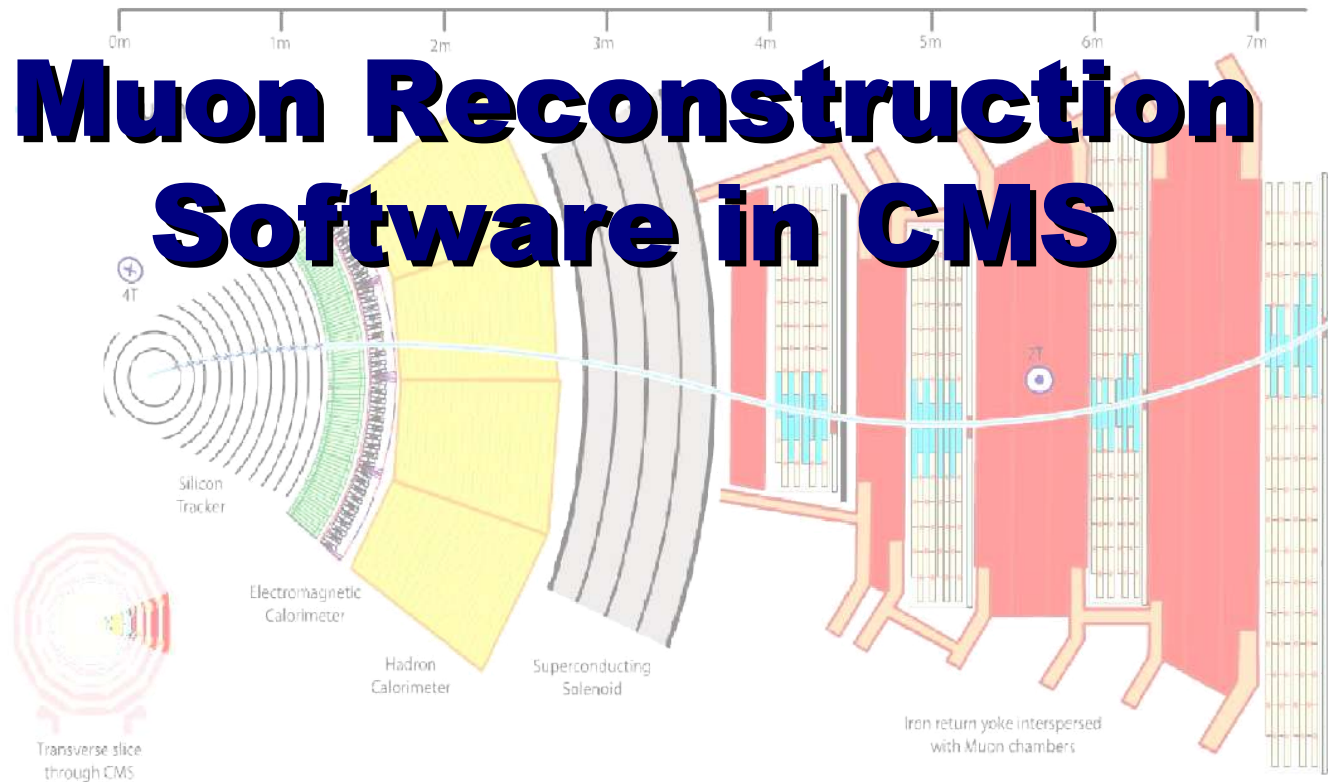




Frontier Science 2005

Muon Reconstruction Software in CMS



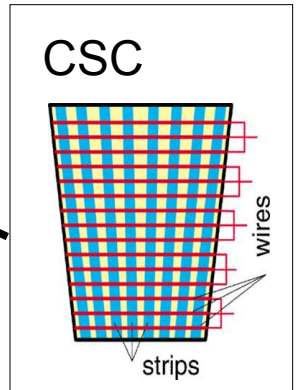
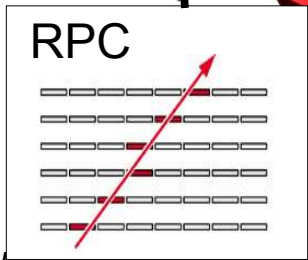
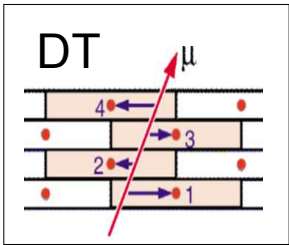
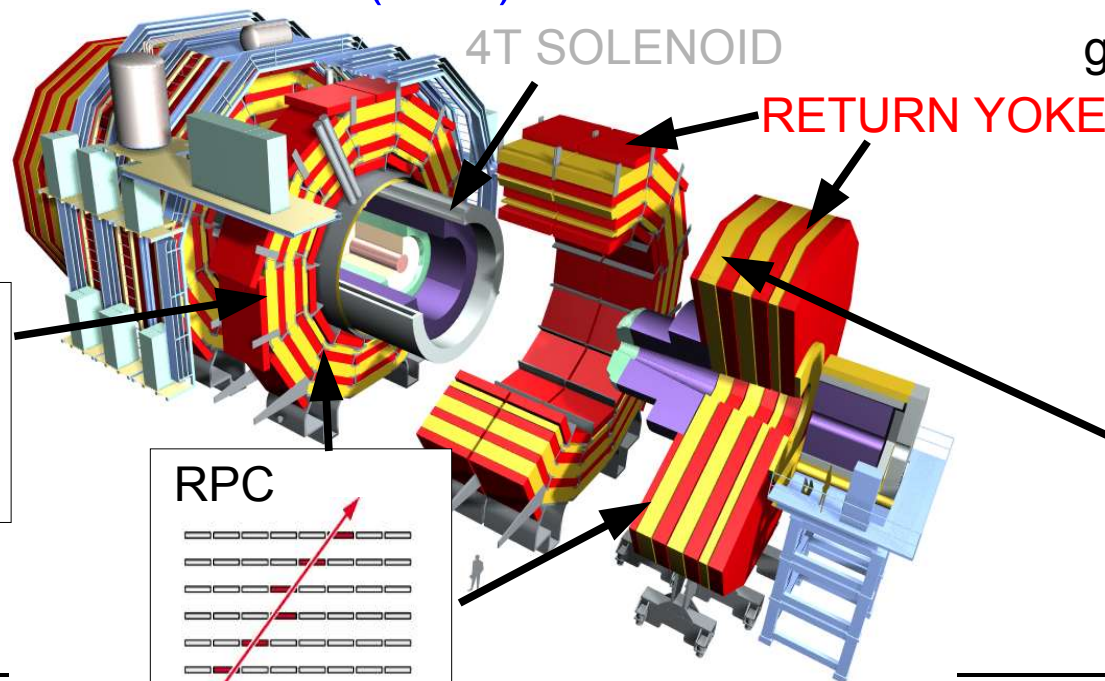
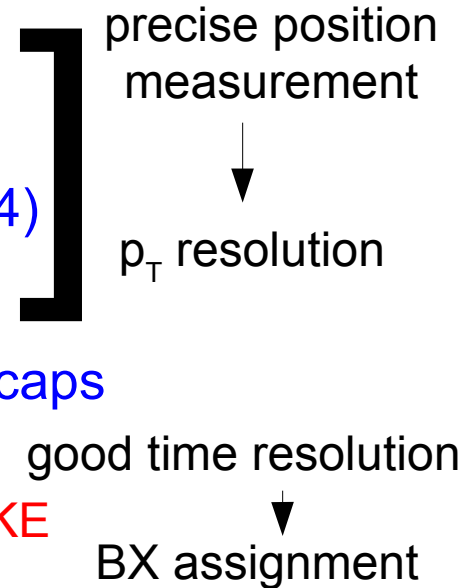
G. Cerminara
University and INFN Torino



