

# *Status and perspectives of measurements of $V_{ub}$ and $\gamma$*

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*INFN and Università Roma 'La Sapienza'*

*BaBar Collaboration*

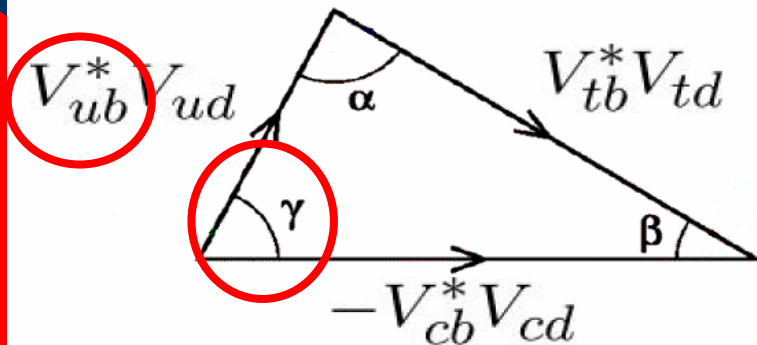
*LHC Flavour*

*Workshop*

*CERN – 7-10 nov 2005*

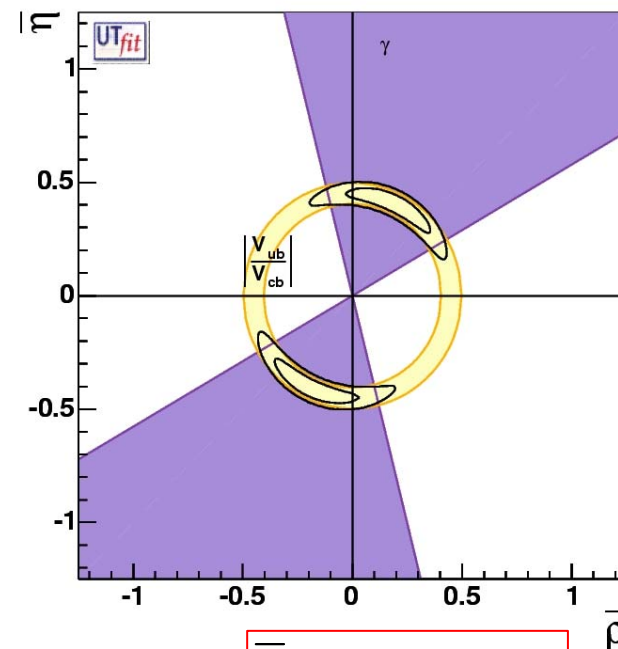
# The reference Unitarity Triangle

*L.Silvestrini,  
LP'05*



- $\gamma$  and  $V_{ub}$  from pure tree level processes!
- Assumptions:
  - 3 generations only
  - No new physics at tree level
- Any new physics must satisfy this constraint

UTfit coll., hep-ph/0501199;  
Botella et al., hep-ph/0502133



$$\bar{\rho} = \pm 0.18 \pm 0.12$$

$$\bar{\eta} = \pm 0.41 \pm 0.05$$

# $V_{ub}$ , inclusive and exclusive

- Inclusive  $B \rightarrow X_u \ell \nu$

- large signal rate, large  $X_c \ell \nu$  background
  - **Select limited region of phase space**

- Total rate evaluates from OPE

$$\Gamma(\bar{B} \rightarrow X_u \ell \bar{\nu}) = \frac{G_F^2 m_b^5}{192\pi^3} |V_{ub}|^2 \times \left\{ 1 + O(\alpha_s) + O\left(\frac{1}{m_b^2}\right) \right\}$$

- Non-perturbative contribution: Shape Function
  - determined experimentally from  $b \rightarrow s \gamma$ ,  $b \rightarrow c \ell \nu$

- Exclusive  $B \rightarrow \pi \ell \nu, \rho \ell \nu, \text{etc.}$

- Low signal rate, background rejection (kin. constraint)
- FormFactors normalization ( $V_{ub}$ ): theory error  
FF shape (**acceptance**) affects exp'l uncert.

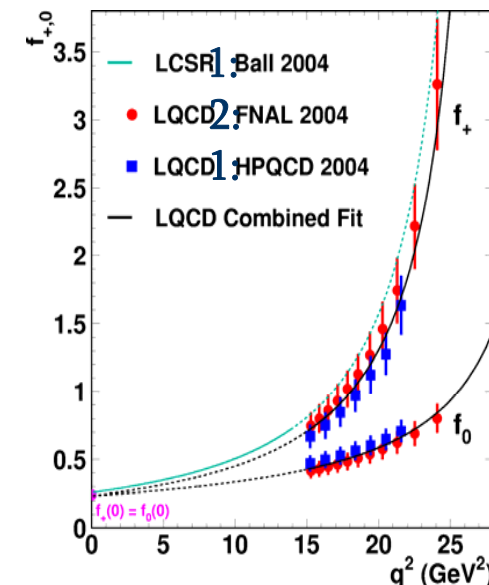
$$\frac{d\Gamma(B \rightarrow \pi \ell \nu)}{dq^2} = \frac{G_F^2}{24\pi^3} |V_{ub}|^2 P_\pi^3 |f_+(q^2)|^2$$

## BNLP

S.W. Bosch, B.O. Lange, M. Neubert, G. Paz, Nucl. Phys. B **669**, 355 (2004)  
B.O. Lange, M. Neubert, G. Paz, hep-ph/0504071

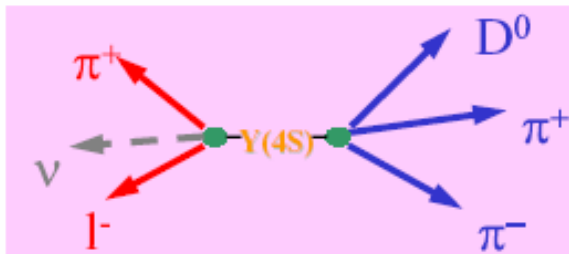
**BLL** C.W. Bauer, Z. Ligeti, M. Luke, hep-ph/0111387

## Form Factor



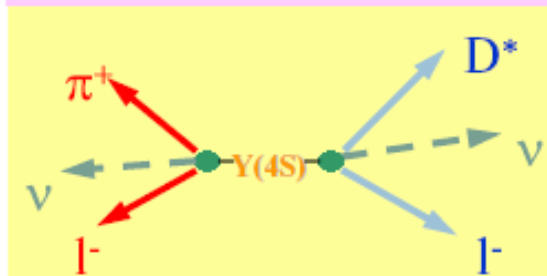
# Measuring $V_{ub}$ , experimental methods

- Tagging methods



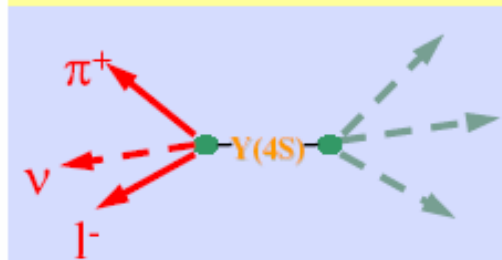
### Hadronic Tag:

Fully reconstruct hadronic decay of one B:  
 $B \rightarrow D^{(*)} + (\pi^+, \pi^0, K^+, K^0) \approx 1000$  modes  
 $\rightarrow$  know kinematics of other B



### Semileptonic Tag:

Reconstruct  $B \rightarrow D^{(*)} l \nu$  and study recoil  
 - Full reconstruction of  $D^{(*)}$   
 - Partial reconstruction of  $D^*$  (only  $l, \pi_{\text{soft}}$ )  
 Two  $\nu \rightarrow$  tag-B kinematics incomplete

