



November 7-10th 2005

Flavour in the
era of the LHC

A Model-Independent Analysis of New Physics Contributions in $|\Delta F| = 2$ transitions

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on behalf the CKMfitter group

Part I. Introduction.

Part II. Exploring New Physics in B_d mixing.

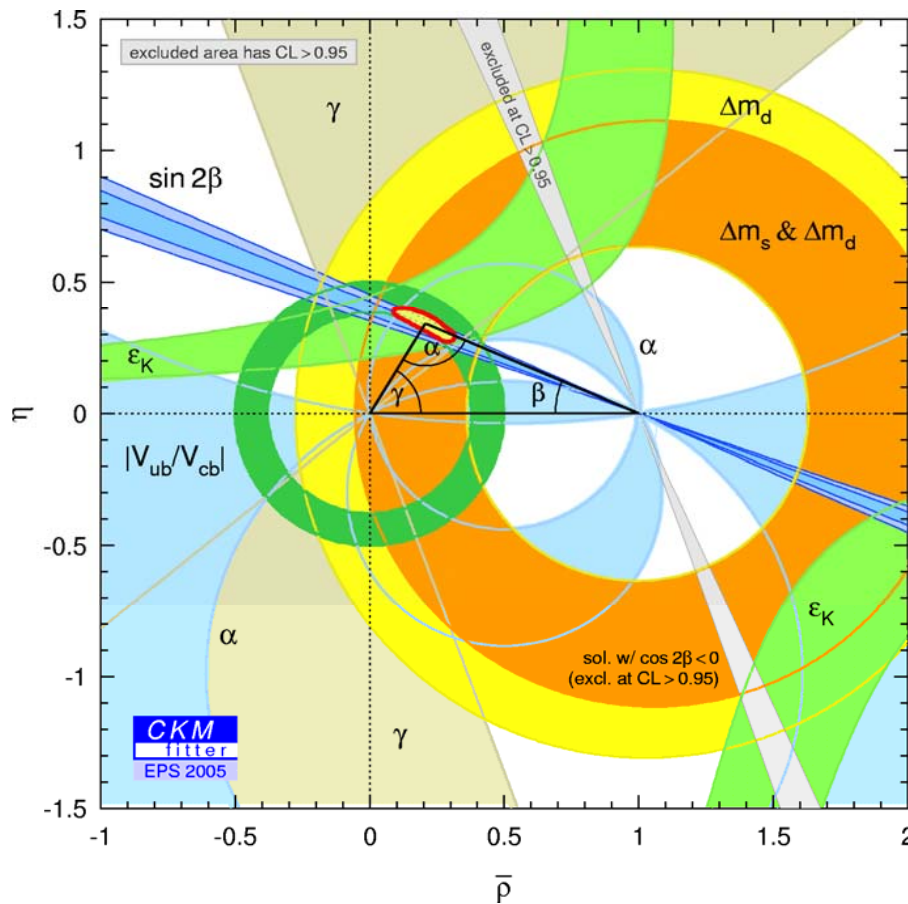
Basic inputs.

Adding γ and α measurements.

Adding a_{SL} contribution.

Part III. Exploring New Physics in K mixing.

Part IV. Prospective for New Physics in the B_s mixing.



⇔ Standard Model accommodates *successfully* all the present flavour data.

There is no need *a priori* for NP contributions in tree-mediated flavour changing processes.

Is there still room for new physics ?

Follow the strategy developed in the paper:

[The CKMfitter group, Eur. Phys. J. C41 \(2005\)](#)

Past & present attempts (a selection of)

Soares, Wolfenstein, Phys. Rev. D47 (1993)

Grossman, Nir, Worah, Phys. Lett. B407 (1996)

Laplace, Ligeti, Nir, Perez, Phys. Rev. D65 (2002)

[Ciuchini et al., hep-ph/0307195](#)

[Bona et al., hep-ph/0509219](#)

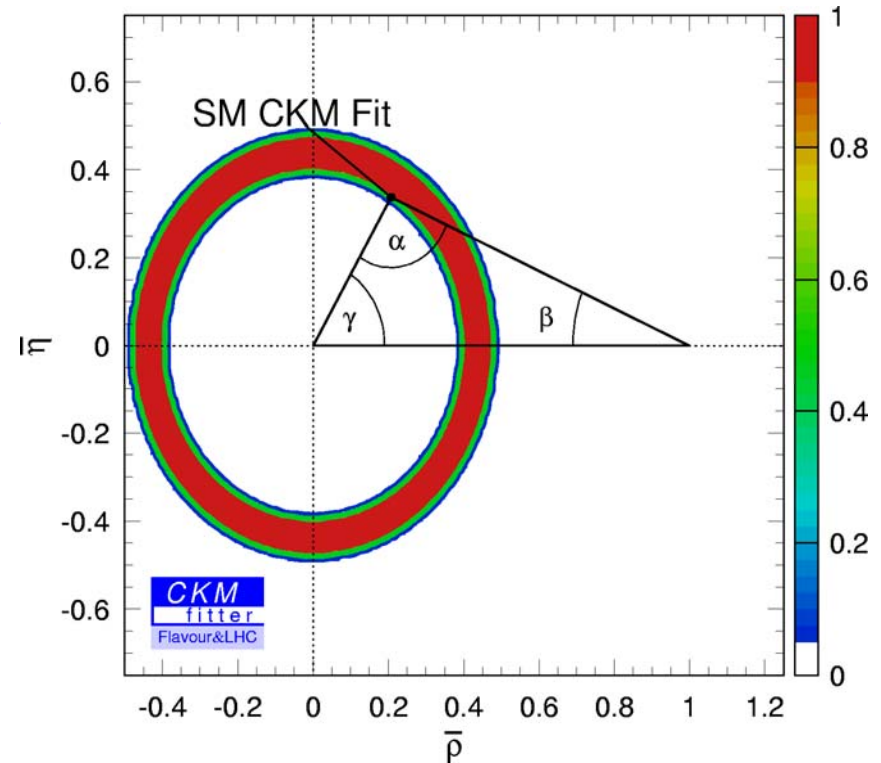
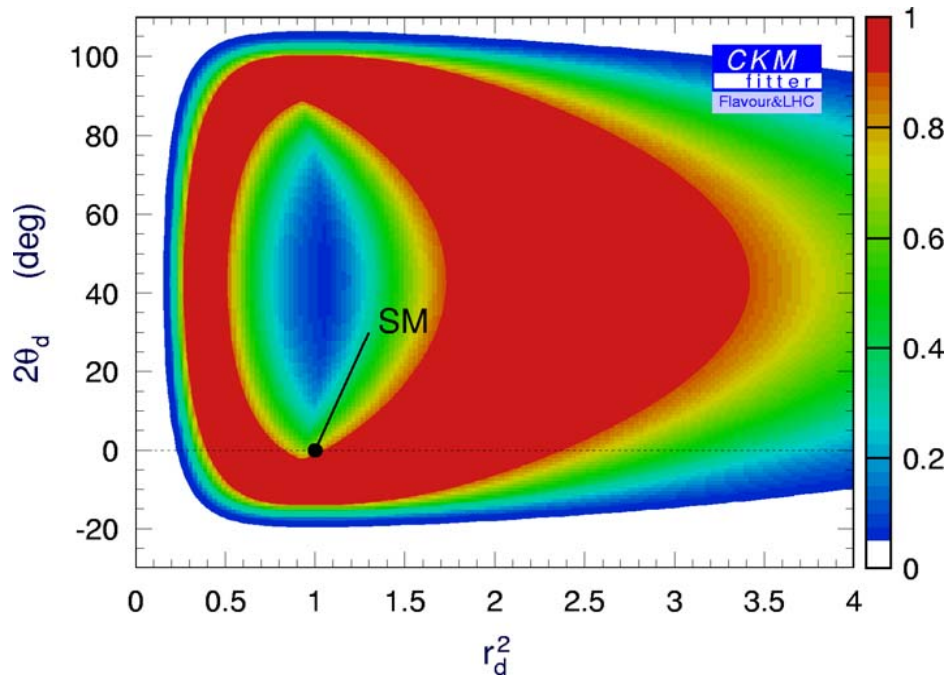
Assumption \Leftrightarrow no NP in tree-mediated decay amplitudes:

$|V_{ub}|/|V_{cb}|$ and γ are the main inputs constraining the CKM parameters.

Introduce NP in $\Delta B=2$ transitions accounted for model-independently through two additional parameters.

$$r_d^2 e^{i2\theta_d} = \frac{\langle B^0 | H_{eff}^{full} | \bar{B}^0 \rangle}{\langle B^0 | H_{eff}^{SM} | \bar{B}^0 \rangle}$$

- $\rightarrow |V_{ub}|, |V_{cb}| \Leftrightarrow$ Remove $b \rightarrow s\gamma$ component from the inclusive V_{ub} average
 $\rightarrow r_d^2 \Delta m_d \quad V_{ub} = (4.15 \pm 0.12 \pm 0.23) \cdot 10^{-3}$
 $\rightarrow \sin(2\beta + 2\theta_d)$
 $\rightarrow \cos(2\beta + 2\theta_d)$



- The SM value on $2\theta_d=0$ is at the border of the CL_{Max} region.
- Shows slight disagreement between V_{ub} and $\sin(2\beta)$.
- Any region with $2\theta_d > \pi/2$ is discarded.

