

# Microwave Transmission: Theory, Simulations, Experiments and Plans

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- Definition and derivation of phase shift
- Phase modulation and side bands
- Experimental and simulation results
- Some details behind the physics of “cyclotron resonance”
- Experimental and simulation results on “cyclotron resonance”
- Plans at ANKA : Support SC undulator research.
- Conclusions

# What we mean by “Phase Shift” in Microwave Transmission due to eclouds

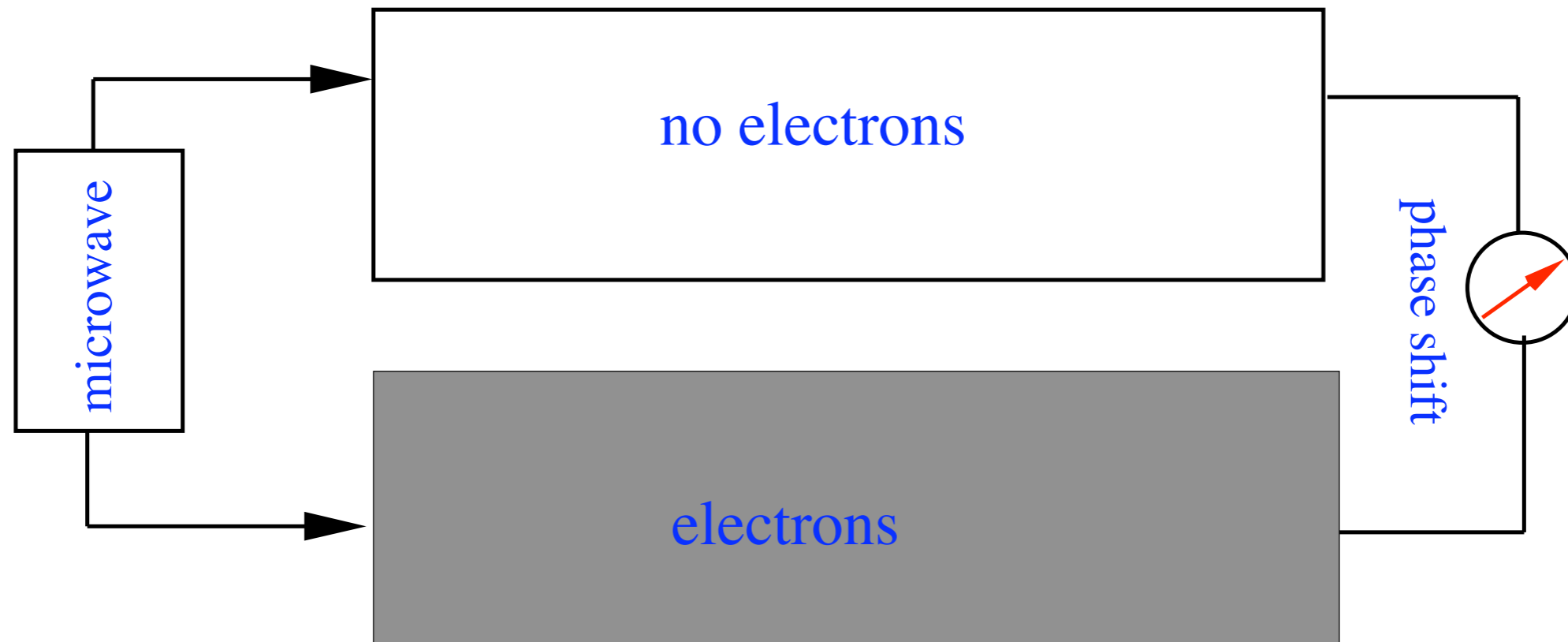


illustration of phase shift due to electrons

$$\begin{aligned} & \sin(\omega t + \phi_1) - \sin(\omega t + \phi_2) = \\ & 2 \sin[(\omega_1 - \omega_2)/2] \cos[\omega t + (\phi_1 + \phi_2)/2] \\ & \sim (\phi_1 - \phi_2) \cos[\omega t + (\phi_1 - \phi_2)/2] \end{aligned}$$

# *This Phase Shift for is simple to derive for unmagnetized plasmas*

The dispersion relationship of a wave traveling through a plasma filled waveguide is given by

$$k^2 = \frac{\omega^2}{c^2} - \frac{\omega_p^2}{c^2} - \frac{\omega_c^2}{c^2}$$

where  $\omega_p^2 = \frac{n_e e^2}{\epsilon_0 m_e}$  plasma frequency,  $\omega_c =$  waveguide cutoff

The “phase shift” is given by

$$\Delta\Phi = [k(\omega_p) - k(\omega_p = 0)]L$$

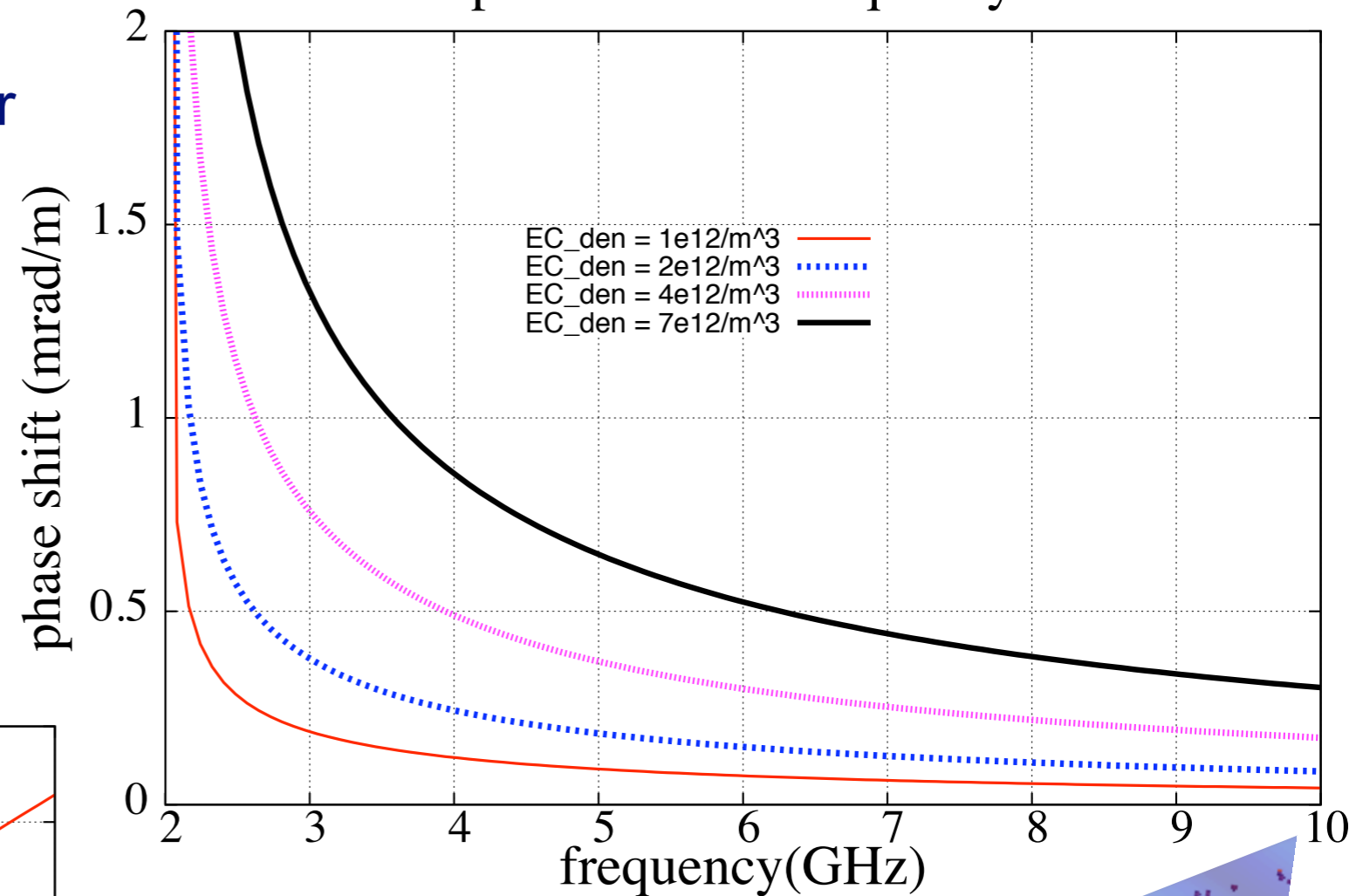
Linearize this about small plasma frequency, then for a unit length

