



# Models leading to Non-Standard Neutrino Interactions

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Based on collaborations with:

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B. Gavela and J. López Pavón



## Introduction: NSI

Generic new physics affecting  $\nu$  oscillations can be parameterized as 4-fermion **Non-Standard Interactions**:

Production or detection of a  $\nu_\beta$  associated to a  $l_\alpha$

$$2\sqrt{2}G_F \varepsilon_{\alpha\beta} (\bar{\nu}_\beta \gamma^\mu P_L l_\alpha) (\bar{f} \gamma_\mu P_{L,R} f')$$

So that  $|\nu_\alpha\rangle = |\nu_\alpha\rangle + \sum_{\beta=e,\mu,\tau} \varepsilon_{\alpha\beta} |\nu_\beta\rangle$

$$\pi \rightarrow \mu + \nu_\alpha \quad n + \nu_\alpha \rightarrow p + l_\beta$$



## Introduction: NSI

Non-Standard  $\nu$  scattering off matter can also be parameterized as 4-fermion **Non-Standard Interactions**:

$$2\sqrt{2}G_F \varepsilon_{\alpha\beta}^m (\bar{\nu}_\beta \gamma^\mu P_L \nu_\alpha) (\bar{f} \gamma_\mu P_{L,R} f)$$

so that  $\tilde{V}_{\text{MSW}} = a_{\text{CC}} \begin{pmatrix} 1 + \varepsilon_{ee}^m & \varepsilon_{e\mu}^m & \varepsilon_{e\tau}^m \\ \varepsilon_{e\mu}^{m*} & \varepsilon_{\mu\mu}^m & \varepsilon_{\mu\tau}^m \\ \varepsilon_{e\tau}^{m*} & \varepsilon_{\mu\tau}^{m*} & \varepsilon_{\tau\tau}^m \end{pmatrix}$

$$\nu_\alpha \rightarrow \nu_\beta \text{ in matter } f = e, u, d$$



## Direct bounds on matter NSI

If matter NSI are uncorrelated to production and detection direct bounds are mainly from  $\nu$  scattering off  $e$  and nuclei

$$2\sqrt{2}G_F \varepsilon_{\alpha\beta}^m (\bar{\nu}_\beta \gamma^\mu P_L \nu_\alpha) (\bar{f} \gamma_\mu P_{L,R} f)$$

$$|\varepsilon^m| < \begin{pmatrix} 0.6 & \mathbf{0.1} & 0.5 \\ \mathbf{0.1} & 0.015 & 0.05 \\ 0.5 & 0.05 & 6 \end{pmatrix}$$

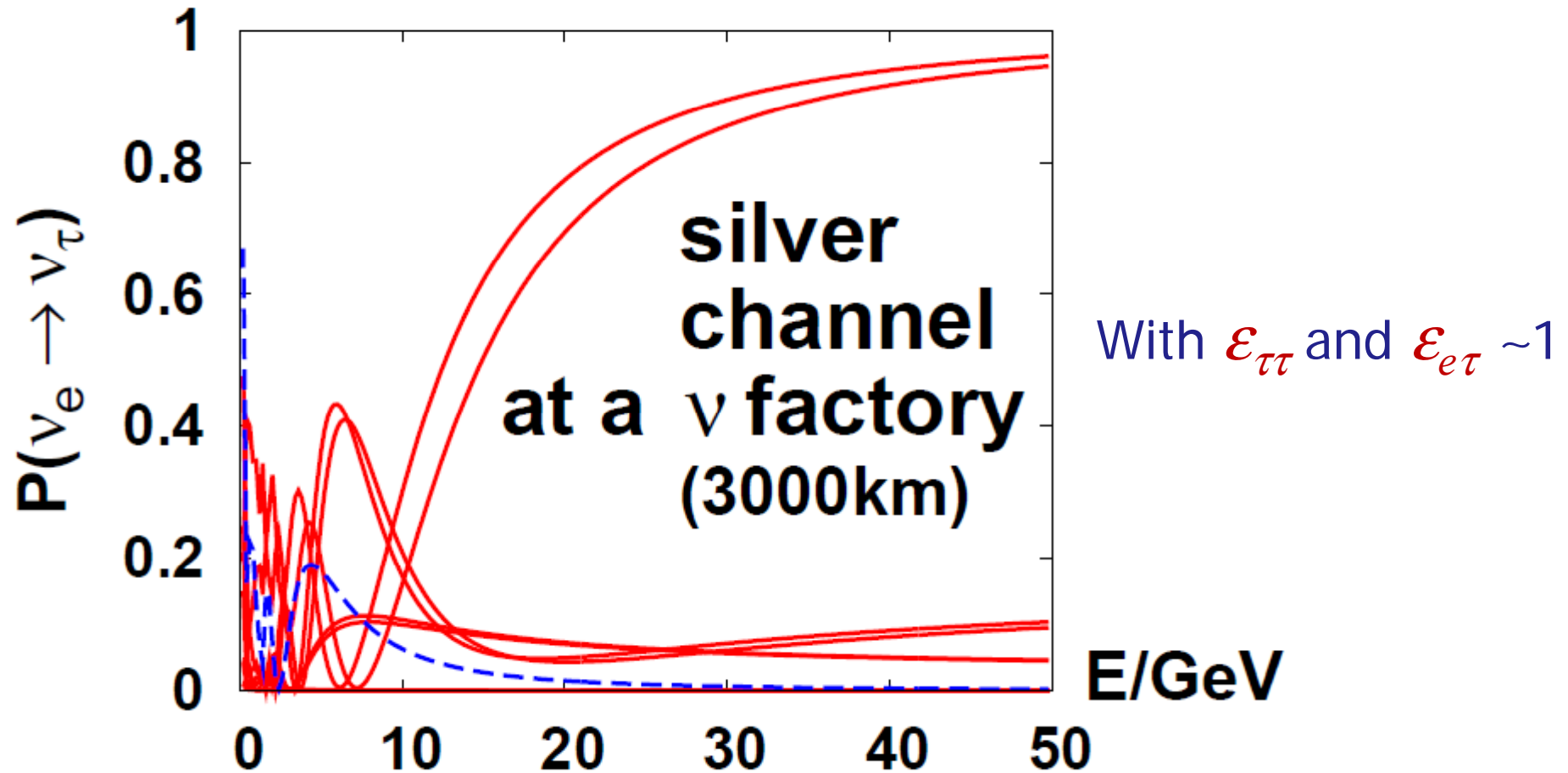
Rather weak bounds...

