

Slepton Flavour Violation

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Flavour in the Era of the LHC, CERN, Nov 2005

- **minimal scenario:** MSSM + 3 families of right-handed neutrino singlet fields ν_R

- superpotential $W \supset W_\nu = \frac{1}{2} \nu_R^{cT} M \nu_R^c + \nu_R^{cT} Y_\nu L \cdot H_2$

- EWSB \rightarrow Dirac mass $m_D = Y_\nu \langle H_2 \rangle \ll$ Majorana mass scale M_R

- neutrino mass matrix $\frac{1}{2} \begin{pmatrix} \overline{\nu_L} & \overline{\nu_R^c} \end{pmatrix} \begin{pmatrix} 0 & m_D^T \\ m_D & M \end{pmatrix} \begin{pmatrix} \nu_L^c \\ \nu_R \end{pmatrix}$

light neutrinos: $M_\nu = -m_D^T M^{-1} m_D \sim \frac{\langle H_2 \rangle^2}{M_R}$

heavy neutrinos: $M \sim M_R$

- diagonalization in flavour space

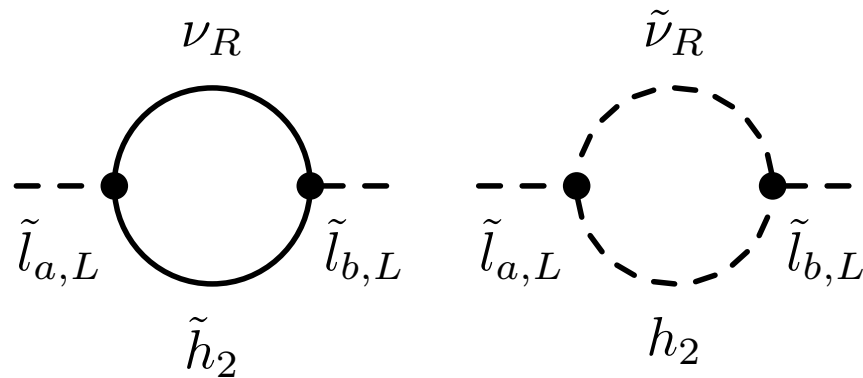
$$U^T M_\nu U = \text{diag}(m_1, m_2, m_3)$$

$$U = \text{diag}(e^{i\phi_1}, e^{i\phi_2}, 1) V(\theta_{12}, \theta_{13}, \theta_{23}, \delta)$$

masses and mixing angles from experiment

in MSUGRA:
$$m_{\tilde{l}}^2 = \begin{pmatrix} m_{\tilde{l}_L}^2 & m_{\tilde{l}_{LR}}^{2\dagger} \\ m_{\tilde{l}_{LR}}^2 & m_{\tilde{l}_R}^2 \end{pmatrix} = \tilde{m}_{MSSM}^2 + \begin{pmatrix} \delta m_L^2 & \delta m_{LR}^{2\dagger} \\ \delta m_{LR}^2 & \delta m_R^2 \end{pmatrix}$$

flavor non-diagonal terms generated by renormalization from M_{GUT} to M_R



$$\begin{aligned} \delta m_L^2 &\simeq -\frac{1}{8\pi^2} (3m_0^2 + A_0^2) Y_\nu^\dagger L Y_\nu \\ \delta m_R^2 &\simeq 0 \text{ (model specific)} \\ \delta m_{LR}^2 &\simeq -\frac{3A_0}{16\pi^2} Y_l Y_\nu^\dagger L Y_\nu v \cos \beta \end{aligned}$$

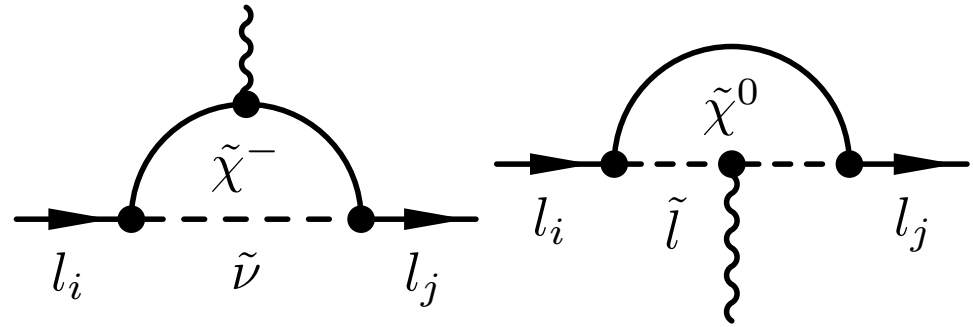
with $L = D \left(\ln \left(\frac{M_{GUT}}{M_i} \right) \right)$ and

neutrino Yukawa coupling matrix ($R = R^T$ undetermined complex matrix)