$$\Delta\Phi = \frac{\omega_p^2}{2c(\omega^2 - \omega_c^2)^{1/2}}$$

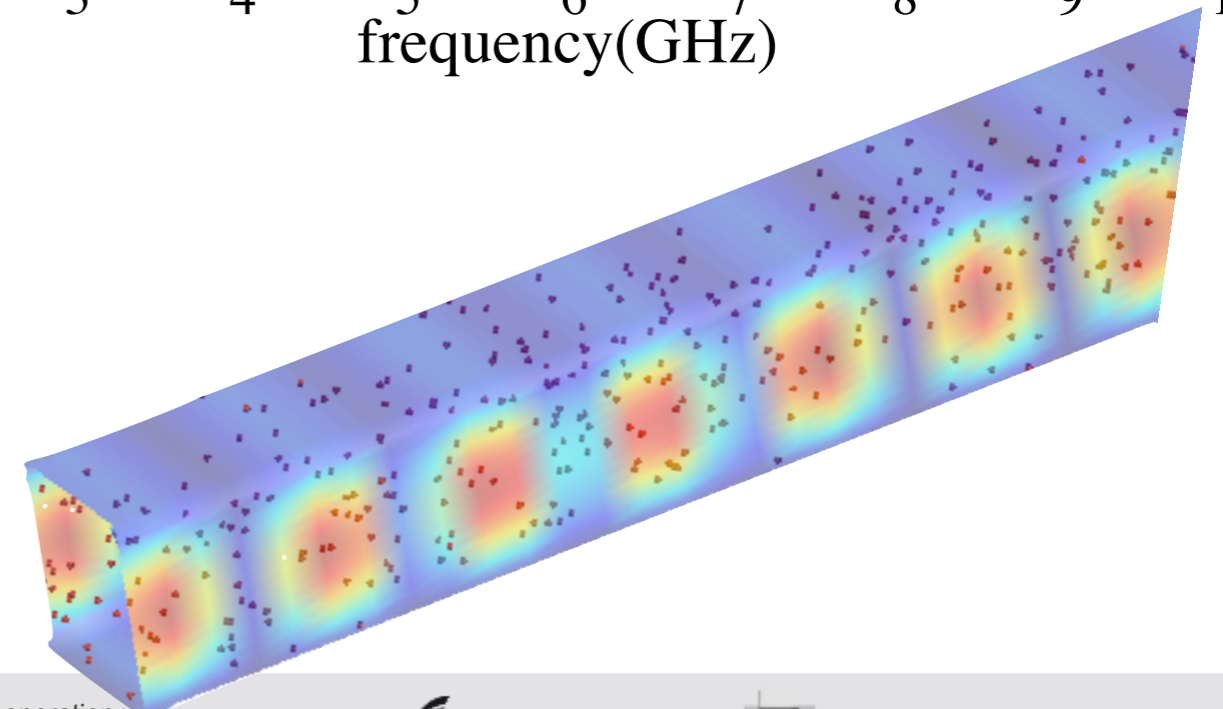
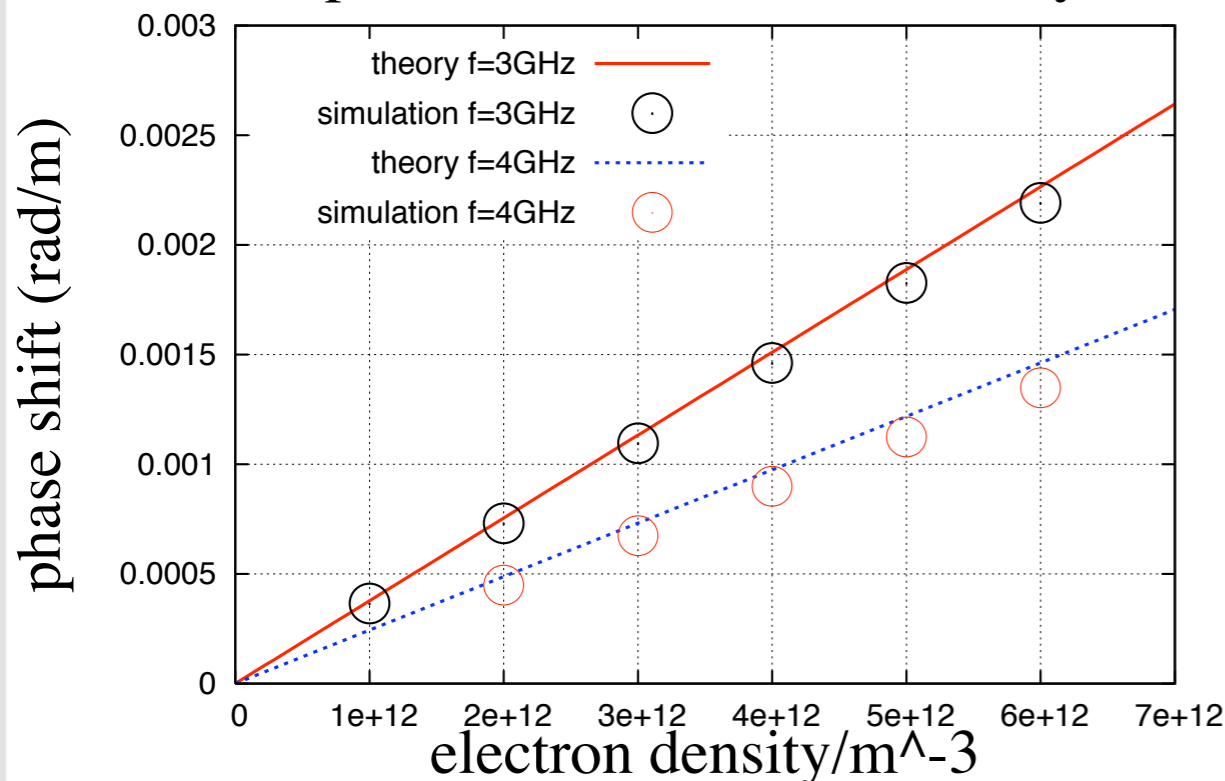
# Analytic results agree with simulations

- Simulations were performed for a rectangular cross section
- They agreed well with analytic estimates of phase shift
- We used the electromagnetic PIC code VORPAL for this.