...can they be saturated avoiding additional constraints?

- S. Davidson, C. Peña garay, N. Rius and A. Santamaria hep-ph/0302093
- J. Barranco, O. G. Miranda, C. A. Moura and J. W. F. Valle hep-ph/0512195
- J. Barranco, O. G. Miranda, C. A. Moura and J. W. F. Valle 0711.0698



# Huge effects in $\nu$ oscillations



N. Kitazawa, H. Sugiyama and O. Yasuda hep-ph/0606013



# Gauge invariance

However  $2\sqrt{2}G_F \varepsilon_{\alpha\beta}^m (\bar{\nu}_\beta \gamma^\mu P_L \nu_\alpha) (\bar{f} \gamma_\mu P_{L,R} f)$

is related to  $2\sqrt{2}G_F \varepsilon_{\alpha\beta}^m (\bar{l}_\beta \gamma^\mu P_L l_\alpha) (\bar{f} \gamma_\mu P_{L,R} f)$

by gauge invariance and very strong bounds exist

$$\varepsilon_{e\mu}^m < \sim 10^{-6}$$

$$\varepsilon_{e\tau}^m < \sim 10^{-2}$$

$$\varepsilon_{\mu\tau}^m < \sim 10^{-2}$$

$\mu \rightarrow e \gamma$

$\mu \rightarrow e$  in nuclei

$\tau$  decays

S. Bergmann et al. hep-ph/0004049

Z. Berezhiani and A. Rossi hep-ph/0111147



## Large NSI?

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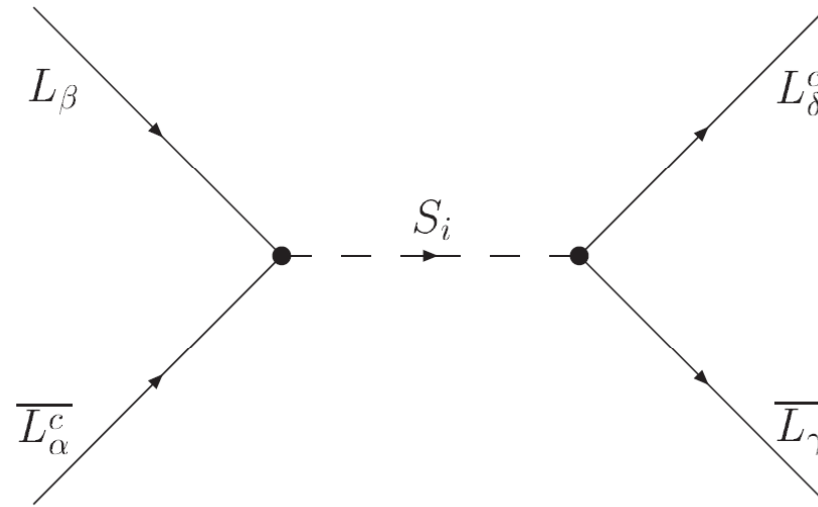
We search for gauge invariant **SM** extensions satisfying:

- Matter **NSI** are generated at tree level
- **4-charged fermion** ops not generated at the same level
- No cancellations between diagrams with **different** messenger particles to avoid constraints
- The Higgs Mechanism is responsible for **EWSB**

S. Antusch, J. Baumann and EFM 0807.1003 See also next talk  
and B. Gavela, D. Hernández, T. Ota and W. Winter 0809.3451

# Large NSI?

At  $d=6$  only one direct possibility: **charged scalar singlet**



$$\mathcal{L}_{int}^S = -\lambda_{\alpha\beta}^i \bar{L}_\alpha^c i\sigma_2 L_\beta S_i + \text{H.c.} = \lambda_{\alpha\beta}^i S_i (\bar{\ell}_\alpha^c P_L \nu_\beta - \bar{\ell}_\beta^c P_L \nu_\alpha) + \text{H.c.}$$

$$\mathcal{L}_{NSI}^{d=6,as} = c_{\alpha\beta\gamma\delta}^{d=6,as} (\bar{L}_\alpha^c i\sigma_2 L_\beta) (\bar{L}_\gamma i\sigma_2 L_\delta^c) \quad \varepsilon_{\alpha\beta}^{m,eL} = \sum_i \frac{\lambda_{e\beta}^i \lambda_{e\alpha}^{i*}}{\sqrt{2} G_F m_{S_i}^2}$$





## Large NSI?

Since  $\lambda_{\alpha\beta} = -\lambda_{\beta\alpha}$  only  $\varepsilon_{\mu\mu}$ ,  $\varepsilon_{\mu\tau}$  and  $\varepsilon_{\tau\tau} \neq 0$