⇔ Adding γ measurements.

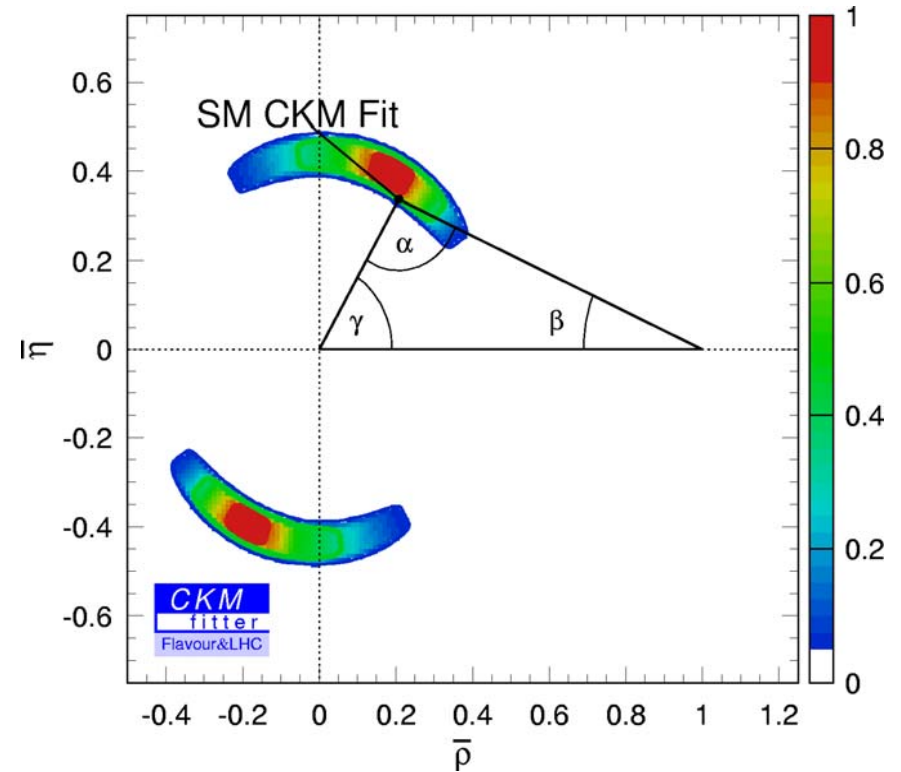
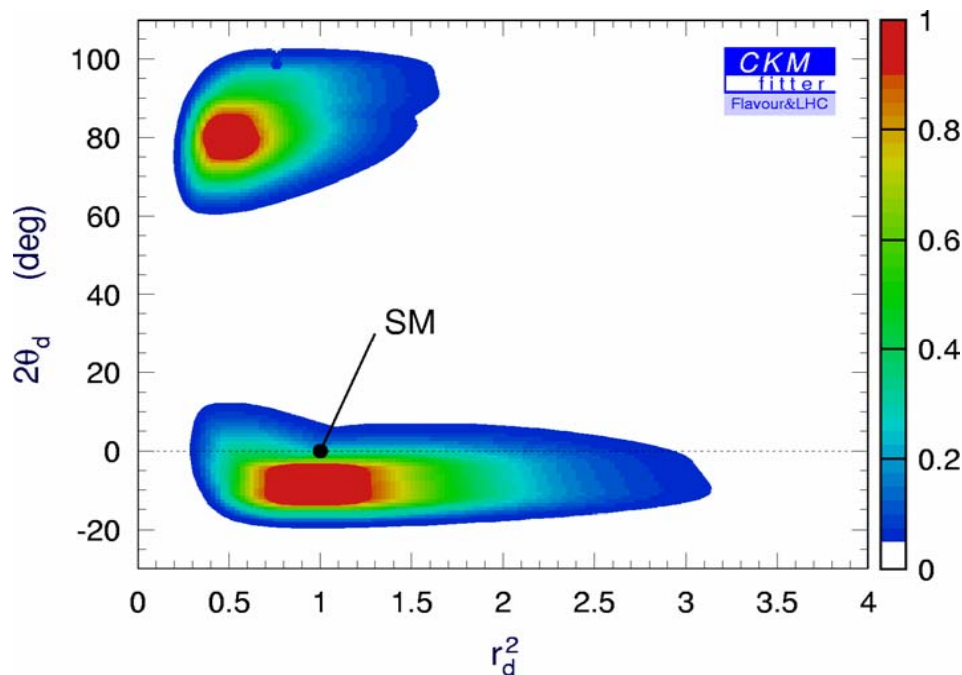
$$\rightarrow |V_{ub}|/|V_{cb}|$$

$$\rightarrow r_d^2 \Delta m_d$$

$$\rightarrow \sin(2\beta + 2\theta_d)$$

$$\rightarrow \cos(2\beta + 2\theta_d)$$

$$\rightarrow \gamma \text{ (ADS + GLW + GGSZ)}$$



- V_{ub} and γ constrain the CKM parameters.
- Two solutions for NP parameters emerge.

⇔ Adding α measurements.

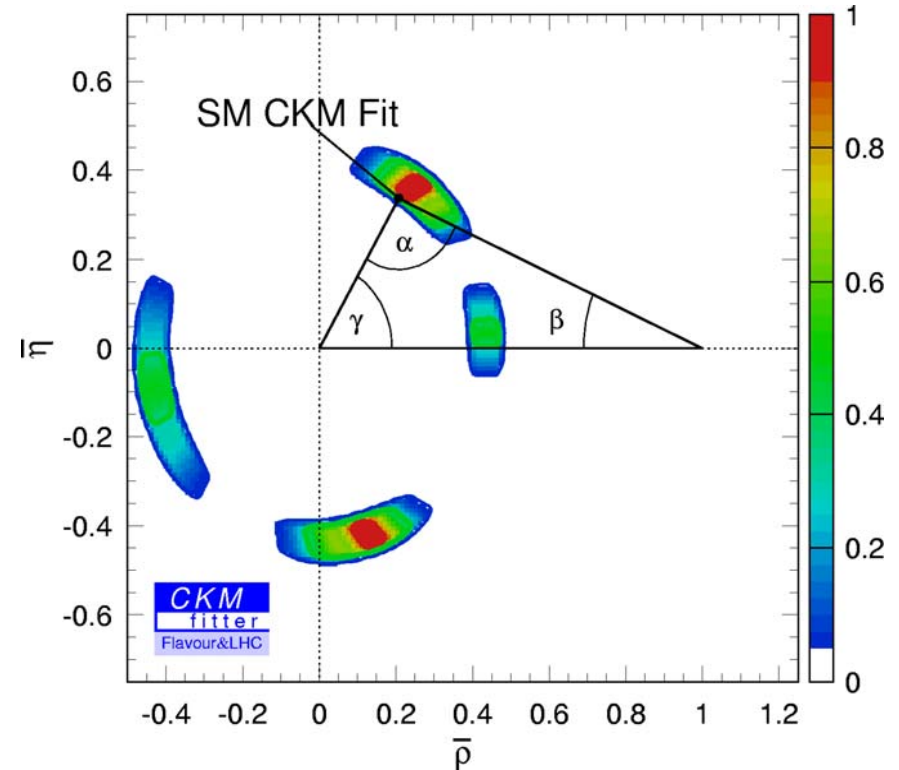
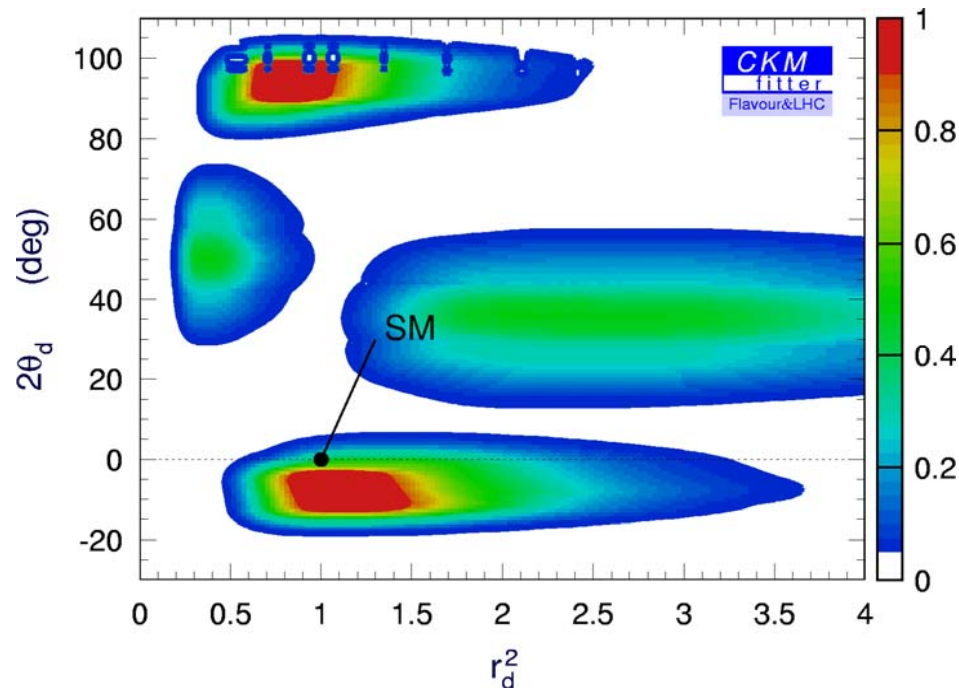
$$\rightarrow |V_{ub}|/|V_{cb}|$$

$$\rightarrow r_d^2 \Delta m_d$$

$$\rightarrow \sin(2\beta + 2\theta_d)$$

$$\rightarrow \cos(2\beta + 2\theta_d)$$

$$\rightarrow \sin(2\beta + 2\theta_d + 2\gamma)$$



The α constraint (w/o γ) displays also four solutions.