phase shift vs frequency



phase shift vs electron density



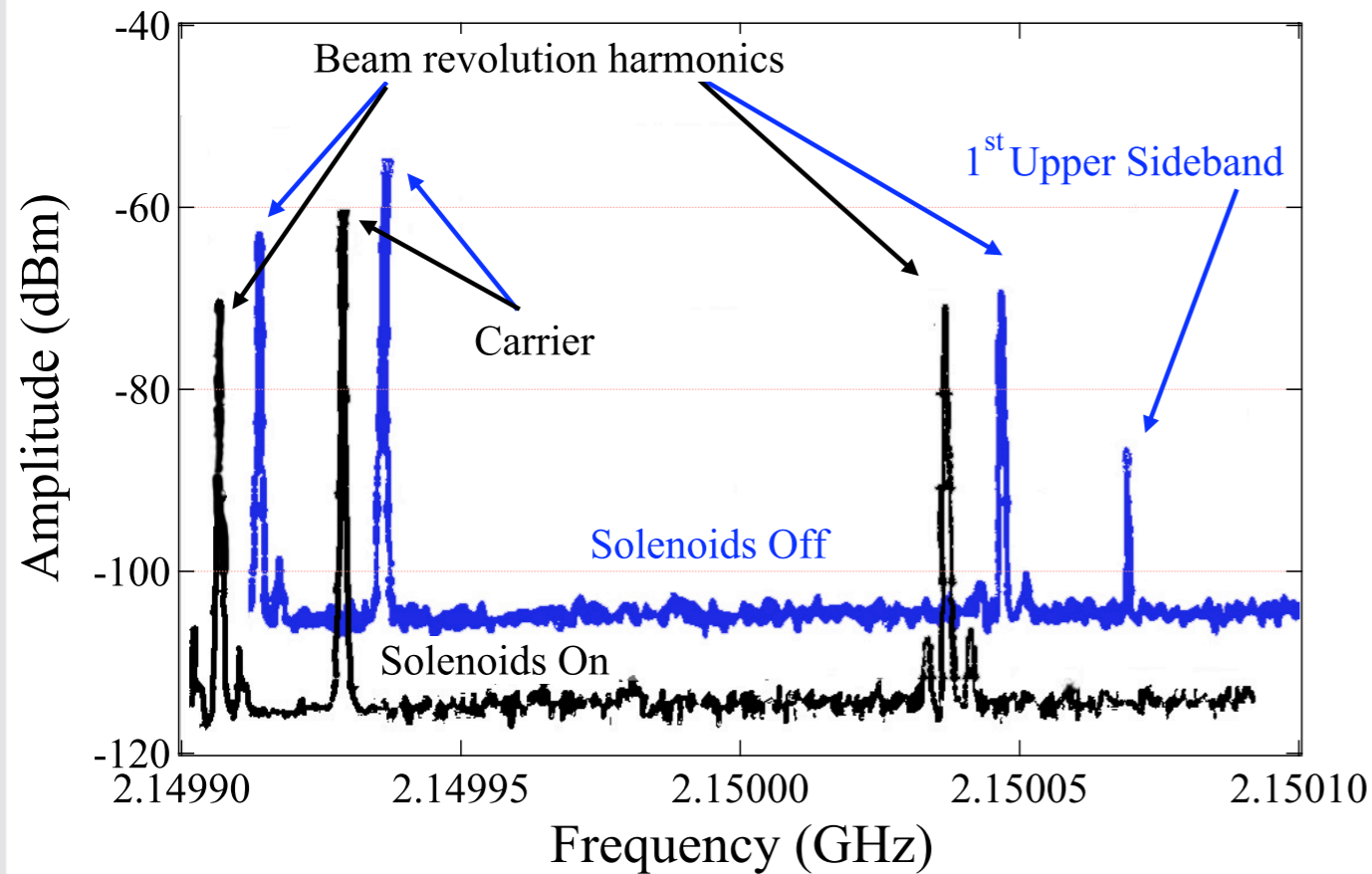
# Phase Shift can be observed through “Side Bands” seen on a Spectrum Analyzer

- The gap in the bunch train creates a periodic clearing of the electrons at the **revolution frequency**.
- This leads to a **phase modulation** in the microwave signal.
- The phase modulation produces **sidebands** to the input signal frequency at harmonics of revolution frequency.
- Assuming **sinusoidal modulation**, we get .....

$$\begin{aligned} W(t) &= \cos[\omega t + \Delta\phi \cos(\omega_m t)] = J_0(\Delta\phi) \cos(\omega t) \\ &+ J_1(\Delta\phi) \cos[(\omega - \omega_m)t + \pi/2] + J_1(\Delta\phi) \cos[(\omega + \omega_m)t + \pi/2] \\ &+ J_2(\Delta\phi) \cos[(\omega - 2\omega_m)t + \pi] + J_2(\Delta\phi) \cos[(\omega + 2\omega_m)t + \pi] \\ &+ \dots \text{ (higher order terms)} \end{aligned}$$

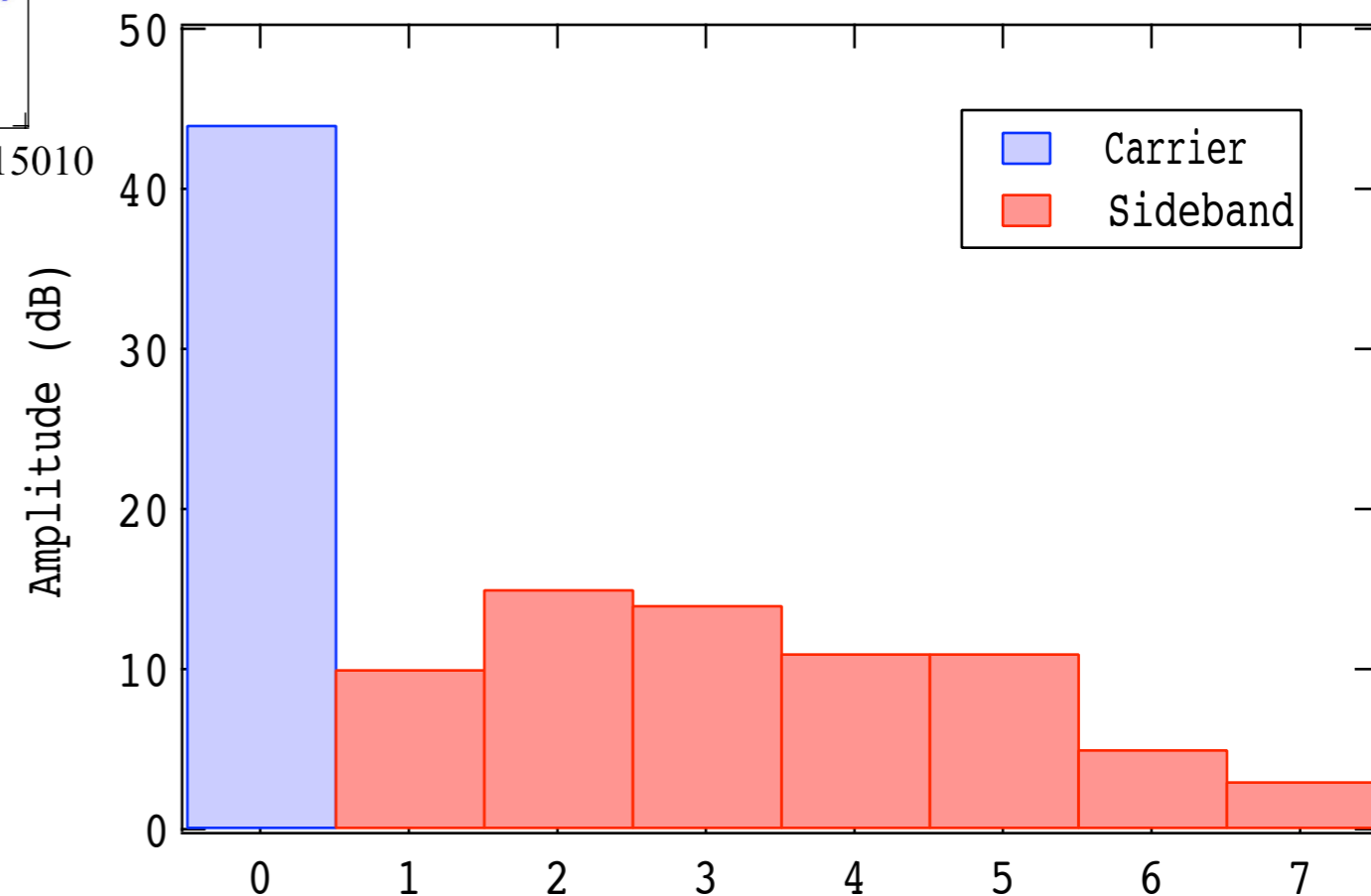
- Expect 1st order **peaks at higher revolution harmonics** as well for **non-sinusoidal modulation**.