$$Y_\nu = \frac{1}{v \sin \beta} D(\sqrt{M_i}) R D(\sqrt{m_j}) U^\dagger$$

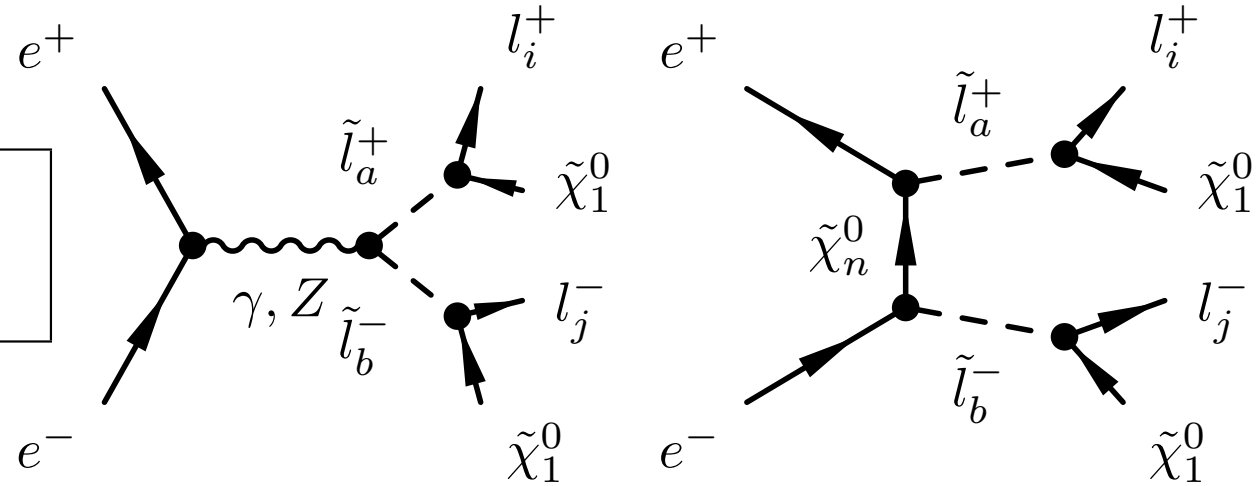
for degenerate M_i and real R :
$$Y_\nu^\dagger L Y_\nu = \frac{M_R}{v^2 \sin^2 \beta} V \cdot D(m_i) \cdot V^\dagger \ln \frac{M_{GUT}}{M_R}$$

$$\mu \rightarrow e\gamma, \tau \rightarrow e\gamma, \tau \rightarrow \mu\gamma$$



$$\Gamma(l_i \rightarrow l_j \gamma) \propto \alpha^3 m_{l_i}^5 \frac{|(\delta m_L)_{ij}^2|^2}{\tilde{m}^8} \tan^2 \beta \propto M_R^2 \text{ for fixed neutrino masses}$$

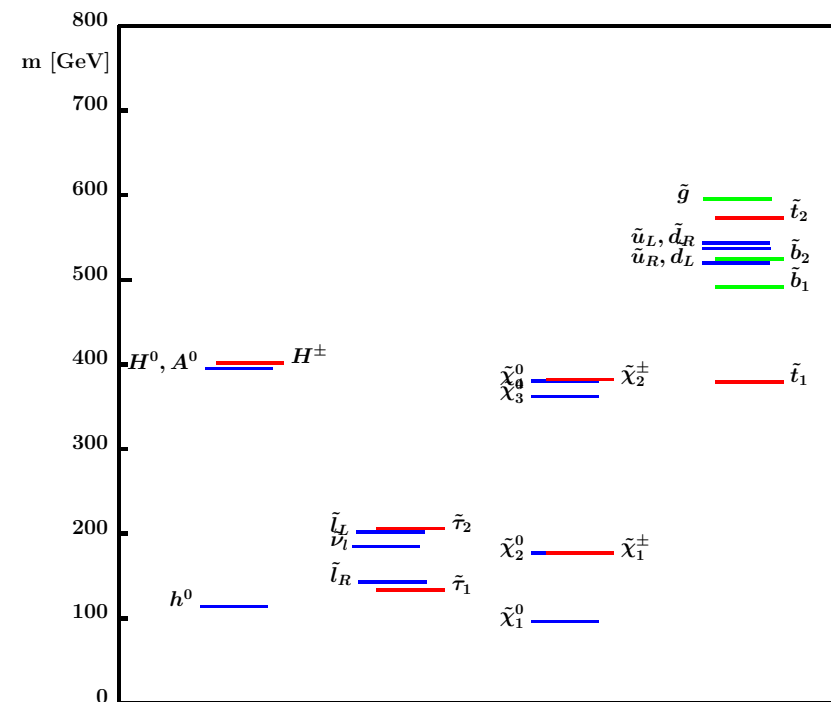
$$e^+ e^- \rightarrow l_i^+ l_j^- + 2\tilde{\chi}_1^0$$



$$\sigma(l_i^+ l_j^-) \propto \frac{|(\delta m_L)_{ij}^2|^2}{\tilde{m}^2 \Gamma_{\tilde{l}}^2} \sigma(e^+ e^- \rightarrow \tilde{l}_a^+ \tilde{l}_b^-) Br(\tilde{l}_a^+ \rightarrow l_i^+ \tilde{\chi}_1^0) Br(\tilde{l}_b^- \rightarrow l_j^- \tilde{\chi}_1^0)$$

Scenario	$m_{1/2}/\text{GeV}$	m_0/GeV	$\tan \beta$	A_0/GeV	$\text{sign}\mu$
B'	250	60	10	0	+
C'	400	85	10	0	+
G'	375	115	20	0	+
I'	350	175	35	0	+
SPS1a	250	100	10	-100	+