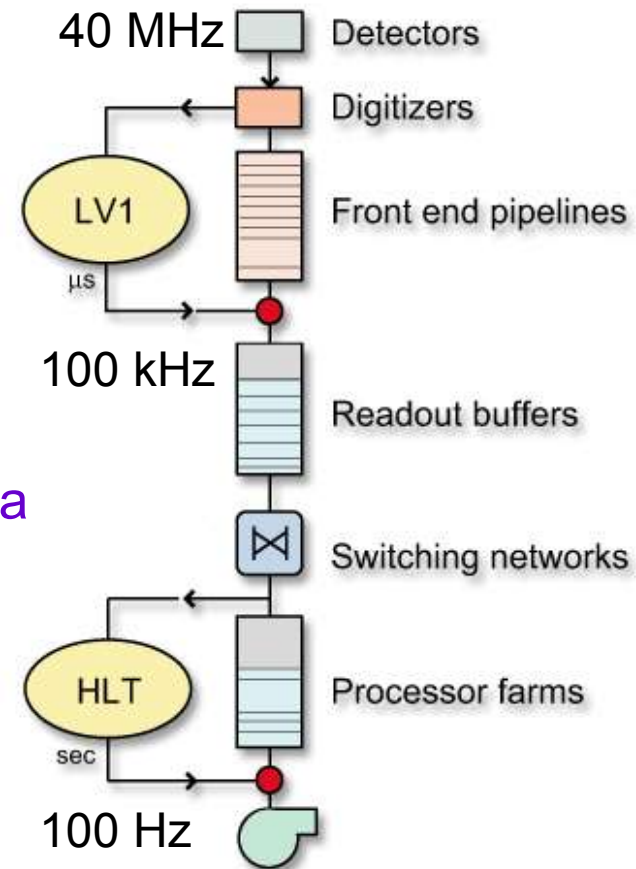
- The Compact Muon Solenoid experiment:
 - muon system
 - trigger design
- Muon reconstruction software
 - HLT design (Level-2 and Level-3 trigger)
 - Local Reconstruction in DTs, CSCs and RPCs
 - Track reconstruction
 - Level-2 (standalone) reconstruction
 - Level-3 (global) reconstruction
- Performance
 - efficiency
 - resolution
- Summary

Three types of muon gas detectors with trigger capabilities:

- **Drift Tubes (DT)** in the central barrel region ($|\eta| < 1.2$)
 - $\sigma_x \approx 200\mu\text{m} / \text{layer}$
- **Cathode Strip Chambers (CSC)** in the endcaps ($|\eta| < 2.4$)
 - $\sigma_x \approx 100 - 240\mu\text{m} / \text{layer}$
- **Resistive Plate Chambers (RPC)** both in barrel and endcaps
 - $\sigma_t \approx 2 \text{ ns}$



- Innovative (No Level-2 dedicated hardware) multilevel trigger design:
 - Level-1 Trigger: implemented on dedicated hardware
 - Calorimeter and muon data (coarse granularity)
 - Dedicated hardware → minimum dead time
 - Input from detector: 40 MHz
 - Output to DAQ: ~100 kHz
 - High Level Trigger (HLT): software running on a farm of commercial processors
 - Uses as much as possible “off-line quality” data
 - Output: max rate for storage $O(100)$ Hz
 - 1 event ~ 1MB



General selection tool: p_T thresholds on particles

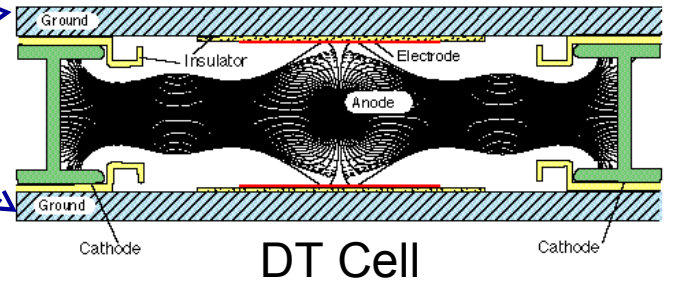
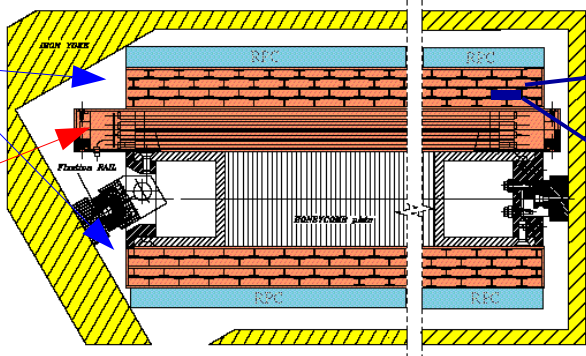


μ Reconstruction Software



- Almost same algorithms for HLT and off-line reconstruction
- HLT muon reconstruction performed in two logical steps (goal: reject events as soon as possible):
 - **Level-2**: uses the muon system data only
 - **Level-3**: uses data from muon system + tracker hits
- Track reconstruction using Kalman Filter
 - off-line vs HLT → different seeds for Kalman Filter and access to calibration data
 - Base ingredients for reconstruction:
 - objects locally reconstructed in the detectors (RecHits)
 - reconstruction “on demand” in a *region of interest* defined from the track extrapolation

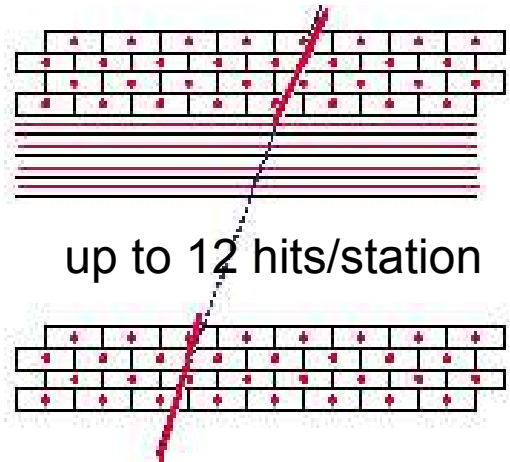
2 $r-\Phi$ superlayers
1 $r-z$ superlayer



- Hit position in the cell estimated from TDC measurement
 - time-to-distance relation within the cell parametrized with GARFIELD:

$$x(t) = f(t, \theta, B_{\text{wire}}, B_{\text{norm}})$$

- Fit 2D segments separately in $r-\Phi$ (8 layers) and $r-z$ SLs (4 layers)
 - L/R ambiguities solved by best χ^2
 - Update $x(t)$ using information on impact angle θ and refit
- Combine $r-\Phi$ and $r-z$ 2D segments in a 3D segment
 - Update $x(t)$ using best knowledge on $B_{\text{wire}}, B_{\text{norm}}$ and refit
 - Resolution in $r-\Phi$ plane:
position $\sim 100 \mu\text{m}$, direction $\sim 1\text{mrad}$



- Cathode Strip Chambers:

- ϕ coordinate measured by strips

- charge distribution on a cluster of adjacent strips fitted with “Gatti” function to determine the centroid

