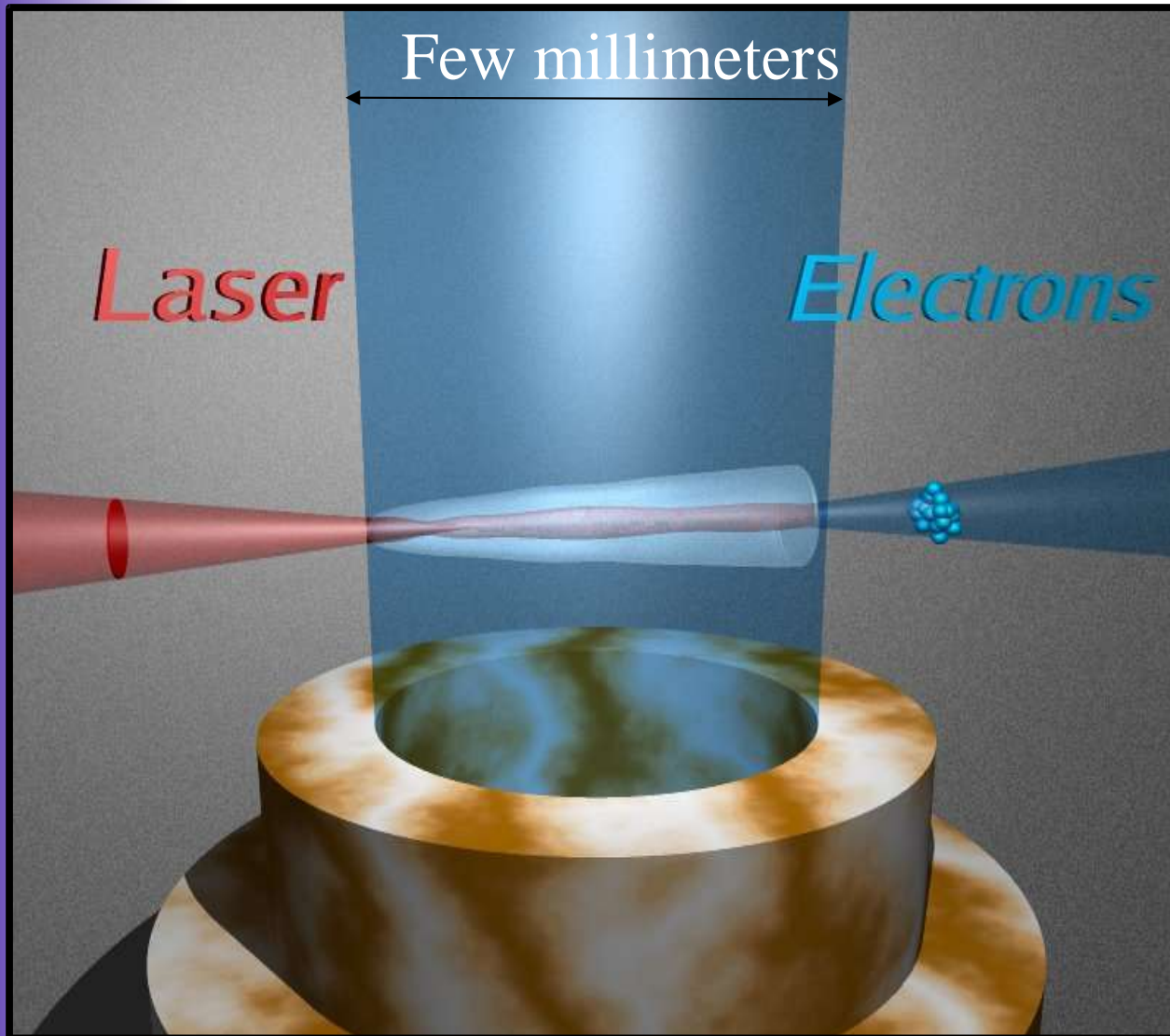


Development of a compact single shot electron spectrometer

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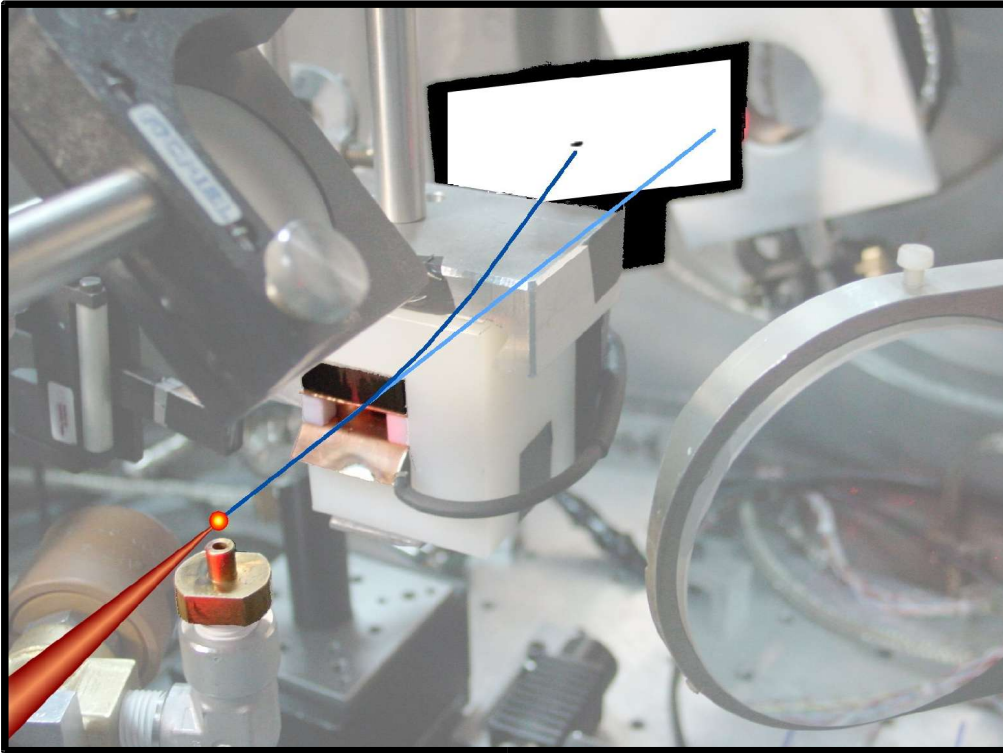
Compact electron accelerator