- MSUGRA benchmark models
B',...I' (*Battaglia et al., hep-ph/0306219*)
SPS1a (<http://spa.desy.de/spa>)
- universal scalar masses keep LFV small



$$\Delta m_{12}^2 = 6.9_{-0.36}^{+0.36} \cdot 10^{-5} \text{ eV}^2$$

$$\Delta m_{13}^2 = 2.6_{-1.2}^{+1.2} \cdot 10^{-3} \text{ eV}^2$$

$$\tan^2 \theta_{12} = 0.43_{-0.22}^{+0.47}$$

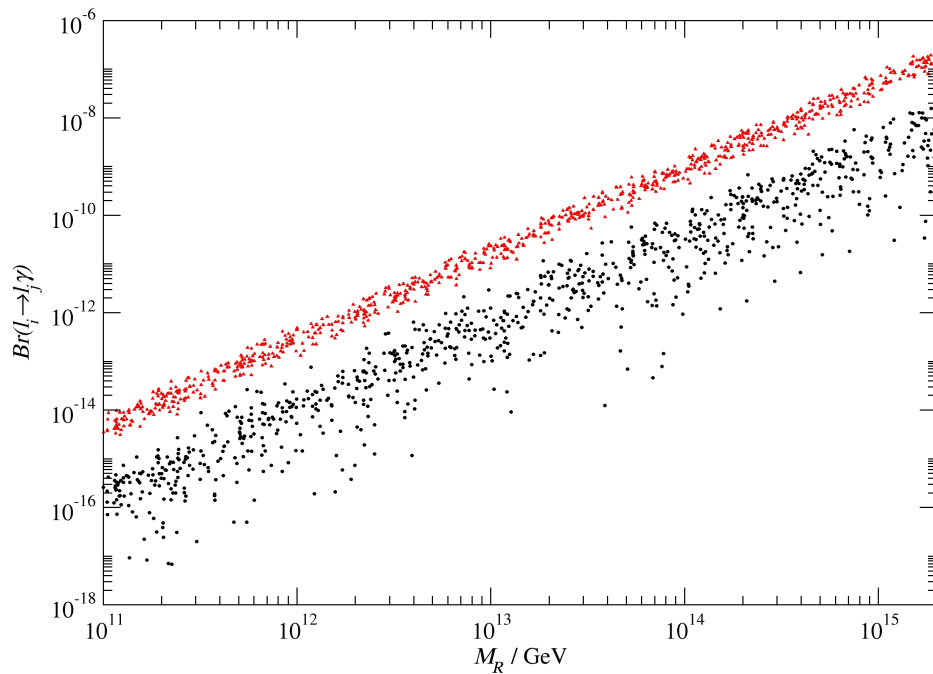
$$\tan^2 \theta_{23} = 1.10_{-0.60}^{+1.39}$$

$$\tan^2 \theta_{13} = 0.006_{-0.006}^{+0.001}$$

- central values from [M. Maltoni et al., PRD68\(2003\)113010](#)
- 90% C.L. errors as anticipated for running/proposed experiments
- Dirac phase unconstrained
- absolute mass scale $m_1 \leq 0.03 \text{ eV}$
- **degenerate Majorana masses, real R-matrix**
18 \rightarrow 8 parameters $(m_i, \theta_i, \delta, M_R)$

$$Br(\mu \rightarrow e\gamma) \text{ and } Br(\tau \rightarrow \mu\gamma)$$

SUSY scenario SPS1a, uncertainties from neutrino data



related LFV decays:

$$\frac{Br(\tau \rightarrow 3\mu)}{Br(\tau \rightarrow \mu\gamma)} \approx 2 \cdot 10^{-3}$$

$$\frac{Br(\mu \rightarrow 3e)}{Br(\mu \rightarrow e\gamma)} \approx 7 \cdot 10^{-3}$$