Very constrained:

$$|\varepsilon_{\mu\mu}^{m,e_L}| < 8.2 \cdot 10^{-4}$$

$$|\varepsilon_{\tau\tau}^{m,e_L}| < 8.4 \cdot 10^{-3}$$

$$|\varepsilon_{\mu\tau}^{m,e_L}| < 1.9 \cdot 10^{-3}$$

$\mu \rightarrow e \gamma$

$\mu$  decays

$\tau$  decays

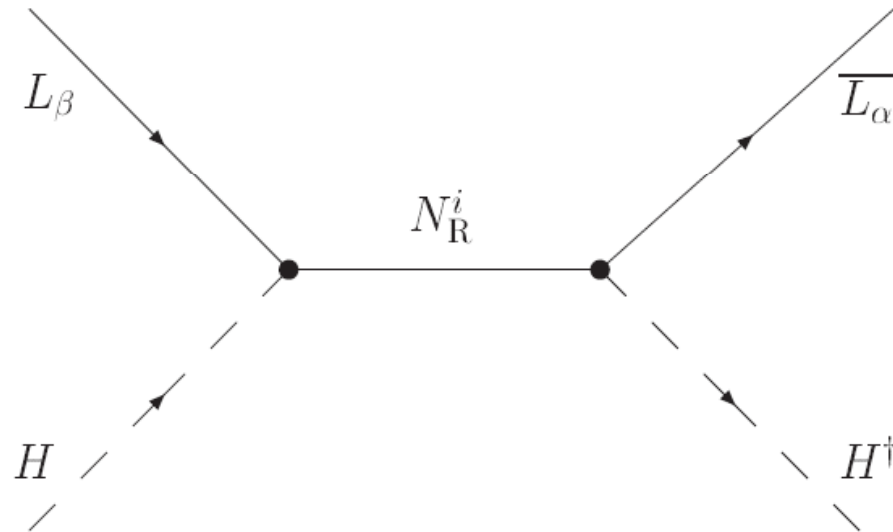
CKM unitarity

F. Cuypers and S. Davidson hep-ph/9310302  
S. Antusch, J. Baumann and EFM 0807.1003



# Large NSI?

At  $d=6$  indirect way: fermion singlets





# Effective Lagrangian

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- 3 light  $\nu$
- all unitarity violation from NP with  $\Lambda > v$
- flavour universality

$$L = i \bar{\nu}_\alpha \partial K_{\alpha\beta} \nu_\beta + \bar{\nu}_\alpha M_{\alpha\beta} \nu_\beta - \frac{g}{\sqrt{2}} (W_\mu^+ \bar{l}_\alpha \gamma^\mu P_L \nu_\alpha + h.c.) - \frac{g}{\cos \theta_W} (Z_\mu \bar{\nu}_\alpha \gamma^\mu P_L \nu_\alpha + h.c.) + \dots$$



# Effective Lagrangian

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Diagonal mass and canonical kinetic terms

$$L = i \bar{\nu}_i \partial \nu_i + \bar{\nu}_i m_{ii} \nu_i - \frac{g}{\sqrt{2}} (W_\mu^+ \bar{l}_\alpha \gamma^\mu P_L N_{\alpha i} \nu_i + h.c.) - \frac{g}{\cos \theta_W} (Z_\mu \bar{\nu}_i \gamma^\mu P_L (N^\dagger N)_{ij} \nu_j + h.c.) + \dots$$



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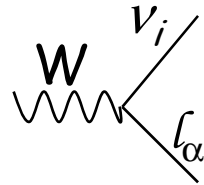
$$\nu_\alpha = N_{\alpha i} \nu_i$$

$N$  is not unitary



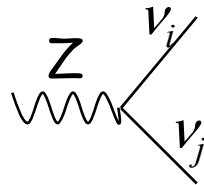
# $(NN^\dagger)$ from decays

- W decays



$$\rightarrow \frac{(NN^\dagger)_{\alpha\alpha}}{\sqrt{(NN^\dagger)_{ee}} \sqrt{(NN^\dagger)_{\mu\mu}}}$$

- Invisible Z

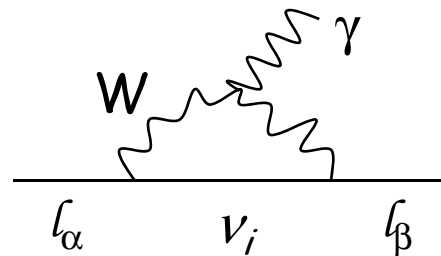


$$\rightarrow \frac{\sum_{\alpha\beta} (NN^\dagger)_{\alpha\beta}}{\sqrt{(NN^\dagger)_{ee}} \sqrt{(NN^\dagger)_{\mu\mu}}}$$

- Universality tests

$$\rightarrow \frac{(NN^\dagger)_{\alpha\alpha}}{(NN^\dagger)_{\beta\beta}}$$

- Rare leptons decays



Info on  $(NN^\dagger)_{\alpha\beta}$

$$\rightarrow \frac{|(NN^\dagger)_{\alpha\beta}|^2}{(NN^\dagger)_{\alpha\alpha} (NN^\dagger)_{\beta\beta}}$$

Info on  $(NN^\dagger)_{\alpha\alpha}$

After integrating out W and Z neutrino NSI induced



## $(NN^\dagger)$ from decays

$$|NN^\dagger| \approx \begin{pmatrix} 0.994 \pm 0.005 & < 7.0 \cdot 10^{-5} & < 1.6 \cdot 10^{-2} \\ < 7.0 \cdot 10^{-5} & 0.995 \pm 0.005 & < 1.0 \cdot 10^{-2} \\ < 1.6 \cdot 10^{-2} & < 1.0 \cdot 10^{-2} & 0.995 \pm 0.005 \end{pmatrix} \quad \text{Experimentally}$$

