

Physics of Particle Detection

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Basic idea

Every effect of particles or radiation can be used as a working principle for a particle detector.

Outline of the Lectures

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- *methods of particle identification:*
 - Measure the bending radius ρ in a magnetic field B ($\vec{p} \perp \vec{B}$):

$$\frac{mv^2}{\rho} = z \cdot e \cdot v \cdot B \Rightarrow \rho = \frac{p}{zeB} \propto \frac{\gamma m_0 \beta c}{z}$$

with p : momentum; $\beta = \frac{v}{c}$; $\gamma = \frac{1}{\sqrt{1 - \frac{v^2}{c^2}}}$.

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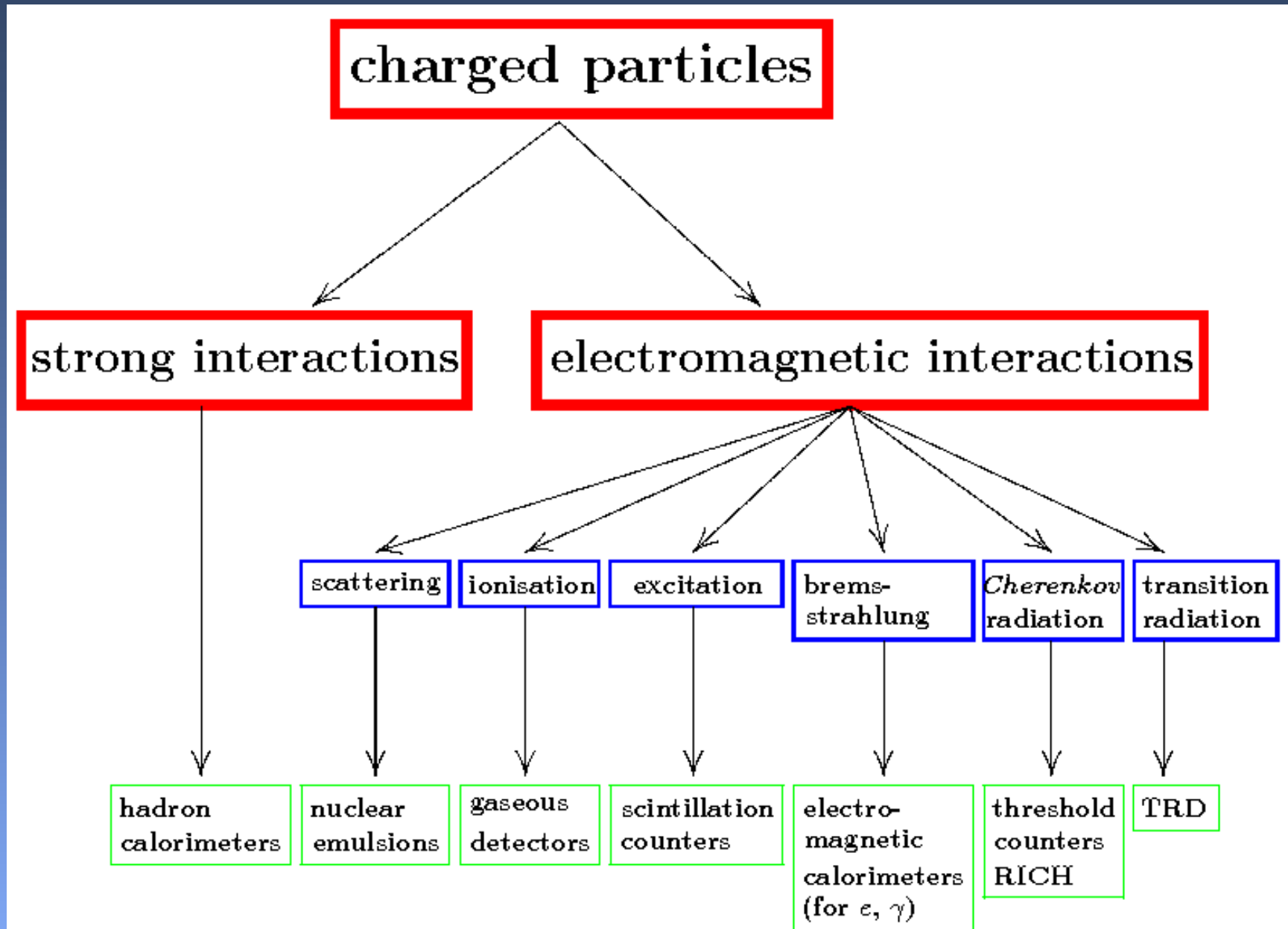
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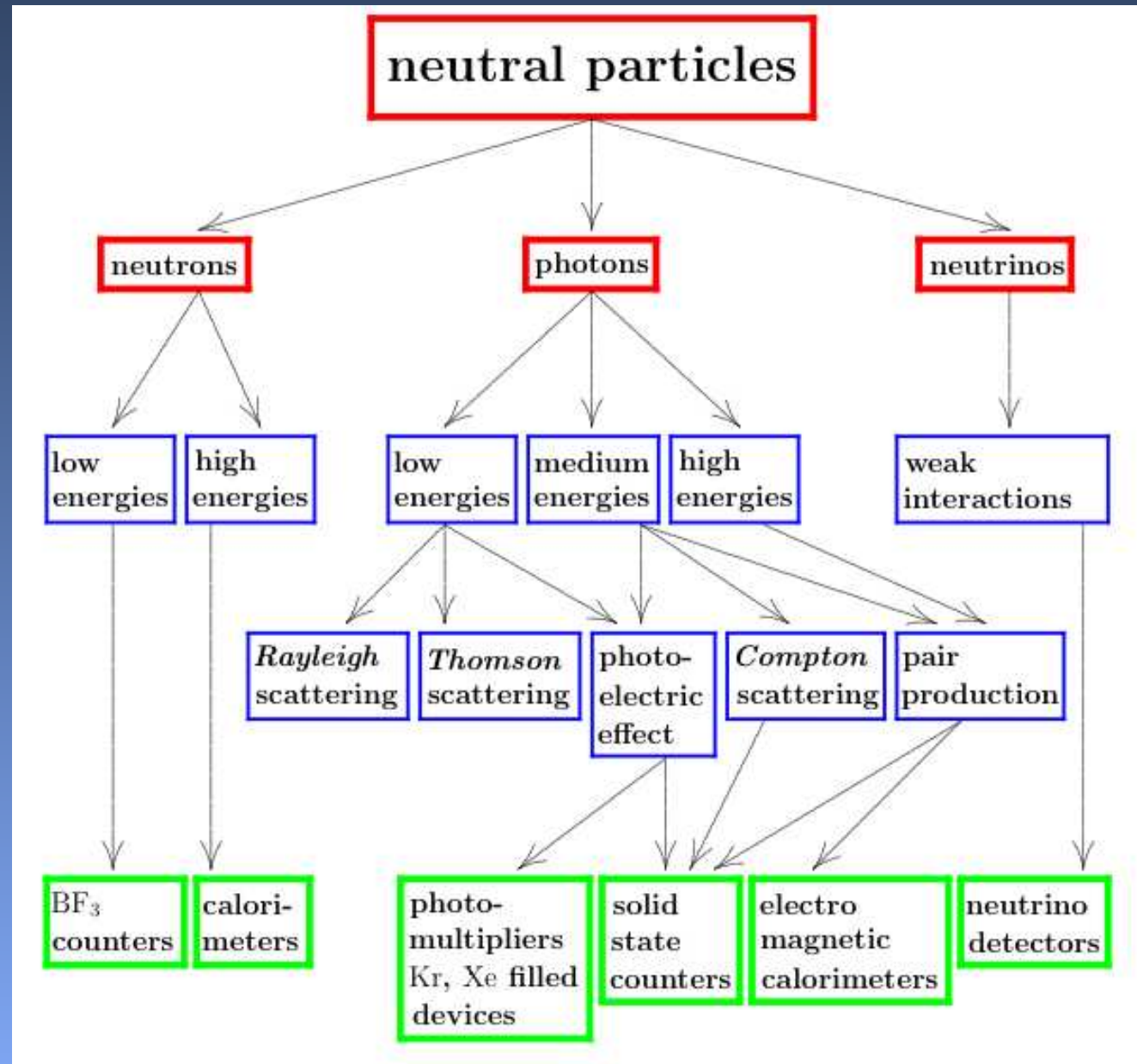
- Measure the energy loss due to transition radiation:

$$\left(\frac{dE}{dx}\right)_{\text{transition}} \propto z^2\gamma.$$

Charged Particles



Neutral Particles



Interaction of Charged Particles

Kinematics: a particle of mass m_0 and velocity $v = \beta c$ collides with an electron; maximum transferable energy:

$$E_{\max}^{\text{kin}} = \frac{2m_e c^2 \beta^2 \gamma^2}{1 + 2\gamma \frac{m_e}{m_0} + \left(\frac{m_e}{m_0}\right)^2} = \frac{2m_e p^2}{m_0^2 + m_e^2 + 2m_e E/c^2}$$

with E : total energy of the particle, $\gamma = \frac{E}{m_0 c^2}$.

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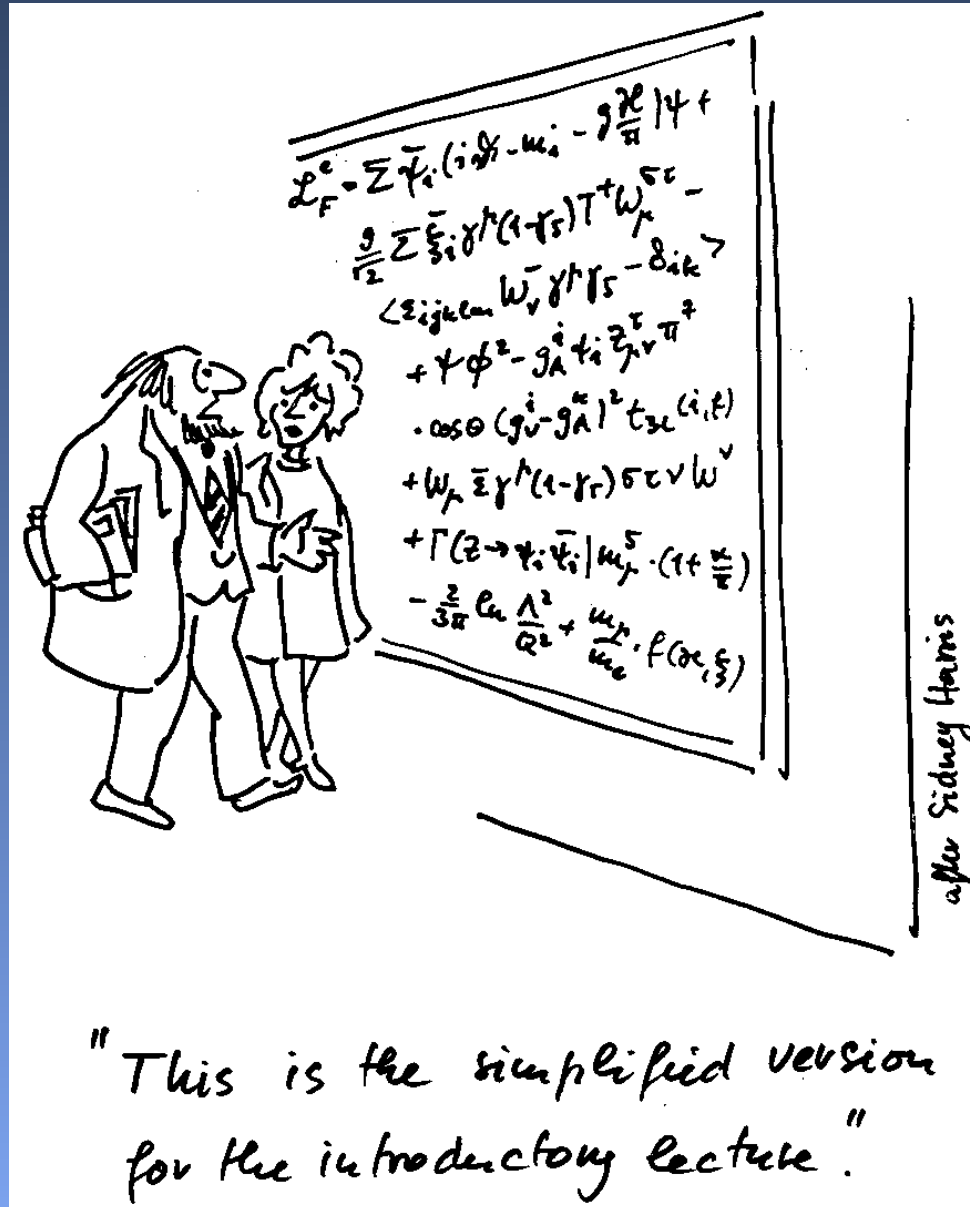
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Examples:

(a) $\mu - e$ - collision: $E_{\max} = \frac{E^2}{E + 11}$ (E in GeV)

(b) if $m_0 = m_e$: $E_{\max}^{\text{kin}} = \frac{p^2}{m_e + E/c^2} = \frac{E^2 - m_e^2 c^4}{E + m_e c^2} = E - m_e c^2$

Simplified Version



Rutherford Scattering

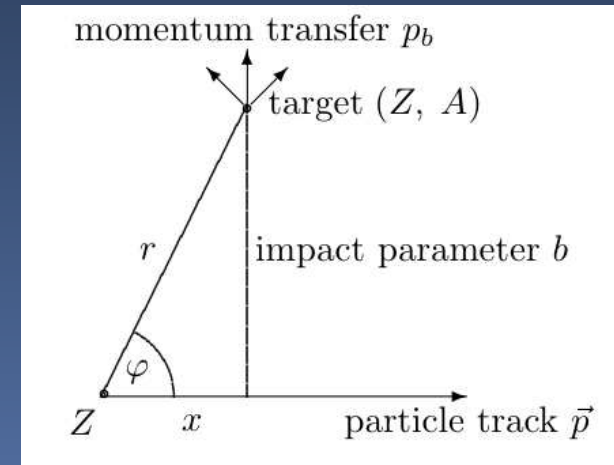
$$\vec{F} = \frac{ze \cdot Ze}{r^2} \cdot \frac{\vec{r}}{r},$$

$$p_b = \int_{-\infty}^{\infty} F_b dt = \int_{-\infty}^{\infty} \frac{zZe^2}{r^2} \cdot \frac{b}{r} \cdot \frac{dx}{\beta c},$$

$$p_b = \frac{zZe^2}{\beta c} \int_{-\infty}^{\infty} \frac{b dx}{(\sqrt{x^2 + b^2})^3}$$

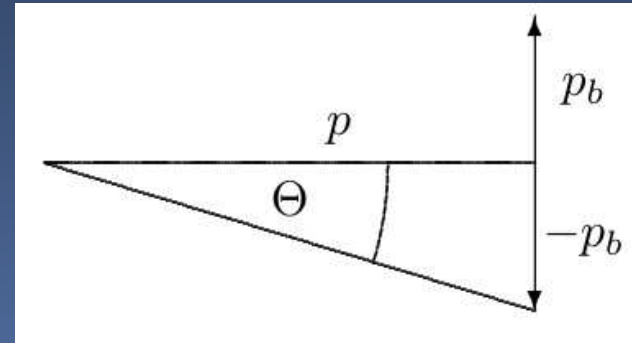
$$= \frac{zZe^2}{\beta cb} \int_{-\infty}^{\infty} \frac{d(x/b)}{(\sqrt{1 + (x/b)^2})^3} = \frac{2zZe^2}{\beta cb},$$

$$\rightsquigarrow p_b = \frac{2r_e m_e c}{b\beta} zZ \quad \text{with} \quad r_e = \frac{e^2}{m_e c^2}.$$



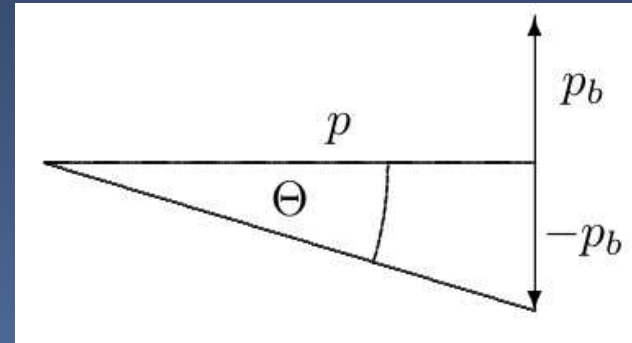
Scattering Angle

$$\Theta = \frac{p_b}{p} = \frac{2zZe^2}{bc\beta} \cdot \frac{1}{p}$$



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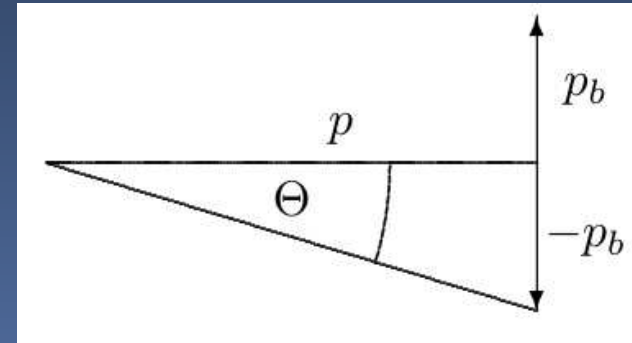
Cross section for scattering into the solid angle:

$$d\Omega = \sin \Theta d\Theta d\varphi = -d \cos \Theta d\varphi$$

with Θ : polar angle, φ azimuthal angle.

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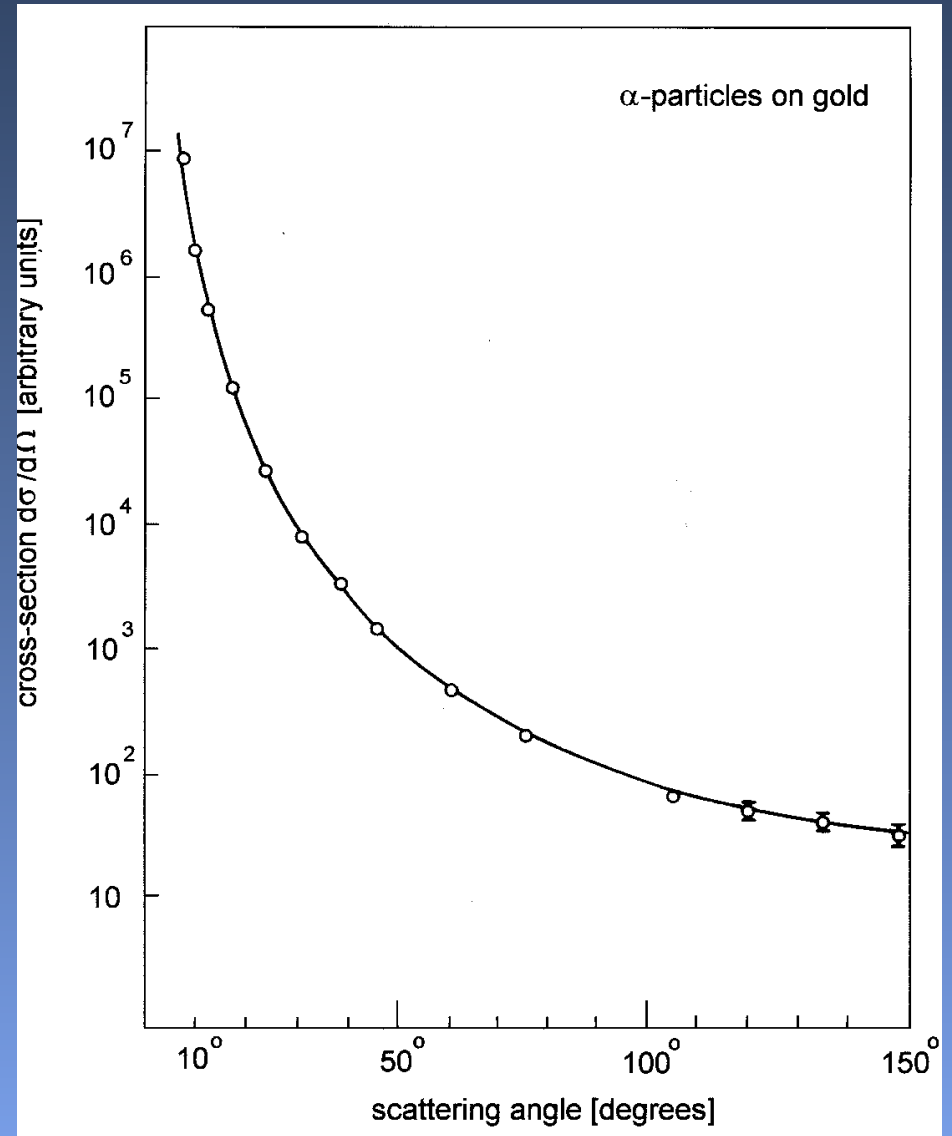
“Rutherford scattering”:

$$\frac{d\sigma}{d\Omega} = \frac{z^2 Z^2}{4} r_e^2 \left(\frac{m_e c}{\beta p} \right)^2 \cdot \frac{1}{\sin^4 \Theta / 2}$$

Scattering of α -Particles on Gold

E. Rutherford
Phil. Mag. 21 (1911) 669

H. Geiger, E. Marsden
Phil. Mag. 25 (1913) 604

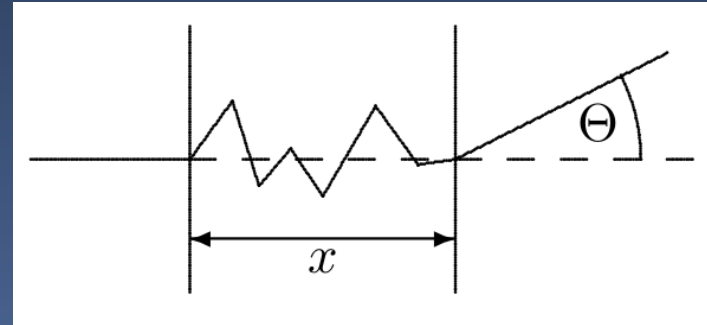


Multiple Scattering

$$\langle \Theta \rangle = 0$$

p in MeV/c

X_0 : radiation length

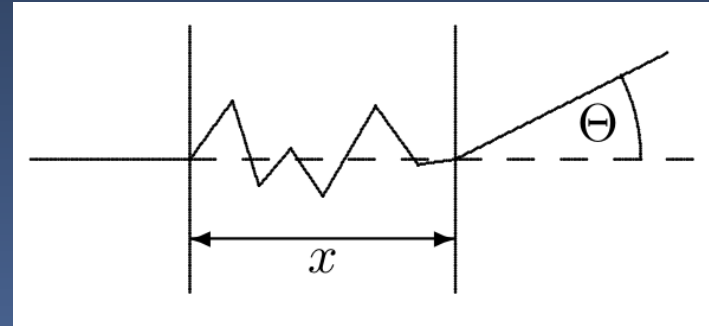


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$$\sqrt{\langle \Theta^2 \rangle} = \Theta_{\text{plane}} = \frac{13.6 \text{ MeV}}{\beta cp} z \sqrt{\frac{x}{X_0}} \left\{ 1 + 0.038 \ln \left(\frac{x}{X_0} \right) \right\}$$

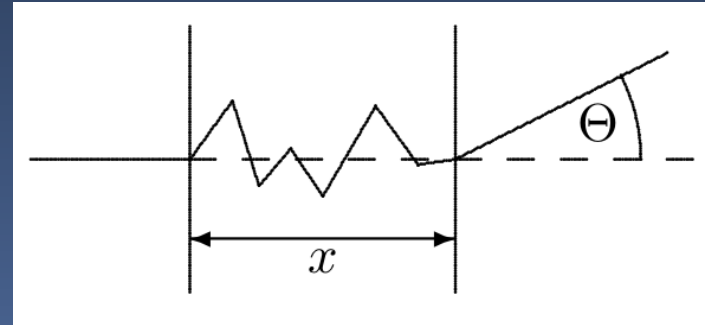
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Projected angular distribution:

$$P(\Theta) d\Theta = \frac{1}{\sqrt{2\pi} \Theta_0} \exp \left\{ -\frac{\Theta^2}{2\Theta_0^2} \right\} d\Theta$$

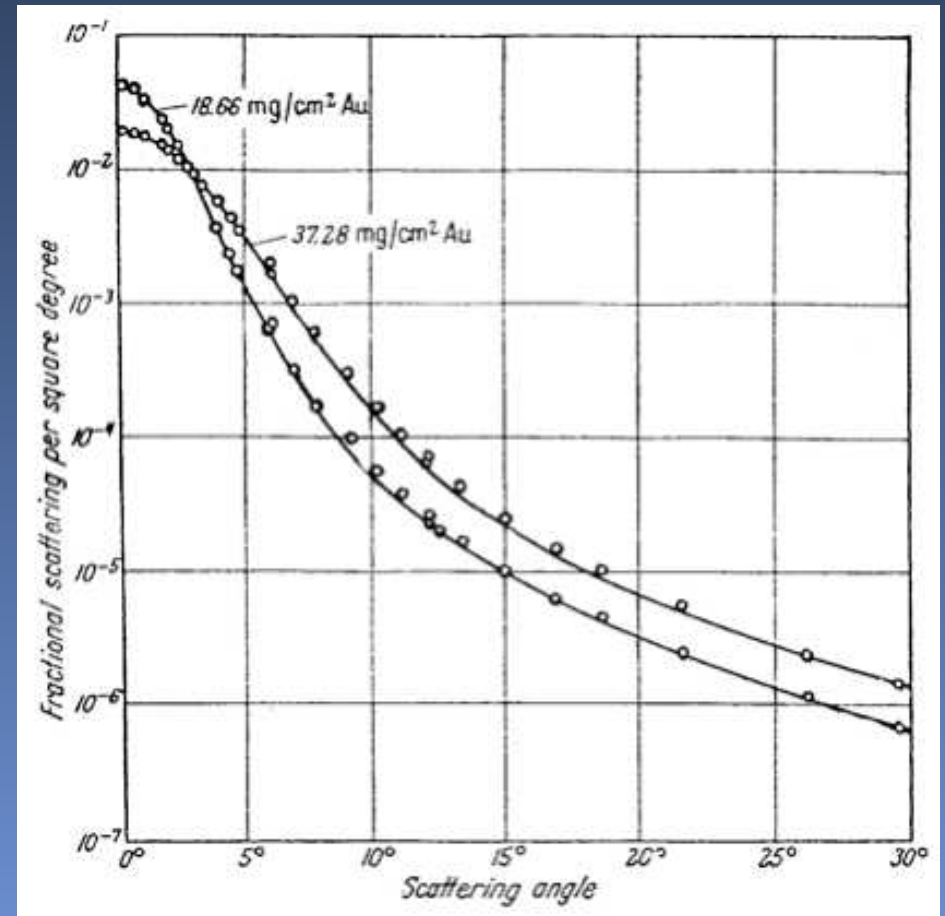
+ tail due to single, large angle Coulomb scattering.

Scattering of α -particles on Gold

Electrons of 15.7 MeV
on Au-foils

$< 5^\circ$ dominated by
multiple scattering

$> 15^\circ$ dominated by
single scattering



A.O. Hanson et al., Phys.Rev. 84 (1951) 634
R.O. Birkhoff, Handb.Phys. XXXIV (1958)

Ionisation Energy Loss (Bethe-Bloch formula, 1)

$$p_b = \frac{2r_e m_e c}{b\beta} z \quad \text{per target electron.}$$

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Interaction rate per (g/cm²), given the atomic cross section:

$$\phi(\text{g}^{-1} \text{ cm}^2) = \frac{N}{A} \cdot \sigma [\text{cm}^2 / \text{atom}]$$

with N : *Avogadro's number*.

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$$\phi(\varepsilon) d\varepsilon = \frac{N}{A} \cdot \underbrace{2\pi b db}_{\text{area of an annulus}} \cdot Z$$

with Z : electrons per target atom.

Ionisation Energy Loss (Bethe-Bloch formula, 2)

$$\varepsilon = f(b) \Rightarrow b^2 = \frac{2r_e^2 m_e c^2}{\beta^2} z^2 \cdot \frac{1}{\varepsilon}.$$

$$\phi(\varepsilon)d\varepsilon = \frac{N}{A} \cdot Z \cdot 2\pi \cdot \underbrace{\frac{r_e^2 m_e c^2}{\beta^2} z^2 \frac{d\varepsilon}{\varepsilon^2}}_{b \text{ db}} \propto \frac{1}{\varepsilon^2}.$$

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$$\frac{dE}{dx} = \frac{2\pi N}{A} \cdot Z \cdot \int_0^{\infty} \varepsilon b \, db = 2\pi \frac{Z \cdot N}{A} \cdot \frac{2r_e^2 m_e c^2}{\beta^2} z^2 \int_0^{\infty} \frac{db}{b}.$$

Problem: the integral is divergent at $b = 0$ and $b = \infty \dots$

Ionisation Energy Loss (Bethe-Bloch formula, 3)

$b = 0$:

Assume $b_{\min} = \frac{h}{2p} = \frac{h}{2\gamma m_e \beta c}$ half the *de Broglie wavelength*.