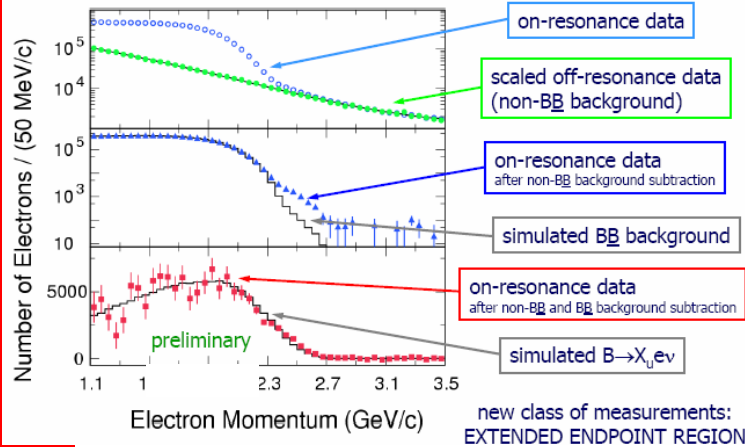


### No Tag:

High statistics  
 High backgrounds and cross-feed  
 $\rightarrow$  Fully reconstruct signal side ( $\nu$  reco.)

# $V_{ub}$ : inclusive analyses

$$|V_{ub}| = \sqrt{\frac{\Delta B}{\Delta \zeta \cdot \tau_B}}$$



## Endpoint spectrum

$$2.0 < E_e < 2.6 \text{ GeV}$$

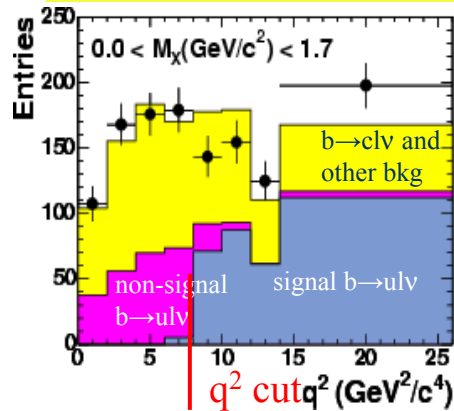
$$|V_{ub}| = (4.44 \pm 0.25_{\text{exp}} \pm 0.42_{\text{th-BLNP}} \pm 0.22_{\text{th-BLNP}} - 0.38_{\text{SF}}) \times 10^{-3} \quad \sigma \sim 12\%$$

$b \rightarrow s\gamma, b \rightarrow clv$  moments (BaBar) [O.Buchmuller and H.Flacher, hep-ph/0507253]

hep-ex/0509040

80 fb<sup>-1</sup>

## $M_X$ vs $q^2$ : hadronic tag



$$|V_{ub}|_{\text{BLL}} = (4.82 \pm 0.26_{\text{stat}} \pm 0.25_{\text{syst}} \pm 0.46_{\text{SF+theo}}) \times 10^{-3} \quad \sigma \sim 12\%$$

$$|V_{ub}|_{\text{BLNP(BaBar } b \rightarrow clv)} = (4.65 \pm 0.24_{\text{stat}} \pm 0.24_{\text{syst}} \pm 0.46_{\text{th}} \pm 0.23_{\text{th}} - 0.36_{\text{SF}}) \times 10^{-3} \quad \sigma \sim 13\%$$

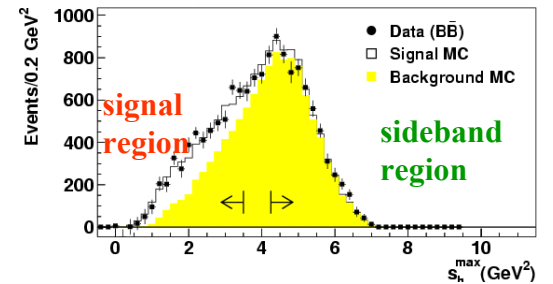
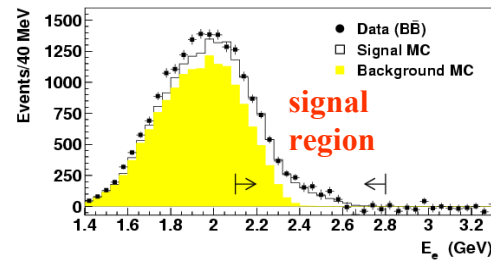
5

hep-ex/0507017

211 fb<sup>-1</sup>

G.Cavoto

## Neutrino reconst.: $E_l$ vs $q^2$



hep-ex/0506036

81 fb<sup>-1</sup>

$$\Delta BR(E_e^* > 2.0 \text{ GeV}, s_h^{\text{max}} < 3.5 \text{ GeV}^2) = (3.54 \pm 0.33_{\text{stat}} \pm 0.34_{\text{syst}}) \times 10^{-4}$$

$$|V_{ub}| = (3.95 \pm 0.26_{\text{exp}} \pm 0.58_{\text{th}} \pm 0.25_{\text{theo}} - 0.42_{\text{HQ}}) \times 10^{-3}$$

# Results (and current limitations)

HFAG results are rescaled

to common HQE inputs:

$$m_b = 4.60 \pm 0.04 \text{ GeV},$$

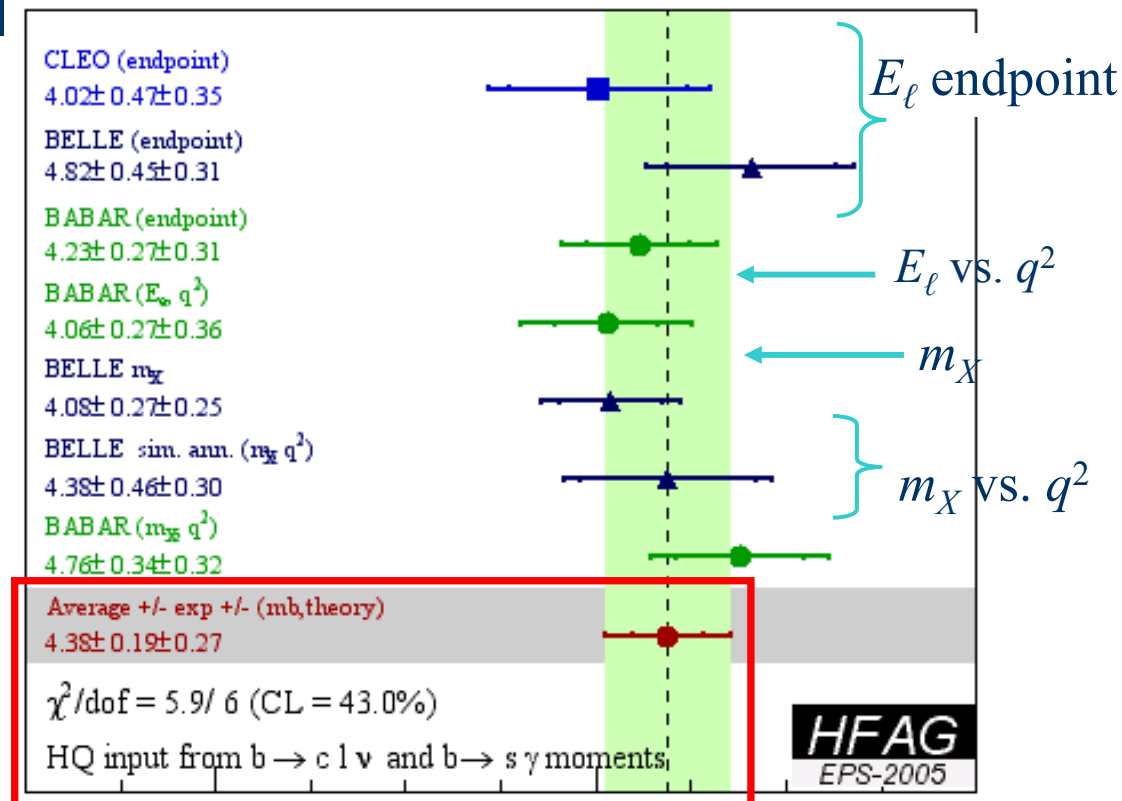
$$\mu_\pi^2 = 0.20 \pm 0.04 \text{ GeV}^2$$