E. Nardi, E. Roulet and D. Tommasini hep-ph/9503228

D. Tommasini, G. Barenboim, J. Bernabeu and C. Jarlskog hep-ph/9503228

S. Antusch, C. Biggio, EFM, B. Gavela and J. López Pavón hep-ph/0607020

The diagonal elements are somewhat smaller than 1 due to the nearly  $2\sigma$  deviation from 3 in the number of  $\nu$  measured by the Z width

$$N_\nu = 2.984 \pm 0.009$$

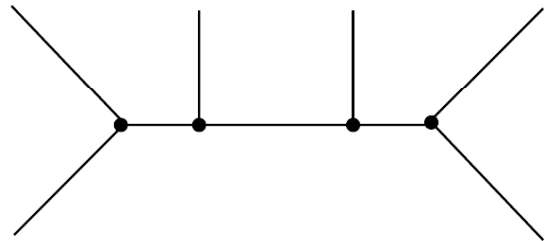


# Large NSI?

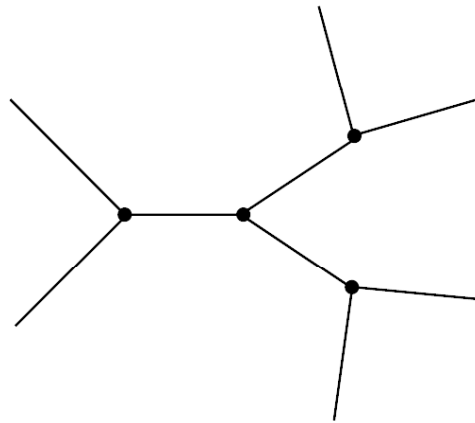
At  $d=8$  more freedom

Can add 2  $H$  to break the symmetry between  $\nu$  and  $l$  with the vev

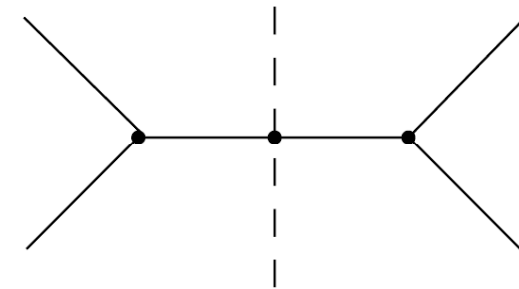
There are 3 topologies to induce effective  $d=8$  ops with  $HLLff$  legs:



(a) Topology 1



(b) Topology 2



(c) Topology 3

We distributed the 6 fields among the legs in the different topologies and studied if the resulting operators satisfied the restrictions





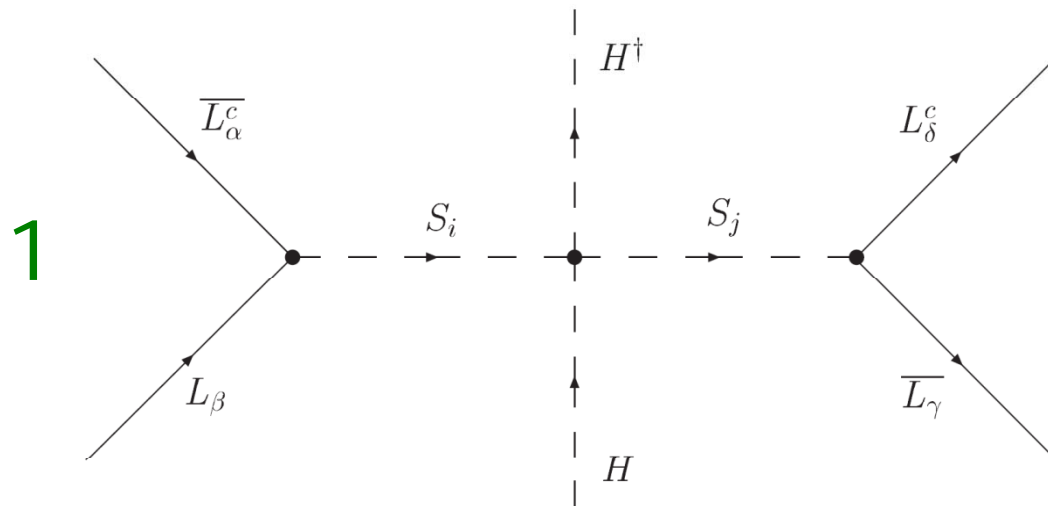
## Large NSI?

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We found three classes satisfying the requirements:

# Large NSI?

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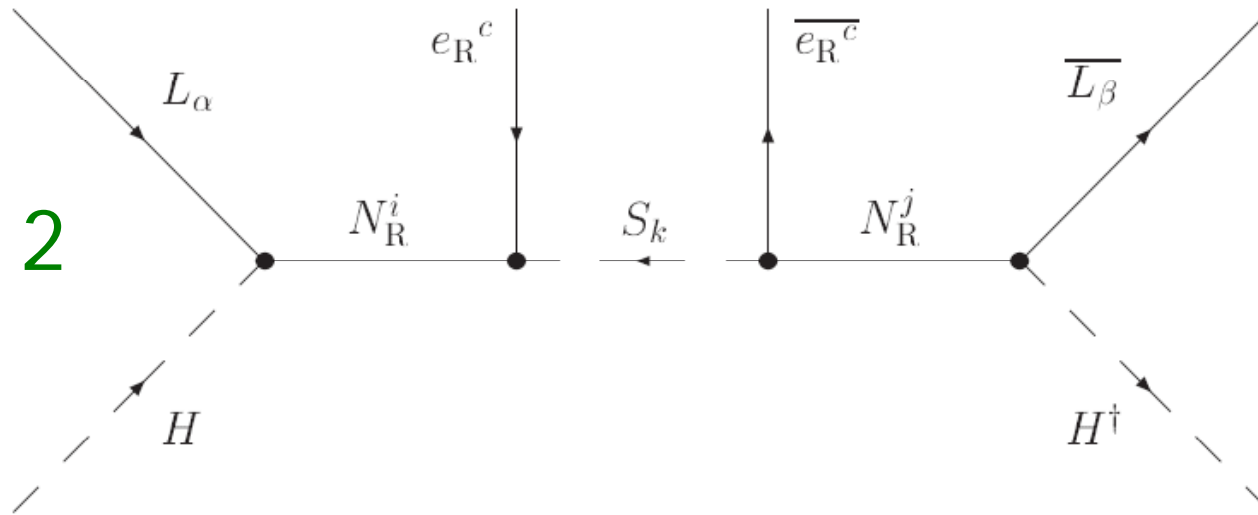
Just contributes to the scalar propagator after EWSB

$$v^2/2 (\bar{L}_\alpha^c i \sigma_2 L_\beta) (\bar{L}_\gamma i \sigma_2 L_\delta)$$

Same as the  $d=6$  realization with the scalar singlet

# Large NSI?

We found three classes satisfying the requirements:

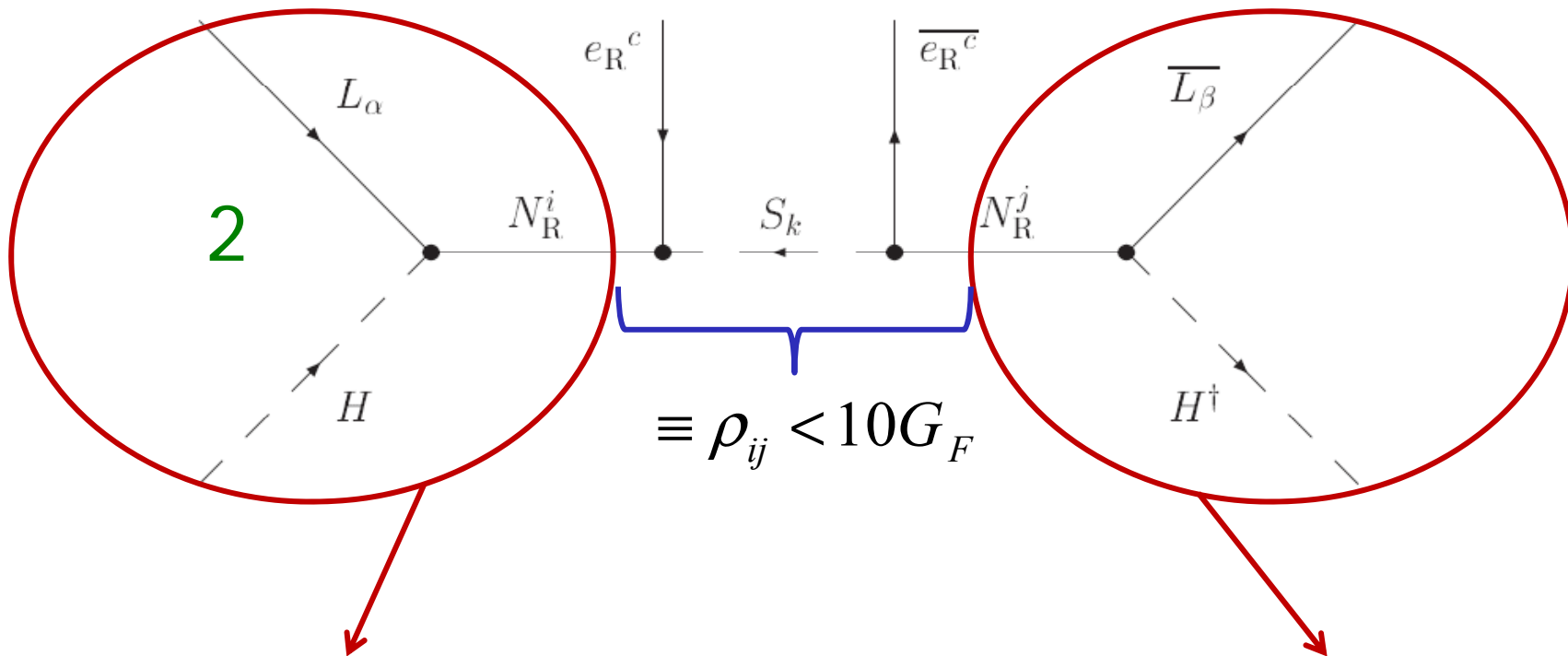


The Higgs coupled to the  $N_R$  selects  $\nu$  after EWSB

$$(\bar{L}_\beta i\sigma_2 H^*) \gamma^\mu (H^t i\sigma_2 L_\alpha) (\bar{f} \gamma_\mu f) \longrightarrow -v^2/2 (\bar{\nu}_\beta \gamma^\mu \nu_\alpha) (\bar{f} \gamma_\mu f)$$