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$$\tau_i = \frac{b_{\max}}{v} \sqrt{1 - \beta^2}$$

with $\sqrt{1 - \beta^2}$: *Lorentz-contraction* of the field at high velocities

$$\tau_r = \frac{1}{\nu_z \cdot Z} = \frac{h}{I} \quad \tau_i = \tau_r \Rightarrow b_{\max} = \frac{\gamma h \beta c}{I}$$

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$$\rightsquigarrow -\frac{dE}{dx} = \frac{2\pi ZN}{A} \frac{2r_e^2 m_e c^2}{\beta^2} z^2 \left[\ln \frac{2\gamma^2 \beta^2 m_e c^2}{I} - \underbrace{\eta}_{\text{screening effect}} \right]$$

Bethe-Bloch formula: exact treatment

$$\frac{dE}{dx} = 2\pi \frac{ZN}{A} \frac{2r_e^2 m_e c^2}{\beta^2} z^2 \left[\frac{1}{2} \ln \left(\frac{2m_e c^2 \gamma^2 \beta^2}{I^2} E_{\max}^{\text{kin}} \right) - \beta^2 - \frac{\delta}{2} \right]$$

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Density correction:

$$\frac{\delta}{2} = \ln \left(\frac{\hbar\omega_p}{I} \right) + \ln(\beta\gamma) - \frac{1}{2}$$

where $\hbar\omega_p = \sqrt{4\pi N_e r_e^3 \frac{m_e c^2}{\alpha}}$ (plasma energy).

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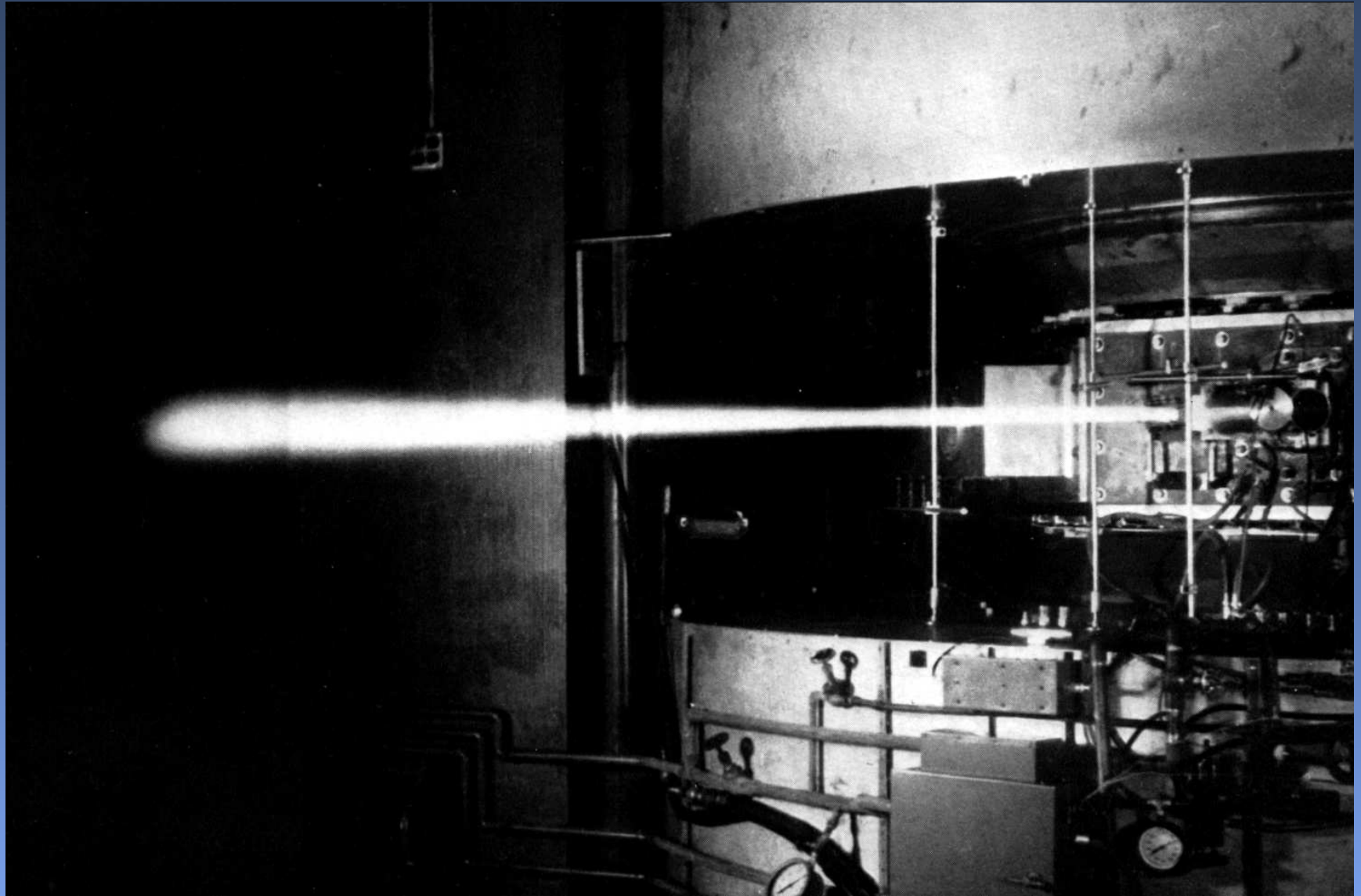
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- N_e : electron density of the absorbing material
- α : fine structure constant = $\frac{1}{4\pi\epsilon_0} \cdot \frac{e^2}{\hbar c}$
- ϵ_0 : permittivity of free space

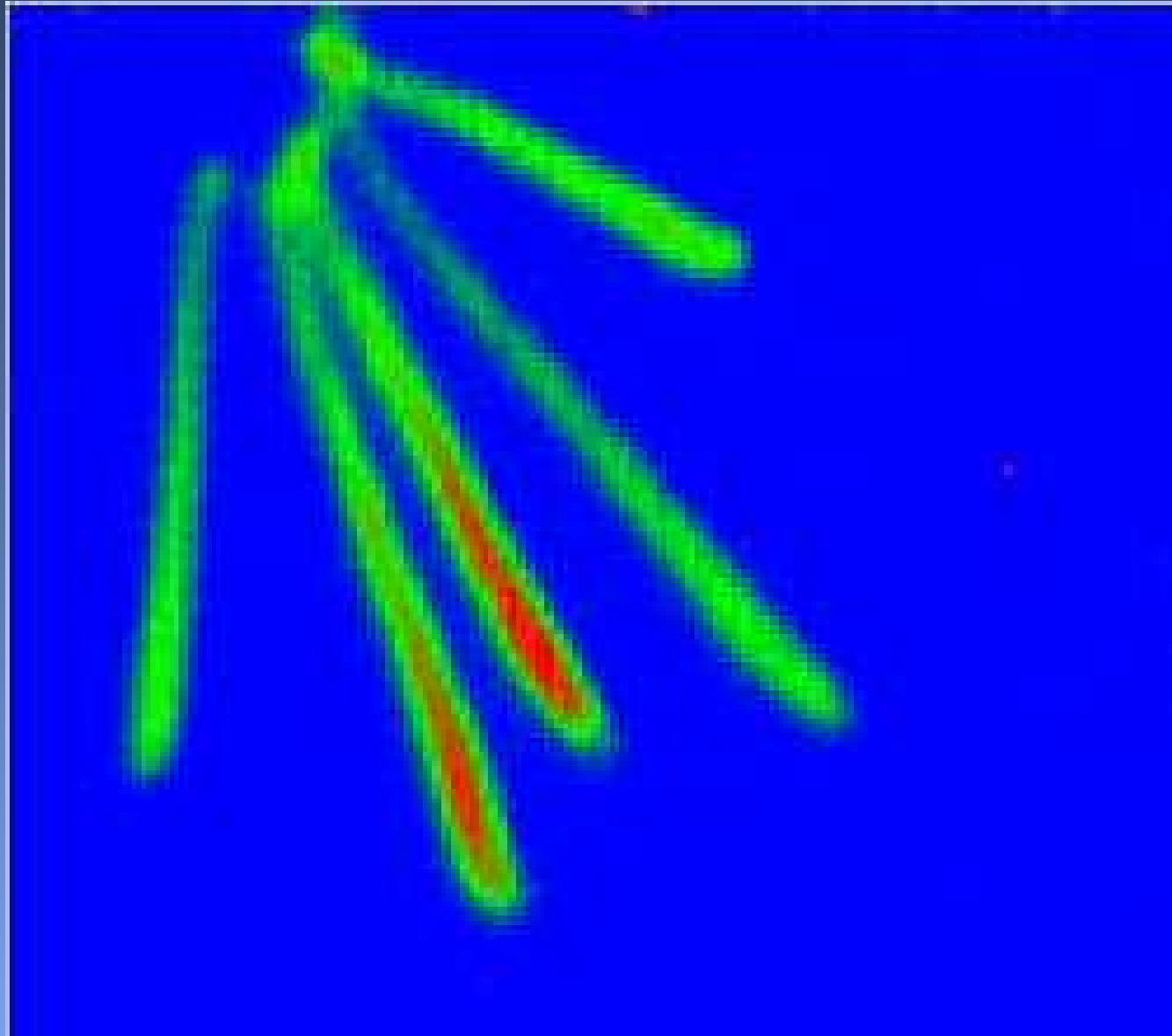
Speed Limit



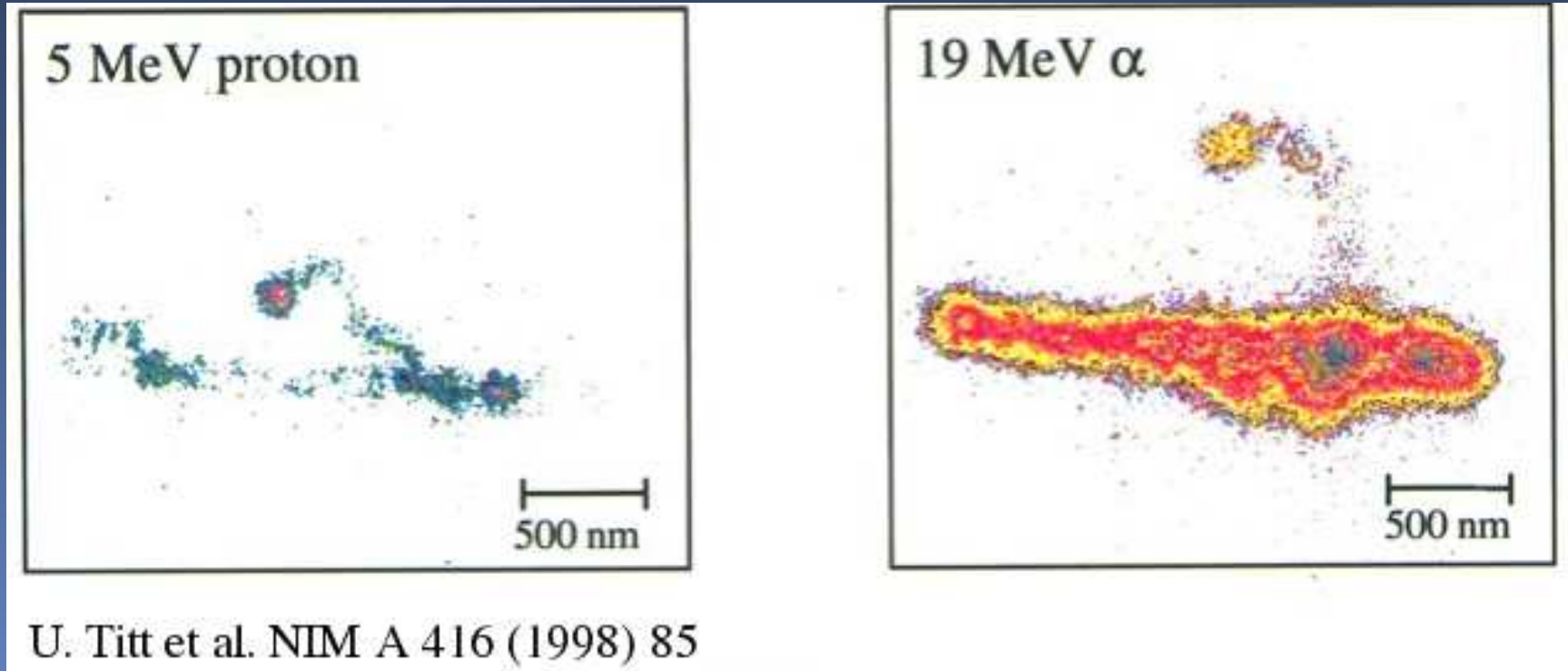
Deuteron Beam Scintillating in Air



α Tracks in a Micro Pattern Chamber



Proton and α Ranging out



Optical avalanche microdosimeter: demonstrates $\left(\frac{dE}{dx}\right)_{\alpha} \gg \left(\frac{dE}{dx}\right)_p$
because $\frac{dE}{dx} \sim z^2$

$$E_p = 5.0 \text{ MeV} \quad \text{with } \delta\text{-ray}$$

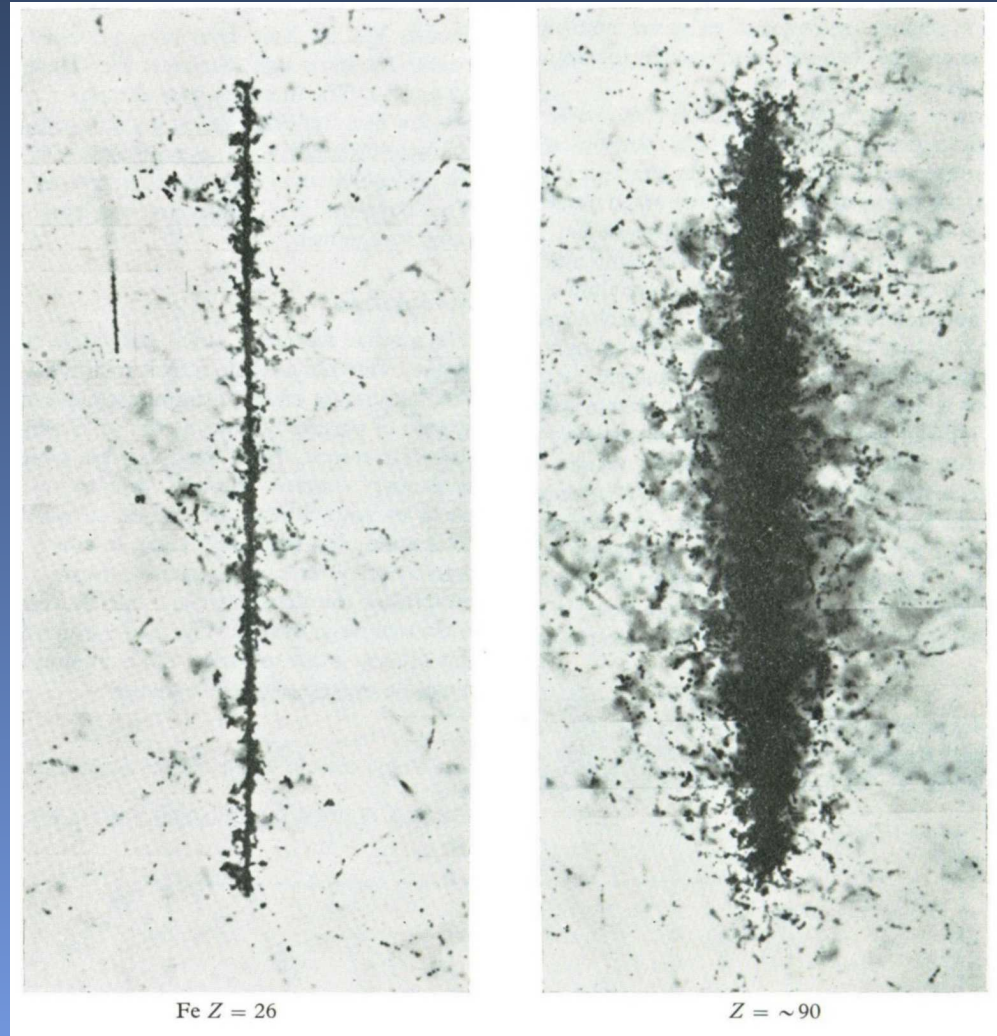
$$E_{\alpha} = 19 \text{ MeV} \quad \text{with } \delta\text{-ray}$$

Heavy Nuclei in Cosmic Rays

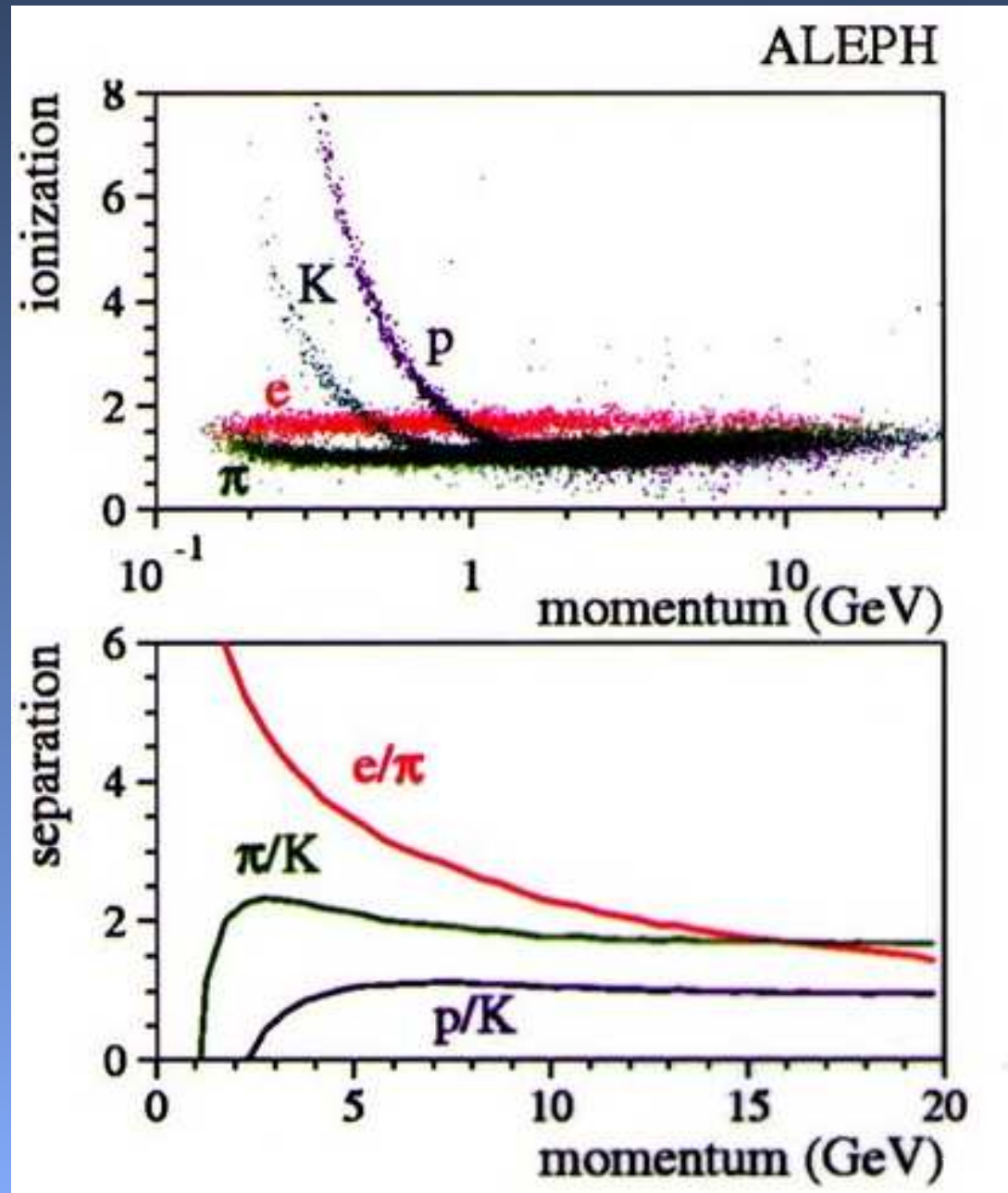
Ionisation density of relativistic heavy ions from cosmic radiation in nuclear emulsions

G. D. Rochester

Advancement of Science
Dec. 1970, p.183-194



(ALEPH): Particle Identification with dE/dx

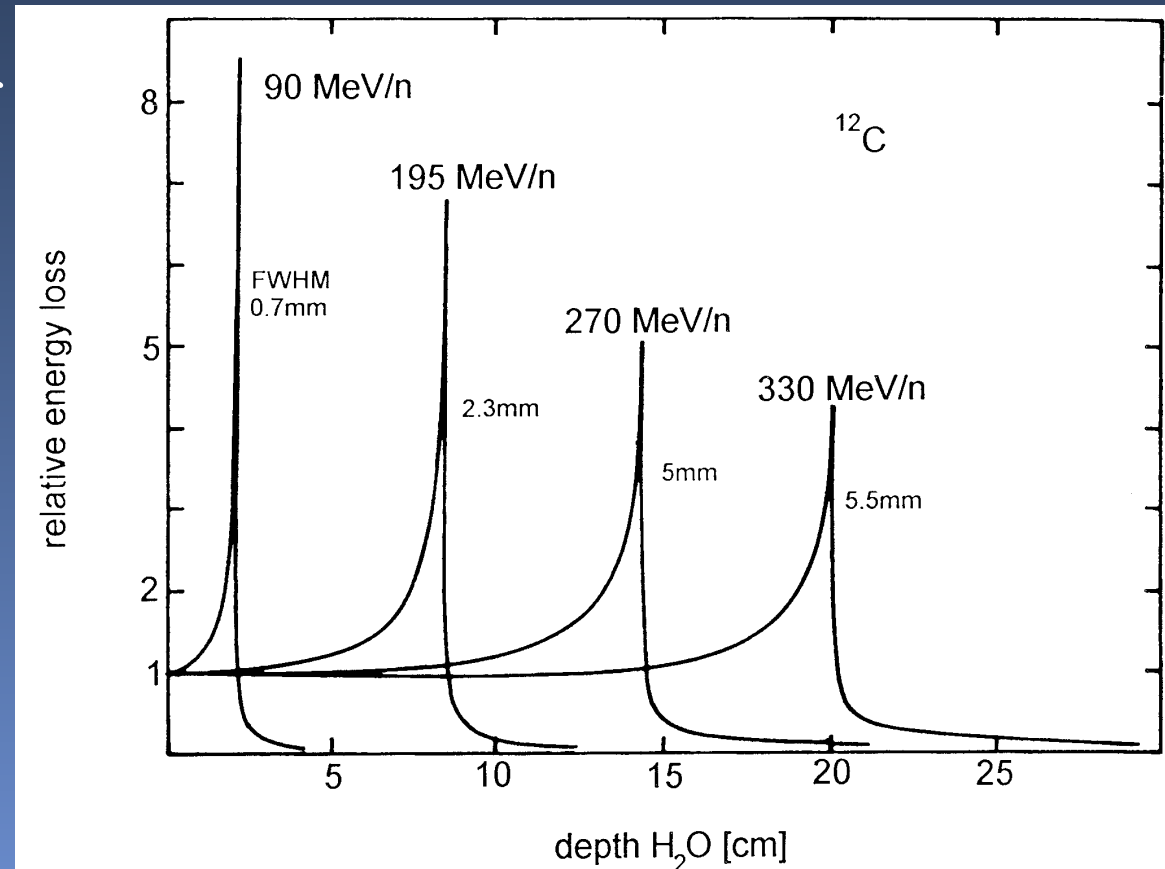


Bragg Curves

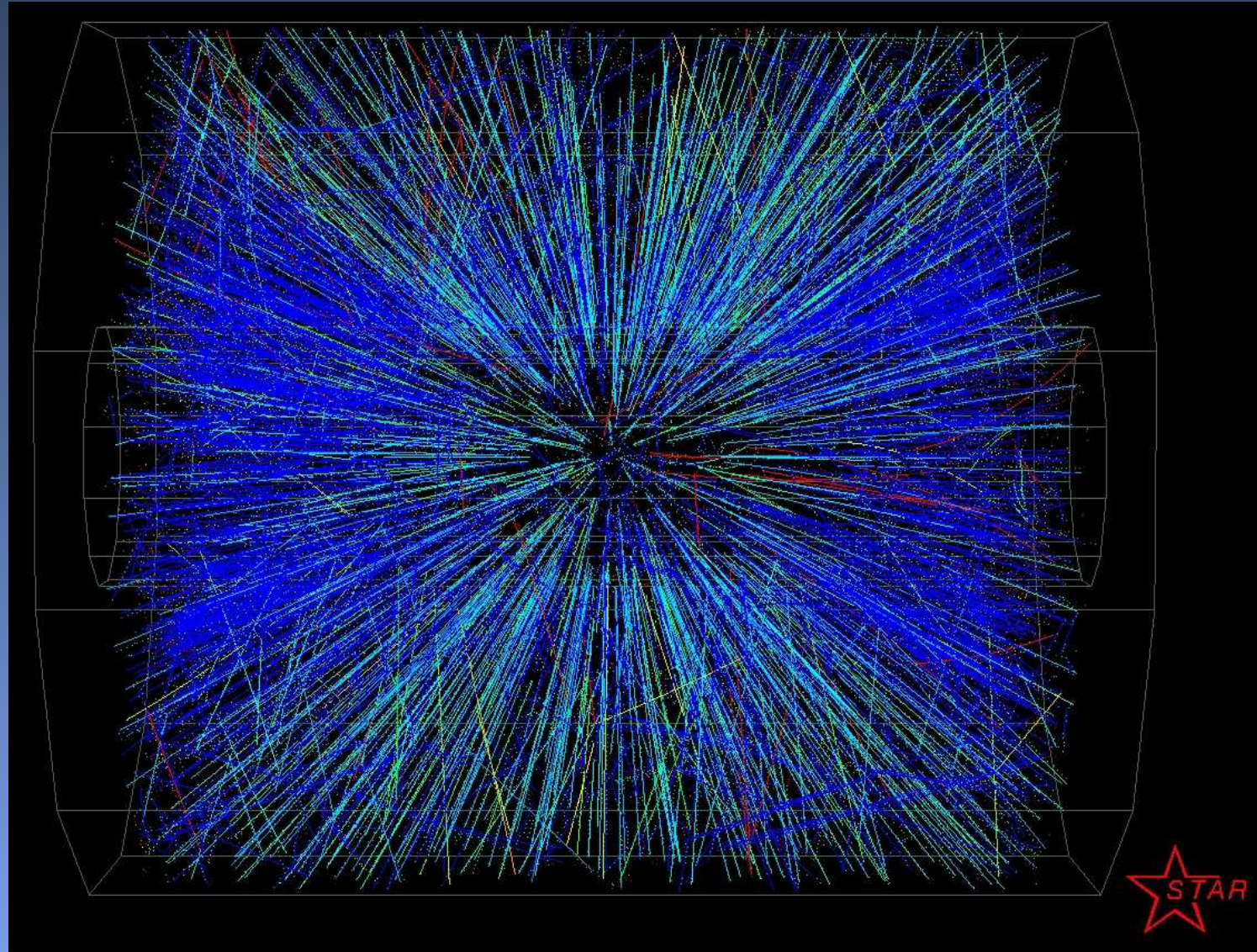
Bragg curves of heavy ions for medical applications

Kraft 1996

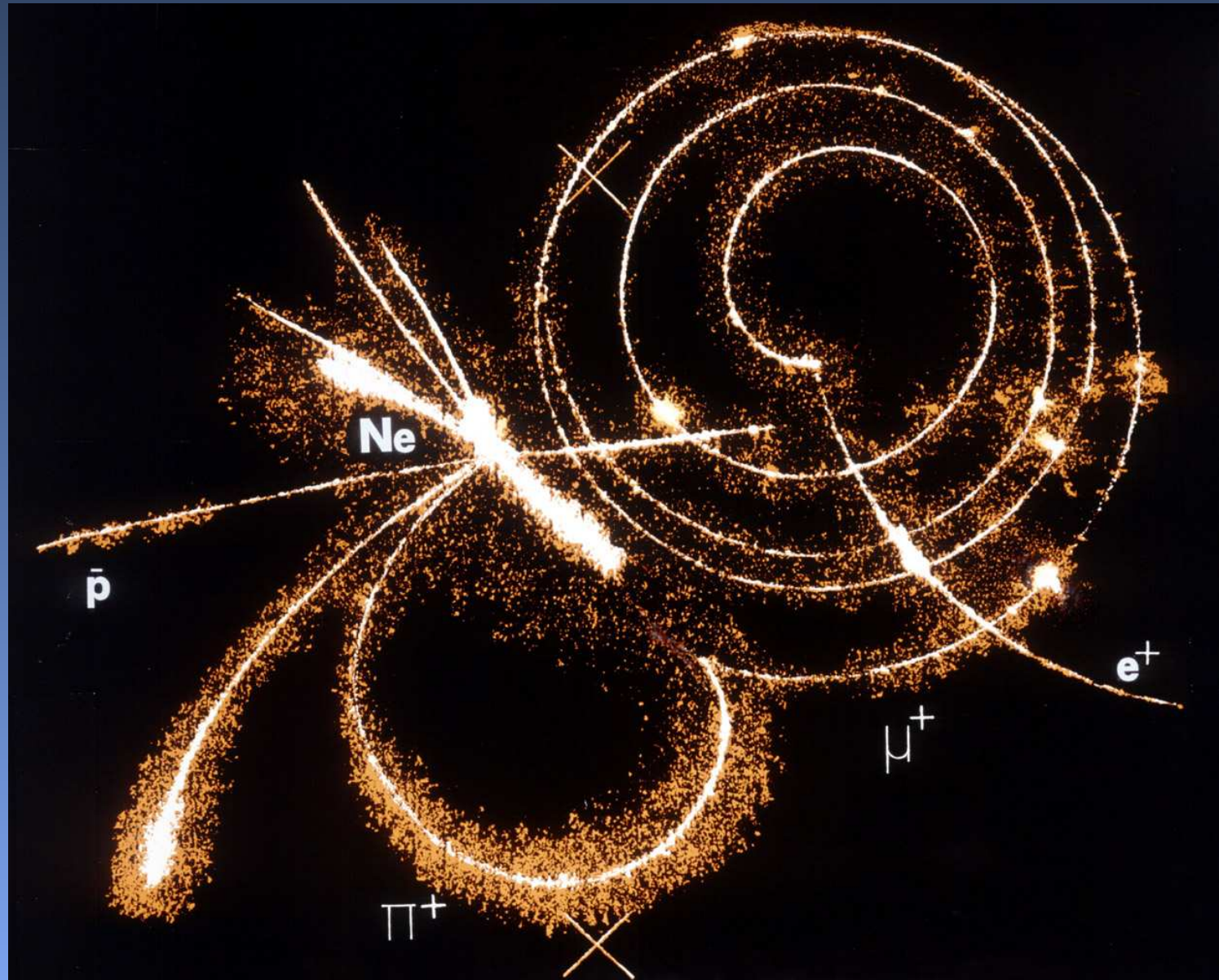
GSI Darmstadt



Heavy Ion Collision in STAR



$\pi \rightarrow \mu \rightarrow e$ decay chain



Landau Distributions (1)

Energy transfer probability: $\phi(\varepsilon) = \underbrace{\frac{2\pi N e^4}{m_e v^2}}_{\xi/x} \cdot \frac{Z}{A} \cdot \frac{1}{\varepsilon^2}$ for $z = 1$

with x : area density in g/cm^2 ($x = \text{density} \times \text{length}$).