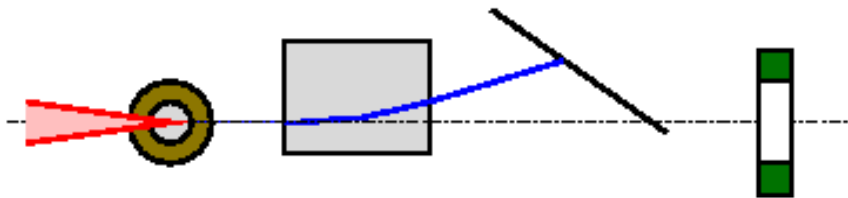
Major enhancements of the electron beam properties :

- Small source size
- Low divergence
- Quasi-monoenergetic
- Short duration
- High charge

In the interaction chamber



Laser Nozzle Magnets Lanex ICT

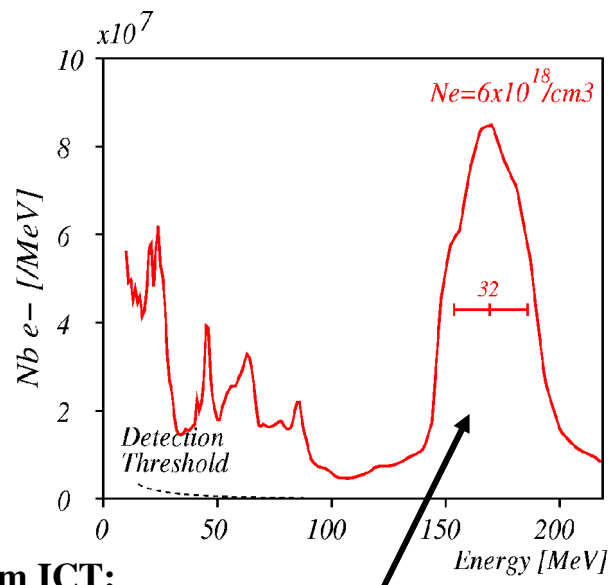
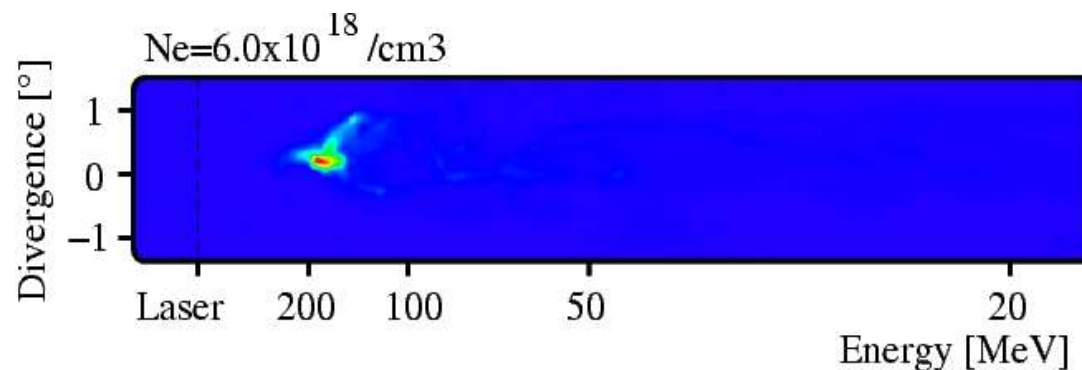


New spectrometer :

- Single shot measurement
- Spectrum and divergence
- Measurement of the charge at high energy

This diagnostic can be used because the electron beam is very collimated.

Measurement of a quasi-monoenergetic electron beam



From ICT:
500 pC +/-200 pC in the bump at 170 MeV

Limitation due to the
spectrometer resolution

Faure *et al.*, Nature **431**, p541 (2004)

Outline

I – Design of a spectrometer for higher energies

- Permanent magnetic field.

II – Analytical calculations

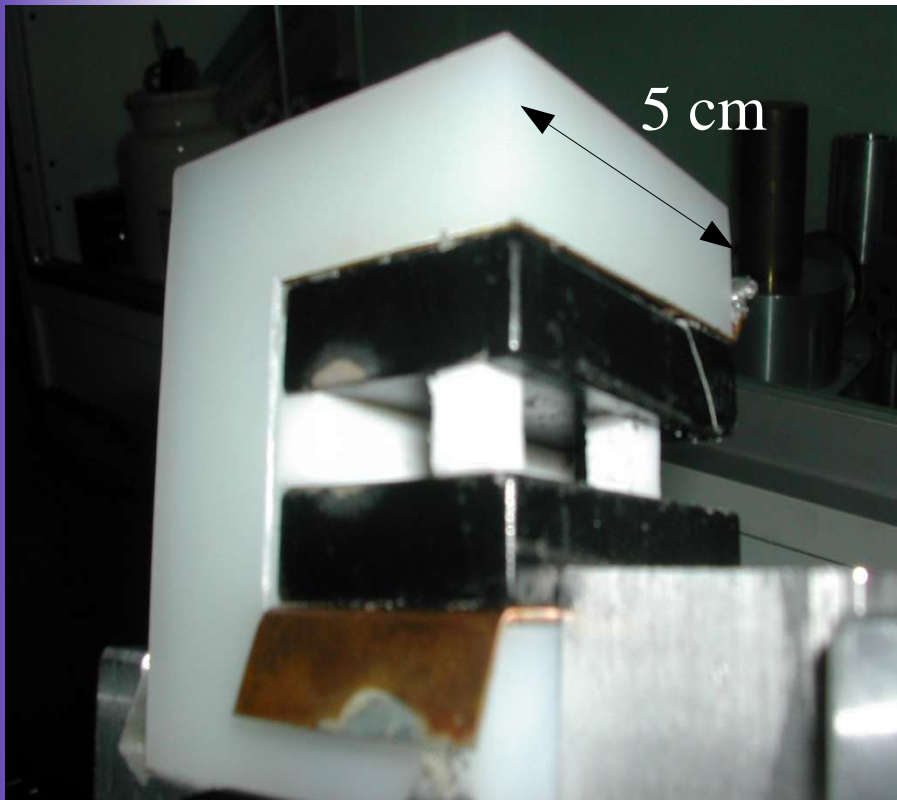
- Trajectories of electrons
- Spectrometer resolution
- Relative and absolute calibration of the number of electrons