# Phase Modulation was observed when electron clouds were present



Experiment performed at the PEP II LER at SLAC in a straight section where solenoids were used to suppress electron clouds

Observation of multiple sidebands due to non sinusoidal modulation



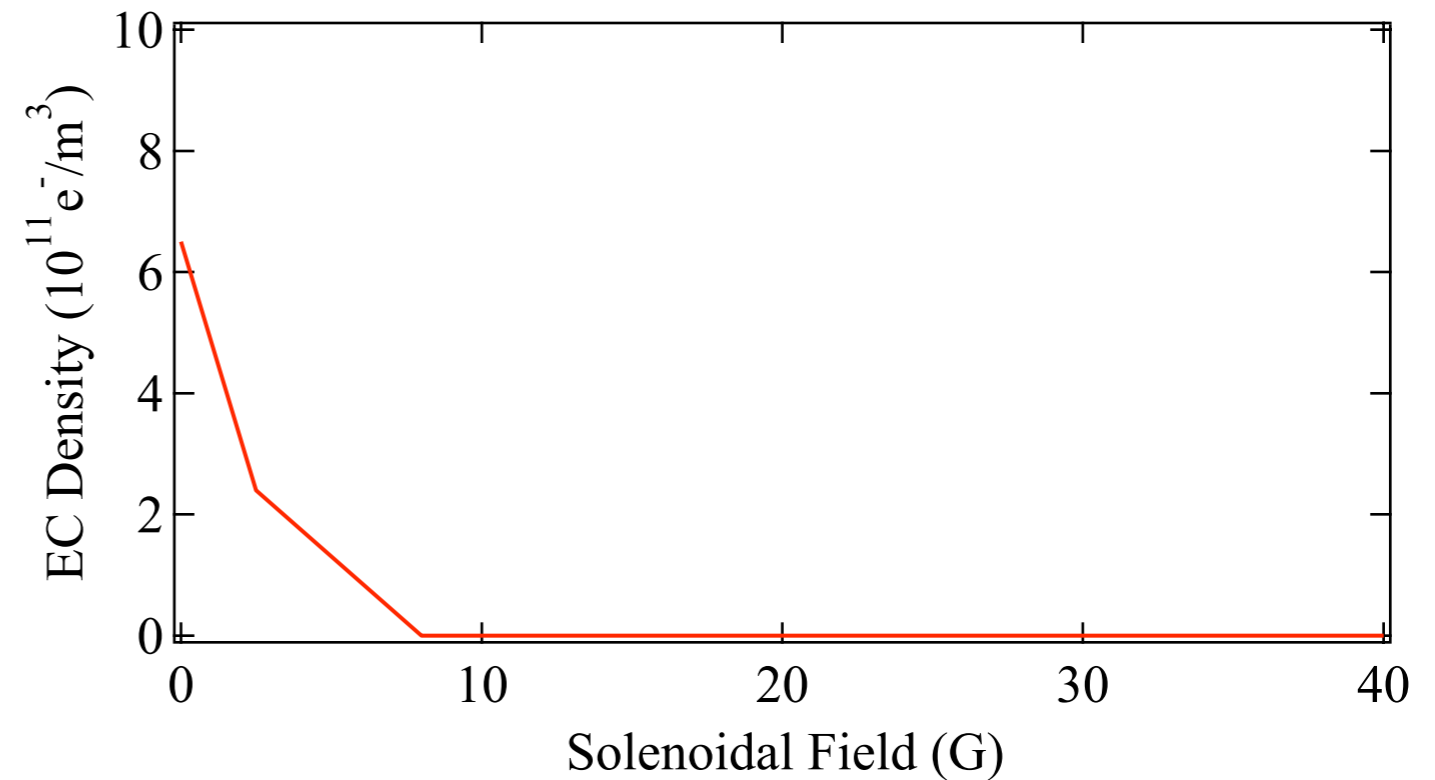
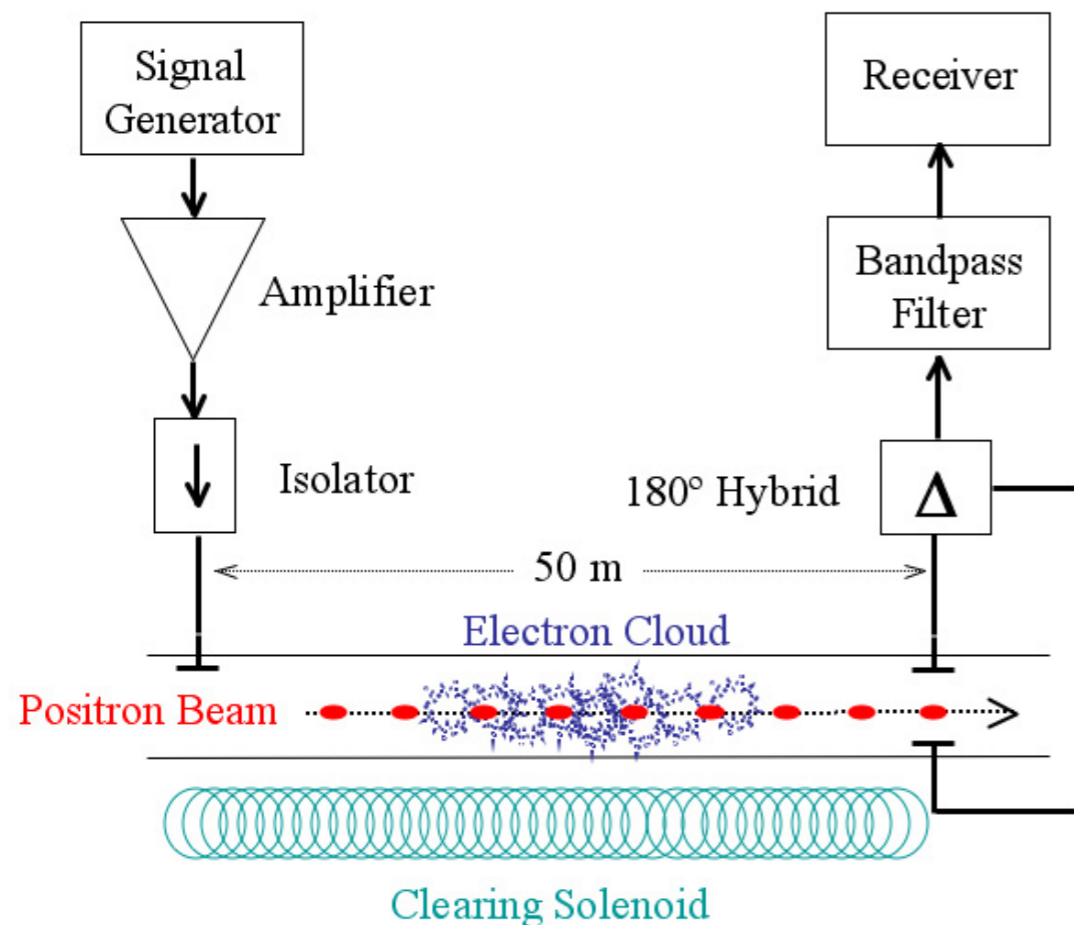
Carrier frequency  $\approx 2.15$ GHz  
Cutoff frequency  $\approx 2$ GHz  
Rev frequency 136 kHz (2.2 km)

Phys. Rev. Lett. 100, 094801 (2008)



# The solenoidal field was used to vary the electron cloud density

bunches  $\sim$  1700 4.2ns apart  
gap length  $\sim$  100ns  
bunch length = 30-40 ps (rms)  
length of transmission = 50m



Estimation of electron cloud using the formula for phase shift (shown earlier) for different solenoidal fields.

# Analysis of phase shift for electrons in a dipole magnetic field is more complex

- The wave propagates through an **anisotropic medium**.
- This can be divided into two components -
  - (1) ordinary or **O-wave** corresponds to the case when the wave electric field is **parallel to the external B field** and
  - (2) extraordinary or **X-wave** - when the wave electric field is **perpendicular to the external B field**
- For the **O-wave**, the external B field plays no role in the wave dynamics. So the **dipole field is never noticed**
- The **X-wave** has some “extraordinary” properties - mainly it leads to a the so called **“upper-hybrid” resonance**.