For 1 cm Ar and $\beta = 1 \Rightarrow \xi = 0.123 \text{ keV}$.

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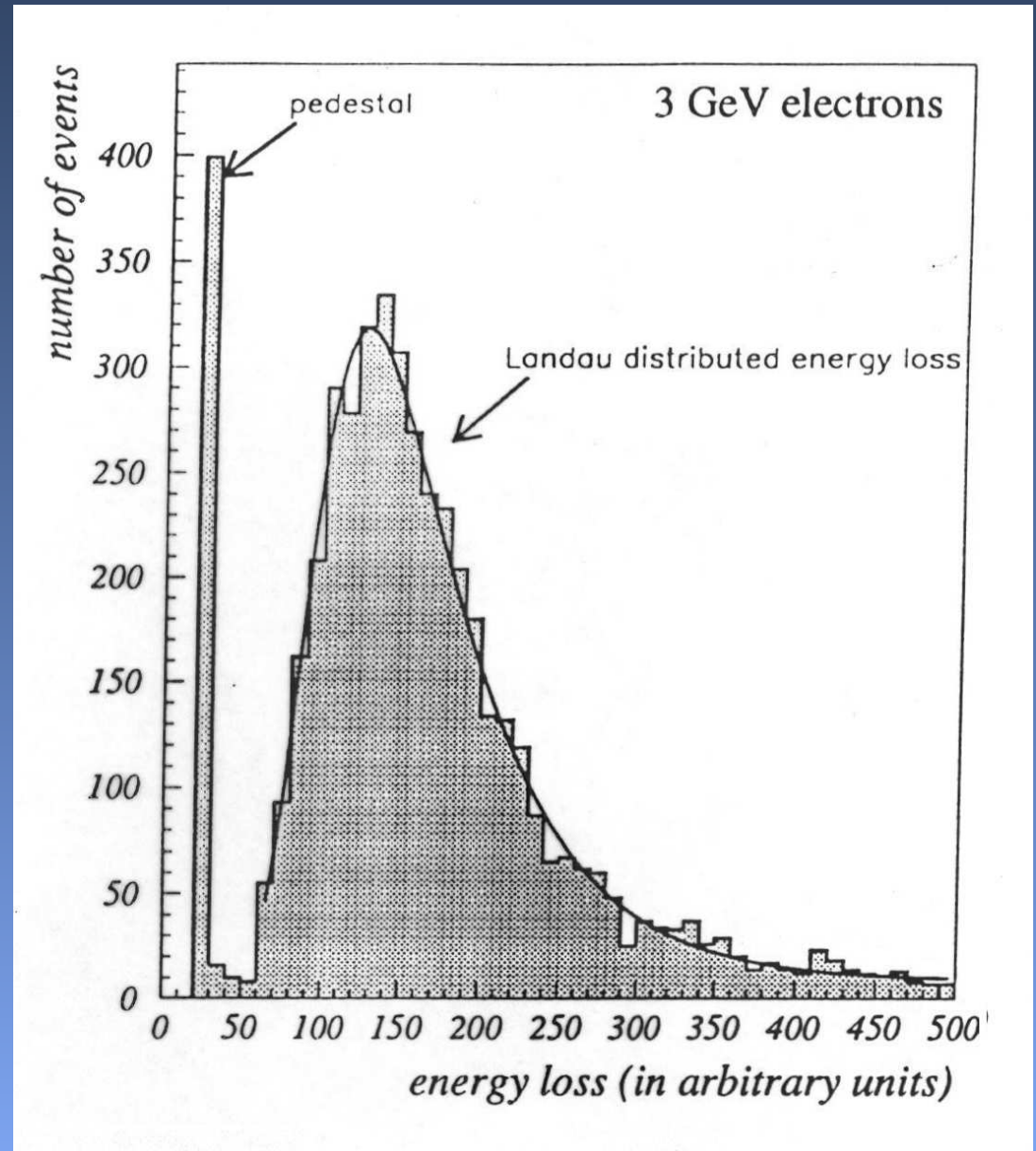
- This distribution is asymmetric due to close collisions with high energy transfers.
- Particularly important for gases and thin absorbers.
- In argon ($\beta\gamma = 4$); $\Delta^{\text{m.p.}} = 1.2 \text{ keV}/\text{cm}$; $\langle \Delta \rangle = 2.69 \text{ keV}/\text{cm}$.

Landau Distributions (2)

Electrons in Ar/CH₄
(80 : 20), gap: 0.5 cm

Affholderbach
et al. 1996

NIM A 410 (1998) 166

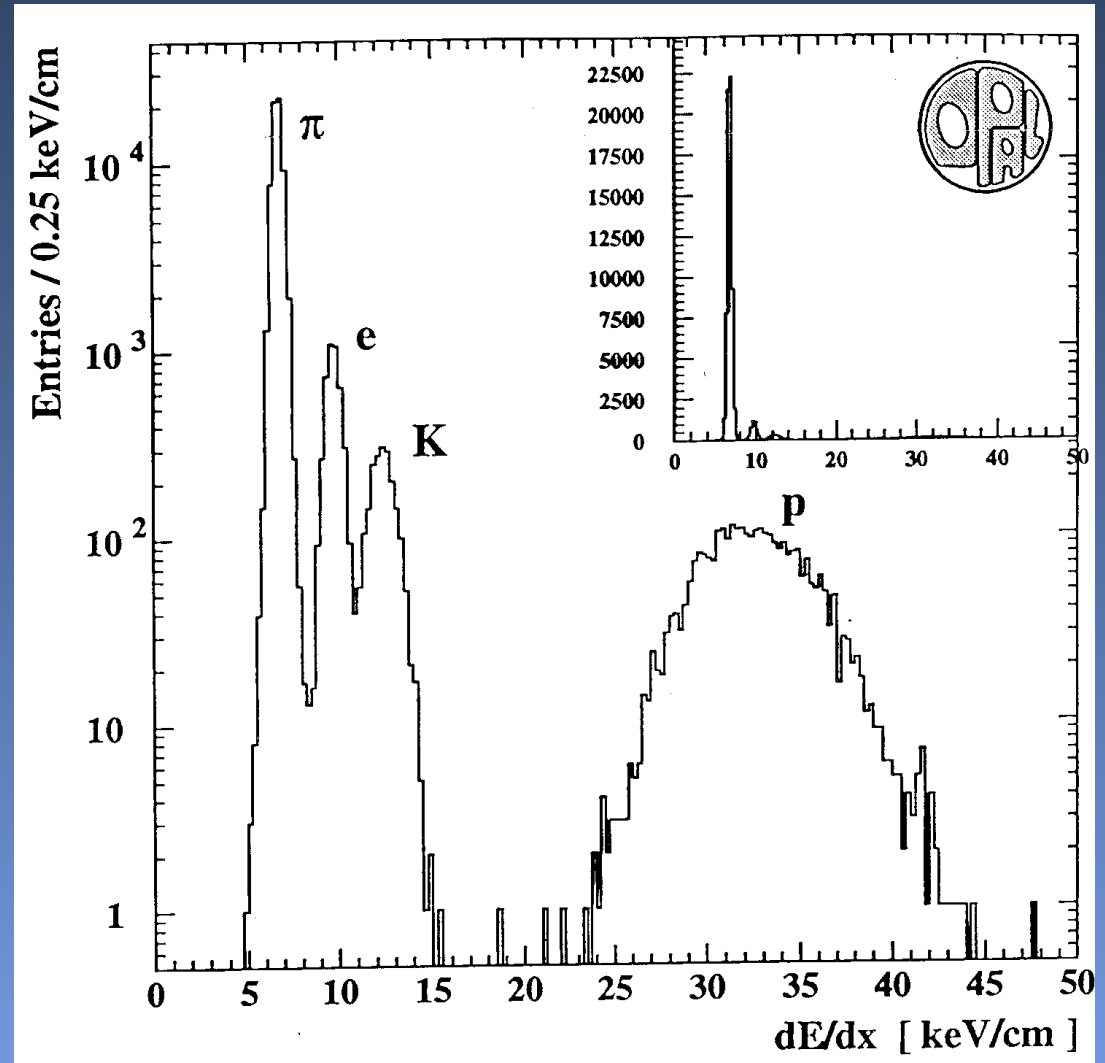


Landau Distributions (3)

OPAL detector at
LEP/CERN

Momentum:
 $\langle p \rangle = 0.465 \text{ GeV}/c$

CERN-PPE 94-49



Channeling (1)

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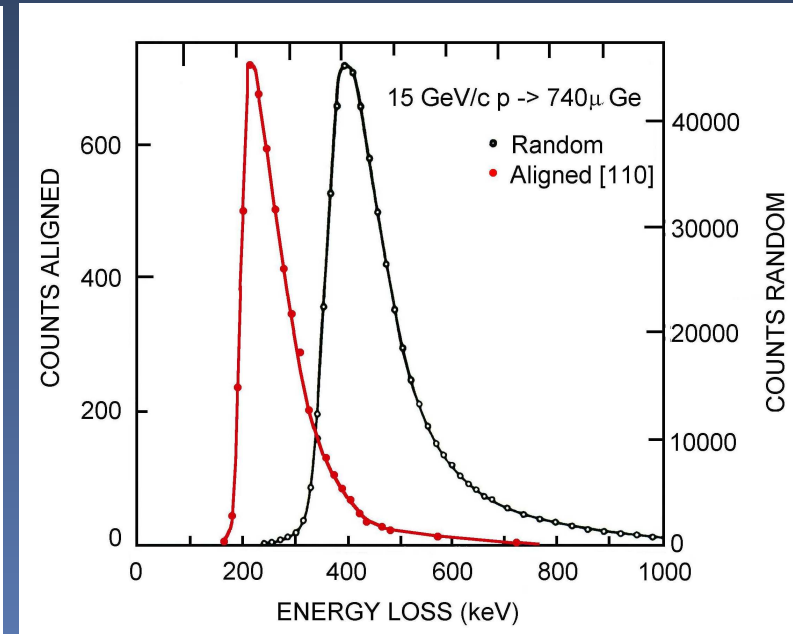
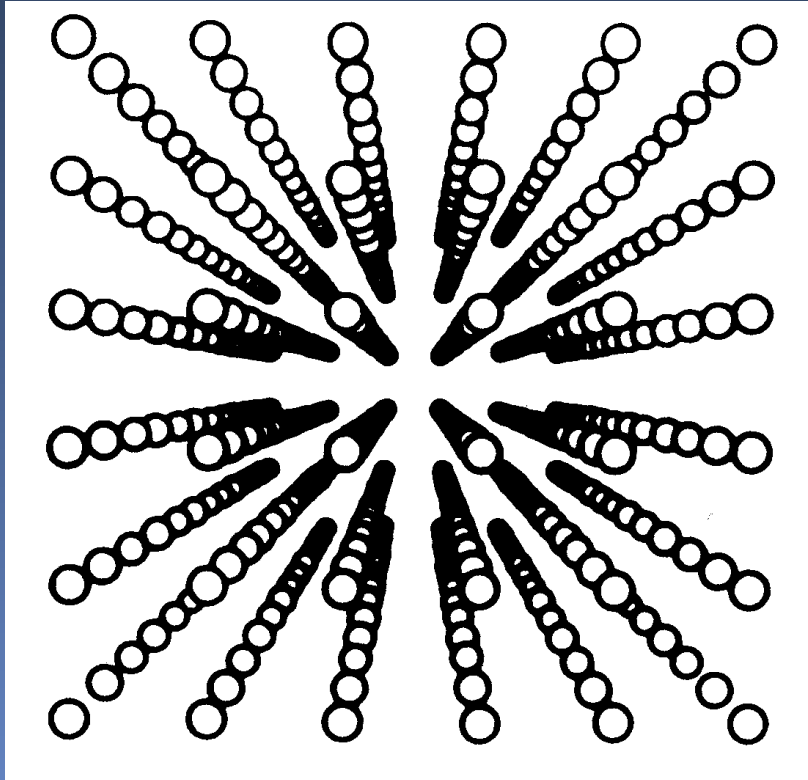
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- Application: beam steering with bent crystals.

Channeling (2)



S. P. Möller CERN 94-05
(1994)

Scintillation

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Effect of the lattice, electron-hole pair creation, excitation, de-excitation at activator centers.
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*: C₂₄H₁₆N₂O₂: 1.4-Bis-(2-[5-phenyloxa-zolile])-benzene

#: C₂₇H₁₉NO: 2.5-di(4-biphenyl)-oxazole

+: C₅H₈O₂: PMMA-polymethylmethacrylate

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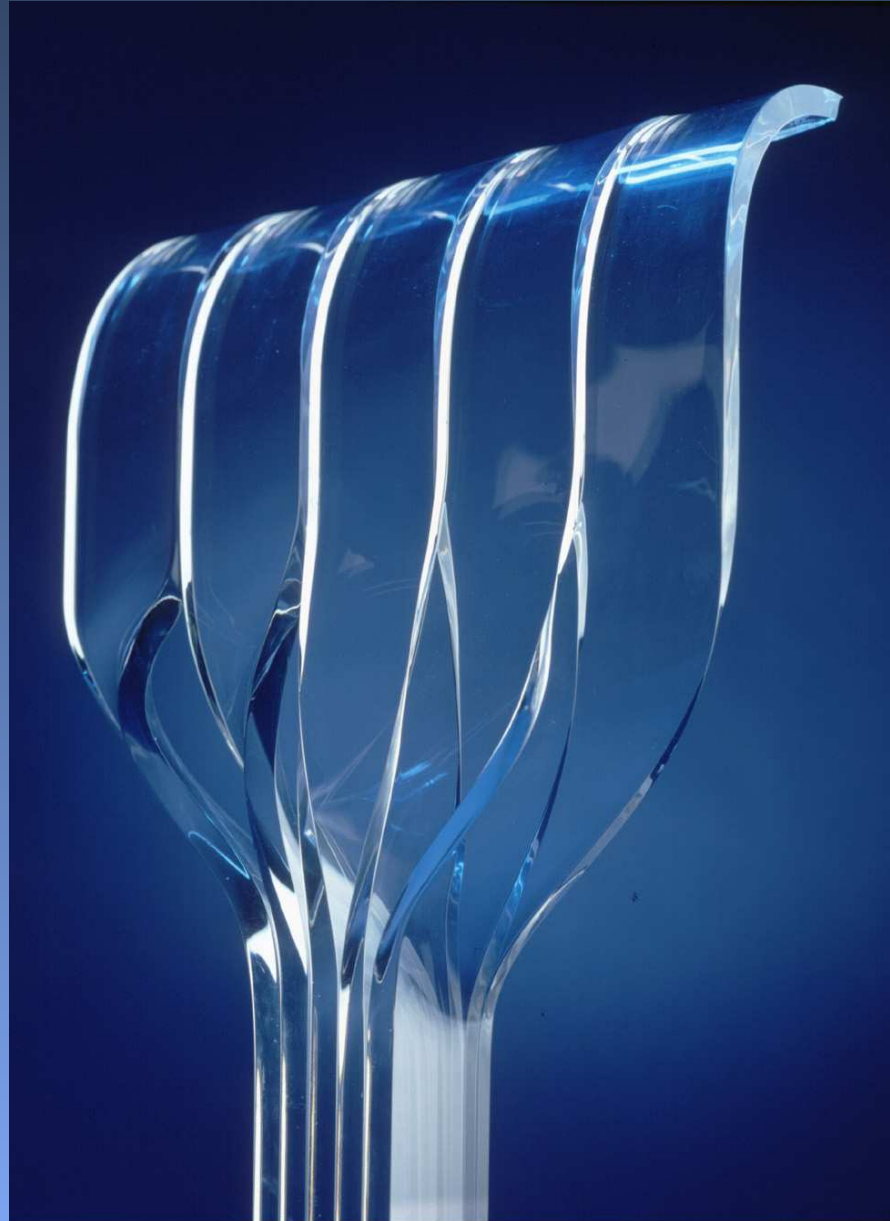
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- Anti-correlation between ionisation and excitation (scintillation).

Adiabatic Light Guide



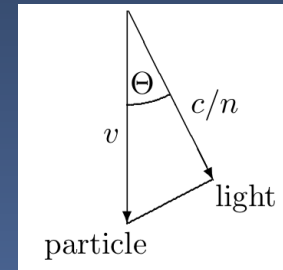
Cherenkov Radiation

Velocity of the particle: v .

Velocity of light in a medium of refractive index n :
 c/n .

threshold condition:

$$v_{\text{thresh}} \geq c/n \Rightarrow \beta_{\text{thresh}} = \frac{v_{\text{thresh}}}{c} \geq \frac{1}{n}.$$

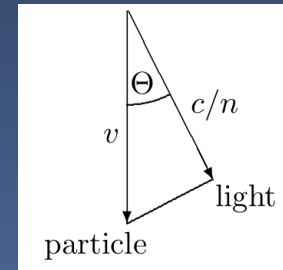


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- $\cos \Theta_C = \frac{1}{n\beta},$

- $\beta = 1 : \Theta_C^{\text{max}} = \arccos \frac{1}{n} = 42^\circ \text{ in water},$

- $E_{\text{thresh}} = \gamma_{\text{thresh}} \cdot m_0 c^2; \quad \gamma_{\text{thresh}} = \frac{1}{\sqrt{1-\beta_{\text{thresh}}^2}} = \frac{n}{\sqrt{n^2-1}}.$

- number of Cherenkov photons per unit path length:

$$\frac{dN}{dx} = 2\pi\alpha z^2 \cdot \int \left(1 - \frac{1}{n^2\beta^2}\right) \frac{d\lambda}{\lambda^2} = 2\pi\alpha z^2 \frac{\lambda_1 - \lambda_2}{\lambda_1 \lambda_2 02} \sin^2 \Theta_C$$

$$= 490 z^2 \sin^2 \Theta_C \text{ [cm}^{-1}\text{]}$$

$$\approx 210 \text{ cm}^{-1} \text{ in water for } z = 1 \text{ and } \beta = 1$$

Cherenkov Counters

- Threshold Cherenkov counter

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- DIRC: Detection of Internally Reflected Cherenkov light

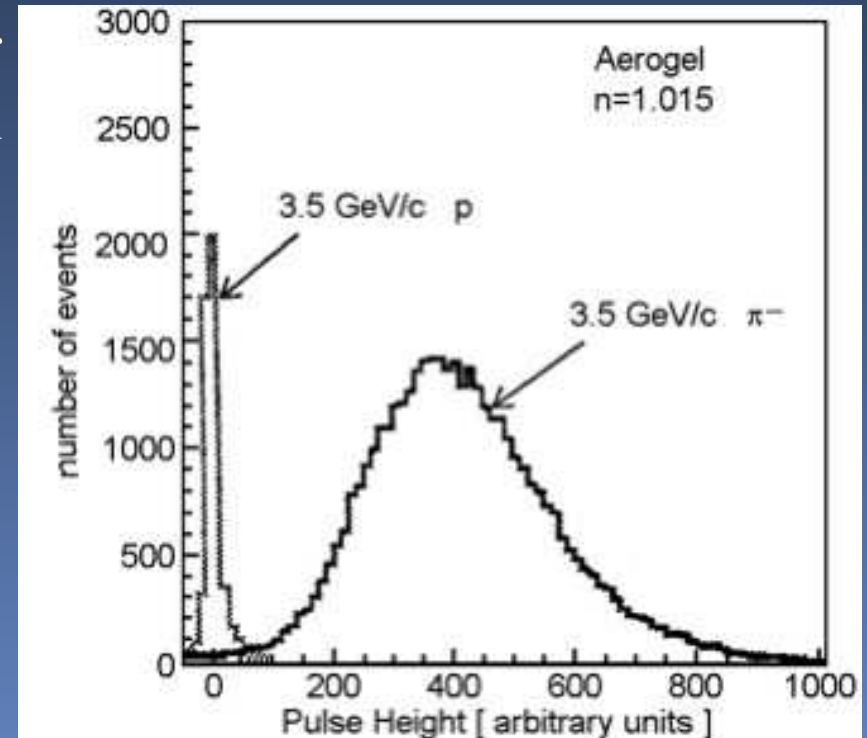
Cherenkov Counters

- Threshold Cherenkov counter
- DIRC: Detection of Internally Reflected Cherenkov light
- RICH - Ring Imaging Cherenkov Counter

Threshold *Cherenkov* counter

Pulse height distribution for 3.5 GeV/ c pions and protons in an aerogel Cherenkov counter.

BELLE Collaboration
hep-ex/9903045 (1999)

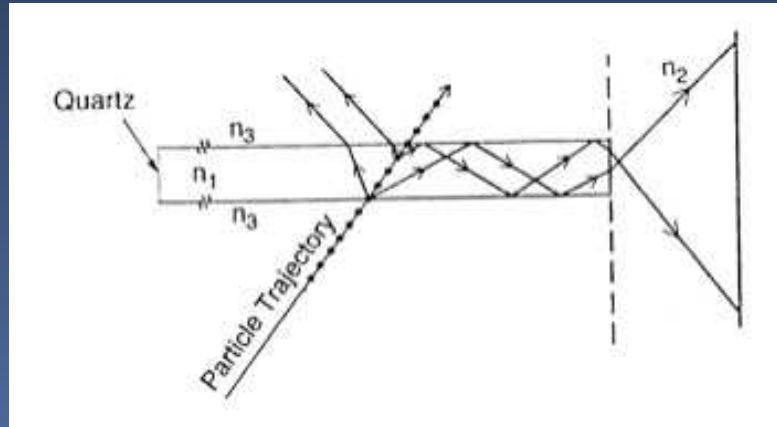


$$\gamma_{\text{thresh}} = \frac{n}{\sqrt{n^2 - 1}} = 5.84 \text{ for aerogel of } n = 1.015$$

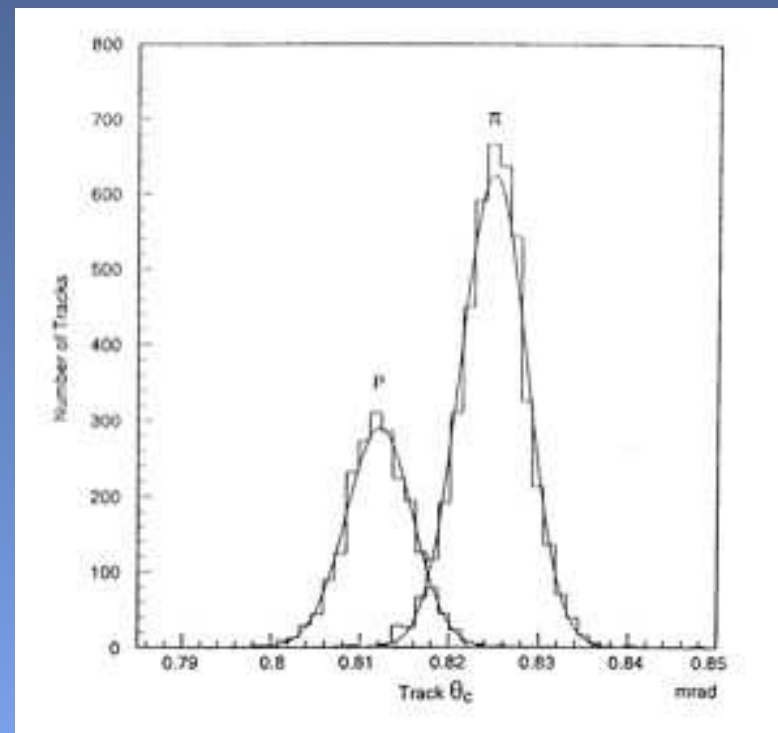
$$p = 3.5 \text{ GeV}/c = \begin{cases} E_{\pi} = 3.50 \text{ GeV}; & \gamma_{\pi} = 25.1 \\ E_p = 3.63 \text{ GeV}; & \gamma_p = 3.86 \end{cases}$$

$$\gamma_{\pi} > \gamma_{\text{thres}}; \quad \gamma_p < \gamma_{\text{thres}}.$$

DIRC



DIRC-counter
5.4 GeV/c
I. Adam et al. 1997

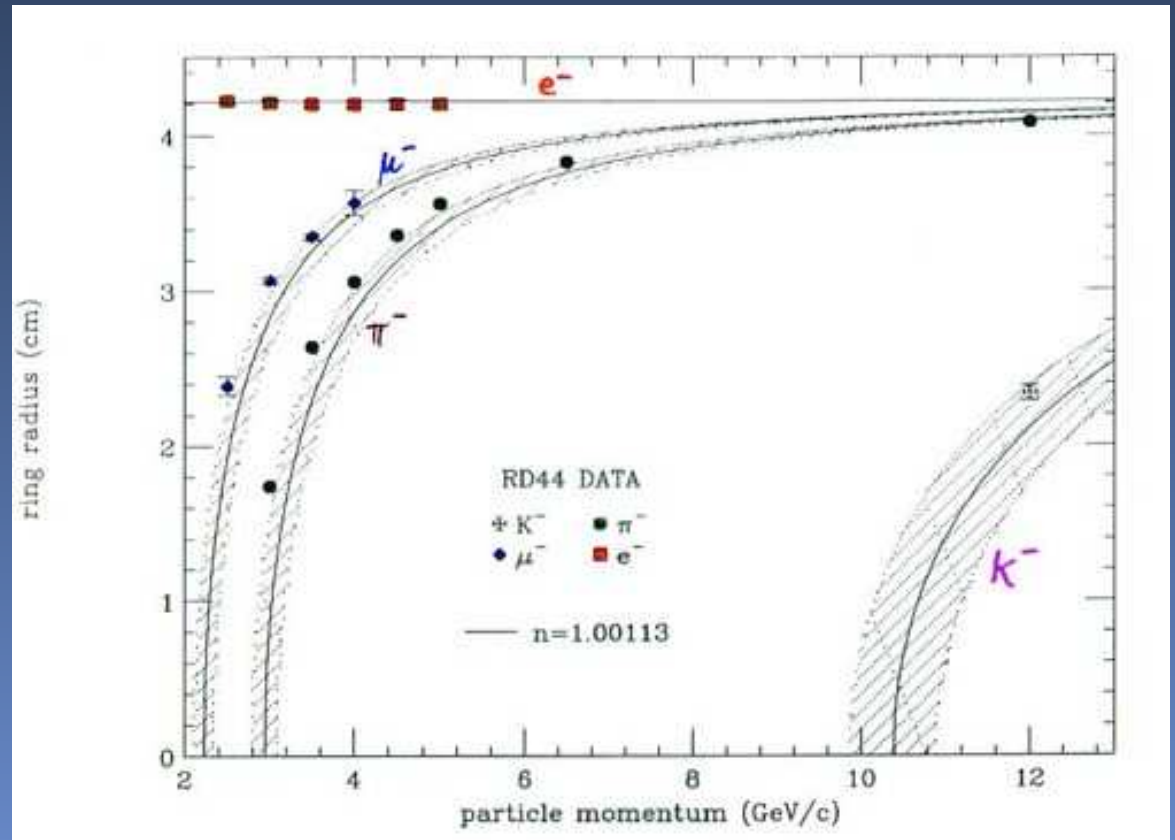


RICH (1)