Limited by uncertainties on SF parameters ( $m_b$ )

- Improve inputs from  $b \rightarrow c l \nu$  and  $b \rightarrow s \gamma$
- Improve SF evaluation

Weak annihilation

- Should be small (2%)
- Can be checked with  $B^0/B^+$  comparison



$$\Delta V_{ub}/V_{ub} = (3.3_{\text{expt}} \oplus 2.9_{\text{model}} \oplus 4.7_{\text{SF}} \oplus 4.0_{\text{theory}})\% = 7.6\%$$

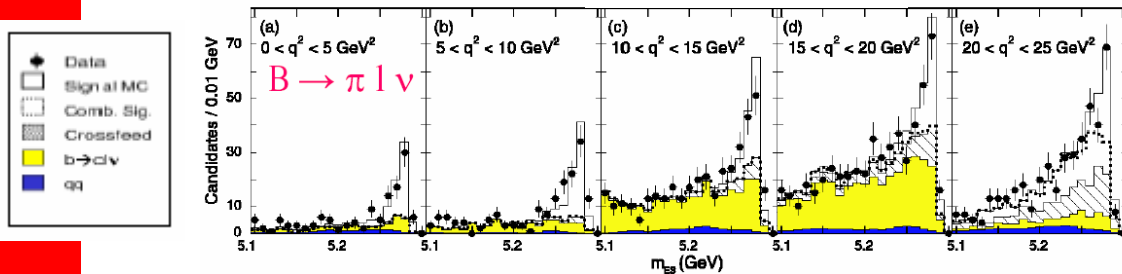
$$|V_{ub}|_{\text{WAvg}} = (4.38 \pm 0.19 \pm 0.27) \times 10^{-3}$$

expt       $m_b, \text{ theory}$

# $V_{ub}$ : exclusive, $B \rightarrow \pi l \nu, \rho l \nu$

Untagged

Binning in  $q^2$



$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.38 \pm 0.10_{stat} \pm 0.18_{syst} \pm 0.08_{FF}) \times 10^{-4}$$

$$B(B^0 \rightarrow \rho^- \ell^+ \nu) = (2.14 \pm 0.21_{stat} \pm 0.53_{syst} \pm 0.28_{FF}) \times 10^{-4}$$

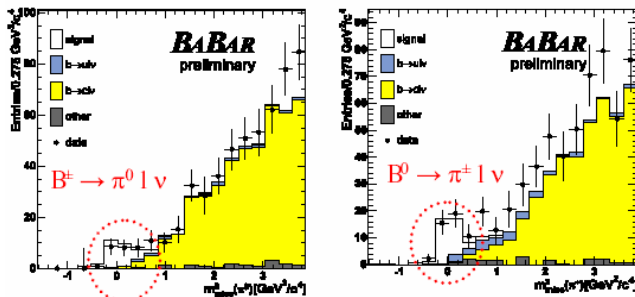
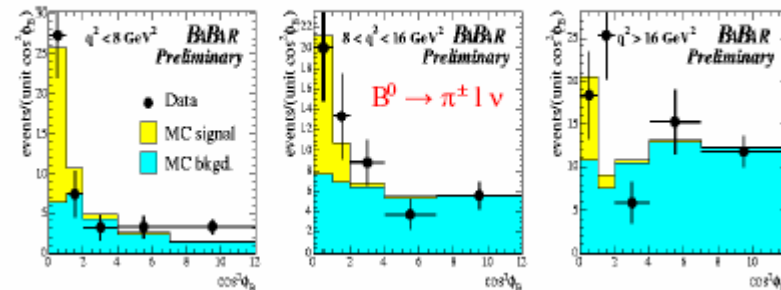
Semileptonic tag

No phase space cut  
Coarse  $q^2$  binning

$$B(B^0 \rightarrow \pi^- \ell^+ \nu) = (1.03 \pm 0.25_{stat} \pm 0.13_{cvt}) \times 10^{-4}$$

$$B(B^+ \rightarrow \pi^0 \ell^+ \nu) = (1.80 \pm 0.37_{stat} \pm 0.23_{syst}) \times 10^{-4}$$

hep-ex/0506064 211 fb<sup>-1</sup>



Hadronic tag

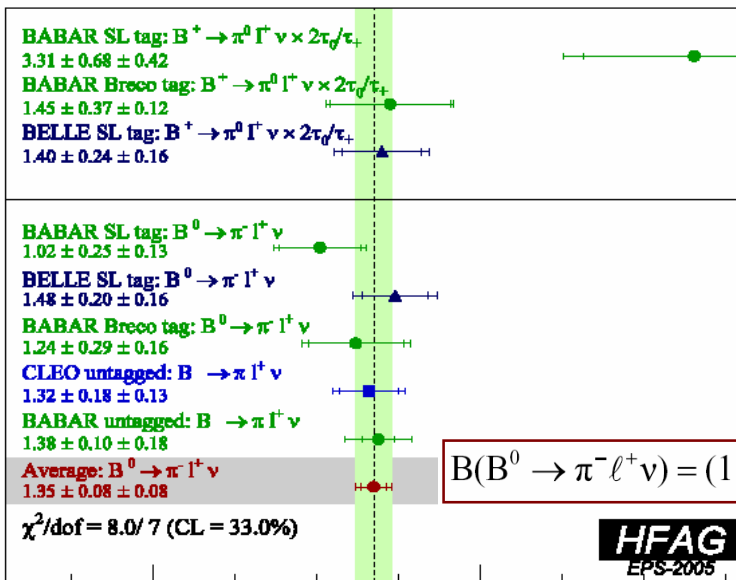
Low background, no phase space cut!!!  
Low signal rate  
More channels in progress:

$\checkmark B \rightarrow \rho l \nu, B \rightarrow \omega l \nu, B \rightarrow \eta l \nu, B \rightarrow \eta' l \nu, B \rightarrow a_0 l \nu$

G. Suvana

# $V_{ub}$ : exclusive results

Full  $q^2$  range  
FNAL LQCD



hadronic tag

$$|V_{ub}| = (3.7 \pm 0.3_{\text{stat}} \pm 0.2_{\text{syst}} \pm 0.5_{\text{FF(LQCD)}}^{+0.8}) \times 10^{-3}$$