III – Application to an experimental electron beam

- Quasimonoenergetic electron spectrum

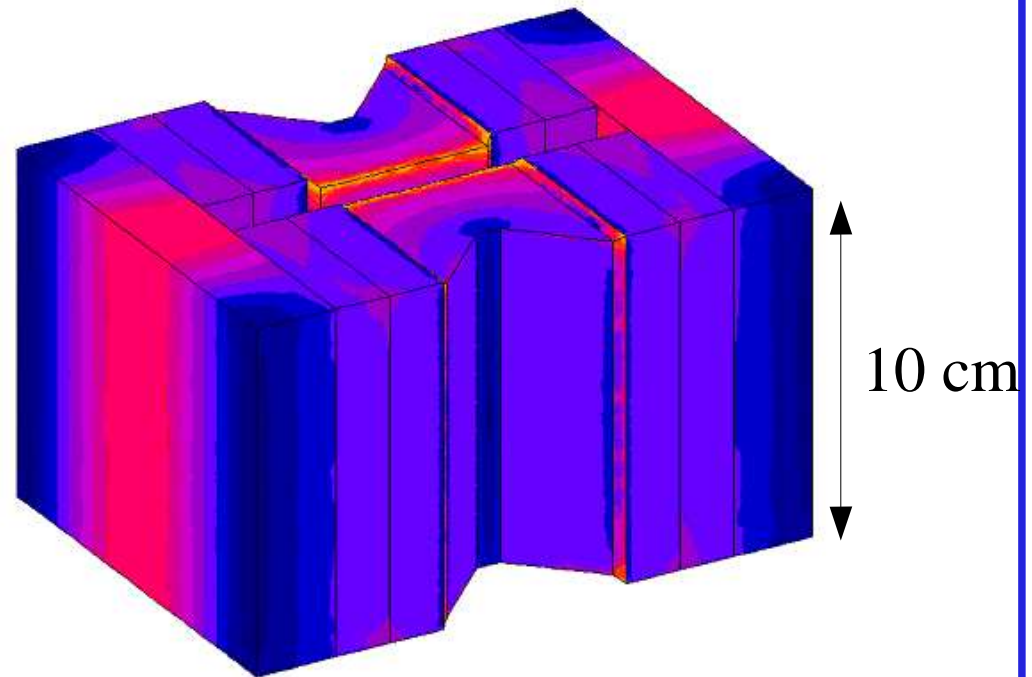
Comparison of the two magnets

$B=0.41\text{ T}$



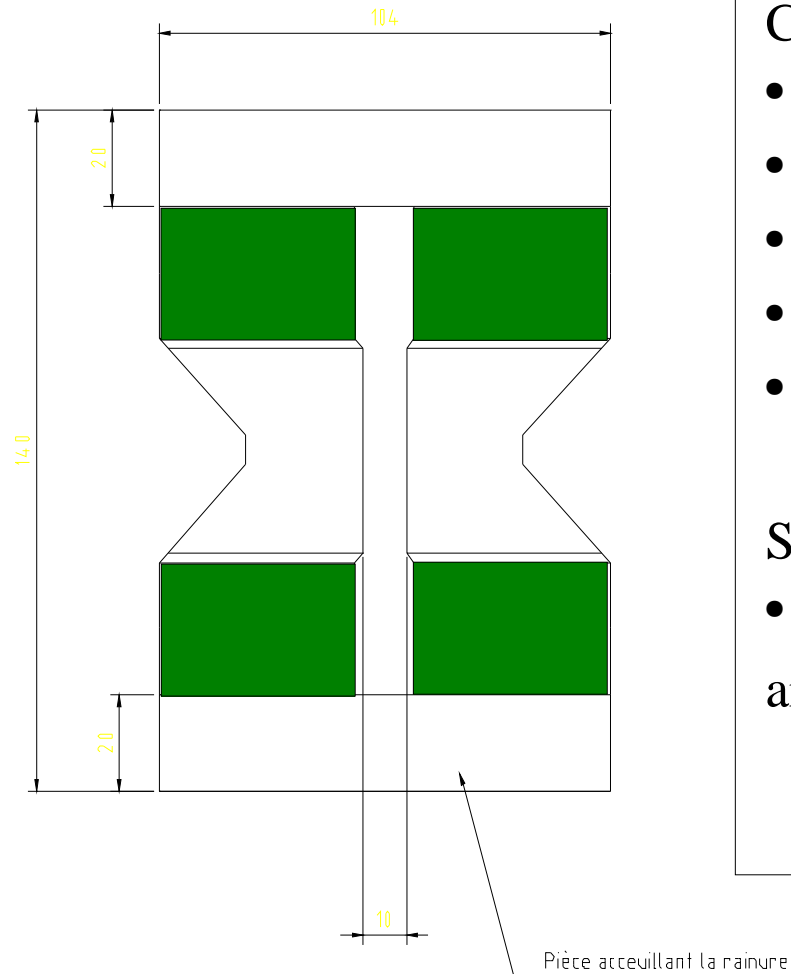
Previous Magnet
home made, up to 100 MeV