RICH

Ar + C₄F₁₀ = 25/75
100 channel PMT
10 × 10 cm²

R. Debbe et al.
hep-ex/9503006

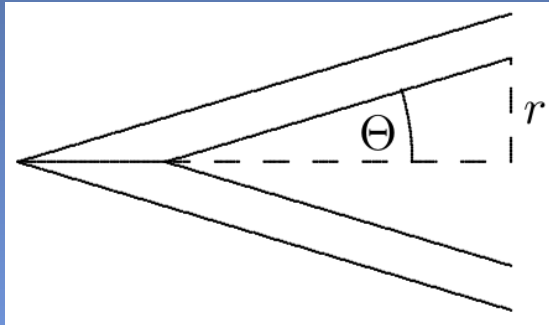


RICH (2)

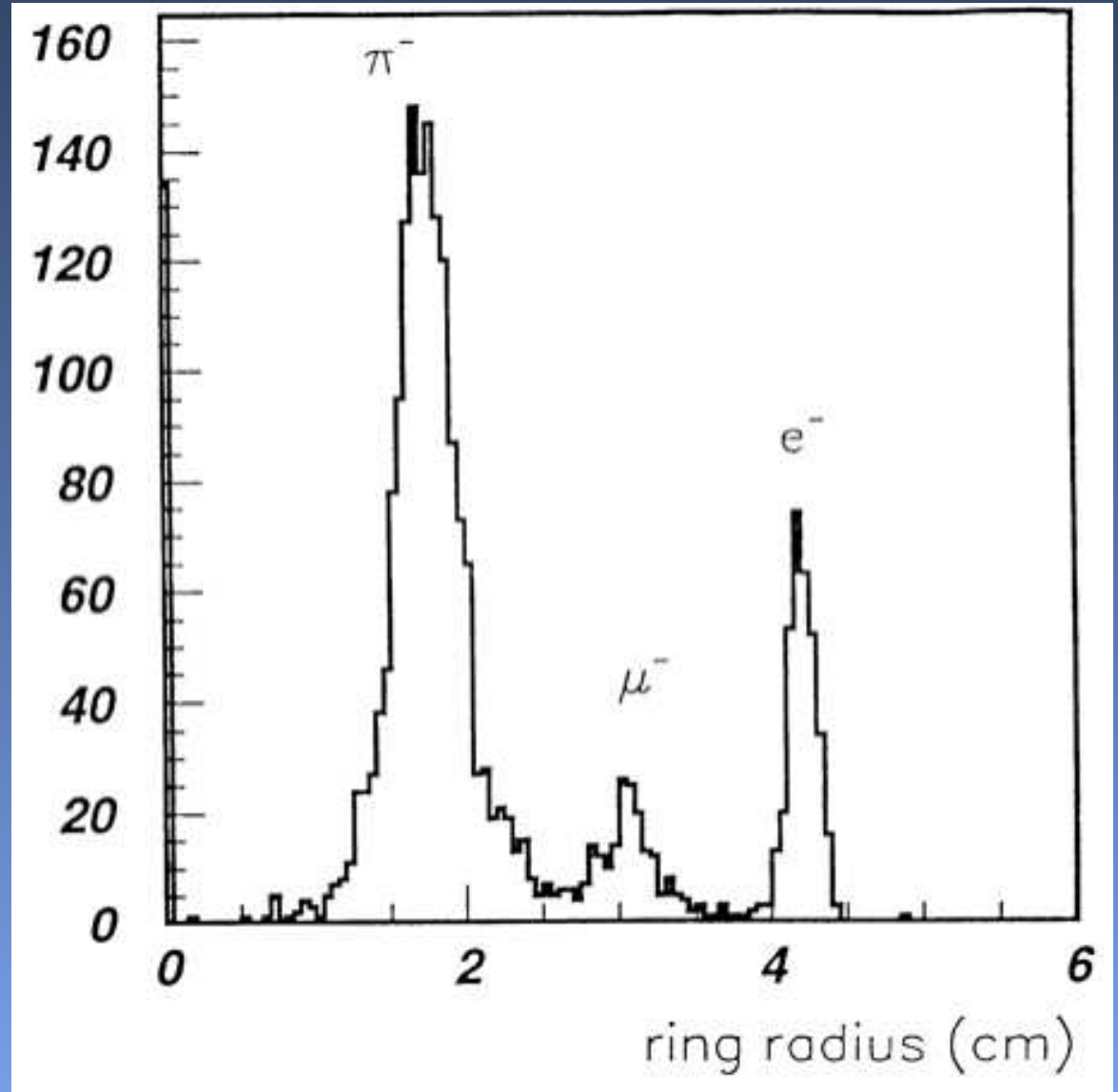
RICH

Ar + C₄F₁₀ = 25/75
100 channel PMT
10 × 10 cm²
3 GeV/c

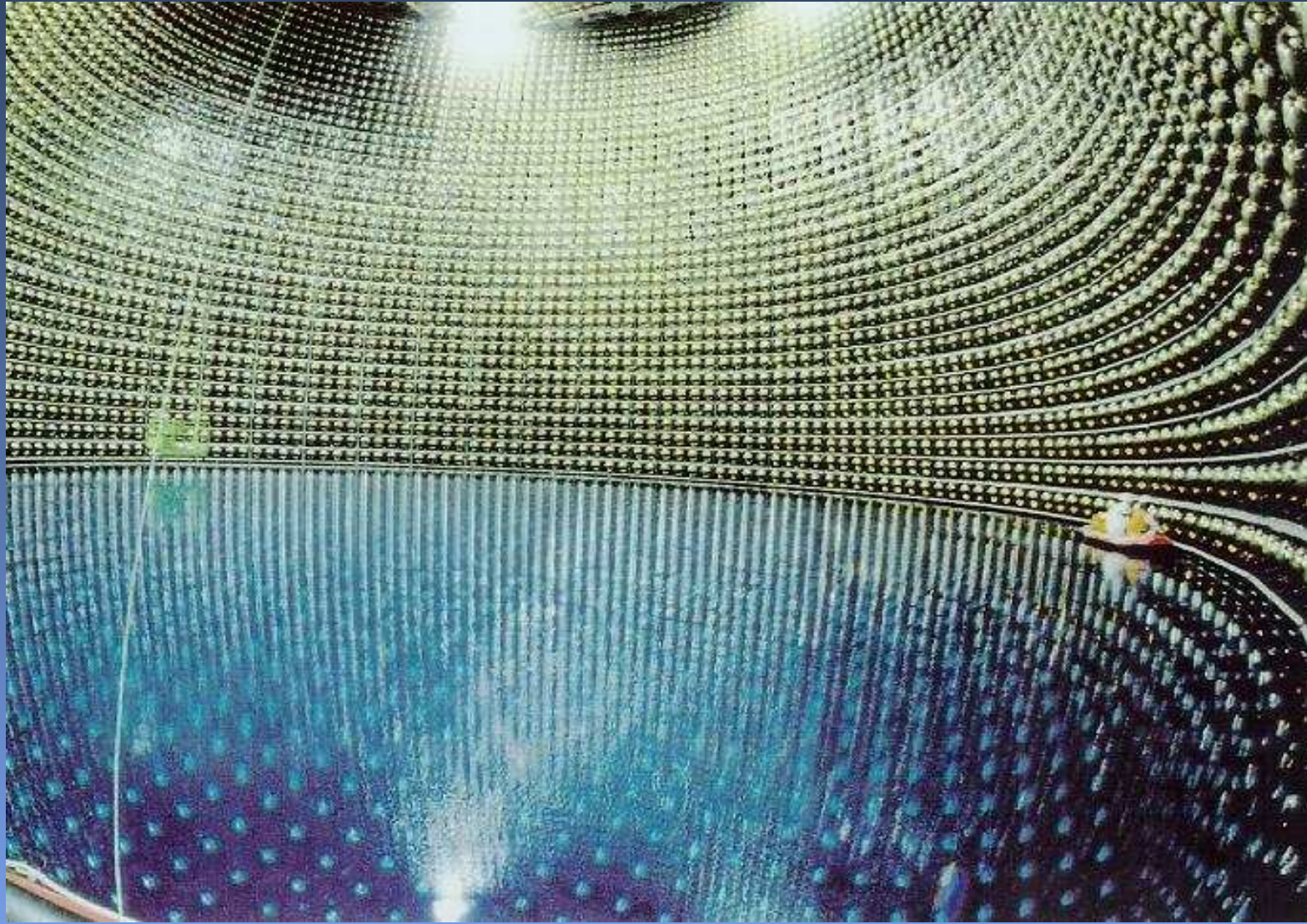
R. Debbe et al.
hep-ex/9503006



$$r \sim \sin \Theta$$



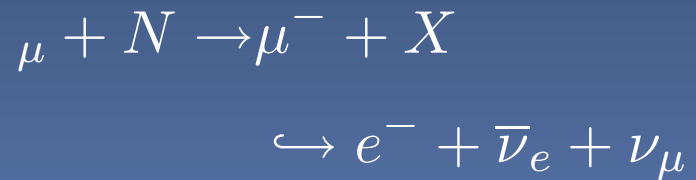
Super-Kamiokande



Filling the water Cherenkov counter.

Super-Kamiokande

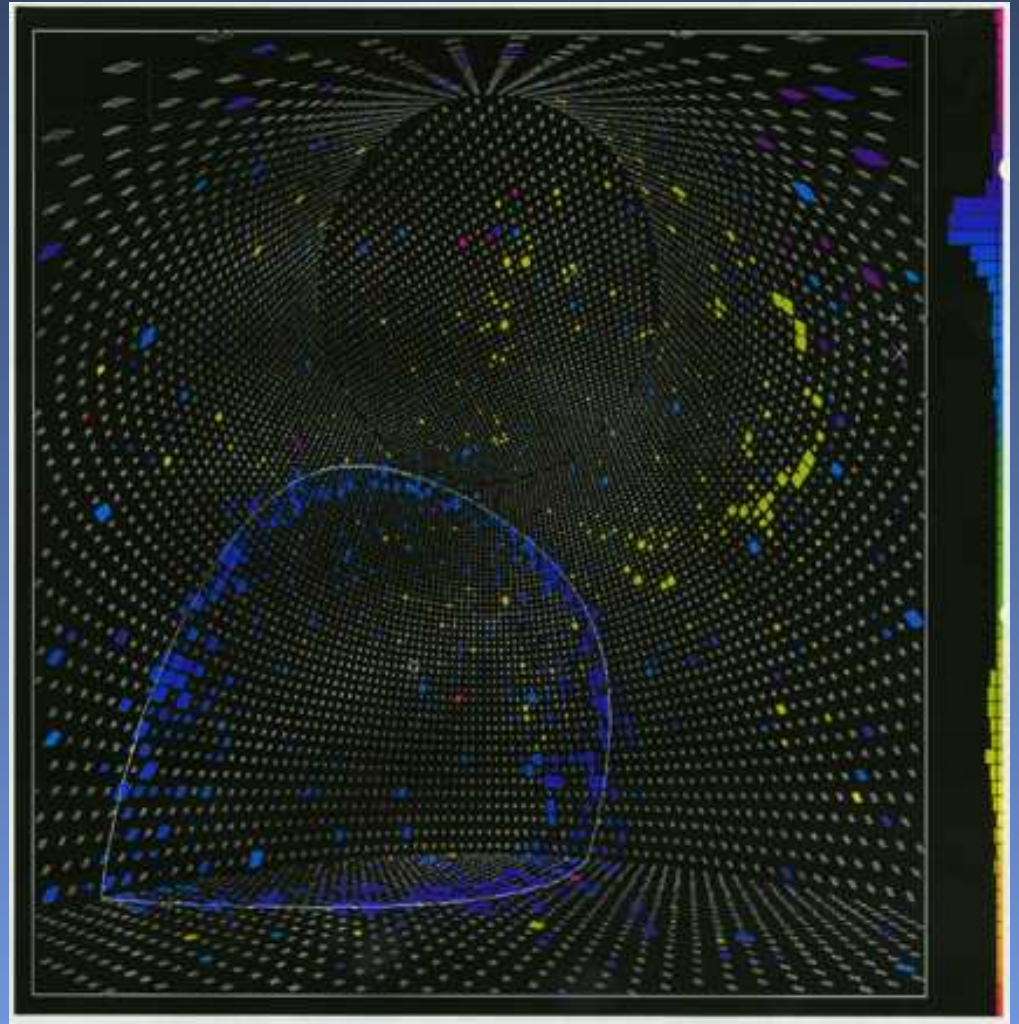
Event with a stopping muon.



$$E_{\nu_\mu} = 481 \text{ MeV}$$

$$E_\mu = 394 \text{ MeV}$$

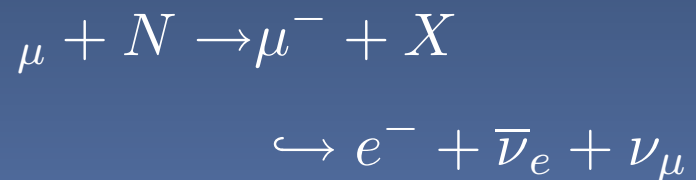
$$E_e = 52 \text{ MeV}$$



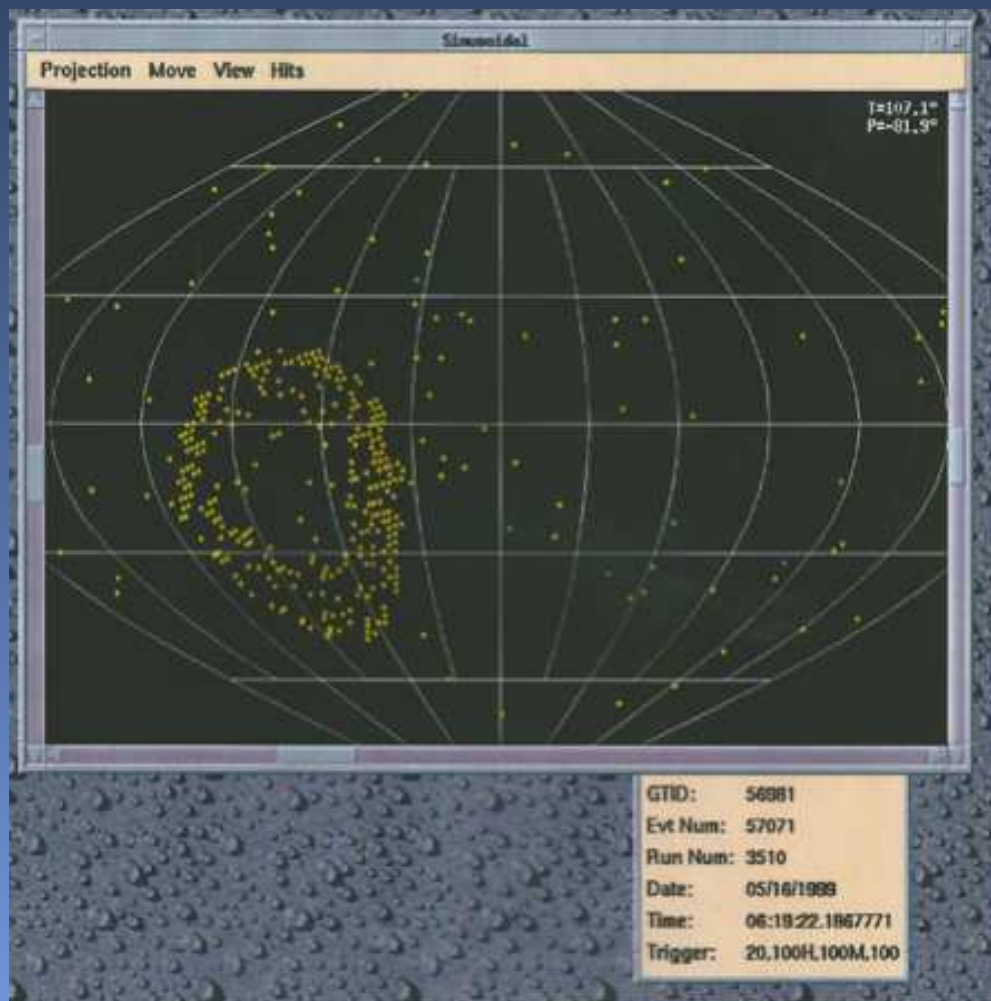
Superkamiokande Photo Gallery

SNO -Sudbury Neutrino Observatory (1)

Event with a stopping muon.

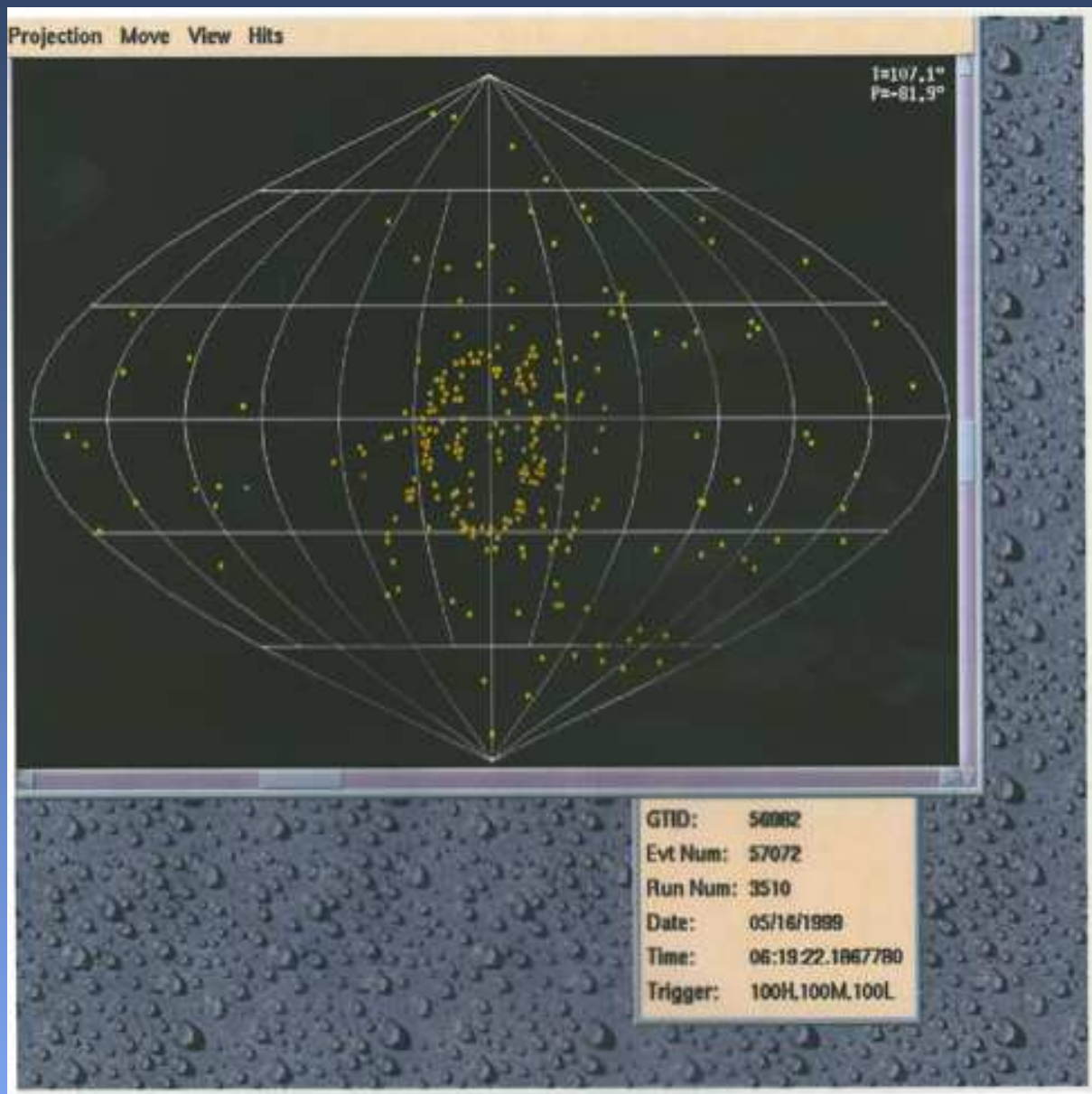


two frames taken at
 $\Delta t = 0.9 \mu s$
time difference



SNO Photo Gallery

SNO -Sudbury Neutrino Observatory (2)



Transition Radiation

Energy radiated from a single boundary:

$$S = \frac{1}{3} \alpha z^2 \hbar \omega_p \gamma \propto \gamma$$

with $\hbar \omega_P$: plasma energy,

$\hbar \omega_P \approx 20 \text{ eV}$ for plastic radiators.

Typical emission angle: $\Theta = \frac{1}{\gamma}$,

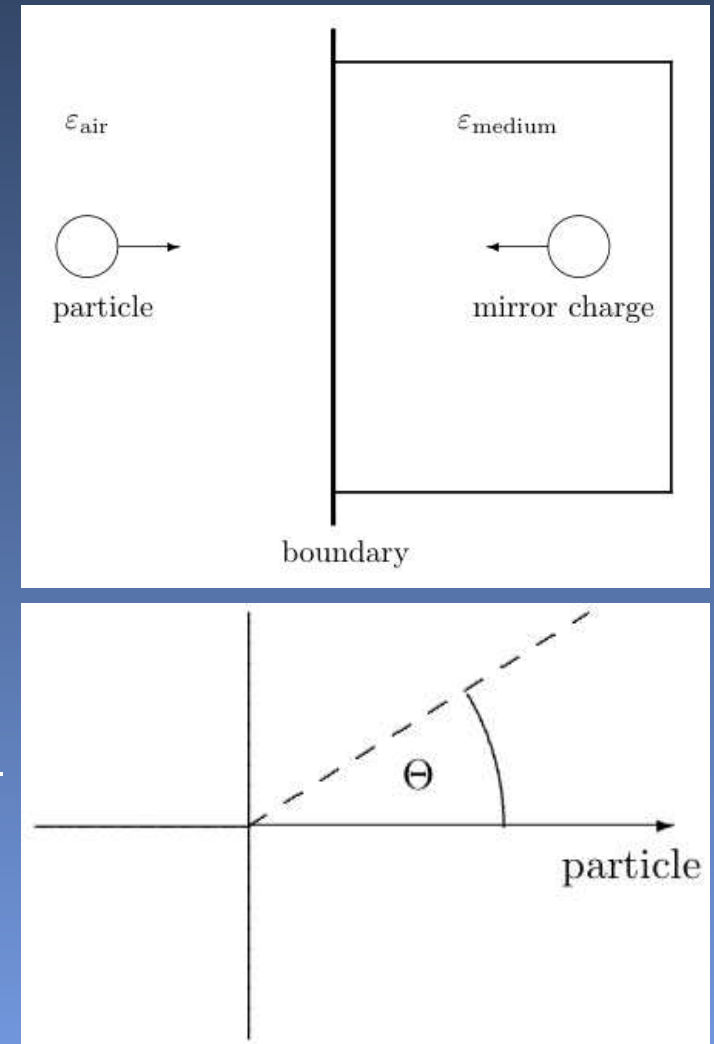
energy of radiated photons $\sim \gamma$,

\rightsquigarrow number of radiated photons: αz^2 .

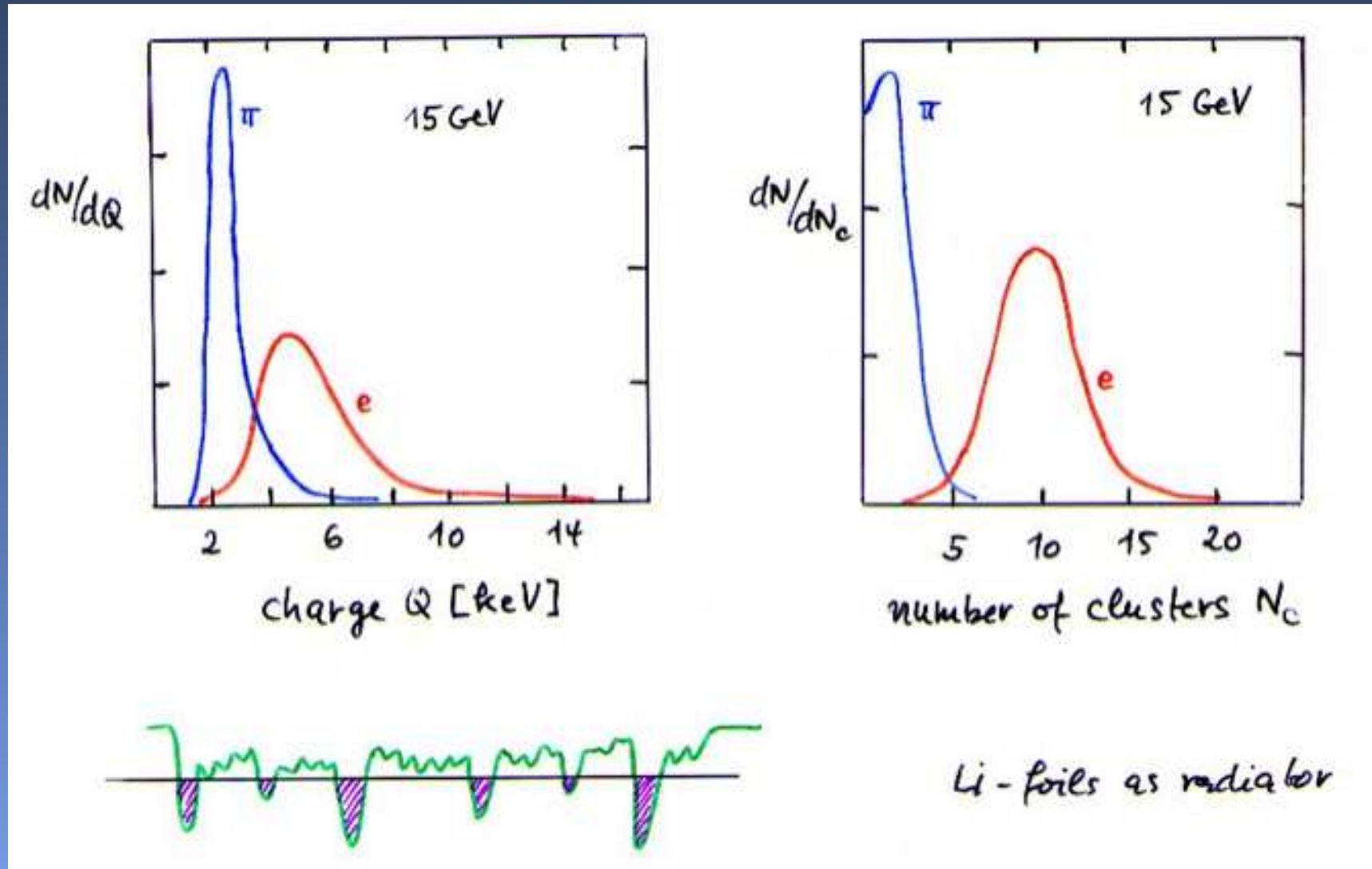
Effective threshold: $\gamma \approx 1000$.

Use stacked assemblies of low Z - material with many transitions.

Detector with high Z gas.