- r coordinate measured by wires

- read out in bunches to limit number of channels \rightarrow limited precision

- Use the measured points to fit a 3D linear segment

- Resolution: 120 – 250 μm for the bending coordinate

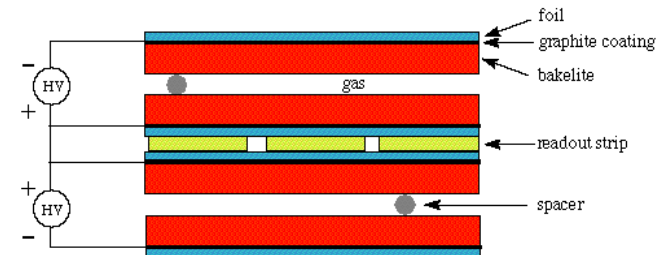
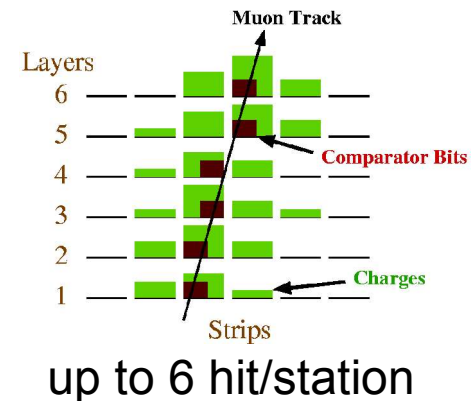
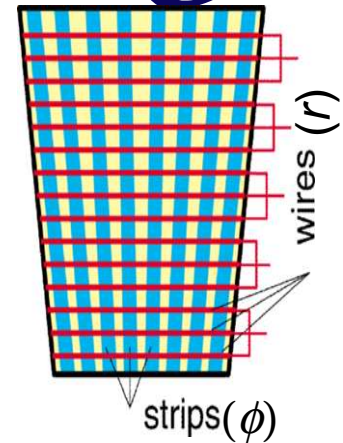
- Resistive Plate Chambers:

- Measure 3D points clustering the strips:

- up to 6 points in the barrel and 4 in the endcaps

- Uncertainties: $L / \sqrt{12}$

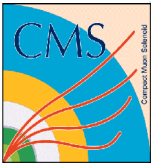
$$L_{\phi} \sim O(1 \text{ cm}) \text{ and } L_z \sim O(100 \text{ cm})$$



- Track reconstruction with a Kalman Filter
 - recursive method to fit a discrete set of data independently of the number of measurements available
 - determine a generic state vector (= position and momentum + covariance matrix)
- Kalman Filter → initial seed:
 - HLT reconstruction: seeded by L1-trigger candidates (*external* seeding: faster)
 - 4 best muons from the Global Trigger:
 - p_T , position, angle, BX and quality
 - L1 p_T resolution: 17 – 22 % depending on η .
 - Efficiency: ~ 97 %
 - Off-line reconstruction: seeded by local segment reconstruction (*internal* seeding: no dependency on L1)

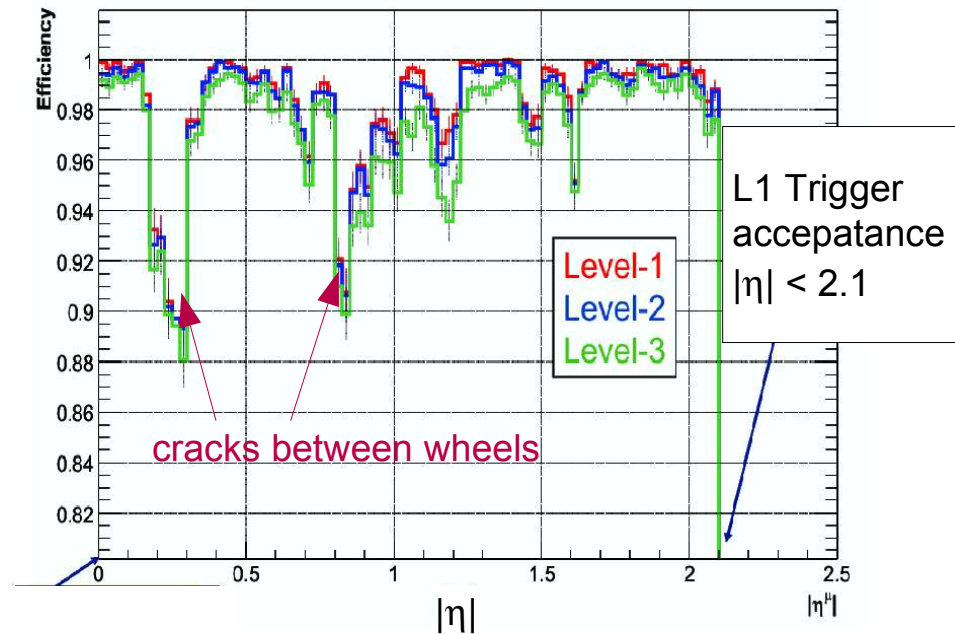
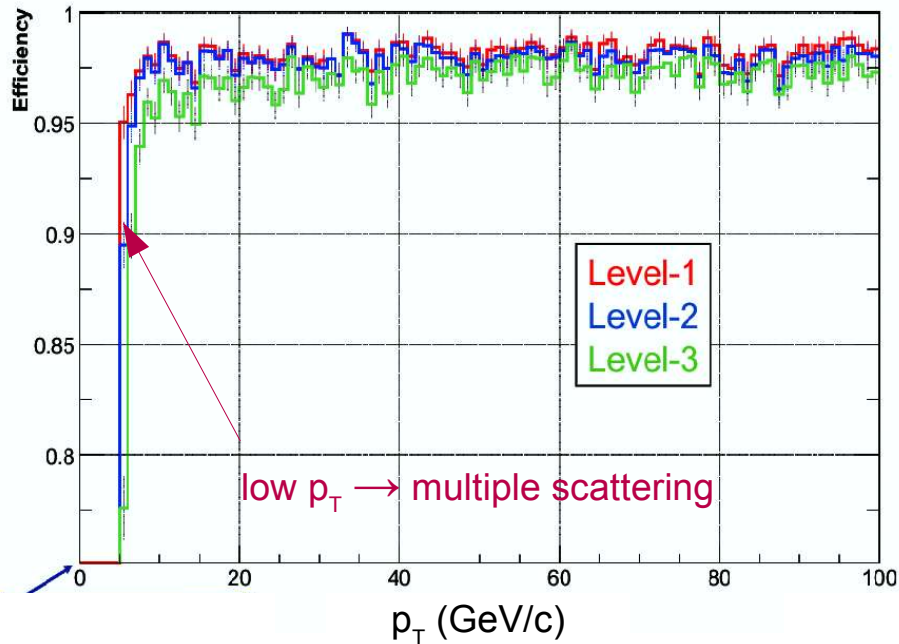
- Initial state extrapolated from track seed
- Hits to be included in the fit are looked for iteratively inside-out, at each step:
 - extrapolate the trajectory to next layer of chambers
 - perform local reconstruction in the chambers on the path
 - if RecHits are compatible (χ^2 test) update the state vector using the Kalman filter
 - DTs: 3D segments are used for the fit
 - CSCs, RPCs: 3D hits are used (inhomogeneous magnetic field)
- The obtained state (at the last station) is used to perform the actual fit going outside-in.
 - Final estimate at the innermost muon station
- Trajectory cleaning, ghosts suppression and “smoothing”
- Vertex extrapolation and constraint
 - Extrapolate the track to the point of closest approach to the beam including the nominal interaction point with its spread ($\sigma = 20 \mu\text{m}$) in the fit