$B=1\text{ T}$



Design of a new magnet
up to 400 MeV

Datasheet



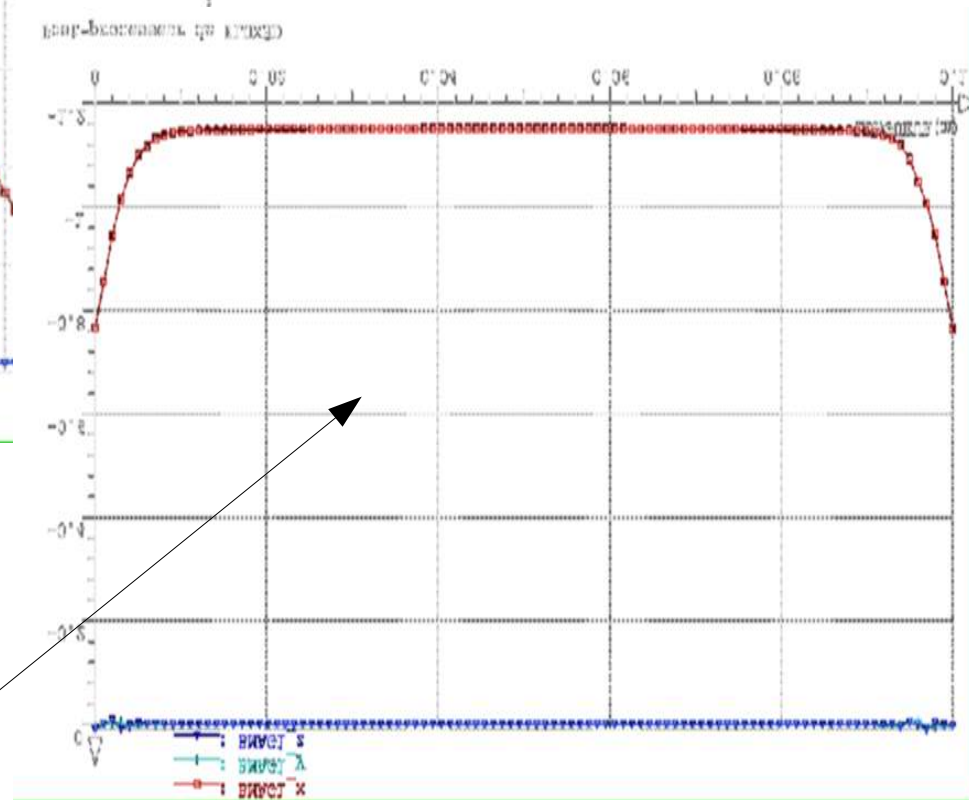
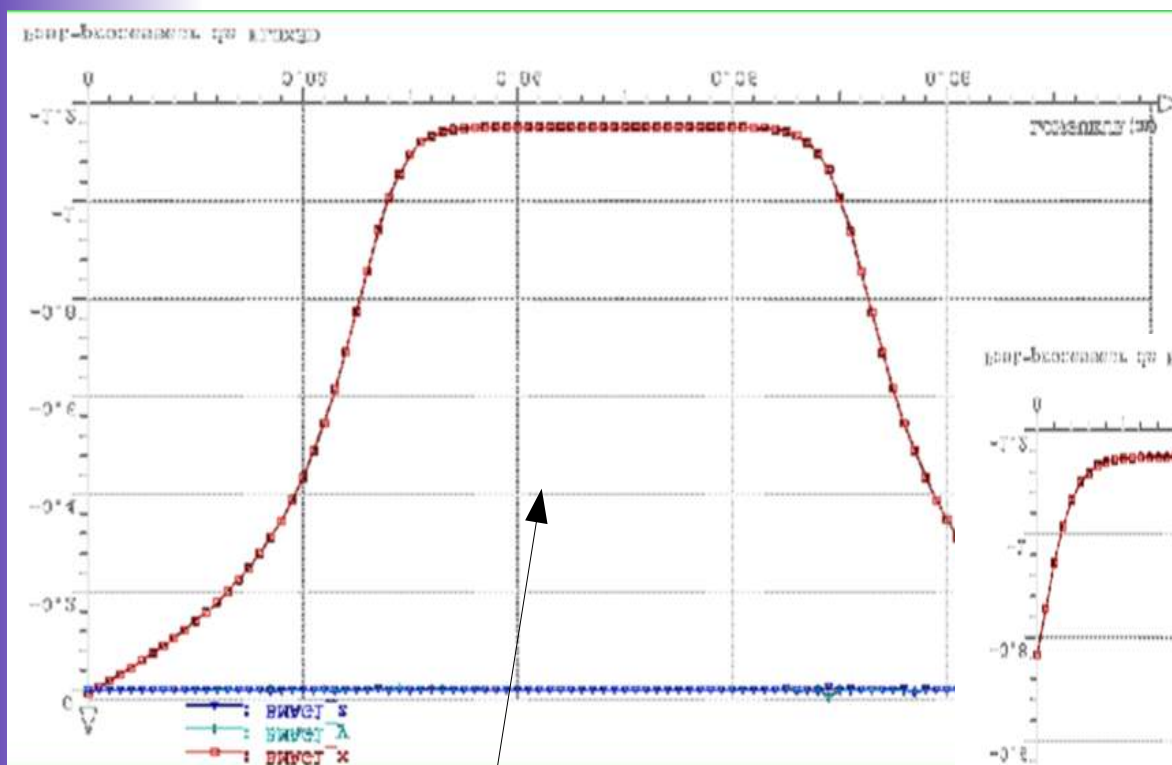
Constraints :

