow Z^0 X$  at Tevatron Run II



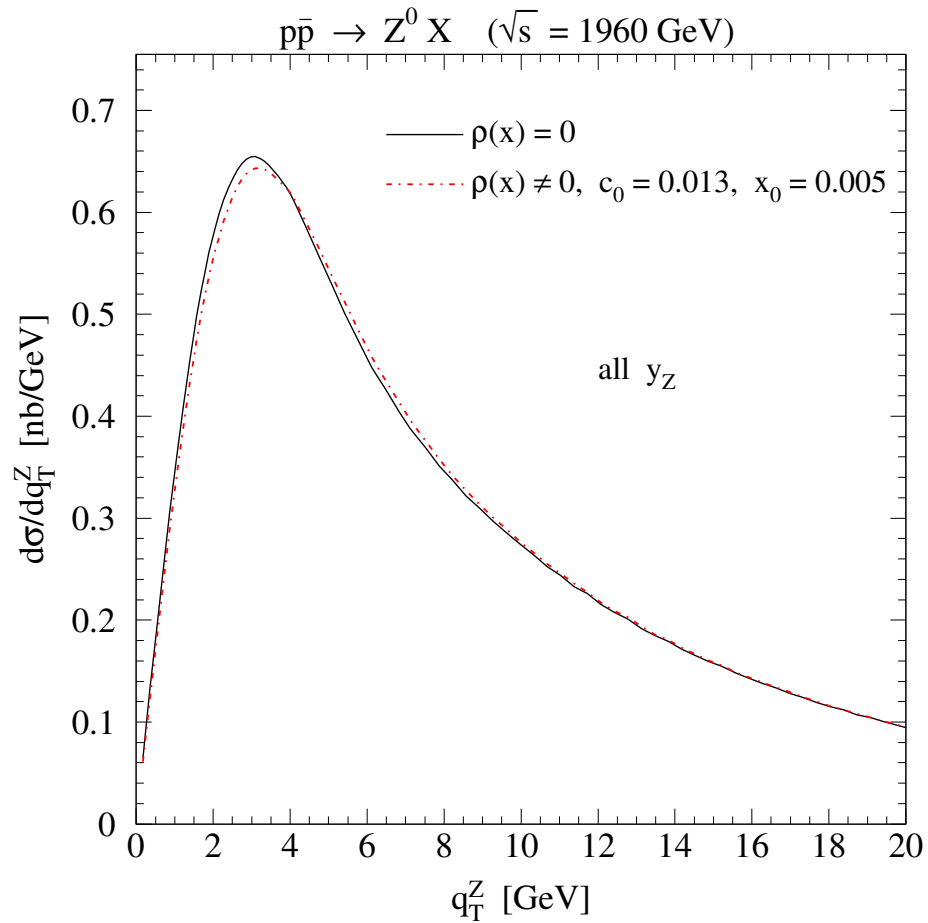
No  $y_W$  cut

Rapidity distribution of  $Z^0$  bosons



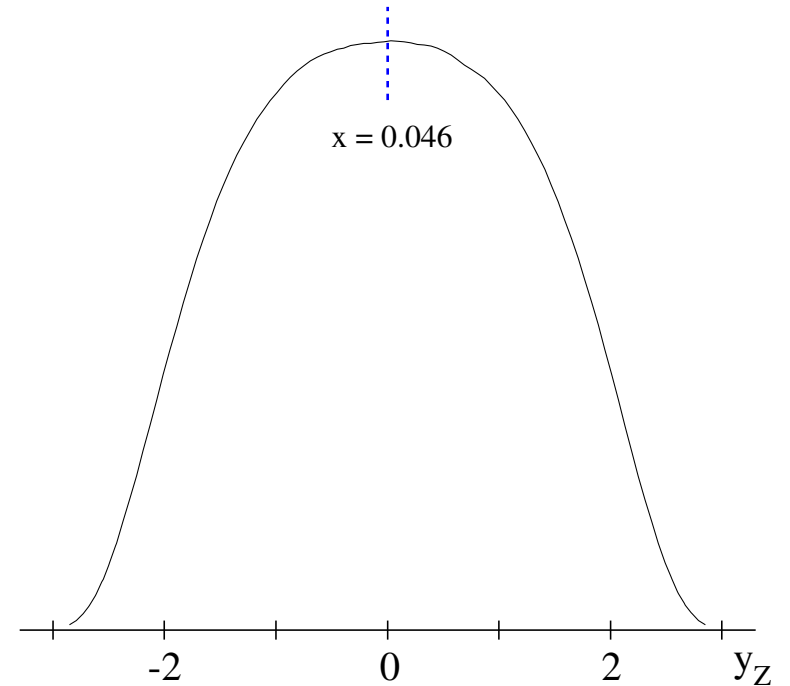
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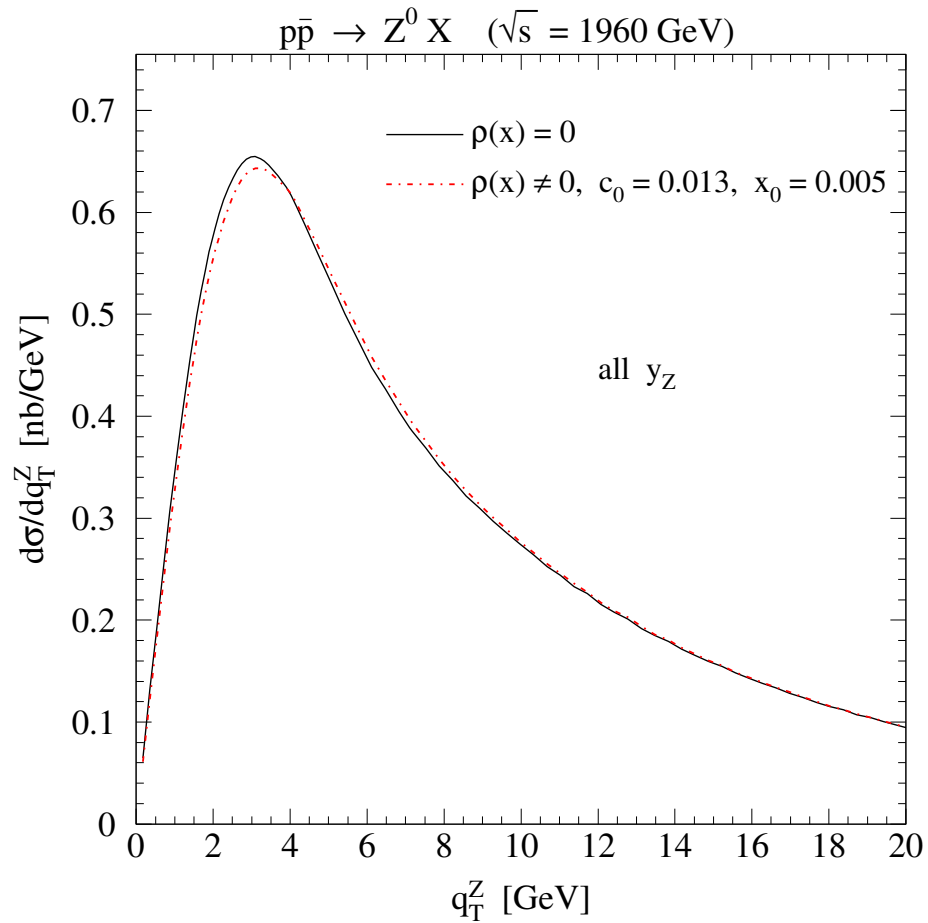
Rapidity distribution of  $Z^0$  bosons





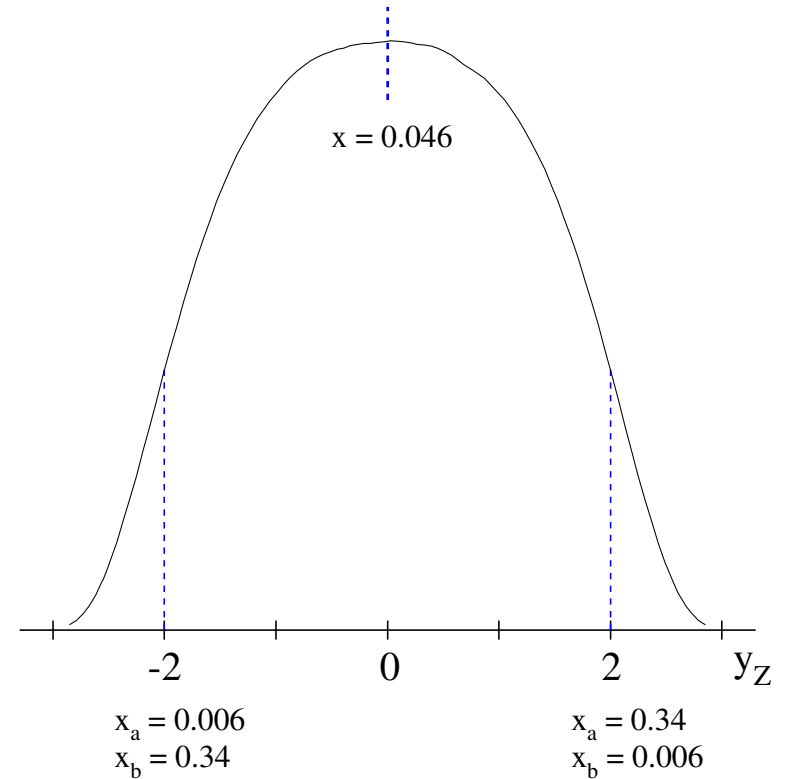
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Small  $x$  broadening in  $p\bar{p} \rightarrow Z^0 X$  at Tevatron Run II