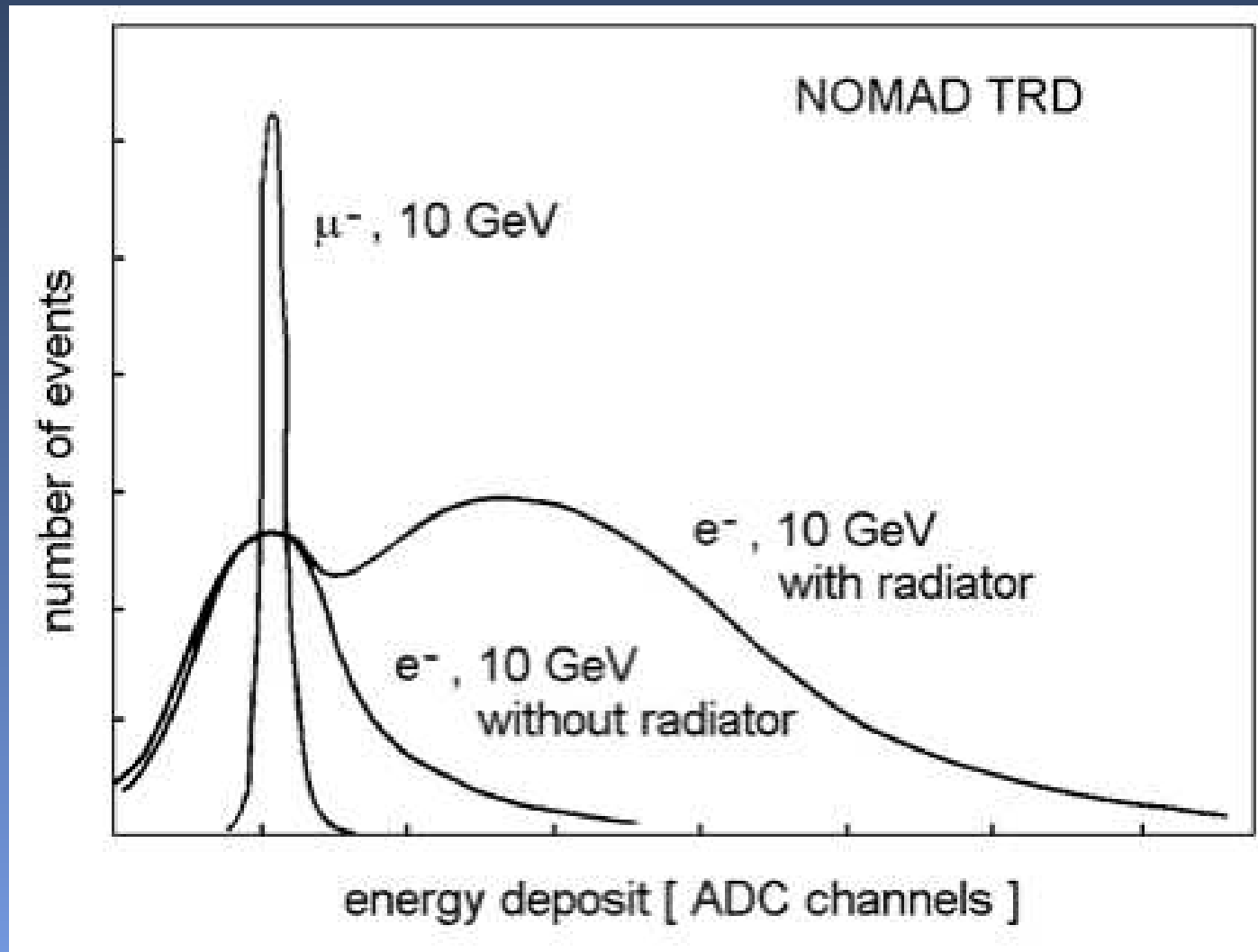


Li-foils as radiator



Fabjan et al. 1980

NOMAD TRD



NOMAD TRD, G. Bassompierre et al., NIM A 403 (1998) 363

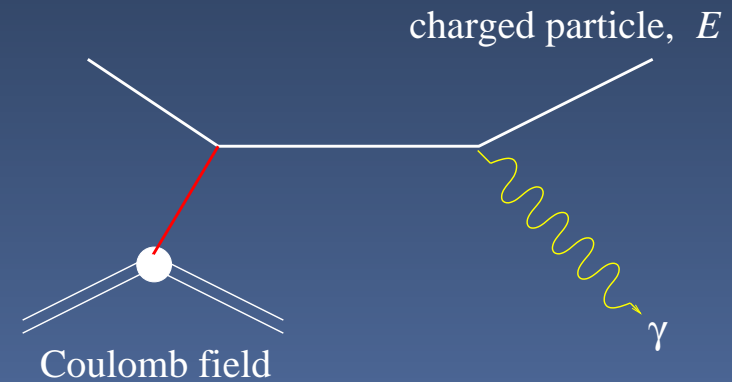
test beam performance: e/μ -separation at 10 GeV

Bremsstrahlung (1)

$$\frac{dE}{dx} = 4\alpha N \frac{Z^2}{A} z^2 r^2 E \ln \frac{183}{Z^{1/3}} \text{ with:}$$

- N : Avogadro number,
- A, Z : target, z : particle,
- $r_e = \frac{e^2}{m_0 c^2}$.

$$\frac{dE}{dx} = \frac{E}{X_0} \Rightarrow \text{radiation length: } X_0^{-1} = 4\alpha r^2 \frac{N}{A} Z^2 \ln \frac{183}{Z^{1/3}}$$



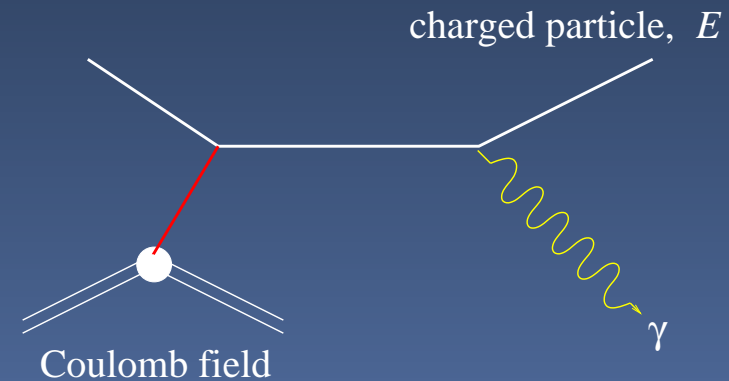
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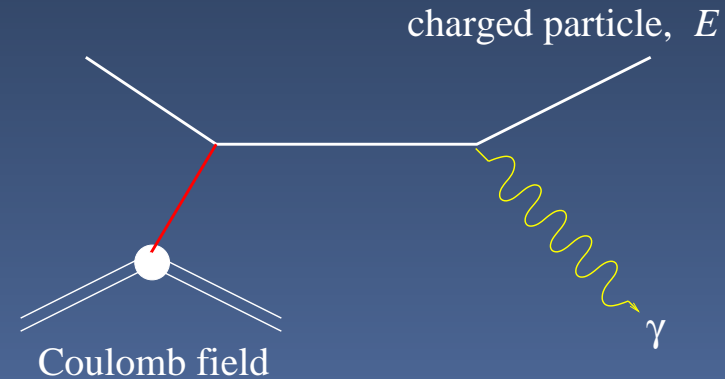
$$\text{Fit to data: } X_0 = \frac{716.4A}{Z(Z+1) \ln(287/\sqrt{Z})} [\text{g/cm}^2] \text{ for electrons}$$



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Usual definition for the critical energy E_c^e :

$$\left(\frac{dE}{dx}\right)_{\text{ionisation}} = \left(\frac{dE}{dx}\right)_{\text{bremsstrahlung}}$$

$$E_c^e = \begin{cases} \frac{610 \text{ MeV}}{Z+1.24} & \text{for solids and liquids} \\ \frac{710 \text{ MeV}}{Z+0.92} & \text{for gases} \end{cases}$$

Bremsstrahlung (2)

material	$X_0[\text{g}/\text{cm}^2]$	$X_0[\text{cm}]$	$E_c[\text{MeV}]$
air	37	30000	84
iron	13.9	1.76	22
lead	6.4	0.56	7.3

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Since $-\frac{dE}{dx} \propto r^2 \propto \frac{1}{m^2}$ electron *bremsstrahlung* dominates, but also other particles radiate, especially at high energies:

$$E_c^\mu = E_c^e \cdot \left(\frac{m_\mu}{m_e}\right)^2 = 960 \text{ GeV.}$$

↪ muon calorimetry at TeV energies

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Since $-\frac{dE}{dx} \propto r^2 \propto \frac{1}{m^2}$ electron *bremsstrahlung* dominates, but also other particles radiate, especially at high energies:

$$E_c^\mu = E_c^e \cdot \left(\frac{m_\mu}{m_e}\right)^2 = 960 \text{ GeV.}$$

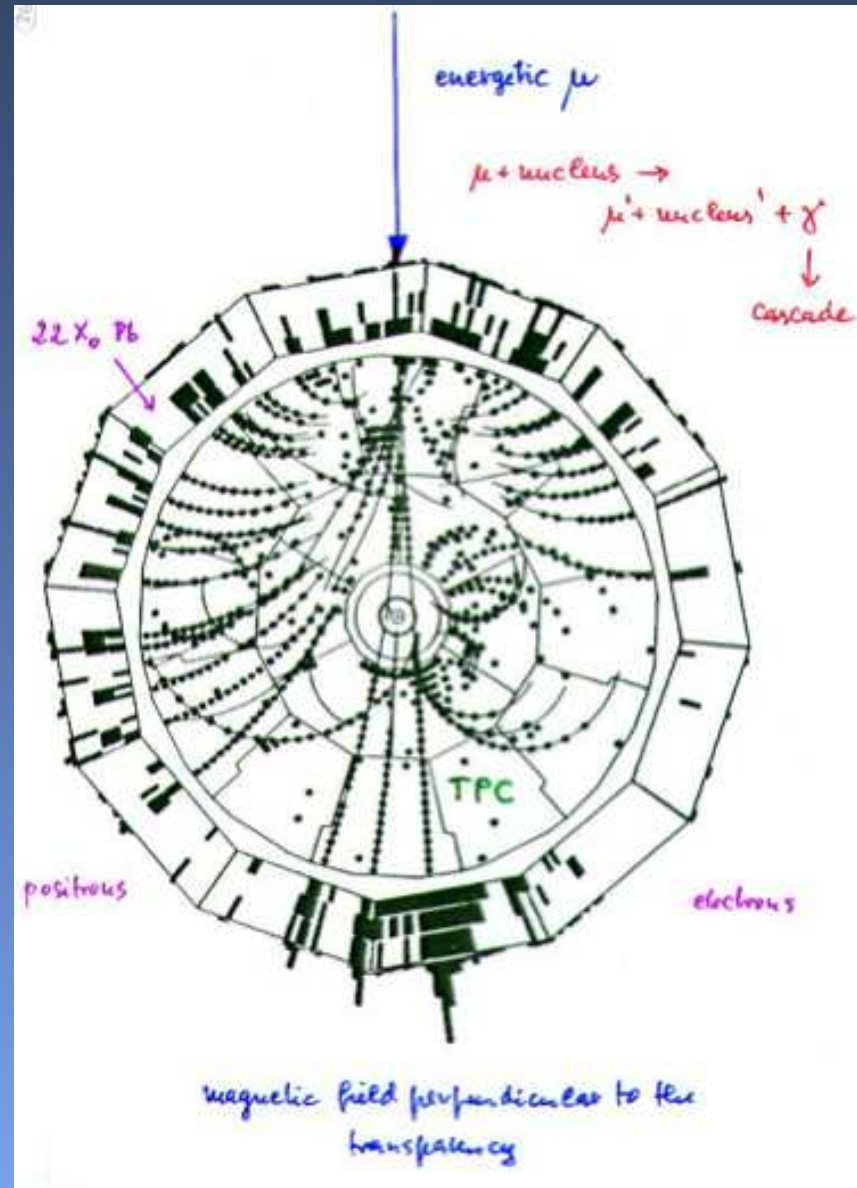
↪ muon calorimetry at TeV energies

Bremsstrahlung is important for electromagnetic cascades.

Bremsstrahlung (3)

C. Grupen
ALEPH

Magnetic field
perpendicular to
the transparency.



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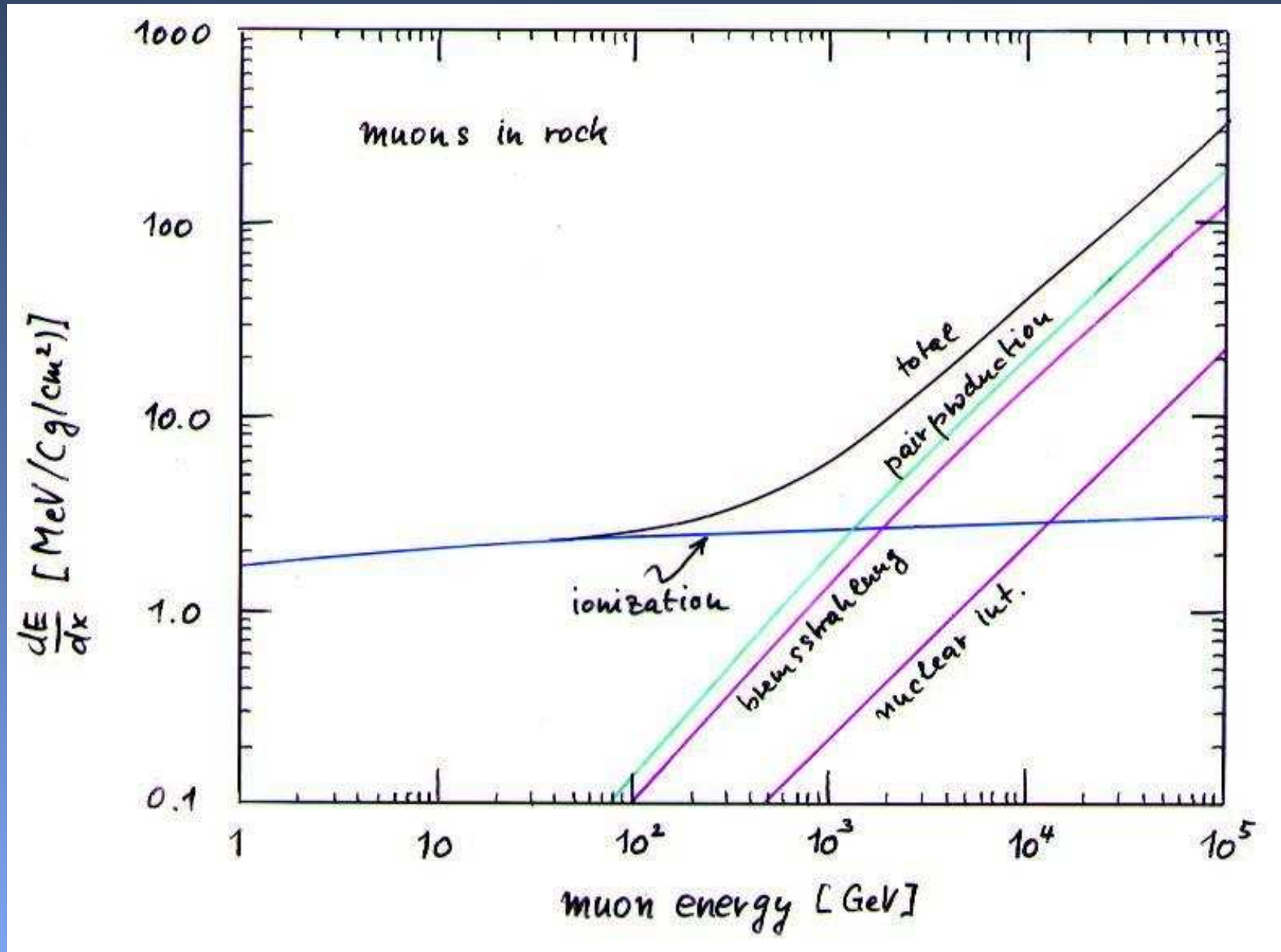
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Range of muons:

$$R = \int_E^0 \frac{dE}{-dE/dx} = \frac{1}{b} \ln \left(1 + \frac{b}{a} E \right) \begin{cases} 140 \text{ m} & \text{rock for } E = 100 \text{ GeV} \\ 800 \text{ m} & \text{rock for } E = 1 \text{ TeV} \\ 2300 \text{ m} & \text{rock for } E = 10 \text{ TeV} \end{cases}$$

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Nuclear interactions

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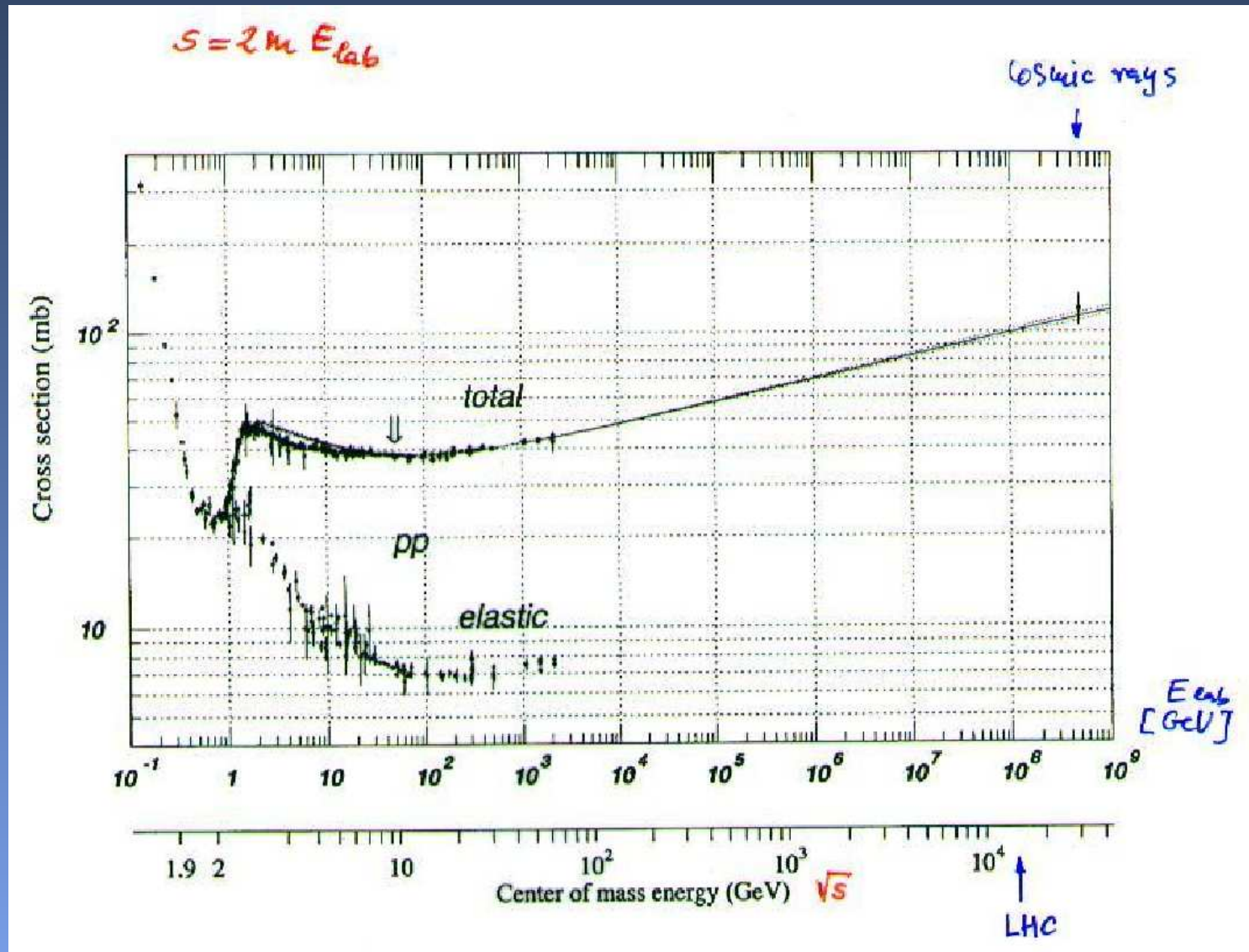
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material	Al	Fe	Pb	air
λ_i/cm	26.2	10.6	10.4	48000
$\lambda_i/(\text{g/cm}^2)$	70.6	82.8	116.2	62.0

for most materials $\lambda_i, \lambda_a > X_0$.

Nuclear interactions



Particle Data Group, Eur. Phys. J. C 15 (2000) 1

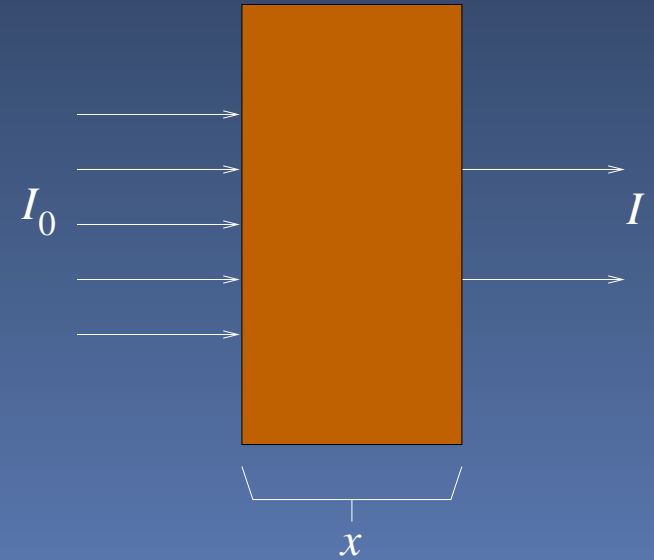
Interactions of Photons (1)

$I = I_0 e^{-\mu x}$ with

$$\mu = \frac{N}{A} \sum_{i=1}^3 \sigma_i$$

(mass attenuation coefficient).

$$\sigma_i = \begin{cases} i = 1 : & \text{photoelectric effect} \\ i = 2 : & \text{Compton scattering} \\ i = 3 : & \text{pair production} \end{cases}$$



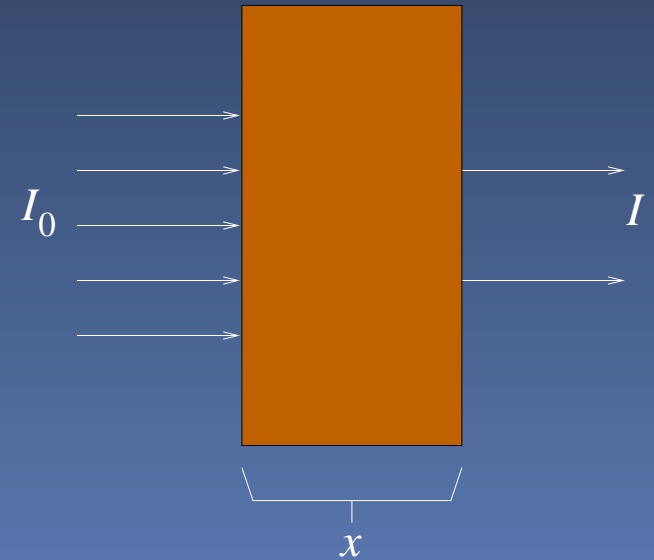
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$\gamma + \text{atom} \rightarrow \text{atom}^+ + e^-$ predominantly in the K-shell.

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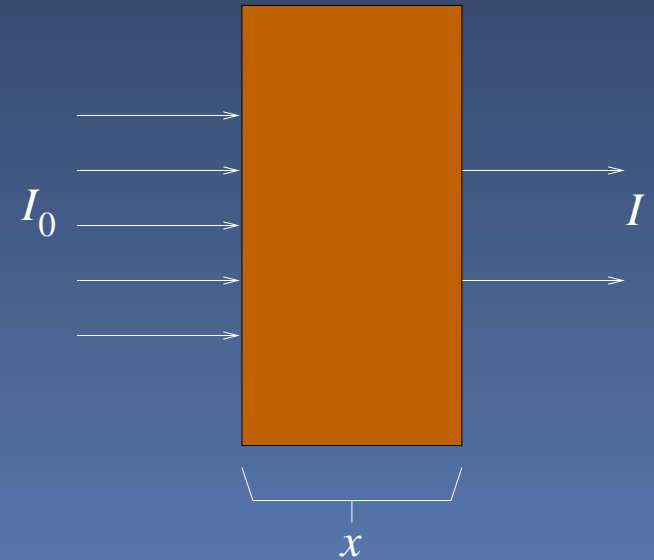
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$$\sigma_{\text{Thomson}} = \frac{8}{3} \pi r_e^2 = 665 \text{ mb.}$$

$$\text{For high energies: } \sigma_{\text{Photo}}^{\text{K}} = 4\pi r_e^2 Z^5 \alpha^4 \cdot \frac{1}{\epsilon}.$$

Interactions of Photons (2)

Compton Scattering:

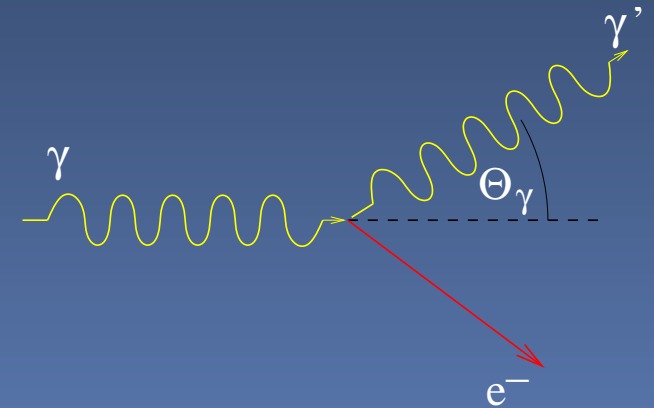
$$\sigma_C \propto \frac{\ln \varepsilon}{\varepsilon} \cdot Z$$

The photon counts the number of electrons in the atom:

$$\frac{E'_\gamma}{E_\gamma} = \frac{1}{1 + \varepsilon(1 - \cos \Theta_\gamma)}.$$

Maximum energy transfer for backscattering ($\Theta_\gamma = \pi$):

$$E_{\max}^{\text{kin}} = \frac{2\varepsilon^2}{1+2\varepsilon} m_e c^2 \xrightarrow{\varepsilon \gg 1} E_\gamma.$$



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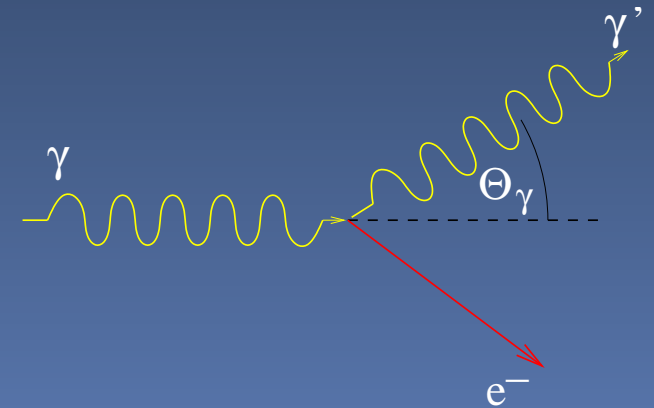
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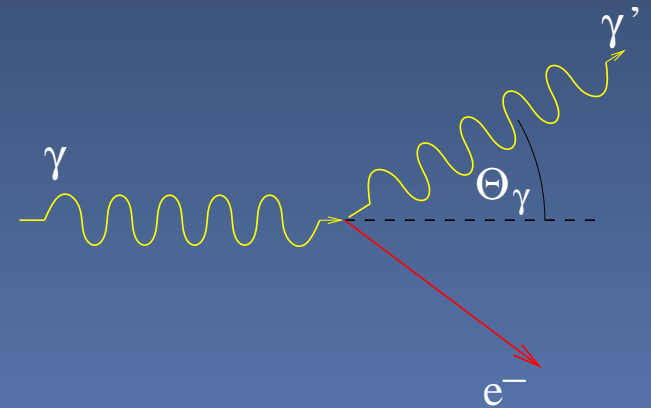
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\Rightarrow Distinction between mass attenuation coefficient (relates to σ_C)

and mass absorption coefficient (relates to σ_{CA})

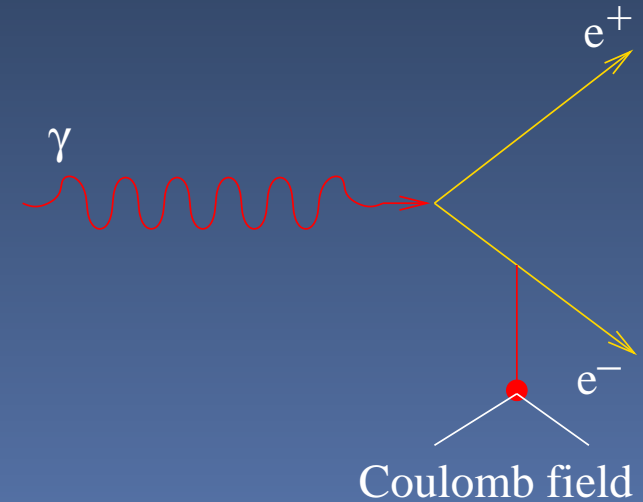
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Threshold energy:

$$E_\gamma = 2m_e c^2 + \frac{2m_e^2 c^2}{m_{\text{target}}}$$
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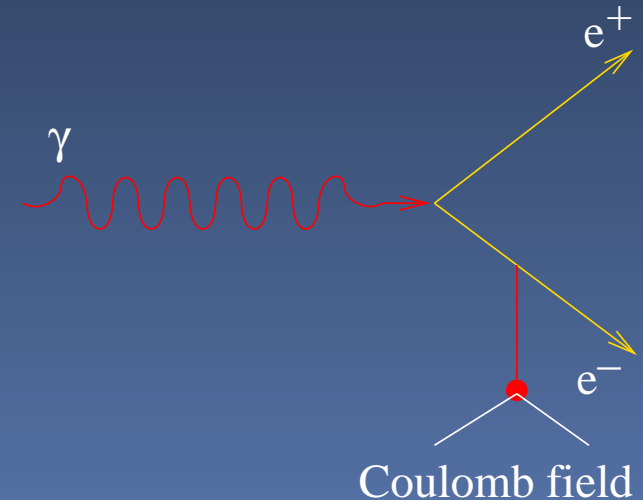
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For $\varepsilon \gg \frac{1}{\alpha Z^{1/3}}$ i.e. $E_\gamma \gg 20 \text{ MeV}$ (complete screening):

$$\sigma_{\text{pair}} = 4\alpha r_e^2 Z^2 \left(\frac{7}{9} \ln \frac{183}{Z^{1/3}} - \frac{1}{54} \right) [\text{cm}^2/\text{atom}] \approx \frac{7}{9} \frac{A}{N} \cdot \frac{1}{X_0}$$