- Gap = 1cm
- Magnetic field $\sim 1\text{T}$
- Length = 10 cm
- Large slit required
- Compact spectrometer

Solution :

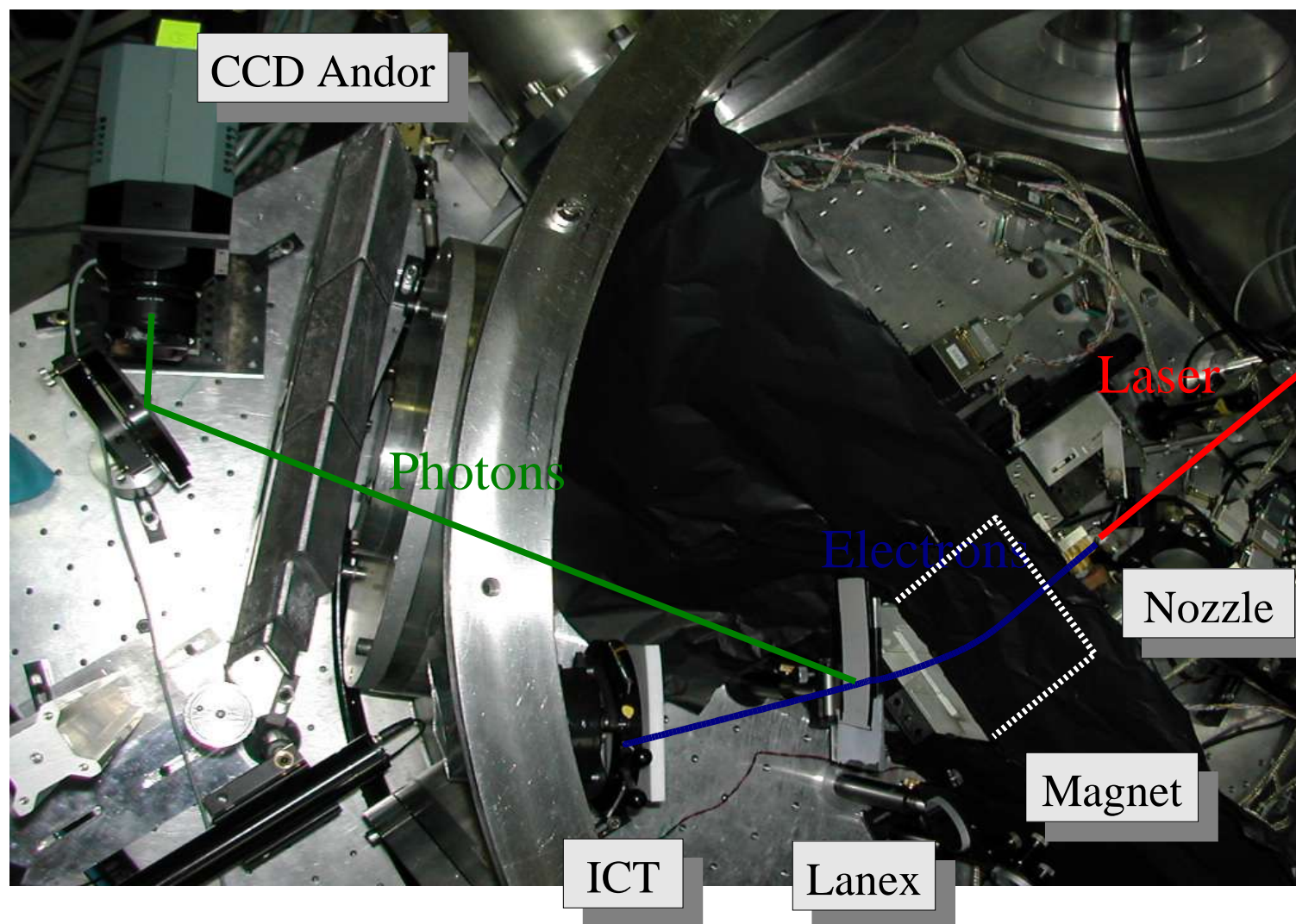
- Good homogeneity due to a special arrangement of magnet poles

Data from the manufacturer



Simulations of the longitudinal magnetic field

Transverse magnetic field



Analytical calculations

- Trajectories of an electron in a permanent magnetic field
 - Radius of curvature (relativistic electron):