Level-3 Reconstruction (Global)



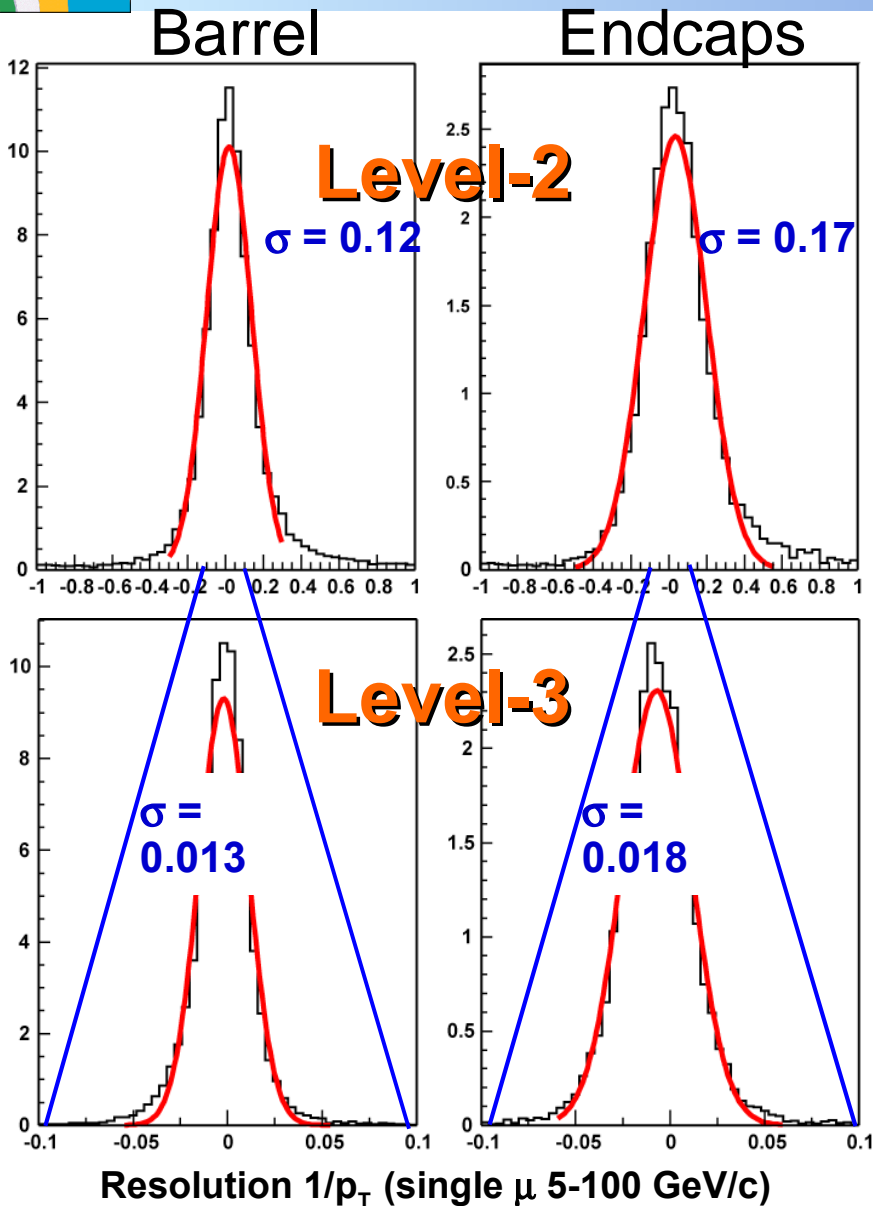
- Start defining a **Region of Interest (ROI)** in the **tracker** using standalone (Level-2) track (with vertex constraint)
 - efficiency and performance crucially depend on Level-2 reconstruction
- Regional reconstruction performed in the ROI
 - Seeds generated from pixels or double sided μ -strip detectors + vertex constraint
 - Again **Kalman filter (inside-out)**
 - up to 30 tracks grown in parallel
 - tracks are discarded if no hit in more than 4 consecutive layers
 - Trajectories which share more than half of the hits are selected on the basis of their χ^2 .
- Tracks are **fitted using also “standalone” reconstructed muons in the spectrometer.**
- Great improvement in resolution with respect to “standalone” reconstruction

- HLT efficiency for muons with $p_T = 5 - 100$ GeV/c



- Overall efficiency ~ 96 %
 - Low energy muons \rightarrow low efficiency because of large multiple scattering
 - Efficiency drops ($\sim 90\%$) in the cracks between wheels
- HLT acceptance is limited to $|\eta| < 2.1$ because no L1 trigger electronics on ME 1/1

HLT Performance: Resolution



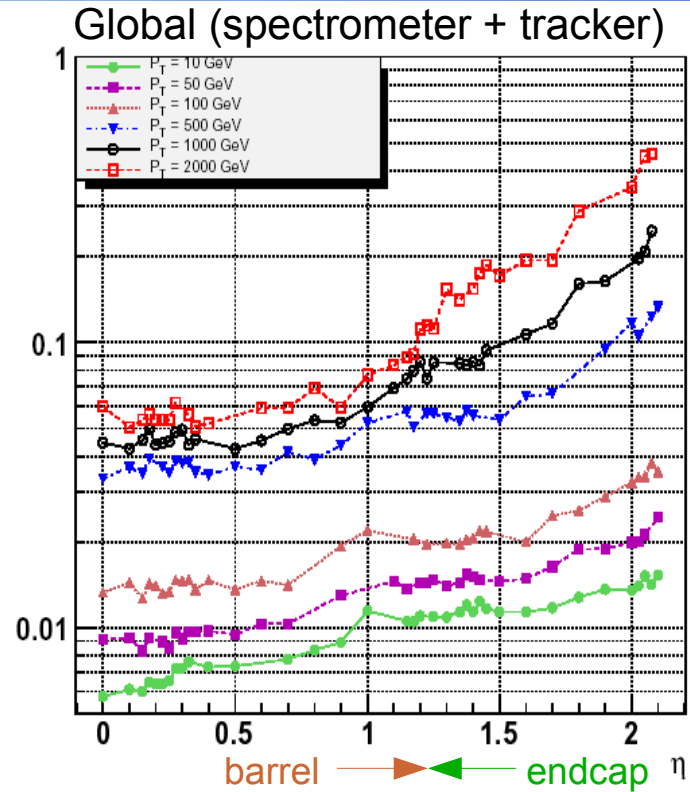
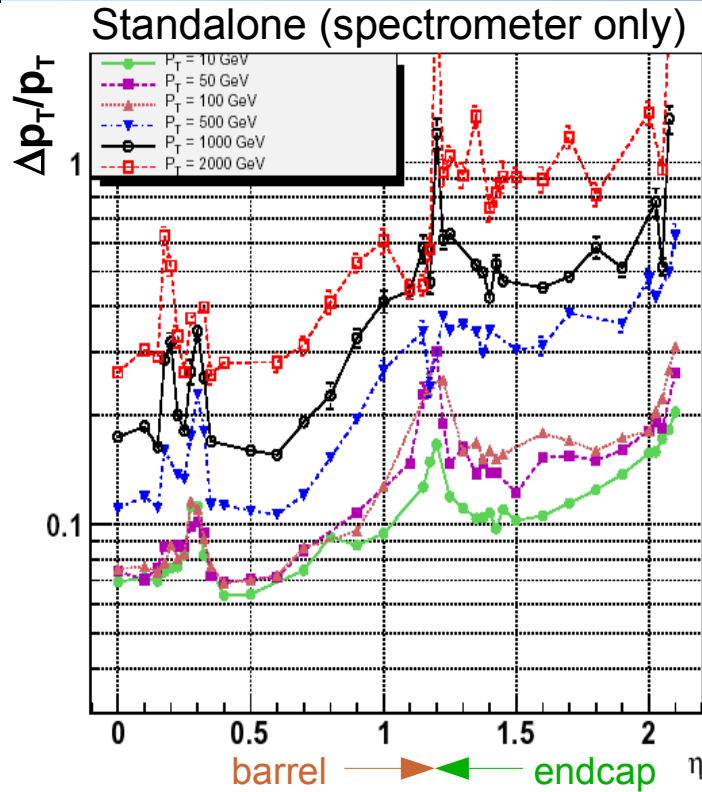
- Good resolution
- Tails under control (very important for trigger rates)

