

# Top quark spin correlations in theories with large extra dimensions at LHC

Karel Smolek

Czech Technical University in Prague, IEAP

Masato Arai, Nobuchika Okada, Vladislav Šimák

# Decay of top quark

$$t \rightarrow b + W^+ \quad - 98.8 \%$$

$$W^+ \rightarrow \begin{cases} \bar{d} + u \\ \bar{s} + c \\ \dots \end{cases} \quad \left. \vphantom{W^+} \right\} 67.6 \%$$

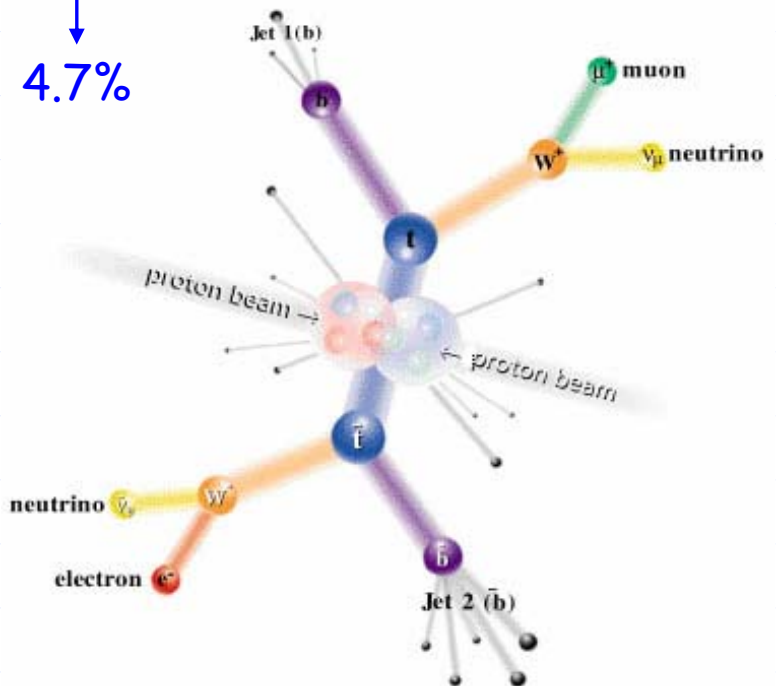
$$\begin{cases} e^+ + \nu_e \\ \mu^+ + \nu_\mu \end{cases} \quad \left. \vphantom{e^+} \right\} 21.6 \%$$

$$\tau^+ + \nu_\tau \quad - 10.8 \%$$

$$\tau^+ \rightarrow \begin{cases} e^+ + \nu_e + \nu_\tau \\ \mu^+ + \nu_\mu + \nu_\tau \end{cases} \quad \left. \vphantom{\tau^+} \right\} 35.2 \%$$

...

$$\begin{aligned} t &\rightarrow b + W^+ \rightarrow e^+ + \nu \\ \bar{t} &\rightarrow \bar{b} + W^- \rightarrow e^- + \bar{\nu} \end{aligned}$$



# Polarization of top quark

It is possible to study the polarization of top quark using the decay products:

$$\frac{1}{N} \frac{dN}{d\cos\theta_f} = \frac{1}{2}(1 + \alpha_f \cos\theta_f)$$

The angle between the direction of particle  $f$  in the top rest frame and the direction of top quark spin.

-0.41 for b  
0.41 for  $W^+$   
0.35 for jet  
**1.0** for  $e^+, \mu^+$

- At LHC top (antitop) quarks are produced as the helicity eigenstates.
- Top and antitop quarks are produced as unpolarized – the same number of left- and right-handed top quarks.

# Spin correlation of top-antitop pairs

The number of  $t\bar{t}$  pairs with the same and opposite helicity is not the same.