# Large NSI?

But can be related to **non-unitarity** and constrained



$$\frac{v}{\sqrt{2}} \sum_i \frac{Y_{\alpha i}}{M_i} < \sqrt{\frac{v^2}{2} \sum_i \left| \frac{Y_{\alpha i}}{M_i} \right|^2} = \sqrt{(NN^\dagger - 1)_{\alpha\alpha}} \quad \frac{v}{\sqrt{2}} \sum_j \frac{Y_{\beta j}}{M_j} < \sqrt{\frac{v^2}{2} \sum_j \left| \frac{Y_{\beta j}}{M_j} \right|^2} = \sqrt{(NN^\dagger - 1)_{\beta\beta}}$$



## Large NSI?

For the matter NSI

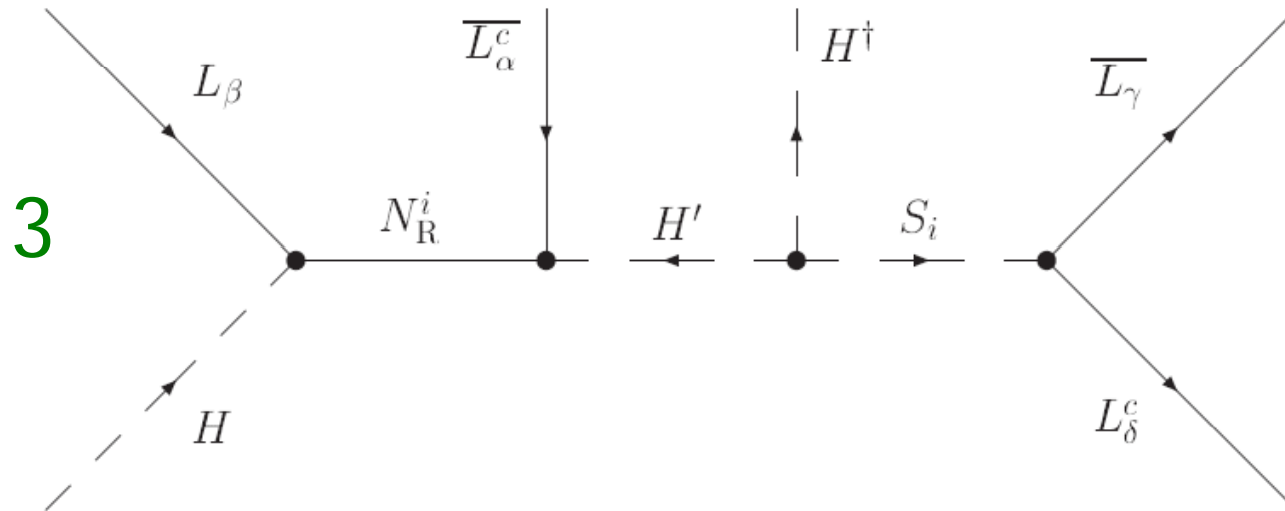
$$|\varepsilon_{\alpha\beta}^{m,f}| < \begin{pmatrix} 1.4 \cdot 10^{-3} & 6.4 \cdot 10^{-4} & 1.1 \cdot 10^{-3} \\ 6.4 \cdot 10^{-4} & 5.8 \cdot 10^{-4} & 7.3 \cdot 10^{-4} \\ 1.1 \cdot 10^{-3} & 7.3 \cdot 10^{-4} & 1.9 \cdot 10^{-3} \end{pmatrix} \frac{\hat{\rho}^{(f)}}{G_F}$$

Where  $\hat{\rho}^{(f)}$  is the largest eigenvalue of  $\rho_{ij}^{(f)}$

And additional source, detector and matter NSI are generated through **non-unitarity** by the **d=6** op

# Large NSI?

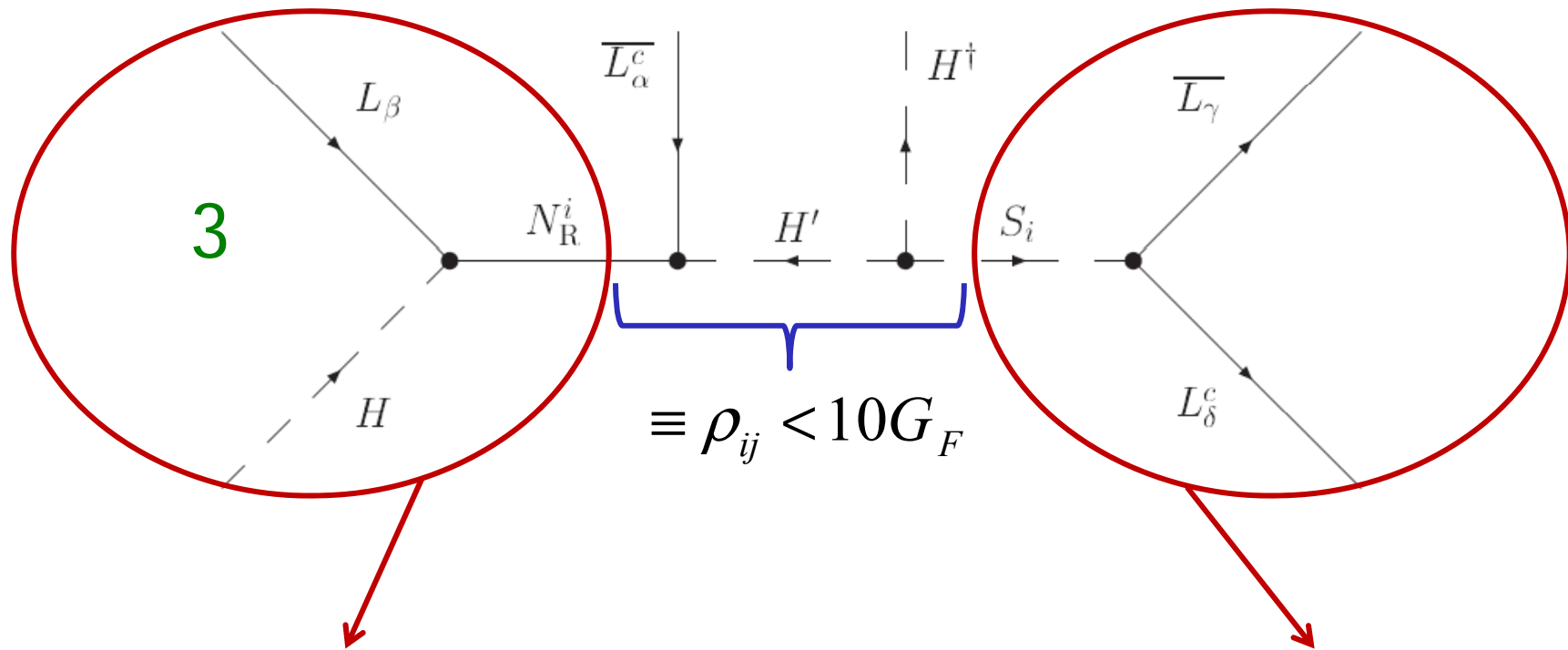
We found three classes satisfying the requirements:



Mixed case, **Higgs** selects one  $\nu$  and scalar singlet **S** the other

# Large NSI?

Can be related to **non-unitarity** and the **d=6** antisymmetric op



$$\frac{v}{\sqrt{2}} \sum_i \frac{Y_{\alpha i}}{M_i} < \sqrt{\frac{v^2}{2} \sum_i \left| \frac{Y_{\alpha i}}{M_i} \right|^2} = \sqrt{(NN^\dagger - 1)_{\alpha\alpha}}$$

$$v \sum_j \frac{\lambda_{\gamma\delta}^j}{M_{Sj}} < \sqrt{v^2 \sum_j \left| \frac{\lambda_{\gamma\delta}^j}{M_{Sj}} \right|^2}$$



## Large NSI?

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At  $d=8$  we found no new ways of selecting  $\nu$

The  $d=6$  constraints on **non-unitarity** and the **scalar singlet** apply also to the  $d=8$  realizations

What if we allow for cancellations among diagrams?

See next talk by T. Ota to see how to obtain

$$\frac{O}{M^4} (\bar{L}_\alpha i \sigma_2 H^*) \gamma^\mu (H^t i \sigma_2 L_\beta) (\bar{f}_\gamma \gamma_\mu f_\delta)$$

cancelling the 4 charged fermion operators





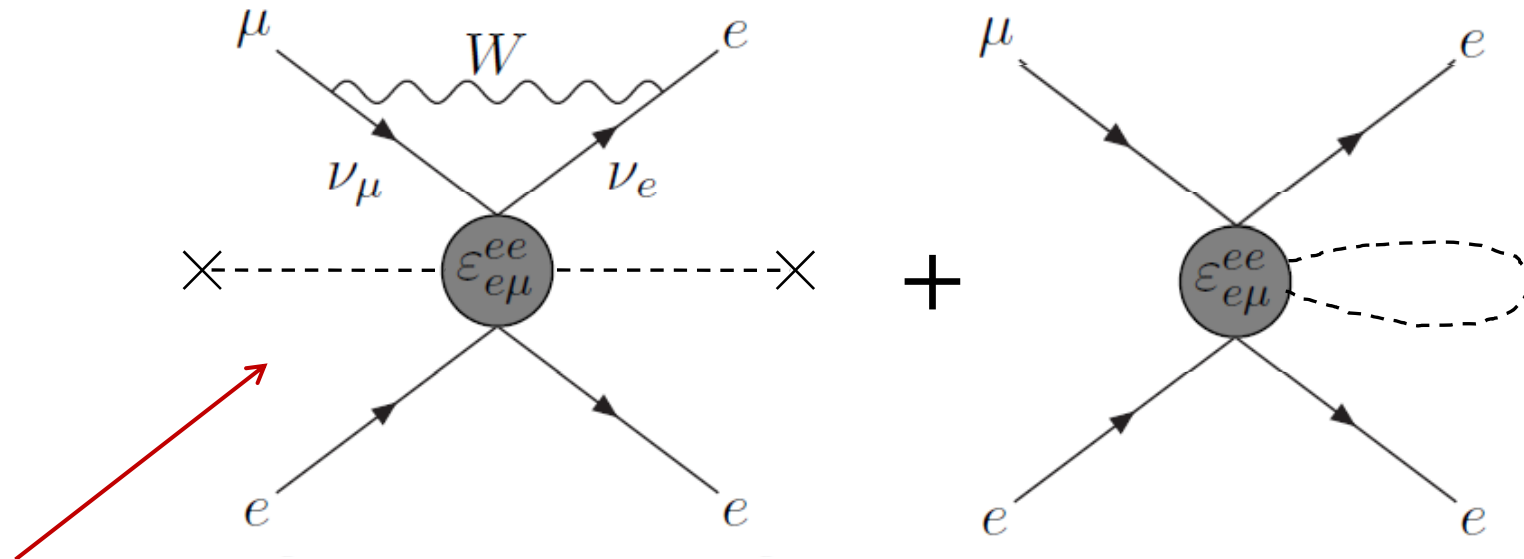
## NSI in loops

Even if we arrange to have

$$\begin{aligned} & \frac{O}{M^4} (\bar{L}_\alpha i \sigma_2 H^*) \gamma^\mu (H^\dagger i \sigma_2 L_\beta) (\bar{E}_\gamma \gamma_\mu E_\delta) \\ &= \frac{O}{2M^4} [(\bar{L}_\alpha \gamma^\mu L_\beta) (H^\dagger H) - (\bar{L}_\alpha \gamma^\mu \bar{\tau} L_\beta) (H^\dagger \bar{\tau} H)] (\bar{E}_\gamma \gamma_\mu E_\delta) \end{aligned}$$

# NSI in loops

These loops are related by gauge invariance:



Used to set loop bounds on  $\epsilon_{e\mu}^{ee}$  through the **log** divergence

However the **log cancels** when adding the diagrams...