Level-2

resolution x 10

Level-3

- Big improvement using tracker hits

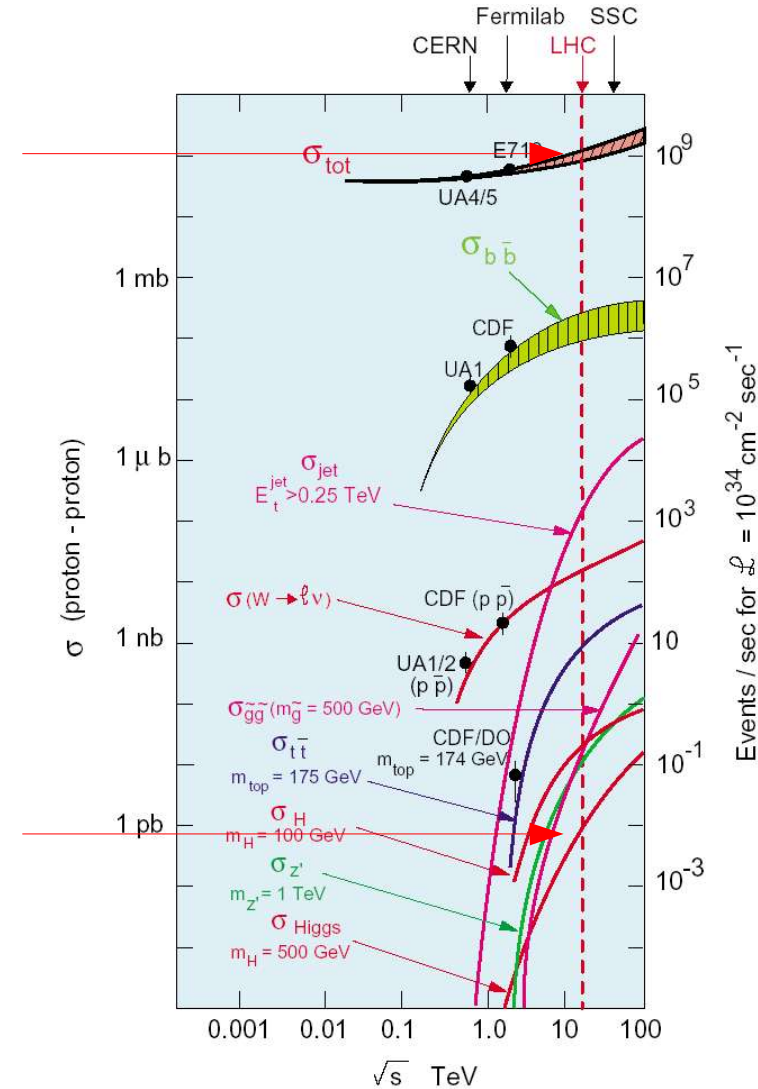


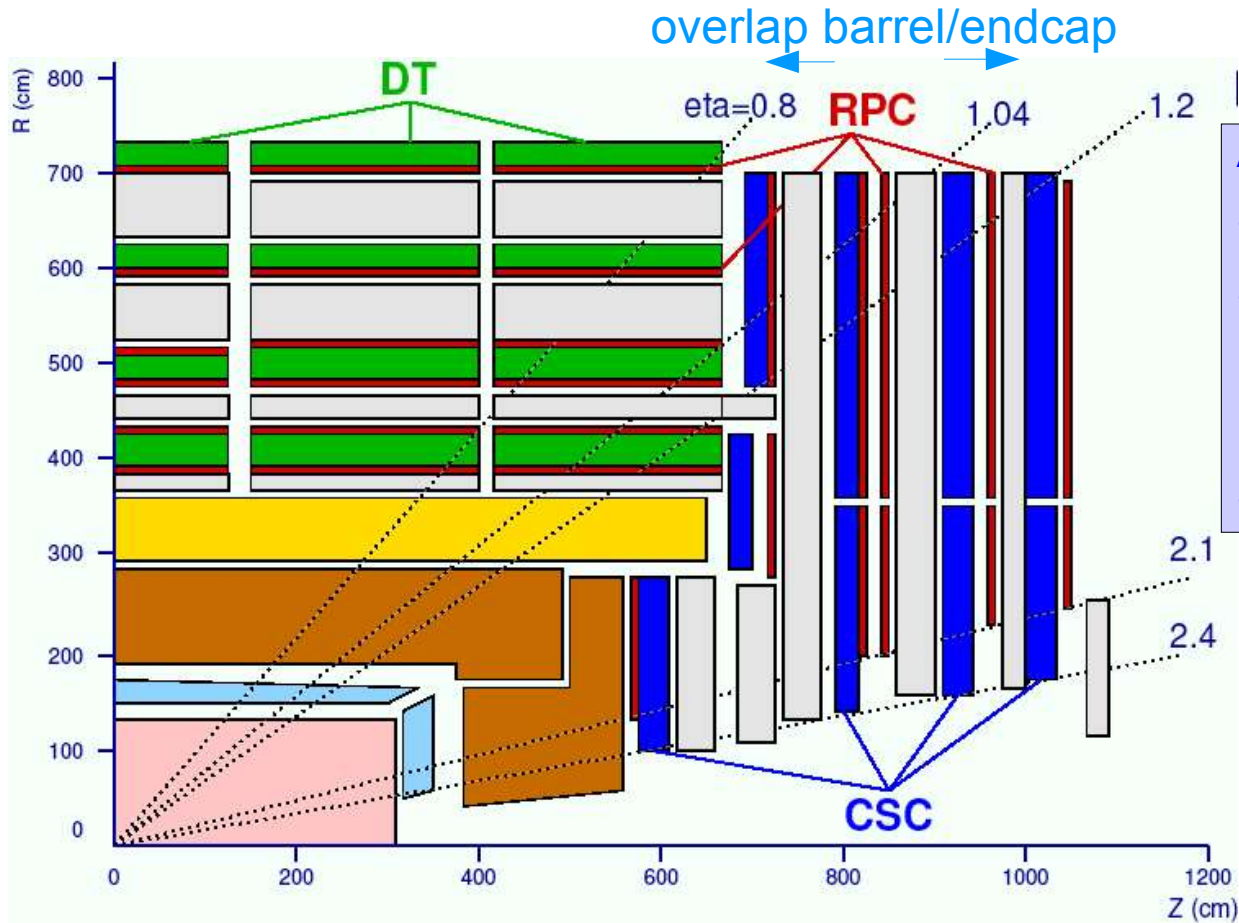
- η dependency due to solenoidal B field
 - High p_T muons ($\sim 1\text{TeV}$):
 - showering in the chambers \rightarrow difficult Local Reconstruction
 - energy loss \rightarrow bias
- New reconstruction strategies under study