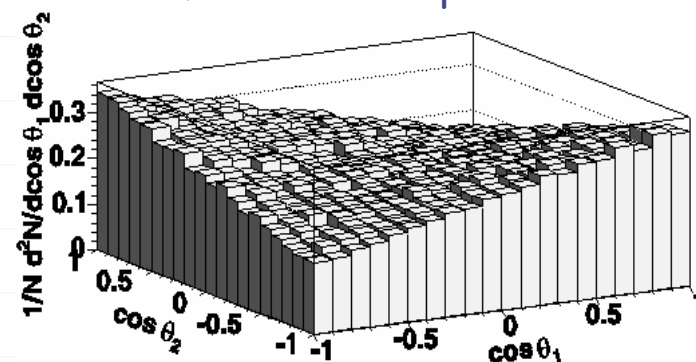
$$A = \frac{\sigma(t_{\uparrow}\bar{t}_{\uparrow}) + \sigma(t_{\downarrow}\bar{t}_{\downarrow}) - \sigma(t_{\uparrow}\bar{t}_{\downarrow}) - \sigma(t_{\downarrow}\bar{t}_{\uparrow})}{\sigma(t_{\uparrow}\bar{t}_{\uparrow}) + \sigma(t_{\downarrow}\bar{t}_{\downarrow}) + \sigma(t_{\uparrow}\bar{t}_{\downarrow}) + \sigma(t_{\downarrow}\bar{t}_{\uparrow})} \neq 0$$

The double differential angular distribution of top and anti-top decay products:

$$\frac{1}{N} \frac{d^2 N}{d\cos\theta_f d\cos\theta_{\bar{f}}} = \frac{1}{4} (1 - A \underbrace{|\alpha_f \alpha_{\bar{f}}|}_{=1 \text{ for double-lepton channel}} \cos\theta_f \cos\theta_{\bar{f}})$$

SM prediction:

$$A = 0.319$$



# Measurement of top-antitop spin correlation in the ATLAS experiment

- F. Hubaut, E. Monnier, P. Pralavorio, K. Smolek, V. Šimák: *ATLAS sensitivity to top quark and W boson polarization in ttbar events*, Eur.Phys.J. C44 (2005) 13-33.
- Semileptonic and dileptonic ttbar channels.
- At LHC, it is possible to increase the asymmetry by applying an upper cut on the ttbar invariant mass:

$$M_{t\bar{t}} < 550 \text{ GeV}/c^2$$



$$A = 0.422$$

- Combining the results of both channels allow to measure the SM spin correlation  $A$  with a 4% precision for  $10 \text{ fb}^{-1}$ .

# ADD model

- Theory with  $n$  extra-dimensions compactified with large radii.