# “Extraordinary waves”, what we understand

For **open boundaries**, the wave dispersion relation is well known

$$\frac{c^2 k^2}{\omega^2} = 1 - \frac{\omega_p^2 (\omega^2 - \omega_p^2)}{\omega^2 (\omega^2 - \omega_h^2)}$$

where  $\omega_h^2 = \omega_p^2 + \omega_c^2$  is **the upper hybrid frequency**,  
 $\omega_c = eB/m_e$  is the **cyclotron frequency**,  
when  $\omega = \omega_h, k \rightarrow \infty$  we reach **upper hybrid resonance**.

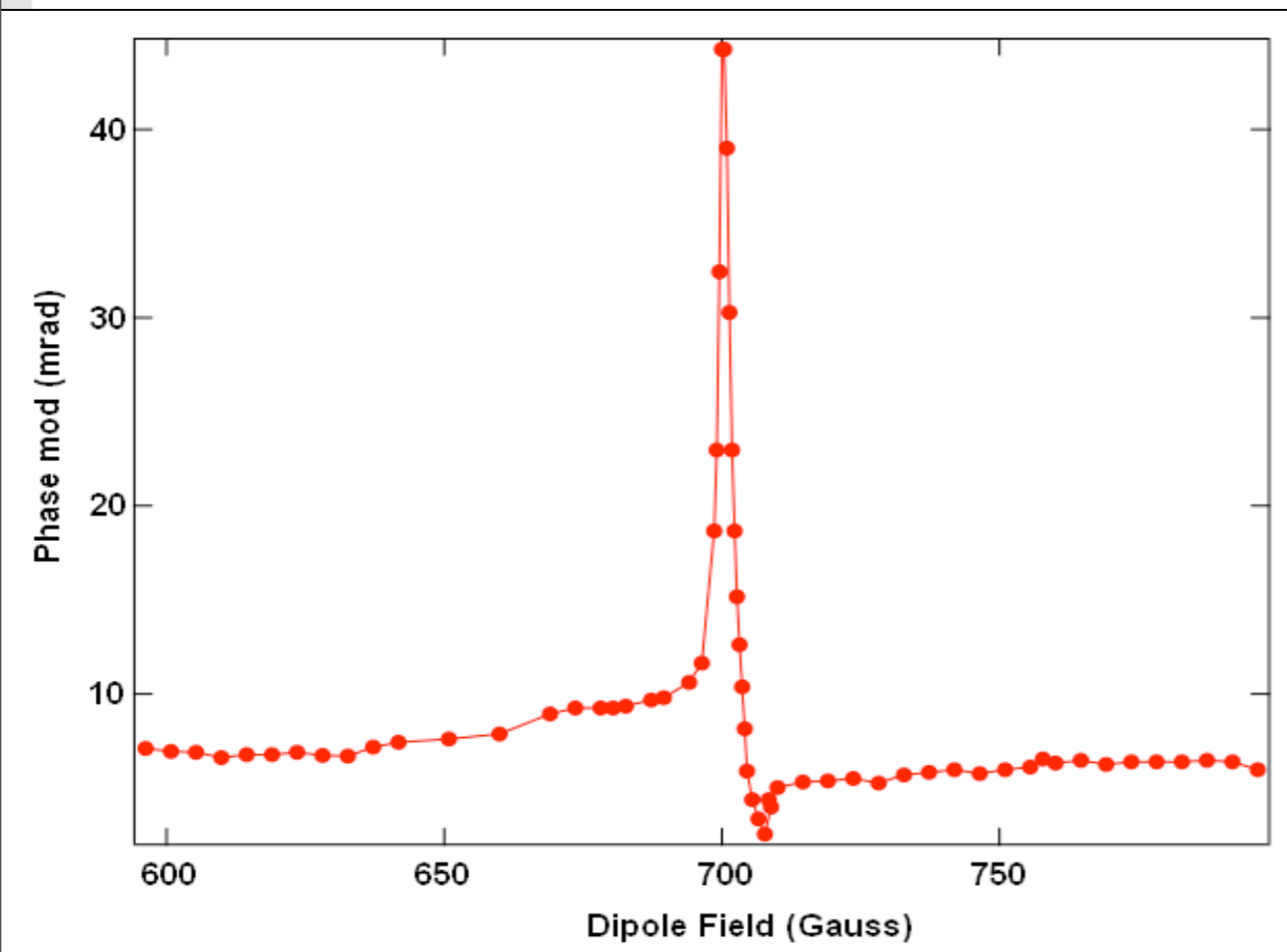
The resonance condition leads, theoretically,  
to an **infinite phase shift**

# “Extraordinary waves”, What we don’t understand yet

- We don’t have a **dispersion relationship** for plasma filled waveguides, **for the dipole field case** as yet.
- It is well known that at upper hybrid resonance, for open boundaries, **the wave E field is parallel k**.
- However, for a **waveguide**, simulations and experiments show the presence of resonance for **pure TE modes**.
- The theory is based on a **linearized, cold fluid model**. To what extent are these approximations valid?
- Even if we do have a dispersion relation, **the X-wave component** will need to be **isolated** from the **O-wave** in measurements before making a fit to the theoretical relationship.

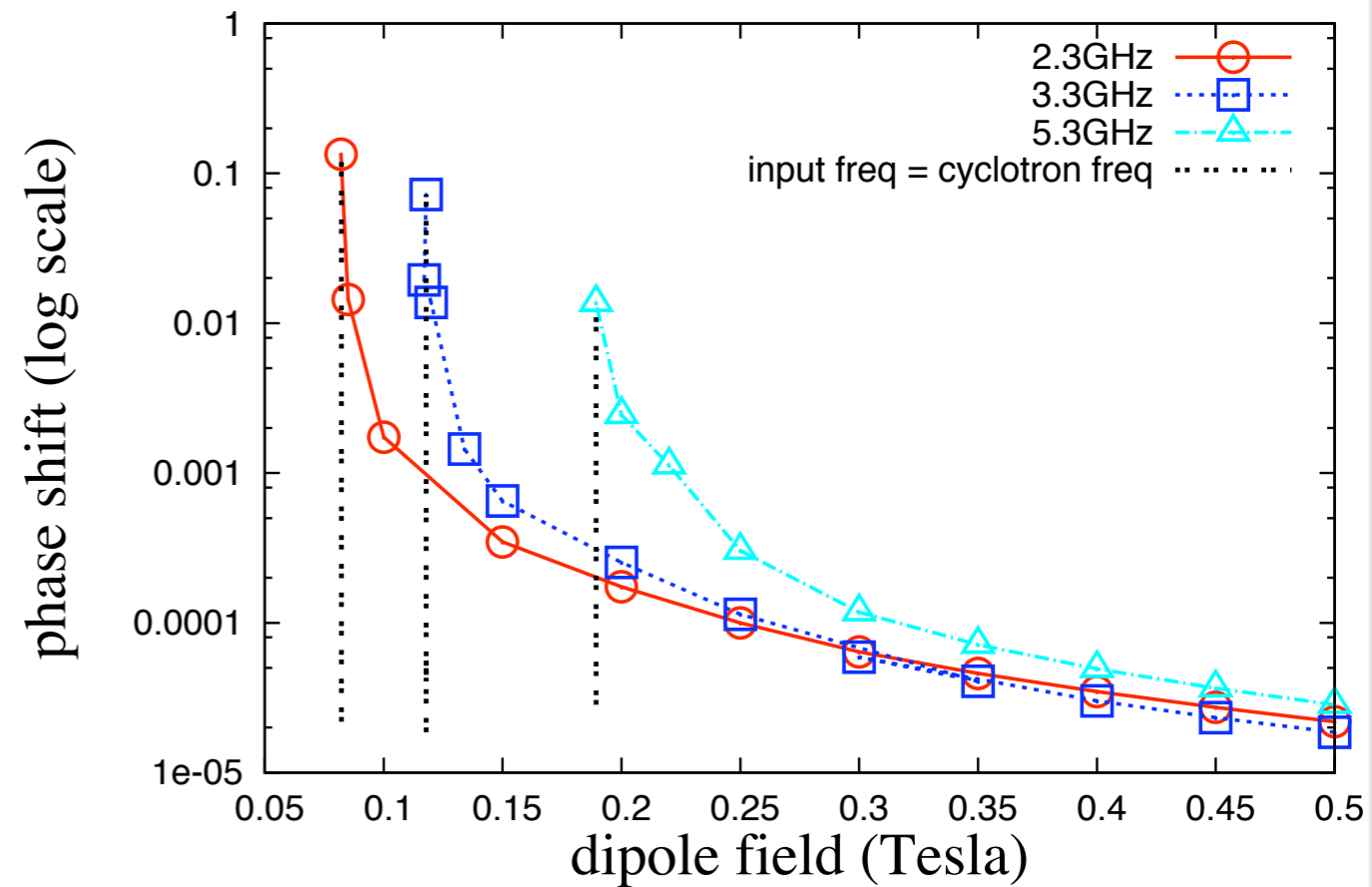
# Simulations and experiments showed the presence of resonance in a dipole field