⇔ Reinforce the SM region but the preferred NP region is not the one defined by γ .

$$\rightarrow |V_{ub}| / |V_{cb}|$$

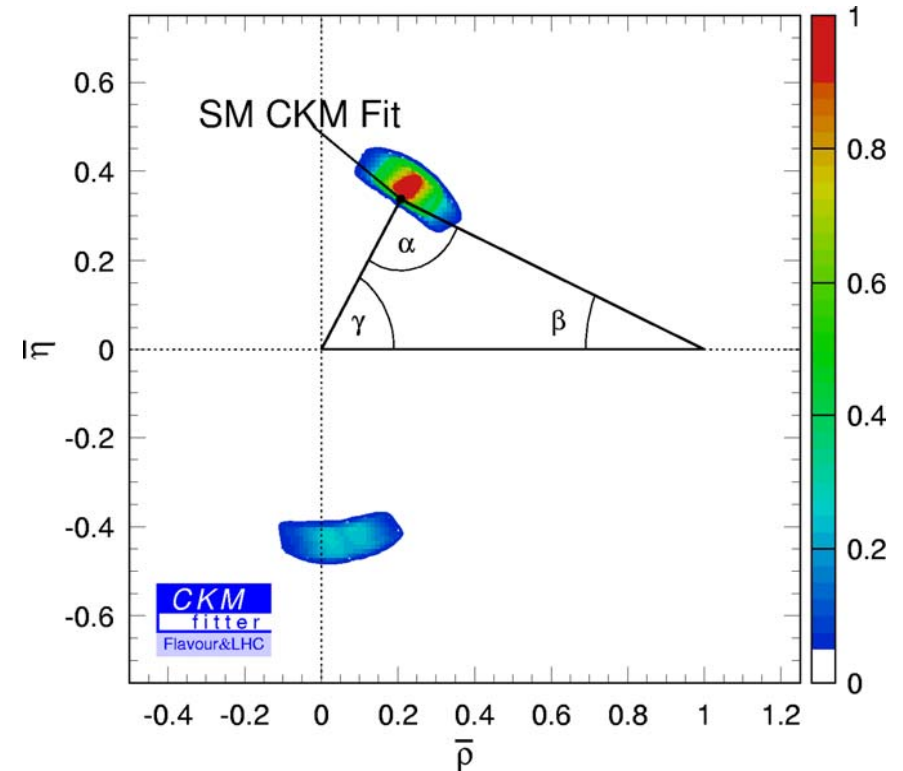
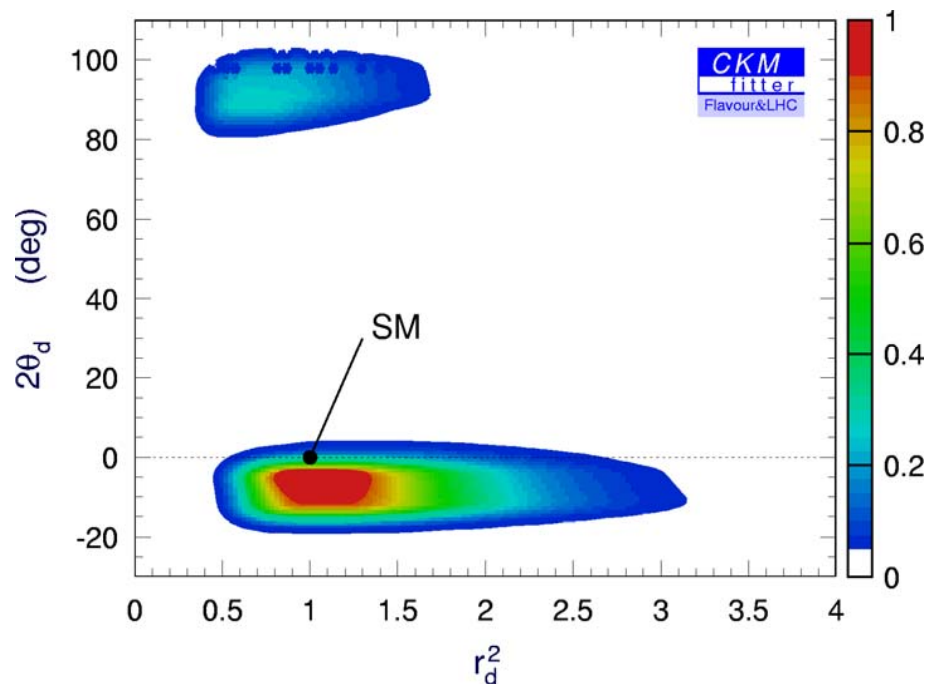
$$\rightarrow r_d^2 \Delta m_d$$

$$\rightarrow \sin(2\beta + 2\theta_d)$$

$$\rightarrow \cos(2\beta + 2\theta_d)$$

$$\rightarrow \gamma \quad (\text{ADS} + \text{GLW} + \text{GGSZ})$$

$$\rightarrow \sin(2\beta + 2\theta_d + 2\gamma)$$



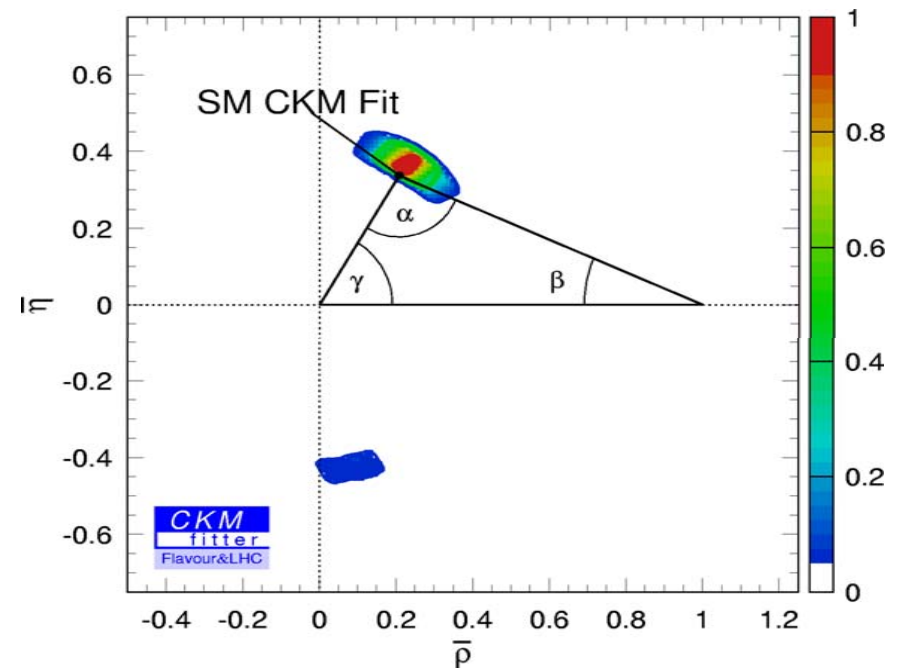
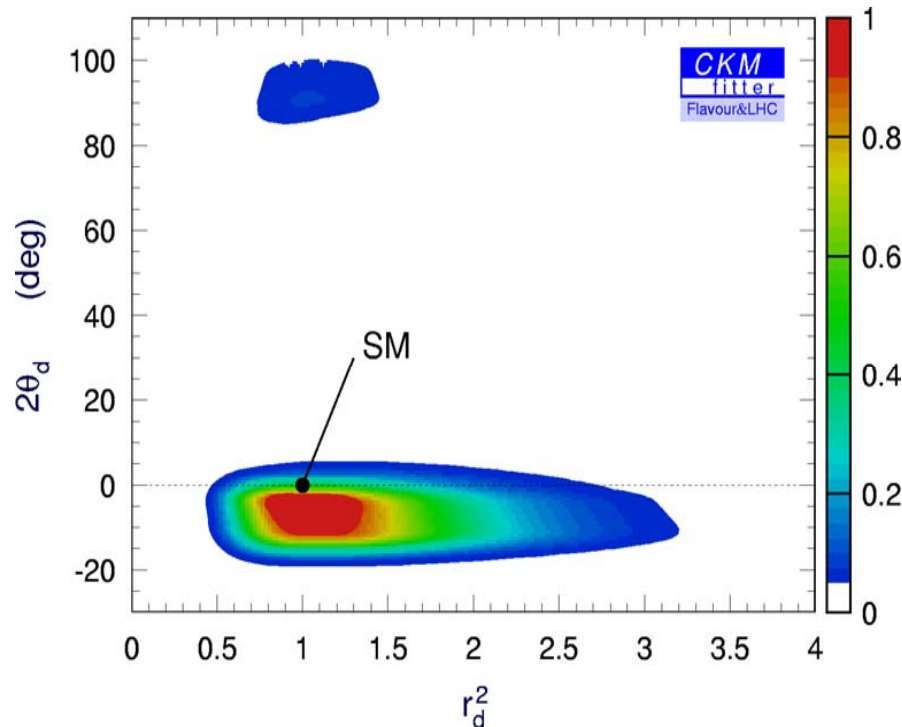
γ and α are of major importance in constraining the NP parameters.