- HLT design allows:
 - great flexibility of the algorithms
 - benefits from continuous improvements of the reconstruction software
- Performance of muon reconstruction software must fulfil HLT requirements:
 - maximum reconstruction efficiency
 - good resolution (tails under control) for efficient selection with p_T cuts
- Muon reconstruction software is already robust and well-performing but there is still place for further developments:
 - local reconstruction of high- p_T muons

Backup Slides

- LHC environment is extremely demanding for trigger system
 - High luminosity
 - High Luminosity: $L=10^{34} \text{ cm}^{-2} \text{ s}^{-1}$
 - High background rates
 - total $\sigma_{\text{inel}}^{pp} \sim 55 \text{ mb} \rightarrow$ Event rate $O(1) \text{ GHz}$
 - Pile-up (PU) of several events in the same Bunch Crossing (BX)
 - ~ 17.3 minimum bias events in the same BX
 - High Bunch Crossing frequency
 - $f = 40 \text{ Mhz} \rightarrow$ 1 BX every 25 ns
- Huge selection needed
 - Rejection factor $\sim 10^{10} - 10^{11}$
 - Total MB Rate $O(1) \text{ GHz}$
 - Interesting Physics $O(10-10^{-2}) \text{ Hz}$



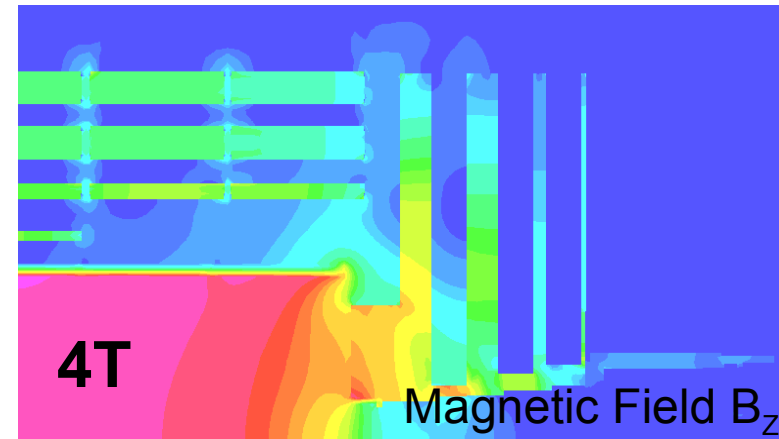
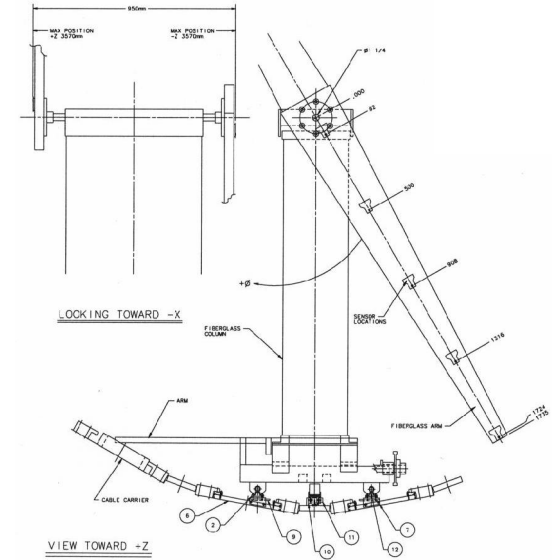


At Startup:

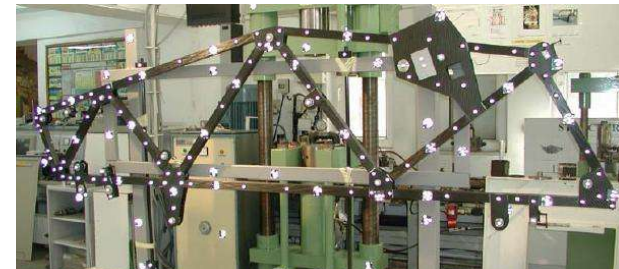
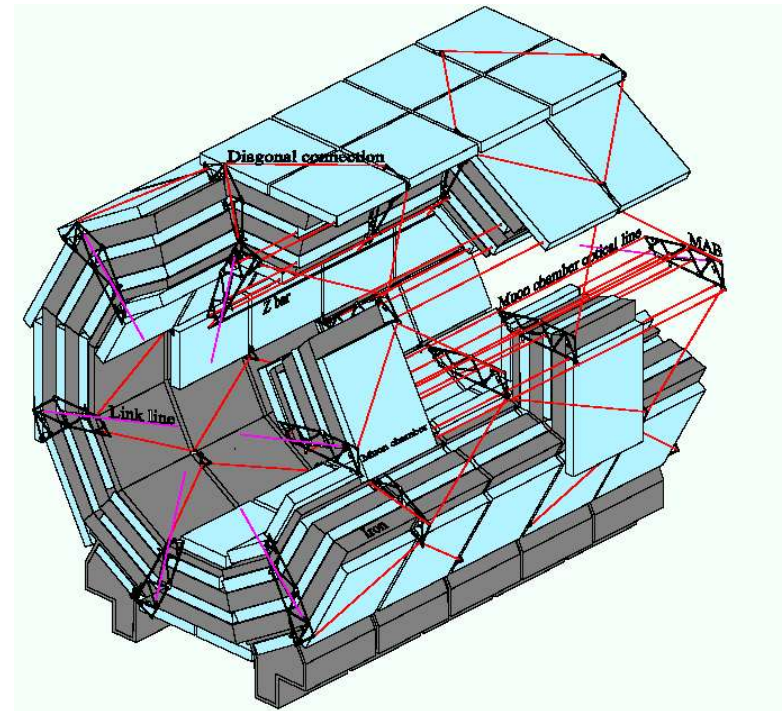
- No ME 4/2
- No trigger electronic on ME1/1
→ trigger $|\eta| < 2.1$
- RPC $|\eta| < 1.6$

- **DT**: 4 stations x 3 superlayers x 4 layers ($|\eta| < 1.2$)
- **CSC**: 4 stations x 6 layers ($0.8 < |\eta| < 1.2$)
- **RPC**: 6 stations in barrel + 4 stations in endcaps ($|\eta| < 1.6$)