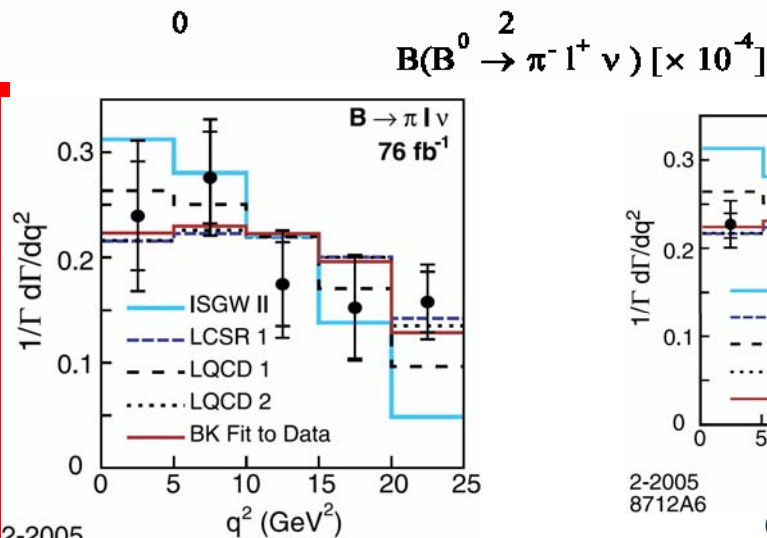
semileptonic tag

$$|V_{ub}| = (3.3 \pm 0.4_{\text{stat}} \pm 0.2_{\text{syst}} \pm 0.4_{\text{FF(LQCD)}}^{+0.8}) \times 10^{-3}$$

untagged

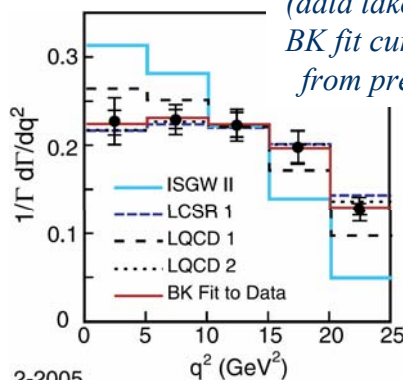
$$|V_{ub}| = (3.82 \pm 0.14_{\text{stat}} \pm 0.24_{\text{syst}} \pm 0.11_{\text{FF-0.52LQCD}}^{+0.88}) \times 10^{-3}$$

$$B(B^0 \rightarrow \pi^- l^+ \nu) = (1.35 \pm 0.08 \pm 0.08) \times 10^{-4}$$



Projection to 1 ab<sup>-1</sup>

(data taken to be on  
BK fit curve  
from present measurement).



2-2005  
8712A6

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In the high  $q^2$  region alone,  
branching fraction at (6-7)% ,  
or (3-3.5)% on  $|V_{ub}|$ .  
Lattice expect to reach 6%



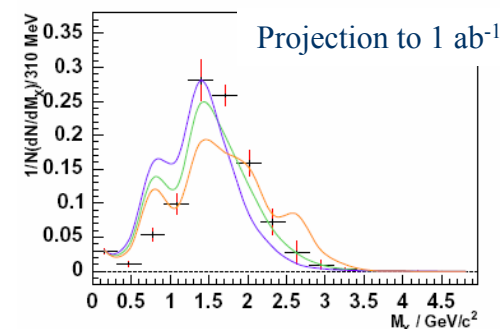
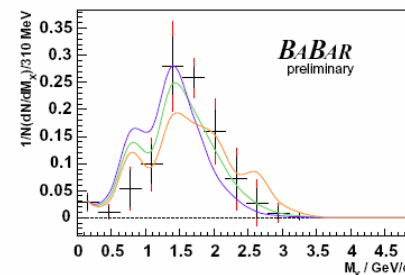
# $V_{ub}$ : outlook

250 fb<sup>-1</sup> → 500 fb<sup>-1</sup>

Inclusive

technique	$\Delta V_{ub}  /  V_{ub} $ (%)	
	Statistical	experimental systematics
$E_1 > 2.0$ GeV	2 → 1	3
$E_1$ vs. $q^2$	3 → 2	4
$M_X$ vs. $q^2$	5 → 3	5

$M_X$  spectrum



Combination of larger dataset and confidence in theory (subleading SF ): 5-7%

Exclusive

	210 fb-1 $\sigma_{exp}$ (%)	1000 fb-1 $\sigma_{exp}$ (%)
hadronic tag	17	9
semileptonic tag	13	9
$\nu$ reconstruction	9	8

Need help from theory: **Uncertainty on  $|V_{ub}|$  dominated by theory error! (~15%)**

➤ Reliable error estimate for plv FF → needed for  $\pi$  and  $\rho$  BF and  $|V_{ub}|$

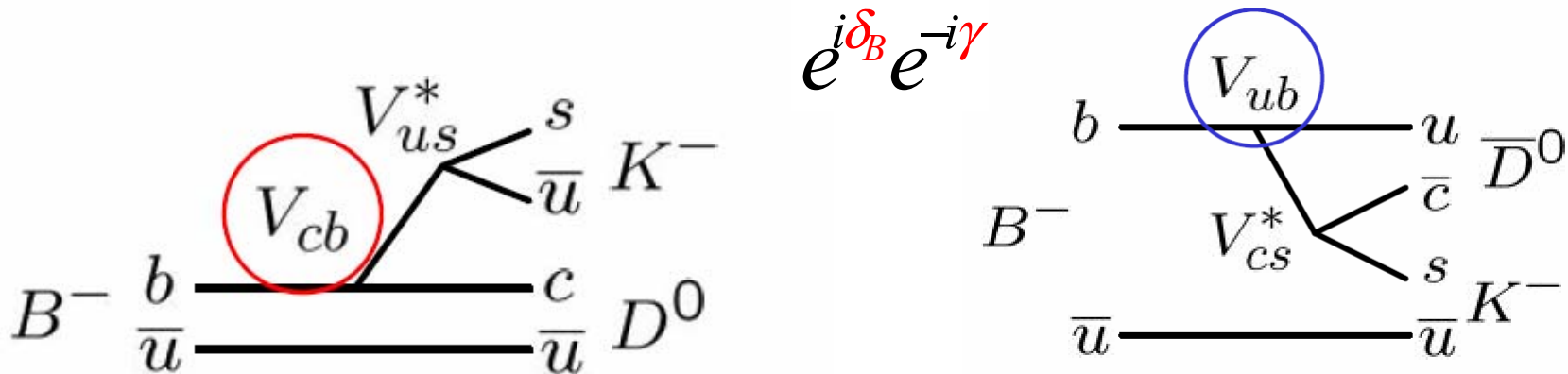
➤ Progress in LQCD for  $\pi l \nu$  : **theory error 6-7% ?**

(Lubicz, Lattice04; Bernard CKMWS 05)

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Big improvements possible  
total error ~ 9%

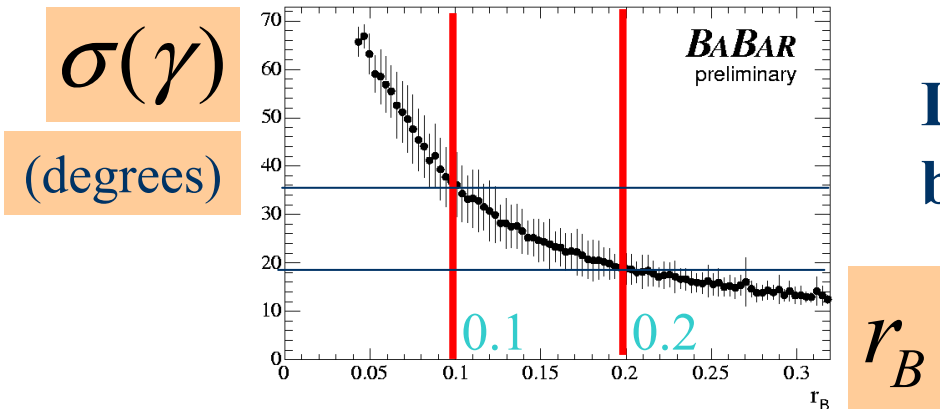
# $\gamma$ from direct CP violation



Interference when  $D$  final state common to both  $\bar{D}^0$  and  $D^0$

Relative size ( $r_B$ ) of  $B$  decay amplitudes

$$r_B = \left| \frac{A(b \rightarrow u)}{A(b \rightarrow c)} \right|$$



Larger  $r_B$ , larger interference,  
better  $\gamma$  experimental precision

## Gronau London Wyler method

### *D decays into CP eigenstate*

*Theoretically clean, but with 8-fold ambiguity*

Select CP-even and CP-odd final states

$$D_{CP\pm}^0 \equiv (D^0 \pm \bar{D}^0) / \sqrt{2}$$

$$R_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{2\Gamma(B^- \rightarrow D^0 K^-)} = 1 \pm 2r_B \cos \gamma \cos \delta_B + r_B^2$$