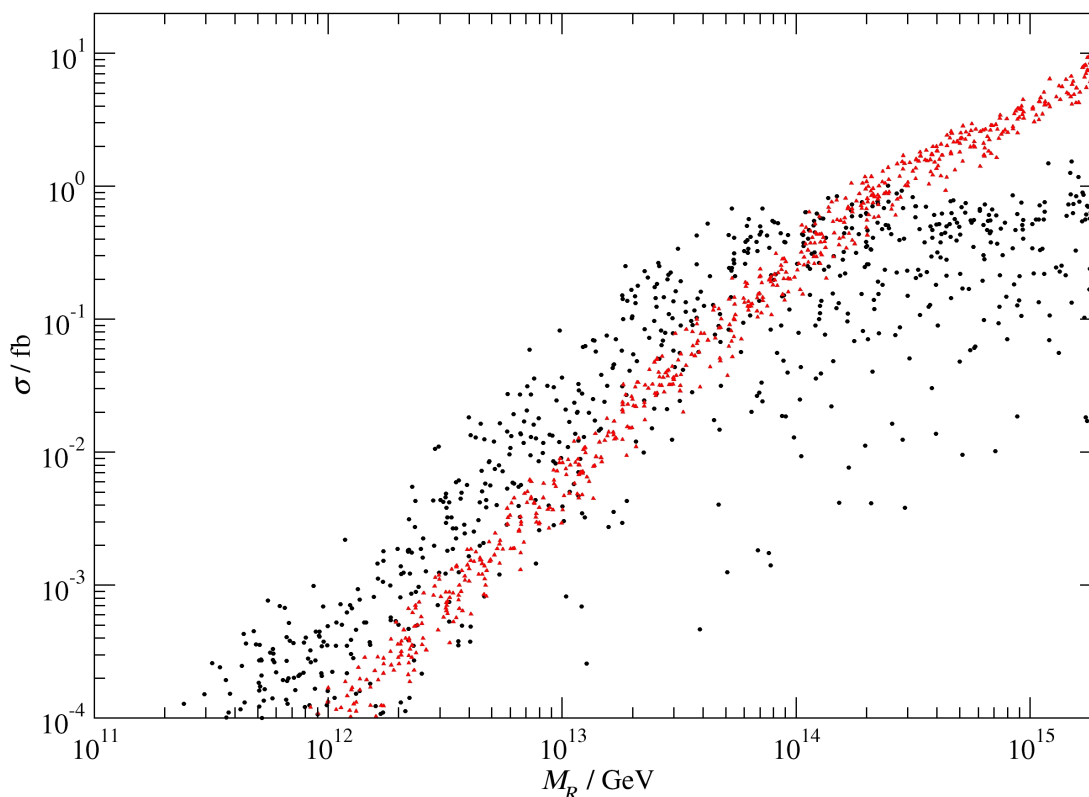
$$Br(\tau \rightarrow \mu\gamma) < 6.8 \cdot 10^{-8} \quad (90\% \text{ C.L., BABAR 2005})$$

$$Br(\mu \rightarrow e\gamma) < 1.2 \cdot 10^{-11} \quad (90\% \text{ C.L., PDG 2004})$$

LFV Slepton Pair Production and Decay at the ILC

$$\sigma(e^+e^- \rightarrow \mu^+e^-(\tau^+\mu^-) + 2\tilde{\chi}_1^0)$$

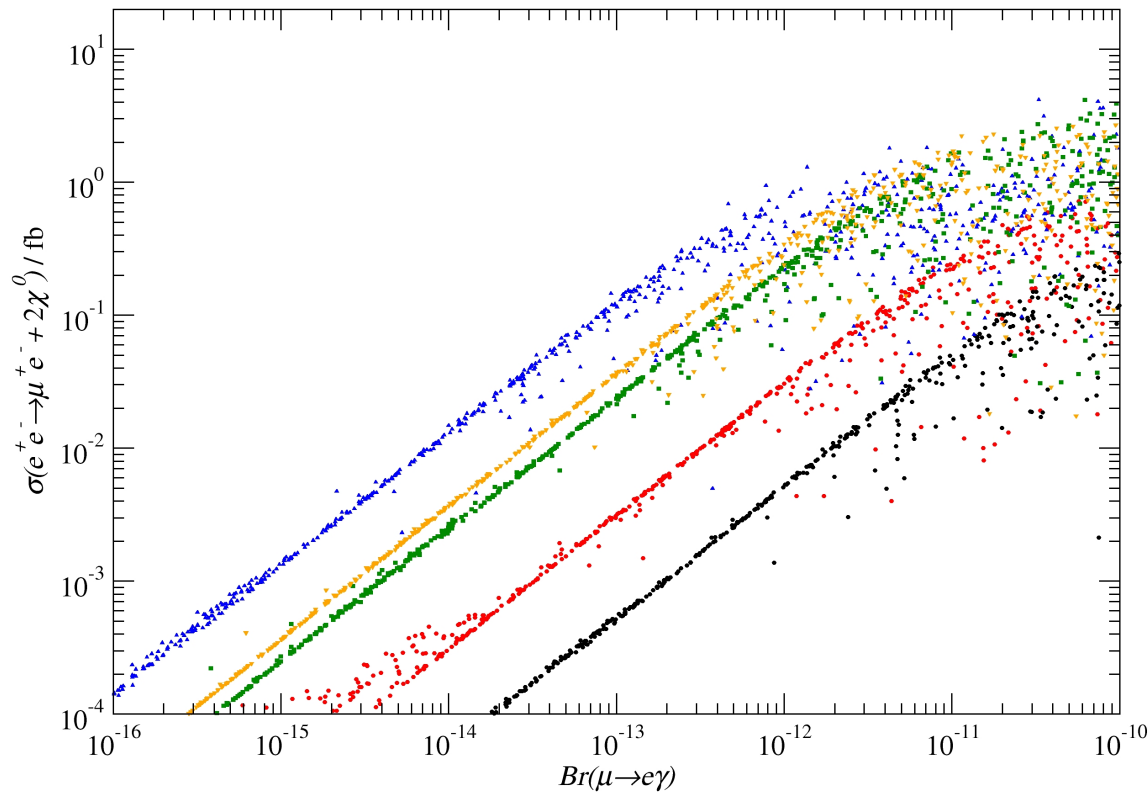
SUSY scenario SPS1a, $\sqrt{s} = 500$ GeV, unpolarized



direct production only, neutralino and chargino cascades not included

SUSY points C', G', B', SPS1a, I'