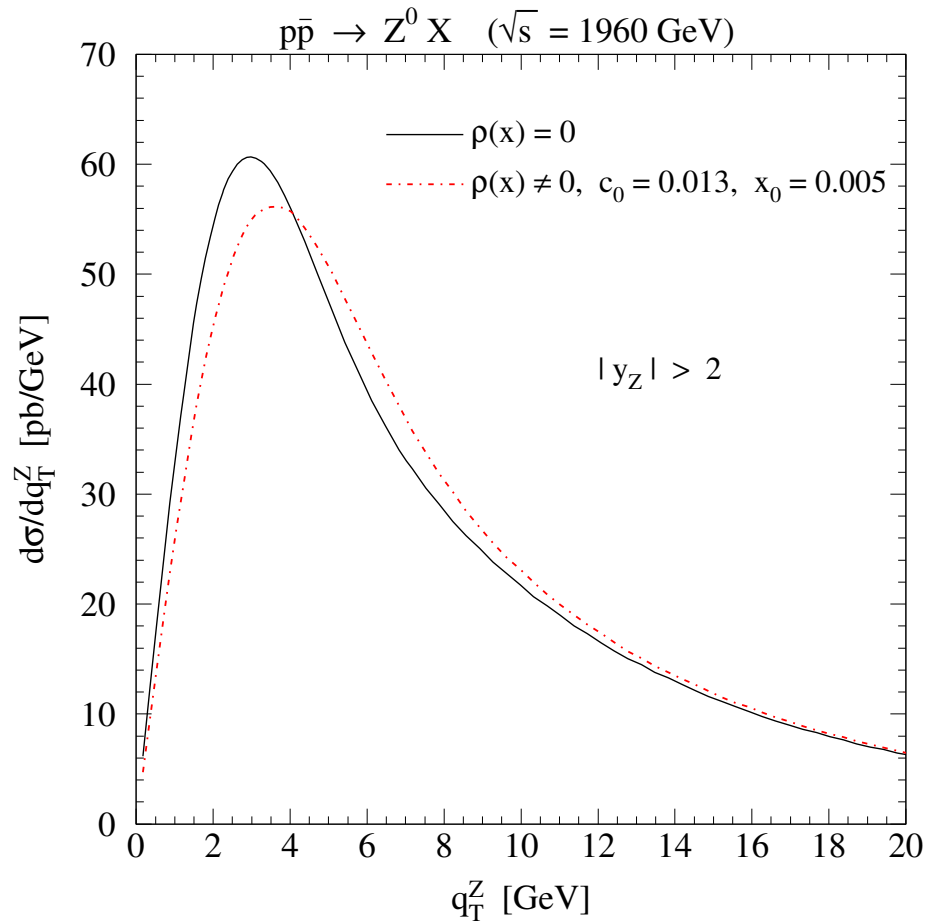
No  $y_W$  cut

Rapidity distribution of  $Z^0$  bosons



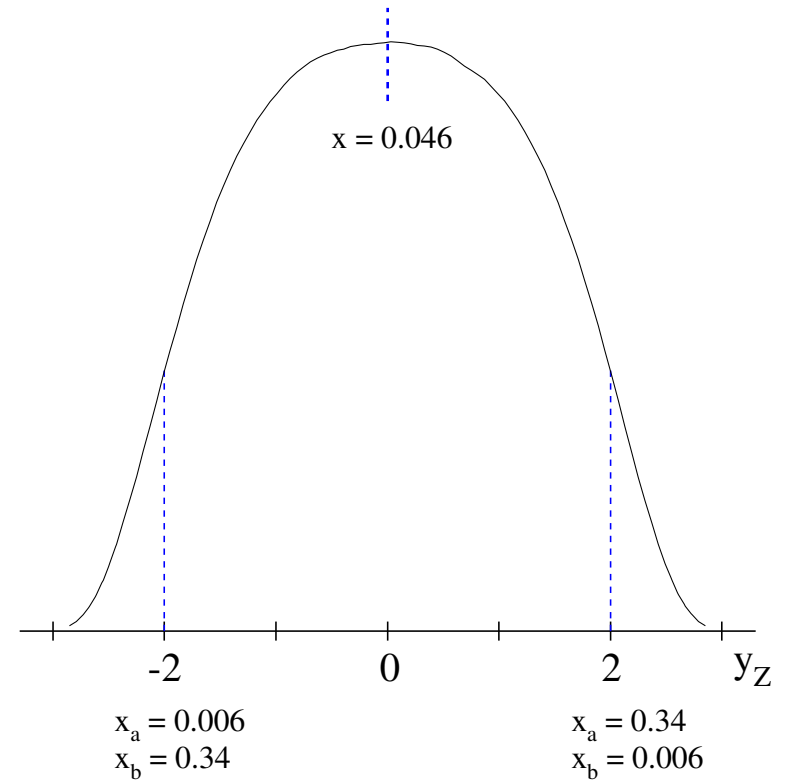
## 2. Small $x$ : Numerical Results

Small  $x$  broadening in  $p\bar{p} \rightarrow Z^0 X$  at Tevatron Run II



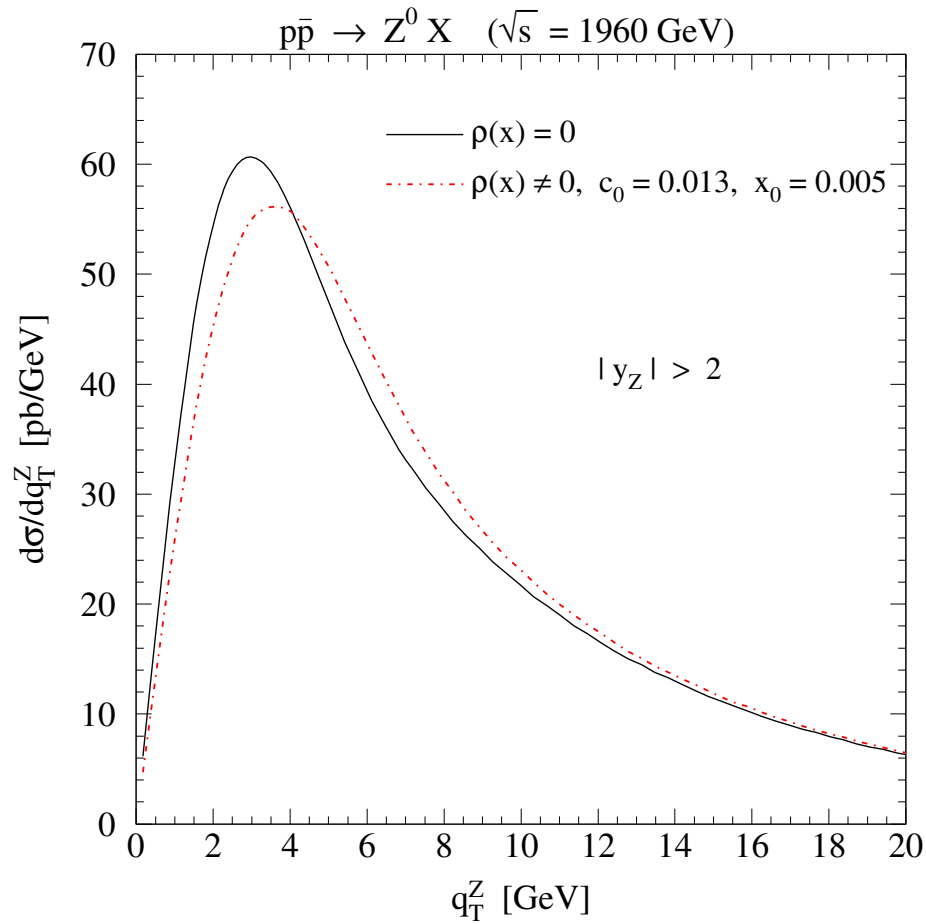
$|y_W| > 2$

Rapidity distribution of  $Z^0$  bosons

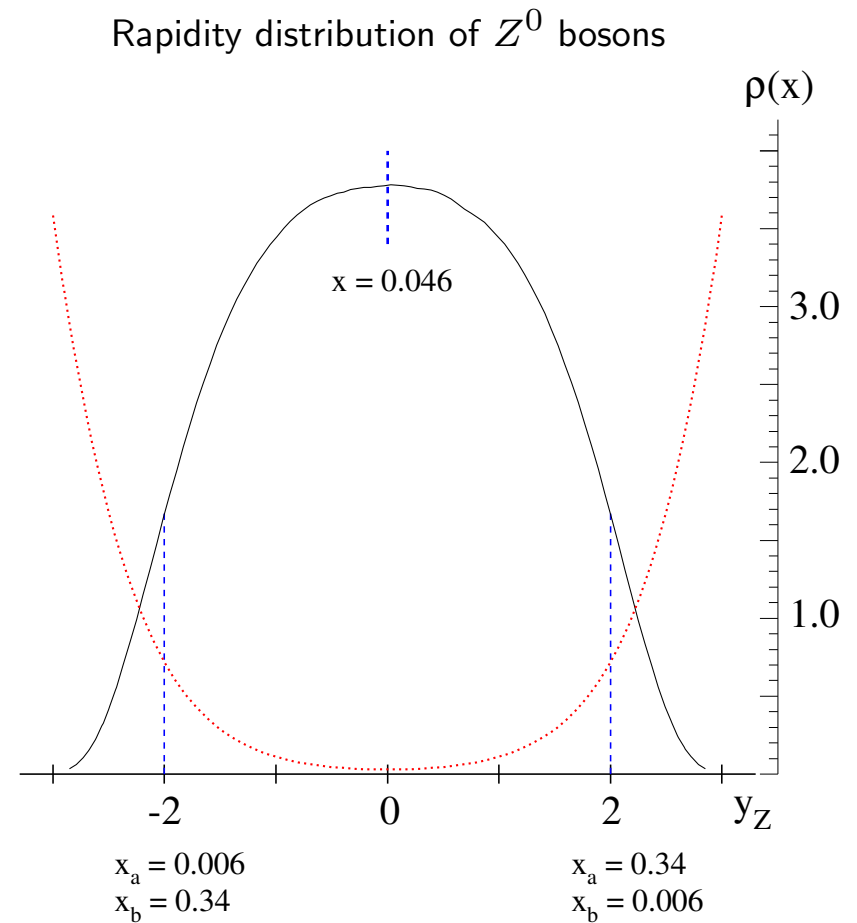


## 2. Small $x$ : Numerical Results

Small  $x$  broadening in  $p\bar{p} \rightarrow Z^0 X$  at Tevatron Run II

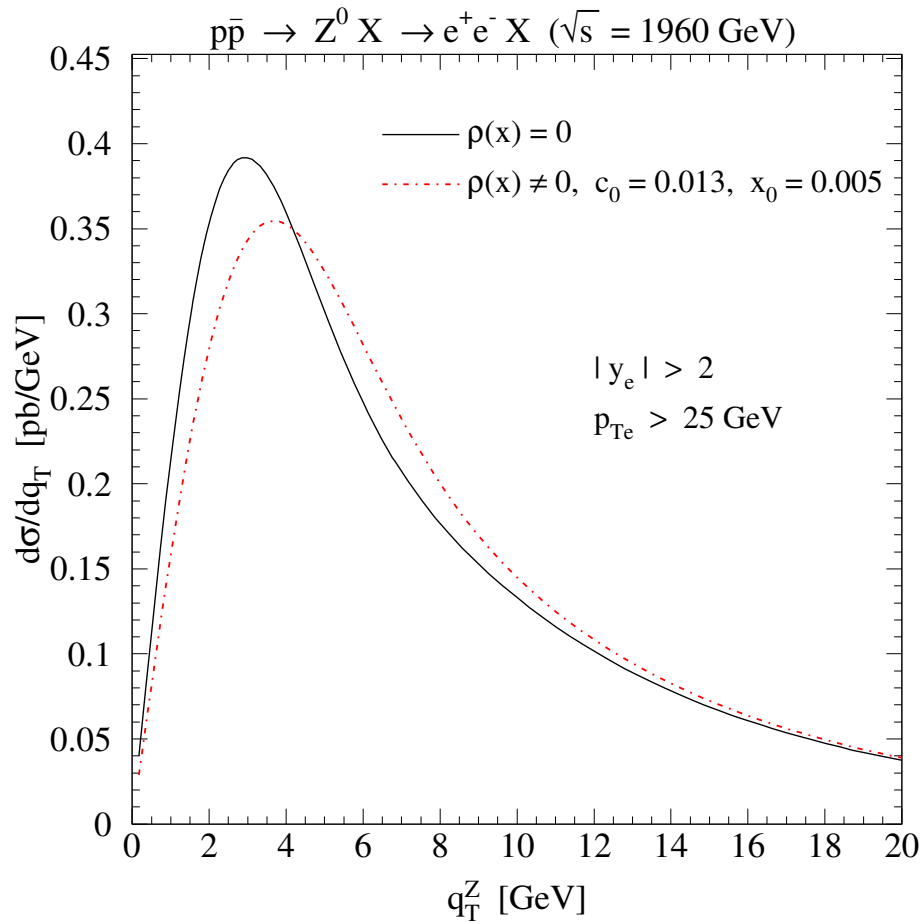


$|y_W| > 2$



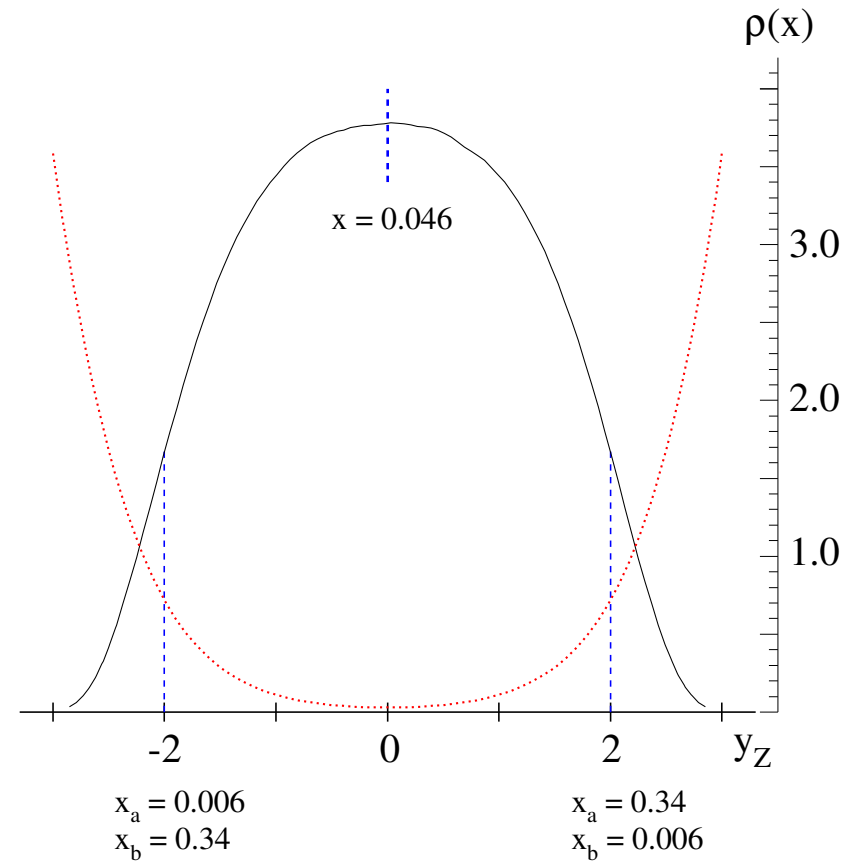
## 2. Small $x$ : Numerical Results

Small  $x$  broadening in  $p\bar{p} \rightarrow Z^0 X$  at Tevatron Run II