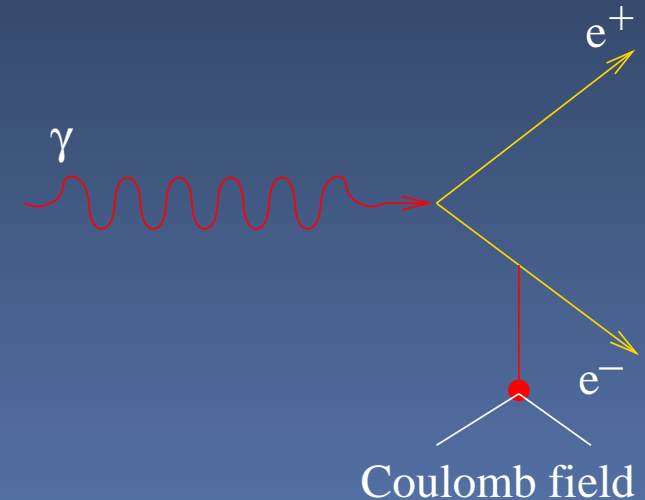
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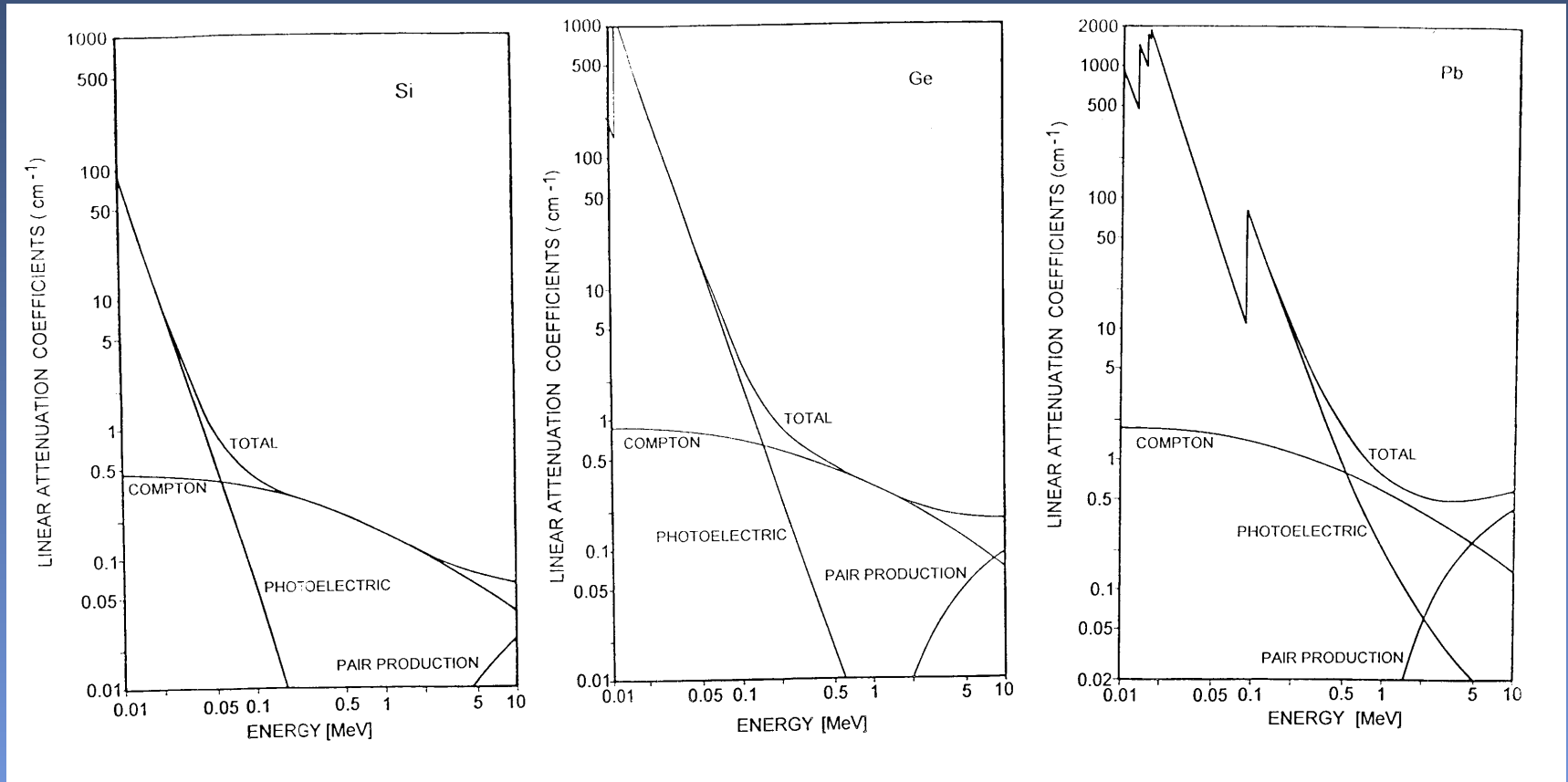


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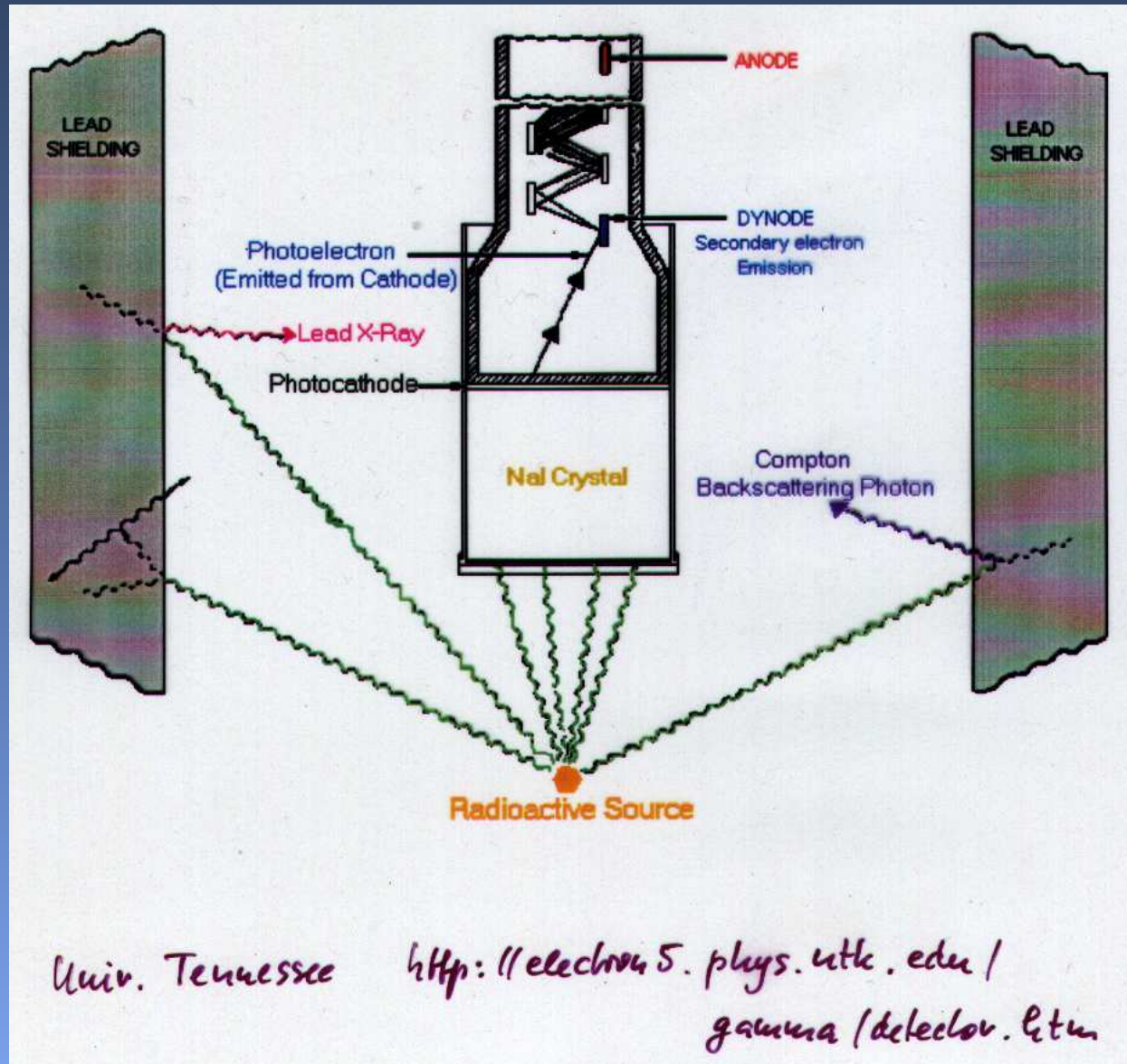
At high energies ($E_\gamma > 1 \text{ GeV}$) asymmetric energy sharing between e^+ and e^- , important for electromagnetic cascades.

Interactions of Photons (4)

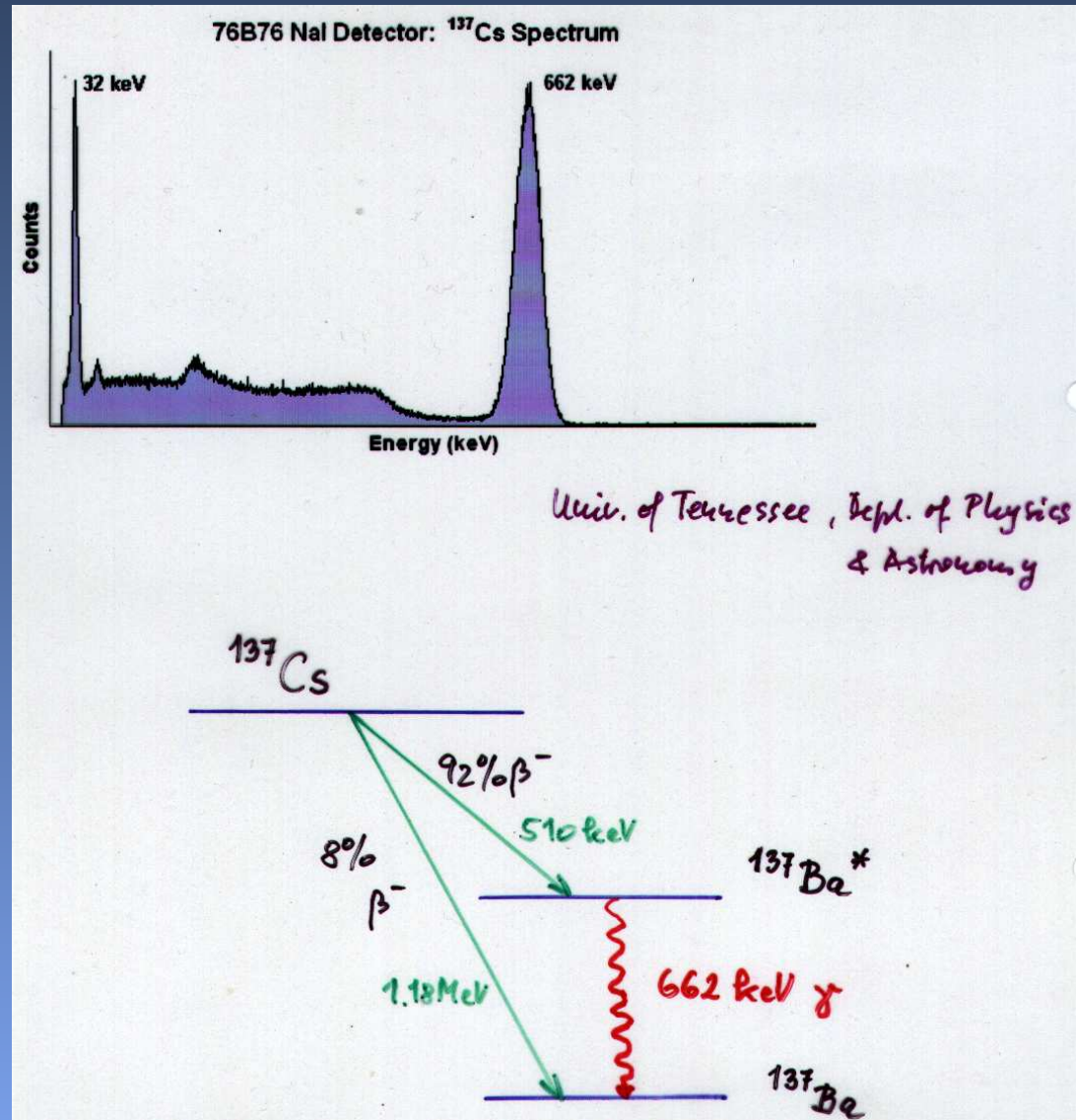


Harshaw 1969

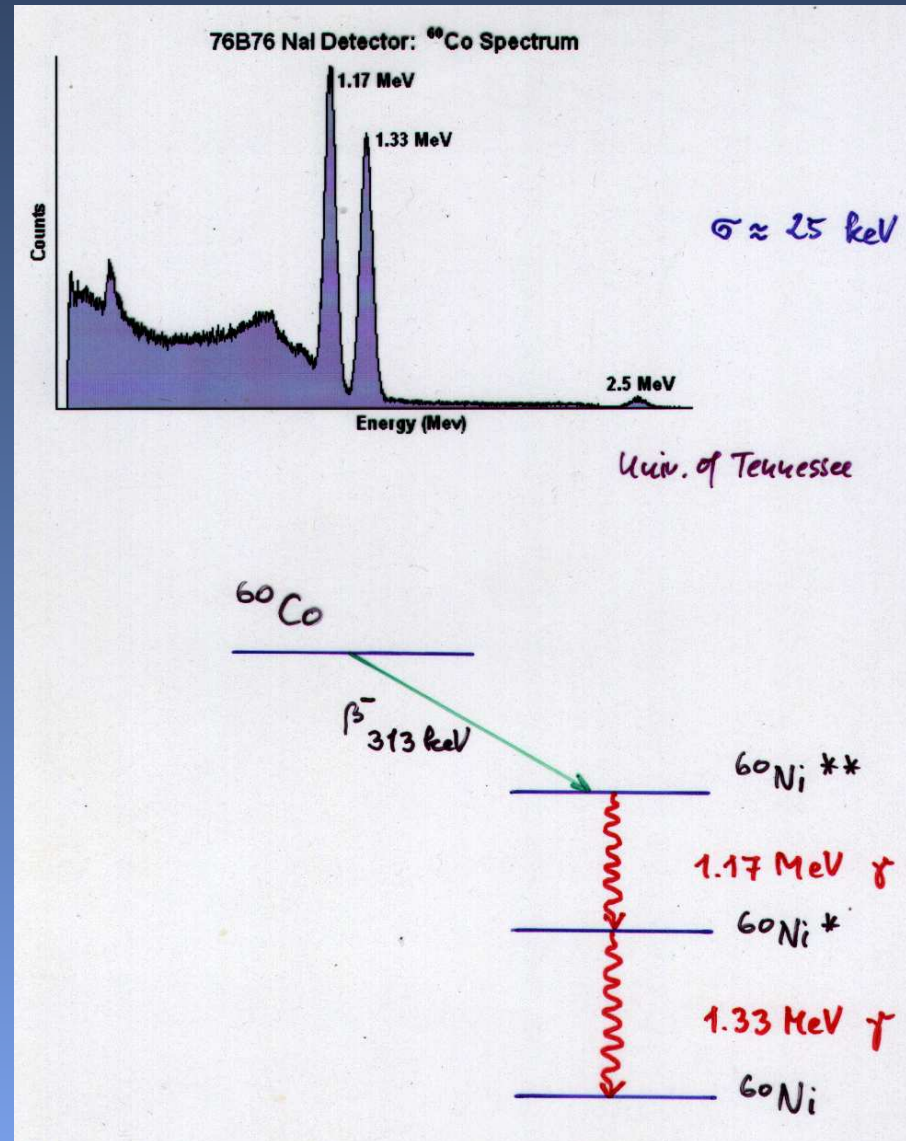
Setup for γ Ray Spectroscopy



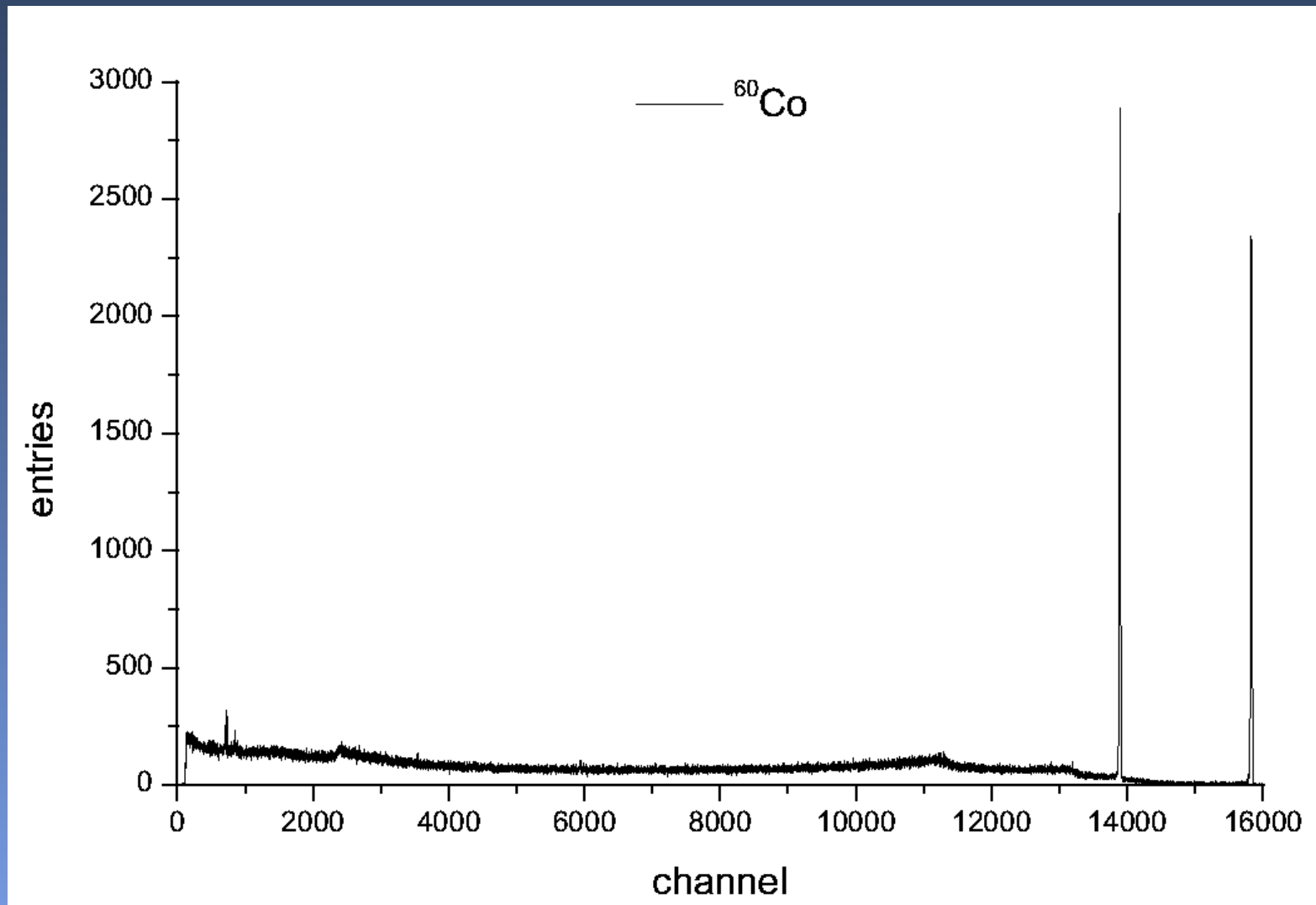
γ Spectrum of ^{137}Cs



γ Spectrum of ^{60}Co with NaI(Tl)



γ Spectrum of ^{60}Co with HPGe



High resolution photon detector

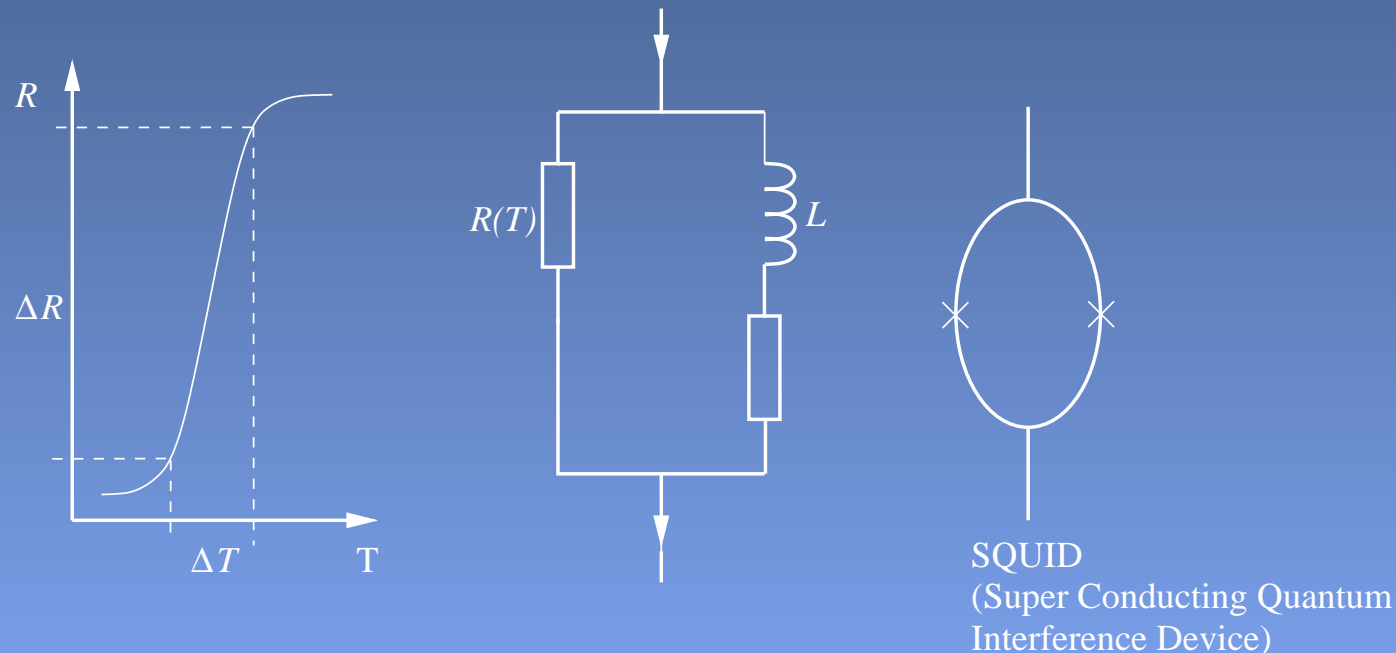
CRESST - Cryogenic Rare Event Search with Superconducting Thermometers

NIM A 354 (1995) 408

avmp01.mppmu.mpg.de/cresst/

Superconducting phase transition thermometer

Principle:



$$\frac{\Delta R}{\Delta T} \Rightarrow \frac{dR}{dT} \rightarrow U_{\text{ind}} \Rightarrow \frac{dH}{dt}$$

Trident Production / Pair Production

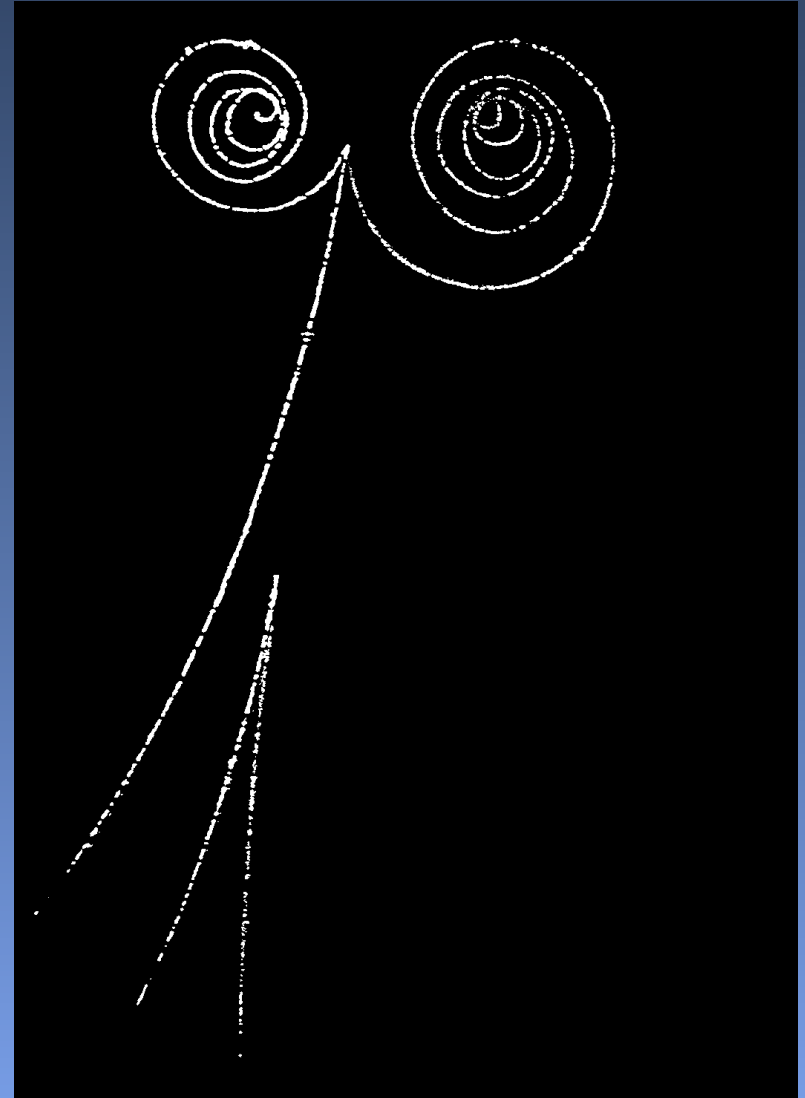
Trident production:

$$\gamma + e^- \rightarrow e^- + e^+ + e^-$$

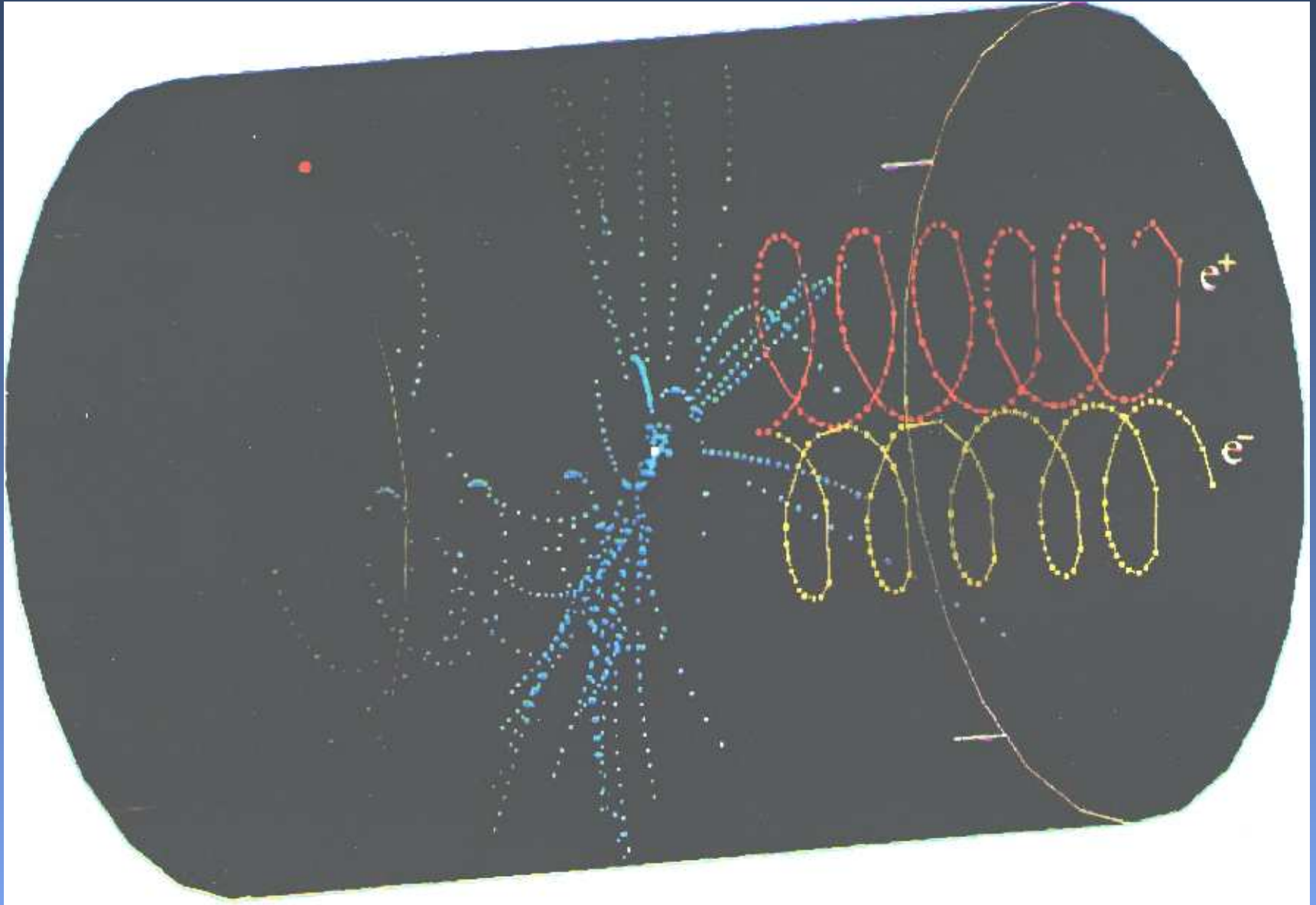
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F. Close et al. 1987