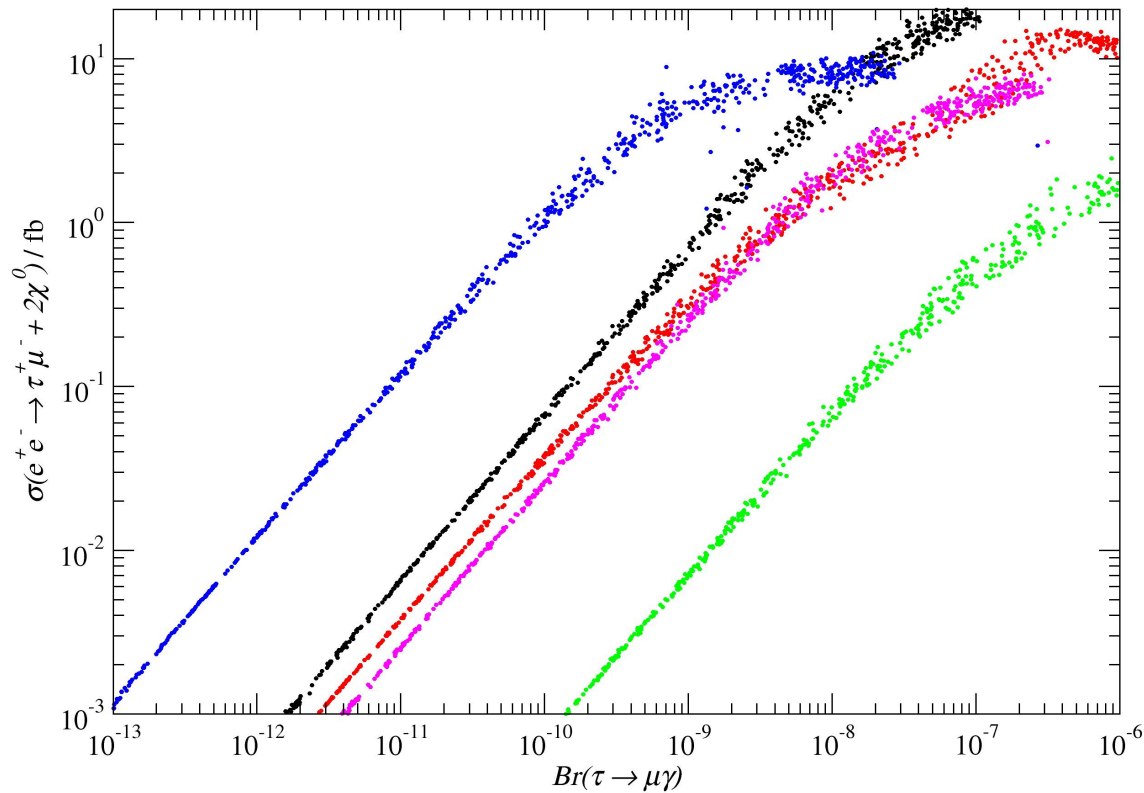
$$\sqrt{s} = 800 \text{ GeV}$$



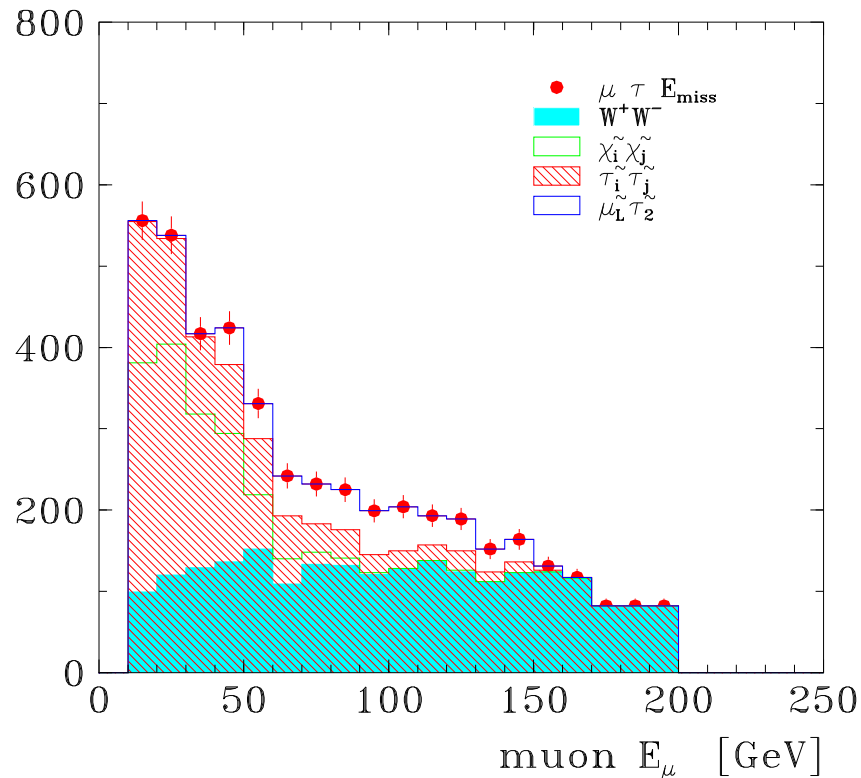
$Br(\mu \rightarrow e\gamma) > 10^{-12}$ implies $\sigma(e^+e^- \rightarrow \mu e + 2\tilde{\chi}_1^0) > 0.01$ to 1 fb