$$A_{CP\pm} \equiv \frac{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) - \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)}{\Gamma(B^- \rightarrow D_{CP\pm}^0 K^-) + \Gamma(B^+ \rightarrow D_{CP\pm}^0 K^+)} = \pm 2r_B \sin \gamma \sin \delta_B / R_{CP\pm}$$

3 observables, 3 unknowns

$$CP = +1 \quad \pi^+ \pi^-, K^+ K^-$$

$$CP = -1 \quad K_S^0 \pi^0, K_S^0 \phi, K_S^0 \omega, K_S^0 \eta, K_S^0 \eta'$$

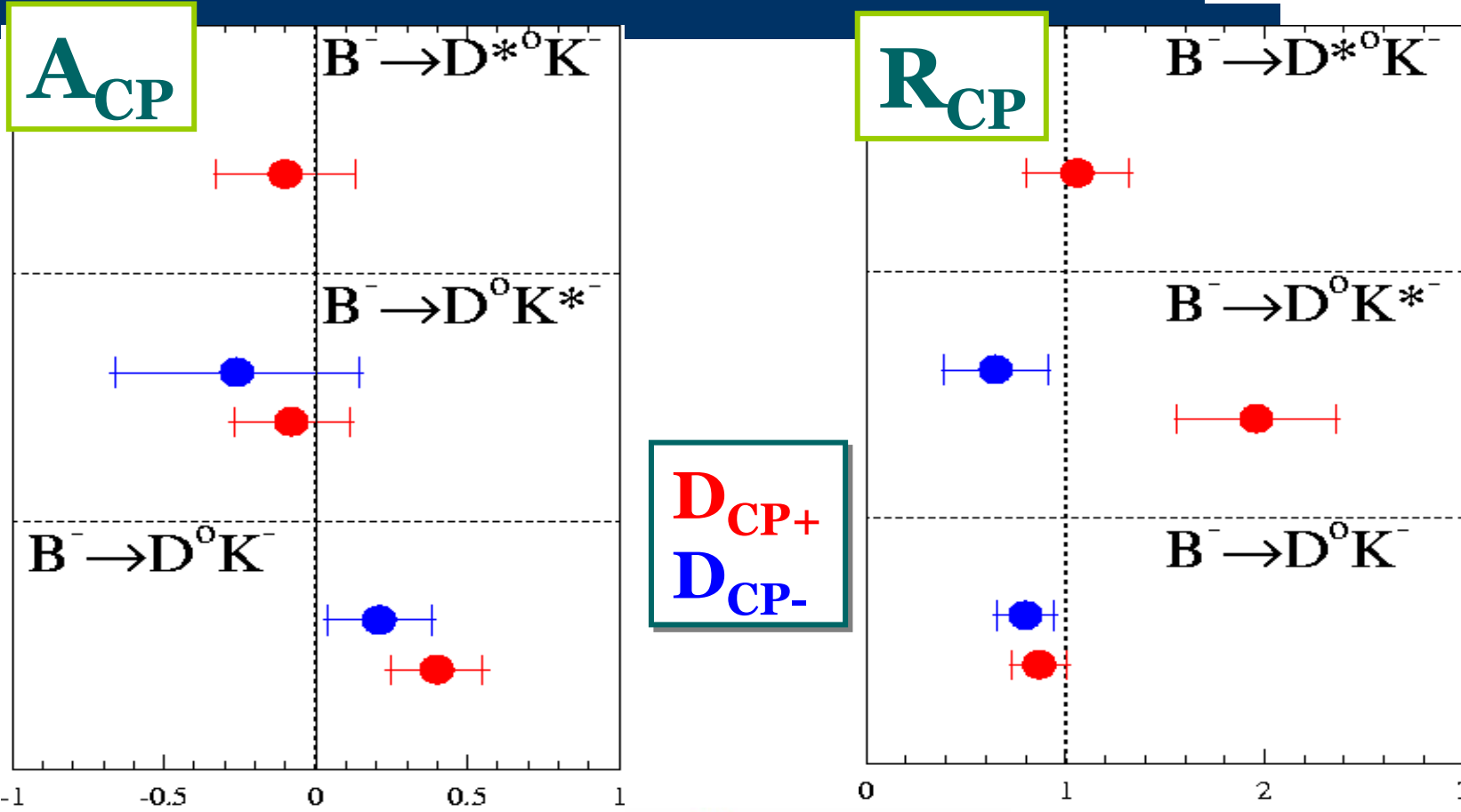
*Experimentally*

- Normalize to  $D^0$  decay into flavour state ( $K^-\pi^+$ )
- CP modes: **small**  $D^0$  branching ratio

# GLW results

PRD71,031102(2005)

Systematic uncertainties hardly visible!



$$\frac{R_{CP+} + R_{CP-}}{2} = 1 + r_B^2$$

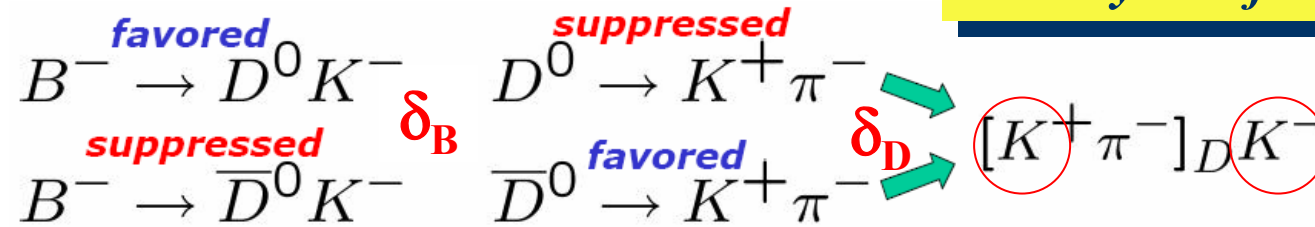
$$\Rightarrow (r_B)^2 (D^0 K^-) = -0.17 \pm 0.16$$

$$\Rightarrow (r_{S_B})^2 (D^0 K^{*-}) = 0.30 \pm 0.25$$

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## Atwood Dunietz Soni method