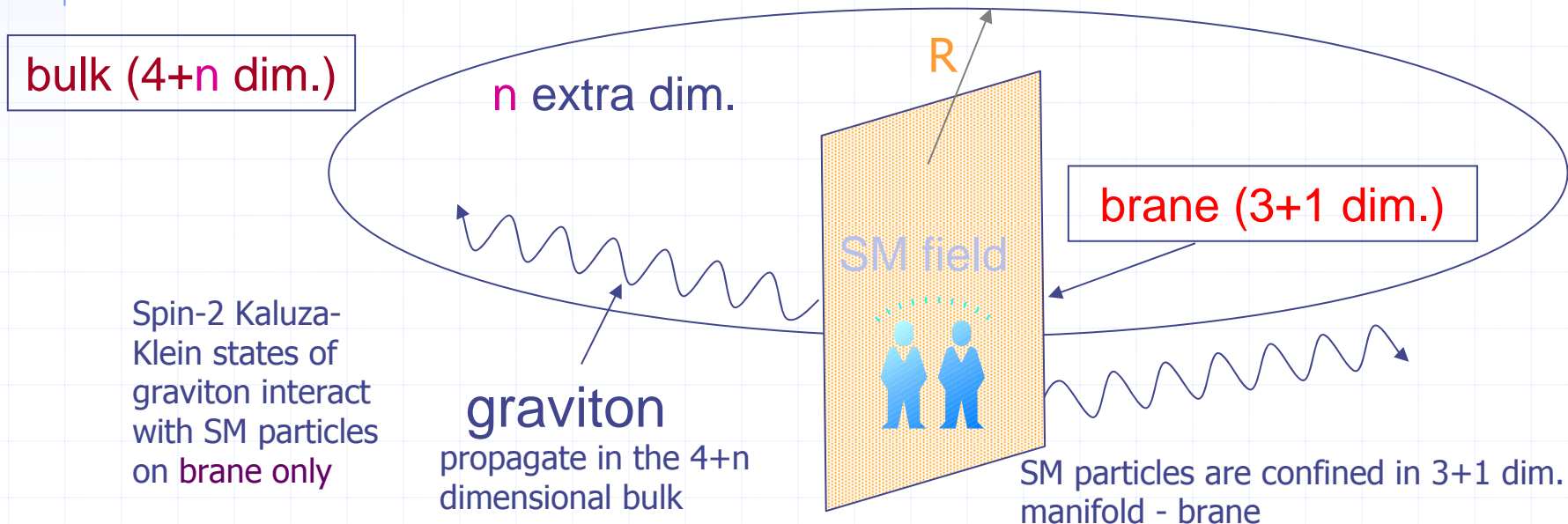
N. Arkani-Hamed, et al, PLB429 (1998) 263, hep-ph/9803315

I. Antoniadis, et al, PLB436 (1998) 257, hep-ph/9804398

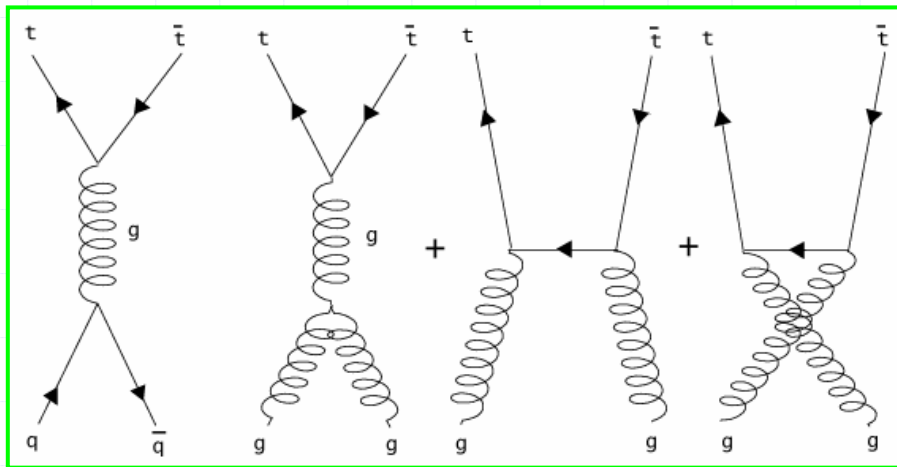
$$M_{\text{PL}}^2 = M_{\text{D}}^{n+2} R^n$$

$M_{\text{D}}$  = low-energy effective string scale ( $\sim 1$  TeV)

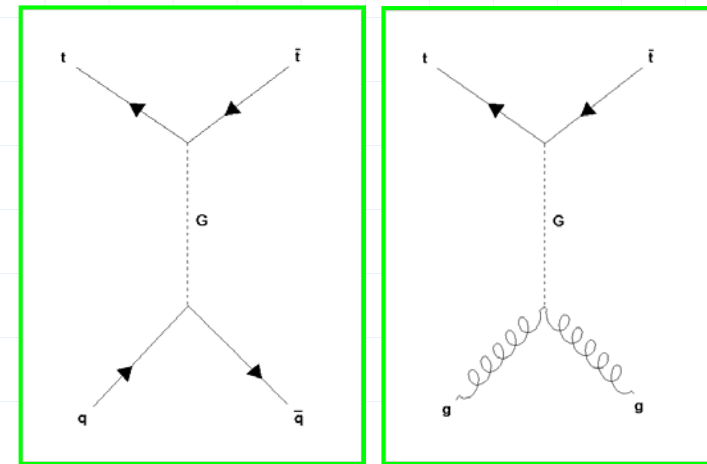
Např.  $M_{\text{D}}=1\text{TeV}$ ,  $M_{\text{PL}} = 10^{19}$  GeV,  $R \sim 1$  mm ( $0.001 \cdot 10^{-19}$  GeV $^{-1}$ ),  $n = 2$