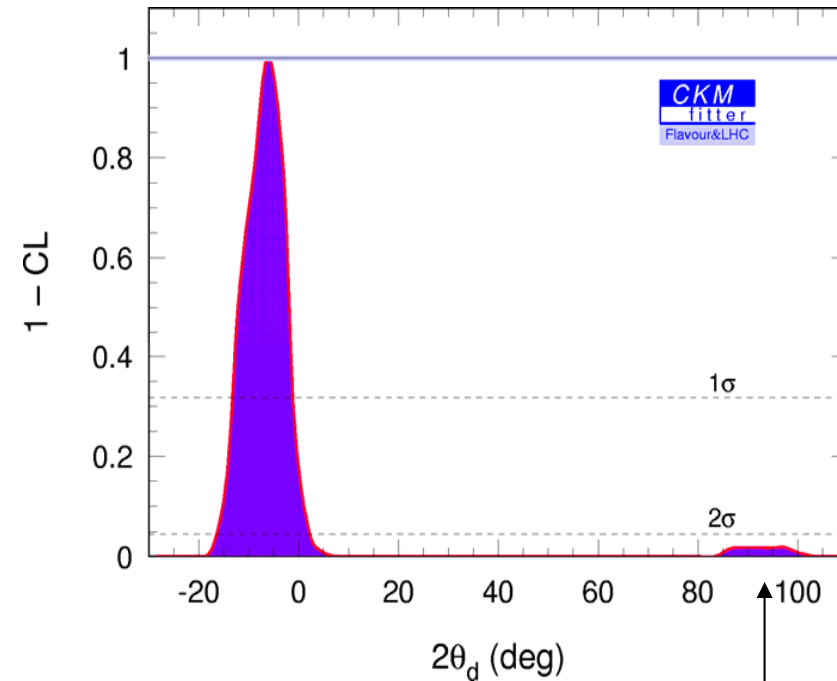
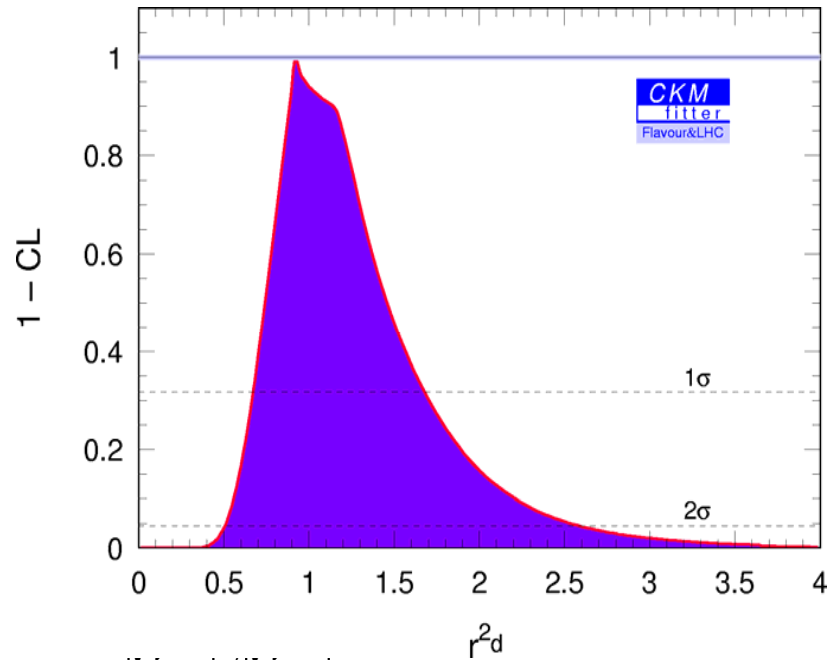
NB: $\sin(2\beta+2\theta_d+\gamma)$ is not included. (almost no influence.)

$$a_{SL} = -\text{Re}\left(\frac{\Gamma_{12}}{M_{12}}\right)^{SM} \frac{\sin 2\theta_d}{r_d^2} + \text{Im}\left(\frac{\Gamma_{12}}{M_{12}}\right)^{SM} \frac{\cos 2\theta_d}{r_d^2} \quad (\Gamma_{12}/M_{12} \text{ is considered here at Leading Order})$$

Though the experimental precision is far from the prediction, a_{SL} is a crucial input for constraining NP parameters. Only observable depending on both r_d^2 and $2\theta_d$.

$$a_{SL} = -0.0026 \pm 0.0067 \quad (\text{HFAG 2005})$$





$$\rightarrow |V_{ub}|/|V_{cb}|$$

$$\rightarrow r_d^2 \Delta m_d$$

$$\rightarrow \sin(2\beta + 2\theta_d)$$

$$\rightarrow \cos(2\beta + 2\theta_d)$$

$$\rightarrow \gamma \quad (\text{ADS} + \text{GLW} + \text{GGSZ})$$

$$\rightarrow \alpha \sin(2\beta + 2\theta_d + 2\gamma)$$

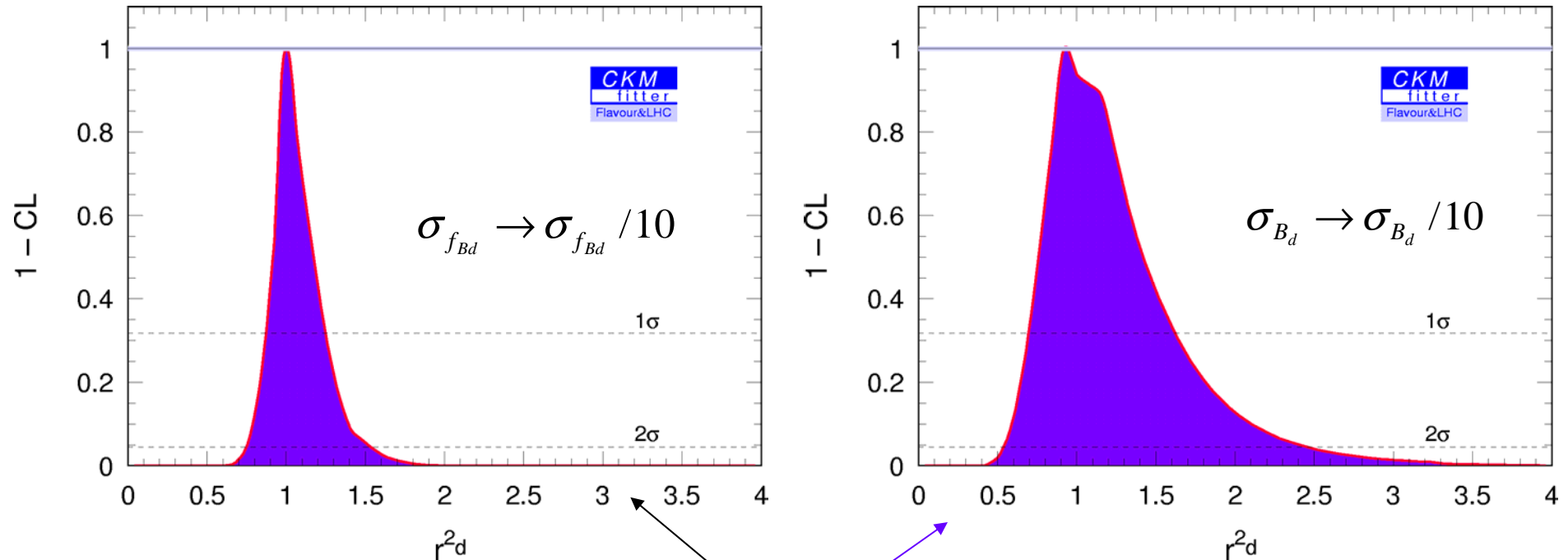
$$\rightarrow a_{\text{SL}}$$

$$\begin{cases} r_d^2 = 0.92^{+0.73}_{-0.23} \\ 2\theta_d = -5.3^{+3.2}_{-8.8} \text{ deg} \end{cases}$$

(Uncertainties are given at 1σ)

The NP solution at $\pi/2$ has $1\text{-CL} < 3\%$.

Influence of non-pert. hadronic parameters in Δm_d



$$\Delta m_d = \frac{G_F^2}{6\pi^2} \eta_B m_{B_d} f_{B_d}^2 B_d m_W^2 S(x_t) |V_{td} V_{tb}^*| r_d^2$$

- As far as the lattice uncertainties are considered, f_{B_d} is the relevant parameter to improve.
- A factor 2 has important impact. A factor 10 is not decisive with the current experimental uncertainties of the observables.