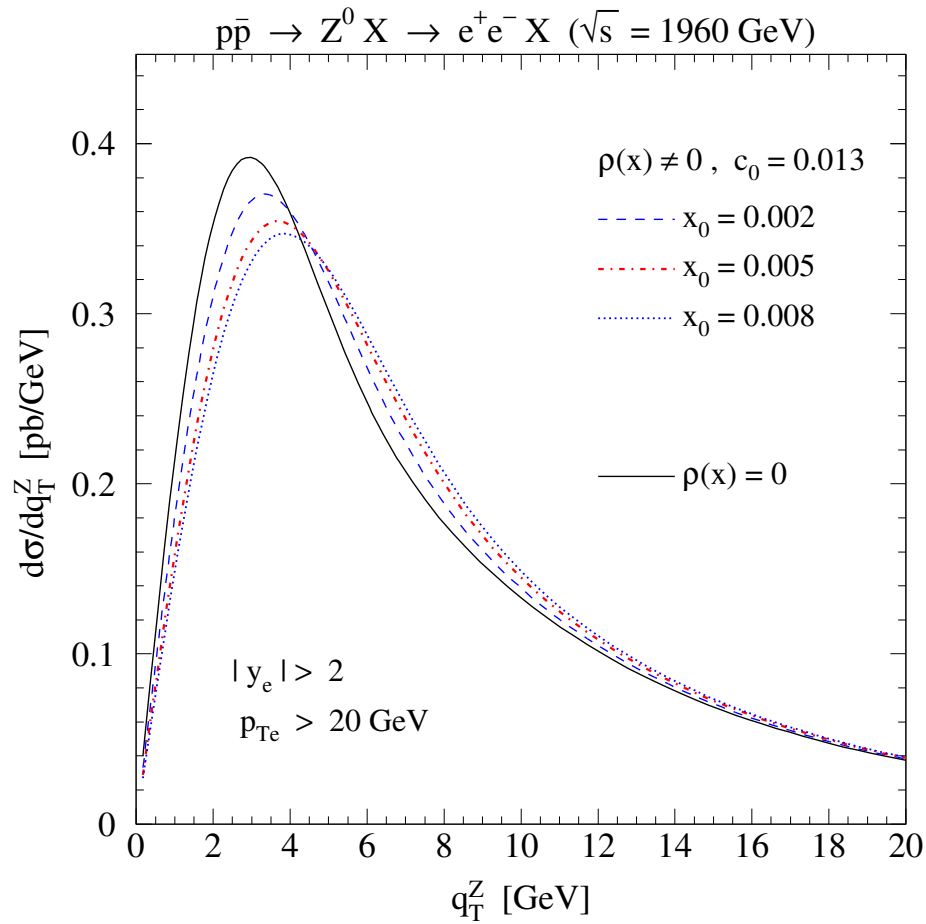
$|y_e| > 2, p_{Te} > 25$  GeV

Rapidity distribution of  $Z^0$  bosons

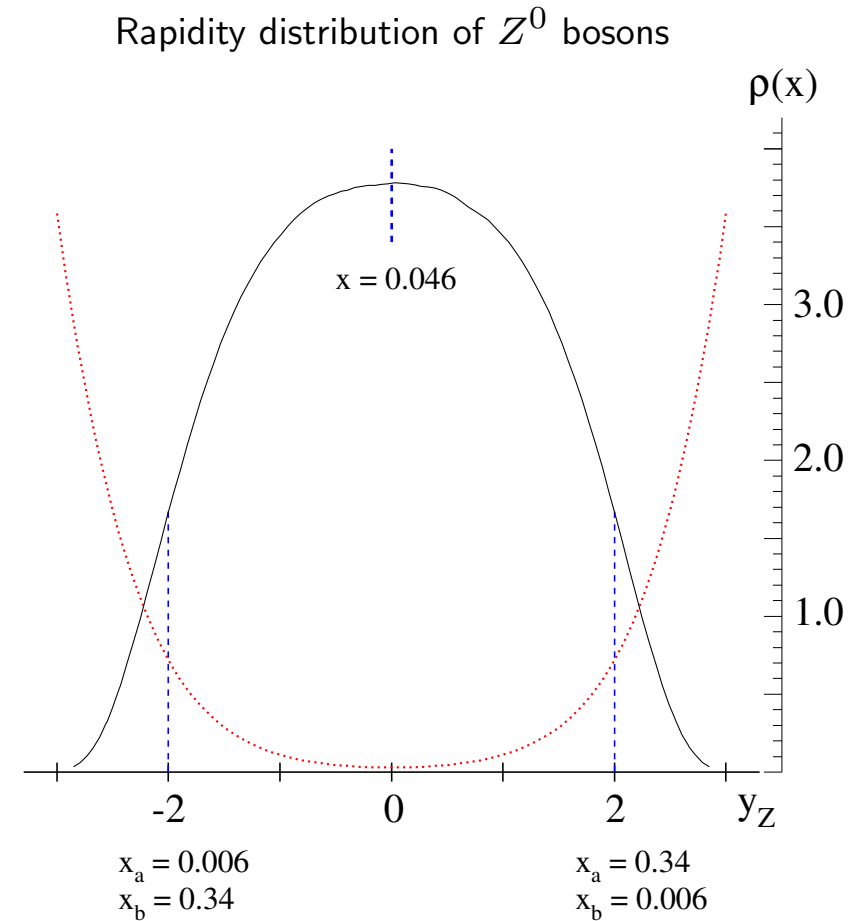


## 2. Small $x$ : Numerical Results

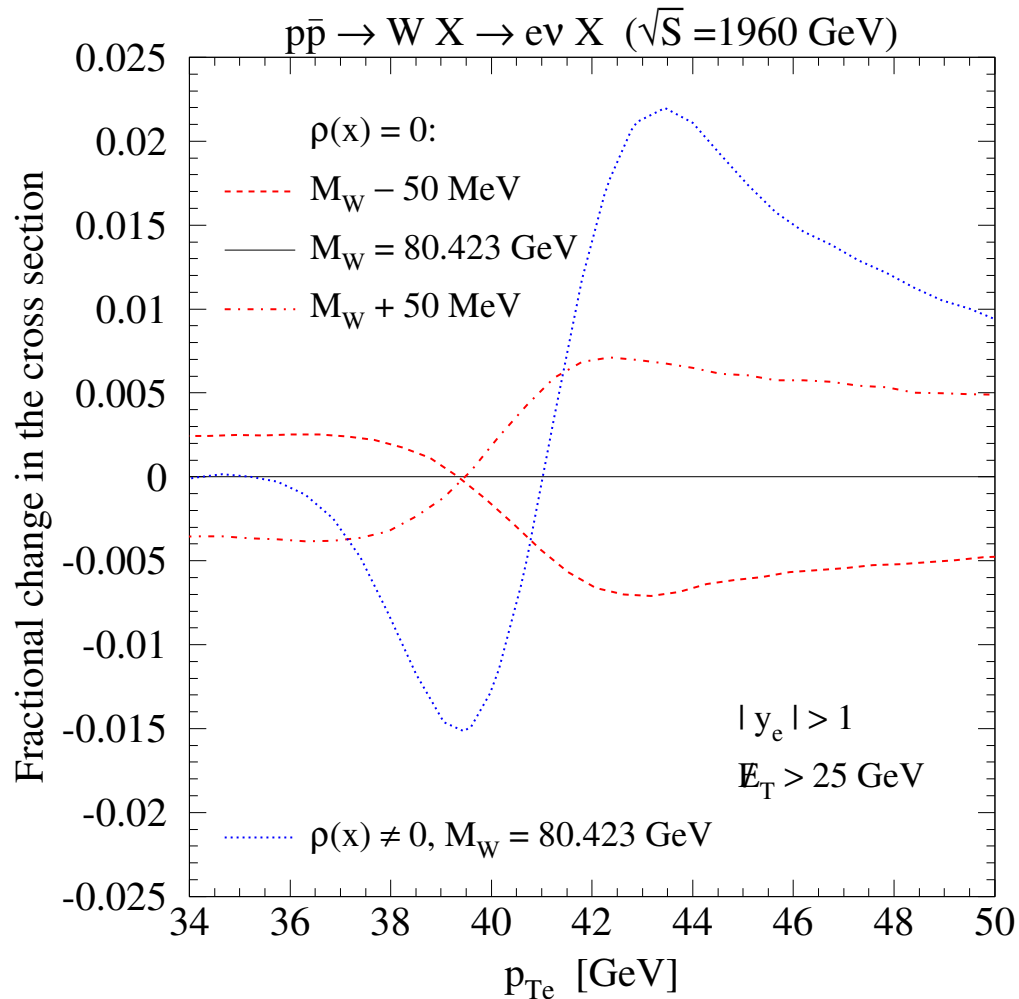
Small  $x$  broadening in  $p\bar{p} \rightarrow Z^0 X$  at Tevatron Run II



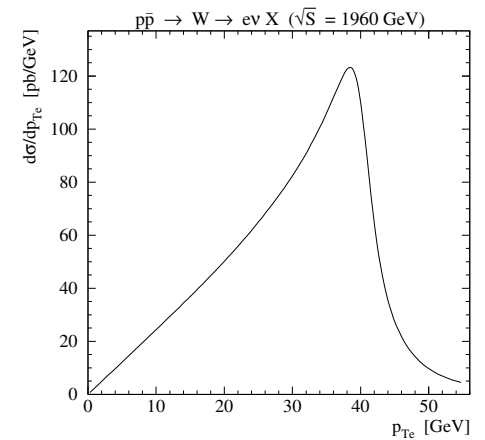
$|y_e| > 2, p_{Te} > 20$  GeV



# Small $x$ : $p\bar{p} \rightarrow W^+ X \rightarrow e^+ \nu_e X$ at Tevatron



$$|y_e| > 1$$



Small  $x$  broadening (blue line) compared to a shift of the W boson mass of  $\pm 50$  MeV (red line).

Plotted is the ratio

$$\frac{d\sigma_X / dq_T^e}{d\sigma_{M_W}^{\rho(x)=0} / dq_T^e}$$

over the lepton transverse momentum  $q_T^e$ !