# ADD model and top-antitop production at LHC



SM contribution



KK states contribution

2 free parameters:

- $M_D$  - low-energy effective string scale
- $\lambda = \pm 1$  - connected to the regularization procedure for the contributions from the infinite number of KK gravitons.  $\lambda$  represents the sign of the interference term between SM and ADD contribution in the  $gg \rightarrow t\bar{t}$  process.

# ttbar production cross section

- Full density matrix:

M. Arai, N. Okada, K. Smolek, V. Šimák: Phys.Rev. D70 (2004) 115015

$$|\mathcal{M}(q\bar{q} \rightarrow t_{\uparrow}\bar{t}_{\uparrow})|^2 = |\mathcal{M}(q\bar{q} \rightarrow t_{\downarrow}\bar{t}_{\downarrow})|^2 = \frac{g^4}{9}(1 - \beta^2) \sin^2 \theta + \frac{f_G s^4 \beta^2}{2}(1 - \beta^2) \sin^2 2\theta,$$

$$|\mathcal{M}(q\bar{q} \rightarrow t_{\uparrow}\bar{t}_{\downarrow})|^2 = |\mathcal{M}(q\bar{q} \rightarrow t_{\downarrow}\bar{t}_{\uparrow})|^2 = \frac{g^4}{9}(1 + \cos^2 \theta) + \frac{f_G s^4 \beta^2}{2}(\cos^2 2\theta + \cos^2 \theta)$$

$$|\mathcal{M}(gg \rightarrow t_{\uparrow}\bar{t}_{\uparrow})|^2 = |\mathcal{M}(gg \rightarrow t_{\downarrow}\bar{t}_{\downarrow})|^2 = \frac{g^4 \beta^2}{96} \mathcal{Y}(\beta, \cos \theta)(1 - \beta^2)(1 + \beta^2 + \beta^2 \sin^4 \theta) \\ + \mathcal{Z}(\beta, \theta, s) f_G s^2 \beta^2 (1 - \beta^2) \sin^4 \theta$$

$$|\mathcal{M}(gg \rightarrow t_{\uparrow}\bar{t}_{\downarrow})|^2 = |\mathcal{M}(gg \rightarrow t_{\downarrow}\bar{t}_{\uparrow})|^2 = \frac{g^4 \beta^2}{96} \mathcal{Y}(\beta, \cos \theta)(1 + \cos^2 \theta) \\ + \mathcal{Z}(\beta, \theta, s) f_G s^2 \beta^2 \sin^2 \theta (1 + \cos^2 \theta)$$