Alternative parametrization of NP in $|\Delta B|=2$

Isolate the pure NP contribution
from (SM+NP) terms:

$$M_{12} = M_{12SM} (1 + h_d e^{2i\sigma_d})$$

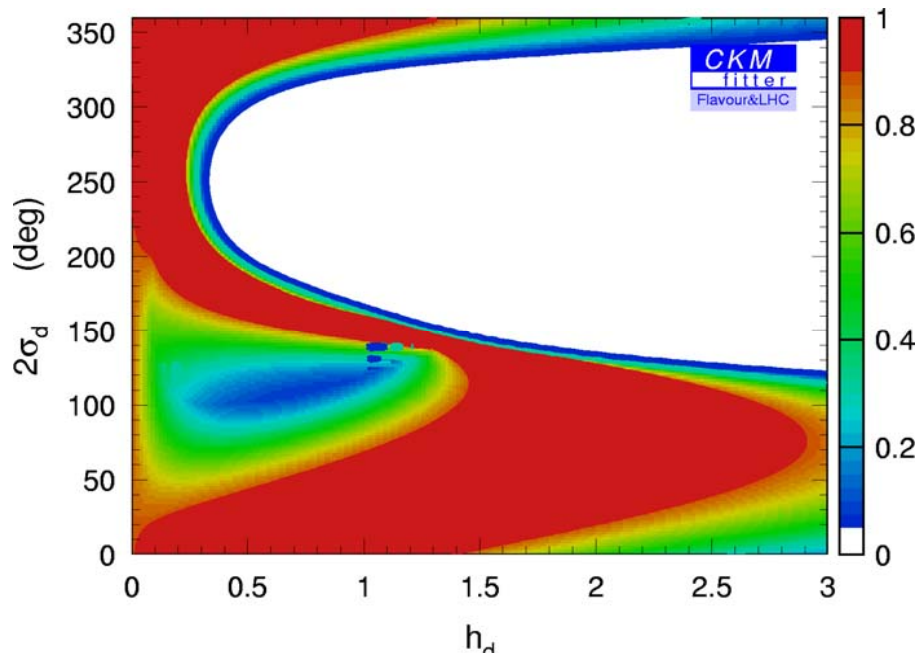
Agashe et al. [hep-ph/0509117](https://arxiv.org/abs/hep-ph/0509117)

$$\Delta m_d = \left| 1 + h_d e^{2i\sigma_d} \right| \Delta m_d^{SM}$$

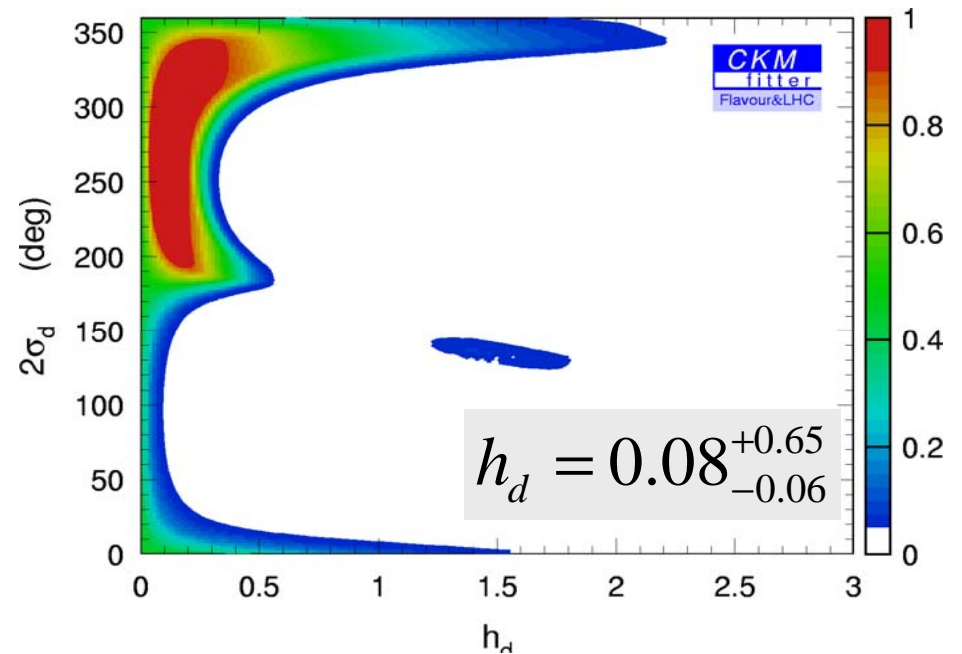
$$2\beta \rightarrow 2\beta + \text{Arg}(1 + h_d e^{2i\sigma_d})$$

$$a_{SL} = \text{Im}\left(\frac{\Gamma_{12}^{SM}}{M_{12}^{SM} (1 + h_d e^{2i\sigma_d})}\right)$$

Without γ , α and a_{SL} constraints

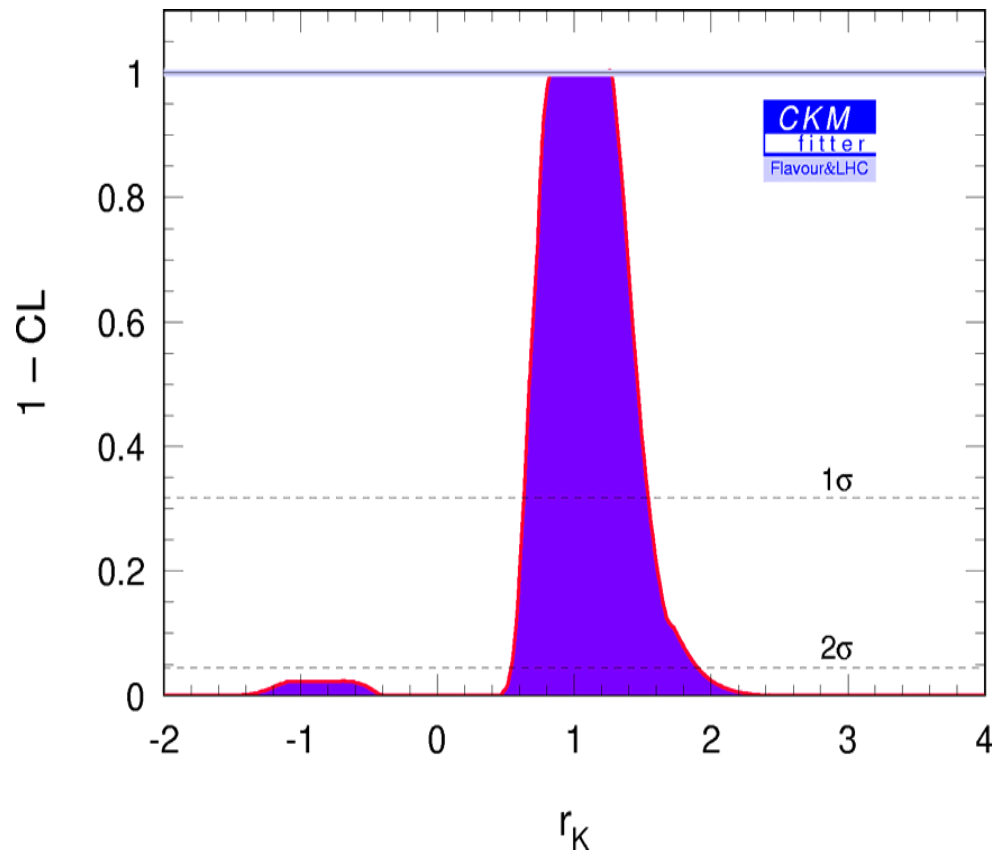


With γ , α and a_{SL} constraints



Allowing in addition NP in K - \bar{K} mixing (I)

$$r_K = \frac{\text{Im} \left\langle K^0 \left| H_{\text{eff}}^{\text{full}} \right| \bar{K}^0 \right\rangle}{\text{Im} \left\langle K^0 \left| H_{\text{eff}}^{\text{SM}} \right| \bar{K}^0 \right\rangle}$$