$$R = \frac{E_0}{B_m e c}$$

E_0 Initial kinetic energy

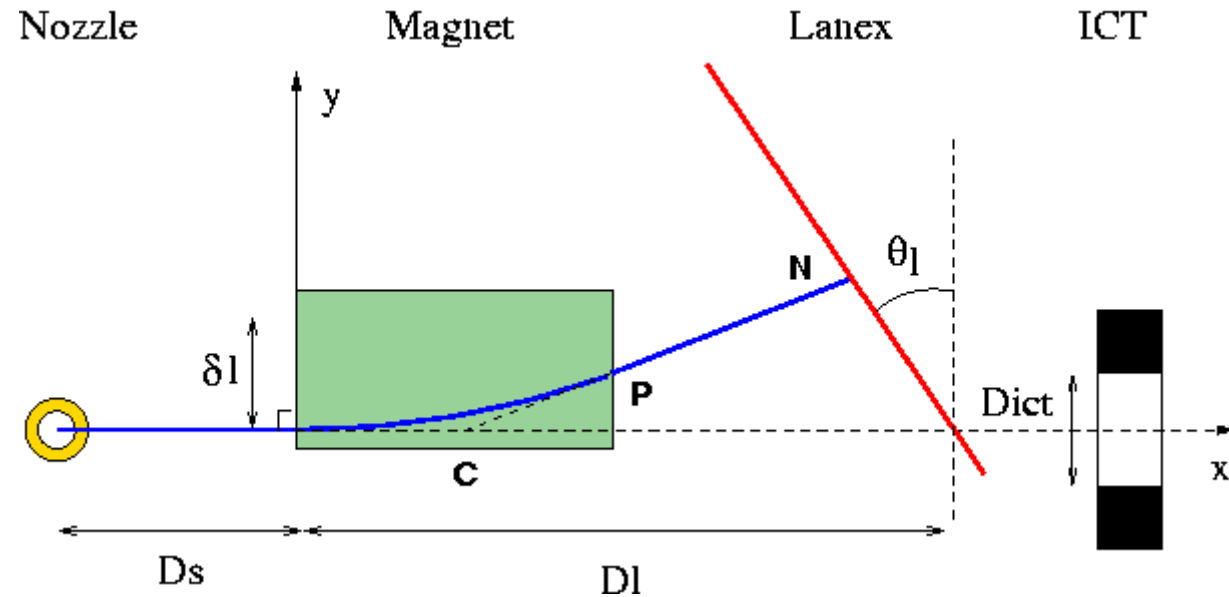
B_m Magnetic field

e Charge of the electron

c Celerity of light

- Assumptions :
 - The magnetic field is uniform in a rectangular area
 - The relativistic incoming electron is perpendicular to the magnet's surface.

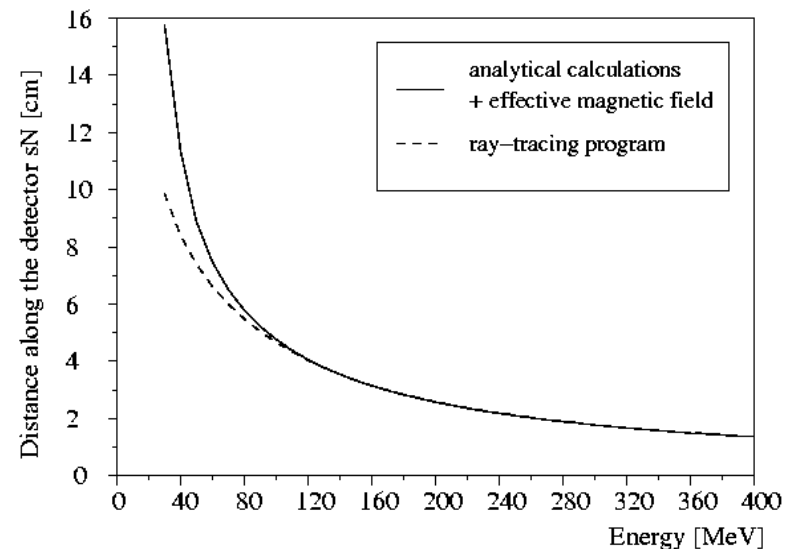
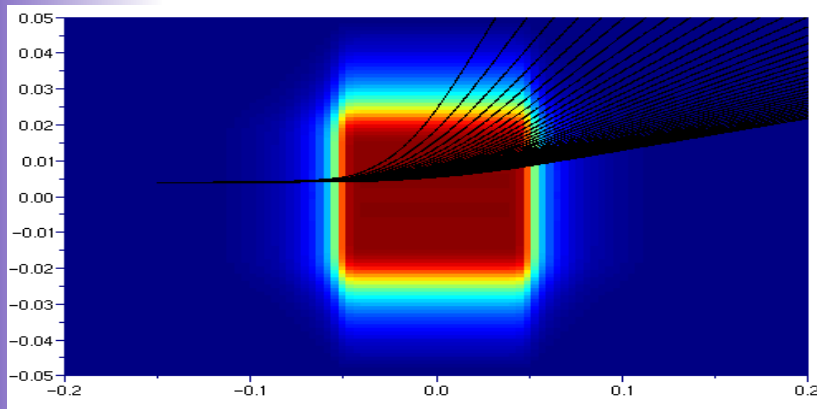
Coordinates



$$\begin{pmatrix} x_P \\ y_P \end{pmatrix} = \begin{pmatrix} L_m \\ R - \sqrt{R^2 - L_m^2} \end{pmatrix} \quad \begin{pmatrix} x_C \\ y_C \end{pmatrix} = \begin{pmatrix} \frac{x_P^2 + y_P^2}{2 x_P} \\ 0 \end{pmatrix} \quad \begin{pmatrix} x_N \\ y_N \end{pmatrix} = \begin{pmatrix} D_l - y_l \tan(\theta_l) \\ \frac{(D_l - x_C) y_P}{x_P - x_C + y_P \tan(\theta_l)} \end{pmatrix}$$

Equivalent magnetic field

- The real magnetic field spreads outside the magnet. The introduction of an equivalent magnetic field allows the use of analytical formulae.



$$B_m^{max} = 1.0 T \longrightarrow B_m^{eff} = 1.2 T$$

- Not valid for electrons below 100 MeV who travel in the gradient of the magnetic field

Resolution

- The resolution is limited by the size of the electron beam on the detector.
The corresponding energy range at a given energy E_0 is :