Large phase shift observed when cyclotron freq = carrier freq



Measured at SLAC PEP II April 3rd '08

phase shift in dipole field

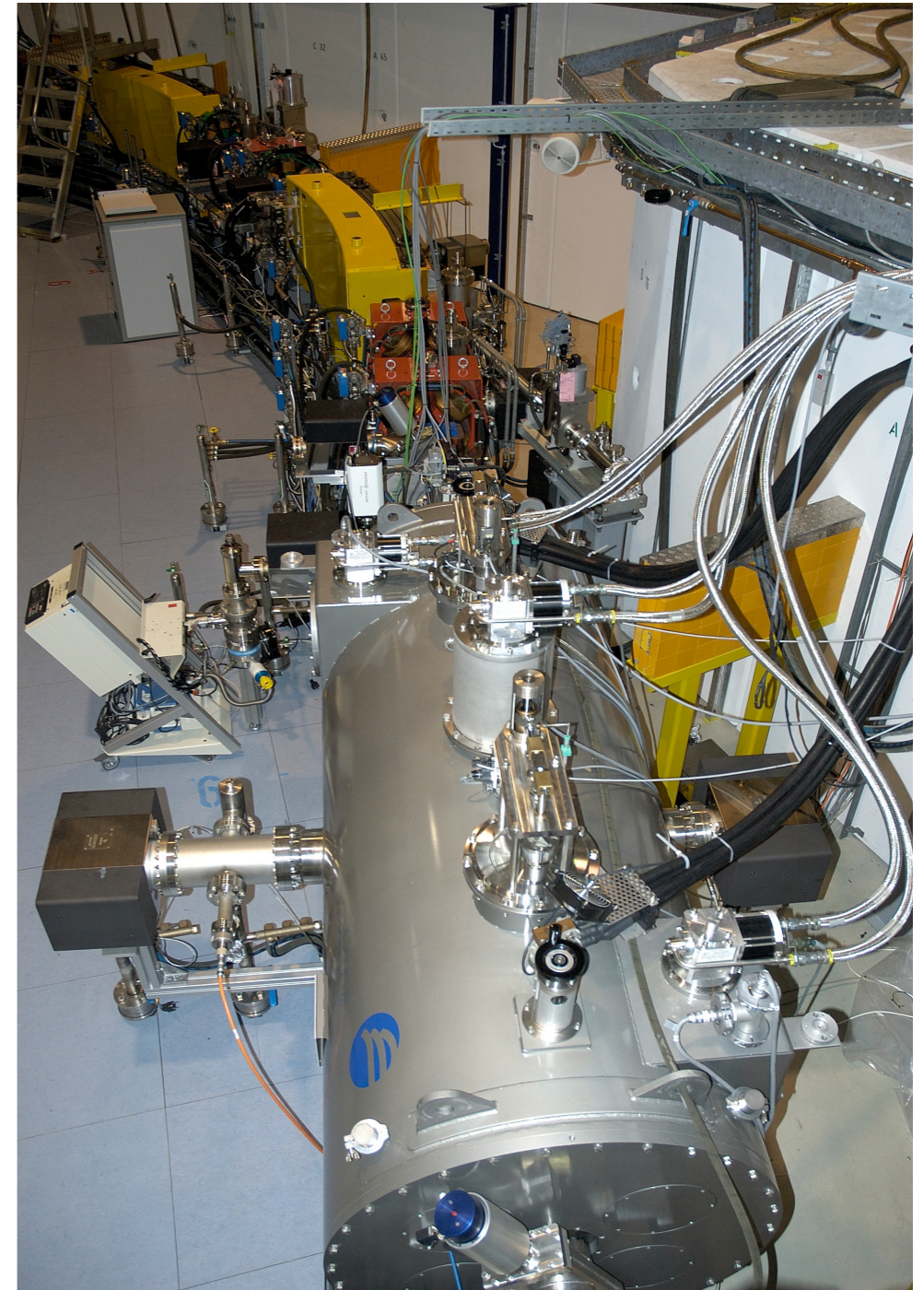
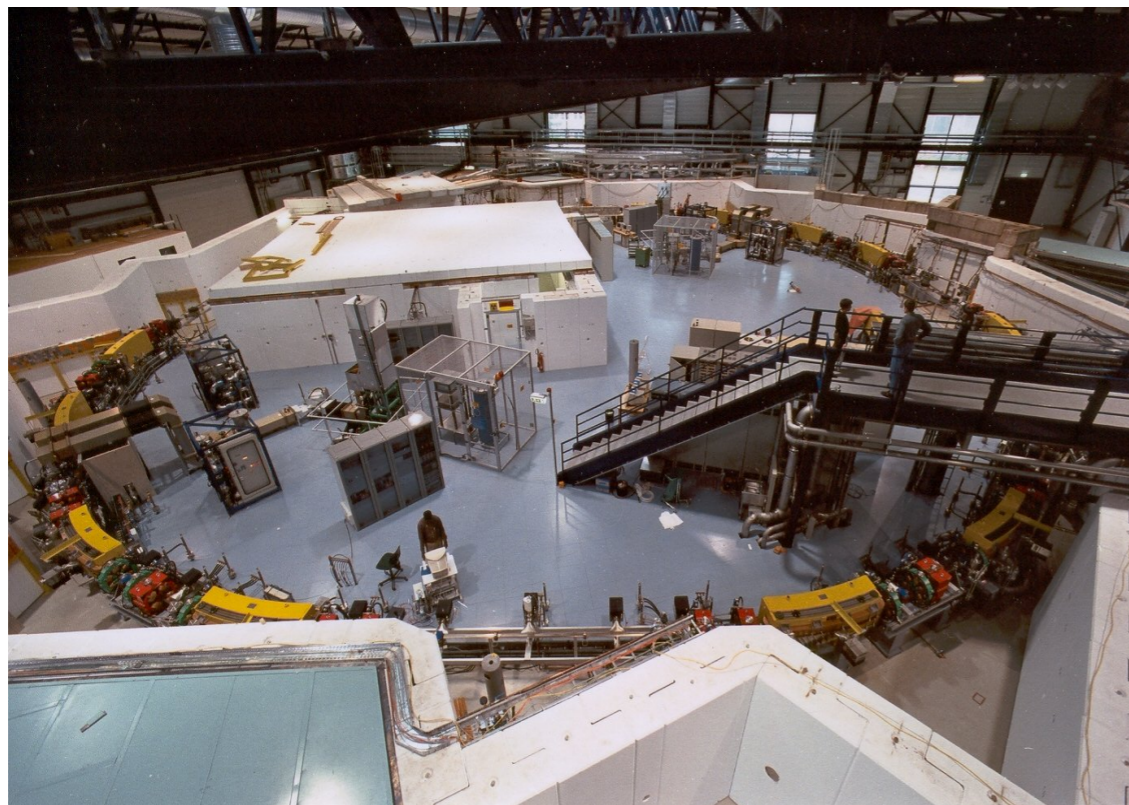