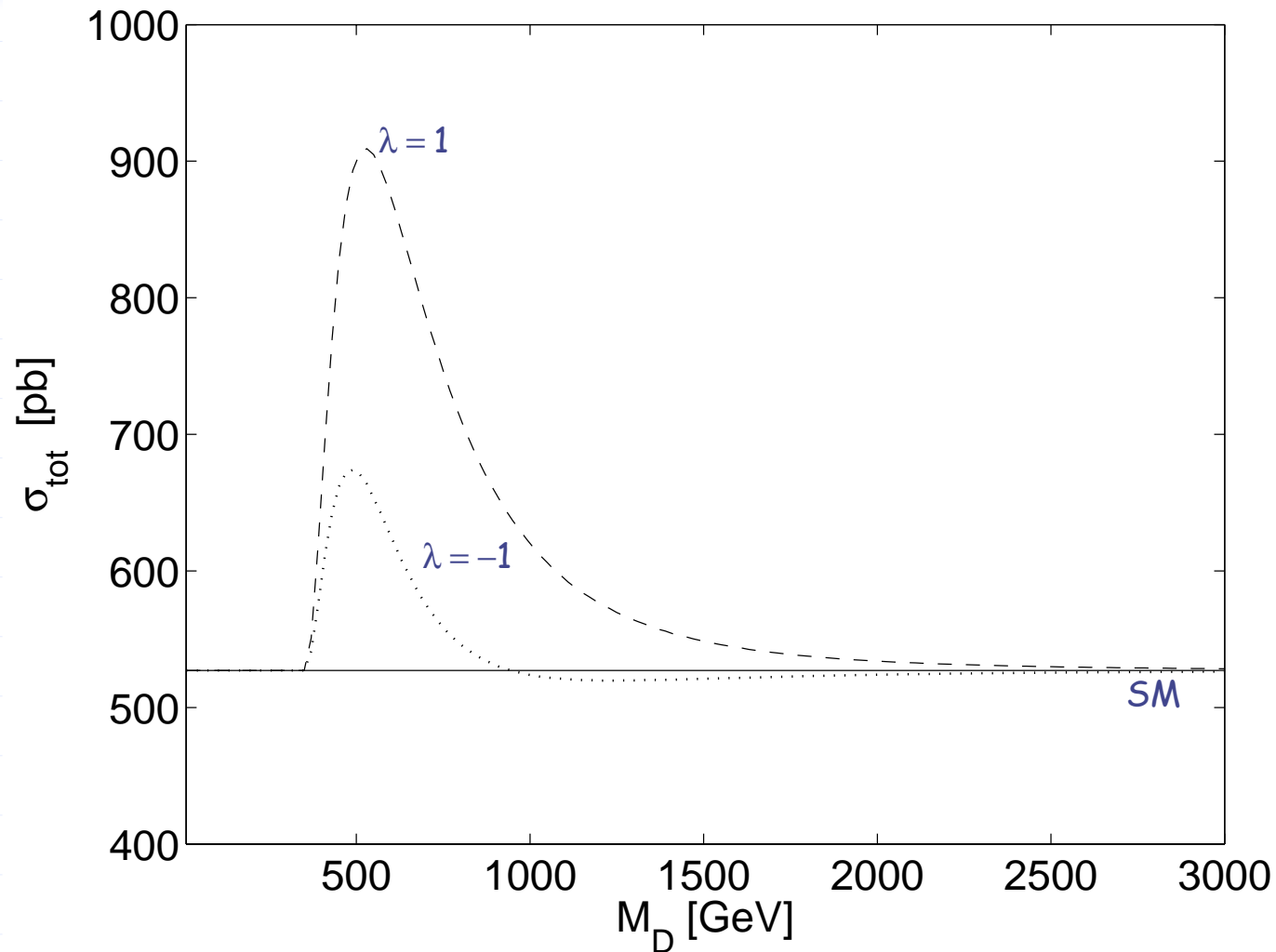
$$\mathcal{Y}(\beta, \cos \theta) = \frac{7 + 9\beta^2 \cos^2 \theta}{(1 - \beta^2 \cos^2 \theta)^2} \quad \mathcal{Z}(\beta, \theta, s) = \frac{g^2}{4(1 - \beta^2 \cos^2 \theta)} + \frac{3}{4} f_G s^2$$