SUSY points C', B', SPS1, G', I'

$$\sqrt{s} = 800 \text{ GeV}$$



$Br(\tau \rightarrow \mu\gamma) < 6.8 \cdot 10^{-8}$ implies $\sigma(e^+e^- \rightarrow \tau\mu + 2\tilde{\chi}_1^0) < 0.3 \text{ to } 20 \text{ fb}$

$\tau\mu$ final statesSUSY scenario SPS1a, $\sqrt{s} = 500$ GeV, unpolarized, 500 fb^{-1} 

- 4 fb signal cross section (flat lepton energy spectrum)
- SM+MSSM background (soft E_μ spectrum)
- standard selection criteria (τ identification via hadronic decays, 25% efficiency)
- $\sigma(\tilde{\tau}_2 \tilde{\mu}_L) = 2 \text{ fb} \rightarrow 5\sigma$ effect

H.-U. Martyn (2004)

defining benchmark models:

MSSM, NMSSM, SUSY breaking, GUT relations,
RPV, seesaw mechanism (type I, II),

constraining parameters:

rare processes, $g-2$, EDM, leptogenesis,

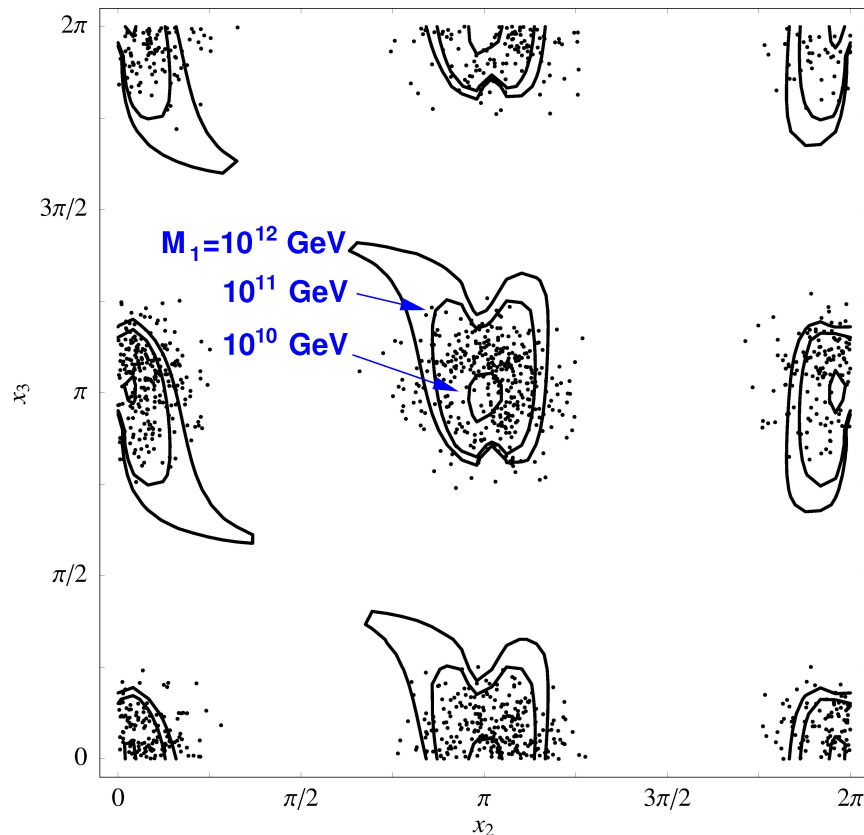
DPRR (2005) to appear

investigating search channels:

lepton-photon, dilepton, trilepton,

generation of lepton asymmetry in **out-of-equilibrium decays of N_1**
 later on transformation to baryon asymmetry through **sphaleron processes**

$$\eta_B = \frac{n_B - n_{\bar{B}}}{n_\gamma} = (6.3 \pm 0.3) \cdot 10^{-10}$$



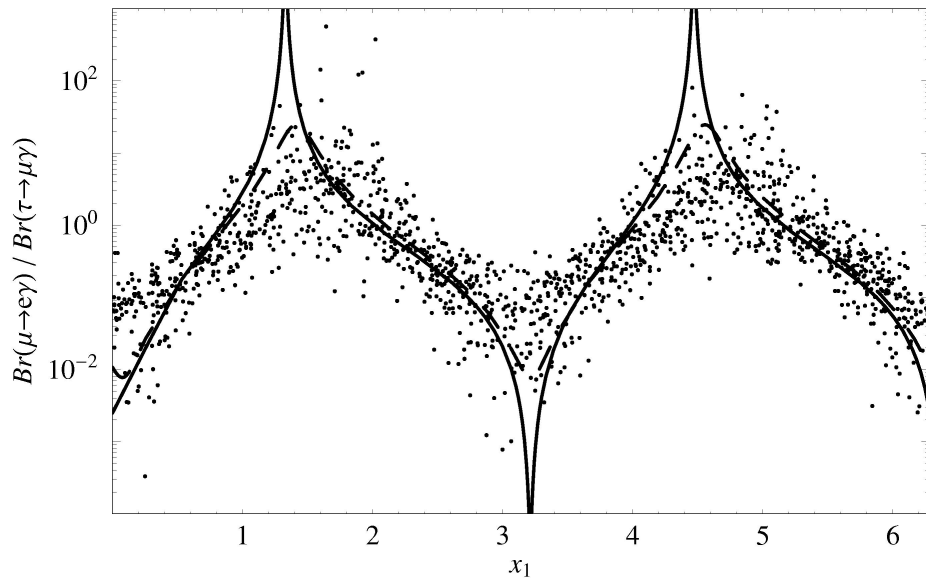
$$Y_\nu = \frac{1}{v \sin \beta} D(\sqrt{M_i}) \mathbf{R} D(\sqrt{m_j}) U^\dagger$$