*D decay into flavor state*



*Count B candidates with opposite sign kaons*

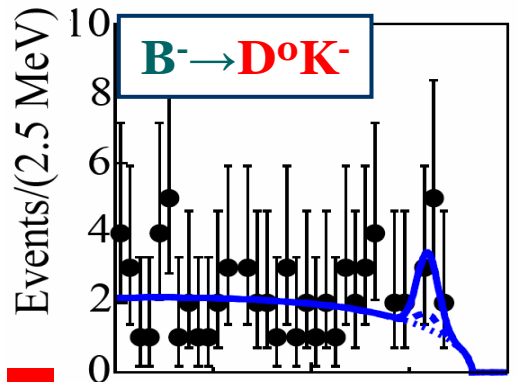
$$R_{ADS} = \frac{Br([K^+ \pi^-]K^-) + Br([K^- \pi^+]K^+)}{Br([K^- \pi^+]K^-) + Br([K^+ \pi^-]K^+)} = r_D^2 + r_B^2 + 2r_B r_D \cos(\delta_D + \delta_B) \cos \gamma$$

$$A_{ADS} = \frac{Br([K^+ \pi^-]K^-) - Br([K^- \pi^+]K^+)}{Br([K^+ \pi^-]K^-) + Br([K^- \pi^+]K^+)} = 2r_B r_D \sin(\delta_D + \delta_B) \sin \gamma / R_{ADS}$$

Input:  $r_D = \frac{|A(D^0 \rightarrow K^+ \pi^-)|}{|A(D^0 \rightarrow K^- \pi^+)|} = 0.060 \pm 0.003$   
Phys.Rev.Lett.91:171801,2003

*D decay strong phase  $\delta_D$  unknown*

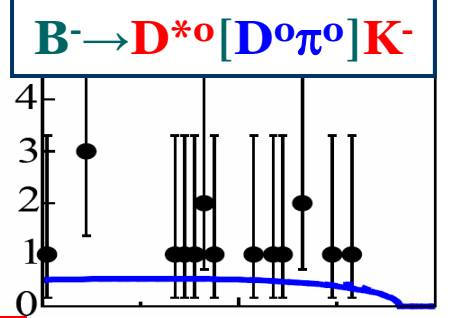
# ADS: results



$$\mathcal{R}_{ADS}^{K\pi} < 0.029^*$$

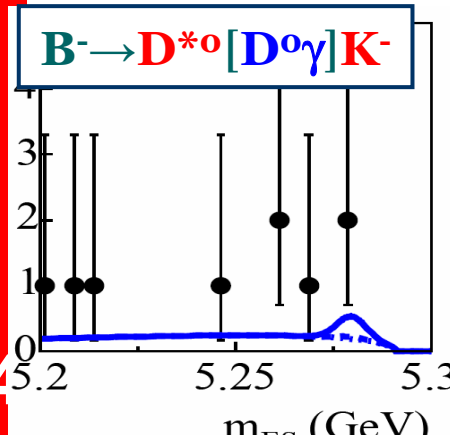
\* @ 90% CL

$\mathcal{R}_{ADS}^{K\pi}$



No DCS signal ...

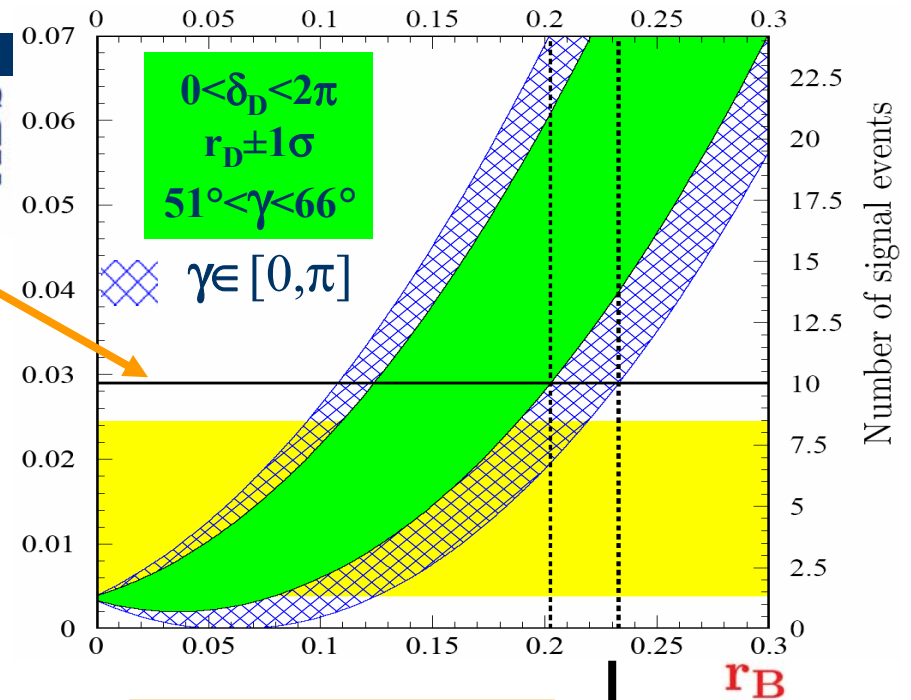
$$\mathcal{R}_{ADS}^{K\pi, D\pi^0} < 0.023^*$$



$$\mathcal{R}_{ADS}^{K\pi, D\gamma} < 0.045^*$$

Bondar & Gershon  
PRD70,091503(2004)

$\Rightarrow D^{*0} \rightarrow D^0 \pi^0 / D^0 \gamma$   
 $\neq$  in  $\delta_{D^*}$  by  $\pi$



$r_B < 0.23$  @ 90% CL

$$\frac{\mathcal{R}_{ADS}^{K\pi, D\pi^0} + \mathcal{R}_{ADS}^{K\pi, D\gamma}}{2} - r_D^2 = r_B^{*2}$$

$(r_B^*)^2 < (0.16)^2$  @ 90% CL  
(Bayesian  $r_B^{*2} > 0$  & uniform,  $\forall \gamma$  and  $\delta_D^*$ )

Giri, Grossman, Soffer, & Zupan, PRD 68, 054018 (2003),  
 Bondar (Belle), PRD 70, 072003 (2004)

*If we knew the charm phase shift  $\delta_D$ ?*

## $B^- \rightarrow D^{(*)0} K^- \quad D^0(K_S \pi \pi)$ Dalitz analysis

*Amplitude for  $B^-/B^+ \rightarrow "D^0" K^-/K^+$*

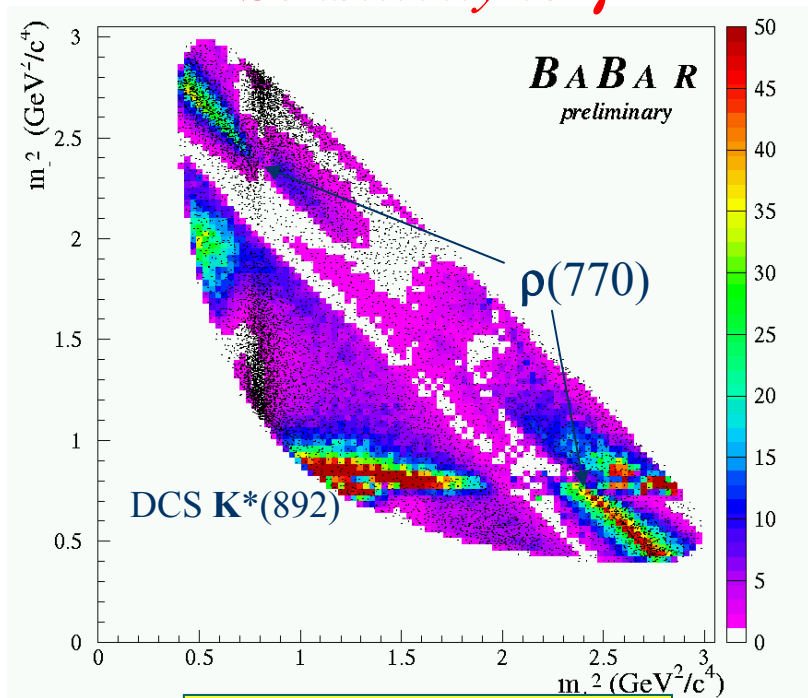
$$M_-(m_-^2, m_+^2) = \mathbf{f}(m_-^2, m_+^2) + r_B e^{i(\delta_B - \gamma)} \mathbf{f}(m_+^2, m_-^2)$$

$$m_-^2 = M(K_S^0 \pi^-)^2$$

$$M_+(m_-^2, m_+^2) = \mathbf{f}(m_+^2, m_-^2) + r_B e^{i(\delta_B + \gamma)} \mathbf{f}(m_-^2, m_+^2)$$

$$m_+^2 = M(K_S^0 \pi^+)^2$$

*Sensitivity to  $\gamma$*



Isobar model for  $\mathbf{f}(m_+^2, m_-^2)$   
 can fix phase variation  
 $\delta_D$  across Dalitz plot.