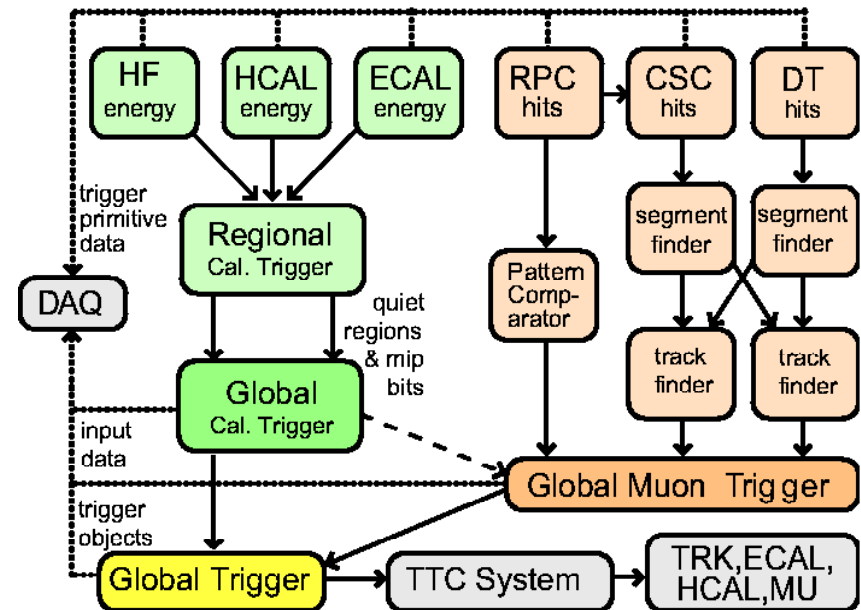
- Superconducting Solenoid
 - $r = 3\text{m}$, $L=14\text{m}$
 - $B = 14\text{T}$ within the solenoid
 - $B \sim 1.8\text{T}$ in the iron return yoke
- Great bending power
- Independent measurement inside / outside
- A lot of material within chambers
- Field measurement:
 - During Magnet Test (2006)
 - Rotating arm instrumented with Hall and NMR probes:
 - $\Delta r = 20\text{ cm}$, $\Delta z = 5\text{ cm}$
 - NMR probes inside the solenoid for on-line monitoring



- Chamber alignment is fundamental
 - chamber resolution $\sim 100 \mu\text{m}$
 - movements due to $B_{\text{on}}/B_{\text{off}}$: $O(1\text{cm})!$
- Optical alignment system
 - rigid structures + optical links (LED, laser, CCD)
 - link system for alignment with tracker
 - performance:
 - $\sigma_{r\phi} \sim 150 \mu\text{m}$ (same sector)
 - $\sigma_{r\phi} \sim 210 \mu\text{m}$ (between sectors)
- Alignment with tracks
 - Problem: knowledge of material and magnetic field
 - Only muons with $p_T > \sim 50 \text{ GeV}/c$ are useful

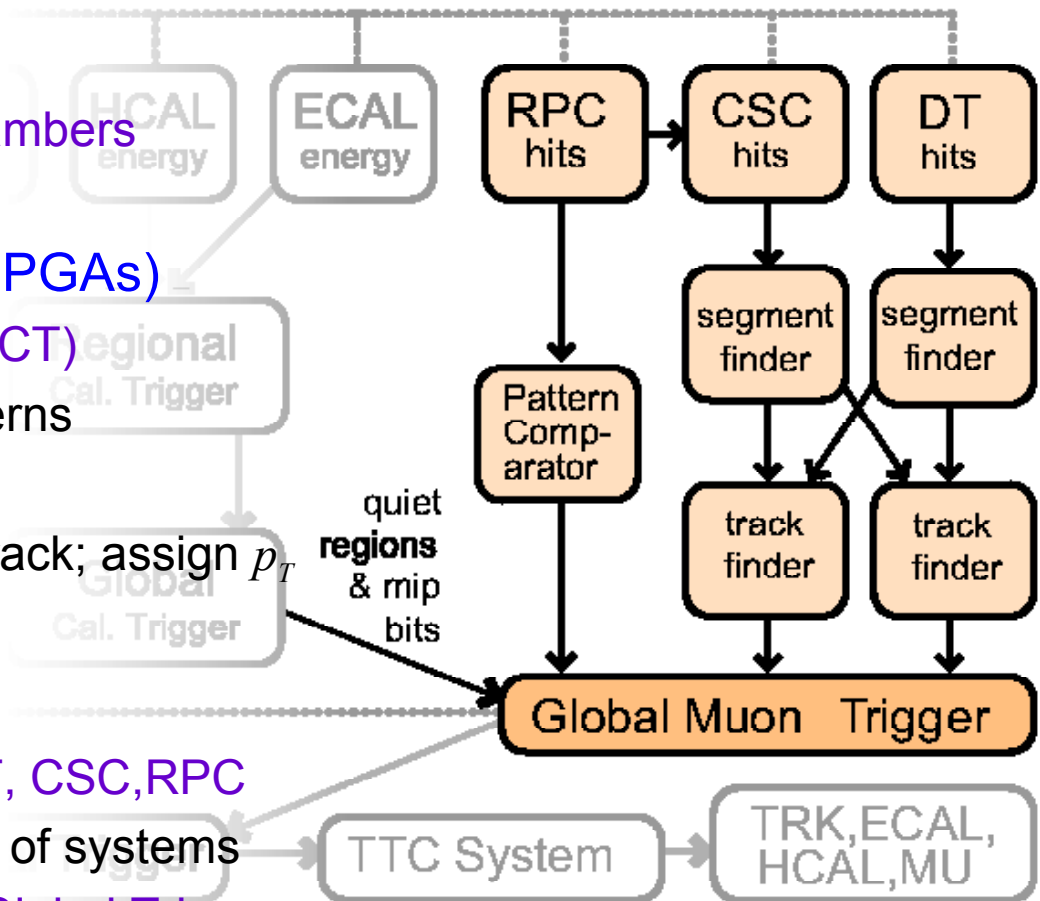


- Implemented on custom hardware
 - minimal dead time
- Synchronous, pipelined (25 ns)
 - delayed by $3.2 \mu\text{s} = 128 \text{ BX}$ including propagation ($\sim 1\text{-}2 \mu\text{s}$)
- Max output \equiv max DAQ input
 - Design: **100 kHz**; at startup: 50 kHz
- 2 Subsystems
 - **Calorimeter Trigger**
 - **Muon Trigger**
 - Result: jet, e/γ , μ , τ jet candidates; E_T^{miss} , ΣE_T



- No local decisions; selection by the “**Global Trigger**”
 - 128 simultaneous, programmable algorithms, each allowing:
 - Thresholds on single and multiple objects of different type
 - Correlations, topological conditions, Prescaling

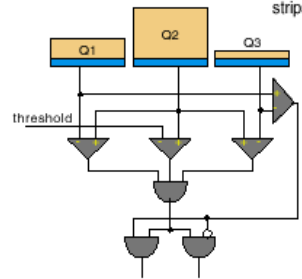
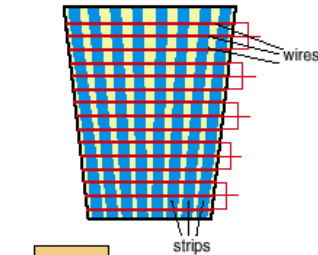
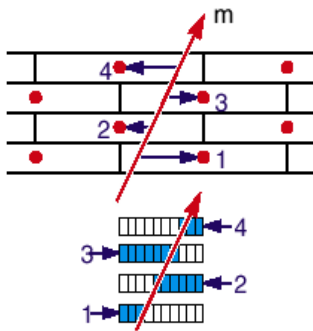
- Local” (chamber) level (ASICs)
 - Find segments in DT/CSC chambers
- “Regional” (subsystem) level (FPGAs)
 - RPC: Pattern Comparator (PACT)
 - looks for predefined patterns
 - DT/CSC Track Finders
 - combine segments into track; assign p_T
- Global Muon Trigger
 - Combines candidates from DT, CSC, RPC
 - Exploits complementarity of systems
 - Delivers 4 best muons to the Global Trigger
 - Each with p_T , position, angle, BX, quality
 - Efficiency: ~97%
 - p_T resolution: 17-22% depending on η (muons from W decays)



Local Trigger: build segments

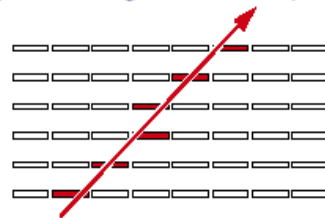
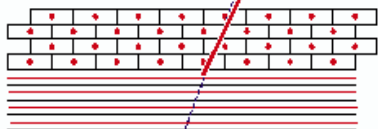
DT

CSC (strips)



Meantimers recognize tracks and form vector / quartet.