$$M_1 \ll M_2 \ll M_3, M_1 \leq 10^{11}$$

$$\mathbf{R}(\cos(x_j + iy_j), \sin(x_j + iy_j), j = 1, 2, 3)$$

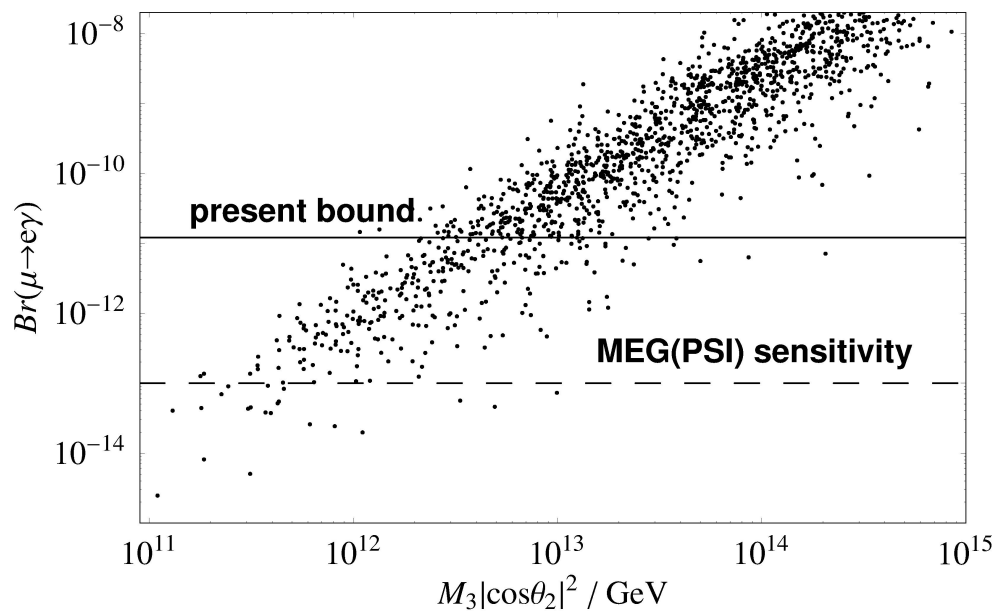
- $0 \leq x_1 \leq 2\pi$
- $10^{-3} < y_i < \mathcal{O}(1)$
- contours with $y_i = 0.1$

$$\Rightarrow x_2, x_3 \simeq n\pi$$



$\Rightarrow x_1$

- successful leptogenesis
- $x_{2,3} \simeq n\pi$
- $0 \leq x_1 \leq 2\pi$
- $10^{-3} < y_i < \mathcal{O}(1)$
- $y_i = 0.01$ (solid), 0.1 (dashed)



$\Rightarrow M_3 \lesssim 10^{13} \text{ GeV}$

very different scenarios

- selected SUSY points or scans in parameter space
- LFV only in L or R sector, 2 or 3 flavour mixing
- maximal LFV allowed by present experimental bounds
- seesaw mechanism and neutrino data

LFV radiative decays: $W \rightarrow \tau\nu, \tau \rightarrow \mu\gamma$
Serin, Stoyanowski, ATLAS Internal Note (1997)

- signal: $M(\mu\gamma) = m_\tau$
- background: QED radiation in production and decay
- reach (30 fb^{-1}): $Br(\tau \rightarrow \mu\gamma) \simeq 6 \cdot 10^{-7}$

direct DY production of sleptons: $\tilde{l}_i \tilde{l}_i \rightarrow l_j l_k 2\tilde{\chi}_1^0$
Bityukov, Krasnirov, hep-ph/9712358
Agashe, Graesser, hep-ph/9904422

- signal: dileptons of different flavour and large missing p_T
- background: $t\bar{t}, W^+W^-, \chi^+\chi^-$
- generally very difficult

LFV neutralino and slepton decays: $\tilde{g}, \tilde{q} \rightarrow \tilde{\chi}_2^0 \rightarrow \tilde{l}_i l_j \rightarrow \tilde{\chi}_1^0 l_k l_j$