Simulation results using VORPAL

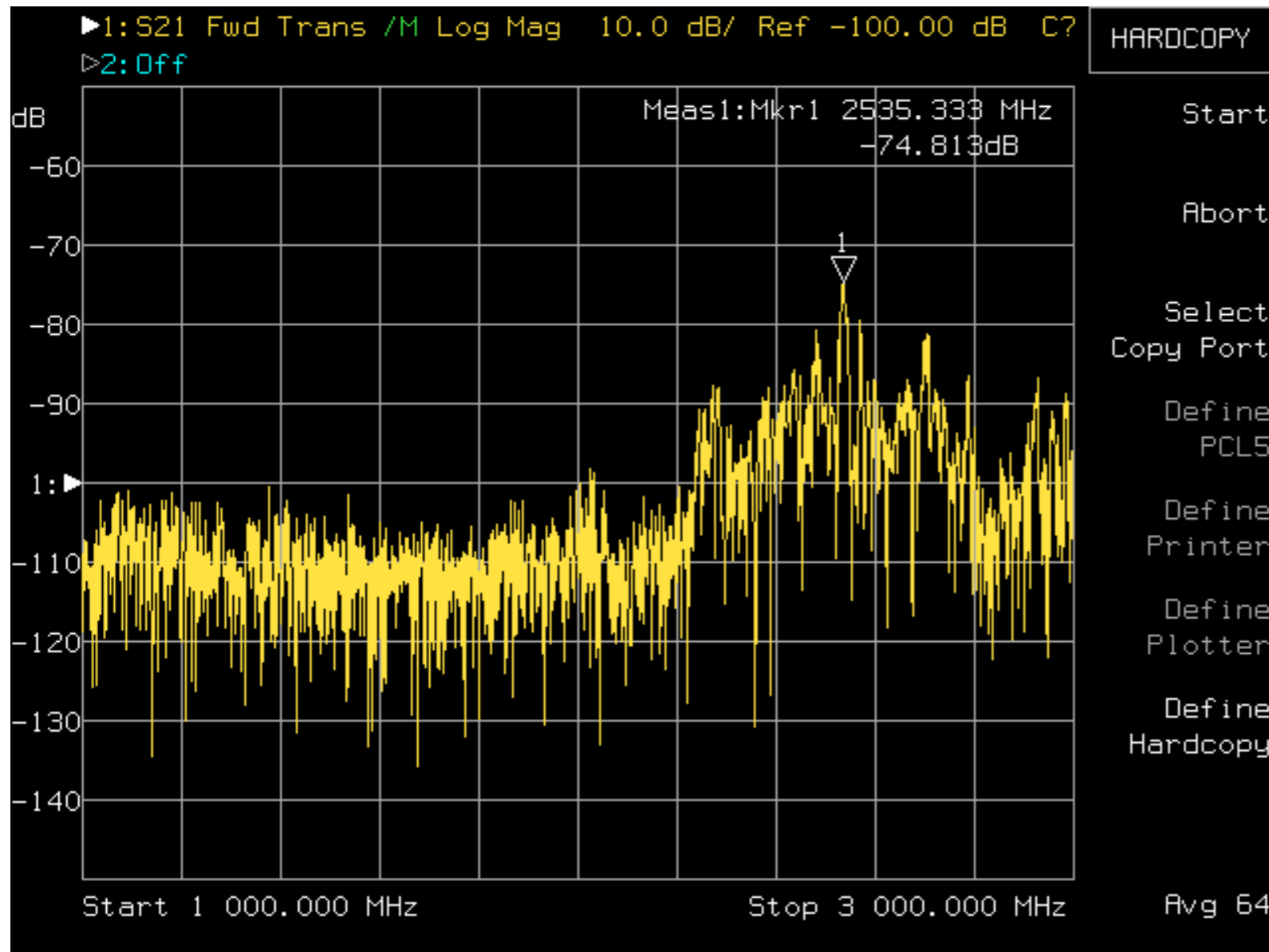
Resonance was seen for **TE waves**  
which means **wave E field  $\perp$  k**  
contradicts theory for open boundaries!

# Electron cloud formation is important for superconducting structures.

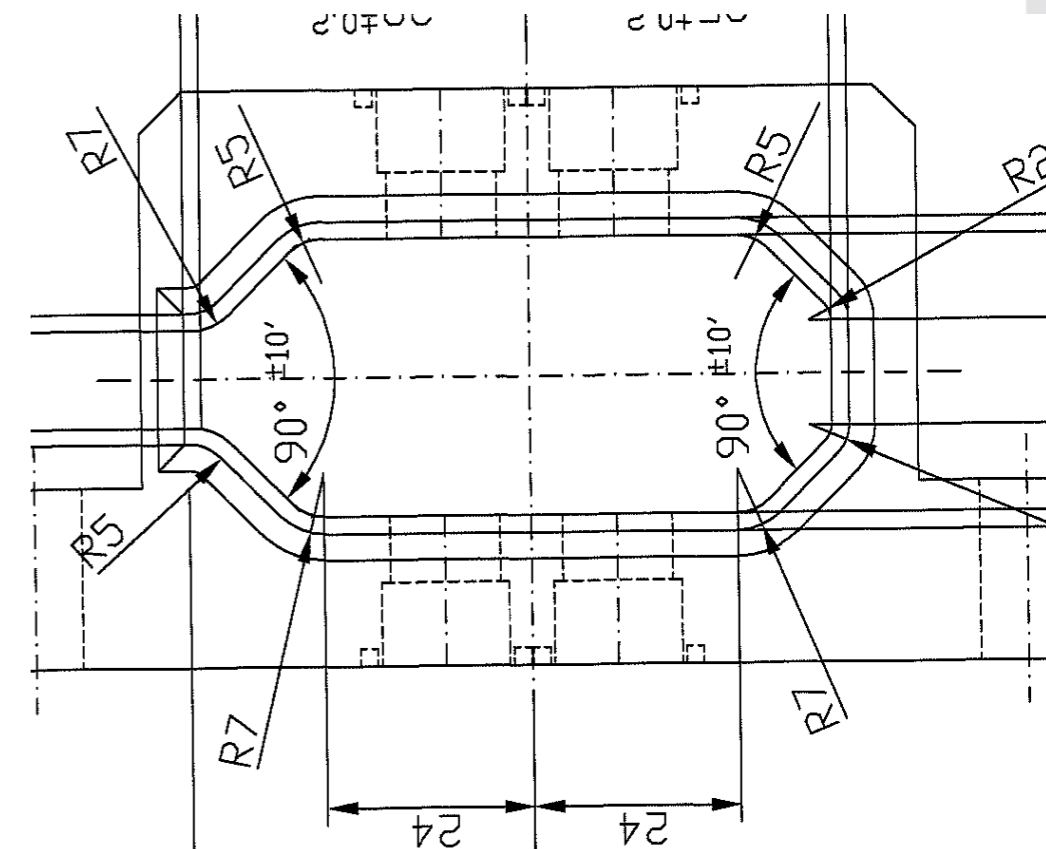
- ➔ The effort would support **superconducting undulator** research (talk by Sara Casalbouni).
- ➔ EClouds will contribute to **heat load**.
- ➔ Our present goal is to make a **qualitative diagnosis** using the microwave technique.
- ➔ Estimations on ECloud buildup for this system have been made (talk by Ubaldo Iriso).