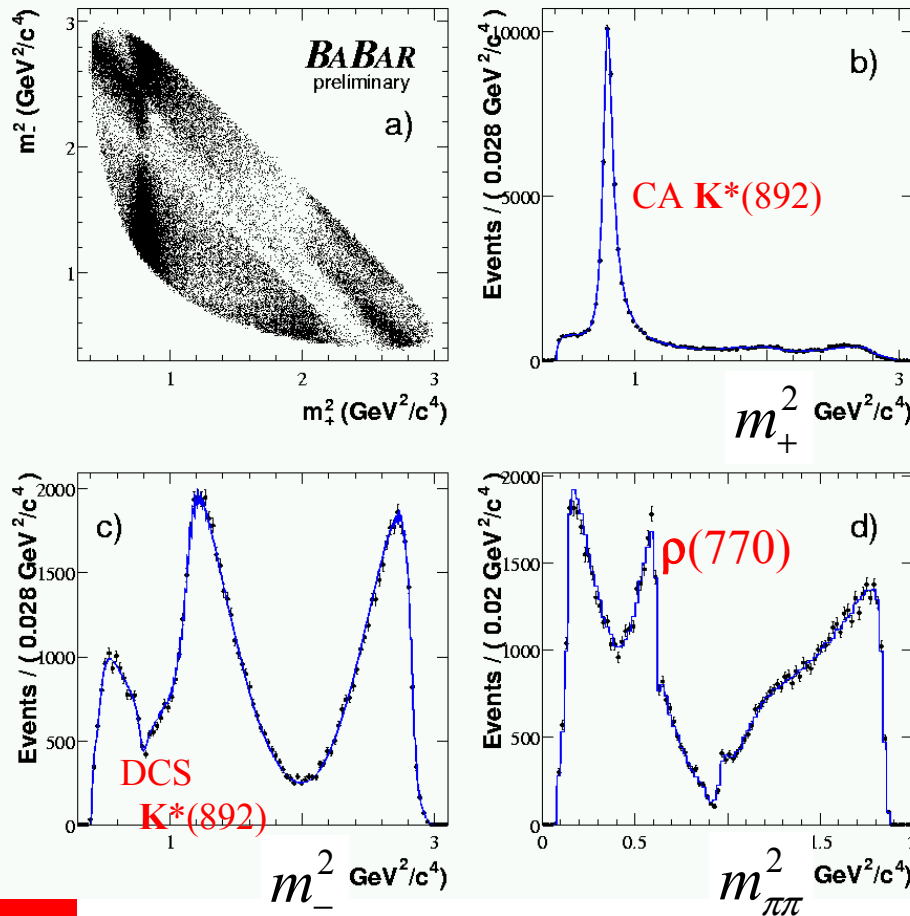
Only two-fold ambiguity  
 in  $\gamma$  extraction

$$\gamma = 75, \delta = 180, r_B = 0.125$$

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Determined on  $D^* \rightarrow D^0 \pi$  sample

# $\bar{D}^0(K_S \pi^+ \pi^-)$ Dalitz model



**D<sup>0</sup> decay model**  $\equiv$  coherent sum of **Breit-Wigner (BW) amplitudes** (quasi 2 body terms).

**13 distinct resonances (3 WS DCS) + 1 NR term.** This isobar model is **not so good for  $\pi\pi$  S waves**  $\Rightarrow$  need controversial  **$\sigma(500) / \sigma'(1000)$**  to describe reasonably well the data.

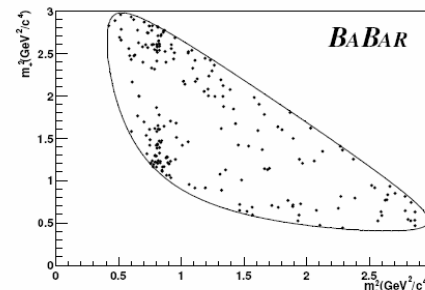
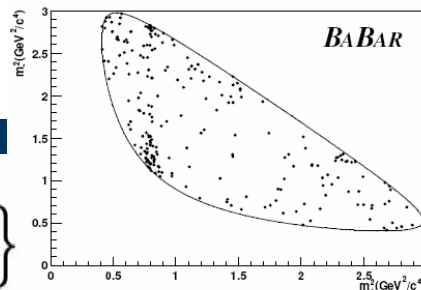
**Better description of quasi 2-body terms:**  
**BW +  $\pi\pi$  S-waves with K-matrix formalism**

Anisovich & Saratev  
Eur. Phys. J A16, 229 (2003)



# $\gamma$ from Dalitz

$$(x_{\pm}, y_{\pm})^{(*)} \equiv (\text{Re}, \text{Im}) \left\{ r_B^{(*)} e^{i(\delta_B^{(*)} \pm \gamma)} \right\}$$

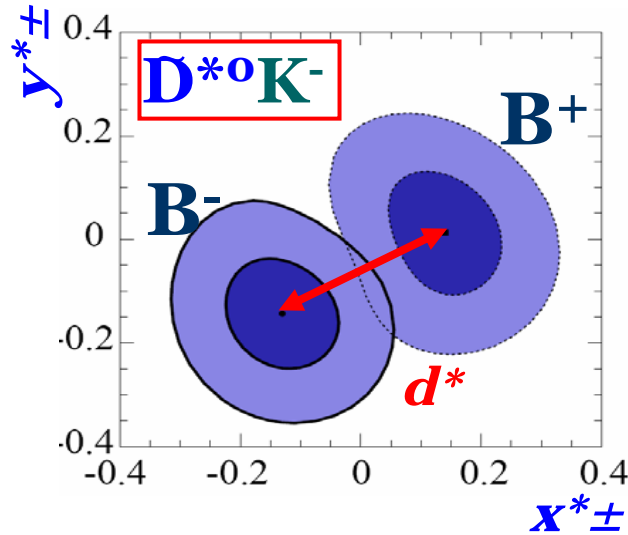
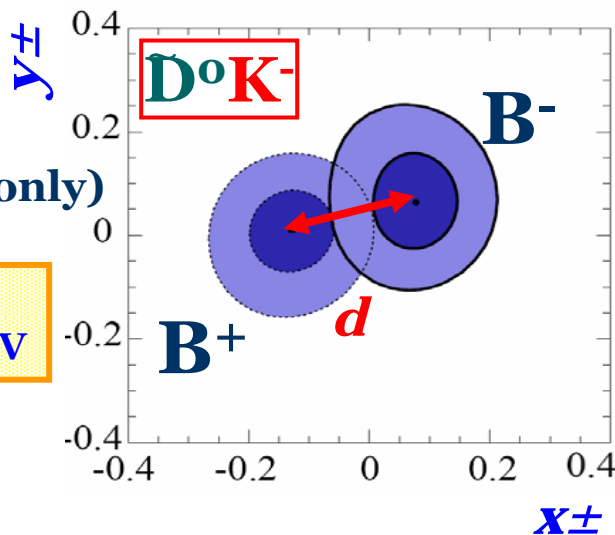