Agashe, Graesser, hep-ph/9904422

Hinchliffe, Paige, hep-ph/0010086

Hisano et al., PRD D65(2002)116002

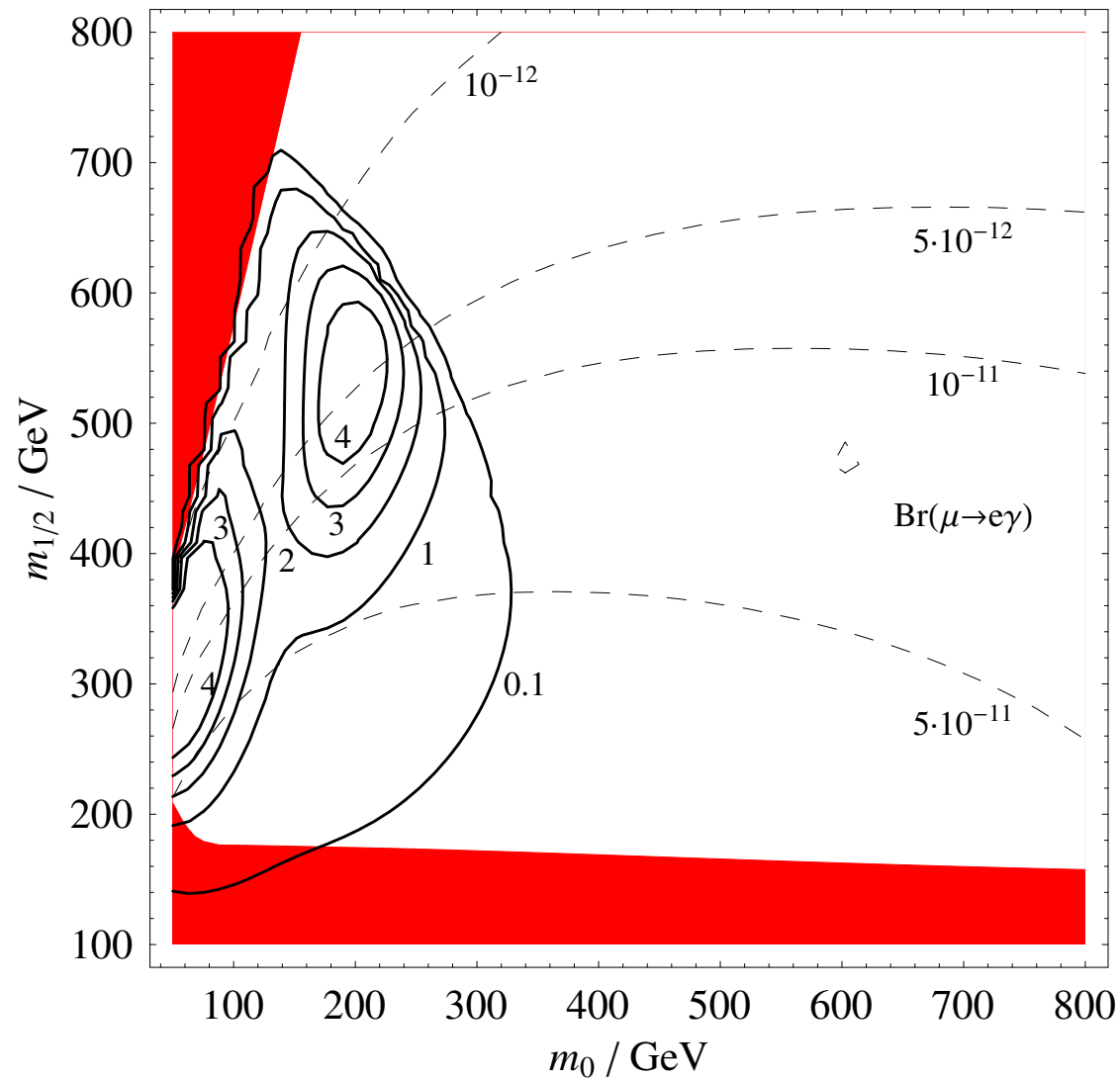
Carvalho et al., hep-ph/0206148

Bartl et al., hep-ph/0510074

- signal: dilepton mass distribution
- background: $t\bar{t}$, SUSY channels
- reach (30 fb^{-1}): $Br(\tilde{\chi}_2^0 \rightarrow \tilde{\chi}_1^0 l_k l_j) \simeq 2 \text{ to } 4 \%$
- complementary to or more sensitive than radiative decays

$A_0 = 0, \tan \beta = 5, \text{sign} \mu = +$

$\sigma(e_L^+ e_R^- \rightarrow \mu^+ e^- + 2\tilde{\chi}_1^0) / \text{fb}, \sqrt{s} = 800 \text{ GeV}$



ratios of branching ratios

$$\frac{Br(l_i \rightarrow l_j \gamma)}{Br(l_{i'} \rightarrow l_{j'} \gamma)} \sim \frac{m_{l_i}^5 \Gamma_{i'}}{m_{l_{i'}}^5 \Gamma_i} \frac{\left| (Y_\nu^\dagger L Y_\nu)_{ij} \right|^2}{\left| (Y_\nu^\dagger L Y_\nu)_{i'j'} \right|^2}$$

Example:

- hierarchical light neutrinos, central best-fit values for neutrino parameters
- vanishing Dirac/Majorana phases, $R = 1$
- SUSY scenario C

Majorana masses		
Ratios	$M_i = M_R$	$M_1 : M_2 : M_3 = 1 : 10 : 100$
$\tau \rightarrow \mu \gamma / \mu \rightarrow e \gamma$	4	12
$\tau \rightarrow \mu \gamma / \tau \rightarrow e \gamma$	2500	160
$\mu \rightarrow e \gamma / \tau \rightarrow e \gamma$	640	13

correlation of signals in $\tau\mu$ and $e\mu$ -channelsSUSY scenario SPS1, $\sqrt{s} = 800$ GeV