$$\rightarrow |V_{ub}| / |V_{cb}|$$

$$\rightarrow r_d^2 \Delta m_d$$

$$\rightarrow \sin(2\beta + 2\theta_d)$$

$$\rightarrow \cos(2\beta + 2\theta_d)$$

$$\rightarrow \gamma \quad (\text{ADS} + \text{GLW} + \text{GGSZ})$$

$$\rightarrow \alpha \sin(2\beta + 2\theta_d + 2\gamma)$$

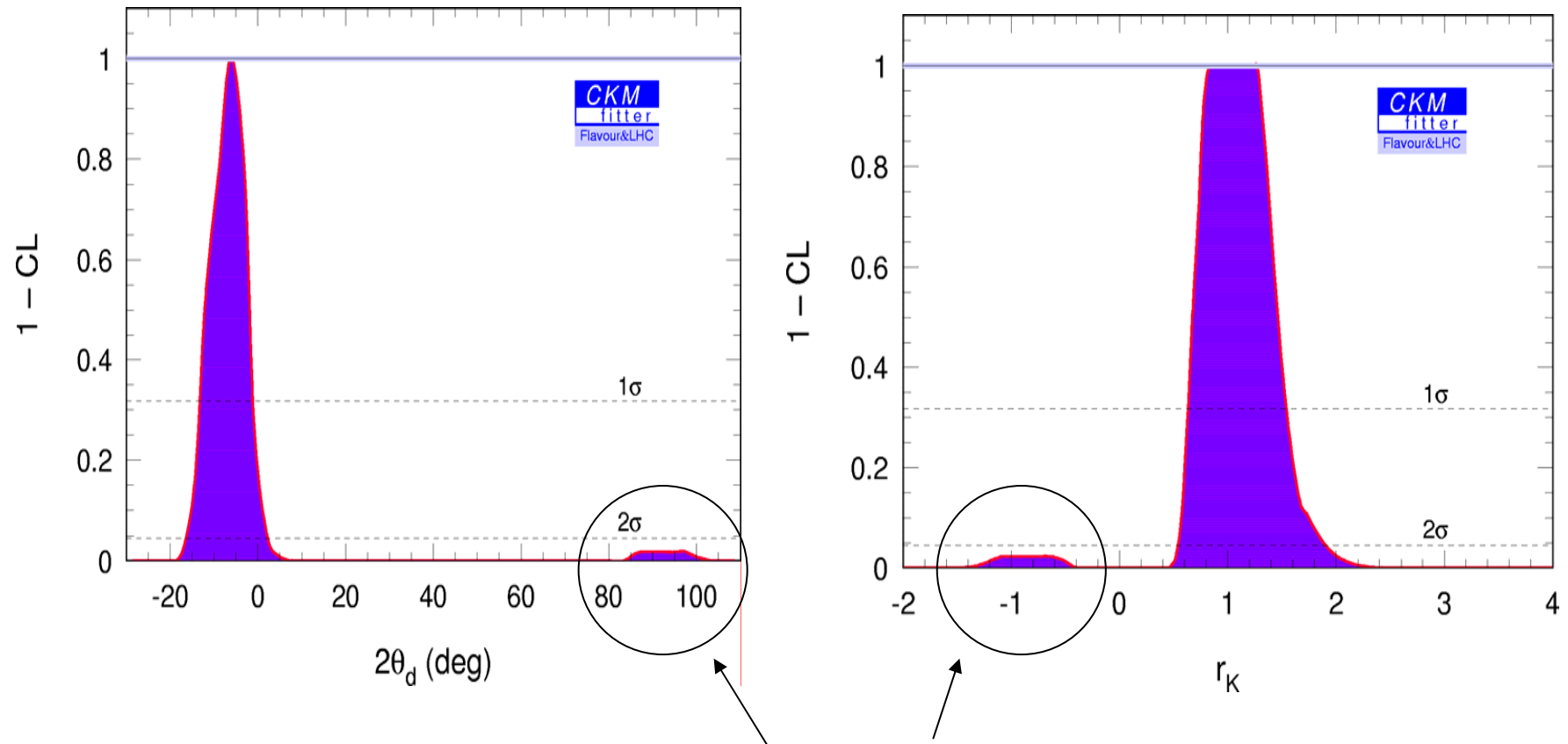
$$\rightarrow a_{\text{SL}}$$

$$\rightarrow r_K \mathcal{E}_K$$

(1σ)

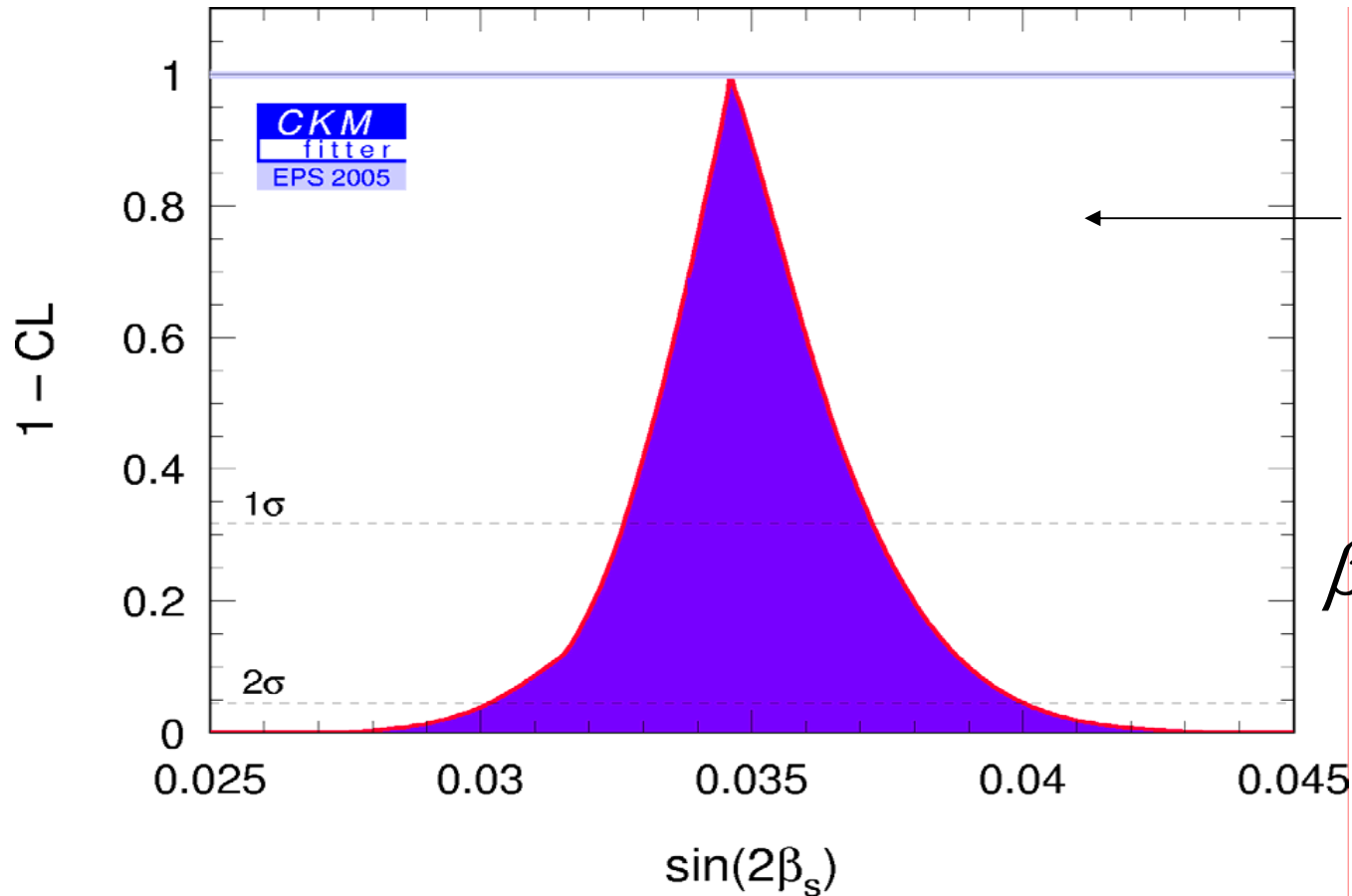
$$\left\{ \begin{array}{l} r_d^2 = 0.92^{+0.76}_{-0.25} \\ 2\theta_d = -4.8^{+4.1}_{-9.1} \text{ deg} \\ r_K = 1.09^{+0.45}_{-0.46} \end{array} \right.$$

Allowing in addition NP in K - K mixing (II)



The NP region at $2\theta_d = \pi/2$ in B_d mixing implies also NP in K mixing corresponding to $\epsilon_K < 0$

The angle governing the mixing in the B_s system is already known to good precision in the SM



$\beta_s \sim \lambda^2 \eta + o(\lambda^4)$ can be extracted from the global Standard Model fit.

$$\beta_s = \arg \left(- \frac{V_{cb} V_{cs}^*}{V_{tb} V_{ts}^*} \right)$$

$$\sin(2\beta_s) = 0.0363 \pm 0.0025$$

NP in B_s mixing ($\Delta B=2$ and $\Delta S=2$) is accounted for model-independently through two additional parameters, akin to the B_d system :

$$r_s^2 e^{i2\theta_s} = \frac{\langle B_s^0 | H_{eff}^{full} | \bar{B}_s^0 \rangle}{\langle B_s^0 | H_{eff}^{SM} | \bar{B}_s^0 \rangle}$$