$$\frac{\delta E_0}{E_0} = \frac{\delta_s}{E_0} \div \frac{d s_N}{dE_0}$$

$s_N = y_N / \cos(\theta_l)$ the distance along the Lanex

δ_s the size of the electron beam on the detector

- The equivalent at high energy is

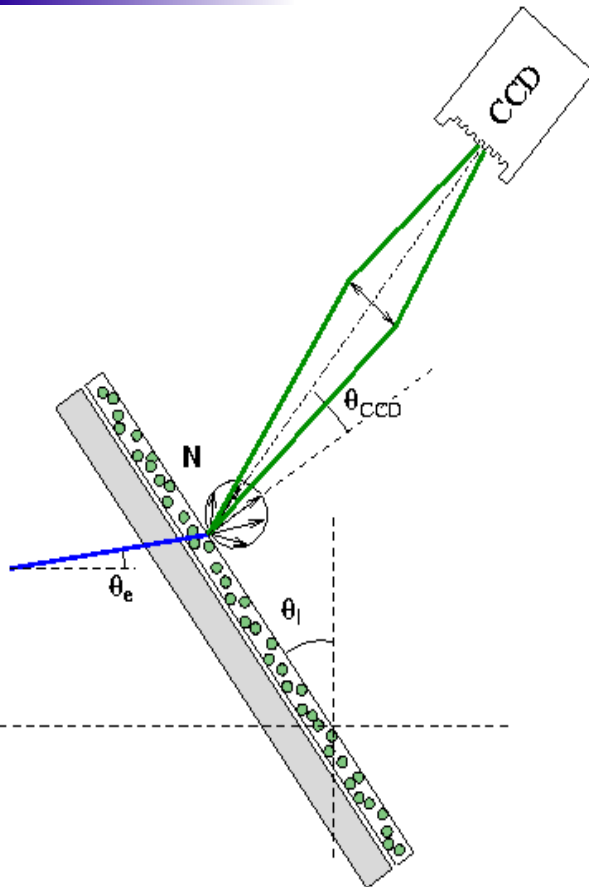
$$\frac{\delta E_0}{E_0} \sim \frac{(D_s + D_l) R \theta_s}{(D_l - L_m/2) L_m} \propto R \propto E_0$$

θ_s divergence

Energy [MeV]	20	50	100	200	400
«home-made» magnet	6%	14%	27%	53%	-
10cm magnet	-	-	5%	10%	20%

Resolution for two different configurations

Detector composition



<i>Item</i>	<i>Material</i>	<i>Density (g/cc)</i>	<i>Thickness (cm)</i>
Laser Shielding			
Shielding	Aluminium	2,70	0,0100
Kodak Lanex Fine Screen			
protective coating	cellulose acetate	1,32	0,0010
plastic substrate	Poly(ethylene terephthalate)	1,38	0,0178
scintillator	Gd ₂ O ₂ S + urethane binder	4,25	0,0084
protective coating	cellulose acetate	1,32	0,0005

Composition of the scintillating screen

The surface loading of Gadolinium Oxysulfide in the urethane binder is 33 mg/cm²

Schach von Wittenau *et al.*, Med. Phys. **29** pp. 2559-2570 (2002)

Absolute calibration

Phosphor layer : conversion

We assume that the conversion into visible light is proportionnal to the energy deposited in the scintillator layer

$$\frac{d N_{cr}}{d N_{el}} = \frac{1}{E_{ph}} \varepsilon \frac{dE}{dx} \delta x$$

$\delta x = h_s / \rho_{GOS}$ effective phosphor thickness

ε efficiency

Transport : photon collection

The transmission at the phosphor boundary and the number of photons collected by the lens of the Andor CCD

$$\frac{d N_{coll}}{d N_{cr}} = \zeta g(\theta_{CCD}) \delta \Omega q_l q_Q q_{IF}$$

ζ output transmission factor

$g(\theta_{CCD})$ lambertian law

Detection by the CCD : number of counts

The yield of the Andor CCD camera

$$\frac{d N_{count}}{d N_{coll}} = \frac{QE}{r}$$

$$\frac{d N_{el}}{d E} d E = Counts \div \left(\frac{d N_{counts}}{d N_{coll}} \frac{d N_{coll}}{d N_{cr}} \frac{d N_{cr}}{d N_{el}} \right)$$

List of parameters

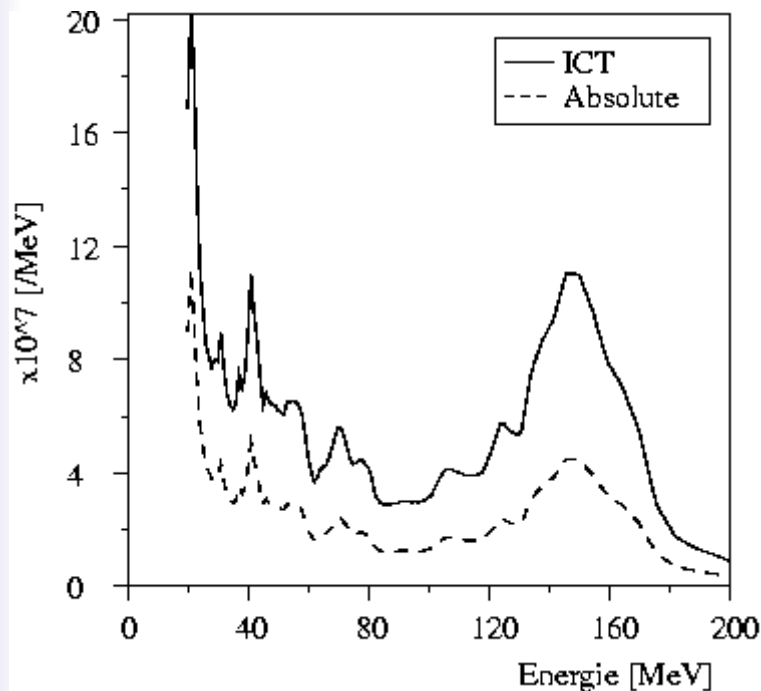
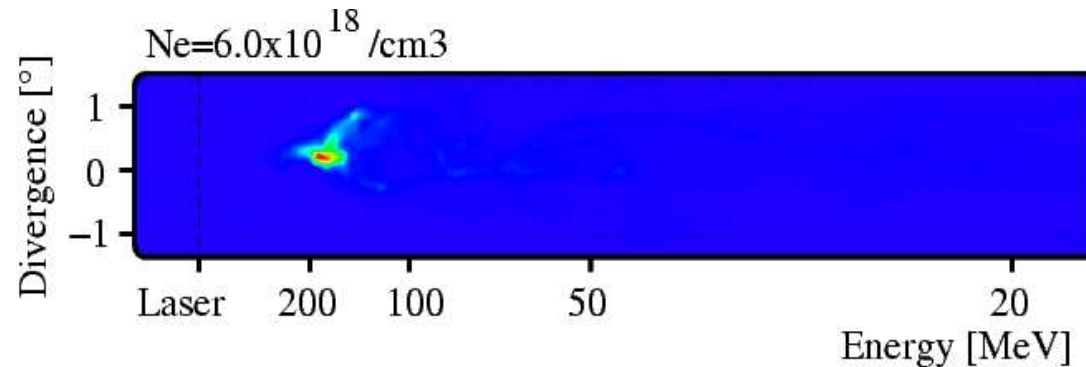
Parameter	Symbol	Value
Spectrometer		
<i>Magnet</i>		
Equivalent magnetic field	Bm	0.41 T
Magnet length	Lm	5 cm
Magnet width	Lm	2.5 cm
Magnet shift	δl_m	1.3 cm
Magnet-Lanex length	Dl	17 cm
<i>Lanex</i>		
Lanex angle	θ_l	55°
Efficiency	ϵ	0,034
Surface Loading	hs	33 mg/cm ²
Phosphor density	ρ_{GOS}	7.44 g/cm ³
Photon energy	E _{ph}	2.27 eV
Transmission factor	ζ	0,22
<i>ICT</i>		
ICT diameter	D _{ict}	10 cm