# Transmission of signal currently under study



66.2 cm X 8-16mm



4 BPMs. The one ones on the same side of the chamber were connected and the 2 pairs were used as electrodes. The wave was received on the other end using a similar arrangement

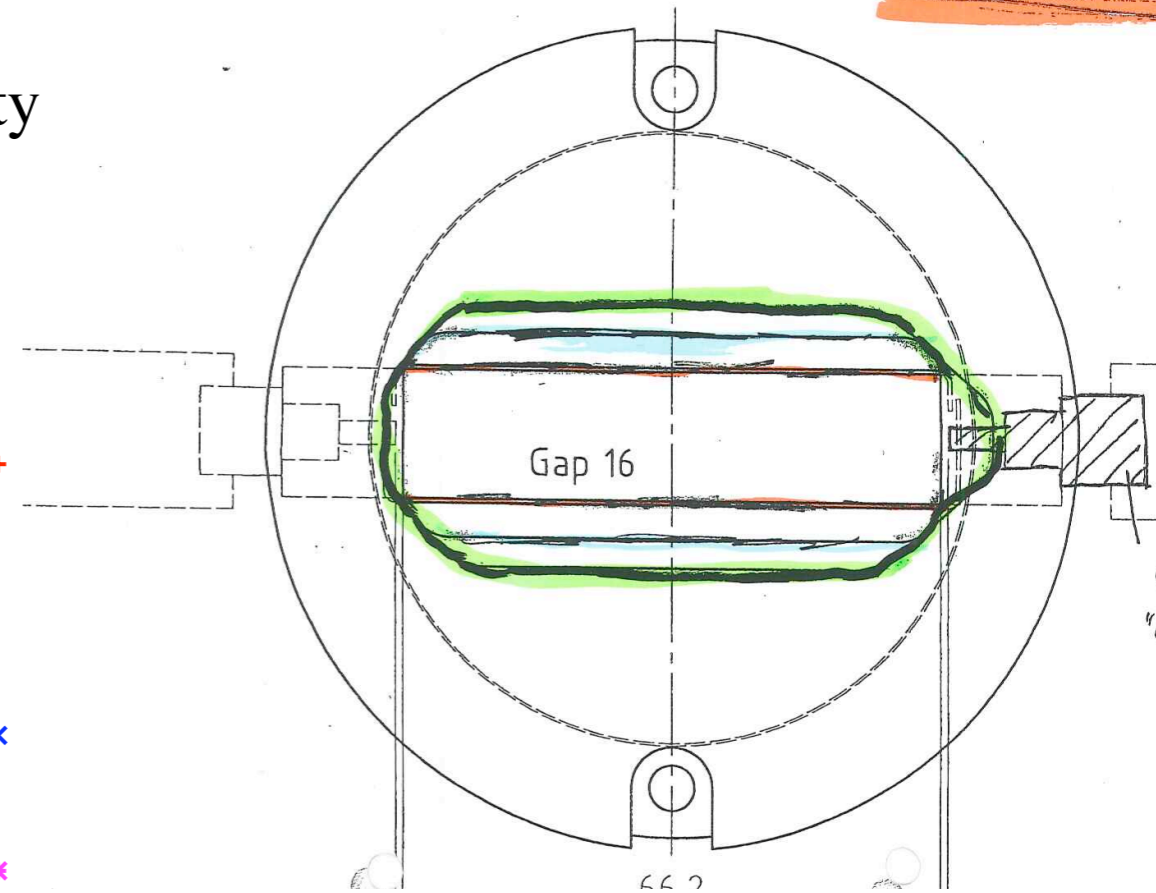
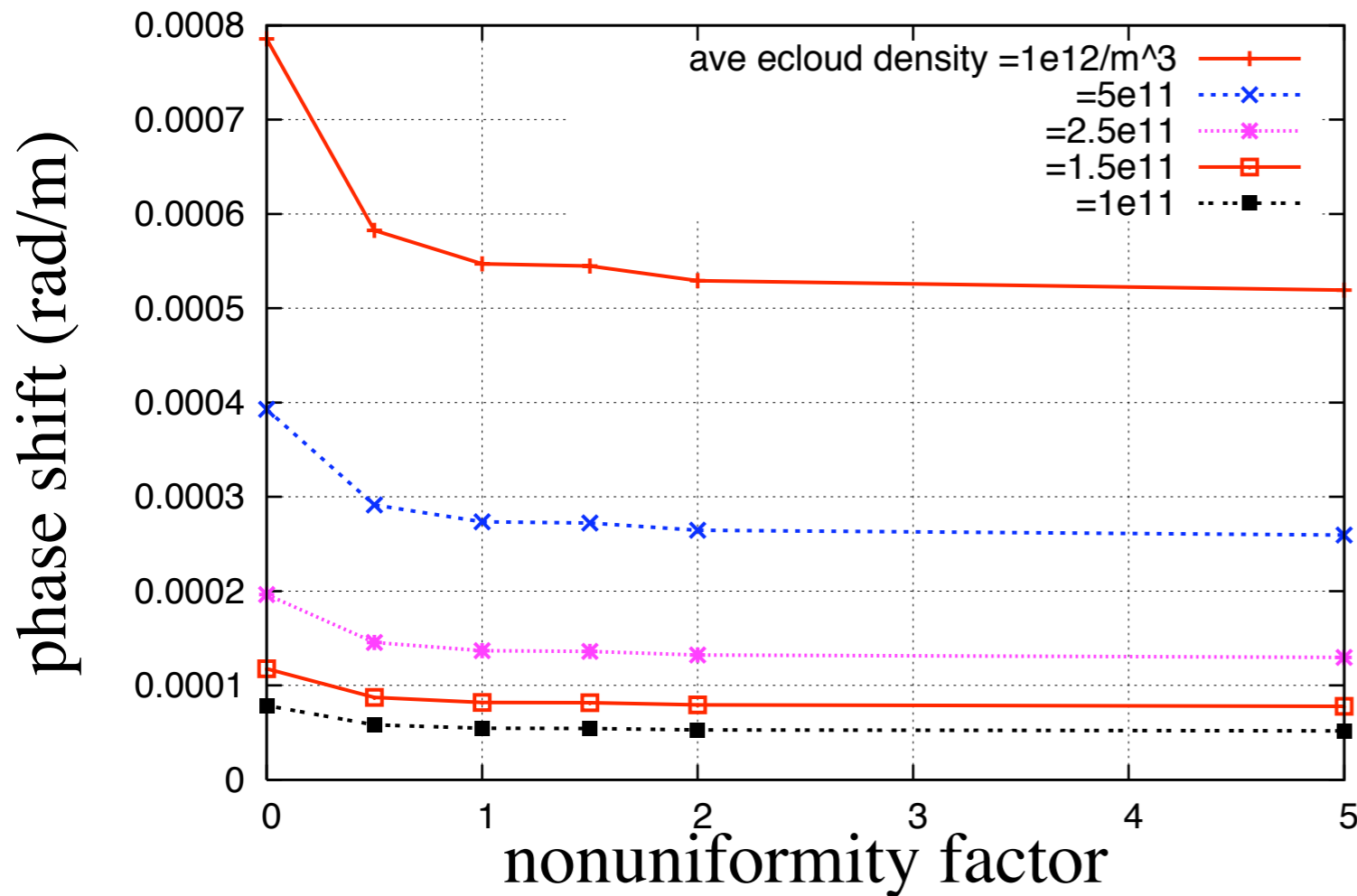
An attempt was made to match the transmission from BPMS into the chamber:  
D. Saez de Jauregui, R. Weigel etc.

# Phase shift does not vanish when electrons are pushed toward the walls

- This is **important for EClouds formed in electron beams** where you may expect this to be the case.
- Simulations were done in the **absence of a magnetic field**.

Kontur E  
 Kontur Eintritt  
 Kontur Kalkula

phase shift vs nonuniformity of electron density



$$\rho(x, y) \sim [1 - \exp(-(x^2 + y^2)/K^2 L^2)] \text{ where } K = \text{"non uniformity factor"}$$



- Analytic expression for phase shift.
- Simulation and analytic results for phase shift.
- Observation of phase shift at SLAC PEP II LER
- Physics associated dipole field : with simulation and experimental results.
- Motivation of this study at ANKA.
- Study of transmission across the undulator chamber.
- Simulated phase shift for different transverse distributions of electrons.