ALEPH



Interaction of Neutrons

Indirect detection technique: induce neutrons to interact and produce charged particles:

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Neutron detection and identification is important in the field of radiation protection because the relative biological effectiveness (quality factor) is high and depends on the neutron energy.

$$H [\text{Sievert}] = q \cdot D [\text{Gray}]$$

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$$\nu_e + n \rightarrow p + e^-$$

$$\bar{\nu}_e + p \rightarrow n + e^+ \text{ (discovery of the neutrino)}$$

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for MeV neutrinos:

$$\sigma(\nu_e N) = \frac{4}{\pi} \cdot 10^{-10} \left\{ \frac{\hbar p}{(m_p c)^2} \right\}^2 = 1.6 \cdot 10^{-44} \text{ cm}^2 \text{ for } 0.5 \text{ MeV.}$$

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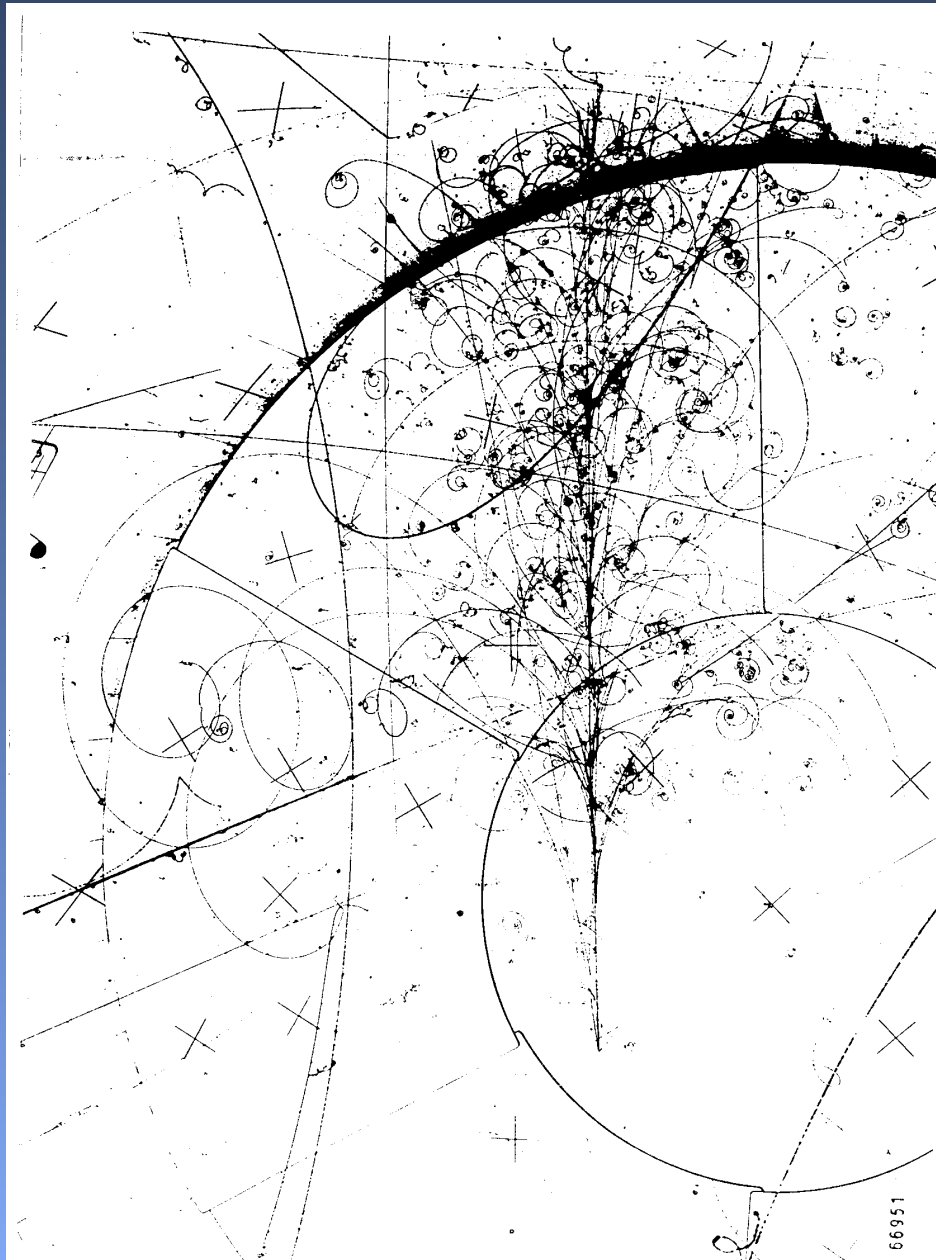
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Measurement by missing momentum and missing energy technique.

Electromagnetic Cascade (1)

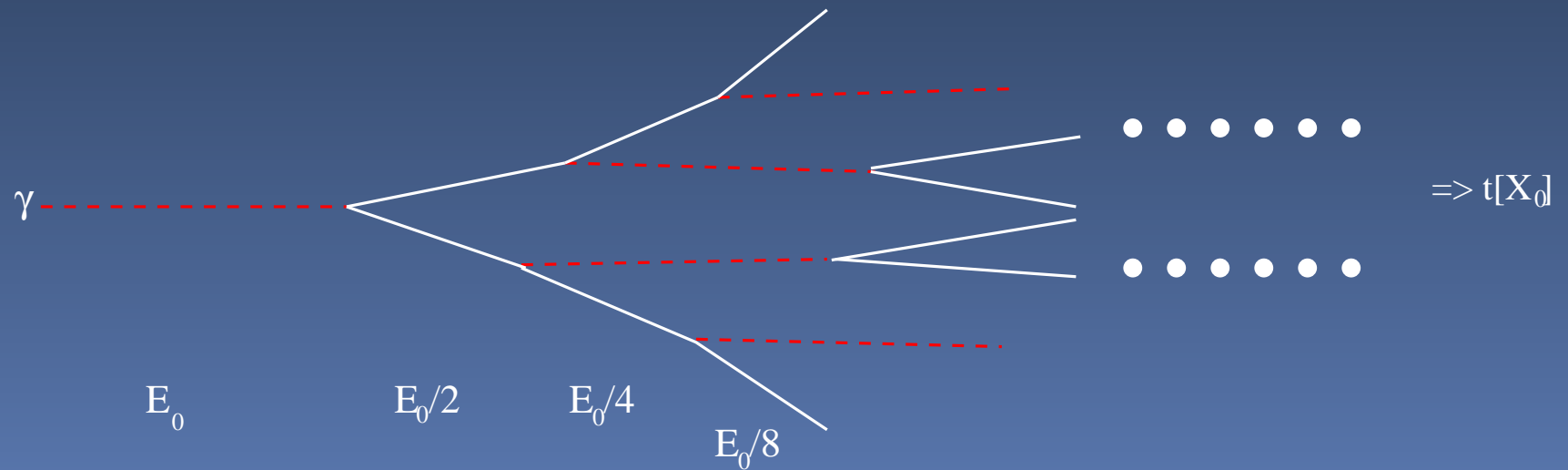


$\nu_e + \text{nucleon} \rightarrow e^- + \text{hadrons}$
electromagnetic cascade

H. Wachsmuth, CERN 1998

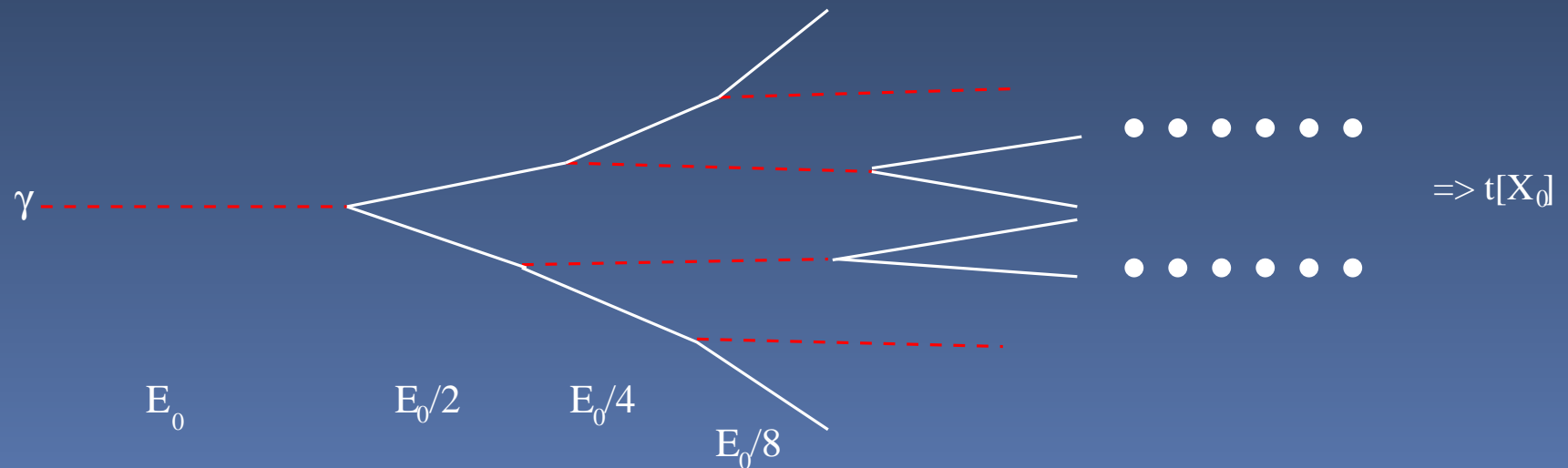
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Number of particles (e^+ , e^- , γ): $N(t) = 2^t$.

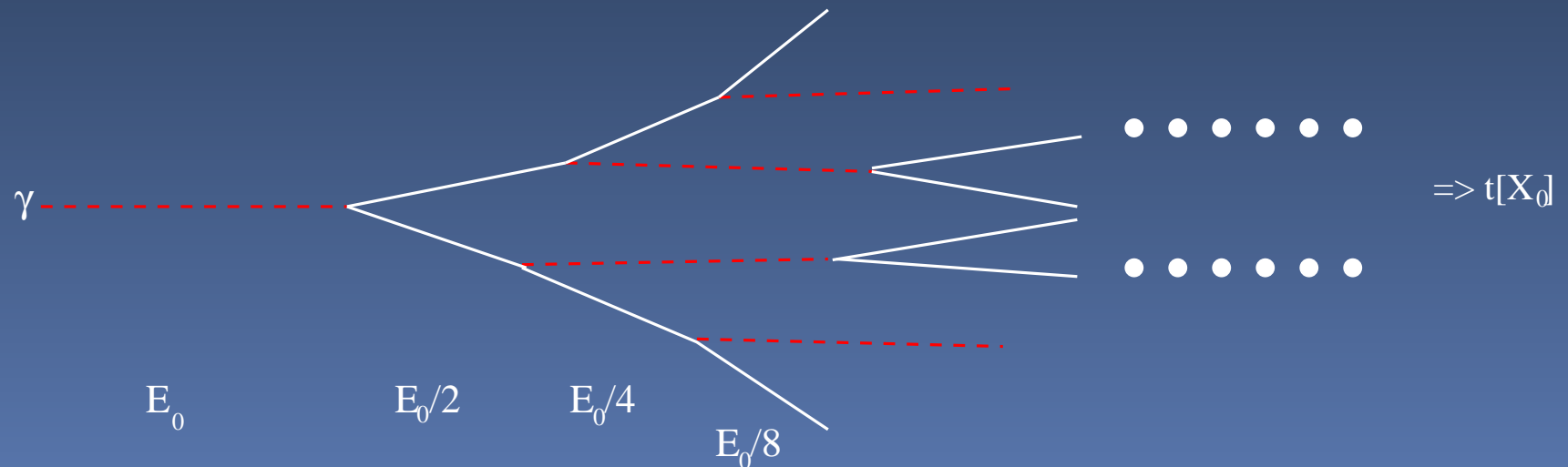
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Total number of shower particles:

$$S = \sum N(t) = \sum 2^t = 2^{t_{\max}+1} - 1 \approx 2 \cdot 2^{t_{\max}} = 2 \cdot \frac{E_0}{E_c} \propto E_0.$$

Energy Resolution of Electromagnetic Calorimeters

Total track length (sampling step t):

$$S^* = \frac{S}{t} = 2 \cdot \frac{E_0}{E_c} \cdot \frac{1}{t},$$

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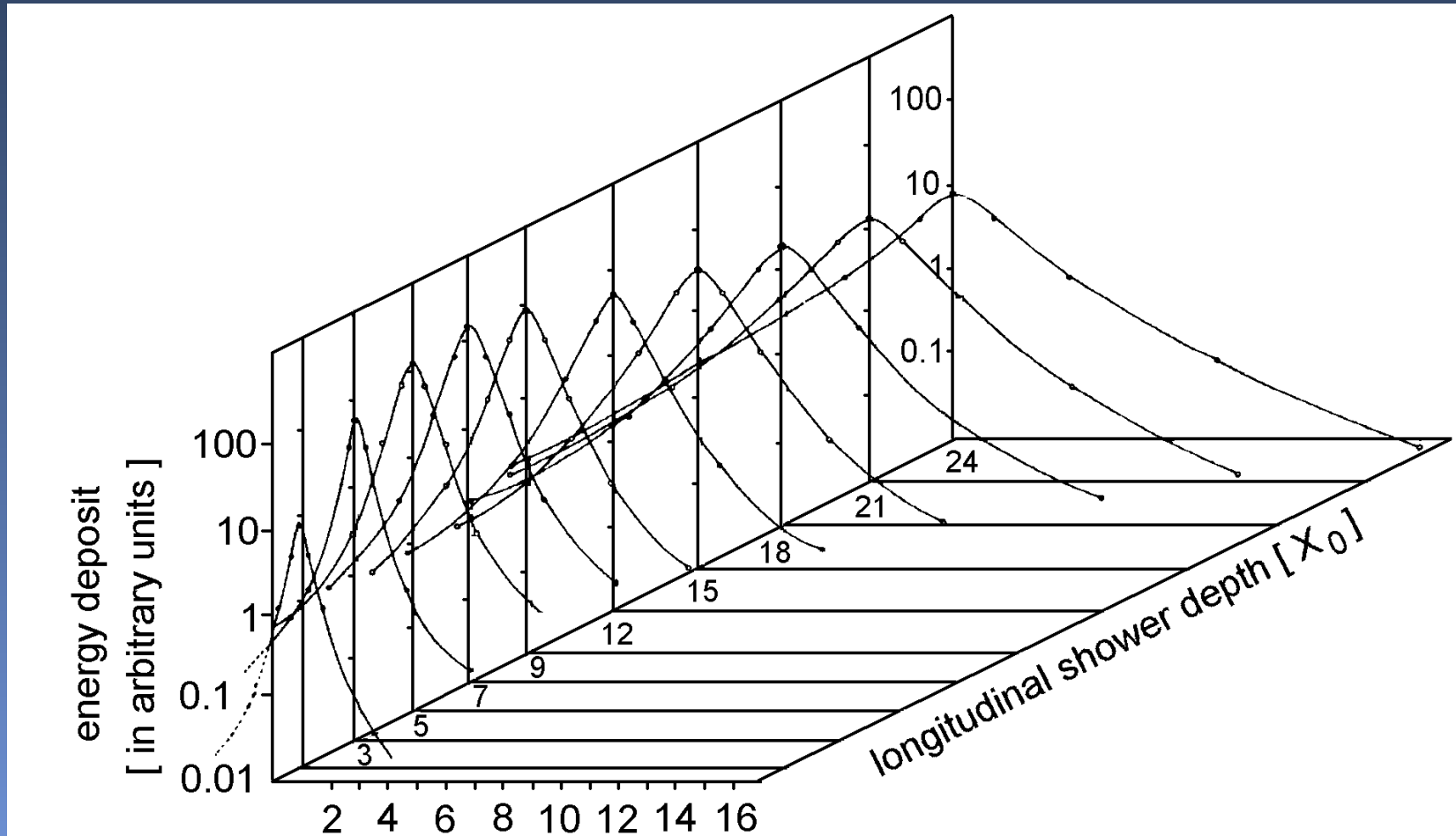
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Attractive alternative: *sampling calorimeters*.

Logitudinal and Lateral Profile of an Electron Shower



6 GeV electrons, Grupen 1996

Multi-Plate Cloud Chamber (1)

$\mu^- + \text{nucleus} \rightarrow \mu^- + \text{nucleus}' + \gamma$
 $\gamma \rightarrow \text{electromagnetic cascade}$

Rochester 1981

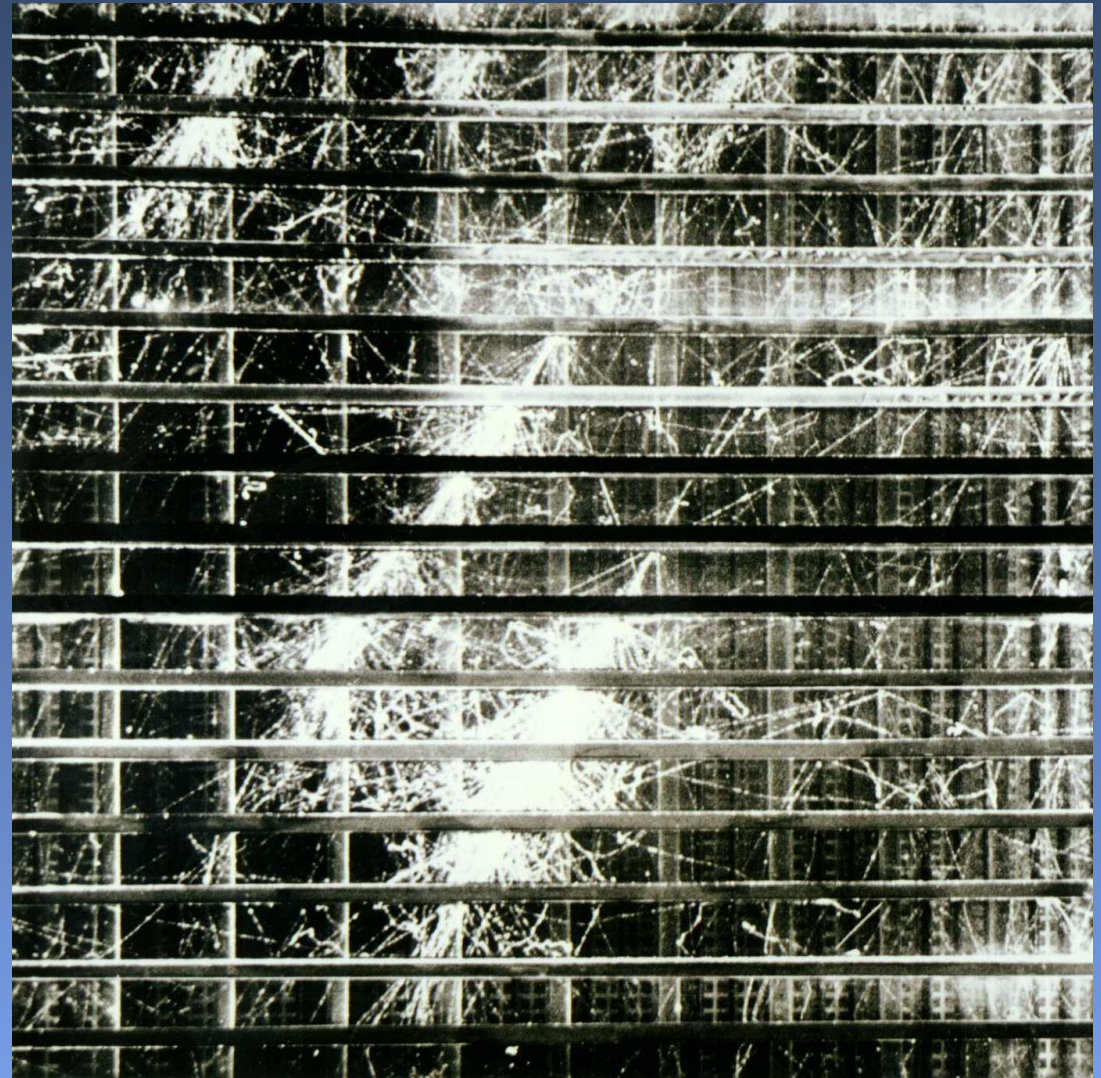


Multi-Plate Cloud Chamber (2)

Multi-plate cloud chamber in an air shower experiment below 3 m of concrete

electromagnetic showers initiated by muon *bremstrahlung*.

Wolter 1970



Hadron Cascades

Longitudinal development: interaction length.

Lateral spread: transverse momentum p_t

since $\lambda > X_0$ and $\langle p_t \rangle \gg \langle p_t \rangle_{\text{multiple scattering}}$

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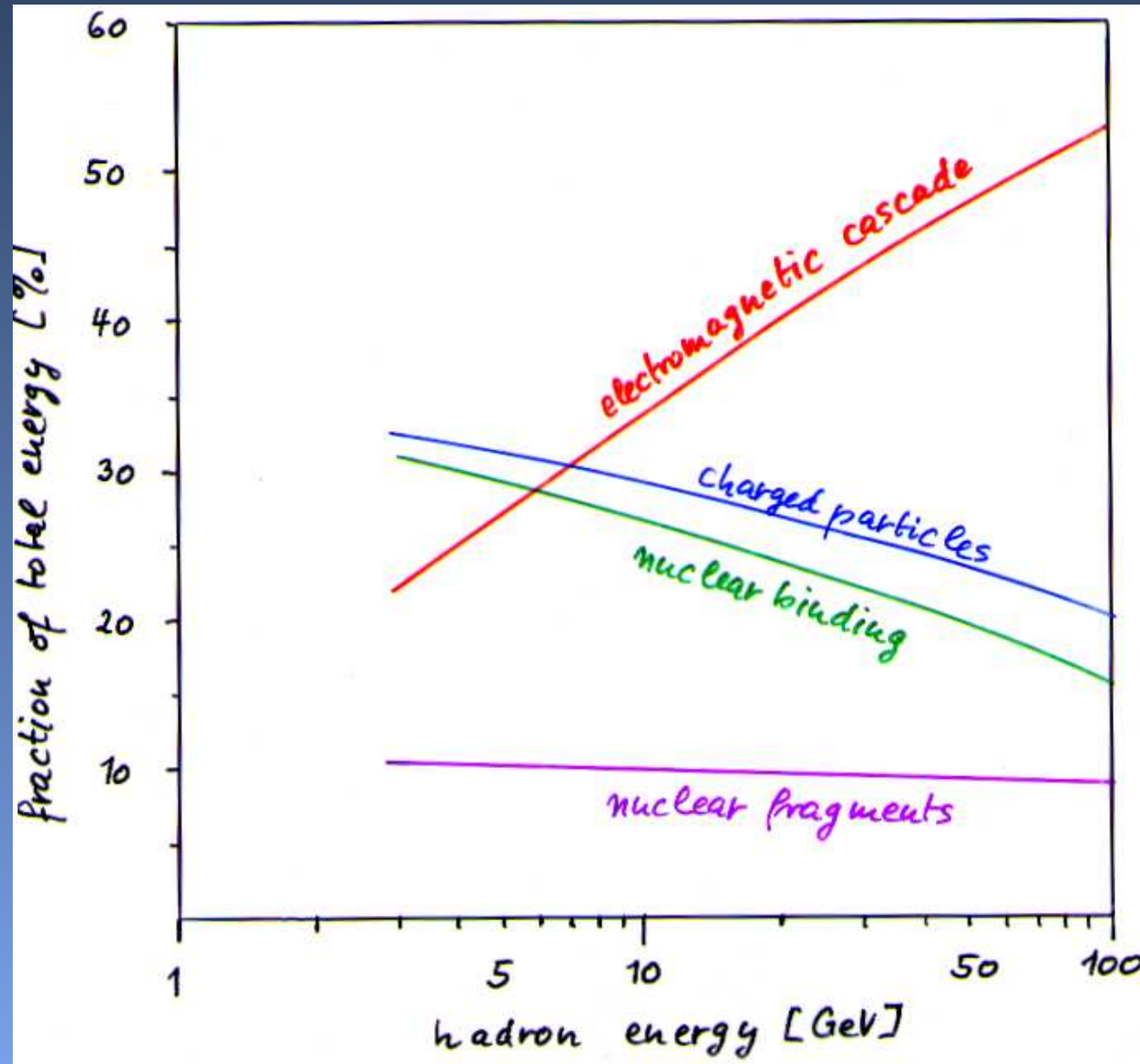
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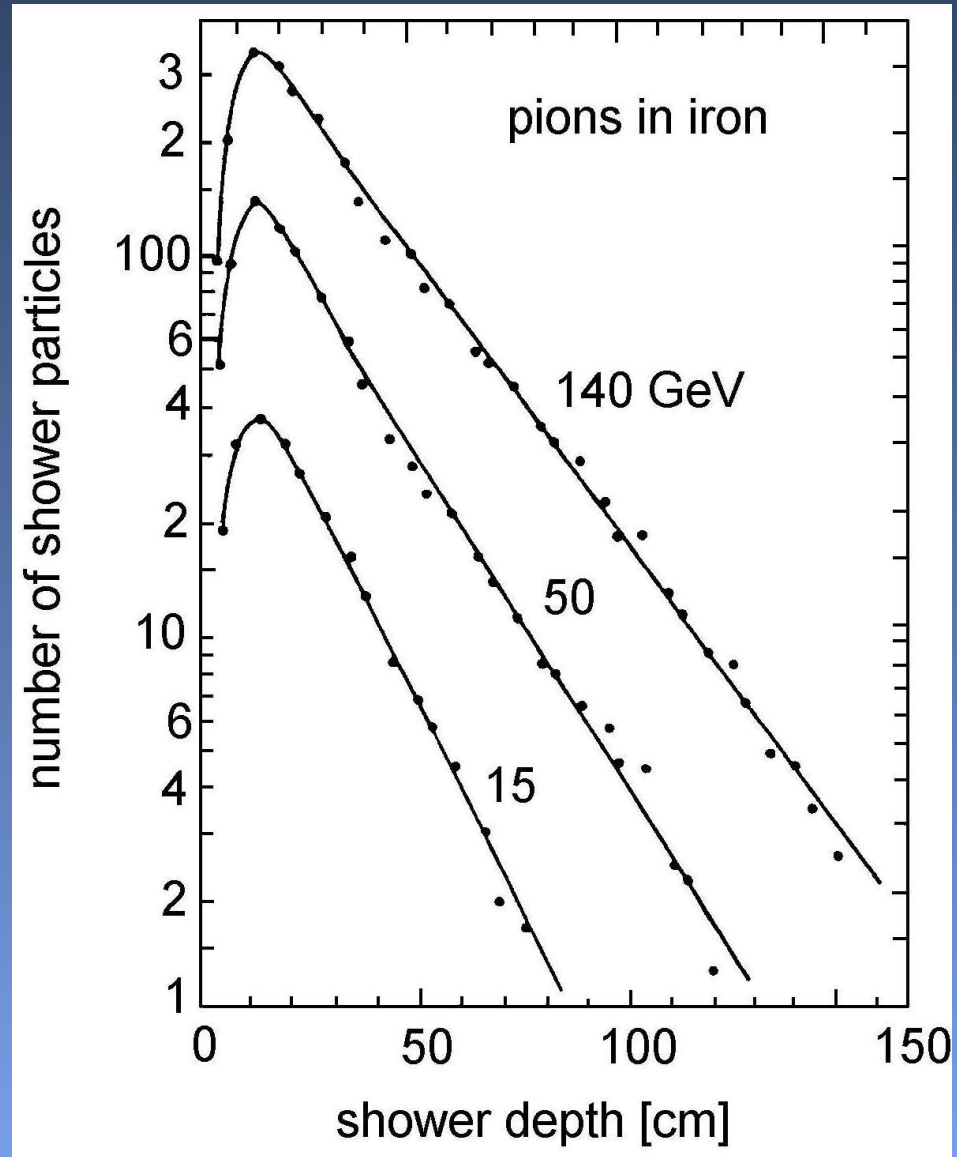
Problem of compensation: different response to electrons and hadrons, aim at balanced response $e/\pi = 1$.