For  $|y_e| < 1$ , small- $x$  effect is comparable with a 10-20 MeV mass shift.

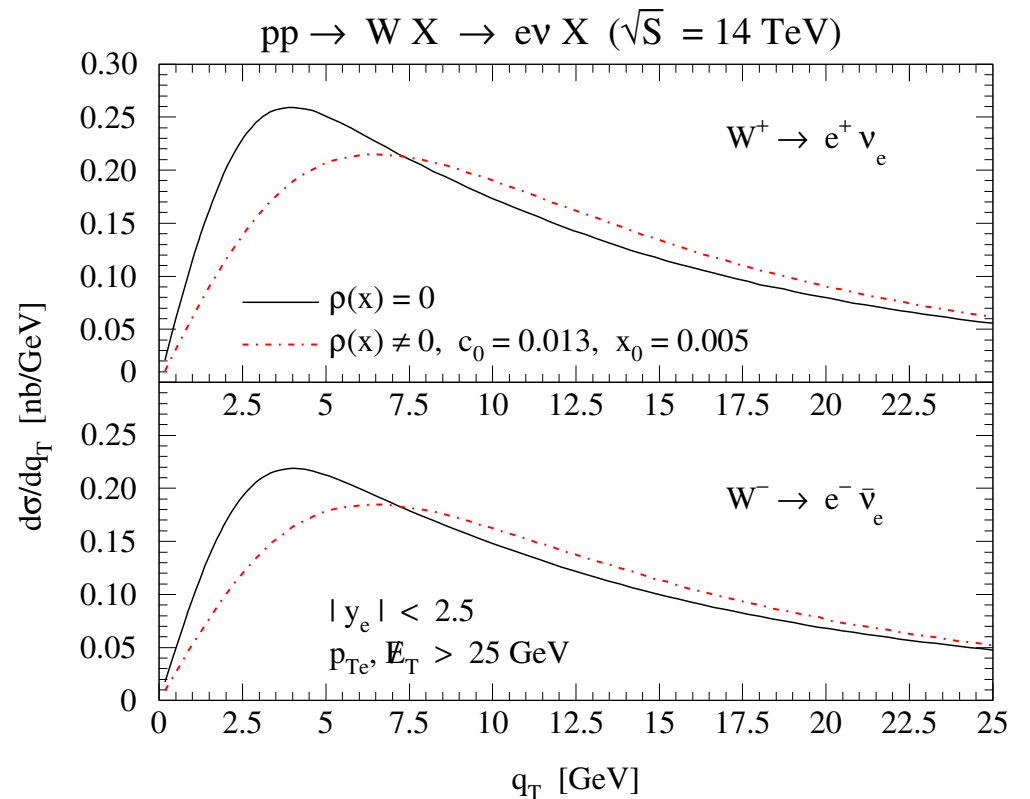
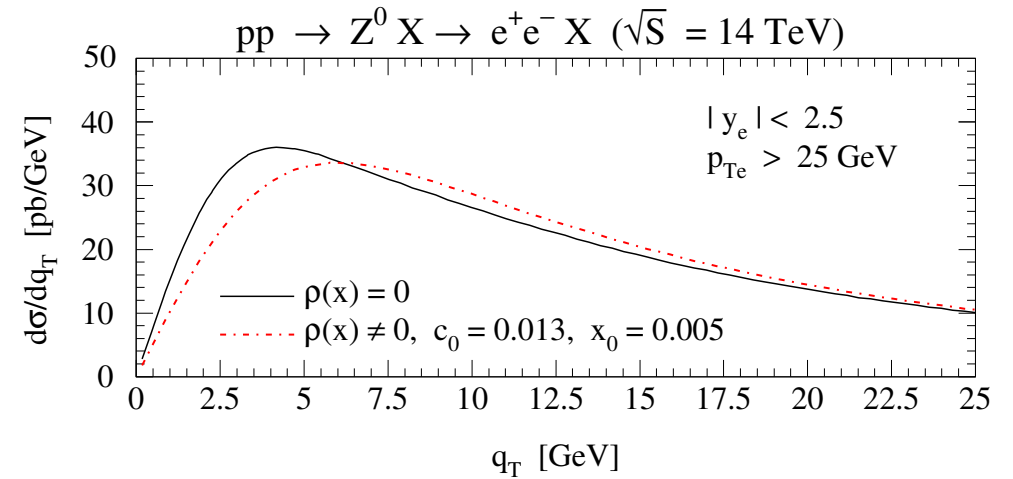
# Small $x$ : $pp \rightarrow Z/W + X$ at LHC

$|y_e| < 2.5$ :

- $x$  stays above  $10^{-4}$  (SIDIS data)
- coverage of the inner ATLAS detector

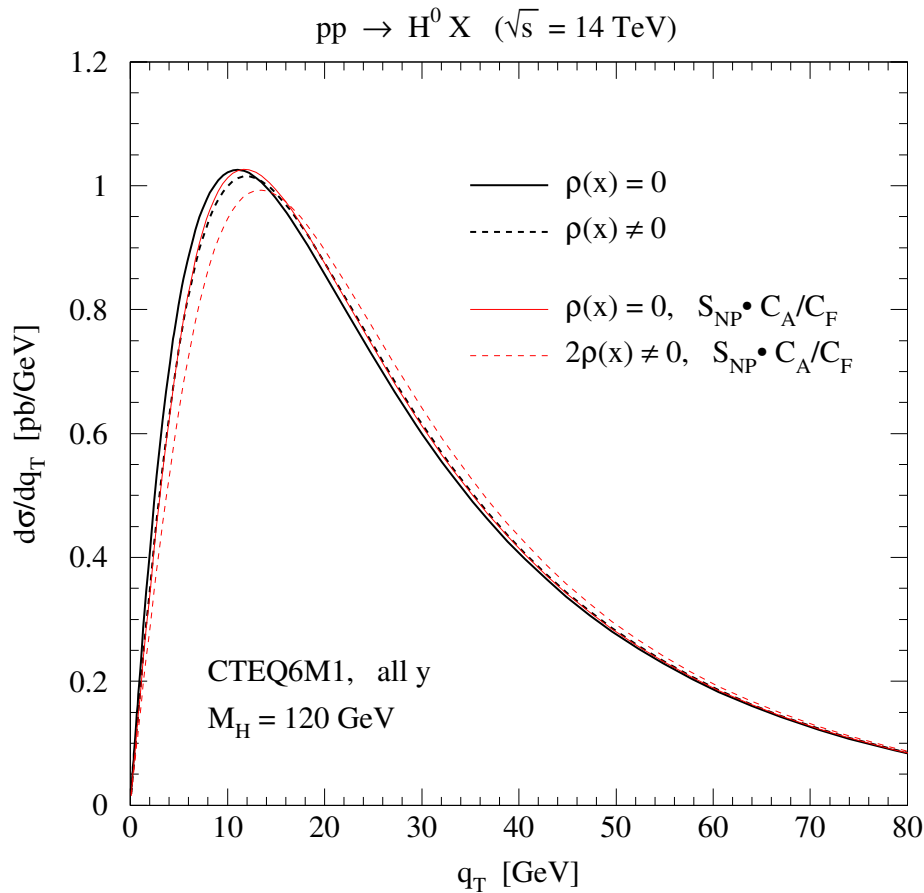
Small  $x$  broadening enhanced even in the central region due to  $x|_{y \approx 0} \approx 0.006$

Dependence of  $d\sigma/dq_T^W$  on transverse W-boson momentum  $q_T^W$



# Small $x$ : $pp \rightarrow H^0 + X$ at LHC

Higgs Boson production at LHC:  $pp(\rightarrow gg) \rightarrow H^0 X$



Dependence of  $d\sigma/dq_T^{H^0}$  on  
transverse H-boson momentum  $q_T^{H^0}$