2D

2  $\sigma$  CL

1  $\sigma$  CL (stat. only)

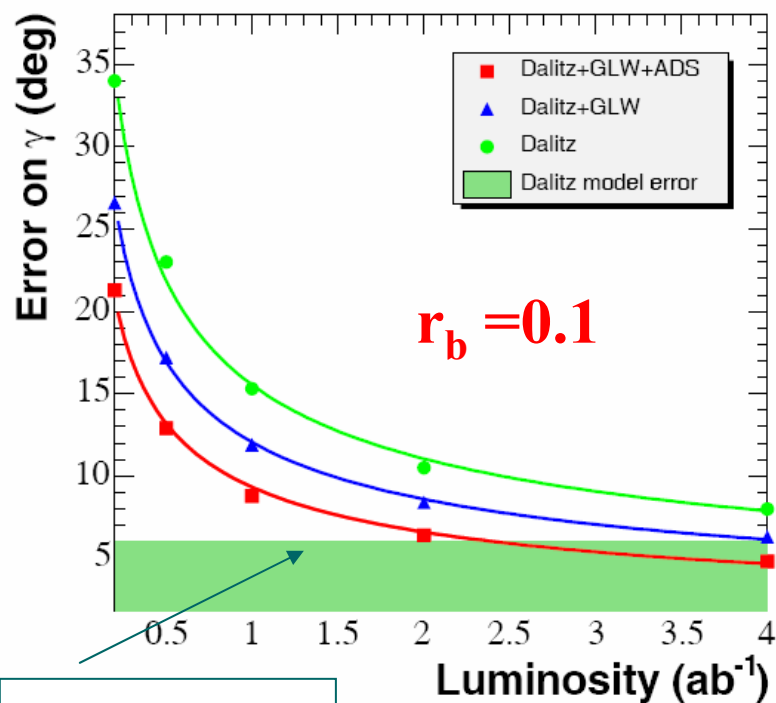
$d \equiv 2 r_B |\sin \gamma| \neq 0$   
 $\Rightarrow$  size of direct CPV



$$\gamma = [67^\circ \pm 28^\circ (\text{stat.}) \pm 13^\circ (\text{syst. exp.}) \pm 11^\circ (\text{Dalitz model}^*) ]$$

\*evaluated removing  $\pi\pi$  S-wave  
 $3^\circ$  for **K-matrix** / **BW difference**

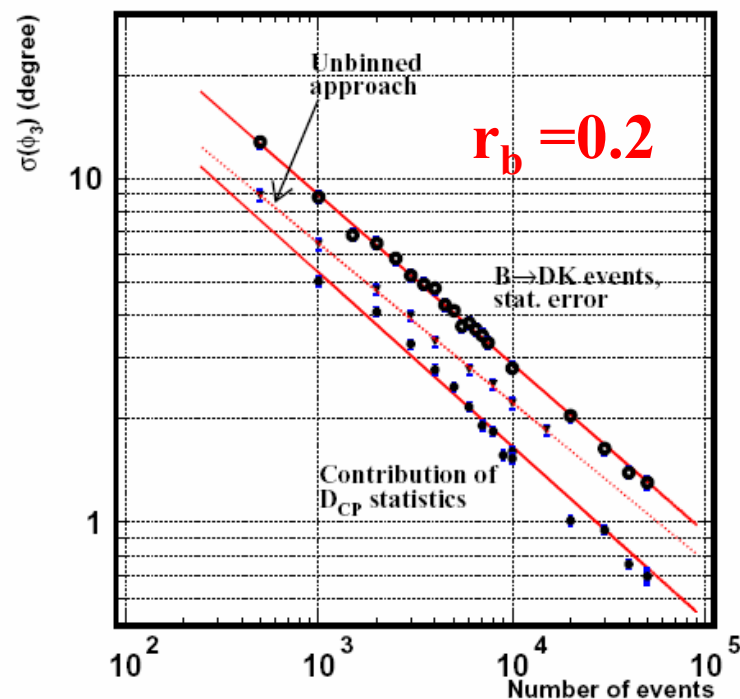
# Projected $\gamma$ uncertainty



Projected sys error due to  $D^0$  Dalitz plot

## Model independent approach

A. Bondar and A. Poluektov, hep-ph/0510246

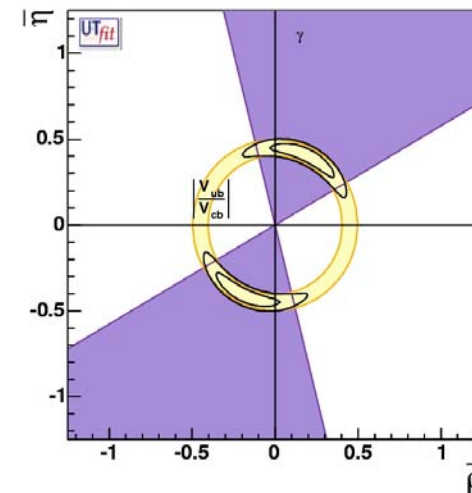


Charm and (super)B-factory interplay

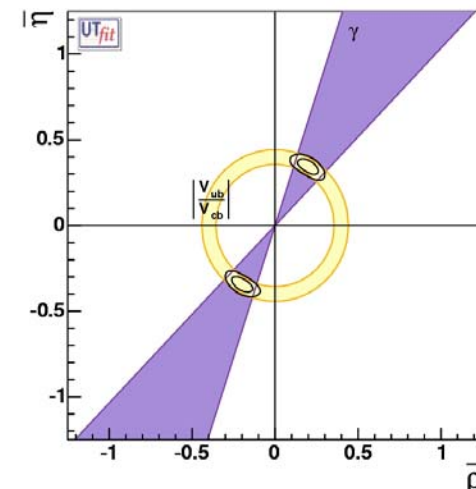
# Summary

- Many different and independent techniques to constrain  $V_{ub}$  and  $\gamma$
- By 2008  $1 \text{ ab}^{-1}/\text{B-factory}$ 
  - $V_{ub}$  inclusive: 5-6%
  - $V_{ub}$  exclusive : dominated by theoretical error  
total error 8% (?)
  - $\gamma$ 
    - Dalitz technique most promising
      - $r_b$  critical parameter for sensitivity
      - Dalitz model limit at  $5^\circ$  ?
      - More stat for model indep.
    - Including more modes/techniques adds to  $1/\sqrt{N}$  improvements

2005



2008

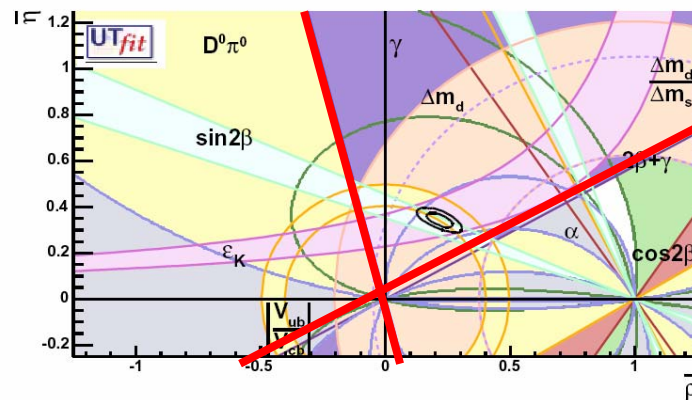


# Backup slides

0

# UT in 2008

2005



2008