## NSI in loops

$$\frac{O}{2M^4} \frac{k\Lambda^2}{16\pi^2} (\bar{L}_\alpha \gamma^\mu L_\beta) (\bar{E}_\gamma \gamma_\mu E_\delta)$$

The loop contribution is a **quadratic** divergence

The coefficient  $k$  depends on the full theory completion:

- Without cancellations  $k \sim O(1)$ 
  - At least  $\Lambda \sim M_W \rightarrow$  old bounds are recovered  $\mathcal{E}_{e\mu} < 8 \cdot 10^{-4}$
  - If no other new physics  $\Lambda = M \rightarrow NSI = 4CF$  if  $1/16\pi^2 > v^2/M^2$
- Allowing cancellations also at **loop** level  $k = 0$ 
  - Only direct **0.1** bound on  $\mathcal{E}_{e\mu}$



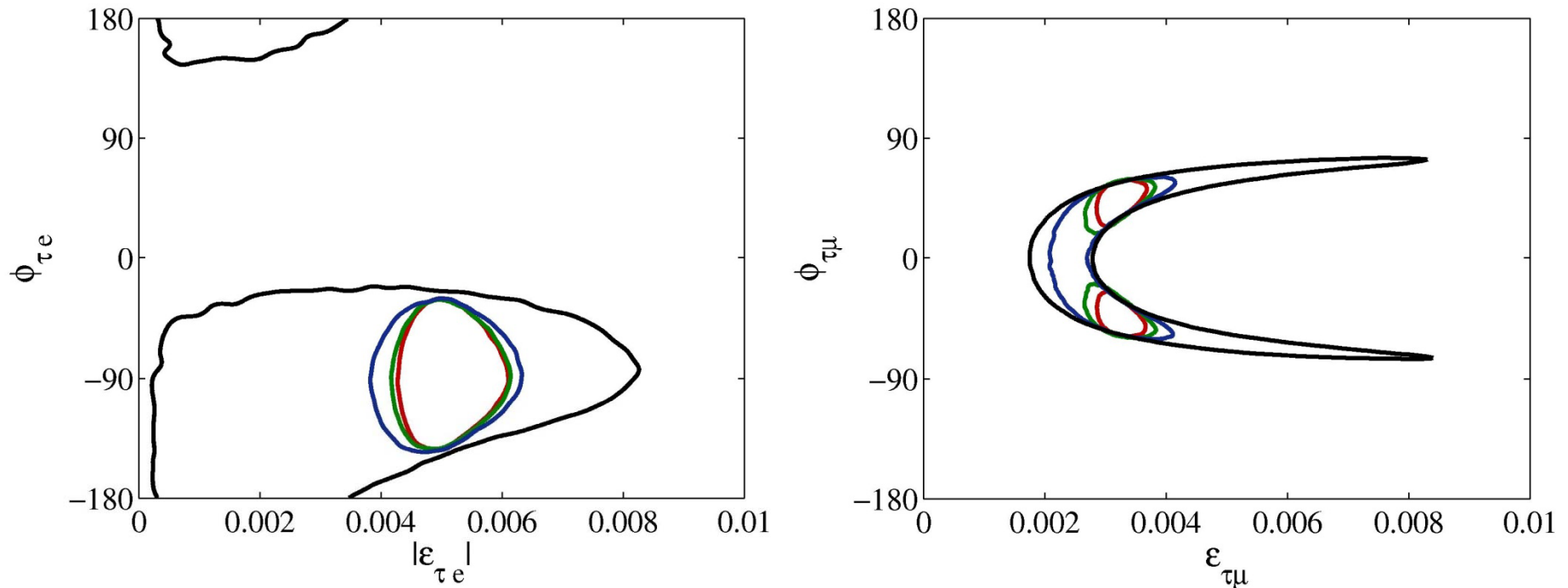
## Conclusions: NSI

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- To realize **large NSI** related **4-charged fermion** operators must be avoided
  - It can be realized at **d=6** by the exchange of a **scalar singlet** or a  $N_R$ , but very constrained
  - At **d=8** no new possibilities without cancellations, similar bounds apply
  - **4-charged fermion** ops can be avoided through cancellations between diagrams: to cook a model check the ingredient list in [arXiv:0809.3451](https://arxiv.org/abs/0809.3451) and next talk
- Even **tuning** at tree level large **4-charged fermion** ops induced at one loop: **cancellations** also needed at **1 loop**



# Non-Unitarity at a NF



Golden channel at **NF** is sensitive to  $\epsilon_{\tau e}$  beyond present bound

$\nu_{\mu}$  disappearance channel **linearly** sensitive to  $\epsilon_{\tau\mu}$  through matter effects

Near  $\tau$  detectors can improve the bounds around 1 order of magnitude

Combination of near and far detectors sensitive to the **new CP phases**

S. Antusch, M. Blennow, EFM and J. López-pavón in preparation