$$f_G \equiv \pi \lambda / 2M_D^4 \quad \lambda = \pm 1$$

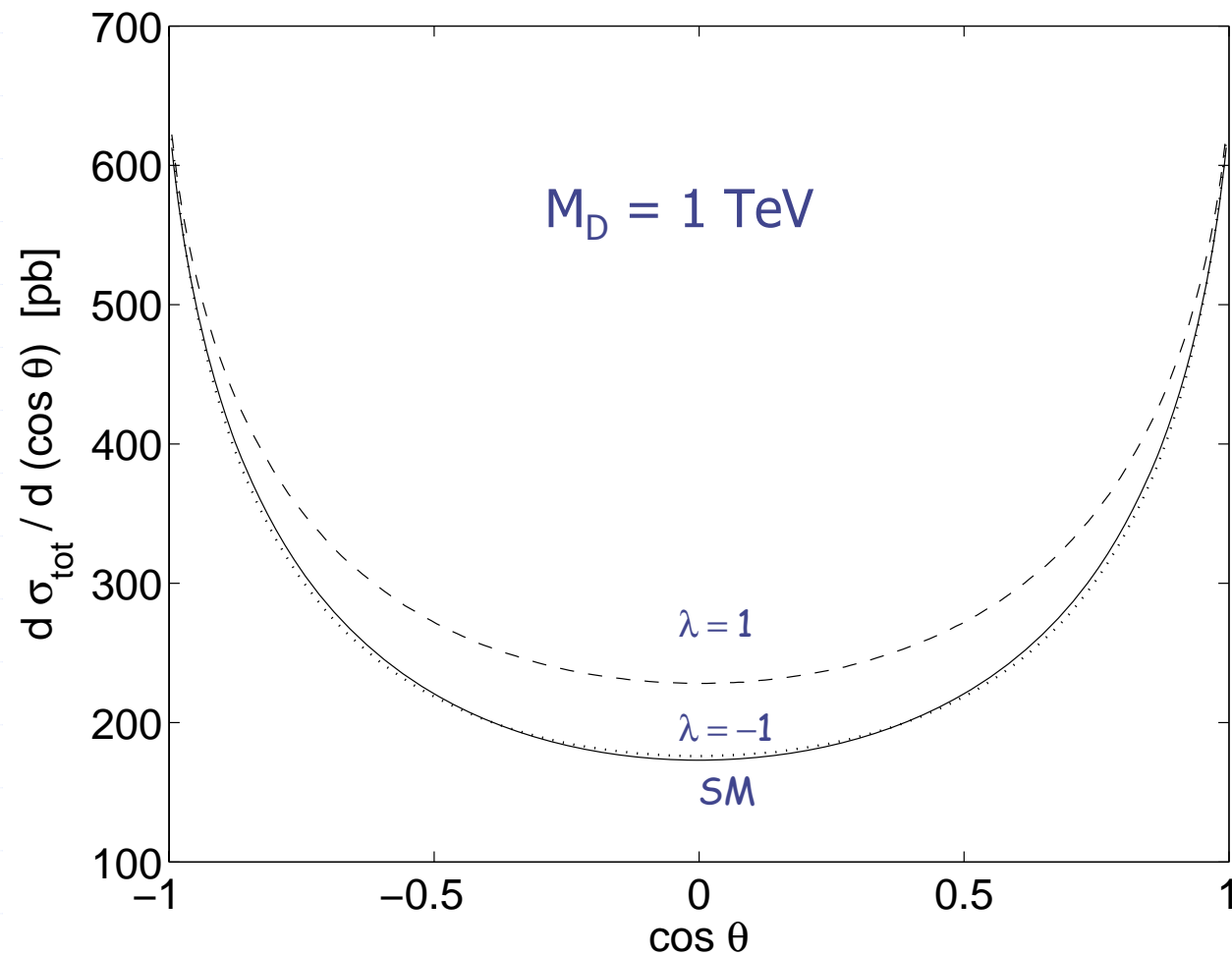
$$\sqrt{s} < M_D$$



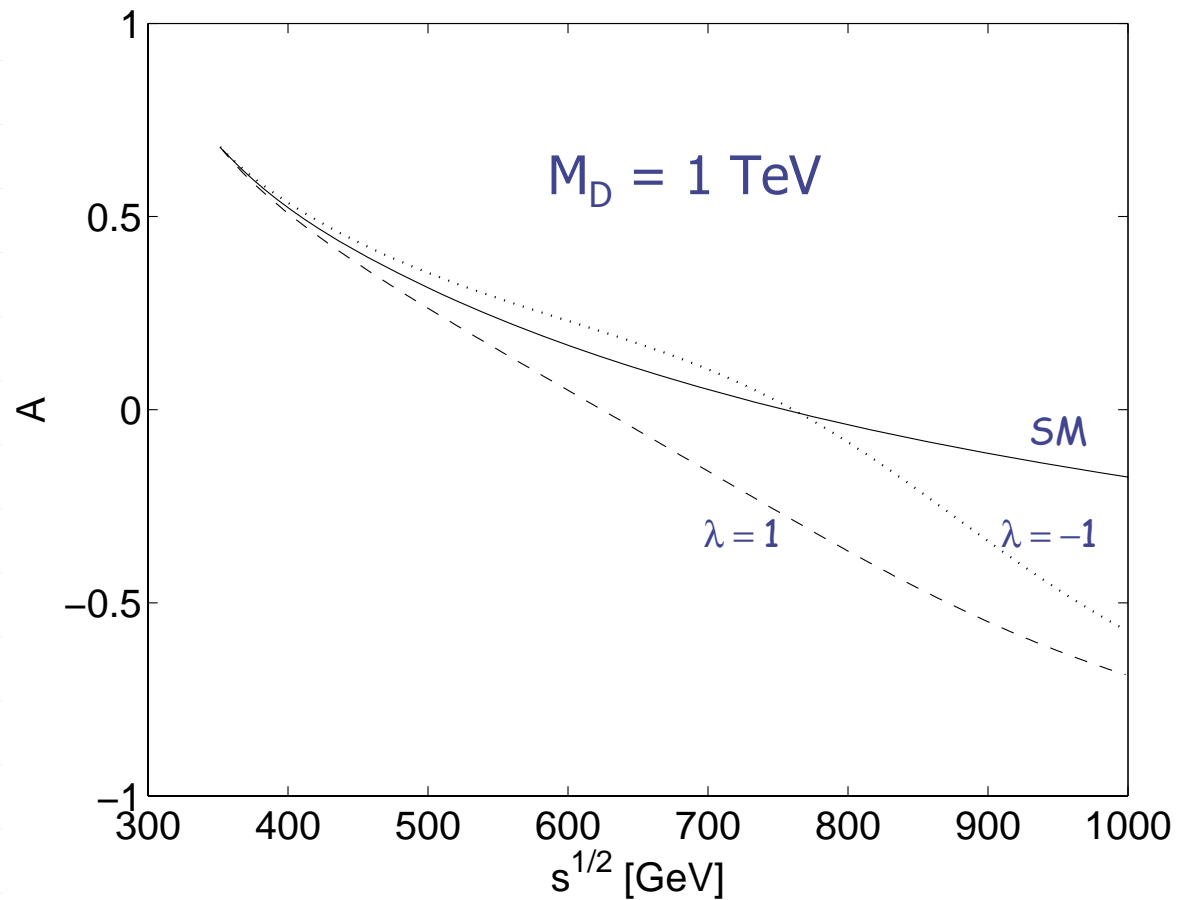
# ttbar production cross section



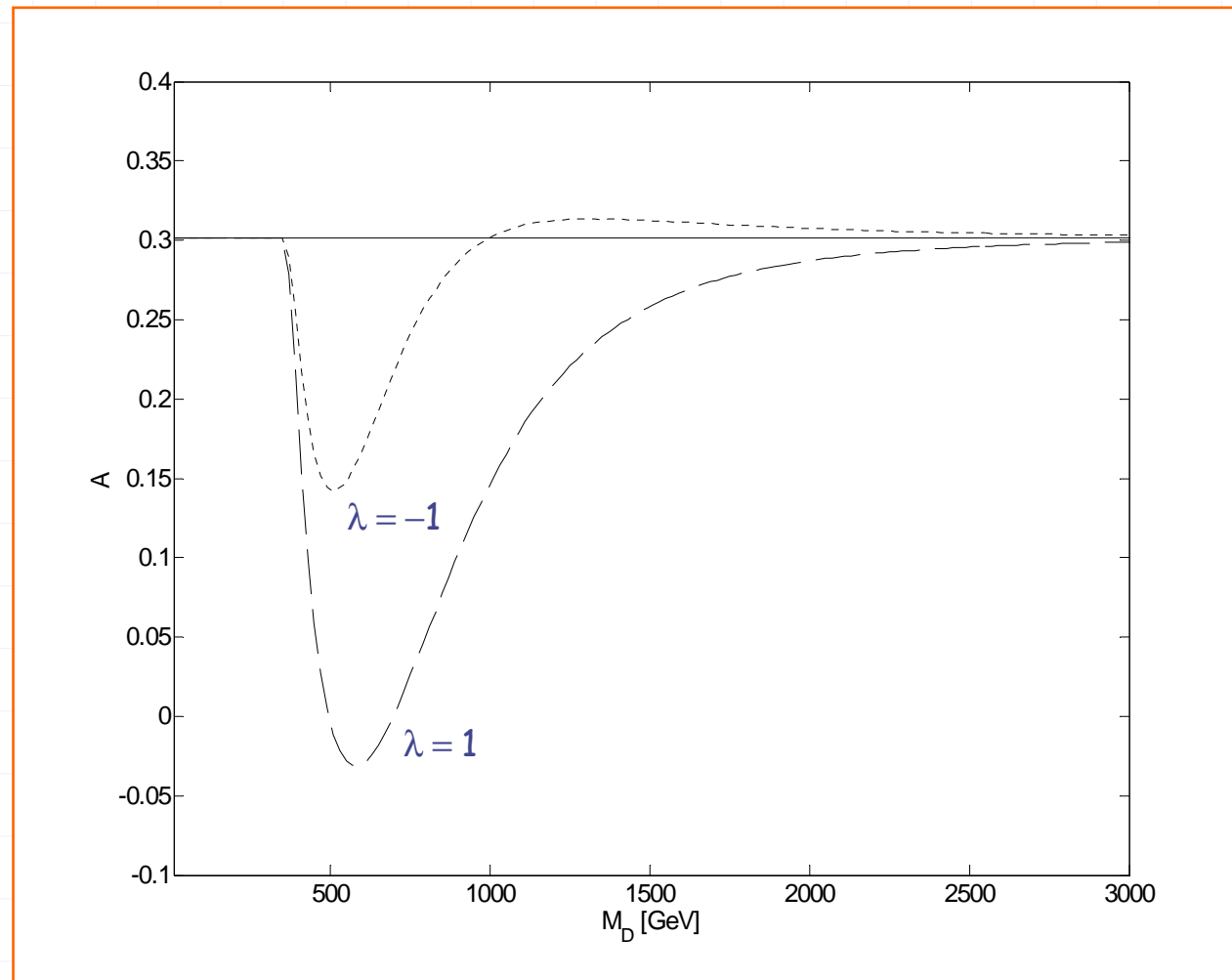
# Angular distribution of the top quark



# ADD model and spin correlation of top quarks at LHC



# ADD model and spin correlation of top quarks at LHC



# Conclusions

- Because of its high mass, the top quark is an ideal place to search for physics beyond the SM.
- The ADD model with large extra dimensions is an example of such physics.
- In addition to cross section and various angular distributions, the spin correlation is sensitive to the existence of large extra dimensions.
- The influence of extra-dimensions on the spin correlation of top-antitop quarks could be visible at the LHC in the case the effective scale  $M_D$  is lower than  $\sim 1.5-2$  TeV.



**Thank you for your  
attention**