No  $y_H$  cut  $\rightarrow$  no large small- $x$  broadening

Distribution peaks at  $q_T = 10 - 20$  GeV

black line:  $\rho(x)$  and  $S_{NP}$  are the same  
as for  $Z^0$  production

red line:  $S_{NP}$  multiplied by  $\frac{C_A}{C_F} = \frac{9}{4}$   
due to larger leading-logarithm coefficient  
( $C_A$ ) in  $gg$  channels compared to  $q\bar{q}$   
channels ( $C_F$ )



### 3. Resummation in heavy flavor production:

- It is well known, how to calculate  $d\sigma/dq_T$  for massless quarks (resummation for  $\ln(q_T^2/Q^2)$ , e.g. CSS)
- Massless approximation neglects terms  $\sim M_H^2/q_T^2$ , which may be important at small  $q_T$

$$\frac{1}{q_T^2 + M_H^2} = \frac{1}{q_T^2} \left( \frac{1}{1 + \frac{M_H^2}{q_T^2}} \right)$$

- Systematic calculation of differential distributions in reactions with heavy quarks  $H$  ( $H = c, b$ ) in the presence of 3 distinct momentum scales (Nadolsky, Kidonakis, Olness, Yuan, 2003)

e.g. Boson production - relevant momentum scales:

- Heavy quark mass  $M_H$
  - Virtuality  $Q$  of the produced boson ( $\Lambda_{QCD}^2 \ll M_H^2 \ll Q^2$ )
  - Transverse momentum  $q_T$  of the produced boson ( $0 \leq q_T^2$ )
- Relies on the usage of a massive variable flavor number (VFN) factorization scheme

### 3. Heavy flavor contribution in W and Z bosons production

$W^+$  production:

$$V_{CKM}^2 \times \text{Parton Luminosity} \sim \sigma_{Born}$$

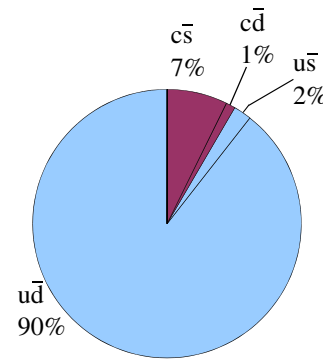
$W^-$  production:

$$V_{CKM}^2 \times \text{Parton Luminosity} \sim \sigma_{Born}$$

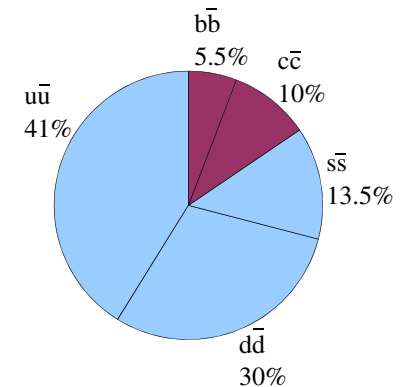
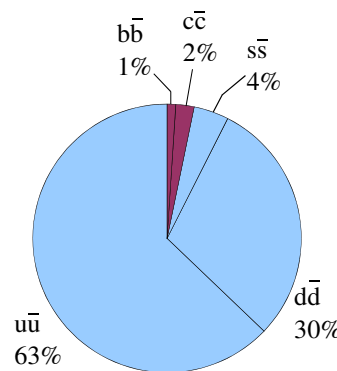
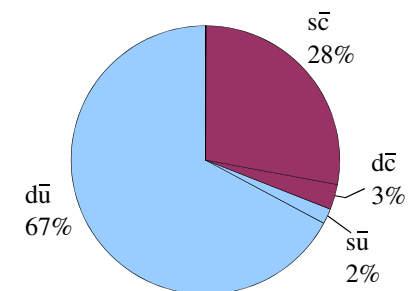
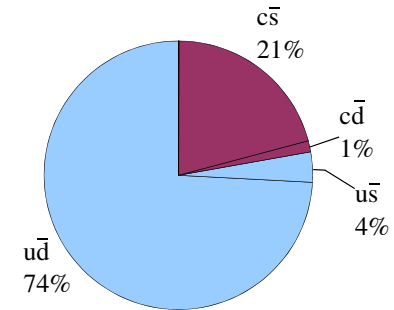
$Z^0$  production:

$$\text{Parton Luminosity} \sim \sigma_{Born}$$

Tevatron Run2



LHC

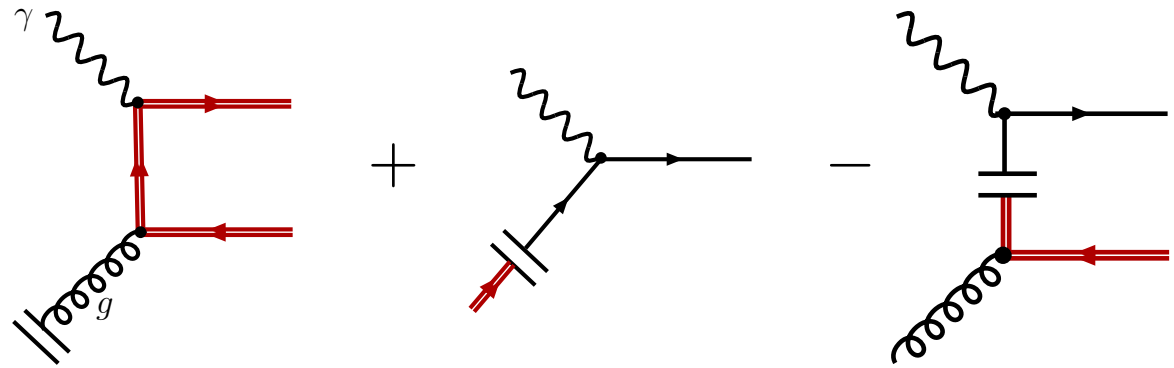


Largest heavy quark contribution in charm quark channel in  $W^-$  boson production (31%) at LHC.

### 3. Heavy Quark

#### Simplified ACOT factorization scheme

(Collins 1998;  
Kramer, Olness, Soper, 2000)



- Set  $M_H = 0$  in coefficient functions for incoming heavy quarks
- Only graphs with explicit flavor creation retain  $M_H \neq 0$
- Significantly simplifies calculations
- $M_H$  is dropped in the Sudakov factor  $S(b, Q)$
- Quark initiated processes from the massless calculation:  $M_H$  is dropped in the function  $C_{jq}^{in}(x, b\mu_F)$ ,  $C_{bj}^{out}(z, b\mu_F)$  with incoming heavy quarks
- Numerical closed to the conventional ACOT scheme
- Included  $\mathcal{O}(\alpha_s)$  contribution of  $g \rightarrow q\bar{q}$  for  $M_H \neq 0$  into Legacy (Landry, Brock, Nadolsky, Yuan, 2003)
- Following plots are computed with Resbos (Balazs, Yuan, 1997)

### 3. Heavy Quark: Z-boson production at LHC

Consider heavy flavor channels ( $c\bar{c}, b\bar{b}$ ) for Z boson production at LHC:

$d\sigma/dq_T$  enhanced by 2.5% in peak region  $q_T \sim 7.5$  GeV

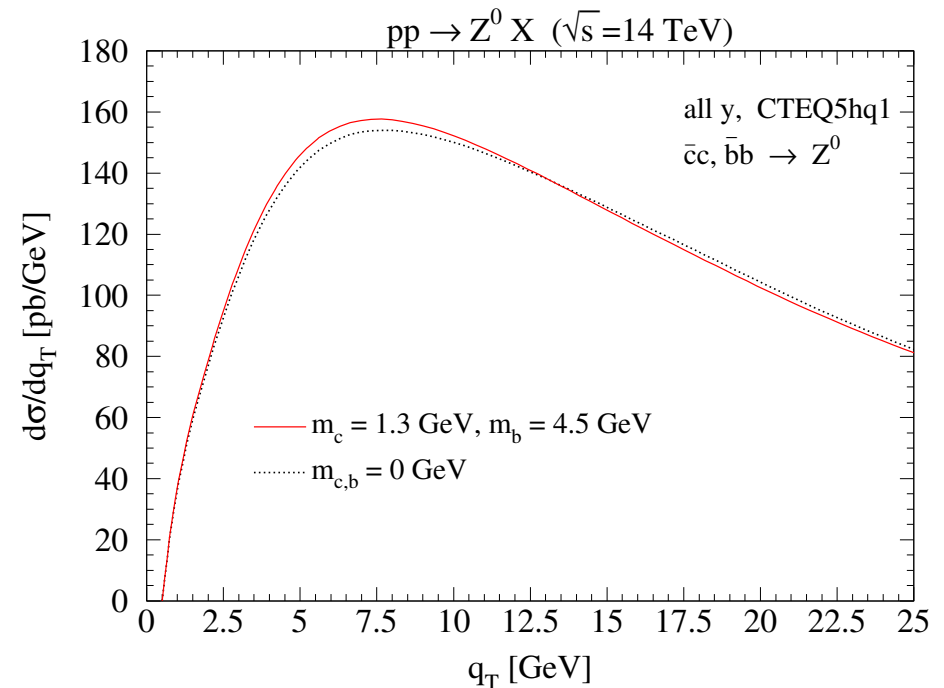
$d\sigma/dq_T$  slightly reduced for  $q_T > 15$  GeV

Heavy flavor channels contribute only to 15% to total cross section

→ increase of less than 0.3% remains

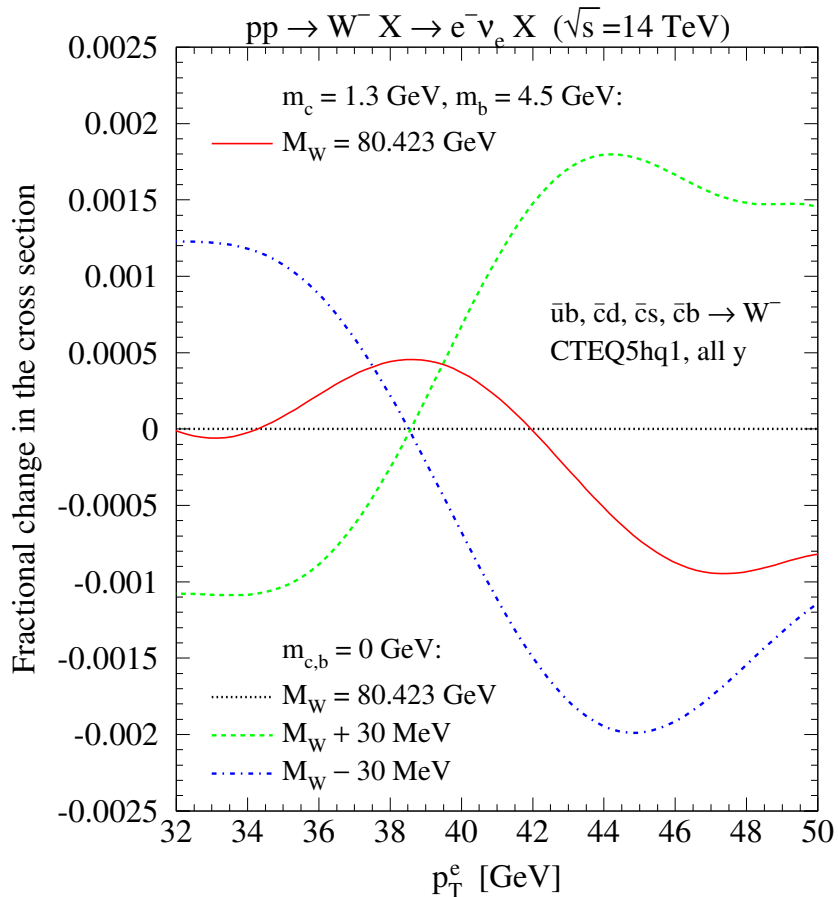
→ curves not distinguishable for cross section including all possible initial quark combinations

Effect for  $Z^0$  production at Tevatron negligible.