- LHCb expected sensitivities correspond to 2 fb^{-1}
(See Talks of O.Schneider & L.Fernandez):

$$\rightarrow \Delta m_s = 20.000 \pm 0.011 \text{ ps}^{-1} \text{ from } B_s \rightarrow D_s \pi$$

$$\rightarrow A_{mix} = \sin(2\beta_s) = 0.036 \pm 0.028$$

from combined $B_s \rightarrow J/\Psi \Phi$, $B_s \rightarrow J/\Psi \eta$ and $B_s \rightarrow \eta_c \phi$

$$\rightarrow \gamma - 2\beta_s = 57 \pm 14 \text{ deg from } B_s \rightarrow D_s K$$

$$\rightarrow \gamma = 59 \pm 8 \text{ deg from } B_d \rightarrow D^{(*)} K$$

$$\rightarrow r_s^2 \Delta m_s$$

$$\rightarrow \sin(2\beta_s + 2\theta_s)$$

$$\rightarrow \sin(2\beta_s + 2\theta_s - \gamma)$$

$$\rightarrow |V_{ub}|/|V_{cb}|$$

$$\rightarrow r_d^2 \Delta m_d$$

$$\rightarrow \sin(2\beta + 2\theta_d)$$

$$\rightarrow \cos(2\beta + 2\theta_d)$$

$$\rightarrow \gamma \quad (ADS + GLW + GGSZ)$$

⊕ Adding LHCb sensitivity

$$\rightarrow \alpha \sin(2\beta + 2\theta_d + 2\gamma)$$

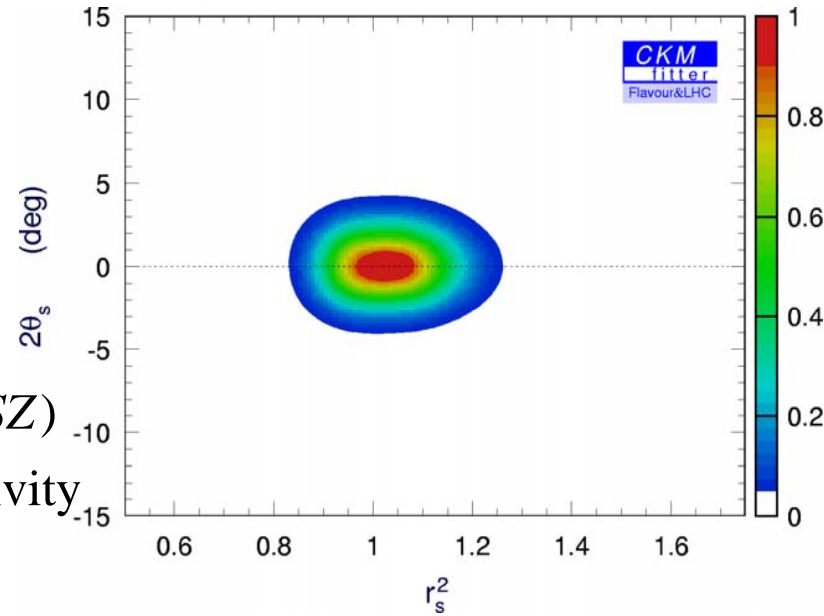
$$\rightarrow a_{SL}$$

$$\rightarrow r_K^2 \mathcal{E}_K$$

$$\rightarrow r_s^2 \Delta m_s$$

$$\rightarrow \sin(2\beta_s + 2\theta_s)$$

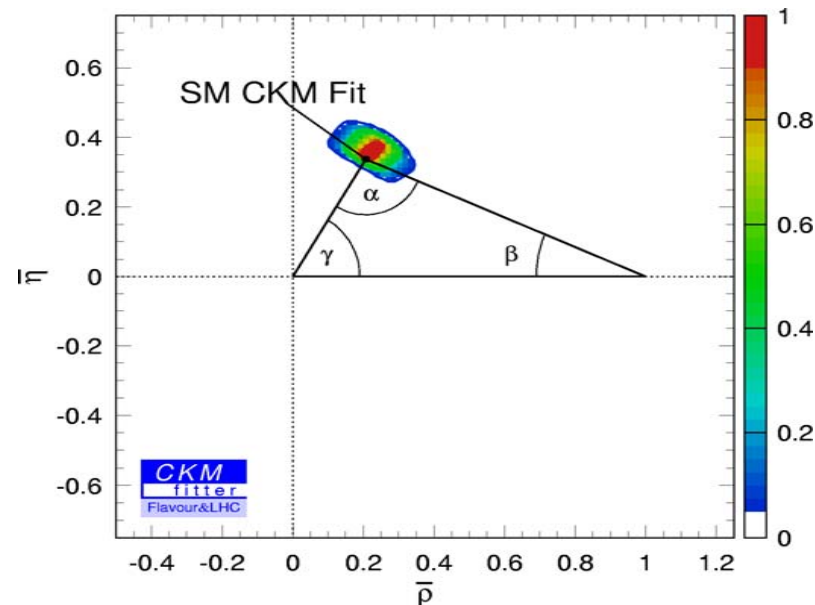
$$\rightarrow \sin(2\beta_s + 2\theta_s - \gamma)$$



(1 σ)

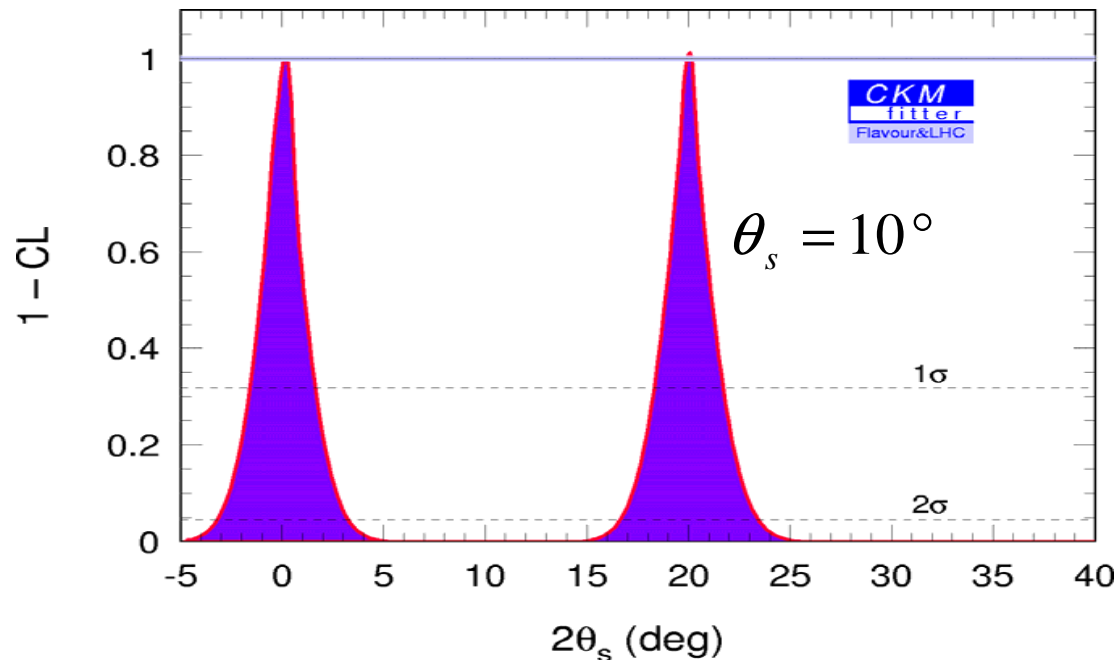
$$r_s^2 = 1.01^{+0.11}_{-0.09}$$

$$2\theta_s = 0.1^{+1.6}_{-1.7} \text{ deg}$$



CONCLUSIONS

- B_d mixing: which room for new physics ? ... Not much.
- K mixing: the only constraint is from $\varepsilon_k \Leftrightarrow$ under constrained pb as far as specific NP phase & modulus are considered.
- B_s mixing: LHCb will immediately see NP if $O(10^\circ)$.



APPENDIX

Main inputs to the fit

$$|V_{ub}| \text{ (average)} = (4.15 \pm 0.12 \pm 0.23) \cdot 10^{-3}$$

$$|V_{cb}| \text{ (incl)} = (41.58 \pm 0.45 \pm 0.58) \cdot 10^{-3}$$

$$|V_{cb}| \text{ (excl)} = (41.4 \pm 2.1) \cdot 10^{-3}$$

$$|\varepsilon_K| = (2.282 \pm 0.017) \cdot 10^{-3}$$

$$\Delta m_d = (0.509 \pm 0.004) \text{ ps}^{-1}$$

$$\sin(2\beta) = 0.687 \pm 0.032$$

$$S_{\pi\pi}^{+-} = -0.50 \pm 0.12$$

$$C_{\pi\pi}^{+-} = -0.37 \pm 0.10$$

$$C_{\pi\pi}^{00} = -0.28 \pm 0.39$$

$$B_{\pi\pi, \text{all charge}} \text{ Inputs to isospin analysis}$$

$$S_{\rho\rho, L}^{+-} = -0.22 \pm 0.22$$

$$C_{\rho\rho, L}^{+-} = -0.02 \pm 0.17$$

$$B_{\rho\rho, L, \text{all charge}} \text{ Inputs to isospin analysis}$$

$$B \rightarrow \rho\pi \rightarrow 3\pi \text{ Time dependent Dalits analysis}$$

$$B \rightarrow D^{(*)} K^{(*)(-)} \text{ Inputs to } GLW, ADS \text{ \& } GGSZ \text{ analysis}$$