Energy Sharing in a Hadron Cascade

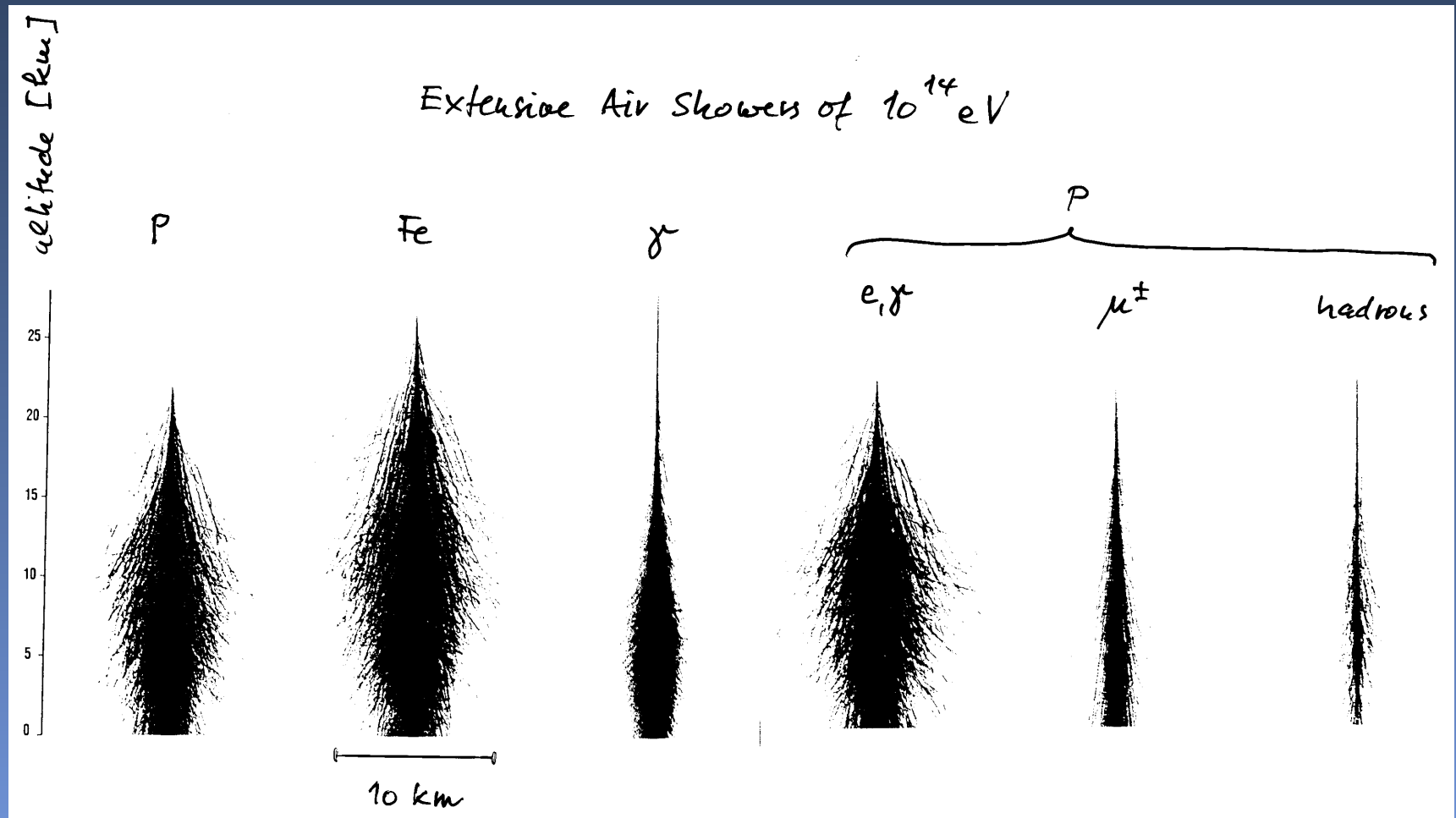


Longitudinal Development of a Hadron Cascade

Holder 1978
NIM 151 (1978) 69



Extensive Air Showers of 10^{14} eV



J. Knapp, D. Heck, Karlsruhe 1998

Methods of Particle Identification

	tracking chamber	Cherenkov counters $n_1 < n_2 < n_3$			electromagn. calorimeter	hadron calorimeter	muon chambers	
γ								
e^+, e^-								
μ^+, μ^-								μ
π^+, π^-								
p								
n								
ν								ν

Particle Identification with Time of Flight (TOF)

$$\Delta t = L \left(\frac{1}{v_1} - \frac{1}{v_2} \right) = \frac{L}{c} \left(\frac{1}{\beta_1} - \frac{1}{\beta_2} \right)$$

using $\gamma = \frac{1}{\sqrt{1-\beta^2}}$ this gives:

$$\Delta t = \frac{L}{c} \left\{ \sqrt{\frac{\gamma_1^2}{\gamma_1^2 - 1}} - \sqrt{\frac{\gamma_2^2}{\gamma_2^2 - 1}} \right\}.$$

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Since in this case $\approx pc$ one gets for a momentum defined beam:

$$\Delta t = \frac{Lc}{2p^2} (m_1^2 - m_2^2).$$

Example: $e/\mu/\pi$ -separation

Example 1:

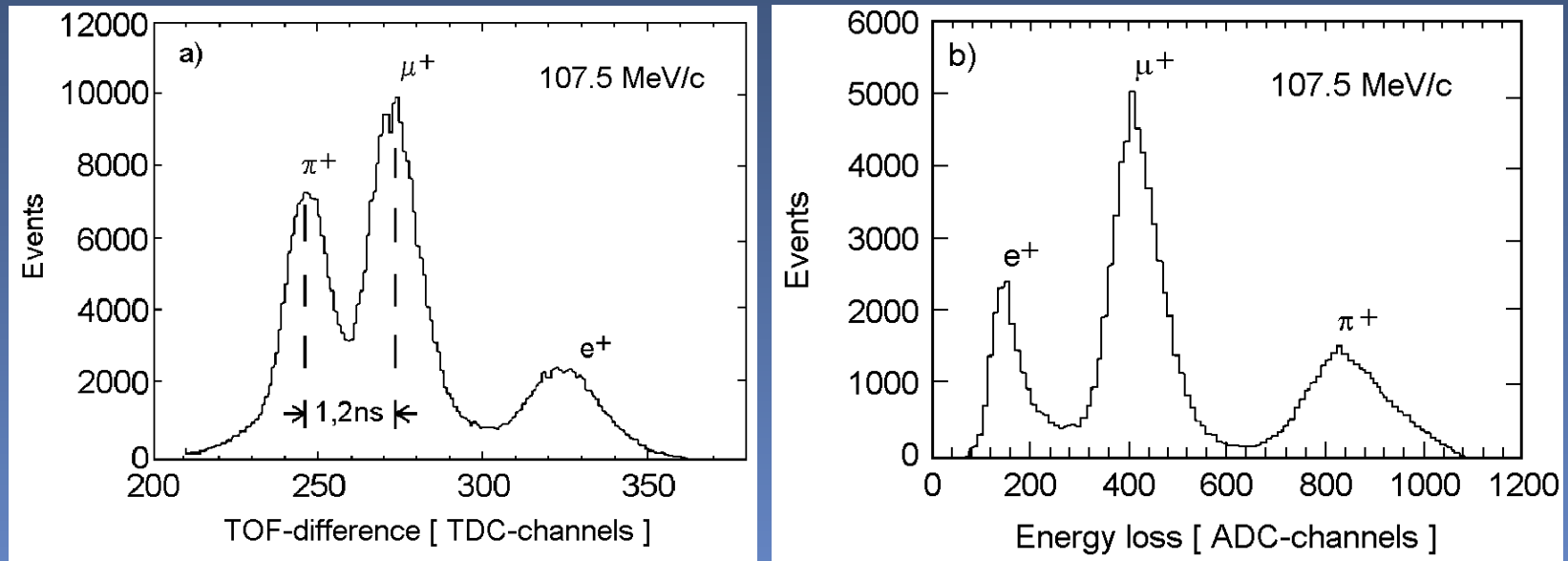
$e/\mu/\pi$ -separation for $L = 149.5$ cm

and $p = 107.5$ MeV/ c using TOF compared to dE/dx .

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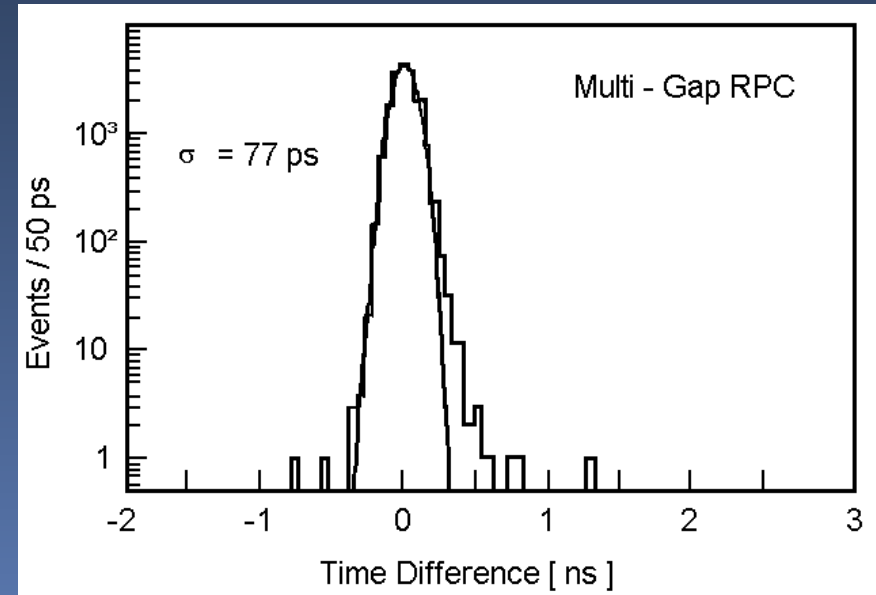
E. Fragiaco et al. NIM A 439 (2000) 45

Examples: TOF-resolution π/p -separation

Example 1:

TOF-resolution with a multi-gap-resistive plate chamber (RPC).

F. Sauli CERN-EP 2000/080



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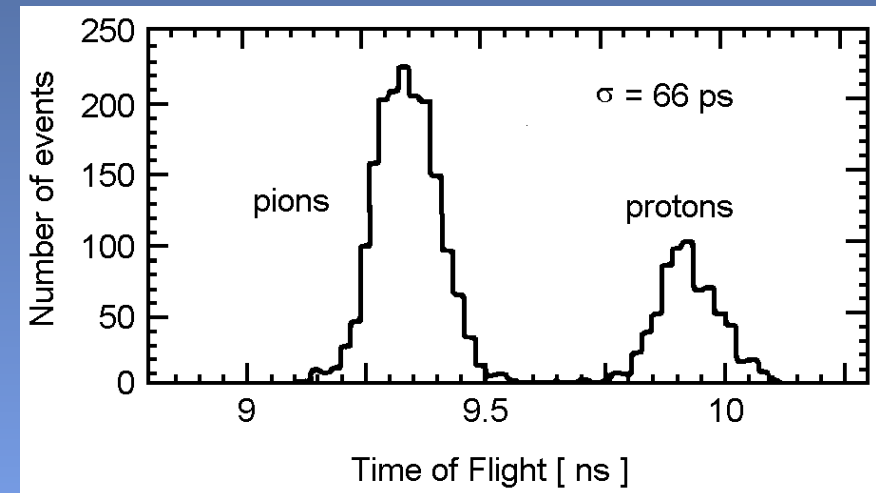
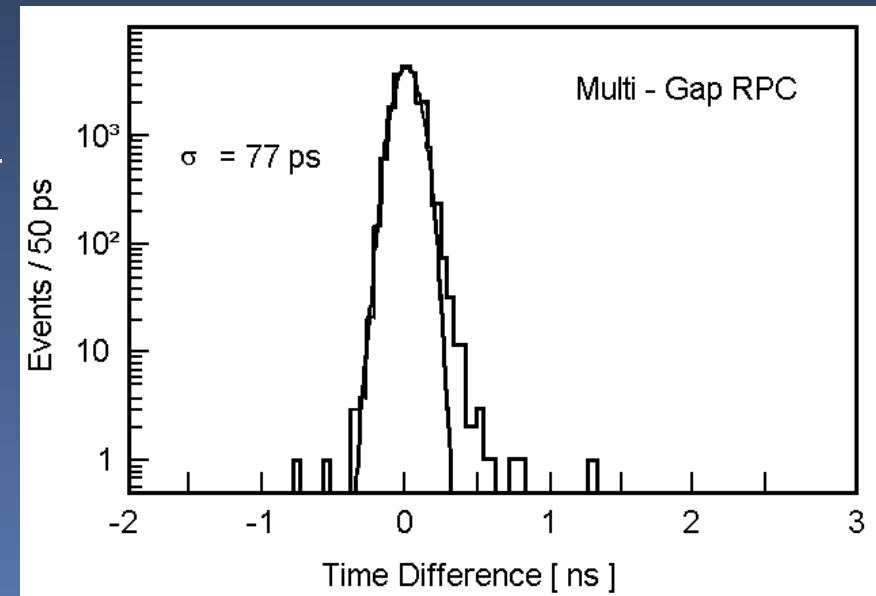
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F. Sauli CERN-EP 2000/080

π/p -separation in a
 $p = 2 \text{ GeV}/c$ scintillator
system.

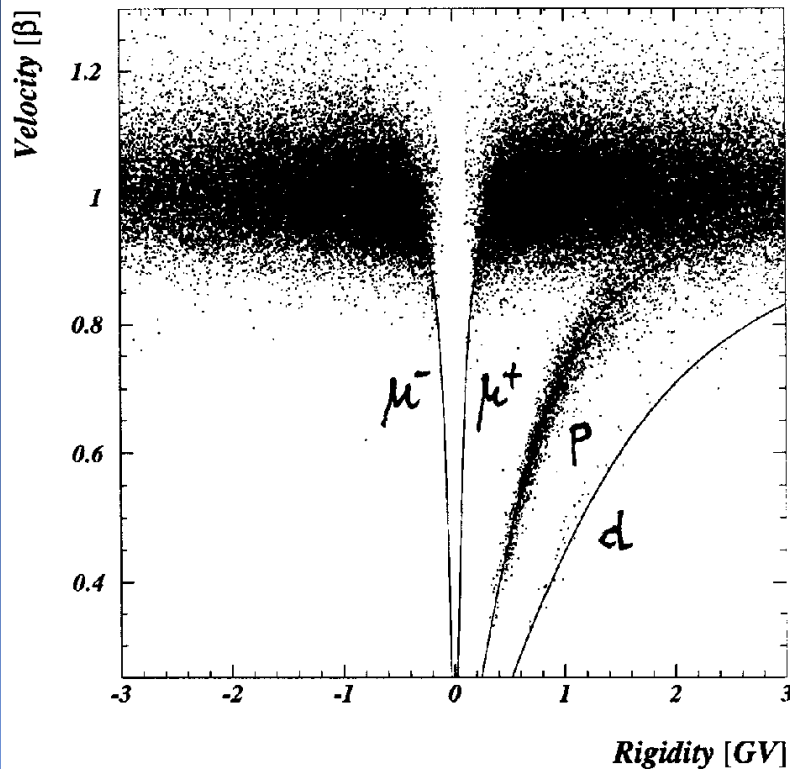
A. Sathya et al., BELLE 1999



Balloon Experiment; dE/dx ; Cherenkov; momentum

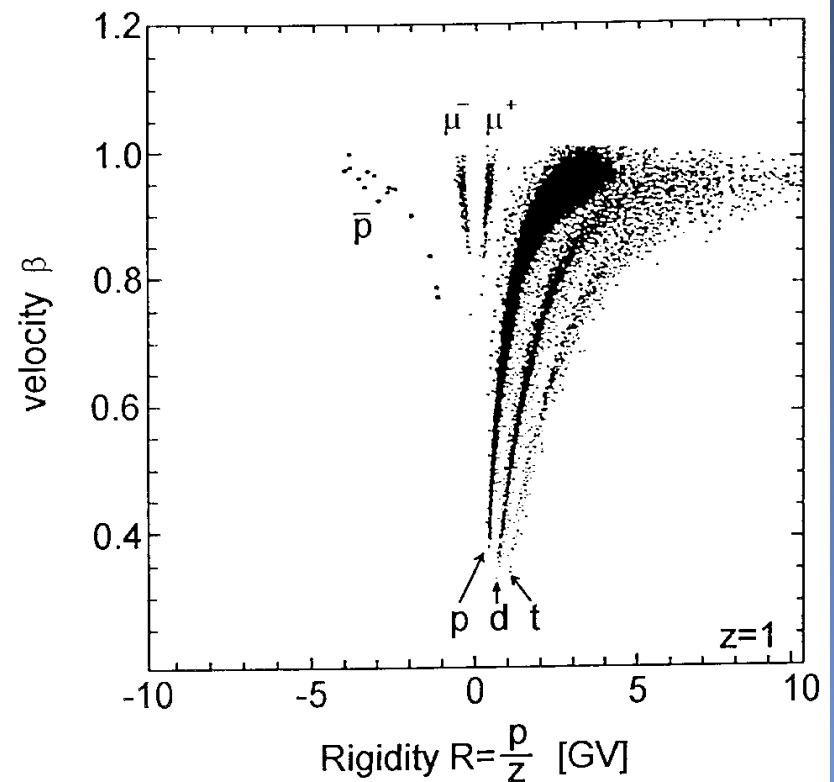
balloon experiment; TOF; dE/dx ; Cherenkov; momentum

altitude: 1234 m



Kremer 1999

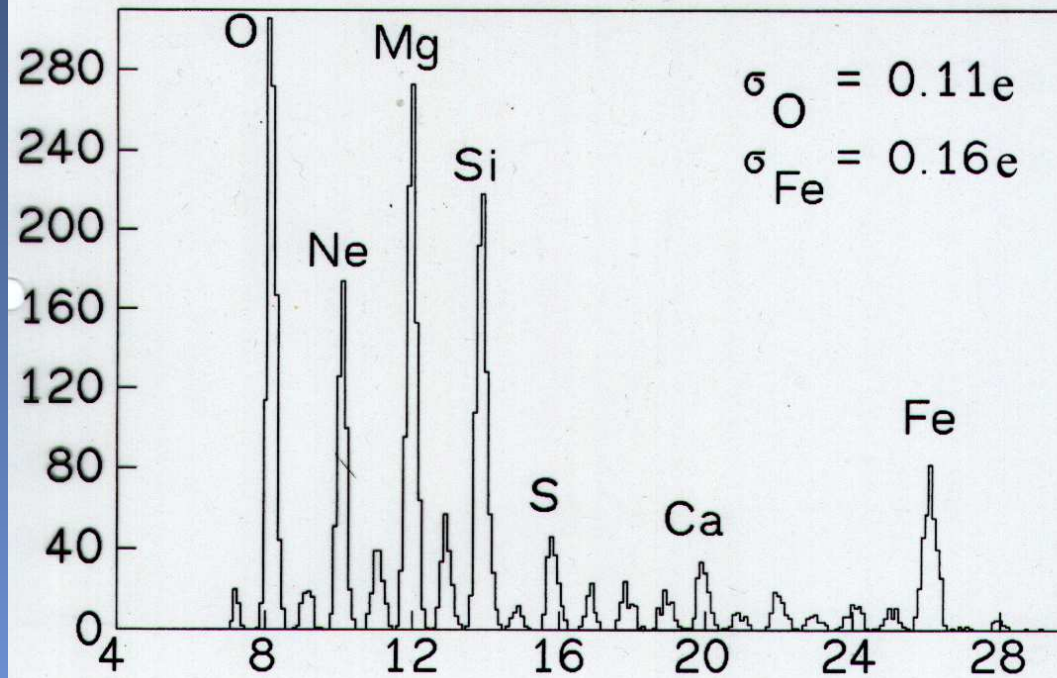
altitude \sim 40 km



Mitchell et al. 1996

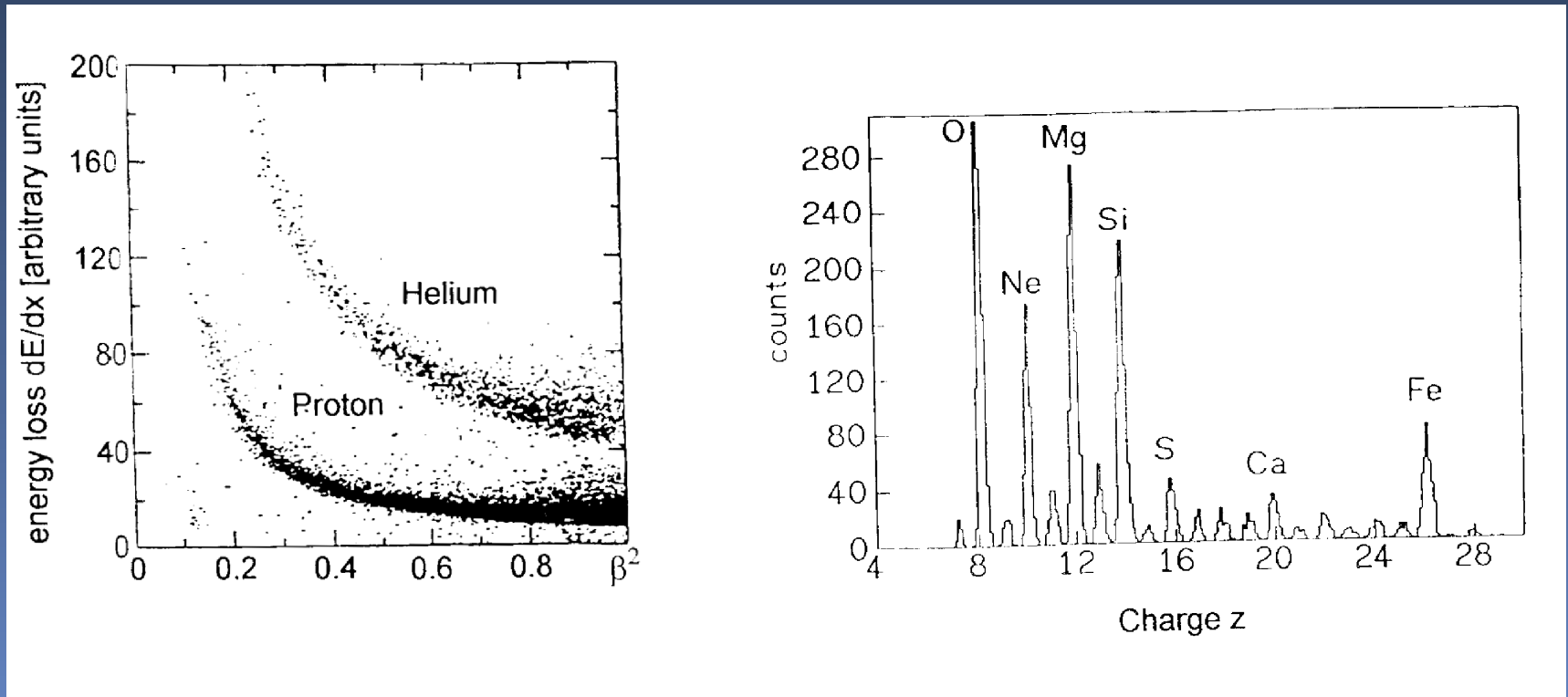
ALICE

Abundance of Cosmic Ray Particles
at 1 GeV/nucleon measured with
the **ALICE**-Experiment



probe of high energy
cosmic matter

Balloon Experiment ~ 40 km



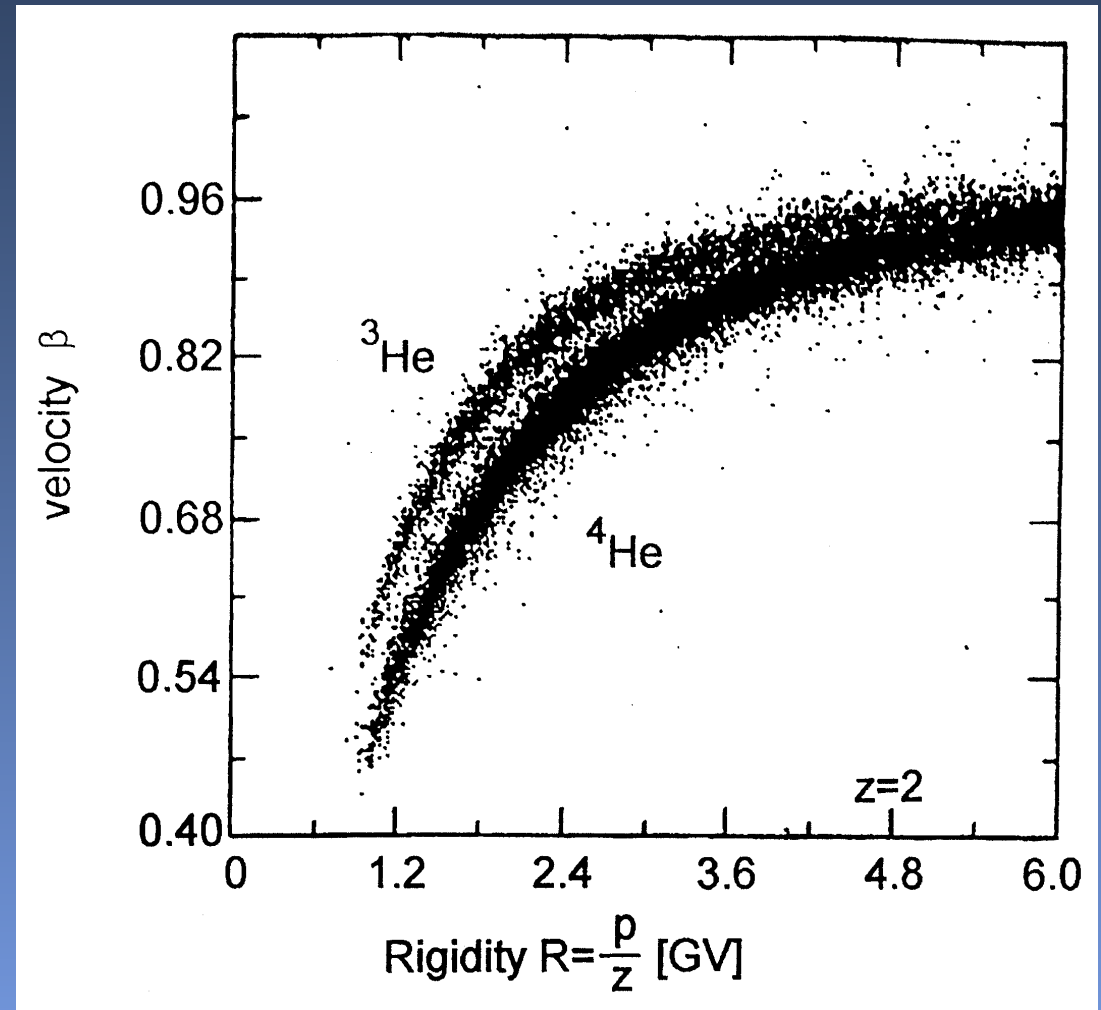
Reimer 1995
Ph. D. Thesis Siegen

Hesse 1991
Proc. ICRC Dublin, Vol. 1, p. 596

Balloon Experiment

Balloon flight 40 km,
TOF, dE/dx ,
momentum,
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