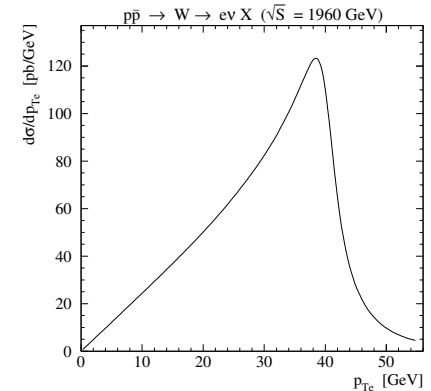
Dependence of  $d\sigma/dq_T^Z$  on transverse momentum  $q_T$  for the  $c\bar{c}, b\bar{b} \rightarrow Z^0$  channels only

### 3. Heavy Quark: $W^-$ production at LHC



plotted is 
$$\frac{d\sigma_X/dq_T^e}{d\sigma_{M_W}^{massless}/dq_T^e}$$

$\bar{u}b, \bar{c}d, \bar{c}s, \bar{c}b \rightarrow W^-$



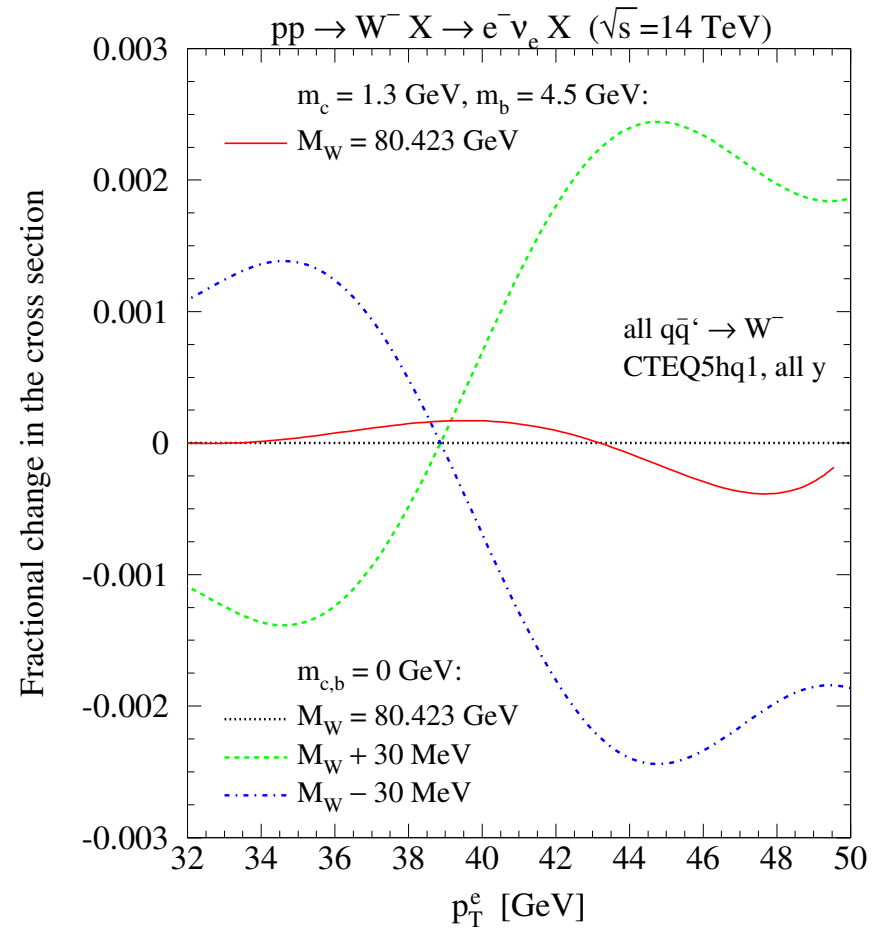
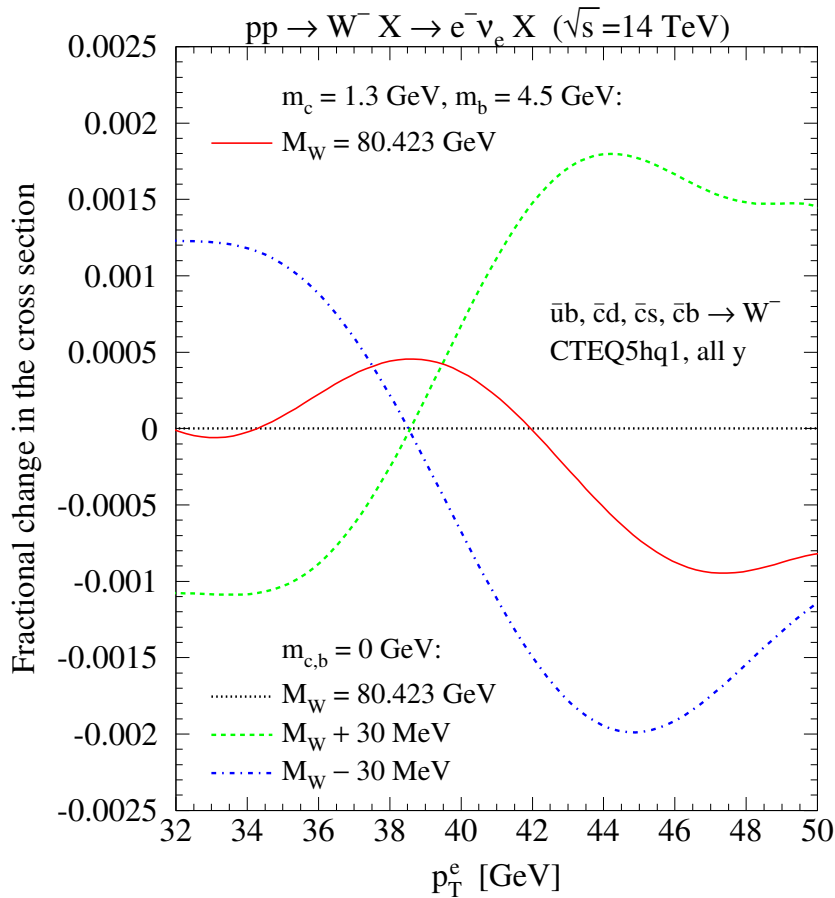
Heavy flavor channels only:

Shifts the Jacobian peak in the negative direction

Size of this effect is comparable to a  $M_W$  shift of about  $-15$  MeV

Similar behavior and size for  $W^+$  production at LHC and  $W$  production at Tevatron (because dominant channel is always  $c\bar{s} \rightarrow W^+$  or  $\bar{c}s \rightarrow W^-$ )

### 3. Heavy Quark: $W^-$ production at LHC



plotted is  $\frac{d\sigma_X/dq_T^e}{d\sigma_{M_W}^{massless}/dq_T^e}$

$\bar{u}b, \bar{c}d, \bar{c}s, \bar{c}b \rightarrow W^-$

all  $q\bar{q}' \rightarrow W^-$

$W^-(W^+)$  at LHC:  $-5(-1.8)$  MeV

$W$  at Tevatron:  $-1.2$  MeV

### 3. Heavy Quark: Higgs boson production

Consider Higgs boson production in:

$$pp \rightarrow b\bar{b} \rightarrow H^0$$

$$M_h = 120 \text{ GeV}$$

Contributes in SM less than 1%  $\rightarrow$  negligible

Can be dominant in MSSM for large  $\tan\beta$  because  $b\bar{b}H$  coupling is enhanced,  $t\bar{t}H$  coupling mostly suppressed

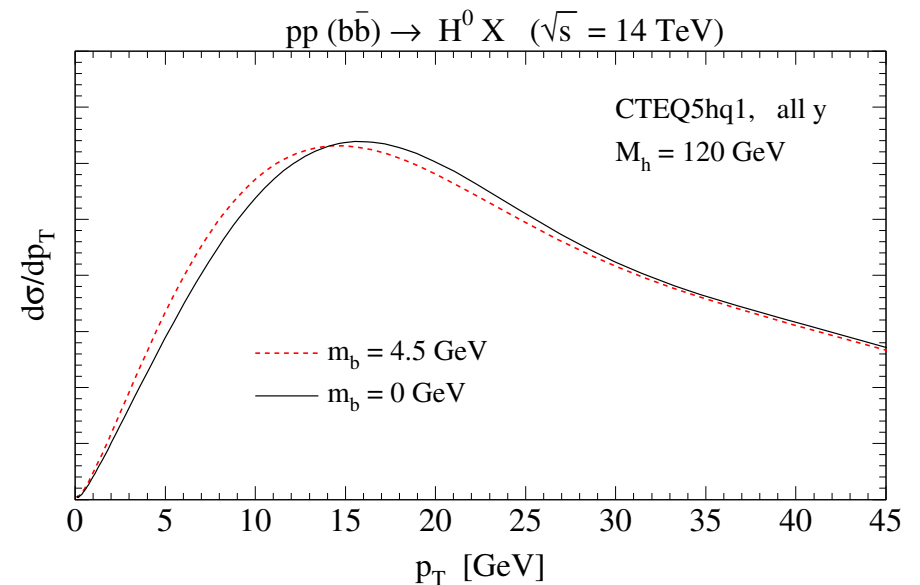
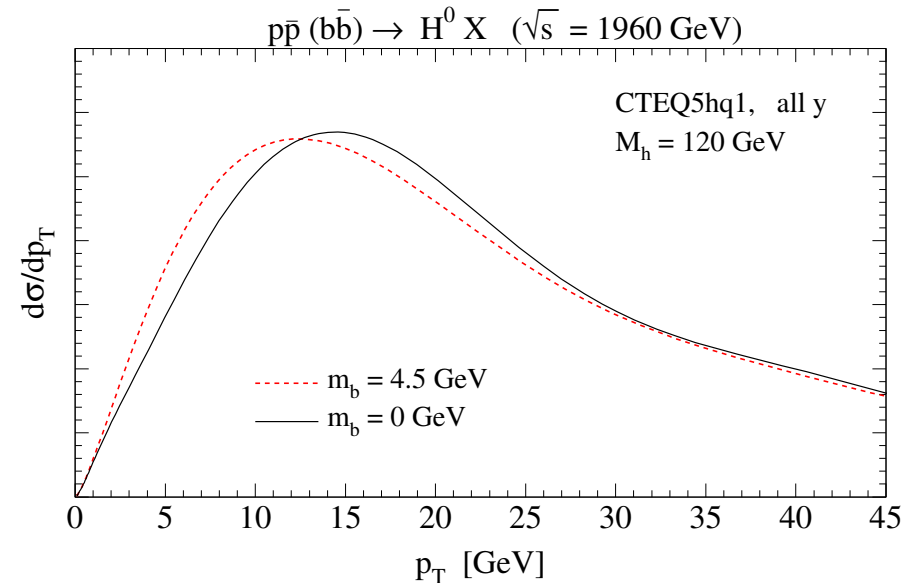
Shift in the peak region:

At Tevatron:  $-2.0 \text{ GeV}$

At LHC:  $-1.2 \text{ GeV}$

(Decreases to  $-0.6 \text{ GeV}$  for  $M_h = 600 \text{ GeV}$ )

Other channels with one initial bottom quark may be affected:  $gb \rightarrow Zb, gb \rightarrow H^0b, gb \rightarrow H^-t, u\bar{b} \rightarrow d\bar{t} \dots$

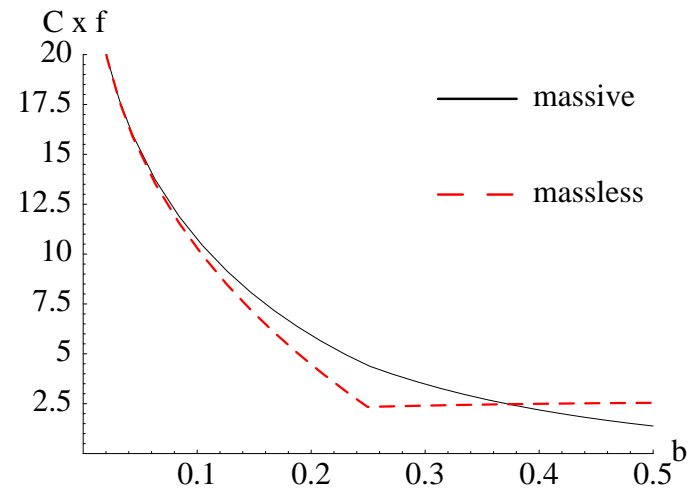


## 4. Conclusion

- **Small  $x$ :**
  - Based on semi-inclusive DIS data, we hypothesize broadening of  $q_T$  distributions at  $x \lesssim 10^{-2}$
  - $q_T$  broadening can possibly be measured in the forward rapidity range ( $|y| \geq 2$ ) in  $Z$ -boson production at Tevatron and will affect the  $W$  mass measurement for  $|y| \geq 1$
  - $q_T$  broadening will strongly influence predictions for  $W$  and  $Z$  production at LHC
  - For  $H^0$  transverse momentum distribution,  $q_T$  broadening might be less important at the LHC
- **Heavy flavor** effects on transverse momentum distribution:
  - Heavy flavor effects on  $Z$  and  $W$  boson production at Tevatron are negligible
  - Heavy flavor effects on  $W$  mass measurement at LHC are smaller than the experimental uncertainties
  - Bottom-antibottom initiated processes can be strongly affected (e.g.  $b\bar{b} \rightarrow H$  at LHC: peak shifted by  $-1.2$  GeV)



### 3. Heavy Quark



- Included  $\mathcal{O}(\alpha_s)$  contribution of  $g \rightarrow q\bar{q}$  for  $M_q \neq 0$  into Legacy

- Following plots are computed with Resbos

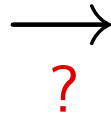
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## 2. Introduction

HERA

SIDIS

$$\overline{\mathcal{P}}_j^{(S)}(x, b)$$



Tevatron/LHC

$Z^0, W^\pm$  ( $\delta M_W = 30/15$  MeV?)

$$\overline{\mathcal{P}}_j^{(T)}(x, b)$$

$$\overline{\mathcal{P}}_j^{(I)}(x, b) = \left| \mathcal{H}^{(I)}(b_0/b) \right| \tilde{U}(b_0/b)^{1/2} \hat{\mathcal{P}}_j(x, b), \quad (\text{Collins, Soper; '82})$$

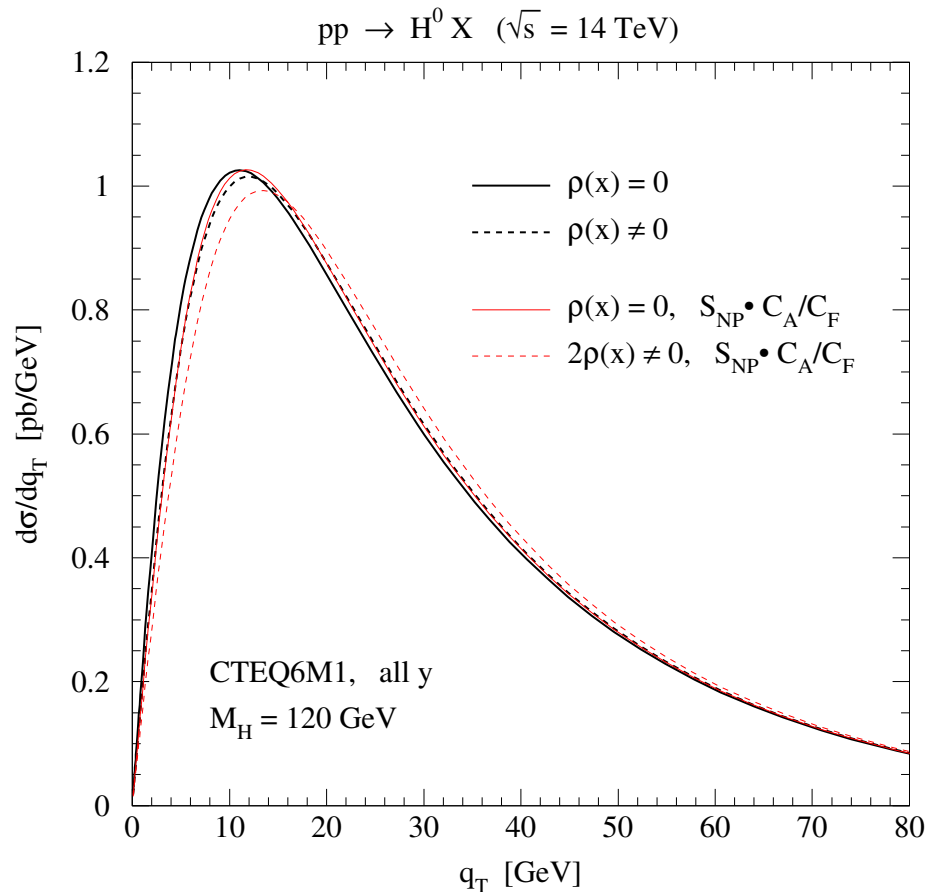
$\mathcal{H}^{(I)}(b_0/b)$  ... virtual corr. to the hard vertex

$\tilde{U}(b_0/b)^{1/2}$  ... collects soft subgraphs attached to  $\mathcal{H}^{(I)}(b_0/b)$

$\hat{\mathcal{P}}_j(x, b)$  ... is the same in SIDIS and Drell-Yan, (Collins, Metz; hep-ph-0408249)

## 4. Numerical Results

Higgs Boson production at LHC:  $pp(\rightarrow gg) \rightarrow H^0 X$



Dependence of  $d\sigma/dq_T^{H^0}$  on  
transverse H-boson momentum  $q_T^{H^0}$

No  $y_H$  cut  $\rightarrow$  no large small  $x$  broadening

Distribution peaks at  $q_T = 10 - 20$  GeV

black line:  $\rho(x)$  and  $S_{NP}$  are the same  
as for  $Z^0$  production

red line:  $S_{NP}$  multiplied by  $\frac{C_A}{C_F} = \frac{9}{4}$   
due to larger leading-logarithm coefficient  
( $C_A$ ) in  $gg$  channels compared to  $q\bar{q}$   
channels ( $C_F$ )

$gg \rightarrow (H \rightarrow \gamma\gamma) X$ :

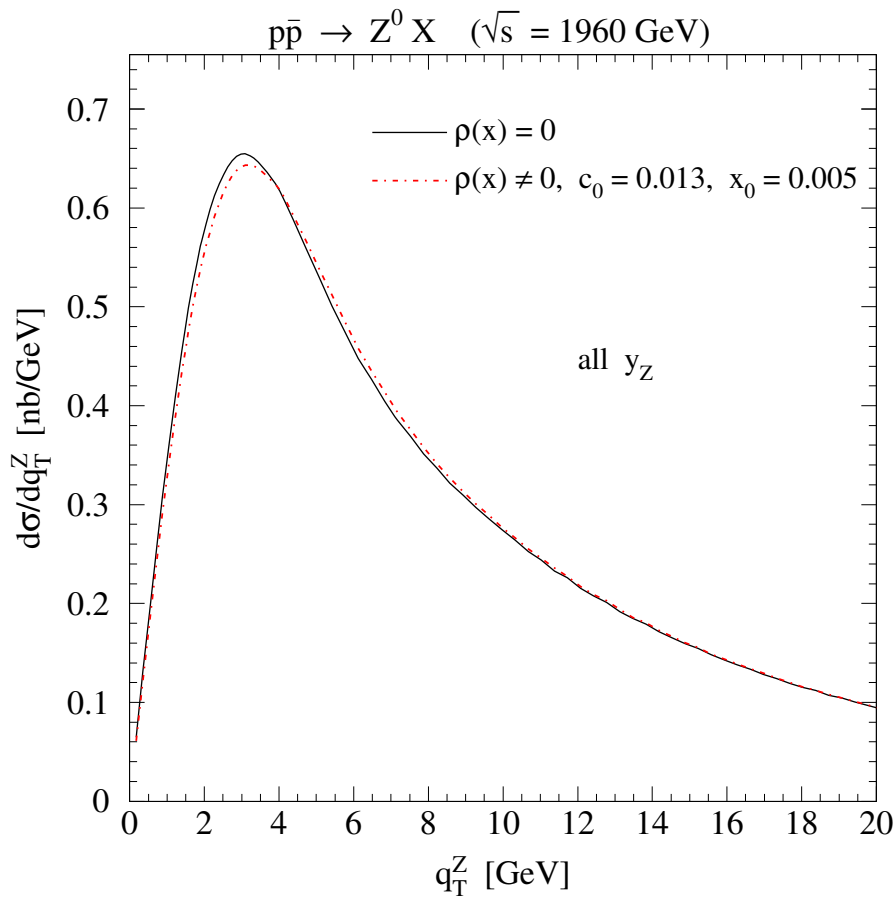
Signal significance can be increased by  
selecting events

with  $q_T^{\gamma\gamma} \gtrsim 30$  GeV (Abdullin et al.)