$$\Delta m_K = (3.490 \pm 0.006) \cdot 10^{-12} \text{ MeV}$$

$$B_K = 0.79 \pm 0.04 \pm 0.09$$

$$m_{K^+} = (493.677 \pm 0.016) \text{ MeV}$$

$$f_K = 159.8 \pm 1.5 \text{ MeV}$$

$$\eta_{\text{tt}} = 0.5765 \pm 0.0065$$

$$\eta_{\text{ct}} = 0.47 \pm 0.04$$

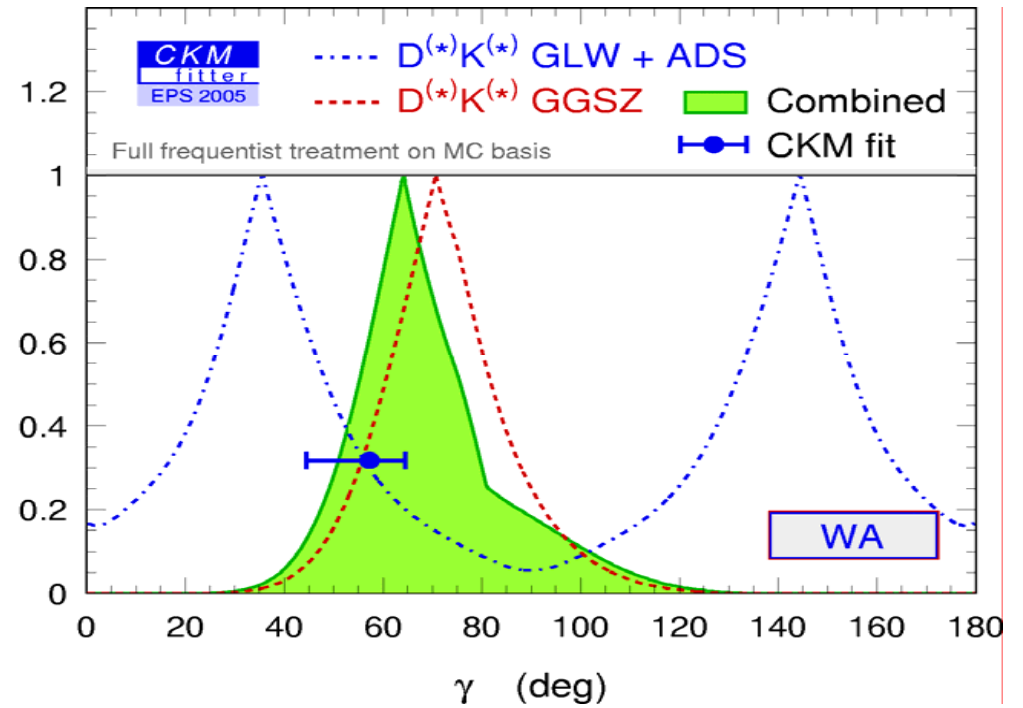
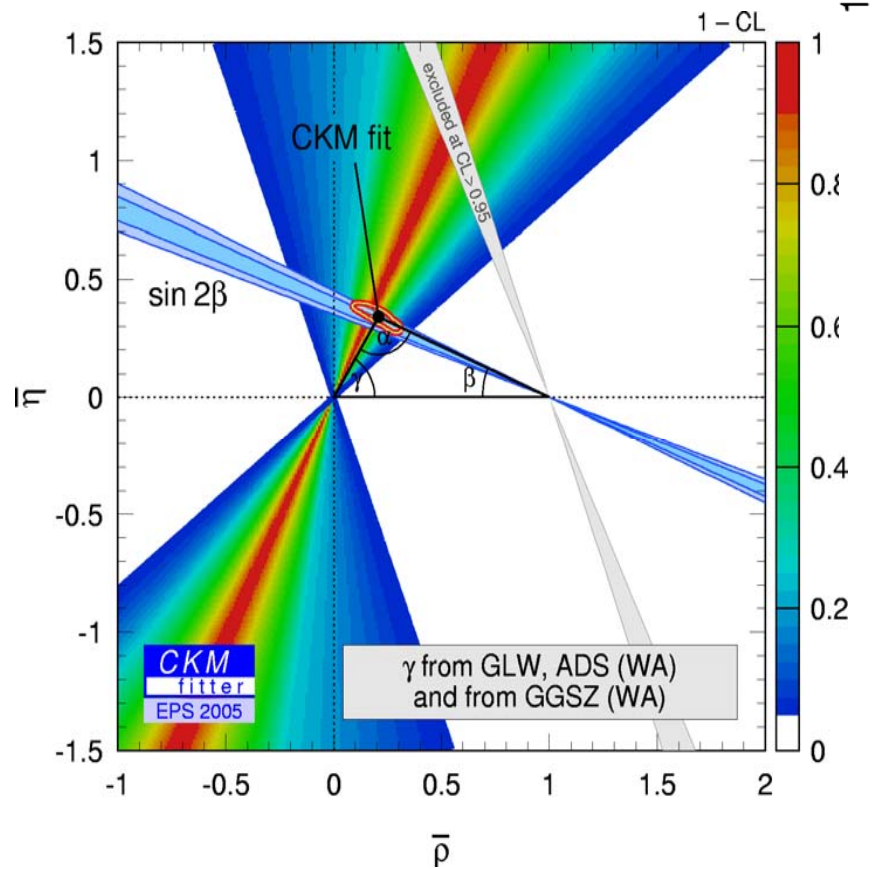
$$\eta_B(\overline{MS}) = 0.551 \pm 0.007$$

$$f_{B_d} \sqrt{B_d} = (223 \pm 33 \pm 12) \text{ MeV}$$

$$a_{SL} = -0.0026 \pm 0.0067$$

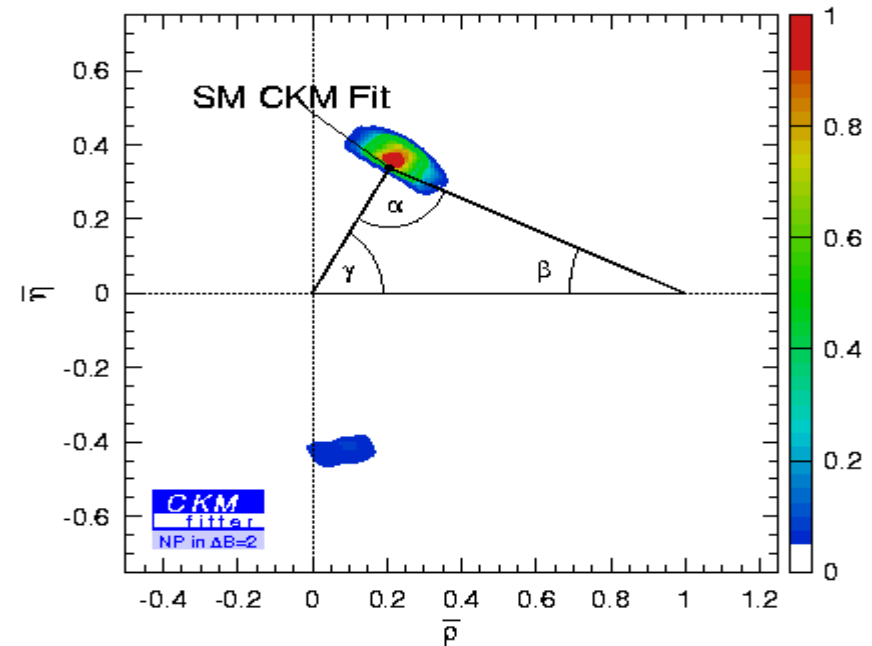
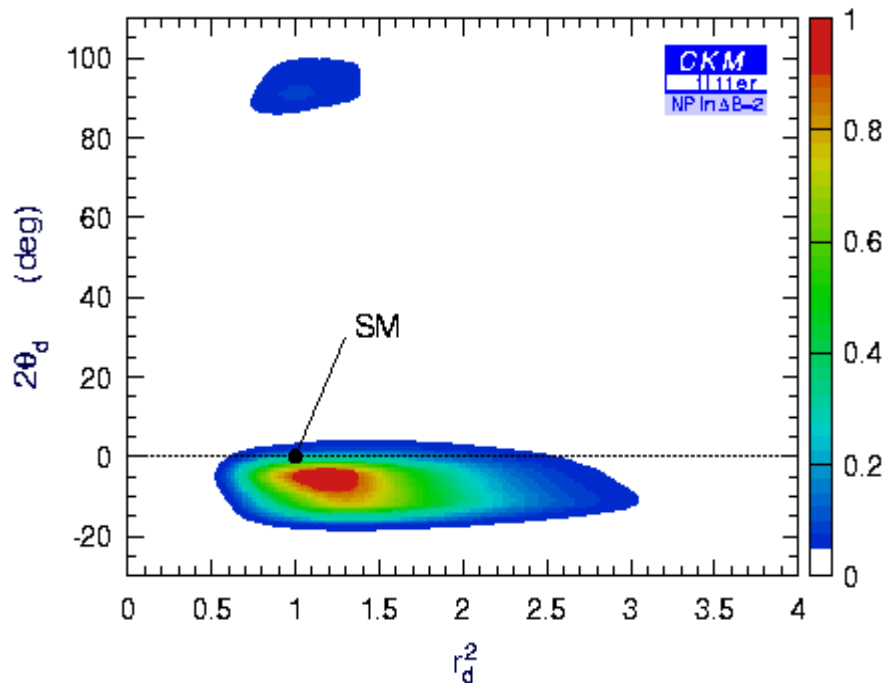
II

γ measurements



$$BR(B^+ \rightarrow \tau^+ \nu) = \frac{G_F^2 m_B \tau_B}{8\pi} m_\tau^2 \left(1 - \frac{m_\tau^2}{m_B^2}\right)^2 f_B^2 |V_{ub}|^2$$

← With Δm_d , remove the f_B dependence



- Powerful in the future for constraining the SM region.
- Potential annihilation by means of H^+ prevents for considering this input in the analysis.