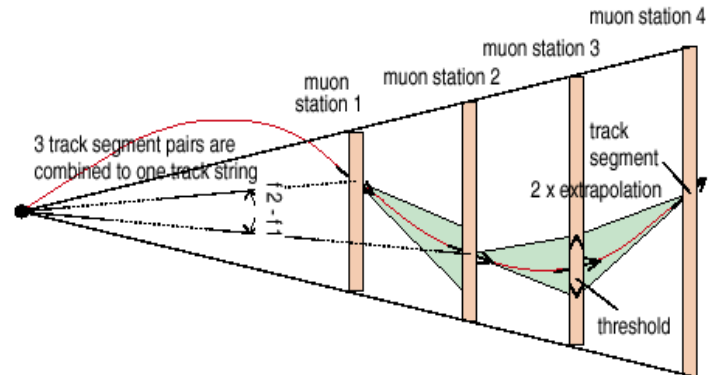
Comparators give 1/2-strip resol.



Correlator combines them into one vector / station.

Hit strips of 6 layers form a vector.

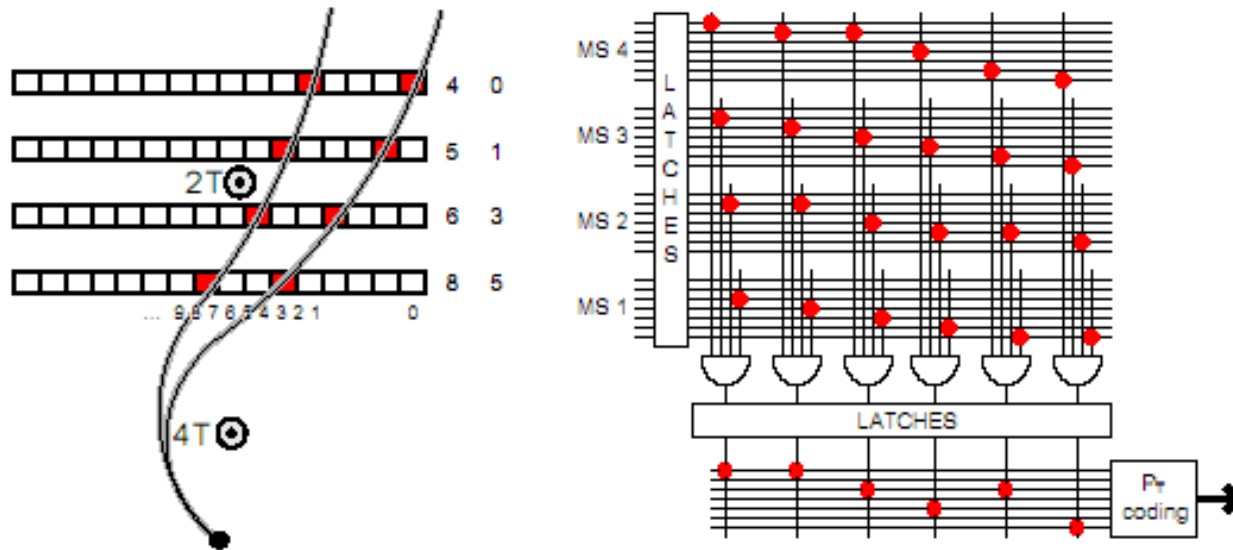
Regional Trigger: DT/CSC Track Finders



- Extrapolation Unit
 - Link segments using look-up tables
- Track Assembler:
 - link segment pairs to tracks
 - cancel fakes
- Assignment Units
 - p_T , charge, η , ϕ , quality

ASICs on detector or peripheral crates

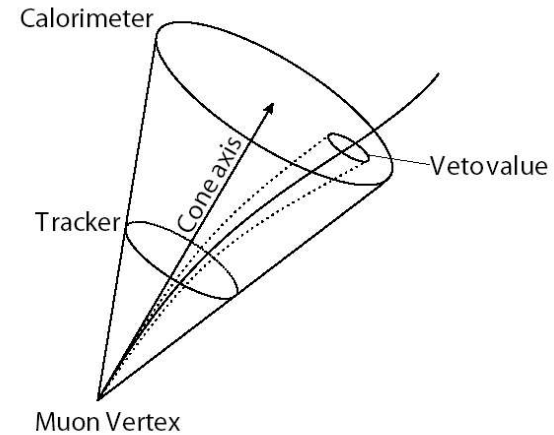
FPGAs in the control room



- Based on Pattern Comparator (PACT)
 - Look for predefined hit patterns in time coincidence
 - At least 3 hits out of 4 stations
 - 2 different groups of 4 stations in the barrel (6 stations in total)
 - Each hit pattern corresponds to a p_T value
 - Hardware: ASICs
 - Located in the counting room

- Kalman Filter is a recursive method for the fit of a discrete set of data
 - Provides track fitting independent of the number of measurement available
- PROBLEM: Determination of a generic state vector \mathbf{x} (= position + momentum to a given surface) given a set of measurement \mathbf{z}_k .
- METHOD:
 - Start from a seed (= initial state vector + covariance matrix)
 - Each step k consists of two phases:
 - *propagation*: predict an a priori state \mathbf{x}_k^- obtained by projecting the previous state with its covariant matrix
 - *update*: use the information from all measurement to update the state \mathbf{x}_k and the covariance matrix
- RESULT:
 - the result is the state on the surface of the last measurement station
- SMOOTHING:
 - Update the trajectory parameters of previous steps using all the measurement at every measured surface.

- $K, \pi, b, c \rightarrow \mu$ decays are accompanied by jets
 - Discard muons with high “activity” in their neighborhood
 - Based on ΣE_T or ΣP_T in cones around the muon
 - Cone sizes and thresholds are optimized
 - To get maximal rejection on background muons for a given efficiency on reference signal ($W \rightarrow \mu\nu$)
 - flat $\varepsilon(\eta)$ on signal by construction



- **Calorimeter Isolation**

ΣE_T from calorimeter towers in a cone around muon

- Can be applied already at L2
- Sensitive to pile-up

- **Tracker Isolation**

ΣP_T of tracks in a cone around L3 muon, exploiting:

- Regional reconstruction in the tracker
- Conditional tracking



Navigation in the Muon Detectors



- **Navigation**
 - find the next detector crossed by one trajectory, given its parameters at a given point
 - extrapolate state vector and errors for the fit
- Navigation must be optimized to cope with trigger timing
 - requires a lot of CPU time
 - extrapolation through the iron with inhomogeneous magnetic field
 - available tool: GEANE (based on ZEBRA/G3 geometry)
- Optimization through organization of the detectors in a hierarchical structure
 - minimize the number of extrapolation steps

$$\mathcal{L} = 10^{34} \text{ cm}^{-2}\text{s}^{-1}$$