**End**

# Numerical Results

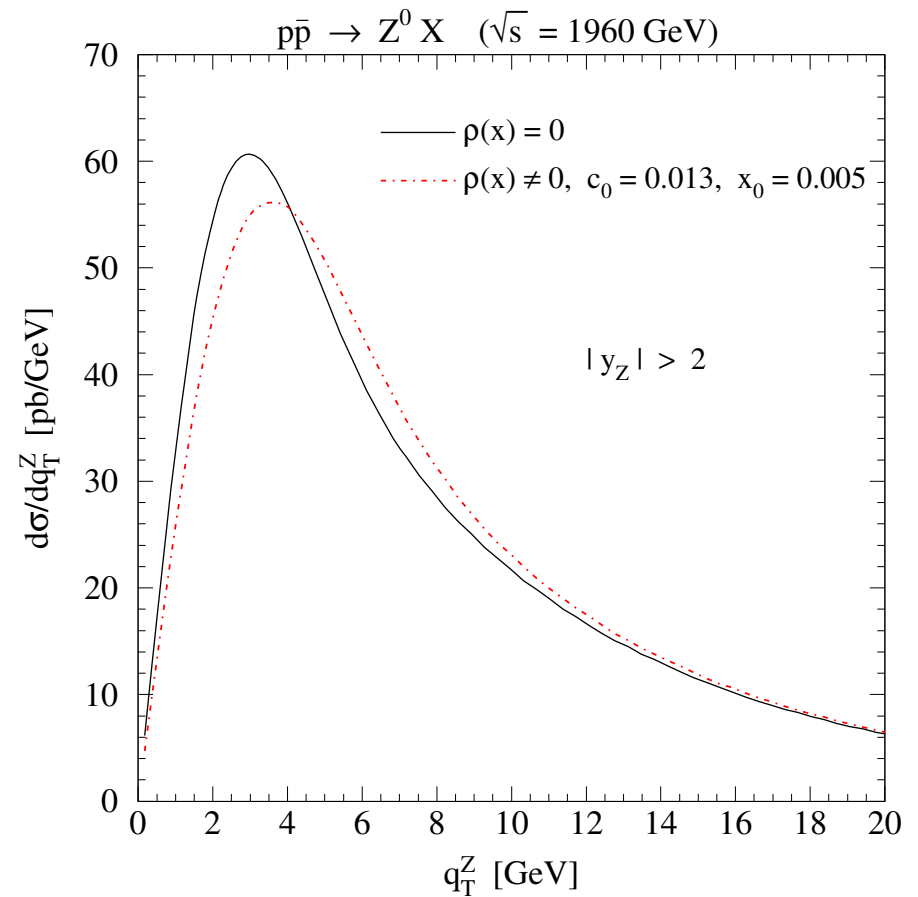
## Small- $x$ effects on $p\bar{p} \rightarrow Z^0 X$ at the Tevatron



No  $y$  cut

(the dominant contribution comes from  $x|_{y \approx 0} \approx 0.05$ )

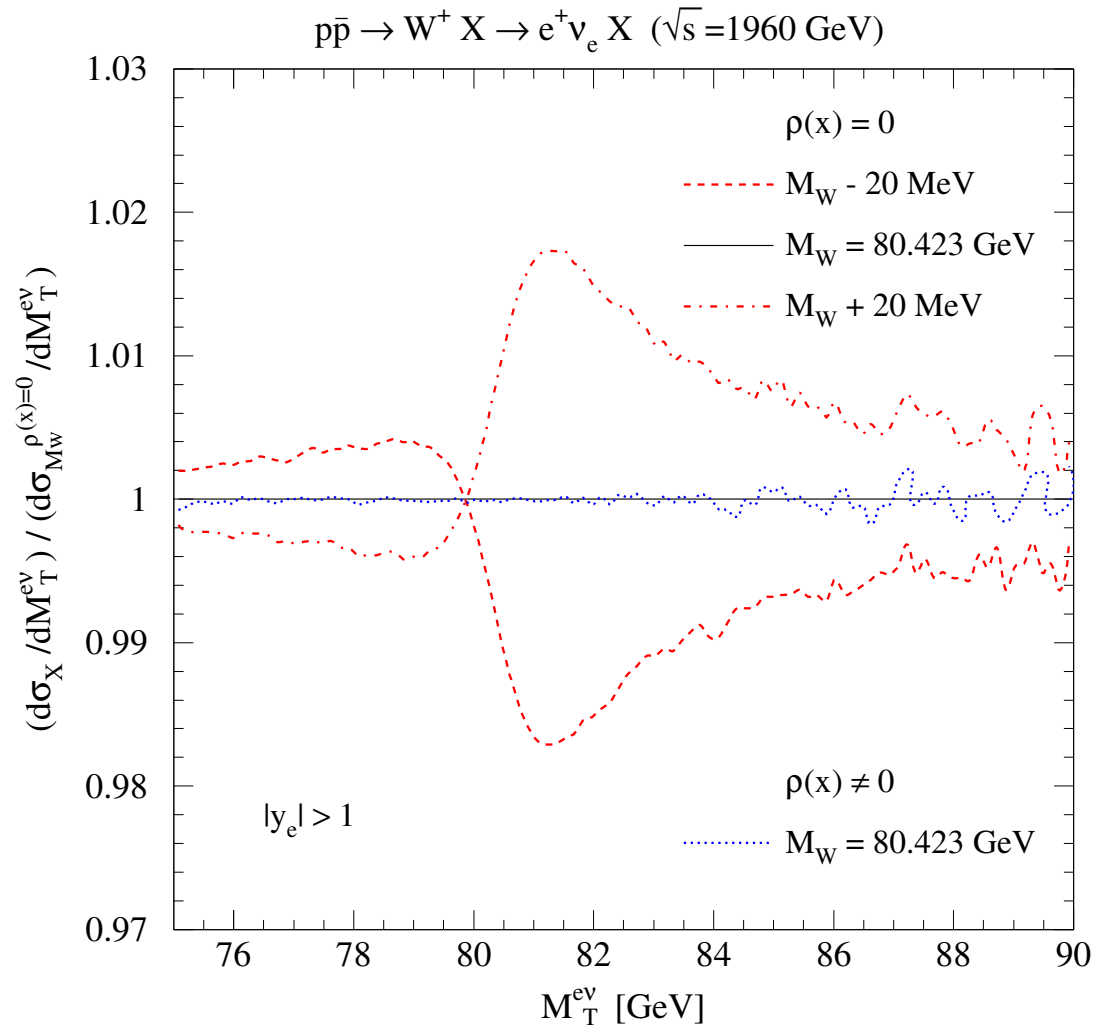
Effect measurable in the Tevatron Run-2



$|y| > 2$

Visible broadening in the forward region  
90% of cross section between  $2 < |y| < 2.5$

# Ratio of W transverse mass distribution

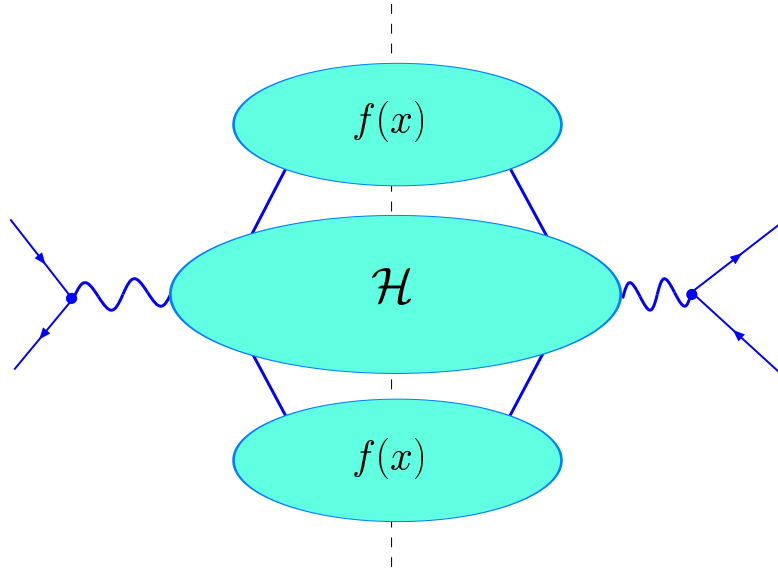


# Resummation

## QCD factorization in hard and soft regions

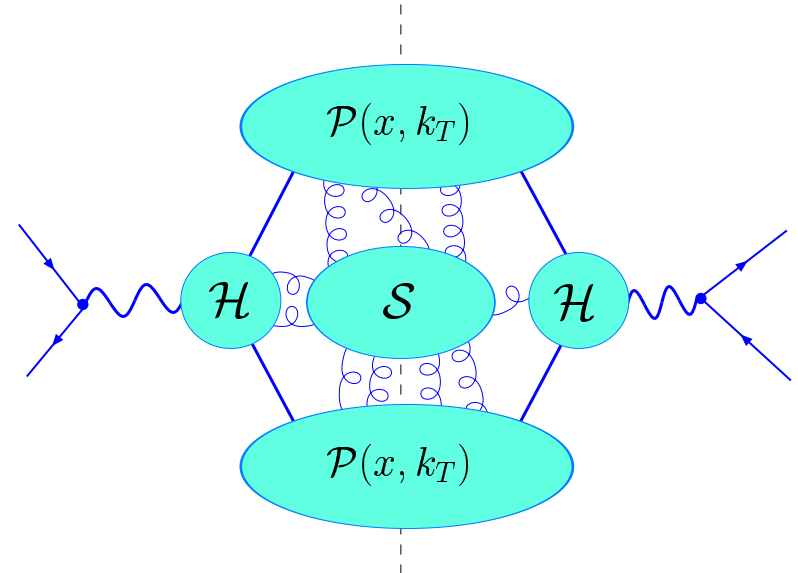
Finite-order (FO) factorization

$$\Lambda_{QCD}^2 \ll q_T^2 \sim Q^2$$



Small- $q_T$  factorization

$$\Lambda_{QCD}^2 \ll q_T^2 \ll Q^2$$



Solution for all  $q_T$ :