Parameter	Symbol	Value
Detection System		
Solid Angle	$\delta\Omega$	2.0e-3 sr
CCD angle	θ_{ccd}	15°
Lens	q _l	0,95
Quartz	q _q	0,95
Interference filter	q _{IF}	0,2
Pixel size on the lanex	L _{pix}	0.28 mm
Electron Source		
Source-Magnet length	D _s	6 cm
Divergence	θ_s	10 mrad

Private discussions with M. Kando
Needs further investigation

Example of image analysed

The quasi-mono energetic spectrum



Mismatch of the two curves for several reasons :

- ICT sensitive to electrical noise
- Efficiency of the lanex estimated from data of collaborators
- Saturation effects in the phosphor film

Conclusion and Perspectives

I – Needs of a compact single shot spectrometer

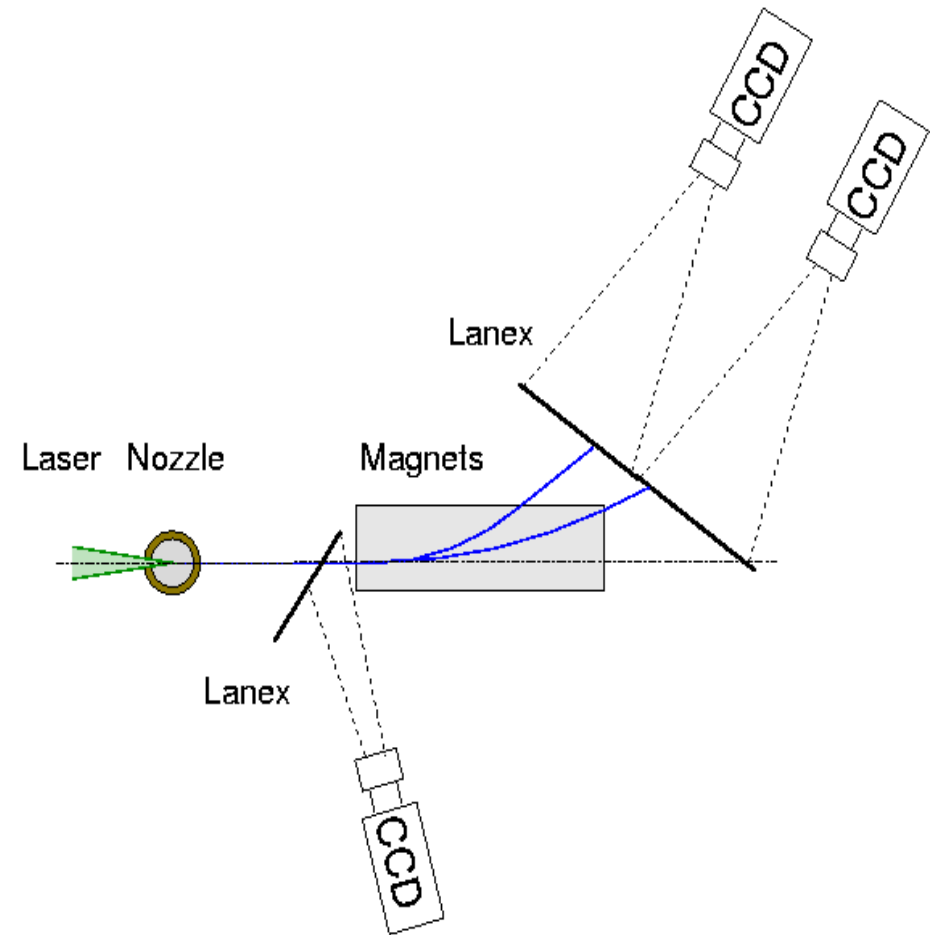
- Requirements
 - Acceleration of electrons up to 200 MeV.
 - Adapted to high repetition rate : no film processing.
- Solution chosen
 - Design and purchase of a strong permanent magnet
 - Purchase of 16 bits Andor CCD cameras.
 - Development of analytical formulaes for spectrum deconvolution
 - Purchase of a hall probe for magnet characterization

II – Further developments

- The present work will help to design a larger magnet for GeV acceleration experiments
- Estimation of the efficiency of the scintillator

Example of possible configuration for a 1 GeV-energy electron spectrometer

- Longer magnet requires larger detector to get the full spectrum
- The electrons may exit the magnetic field by the edges, in order to reduce the deflection angle for low energies
 - Beware that the each pixel on the detector corresponds to a single energy.
- A third camera with less pixel depth to monitor the electron beam axis before the magnets.
 - Valid if the scattering angle is smaller than the natural divergence. Depends on the phosphor thickness. OTR may be required.



Transmission of the interference filter

